



Exercise: magnetic & electric fields

Apply fields to a simple beamline

The problem

- We will use the beamline constructed in the geometry exercise
- The first objective is to use the dipole to deflect the incoming beam (previously impacting on the beam dump) exactly onto the z-axis and through the quadrupoles
- Then, we will change the beam characteristics and use the quadrupoles to focus it at a desired location
- As an extra problem, we will accelerate the protons with an electric field

The input file

- You can start from the provided input or from your own solution to the geometry exercise, if complete
- All the magnets are in place and the initial beam is defined

Apply magnetic field to the dipole and run

1. Define a **dipole** field (**MGNCREAT**) and apply it to the dipole replica (**MGNFIELD**)
 - What is the correct magnetic field strength B to deflect the incoming beam by an angle $\theta=20^\circ$ and deflect it onto the z-axis? The strength is given by:

$$B[T] = \frac{p \left[\frac{eV}{c} \right]}{c \left[\frac{m}{s} \right] \cdot R[m]}$$

where p is the momentum, c is the speed of light and R is the required bending radius, already **#define**'d in the input (as *Rbend*)

2. Run the input (just a few particles are enough) and plot the proton fluence scoring on the x-z plane (i.e. top view of the beamline)
 - Is the beam brought onto the z-axis? If not, check your input.

Apply magnetic fields to the quadrupoles

- The three quadrupoles will be in an FDF configuration (Focusing-Defocusing-Focusing)
 - By convention, “focusing” means “focusing on the horizontal plane for positively charged particles”
- 3. Define a focusing and a defocusing quadrupole field (**MGNCREAT**) and apply the focusing field to Q1 and Q3, and the defocusing one to Q2 (**MGNFIELD**)
 - What is the difference between the two? Just a 90° azimuthal rotation!
 - Apply the following gradients (careful with the unit):
 - $g_{Q1} = 25.268 \text{ T/m}$
 - $g_{Q2} = 28.683 \text{ T/m}$
 - $g_{Q3} = 46.449 \text{ T/m}$
- 4. Plot the fields in the quadrupoles on the transverse plane (x-y) and check that the quadrupole configuration you have defined is indeed correct

Adjust beam parameters and run

- If you run now (with the pencil beam) nothing will happen, since the beam will still be encountering zero field on the z-axis inside the quadrupoles
5. Change the beam parameters so that the effect of the quadrupoles can become apparent
 - Define a $\pm 3\%$ uniform momentum spread
 - Define a Gaussian divergence with $\sigma = 5$ mrad
 - Define a Gaussian beam profile with $\sigma = 2.5$ mm
 6. Run 5 cycles of 50000 primaries each; since the beam should not be hitting anything, this will be quite fast.
 7. Plot the proton fluence scoring on the x-z plane (i.e. top view of the beamline) and on the y-z plane (side view). Observe the action of the quadrupoles and the focusing of the beam on both planes at around $z = 3$ m.

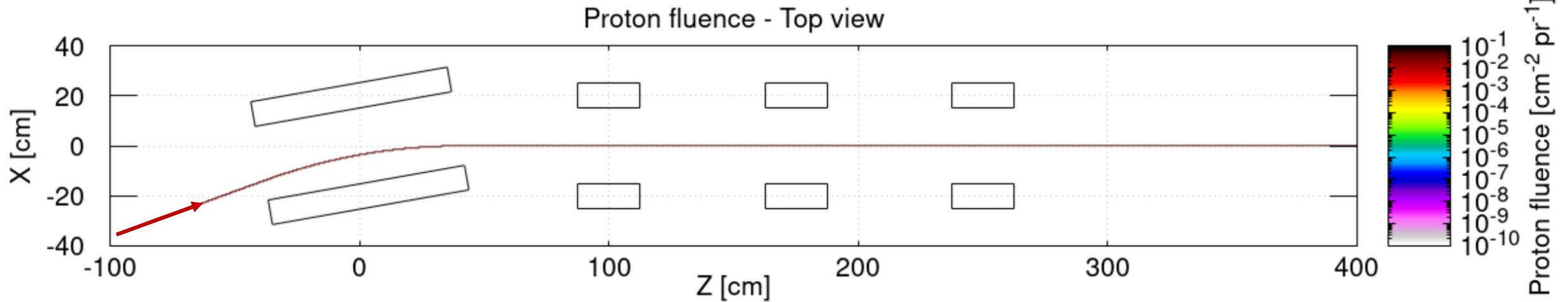
Extra problem: electric field

- Let's give a small push to the protons after they exit the beamline
- Define a vacuum region within an RCC placed around $z=300\text{cm}$, with a radius of 5 cm and a length of 20 cm
- Apply an electric field to this region so that the protons receive an additional 50 MeV of energy
 - What should be the magnitude of the electric field component along the z -axis (in kV/cm) to achieve this?
- Add two **USRBDX** scorings to score the energy spectrum of the incoming and outgoing protons in this region
- Run once more and plot the energy spectrum of protons entering and exiting the electric field region. Can you observe the acceleration?

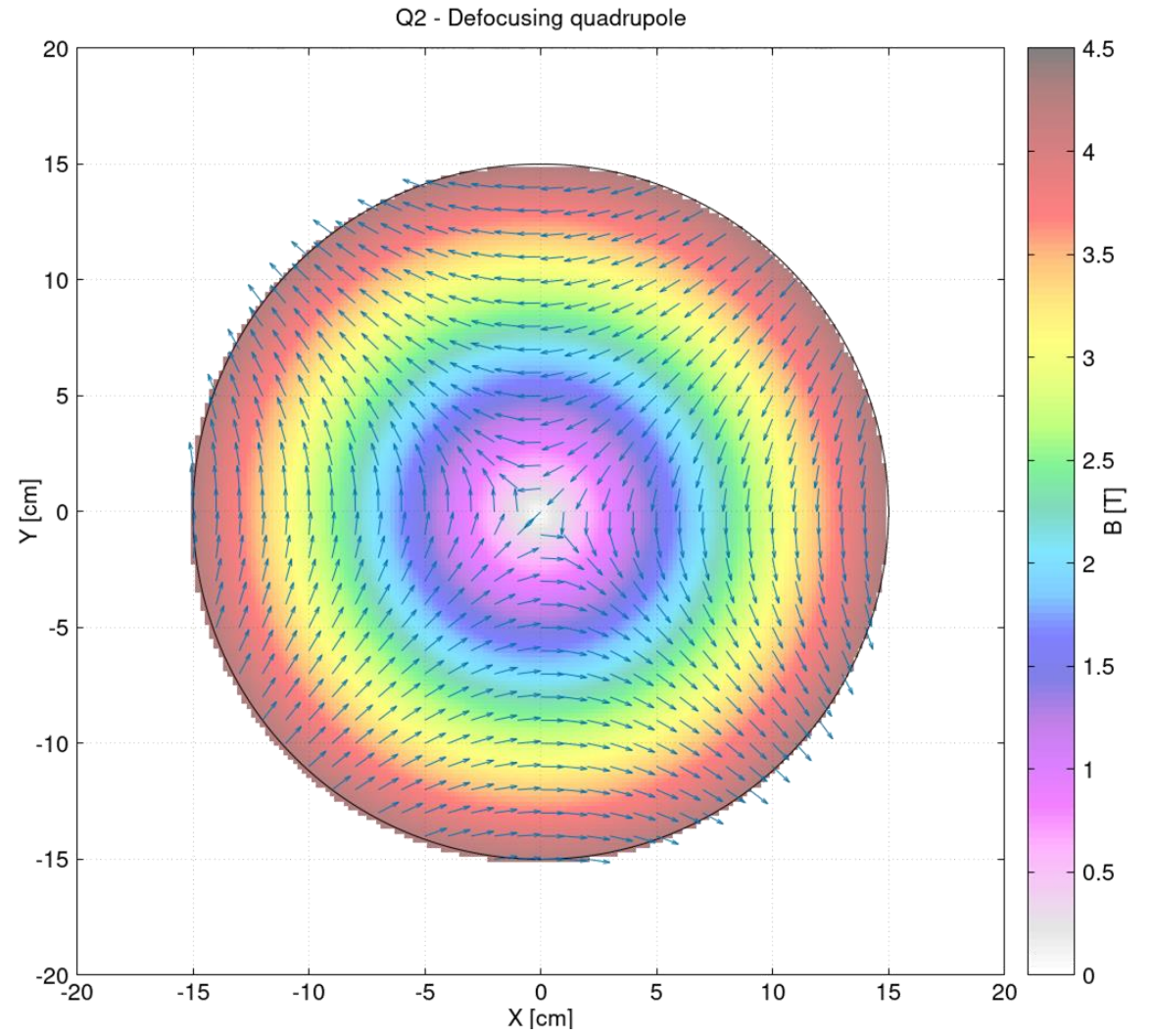
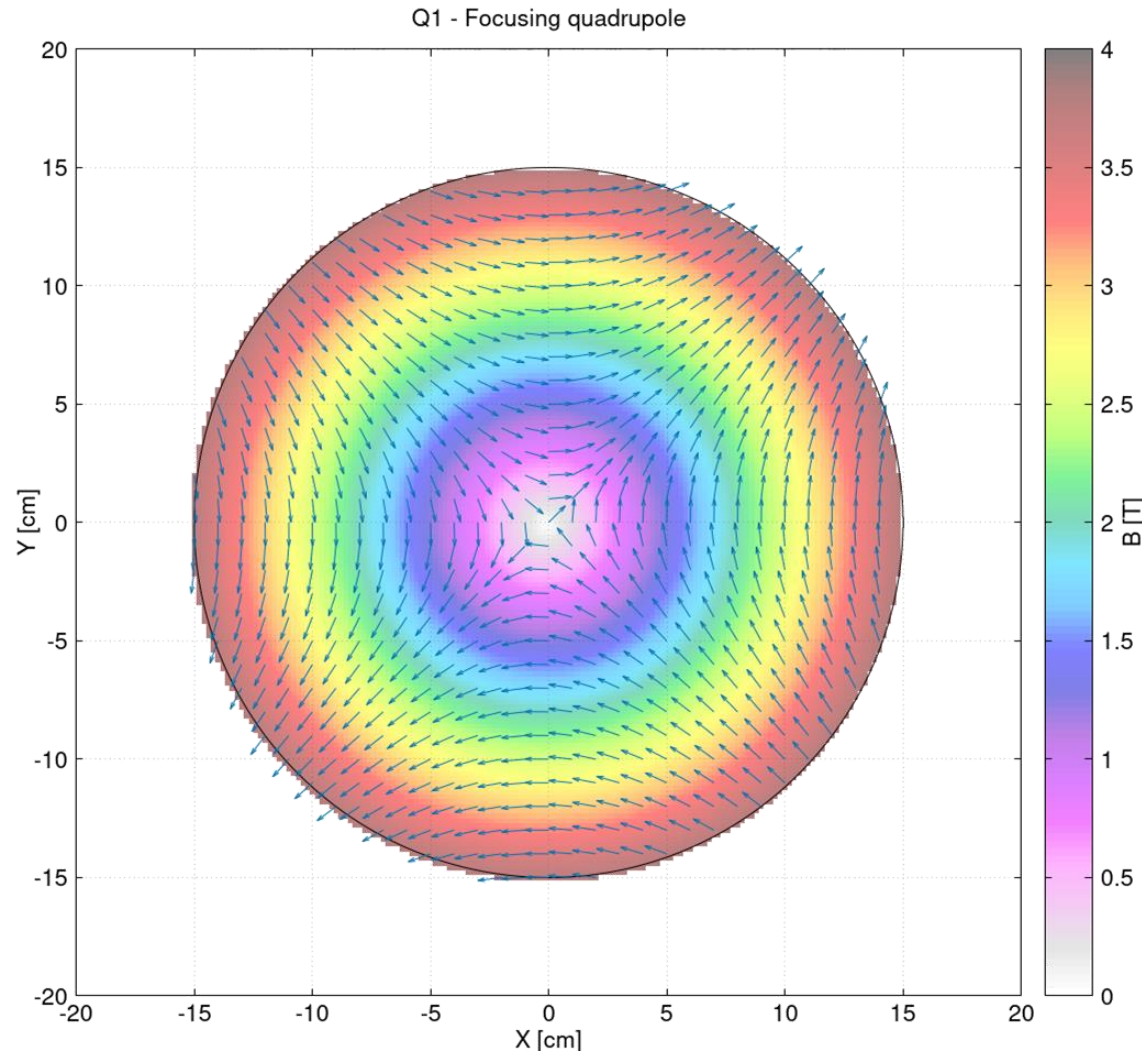
Results

Proton fluence with pencil beam

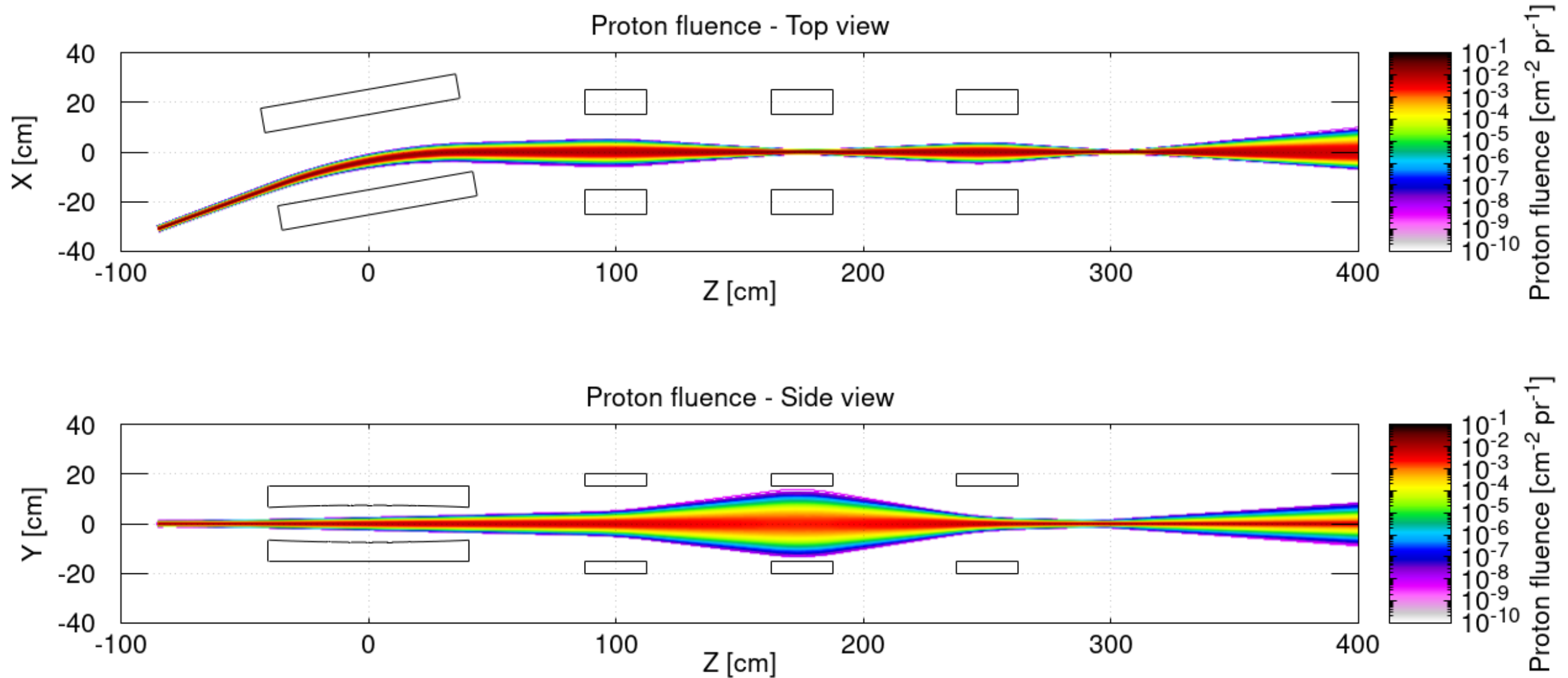
- The dipole deflects the incoming beam onto the z-axis



Quadrupole fields



Proton fluence with $dp/p=3\%$, $\Delta\phi=5$ mrad(σ), $\Delta x/y=2.5$ mm(σ)



Acceleration with electric field

