



WG6 Future experiments

# Top and EW studies at the LHeC and FCC-he

**Sookhyun Lee** (U Michigan/U Tennessee)

on behalf of the LHeC/FCC-eh study group

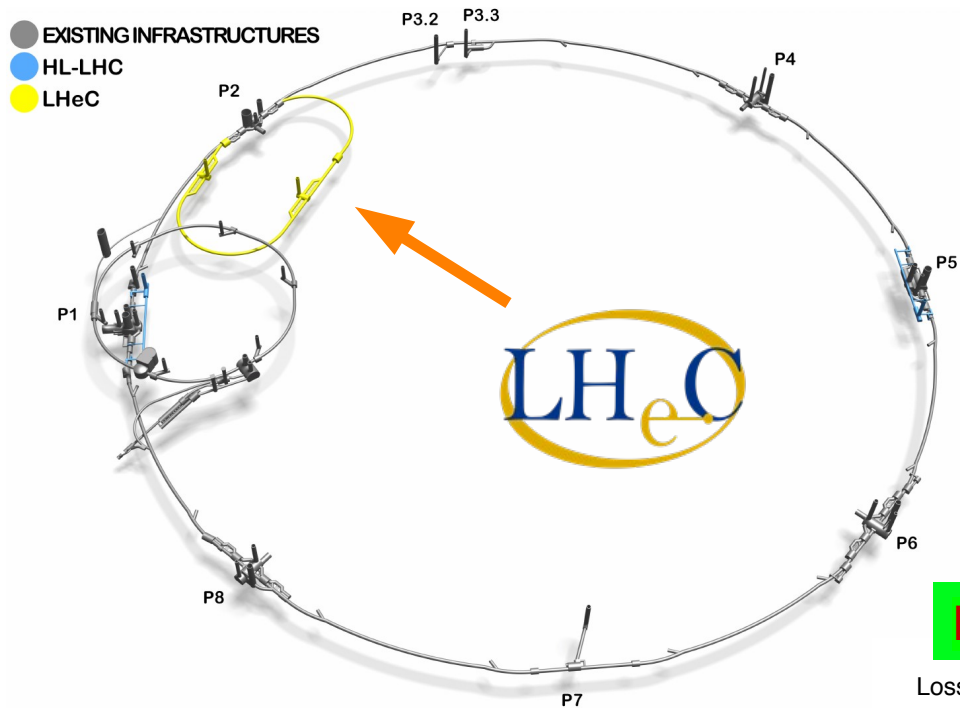
*XXX International Workshop on Deep-inelastic Scattering and Related Subjects*

March 30, 2023

- **LHeC CDR :**  
J. Phys. G 39 (2012) 075001, 1206.2913  
J. Phys. G 48 (2021) 11, 110501, 2007.14491
- **FCC CDR:**  
EPJ. C 79, no. 6, 474 (2019) - Physics  
EPJ. ST 228, no. 4, 755 (2019) - FCC-hh/eh



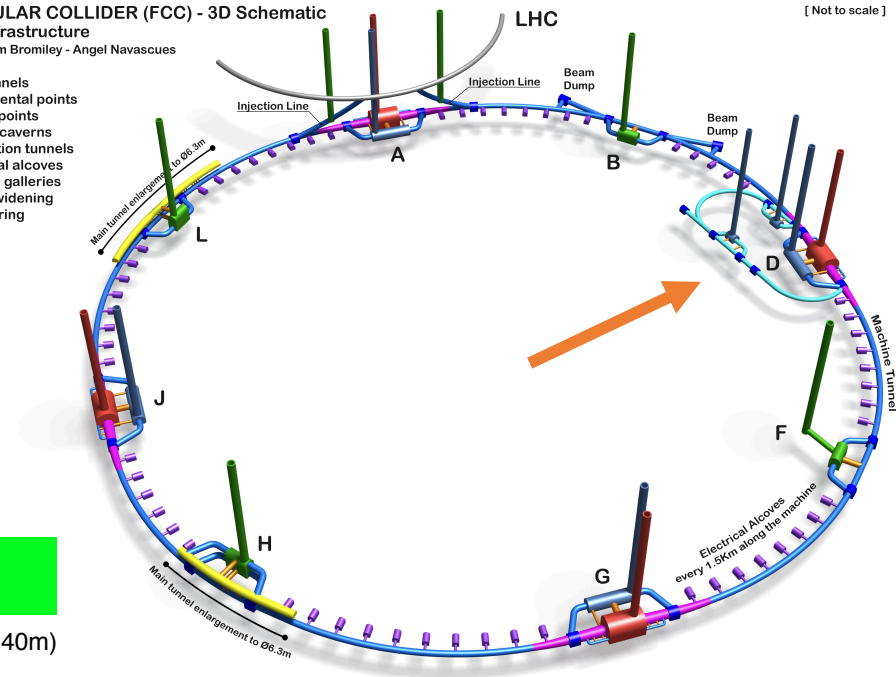
# LHeC and FCC-eh (Linac-Ring Collider )



FUTURE CIRCULAR COLLIDER (FCC) - 3D Schematic  
Underground Infrastructure  
John Osborne - William Bromiley - Angel Navascues

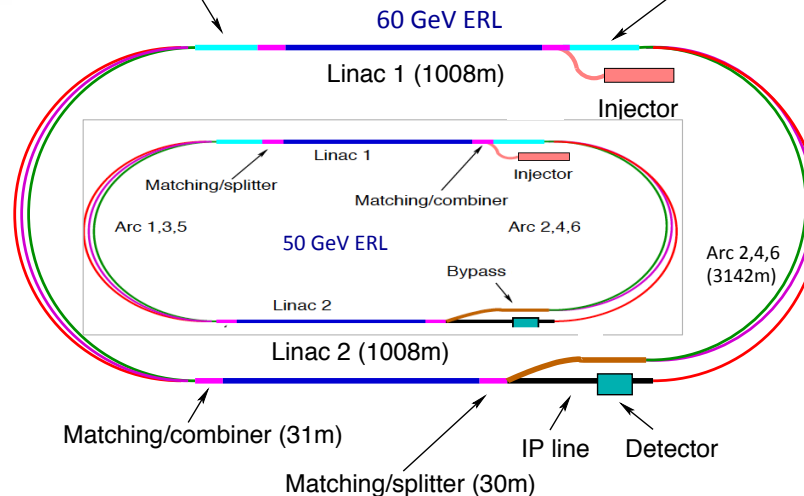
Legend for FCC-eh ring:

- FCC Tunnels
- Experimental points
- Access points
- Service caverns
- Connection tunnels
- Electrical alcoves
- Klystron galleries
- Tunnel widening
- FCC-eh ring
- LHC



## Energy Recovery Linac (ERL)

Loss compensation 2 (90m) Loss compensation 1 (140m)



## LHeC

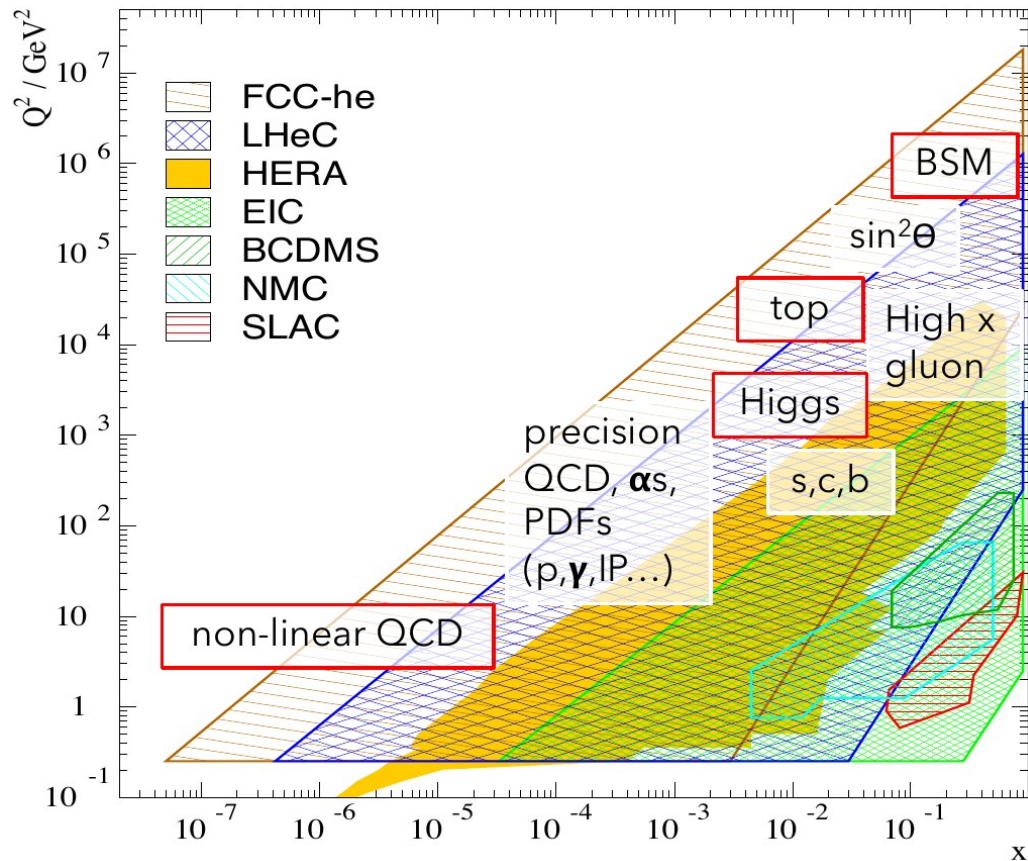
- Operated **synchronously** with **HL-LHC**  
 $\sqrt{s} = 1.2 \text{ TeV}$ ,  $E_e (= 50 \text{ GeV}) \times E_p (= 7 \text{ TeV})$
- Time scale: 2035+
- Luminosity:  $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

Sookhyun Lee, DIS 2023

## FCC-eh

- Operated **synchronously** with **FCC-hh**  
 $\sqrt{s} = 3.5 \text{ TeV}$ ,  $E_e (= 60 \text{ GeV}) \times E_p (= 50 \text{ TeV})$
- Time scale: 2050+

# LHeC/FCC-eh kinematics



$L_{int} = 1-3 \text{ ab}^{-1}$  (2000×HERA!)

- Clean and high resolution QCD factory with ep/eA at energy frontier
- Rich physics at all scales, precision and discovery
- Strengthen LHC/FCC program while keeping energy cost low with ERL technology
- **Top** and **EW** and **Higgs** physics:  
*require* high  $Q^2$  and high luminosity

## See talks:

IR and Detectors (Paul Newman, Tues )

Overview, and Higgs and BSM physics (Nestor Armesto, Wed 11.50)

Proton structure/precision QCD (Francesco Giuli, Thurs 17.10)

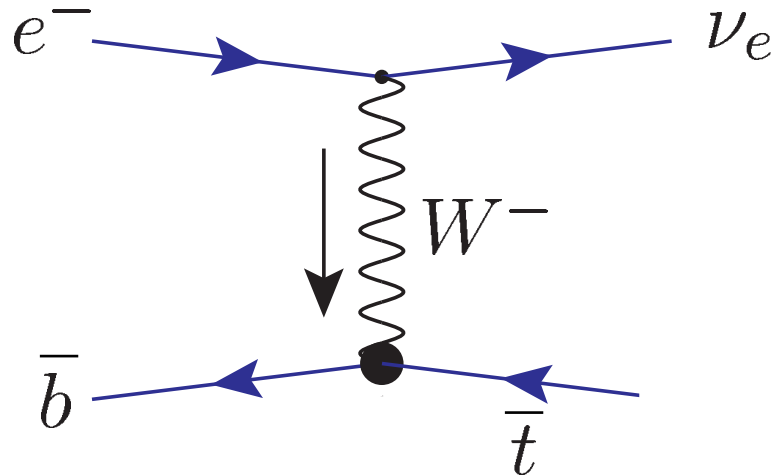
Diffraction/forward physics (Anna Stasto, Thurs 17.30)

High energy QCD and eA (Claire Gwenlan, Thurs 17.50)

# Top production in ep

## Charged Current (CC)

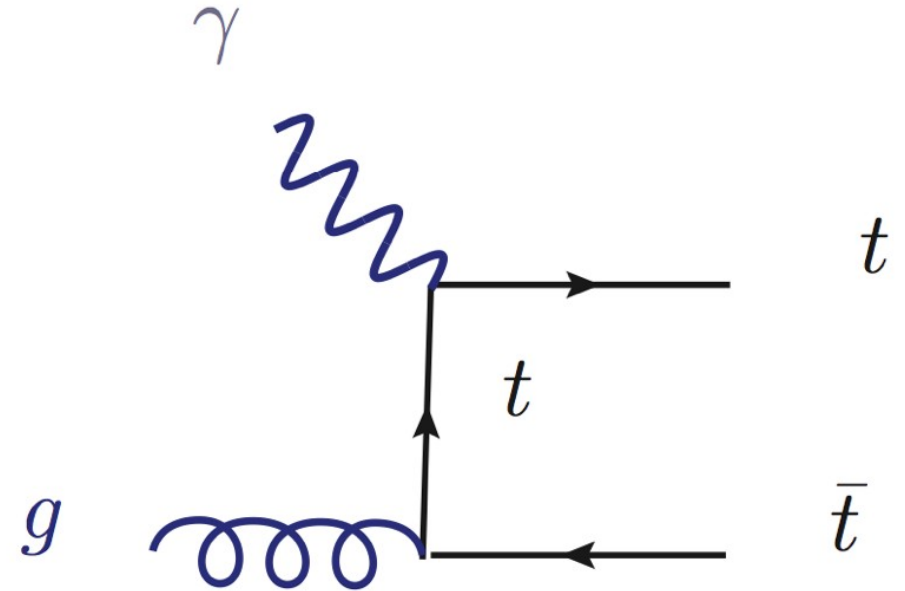
DIS *single top-quark* production



- $\sigma = 1.89\text{pb}$  (LHeC)
- $\sigma = 15.3\text{pb}$  (FCC-eh) with  $E_e=60$  GeV
- CKM matrix ( $V_{tx}$ );  $Wtb$  couplings,  $V_{td}$ ,  $V_{ts}$

## Neutral Current (NC)

*top-quark pair* photoproduction



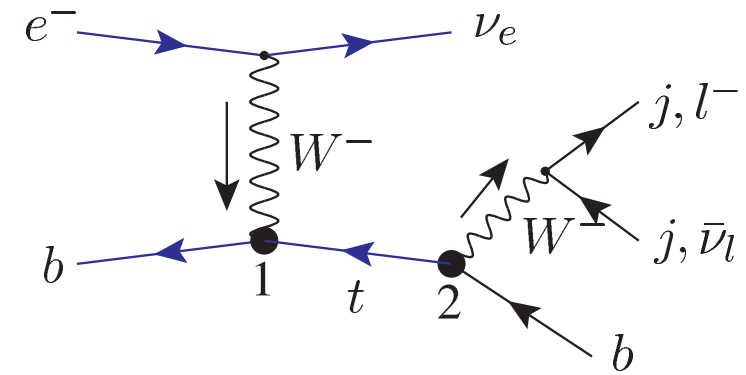
- $\sigma = 0.05\text{pb}$  (LHeC)
- $\sigma = 1.14\text{pb}$  (FCC-eh) with  $E_e=60$  GeV
- Top charge and anomalous form factors



# Wtb couplings

$$\mathcal{L}_{Wtb} = \frac{g}{\sqrt{2}} \left[ W_\mu \bar{t} \gamma^\mu (V_{tb} \overset{\text{orange}}{f_1^L} P_L + \overset{\text{orange}}{f_1^R} P_R) b \right. \\ \left. - \frac{1}{2m_W} W_{\mu\nu} \bar{t} \sigma^{\mu\nu} (\overset{\text{green}}{f_2^L} P_L + \overset{\text{green}}{f_2^R} P_R) b \right] + h.c.$$

**SM :**  $V_{tb} f_1^L \cong 1,$   
 $f_1^R = f_2^L = f_2^R = 0$

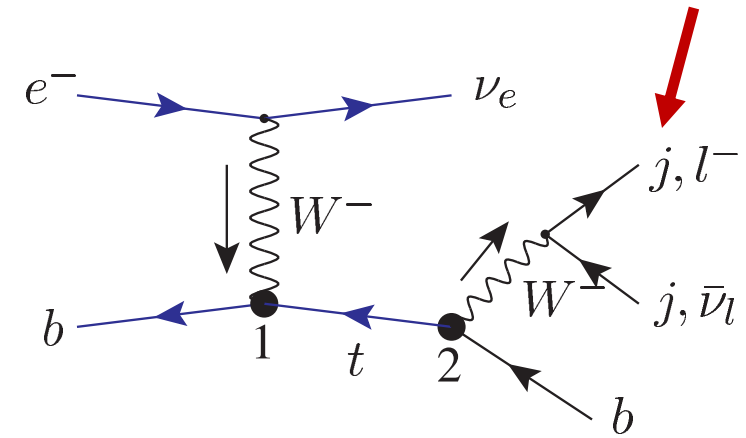


- Wtb couplings via single top production at LHeC
  - Direct access to anomalous couplings
  - Clean measurements and suppressed background from strong interaction initiated processes

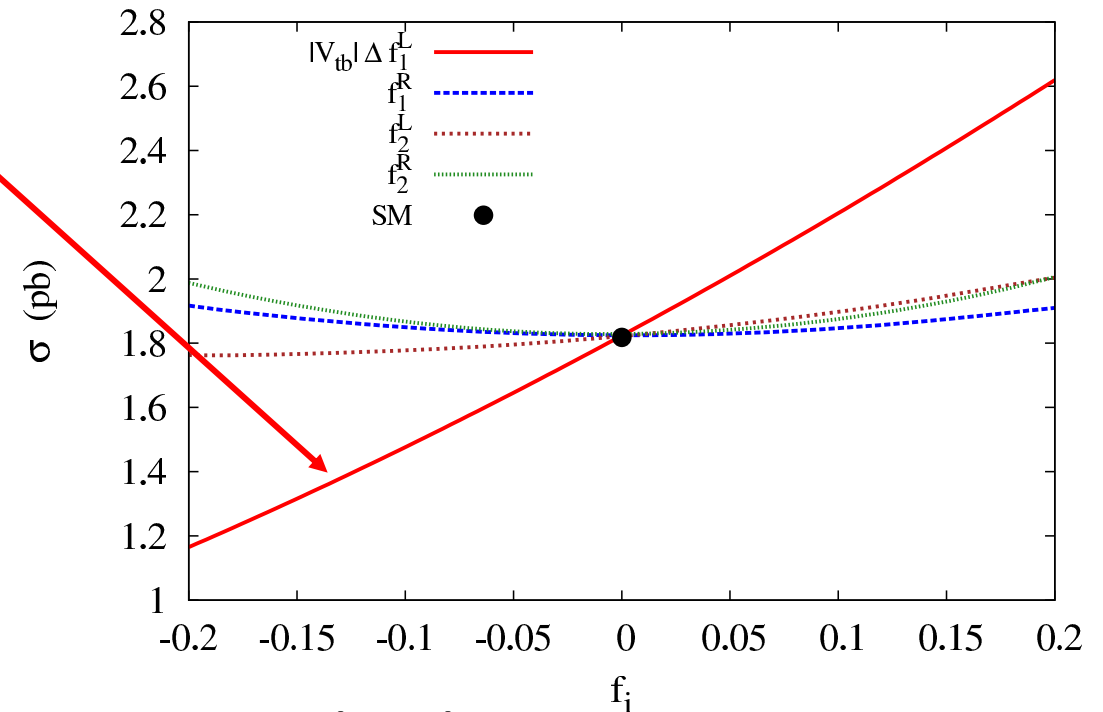
$$V_{tb} f_1^L$$

$$\mathcal{L}_{Wtb} = \frac{g}{\sqrt{2}} \left[ W_\mu \bar{t} \gamma^\mu (V_{tb} f_1^L P_L + f_1^R P_R) b - \frac{1}{2m_W} W_{\mu\nu} \bar{t} \sigma^{\mu\nu} (f_2^L P_L + f_2^R P_R) b \right] + h.c.$$

$$f_1^L \equiv 1 + \Delta f_1^L$$



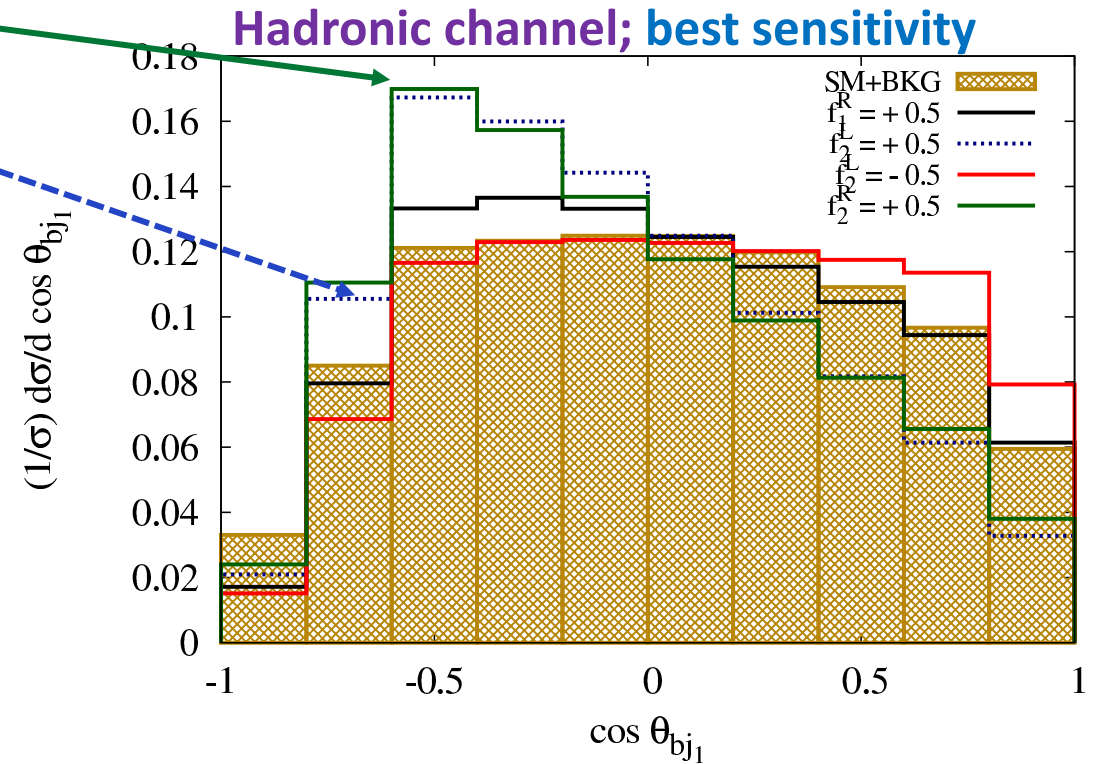
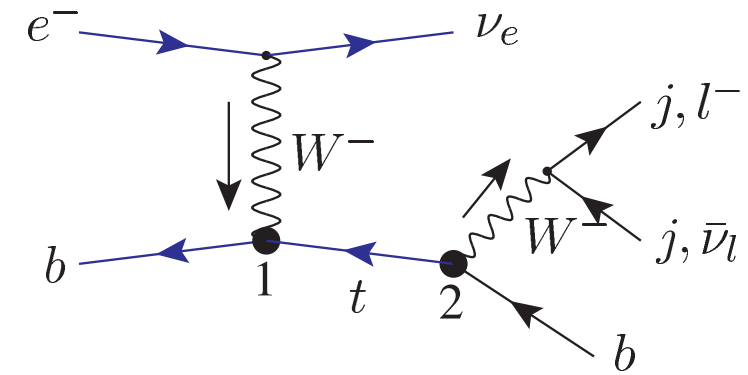
- Wtb couplings via single top production at LHeC
  - Hadronic and leptonic decays studied using DELPHE and analysis cuts with  $E_e = 60$  GeV



EPJC 75 (2015) 577,  
Dutta, Goyal, Kumar, Mellado,

# $f_1^R, f_2^L$ and $f_2^R$

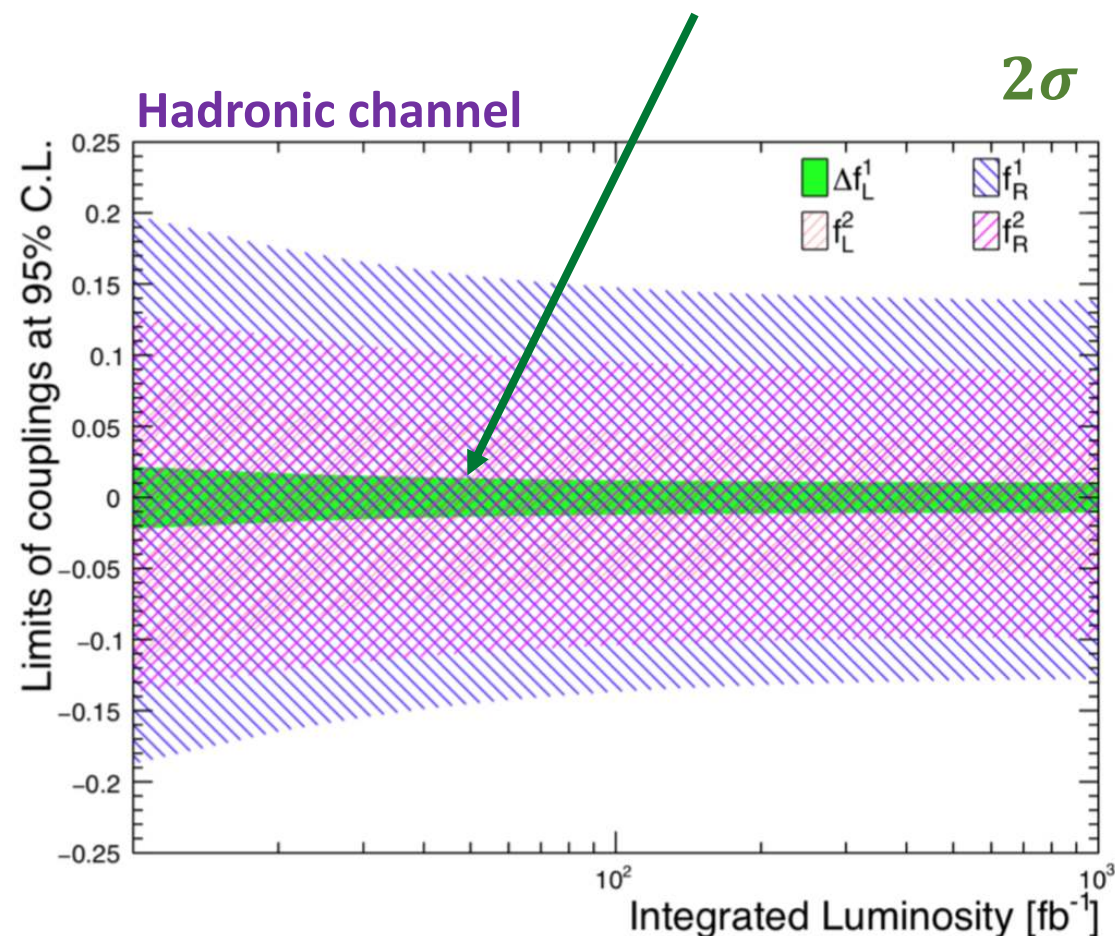
$$\mathcal{L}_{Wtb} = \frac{g}{\sqrt{2}} \left[ W_\mu \bar{t} \gamma^\mu (V_{tb} f_1^L P_L + f_1^R P_R) b \right. \\ \left. - \frac{1}{2 m_W} W_{\mu\nu} \bar{t} \sigma^{\mu\nu} (f_2^L P_L + f_2^R P_R) b \right] + h.c.$$



- Wtb couplings via single top production at LHeC
  - Hadronic and leptonic decays studied using DELPHE and analysis cuts with  $E_e = 60$  GeV

-  $j_1$ : hardest  $p_T$  jet  
 - Distributions normalized to unity

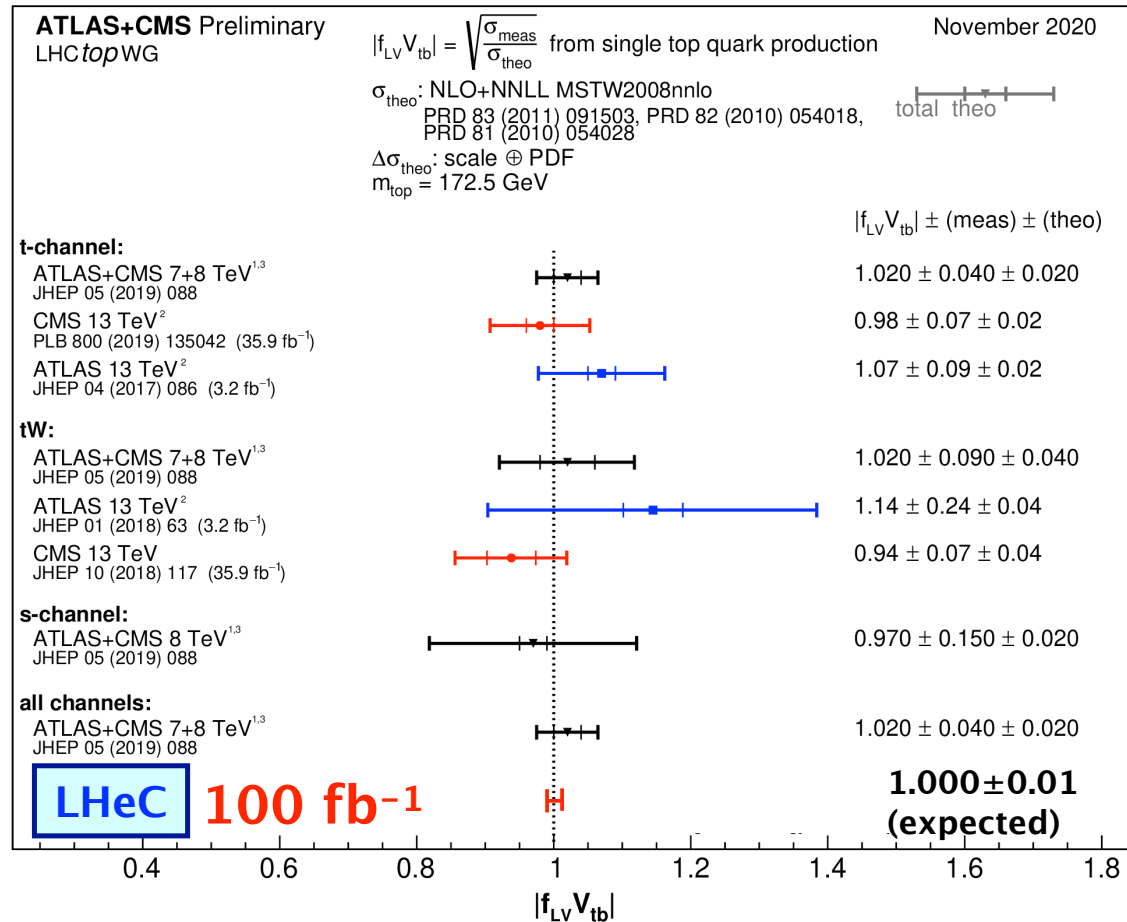
# Anomalous Wtb Couplings



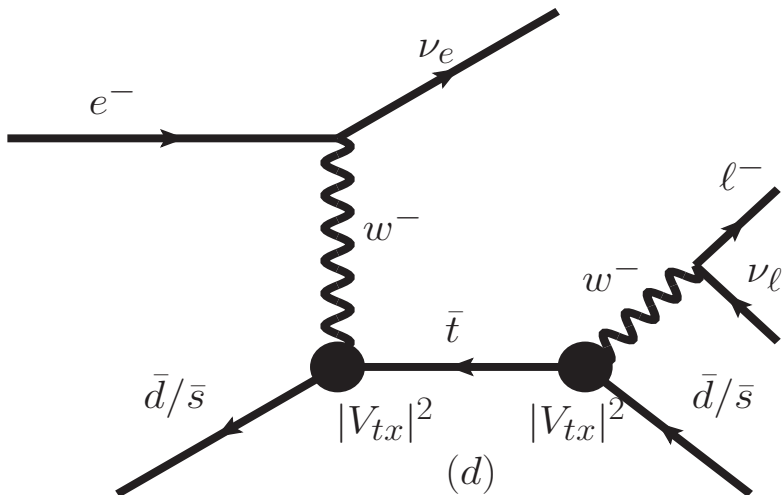
EPJC 75 (2015) 577, arXiv:1307.1688,  
Dutta, Goyal, Kumar, Mellado,

$$V_{tb}f_1^L$$

- <sup>1</sup> including top-quark mass uncertainty  
<sup>2</sup>  $\sigma_{\text{theo}}$ : NLO PDF4LHC11  
<sup>3</sup> NPPS205 (2010) 10, CPC191 (2015) 74  
 including beam energy uncertainty



Even smaller than 1% with 1 ab<sup>-1</sup>!

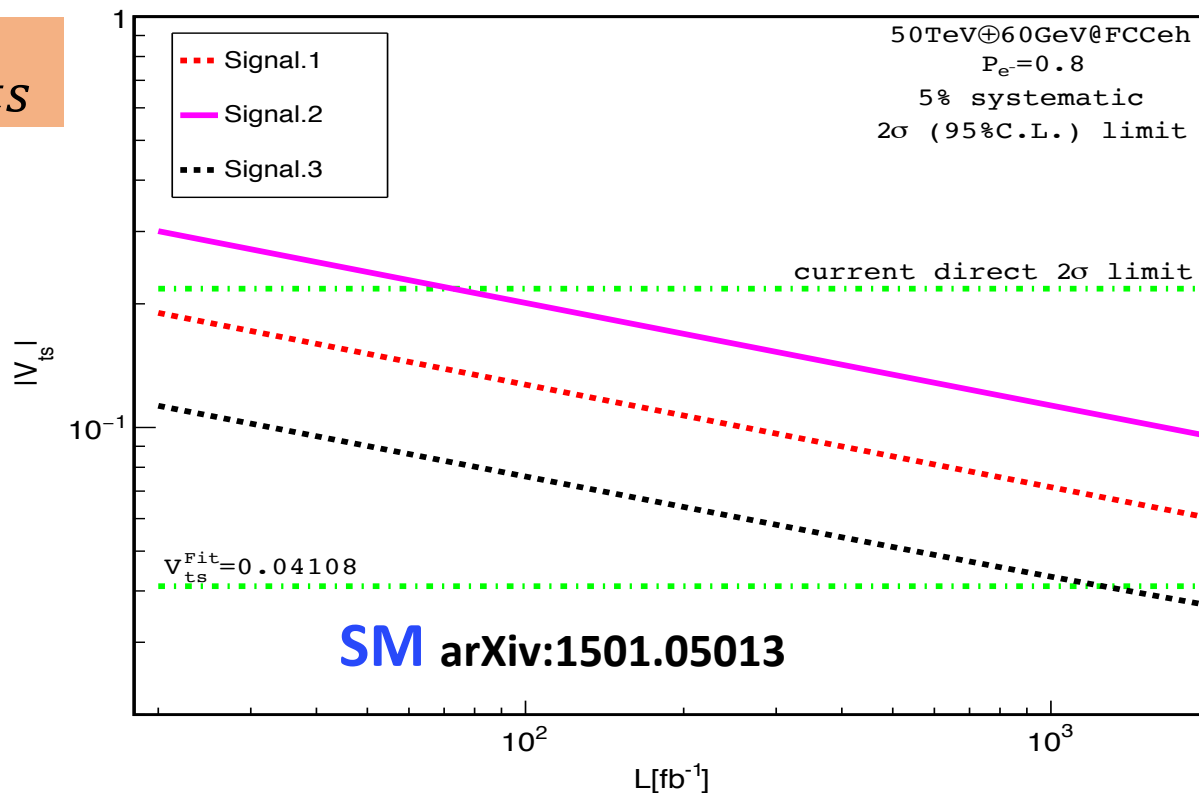


# $V_{td}$ and $V_{ts}$

- Direct measurements of  $V_{td}$  and  $V_{ts}$
- Top-pair production background suppressed
- Probing SM predictions directly for the first time

PoS DIS 2018 (2018) 167, H. Sun

$V_{ts}$



LHC arXiv:1709.07887

← FCC-eh  $|V_{ts}| < 0.037$   
Leptonic channel



# Top-quark form factors

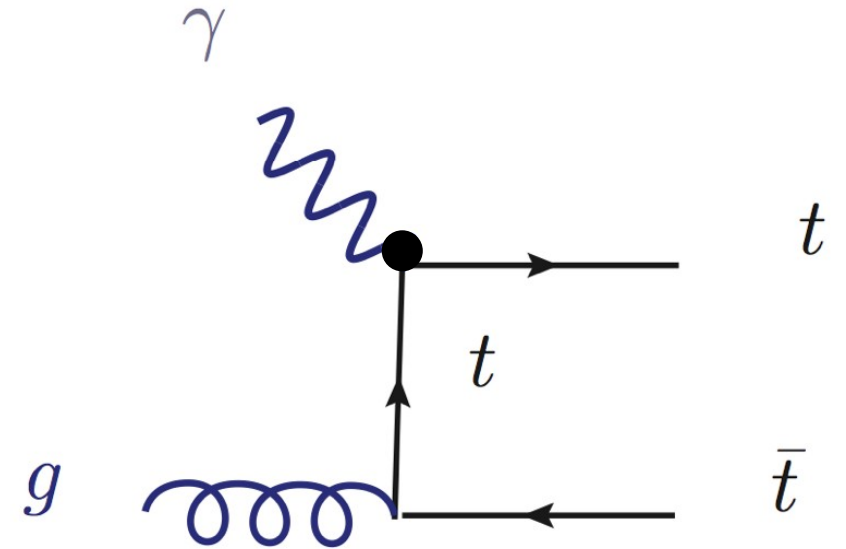
$\kappa$  : magnetic dipole moment  
(MDM)

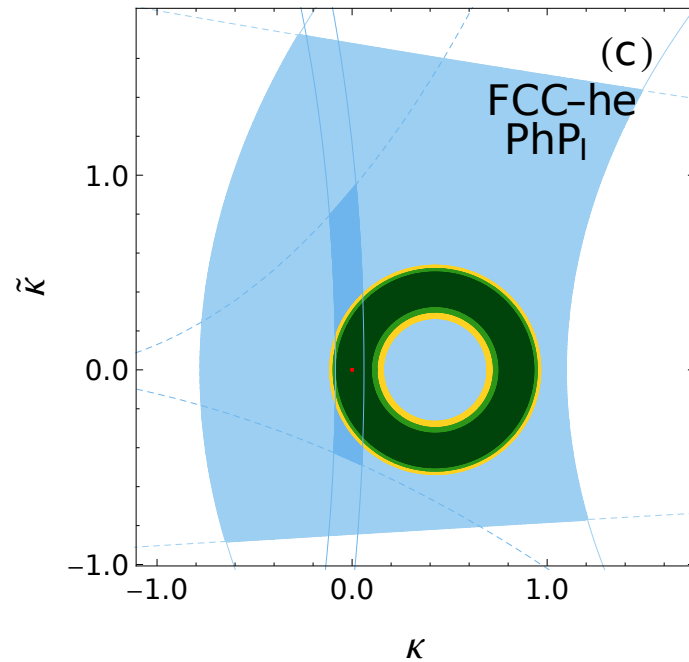
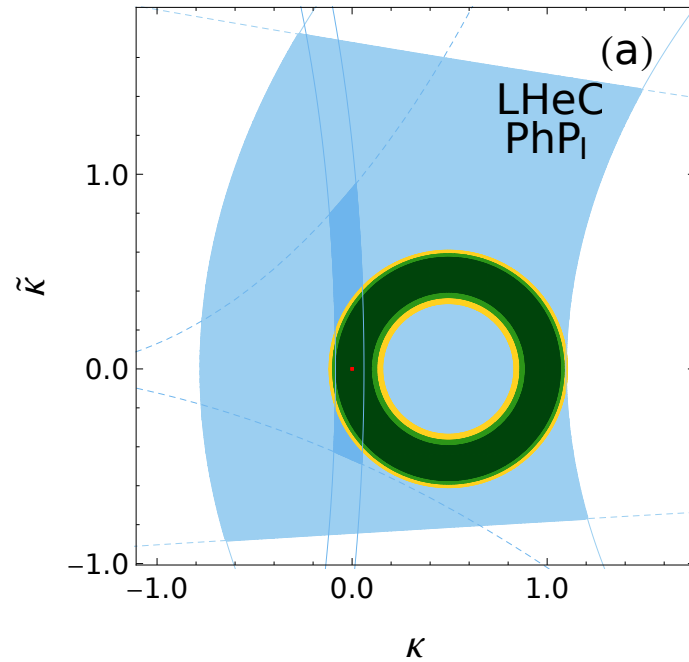
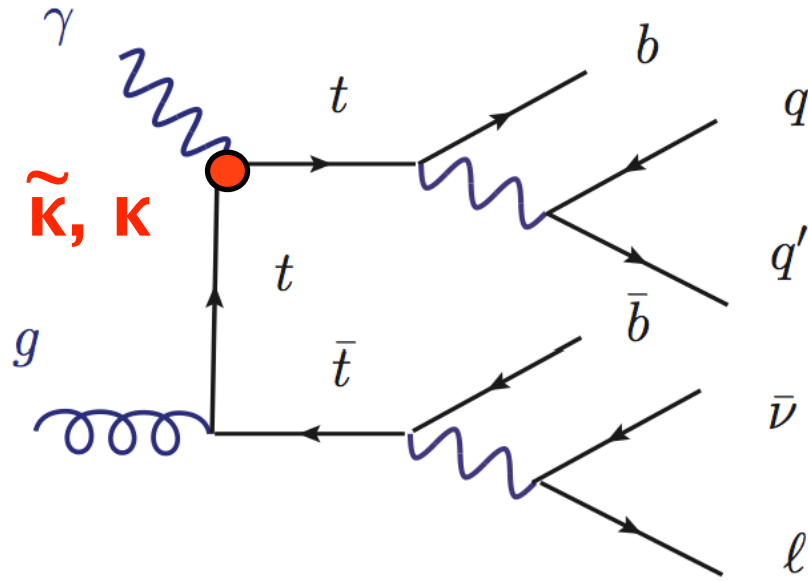
$\tilde{\kappa}$  : electric dipole moment  
(EDM)

$$\mathcal{L}_{t\bar{t}\gamma} = e\bar{t} \left( Q_t \gamma^\mu A_\mu + \frac{1}{4m_t} \sigma^{\mu\nu} F_{\mu\nu} (\kappa + i\tilde{\kappa}\gamma_5) \right) t$$

$eQ_t$  : electric charge

- Photoproduction of top-quark pairs
- Clean measurements thanks to absence of final state radiation





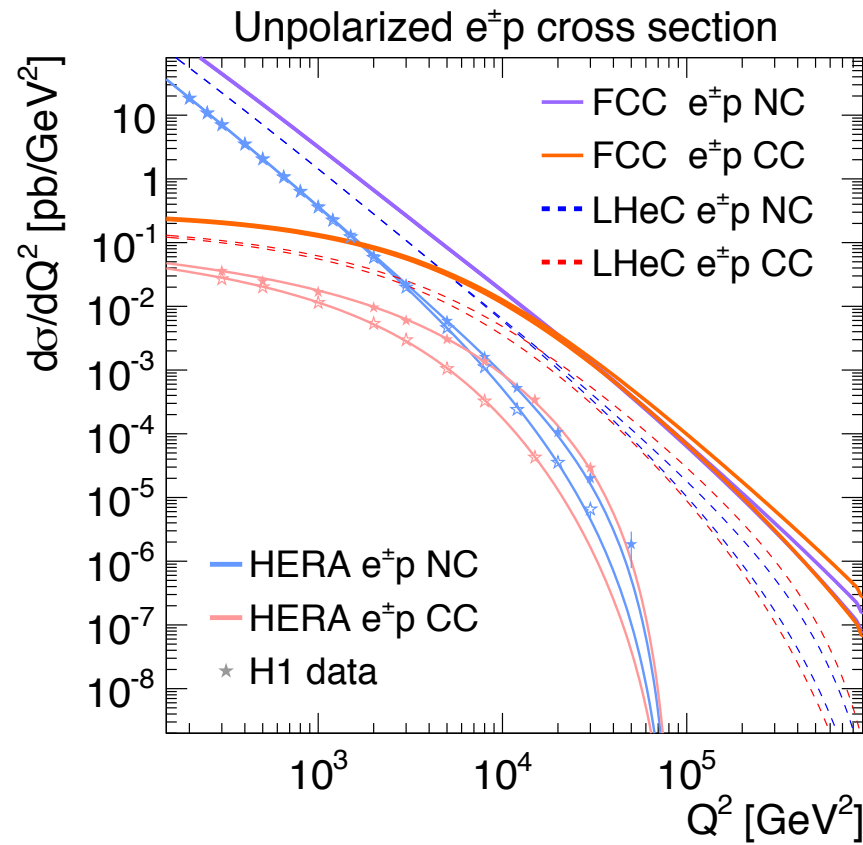
Bouzas, Larios  
PRD 88 (2013) 094007  
PRD 105 (2022) 115002

(blue) Branching ratio  
and CP asymmetries  
of  $B \rightarrow X_s \gamma$

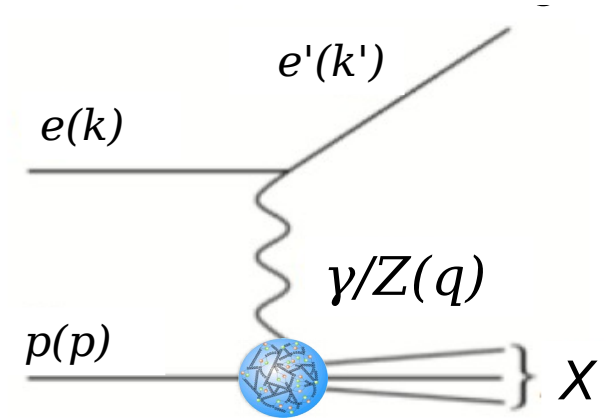
- Semi-leptonic weak decay mode, most sensitive
- Realistic analysis with SMEFT + full QED + parton shower + hadronization + fast detector simulation
- Pseudo-data with experimental uncertainties of 12% (dark green), 15% (light green), and 18% (yellow)
- Corona thickness increase from 0.1 (parton-level) to 0.15 (detector-level) for 18% uncertainty

# Electroweak physics in DIS

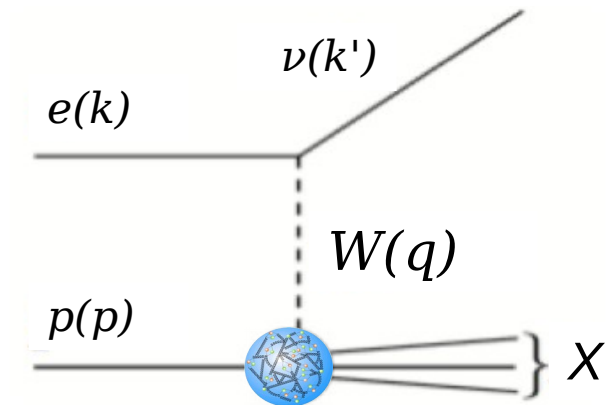
- Electron/positron beam polarizations of  $\pm 80\%$
- Precision determination of parameters in NC+CC
  - Weak-mixing angle
  - Gauge boson masses
  - NC/CC couplings of the gauge bosons



## NC inclusive DIS



## CC inclusive DIS



# Neutral Current inclusive DIS

$$\frac{d^2\sigma^{\text{NC}}(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[ Y_+ \tilde{F}_2^\pm(x, Q^2) \mp Y_- x \tilde{F}_3^\pm(x, Q^2) - y^2 \tilde{F}_L^\pm(x, Q^2) \right] ,$$

where  $\tilde{F}_2^\pm = F_2 - (g_V^e \pm P_e g_A^e) \kappa_Z F_2^{\gamma Z} + [(g_V^e g_V^e + g_A^e g_A^e) \pm 2P_e g_V^e g_A^e] \kappa_Z^2 F_2^Z$  ,

and  $\left[ F_2, F_2^{\gamma Z}, F_2^Z \right] = x \sum_q \left[ Q_q^2, 2Q_q g_V^q, g_V^q g_V^q + g_A^q g_A^q \right] \{q + \bar{q}\}$  in quark-parton model

Z normalization  $\kappa_Z(Q^2) = \frac{Q^2}{Q^2 + m_Z^2} \frac{1}{4 \sin^2 \theta_W \cos^2 \theta_W}$

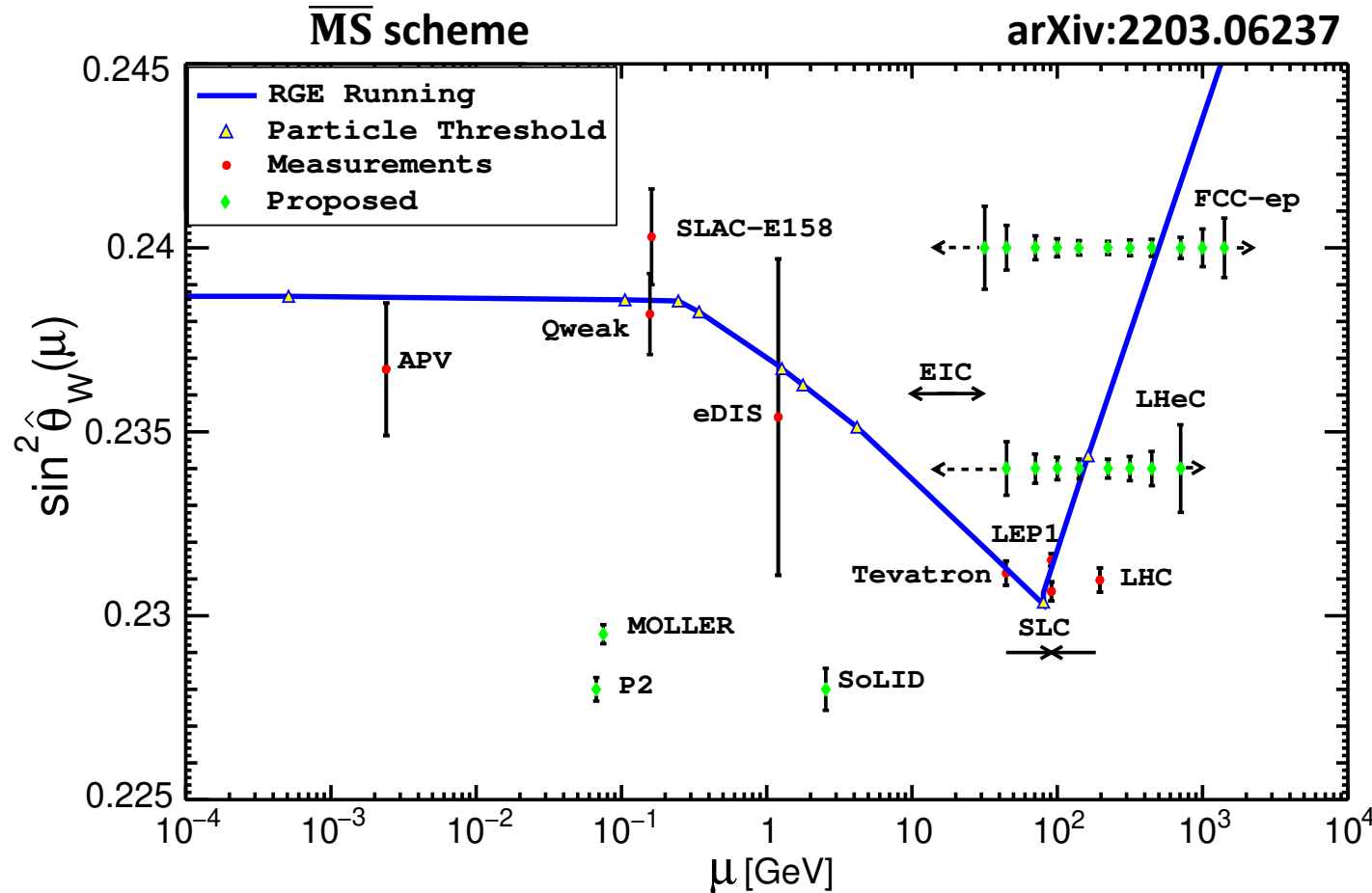
NC couplings  $g_V^f = \sqrt{\rho_{\text{NC},f}} (I_{\text{L},f}^3 - 2Q_f \kappa_{\text{NC},f} \sin^2 \theta_W)$  in SM  
 $g_A^f = \sqrt{\rho_{\text{NC},f}} I_{\text{L},f}^3$

- Independent SM parameters:

- $\alpha, m_Z, m_W$  + PDFs

# Scale dependence of weak mixing angle

Britzger, Klein, Spiesberger  
arXiv:2203.06237

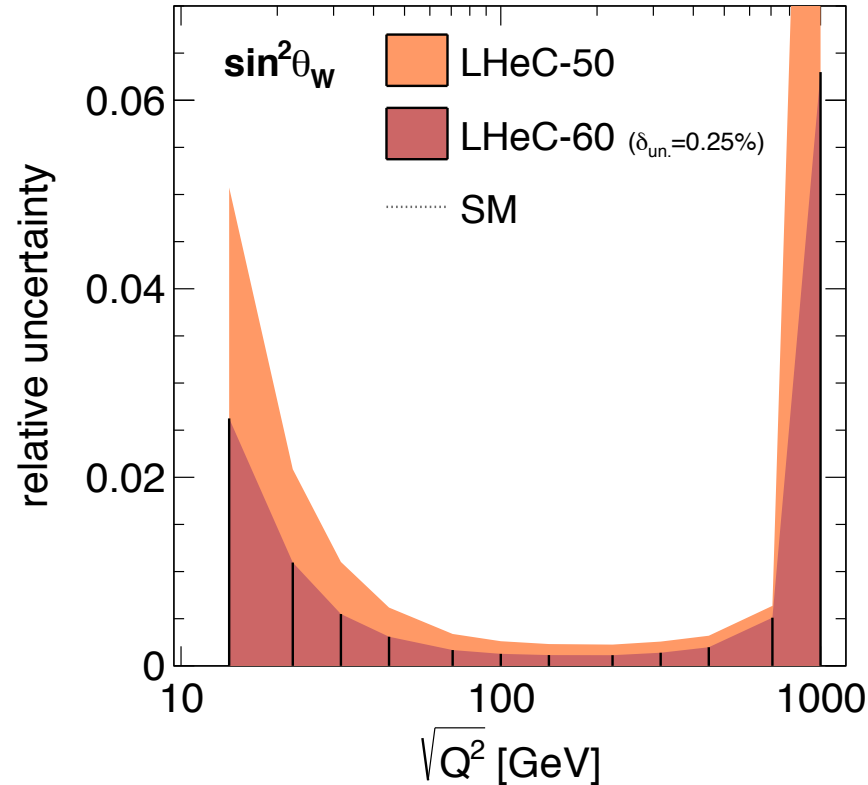


- Most high energy data measured at Z-pole
- Existing low energy data with large uncertainties
- LHeC/FCC-ep together access a wide range of scale at energy frontier
- Test of SM, potential discovery of BSM



# Uncertainties on weak mixing angle

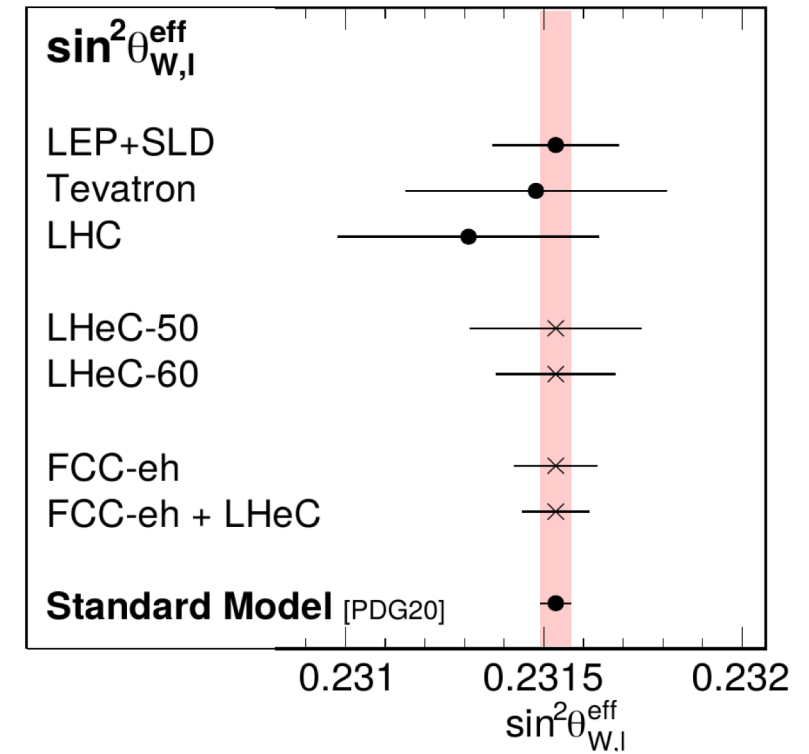
Britzger, Klein, Spiesberger  
arXiv:2203.06237



On shell scheme:

$$\sin^2\theta_W \equiv 1 - \frac{m_W^2}{m_Z^2}$$

- Fit  $\sin^2\theta_W$  + PDFs
- Comparison to Z-pole data



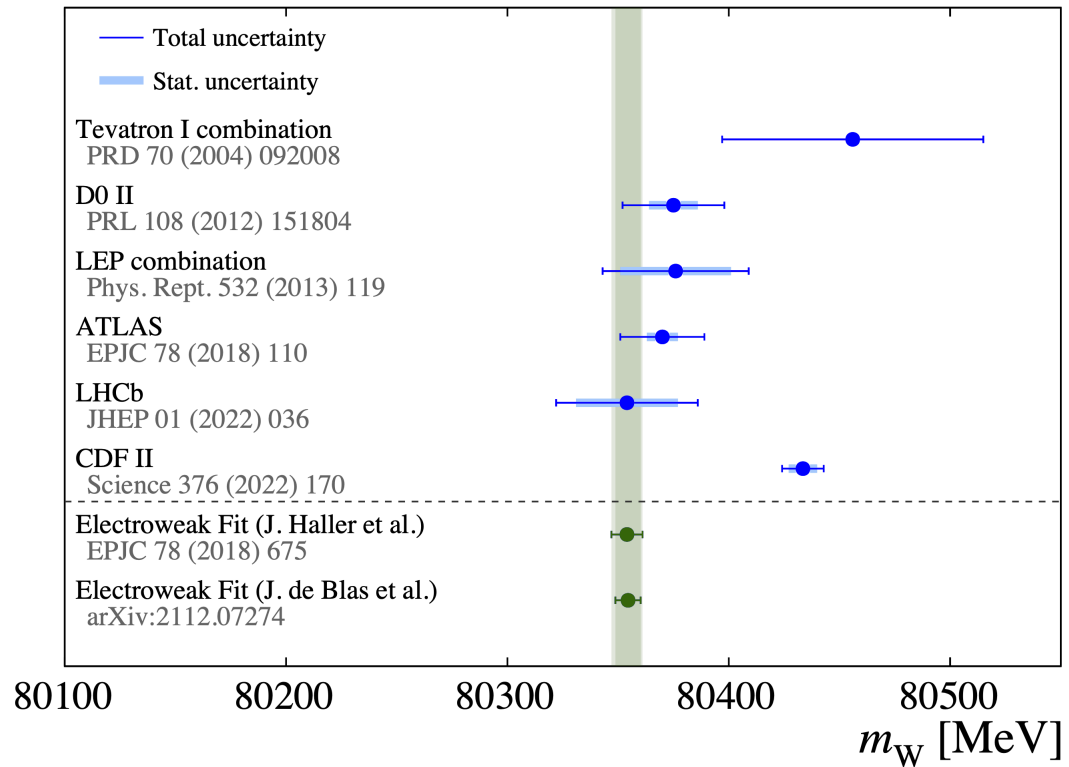
$$\Delta\sin^2\theta_W (\text{FCC-eh}) = \pm 0.00011$$

$$= \pm 0.00010_{(\text{exp})} \pm 0.00004_{(\text{PDF})}$$

$$\begin{aligned} \Delta\sin^2\theta_W (\text{LHeC-50}) &= \pm 0.00021 \\ \Delta\sin^2\theta_W (\text{LHeC-60}) &= \pm 0.00015 \\ \Delta\sin^2\theta_W (\text{FCC-eh+LHeC}) &= \pm 0.000086 \end{aligned}$$

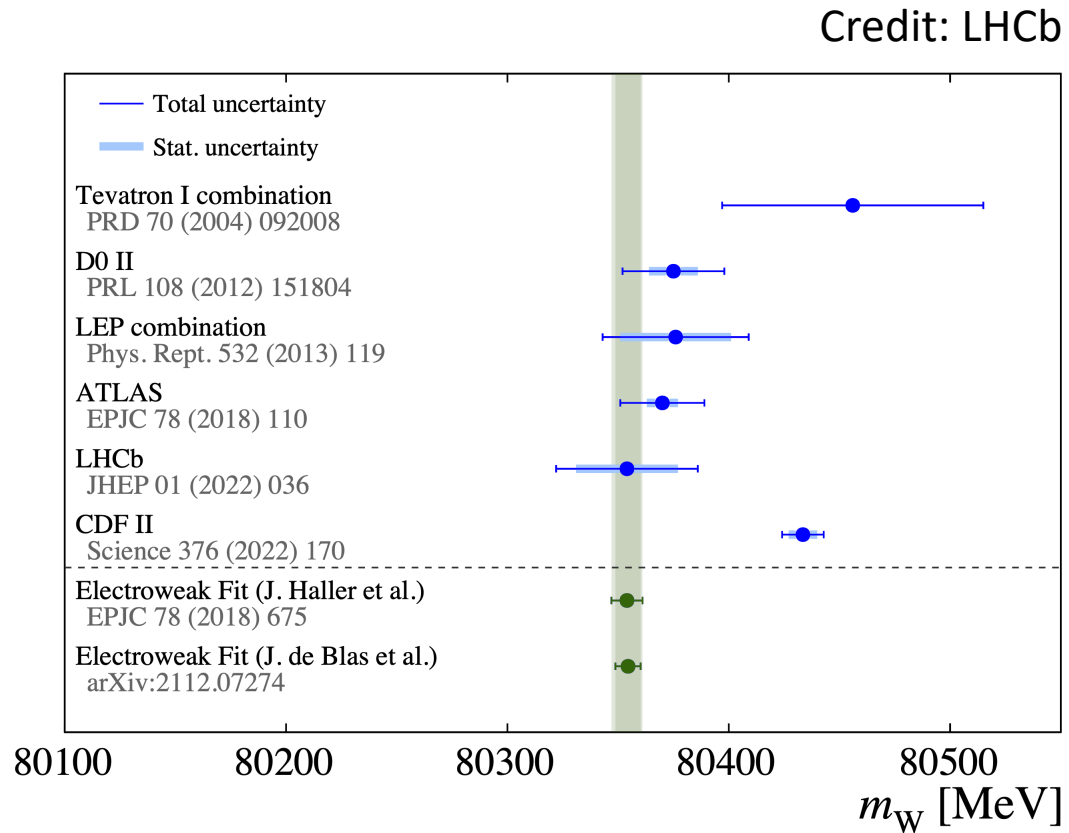
# W-boson mass

Credit: LHCb

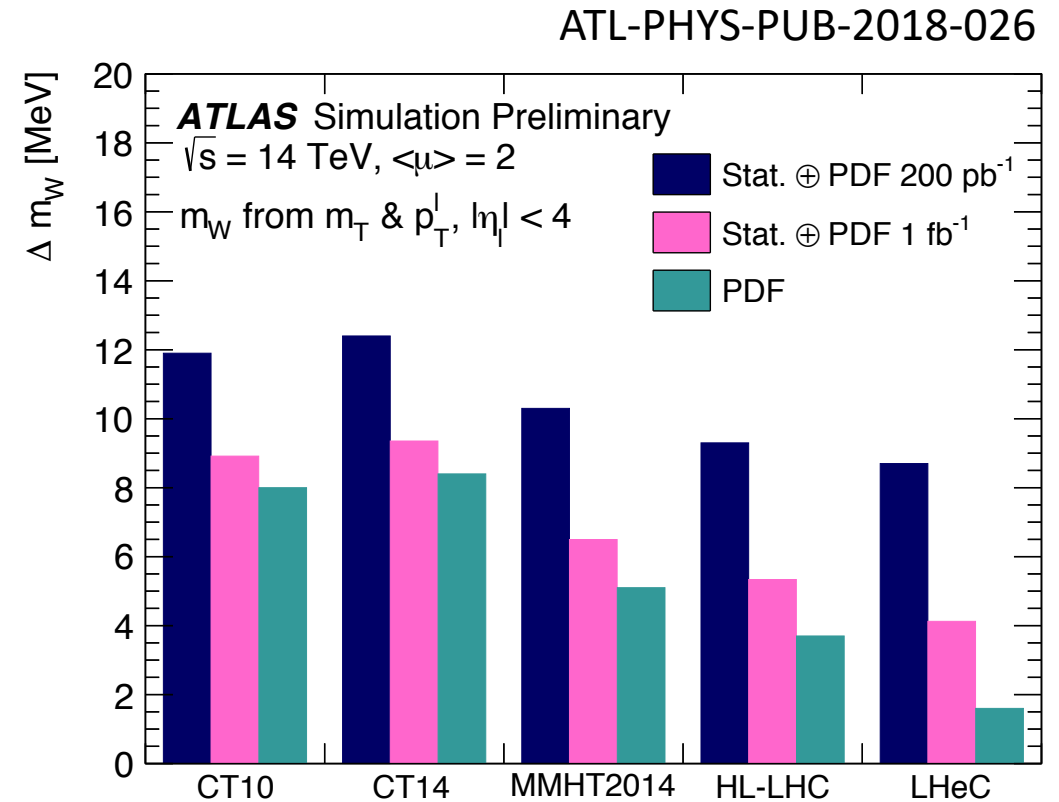


- Currently Large theory uncertainty originates from knowledge of **PDFs**

# W-boson mass



- Currently Large theory uncertainty originates from knowledge of **PDFs**



**$\Delta m_W(\text{PDF})$ :**

$\pm 8 \text{ MeV}$   
(CT10)

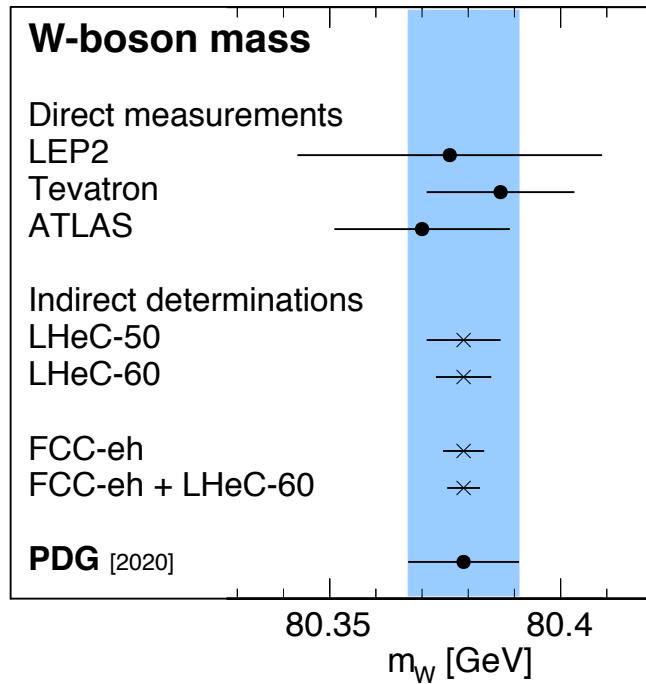


$\pm 3.6 \text{ MeV}$   
(HL-LHC)



**$\pm 1.6 \text{ MeV}$   
(LHeC)**

# W-boson mass

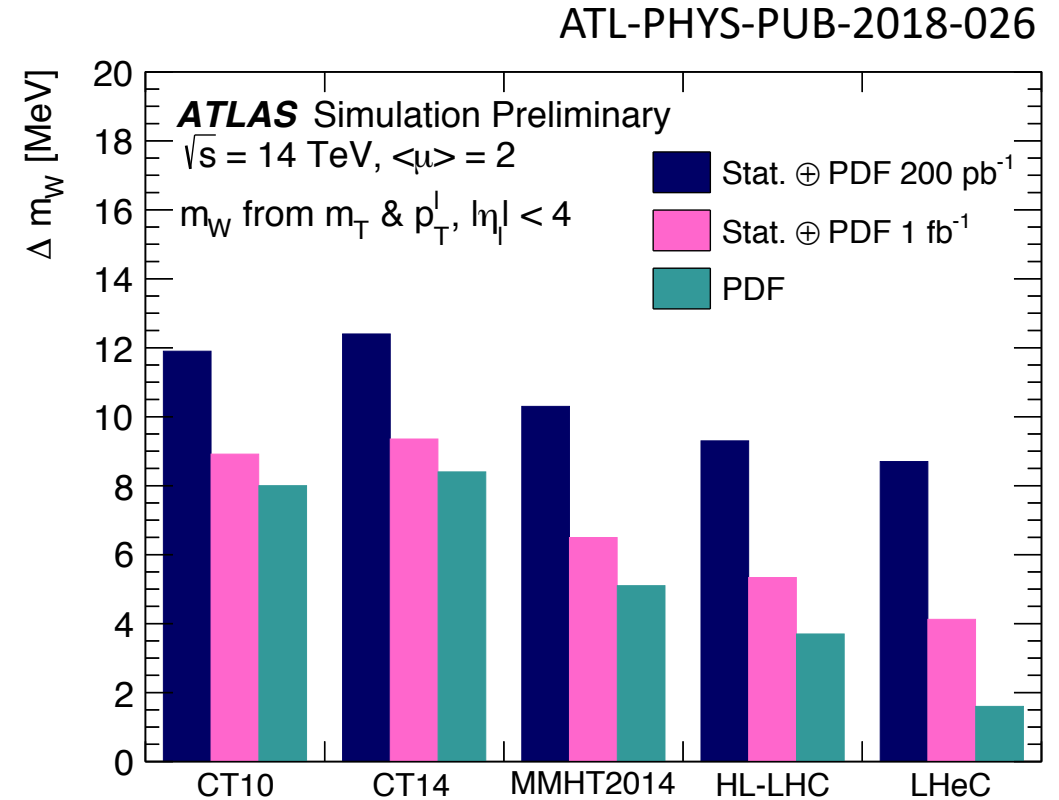


$$\Delta m_W (\text{FCC-eh}) = \pm 4.5 \text{ MeV}$$

including  $\pm 3.6 \text{ MeV}_{(\text{PDF})}$

$\Delta m_W$ (LHeC-50)	= $\pm 8 \text{ MeV}$
$\Delta m_W$ (LHeC-60)	= $\pm 6 \text{ MeV}$
$\Delta m_W$ (FCC-eh+LHeC)	= $\pm 3.6 \text{ MeV}$

arXiv:2203.06237



**$\Delta m_W(\text{PDF})$ :**

$\pm 8 \text{ MeV}$   
(CT10)



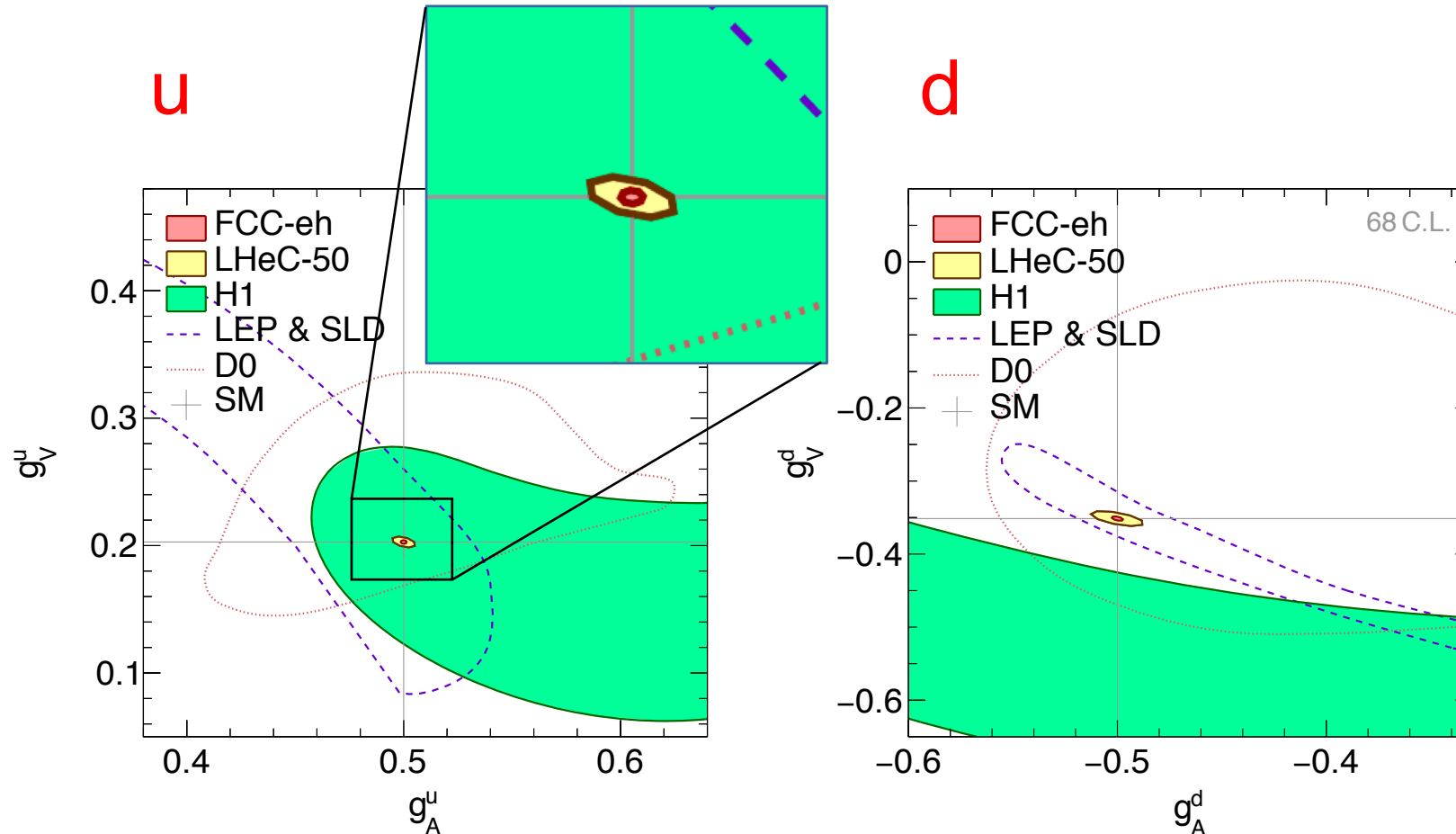
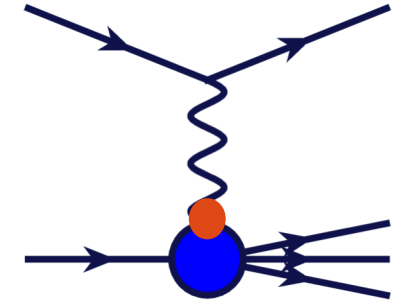
$\pm 3.6 \text{ MeV}$   
(HL-LHC)



**$\pm 1.6 \text{ MeV}$   
(LHeC)**

# Neutral Current DIS

## Electroweak light-quark couplings



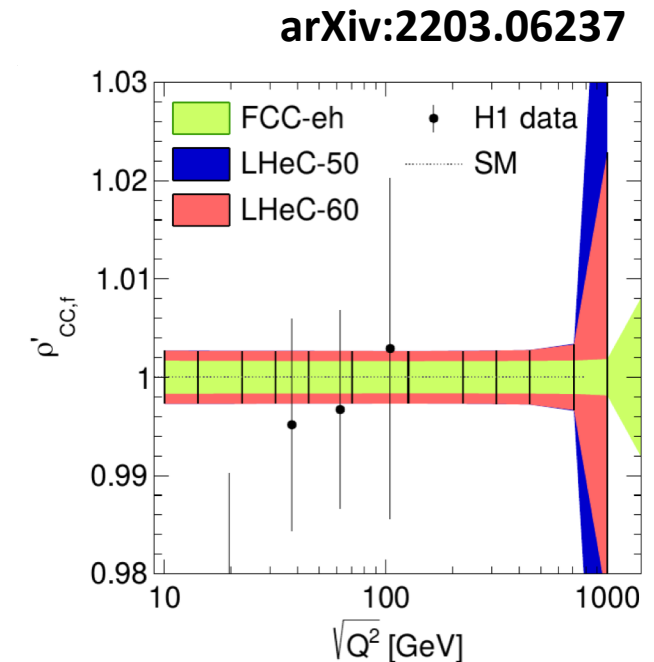
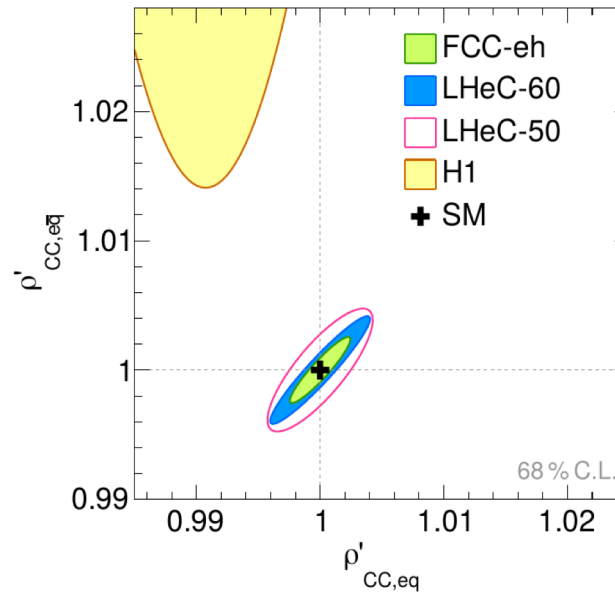
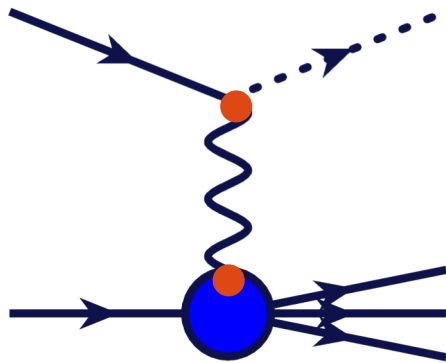
arXiv:2203.06237

- Precision per mille level – largely inaccessible in  $e^+e^-$
- Complementary to lepton coupling
- PDFs are not a limiting factor for EW couplings
- Scale dependence ('running') can be tested with high precision



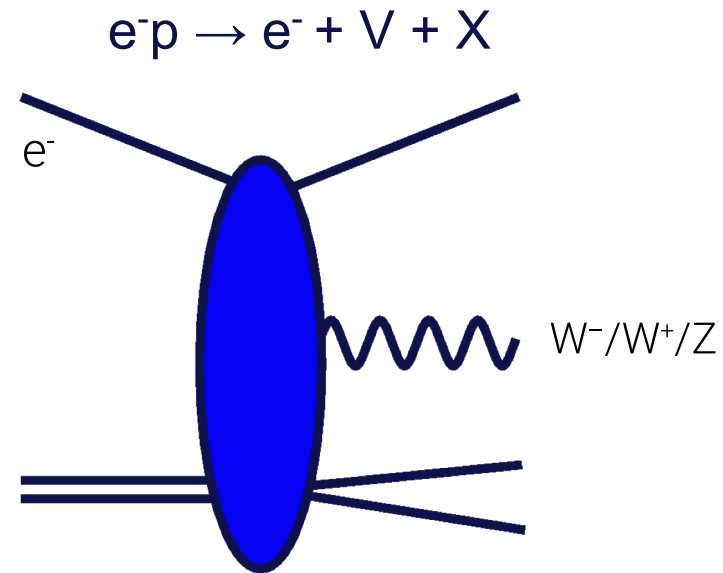
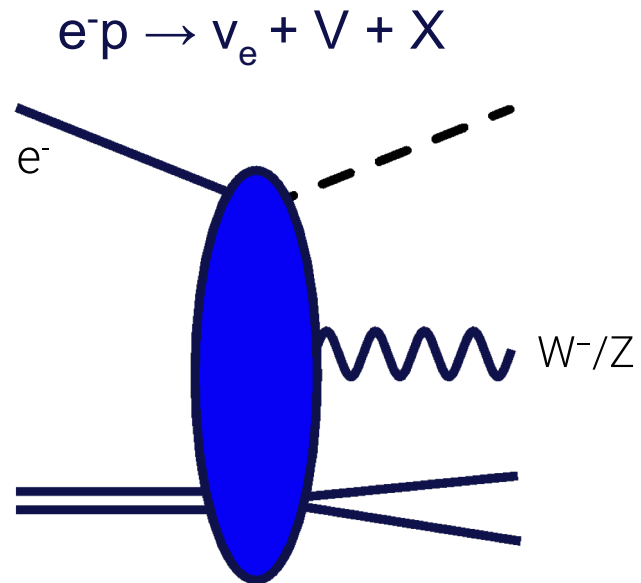
# Anomalous form factors in Charged Current DIS

- EW theory provides precise predictions for charged currents, but they are poorly measured in other processes  
→ neutrino escapes undetected



- In DIS, the kinematics of charged currents are completely measured from final state and incoming electron  
→ Weak couplings of the W-boson measured at a couple per mille level– even their scale dependence

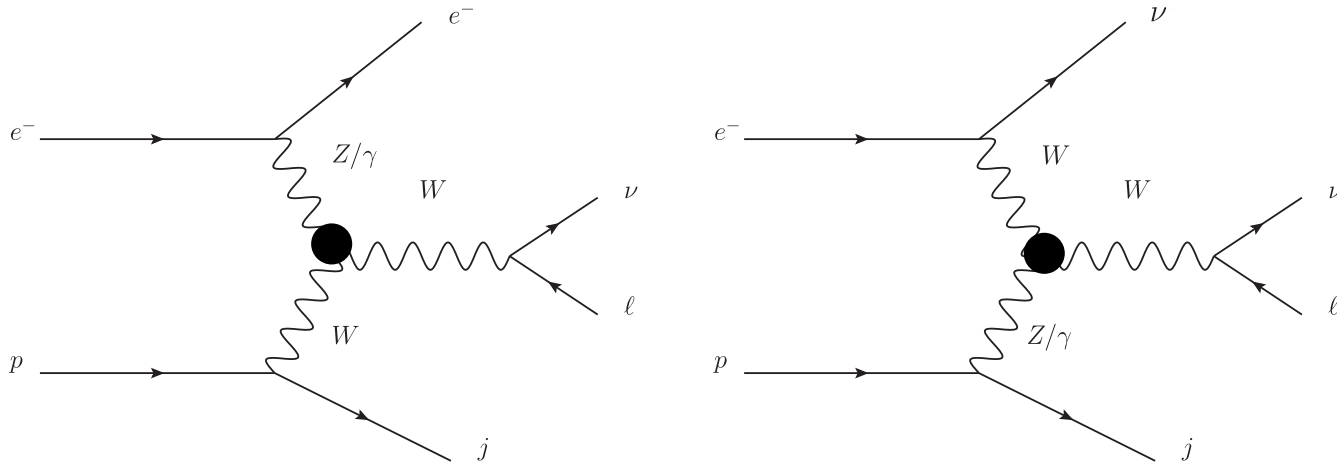
# Direct W and Z productions



- Through 5 production channels
- Total cross sections:  $\sigma(e^-p \rightarrow W^- X) \sim 15\text{pb}$   
 $\sigma(e^-p \rightarrow W^+ X) \sim 14\text{pb}$   
 $\sigma(e^-p \rightarrow Z X) \sim 5\text{pb}$

# Anomalous Triple Gauge Couplings

- 5 anomalous TGCs [ $\Delta g_{1Z}$ ,  $\Delta \kappa_V$ ,  $\lambda_V$ ]
- 3 are independent



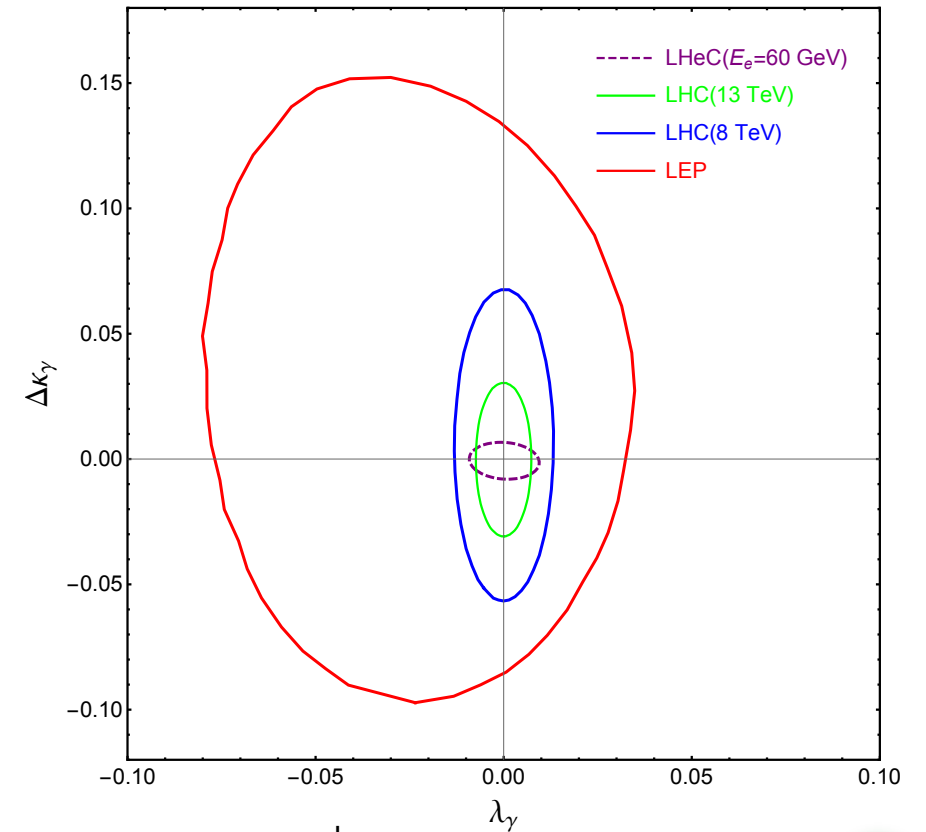
- Above Vector Boson Fusion process sensitive to  $WW\gamma$  couplings;  $WWZ$  suppressed due to  $Z$  mass (no interference)
- LHeC-60 significantly improves constraints on  $\Delta \kappa_\gamma$

**LHeC-60**

1 ab<sup>-1</sup>

2 $\sigma$  (95% C.L.)

NPB **375** (1992) 3, U. Baur, et al.  
PRD **97** (2018) 075043, R. Li, et al.



$$e^- p \rightarrow e^- \mu^+ \nu_\mu j$$

$\chi^2$  analysis of  $\Delta \phi_{ej}$  at parton level

# Summary

- LHeC and FCC-eh
  - Energy frontier electron hadron collider  
with  $E_e = 50$  GeV (LHeC) and 60 (FCC-eh) GeV  
synchronously run with HL-LHC (LHeC) and FCC-hh (FCC-eh)
- Top physics
  - Rich top-physics with single top production, photoproduction of top-quark pairs and FCNC
  - CKM third-row, MDM, EDM, electric charge, polarization, PDFs ...
- Electroweak physics
  - Precision measurements of fundamental EW parameters
  - Weak mixing angle, W mass, anomalous couplings to light quarks and TGC
  - Unprecedented precise determination of PDFs using LHeC data needed at HL-LHC
  - Complementary to Z-pole and (planned) low energy data

Thank you!