

# Flavoured jets and particles at the LHC

Giovanni Stagnitto



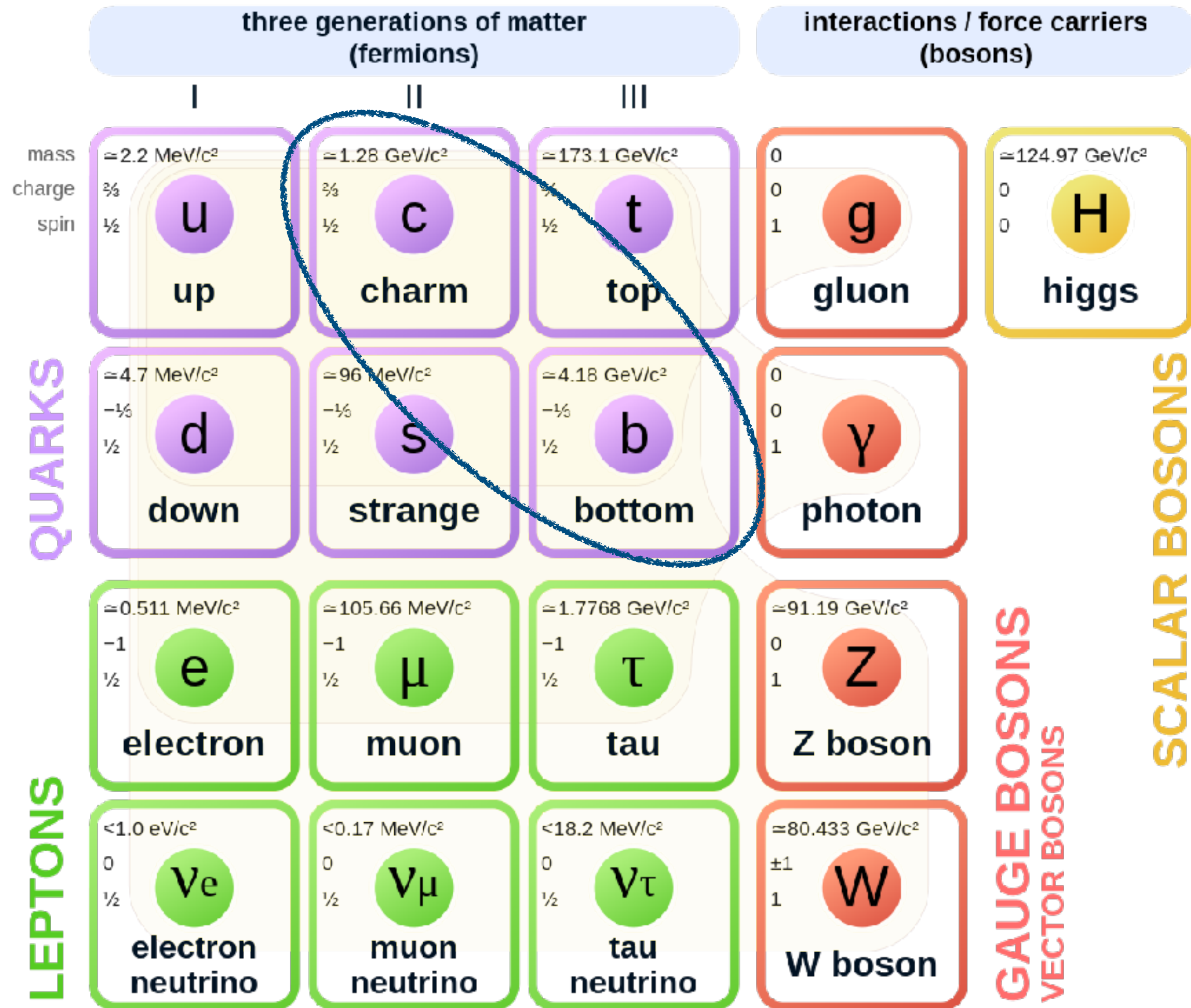
**University of  
Zurich**<sup>UZH</sup>



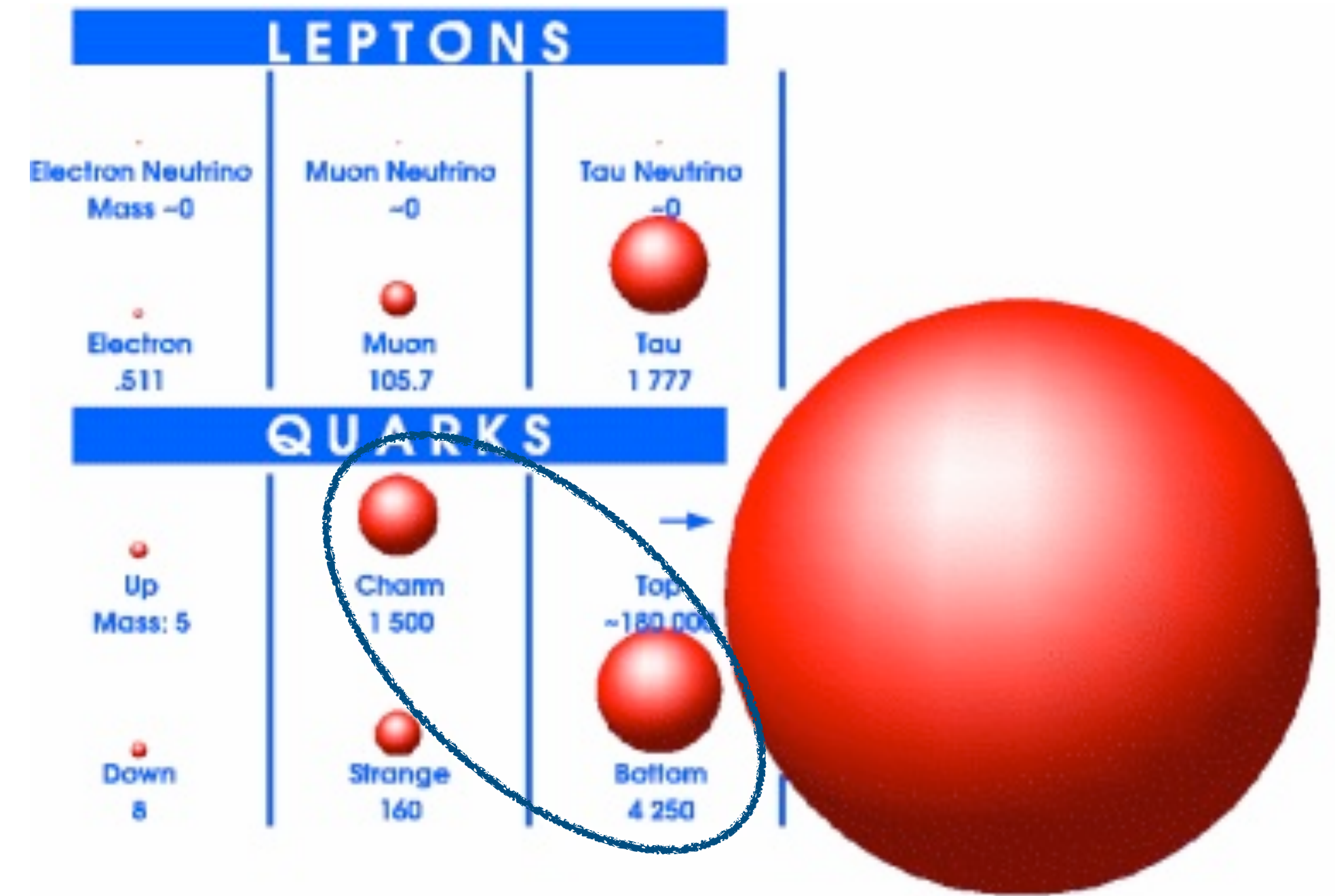
**Swiss National  
Science Foundation**

Milan Joint Phenomenology Seminar, 16.01.2023

# Standard Model of Elementary Particles



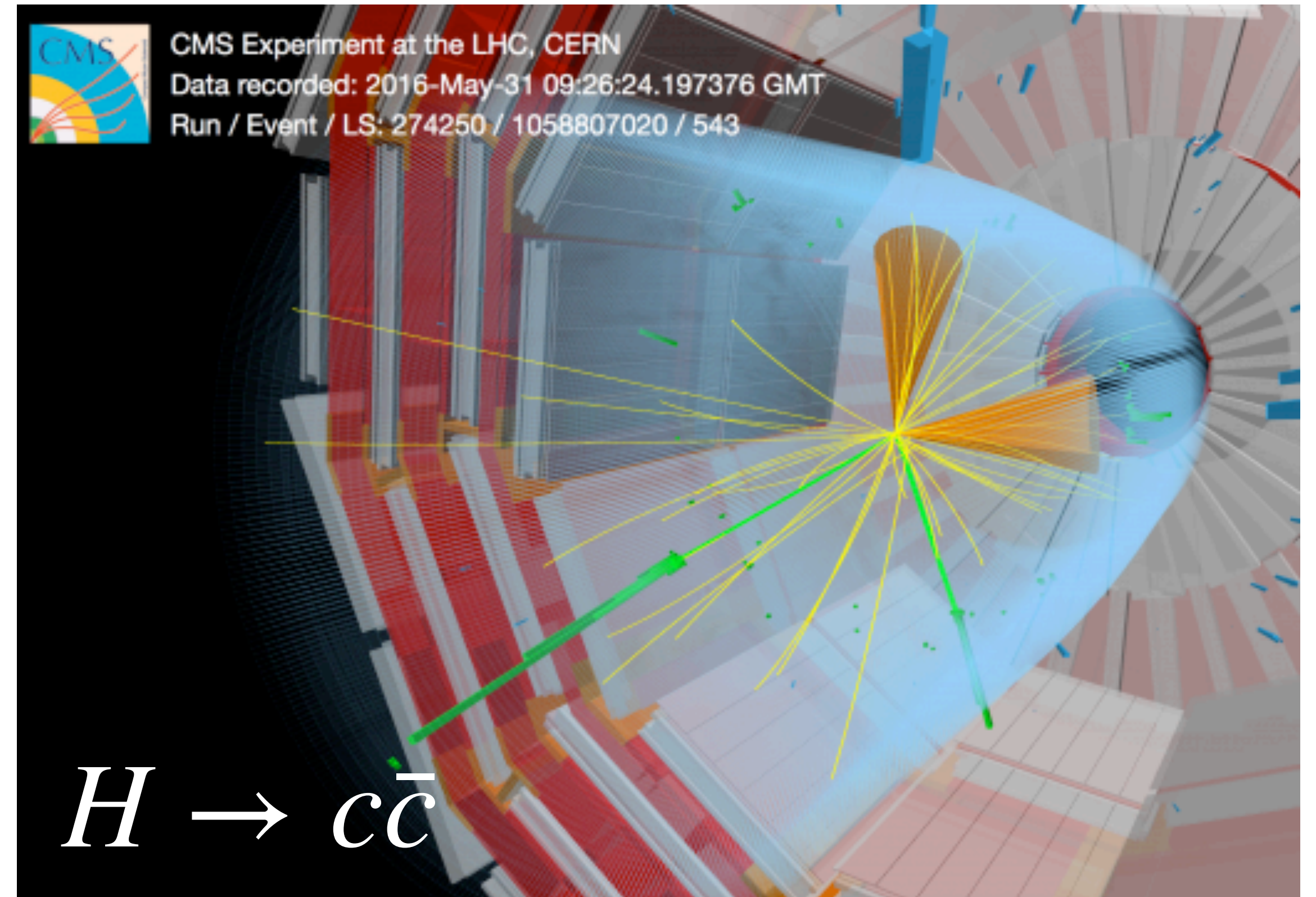
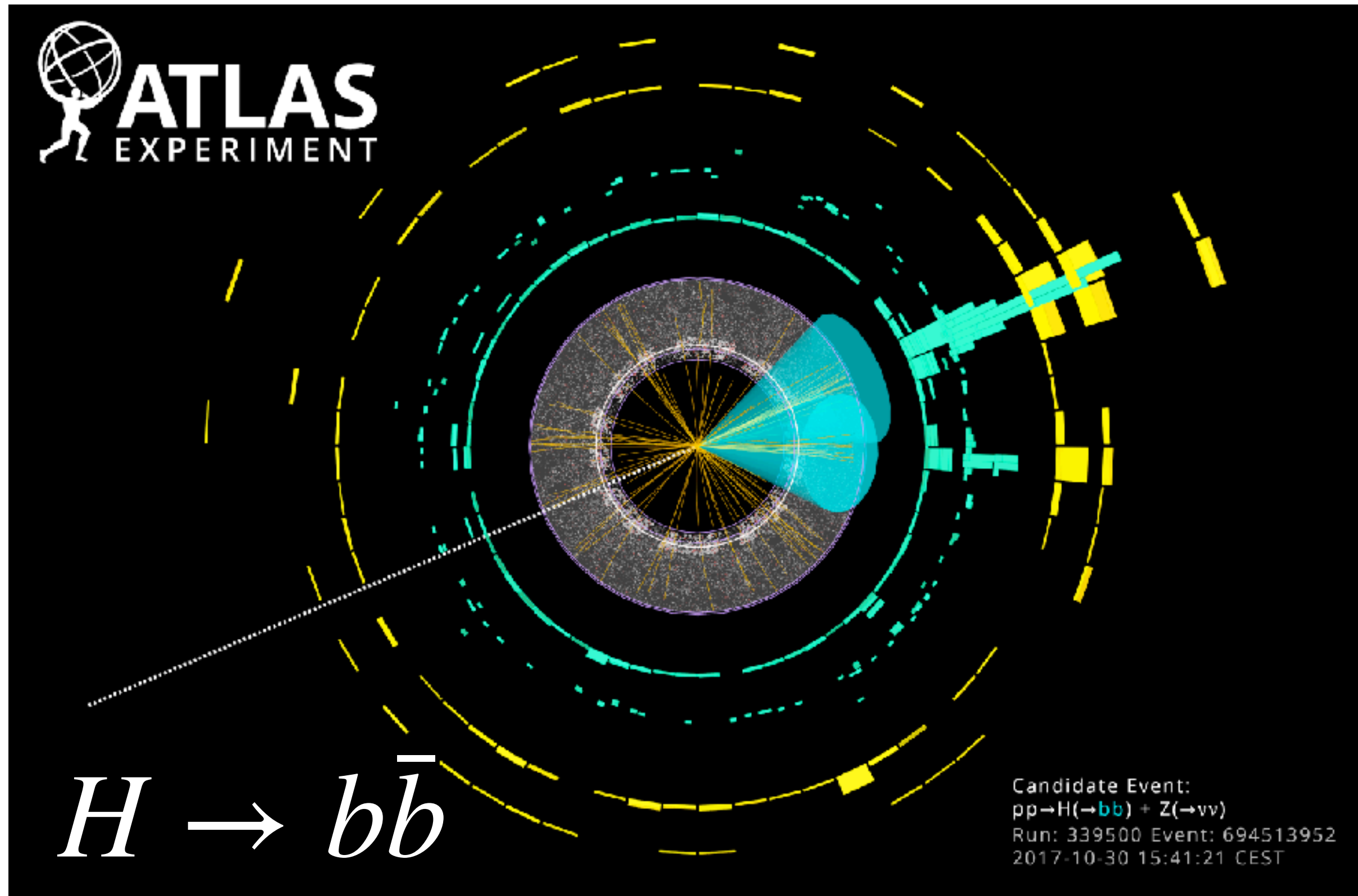
# Flavoured (heavy) quarks



*There's a difference between beauty and charm.  
 A beautiful person/quark is one I notice.  
 A charming person/quark is one who notices me.  
 (John Erskine)*



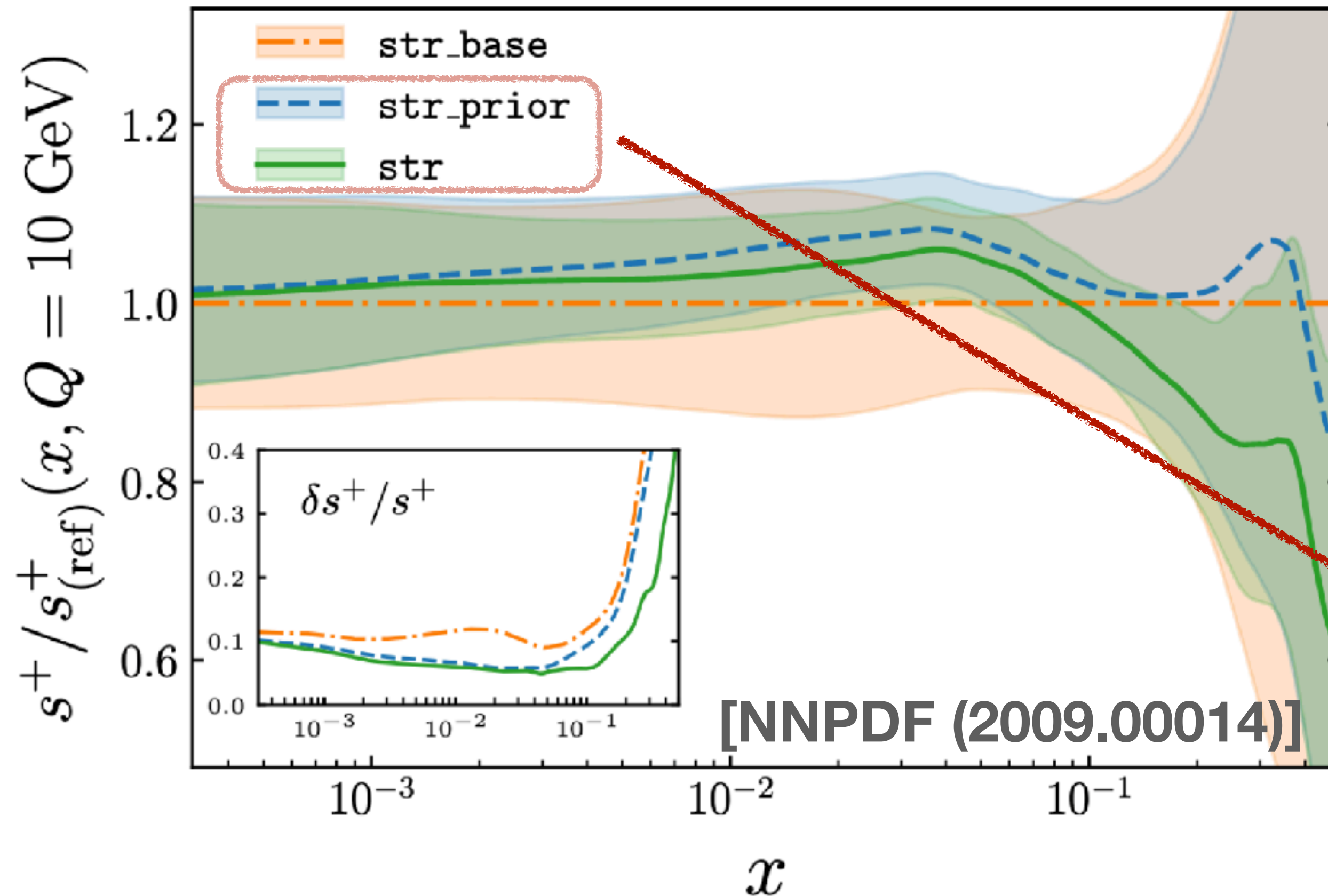
# Flavoured objects at the LHC



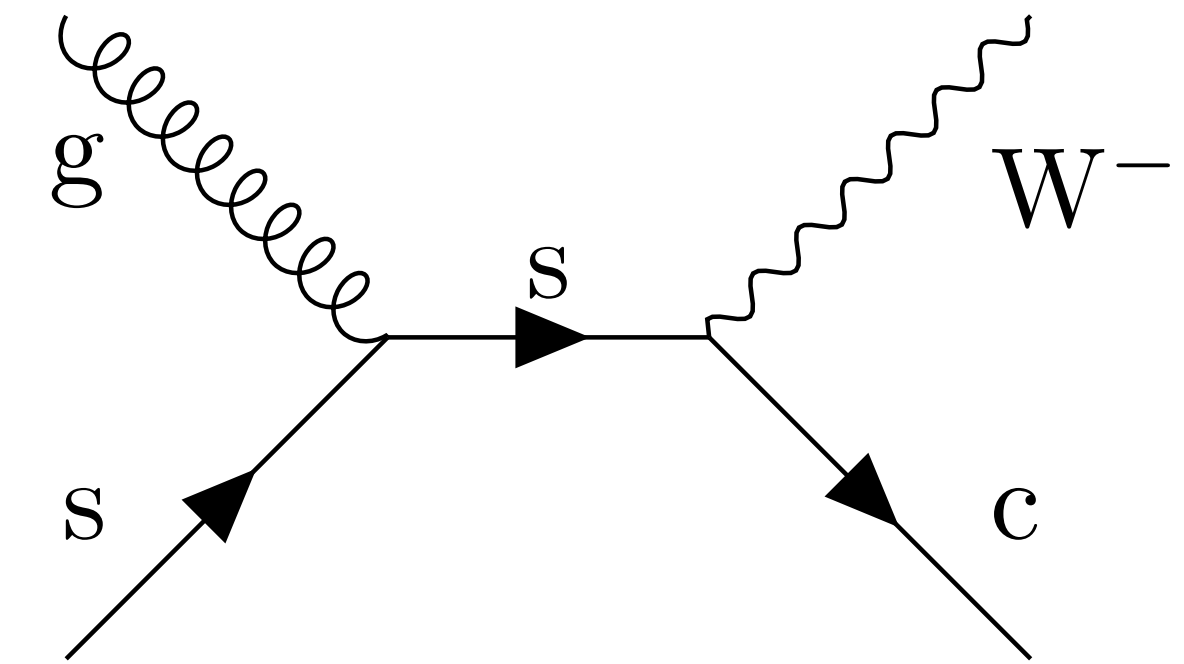
Decay products of B- or D-hadrons  
as a **proxy** for b or c quarks in the hard scattering process



# Why **flavoured** objects?



An example: W+D-hadron/c-jet  
unique probe into the strange PDF



contain [ATLAS (1402.6263)] and  
[CMS (1310.1138)] 7 TeV data

... but **flavoured jets/particles appear everywhere:**  
top, Higgs, new physics searches, ...  
useful to pinpoint specific scattering processes and reject backgrounds



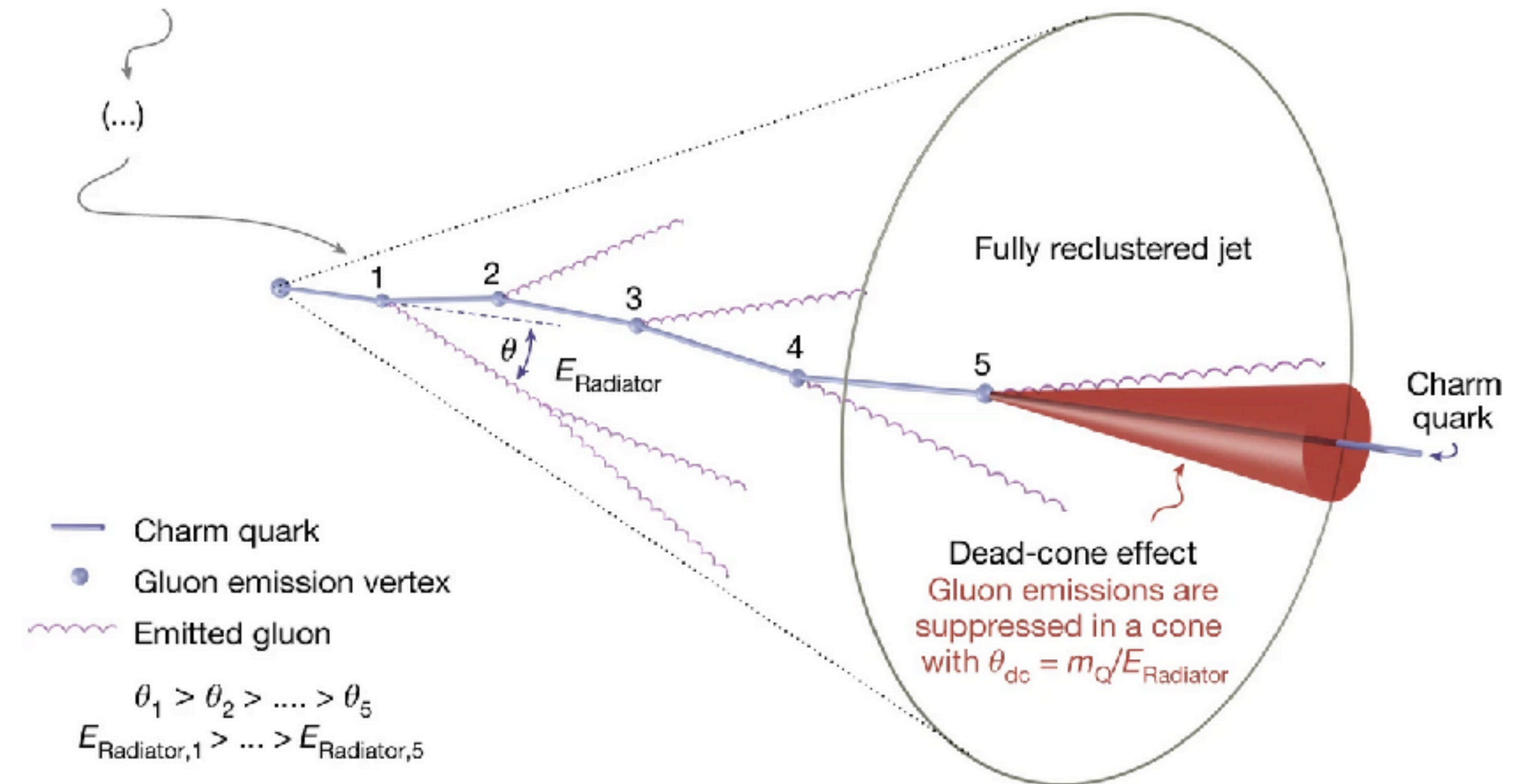
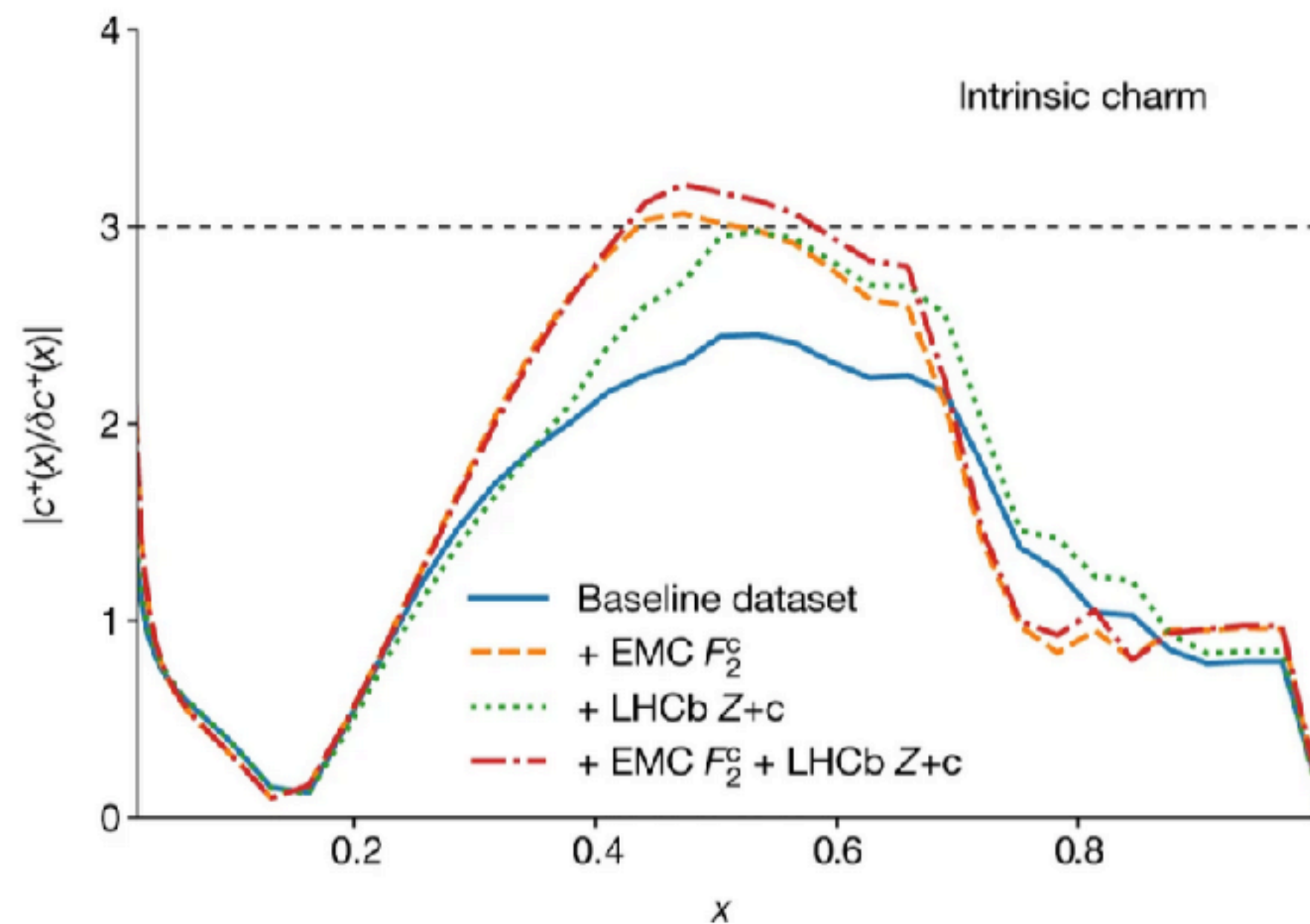
# Heavy quarks are *Nature's* aficionados

Article | [Open Access](#) | [Published: 18 May 2022](#)

## Direct observation of the dead-cone effect in quantum chromodynamics

[ALICE Collaboration](#)

[Nature](#) **605**, 440–446 (2022) | [Cite this article](#)



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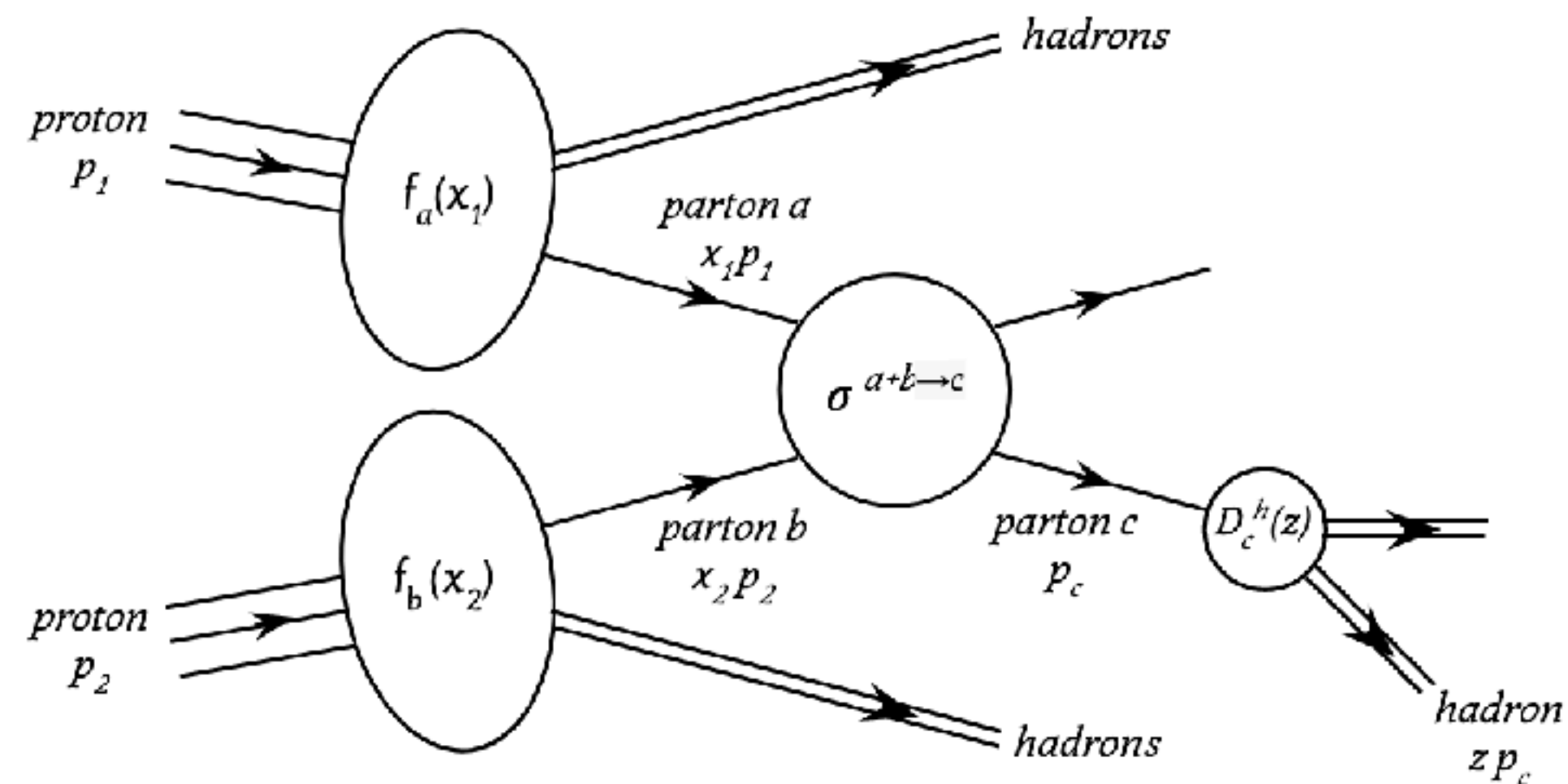
## Evidence for intrinsic charm quarks in the proton

[The NNPDF Collaboration](#)

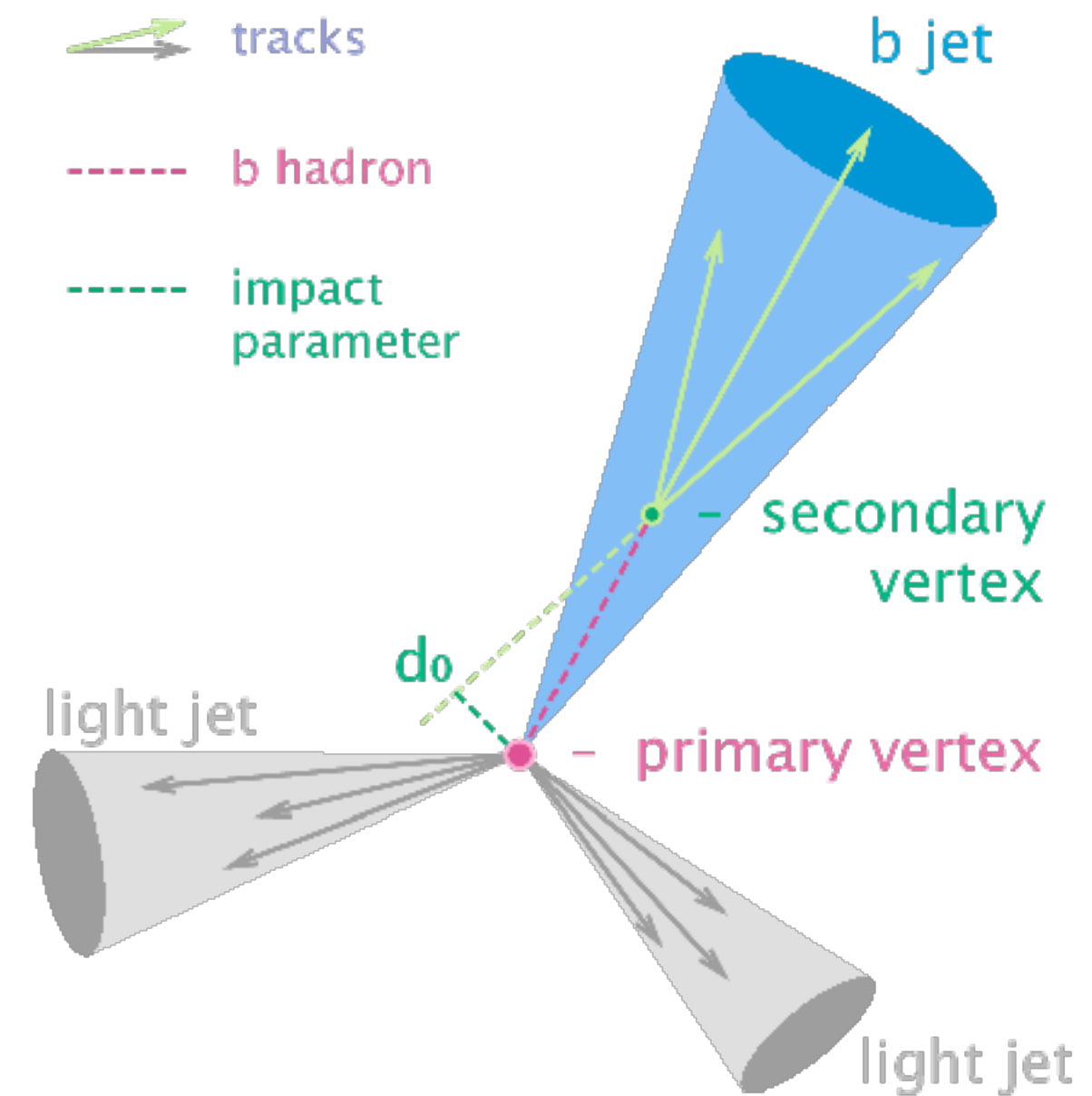
[Nature](#) **608**, 483–487 (2022) | [Cite this article](#)

# Two ways of looking at flavour

\*not a review, presentation biased towards my ongoing projects



**Identified hadrons**

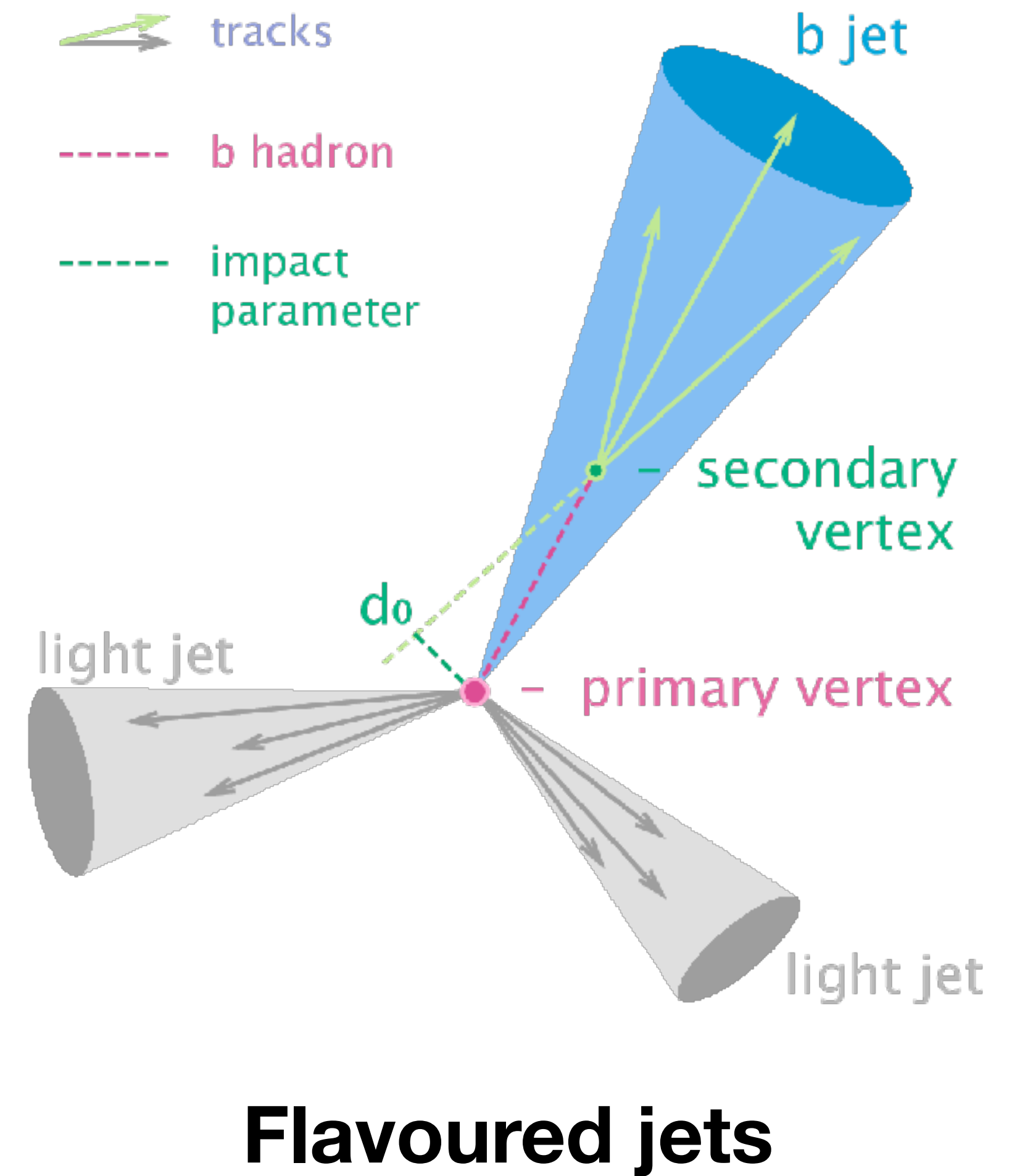
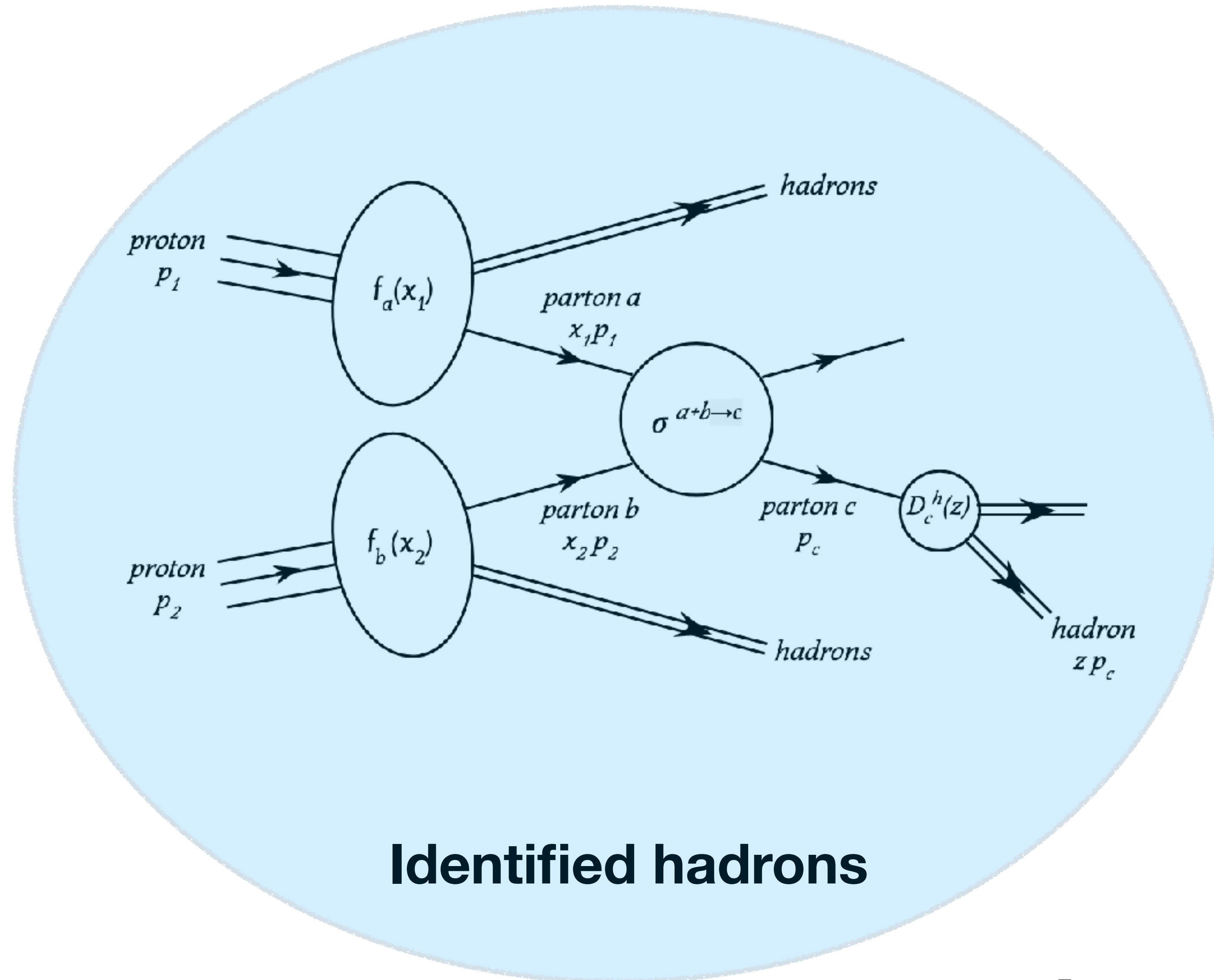


**Flavoured jets**

Flavoured particles and flavoured jets are **two complementary ways** of looking at the same events



# Two ways of looking at flavour



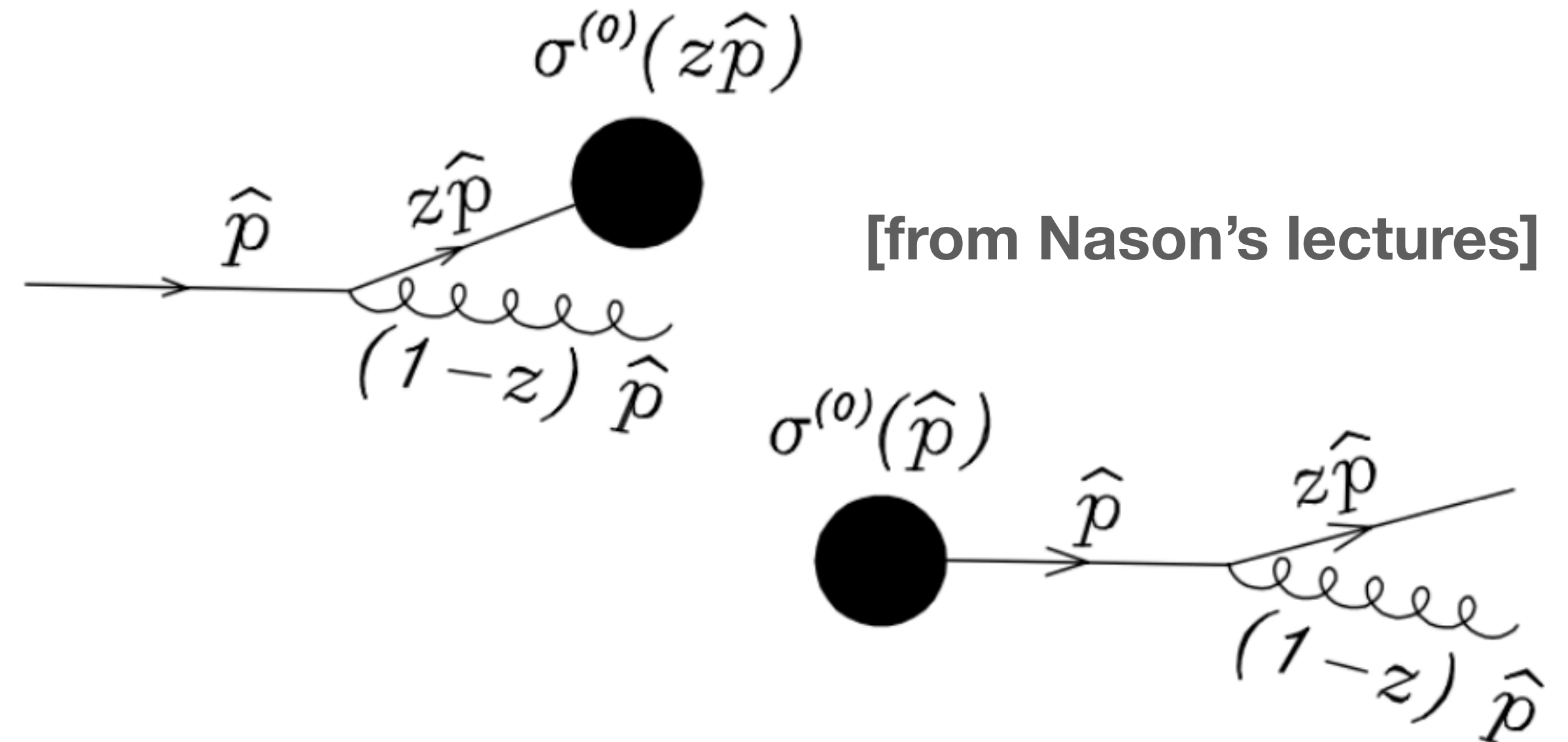
# Identified hadrons

$$d\sigma^H = \sum_p \int d\eta D_{H \leftarrow p}(\eta, \mu_a^2) d\hat{\sigma}_p(\eta, \mu_a^2)$$

Fixed order parton prediction convolved with a non-perturbative **fragmentation function (FF)** to describe transition to hadrons

Whenever we identify a QCD particle, we spoil the cancellation of collinear divergences! **FF = “final-state PDF”**

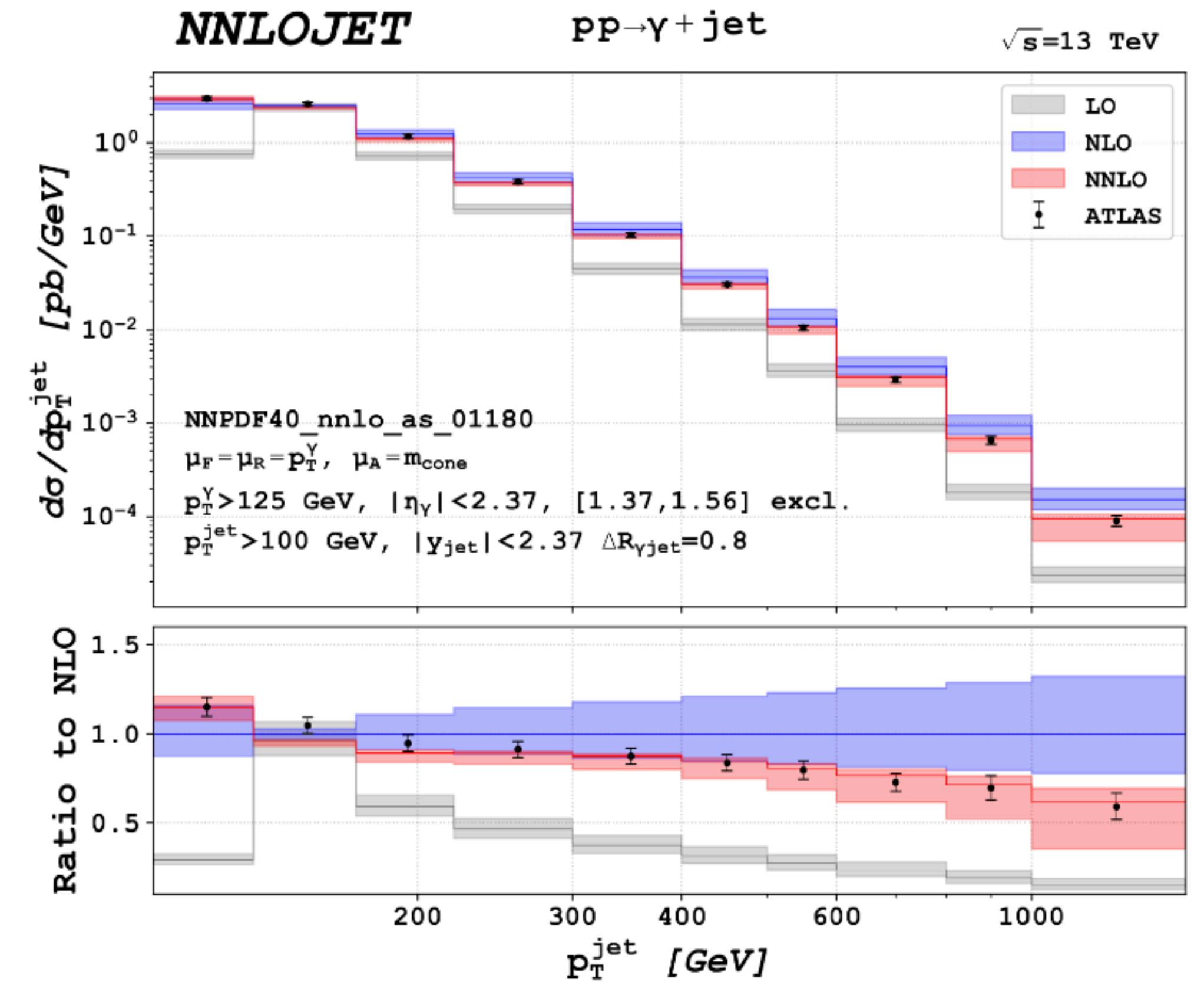
We absorb divergences into a bare FF to result in the physical FF





# NNLO QCD with identified particles

- Parton-to-photon fragmentation processes in the antenna subtraction formalism (photon as the identified particle)  $\rightarrow \rightarrow$  [Schürmann, Gehrmann 2022] [Chen et al. 2022]
- B-hadron production in  $t\bar{t}$  events in the sector-improved residue subtraction scheme [Czakon et al. 2021]
- Analytic ingredients for **fully exclusive identified hadrons (i.e. possible presence of additional jets)** in  $e^+e^-$  in the antenna subtraction formalism [Gehrmann, GS 2022]



# Antenna subtraction with identified hadrons

[Gehrmann, GS 2022]

$$e^+e^- \rightarrow h + X(+\text{jets})$$

$$d\hat{\sigma} = d\hat{\sigma}^{\text{LO}} + \left(\frac{\alpha_s}{2\pi}\right) d\hat{\sigma}^{\text{NLO}} + \left(\frac{\alpha_s}{2\pi}\right)^2 d\hat{\sigma}^{\text{NNLO}}$$

Deal with infrared divergences in the intermediate steps of the calculations, by introducing subtraction terms and adding them back analytically integrated

$$d\hat{\sigma}^{\text{LO}} = \int_n [d\hat{\sigma}^{\text{B}}]$$

$$d\hat{\sigma}^{\text{NLO}} = \int_{n+1} [d\hat{\sigma}^{\text{R}} - d\hat{\sigma}^{\text{S}}] + \int_n [d\hat{\sigma}^{\text{V}} - d\hat{\sigma}^{\text{T}} - \underline{d\hat{\sigma}^{\text{MF}}}]$$

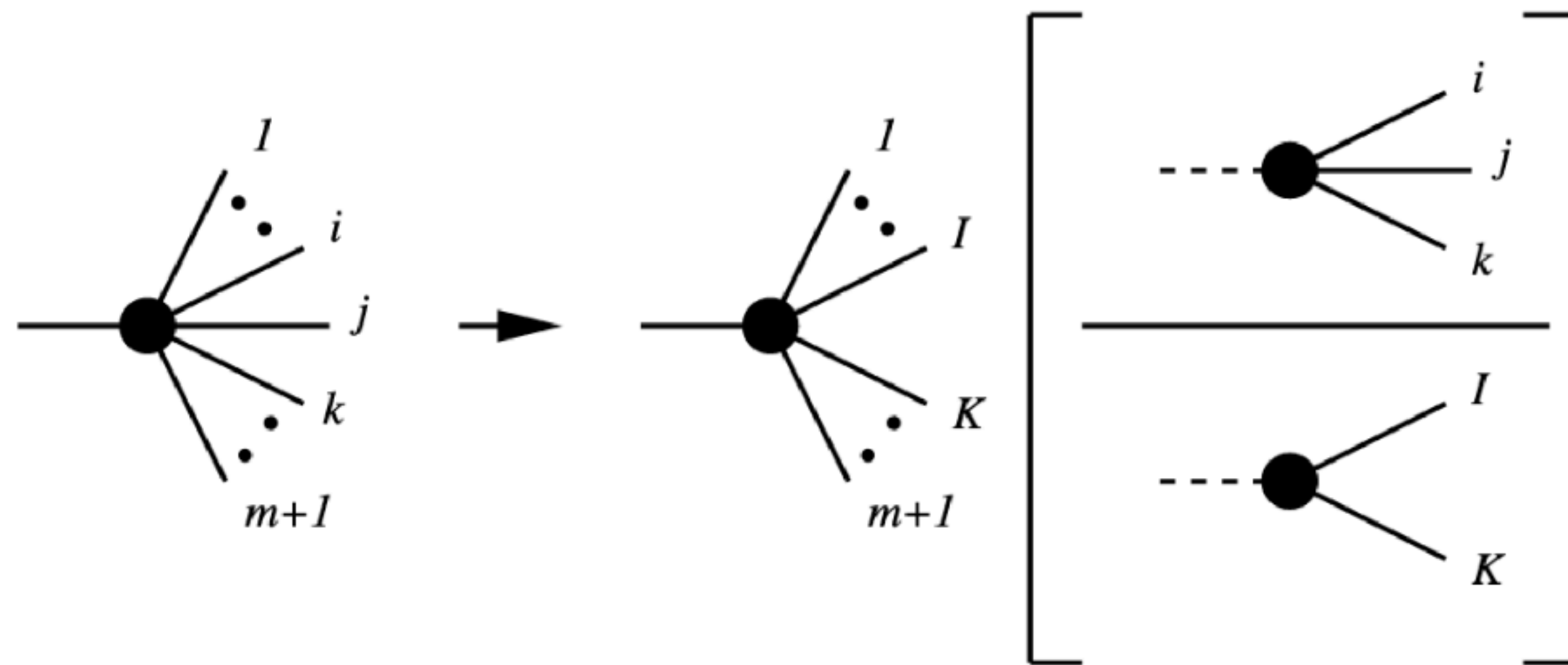
Timelike  
mass factorisation

$$d\hat{\sigma}^{\text{NNLO}} = \int_{n+2} [d\hat{\sigma}^{\text{RR}} - d\hat{\sigma}^{\text{S}}] + \int_{n+1} [d\hat{\sigma}^{\text{RV}} - d\hat{\sigma}^{\text{T}} - \underline{d\hat{\sigma}^{\text{MF,RV}}}] + \int_n [d\hat{\sigma}^{\text{VV}} - d\hat{\sigma}^{\text{U}} - \underline{d\hat{\sigma}^{\text{MF,VV}}}]$$



# NLO real subtraction term $d\hat{\sigma}^S$

Antenna functions encapsulate unresolved radiation between a pair of hard emitters



$X(p_i, p_j, p_k)$  = **antenna function**  
(basically matrix element  
of simple processes,  
properly normalised)

$M_n(\dots, \tilde{p}_{ij}, \tilde{p}_{jk}, \dots)$  = **reduced  
matrix element with mapped  
momenta**

$$M_{n+1}(\text{original momenta}) \rightarrow M_n(\text{mapped momenta}) \times X(\text{original momenta})$$

If the identified particle not involved in the infrared limit,  
just standard momentum mapping [Gehrmann-De Ridder, Gehrmann, Glover 2005]

# NLO real subtraction term $d\hat{\sigma}^S$

When the **identified parton**  $k_p$  is involved in the antenna, we need a **new mapping**:

$$M(k_1, \dots, k_p, k_j, k_k, \dots, k_{1+m}) \rightarrow M(k_1, \dots, K_p, K, \dots, k_{1+m}) \times X(k_p, k_j, k_k)$$

$$z = \frac{s_{pj} + s_{pk}}{s_{pj} + s_{pk} + s_{jk}}, \quad K_p = k_p/z, \quad K = k_j + k_k - (1-z)\frac{k_p}{z}$$

The phase space factorises as:

$$d\Phi_{m+1}(k_1, \dots, k_p, k_j, k_k, \dots, k_{m+1}) = d\Phi_m(k_1, \dots, K_p, K, \dots, k_{m+1}) \frac{q^2}{2\pi} d\Phi_2(k_j, k_k; q - k_h) z^{1-2\epsilon} dz$$

$$q = k_j + k_k + k_h$$



# NLO virtual subtraction term $d\hat{\sigma}^T$

We analytically integrate the antenna function, by leaving an **explicit dependence** on  $z$ :

$$\mathcal{X}_{30}^{\text{id}.p}(z) = \frac{1}{C(\epsilon)} \int d\Phi_2 \frac{q^2}{2\pi} z^{1-2\epsilon} X_{30}^{\text{id}.p}, \quad C(\epsilon) = (4\pi e^{-\gamma_E})^\epsilon / (8\pi^2)$$

over the two-particle phase space with kinematics

$$q(q^2) + (-k_p) \rightarrow k_j + k_k, \quad s_{jk} = (q - k_p)^2 = q^2(1 - z)$$

The **poles** of the integrated antenna function **cancel** against some of the explicit poles of the virtual matrix element; the remaining poles are removed by the mass factorisation terms.

# Subtraction at NNLO

- *Double-real subtraction term*  $d\hat{\sigma}^S$ : single unresolved subtracted by  $X_3^0$ , double unresolved limit subtracted by  $X_4^0$ , with product of  $X_3^0 X_3^0$  to avoid over-subtraction; large-angle soft subtraction terms. With identified particle, generalisation of NLO mapping:

$$z = \frac{s_{pj} + s_{pk} + s_{pl}}{s_{pj} + s_{pk} + s_{jk} + s_{pl} + s_{jl} + s_{kl}}, \quad K_p = k_p/z, \quad K = k_j + k_k + k_l - (1 - z)\frac{k_p}{z}$$

- *Real-virtual subtraction term*  $d\hat{\sigma}^V$ : explicit poles cancel against integration of  $X_3^0$  and mass factorisation terms; single unresolved limit subtracted by  $X_3^0 M_n^1 + X_3^1 M_n^0$ .

- *Double-virtual subtraction term*: no unresolved limits; all the explicit poles cancel against integrated pieces from the layers above, and mass factorisation terms.



# Integration of NNLO antenna functions

$$\mathcal{X}_{40}^{\text{id.}p}(z) = \frac{1}{[C(\varepsilon)]^2} \int d\Phi_3 \frac{q^2}{2\pi} z^{1-2\varepsilon} X_{40}^{\text{id.}p} \quad \mathcal{X}_{31}^{\text{id.}p}(z) = \frac{1}{C(\varepsilon)} \int d\Phi_2 \frac{q^2}{2\pi} z^{1-2\varepsilon} X_{31}^{\text{id.}p}$$

with kinematics:  $q(q^2) + (-k_p) \rightarrow k_1 + k_2(+k_3)$ ,  $s = q^2(1 - z)$

Well-known technique: phase space expressed in terms of cut propagators; reduction to master integrals with Reduze [Manteuffel, Studerus 2012]; master integrals derived by explicit evaluation or via differential equations [Gehrmann, Remiddi 2000] in the canonical form [Henn 2015]; solutions in terms of harmonic polylogarithms [Remiddi, Vermaseren 2000] with boundary conditions fixed by internal consistency or explicit evaluation at  $z = 1$ ; finally expansion of  $(1 - z)^{-2\varepsilon}$  in term of distributions.

**All analytical ingredients for identified hadron production in  $e^+e^-$  available**

**First application: hadron-in-jet fragmentation in  $e^+e^- \rightarrow 3$  jets**

[work in progress Bonino, GS et al.]

# Checks

Since antenna functions are derived from physical matrix elements, we can check integrated expressions against known analytical results for **one-particle inclusive coefficient functions**  $\mathbb{C}_j$

$$\frac{d\sigma^H}{dx} = \sum_{i=q,\bar{q},g} \int_x^1 \frac{dz}{z} D_i^H \left( \frac{x}{z} \right) \frac{d\sigma_i^H}{dz} = \sum_j \sigma_j^{(0)} \int_x^1 \frac{dz}{z} D_j^H \left( \frac{x}{z} \right) \mathbb{C}_j(z), \quad x = \frac{2E_h}{\sqrt{s}}$$

The coefficient functions can be expressed as a linear combination of:

$e^+e^- \rightarrow \gamma^* \rightarrow q\bar{q}$  [Rijken, Van Neerven 1996,1997] [Mitov, Moch, Vogt 2006]

**quark-quark antennae  $\mathcal{A}, \mathcal{B}, \mathcal{C}$  + quark form factors**

$e^+e^- \rightarrow H \rightarrow gg$  [Almasy, Moch, and Vogt 2012]

**gluon-gluon antennae  $\mathcal{F}, \mathcal{G}, \mathcal{H}$  + gluon form factors**



# Moving towards $ep$ and $pp$ collisions

Missing ingredient: integrated antenna functions for unresolved radiation with **one hard radiator  $k_i$  in the initial state** and **one identified parton  $k_p$** , already developed in part in the context of photon fragmentation  
[Schürmann, Gehrmann 2022]

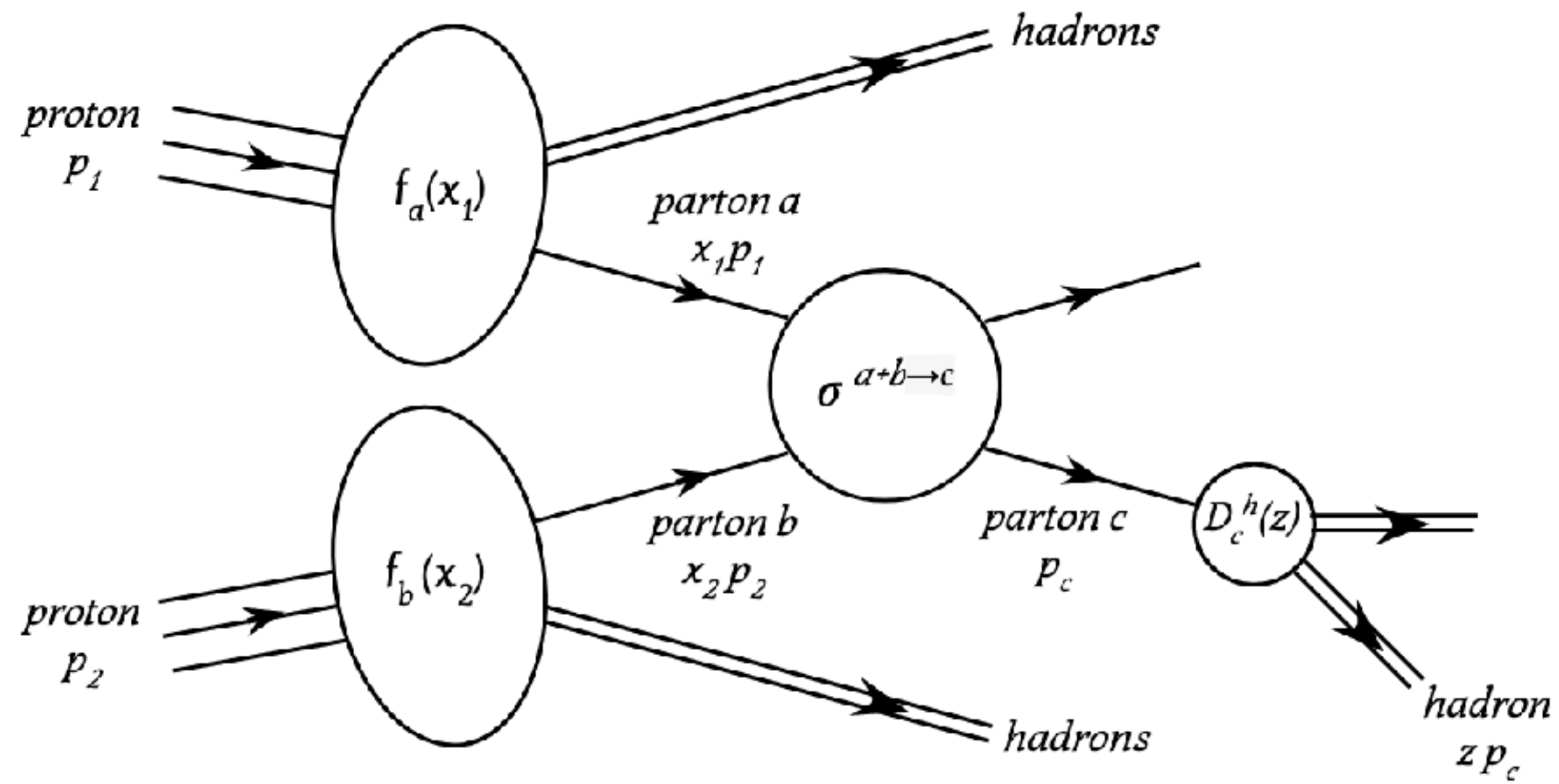
$$\mathcal{X}_{i,pkl}^{0,\text{id.p}} = \frac{1}{C(\varepsilon)^2} \int d\Phi_3(k_p, k_k, k_l; p_i, q) \delta \left( z - x \frac{(k_p + k_i)^2}{Q^2} \right) \frac{Q^2}{2\pi} X_{i,pkl}^0$$

with a different definition of  $z$ , where the initial state parton  $k_i$  acts as reference momentum

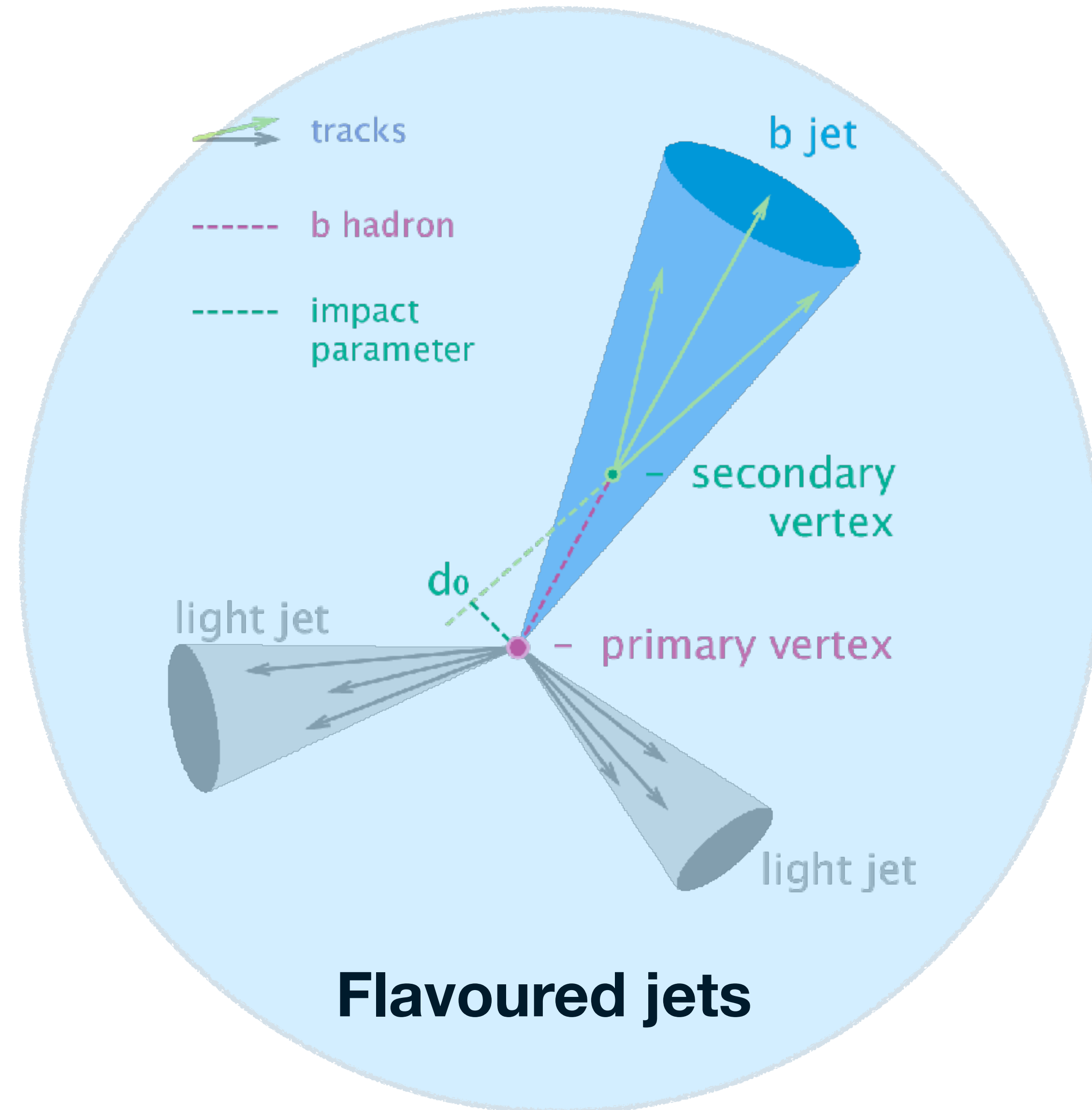
$$z = x \frac{(k_p + k_i)^2}{Q^2} = \frac{s_{pi}}{s_{pi} + s_{ki} + s_{li}} \equiv \frac{k_p \cdot k_i}{q \cdot k_i}$$

**Work ongoing**, we are integrating the missing antenna functions.  
Stay tuned for first applications!

# Two ways of looking at flavour



**Identified hadrons**

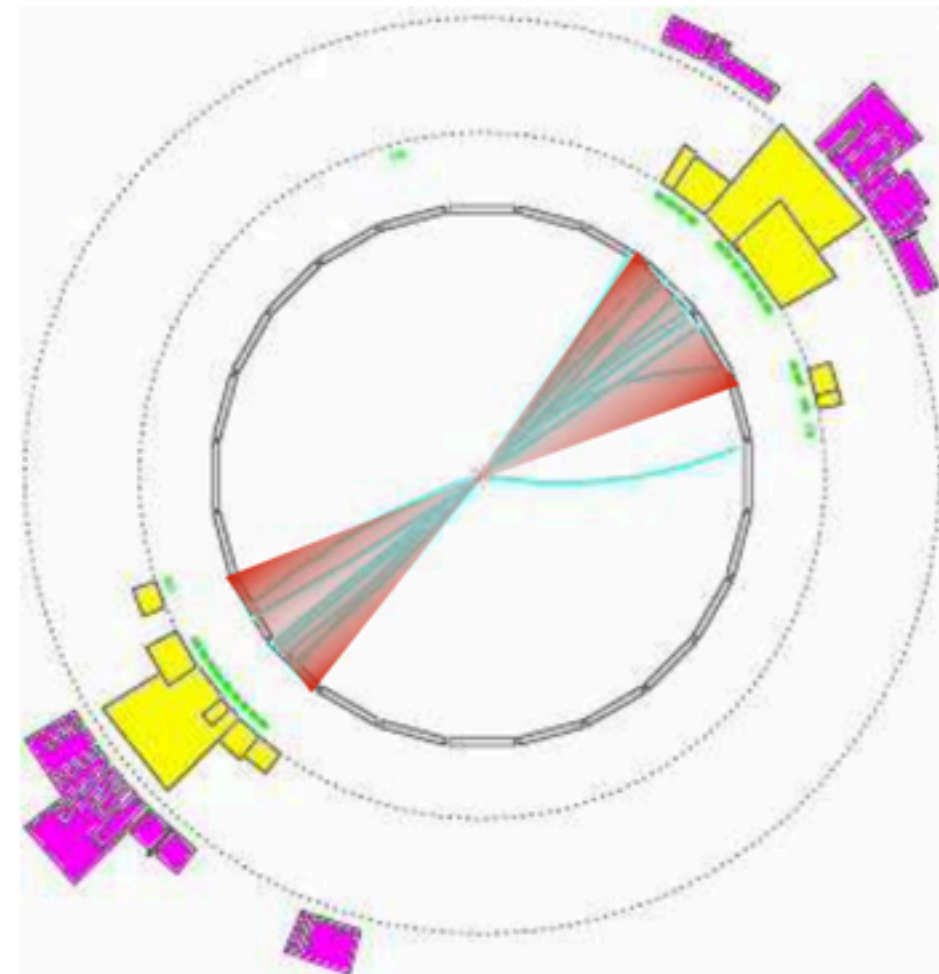


**Flavoured jets**

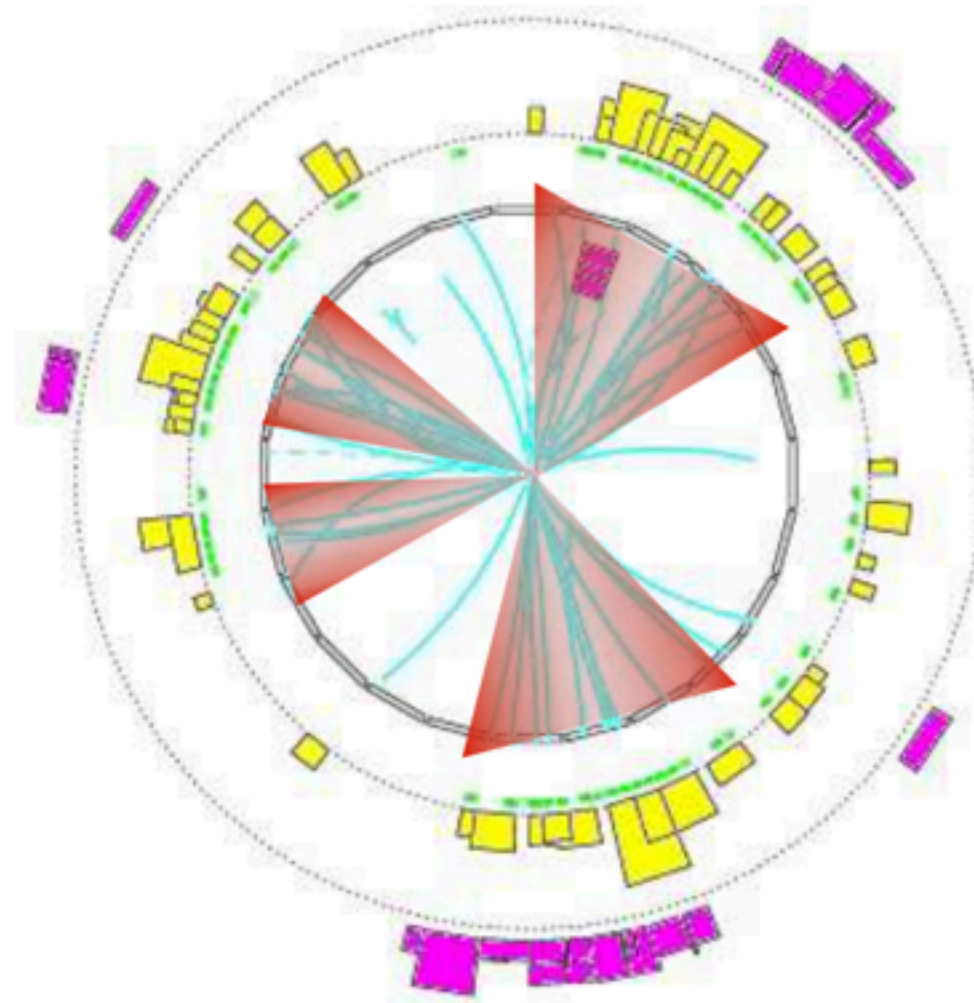


# What are jets?

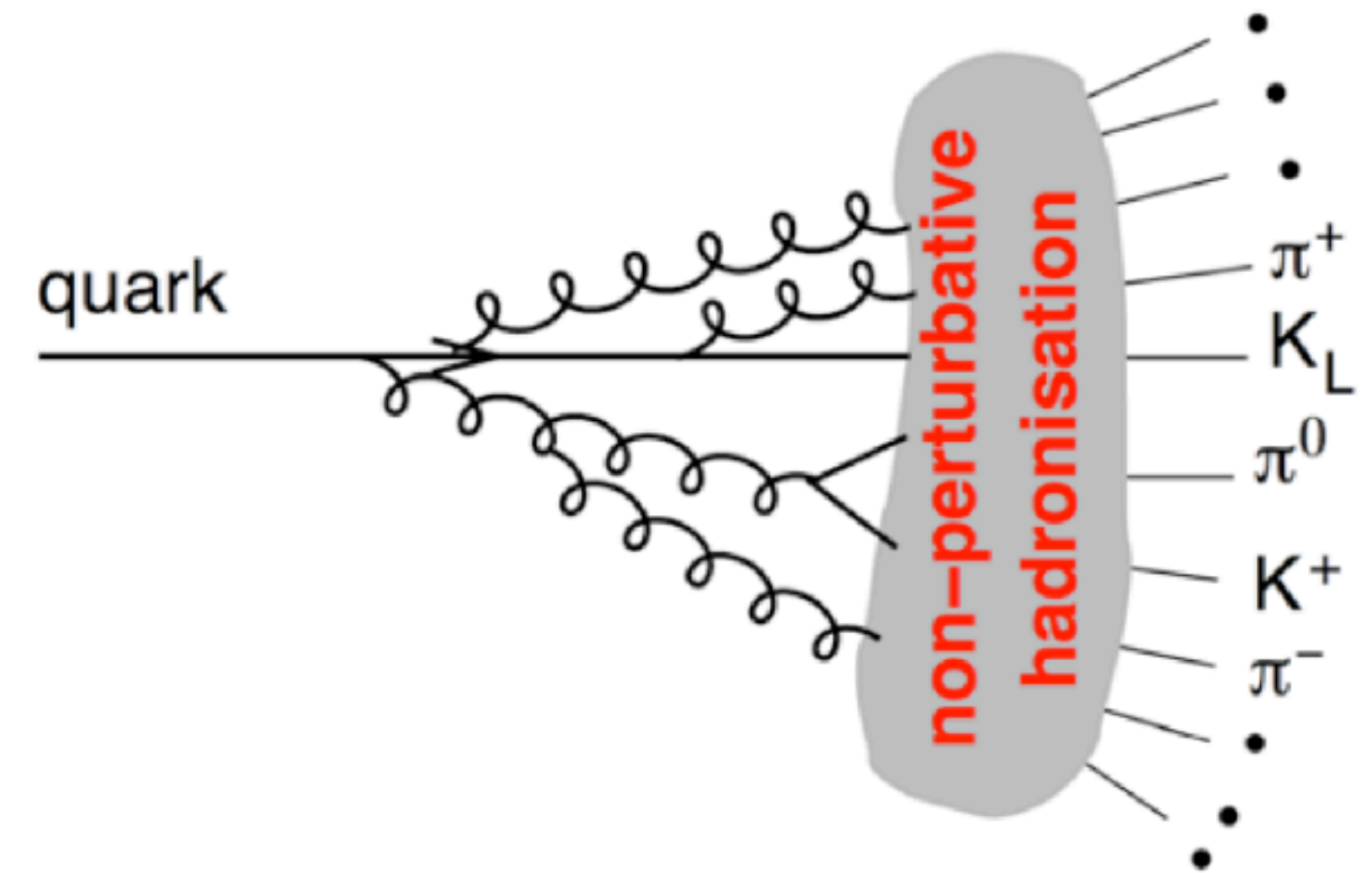
*Naive definition:* **collimated bunch of hadrons** flying roughly in the same direction



2 clear jets



3 jets?  
or 4 jets?



*Proper definition:* a collection of hadrons defined by means of a **jet algorithm**

*“Jet [definitions] are legal contracts between theorists and experimentalists”*

MJ Tannenbaum

# IRC safety

An observable is **infrared and collinear safe** if, in the limit of a **collinear splitting**, or the **emission of an infinitely soft** particle, the observable remains **unchanged**:

$$O(X; p_1, \dots, p_n, p_{n+1} \rightarrow 0) \rightarrow O(X; p_1, \dots, p_n)$$

$$O(X; p_1, \dots, p_n \parallel p_{n+1}) \rightarrow O(X; p_1, \dots, p_n + p_{n+1})$$

This property ensures cancellation of **real** and **virtual** divergences in higher order calculations

If we wish to be able to calculate a jet rate in perturbative QCD the jet algorithm that we use must be IRC safe:  
**soft emissions and collinear splittings must not change the hard jets**

slide stolen from Matteo Cacciari



# The $k_t$ algorithm and its siblings

$$d_{ij} = \min(p_{ti}^{2p}, p_{tj}^{2p}) \frac{\Delta y^2 + \Delta \phi^2}{R^2} \quad d_{iB} = p_{ti}^{2p}$$

**p = 1**  $k_t$  algorithm

S. Catani, Y. Dokshitzer, M. Seymour and B. Webber, Nucl. Phys. B406 (1993) 187  
S.D. Ellis and D.E. Soper, Phys. Rev. D48 (1993) 3160

**p = 0** Cambridge/Aachen algorithm

Y. Dokshitzer, G. Leder, S. Moretti and B. Webber, JHEP 08 (1997) 001  
M. Wobisch and T. Wengler, hep-ph/9907280

**p = -1** **anti- $k_t$  algorithm**

MC, G. Salam and G. Soyez, arXiv:0802.1189

NB: in anti- $k_t$  pairs with a **hard** particle will cluster first: if no other hard particles are close by, the algorithm will give **perfect cones**

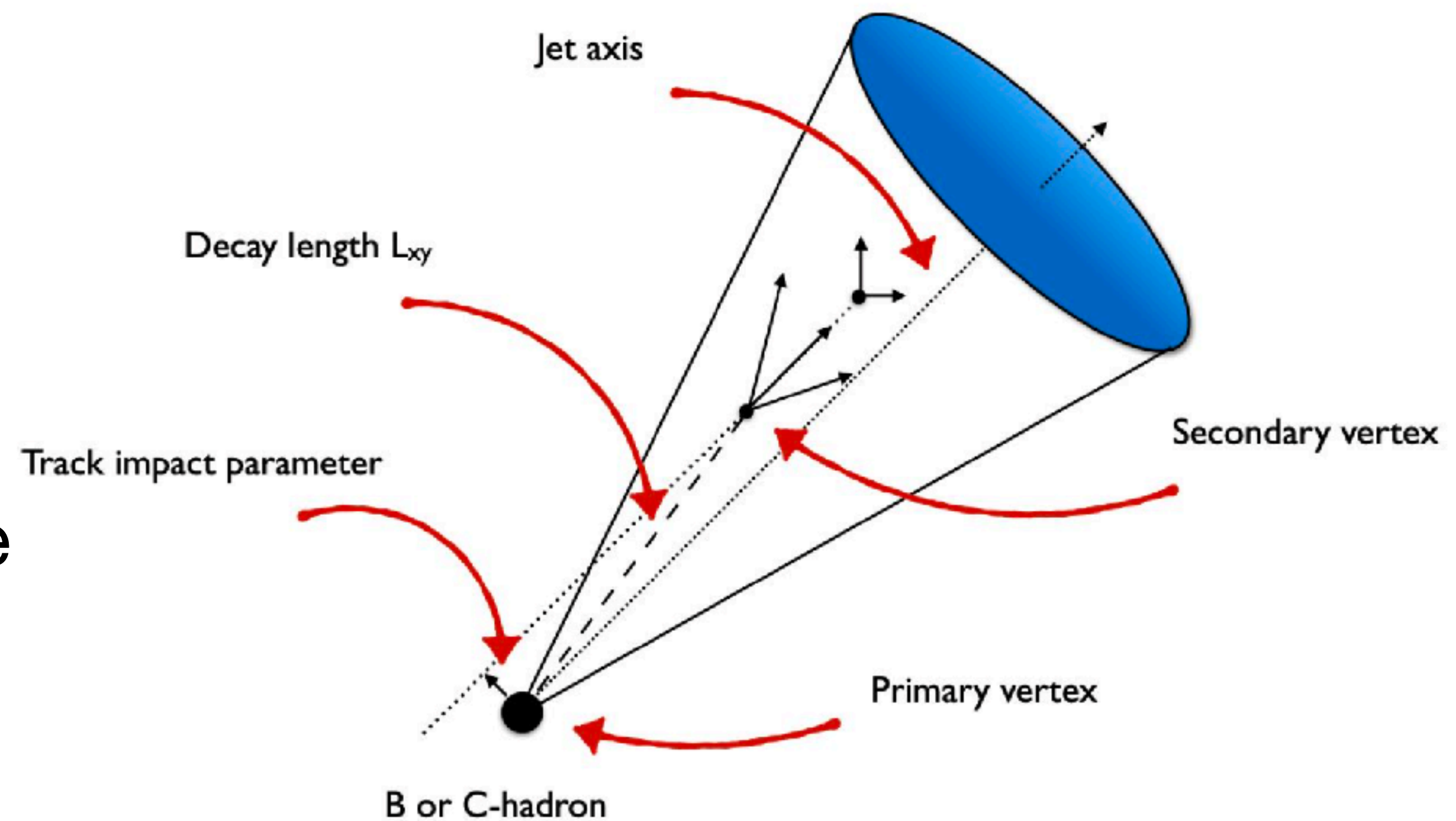
slide stolen from Matteo Cacciari



# (Usual) experimental definition of flavoured jet

A jet is defined as flavoured if it contains  
at least one heavy hadron  
within  $\Delta R < R$  from the jet axis  
and with  $p_T > p_{T,\text{cut}}$

This is the “truth” labelling used in Monte Carlo samples, used to train a ML architecture (“high-level tagger”) which adopts low-level variables as inputs



# IRC flavour safety

The experimental definition is both **collinear and soft unsafe**  
(in massless fixed order calculations)

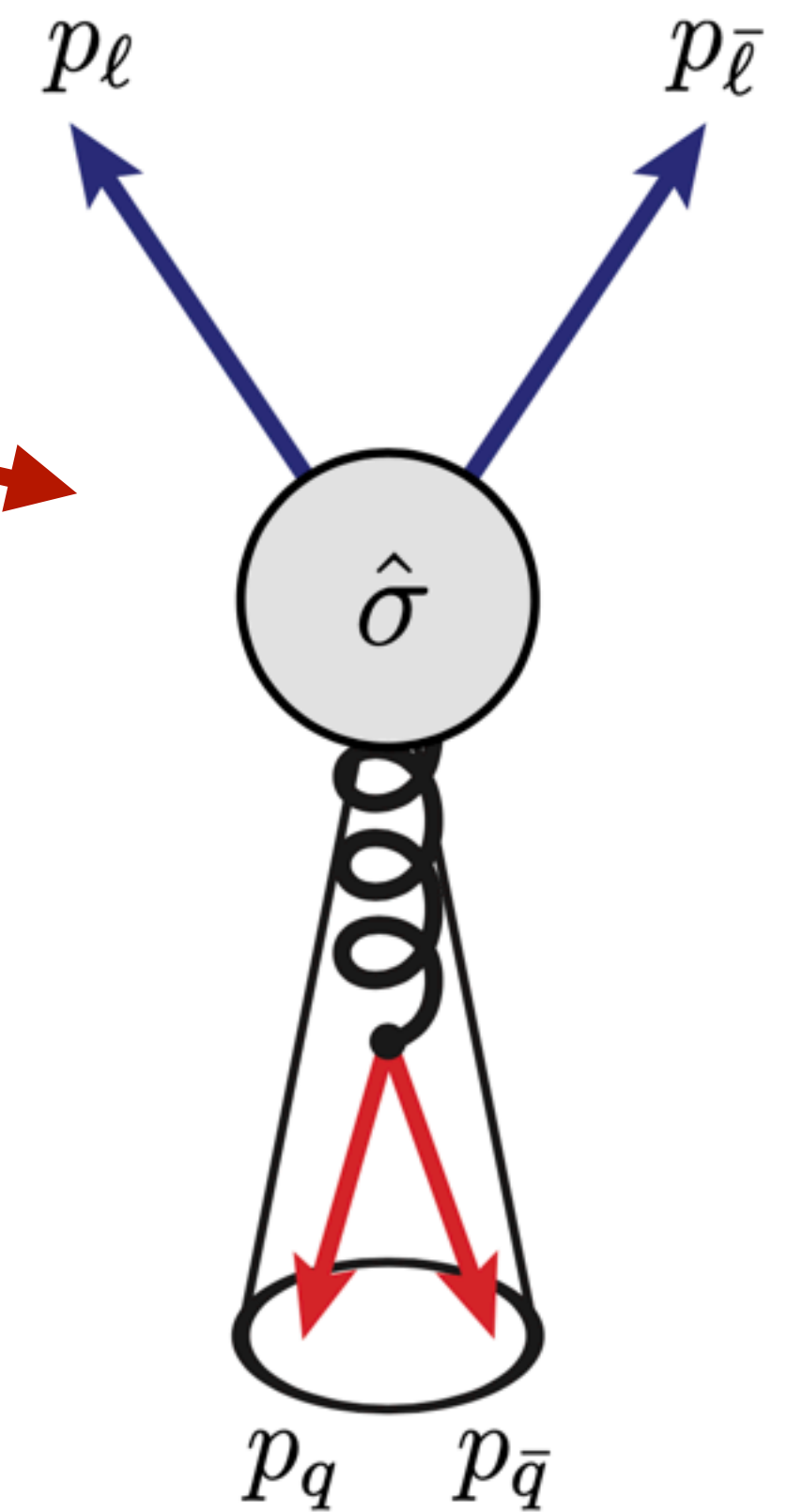
“A jet defined as flavoured if it contains  
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and with  $p_T > p_{T,\text{cut}}$ ”

*$g \rightarrow b\bar{b}$  is always flavoured  
even in the collinear limit  
(an “even tag” removal is  
enough to fix this)*



drawing stolen from Rhorry Gauld

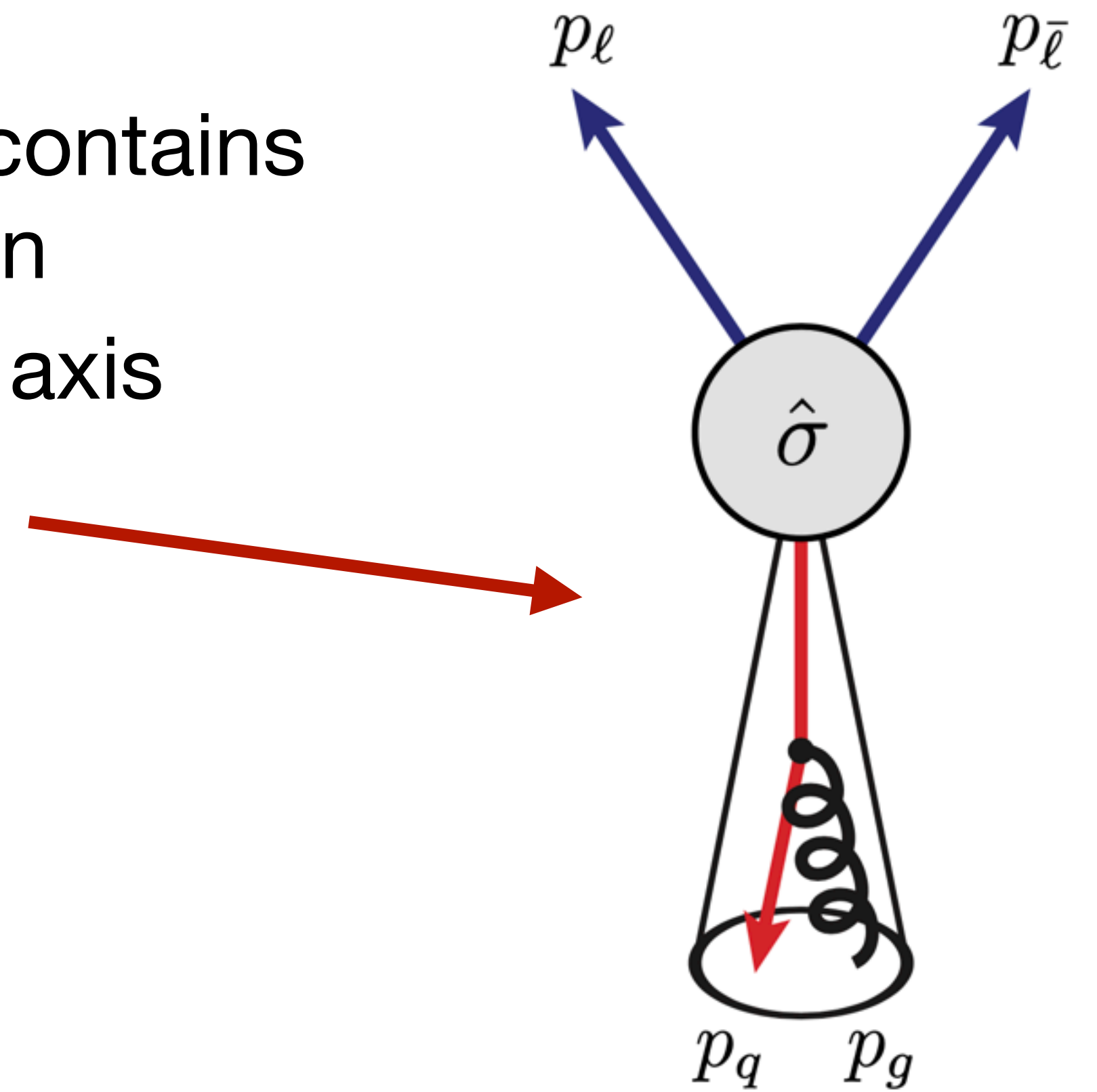


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within  $\Delta R < R$  from the jet axis  
and with  $p_T > p_{T,\text{cut}}$ ”

*$b \rightarrow bg$  collinear with the gluon carrying  
most of the momentum  
(would be ok with fragmentation function)*



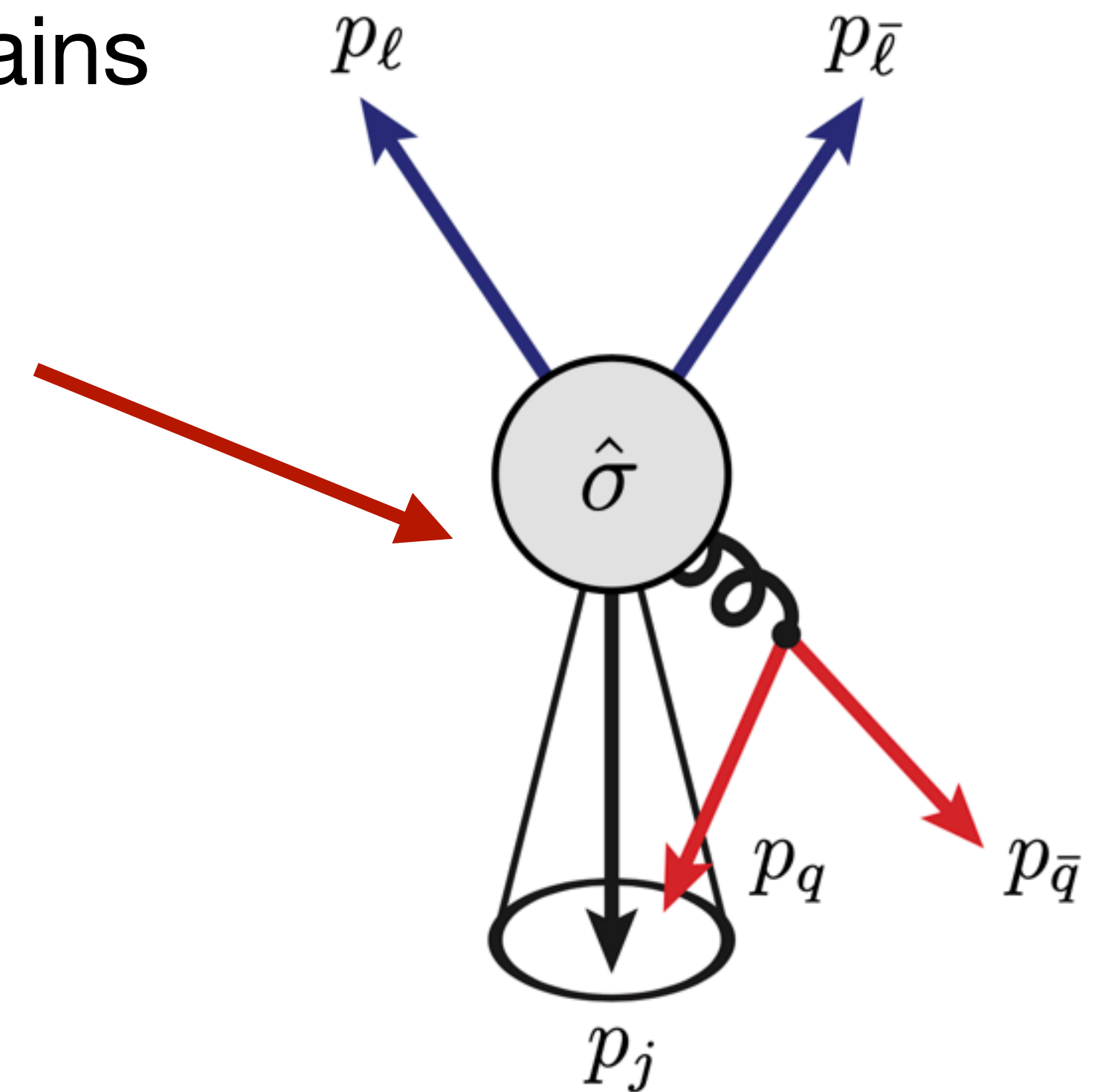
drawing stolen from Rhorry Gauld

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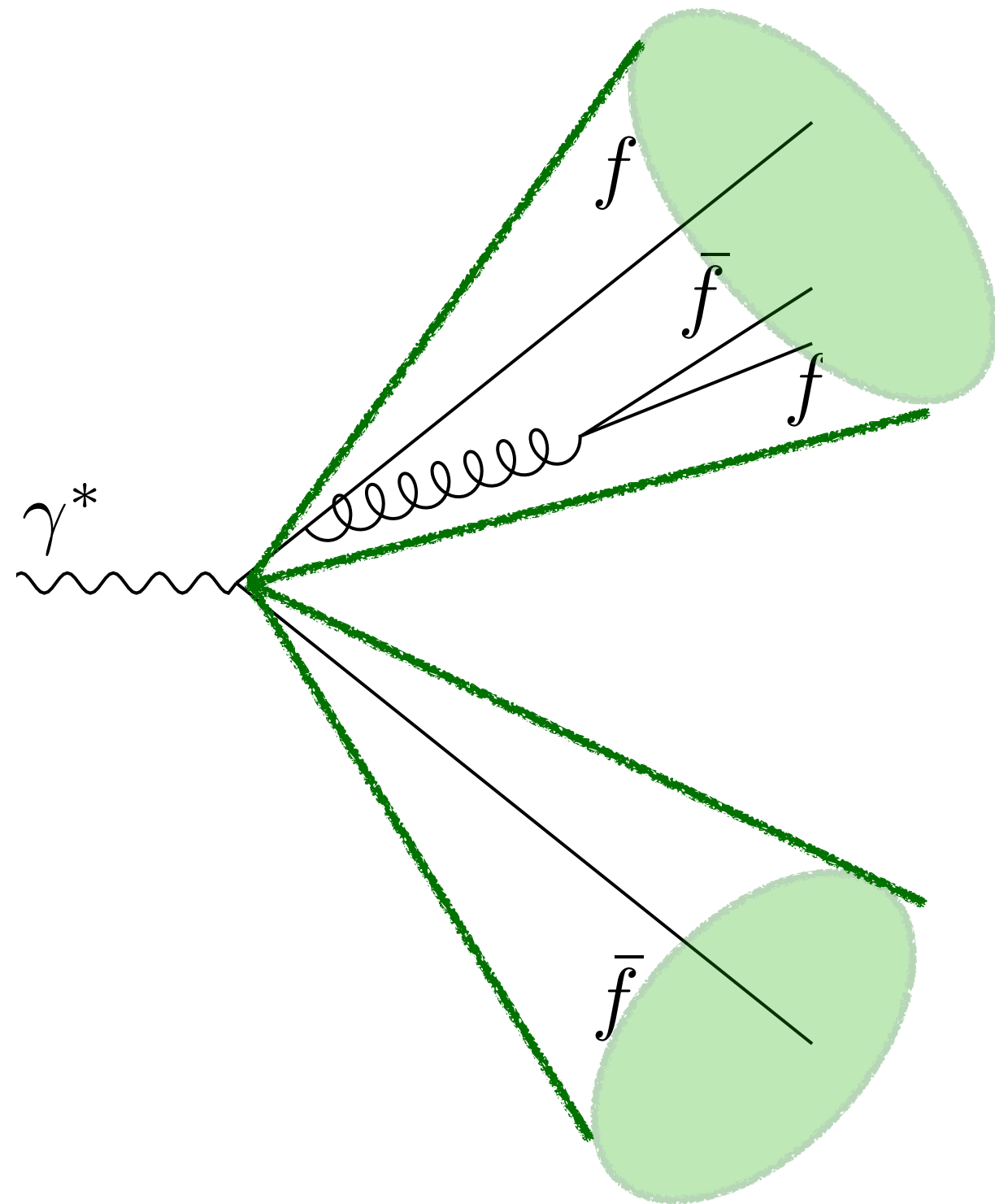
*Soft large angle  $g \rightarrow b\bar{b}$   
polluting different jets*



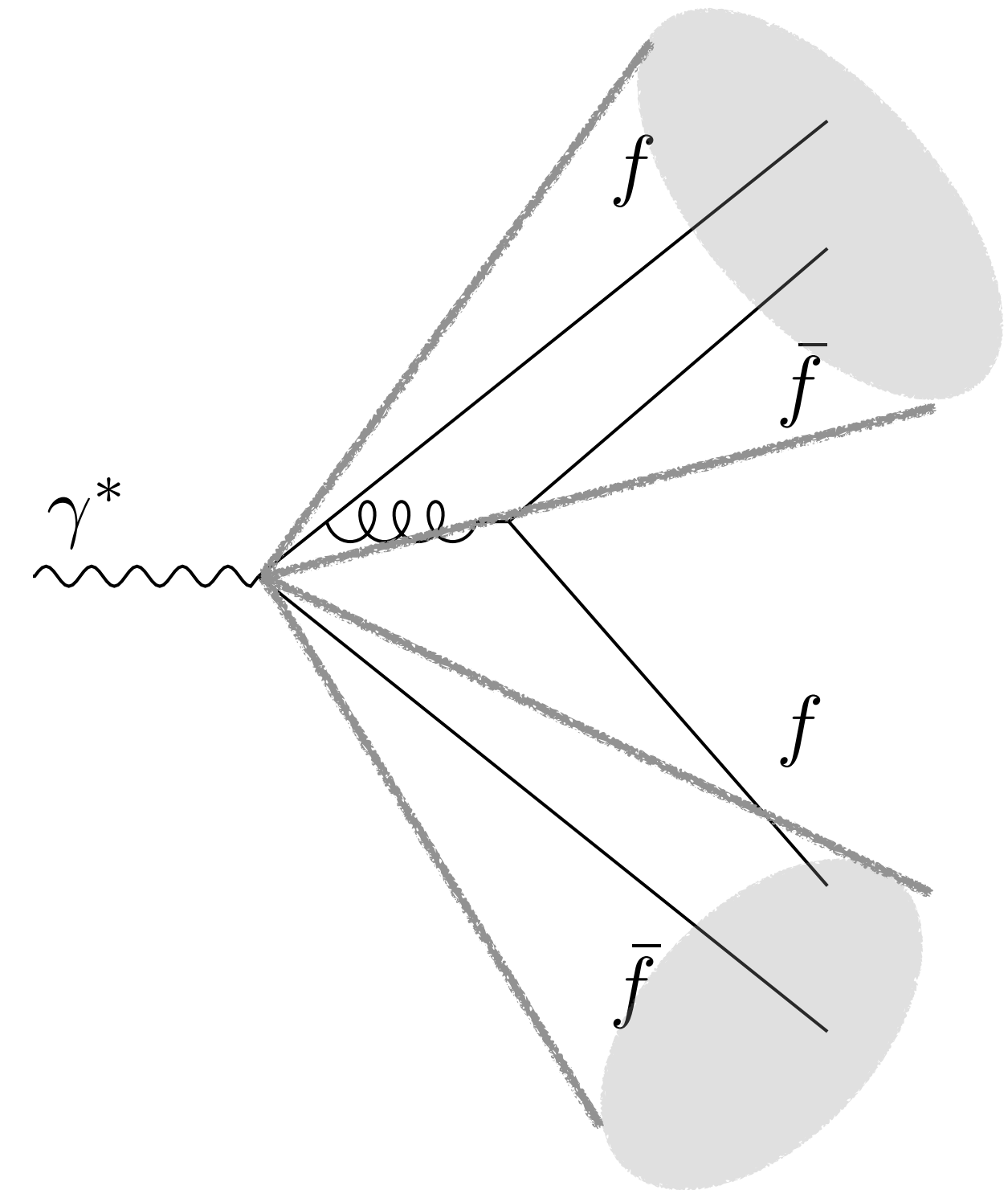
drawing stolen from Rhorry Gauld

# Example: $e^+e^-$ to 2 flavoured jets with $k_t$ algorithm

In the soft and collinear limits, we should obtain two flavoured jets



$\mathcal{O}(\alpha_s^2)$  with a  $f\bar{f}$  collinear pair:  
any IRC safe algorithm is OK



$\mathcal{O}(\alpha_s^2)$  with a  $f\bar{f}$  soft pair:  
large-angle polluting issue



# The flavour- $k_t$ algorithm

[Banfi, Salam, Zanderighi (hep-ph/0601139)]

1. Introduce a distance measure  $d_{ij}^{(F)}$  between every pair of partons  $i, j$ :

$$d_{ij}^{(F,\alpha)} = (\Delta\eta_{ij}^2 + \Delta\phi_{ij}^2) \times \begin{cases} \max(k_{ti}, k_{tj})^\alpha \min(k_{ti}, k_{tj})^{2-\alpha}, & \text{softer of } i, j \text{ is flavoured,} \\ \min(k_{ti}^2, k_{tj}^2), & \text{softer of } i, j \text{ is flavourless,} \end{cases} \quad (17)$$

as well as distances to the two beams,

$$d_{iB}^{(F,\alpha)} = \begin{cases} \max(k_{ti}, k_{tB}(\eta_i))^\alpha \min(k_{ti}, k_{tB}(\eta_i))^{2-\alpha}, & i \text{ is flavoured,} \\ \min(k_{ti}^2, k_{tB}^2(\eta_i)), & i \text{ is flavourless,} \end{cases} \quad (18)$$

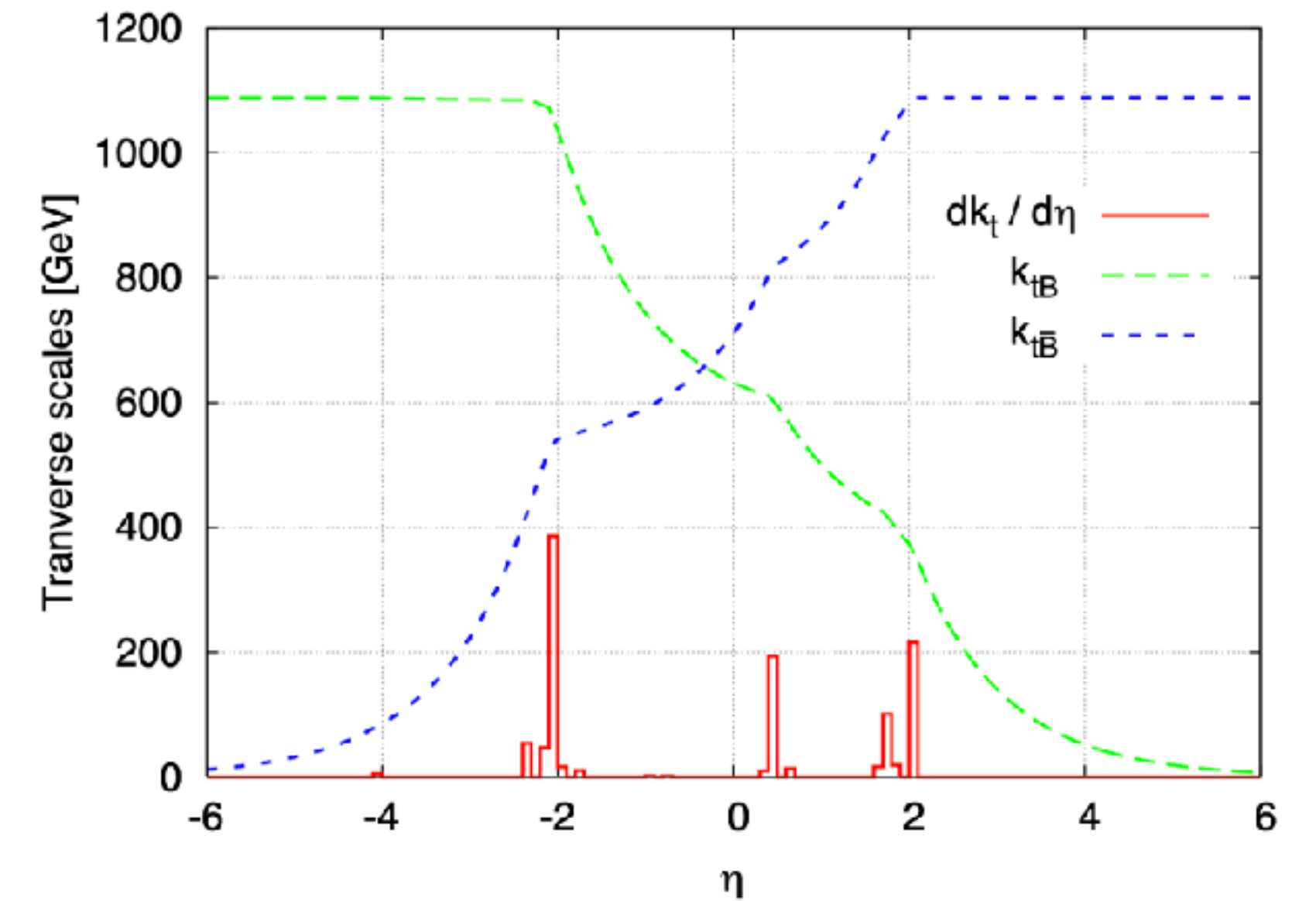
and an analogous definition of  $d_{i\bar{B}}^{(F,\alpha)}$  involving  $k_{t\bar{B}}(\eta_i)$  instead of  $k_{tB}(\eta_i)$  (both defined as in eqs. (15) and (16)).<sup>9</sup> As in section 2 we have introduced a class of measures, parametrised by  $0 < \alpha \leq 2$ .

2. Identify the smallest of the distance measures. If it is a  $d_{ij}^{(F,\alpha)}$ , recombine  $i$  and  $j$ ; if it is a  $d_{iB}^{(F,\alpha)}$  ( $d_{i\bar{B}}^{(F,\alpha)}$ ) declare  $i$  to be part of beam  $B$  ( $\bar{B}$ ) and eliminate  $i$ ; in the case where the  $d_{iB}^{(F,\alpha)}$  and  $d_{i\bar{B}}^{(F,\alpha)}$  are equal (which will occur if  $i$  is a gluon), recombine with the beam that has the smaller  $k_{tB}(\eta_i)$ ,  $k_{t\bar{B}}(\eta_i)$ .
3. Repeat the procedure until all the distances are larger than some  $d_{cut}$ , or, alternatively, until one reaches a predetermined number of jets.<sup>10,11</sup>

Modified beam distance:

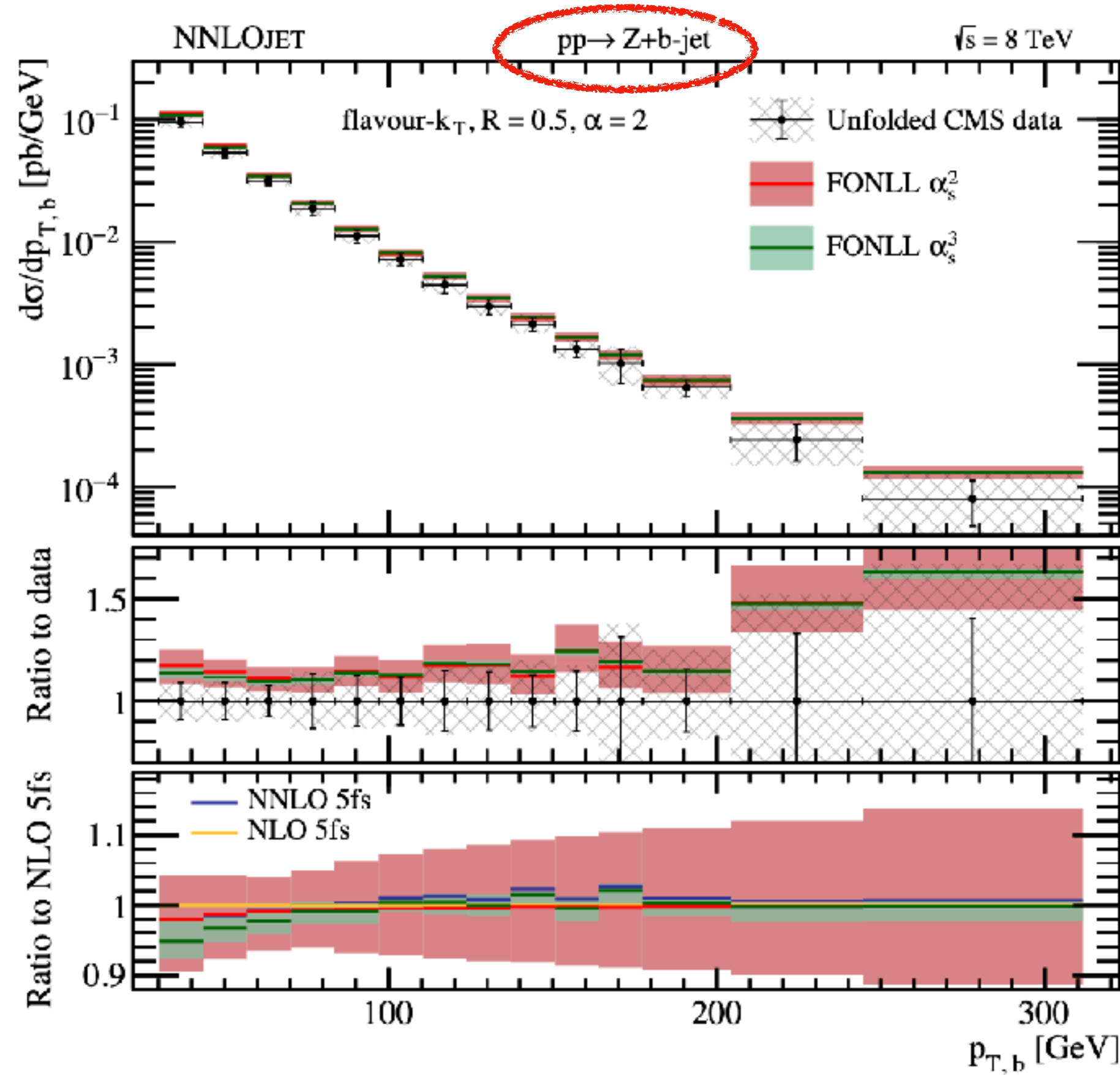
$$k_{tB}(\eta) = \sum_i k_{ti} (\Theta(\eta_i - \eta) + \Theta(\eta - \eta_i) e^{\eta_i - \eta})$$

$$k_{t\bar{B}}(\eta) = \sum_i k_{ti} (\Theta(\eta - \eta_i) + \Theta(\eta_i - \eta) e^{\eta - \eta_i})$$

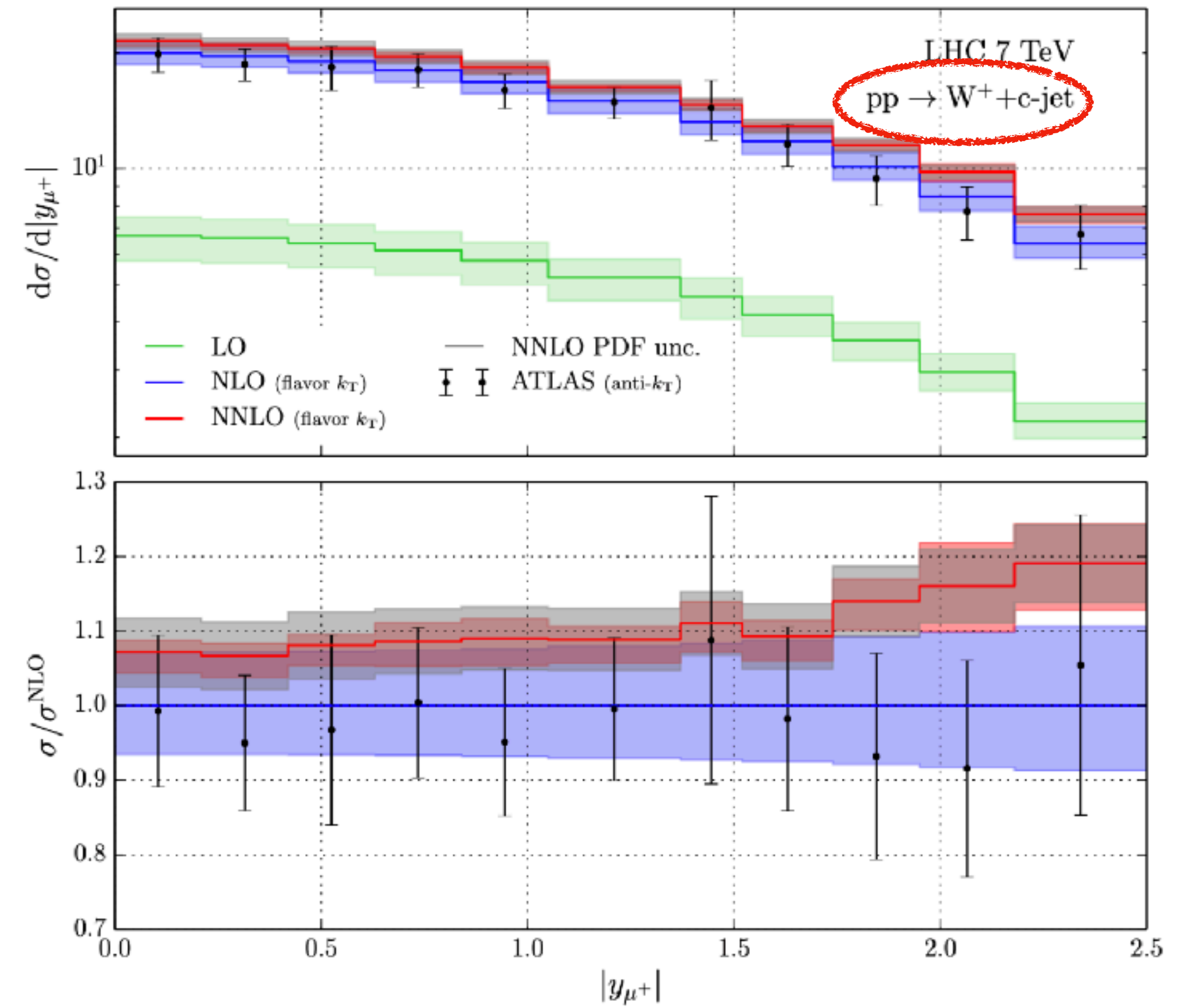


IRC flavour safe to all orders,  
but different kinematics  
(because new distance)

# Recent NNLO predictions with flavour- $k_t$



[Gauld et al. (2005.03016)]



[Czakon et al. (2011.01011)]

Comparison with experimental data **not straightforward**

# A lot of recent alternative proposals!

- based on Soft Drop grooming techniques  
[Caletti, Larkoski, Marzani, Reichelt (2205.01109)]
- through the alignment of particles along the Winner-Take-All axis  
[Caletti, Larkoski, Marzani, Reichelt (2205.01117)]
- through a modification of anti- $k_t$  clustering distance  
[Czakon, Mitov, Poncelet (2205.11879)]
- with successive iterations of flavour- $k_t$  and anti- $k_t$   
[Caletti, Fedkevych, Marzani, Reichelt (2108.10024)]
- using jet angularities and primary Lund jet plane as discriminants  
[Fedkevych, Khosa, Marzani, Sforza (2202.05082)]

However, none of the above reproduces the same jets as anti- $k_t$ ,  
can be applied to a generic process with one or more jets  
and it is IRC safe to all orders.



# The **flavour** dressing algorithm

[Gauld, Huss, GS (2208.11138)]

Flavour assignment *factorised* from jet reconstruction:  
**we assign flavour to flavour-agnostic jets in an IRC safe way**

Inputs:

flavour agnostic jets  $\{j_k\}$ , flavoured clusters  $\{\hat{f}_i\}$ , association criterion, accumulation criterion

Run a sequential recombination algorithm with flavour- $k_t$ -like distances:

- $d(\hat{f}_i, \hat{f}_j)$  between flavoured clusters;
- $d(\hat{f}_i, j_k)$  if flavoured cluster  $\hat{f}_i$  associated to jet  $j_k$
- $d_B(\hat{f}_i)$  if  $\hat{f}_i$  not associated to any jet

Finally, assign flavour to jet  $j_k$  according to collected tag  $g_k$  and *accumulation* criterion

# The **flavour** dressing algorithm: inputs

- *Flavour agnostic jets*  $\{j_k\}$ : set of jets obtained with an IRC safe jet algorithm (e.g. gen- $k_t$  family), possibly after a fiducial selection.
- *Flavoured clusters*  $\{\hat{f}_i\}$
- *Association criterion*
- *Accumulation criterion*

# The **flavour** dressing algorithm: inputs

- *Flavour agnostic jets*  $\{j_k\}$
- *Flavoured clusters*  $\{\hat{f}_i\}$ : built out of quarks (e.g. c, b) or stable heavy-flavour hadrons (e.g. D, B), by **dressing them with radiation close in angle, but without touching the soft particles.**

Exploiting the Soft Drop criterion [Larkoski, Marzani, Soyez, Thaler 1402.2657]

“Naked” flavoured objects are collinear unsafe

$$\frac{\min(p_{t,a}, p_{t,b})}{(p_{t,a} + p_{t,b})} > z_{\text{cut}} \left( \frac{\Delta R_{ab}}{\delta R} \right)^\beta$$

- *Association criterion*
- *Accumulation criterion*



# The **flavour** dressing algorithm: inputs

- *Flavour agnostic jets*  $\{j_k\}$
- *Flavoured clusters*  $\{\hat{f}_i\}$
- *Association criterion*: whether  $\hat{f}_i$  is “associated” to  $j_k$   
At parton-level simply if  $\hat{f}_i$  is a constituent of  $j_k$   
Other options:  $\Delta R(\hat{f}_i, j_k) < R_{\text{tag}}$ , ghost association, ...

Flavour assignment based only on association is soft unsafe

- *Accumulation criterion*

# The **flavour** dressing algorithm: inputs

- *Flavour agnostic jets*  $\{j_k\}$
- *Flavoured clusters*  $\{\hat{f}_i\}$
- *Association criterion*
- *Accumulation criterion*: how to “sum” flavours
  - sum flavoured if unequal number of  $f$  and  $\bar{f}$  (need charge information)
  - sum flavoured if odd number of  $f$  or  $\bar{f}$  (if no charge information)

# Definition of flavoured cluster $\hat{f}_i$

1. Initialise a set with all the flavourless objects  $p_i$  (particles used as input to jets) and all the flavoured objects  $f_i$  (bare flavours), avoiding double counting if necessary.
2. Find the pair with the smallest angular distance  $\Delta R_{ab}$ :
  - flavourless  $p_a, p_b$ : combine  $p_a$  and  $p_b$  into a flavourless  $p_{ab}$ ;
  - flavoured  $f_a, f_b$ : remove both from the set;
  - flavoured  $f_a$ , unflavoured  $p_b$ : remove  $p_b$  from the set and check a Soft Drop criterion

$$\frac{\min(p_{t,a}, p_{t,b})}{(p_{t,a} + p_{t,b})} > z_{\text{cut}} \left( \frac{\Delta R_{ab}}{\delta R} \right)^\beta$$

to **recombine collinear while preserving soft**. [default:  $\delta R = 0.1$ ,  $z_{\text{cut}} = 0.1$ ,  $\beta = 2$ ]

If satisfied, combine  $f_a$  and  $p_b$  into a flavoured  $f_{ab}$ .

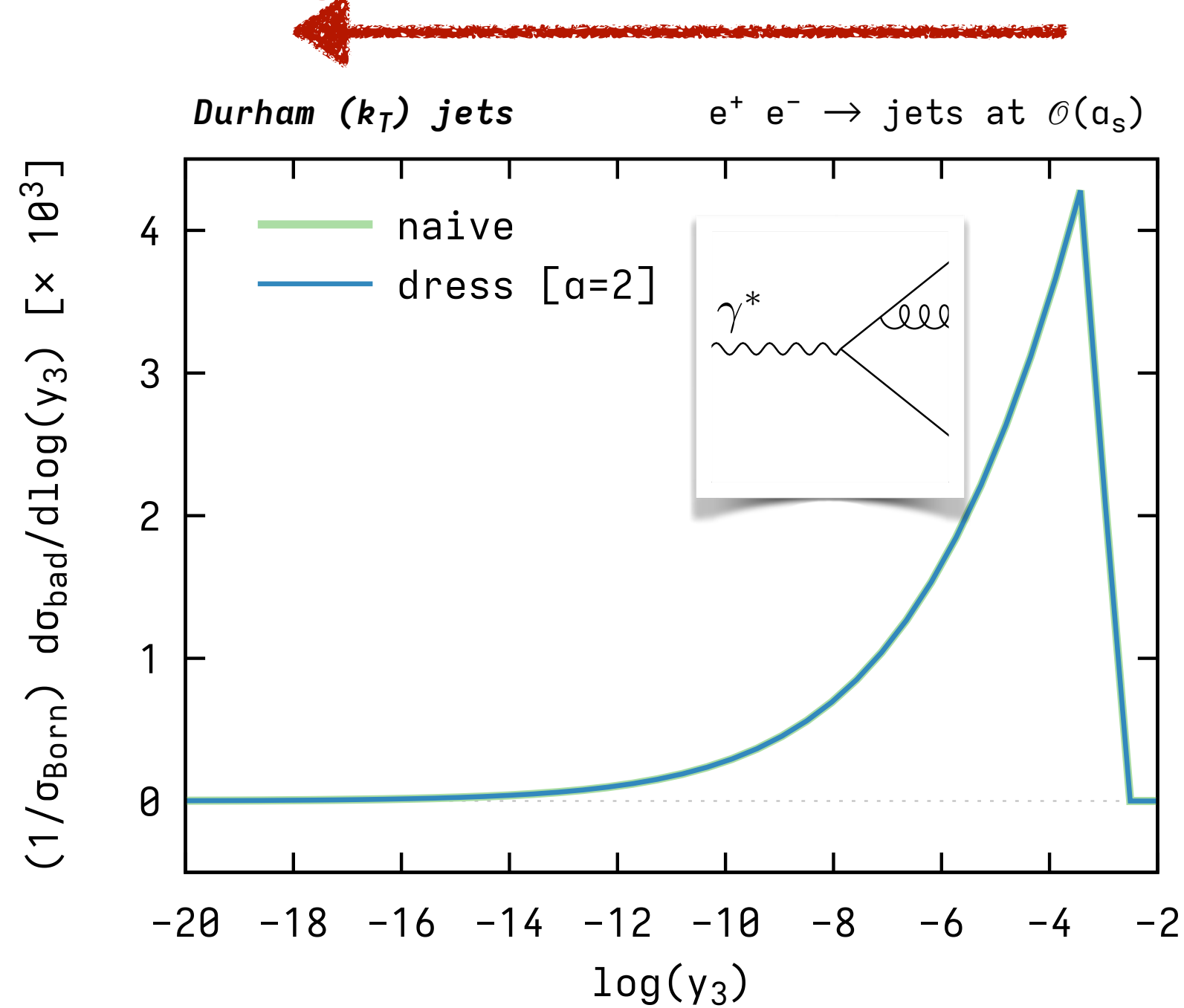
3. Iterate while there are at least two objects in the set until  $\Delta R_{ab} > \delta R$ .  
The momentum of  $\hat{f}_i$  is given by the accumulated momentum into  $f_i$ .



# IRC safety test in $e^+e^- \rightarrow \text{jets}$

Vanishing mis-identification of flavours in the fully unresolved regime = IRC safety

only soft and/or collinear radiation

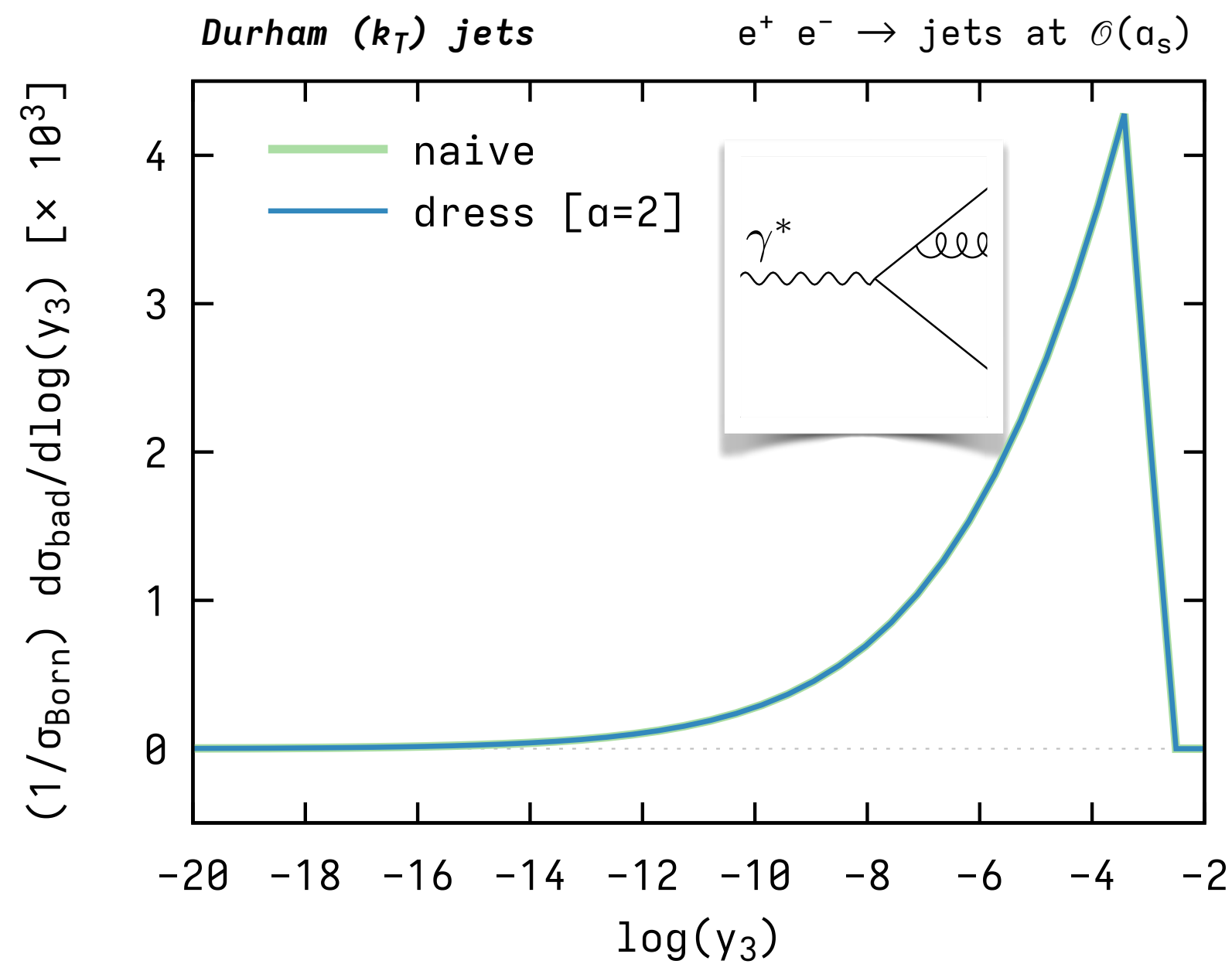


Any gen- $k_T$  algo is safe!

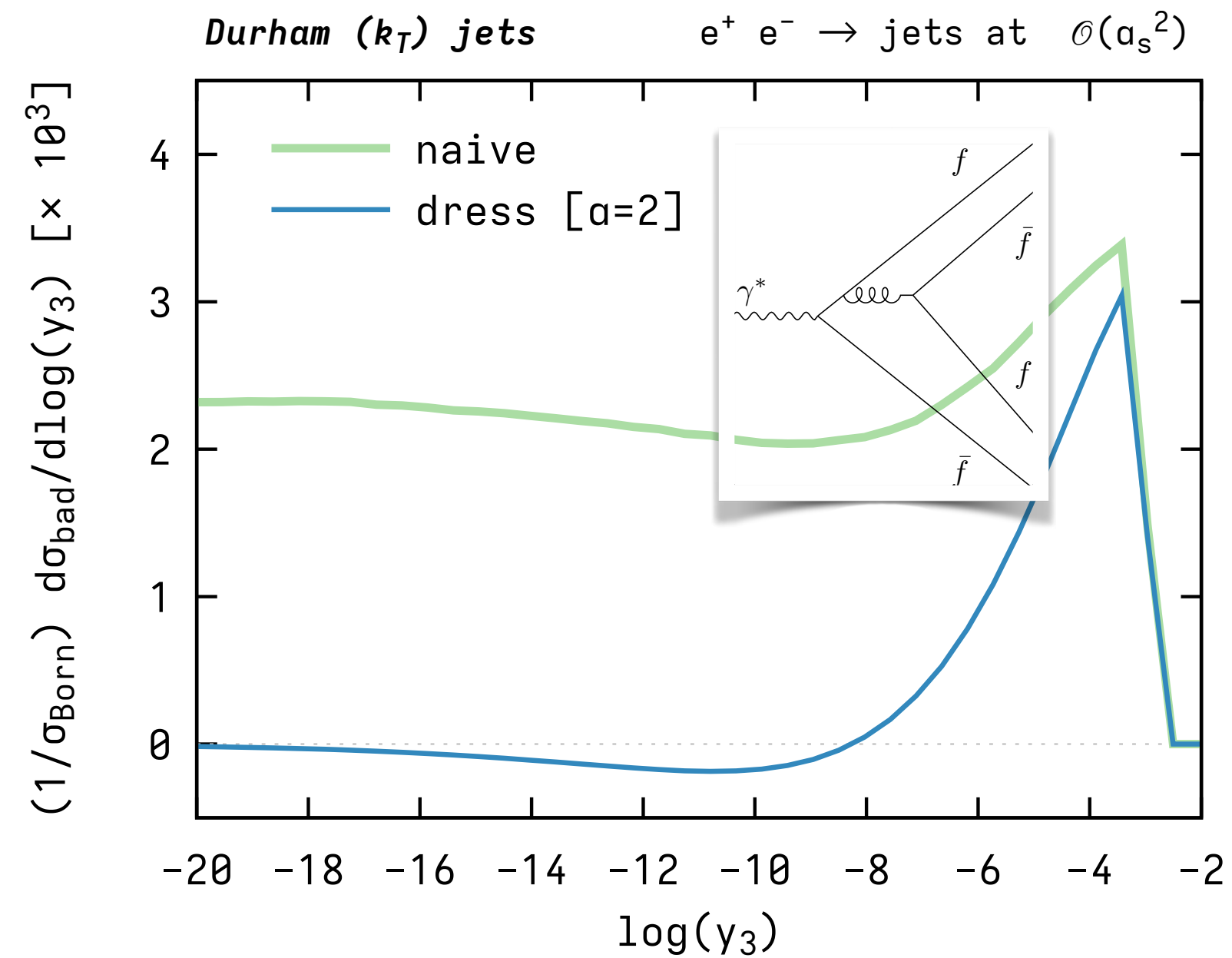
# IRC safety test in $e^+e^- \rightarrow \text{jets}$

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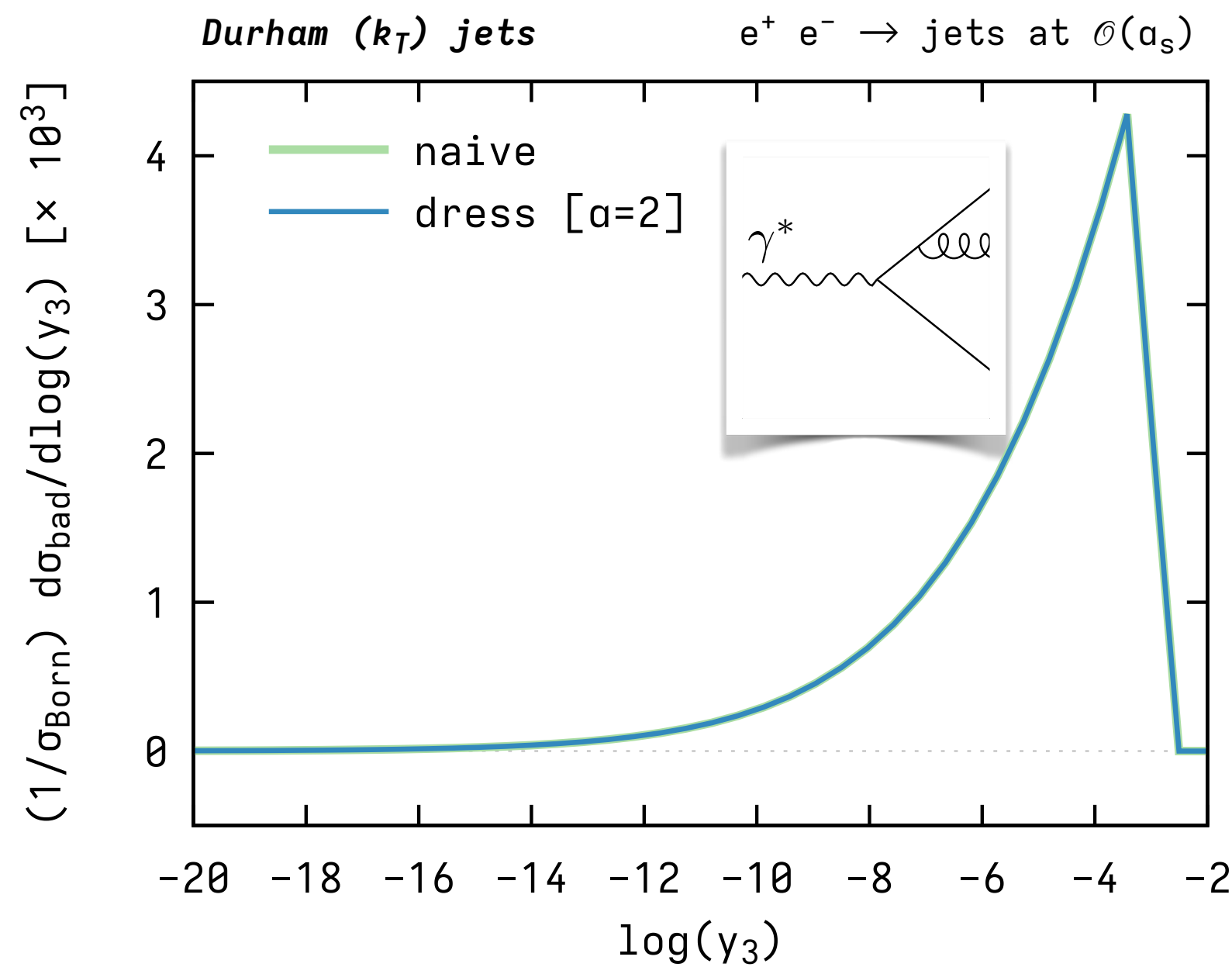


Naive dressing unsafe,  
flavour dressing safe!

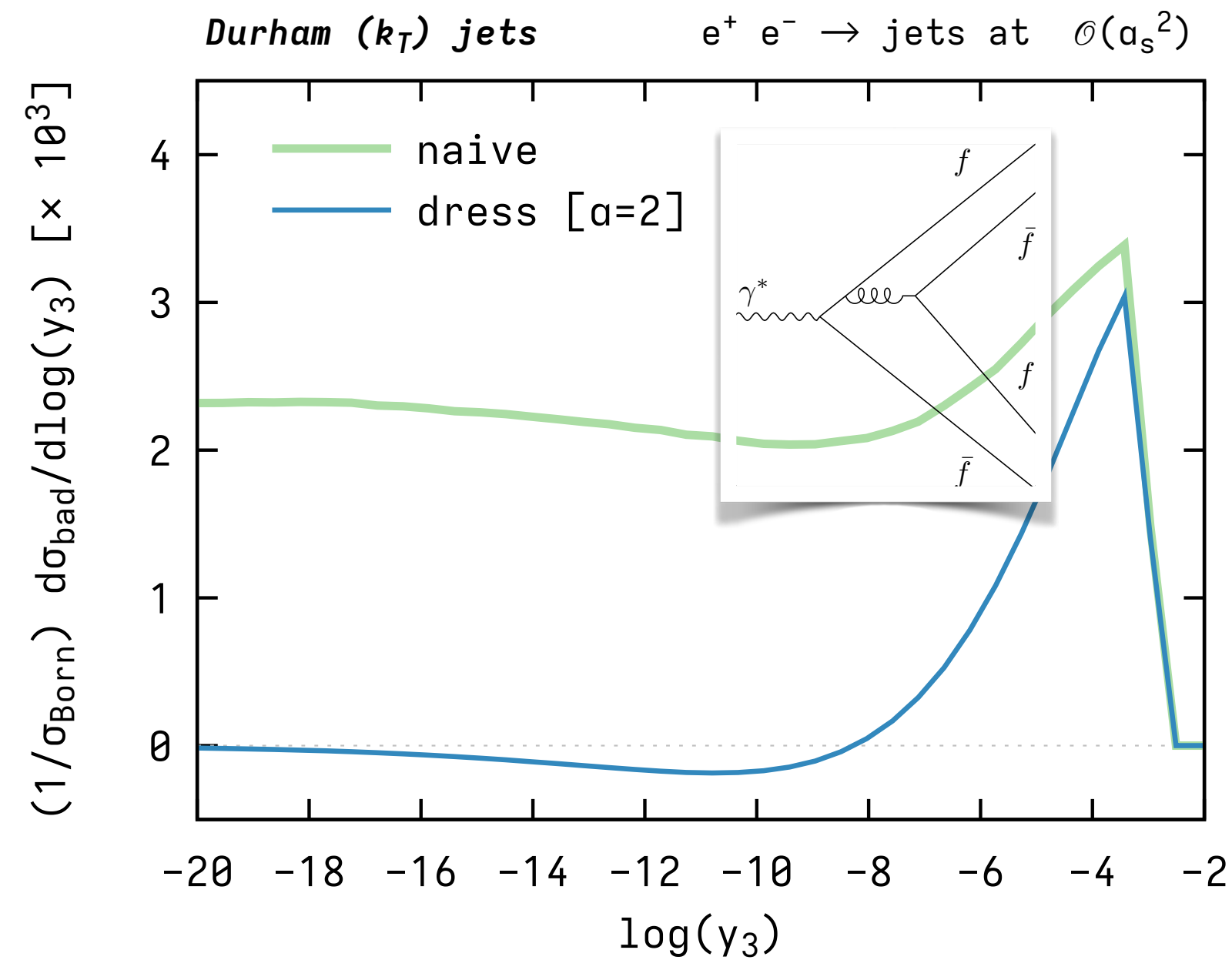
# IRC safety test in $e^+e^- \rightarrow \text{jets}$

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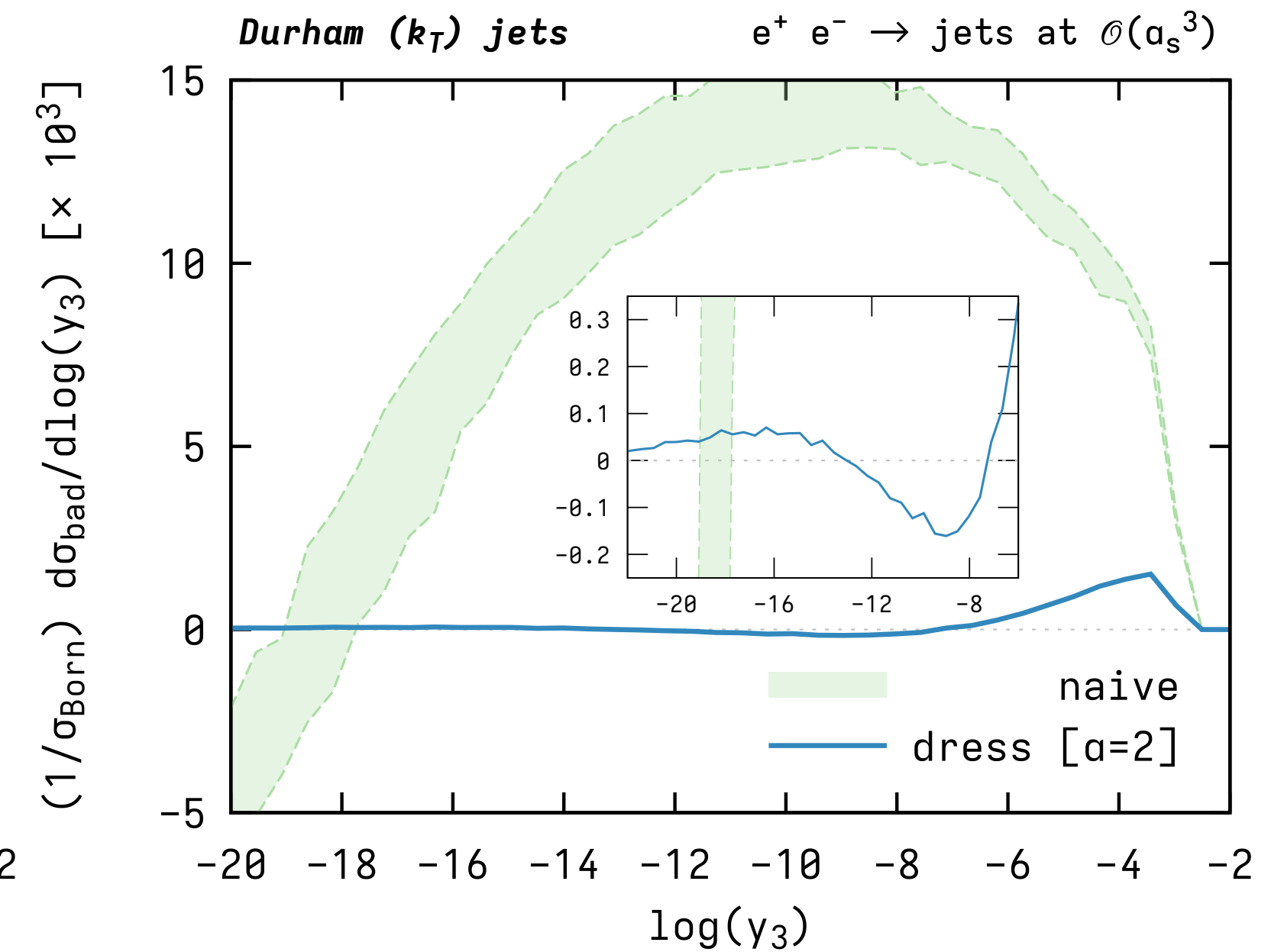
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Any gen- $k_T$  algo is safe!



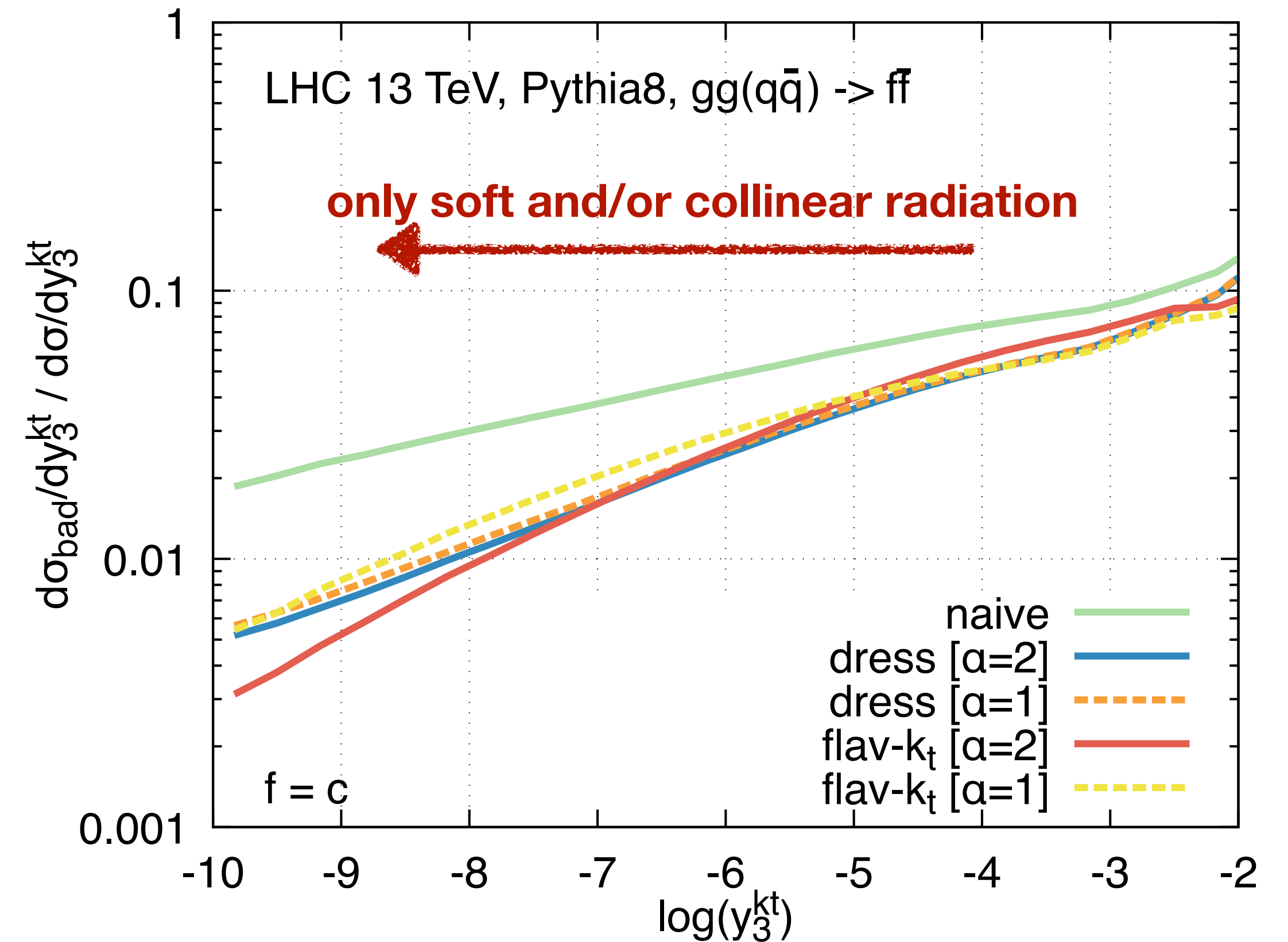
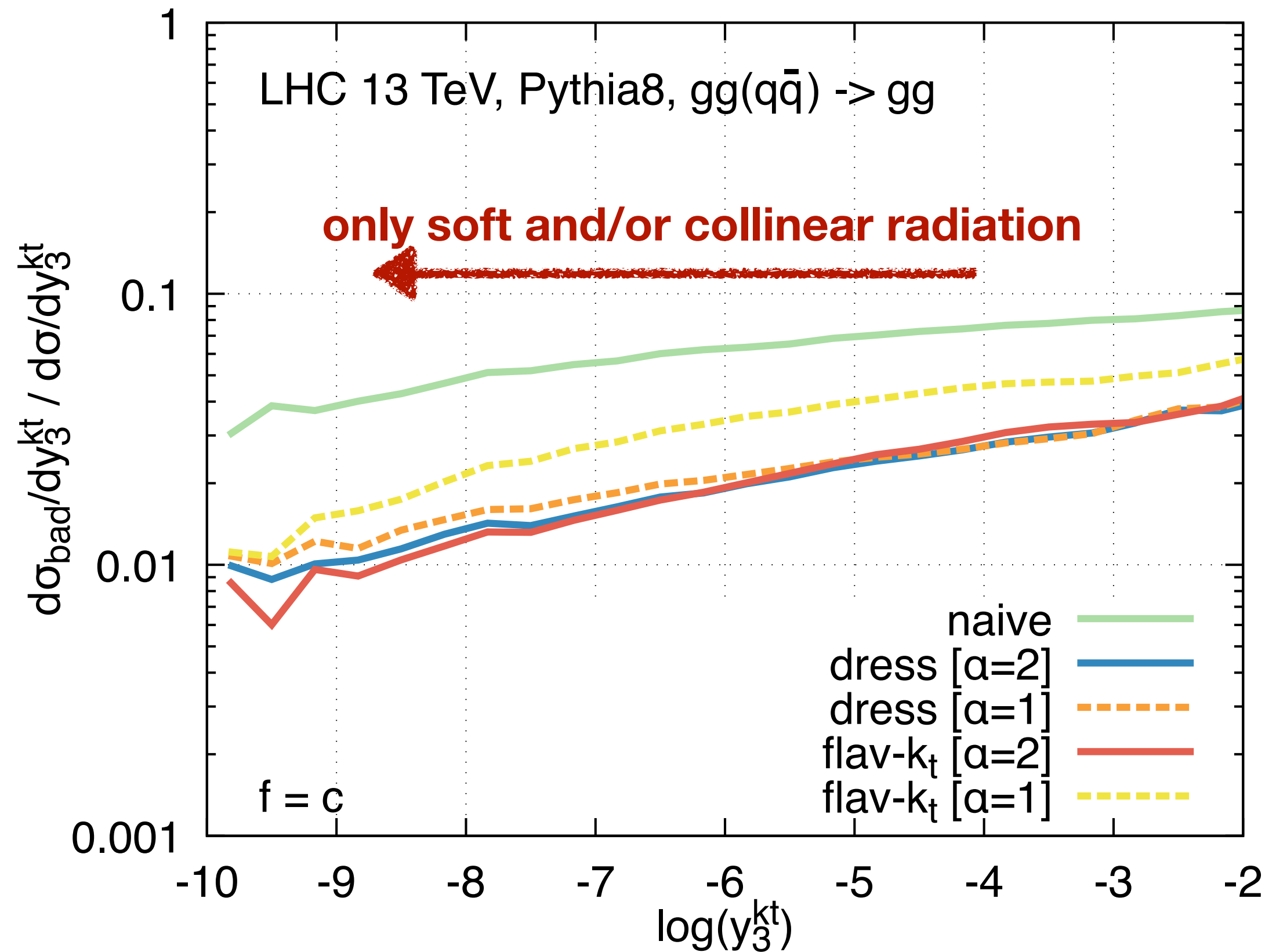
Naive dressing unsafe,  
flavour dressing safe!



Naive dressing unsafe,  
flavour dressing still safe!

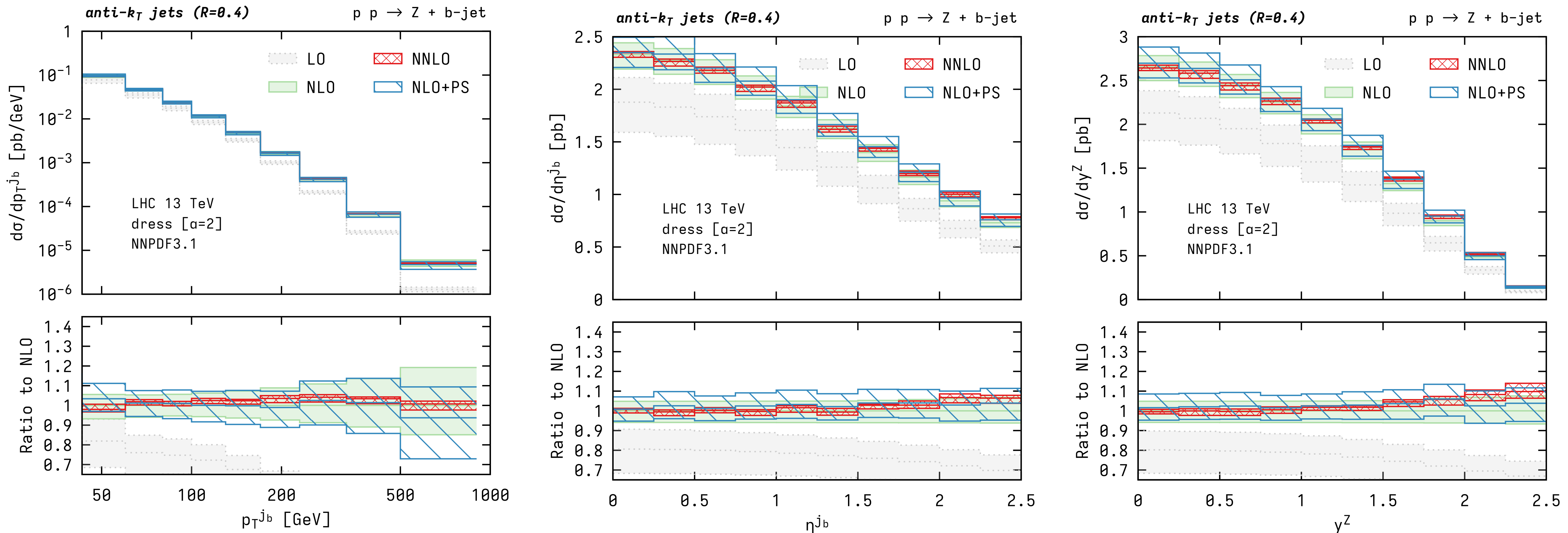


# IRC sensitivity in $2 \rightarrow 2$ QCD events in $pp$



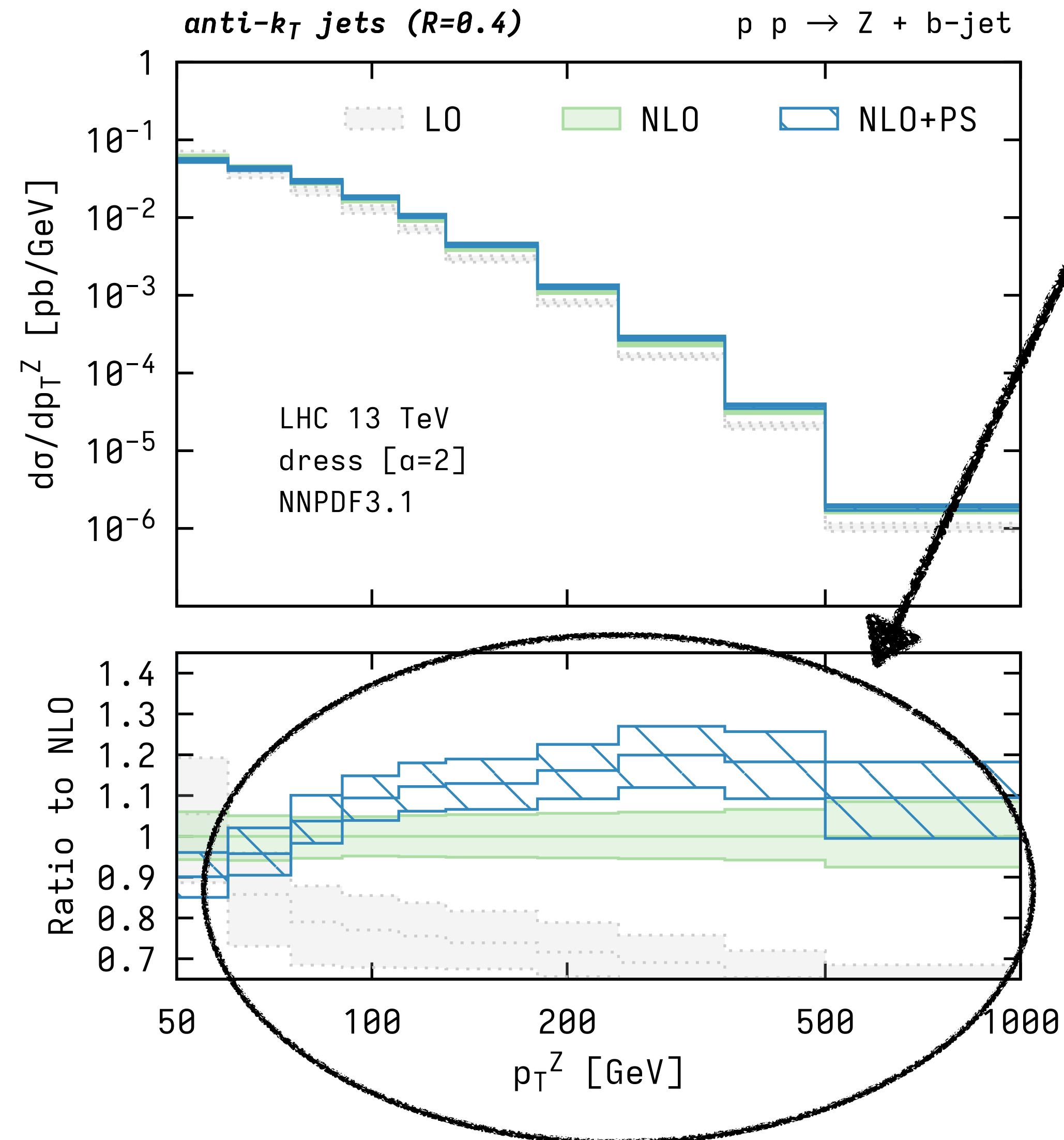
Flavour dressing approaches zero faster than a naive flavour tagging as  $y_3^{k_t} \rightarrow 0$

# Test in a realist scenario: $Z + b$ -jet

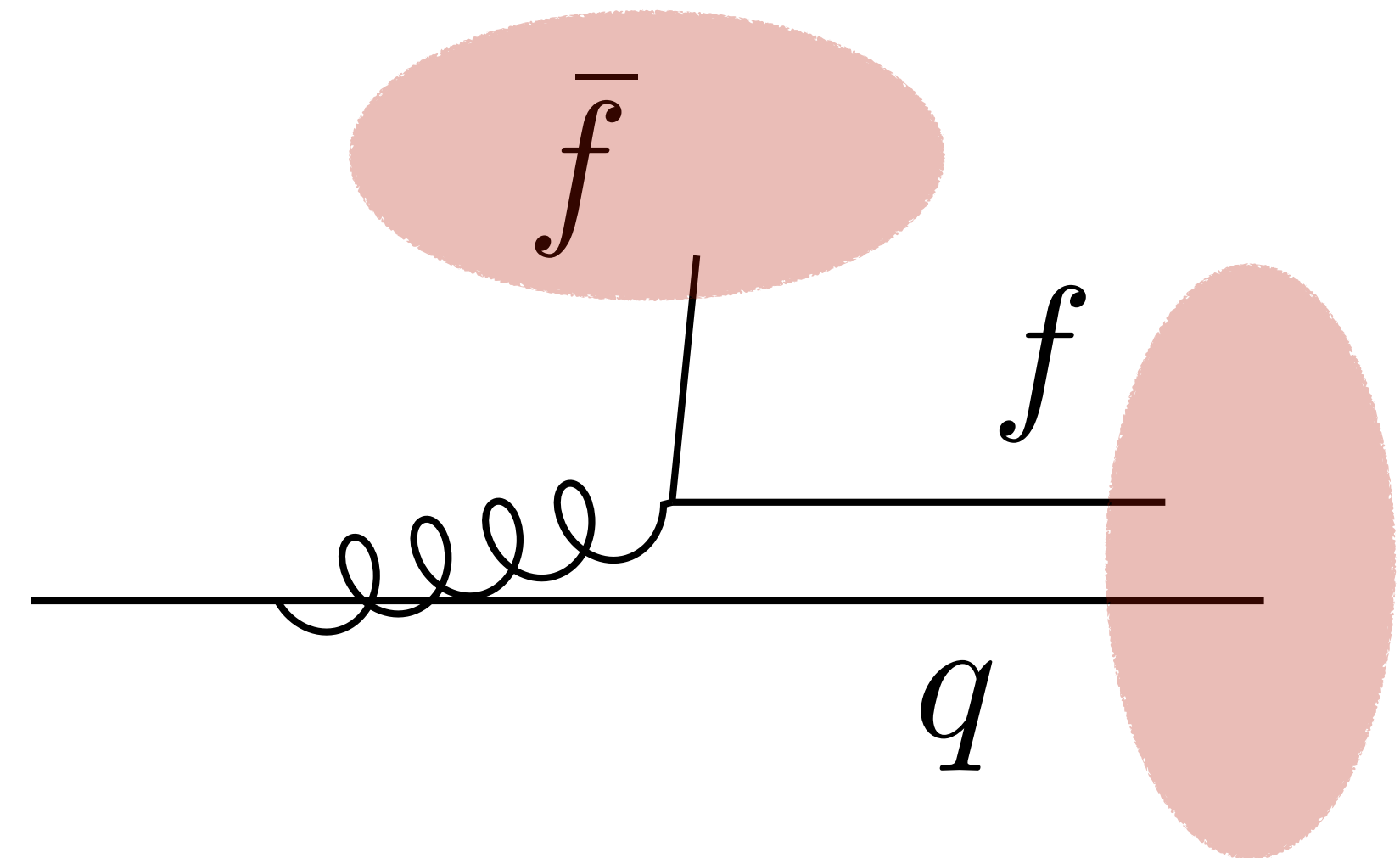


Remarkable agreement between (N)NLO and NLO+PS  
 → for most distributions **largely insensitive to all-order corrections**

# Test in a realist scenario: $Z + b$ -jet



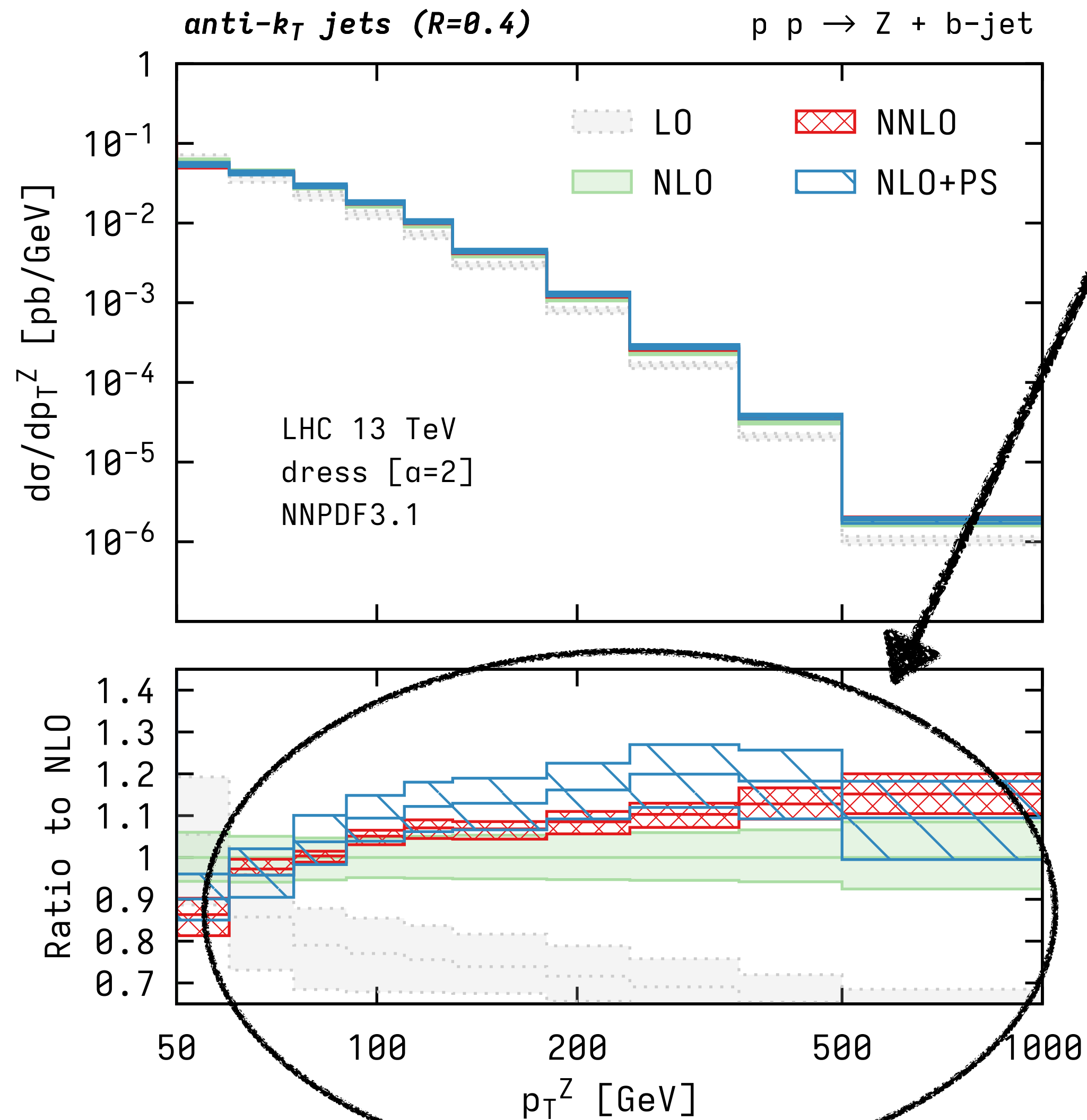
Some sensitivity observed in  $p_T^Z$ , likely due to:



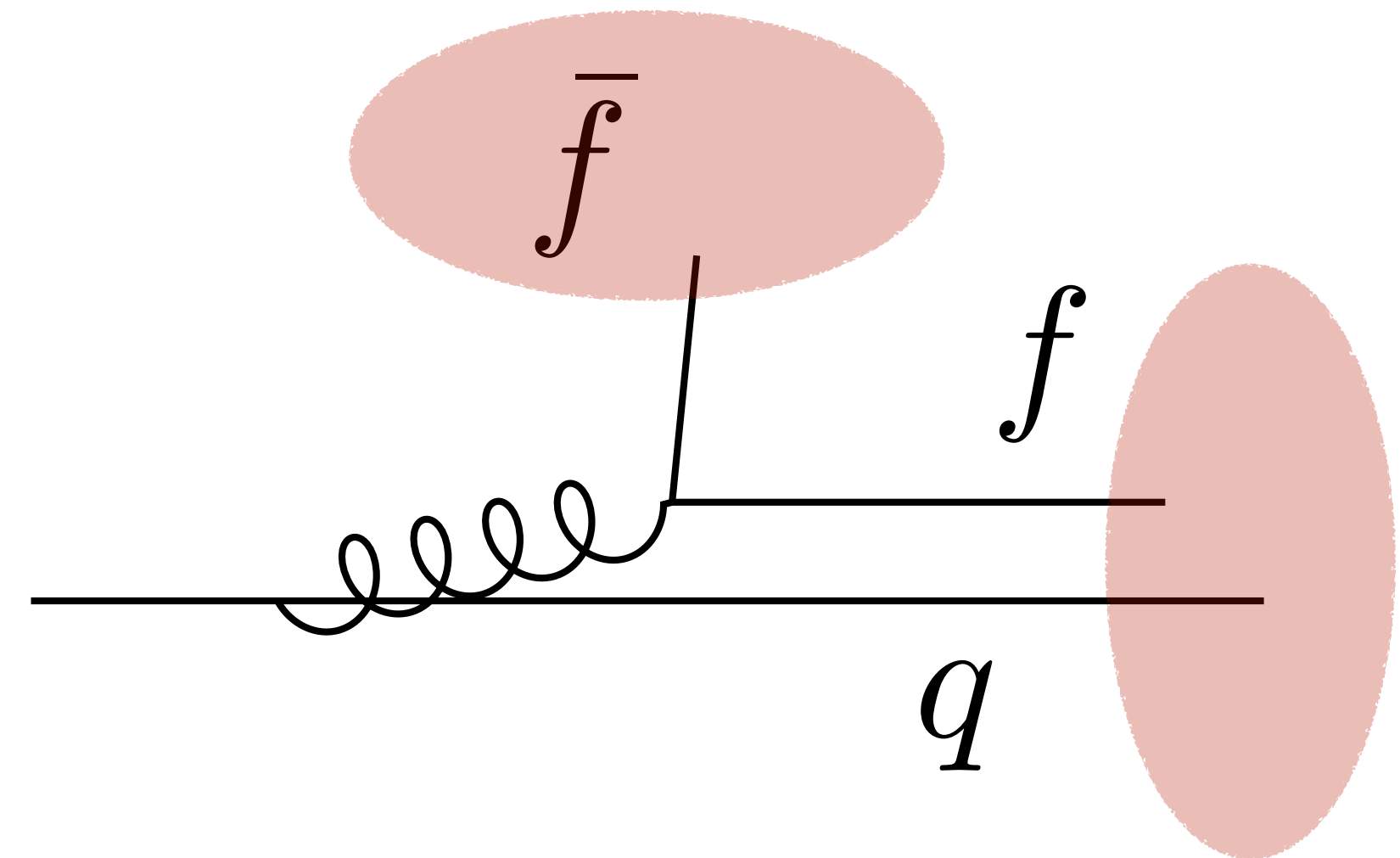
Even if IRC finite, it leads to large migration of (unflavoured)-jet into the  $b$ -jet sample.



# Test in a realist scenario: $Z + b$ -jet



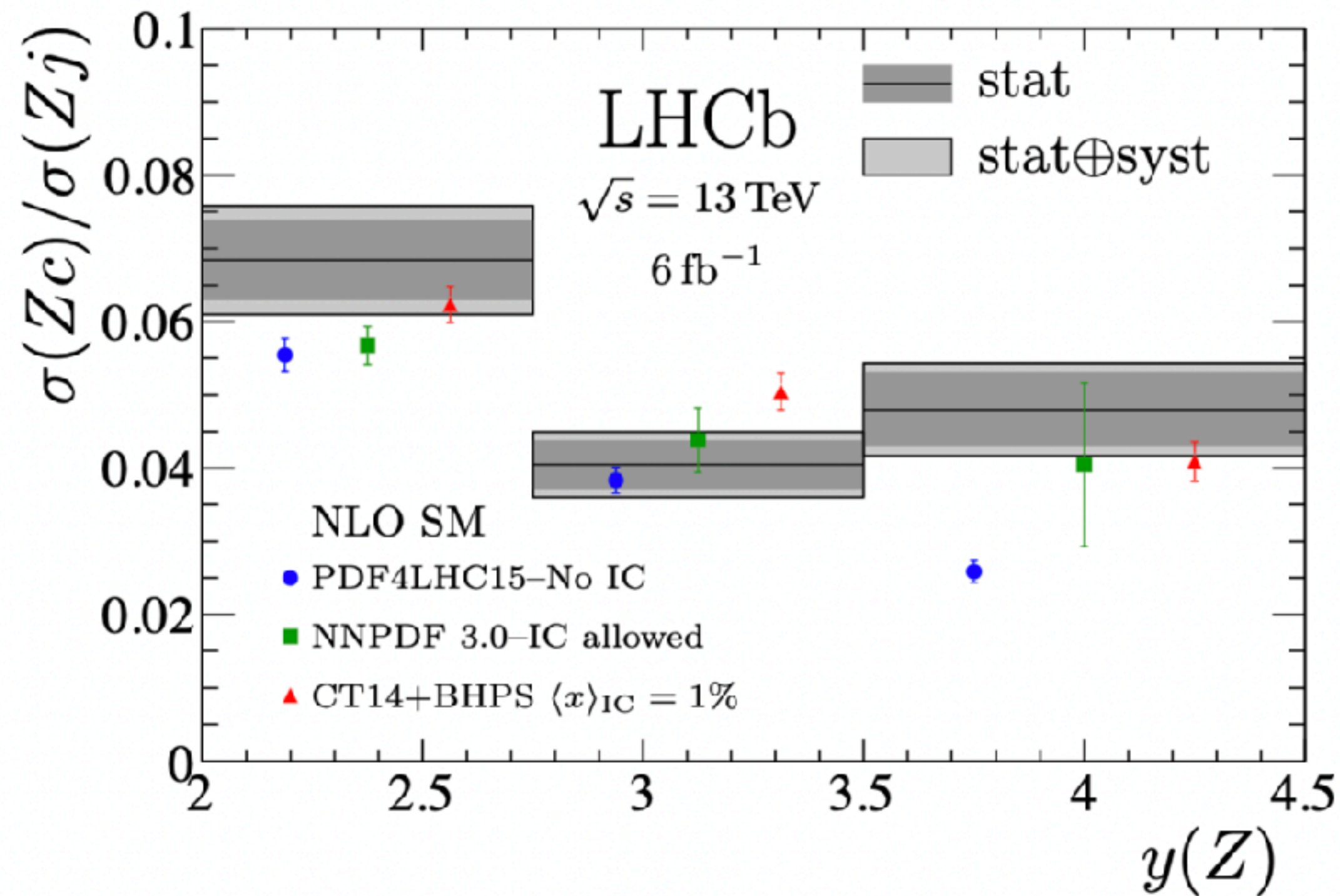
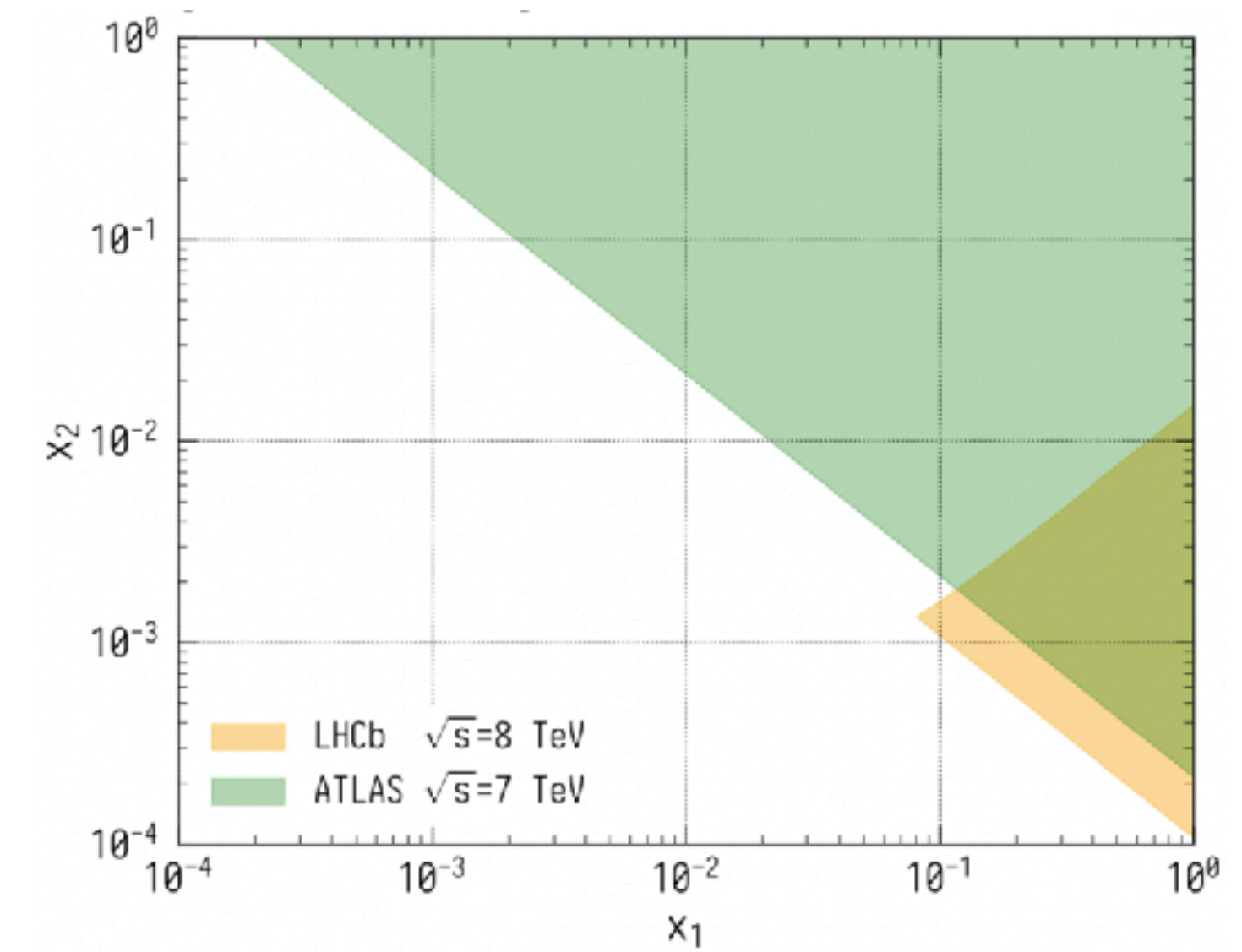
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**Effect captured at NNLO**

# Z + c-jet at LHCb

Sensitive to intrinsic charm in the proton, since LHCb suited to probe highly asymmetric momentum fractions

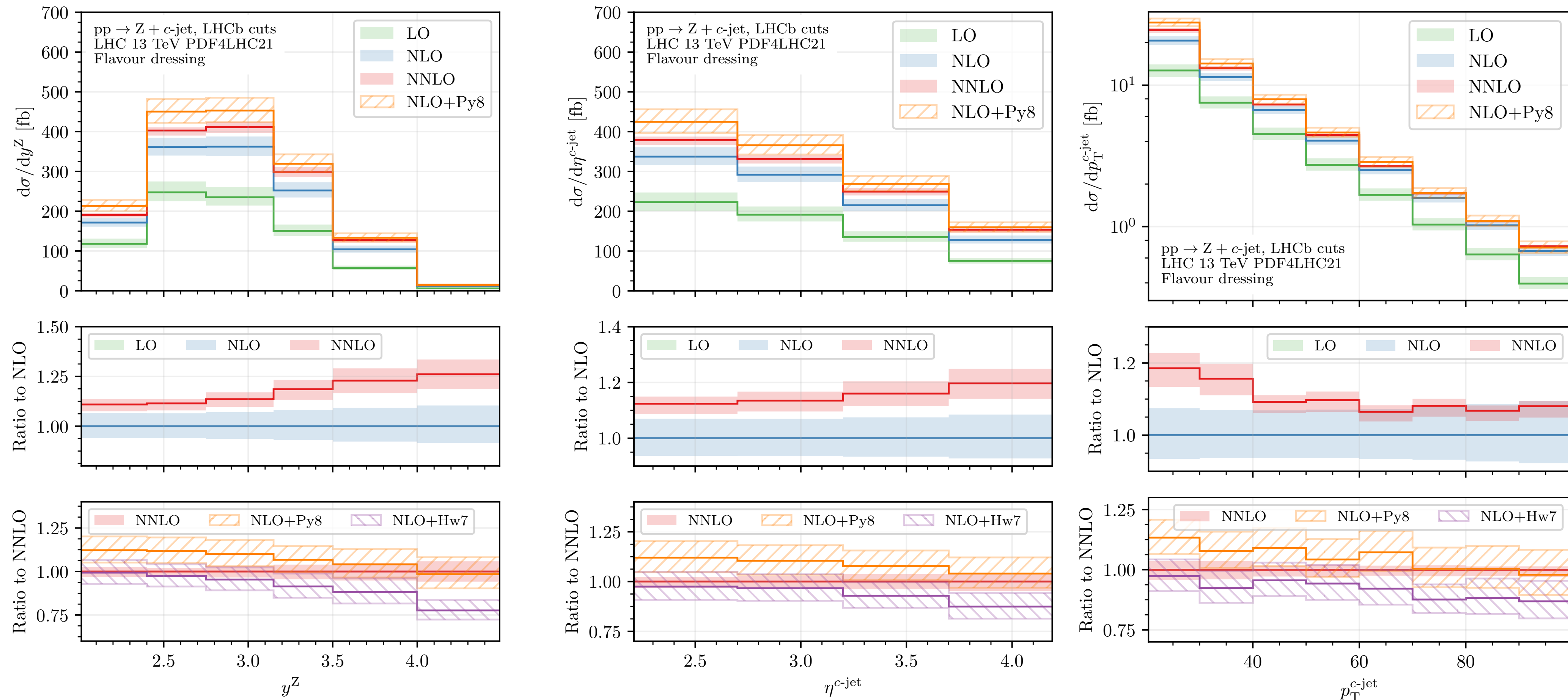


Exp. data at 13TeV for ratio  
 $(d\sigma_{Z+c}/dy_Z) / (d\sigma_{Z+j}/dy_Z)$  available

Z bosons	$p_T(\mu) > 20 \text{ GeV}, 2.0 < \eta(\mu) < 4.5, 60 < m(\mu^+\mu^-) < 120 \text{ GeV}$
Jets	$20 < p_T(j) < 100 \text{ GeV}, 2.2 < \eta(j) < 4.2$
Charm jets	$p_T(c \text{ hadron}) > 5 \text{ GeV}, \Delta R(j, c \text{ hadron}) < 0.5$
Events	$\Delta R(\mu, j) > 0.5$

# Z + c-jet in the forward kinematics

[Gauld, Gehrmann-De Ridder, Glover, Huss, Rodriguez Garcia, GS 2302.xxxxx]



Good agreement between NNLO and  $p_T$ -ordered NLO+PS



# Z + c-jet in the forward kinematics

[Gauld, Gehrmann-De Ridder, Glover, Huss, Rodriguez Garcia, GS 2302.xxxxx]

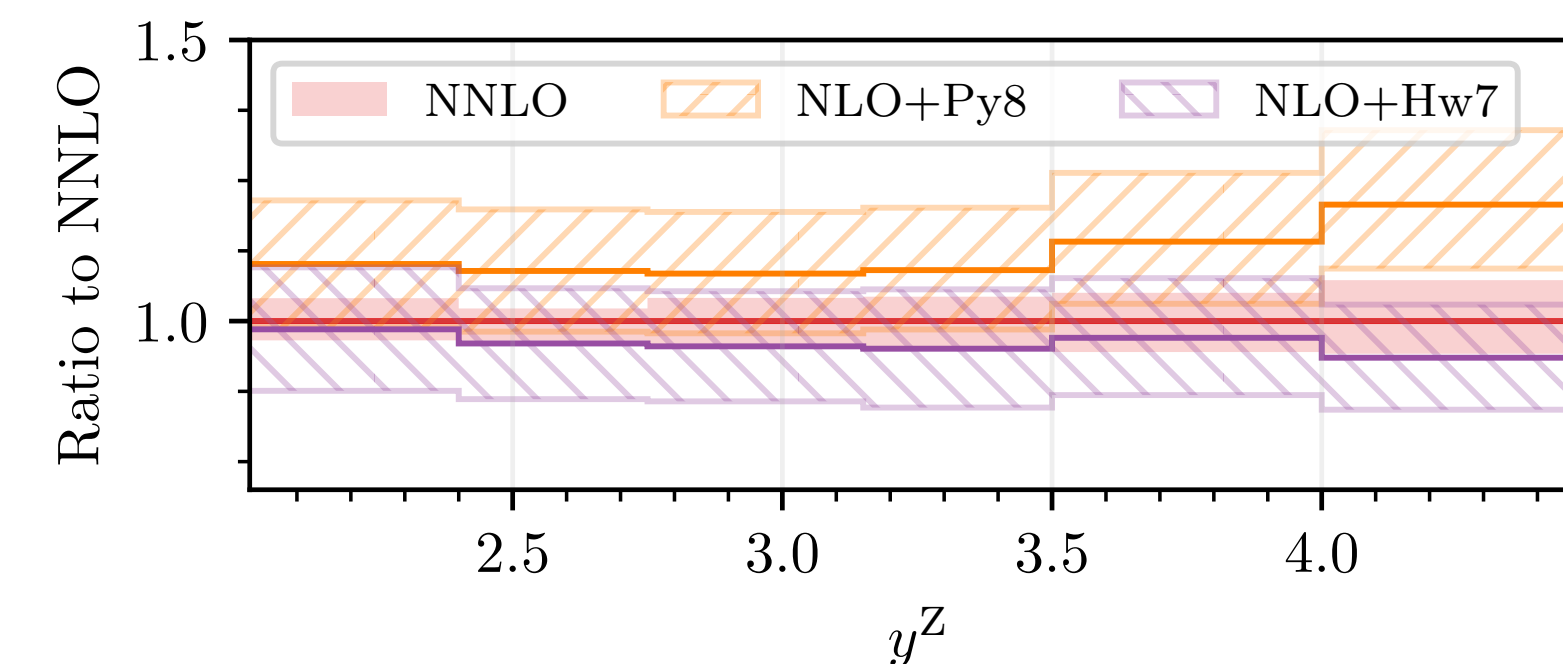
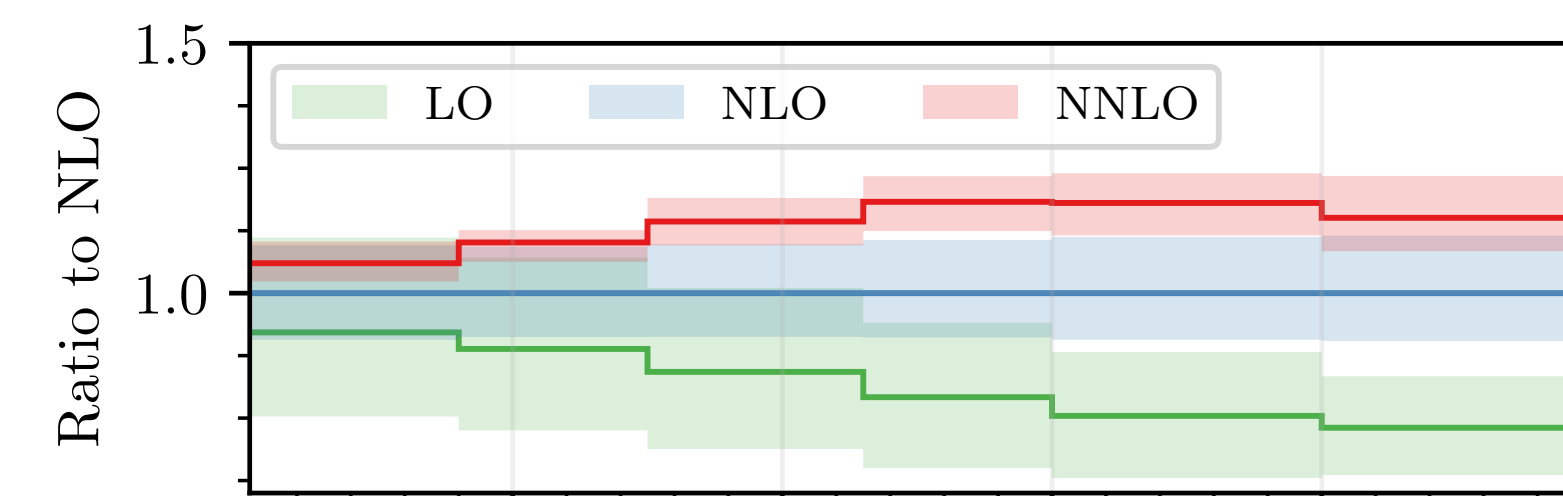
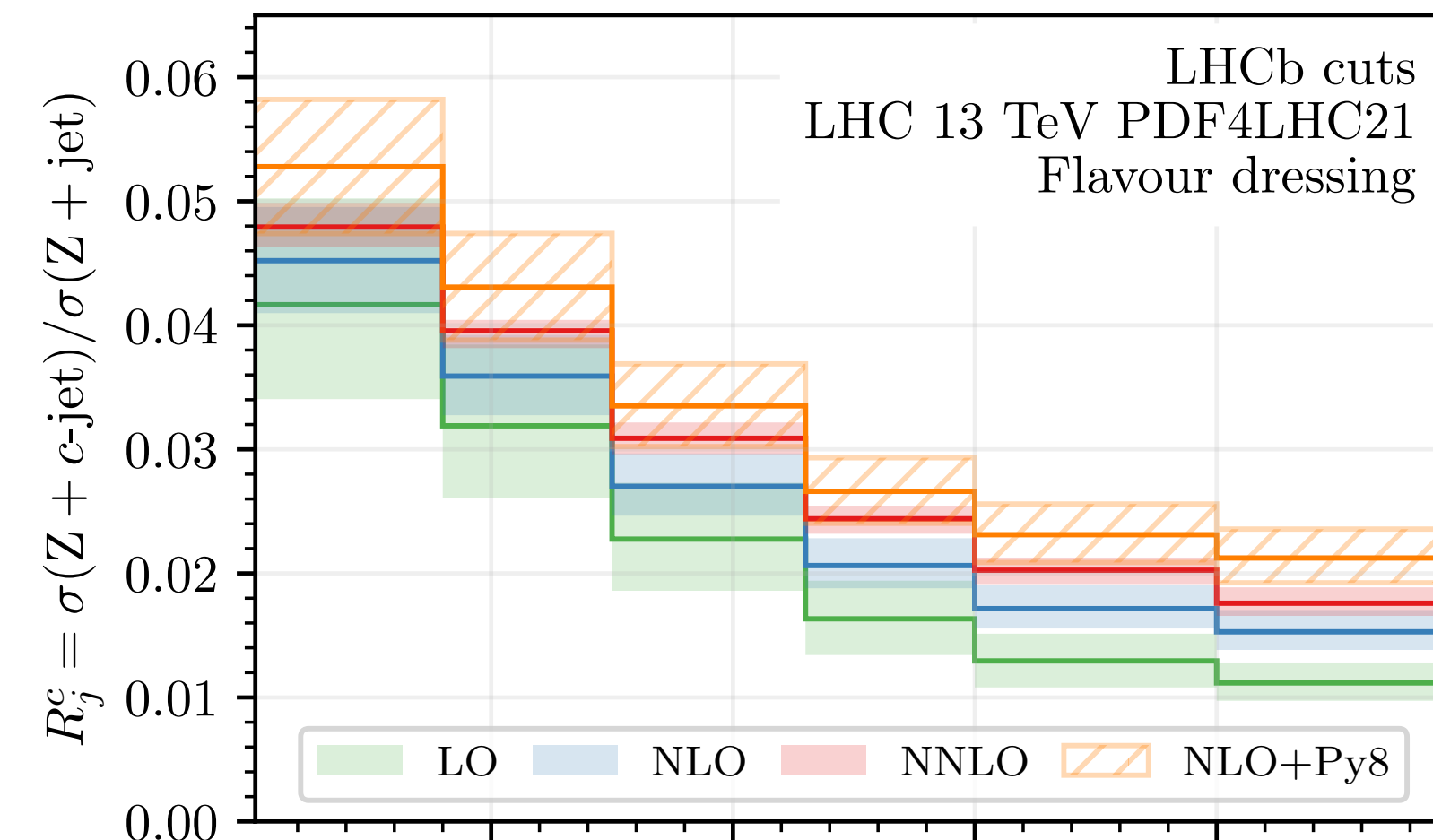
$$R_j^c = (d\sigma_{Z+c}/dy_Z) / (d\sigma_{Z+j}/dy_Z)$$

Thanks to flavour dressing,  
numerator and denominator

both feature the same anti- $k_T$  jets!

However, comparison to available  
LHCb data not possible...

Interesting to explore experimental  
feasibility of flavour dressing





# Final remarks on flavour dressing

With **flavour** dressing, **flavour assignment *factorised* from the initial jet reconstruction**, hence it can be **combined with any IRC safe definition of a jet**

The IRC safe flavour assignment allows for massless fixed-order predictions, and in the case of massive calculations and/or parton showered events, implies a suppressed sensitivity on  $\log(Q^2/m_f)$

A fastjet-contrib (<https://fastjet.hepforge.org/contrib/>) is in preparation.

# Conclusions

Heavy **Flavours** are of **paramount importance** in particle physics

Flavoured particles and flavoured jets are **two complementary ways** of looking at the same events

Accurate phenomenology requires both precise theory predictions and good (e.g. IRC safe) definitions of objects

Work in progress, stay tuned!