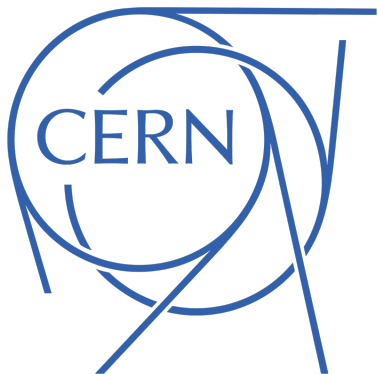


Future (possible) studies with the xFitter fitting framework

Francesco Giuli (on behalf of the xFitter Developers' team)

30th International Workshop on Deep Inelastic
Scattering and Related Topics (MSU, USA)

28/03/2023



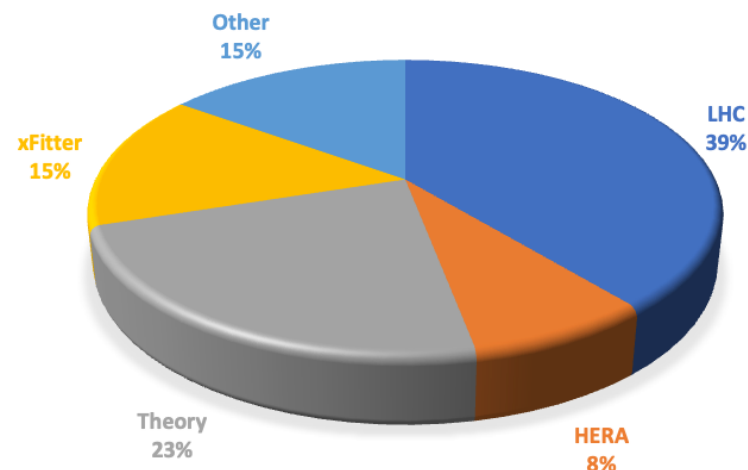
The xFitter Project

➤ The xFitter project (former HERAFitter) is a **unique open-source QCD fit framework**

➤ GitLab repository (open access)

➤ This code allows users to:

- **extract PDFs** from a large variety of data
- assess the **impact** of **new data on PDFs**
- check the **consistency** of experimental data
- test different **theoretical assumptions**



➤ Several active developers between experimentalists and theorists

➤ More than 100 publications obtained using xFitter since the beginning of the project

➤ List of recent analyses by the xFitter Developers' Team:

MORE IN PREPARATION!

Phys.Rev.D 104 (2021) 5, 056019,
arXiv:2105.11306

🌐 QCD analysis of pion fragmentation functions in the xFitter framework

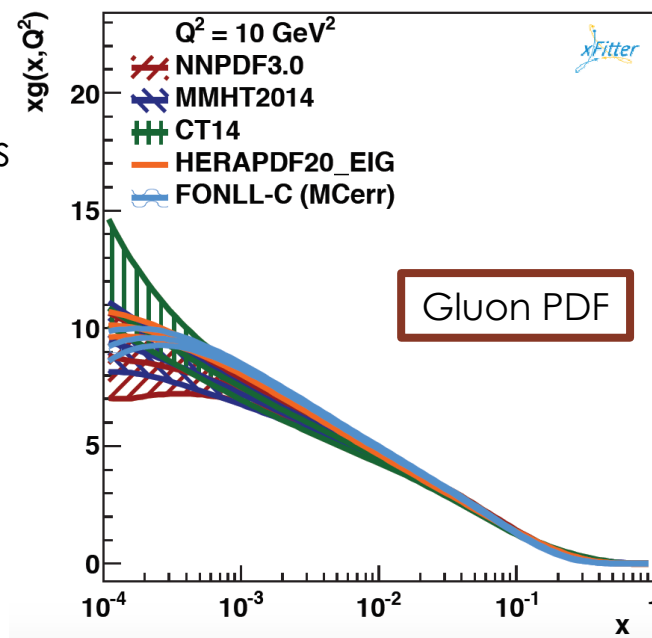
Phys.Rev.D 102 (2020) 1, 014040,
arXiv:2002.02902

🌐 Parton Distribution Functions of the Charged Pion Within The xFitter Framework

xFitter in a nutshell



- **Parametrise** PDFs at the initial scale:
 - several functional forms available
 - define PDF parameters to be minimised
- **Evolve** PDFs to the scales of the fitted data points:
 - DGLAP evolution up to NNLO in QCD and NLO QED (QCDNUM, APFEL, MELA)
 - non-DGLAP evolutions (dipole, CCFM)
- **Compute** predictions for the data points:
 - several mass schemes available in DIS (ZM-VFNS, ACOT, FONLL, TR, FFNS)
 - predictions for hadron-collider data through fast interfaces (APPLgrid, FastNLO)
- **Comparison data-predictions** via χ^2 :
 - multiple definitions available
 - consistent treatment of the systematic uncertainties
- **Minimise** the χ^2 w.r.t. the fitted parameters
 - using MINUIT or by Bayesian reweighting
- **Useful drawing tools** – nice and colorful plots
- Last xFitter workshop in Orsay (9-11 March 2022)



xFitter release 2.2.0



xFitter

Sample data files:

LHC: ATLAS, CMS, LHCb

Tevatron: CDF, D0

HERA: H1, ZEUS, Combined

Fixed Target: ...

User Supplied: ...

GitLab

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Releases of the xFitter QCD analysis package

- The release notes can be found in this attachment: [xFitter_release_notes.pdf](#).
- Installation script for xFitter together with QCDNUM, APFEL, APPLGRID, LHAPDF [install-xFitter-2.0.1](#)
 - New installation script from master branch [install-xfitter-master](#)
- Data and theory files can be downloaded from gitlab [gitlab data repository](#)

Date	Version	Files	Remarks
 03/2022	2.2.0 FutureFreeze	xfitter-2.2.0.tgz	Major update of evolution and reaction interfaces
 05/2019	2.0.1 OldFashioned	xfitter-2.0.1.tgz	update/bug fix to 2.0.0 FrozenFrog
 03/2017	2.0.0 FrozenFrog	xfitter-2.0.0.tgz	stable release with decoupled data and theory files



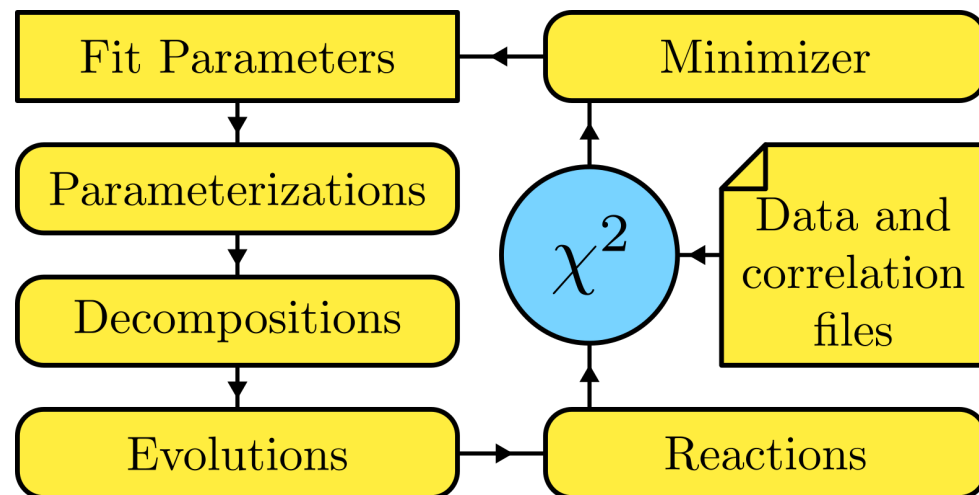
**2.2.0
Future Freeze**

<https://www.xfitter.org/xFitter/xFitter/DownloadPage>

- Release 2.2.0 released! (major update of evolution and reaction interfaces)
- Script to install xFitter and all its dependencies: **install-xFitter**

Talking about the new release...

- **Significant changes** in the internal structure
- **Re-written interfaces** to minimizers, PDF parameterisation, decomposition, evolution and theory reactions
- **Large changes in the user interface**
- Data handling, format and χ^2 calculation remain largely the same (but there are changes)
- Nicely summarized in this [talk](#) by S. Glazov
- Picture taken from Ivan Novikov's [talk](#)



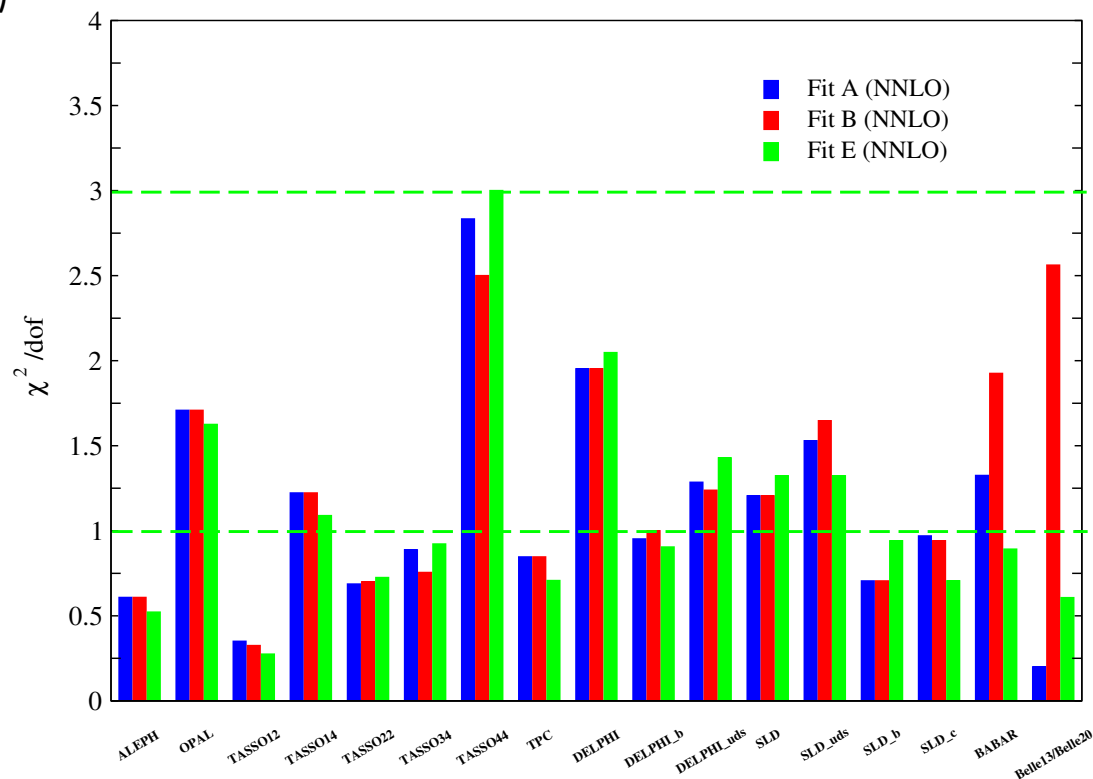
Pion Fragmentation Functions

[PRD 104 \(2021\) 5 056019](#)

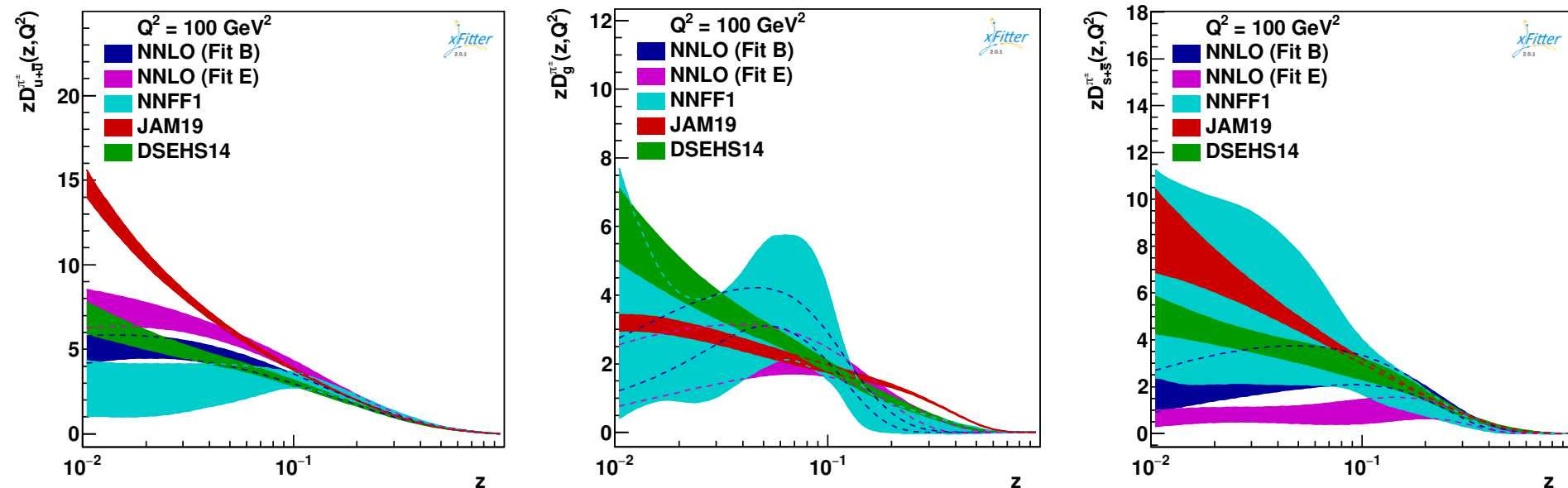
- To perform the extraction of **pion fragmentation functions** (FFs) from single inclusive electron-positron annihilation (SIA) + BELLE13/20 data
- SIA $e^+e^- \xrightarrow{\gamma^*, Z} \pi^\pm X$ data allow to separate Δq and $\Delta \bar{q}$
- **Parametrization form:**
$$D_i^{\pi^\pm}(z, Q_0) = \frac{\mathcal{N}_i z^{\alpha_i} (1-z)^{\beta_i} [1 + \gamma_i (1-z)^{\delta_i}]}{B[2+\alpha_i, \beta_i+1] + \gamma_i B[2+\alpha_i, \beta_i+\delta_i+1]}$$
- We assume isospin symmetry $D_u^{\pi^+} = D_{\bar{d}}^{\pi^-}$ and $D_{\bar{u}}^{\pi^+} = D_d^{\pi^-}$
- We assume the charge conjugate $D_i^{\pi^+} = D_i^{\pi^-}$ for all the flavour component
- We fit the flavour combinations $i = u^+, d^+, s^+, c^+, b^+$ and g
- We parametrise FFs at a starting scale of $Q_0^2 = 5 \text{ GeV}^2$
- **19 free parameters in total**
- Fitted distributions: $\frac{d\sigma^h}{dz}, \frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}, \frac{s}{\beta} \frac{d\sigma^h}{dz}, \frac{1}{\beta\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}, \dots$ ($\mathbf{z} = 2E_h/\sqrt{s}$)

Pion Fragmentation Functions

- Several fits ran:
 - **Fit A** focuses on the impact of BELLE13 data (no BELLE20 data)
 - **Fit B** focuses on the impact of BELLE20 data (no BELLE13 data)
 - **Fit C** focuses on the impact of BELLE20 data without BaBar set (no BELLE13 data)
 - **Fit D** focuses on the impact of low-z BELLE20 data (No BELLE13 and BaBar data) – $z > 0.2$
 - **Fit E** focuses on the impact of low-z BELLE20 and BaBar data (no BELLE 13 data) – $z > 0.2$ (BELLE20) and $z > 0.1$ (BaBar)
- The inclusion of higher-order QCD corrections noticeably improves the quality of our fits
- Fits performed with enhanced tolerance $T = \sqrt{\Delta\chi^2} = 20$
- FFS NLO and NNLO uncertainty bands overlap \rightarrow perturbative uncertainties are under control (and reasonable choice of T)



Pion Fragmentation Functions



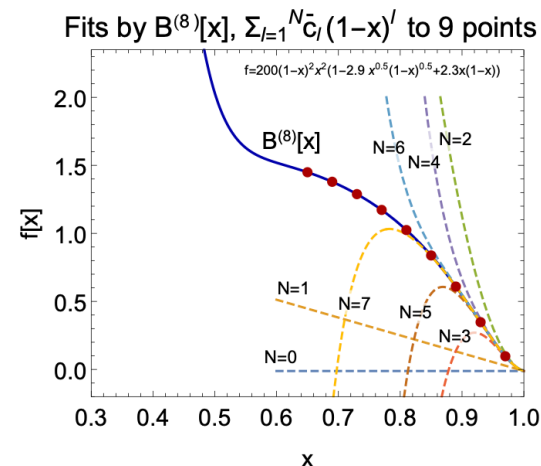
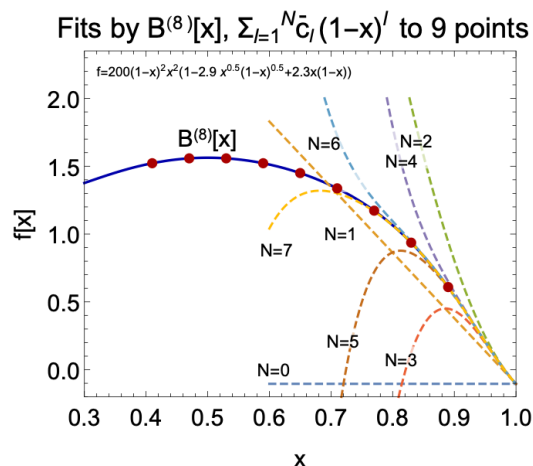
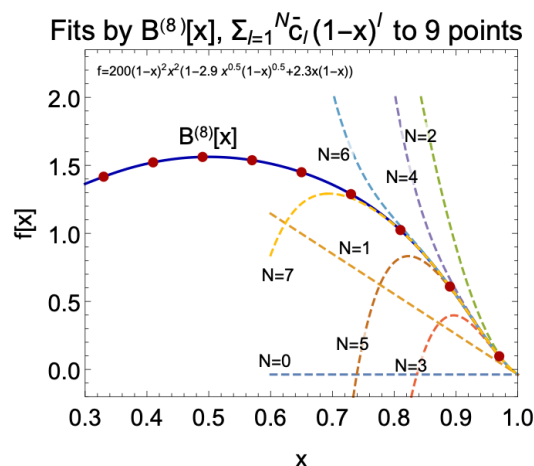
- Comparison with NNLO NNFF1 and NLO JAM19 and DSEHS14
- **Generally compatible with NNFF1 and DSEHS14 at larger z** , but they differ at low- z (more pronounced for Fit E)
- The **gluon** is generally **compatible with NNFF1** (larger uncertainties)
- FFs generally have a different behaviour as compared to JAM19 – they have much steeper slope at low- z for quarks, with the gluon lying above our curves for intermediate- to larger- z

More on mesons PDF

- Charged pion PDF studied in [PRD 102 \(2020\) 014040](#)

$$xv(x) = A_v x^{B_v} (1-x)^{C_v} (1 + D_v x^{\frac{5}{2}}), \quad \mathbf{C_v \sim 1} \text{ (but some theories predict } C_v \sim 2)$$

- It is not possible to uniquely determine the exact $(1-x)$ -exponent given the present data – [A. Courtoy, P. Nadolsky](#)



Main idea: **New parameterization methods for mesons PDF fits**

The new modular xFitter 2.2 version was a HUGE help for this project

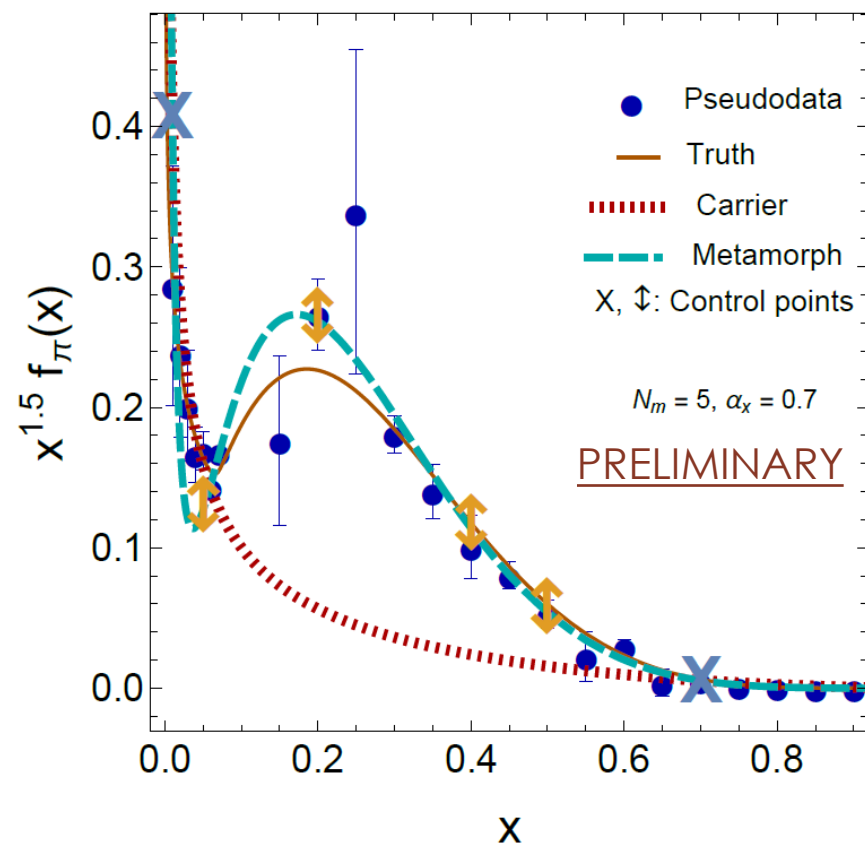
Fantômas4QCD: advanced polynomial parametrisations

L. Kotz, M. Chavez, A. Courtoy, P. Nadolsky, F. Olness, V. Purohit, 2023

Parametrize PDFs using **Bézier curves** $B^{(n)}(x; a) = \sum_{k=0}^n a_{k+2} \binom{n}{k} x^k (1-x)^{n-k}$

A metamorph $f(x) \equiv \underbrace{a_0 x^{a_1} (1-x)^{a_2}}_{\text{carrier}} B^{(n)}(x^{\alpha_x}; a)$

- Metamorphs can mimic a variety of behaviors of PDFs and their uncertainties. A versatile alternative to neural networks!
- The shape of a metamorph is computed from function values at user-specified **control points**
- The carrier component controls asymptotic limits at $x \rightarrow 0$ and $x \rightarrow 1$
- [L. Kotz's talk](#) for more details (WG1)



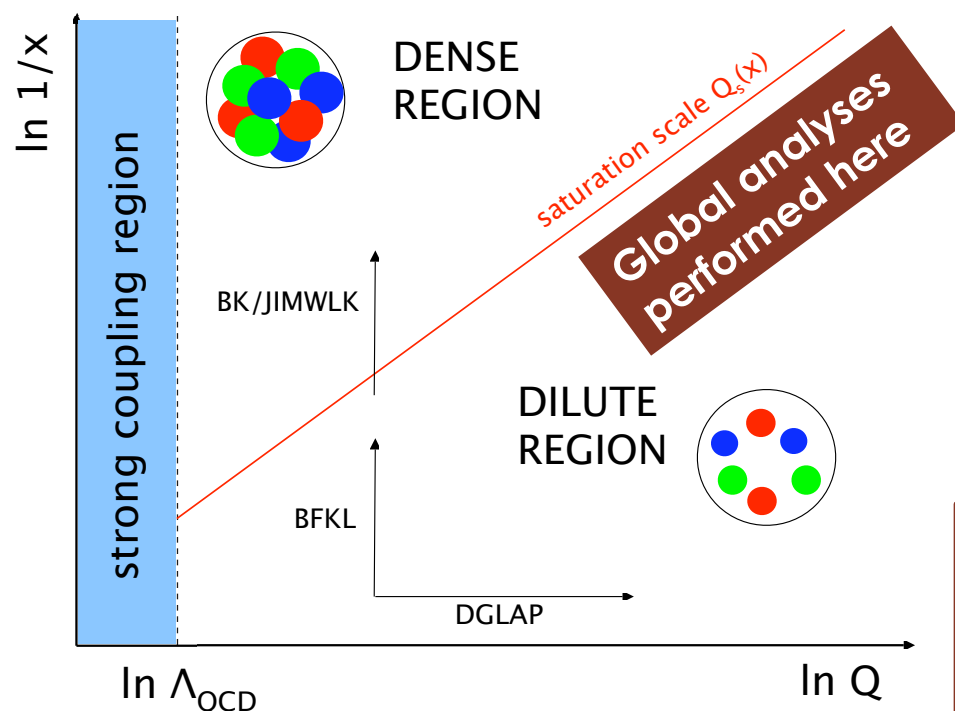
xFitter usage in the HEP community

- xFitter is the **tool of choice for PDF/QCD analyses by the LHC Collaborations**
- **ATLAS:**
 - PDF fit from diverse ATLAS data at $\sqrt{s} = 7, 8$ and 13 TeV - [EPJC 82 \(2022\) 5 438](#)
- **Drell-Yan phenomenology:**
 - PDF impact of A_{FB} in NC Drell-Yan events - [JHEP 10 \(2019\) 176](#)
 - PDF sensitivity of the longitudinal Z-boson polarisation - [Phys.Lett.B 821 \(2021\) 136613](#)
 - PDF sensitivity to A_{FB} and A_W in Drell-Yan for Precision EW Measurements and New Physics Searches - [Nucl.Phys.B 968 \(2021\) 115444](#)
 - Enhancing the LHC sensitivity to broad W'/Z' resonances of new gauge sectors - [JHEP 02 \(2022\) 179](#), [2211.06188](#)
- Important contribution in **several ongoing activities of the LHC EW WG:**
 - **Correlations between different PDFs** through pseudo-data fits
 - ATLAS/CMS/LHCb $\sin^2 \theta_{eff}^l$ **pseudo data** and combination exercise
 - Tevatron/ATLAS (and in future LHCb and CMS) m_W **combination**
- α_s **extraction** from Z boson transverse momentum distribution - [2203.05394](#), [ATLAS-CONF-2023-015](#)

xFitter and EIC

➤ Exploring QCD in extreme limits

➤ SURGE collaboration



➤ Current PDF analyses use "standard" DGLAP

➤ Extend analyses into extreme limits of QCD

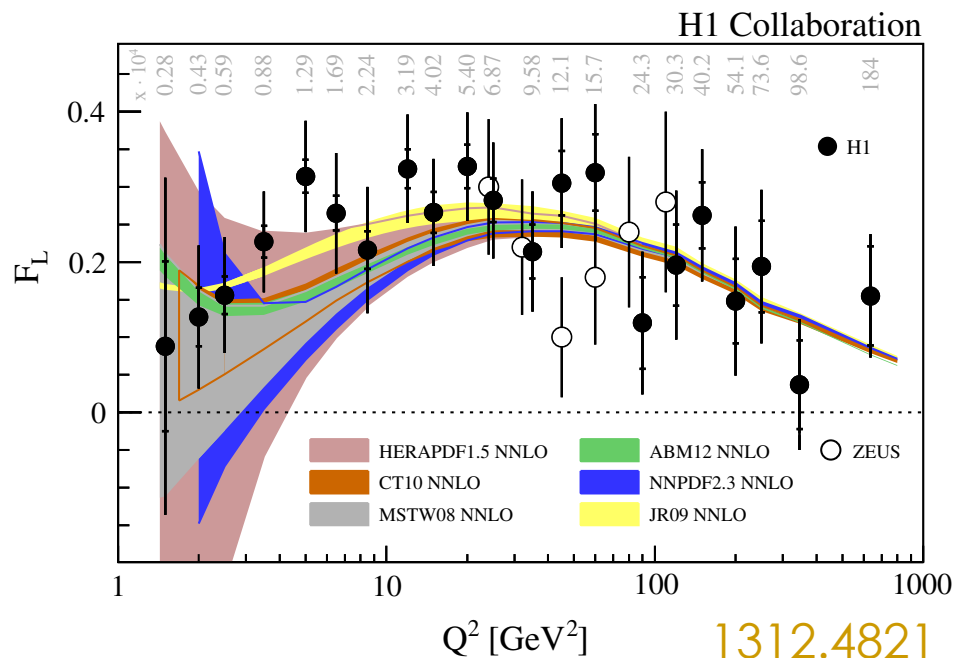
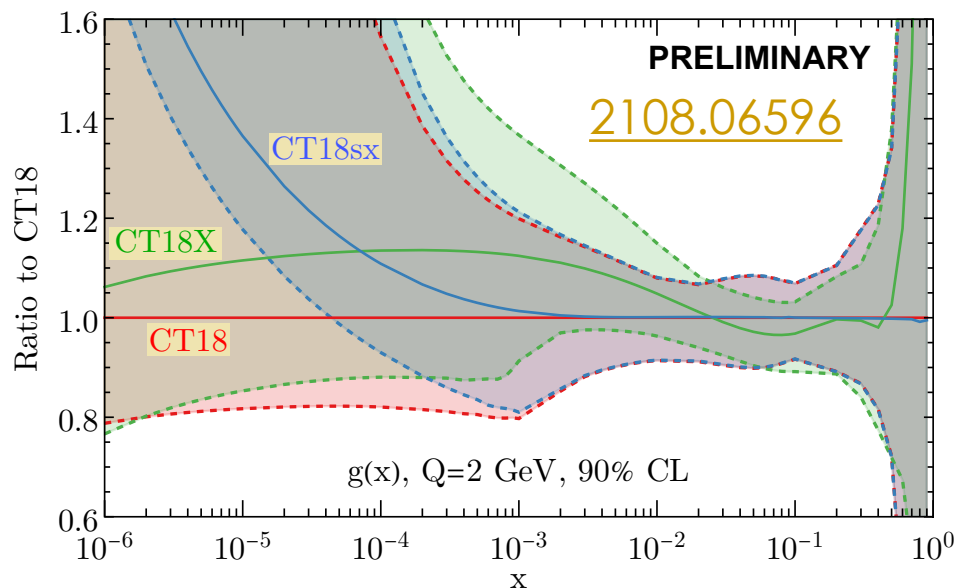
➤ Include additional effects into PDF fits

➤ This can all be done with xFitter! Thanks to its modular framework

To unequivocally:

- establish **saturation**
- perform **comprehensive global analysis** minimizing uncertainties
- extracting universal building blocks of **high energy factorization**

xFitter and EIC



Gluon PDF:

- Differences: DGLAP, BFKL, saturation
- Different $\{x, Q^2, A\}$ dependence
- Large uncertainties: EIC can improve

Longitudinal Structure Function F_L :

- Current theory is challenged
- Gluon strongly influences F_L
- Older xFitter-based analyses: small-x resummation, dipole and tensor pomeron models
- Large uncertainties: EIC can improve

Conclusion & outlook

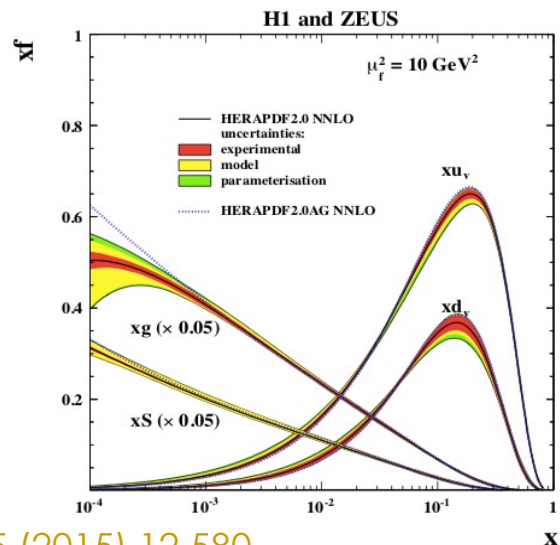
- The xFitter project (former HERAFitter) is a **unique open-source QCD fit framework**
- With its flexibility and modular structure, easy to use – **Future Freeze 2.2.0** out!
- **Improved user interface** for more flexible PDF parametrisation and adding new processes, QCD + EW fits, (SM)EFT interpretation, etc.
- Interfaced with APFEL/[APFEL++](#) → TMD phenomenology and FO predictions matched to small- q_T resummed calculations (SIDIS)
- NNLO grids can be used in xFitter → consistent set of predictions - [APPLfast](#)
- **Foreseen future physics** (low-x phenomenology, nuclear PDF, FFs, etc.)
- Fits of PDFs with resummation scale variations - [2202.03380](#)
- Heavy flavour and quarkonia production ([HEFTY Collaboration](#))
- Nice [summary](#) of xFitter capabilities submitted to Snowmass

Backup Slides



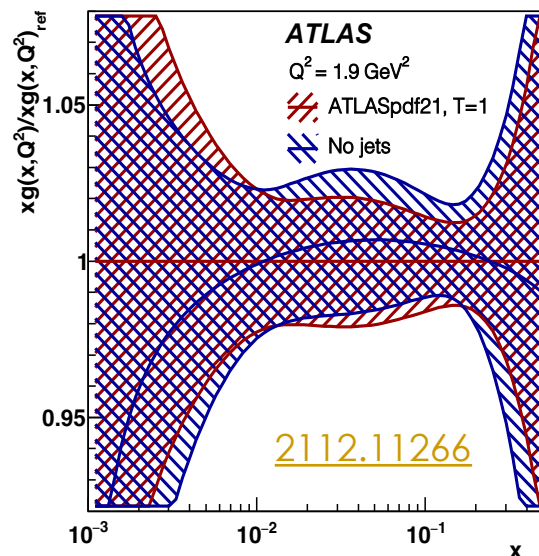
Results obtained with xFitter

DIS inclusive processes (ep)



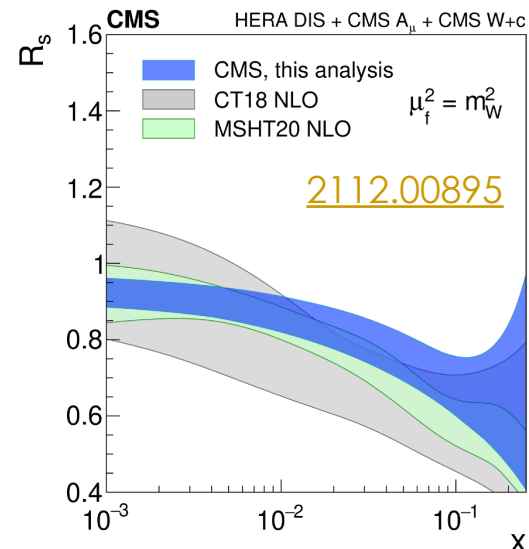
[EPJC 75 \(2015\) 12 580](#)

Jet production ($ep, pp, p\bar{p}$)



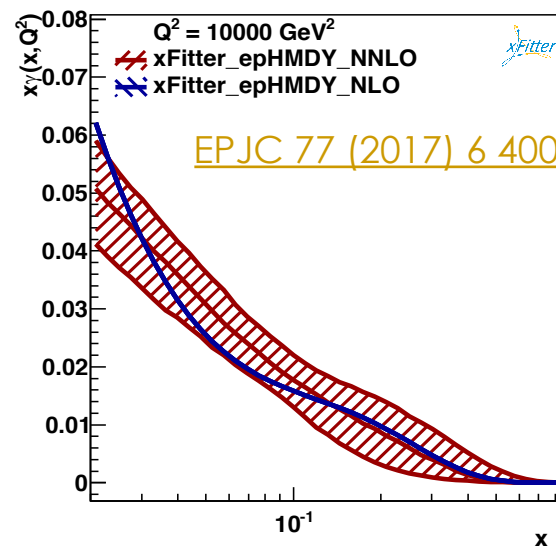
[2112.11266](#)

Drell-Yan processes ($pp, p\bar{p}$)



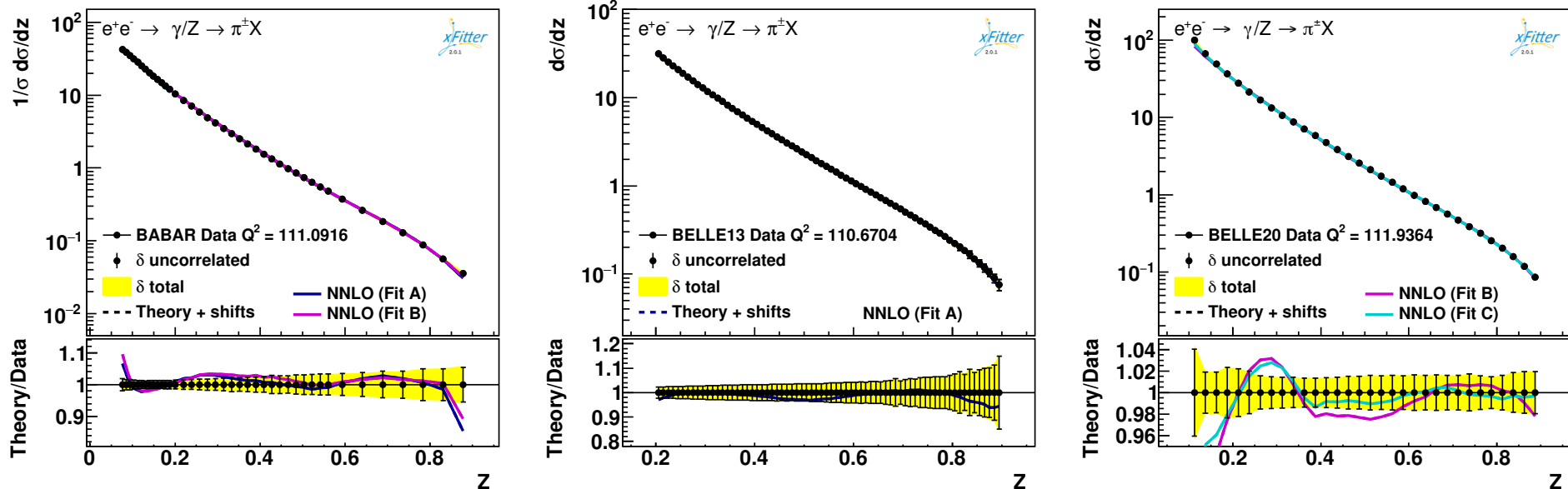
[2112.00895](#)

DY data sensitivity to photon PDF



[EPJC 77 \(2017\) 6 400](#)

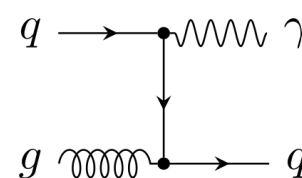
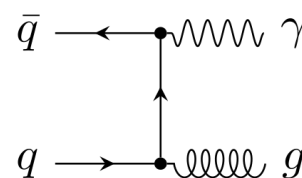
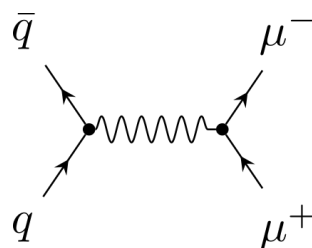
Pion Fragmentation Functions



- Theoretical predictions entirely consistent with the experimental data – partly due to larger uncertainties (BELLE13)
- Fits yield a **good description of the data** with the exception of the low- z region (BELLE20 and BaBar)
- **BELLE and BaBar** data sets appear to pull the fit in **opposite directions** - χ^2 (Fit B) for BELLE20 is 82/32 vs χ^2 (Fit C) for BELLE20 is 32/32
- The effect of excluding low- z data is dramatic - $\chi^2/\text{dof} \sim 1.2$ (similar cuts applied in JAM19)

Charged Pion PDF

- Pion structure is poorly studied experimentally [PRD 102 \(2020\) 014040](#)
- Currently available pion PDF sets in LHAPDF6 are provided without error bands
- Data from **E615**, **NA10** and **WA70** experiments (di-muon and direct photon production)
- Charge symmetry $d = \bar{u}$ and SU(3)-symmetric sea $u = \bar{d} = s = \bar{s}$ at the initial scale $Q_0^2 = 1.9 \text{ GeV}^2$



$$v := (d - \bar{d}) - (u - \bar{u}),$$

$$S := 2u + 2\bar{d} + s + \bar{s} = 6u,$$

$$g := g,$$

$$xv(x) = A_v x^{B_v} (1-x)^{C_v} (1 + D_v x^{\frac{5}{2}}),$$

$$xs(x) = A_S x^{B_S} (1-x)^{C_S},$$

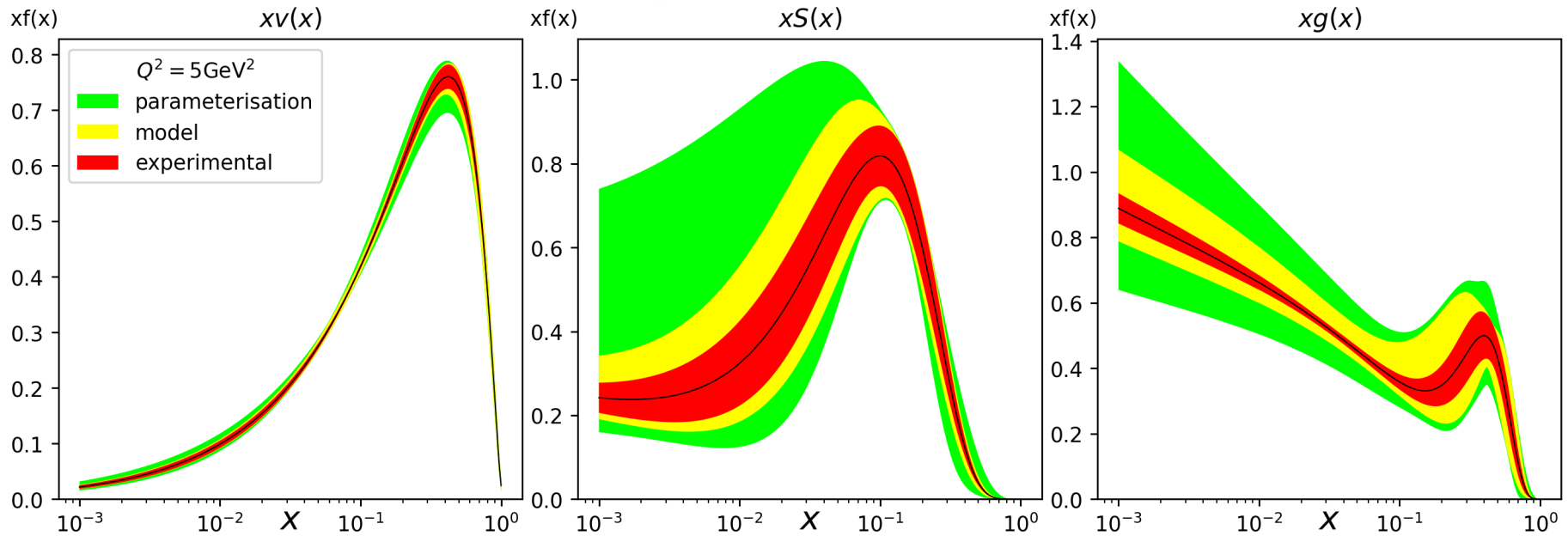
$$xg(x) = A_g x^{B_g} (1-x)^{C_g}.$$

- The A_v and A_g parameters are determined by the sum rules:

$$\int_0^1 v(x) dx = 2,$$

$$\int_0^1 x(v(x) + S(x) + g(x)) dx = 1$$

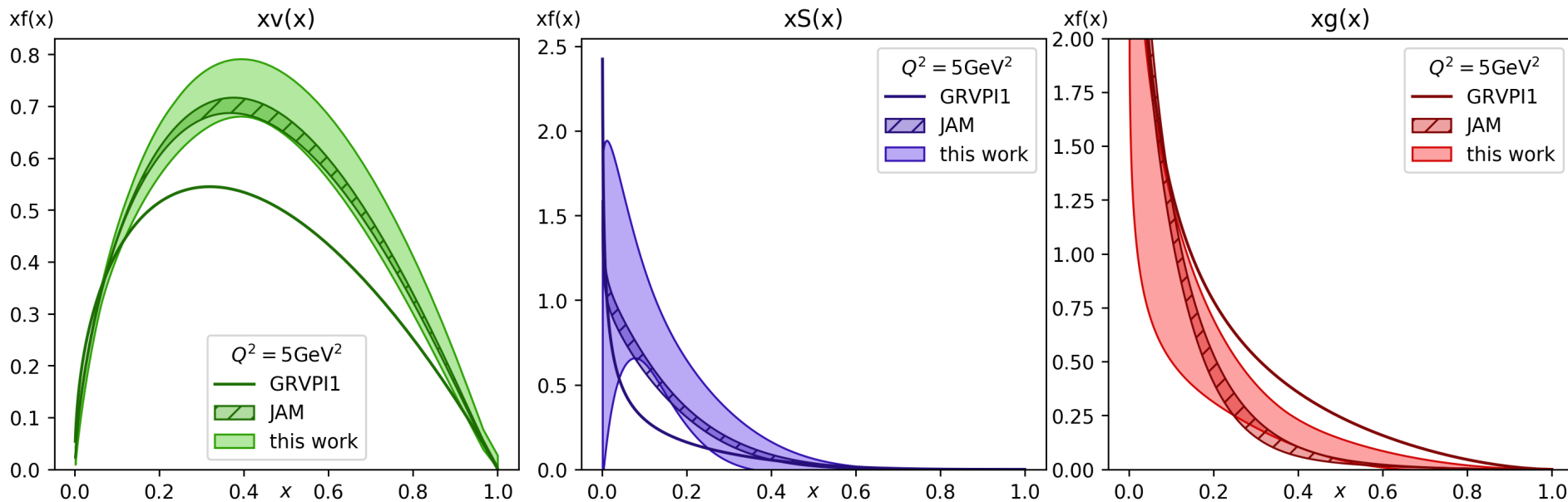
Charged Pion PDF



- PDFs with full uncertainties (e.g. α_S , Q_0^2 , μ_R variations)
- Parametrisation uncertainties considered as well (e.g. fixing C_g or C_s)
- μ_R variation has the strongest impact
- Valence distribution is well-constrained
- Hard to determine sea and gluon distributions

Experiment	χ^2/N_{points}
E615	194/140
NA10 (194 GeV)	98/67
NA10 (286 GeV)	92/73
WA70	74/99

Charged Pion PDF



- Comparison with recent pion PDF determinations:
 - JAM collaboration
 - GRVPI1 pion PDF set
- Valence distribution in good agreement with JAM and both disagree with the early GRV analysis
- The relatively hard-to-determine sea and gluon distributions are different in all the three PDF sets

xFitter usage in the HEP community

➤ CMS:

- Multi-differential $t\bar{t}$ cross sections at 13 TeV - [EPJC 80 \(2020\) 7 658](#)
- Extraction of PDFs, α_s and contact-interactions from new inclusive jet cross section measurement at 13 TeV - [JHEP 02 \(2022\) 142](#) (more in this [talk](#))
- W+charm analysis at 8 TeV - [2112.00895](#)

- Strange quark PDF analysis with DIS HERA2 data, ATLAS W,Z cross-sections and ATLAS, CMS W+charm cross-sections - [PRD 104 \(2021\) 7 076004](#)

- NLO analysis of heavy-quark production cross-sections using **different mass renormalisation schemes** - [JHEP 04 \(2021\) 043](#)

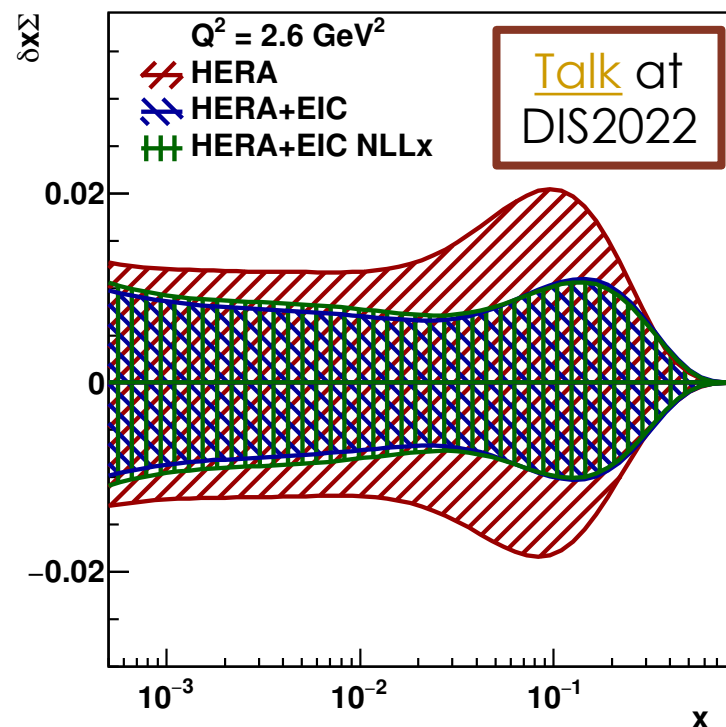
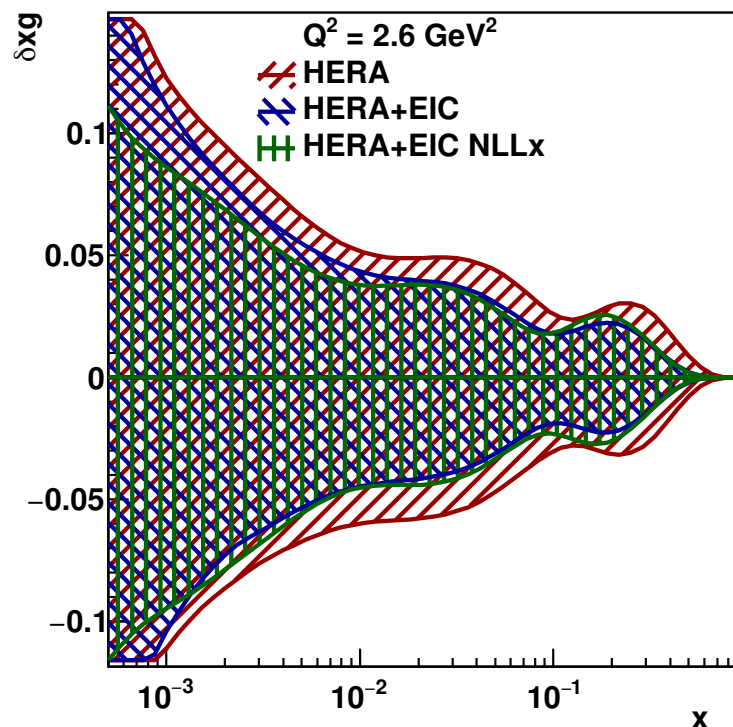
- **TMD parton densities** and corresponding parton showers: the advantage of four- and five-flavour schemes - [2106.09791](#)

- Implementation of **target mass corrections and higher-twist effects** in the xFitter framework - [PRD 101 \(2020\) 7 074015](#)

- NNLO PDFs with EW boson data from the LHC (**nuclear PDFs**) - [2112.11904](#)

Small-x resummation and EIC data

- Study with the pseudo-data properly generated with the low-x resummation
- Small-x resummation corrections available through HELLx+APFEL (starting from $Q^2 = 2.5 \text{ GeV}^2$)

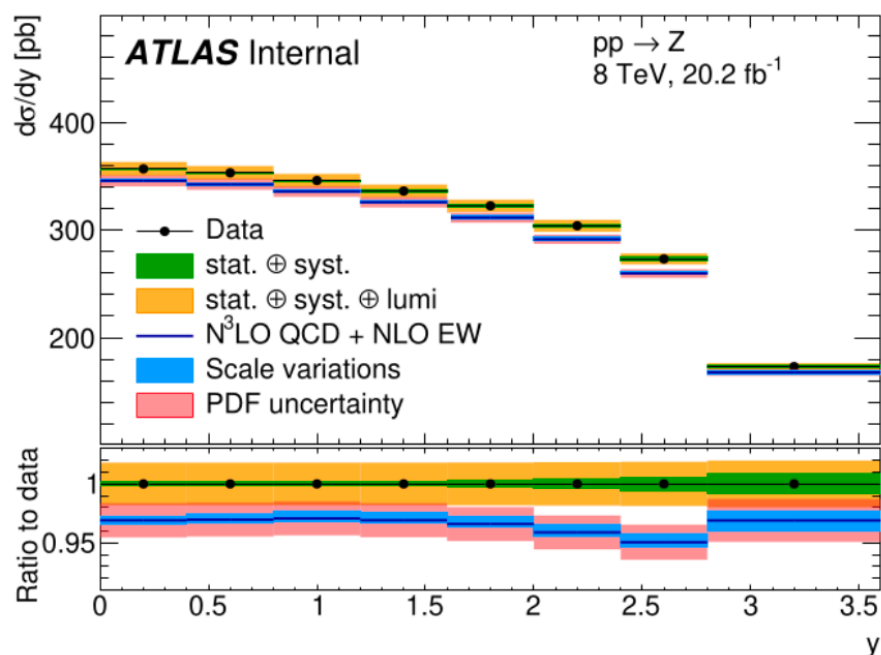


- When including NLLx corrections, uncertainties mildly affected – just the gluon at low-x
- Adding NLLx resummation does not impact valence distributions – neither in shape nor in the size of the PDF uncertainties

New determination of $\alpha_s(m_Z)$

- ATLAS measurement of $\alpha_s(m_Z)$ from **Z p_T distribution** – full lepton phase space
- Exquisite per-mille level precision in the central region - enables precise and unambiguous PDF interpretation
- **Most precise experimental determination of $\alpha_s(m_Z)$**
- Measurement dominated by theory uncertainties, but most of them can be constrained with more precise cross-section measurements

[ATLAS-CONF-2023-015](#)



ATLAS TEEC
CMS jets
W, Z inclusive
t \bar{t} inclusive
 τ decays
Q \bar{Q} bound states
PDF fits
e⁺e⁻ jets and shapes
Electroweak fit
Lattice
World average
ATLAS Z p_T

