

# Higher-order corrections for $tqZ$ production

Nikolaos Kidonakis

in collaboration with Nodoka Yamanaka

- $tqZ$  production
- Resummation of soft gluon corrections
- aNNLO cross sections
- Top-quark rapidity distributions



**KENNESAW STATE  
UNIVERSITY**  
COLLEGE OF SCIENCE AND MATHEMATICS  
*Department of Physics*

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## $tqZ$ production

observation of  $pp \rightarrow tqZ$  at 13 TeV collisions at the LHC

recent data is well above NLO theoretical prediction

the cross section for  $tqZ$  allows study of  $t$ - $Z$  and  $W$ - $W$ - $Z$  couplings

and is sensitive to any anomalous top-quark couplings and moments

QCD corrections are significant at NLO and they are needed for good theoretical predictions

further improvement in theoretical accuracy by inclusion of soft-gluon corrections

→ approximate NNLO (aNNLO) predictions

## Soft-gluon corrections

processes:  $pp \rightarrow tqZ$

partonic processes at LO  $a(p_a) + b(p_b) \rightarrow t(p_t) + q(p_q) + Z(p_Z)$

if an additional gluon is emitted with momentum  $p_g$  in the final state

then we define the variable  $s_4 = (p_q + p_Z + p_g)^2 - (p_q + p_Z)^2$

At partonic threshold  $s_4 \rightarrow 0$

Soft corrections  $\left[ \frac{\ln^k(s_4/m_t^2)}{s_4} \right]_+$  with  $k \leq 2n - 1$  for the order  $\alpha_s^n$  corrections

Factorization and Resummation of these soft-gluon corrections

Soft anomalous dimension  $\Gamma_{S\ ab \rightarrow tqZ}$  controls the evolution of the soft function

two-loop results and partial three-loop results are known for  $\Gamma_{S\ ab \rightarrow tqZ}$

Finite-order expansions  $\rightarrow$  no prescription needed

Approximate NNLO (aNNLO) theoretical predictions

aNNLO = NLO + soft-gluon NNLO corrections

## Soft-gluon resummation

$$d\sigma_{pp \rightarrow tqZ} = \sum_{a,b} \int dx_a dx_b \phi_{a/p}(x_a, \mu_F) \phi_{b/p}(x_b, \mu_F) d\hat{\sigma}_{ab \rightarrow tqZ}(s_4, \mu_F)$$

take Laplace transforms  $d\tilde{\sigma}_{ab \rightarrow tqZ}(N) = \int_0^s (ds_4/s) e^{-Ns_4/s} d\hat{\sigma}_{ab \rightarrow tqZ}(s_4)$  with  $N$  the transform variable

and  $\tilde{\phi}(N) = \int_0^1 e^{-N(1-x)} \phi(x) dx$

Then

$$d\tilde{\sigma}_{ab \rightarrow tqZ}(N) = \tilde{\phi}_{a/a}(N_a, \mu_F) \tilde{\phi}_{b/b}(N_b, \mu_F) d\tilde{\sigma}_{ab \rightarrow tqZ}(N, \mu_F)$$

Refactorization in terms of hard and soft functions

$$d\tilde{\sigma}_{ab \rightarrow tqZ}(N) = \tilde{\psi}_{a/a}(N_a, \mu_F) \tilde{\psi}_{b/b}(N_b, \mu_F) \tilde{J}_q(N, \mu_F) \text{tr} \left\{ H_{ab \rightarrow tqZ}(\alpha_s(\mu_R)) \tilde{S}_{ab \rightarrow tqZ} \left( \frac{\sqrt{s}}{N\mu_F} \right) \right\}$$

Thus

$$d\tilde{\sigma}_{ab \rightarrow tqZ}(N) = \frac{\tilde{\psi}_{a/a}(N_a, \mu_F) \tilde{\psi}_{b/b}(N_b, \mu_F) \tilde{J}_q(N, \mu_F)}{\tilde{\phi}_{a/a}(N_a, \mu_F) \tilde{\phi}_{b/b}(N_b, \mu_F)} \text{tr} \left\{ H_{ab \rightarrow tqZ}(\alpha_s(\mu_R)) \tilde{S}_{ab \rightarrow tqZ} \left( \frac{\sqrt{s}}{N\mu_F} \right) \right\}$$

## Resummed cross section

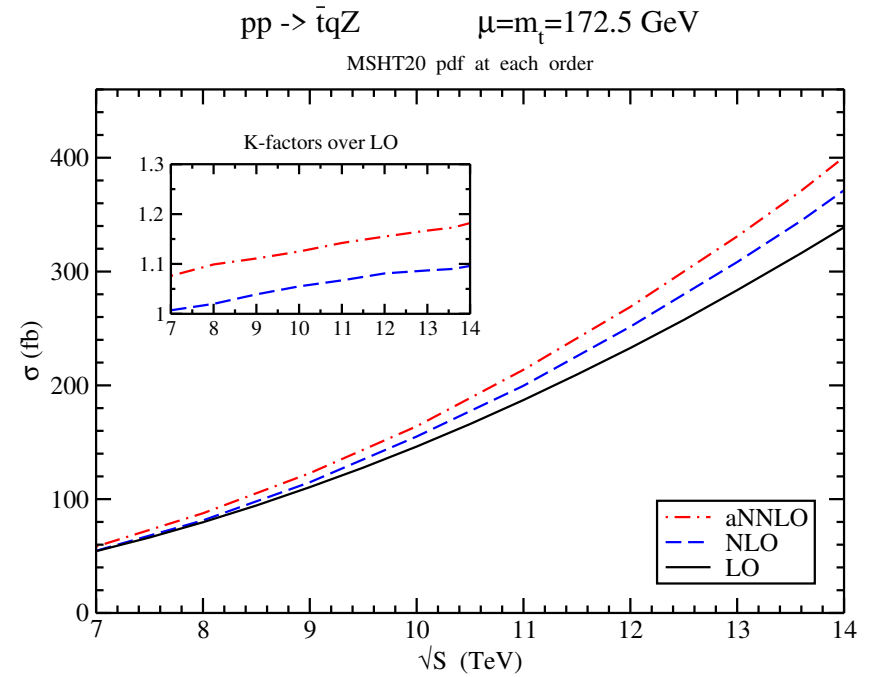
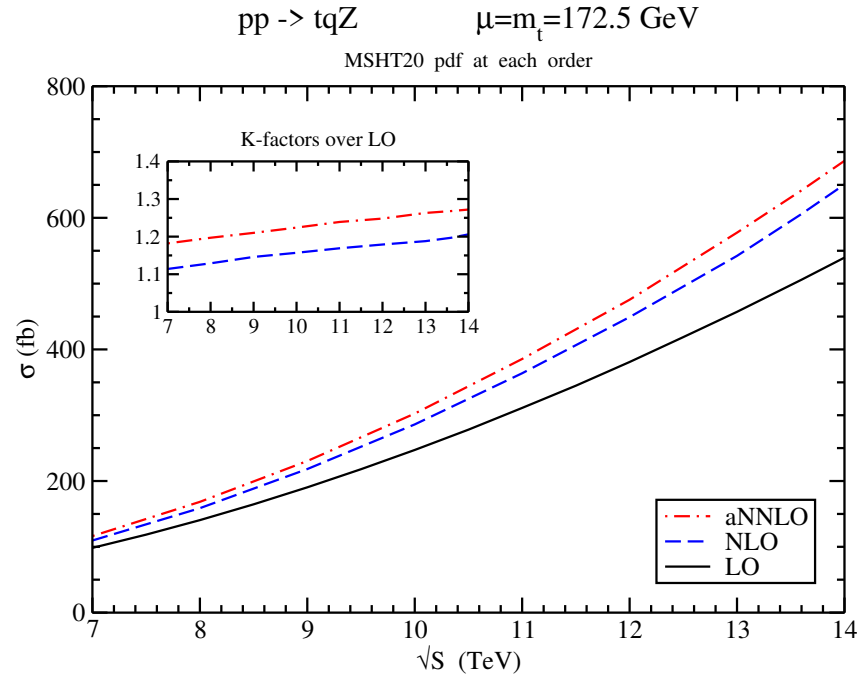
Renormalization group evolution  $\rightarrow$  resummation

$$\begin{aligned}
 d\tilde{\sigma}_{ab \rightarrow tqZ}^{\text{resum}}(N) &= \exp \left[ \sum_{i=a,b} E_i(N_i) \right] \exp \left[ \sum_{i=a,b} 2 \int_{\mu_F}^{\sqrt{s}} \frac{d\mu}{\mu} \gamma_{i/i}(N_i) \right] \exp \left[ E'_q(N) \right] \\
 &\times \text{tr} \left\{ H_{ab \rightarrow tqZ} \left( \alpha_s(\sqrt{s}) \right) \bar{P} \exp \left[ \int_{\sqrt{s}}^{\sqrt{s}/N} \frac{d\mu}{\mu} \Gamma_{S ab \rightarrow tqZ}^\dagger \left( \alpha_s(\mu) \right) \right] \right. \\
 &\quad \left. \times \tilde{S}_{ab \rightarrow tqZ} \left( \alpha_s \left( \frac{\sqrt{s}}{N} \right) \right) P \exp \left[ \int_{\sqrt{s}}^{\sqrt{s}/N} \frac{d\mu}{\mu} \Gamma_{S ab \rightarrow tqZ} \left( \alpha_s(\mu) \right) \right] \right\}
 \end{aligned}$$

The soft anomalous dimensions  $\Gamma_{S ab \rightarrow tqZ}$  for this process are  $2 \times 2$  matrices and are known at one and two loops, and partly at three loops

Expansion of the resummed cross section and inversion to momentum space  
 $\rightarrow$  aNNLO corrections

# aNNLO cross sections for $tqZ$ production



soft-gluon emission dominates the corrections

$K$ -factors not sensitive to cuts on  $p_T$  of the  $Z$ -boson

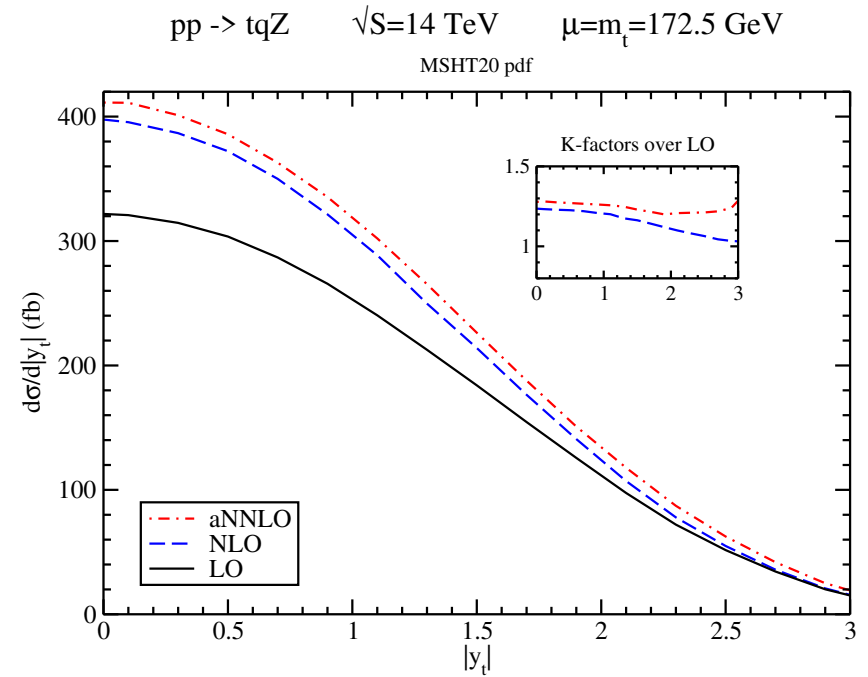
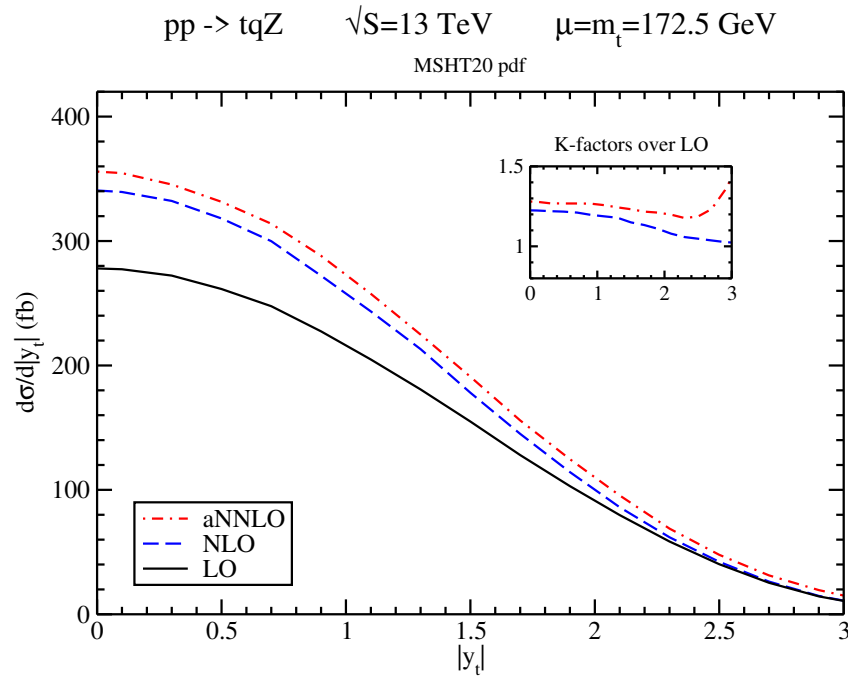
## aNNLO cross sections for $tqZ$ production

$tqZ$ cross sections in $pp$ collisions at the LHC					
$\sigma$ in fb	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
LO	$98.4^{+1.6+1.6}_{-3.9-0.9}$	$141^{+3}_{-7} \pm 2$	$457^{+21+6}_{-32-3}$	$506^{+24+6}_{-36-4}$	$540^{+26+6}_{-40-4}$
NLO	$110 \pm 2^{+1}_{-2}$	$159^{+3}_{-2} \pm 2$	$542 \pm 11^{+6}_{-5}$	$606^{+11}_{-12} \pm 6$	$651^{+14}_{-16} \pm 6$
aNNLO	$116^{+1}_{-2} \pm 2$	$168 \pm 2^{+3}_{-2}$	$577^{+4+6}_{-9-5}$	$641^{+4}_{-10} \pm 6$	$686^{+5}_{-13} \pm 7$

$\bar{t}qZ$ cross sections in $pp$ collisions at the LHC					
$\sigma$ in fb	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
LO	$54.3^{+0.8+0.9}_{-2.1-1.2}$	$79.7^{+1.8+1.2}_{-3.6-1.5}$	$284^{+13+3}_{-20-5}$	$316^{+15+3}_{-23-5}$	$339^{+17+3}_{-25-5}$
NLO	$54.6^{+1.3+1.3}_{-0.8-1.0}$	$81.3^{+1.9+1.7}_{-1.3-1.4}$	$308^{+8+5}_{-7-4}$	$345^{+8}_{-9} \pm 5$	$371^{+10+6}_{-9-4}$
aNNLO	$58.4^{+0.4+1.2}_{-0.7-1.0}$	$87.6^{+0.4+1.7}_{-1.2-1.4}$	$331^{+2}_{-6} \pm 4$	$371^{+2}_{-8} \pm 4$	$401^{+2+5}_{-8-4}$

Sum of $tqZ$ and $\bar{t}qZ$ cross sections in $pp$ collisions at the LHC					
$\sigma$ in fb	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
LO	$153^{+2+3}_{-6-2}$	$221^{+5}_{-11} \pm 3$	$741^{+34+9}_{-52-8}$	$822^{+39}_{-59} \pm 9$	$879^{+43}_{-65} \pm 9$
NLO	$165 \pm 3^{+2}_{-3}$	$240^{+5+4}_{-3-3}$	$850^{+19+11}_{-18-9}$	$951^{+19}_{-21} \pm 11$	$1022^{+24+12}_{-25-10}$
aNNLO	$174^{+1}_{-3} \pm 3$	$256^{+2+5}_{-3-3}$	$908^{+6}_{-15} \pm 10$	$1012^{+6}_{-18} \pm 10$	$1087^{+7}_{-21} \pm 12$

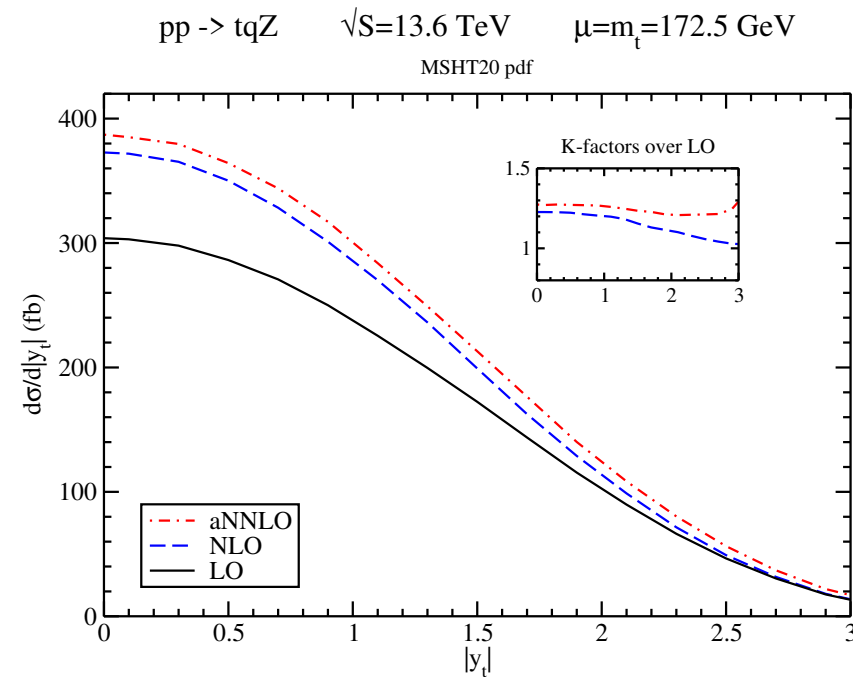
# Top-quark rapidity distributions in $tqZ$ production



significant enhancements from aNNLO corrections  
particularly at large rapidities



# Top-quark rapidity distributions in $tqZ$ production



scale and pdf uncertainties get bigger at

larger rapidities,  $|y_t| > 2$

## Summary

- $tqZ$  production in high-energy  $pp$  collisions
- NLO corrections are significant
- soft-gluon resummation improves the theoretical predictions
- aNNLO corrections for total cross section and top-quark rapidity distributions