# Joint parameter estimation on overlapping gravitational wave signals from coalescing compact binaries with Einstein Telescope and Cosmic Explorer 

Tomasz Baka, Justin Janquart, Harsh Narola, Anuradha Samajdar, Tim Dietrich, Chris Van Den Broeck

## Signals we get with ET + CE

## Over a year:

- 104889 detected BBHs
- 44138 detected BNSs
- 100588 detected NSBHs

Overlaps within 0.1 s

- 32 BBH-BBH
- 46 BBH-BNS
- 78 BBH-NSBH
- 1 NSBH-NSBH
- 0 BNS-BNS
- 0 BNS-NSBH


## Size of the data

|  | Property | BBH (GW150914 like) | BNS (GW170817 like) |
| :--- | :--- | :--- | :--- |
|  | Chirp mass | $31 \mathrm{M} \cdot$ | $1.195 \mathrm{M} \cdot$ |
|  | Sampling frequency | 2048 Hz | 4096 Hz |
| Current detectors | Minimum frequency | 20 Hz | 20 Hz |
|  | Signal duration | 3 s | 185 s |
|  | Waveform size | 3072 | 378880 |

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|  | Minimum frequency | 5 Hz | 5 Hz |
|  | Signal duration | 35 s | 2 h 2 min |
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BBHs impractical to do with ET, while BNSs computationally impossible

## Relative binning

- Choose a reference waveform
- Express other waveforms as ratios to the reference waveform
- The ratios close to reference are well approximated by piecewise linear functions
- Divide the waveform to frequency bands and do computations only on the edges


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| ET + CE (relative binning) | Waveform size | 2479 | 14968832 |

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With Relative binning parameter estimation is as fast as for the shortest BBHs now

## Overlapping signals



Signal A

## Overlapping signals



Signal A + Signal B

## Overlapping signals



Signal A + Signal B = Overlapping signal

## How parameter estimation works?



## How joint parameter estimation works?

Double the parameter space so that it covers both signals


Modify likelihood to model both signals

Time-order the signals in post-processing

## BNS, zero noise




## BBH, zero noise



## BBH, noise



## BBH, noise



## Conclusions

- Relative binning generalizes to multiple signals without problem and approximates the likelihood accurately
- We can do accurate PE on overlapping signals modeling both signals at once
- We properly recover injected parameters and the posteriors have appropriate shape (apart from spin parameters)
- Ignoring one of the signals and hierarchical subtraction can often fail to recover injected parameters, even with no noise

