

# ***Study of thermal vorticity and hyperon polarization in heavy-ion collisions at intermediate energies***



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in collaboration with  
**O. Vitiuk and E. Zabrodin**

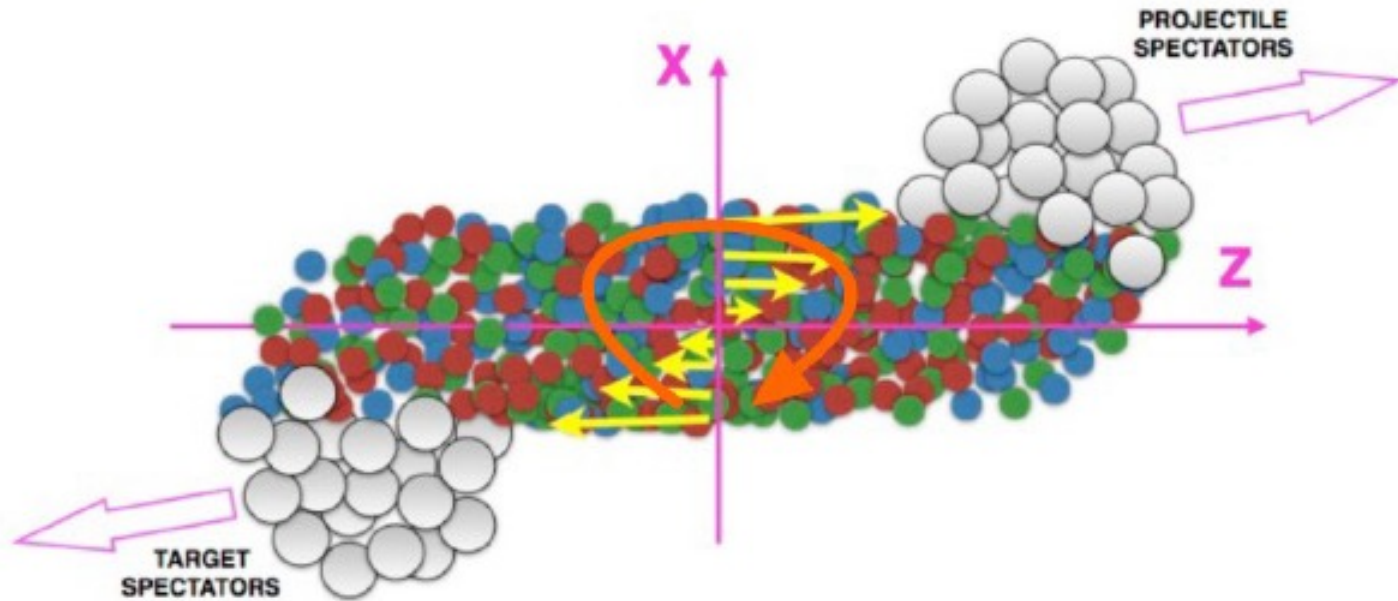


*ICNFP-2023, OAC, Kolymbari, Crete, Greece, 10.07 – 23.07.2023*

# MOTIVATION

The image features a purple gradient background with several realistic water droplets of various sizes scattered across it. The droplets have highlights and shadows, giving them a three-dimensional appearance. The word 'MOTIVATION' is centered in a bold, white, sans-serif font.

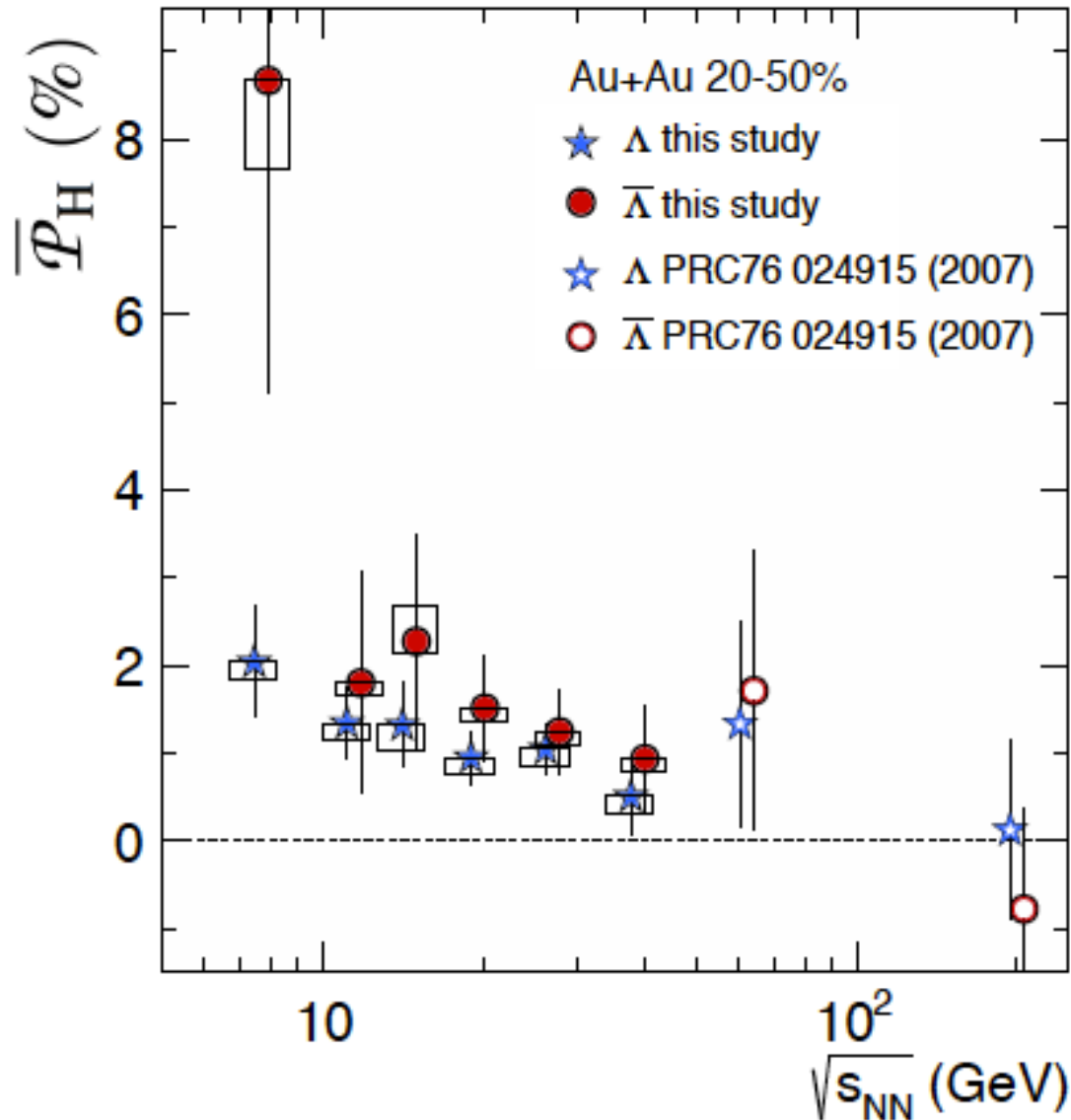
# MOTIVATION



In non-central collisions, the initial collective longitudinal flow velocity depends on  $x$ :

$$\omega_y = \frac{1}{2}(\nabla \times v)_y \approx -\frac{1}{2} \frac{\partial v_z}{\partial x}$$

# MOTIVATION

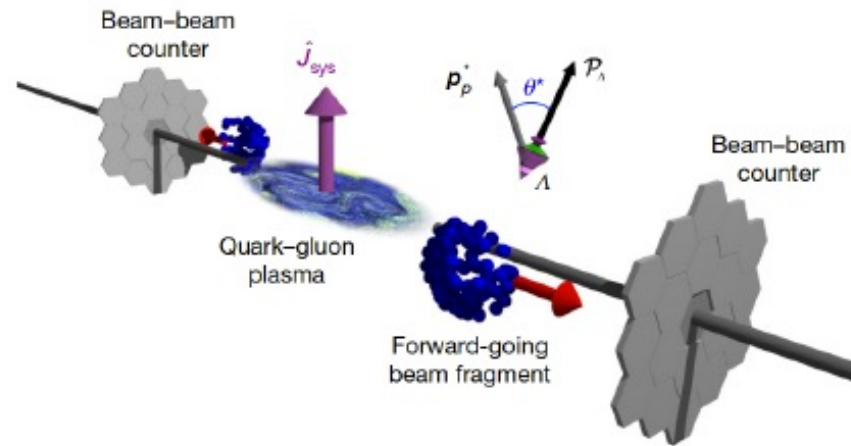


“The discovery of global Lambda polarization in non-central heavy ion collisions opens new directions in the study of the hottest, least viscous - and now, most vortical - fluid ever produced in the laboratory.”

STAR Collaboration,  
Nature 548 (2017) 62

# MEASUREMENT OF $\Lambda$ POLARIZATION

$\Lambda$  and  $\bar{\Lambda}$  hyperons are “self-analyzing”. That is, in the weak decay  $\Lambda \rightarrow p + \pi^-$ , the proton tends to be emitted along the spin direction of the parent  $\Lambda$ .



If  $\theta^*$  is the angle between the daughter proton momentum  $\Lambda$  polarization vector in the hyperon rest frame, then:

$$\frac{dN}{d \cos \theta^*} = \frac{1}{2} (1 + \alpha_H |\vec{P}_H| \cos \theta^*) \quad \rightarrow \quad P_H = \frac{8}{\pi \alpha_H} \sin(\phi_p^* - \Psi_{RP})$$

[Nature 548 (2017) 62]

# THERMAL VORTICITY AND POLARIZATION

In local thermal equilibrium, the ensemble average of the spin vector for spin-1/2 fermions with four-momentum  $p$  at space-time point  $x$  is obtained from the statistical-hydrodynamical model as well as the Wigner function approach and reads

$$S^\mu(x, p) = -\frac{1}{8m} (1 - n_F) \epsilon^{\mu\nu\rho\sigma} p_\nu \varpi_{\rho\sigma}(x),$$

where the thermal vorticity tensor is given by

$$\varpi_{\mu\nu} = \frac{1}{2} (\partial_\nu \beta_\mu - \partial_\mu \beta_\nu),$$

with  $\beta^\mu = u^\mu / T$  being the inverse-temperature four-velocity. The number density of  $\Lambda$ 's is very small so that we can make the approximation  $1 - n_F \simeq 1$  Therefore:

$$S^\mu(x, p) = -\frac{1}{8m} \epsilon^{\mu\nu\rho\sigma} p_\nu \varpi_{\rho\sigma}(x).$$

By decomposing the thermal vorticity into the following components,

$$\varpi_T = (\varpi_{0x}, \varpi_{0y}, \varpi_{0z}) = \frac{1}{2} \left[ \nabla \left( \frac{\gamma}{T} \right) + \partial_t \left( \frac{\gamma \mathbf{v}}{T} \right) \right],$$

$$\varpi_S = (\varpi_{yz}, \varpi_{zx}, \varpi_{xy}) = \frac{1}{2} \nabla \times \left( \frac{\gamma \mathbf{v}}{T} \right),$$

Equation can be rewritten as

$$S^0(x, p) = \frac{1}{4m} \mathbf{p} \cdot \varpi_S, \quad \mathbf{S}(x, p) = \frac{1}{4m} (E_p \varpi_S + \mathbf{p} \times \varpi_T),$$

where  $E_p$ ,  $\mathbf{p}$ ,  $m$  are the  $\Lambda$ 's energy, momentum, and mass, respectively. The spin vector of  $\Lambda$  in its rest frame is denoted as  $S^{*\mu} = (0, \mathbf{S}^*)$  and is related to the same quantity in the c.m. frame by a Lorentz boost. Finally:

$$P = \frac{\langle \mathbf{S}^* \rangle \cdot \mathbf{J}}{|\langle \mathbf{S}^* \rangle| |\mathbf{J}|},$$

[F. Becattini et al, Phys. Rev. C 95, 054902 (2017)]

The background of the slide is a gradient of purple and blue. It is decorated with several realistic water droplets of various sizes, some with highlights and shadows, scattered across the top and right sides. The text is centered in the middle of the slide.

# **MODELS AT OUR DISPOSAL**



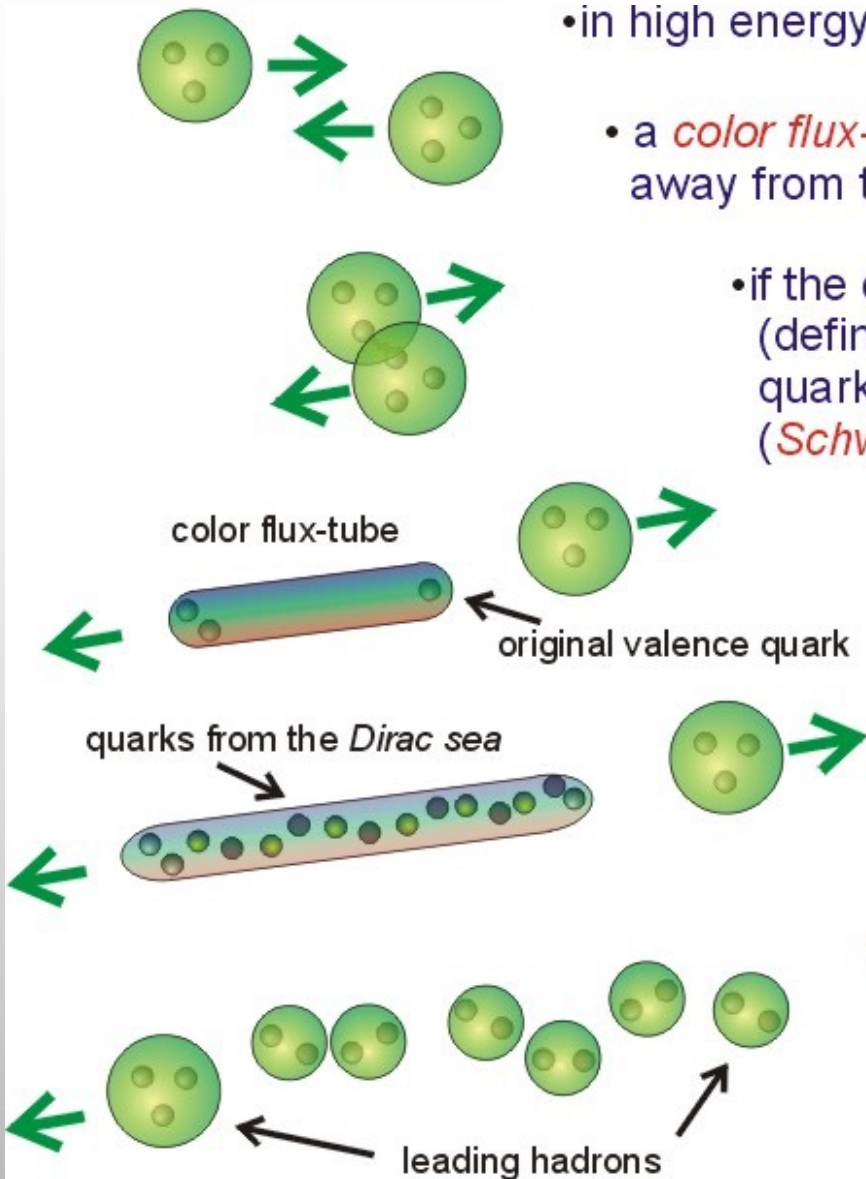
# TRANSPORT MODEL: UrQMD

- Represents a Monte Carlo method for the time evolution of the various phase space densities of particle species.
- Based on the covariant propagation of all hadrons on classical trajectories, stochastic binary scatterings, resonance and string formation with their subsequent decay.
- Provides the solution of the relativistic Boltzmann equation.
- The collision criterion (black disk approximation):  
$$d < d_0 = \sqrt{\sigma_{tot}(\sqrt{s}, \text{type})} / \pi$$
- 55 baryons and 32 mesons are included. All antiparticles and isospin-projected states are implemented.
- Cross sections are taken from PDG.
- Resonances are implemented in Breit–Wigner form.

[S. A. Bass et al, Prog. Part. Nucl. Phys. 41 (1998) 255-369,

M. Bleicher et al, J. Phys. G: Nucl. Part. Phys. 25 (1999) 1859-1896]

# PARTICLE PRODUCTION VIA STRINGS IN URQMD



- in high energy collisions hadrons can be excited into *strings*

- a *color flux-tube* is formed by pulling one valence quark away from the remaining ones in the hadron

- if the color-field increases beyond a critical value (defined by the *string-tension*), spontaneous quark-antiquark creation from the *Dirac sea* occurs (*Schwinger mechanism*)

- newly created (anti-)quarks require a *formation time* to form hadrons

- *leading hadrons* interact with *reduced cross sections* during their formation time

- *newly created hadrons* have *zero cross section* during their formation time

# STATISTICAL MODEL OF IDEAL HADRON GAS

input values

output values

$$\epsilon^{\text{mic}} = \frac{1}{V} \sum_i E_i^{\text{SM}}(T, \mu_B, \mu_S),$$

$$\rho_B^{\text{mic}} = \frac{1}{V} \sum_i B_i \cdot N_i^{\text{SM}}(T, \mu_B, \mu_S),$$

$$\rho_S^{\text{mic}} = \frac{1}{V} \sum_i S_i \cdot N_i^{\text{SM}}(T, \mu_B, \mu_S).$$

Multiplicity  $\rightarrow$

Energy  $\rightarrow$

Pressure  $\rightarrow$

Entropy density  $\rightarrow$

$$N_i^{\text{SM}} = \frac{V g_i}{2\pi^2 \hbar^3} \int_0^\infty p^2 f(p, m_i) dp,$$

$$E_i^{\text{SM}} = \frac{V g_i}{2\pi^2 \hbar^3} \int_0^\infty p^2 \sqrt{p^2 + m_i^2} f(p, m_i) dp$$

$$P^{\text{SM}} = \sum_i \frac{g_i}{2\pi^2 \hbar^3} \int_0^\infty p^2 \frac{p^2}{3(p^2 + m_i^2)^{1/2}} f(p, m_i) dp$$

$$s^{\text{SM}} = - \sum_i \frac{g_i}{2\pi^2 \hbar^3} \int_0^\infty f(p, m_i) [\ln f(p, m_i) - 1] p^2 dp$$

Input from UrQMD:

$$\epsilon_{UrQMD} = \frac{1}{V} \sum_i E_i$$

$$\rho_{B_{UrQMD}} = \frac{1}{V} \sum_i B_i$$

$$\rho_{S_{UrQMD}} = \frac{1}{V} \sum_i S_i$$

Stat. Physics:

$$\epsilon_{stat} = \sum_i \epsilon_i(T, \mu_B, \mu_S)$$

$$\rho_{B_{stat}} = \sum_i B_i n_i(T, \mu_B, \mu_S)$$

$$\rho_{S_{stat}} = \sum_i S_i n_i(T, \mu_B, \mu_S)$$

$$\chi^2 = \frac{(\epsilon_{UrQMD} - \epsilon_{stat})^2}{\sigma_\epsilon^2} +$$
$$+ \frac{(\rho_{B_{UrQMD}} - \rho_{B_{stat}})^2}{\sigma_{\rho_B}^2} +$$
$$+ \frac{(\rho_{S_{UrQMD}} - \rho_{S_{stat}})^2}{\sigma_{\rho_S}^2}$$

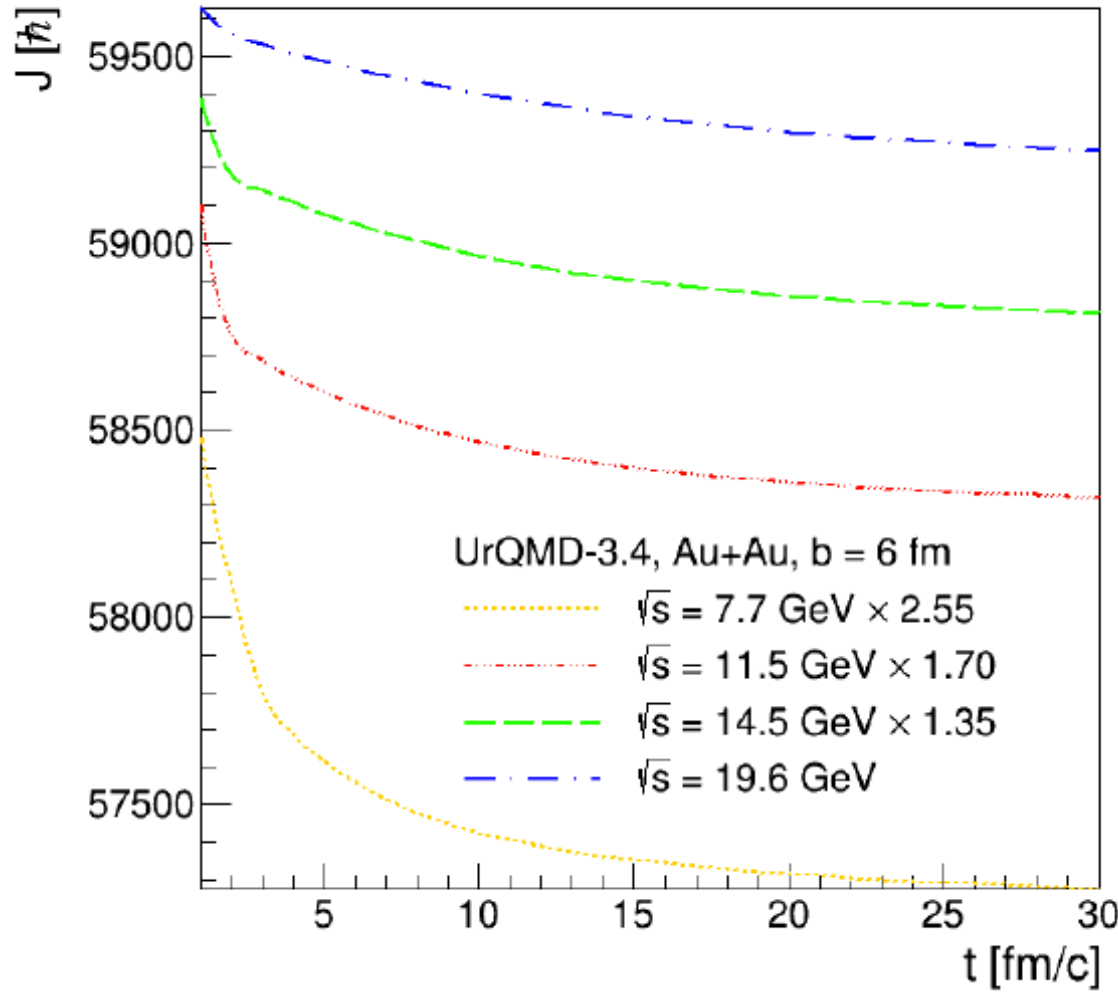
Minuit2 numerical minimizer

Output:  
 $T, \mu_B, \mu_S$

The background is a gradient of purple and blue. It is decorated with several realistic water droplets of various sizes, some clustered together and others isolated. The droplets have highlights and shadows, giving them a three-dimensional appearance. The word "RESULTS" is centered in the middle of the page in a white, bold, sans-serif font.

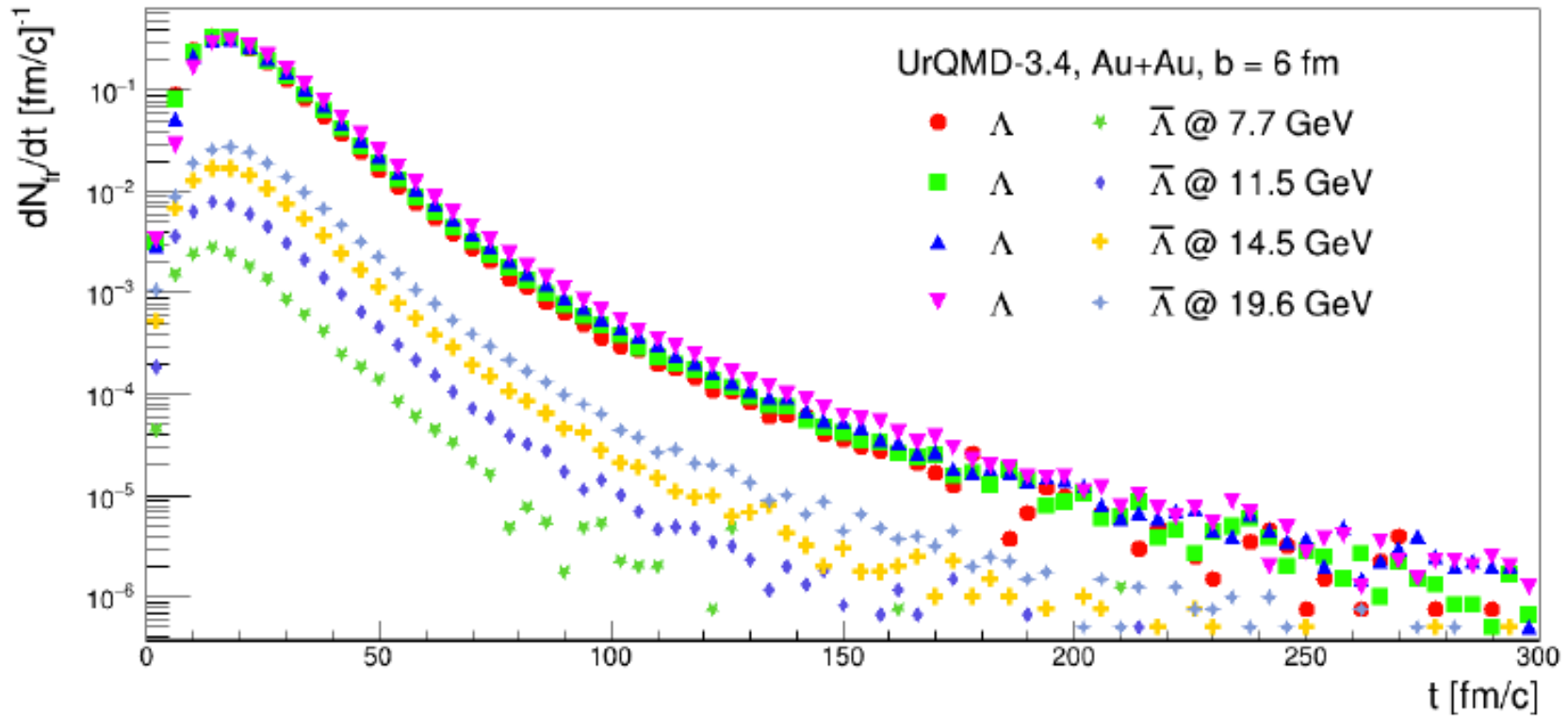
# RESULTS

# ANGULAR MOMENTUM



Angular momentum is not exactly conserved at the early stage of the collision because of inelastic collisions (especially, in the fragmentation of strings). The maximum deviation, however, does not exceed 2%.

# FREEZE-OUT OF HYPERONS

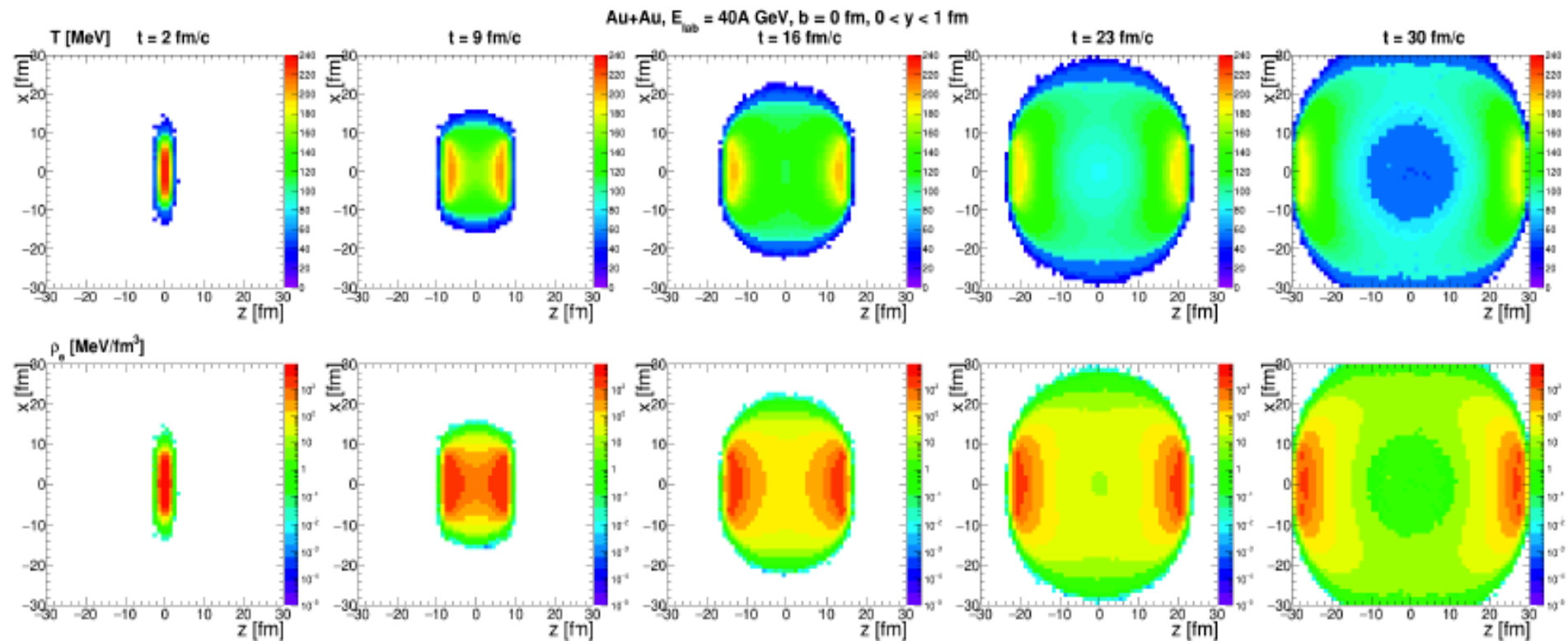


$\Lambda$ 's and  $\bar{\Lambda}$ 's with  $|y| < 1$  and  $0.2 < p_t < 3$  GeV/c were analyzed.

$\sqrt{s}$ [GeV]	7.7	11.5	14.5	19.6
Mean freeze-out time $\Lambda$ [fm/c]	21.3009	21.9568	23.066	24.3462
Mean freeze-out time $\bar{\Lambda}$ [fm/c]	19.7806	21.0302	21.959	23.1288

# EVOLUTION OF TEMPERATURE AND ENERGY DENSITY

L.B. et al, Symmetry 13 (2021) 10, 1852

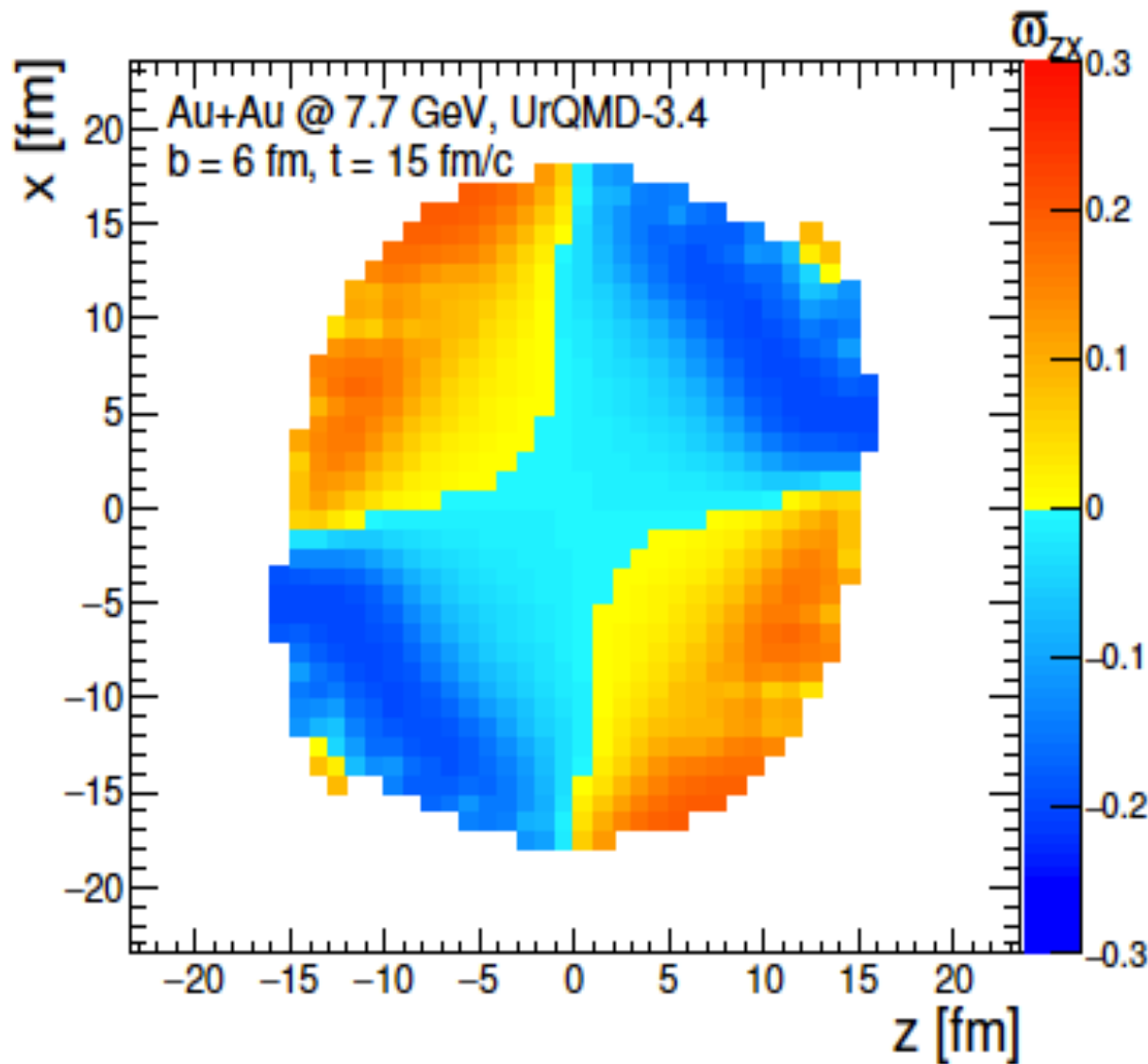


Neither energy density nor temperature is uniformly distributed within the expanding hot and dense nuclear matter



# THERMAL VORTICITY IN THE REACTION PLANE

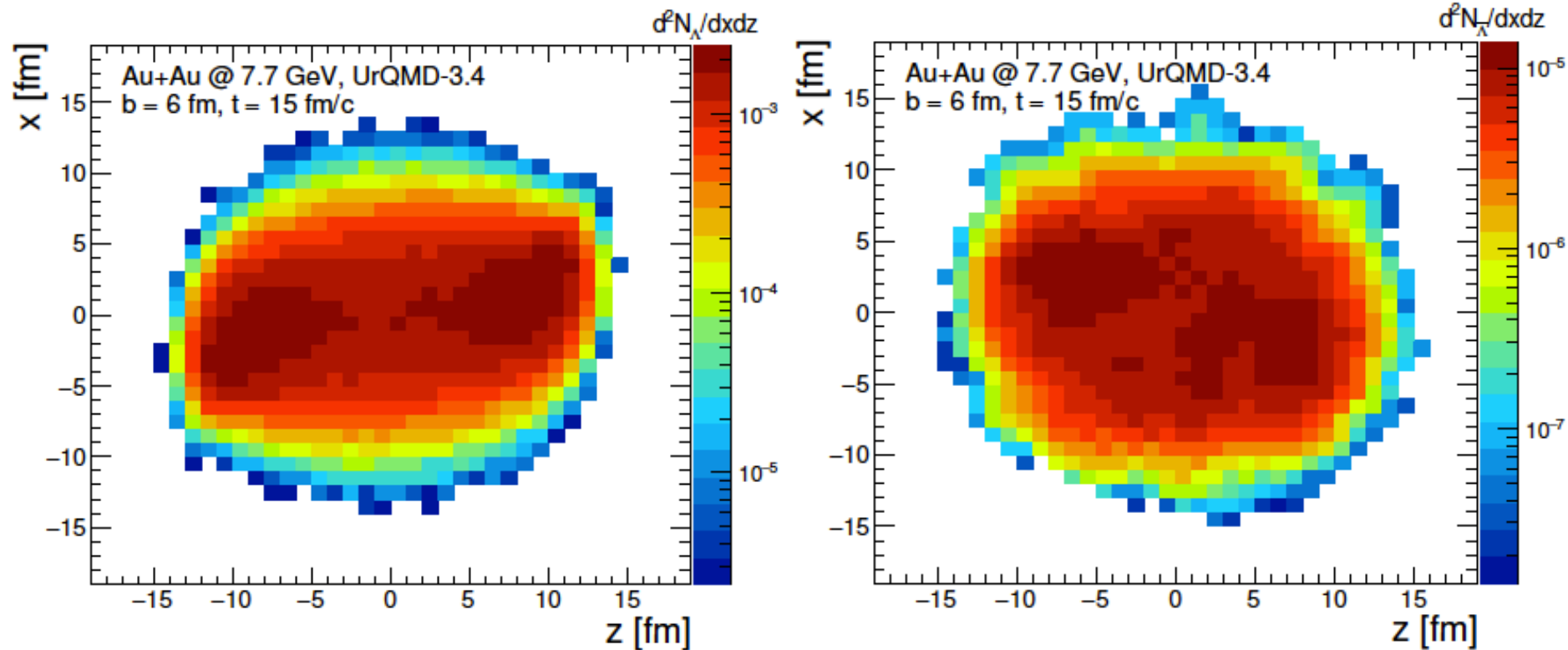
O. Vitiuk, L.B., E. Zabrodin,  
PLB 803 (2020) 135298



Thermal vorticity component  $\omega_{zx}$  has a quadruple structure in the reaction plane. It is stable in time, but its magnitude decreases because of the system expansion. At intermediate energies, first and third quadrants are connected in the central area which has a small negative vorticity. This connection part becomes smaller with increasing energy of heavy ion collisions.

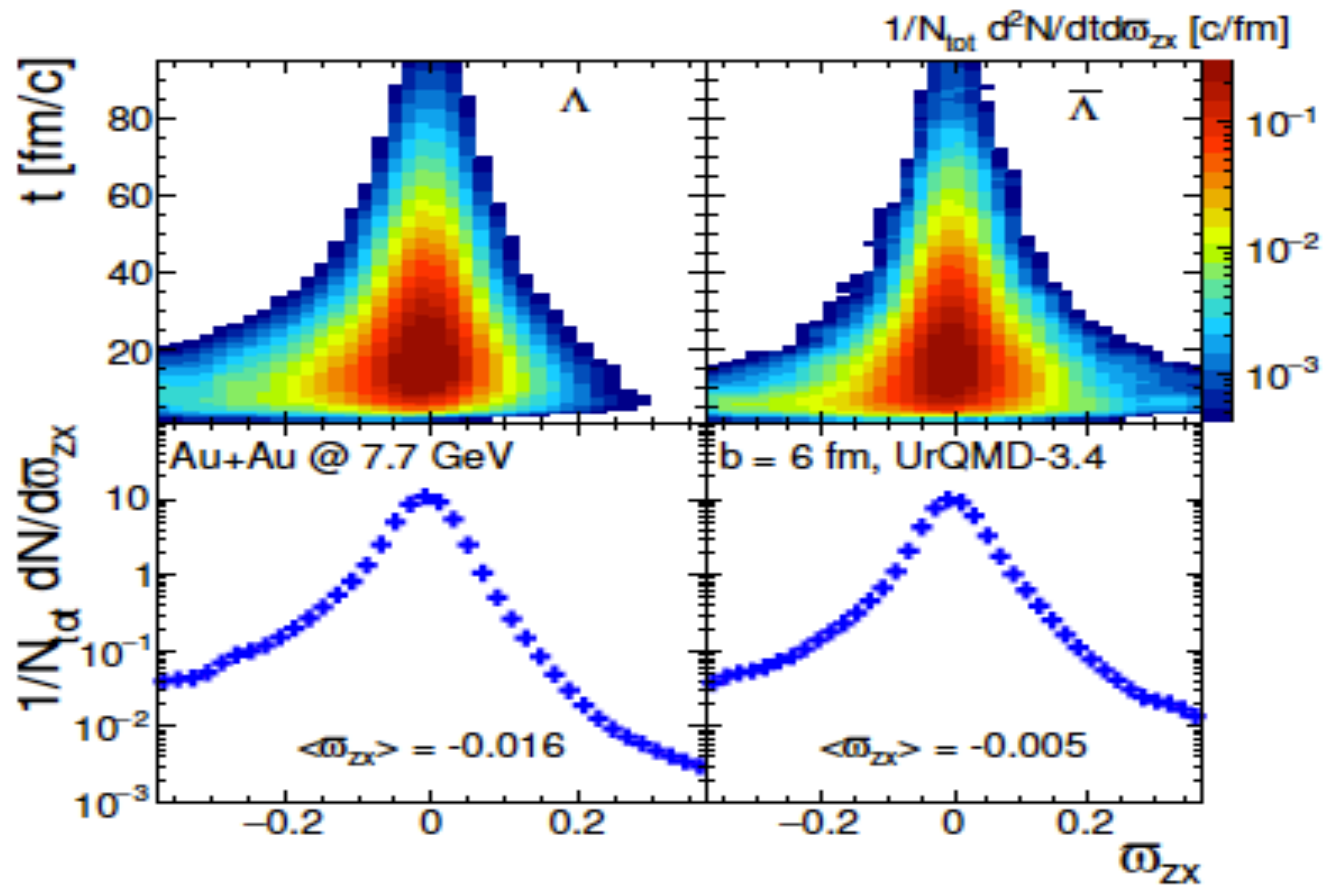
# SPATIAL DISTRIBUTION OF $\Lambda$ AND ANTI- $\Lambda$

O. Vitiuk, L.B., E. Zabrodin,  
PLB 803 (2020) 135298



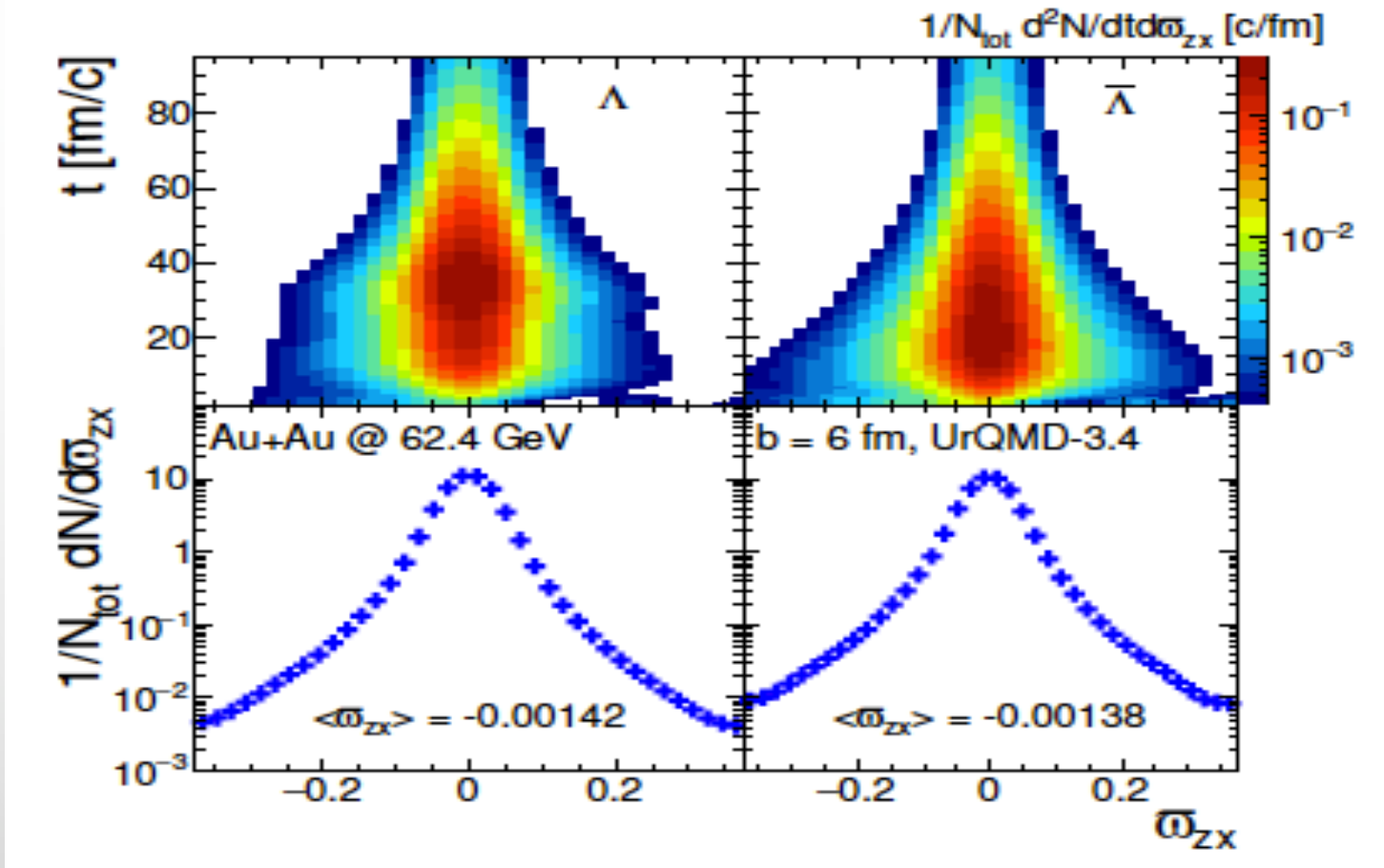
At  $\sqrt{s} = 7.7$  GeV  $\Lambda$  are mostly located near hot and dense regions and  $\bar{\Lambda}$  are distributed more uniformly near system center.

# DEPENDENCE ON COLLISION ENERGY



At  $\sqrt{s} = 7.7 \text{ GeV}$   $\Lambda$  and  $\bar{\Lambda}$  are mainly emitted from regions with small negative vorticity, thus they should have non-zero positive polarization.  $\bar{\Lambda}$  has mean value of  $\omega_{zx}$  with larger magnitude than  $\Lambda$

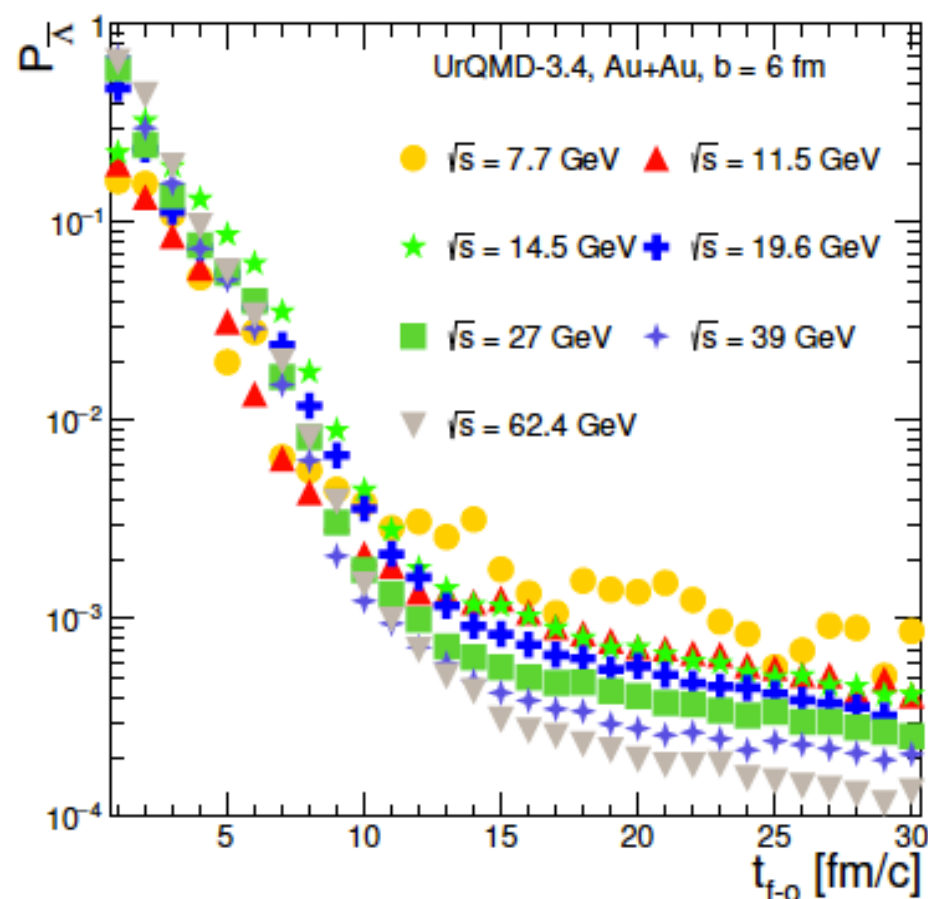
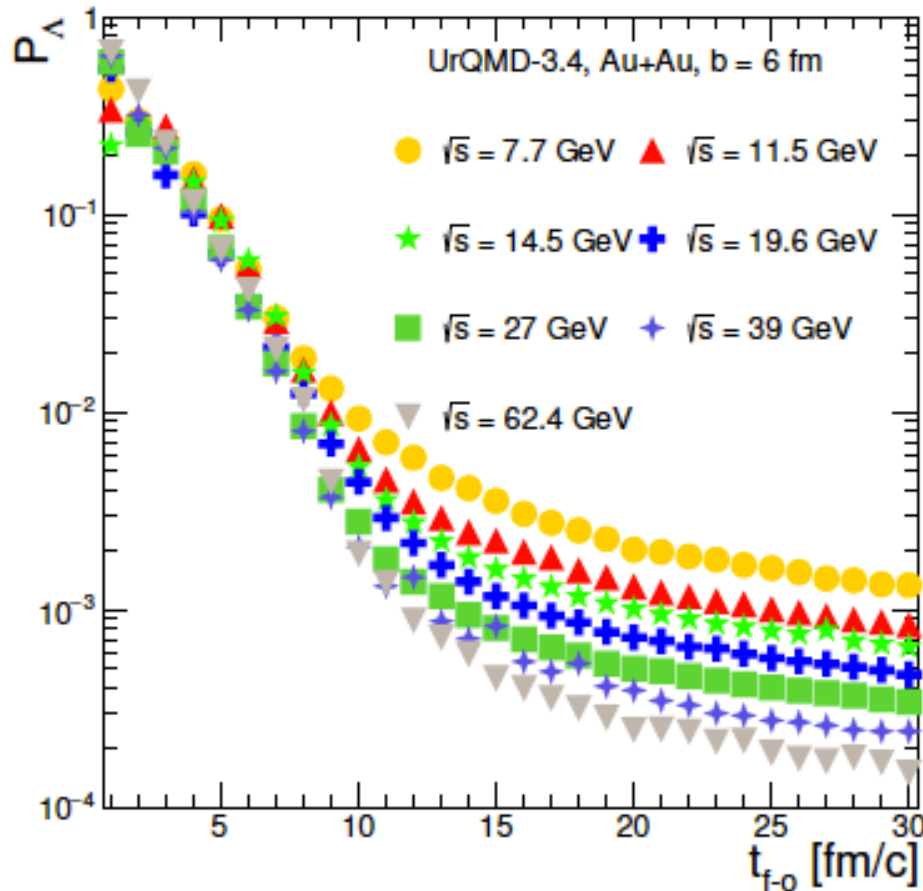
# DEPENDENCE ON COLLISION ENERGY



At  $\sqrt{s} = 62.4$  GeV  $\Lambda$  and  $\bar{\Lambda}$  are also mainly emitted from regions with small negative vorticity, but distributions are more symmetric and wide.

# POLARIZATION OF $\Lambda$ AND ANTI- $\Lambda$

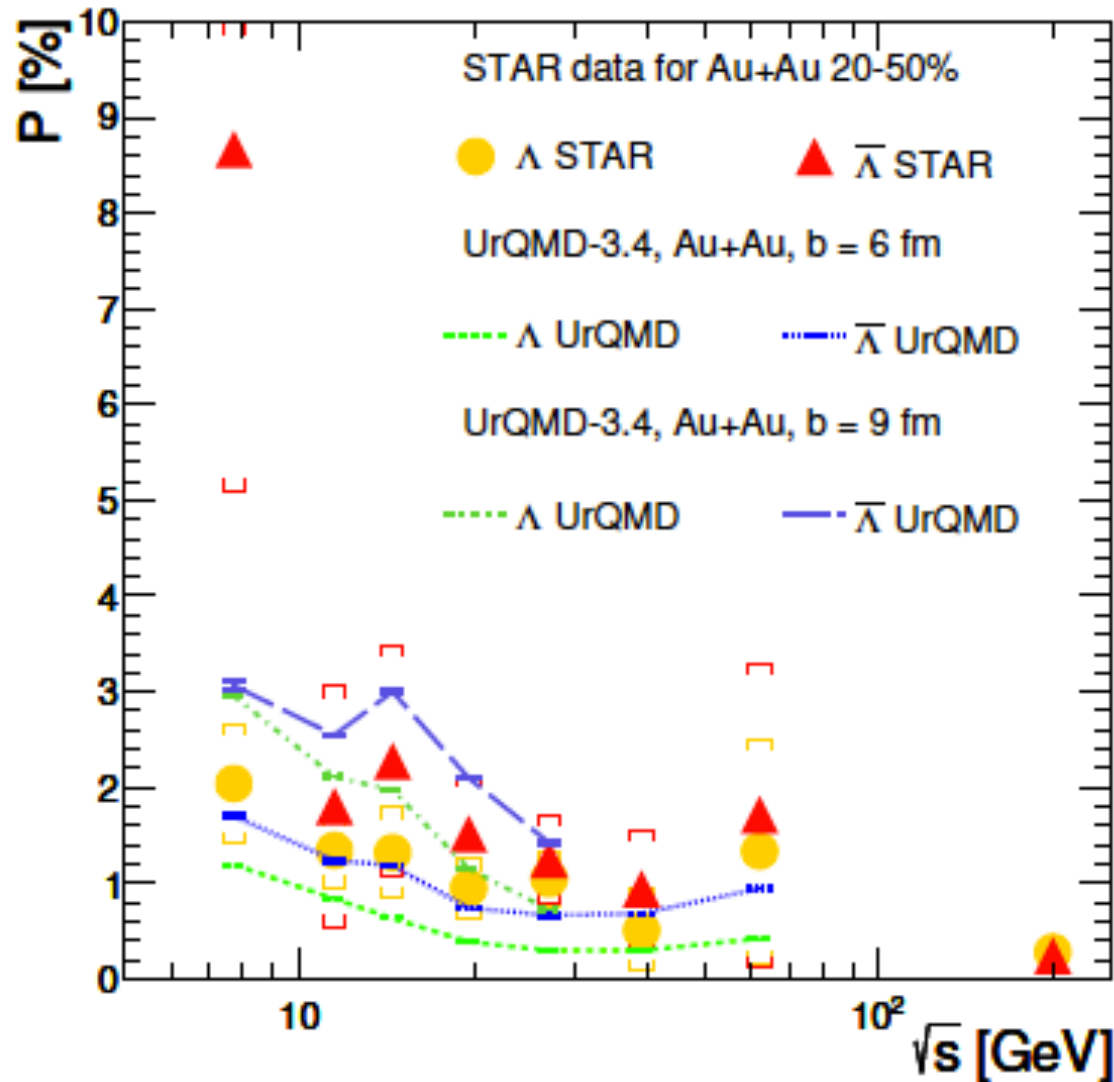
O. Vitiuk, L.B., E. Zabrodin, PLB 803 (2020) 135298



Polarization of both hyperons decreases with time. At the initial stage, they are mainly formed in hot and dense areas with high polarization. Later on polarization of newly formed hyperons rapidly drops

# ENERGY DEPENDENCE OF $\Lambda$ AND ANTI- $\Lambda$ POLARIZATION

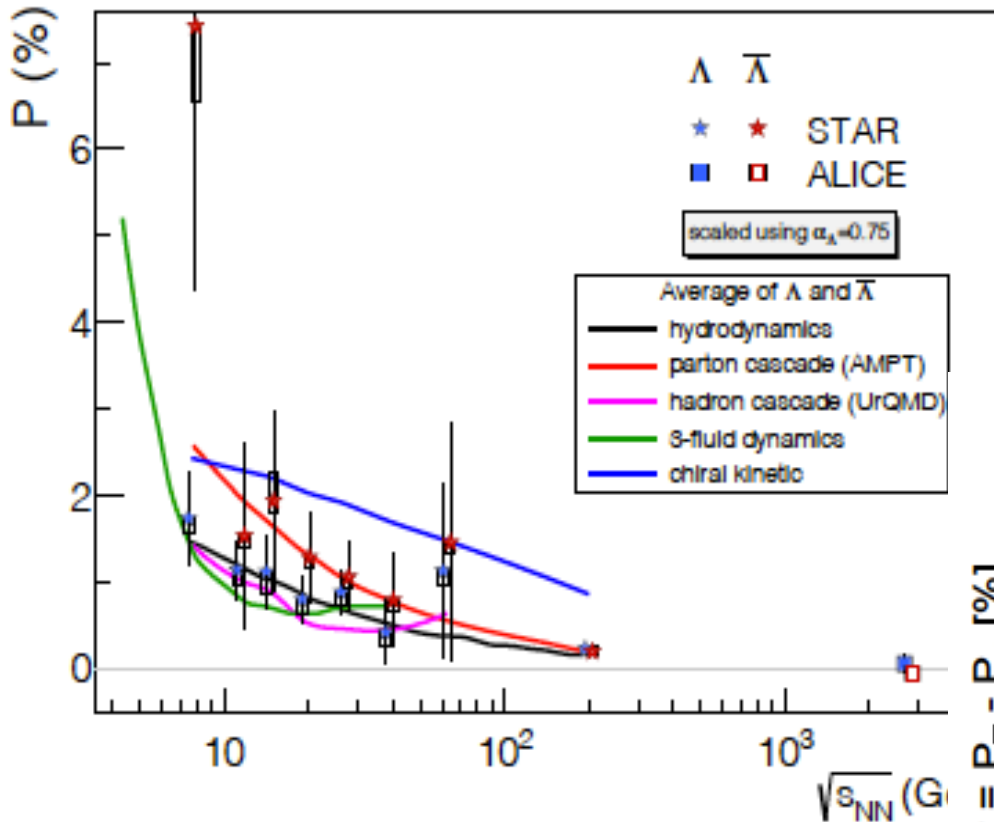
O. Vitiuk, L.B., E. Zabrodin,  
PLB 803 (2020) 135298



Difference in global polarization of both hyperons arises from

- (1) different spatio-temporal distributions of  $\Lambda$  and anti- $\Lambda$
- (2) different thermal vorticity in the freeze-out regions

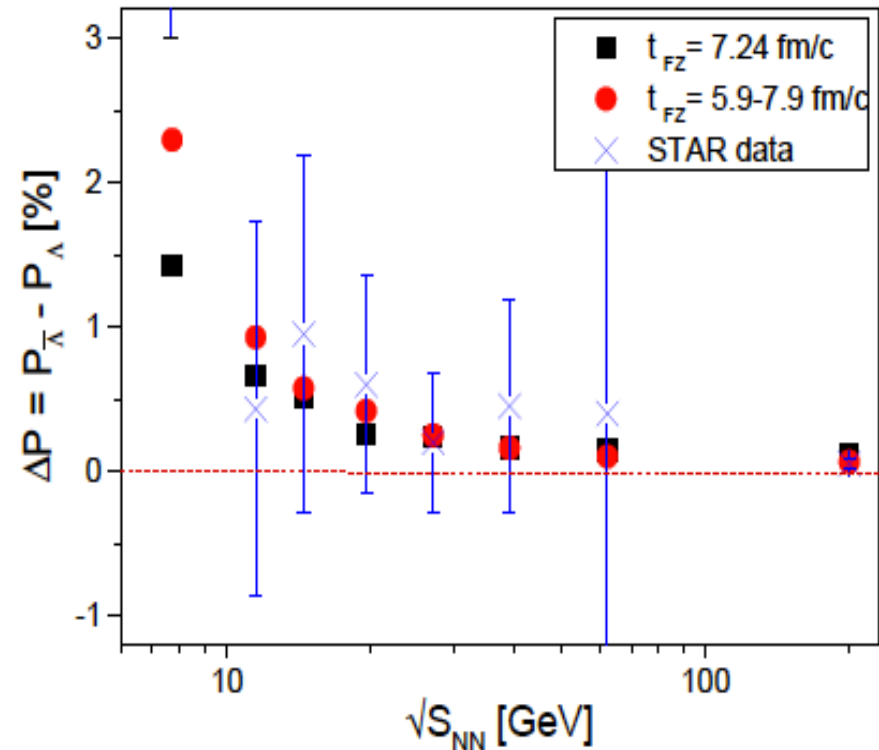
# OTHER MODELS



F.Becattini and M.A.Lisa,  
 Ann. Rev. Nucl. Part. Sci.  
 70 (2020) 395

The idea of different FO can  
 be employed in other models  
 also

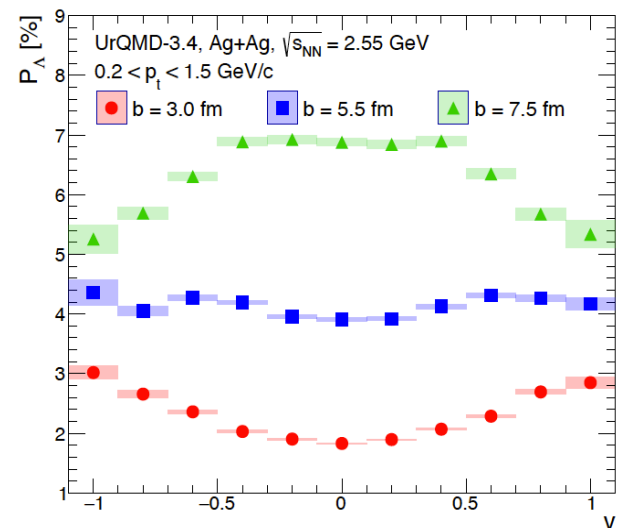
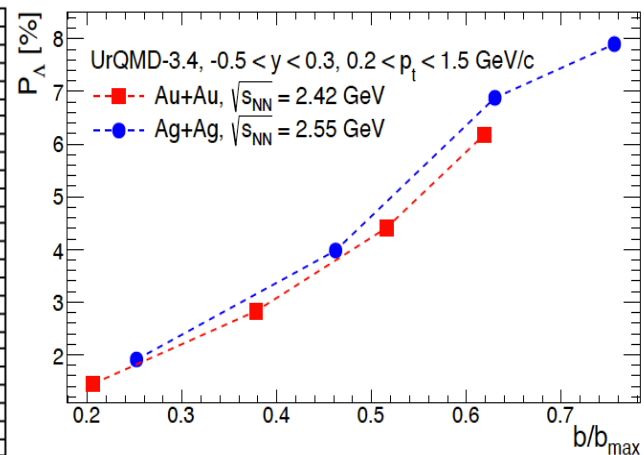
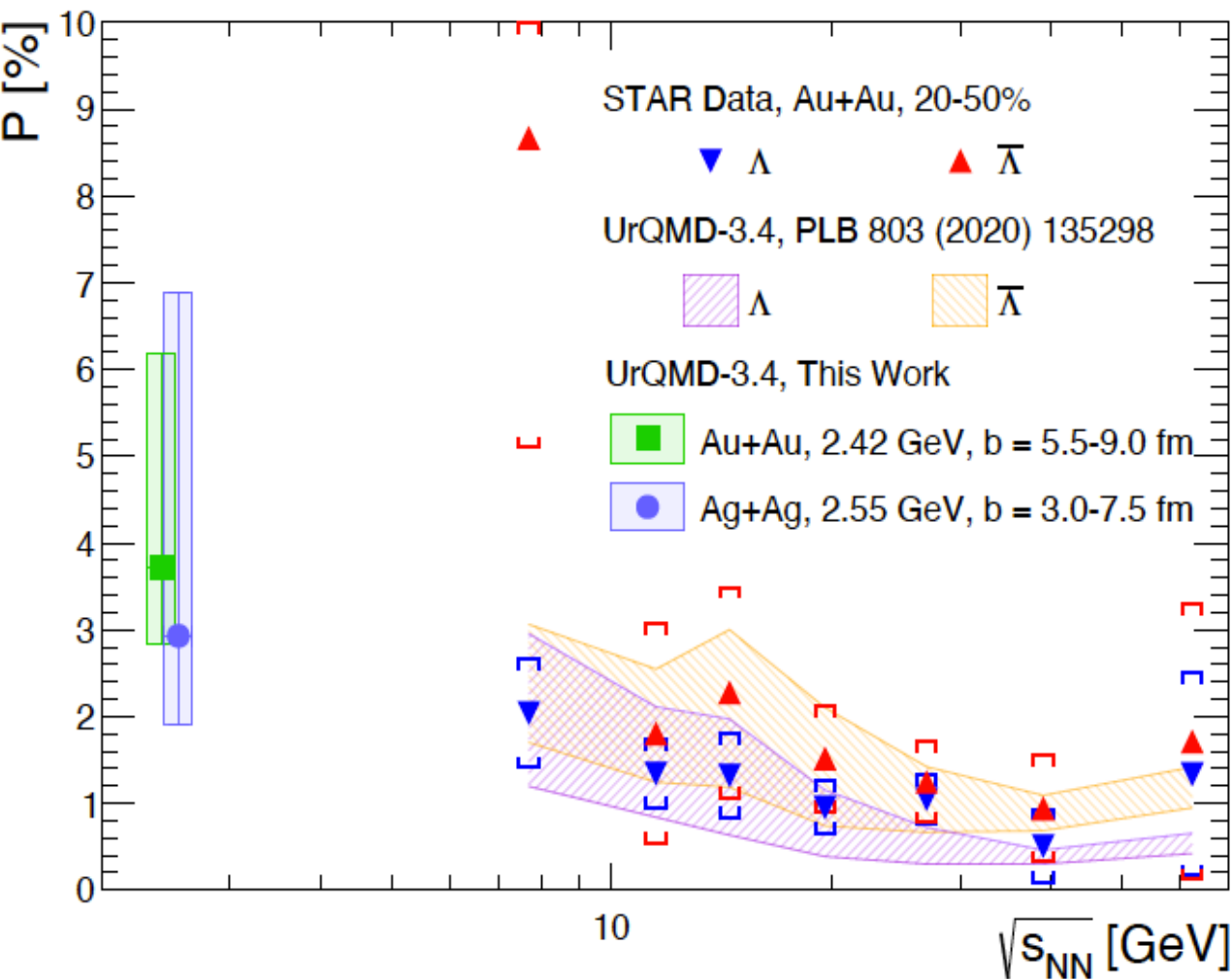
Y.Xie, G.Chen, L.P.Csernai,  
 EPJC 81 (2021) 12



# ENERGY DEPENDENCE OF $\Lambda$ AND ANTI- $\Lambda$ POLARIZATION

Request from HADES Collaboration:

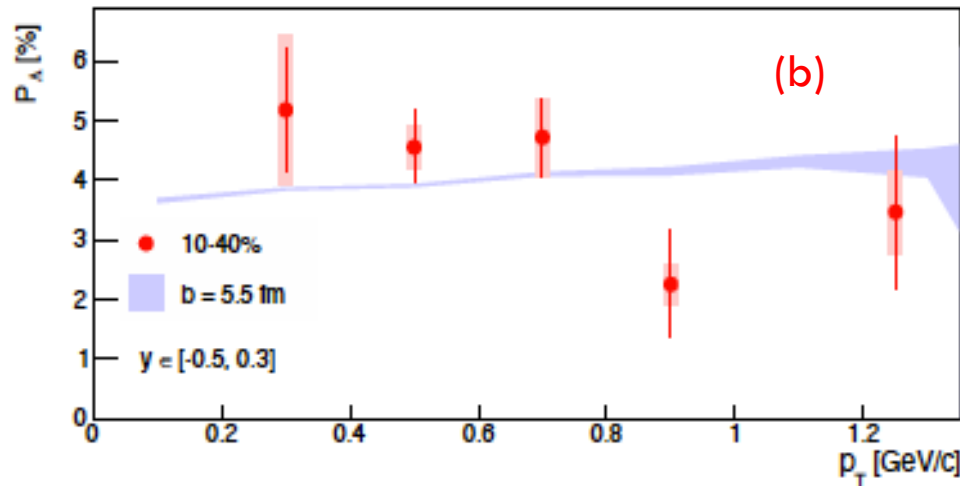
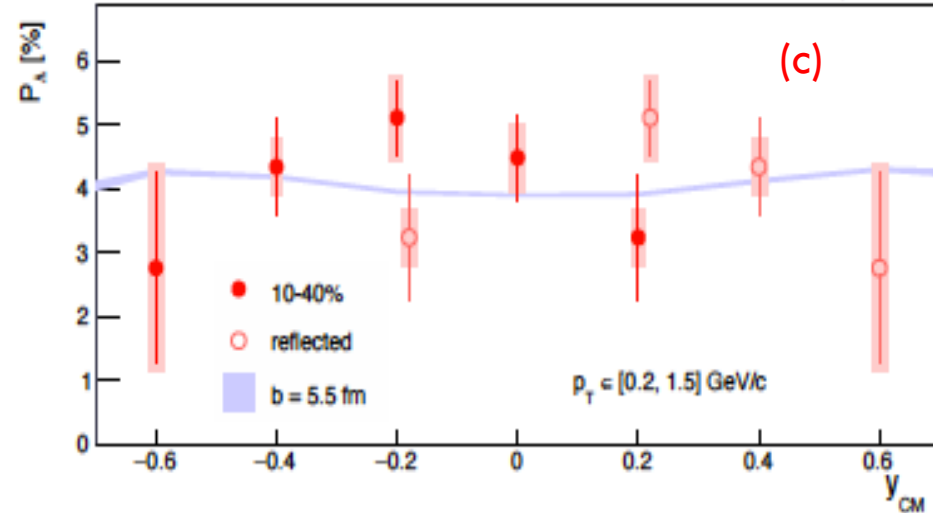
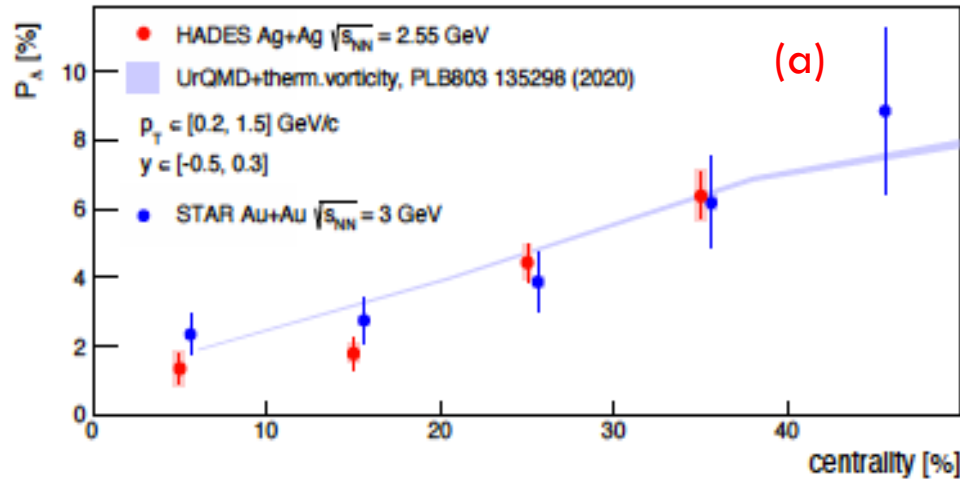
Provide model predictions for  $\Lambda$  and anti- $\Lambda$  polarization in (i) Ag+Ag @ 2.55 GeV and (ii) Au+Au @ 2.42 GeV for given centrality and kinematic windows





# COMPARISON WITH THE DATA

HADES Collab., PLB 835 (2022) 137506



Global polarization of  $\Lambda$  as function of centrality (a), transverse momentum (b), and rapidity (c) in Ag+Ag collisions at  $\sqrt{s} = 2.55$  GeV

“The agreement is remarkable ...” (PLB 835, 137506)

The background of the slide is a gradient of purple, transitioning from a lighter shade at the top to a darker shade at the bottom. Scattered across the upper and right portions of the slide are several realistic water droplets of various sizes. Each droplet has a bright highlight on its upper-left side, giving it a three-dimensional appearance. The word "CONCLUSIONS" is centered in the middle of the slide in a bold, white, sans-serif font.

# CONCLUSIONS

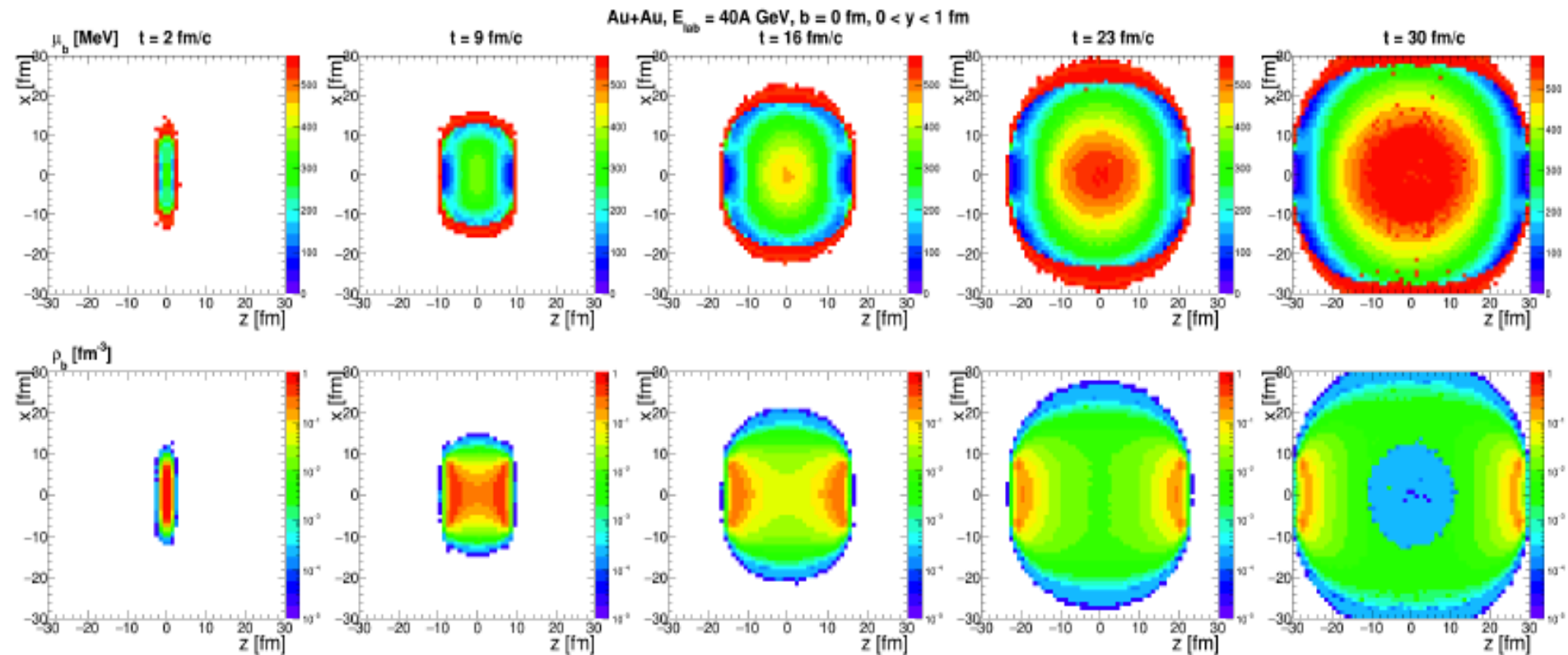
# CONCLUSIONS

1. Thermal vorticity in non-central heavy ion collisions, Au+Au and Ag+Ag, was studied at  $\sqrt{s} = 2,4 \text{ --} 19,6 \text{ GeV}$  within the framework of UrQMD model
2. Quadruple structure of  $\omega_{zx}$  was obtained
3. The magnitude of vorticity dependence on time and energy of colliding nuclei is studied
4. Self-consistent method for calculation of  $\Lambda$ -polarization in microscopic transport model is developed
5. The distribution of  $\Lambda$  and anti- $\Lambda$  is different in space, their freeze-out distributions are (slightly) different in time, therefore these hyperons are emitted from regions with different vorticity

The background is a gradient of purple and blue, with several realistic water droplets of various sizes scattered across it. The droplets have highlights and shadows, giving them a three-dimensional appearance. The text is centered in the upper half of the image.

**THANK YOU FOR YOUR  
ATTENTION !**

# EVOLUTION OF BARYON CHEMICAL POTENTIAL AND DENSITY



# EVOLUTION OF STRANGENESS CHEMICAL POTENTIAL AND STRANGENESS DENSITY

