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# Parton Showers at zero temperature

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#### **Parton Showers**

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PS dresses hard process with soft and collinear gluons/quarks; Probabilities given by soft/collinear splitting kernels:  $|\mathcal{M}_{qqg}|^2 \approx 2 \frac{p_i p_k}{(p_i p_j)(p_j p_k)} |\mathcal{M}_{qq}|^2 \qquad |\mathcal{M}_{qqg}|^2 \approx \frac{P_{qq}(z)}{2(p_i p_j)} |\mathcal{M}_{qq}|^2$ 

> Momentum conservation must be enforced! Need on-shell momentum mapping from n+1 to n parton configurations

Interfacing to (N)NLO calculation needs PS matching to remove double counting  $\rightarrow$  See Talks by <u>Frederico</u> <u>Buccioni</u>, <u>Giulia Zanderighi</u>, ...

PS resums large logarithms, but to what order?

#### **Parton Showers**



#### **Parton Showers**

Color coherent evolution Backward evolution	ME correction Color dipole formalism Spin correlations	Color dipole showers	LO merci.	NLO matching Dipole_In	Antenna showers NLO merging Color	NNLO ME corrections Inteshold effects NLO splitting kernels Higher order of	Accuracy quantification	NLL & NGLS in one framewor Efficient 1/Nc corrections	
1985	1990	1995	2000	2005	2010	2015	2018	2022	

Many developments, but the basics are still the same!

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#### Algorithms used in Practice

We have a good selection of Parton Showers for LHC simulations, allowing for cross-checks and some uncertainty estimates

Project	Evolution variable	Coherence	References
Herwig++	Angle or Dipole-k $_{\perp}$	Angular Ordering / Dipole	[Marchesini, Webber <u>Nucl. Phys. B (1988), 461]</u> [Corcella et al. <u>arXiv:hep-ph/0011363]</u>
Pythia	(Dipole-)k $_{\perp}$	Dipole	[Sjöstrand, Skands <u>hep-ph/0408302]</u> [Höche, Prestel <u>1506.05057</u> ] (Dire)
Sherpa	(Dipole-)k $_{\perp}$	Dipole	[Schumann, Krauss <u>0709.1027]</u> [Höche, Prestel <u>1506.05057]</u> (Dire)
Vincia	Dipole-k $_{\perp}$	(Sector) Antenna	[Giele, Kosower, Skands <u>0707.3652, 1102.2126]</u>

The agreement between Vincia's antenna shower and the more standard dipole showers validates the dipole approximation

# Comparisons

One way to assess the reliability of parton showers is to compare their predictions [Buckley et al. <u>2105.11399</u>] [Bellm et al. <u>1903.12563</u>]

 $\rightarrow$  Non-trivial, all parameters and hidden assumptions must be the same

NLOPS and NNLO agree reasonably well in most of the phase space

Throughout most of the phase space, different showers show reasonable agreement

PS variation are of similar size as scale variations





Where would we like to be in 10 years from now?

Comparing different parton showers to each other is not a good way to estimate uncertainties

 $\rightarrow$  We need (parametric) uncertainty bands!

We need to make use of the plethora of fixed-order calculations

 $\rightarrow$  Matching!

Parton Showers naively only capture the leading soft and collinear behaviour correctly

 $\rightarrow$  We need to study next-to-leading power corrections!

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The way to go is to construct parton showers at NLO and (N)NLL

 $\rightarrow$  Lot's of recent developments

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People are working towards NNLO matching and even N3LO!

 $\rightarrow$  Lot's of recent developments

Systematic studies of subleading power effects in different kinematics mappings need to be conducted



# (N)NNLO Matching Updates







Geneva uses known resummation in jettiness/qT and matches to NNLO [Aioli, Broggio, Gavardi, Kallweit, Lim, Nagar, Napoletano, Rottoli <u>2102.08390</u>]

Allows choice of resolution variable and assessment of shower scheme uncertainty

See Davide Napoletano's <u>Talk at HP2</u>





New results on di-photon production at NNLO [Galvari, Oleari, Re <u>2204.12602]</u>

and WZ production at NNLO QCD/NLO EW using the MiNNLOPS Method [Lindert, Lombardi, Wiesemann, Zanderighi, Zanoli <u>2208.12660</u>]

Work towards fully differential matching at NNLO in Vincia [Campbell, Höche, Li, Preuss, Skands <u>2108.07133</u>]

Shower matches NNLO singularity structure, "POWHEG @NNLO"

See Christian Preuss' <u>Talk at HP2</u>



$$\langle O \rangle_{\rm NNLO+PS}^{\rm VINCIA} = \int d\Phi_2 \, B(\Phi_2) \underbrace{k_{\rm NNLO}(\Phi_2)}_{\rm local \ K-factor} \underbrace{\mathcal{S}_2(t_0, O)}_{\rm shower \ operator}$$



First N3LO parton shower matching:

**TOMTE** [Prestel <u>2106.03206]</u>, [Bertone, Prestel <u>2202.01082]</u>

Matching to inclusive results
 Extension of UN2LOPS







Shower precision not there yet, but we would like to use the best perturbative precision available

TOMTE can work with any parton shower!



# **NLL Parton Showers**

Criteria for NLL accuracy at leading color outlined in: [Dasgupta,Dreyer,Hamilton,Monni,Salam,Soyez 2002.11114]

Where do the logarithms come from? (see also [Banfi, Salam, Zanderighi <u>hep-ph/0407286]</u>)

Depends on logarithmic variables of emission pairs:

Energies/Angles	Distinctly different	Comparable
Distinctly different	LL	NLL
Comparable	NLL	NNLL

Shower needs to reproduce the correct tree-level ME squared in these regions

Shower needs to reproduce results of analytic resummation of rIRC observables

 $\ln k_{\perp}/Q$ 

• 1

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• 1

• 2

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$$k = zp_{+} + 2\frac{|k_{\perp}^{2}|}{2zp_{+} \cdot p_{-}}p_{-} + k_{\perp} \qquad t \sim |k_{\perp}^{2}|e^{-2\beta y}$$

Project	Ordering	Recoil -	Recoil ⊥	Tests	Refs.
Herwig	Angle	Global	Local	Analytical for global observables, Phase space not covered in non-global case	[Marchesini, Webber <u>Nucl. Phys. B (1988).</u> <u>461]</u>
PanLocal	<b>0 &lt;</b> β < 1	Local	Local	Numerical tests in e+ e-, pp (colour singlet), DIS	[Dasgupta et al. 2002.11114]
PanGlobal	0≤β<1	Local	Global	for a variety of global and non-global observables	
Deductor	β = 1	Global	Local	Analytical and numerical for thrust	[Nagy, Soper <u>2011.04777</u> ]
FHP	β <b>= 0</b>	Global	Global	Analytical and numerical for thrust, multiplicity	[Forshaw, Holguin, Plätzer <u>2003.06400</u> ]
Alaric	β <b>= 0</b>	Global	Global	General, analytical proof for any global rIRC safe observable; Numerical tests for LEP event shapes and y <sub>23</sub>	[Herren et al. <u>2208.06057</u> ]

PanScales has demonstrated NLL accuracy for a wide range of observables in colour singlet production,  $e^+ e^- \rightarrow$  Hadrons and recently DIS/VBF

For Alaric an analytic proof of NLL accuracy for global observables exists (both for IS and FS evolution) & numerical tests in  $e^+ e^- \rightarrow$  Hadrons









Thrust ( $E_{\text{CMS}} = 91.2 \text{ GeV}$ )



#### **NLO Status**

$$D_{ji}^{(2)}(z,\mu) = -\frac{1}{2\varepsilon} P_{ji}^{(1)}(z) + \frac{\beta_0}{4\varepsilon^2} P_{ji}^{(0)}(z) + \frac{1}{2\varepsilon^2} \int_z^1 \frac{\mathrm{d}x}{x} P_{jk}^{(0)}(x) P_{ki}^{(0)}(z/x)$$
$$\leftrightarrow \left( \underbrace{\bigcap_{i} \bigcirc_{j} \frown_{i} z}_{j} + \underbrace{\bigcap_{i} \bigcirc_{j} \frown_{i} z}_{i} + \underbrace{\bigcap_{i} \bigcirc_{j} \frown_{i} z}_{j} \right) \Big/ \underbrace{\bigcap_{i} \frown_{i} \frown_{i} 1}_{i}$$

At NLO, various effects have to be included correctly, avoiding any double counting:

- Iterated LO splittings
- Virtual corrections to splittings
- Genuine triple collinear splittings
- Genuine double soft emissions

#### **NLO Status**

-4 -3.5 -3 -2.5 -2

Studies of triple collinear and double soft effects in Dire:

[Höche, Prestel <u>1705.00742</u>] [Dulat, Höche, Prestel 1805.03757] [Gellersen, Höche, Prestel 2110.05964]



-4

 $\log_{10}(y_{23})$ 

-3.5

-3

-2

 $\log_{10}(y_{34})$ 

-4 -3.5 -2.5 -2 -1.5 -1 -0.5



25

15

10

 $\log_{10} y_{nn+1}$ 

-4

y45

-2.5

-2

-3.5

-0.5

all  $1 \rightarrow 3$ 

. . . . . . . . . . . . . . . . . .

-1.5

-1

 $\log_{10} y_{nn+1}$ 

#### **NLO Status**

Work on higher order splittings on amplitude level: [Löschner, Plätzer, Simpson-Dore <u>2112.14454</u>]

NNLL studies to go beyond CMW coupling: [Dasgupta, El-Menoufi 2109.07496]

$$\begin{split} \mathbf{P} & - \mathbf{P} & \mathbf{P$$

$$\mathcal{B}_{2}^{q,(\mathrm{ab.})}(z) = \left(\frac{\theta^{2}}{\sigma_{0}}\frac{d^{2}\sigma}{dzd\theta^{2}}\right)^{\mathrm{d-r}} - \left(\frac{\theta^{2}}{\sigma_{0}}\frac{d^{2}\sigma}{dzd\theta^{2}}\right)^{\mathrm{s-o}} + \left(\frac{\theta^{2}}{\sigma_{0}}\frac{d^{2}\sigma}{dzd\theta^{2}}\right)^{\mathrm{r-v}}$$

$$= \left(\frac{C_{F}\alpha_{s}}{2\pi}\right)^{2} \left(\frac{1+z^{2}}{1-z}\left(-3\ln z + 2\mathrm{Li}_{2}\left(\frac{z-1}{z}\right) - 2\ln z\ln(1-z)\right) - 1 + H^{\mathrm{fin.}}(z)\right).$$

$$(3.46)$$

$$(3.47)$$

# Conclusions

There have been a lot of exciting developments on parton showers in recent years!

- We are getting close to fully differential NNLO matching
- We are on a good way to understand Parton Showers at NLL

However, a lot of work remains:

- Showers at NLO are not quite there yet
- Massive quarks need to be included consistently, velocity logarithms, Quarkonia?
- NLP corrections might be necessary
- Can we do MC@NNLO?
- Most importantly: Implementation and Validation for use by experiments





# Backup

#### Soft Radiation in Alaric



#### **Recoil in Alaric**



#### **Recoil in Alaric**

Momentum mapping works for initial and final state emitters/spectator  $\rightarrow$  e+ e-, pp, DIS, ... all treated on same footing



#### NLL Proof for Alaric

Recoil distributed to remaining momenta through Lorentz Transformation:

$$p_l^{\mu} \to \Lambda_{\nu}^{\mu}(K, \tilde{K}) p_l^{\nu}$$

Suppressed by

 $\mathcal{O}(k_{\perp}/K)$ 

$$\begin{split} & \overset{\text{Define}}{X^{\mu}} = p^{\mu}_{j} - \left(1 - z\right) \tilde{p}^{\mu}_{i} \\ & = v \left( \tilde{K}^{\mu} - \left(1 - z + 2\kappa\right) \tilde{p}^{\mu}_{i} \right) + k^{\mu}_{\perp} \end{split}$$

$$\Lambda^{\mu}_{\nu}(K,\tilde{K}) = g^{\mu}_{\nu} + \tilde{K}^{\mu}A_{\nu} + X^{\mu}B_{\nu}$$
$$A^{\nu} = 2\left[\frac{(\tilde{K}-X)^{\nu}}{(\tilde{K}-X)^{2}} - \frac{(\tilde{K}-X/2)^{\nu}}{(\tilde{K}-X/2)^{2}}\right] \quad B^{\nu} = \frac{(\tilde{K}-X/2)^{\nu}}{(\tilde{K}-X/2)^{2}}$$

$$\Lambda^{\mu}_{\nu} \approx g^{\mu}_{\nu} + \frac{K_{\rho} X_{\sigma}}{K^2} T^{\mu\rho\sigma}_{\nu} + \mathcal{O}(k_{\perp}^2)$$

#### **NLL Proof for Alaric**



For one emission kinematic variables in the Lund plane scale like:

$$k_{t,l} \to k'_{t,l} = k_{t,l} \rho^{(1-\xi_l)/a+\xi_l/(a+b)}$$
$$\eta_l \to \eta'_l = \eta - \xi_l \frac{\ln \rho}{a+b}$$
$$\xi_l = \frac{\eta_l}{\eta_{l,\max}}$$

where a = 1 and b = 0 for Alaric

Working in the rest frame of the color dipole, the other momenta scale like:

$$\begin{split} \tilde{p}_l^0 &\sim \rho^{1-\xi_l} \\ \tilde{p}_l^{1,2} &\sim \rho \\ \tilde{p}_l^3 &\sim \rho^{1-\xi_l} \\ \text{for } \rho &\to 0 \end{split}$$

