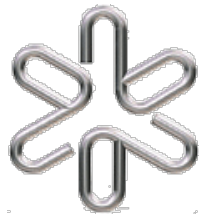


The sharpness of the quark hadron transition and the properties of hybrid stars

F.S. Navarra

University of São Paulo



IFUSP
São Paulo
Brazil

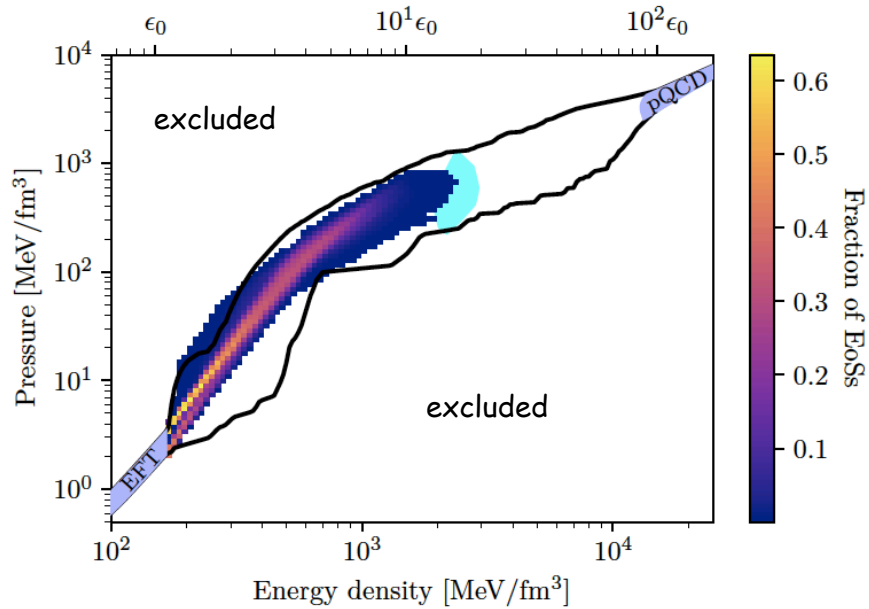
In collaboration with M. Albino, R. Fariello and G. Lugones



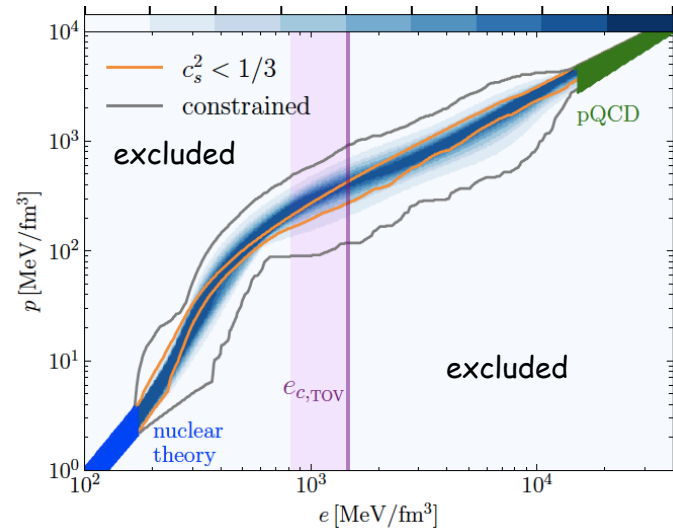
19th International Conference on
QCD in Extreme Conditions (XQCD 2023)

26 – 28 de jul. de 2023
Department of Physics (University of Coimbra)
Fuso horário Europe/Lisbon

The EOS of compact stars



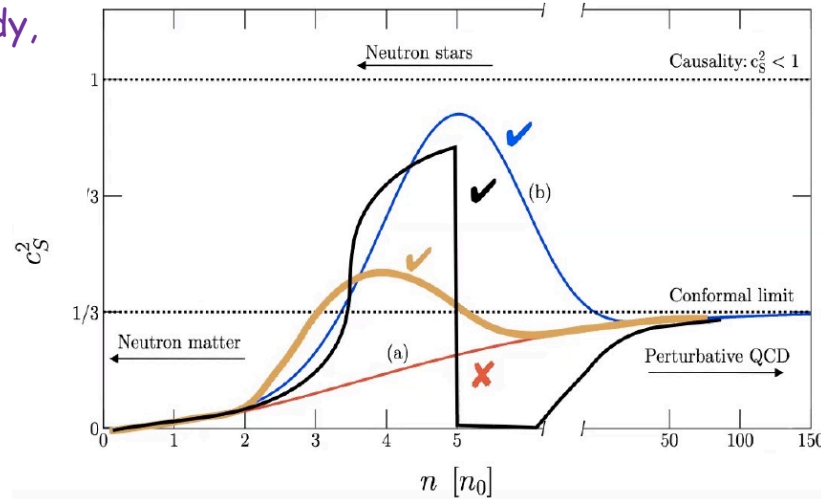
Gorda, Hebeler, Kurkela, Schwenk, Vuorinen,
arXiv:2212.10576



Altiparmak, Ecker, Rezzolla,
arXiv:2212.10576

The speed of sound

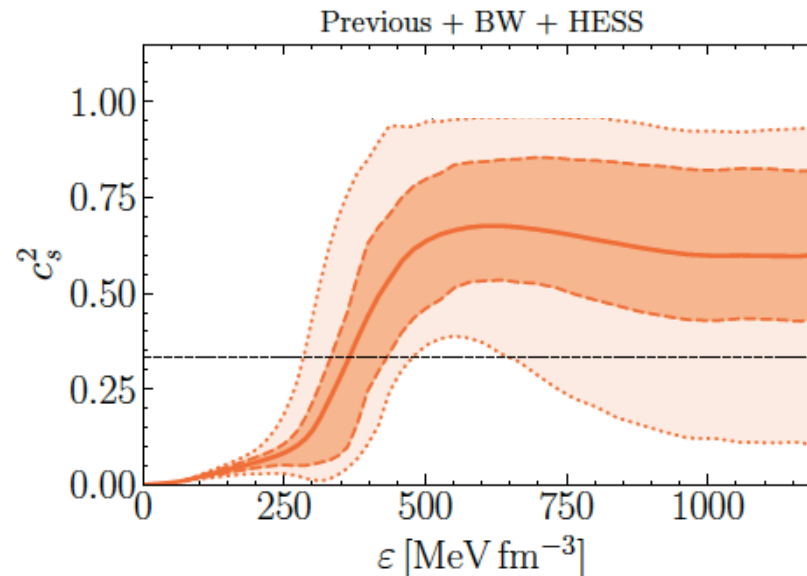
Tews, Carlson, Gandolfi, Reddy,
arXiv:1801.01923



$$c_s^2 = \frac{\partial p}{\partial \epsilon}$$

Brandes, Weise, Kaiser
arXiv:2306.06218

Evidence against a first-order phase transition in neutron star cores:
impact of new data



Can data tell us how sharp is the phase transition in hybrid stars?

Phenomenology of the phase transition

Hadron-Quark Crossover and Massive Hybrid Stars

Masuda, Hatsuda, Takatsuka, arXiv:1212.6803

Two Novel Approaches to the Hadron-Quark Mixed Phase in Compact Stars

Abgaryan, Alvarez-Castillo, Ayriyan, Blaschke, Grigorian, arXiv:1807.08034

On the stability of strange dwarf hybrid stars

Alford, Harris, Sachdeva, arXiv:1705.09880

Tidal deformability with sharp phase transitions in (binary) neutron stars

Han and Steiner, arXiv:1810.10967

Differentiating between sharp and smoother phase transitions in neutron stars

Pereira, Bejger, Zdunik, Haensel, arXiv:2201.01217

Phase Transition Phenomenology with Nonparametric Representations of Neutron Star EOS

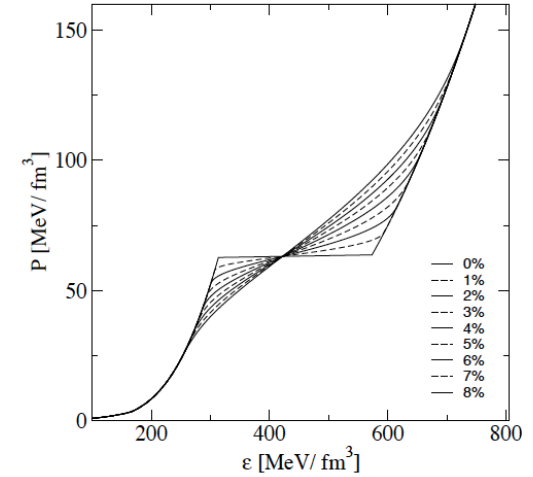
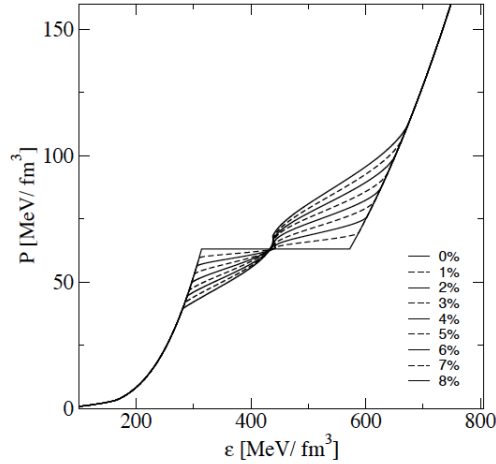
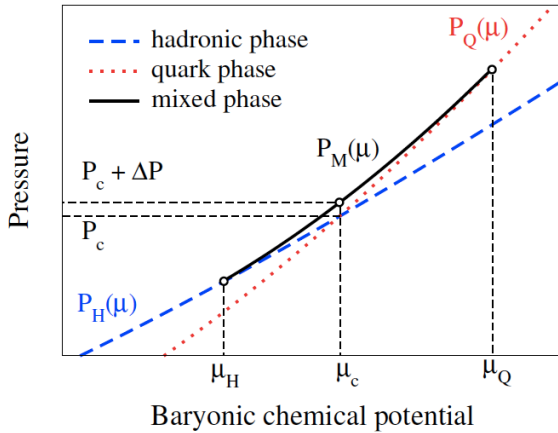
Essick, Legred, Chatziioannu, Han, Landry, arXiv:2305.07411

Evidence against a first-order phase transition in neutron star cores: impact of new data

Brandes, Weise, Kaiser arXiv:2306.06218

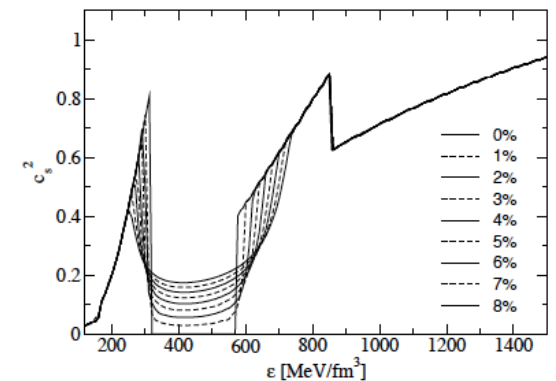
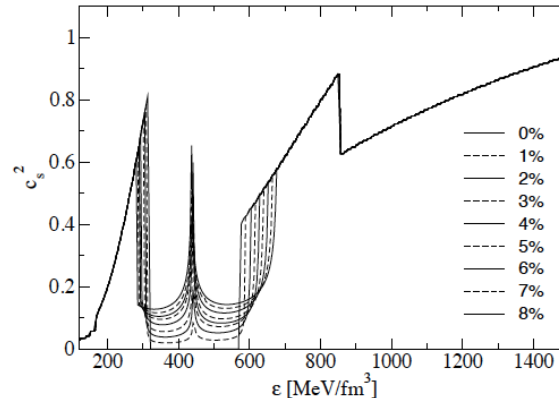
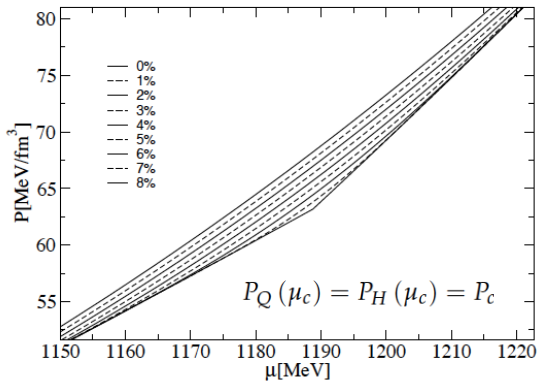
Controlling the sharpness of the transition

Abgaryan, Alvarez-Castillo, Ayriyan, Blaschke, Grigorian, arXiv:1807.08034



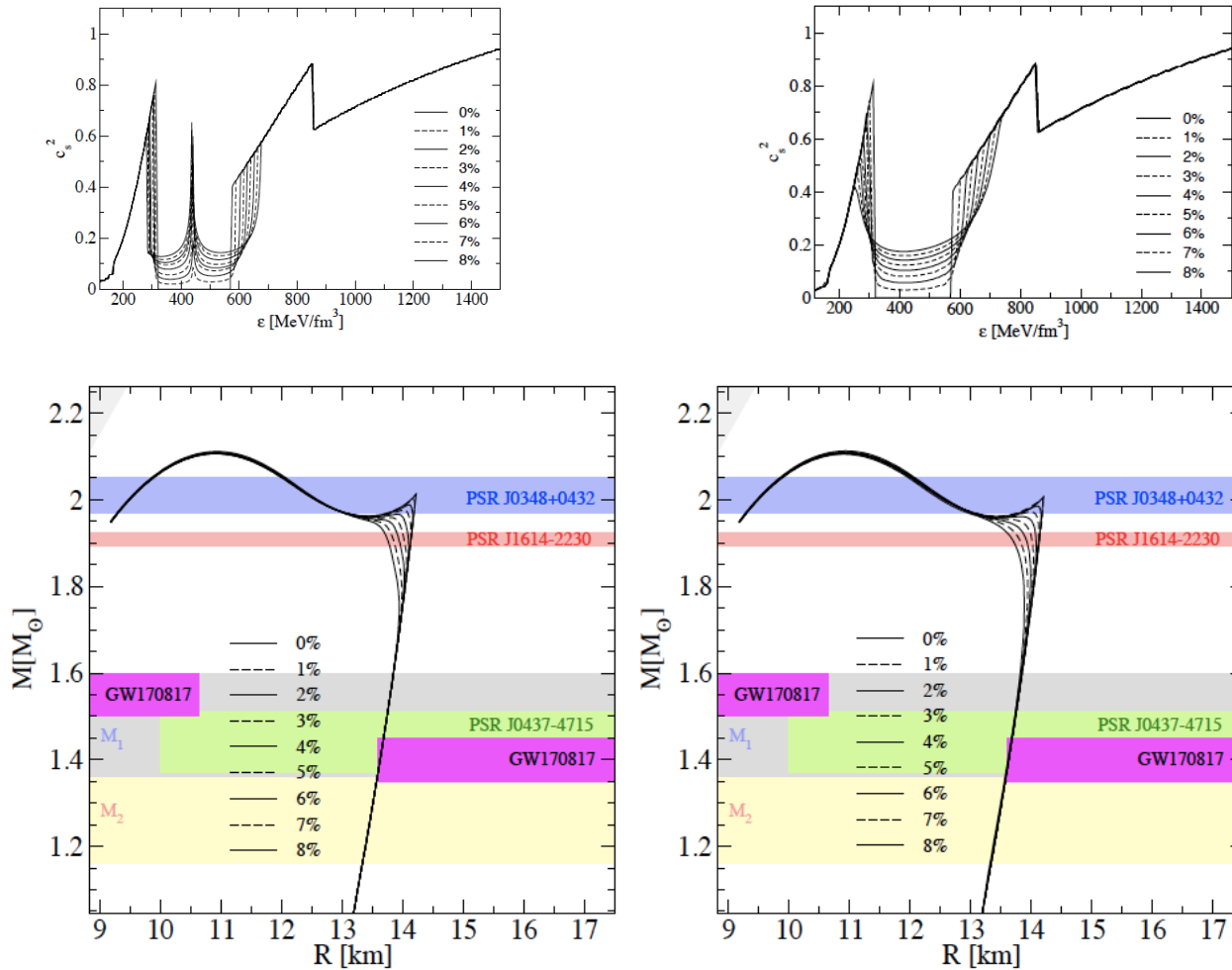
$$P_M(\mu) = \alpha_2 (\mu - \mu_c)^2 + \alpha_1 (\mu - \mu_c) + (1 + \Delta P) P_c$$

$$P(\mu) = P_H(\mu) f_{\text{off}}(\mu) + P_Q(\mu) f_{\text{on}}(\mu) + \Delta(\mu) \Delta P$$

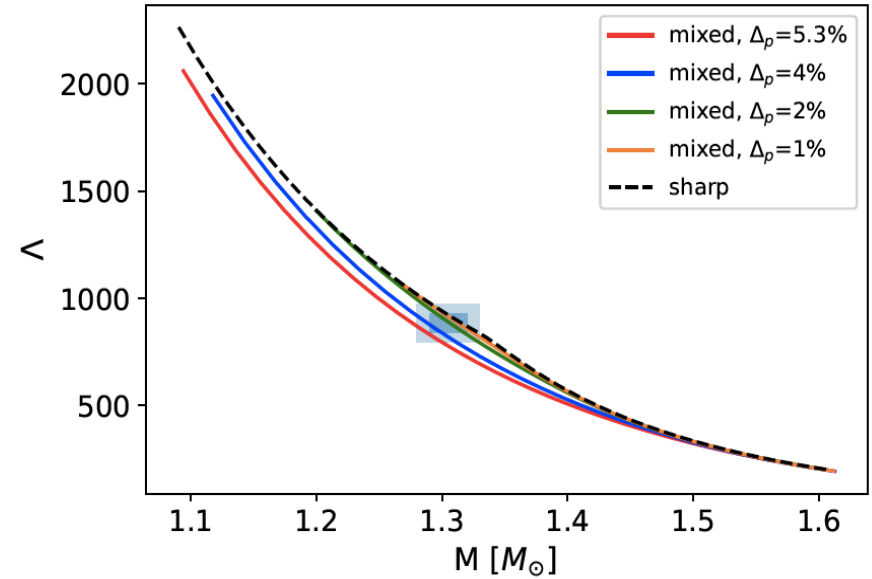
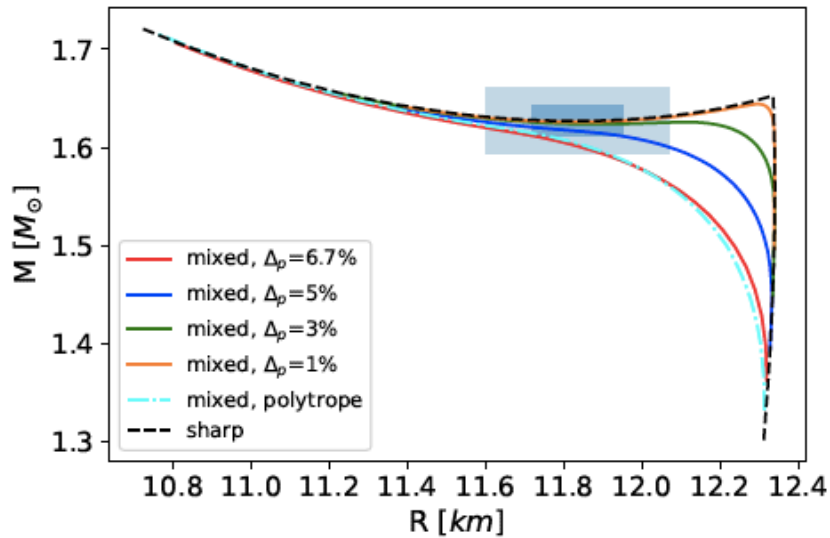


Controlling the sharpness of the transition

Abgaryan, Alvarez-Castillo, Ayriyan, Blaschke, Grigorian, arXiv:1807.08034



Modest changes in the M - R diagram ...



Zhang et al., eXTP, arXiv:1607.08823

Watts et al., eXTP, arXiv:1812.04021

Chatziioannou et al., LIGO, arXiv:2108.12368

Uncertainty less than 5 %

New way of matching the two phases with continuous c_s

$$(P - P_Q)(P - P_H) = \delta^2(\mu_B)$$

$$\delta(\mu_B) = \delta_0 \exp \left[-\frac{(\mu_B - \mu_c)^2}{2\sigma^2} \right]$$

$$\frac{1}{c_s^2} = \frac{\mu}{n} \frac{\partial^2 P}{\partial \mu^2}$$

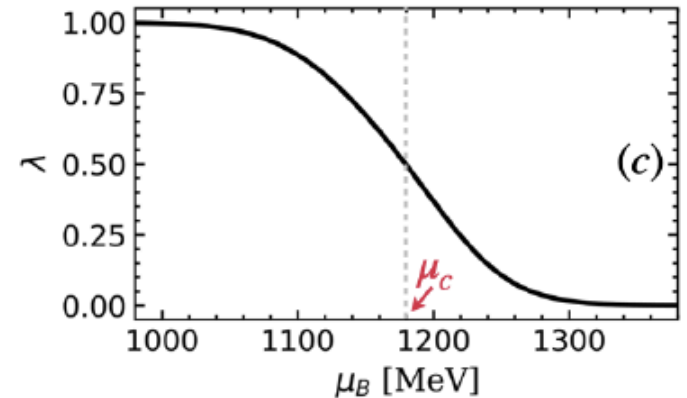
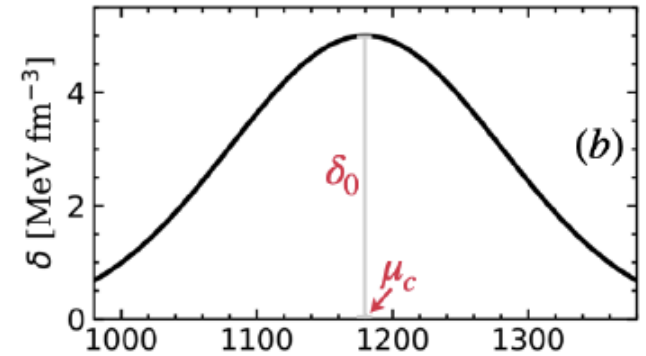
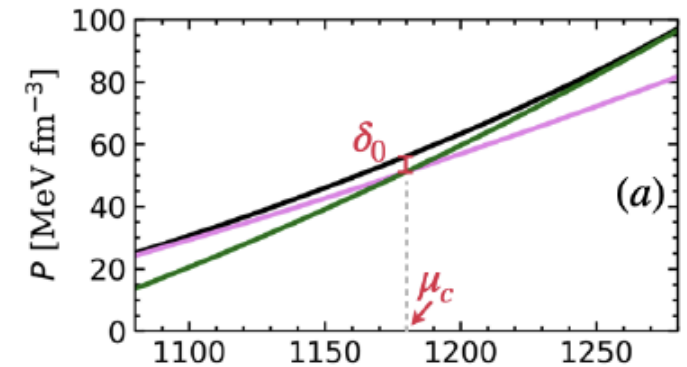
$$P_H(\mu_c) = P_Q(\mu_c)$$

$\sigma =$ width of the transition region

$\delta_0 =$ "overpressure" in the transition

$$P = \lambda P_H + (1 - \lambda) P_Q + \frac{2\delta^2}{\sqrt{(P_Q - P_H)^2 + 4\delta^2}}$$

$$\lambda(\mu_B) = \frac{1}{2} \left[1 - \frac{P_Q - P_H}{\sqrt{(P_Q - P_H)^2 + 4\delta^2}} \right]$$



New way of matching the two phases with continuous c_s

$$n_B = \frac{\partial P}{\partial \mu_B}$$

$$n_B = \lambda n_{B,H} + (1 - \lambda) n_{B,Q} - \frac{(\mu_B - \mu_c)}{2\sigma^2} \frac{\delta^2}{\sqrt{(P_Q - P_H)^2 + 4\delta^2}}$$

$$\delta(\mu_B) = \delta_0 \exp \left[-\frac{(\mu_B - \mu_c)^2}{2\sigma^2} \right]$$

$$\epsilon = -P + \mu_B n_B$$

$$\frac{1}{c_S^2} = \frac{\mu}{n} \frac{\partial^2 P}{\partial \mu^2}$$

The quark EOS

MIT bag model with vector interactions

Lopes, Biesdorf, Menezes, arXiv:2005.13136 ; arXiv: 2005.13552

$$\begin{aligned}\mathcal{L} = & \sum_q \{ \bar{\psi}_q [i\gamma^\mu \partial_\mu - m_q] \psi_q - B \} \Theta(\bar{\psi}_q \psi_q) \\ & + \sum_q g \{ \bar{\psi}_q [\gamma^\mu V_\mu] \psi_q \} \Theta(\bar{\psi}_q \psi_q) + \frac{1}{2} m_V^2 V_\mu V^\mu \\ & + \bar{\psi}_e \gamma_\mu (i\partial^\mu - m_e) \psi_e,\end{aligned}$$

$$m_V V_0 = G_V^{1/2} (n_u + n_d + n_s)$$

$$\Omega = \sum_q \Omega_q^* + B - \frac{1}{2} m_V^2 V_0^2 + \Omega_e$$

$$\mu_q^* = \mu_q - G_V^{1/2} m_V V_0 \quad G_V = \left(\frac{g}{m_V} \right)^2$$

The hadron EOS

Generalized piecewise polytropic (GPP) with continuous speed of sound

O'Boyle, Markakis, Stergioulas and Read, arXiv:2008.03342

Consistent with chiral effective field theory results

$$p(\rho) = K\rho^\Gamma + \Lambda$$

$$\epsilon(\rho) = \frac{K}{\Gamma - 1}\rho^\Gamma + (1 + a)\rho - \Lambda$$

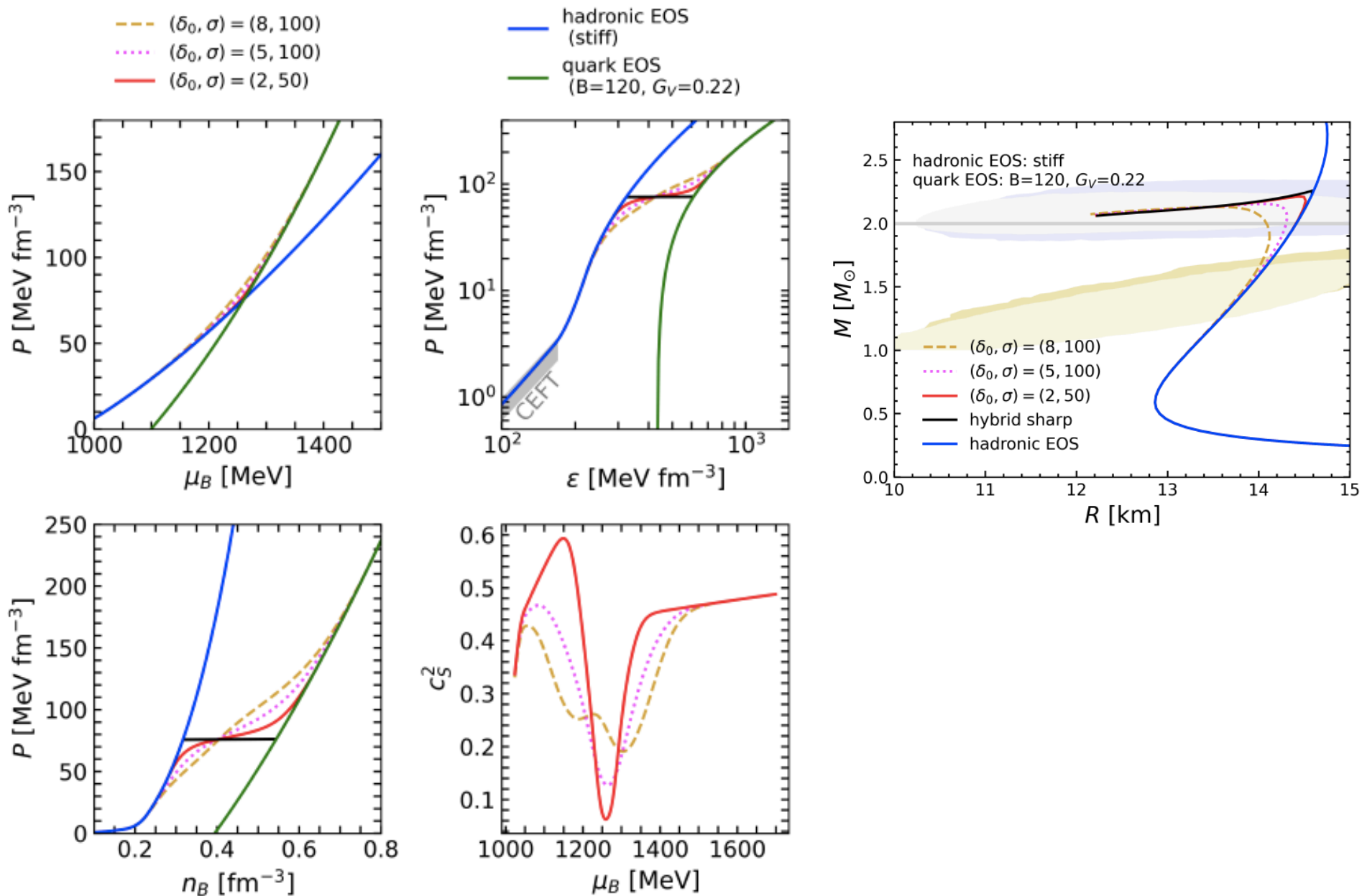
$$c_s = \left[\frac{1}{\Gamma_i - 1} + \frac{1 + a_i}{K_i \Gamma_i \rho^{\Gamma_i - 1}} \right]^{-\frac{1}{2}}$$

Examples of Results

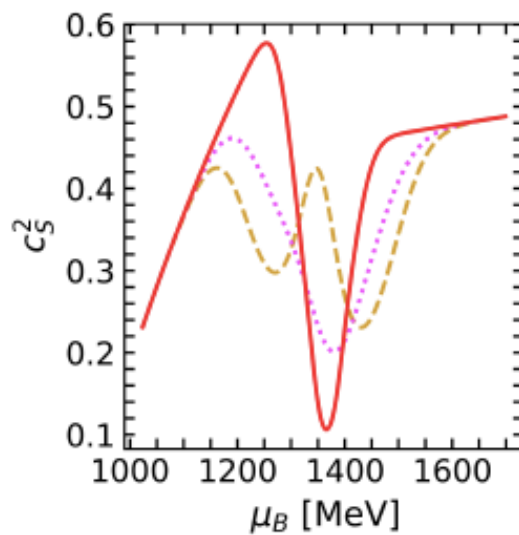
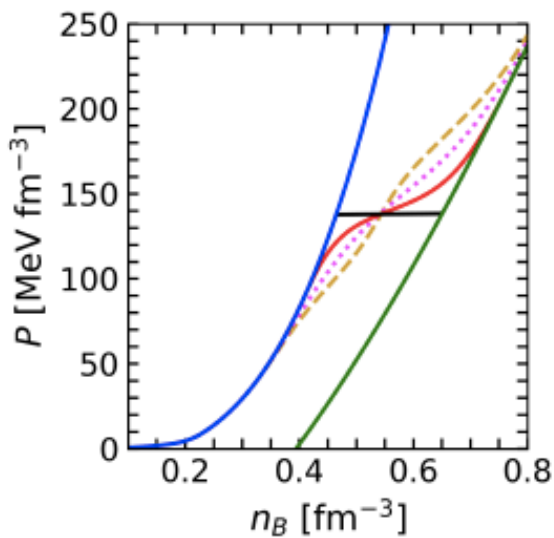
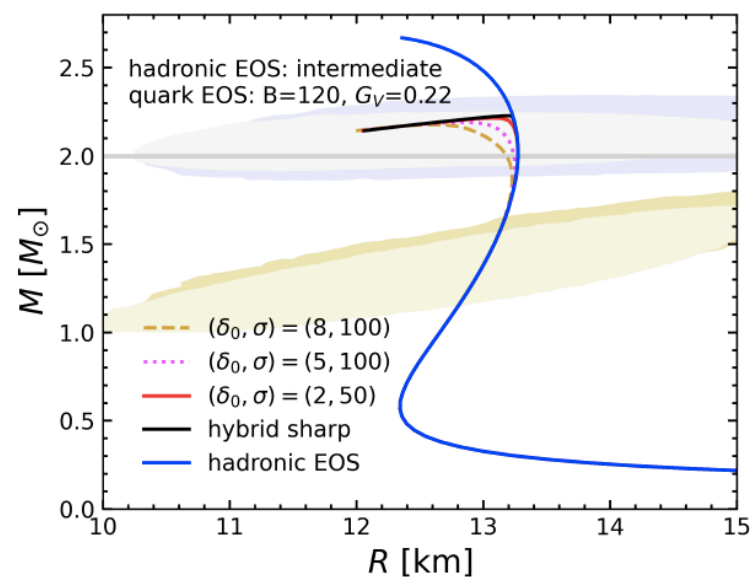
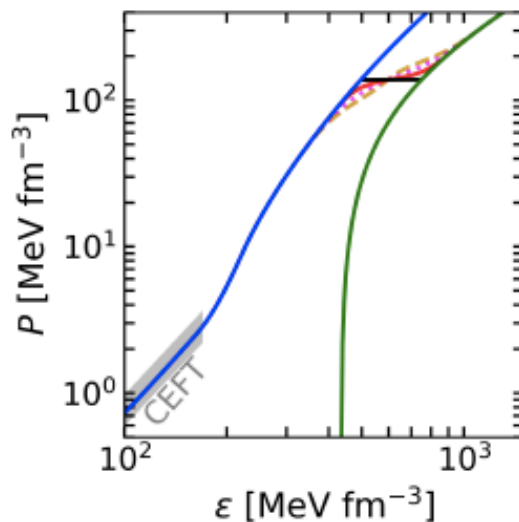
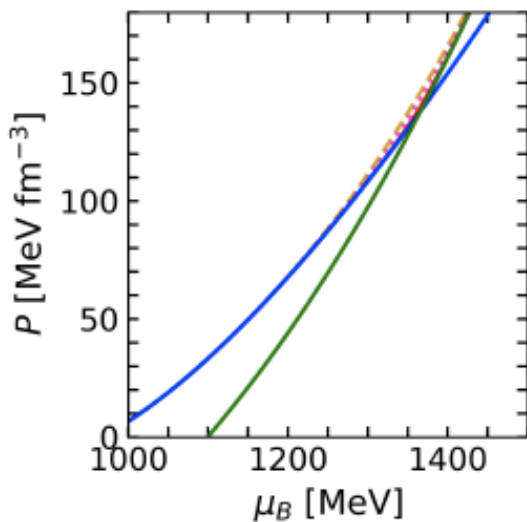
Three hadronic EOS (OMSR soft, intermediate, stiff)

Two quark EOS (B , G_V : softer or stiffer)

Stiff hadron EOS + soft quark EOS



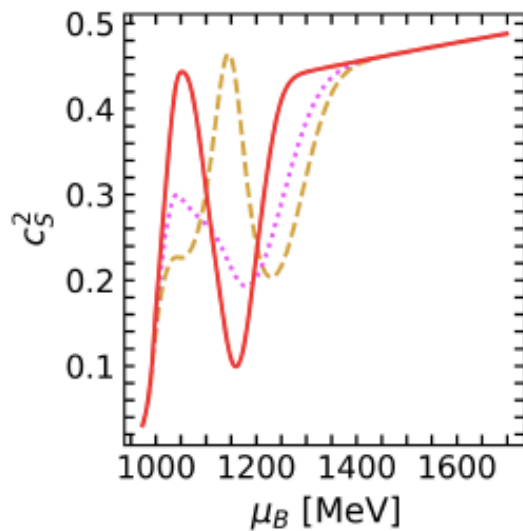
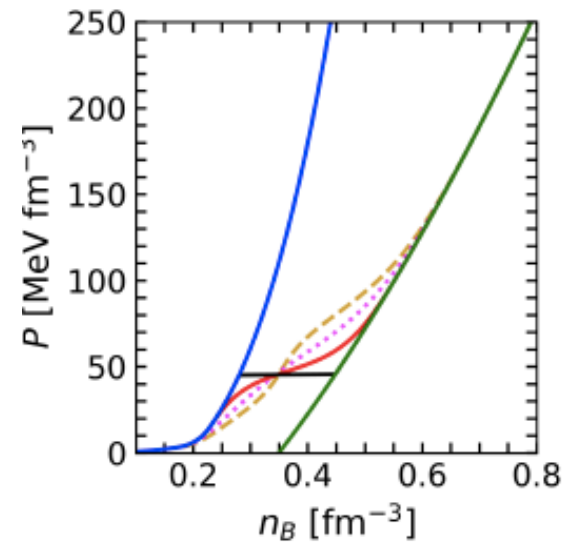
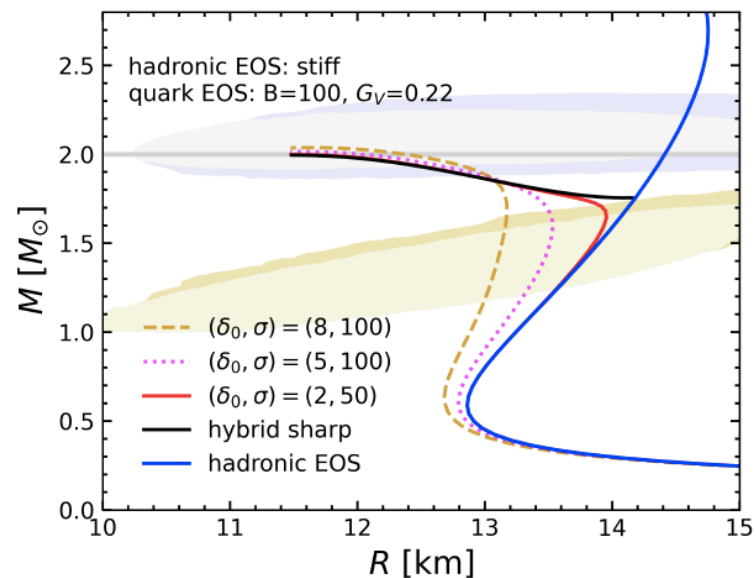
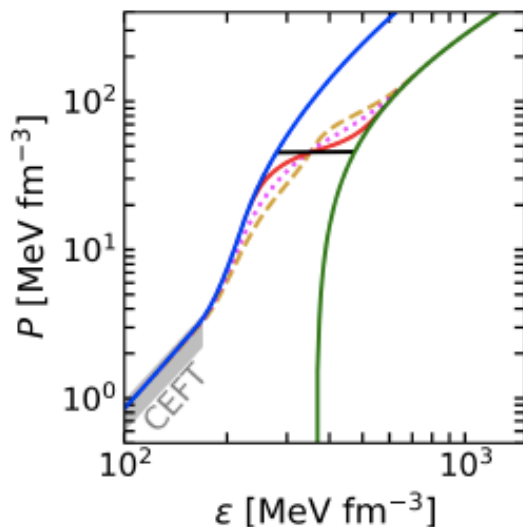
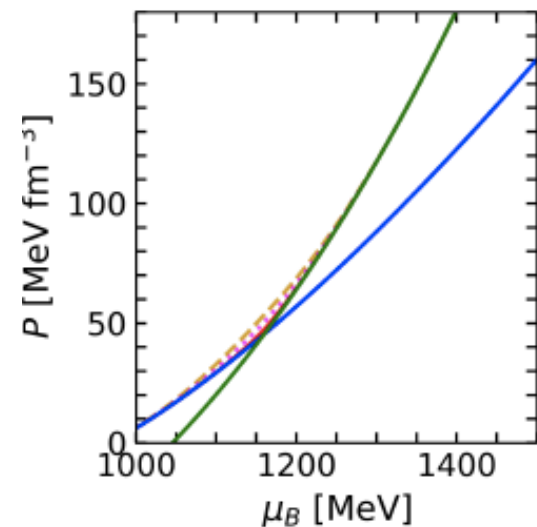
Intermediate hadron EOS + soft quark EOS



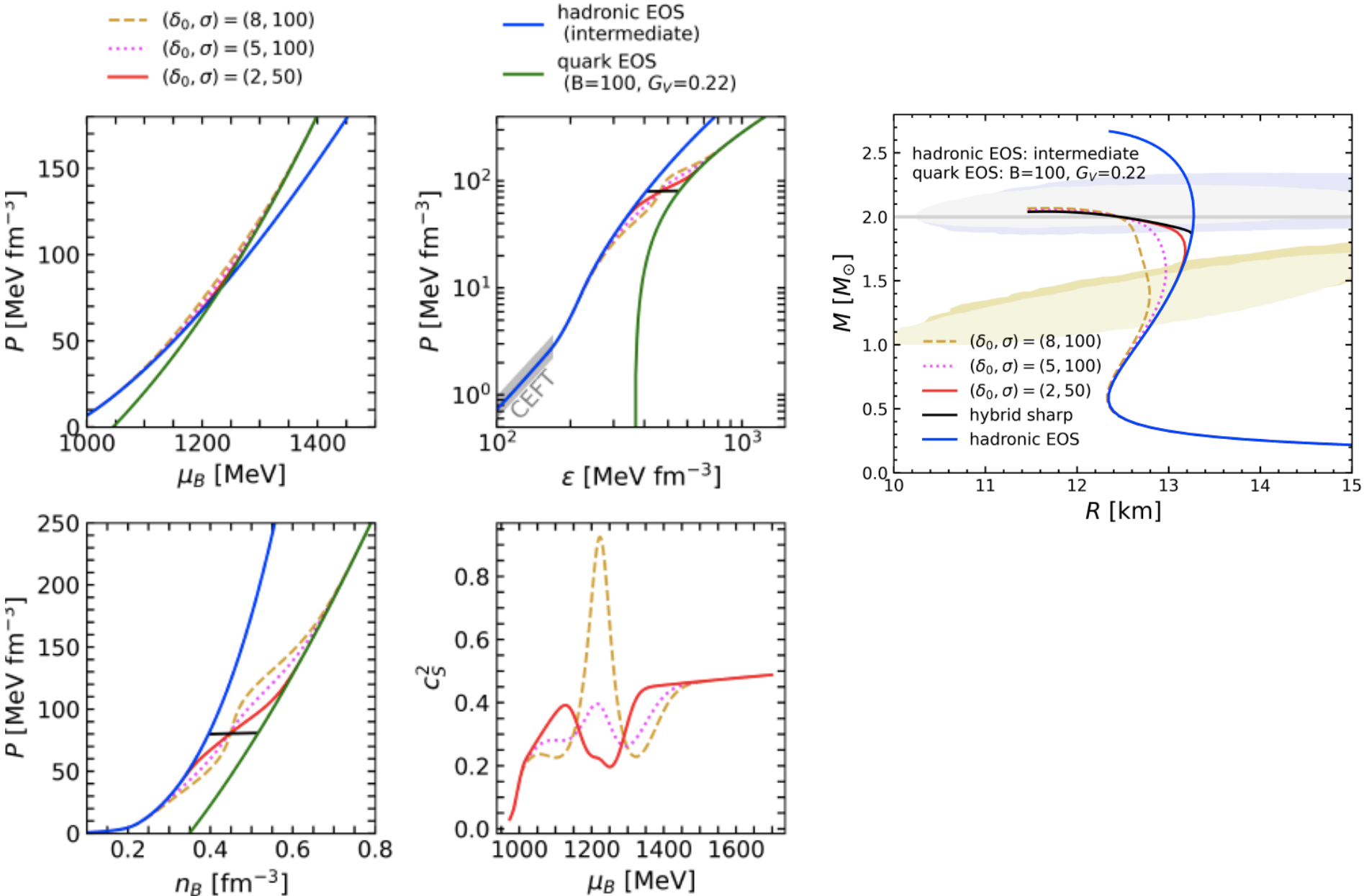
Stiff hadron EOS + stiff quark EOS

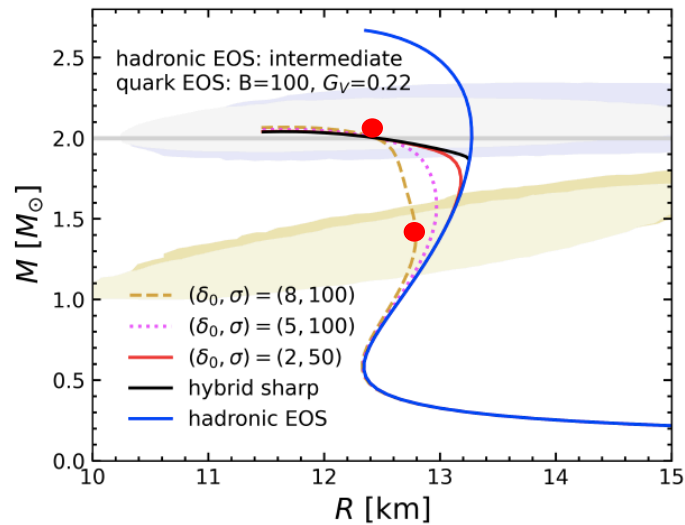
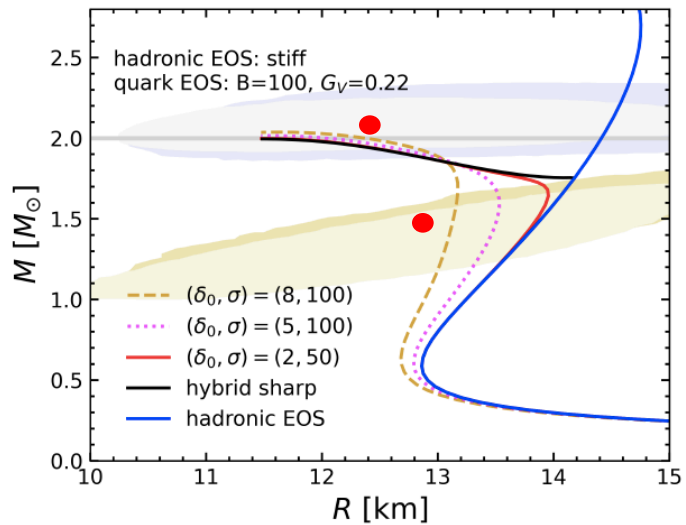
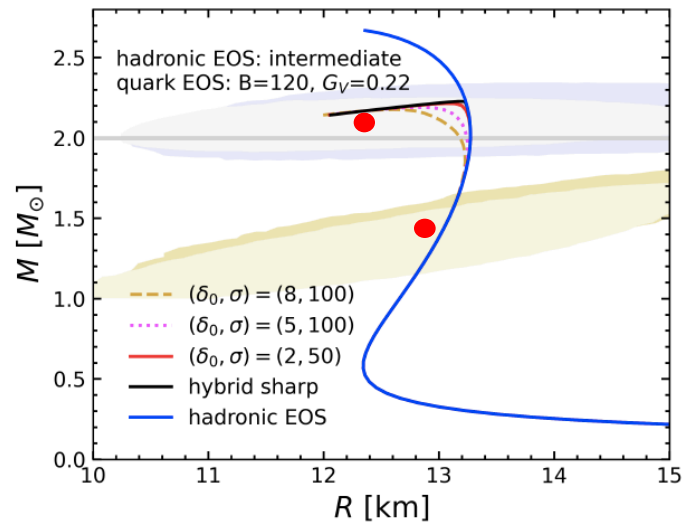
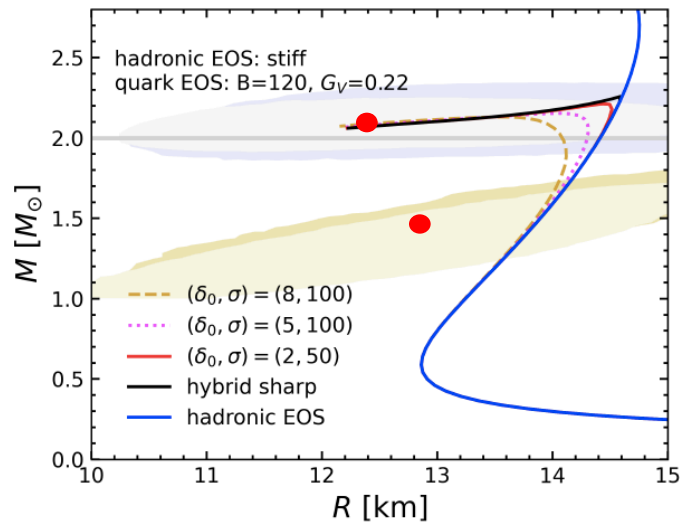
- $(\delta_0, \sigma) = (8, 100)$
- ⋯ $(\delta_0, \sigma) = (5, 100)$
- $(\delta_0, \sigma) = (2, 50)$

- hadronic EOS (stiff)
- quark EOS ($B=100, G_V=0.22$)

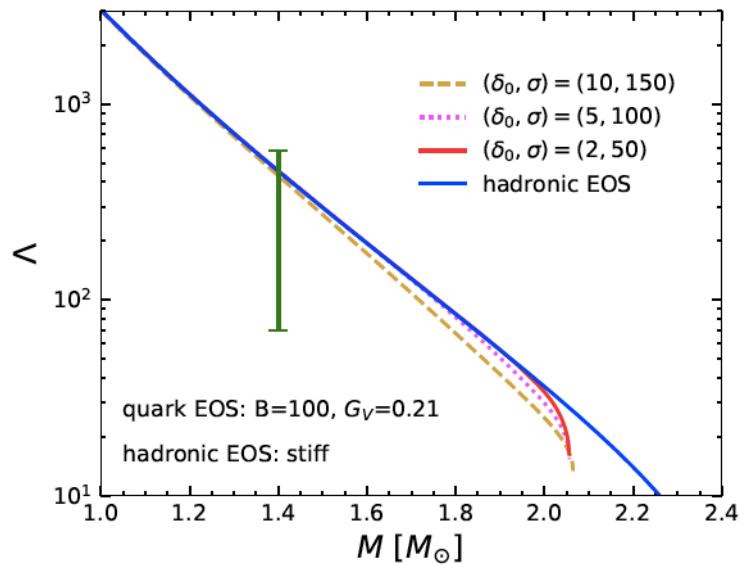
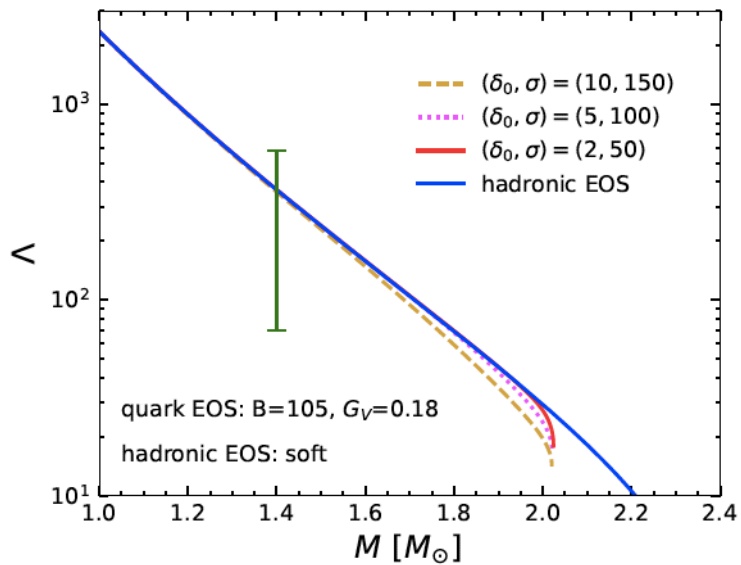
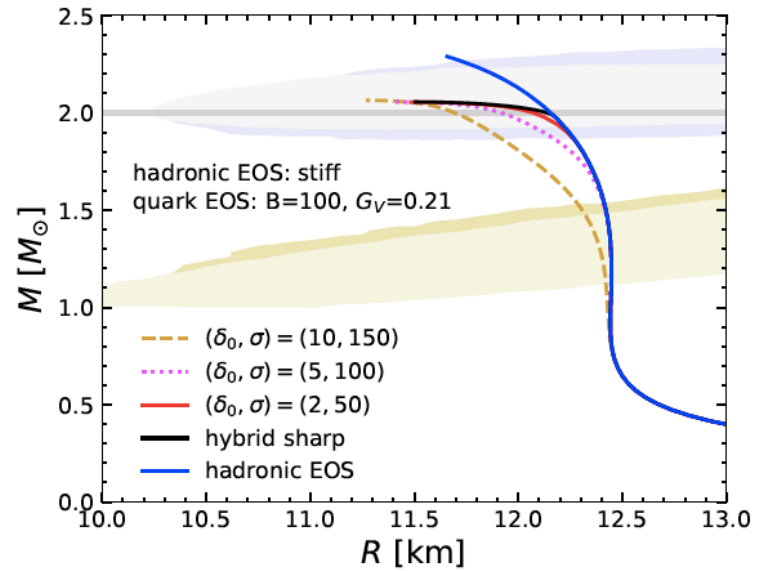
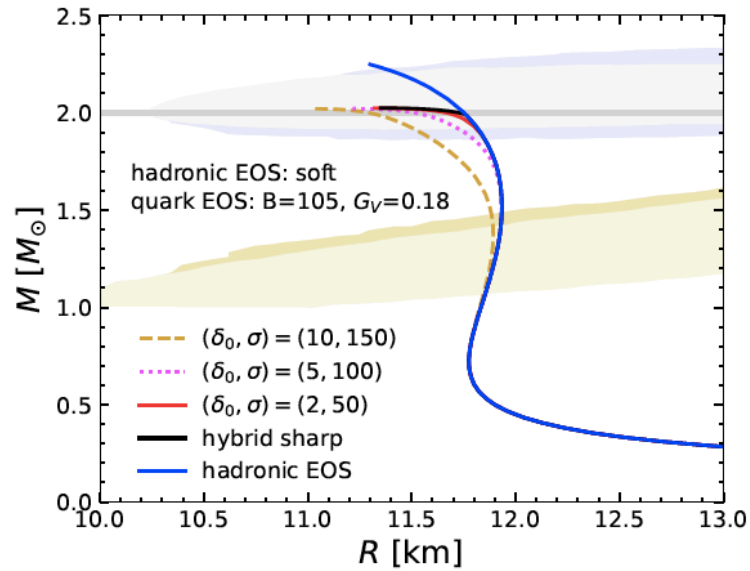


Intermediate hadron EOS + stiff quark EOS





Tidal deformability



Summary

We have updated the studies of sensitivity of NS global observables to the sharpness of the phase transition in hybrid stars

We have introduced a new matching procedure

Results are consistent with previous works

Strong dependence on the choice of hadronic and quark matter EOS

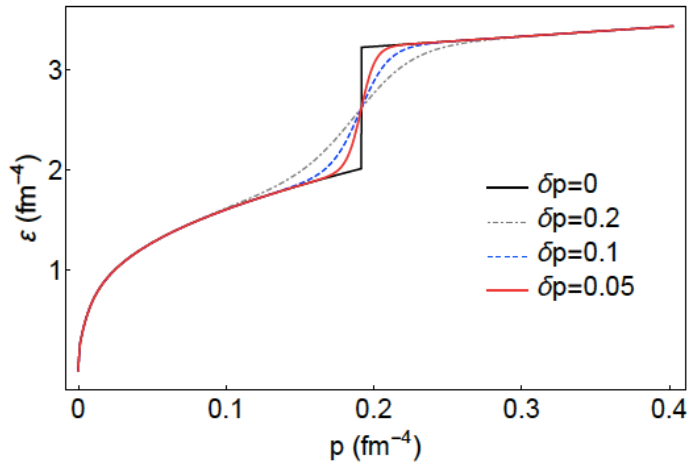
Weak dependence on the matching scheme

Increasing the precision, sharpness may be visible in the M - R diagram

Thank you for
your attention !

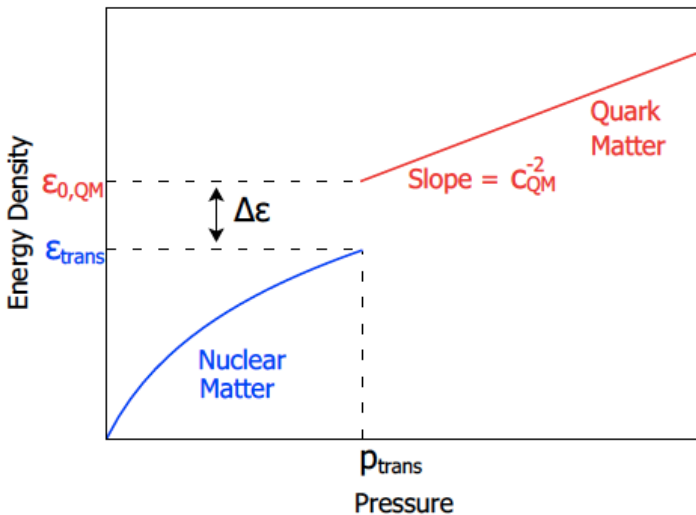
Controlling the sharpness of the transition

Han and Steiner, arXiv:1810.10967



$$\varepsilon(p) = \frac{1}{2} \left[1 - \tanh \left(\frac{p - p_{\text{trans}}}{\delta p} \right) \right] \varepsilon_{\text{NM}}(p) + \frac{1}{2} \left[1 + \tanh \left(\frac{p - p_{\text{trans}}}{\delta p} \right) \right] \varepsilon_{\text{QM}}(p);$$

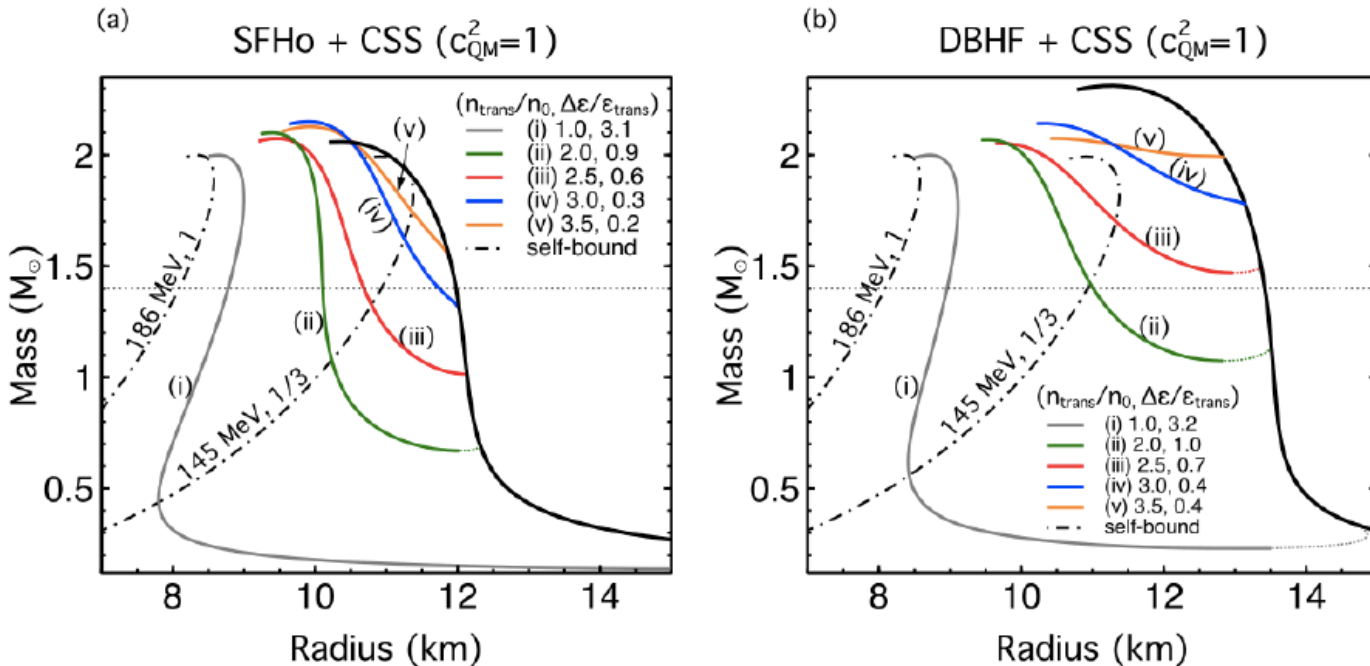
"round the gap"



$$\varepsilon(p) = \begin{cases} \varepsilon_{\text{NM}}(p) & p < p_{\text{trans}} \\ \varepsilon_{\text{NM}}(p_{\text{trans}}) + \Delta\varepsilon + c_{\text{QM}}^{-2}(p - p_{\text{trans}}) & p > p_{\text{trans}} \end{cases} \quad (1)$$

"shrink the gap"

$$\varepsilon(p) = \begin{cases} \varepsilon_{\text{NM}}(p) & p < p_{\text{trans}} \\ \varepsilon_{\text{NM}}(p_{\text{trans}}) + \Delta\varepsilon + c_{\text{QM}}^{-2}(p - p_{\text{trans}}) & p > p_{\text{trans}} \end{cases} \quad (1)$$



Significant changes in the M-R diagram ...

