

# Long-Range Interactions of $L_\mu - L_\tau$ symmetry at INO-ICAL

## Long-range Neutrino Interactions due to $L_\mu - L_\tau$ symmetry

- We focus on new interactions generated by the anomaly-free, gauged, abelian lepton-number symmetry  $L_\mu - L_\tau$ . This is a renormalizable and minimal extension of the Standard Model (SM).
- Due to neutrino flavor oscillation, this symmetry must be broken, which gives rise to a new gauge boson  $Z'$ . This  $Z'$  can mix with  $Z$  and introduces a four-fermion neutrino matter interaction term via  $Z - Z'$  mixing (Phys. Rev. D 57 (1998) 6788):

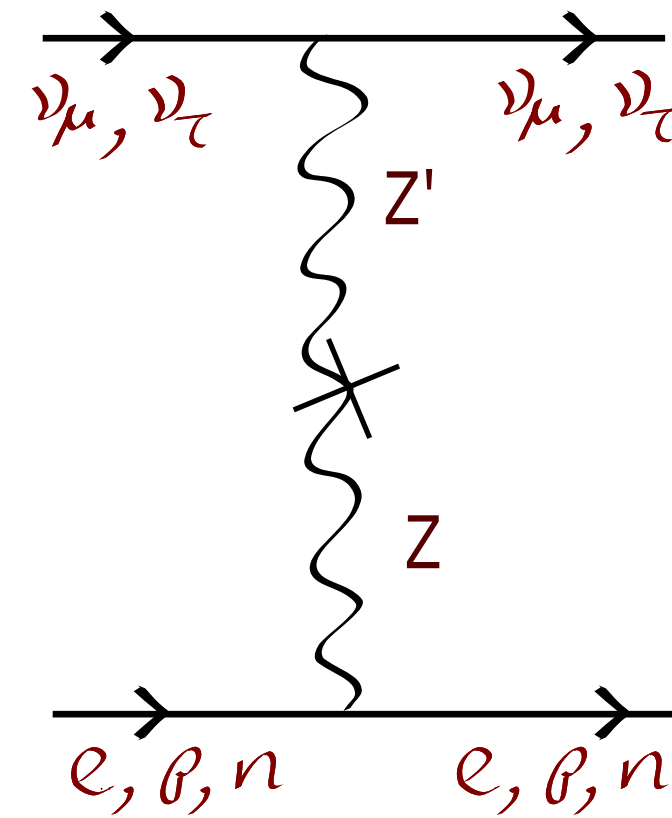
$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{Z'} + \mathcal{L}_{mix}$$

with

$$\mathcal{L}_{Z'} = -\frac{1}{4}Z'_{\mu\nu}Z'^{\mu\nu} + \frac{1}{2}\hat{M}_{Z'}^2\hat{Z}'_\mu\hat{Z}'^\mu - \hat{g}'j'^\mu\hat{Z}'_\mu,$$

$$j'^\mu = \bar{\mu}\gamma^\mu\mu + \bar{\nu}_\mu\gamma^\mu P_L\nu_\mu - \bar{\tau}\gamma^\mu\tau - \bar{\nu}_\tau\gamma^\mu P_L\nu_\tau$$

$$\mathcal{L}_{mix} = -\frac{\sin\chi}{2}Z'_{\mu\nu}\hat{B}^{\mu\nu} + \delta\hat{M}_{Z'}^2\hat{Z}'_\mu\hat{Z}'^\mu$$



- Under  $L_\mu - L_\tau$  symmetry, a neutrino experiences a flavor-dependent Yukawa interaction with a range  $\sim 1/m'_{\mu\tau}$ . If the mass of the new gauge boson is ultralight ( $m'_{\mu\tau} \sim 0$ ), then the interaction is long ranged, which is denoted as Long-Range Interaction (LRI).

## New Flavor-diagonal NC Interactions for Atmospheric Neutrinos

- Coherent forward elastic interactions of terrestrial neutrinos with electron, proton, and neutron in Sun produce new potentials.
- Contributions from electrons and protons cancel each other, thus only neutrons contribute to the extra potential for terrestrial neutrinos and antineutrinos.
- For  $1/m_{\mu\tau} >$  Earth-Sun distance ( $R_{SE}$ ) or  $m_{\mu\tau} \ll 1 \text{ AU}^{-1} \approx 1.32 \times 10^{-18} \text{ eV}$ , effective potential due to neutrons in Sun is  $V_{\mu\tau}^\odot = \alpha_{\mu\tau} \frac{e}{4s_W c_W} \frac{N_n^\odot}{4\pi R_{SE}^2}$ , where  $N_n^\odot$  is total number of neutrons in Sun.
- Due to neutrons in Earth, the effective LR potential is  $V_{\mu\tau}^\oplus = \alpha_{\mu\tau} \frac{e}{4s_W c_W} \frac{N_n^\oplus}{4\pi R_\oplus^2}$ , where  $N_n^\oplus$  is total number of neutrons in Earth, and  $R_\oplus$  is radius of Earth.
- Assuming proper neutron number density in the Sun, we get  $V_{\mu\tau}^\odot = 3.6 \times 10^{-14} \times \frac{\alpha_{\mu\tau}}{10^{-50}} \text{ eV}$ .
- We get contribution from Earth's neutrons with PREM profile  $V_{\mu\tau}^\oplus = 0.79 \times 10^{-14} \times \frac{\alpha_{\mu\tau}}{10^{-50}} \text{ eV}$ .

The total LRI induced potential for the neutrons in Sun and Earth is

$$V_{\mu\tau} = V_{\mu\tau}^\odot + V_{\mu\tau}^\oplus = 4.4 \times 10^{-14} \times \frac{\alpha_{\mu\tau}}{10^{-50}} \text{ eV}. \quad (1)$$

The parameter  $\alpha_{\mu\tau}$  is combination of coupling strength of LRI and  $Z - Z'$  mixing parameters

✓ For antineutrino, the sign of  $V_{\mu\tau}$  is reversed

## Impact of LRI on the Evolution of Neutrinos

The Effective Hamiltonian in presence matter and LRI of  $L_\mu - L_\tau$  symmetry is

$$H_f = U \begin{bmatrix} 0 & 0 & 0 \\ 0 & \frac{\Delta m_{31}^2}{2E_\nu} & 0 \\ 0 & 0 & \frac{\Delta m_{31}^2}{2E_\nu} \end{bmatrix} U^\dagger + \begin{bmatrix} V_{CC} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 \\ 0 & V_{\mu\tau} & 0 \\ 0 & 0 & -V_{\mu\tau} \end{bmatrix},$$

U : PMNS matrix,  $V_{CC}$  : Matter induced potential

$\alpha_{\mu\tau} \sim 5 \times 10^{-50}$  corresponds to the LR potential ( $2.2 \times 10^{-13} \text{ eV}$ ) which is similar to the value of  $\Delta m_{31}^2/2E_\nu$  ( $2.5 \times 10^{-13} \text{ eV}$ ) with  $\Delta m_{31}^2 = 2.5 \times 10^{-3} \text{ eV}^2$  and  $E_\nu = 5 \text{ GeV}$ , thus is expected to affect neutrino and antineutrino oscillations.

## Impact on oscillations of neutrino and antineutrino with LRI

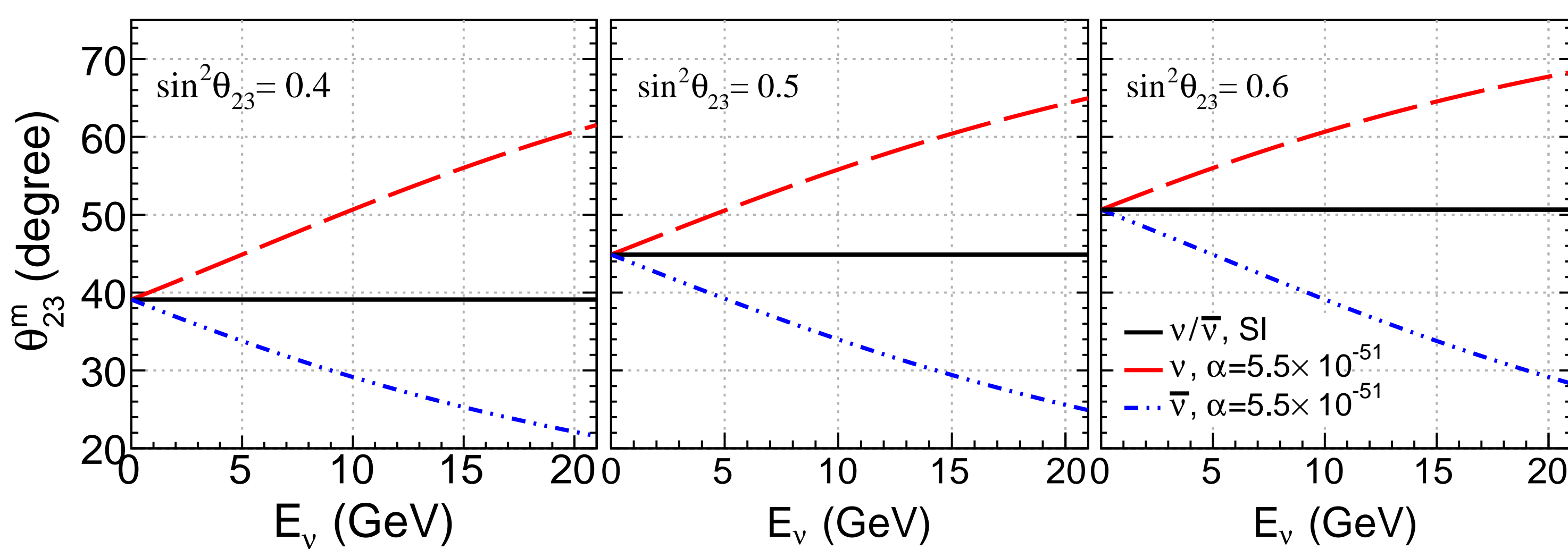


Figure 1: The variation of 2-3 mixing angle with neutrino energy for 5000 km baseline and normal mass ordering.

- In the presence of LRI,  $\theta_{23}^m$  changes from its vacuum value ( $\theta_{23}$ ) in opposite ways for neutrino and antineutrino. Depending on whether it approaches  $45^\circ$ , the survival probabilities of neutrinos change differently with different  $\theta_{23}$ .
- With  $\sin^2\theta_{23} = 0.5$ ,  $P(\nu_\mu \rightarrow \nu_\mu)$  is higher with SI+LRI than with SI for neutrino as well as antineutrino.
- With  $\sin^2\theta_{23} \neq 0.5$ , when  $\theta_{23}^m$  approaches  $45^\circ$ ,  $P(\nu_\mu \rightarrow \nu_\mu)$  with SI + LRI is smaller than SI.

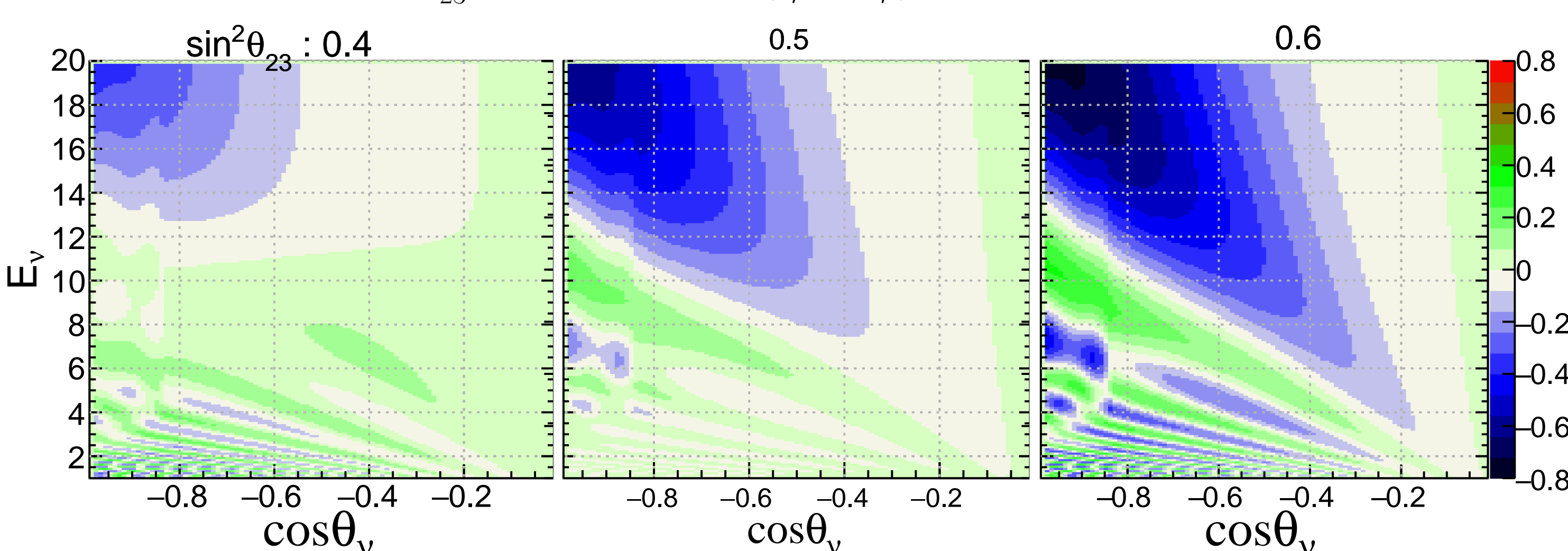


Figure 2: Difference of  $P(\nu_\mu \rightarrow \nu_\mu) + 0.5 \times P(\nu_e \rightarrow \nu_e)$  between SI ( $\alpha_{\mu\tau} = 0$ ) and SI + LRI ( $\alpha_{\mu\tau} = 5.5 \times 10^{-51}$ ).

## Important Features of Proposed ICAL Detector at INO

- Optimized for multi-GeV energy and wide ranges of baselines**
- Good energy and direction resolutions for muons:** in multi-GeV energy range, energy resolution for muons  $\sim 10\%$  to  $15\%$ , direction resolution is  $< 1^\circ$ .
- Excellent charge identification capability (CID):** distinguish  $\mu^-$  from  $\mu^+$ , thus  $\nu_\mu$  from  $\bar{\nu}_\mu$  CC interactions with  $\sim 99\%$  efficiency. JINST 9 (2014) P07001
- Reconstruction of hadron energy ( $E'_{had}$ ):** energy carried by hadrons at final state of neutrino and antineutrino interactions can be reconstructed at ICAL with a resolution of around  $40\%$ . JINST 8 (2013) P11003

## Event Distributions at ICAL after 10 Years of Running

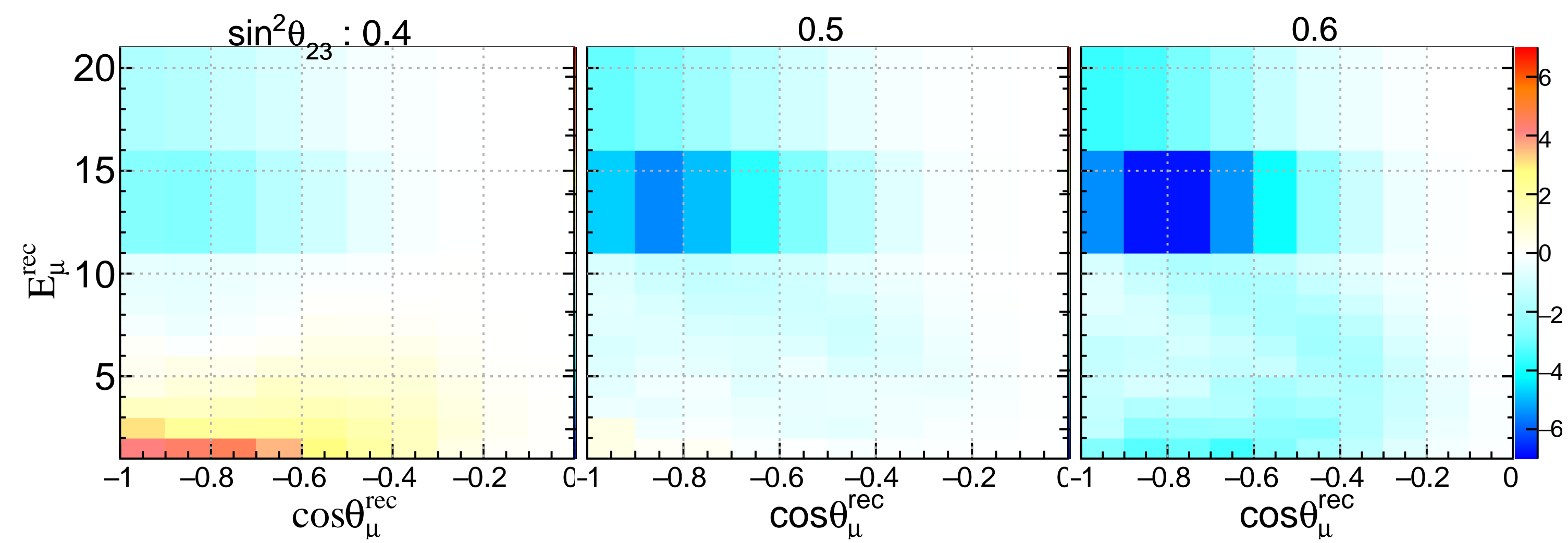


Figure 3: Difference in reconstructed  $\mu^-$  events between SI ( $\alpha_{\mu\tau} = 0$ ) and SI + LRI ( $\alpha_{\mu\tau} = 5.5 \times 10^{-51}$ ).

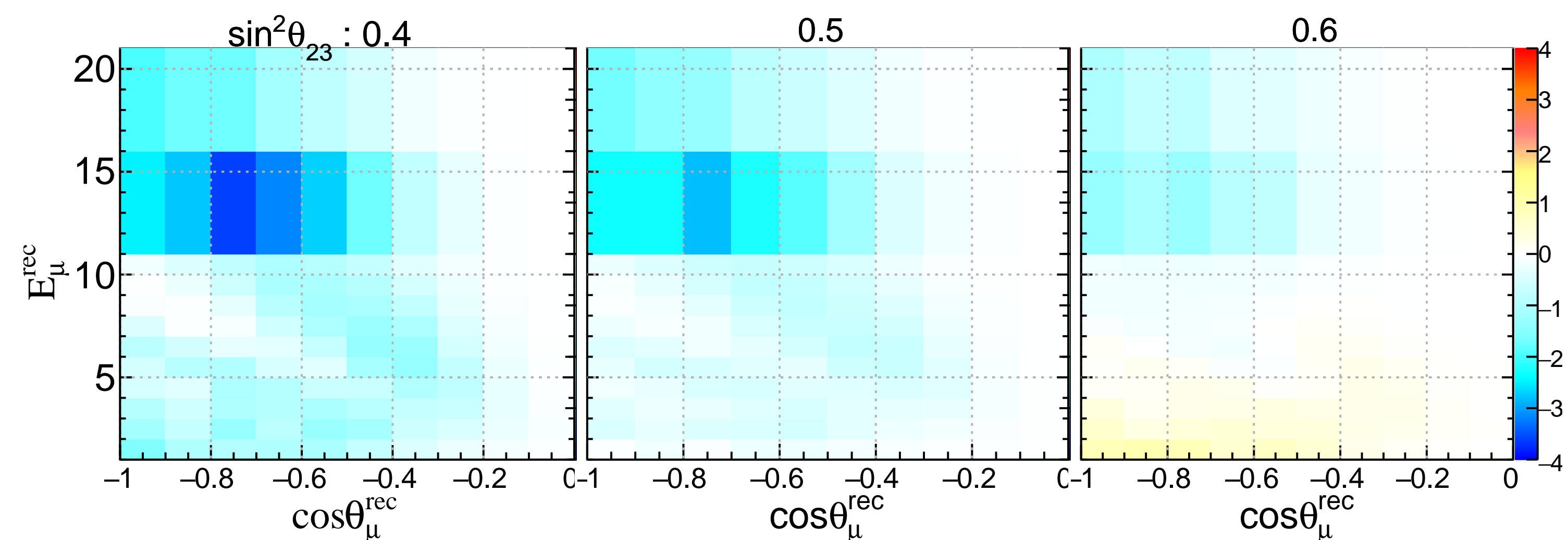
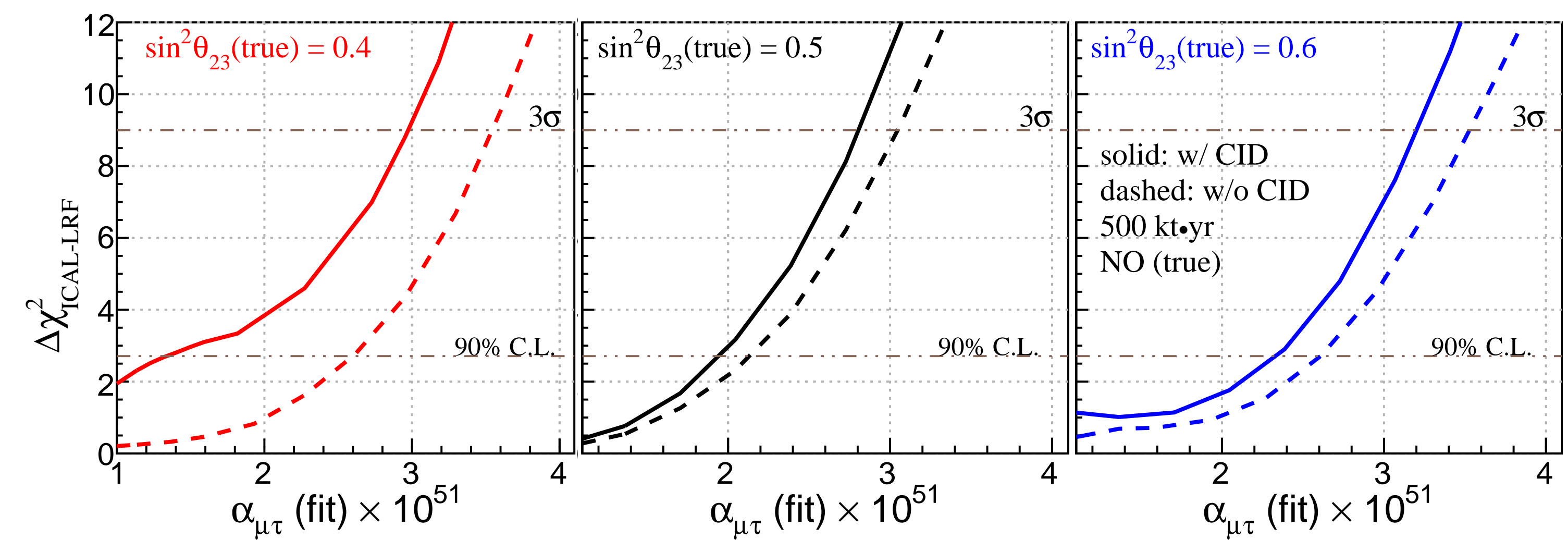


Figure 4: Difference in reconstructed  $\mu^+$  events between SI ( $\alpha_{\mu\tau} = 0$ ) and SI + LRI ( $\alpha_{\mu\tau} = 5.5 \times 10^{-51}$ ).

In presence of non-zero  $\alpha_{\mu\tau}$ ,  $\mu^-$  and  $\mu^+$  events are obtained to be higher in number than that with  $\alpha_{\mu\tau} = 0$  (SI), except for  $\mu^-$  events with  $\theta_{23}$  in low octant and for  $\mu^+$  with in  $\theta_{23}$  in high octant at around reconstructed muon energy  $\sim 2 \text{ GeV}$ .

## Sensitivity of ICAL to Constrain $\alpha_{\mu\tau}$ with 10 Years data

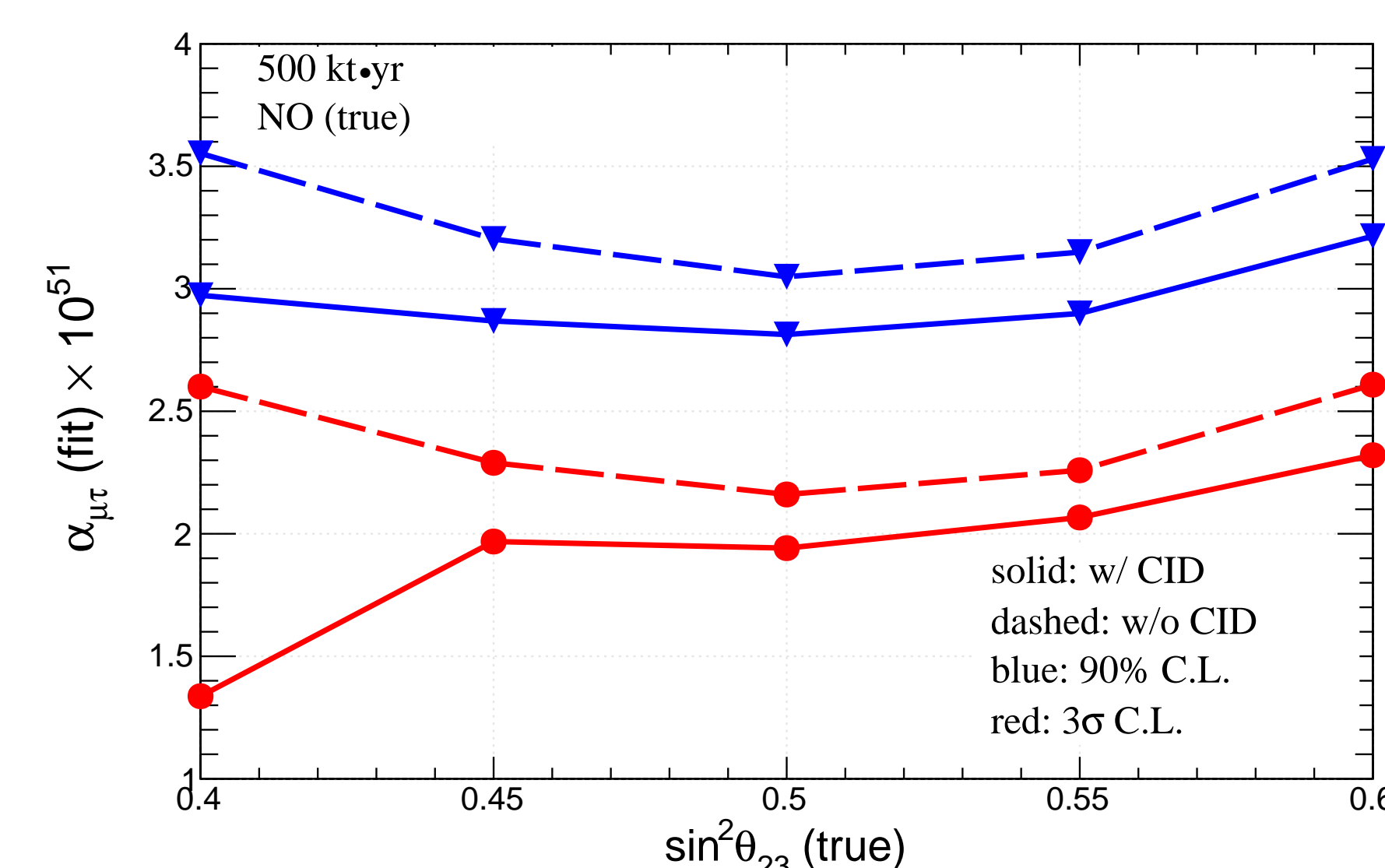
✓ Binning scheme: 12  $E_\mu$  bins in  $[1, 21] \text{ GeV}$ , 15  $\cos\theta$  bins in  $[-1, 1]$ , and 4  $E'_{had}$  bins in  $[0, 25] \text{ GeV}$ , for both  $\mu^-$  and  $\mu^+$  events. Poissonian  $\chi^2$  is used with systematic uncertainties using pull method.



✓ Results are marginalized over systematics as well as the oscillation parameters over current  $3\sigma$  allowed ranges of  $\theta_{23}$ ,  $\Delta m_{31}^2$ , and choices of neutrino mass hierarchy (normal and inverted ordering).

- MINOS anomaly (it has disappeared later) was resolved with  $\alpha_{\mu\tau} = 1.5 \times 10^{-50}$  J.Phys. G38 (2011)
- From gravitational fifth force searches, based on lunar ranging and torsion balance experiments, the constraint is  $\alpha_{\mu\tau} < 5 \times 10^{-24}$ . Phys. Rev. Lett. 100 (2008)

## Summary and Concluding Remarks



- ICAL will provide constraint  $\alpha_{\mu\tau} < 2.82 \times 10^{-51}$  at  $3\sigma$  C.L. with 500 kt-yr exposure and  $\theta_{23}(\text{true}) = 45^\circ$ .
- The charge identification capability of ICAL helps to improve the limit on  $\alpha_{\mu\tau}$ .

ICAL will play an important role in breaking the degeneracy between the octant of  $\theta_{23}$  and neutrino polarities due to LRI of  $L_\mu - L_\tau$  symmetry using separate data of  $\mu^-$  and  $\mu^+$ .