



Study of the processes of electron-positron annihilation into hadron states with SND at VEPP-2000 collider

Dmitry A. Shtol

On behalf of SND collaboration

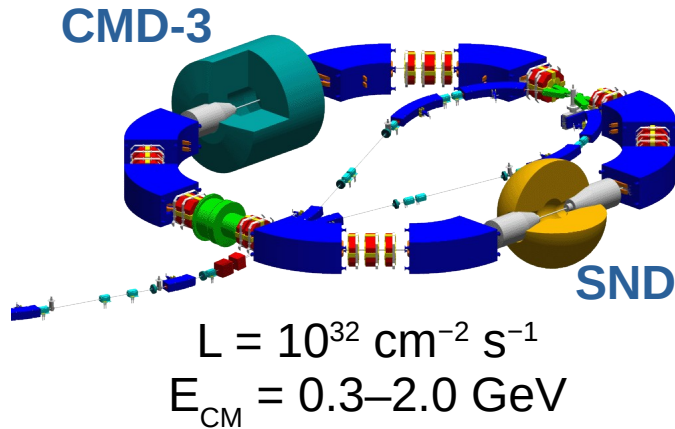
Budker Institute of Nuclear Physics

Novosibirsk, Russia

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Crete, Greece

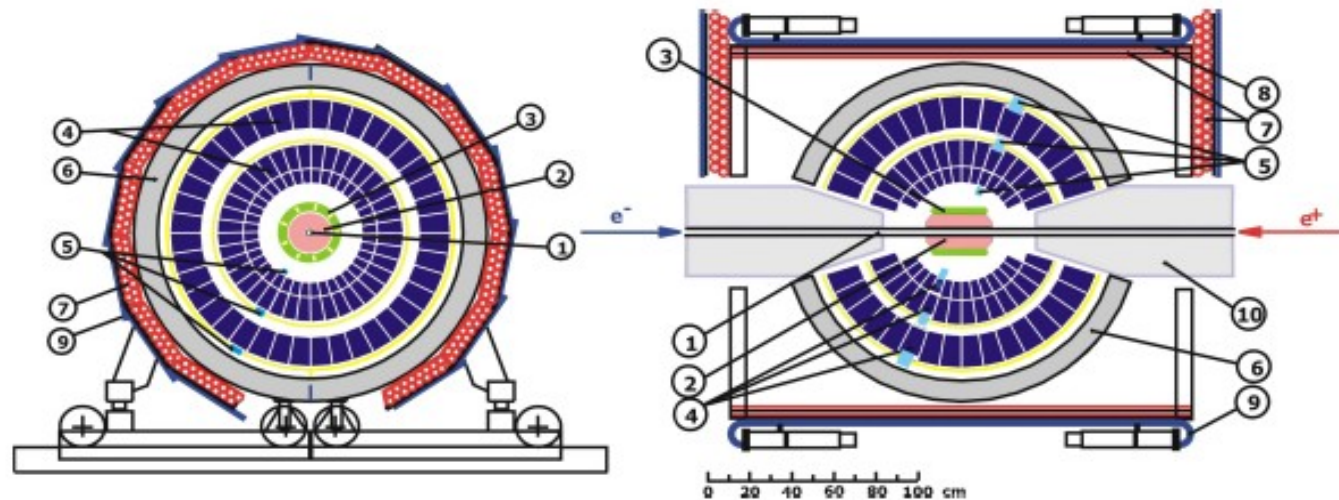
SND experiment at VEPP-2000



Spherical Neutral Detector

Integrated luminosity is measured using:

- $e^+e^- \rightarrow e^+e^-$ for charged final states
- $e^+e^- \rightarrow \gamma\gamma$ for neutral final states



1 – beam pipe, 2 – tracking system, 3 – aerogel cherenkov counter, 4 – NaI(Tl) crystals, 5 – phototriodes, 6 – iron absorber, 7–9 – muon detector, 10 – focusing solenoids.

Total IL=885 pb⁻¹ for June, 2023

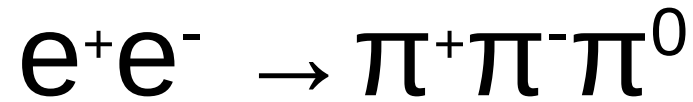
Until 2021 — 300 pb⁻¹

2022 and 2023 — 585 pb⁻¹ (not processed yet)

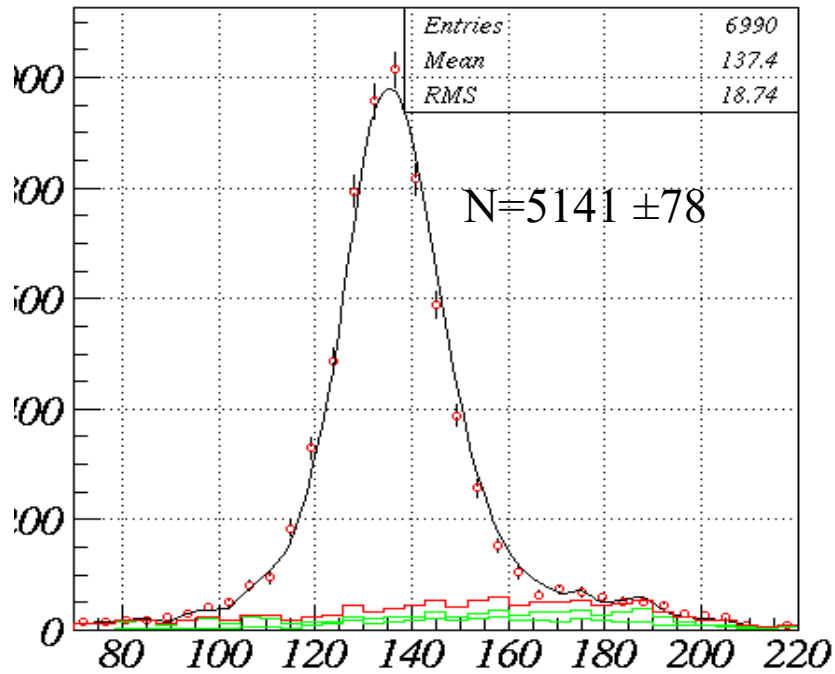
SND physics program

The physics program of experiments at VEPP-2000 includes the following main topics:

- Measurement of total hadronic cross section below 2 GeV for calculation HVP contribution to $(g-2)_\mu$.
- Study of dynamics of hadron production, i.e. separation between different intermediate states, for example, $\omega\eta$, $\phi\eta$, etc.
- Hadron spectroscopy: study of light-vector-meson excitations.
- Search for rare and forbidden decays of the ρ , ω , and ϕ mesons.
- Study of nucleon-antinucleon pair production, extraction of the proton and neutron electromagnetic form factors.
- Search for production of C-even resonances: $e^+e^- \rightarrow \eta$, η' , f_1 , f_2 , a_2 , etc.
- Using the radiative return technique as alternative method for measurement of hadronic cross sections.



$\sqrt{s}=1281 \text{ MeV} (L\sim 7.3 \text{ pb}^{-1})$

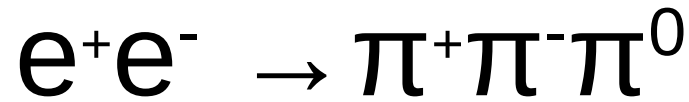


Number of events is calculated by fit of $M_{\gamma\gamma}$ spectrum

Fraction of $\rho\pi$ and $\rho'\pi$ measured by fit of Dalitz-plot $(M_{\pi^+\pi^0})^2$ vs $(M_{\pi^+\pi^-})^2$, using model

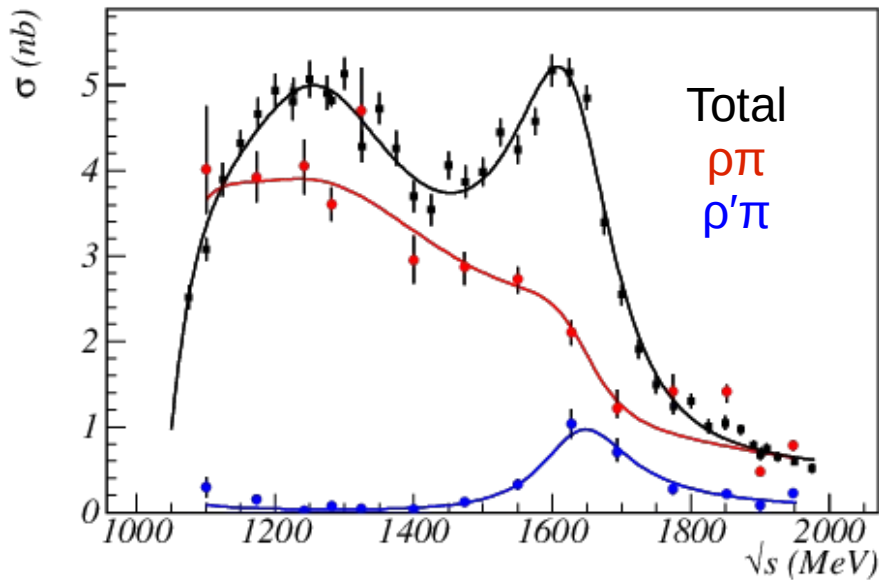
$$\frac{d\sigma}{d\Gamma} = |\alpha A_{\rho\pi} + \beta A_{\rho'\pi} + \gamma A_{\omega\pi}|^2$$

Where $|\gamma|$ was fixed using $\omega\pi^0$ data, parameters of fit are $|\alpha|, |\beta|$ and two phases $\varphi_{\rho\pi-\omega\pi}, \varphi_{\rho\pi-\rho'\pi}$



$$\sigma_{\text{vis}}(E) = \frac{N_{\text{exp}}}{\varepsilon L} \quad \sigma_{\text{born}}(E) = \frac{N_{\text{exp}}}{\varepsilon L(1 + \delta)}$$

$$\sigma_{\text{vis}}(E) = \int_0^\varepsilon F(x, E) \sigma_{\text{born}}(E\sqrt{1-x}) dx$$



Systematics error estimate 7.3%

Model includes mechanisms:

$e^+e^- \rightarrow (\omega, \varphi, \omega', \omega'') \rightarrow \rho\pi \rightarrow \pi^+\pi^-\pi^0$

$e^+e^- \rightarrow (\varphi, \omega', \omega'') \rightarrow \rho'\pi \rightarrow \pi^+\pi^-\pi^0$

$$M(\omega') = 1190 \pm (45/38) \quad (1450 \pm 60)$$

$$\Gamma(\omega') = 380 \pm (42/31) \quad (450 \pm 300)$$

$$M(\omega'') = 1640.7 \pm (7.1/7.8) \quad (1670 \pm 150)$$

$$\Gamma(\omega'') = 159 \pm (15/14) \quad (300 \pm 200)$$

Phases for $\rho\pi$:

$$\varphi_{\omega\omega'} = 176^\circ \pm (12/14)$$

$$\varphi_{\omega\omega''} = -40^\circ \pm (15/18)$$

Phases for $\rho'\pi$:

$$\varphi_{\varphi\omega'} = 173^\circ \pm (11/14)$$

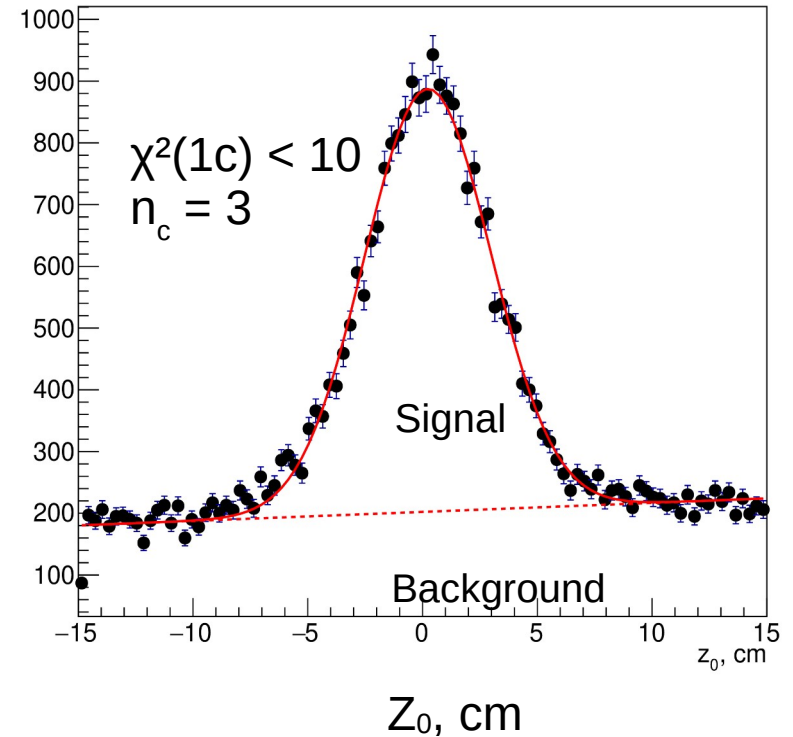
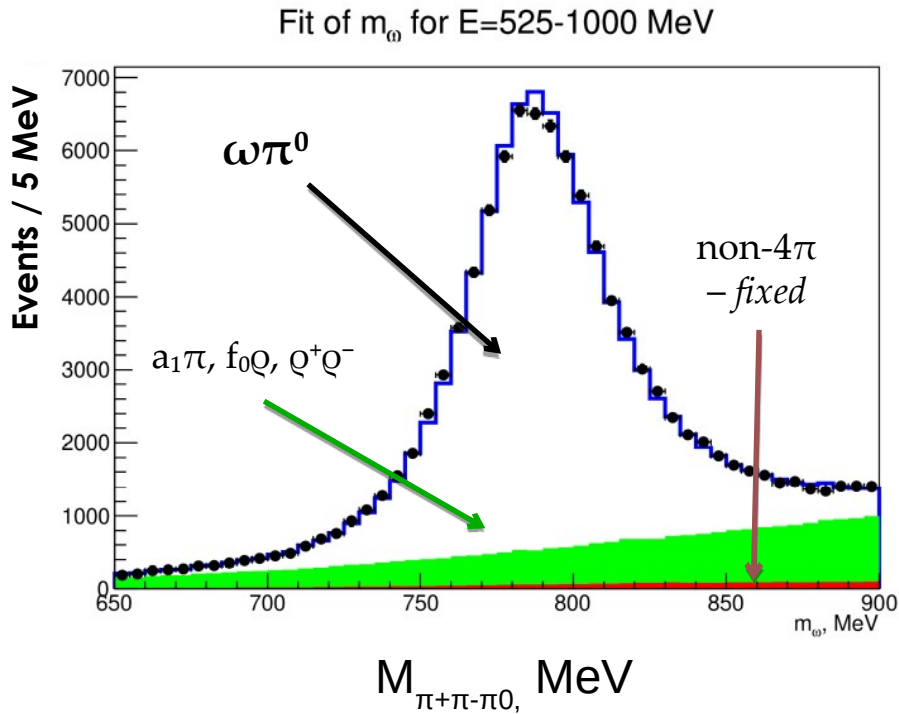
$$\varphi_{\varphi\omega''} = 30^\circ \pm (15/19)$$

Phase for $\rho\pi$ is measured relatively to ω ,
for $\rho'\pi$ - relatively φ .

Input of $\rho'\pi$ on φ mass taken from KLOE
data and was fixed

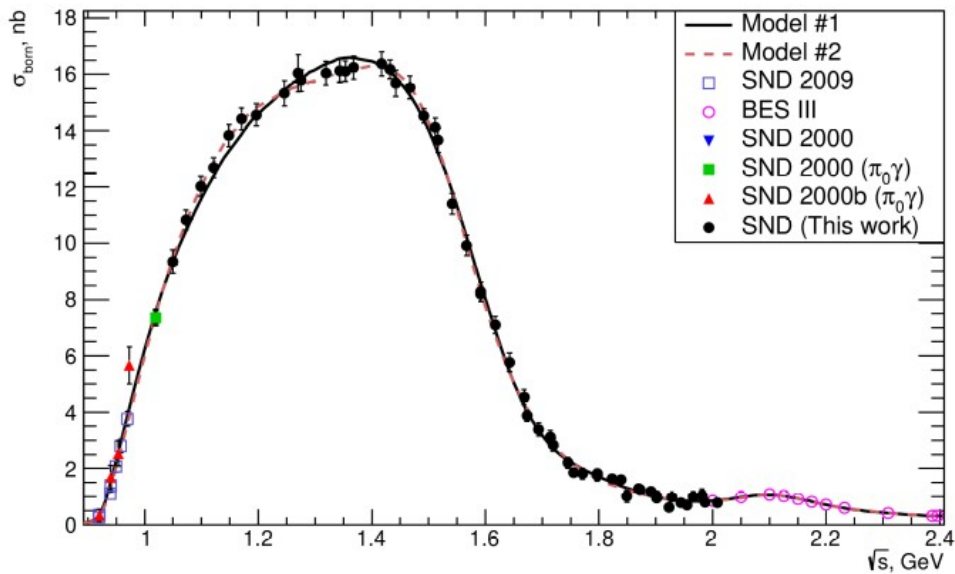
$$\sigma(\varphi \rightarrow \rho'\pi) = 47 \pm 14 \quad (40 \pm 15)$$

$$e^+e^- \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-\pi^0\pi^0$$

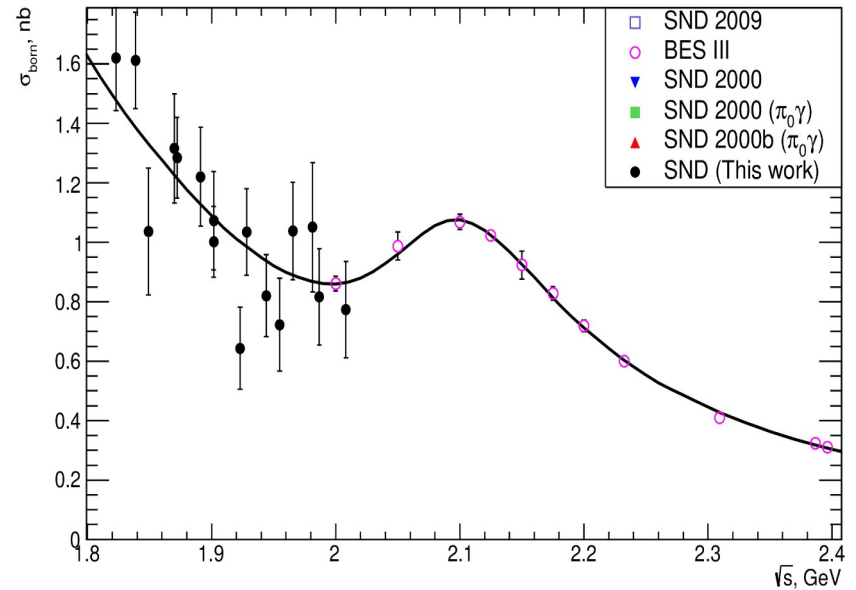


- Events are selected using kinematic reconstruction in $\pi^+\pi^-\pi^0\pi^0$ hypothesis
- For background processes subtraction a distribution of $M_{\pi^+\pi^-\pi^0}$ is used
- Subtraction of beam and cosmic background was done using Z_0 distribution (only when calculating efficiency corrections)

$$e^+e^- \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-\pi^0\pi^0$$



Model includes $\rho(770)$, $\rho(1450)$,
 $\rho(1700)$ and $\rho(2150)$

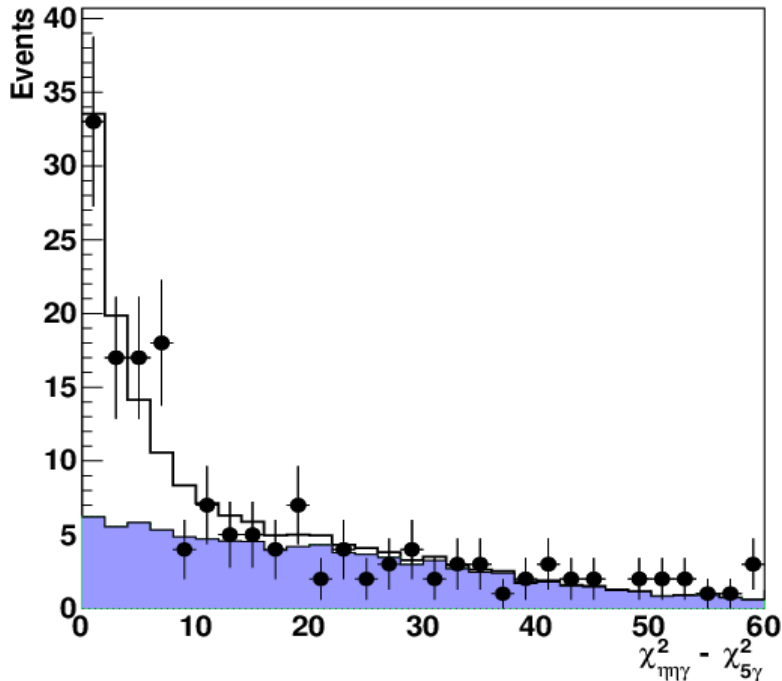


$\rho(2150)$ region (SND and BESIII data)

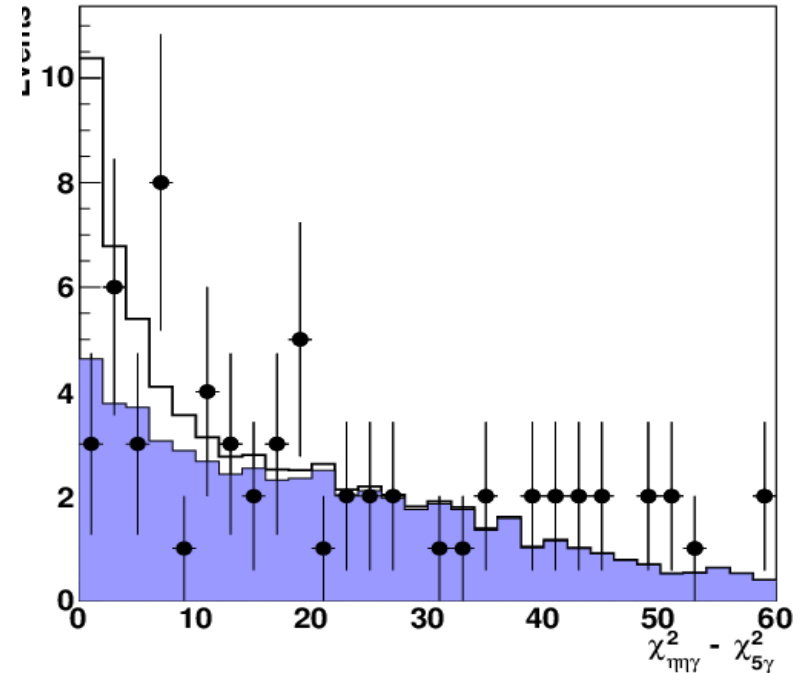
Cross section

E, GeV	syst. error
1.0 — 1.5	3.0 — 4.0 %
1.5 — 2.0	4.0 — 14.3 %

$e^+e^- \rightarrow \eta\eta\gamma$



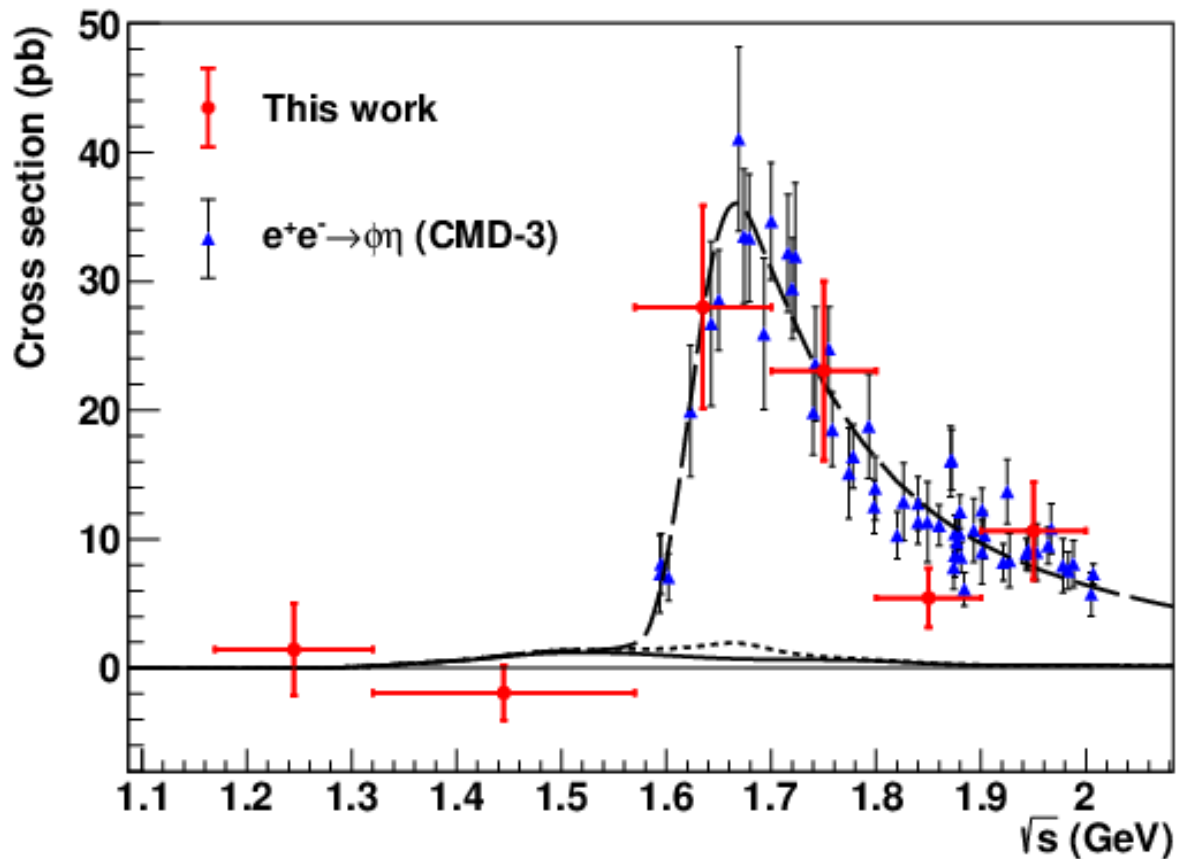
$\chi^2_{\eta\eta\gamma} - \chi^2_{5\gamma}$ for selected events



$\chi^2_{\eta\eta\gamma} - \chi^2_{5\gamma}$ with additional cut $\chi^2_{\eta\phi} - \chi^2_{5\gamma} > 20$

- $\chi^2_{\eta\eta\gamma} - \chi^2_{5\gamma}$ fit is used for event number calculation
- Effect is described by MC in $e^+e^- \rightarrow (\phi\eta, \rho\eta, \omega\eta) \rightarrow \eta\eta\gamma$ model
- Background by MC of $\pi^0\pi^0\gamma$, $\eta\pi^0\gamma$, $\pi^0\pi^0\pi^0\gamma$, $\eta\pi^0\pi^0\gamma$, QED 4γ (with fake photons), 5γ
- Data with suppressed $\phi\eta$ events are described by background processes - no significant mechanism other than $\phi\eta$, $\rho\eta$, $\omega\eta$.

$$e^+e^- \rightarrow \eta\eta\gamma$$



- Solid curve — $\eta\rho$ cross section
- Dotted curve — $\eta\rho+\omega\rho$ cross section
- Dashed curve — $\eta\phi+\eta\rho+\omega\rho$ cross section

E, GeV	syst. error
<1.32	21 %
1.32 — 1.57	23 %
>1.57	12

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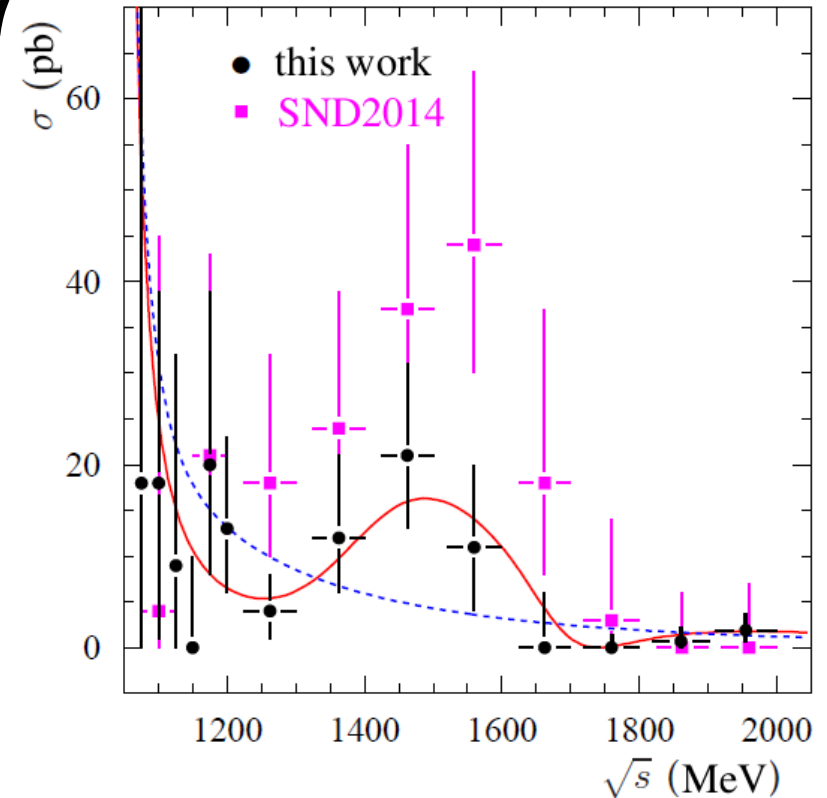
$e^+e^- \rightarrow \eta\gamma$

$$\sigma_{\eta\gamma}(\sqrt{s}) = \left(\frac{k_\gamma(\sqrt{s})}{\sqrt{s}} \right)^3 \left| \sum_{V=\rho, \omega, \phi, \dots} A_V(\sqrt{s}) \right|^2$$

$$A_V(\sqrt{s}) = \frac{m_V \Gamma_V(m_V) e^{i\varphi_V}}{D_V(\sqrt{s})} \sqrt{\frac{m_V^3}{k_\gamma(m_V)^3} \sigma_{V\eta\gamma}}$$

$$D_V(\sqrt{s}) = m_V^2 - s - i\sqrt{s}\Gamma_V(\sqrt{s})$$

$$k_\gamma(\sqrt{s}) = \frac{\sqrt{s}}{2} \left(1 - \frac{m_\eta^2}{s} \right)$$



Dashed curve — only ρ, ω, ϕ
 Solide curve includes aslo ρ' and ϕ' .

$$\sigma_{\rho'\eta\gamma} = 16_{-10}^{+15} \pm 2 \text{ pb}$$

$$\sigma_{\phi'\eta\gamma} = 14_{-10}^{+14} \pm 2 \text{ pb}$$

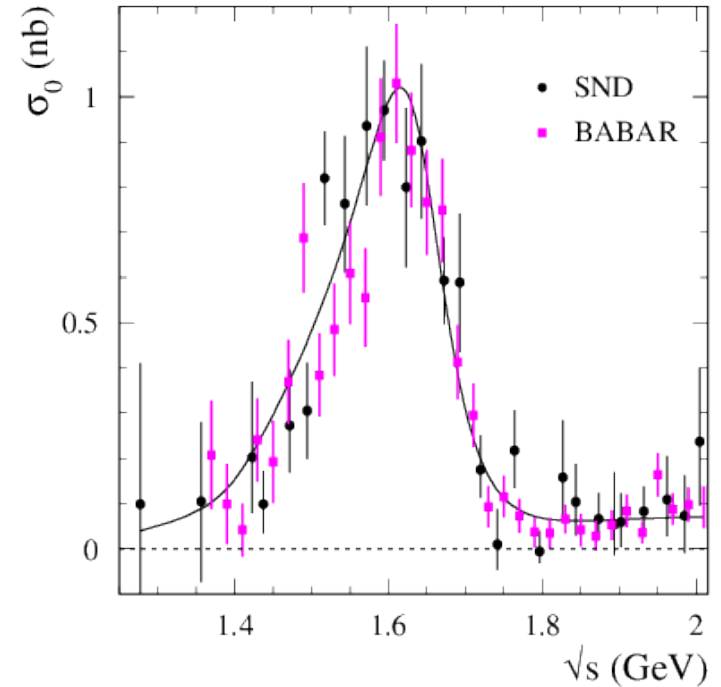
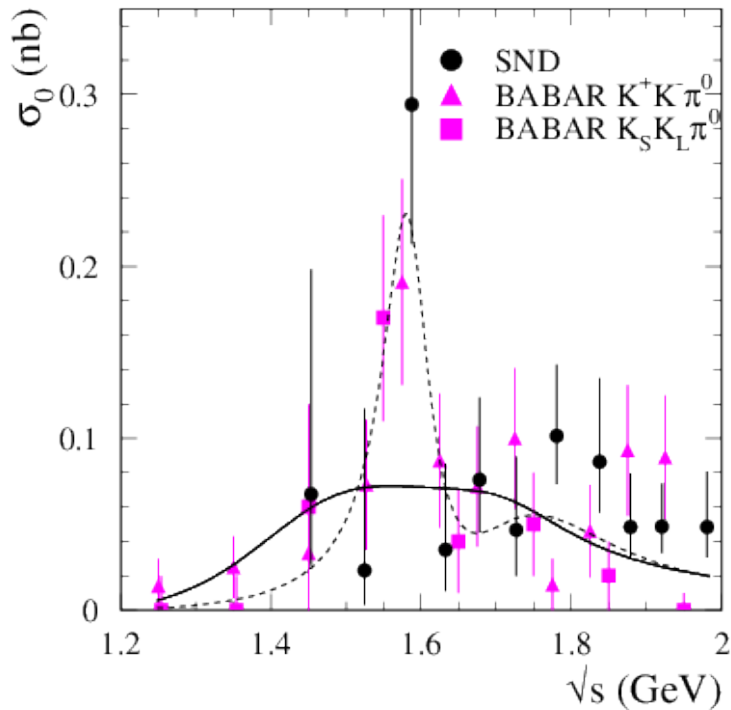
Quark model prediction¹ is

$$\sigma_{\rho'\eta\gamma} \approx 15 \text{ pb}, \quad \sigma_{\phi'\eta\gamma} \approx 10 \text{ pb}$$

¹ F. E. Close, A. Donnachie and Y. S. Kalashnikova, Phys. Rev. D 65, 092003 (2002).

$e^+e^- \rightarrow K^+K^-\pi^0$

$e^+e^- \rightarrow K^+K^-\pi^0$ without $\phi\pi^0$ events ($m_{\text{rec}}^{\gamma\gamma} > 1.05 \text{ GeV}/c^2$)

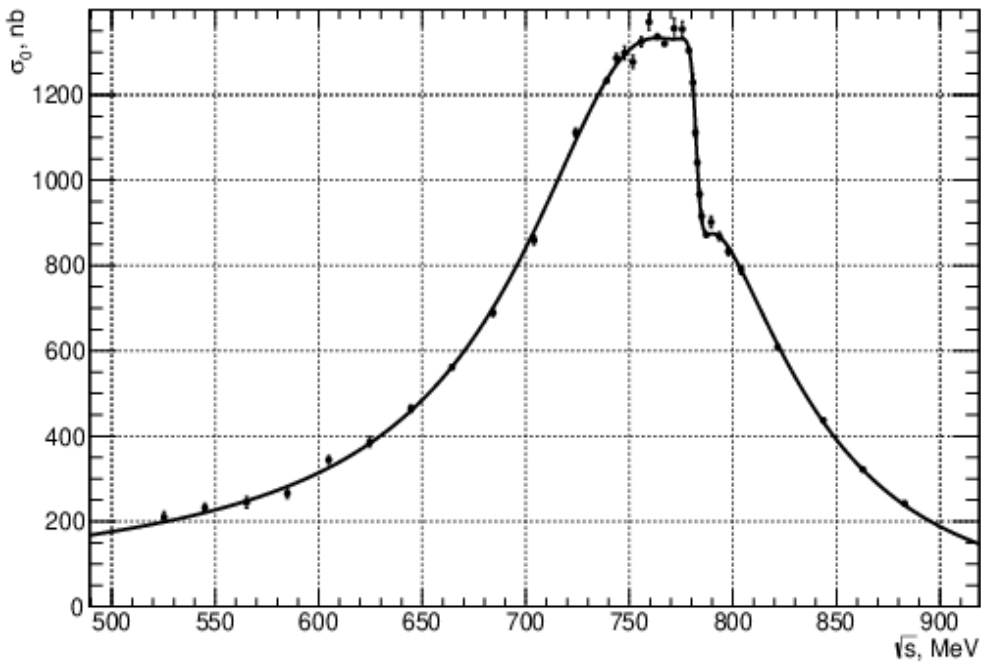


Two models:

1. $\rho(1450)$ and $\rho(1700)$ with masses fixed on PDG values (solid line, $\chi^2/\text{ndf}=50/28$).
2. Fixed $\rho(1700)$ and free resonance (dashed line), gives $M=1585 \pm 15 \text{ MeV}$ and $\Gamma=75 \pm 30 \text{ MeV}$ for free resonance, $\chi^2/\text{ndf}=38/26$. Such vector resonance is not known

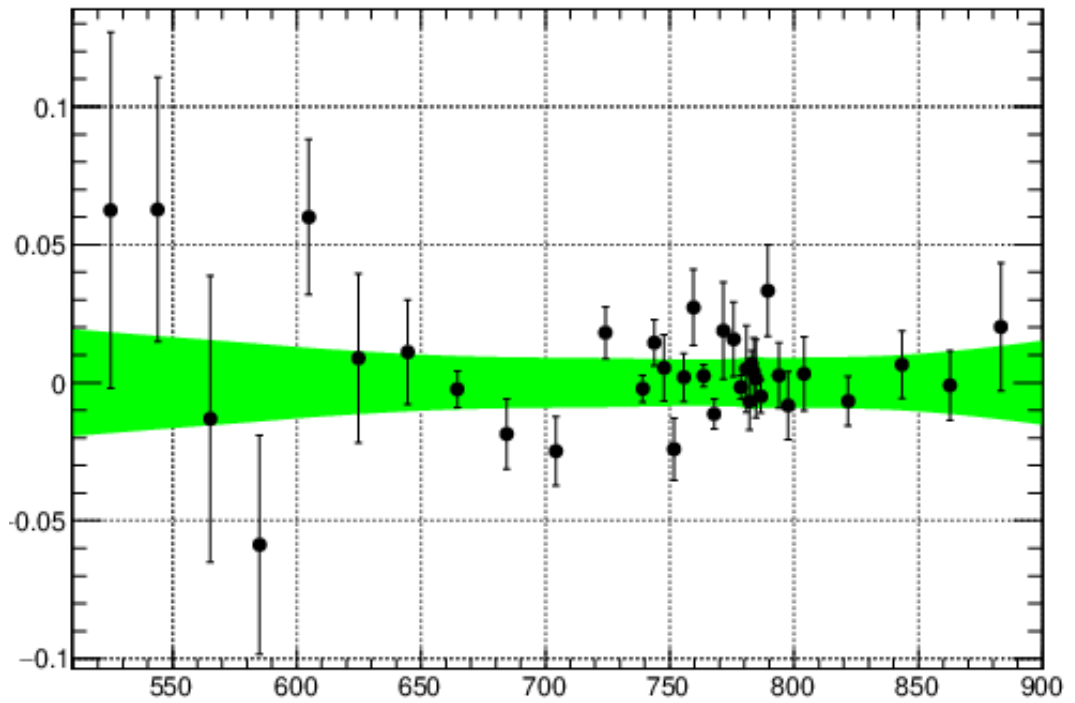
$e^+e^- \rightarrow \phi\pi^0 \rightarrow K^+K^-\pi^0$ ($m_{\text{rec}}^{\gamma\gamma} < 1.11 \text{ GeV}/c^2$)

$$e^+e^- \rightarrow \pi^+\pi^-$$



Born cross section

Model for fit includes ρ and ω



Fit - data difference for cross section

M_ρ , MeV	$775.3 \pm 0.5 \pm 0.6$	
Γ_ρ , MeV	$145.6 \pm 0.6 \pm 0.8$	
$\varphi_{\rho\omega}$, deg	$110.7 \pm 1.1 \pm 1.0$	
$B_{\rho \rightarrow e^+e^-} \cdot B_{\rho \rightarrow \pi^+\pi^-}$	$(4.889 \pm 0.015 \pm 0.039) 10^{-5}$	
$B_{\omega \rightarrow e^+e^-} \cdot B_{\omega \rightarrow \pi^+\pi^-}$	$(1.318 \pm 0.051 \pm 0.021) 10^{-6}$	

E, MeV	syst. error
525 — 600	0.9 — 1.2 %
600 — 883	0.8 %

$e^+e^- \rightarrow n\bar{n}$

Total cross section:

$$\sigma(e^+e^- \rightarrow B\bar{B}) = \frac{4\pi\alpha^2\beta C}{3m^2} \left(|G_M|^2 + \frac{2m_B^2}{m^2} |G_E|^2 \right)$$

Effective form factor

$$|F|^2 = \frac{|G_M|^2 + |G_E|^2 / 2\tau}{1 + 1/2\tau}, \quad \tau = \frac{m^2}{4m_B^2}$$

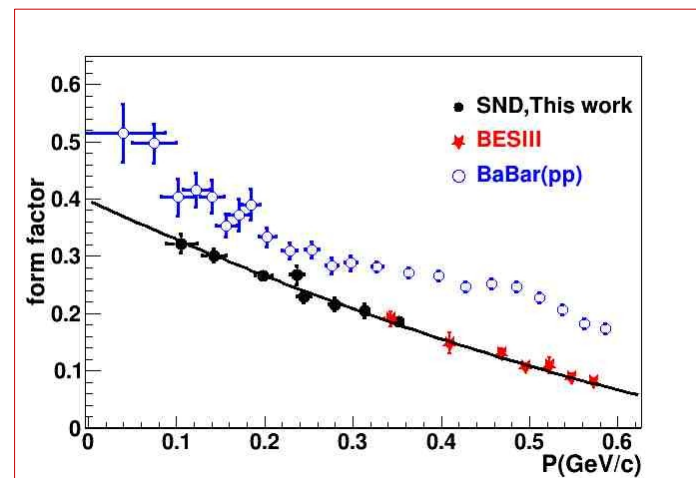
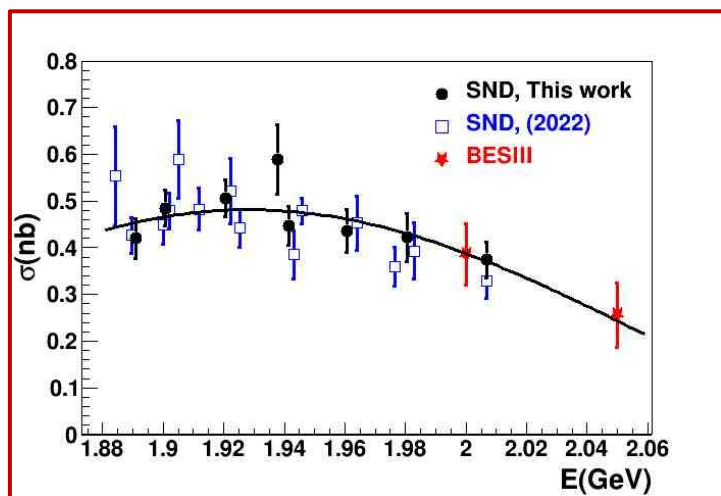
$m^2=s$ Two measurable values:
 1 - effective FF,
 2 - G_E/G_M

At threshold : $s=4m_B^2 \rightarrow |G_E| = |G_M| = |F|$

Asymptotic prediction: $F_n = -F_p / 2$

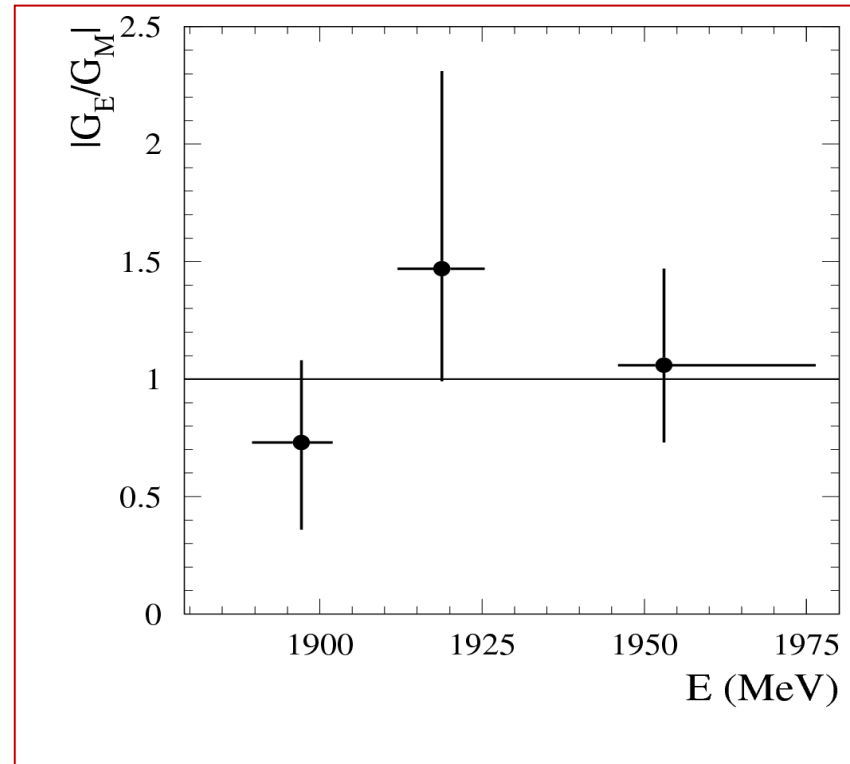
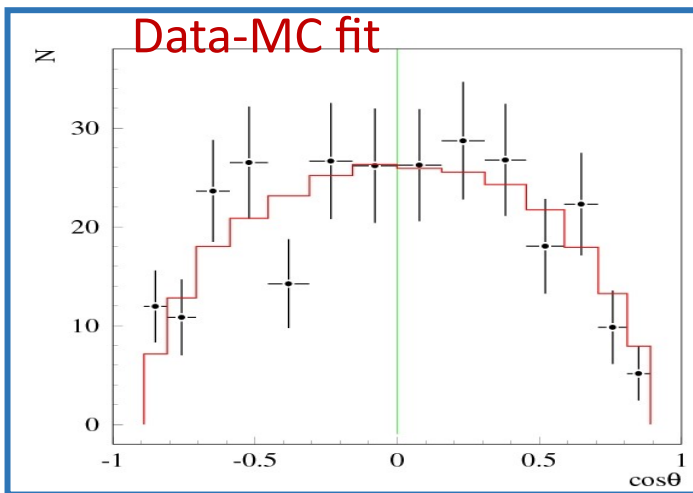
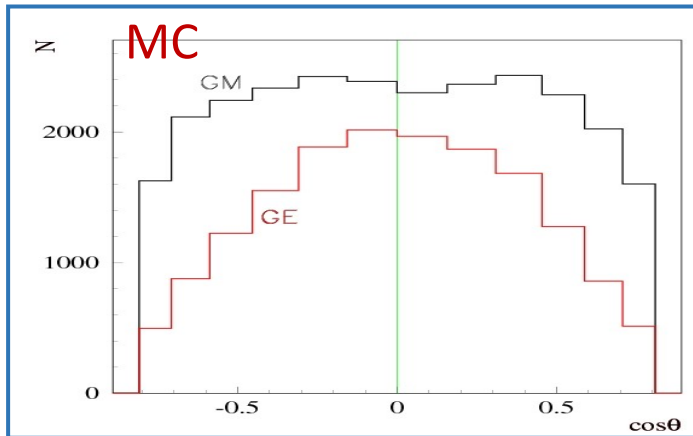
2 - G_E/G_M

C=1 for neutrons



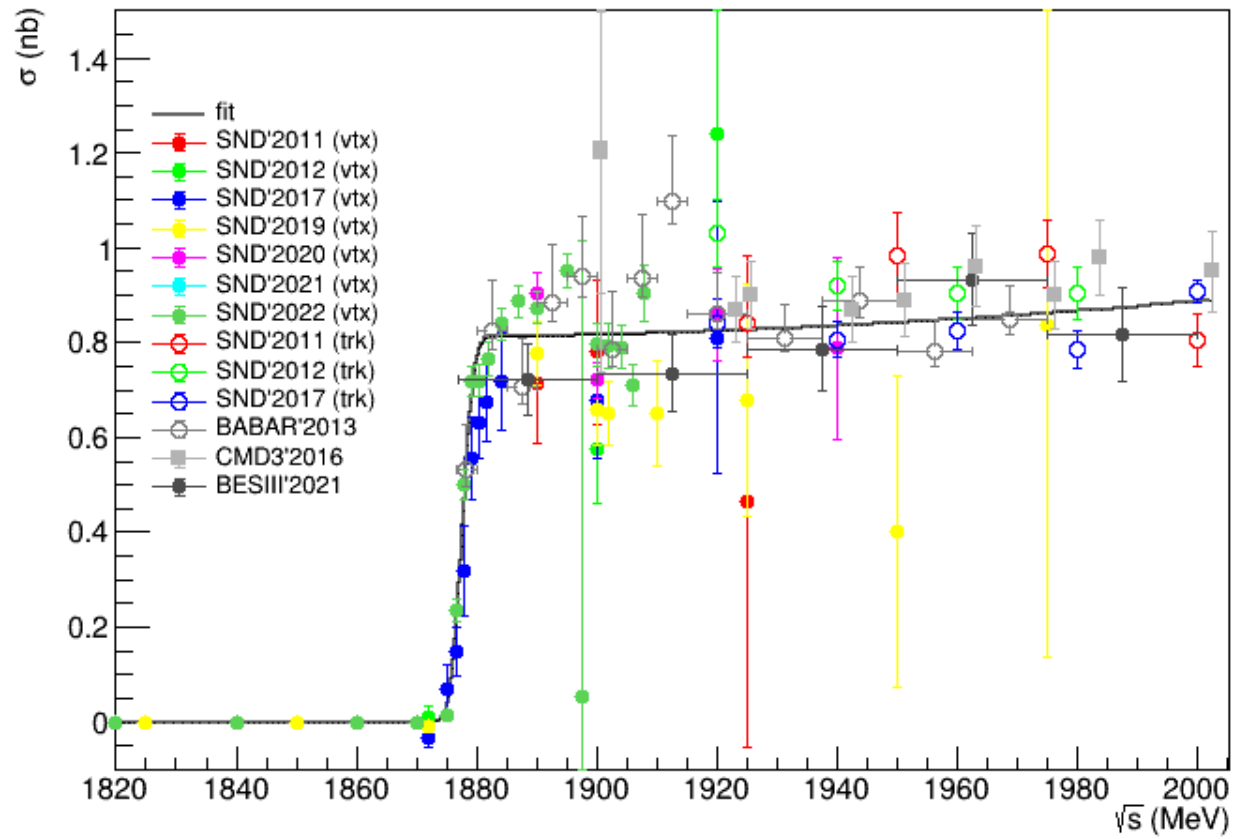
$|G_E|/|G_M|$ measurement

$$d\sigma(e^+e^- \rightarrow B\bar{B}) = \frac{\alpha^2 \beta C^2}{4m^2} \left(|G_M|^2 (1 + \cos^2 \theta) + \frac{4m_B^2}{m^2} |G_E|^2 (1 - \cos^2 \theta) \right) d\Omega$$



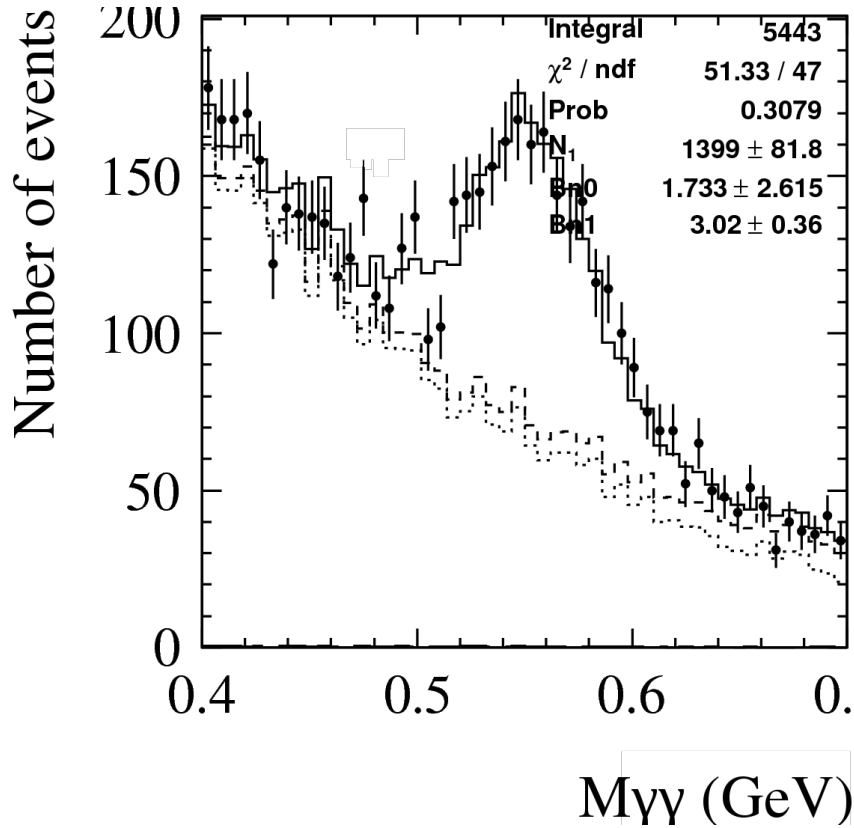
- More than 2500 $n\bar{n}$ pairs detected.
- Effective form-factor was measured, consistent with BESIII results for greater momentum
- $|G_E|/|G_M|$ is consistent with 1 near threshold

$$e^+e^- \rightarrow p\bar{p}$$



Preliminary

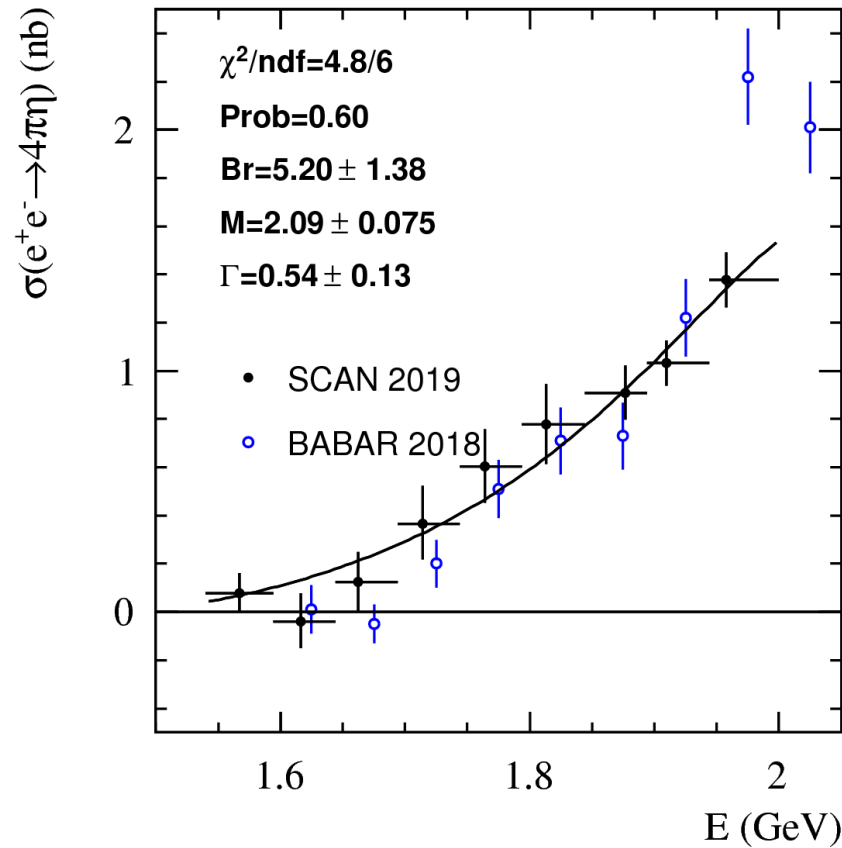
$$e^+e^- \rightarrow \eta\pi^+\pi^-\pi^0\pi^0$$



Background subtraction using $M_{\gamma\gamma}$

Fit is done in a model
 $e^+e^- \rightarrow \phi(2170) \rightarrow \eta\pi^+\pi^-\pi^0\pi^0$

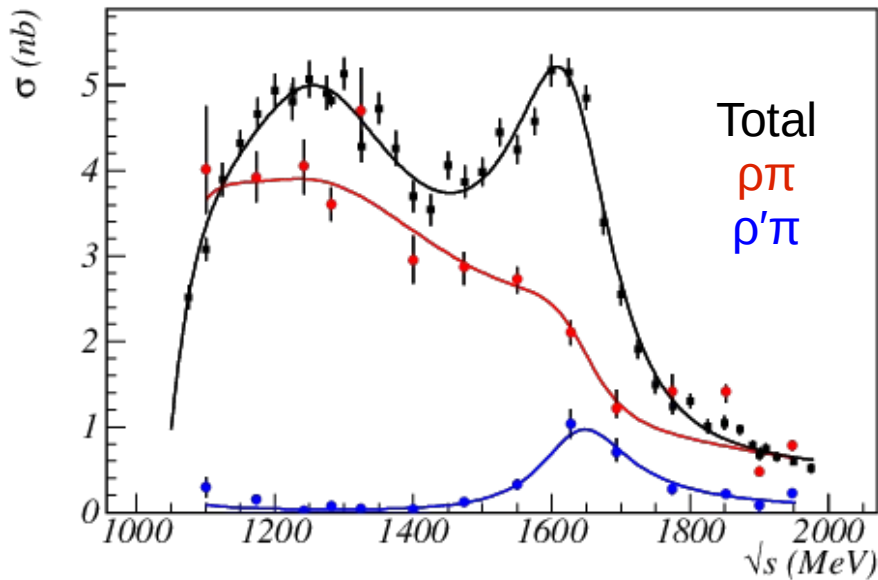
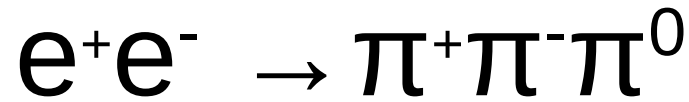
Preliminary



Summary

- In experiment SND at VEPP2000 the following processes are studied:
 - $e^+e^- \rightarrow \pi^+\pi^-\pi^0$
 - $e^+e^- \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-\pi^0\pi^0$
 - $e^+e^- \rightarrow \eta\eta\gamma$
 - $e^+e^- \rightarrow \eta\gamma$
 - $e^+e^- \rightarrow K^+K^-\pi^0$
 - $e^+e^- \rightarrow \pi^+\pi^-$
 - $e^+e^- \rightarrow n\bar{n}$
 - $e^+e^- \rightarrow p\bar{p}$
 - $e^+e^- \rightarrow \eta\pi^+\pi^-\pi^0\pi^0$
- For the most of the processes cross sections are compatible with the previous but has better accuracy
- This results are using statistics of VEPP-2000 until 2021 (including), $IL=300 \text{ pb}^{-1}$.
- Results using 2022 and 2023 statistics are coming soon, $IL=585 \text{ pb}^{-1}$.

BACKUP



Model includes mechanisms:

$$e^+e^- \rightarrow (\omega, \phi, \omega', \omega'') \rightarrow \rho\pi \rightarrow \pi^+\pi^-\pi^0$$

$$e^+e^- \rightarrow (\phi, \omega', \omega'') \rightarrow \rho'\pi \rightarrow \pi^+\pi^-\pi^0$$

$$M(\omega') = 1190 \pm (45/38) \quad (1450 \pm 60)$$

$$\Gamma(\omega') = 380 \pm (42/31) \quad (450 \pm 300)$$

$$\sigma(\omega' \rightarrow \rho\pi) = 6.62 \pm (0.48/0.70) \text{ nb}$$

$$\sigma(\omega' \rightarrow \rho'\pi) = 0.068 \pm (0.018/0.016) \text{ nb}$$

$$M(\omega'') = 1640.7 \pm (7.1/7.8) \quad (1670 \pm 150)$$

$$\Gamma(\omega'') = 159 \pm (15/14) \quad (300 \pm 200)$$

$$\sigma(\omega'' \rightarrow \rho\pi) = 0.126 \pm (0.052/0.040)$$

$$\sigma(\omega'' \rightarrow \rho'\pi) = 1.31 \pm (0.15/0.14)$$

Фазы: для $\rho\pi$:

$$\varphi_{\omega\omega'} = 176^\circ \pm (12/14)$$

$$\varphi_{\omega\omega''} = -40^\circ \pm (15/18)$$

Фаза для $\rho'\pi$:

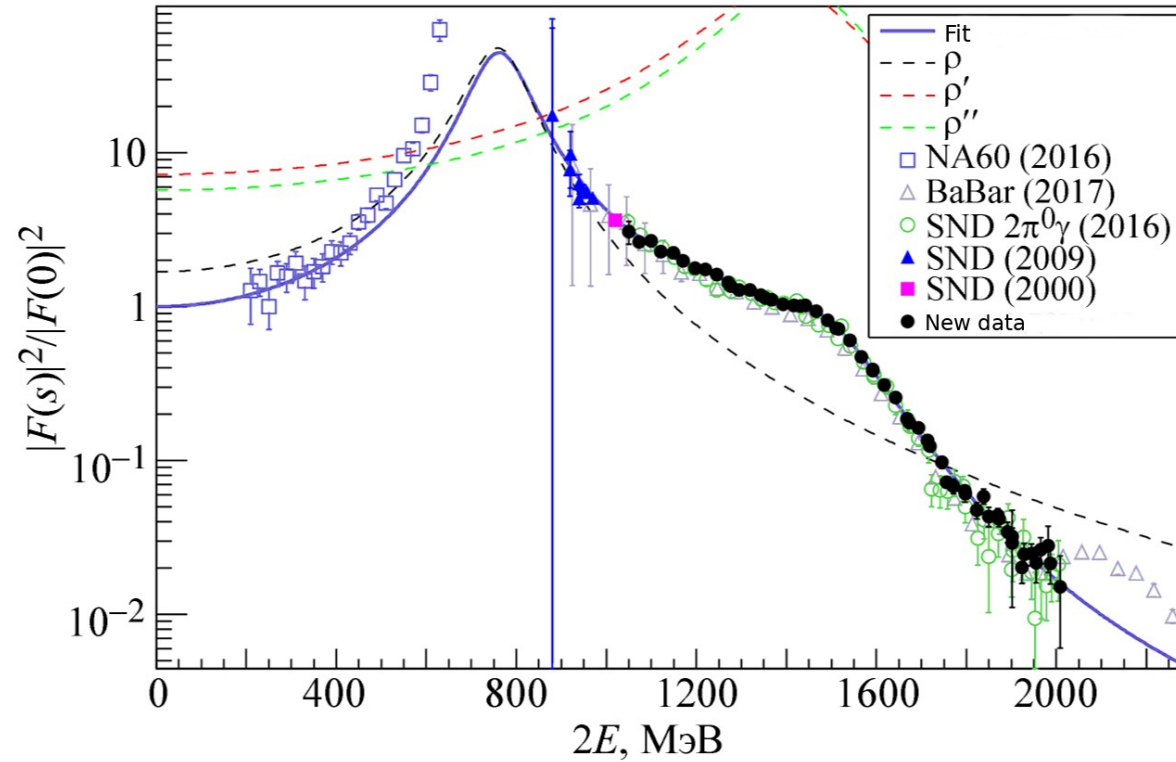
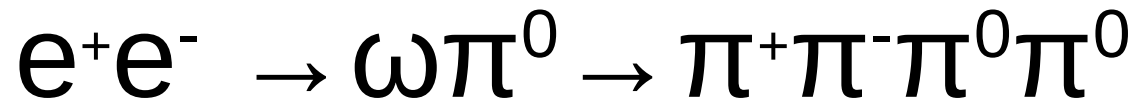
$$\varphi_{\phi\omega'} = 173^\circ \pm (11/14)$$

$$\varphi_{\phi\omega''} = 30^\circ \pm (15/19)$$

Phase for $\rho\pi$ is measured relatively to ω ,
for $\rho'\pi$ - relatively ϕ .

Input of $\rho'\pi$ on ϕ mass taken from KLOE
data and was fixed

$$\sigma(\phi \rightarrow \rho'\pi) = 47 \pm 14 \quad (40 \pm 15)$$



Form-factor

$$\sigma_{\text{born}}(E) = \frac{4\pi\alpha^2}{E^3} |F_{\gamma\omega\pi}(E)|^2 P_f(E)$$