# Probing quark TMDs in the CGC: quark-gluon dijets in DIS

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#### TMD vs CGC: from gluons to quark

For a process with a hard  ${\bf P}$  and a not so hard  ${\bf k}$  transverse momenta:

- TMD factorization: leading power (twist 2) in the limit  $|{f k}| \ll |{f P}| \sim \sqrt{s}$
- ullet CGC result: leading power (eikonal) in the limit  $|{f k}|\sim |{f P}|\ll \sqrt{s}$

Consistency of both approaches shown in the double limit  $|\mathbf{k}|\ll |\mathbf{P}|\ll \sqrt{s}$  (Dominguez, Marquet, Xiao, Yuan, 2011), involving gluon TMDs

Only the gluon TMDs are relevant in this double limit because the target is described by a gluon background field  $\mathcal{A}^-(x)$  in the (eikonal) CGC

Quark background field of the target should be included as well beyond the eikonal limit.

⇒ Possibility to recover the quark TMDs from (non-eikonal) CGC?

#### Power counting for the quark background field $\Psi(z)$

ullet Under a boost of the target of parameter  $\gamma_t$  along the "-" direction, a current associated with the target should behave as

$$J^-(z) \propto \gamma_t$$
,  $J^j(z) \propto (\gamma_t)^0$ ,  $J^+(z) \propto (\gamma_t)^{-1}$ ,

• The quark background field of the target can be split as  $\Psi(z) = \Psi^{(-)}(z) + \Psi^{(+)}(z)$ , with

$$\Psi^{(-)}(z) \equiv \frac{\gamma^+ \gamma^-}{2} \Psi(z), \quad \Psi^{(+)}(z) \equiv \frac{\gamma^- \gamma^+}{2} \Psi(z).$$

Then, the components of the background quark current write

$$\begin{split} \overline{\Psi}(z)\,\gamma^-\,\Psi(z) &= \overline{\Psi^{(-)}}(z)\,\gamma^-\,\Psi^{(-)}(z),\\ \overline{\Psi}(z)\,\gamma^j\,\Psi(z) &= \overline{\Psi^{(-)}}(z)\,\gamma^j\,\Psi^{(+)}(z) + \overline{\Psi^{(+)}}(z)\,\gamma^j\,\Psi^{(-)}(z),\\ \overline{\Psi}(z)\,\gamma^+\,\Psi(z) &= \overline{\Psi^{(+)}}(z)\,\gamma^-\,\Psi^{(+)}(z)\,. \end{split}$$

Under a boost of the target, the projections  $\Psi^{(-)}(z)$  and  $\Psi^{(+)}(z)$  should thus scale as

$$\Psi^{(-)}(z) \propto (\gamma_t)^{\frac{1}{2}}, \quad \Psi^{(+)}(z) \propto (\gamma_t)^{-\frac{1}{2}},$$

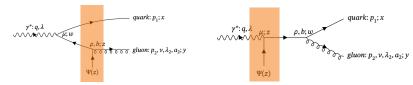
 $\Rightarrow$  Let us keep only the leading components  $\Psi^{(-)}(z)$  of  $\Psi(z)$ 

See also Kovchegov et al. (2016-2023), and Chirilli (2019).



# Contributions to $\gamma^* \to qg$ dijets from quark background

qg dijet production in DIS: a simple process sensitive to the quark background beyond eikonal CGC



$$\begin{split} S^{\text{bef}}_{\gamma \to q_1 g_2} &= \lim_{x^+,y^+ \to +\infty} \int_{\mathbf{x},\mathbf{y}} \int_{x^-,y^-} e^{ip_1 \cdot x} \, \bar{u}(1) \gamma^+ \, e^{ip_2 \cdot y} \epsilon_{\nu}^{\lambda_2}(p_2)^*(-2p_2^+) \\ &\times \int_{w,z} e^{-iq \cdot w} \epsilon_{\mu}^{\lambda}(q) \, G_F^{\nu\rho}(y,z)_{a_2b} S_F(x,w) (-iee_f) \gamma^\mu S_F(w,z) (-ig) \gamma_\rho t^b \Psi(z), \end{split}$$

$$\begin{split} S_{\gamma \to q_1 g_2}^{\mathrm{in}} &= \lim_{x^+, y^+ \to +\infty} \int_{\mathbf{x}, \mathbf{y}} \int_{x^-, y^-} e^{ip_1 \cdot x} \, \bar{u}(1) \gamma^+ \, e^{ip_2 \cdot y} \epsilon_{\nu}^{\lambda_2}(p_2)^* (-2p_2^+) \\ &\times \int_{w, z} e^{-iq \cdot z} \epsilon_{\mu}^{\lambda}(q) \, G_{F, 0}^{\nu \rho}(y, w)_{a_2 b} S_{F, 0}(x, w) (-ig) \gamma_{\rho} t^b S_F(w, z) (-iee_f) \gamma^{\mu} \Psi(z) \end{split}$$

#### Propagators from inside to outside a gluon background

Eikonal quark propagator from y (inside the target) to x (after the target):

$$S_F(x,y)\Big|_{\rm Eik.}^{\rm IA,q} = \int \frac{d^2{\bf p}}{(2\pi)^2} \frac{dp^+}{(2\pi)^2} \frac{\theta(p^+)}{2p^+} \, e^{-ix\cdot p} \, (\not p+m) \, \mathcal{U}_F(+\infty,y^+;{\bf y}) \, \left[1 - \frac{\gamma^+\gamma^i}{2p^+} \, i \, \frac{\overleftarrow{\mathcal{U}_F}}{\overleftarrow{\mathcal{U}_Y}^i} \right] \, e^{iy^-p^+} \, e^{-i{\bf y}\cdot {\bf p}} \, e^{-i{\bf y}\cdot$$



Eikonal quark propagator from y (inside the target) to x (before the target):

$$S_F(x,y)\Big|_{\rm Eik.}^{\rm IB,q} = \int \frac{d^2{\bf p}}{(2\pi)^2} \frac{dp^+}{(2\pi)} \frac{\theta(p^+)}{2p^+} \, e^{ix\cdot p} \, (\not\! p-m) \, (-1) \mathcal{U}_F^\dagger(y^+,-\infty;{\bf y}) \, \left[1 + \frac{\gamma^+\gamma^i}{2p^+} \, i \, \frac{\overleftarrow{\mathcal{D}_F^F}}{\overleftarrow{\mathcal{D}_F^{ij}}} \right] \, e^{-iy^-p^+} \, e^{i{\bf y}\cdot {\bf p}} \, e^{i{\bf$$

Eikonal gluon propagator from y (inside the target) to x (after the target):

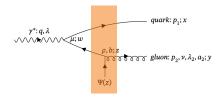
$$G_F^{\mu\nu}(x,y) \bigg|_{\mathrm{Eik.}}^{\mathrm{IA},g} = \int \frac{d^2\mathbf{p}}{(2\pi)^2} \frac{dp^+}{(2\pi)^2} \frac{dp^+}{2p^+} e^{-ix\cdot p} \left[ -g^{\mu j} + \frac{\mathbf{p}^j}{p^+} g^{\mu +} \right] \, \mathcal{U}_A(+\infty,y^+;\mathbf{y}) \left[ g^\nu{}_j + \frac{g^{\nu +}}{p^+} \left( \mathbf{p}^j + i \overleftarrow{\mathcal{D}_{\mathbf{y}^j}^A} \right) \right] e^{iy^-p^+} e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^{\mu j} + \frac{\mathbf{p}^j}{p^+} g^{\mu +} \right] \, \mathcal{U}_A(+\infty,y^+;\mathbf{y}) \left[ -g^\nu{}_j + \frac{g^{\nu +}}{p^+} \left( \mathbf{p}^j + i \overleftarrow{\mathcal{D}_{\mathbf{y}^j}^A} \right) \right] e^{iy^-p^+} e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^{\mu j} + \frac{\mathbf{p}^j}{p^+} g^{\mu +} \right] \, \mathcal{U}_A(+\infty,y^+;\mathbf{y}) \left[ -g^\nu{}_j + \frac{g^{\nu +}}{p^+} \left( \mathbf{p}^j + i \overleftarrow{\mathcal{D}_{\mathbf{y}^j}^A} \right) \right] e^{iy^-p^+} e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\nu{}_j}{p^+} g^{\mu +} \right] \, \mathcal{U}_A(+\infty,y^+;\mathbf{y}) \left[ -g^\nu{}_j + \frac{g^\nu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\nu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\nu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\nu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\nu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\nu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^{\mu +} g^\mu{}_j \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left[ -g^\mu{}_j + \frac{g^\mu{}_j}{p^+} g^\mu{}_j \right] e^{-i\mathbf{y}\cdot \mathbf{p}} \left$$







# Contribution with $\gamma^*$ splitting before the target



$$\begin{split} S_{\gamma_{T,L} \rightarrow q_{1}g_{2}}^{\text{bef}} &= iee_{f}g2\pi\delta(p_{1}^{+} + p_{2}^{+} - q^{+})\int_{\mathbf{v},\mathbf{z}} e^{-i\mathbf{v}\cdot\mathbf{p}_{1} - i\mathbf{z}\cdot\mathbf{p}_{2}} \int \frac{d^{2}\mathbf{K}}{(2\pi)^{2}} \frac{e^{i(\mathbf{v}-\mathbf{z})\cdot\mathbf{K}}}{\left[\mathbf{K}^{2} + m^{2} + \frac{p_{1}^{+}p_{2}^{+}}{(q^{+})^{2}}Q^{2}\right]} \\ &\times \bar{u}(1)\frac{\gamma^{+}\gamma^{-}}{2}\Gamma_{T,L}^{\text{bef}} \int_{z^{+}} U_{A}\left(+\infty, z^{+}; \mathbf{z}\right)_{a_{2}b} U_{F}(\mathbf{v})U_{F}^{\dagger}\left(z^{+}, -\infty; \mathbf{z}\right)t^{b}\Psi(z^{+}, \mathbf{z}) \end{split}$$

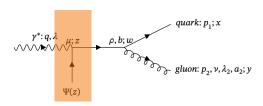
with

$$\Gamma_L^{\mathrm{bef}} = 2 \frac{p_1^+ p_2^+}{(q^+)^2} Q \varepsilon_{\lambda_2}^{j*} \gamma^j \qquad \qquad \Gamma_T^{\mathrm{bef}} = \varepsilon_\lambda^i \varepsilon_{\lambda_2}^{j*} \left\{ \mathbf{K}^l \left[ \left( \frac{p_1^+ - p_2^+}{q^+} \right) \delta^{il} - \frac{[\gamma^i, \gamma^l]}{2} \right] + m \gamma^i \right\} \gamma^j$$

Similar to the case of  $\gamma^* \to q\bar{q}$  dijet production in the the dipole picture/CGC at eikonal accuracy, but with a different color structure



# Contribution with $\gamma^*$ conversion inside the target



$$S_{\gamma_{T} \to q_{1}g_{2}}^{\mathrm{in}} = i \frac{ee_{f}g2\pi\delta(p_{1}^{+} + p_{2}^{+} - q^{+})}{\left[\left(\mathbf{p}_{1} - \frac{p_{1}^{+}}{p_{2}^{+}}\mathbf{p}_{2}\right)^{2} + m^{2}\right]} \int_{\mathbf{z}} e^{-i\mathbf{z}\cdot(\mathbf{p}_{1} + \mathbf{p}_{2})} \bar{u}(1) \frac{\gamma^{+}\gamma^{-}}{2} \frac{\Gamma_{T}^{\mathrm{in}}}{1} \int_{z^{+}} t^{a_{2}} U_{F}\left(+\infty, z^{+}; \mathbf{z}\right) \Psi(z^{+}, \mathbf{z})$$

with

$$\begin{split} & \mathbf{\Gamma}_{T}^{\text{in}} = \varepsilon_{\lambda_{2}}^{l*} \varepsilon_{\lambda}^{j} \left\{ \left[ \mathbf{p}_{1}^{i} - \frac{p_{1}^{+}}{p_{2}^{+}} \mathbf{p}_{2}^{i} \right] \left[ - \left( \frac{2p_{1}^{+} + p_{2}^{+}}{p_{2}^{+}} \right) \delta^{il} + \frac{\left[ \gamma^{i}, \gamma^{l} \right]}{2} \right] + m \gamma^{l} \right\} \gamma^{j} \end{split}$$

Note:  $S_{\gamma_L \to q_1 g_2}^{\rm in} = 0$  at NEik in Light-cone gauge, because  $\oint_L (q) \Psi^{(-)}(z) = rac{Q}{q^+} \gamma^+ \Psi^{(-)}(z) = 0$ .



#### Back-to-back jets: inside diagram

Back-to-back limit of dijets are conveniently expressed in terms of:

(dijet momentum imbalance) 
$$\mathbf{k}=\mathbf{p}_1+\mathbf{p}_2$$
 and (relative momentum)  $\mathbf{P}=(1-z)\mathbf{p}_1-z\mathbf{p}_2$  
$$z=p_1^+/(p_1^++p_2^+) \text{ and } (1-z)=p_2^+/(p_1^++p_2^+)$$

S-matrix for in contribution in the back-to-back limit: upon renaming  $z \to b$  (No limit required!!)

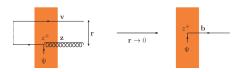
$$S_{\gamma_T \to q_1 g_2}^{\text{in}} = i \frac{ee_f g}{[\mathbf{P}^2 + (1-z)^2 m^2]} (1-z)^2 \bar{u}(1) \frac{\gamma^+ \gamma^-}{2} \Gamma_T^{\text{in}} \int_{\mathbf{b}} e^{-i\mathbf{b} \cdot \mathbf{k}} \int_{z^+} t^{a_2} U_F \left( +\infty, z^+; \mathbf{b} \right) \Psi(z^+, \mathbf{b})$$

#### Back-to-back jets: *before* diagram

S-matrix for *bef* contribution in the back-to-back limit:

- define  $\mathbf{b} = z\mathbf{v} + (1-z)\mathbf{z}$ .  $\mathbf{r} = \mathbf{z} \mathbf{v}$
- $\bullet \text{ phase: } e^{-i\mathbf{v}\cdot\mathbf{p}_1-i\mathbf{z}\cdot\mathbf{p}_2+i(\mathbf{v}-\mathbf{z})\cdot\mathbf{K}} \to e^{-i\mathbf{k}\cdot\mathbf{b}+i\mathbf{r}\cdot(\mathbf{P}-\mathbf{K})}$
- back-to-back limit:  $\mathbf{P}^2 \gg \mathbf{k}^2 \Rightarrow \mathbf{r}^2 \ll \mathbf{b}^2$  (because of the phase factor), the color structure simplifies:

$$\begin{split} U_A \left( + \infty, z^+; \mathbf{z} \right)_{a_2b} U_F (\mathbf{v}) U_F^\dagger \left( z^+, - \infty; \mathbf{z} \right) t^b \Psi (z^+, \mathbf{z}) & \rightarrow U_A \left( + \infty, z^+; \mathbf{b} \right)_{a_2b} U_F (\mathbf{b}) U_F^\dagger \left( z^+, - \infty; \mathbf{b} \right) t^b \Psi (z^+, \mathbf{b}) \\ &= t^{a_2} U_F \left( + \infty, z^+; \mathbf{b} \right) \Psi (z^+, \mathbf{b}) \end{split}$$



$$S_{\gamma_{T,L} \to q_{1}g_{2}}^{\text{bef}} \simeq i \frac{ee_{f}g \, 2\pi \delta(p_{1}^{+} + p_{2}^{+} - q^{+})}{\left[\mathbf{P}^{2} + \bar{Q}^{2}\right]} \, \bar{u}(1) \frac{\gamma^{+} \gamma^{-}}{2} \Gamma_{T,L}^{\text{bef}} \int_{\mathbf{b}} e^{-i\mathbf{b}\cdot\mathbf{k}} \int_{z^{+}} t^{a_{2}} U_{F}\left(+\infty, z^{+}; \mathbf{b}\right) \Psi(z^{+}, \mathbf{b})$$

#### Back-to-back qg dijet cross sections

In the back-to-back limit, the photon-target dijet cross section reads

$$(2\pi)^{6}(2p_{1}^{+})(2p_{2}^{+})\frac{d\sigma^{\gamma_{T,L}\to q_{1}g_{2}}}{dp_{1}^{+}d^{2}\mathbf{p}_{1}dp_{2}^{+}d^{2}\mathbf{p}_{2}}\bigg|_{\text{corr.lim.}} = 2\pi\delta(p_{1}^{+}+p_{2}^{+}-q^{+})(4\pi)^{2}\alpha_{\text{em}}\alpha_{s}C_{F}e_{f}^{2}\mathcal{H}_{T,L}(\mathbf{P},z,Q)\mathcal{T}(\mathbf{k})$$

with the hard factors for the longitudinal and the transverse photon polarizations

$$\mathcal{H}_L = \frac{4Q^2z^3(1-z)^2}{[{\bf P}^2 + \bar{Q}^2]^2} \qquad \qquad \bar{Q}^2 \equiv m^2 + z(1-z)Q^2$$

$$\mathcal{H}_T = z \left\{ \frac{(1+z^2)\mathbf{P}^2 + (1-z)^4 m^2}{[\mathbf{P}^2 + (1-z)^2 m^2]^2} + \frac{[z^2 + (1-z)^2]\mathbf{P}^2 + m^2}{[\mathbf{P}^2 + \bar{Q}^2]^2} - \frac{2z^2\mathbf{P}^2}{[\mathbf{P}^2 + \bar{Q}^2][\mathbf{P}^2 + (1-z)^2 m^2]} \right\}$$

and the target averaged color operator

$$\mathcal{T}(\mathbf{k}) = \int_{\mathbf{b}, \mathbf{b}'} e^{-i\mathbf{k}\cdot(\mathbf{b}-\mathbf{b}')} \int_{z^+, z'^+} \left\langle \bar{\Psi}(z'^+, \mathbf{b}')\gamma^- U_F^{\dagger}(+\infty, z'^+; \mathbf{b}') U_F(+\infty, z^+; \mathbf{b}) \Psi(z^+, \mathbf{b}) \right\rangle$$

with a generalized CGC target average  $\langle \dots \rangle$  over both the quark and gluon background fields.

Not yet known how to explicitly perform this target average!



#### Recovering the unpolarized quark TMD

$$\mathcal{T}(\mathbf{k}) = \int_{\mathbf{b},\mathbf{b}'} e^{-i\mathbf{k}\cdot(\mathbf{b}-\mathbf{b}')} \int_{z^+,z'^+} \left\langle \bar{\Psi}(z'^+,\mathbf{b}')\gamma^- U_F^{\dagger}(+\infty,z'^+;\mathbf{b}') U_F(+\infty,z^+;\mathbf{b}) \Psi(z^+,\mathbf{b}) \right\rangle$$

Can be related to the unpolarized quark TMD:

$$f_1^q(x,\mathbf{k}) = \frac{1}{(2\pi)^3} \int_{\mathbf{b}} e^{i\mathbf{k}\cdot\mathbf{b}} \int_{z^+} e^{-iz^+xP^-_{tar}} \langle P_{tar}|\bar{\Psi}(z^+,\mathbf{b}) \frac{\gamma^-}{2} U_F^\dagger(+\infty,z^+;\mathbf{b}) U_F(+\infty,0;\mathbf{0}) \Psi(0,\mathbf{0}) | P_{tar} \rangle$$



Indeed, the CGC-like target average  $\langle \cdots \rangle$  is an effective model for the quantum expectation value in the target state  $\langle P_{tar}|\cdots|P_{tar}\rangle$ , but with a normalization  $\langle 1\rangle=1$ .

⇒ Both expectation values can be related as

$$\langle \mathcal{O} \rangle = \lim_{P'_{tar} \rightarrow P_{tar}} \frac{\langle P'_{tar} | \hat{\mathcal{O}} | P_{tar} \rangle}{\langle P'_{tar} | P_{tar} \rangle} = \lim_{P'_{tar} \rightarrow P_{tar}} \frac{\langle P'_{tar} | \hat{\mathcal{O}} | P_{tar} \rangle}{2P_{tar}^{-} (2\pi)^{3} \, \delta(P'_{tar} - P_{tar}^{-}) \, \delta^{(2)}(\mathbf{P}'_{tar} - \mathbf{P}_{tar})}$$

With this relation, and after performing translations of the whole operator in  $\mathcal{T}(\mathbf{k})$  in the + and transverse directions, one finds

$$\mathcal{T}(\mathbf{k}) = \frac{(2\pi)^3}{P_{tar}^-} f_1^q(x=0, \mathbf{k})$$

#### Factorized cross section with the quark TMD

Alternatively, in the correlation limit we can write the cross section in terms of  ${f k},\,z$  and the dijet mass  $M_{jj}$ 

$$M_{jj}^2 \equiv (p_1 + p_2)^2 = \frac{\mathbf{P}^2}{z(1-z)} + \frac{m^2}{z}$$

The cross section in the back-to-back limit in terms of the dijet mass:

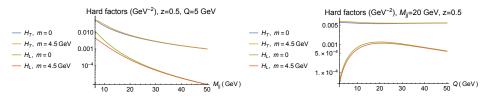
$$\left. \frac{d\sigma^{\gamma_{T,L} \to q_1 g_2}}{dz \, dM_{jj}^2 \, d^2 \mathbf{k}} \right|_{\text{corr.lim.}} = (2\pi) \, \frac{\alpha_{\text{em}} \, \alpha_s \, C_F \, e_f^2}{W^2} \, \widetilde{\mathcal{H}}_{T,L}(M_{jj},z,Q) f_1^q(x=0,\mathbf{k})$$

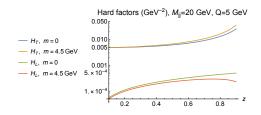
with the  $\gamma^*$ -target center of mass energy  $W \simeq \sqrt{2q^+\,P_{tar}^-}$  and the new hard factors

$$\widetilde{\mathcal{H}}_L(M_{jj}, z, Q) = \frac{4Q^2 z (1 - z)^2}{\left[ (1 - z)(M_{jj}^2 + Q^2) + m^2 \right]^2}$$

$$\begin{split} \widetilde{\mathcal{H}}_T(M_{jj},z,Q) &= \frac{(1+z^2)}{(1-z)} \frac{1}{\left[M_{jj}^2 - m^2\right]} + \frac{(1-2z)}{\left[(1-z)(M_{jj}^2 + Q^2) + m^2\right]} + \frac{(1-z)\left[2m^2 - \left(z^2 + (1-z)^2\right)Q^2\right]}{\left[(1-z)(M_{jj}^2 + Q^2) + m^2\right]^2} \\ &- \frac{2m^2}{\left[M_{jj}^2 - m^2\right]^2} + \frac{2z(1-z)m^2}{\left[M_{jj}^2 - m^2\right]\left[(1-z)(M_{jj}^2 + Q^2) + m^2\right]} \end{split}$$

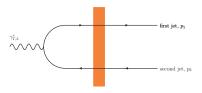
#### Behavior of the hard factors





# Background from eikonal $q\bar{q}$ dijet

First background process to qg dijet production: (Eikonal)  $q\bar{q}$  dijet production in DIS



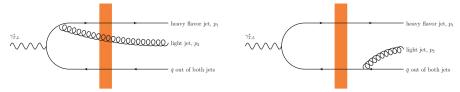
Distinguishing these two processes depends on our ability to distinguish quark and gluon jets

- Very challenging in general, for light quarks
- Heavy quark jets can be distinguished from light quark or gluon jets with heavy flavor tagging techniques
- $\Rightarrow$  Focus on the heavy quark case to be able to separate qg dijets from  $qar{q}$  dijets

# Background from eikonal $q \bar{q} g$ production

Second background process to qg dijet production:

(Eikonal)  $q\bar{q}g$  production in DIS, reconstructed as a qg dijet, and  $\bar{q}$  outside of both jets



Main difference with our qg process:

Emitted  $\bar{q}$  will take away some + momentum and some transverse momentum

- $\Rightarrow$  Background can be suppressed by imposing cuts on such momentum leaks :
  - $\textbf{1} \ \text{Impose} \ (q^+ p_1^+ p_2^+) \ll q^+$
  - 2 Impose  ${\bf k}^2\ll {\bf P}^2=(1-z)\left[z\,M_{jj}^2-m^2
    ight]$  (back-to-back limit)



#### Summary

- The quark background field of the target is relevant in CGC beyond the eikonal approximation
- ullet We have calculated the qg dijet production in DIS in NEik CGC, driven by interaction with this quark background field
- The TMD factorization of the cross section is recovered in the back-to-back limit, with the quark TMD obtained from a (non-eikonal) CGC calculation for the first time
- ullet qg dijet in DIS: new way to probe the unpolarized quark TMD, in particular at the EIC
- This process can be distinguished from background processes at least in the heavy quark case, by required heavy flavor tagging on a single jet of the dijet, and using appropriate kinematical cuts.