

# Higgs theory facing data

Gauthier Durieux  
(CERN)

*Gegenbauer Goldstones*, JHEP 01 (2022) 076, [2110.06941]

*Gegenbauer's Twin*, JHEP 05 (2022) 140, [2202.01228]

*Charting the Higgs self-coupling boundaries*, JHEP 12 (2022) 148, [2209.00666]

with Matthew McCullough and Ennio Salvioni



## Where we stand

$$\mathcal{L}_{\text{SM}} = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + \bar{\psi}i\not{D}\psi + |D_{\mu}H|^2 \\ + Y\bar{\psi}\psi'H + \mu^2|H|^2 - \lambda|H|^4$$

all particles seen  
all parameters determined

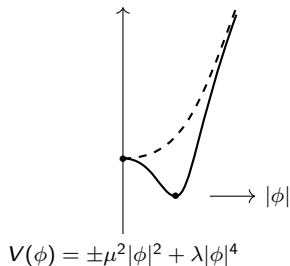
missing pieces  
(neutrino oscillation, matter/antimatter asymmetry, dark matter, etc.)

untested correlations  
(EW fit, CKM unitarity,  $m_{\times}/g_{hxx}/g_{hhxx}$ )

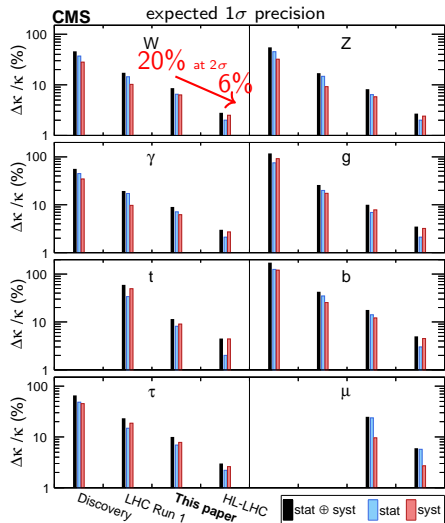
structural weaknesses  
(flavour hierarchies, strong CP, weak-scale and CC naturalness)

# Electroweak symmetry breaking

Phenomenological description of a more microscopic dynamics like the Ginzburg-Landau theory of superconductivity?

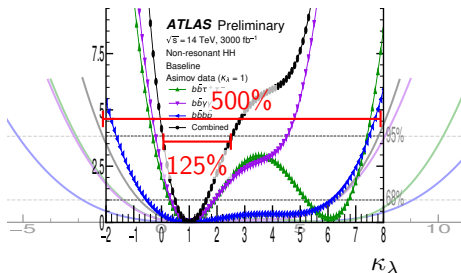
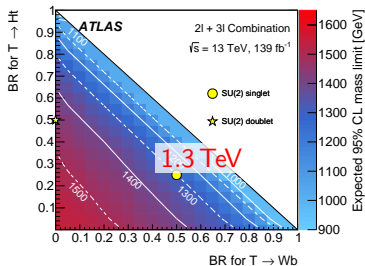


# Data



[CMS-HIG-22-001]

[EXOT-2018-58]



[HDBS-2022-03]

[ATL-PHYS-PUB-2022-053]

## Any example of Higgs theory with

$$\text{structural } \frac{m_h^2}{M_X^2} \sim \% ?$$

$$\text{structural } \delta\kappa_V \sim \% ?$$

$$\text{structural } \frac{\delta\kappa_V}{\delta\kappa_\lambda} \sim \% ? \text{ (bonus)}$$

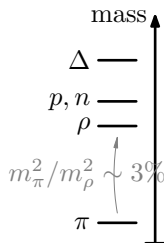
# Composite Higgs

realise the Higgs as the  
pseudo-Nambu-Goldstone boson (pNGB)  
of a new strong sector

e.g. global  $SO(5) \rightarrow SO(4)$  spontaneous breaking  
at scale  $f$

small mass obtained from the  
explicit breaking of  $SO(5)$   
by e.g. the SM

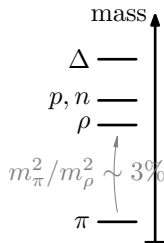
small  $\delta\kappa_V$  implies  $v^2/f^2 \ll 1$   
and requires fine-tuning in minimal models



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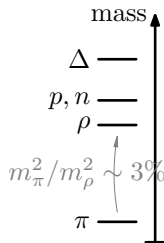
small  $m_h$  the  
small(ish)  $m_h^2/M_X^2!$

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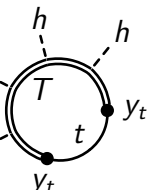


small  $m_h$  the  
small(ish)  $m_h^2/M_X^2!$

and require  $\delta\kappa_V$  or  $v/f!$  models



## Minimal composite Higgs

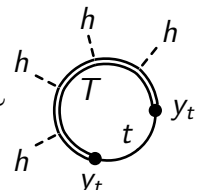


$$V(h) \sim \text{loop} + \dots \sim \kappa \frac{y_t^2 N_c}{16\pi^2} f^2 M_T^2 \left( -\sin^2 \frac{h}{f} + \delta \sin^4 \frac{h}{f} \right)$$

$$\rightarrow \frac{v^2}{f^2} = \sin^2 \frac{\langle h \rangle}{f} = \frac{1}{2\delta} \quad \text{vs.} \quad |\delta \kappa_V| \simeq \frac{v^2}{2f^2} \lesssim 6\%$$

$$\rightarrow \frac{m_h^2}{M_T^2} = \kappa \underbrace{\frac{y_t^2 N_c}{4\pi^2} \left( 1 - \frac{1}{2\delta} \right)}_{\sim 7\%} \quad \text{vs.} \quad M_T \gtrsim 2 \text{ TeV}$$

## Minimal composite Higgs



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$$\rightarrow \frac{v^2}{f^2} = \sin^2 \frac{\langle h \rangle}{f} = \frac{1}{2\delta} \quad \boxed{1/\delta \lesssim 0.24} \quad |\delta \kappa_V| \simeq \frac{v^2}{2f^2} \lesssim 6\%$$

$$\rightarrow \frac{m_h^2}{M_T^2} = \kappa \underbrace{\frac{y_t^2 N_c}{4\pi^2} \left( 1 - \frac{1}{2\delta} \right)}_{\sim 7\%} \quad \boxed{\kappa \lesssim 0.06} \quad M_T \gtrsim 2 \text{ TeV}$$

Few percent fine-tuning wrt  $\delta \lesssim 1$ ,  $\kappa \simeq 1$  expectation

## Structurally small $v_{ev}$

radiatively stable deepest minimum  
close to the origin



# Radiatively stable potentials

Explicit  $SO(5) \rightarrow SO(4)$  breaking by an irrep spurion  $K$ :

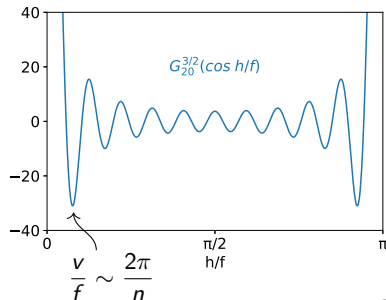
$$K^{i_1 \dots i_n} \phi_{i_1} \cdots \phi_{i_n} \quad (\text{symmetric traceless})$$

$$\vec{\phi} \equiv \left( \frac{\vec{h}}{h} \sin \frac{h}{f}, \cos \frac{h}{f} \right), \quad h \equiv |\vec{h}|$$

No other invariant, linear in  $K$ , can be constructed,  
so all-loop linear renormalisation can only be multiplicative.

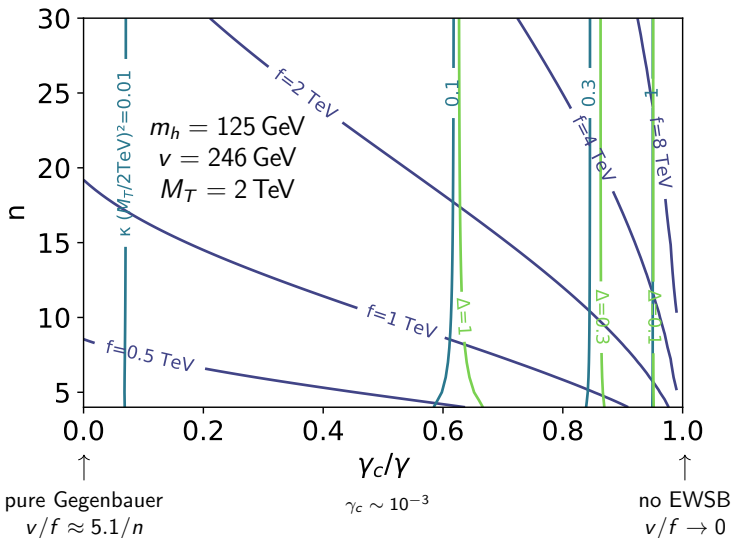
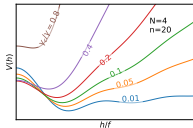
Actually, Gegenbauer polynomials:

$$K^{i_1 \dots i_n} \phi_{i_1} \cdots \phi_{i_n} \propto G_n^{3/2}(\cos \frac{h}{f})$$



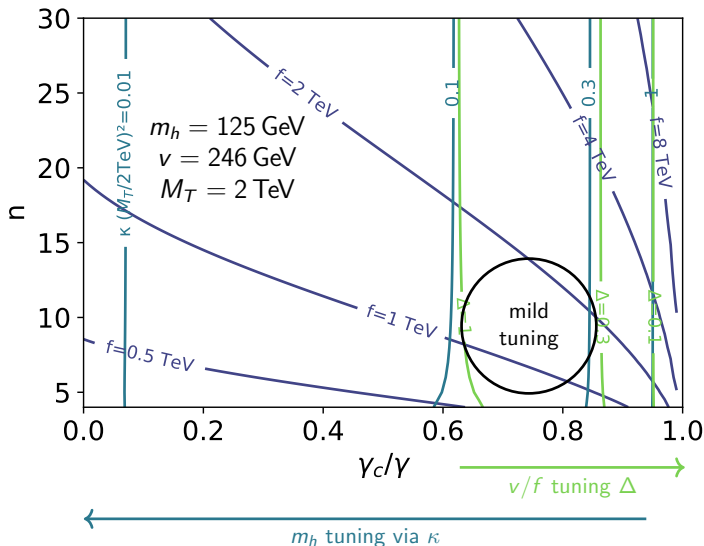
# The Gegenbauer Higgs

$$V(h) = \kappa \frac{N_c y_t^2}{16\pi^2} f^2 M_T^2 \left[ \sin^2 \frac{h}{f} + \gamma G_n^{3/2} \left( \cos \frac{h}{f} \right) \right]$$



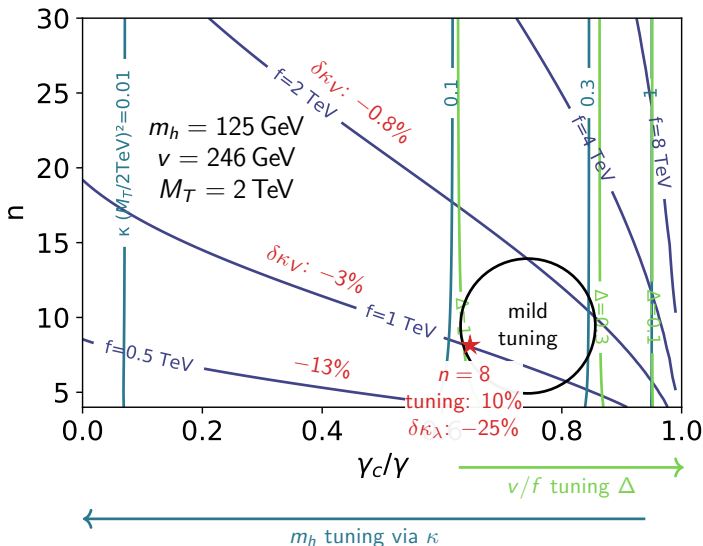
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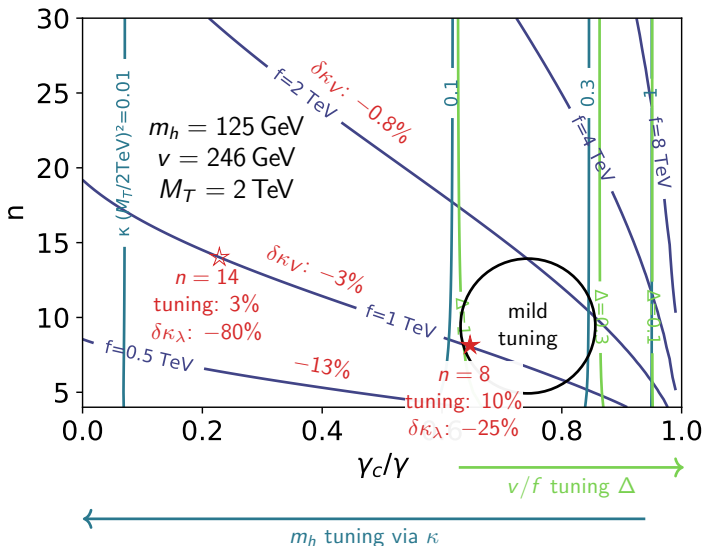
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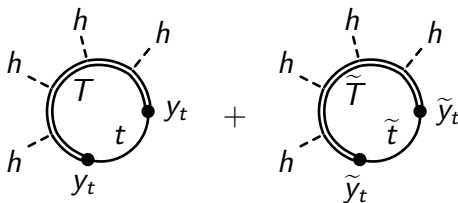




# Structurally smaller mass

[Chacko, Goh, Harnik '05]

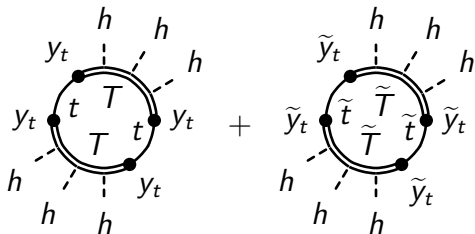
[Barbieri, Greco, Rattazzi, Wulzer '15]



$$\frac{N_c y_t^2}{16\pi^2} f^2 M_T^2 \sin^2 \frac{h}{f} + \frac{N_{\tilde{c}} \tilde{y}_t^2}{16\pi^2} f^2 M_{\tilde{T}}^2 \cos^2 \frac{h}{f}$$

if twin parity enforces  $y_t = \tilde{y}_t$  and  $M_T = M_{\tilde{T}}$   
no  $M_T^2$  sensitivity

# Structurally smaller mass



$$\frac{N_c y_t^4}{16\pi^2} f^4 \sin^4 \frac{h}{f} \log M_T \quad + \quad \frac{N_c \tilde{y}_t^4}{16\pi^2} f^4 \cos^4 \frac{h}{f} \log M_{\tilde{T}}$$

retaining  $\log M_T$  sensitivity only

# Gegenbauer's Twin

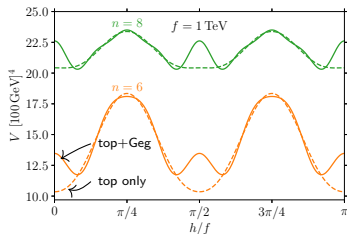
- global  $SO(8) \supset SO(4) \times \widetilde{SO(4)}$
- spontaneous  $SO(8) \rightarrow SO(7)$ 
  - 7 NGBs
  - 6 eaten by  $W^\pm, Z$  and  $\widetilde{W}^\pm, \widetilde{Z}$
  - 1 Higgs:  $\vec{\phi} = (\vec{0}_3, \sin \frac{h}{f}; \vec{0}_3, \cos \frac{h}{f})^T$  in unitary gauge



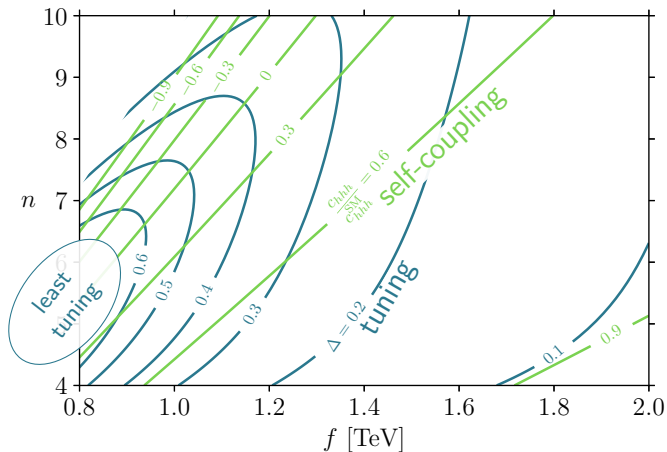
Leopold B. Gegenbauer  
1849–1903

- minimal explicit breaking is insufficient

- explicit  $SO(8) \rightarrow SO(4) \times \widetilde{SO(4)}$ 
  - radiative stability from irrep spurion
  - $G_n^{3/2}(\cos \frac{2h}{f})$  potential

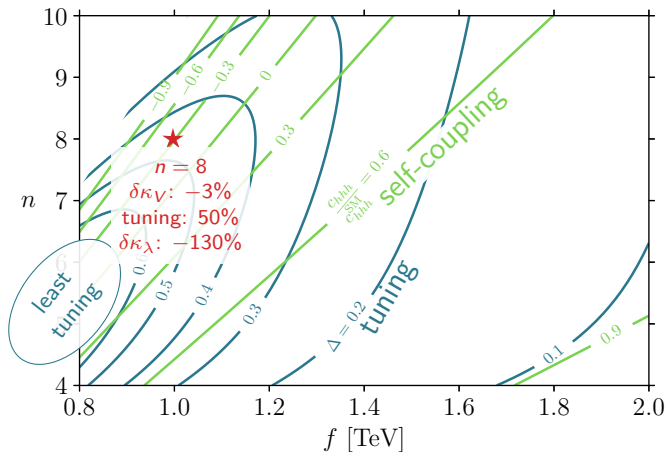


# Gegenbauer's Twin



(and possibly large  $M_T$ , with unitarity violating  $H$  scattering towards 6 TeV)

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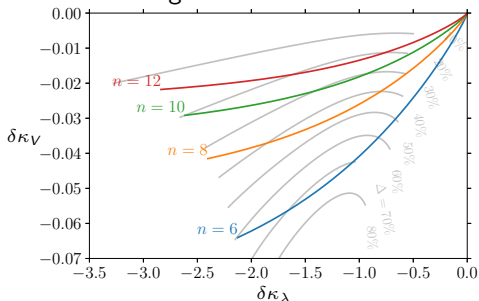


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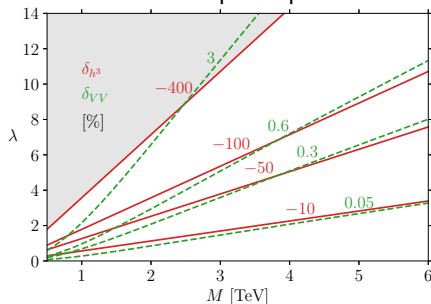
# Structurally large $\delta\kappa_\lambda/\delta\kappa_V$

see also: [Di Luzio, Gröber, Spannowsky '17]  
 [Gupta, Rzehak, Wells '13] [Falkowski, Rattazzi '19]  
 [Logan, Rantala '15] [Chala, Krause, Nardini '18] [etc.]

Gegenbauer's Twin



custodial weak-quadruplet scalar



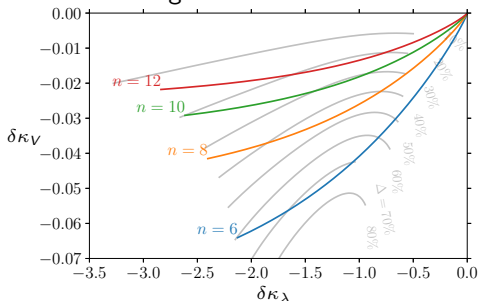
$$\lambda H^* H^* (\epsilon H) \Phi + \lambda \frac{1}{\sqrt{3}} H^* H^* H^* \tilde{\Phi}$$

- a loop factor allowed dimensionally (or  $v^2/M_\chi^2$  if dim-6/dim-8)
- $\text{dim} \gg 6$  operators may be very relevant
- vacuum stability as limiting constraint

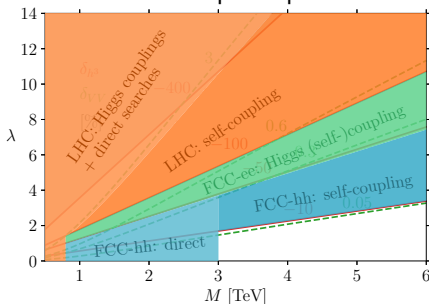
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Gegenbauer's Twin



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## Higgs theory facing data

An example Higgs theory exists with structural  $\frac{m_h^2}{M_X^2} \sim \%$

structural  $\delta\kappa_V \sim \%$

structural  $\frac{\delta\kappa_V}{\delta\kappa_\lambda} \sim \%$  (bonus)

Namely, a composite Higgs scenario with non-minimal global symmetry breaking source.

In passing, we determined the pNGB potentials that are eigenfunctions of linear renormalisation.

A custodial quadruplet scalar also achieves  $\frac{\delta\kappa_V}{\delta\kappa_\lambda} \sim \%$ .



Extras

## Radiatively stable $SO(5) \rightarrow SO(4)$ potentials (II)

Linear one-loop correction to  $V(\frac{h}{f})$ :

$$\frac{\Lambda^2}{32\pi^2 f^2} \left( V''' + 3 \cot \frac{h}{f} V' \right)$$

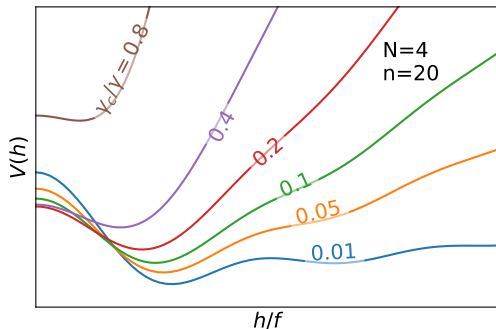
Radiative stability at one-loop and linear order order if  $\propto V$

Differential equation of Gegenbauer polynomials

$$V\left(\frac{h}{f}\right) \propto G_n^{3/2}\left(\cos \frac{h}{f}\right)$$

## Gegenbauer Higgs potential

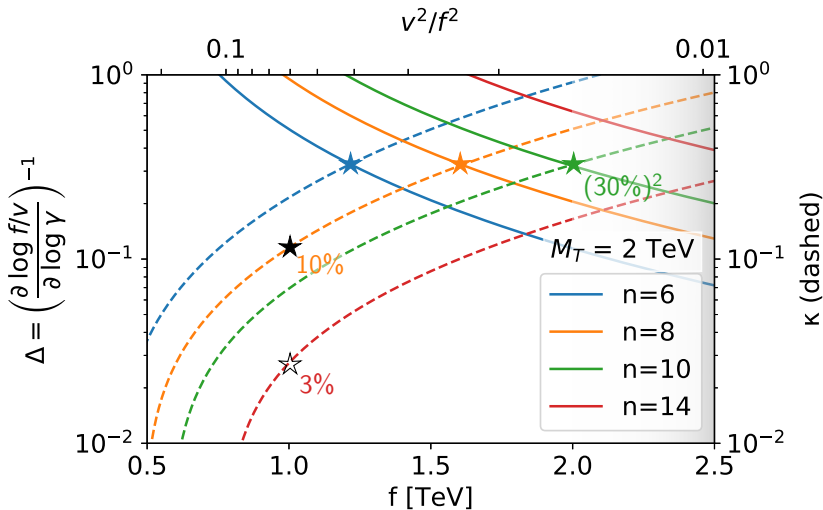
$$V(h) = \kappa \frac{N_c y_t^2}{16\pi^2} f^2 M_T^2 \left[ \sin^2 \frac{h}{f} + \gamma G_n^{3/2} \left( \cos \frac{h}{f} \right) \right]$$



$$v/f \rightarrow 0 \quad \text{as} \quad \gamma \rightarrow \gamma_c$$

$$\frac{m_h^2}{\kappa \frac{N_c y_t^2}{16\pi^2} M_T^2} \rightarrow \quad \text{as} \quad \gamma \rightarrow \gamma_c \quad \text{relaxing} \quad \kappa \rightarrow 1$$

# Gegenbauer Higgs tunings

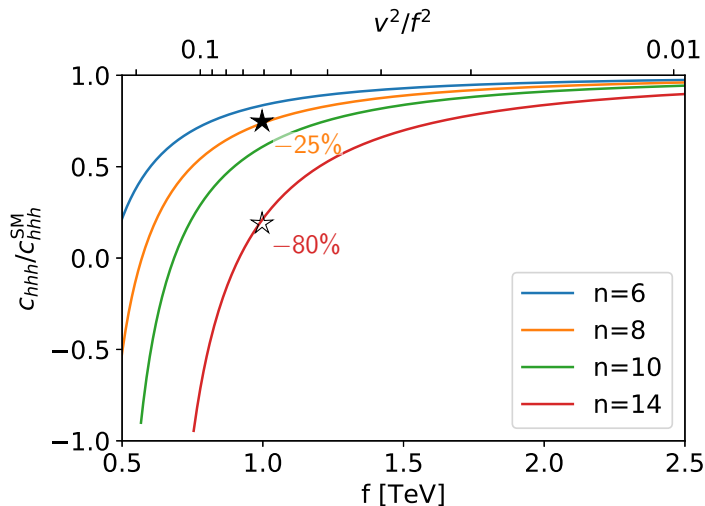


$$\Delta \approx 30\% \left(\frac{f}{4v} \frac{5.1}{n}\right)^{-2.1}$$

$$\kappa \approx 30\% \left(\frac{f}{4v} \frac{5.1}{n} \frac{2 \text{ TeV}}{M_T}\right)^2$$

$(M_T \gtrsim y_t f / \sqrt{2} \text{ since } m_t \sim M_T v / f \text{ for } y_t f \gg M_T)$

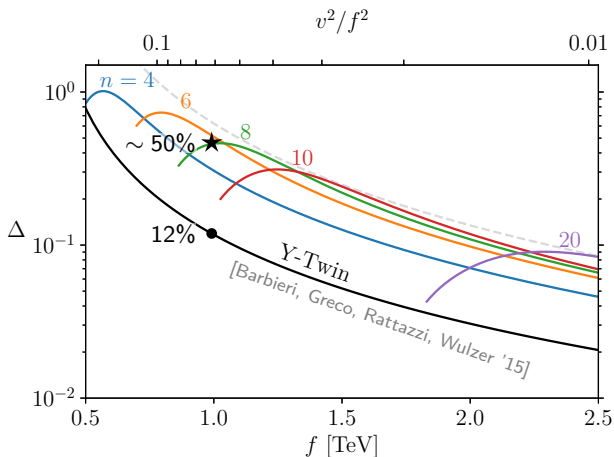
# Gegenbauer Higgs self-coupling



$$\frac{C_{hhh}}{C_{hhh}^{SM}} \approx 1 - 1.2 \left( \frac{f}{v} \frac{5.1}{n + \lambda} \right)^{-2} \quad \text{when close to 1}$$

## Gegenbauer's Twin tunings

- conservative definition RMS(eig. log-derivative matrix)
- dominated by top-sector dependence of  $v/f$
- about 4 times better than usual  $\Delta \approx 2v^2/f^2$  minimum



# Gegenbauer's Twin self-coupling

