

# MSHT20: Updates

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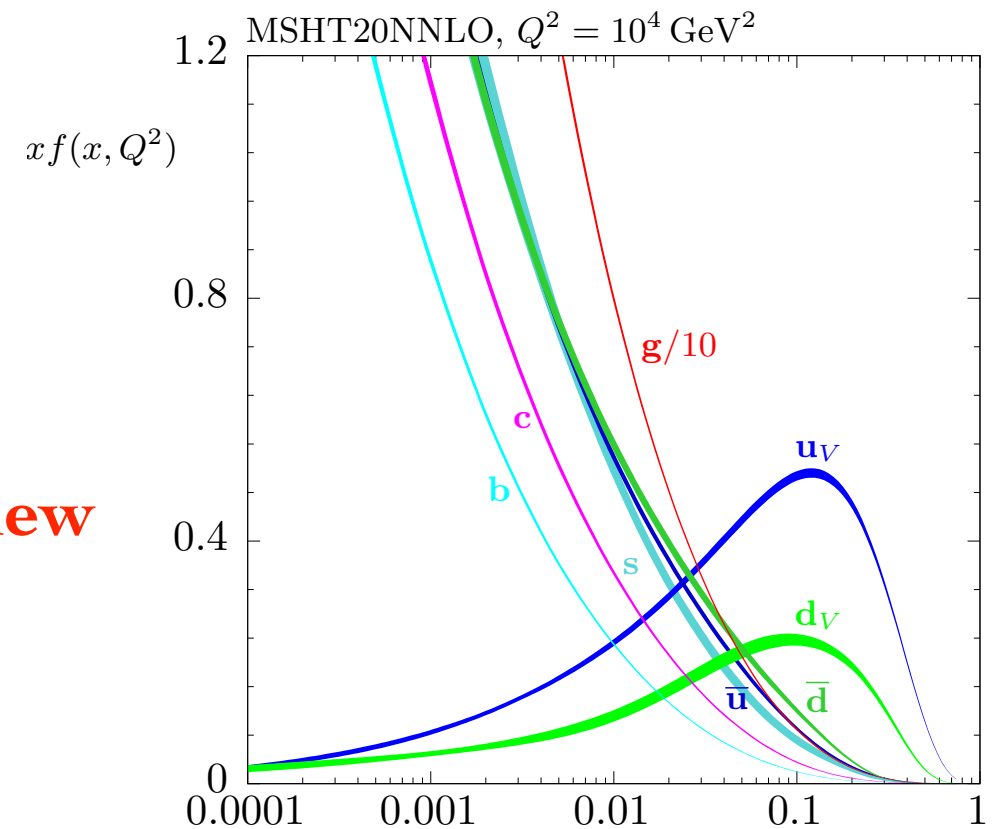
DIS 2023, MSU, 28 March 2023

*In collaboration with Tom Cridge, Jamie McGowan and Robert Thorne*



# Outline

- The ‘Post-Run I’ set from the MSTW, MMHT... group: **MSHT20**.
- Focus on including significant amount of **new data**, higher **precision theory** and on **methodological improvements**.



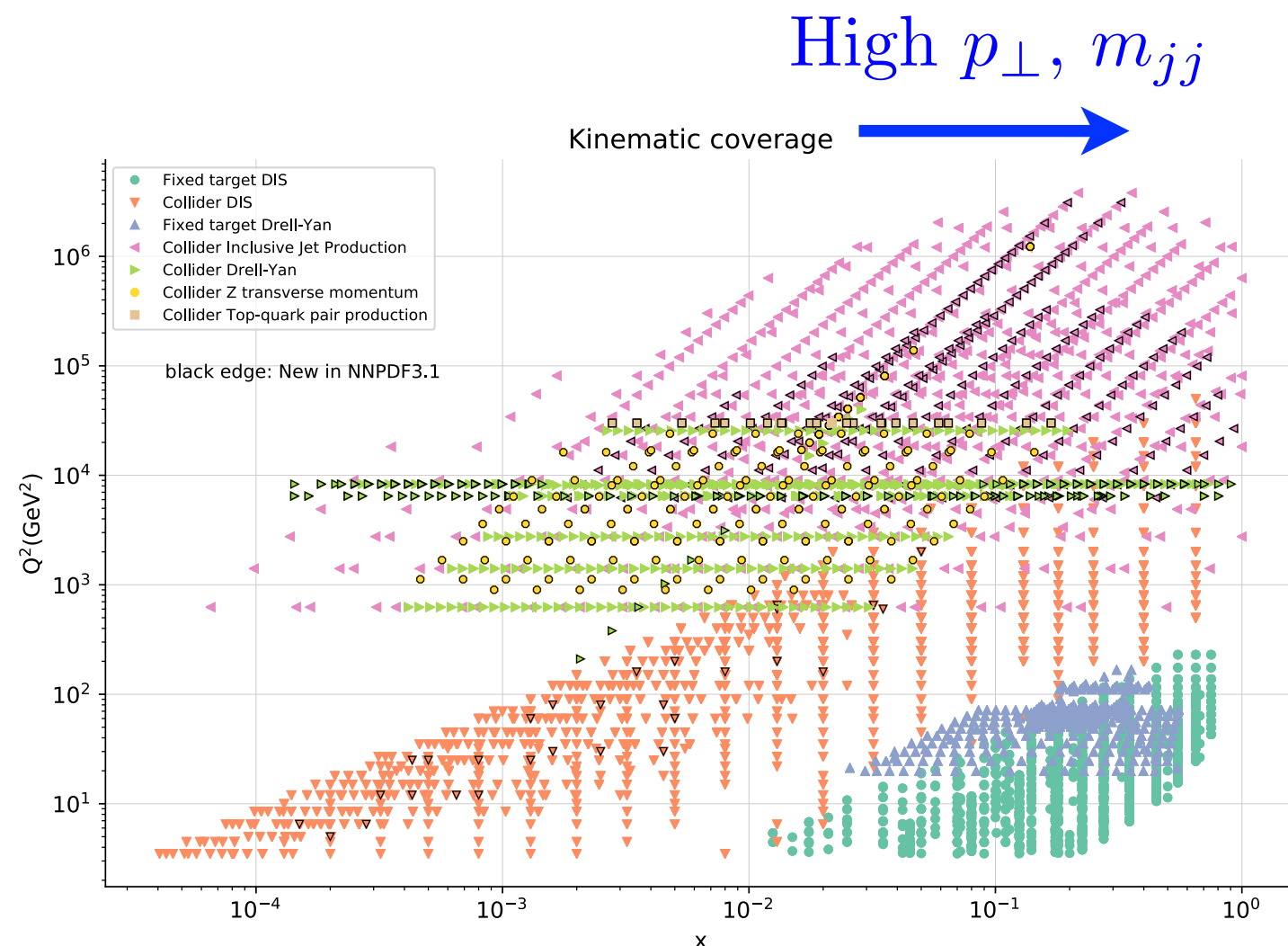
**See talk by T. Cridge**

- More recent major update: extended to (approximate) N3LO order.
- Will discuss here on a selection of follow up studies, at both NNLO and aN3LO.
- **Main Focus**: analysis of jet and dijet data at NNLO and aN3LO.

# **Jets and Dijets in *MSHT20***

# Jets for PDF fits

- Jet production a **key ingredient** in modern PDF fits.
  - By pushing to larger jet  $p_\perp$  (dijet  $m_{jj}$ ) go to larger  $x$ .
  - Quark-initiated contribution tends to be better constrained  $\rightarrow$  particularly relevant for **gluon** at high  $x$ .
- 
- **NNLO QCD** (and **NLO EW**) theory available for both inclusive and dijet data.
  - In addition, high **precision** LHC data available, spanning large range of kinematic space.



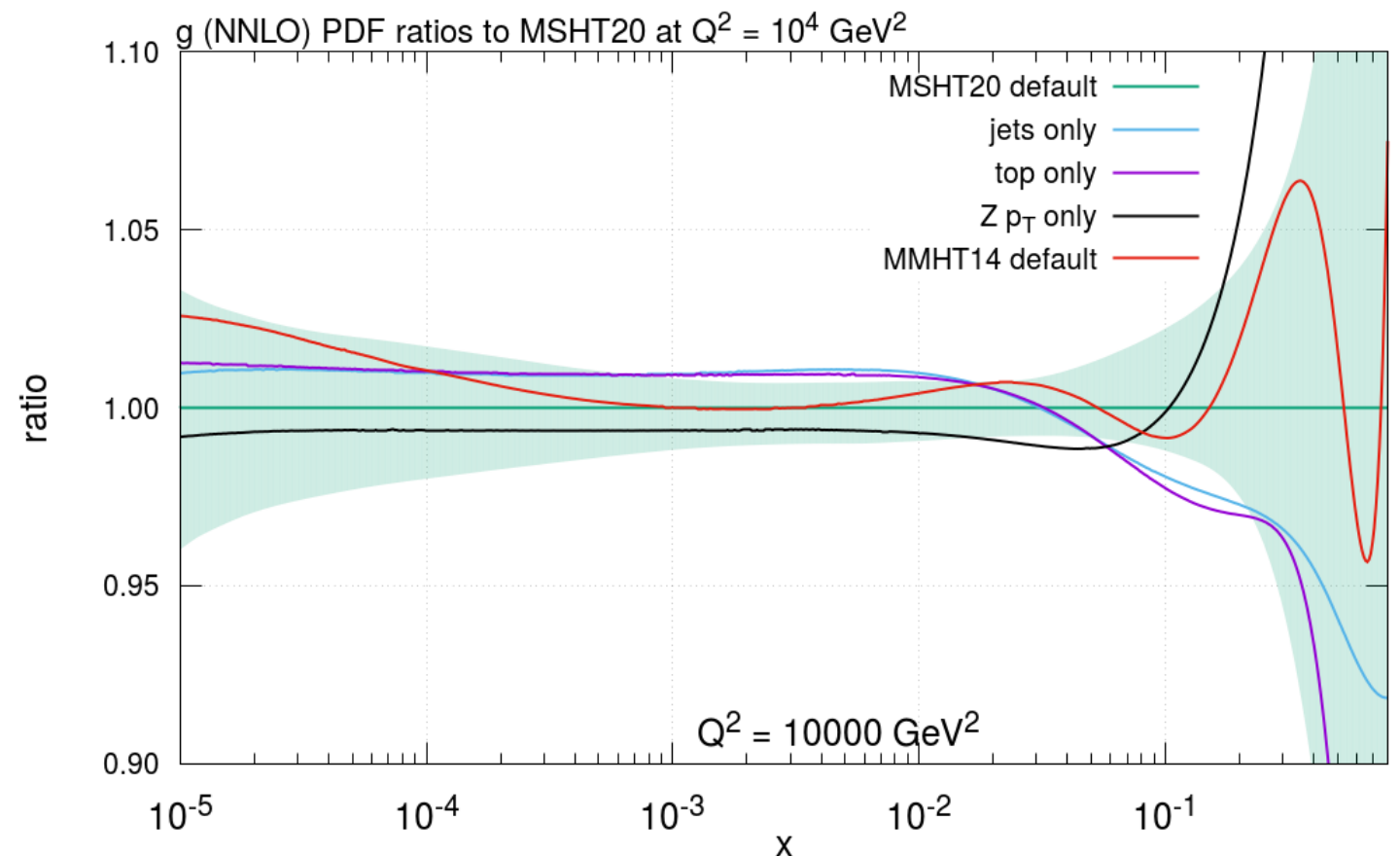


# Jets in MSHT20

NNLO,  $\chi^2/N_{\text{pt}}$

- Range of inclusive LHC jet dat fit:
- Fit quality acceptable. N.B. For ATLAS data smooth decorrelation of systematic errors applied.
- PDF impact tied up with other high  $x$  gluon sensitive data....

ATLAS 7 TeV jets [18]	221.6/140
CMS 2.76 TeV jet [107]	102.9/81
CMS 7 TeV jets [100]	175.8/158
CMS 8 TeV jets [101]	261.3/174



# MSHT20 updates: Jet data

- Focussing on Run-I data (i.e. current PDF fits):
$$\frac{d^2\sigma}{dp_\perp dy}$$
    - Inclusive jets:
$$0.0 < |y| < 2.5 - 3.0$$
      - ★ CMS 2.76 TeV: 81 points — 5.43 pb<sup>-1</sup> — 74 < p<sub>⊥</sub> < 592 GeV
      - ★ CMS 7 TeV: 158 points — 5.0 fb<sup>-1</sup> — 74 < p<sub>⊥</sub> < 2500 GeV
      - ★ CMS 8 TeV: 174 points — 19.7 fb<sup>-1</sup> — 60 < p<sub>⊥</sub> < 1300 GeV
      - ★ ATLAS 7 TeV: 140 points — 4.5 fb<sup>-1</sup> — 100 < p<sub>⊥</sub> < 2000 GeV
      - ★ ATLAS 8 TeV: 171 points — 20.2 fb<sup>-1</sup> — 70 < p<sub>⊥</sub> < 2500 GeV
- 724 points in total, v.s. ~ 4500 in global MSHT fit (inc.).
- We take the larger of the jet radii available in both cases, i.e. R=0.6/0.7.

- **Dijets:**

$$\star \text{ ATLAS 7 TeV: } 90 \text{ points} - 4.5 \text{ fb}^{-1} - \frac{d^2\sigma/dm_{jj}d|y_{\max}|}{0.26 < m_{jj} < 5.04 \text{ TeV}}$$

$$\star \text{ CMS 7 TeV: } 54 \text{ points} - 5.0 \text{ fb}^{-1} - \frac{d^2\sigma/dm_{jj}d|y^*|}{0.25 < m_{jj} < 4.48 \text{ TeV}}$$

$$\star \text{ CMS 8 TeV: } 122 \text{ points} - 19.7 \text{ fb}^{-1} - \frac{d^3\sigma/dp_{\perp,avg}dy_bdy^*}{143 < p_{\perp,avg} < 1638 \text{ GeV}}$$

→ 266 points in total, v.s.  $\sim 4000$  in global MSHT fit (inc.).

- Again take the larger of the jet radii available in both cases, i.e.  $R=0.6/0.7$ .

- **CMS 8 TeV** data the only cases where this is **triple differential**. Only case where LO kinematics specified  $\Rightarrow$  higher impact (backup).

# Fit Quality

- Consider impact of both inclusive or dijet data at NNLO and aN<sup>3</sup>LO in the MSHT20 fit.

**Jet fit:**

	$N_{\text{pts}}$	NNLO	aN <sup>3</sup> LO
ATLAS 7 TeV jets	140	1.54	1.46
CMS 7 TeV jets	158	1.29	1.32
ATLAS 8 TeV jets	171	1.96	1.90
CMS 8 TeV jets	174	1.83	1.80
Total Jets	643	<u>1.67</u>	<u>1.63</u>

**NB: smooth decorrelation of systematics applied for ATLAS inclusive jet data.**

$\chi^2/N_{\text{pts}}$

**Dijet fit:**

	$N_{\text{pts}}$	NNLO	aN <sup>3</sup> LO
ATLAS 7 TeV dijets	90	1.06	1.12
CMS 7 TeV dijets	54	1.43	1.39
CMS 8 TeV dijets	122	1.05	0.82
Total Dijets	266	<u>1.13</u>	<u>1.04</u>

- ★ **NNLO**: Fit quality to dijet data very good (1.13), clearly worse for jets (1.67).
- ★ **aN<sup>3</sup>LO**: Some improvement in both cases (1.13, 1.63 for jets, dijets) but inclusive jet remains a rather bad fit!

**Dijets**



**Jets**



- What about interplay with other gluon sensitive data?

### Jet fit:

	$N_{\text{pts}}$	NNLO	aN <sup>3</sup> LO
ATLAS $Z p_{\perp}$	104	<u>1.89</u>	1.03
Diff. top	54	1.10	1.06
7 + 8 TeV dijets	266	[1.30]	[1.10]
7 + 8 TeV jets	643	1.67	1.63

### Dijet fit:

	$N_{\text{pts}}$	NNLO	aN <sup>3</sup> LO
ATLAS $Z p_{\perp}$	104	<u>1.66</u>	1.05
Diff. top	54	1.26	1.09
7 + 8 TeV jets	643	[1.75]	[1.65]
7 + 8 TeV dijets	266	1.13	1.04

- ★ Jet data: no signs of significant inconsistency in fit vs. prediction though some difference in pull implied.
- ★ **NNLO**: Fit quality to top ( $Z p_{\perp}$ ) data better in jet (dijet) fit. Latter particularly notable  $\Rightarrow$  overall tension less in dijet fit.
- ★ **aN<sup>3</sup>LO**: tensions reduced in all cases. No clear difference between jet/dijets.
- ★ (Not shown) - fit quality to other data in global fit v. similar.

**Dijets** 


**Jets** 

**With some preference for aN<sup>3</sup>LO**

# Impact of EW corrections

<b>Jet fit:</b>	<b>NNLO:</b>	$\chi^2$ (no EW) $\rightarrow$ $\chi^2$ (EW) : 1.57 $\rightarrow$ 1.67
	<b>aN3LO:</b>	$\chi^2$ (no EW) $\rightarrow$ $\chi^2$ (EW): 1.59 $\rightarrow$ 1.63
<b>Dijet fit:</b>	<b>NNLO:</b>	$\chi^2$ (no EW) $\rightarrow$ $\chi^2$ (EW) : 1.37 $\rightarrow$ 1.13
	<b>aN3LO:</b>	$\chi^2$ (no EW) $\rightarrow$ $\chi^2$ (EW) : 1.27 $\rightarrow$ 1.04

- ★ Significant improvement in dijet fit upon including EW corrections.  
However trend is opposite for inclusive jets (!). Given these are there:

**Dijets**  **Jets** 

indeed even absent EW correction dijet fit quality is better.

- ★ Remains true at **aN3LO**. Deterioration in fit quality for no EW fit somewhat improved but not entirely  $\Rightarrow$  not true that freedom in **aN3LO** K-factors can (fully) absorb other theoretical deficiencies.

# Inclusive Jets: scale choice

J. Currie et al.,  
*JHEP* 10 (2018) 155

- Default inclusive fits taken with  $\mu = p_{\perp}^j$  scale choice. However some indication that  $\mu = \hat{H}_{\perp}$  may be preferable.

$$\hat{H}_{\perp} = \sum_i p_{i\perp}$$

- What does global fit say?

**NLO:**  $\chi^2(p_{\perp}^j) \rightarrow \chi^2(\hat{H}_{\perp}) : 1.68 \rightarrow 1.60$

**NNLO:**  $\chi^2(p_{\perp}^j) \rightarrow \chi^2(\hat{H}_{\perp}) : 1.64 \rightarrow 1.65$

**aN3LO:**  $\chi^2(p_{\perp}^j) \rightarrow \chi^2(\hat{H}_{\perp}) : 1.58 \rightarrow 1.60$

★ **NLO** fit quality better with  $\mu = \hat{H}_{\perp}$  but difference marginal at **NNLO/aN3LO**.

★ Trend for improved description with order not present with  $\mu = \hat{H}_{\perp}$ .

→ Scale choice does not appear to play significant role at **NNLO** and beyond.

**Impact on PDFs small: Backup**

# Taking step back: pQCD working?

- Worth taking a look at **NLO** fit quality...

## Jets fit:

	$N_{\text{pts}}$	NLO	NNLO	aN <sup>3</sup> LO
ATLAS 7 TeV jets	140	1.61	1.54	1.46
CMS 7 TeV jets	158	1.37	1.29	1.32
ATLAS 8 TeV jets	171	2.24	1.96	1.90
CMS 8 TeV jets	174	1.66	1.83	1.80
Total Jets	643	<u>1.73</u>	1.67	1.63

## Dijets fit:

	$N_{\text{pts}}$	NLO	NNLO	aN <sup>3</sup> LO
ATLAS 7 TeV dijets	90	1.12	1.06	1.12
CMS 7 TeV dijets	54	1.70	1.43	1.39
CMS 8 TeV dijets	122	5.27	1.05	0.82
Total Dijets	266	<u>3.14</u>	1.13	1.04

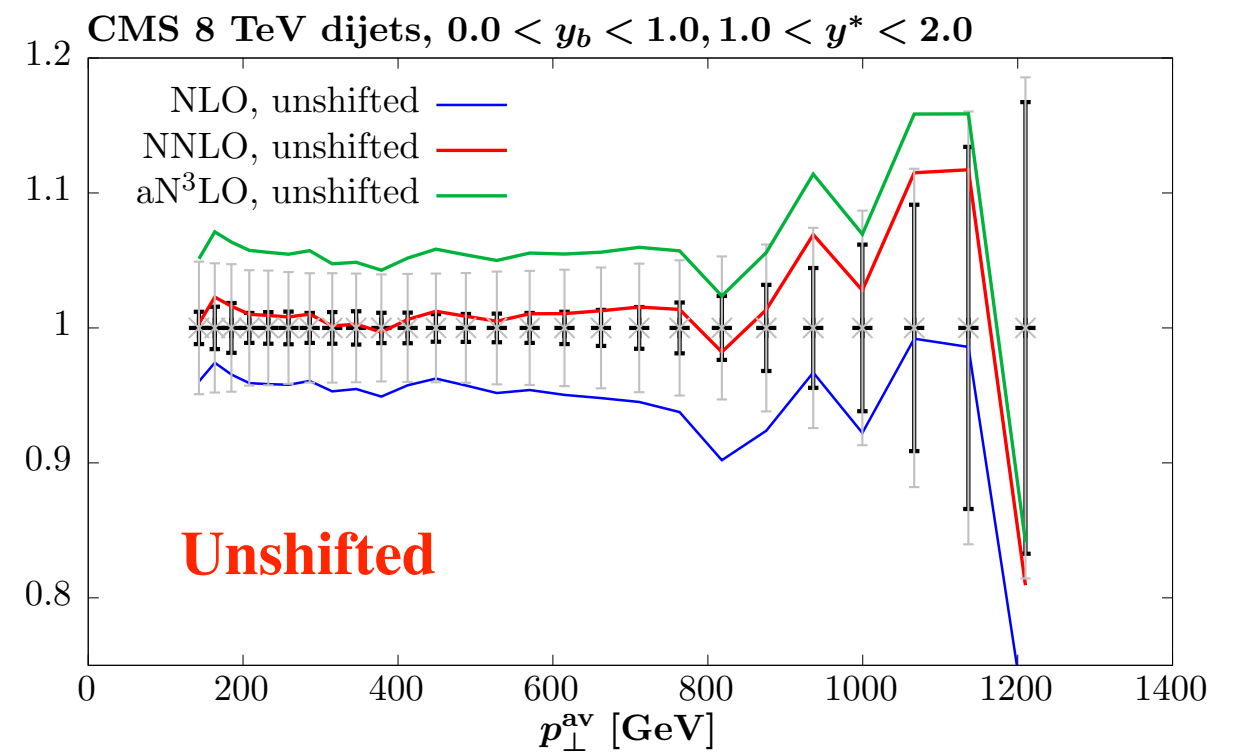
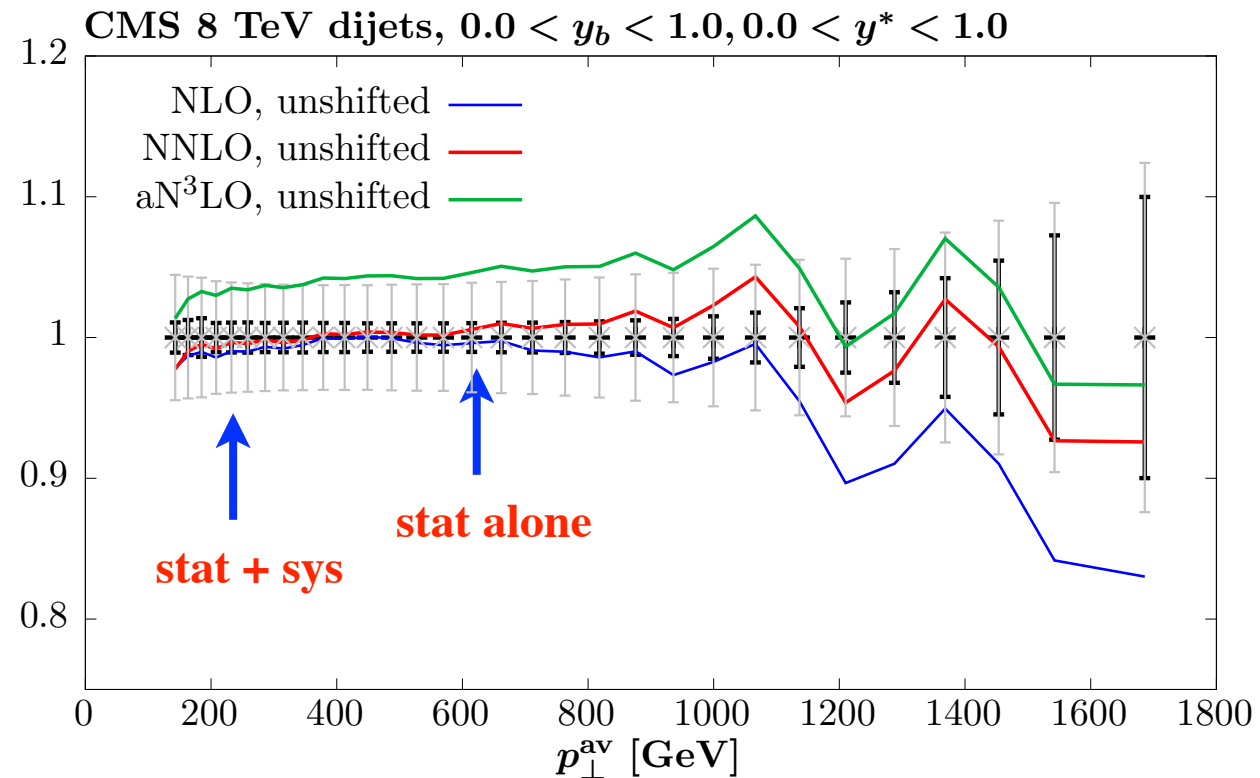
**Not a typo!**

- ★ Clear trend in both cases for QCD corrections to improve fit quality. pQCD working as it should!
- ★ Improvement in CMS 8 TeV dijets particularly **remarkable**. Clear need for NNLO QCD at high precision + multi-differential LHC. In more detail...

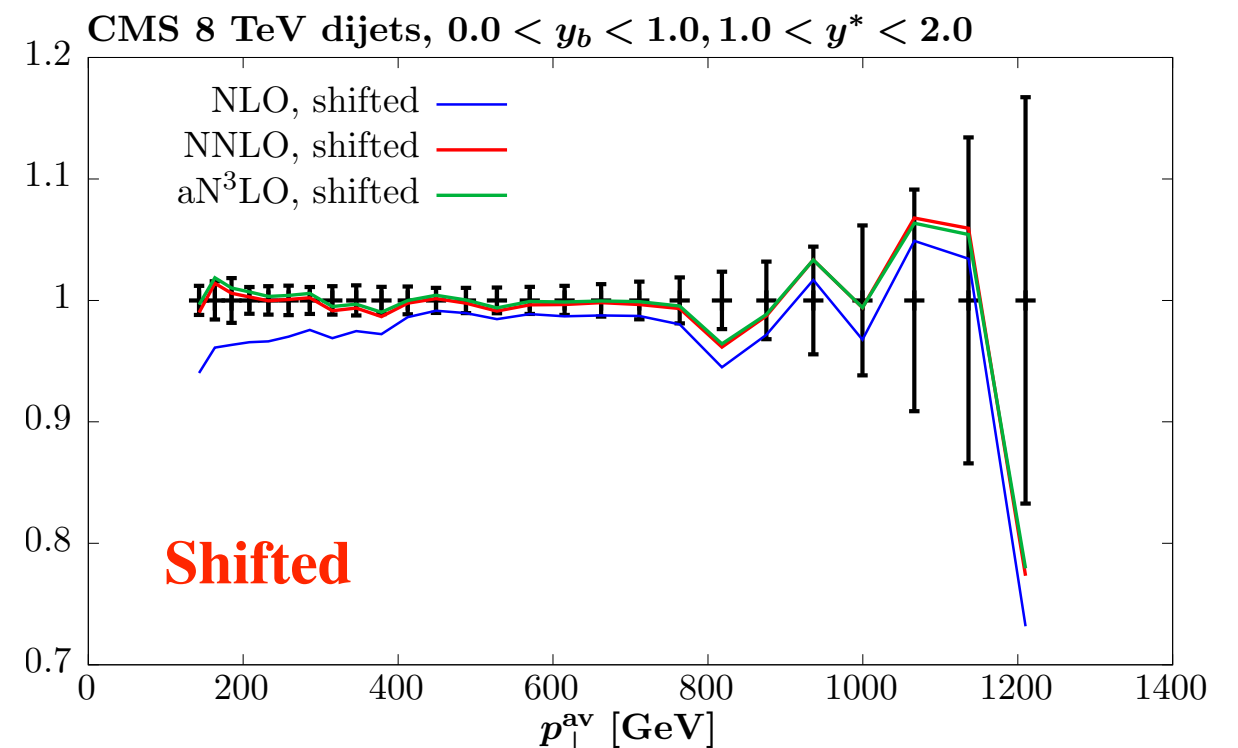
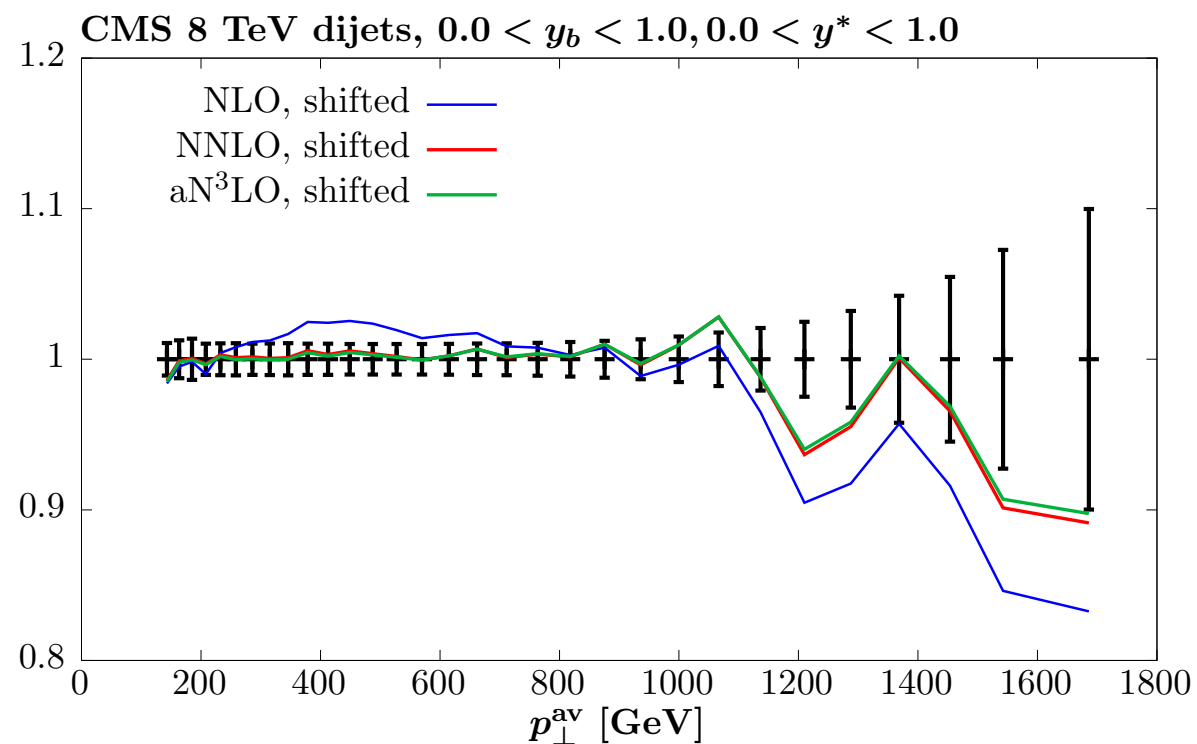
**See also: ATLAS high precision W,Z**



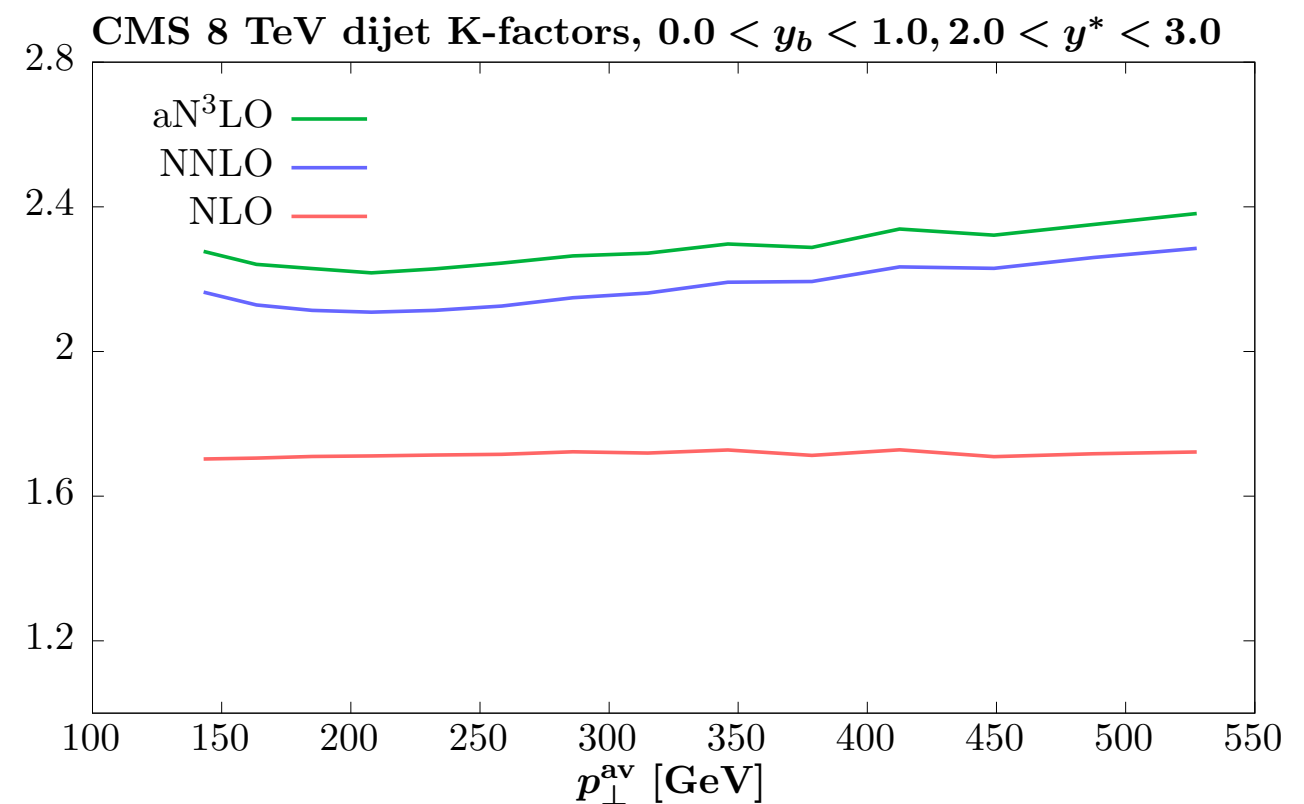
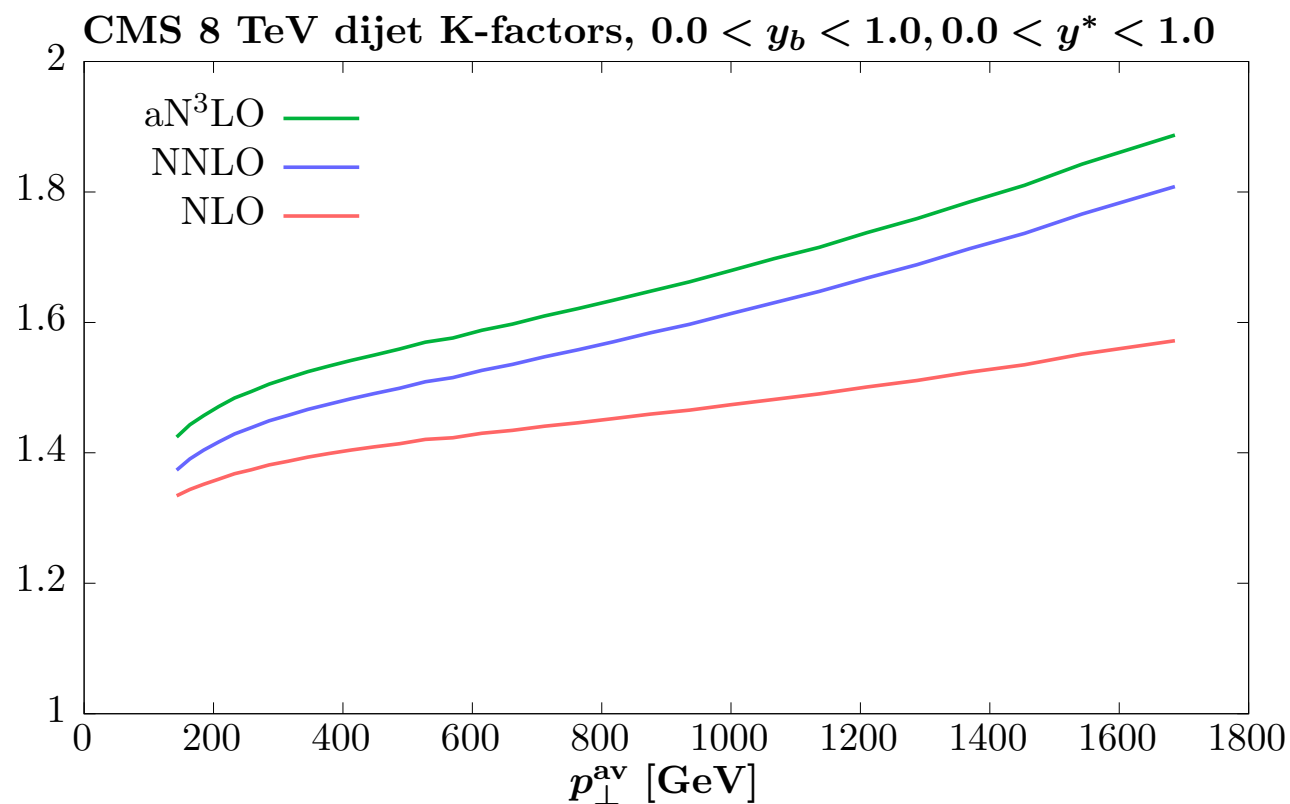
- No clear, by eye, trend for better description at NNLO, aN3LO.



- However this is **before** shifting by correlated systematics.

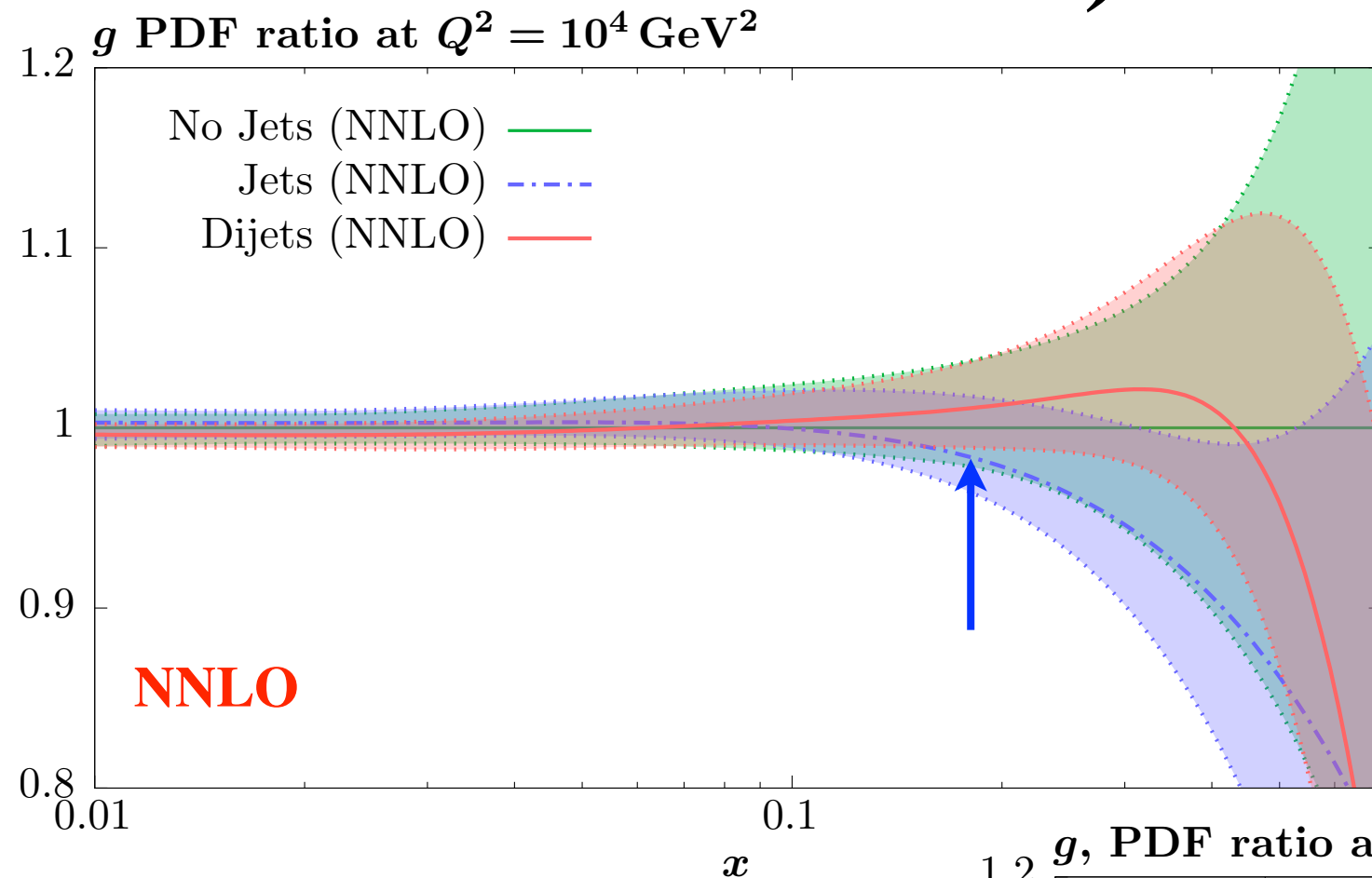


- Impact on shape of distributions in 3D kinematic space and interplay with correlated systematics drives this.
- However some clue from looking at K-factors:



- ★ **NNLO** corrections reasonable large, in particular in some regions of phase space.
- ★ Also shown are the **aN<sup>3</sup>LO** K-factors preferred by the fit: nice trend for perturbative stability, in line with lower orders.
- ★ Similar stability in inclusive jet case (backup).

# PDFs: dijets vs. Jets

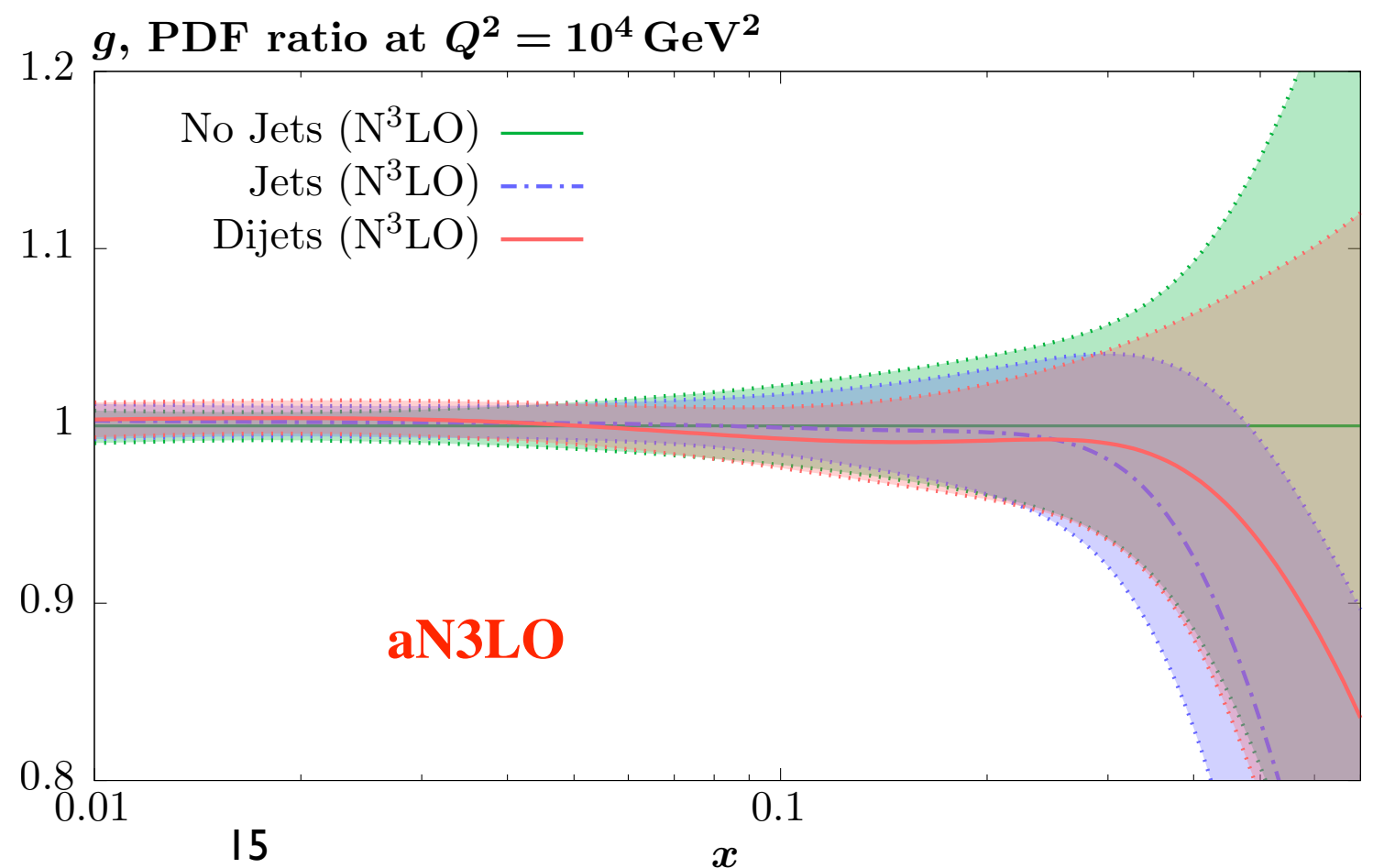


★ Focus on gluon: largest expected impact.

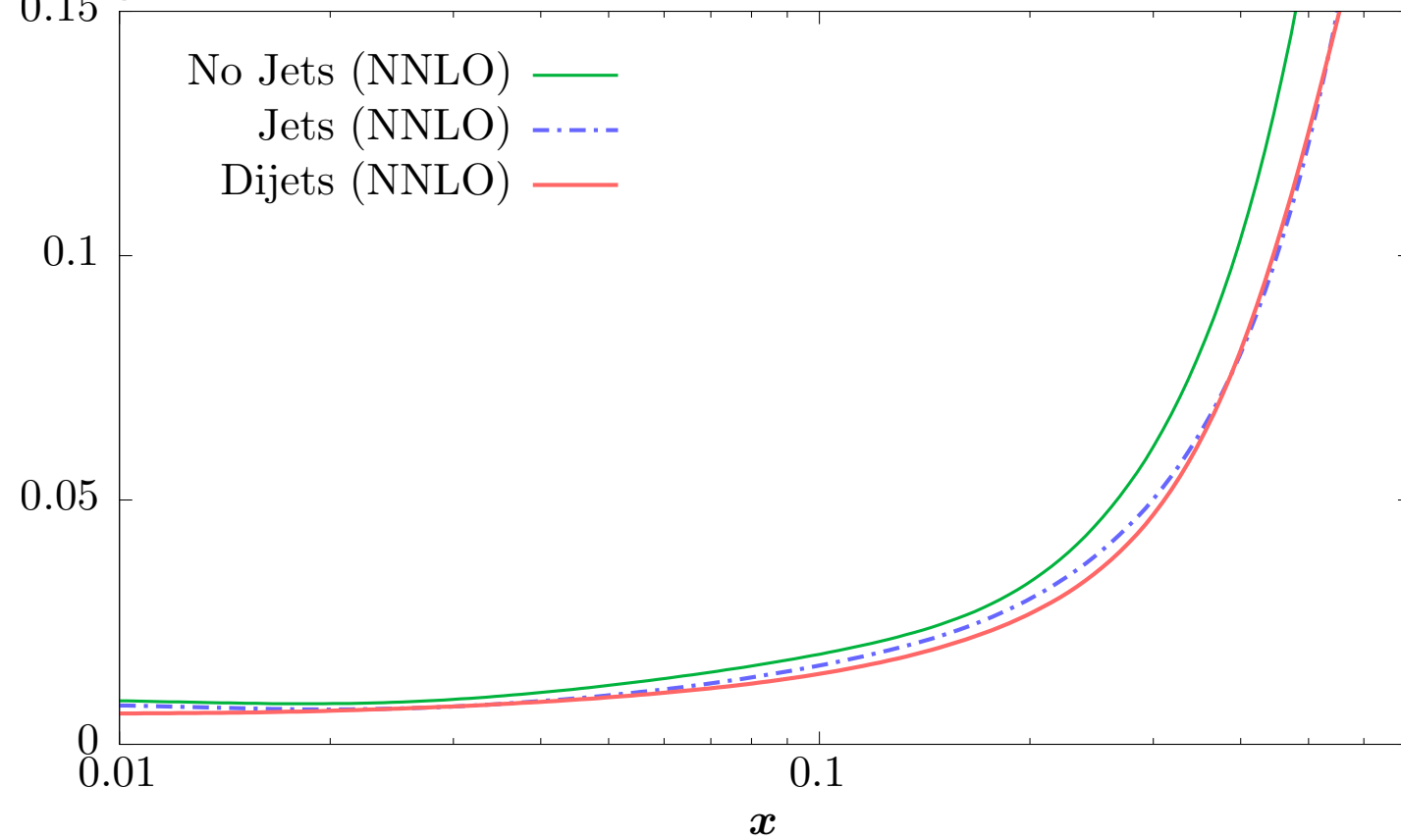
★ Overall **consistency** between two cases...

★ But some difference in pull observed between jets/dijets at NNLO.

★ At aN3LO pulls rather similar.



$g$ , PDF errors at  $Q^2 = 10^4 \text{ GeV}^2$

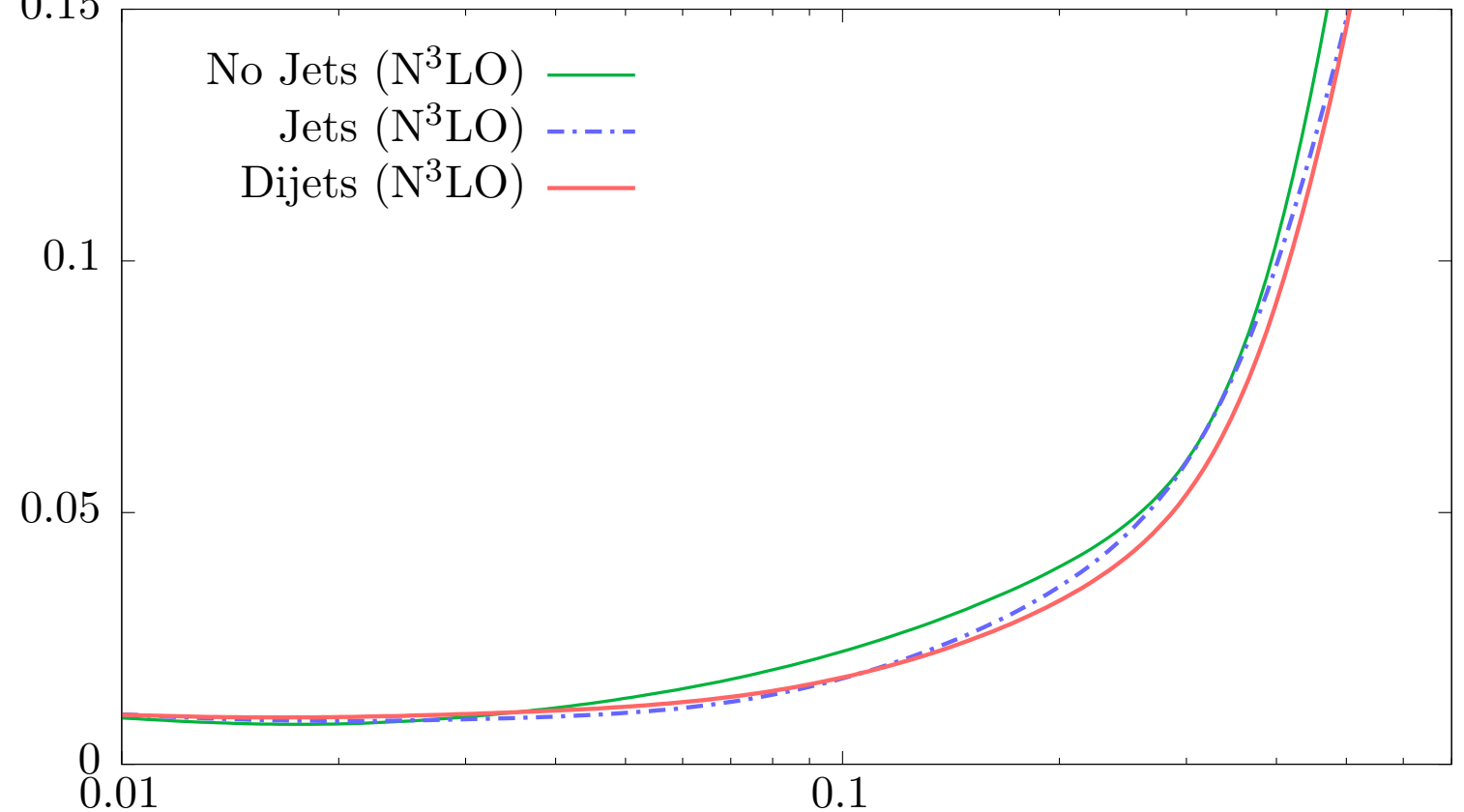


★ Clear reduction in uncertainty in both cases and at both orders.

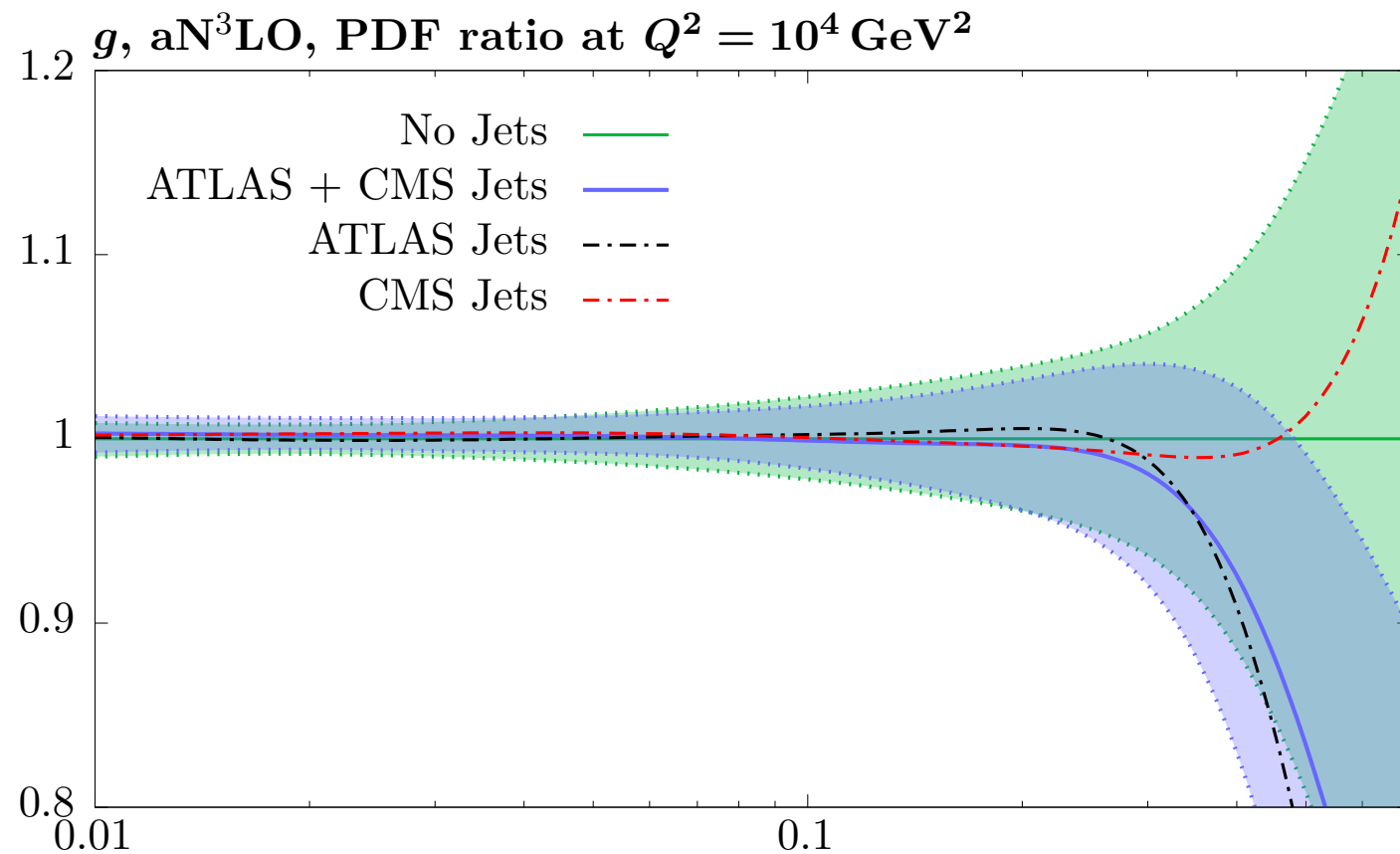
★ Marginally more significant for dijets.

★ Slightly less significant at aN3LO.

$g$ , PDF errors at  $Q^2 = 10^4 \text{ GeV}^2$

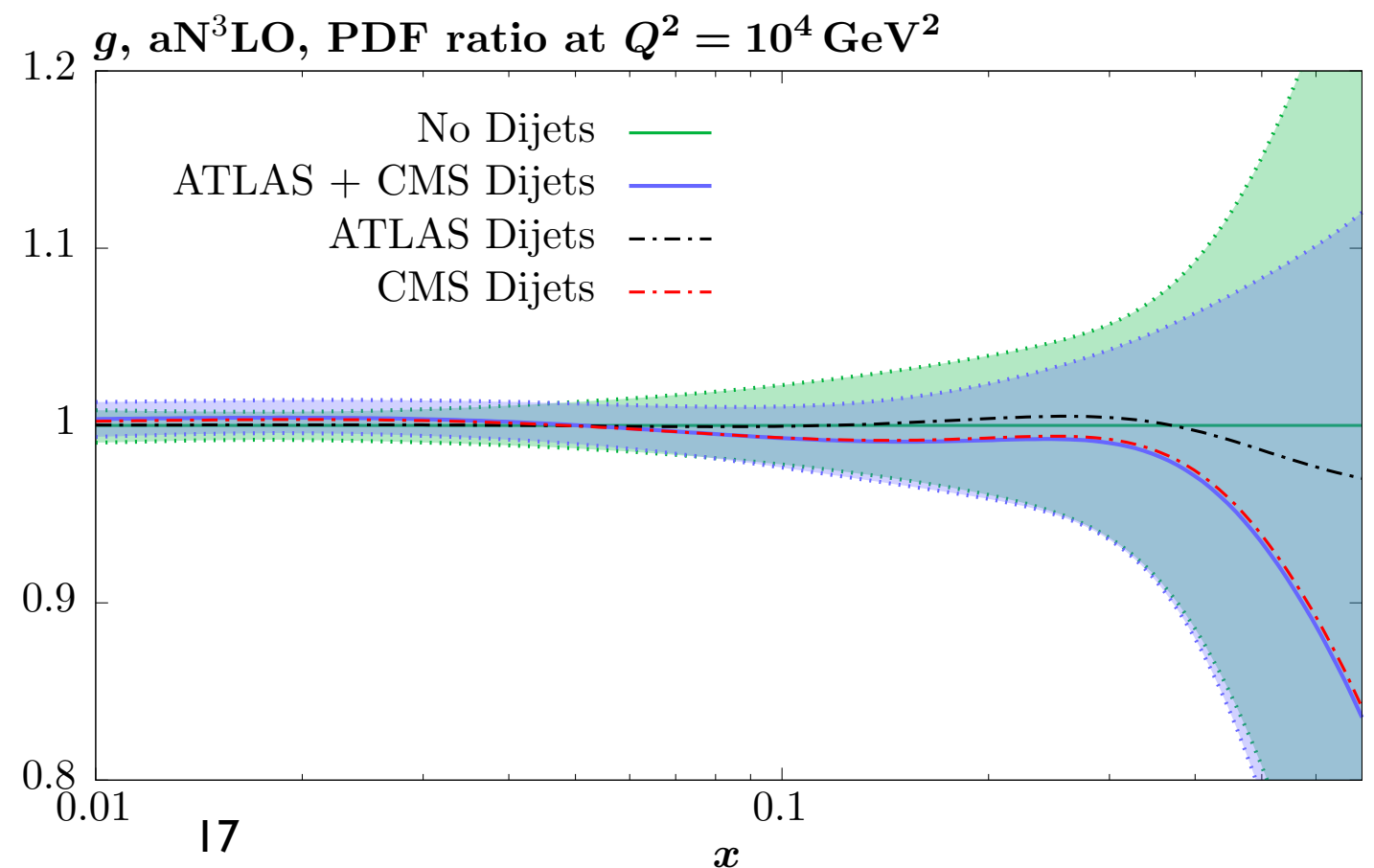


# Consistency within datasets



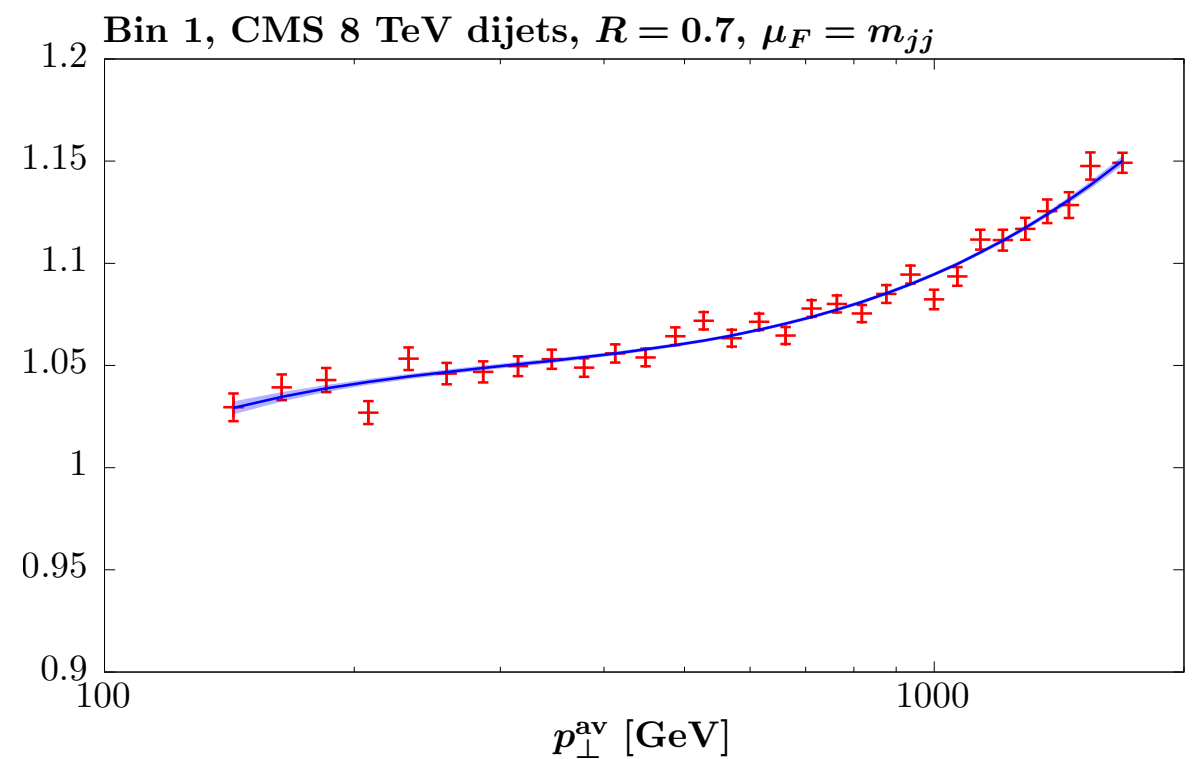
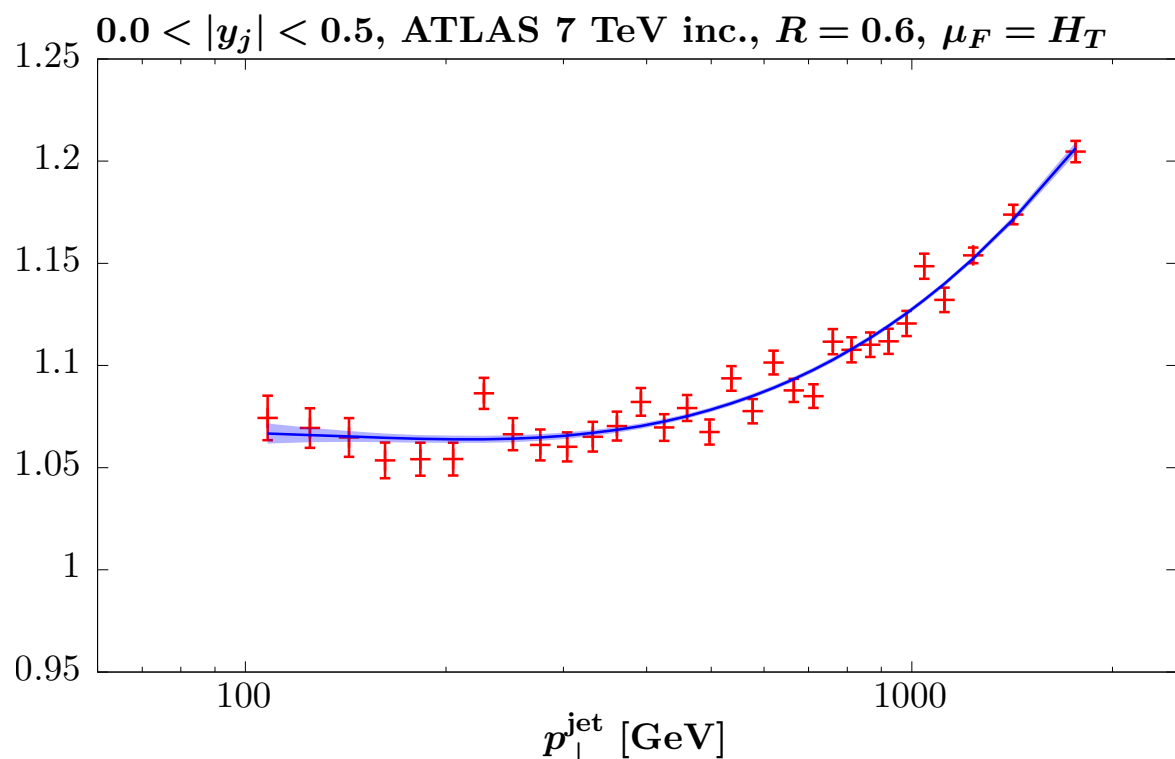
- At higher  $x$  clear difference between pulls of ATLAS and CMS (also seen in MSHT20).
- Final result compromise between these.

- Consistency between  $x$  CMS and ATLAS, but latter has very little impact alone.
- Again CMS 8 TeV driving fit.
- Again similar story at NNLO (not shown).



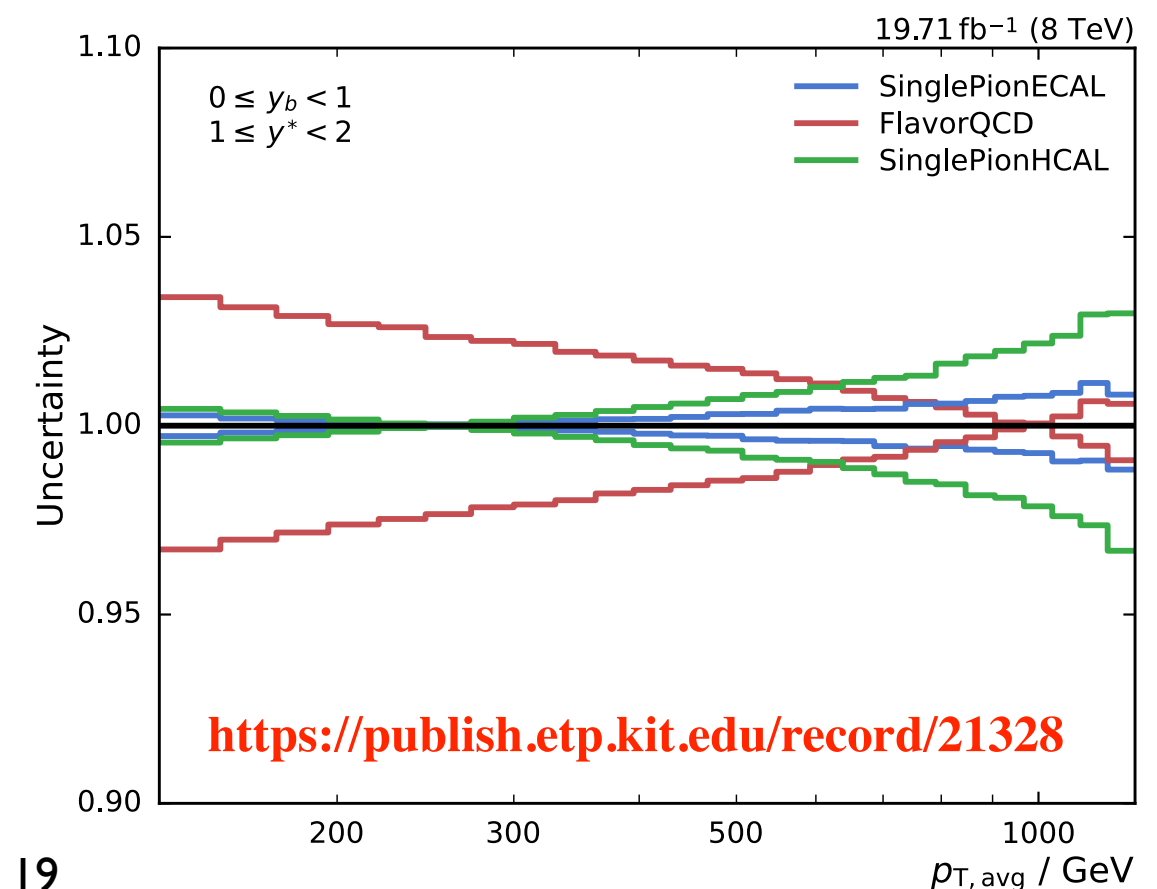
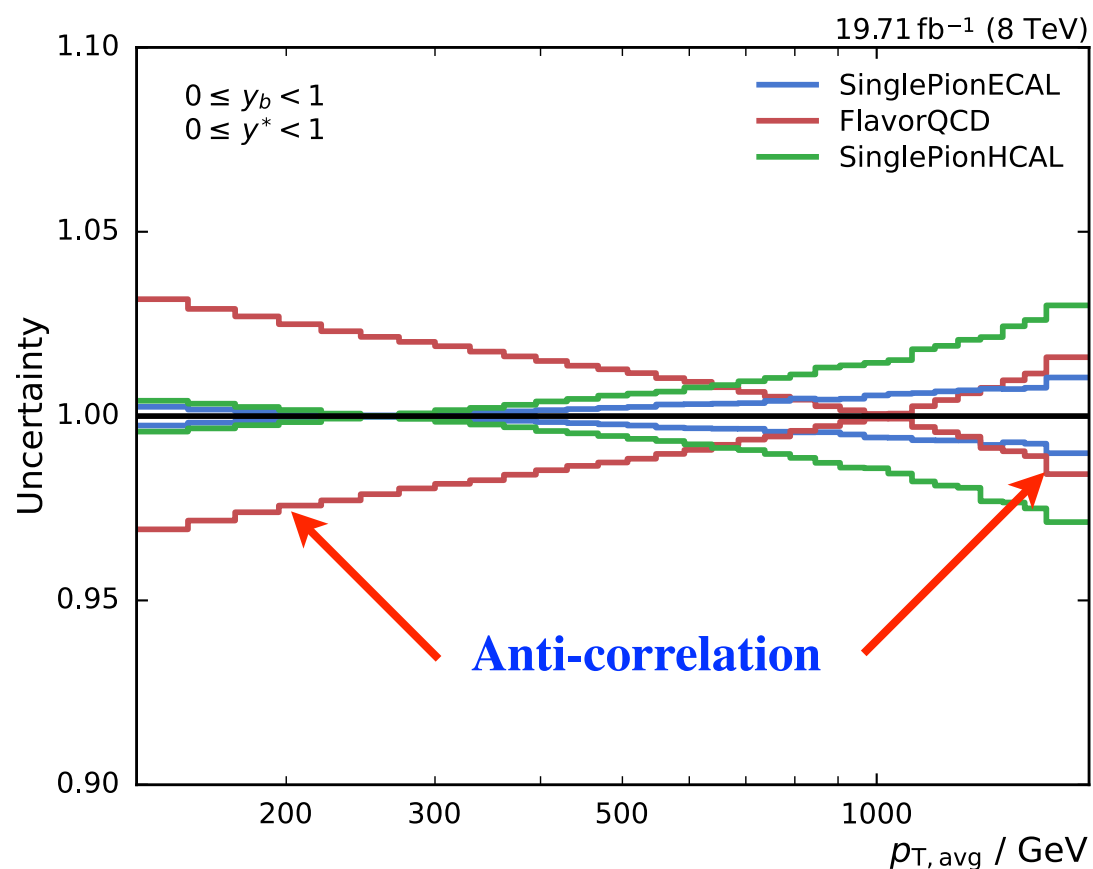
# Technical aside (1) - K-factors

- NNLO QCD corrections included via K-factors. MC uncertainties on these not negligible.
- We argue better to fit these to smooth functions. Can impact on fit quality at the  $\sim 0.1$ - $0.2$  per point level, though PDFs very stable.
- Provides cleaner idea of improvements from NLO to NNLO etc. Find that interpretation can be washed out somewhat otherwise.



# Technical aside (2) - CMS 8 dijets

- Systematic uncertainties related to jet calibration correlated across kinematic (rapidity/ $p_{\perp}$ ) space. Shape of these indicates anti-correlation between certain regions. However [hepdata](#) entries **entirely positive**.
- Through discussion with CMS colleagues have changed sign to more ‘natural’ (anti)-correlation.
- In the end this makes very little difference: improves  $\chi^2$  by  $\sim 1$ -2 points and gluon very stable. But more by chance than design.
- Detailed understanding/bookkeeping of systematic correlations key.

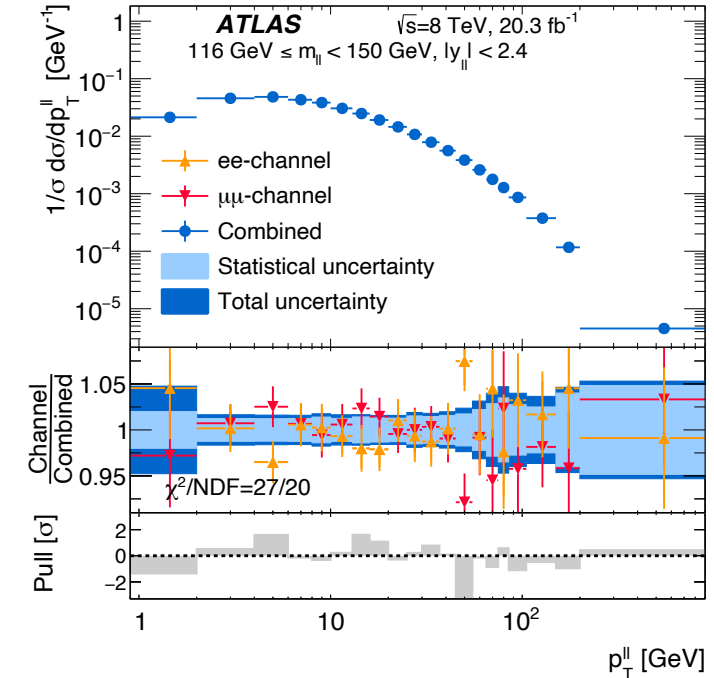
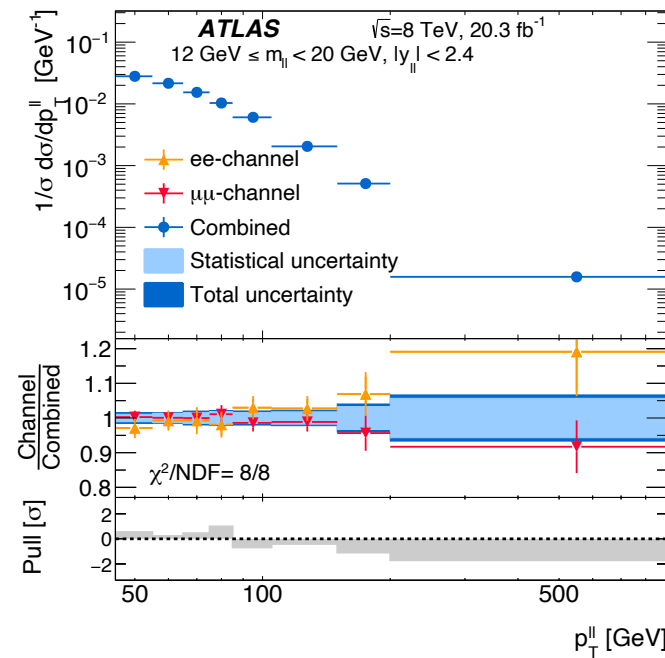


# **ATLAS $Z p_{\perp}$ data: a closer look**



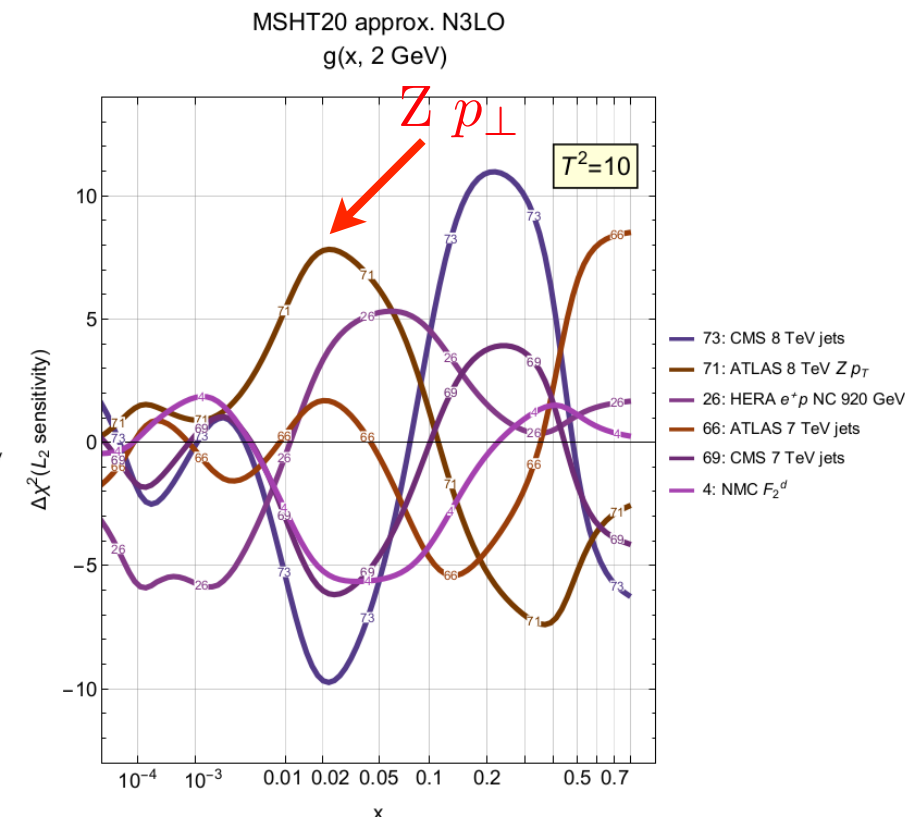
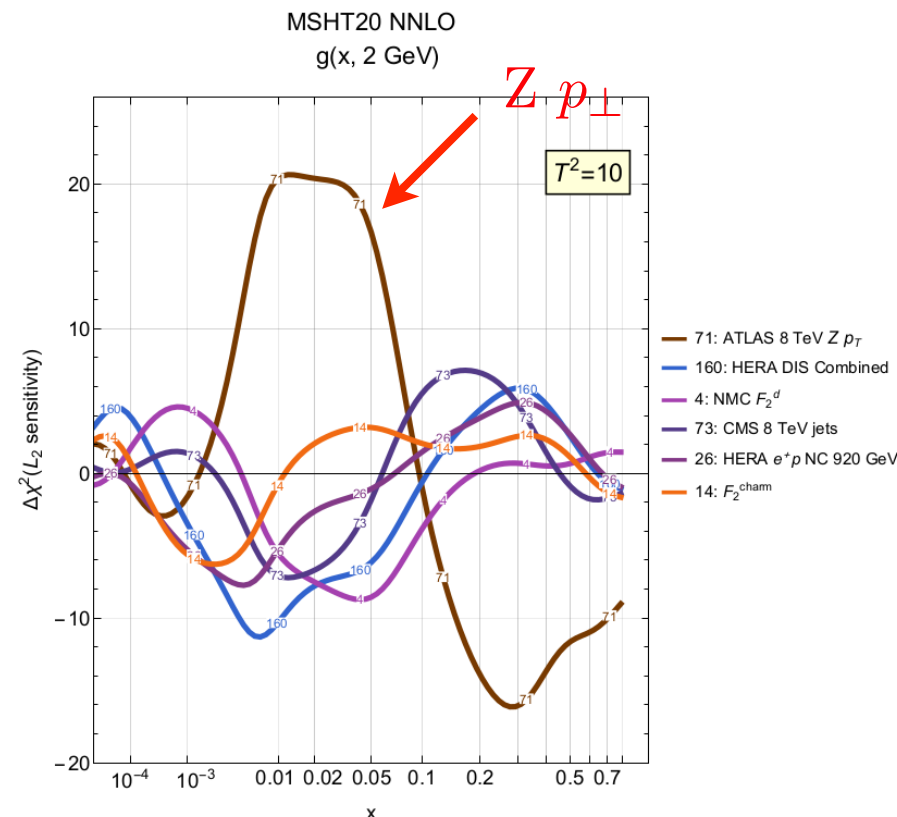
- ATLAS  $Z p_{\perp}$  (more properly dilepton  $p_{\perp}$ ) data presented double differentially in  $m_{ll}, p_{\perp}^{ll}$

$$12 < m_{ll} < 150 \text{ GeV} \quad p_{\perp}^{ll} > 30 \text{ GeV}$$



- Treatment of this dataset rather different between groups.
- Fit quality v. poor in default NNLO fit, with dramatic improvement at aN3LO (1.86 vs. 1.04), and highly sensitive to other data in fit (jets vs. dijets).

- Reduced **tension** at aN3LO also backed up by L2 sensitivities (reduced scale).



→ Worth revisiting, and considering impact of data selection/  
treatment.

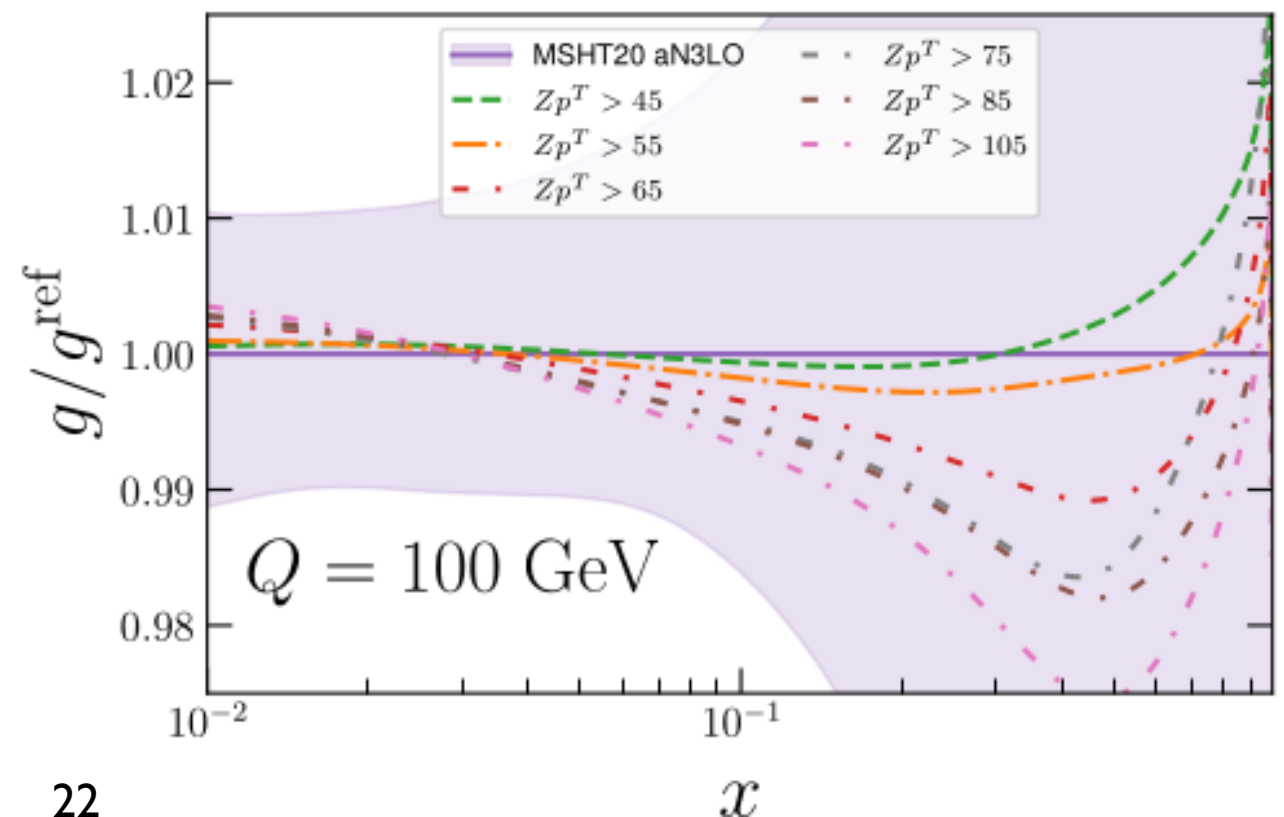
- **First step:** consider impact of raising  $p_{\perp}^{ll}$  cut.

$\chi^2/N_{pts}$

Order of fit/ $p_T^{cut}$ (GeV)	30 (default)	45	55	65	75	85	105
NNLO	1.86	1.68	1.67	1.42	1.39	1.42	1.21
aN3LO	1.04	0.95	1.01	0.84	0.86	0.87	0.81
$N_{pts}$	104	88	77	66	55	44	33

- Fit quality improves slowly as amount of data is reduced.
- Effect larger at **NNLO**, but **NNLO** always worse.

- No obvious sign of issue with particular  $p_{\perp}^{ll}$  region.
- Next steps: impact of  $m_{ll}$  selection, interplay with other datasets...

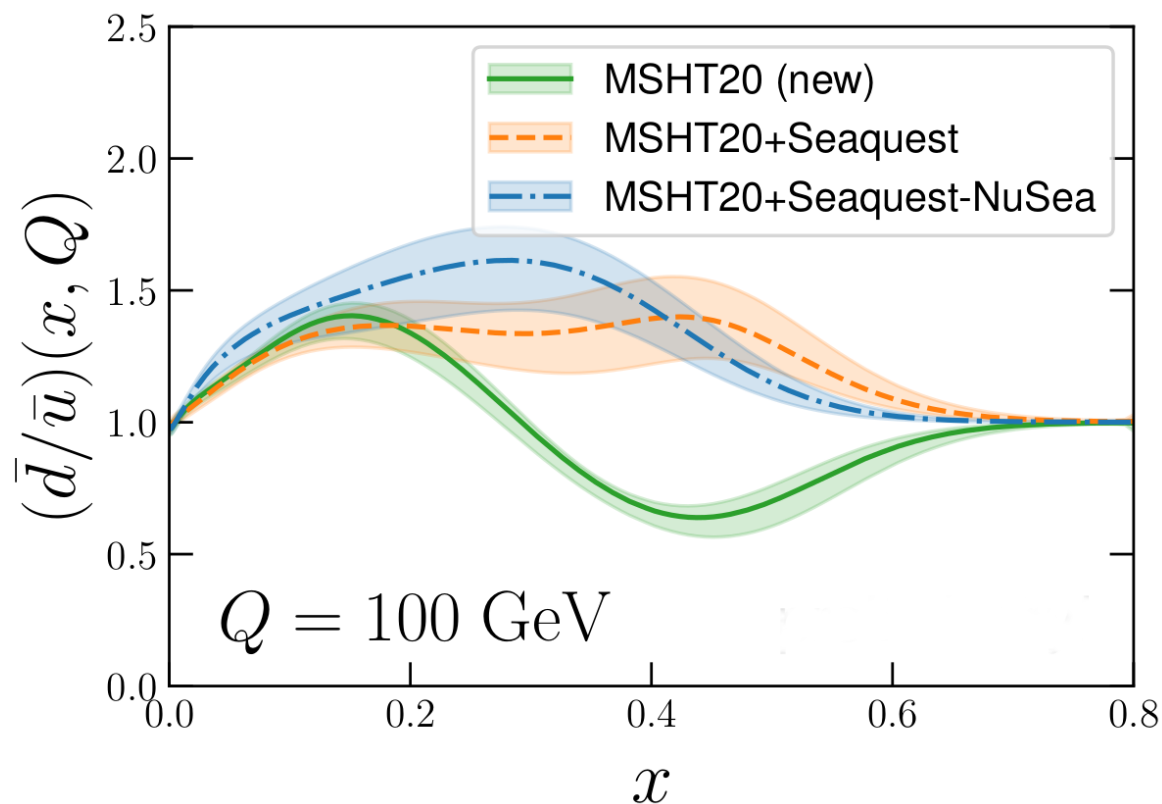


# Impact of SeaQuest data

# New data - Seaquest (NNLO)

Preliminary!

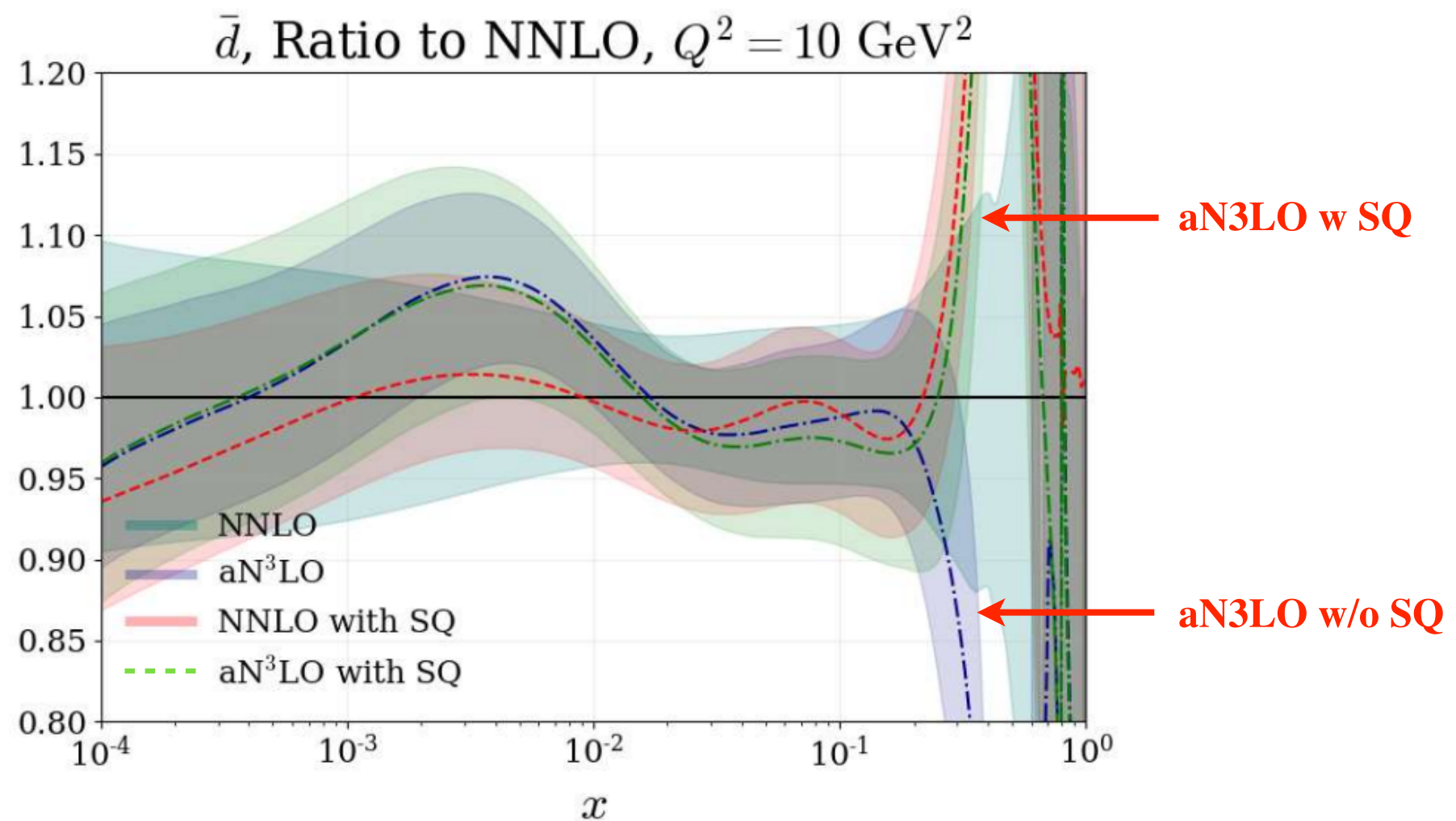
- Seaquest (E906) fixed target DY data - sensitivity to high  $x$   $q$ ,  $\bar{q}$ :  
 $\Rightarrow \sigma_D/\sigma_H \sim 1 + \bar{d}/\bar{u}$ . Direct measurement of  $\bar{d}/\bar{u}$  at high  $x$ .
- Various models for  $\bar{d}/\bar{u}$  at high  $x$ : Pauli blocking, pion cloud, etc.
- Previous questions of NuSea (E866) data preferring  $\bar{d} < \bar{u}$  at  $x \approx 0.4$ .
- Clearly raises high  $x$   $\bar{d}/\bar{u}$ . Tension with NuSea which pulls it down.



Dataset	$N_{\text{pts}}$	MSHT20	New
Seaquest	6	-	8.2
NuSea	15	9.8	19.0
Total (without Seaquest or NuSea)	4348	5102.3	5112.1

- NuSea  $\chi^2/N_{\text{pts}}$ :  $0.65 \rightarrow 1.27$ , when Seaquest added.
- Rest of data also worsens in  $\chi^2$  by 9 points, with 4.5 in E866 absolute DY (rather than ratio), 4.4 in NMC n/p, 4.3 in DØ  $W$  asymmetry.

- At aN3LO, the  $\bar{d}$  become negative above  $x \sim 0.5$  with a minimum at  $x \sim 0.6$ . Nonetheless remains positive within uncertainties.
- Like at NNLO, adding the Seaquest data raises the  $\bar{d}/\bar{u}$ .
- Adding Seaquest  $\Rightarrow$  NNLO and aN3LO  $\bar{d}$ ,  $\bar{u}$  again very similar.
- Effect on fit quality of adding Seaquest similar to NNLO,  $\Delta\chi^2 = +6$  in rest of data, NuSea  $\chi^2/N$  doubles from  $\sim 0.6$  to  $\sim 1.3$ .



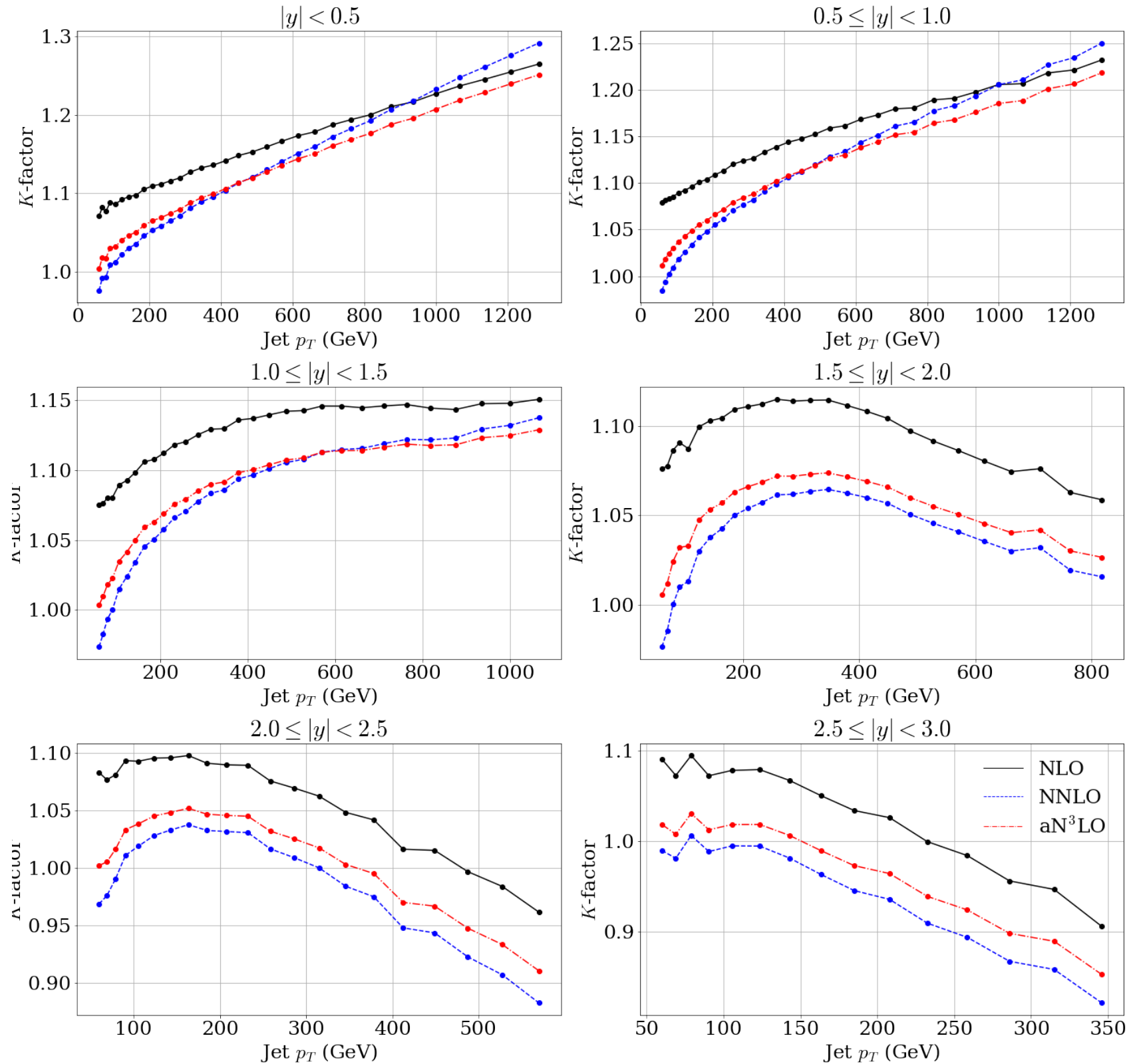
# Summary

- ★ MSHT group busy working on range of follow up studies, making use of NNLO and new aN3LO machinery.
- ★ Jets/Dijets:
  - Jet fit quality relatively poor, remains so in aN3LO fit.
  - Dijet fit quality good, and with improvement at aN3LO in line with expectations.
  - Scale choice does not play big role in inclusive, EW corrections make fit quality worse (!).
- ★ All indicates that dijet data may be preferable.
- ★ Working ongoing to understand these questions, and connected ones related to high  $x$  ( $Z p_{\perp}$ , Seaquest) at NNLO and aN3LO.

Thank you for listening!

# Backup

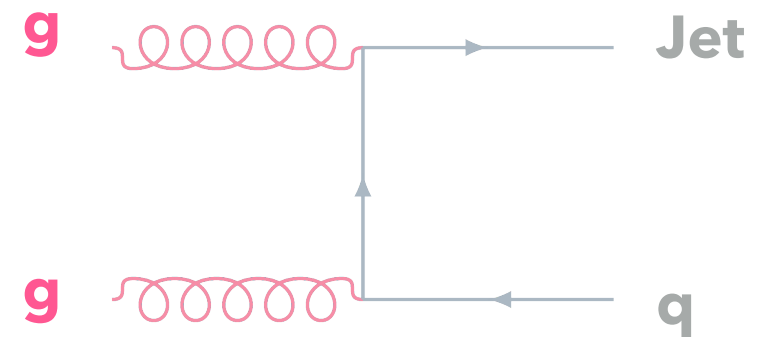
# Inclusive Jet K-factors





# Jet Kinematics: Inclusive

- Inclusive jets measured in terms of jet  $p_{\perp}$  and  $y_j$ .
- Schematically, **LO** relationship to high  $x$  parton:



$$x = \frac{p_{\perp}}{\sqrt{s}} (e^{y_j} + e^{y_{j'}})$$

Observed Jet  $j$  ( $y_j > 0$ )  
'Unobserved' Jet  $j'$

→ Need 3 kinematic inputs to uniquely determine  $x$ .

- Inclusive jets: effectively integrate over  $x \gtrsim \frac{p_{\perp}}{\sqrt{s}} e^{y_j}$ .
- So certainly sensitive to high  $x$  region, but washed out somewhat.

# Jet Kinematics: Dijets

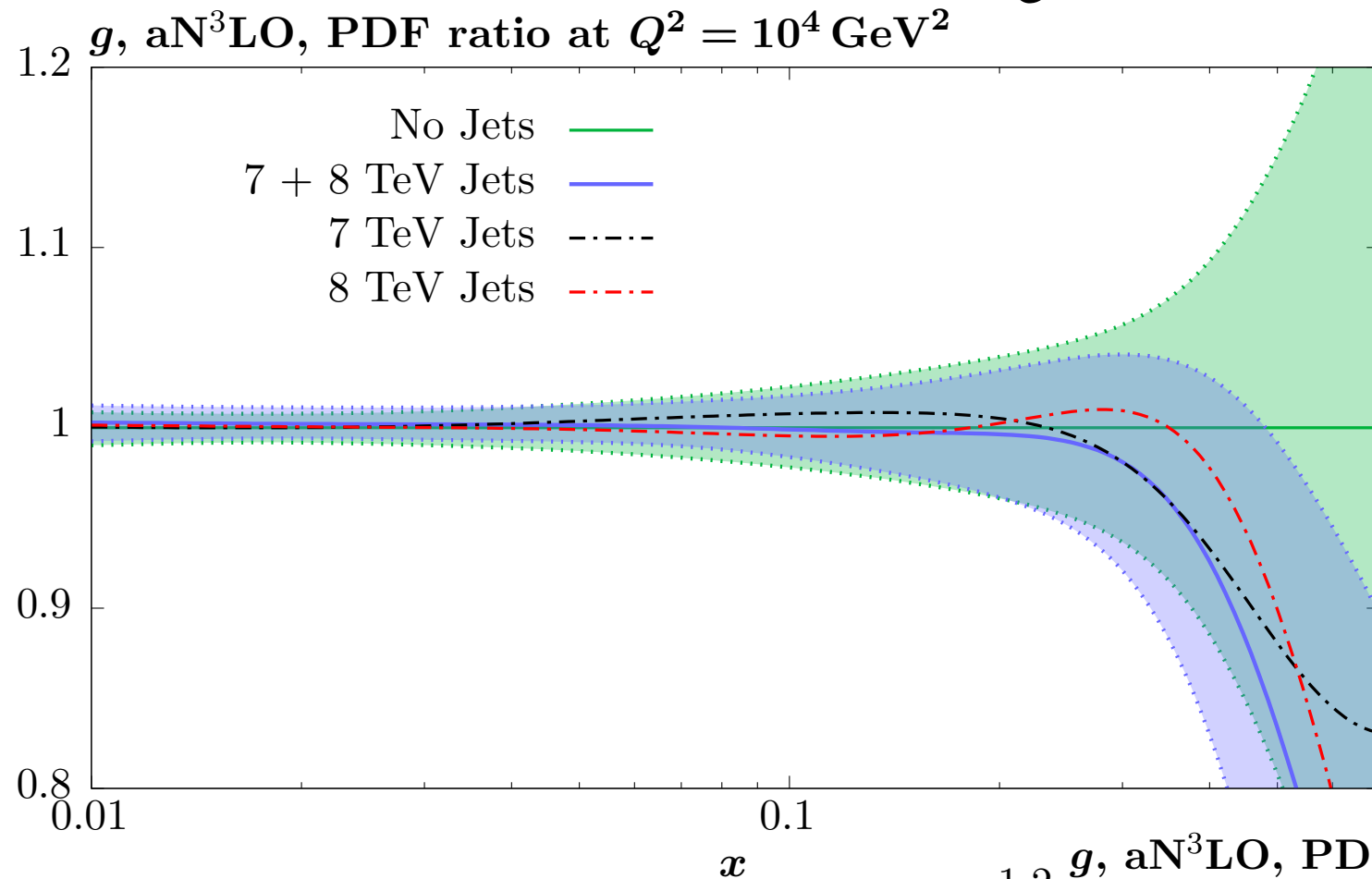
- For dijets, both jets measured. Same schematic **LO** relationship:

$$x_{1,2} = \frac{p_{\perp}}{\sqrt{s}} \left( e^{\pm y_j} + e^{\pm y_{j'}} \right)$$

- Double differential measurements in terms of  $m_{jj}$  and  $y^*/y_{\max}$  : not sufficient to uniquely pin down LO  $x$ .
- That is, some washing out (though precise effect depends on choice of variable).
- However, also possible to measure triple differentially - expect to provide stronger, more direct constraints.

$$d^3\sigma/dp_{\perp,avg}dy_bdy^*$$

# Consistency within datasets

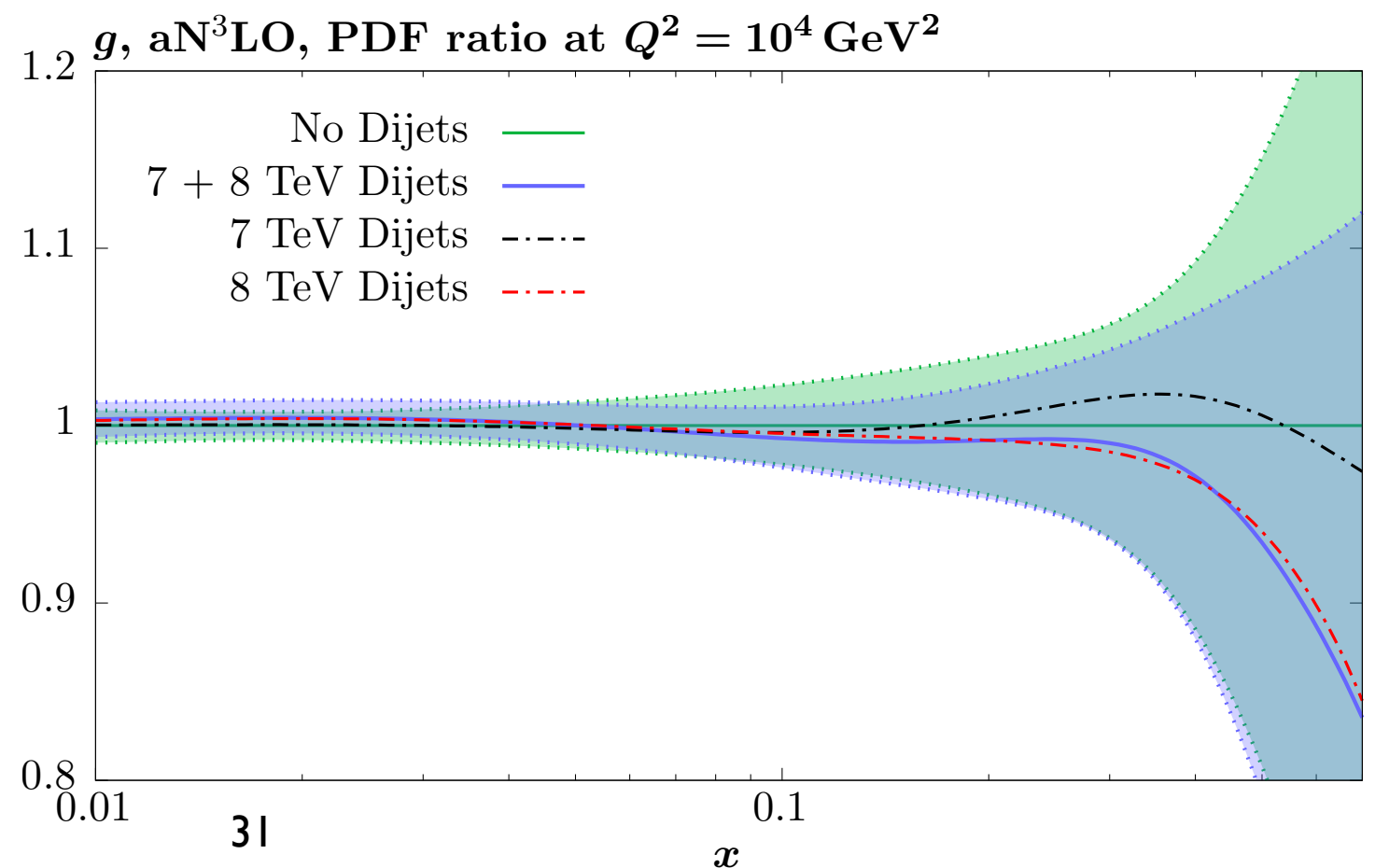


- 7 & 8 TeV data ~ consistent pulls inclusive jets.
- Similar for NNLO (not shown).

- 7 & 8 TeV data consistent for dijets, but this is due to broader result.

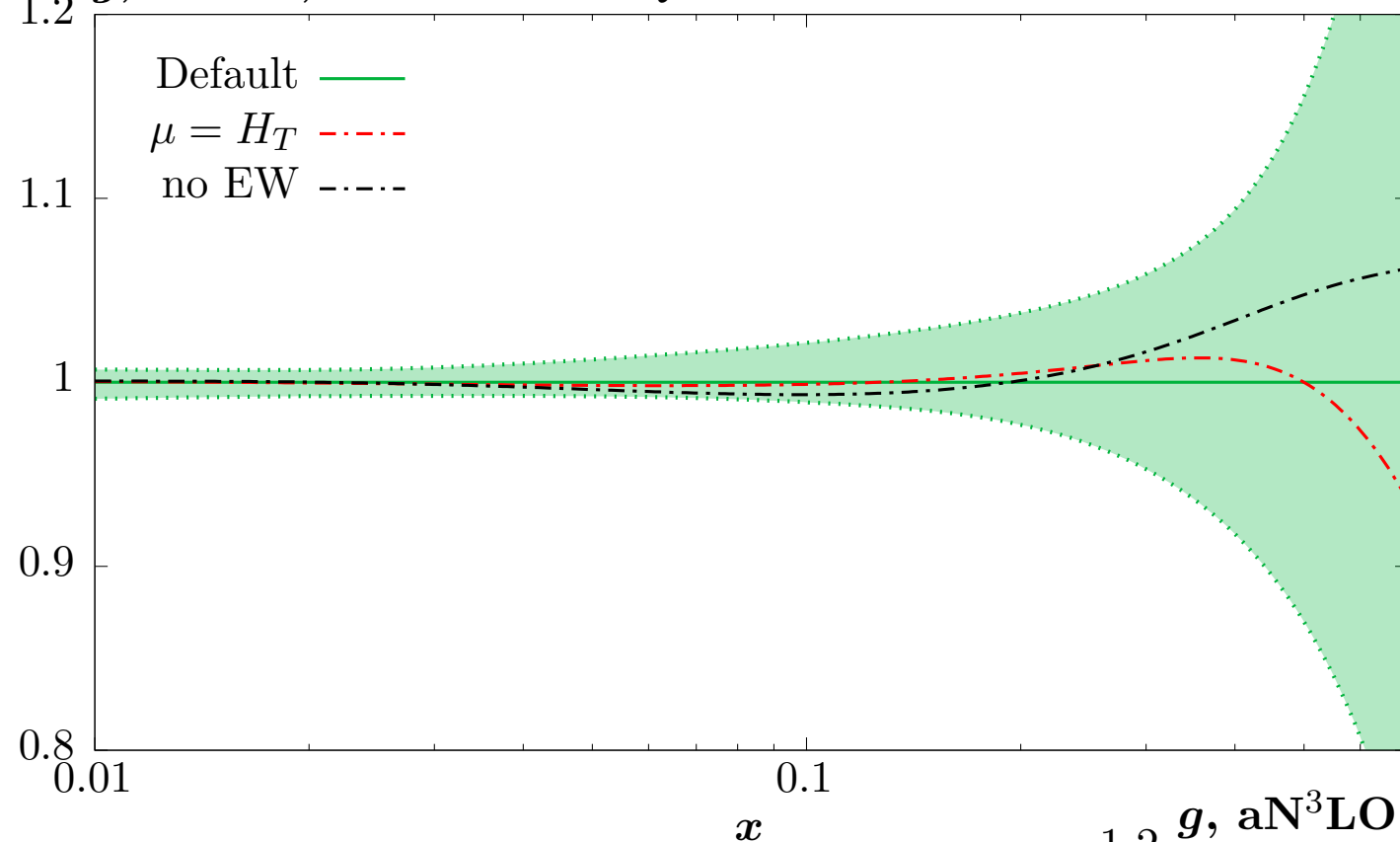
- All dijet fits completely driven by CMS 8 TeV data

- Similar for NNLO (not shown).



# PDFs: EW corrections/scale choice

$g$ , NNLO, PDF ratio at  $Q^2 = 10^4 \text{ GeV}^2$



★ Impact of these on gluon  
small, though not completely  
negligible.

$g$ , aN<sup>3</sup>LO, PDF ratio at  $Q^2 = 10^4 \text{ GeV}^2$

