

Report on Experimental Measurements and Observables for EFT Interpretations

Andrei Gritsan

Johns Hopkins University

based on recent WG note by

Nuno Castro¹, Kyle Cranmer², Andrei V. Gritsan³, James Howarth⁴, Giacomo Magni^{5,6}, Ken Mimasu⁷, Juan Rojo^{5,6}, Jeffrey Roskes³, Eleni Vryonidou⁸, Tevong You^{9,10,11}

December 2, 2022

5th General Meeting of LHC EFT WG
CERN, Geneva, Switzerland

Area 3: Experimental Measurements and Observables

Editors: **Eleni Vryonidou**, **Nuno Castro**, **Andrei Gritsan**

(theory)

(ATLAS)

(CMS)

CERN-LHCEFTWG-2022-001
CERN-LPCC-2022-05

November 15, 2022

Nuno Castro¹, Kyle Cranmer², Andrei V. Gritsan³, James Howarth⁴, Giacomo Magni^{5,6}, Ken Mimasu⁷, Juan Rojo^{5,6}, Jeffrey Roskes³, Eleni Vryonidou⁸, Tevong You^{9,10,11}

- Started with dedicated meetings

kick-off [11 January 2021](#)

- Several iterations

[LHCEFTWG-2022-001](#)

- Submitted to [arXiv](#)

15 November 2022

arXiv:2211.08353v1 [hep-ph] 15 Nov 2022

¹ LIP, Departamento de Física, Escola de Ciências, Universidade do Minho, 4710-057 Braga, Portugal

² Department of Physics, University of Wisconsin, Madison, WI 53706, USA

³ Department of Physics and Astronomy, Johns Hopkins University, Baltimore, MD 21218, USA

⁴ SUPA - School of Physics and Astronomy, University of Glasgow, Glasgow, UK

⁵ Nikhef, Science Park 105, 1098 XG Amsterdam, The Netherlands

⁶ Department of Physics and Astronomy, Vrije Universiteit, NL-1081 HV Amsterdam, The Netherlands

⁷ Department of Physics, King's College London, Strand, London WC2R 2LS, UK

⁸ Department of Physics and Astronomy, University of Manchester, Oxford Road, Manchester M13 9PL, UK

⁹ Theoretical Physics Department, CERN, CH-1211 Geneva 23, Switzerland

¹⁰ AMTP, University of Cambridge, Wilberforce Road, Cambridge CB3 0WA, UK

¹¹ Cavendish Laboratory, University of Cambridge, J.J. Thomson Avenue, Cambridge CB3 0HE, UK

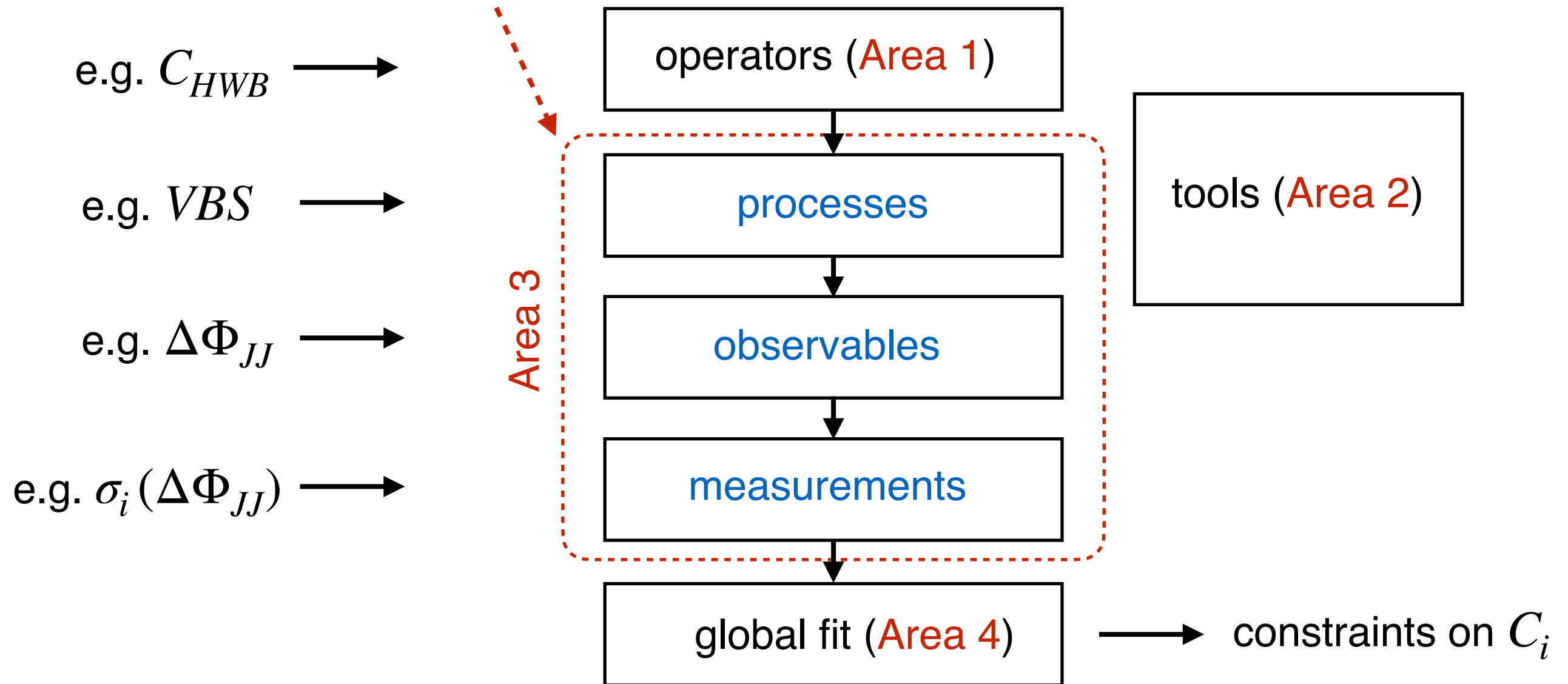
Abstract

The LHC effective field theory working group gathers members of the LHC experiments and the theory community to provide a framework for the interpretation of LHC data in the context of EFT. In this note we discuss experimental observables and corresponding measurements in analysis of the Higgs, top, and electroweak data at the LHC. We review the relationship between operators and measurements relevant for the interpretation of experimental data in the context of a global SMEFT analysis. One of the goals of ongoing effort is bridging the gap between theory and experimental communities working on EFT, and in particular concerning optimised analyses. This note serves as a guide to experimental measurements and observables leading to EFT fits and establishes good practice, but does not present authoritative guidelines how those measurements should be performed.

Area 3: Experimental Measurements and Observables

Area 3: measurements and observables

- (1) define **observables** and **measurements**
- (2) relate **operators** and **observables**

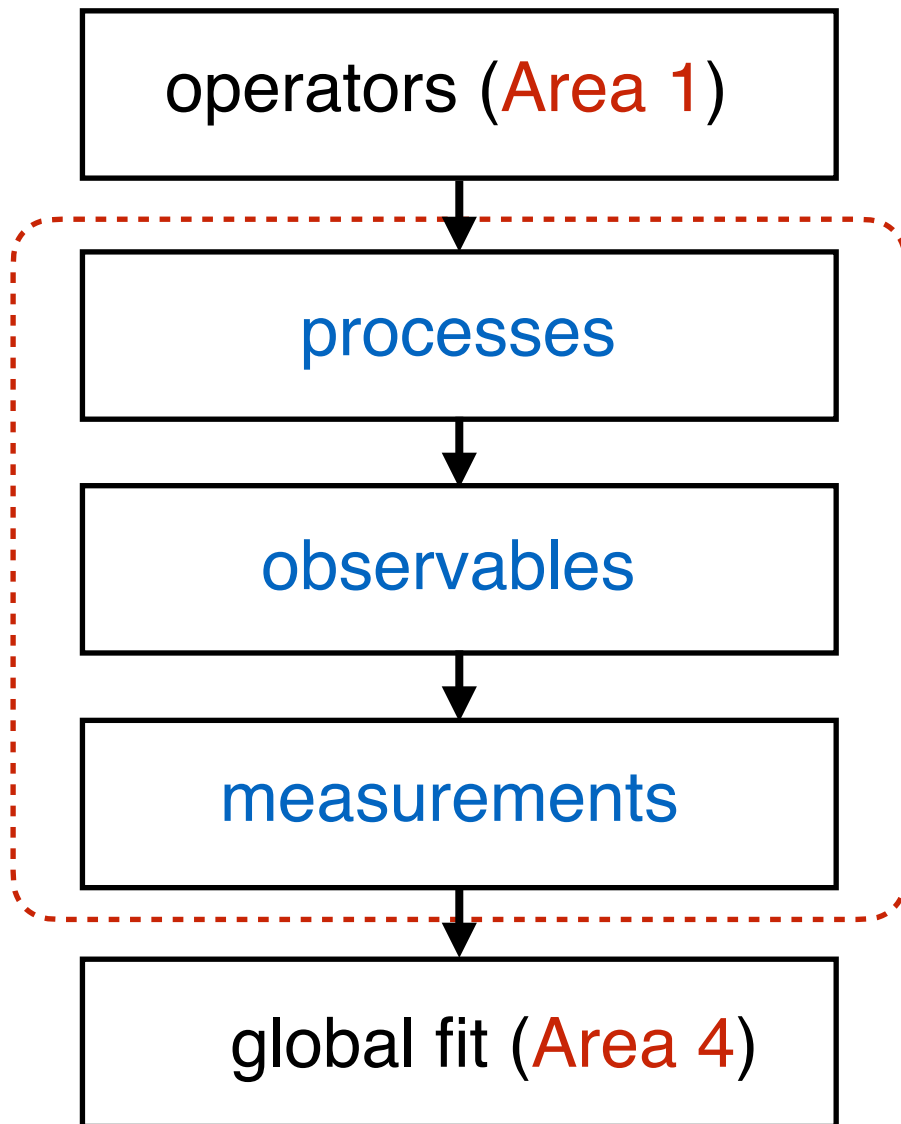


Outline

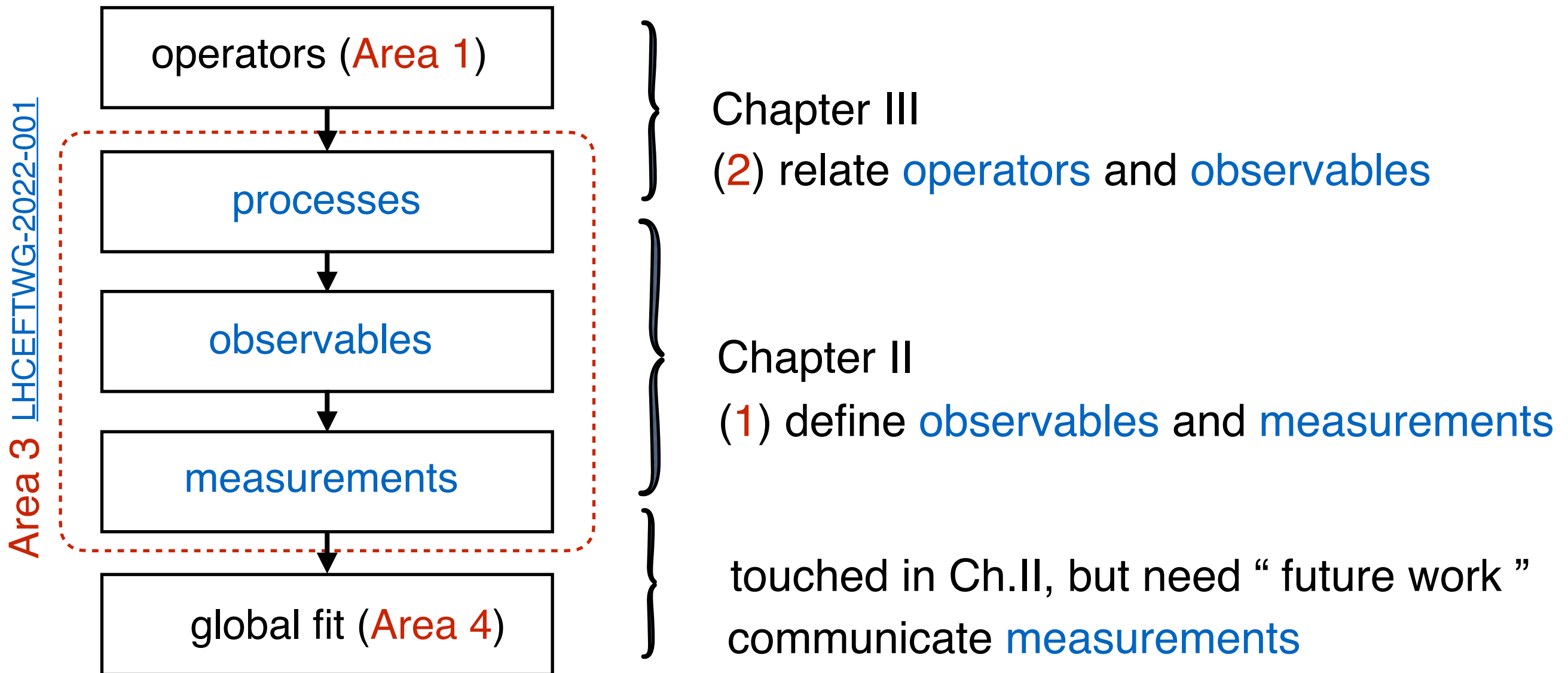
Contents

1	Introduction	3
2	Experimental observables and corresponding measurements	4
2.1	Approaches to experimental observables	6
2.1.1	Observables sensitive to EFT effects	7
2.1.2	Observables optimized with matrix-element calculations	7
2.1.3	Observables optimized with machine learning	9
2.2	Approaches to experimental measurements	10
2.3	Statistical methods for experimental measurements	13
2.3.1	Unfolding	13
2.3.2	Simplified template cross sections	15
2.3.3	Template likelihood fit	16
2.3.4	Matrix element method	18
2.3.5	Inference with machine learning	18
3	Operators and measurements for global SMEFT fits	21
3.1	Computational framework	22
3.1.1	Operator basis in SMEFiT 2021 analysis	22
3.1.2	Operators in the fitmaker analysis	26
3.2	Experimental measurements	27
3.2.1	Input experimental data in SMEFiT 2021 analysis	27
3.2.2	Input experimental data in fitmaker analysis	30
3.3	Mapping between data and EFT coefficients.	30
3.3.1	Linear dependences of measurements on operators (Fitmaker)	30
3.3.2	Fisher information matrix analysis (SMEFiT)	37
3.4	Impact of measurements on individual constraints (Fitmaker)	42
3.5	Global sensitivity from dataset variations (SMEFiT)	46
4	Summary	48

Area 3 LHCEFTWG-2022-001



Outline



(1) Measurements and Observables

measurements

observables

processes

$$\mathcal{P}(\vec{x}_{\text{reco}} | \vec{\theta})$$

reco observables

\vec{x}_{reco}

measurement

=

$$\int d\vec{x}_{\text{part}} p(\vec{x}_{\text{reco}} | \vec{x}_{\text{part}})$$

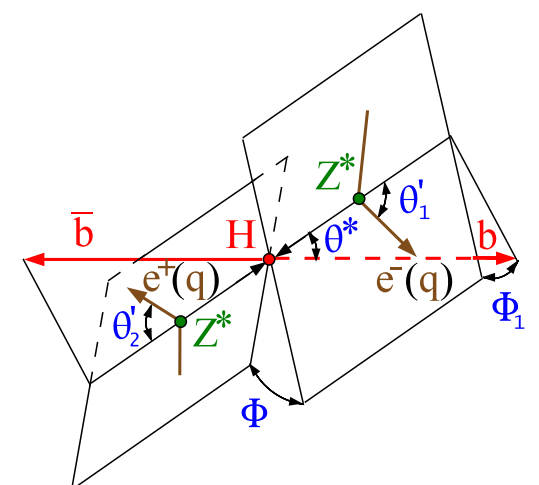
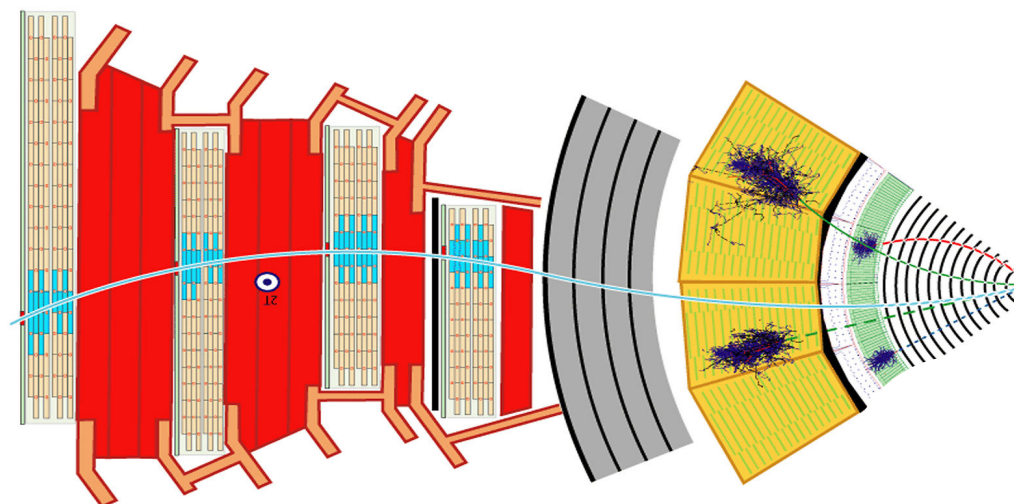
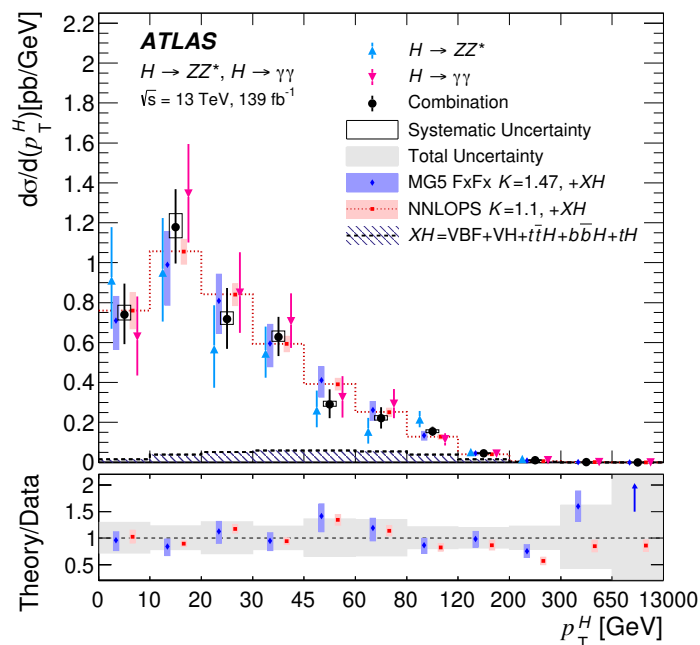
parton shower
detector effects
reconstruction

$$\mathcal{P}(\vec{x}_{\text{part}} | \vec{\theta})$$

hard process
matrix elements

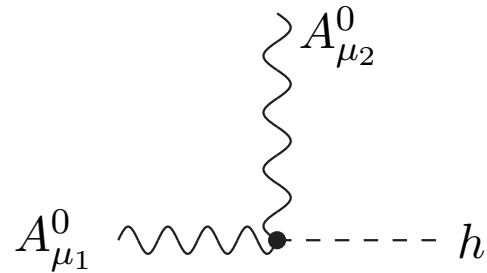
EFT params $\vec{\theta}$

parton mom \vec{x}_{part}



(2) Operators and Processes / Observables

- Feynman rules for SMEFT (Area 1)
 - relate processes and operators



$$\begin{aligned}
 & + \frac{4i\bar{g}'^2 v}{\bar{g}^2 + \bar{g}'^2} C^{\varphi W} (p_1^{\mu_2} p_2^{\mu_1} - p_1 \cdot p_2 \eta_{\mu_1 \mu_2}) \\
 & + \frac{4i\bar{g}^2 v}{\bar{g}^2 + \bar{g}'^2} C^{\varphi B} (p_1^{\mu_2} p_2^{\mu_1} - p_1 \cdot p_2 \eta_{\mu_1 \mu_2}) \\
 & - \frac{4i\bar{g}\bar{g}' v}{\bar{g}^2 + \bar{g}'^2} C^{\varphi WB} (p_1^{\mu_2} p_2^{\mu_1} - p_1 \cdot p_2 \eta_{\mu_1 \mu_2}) \\
 & + \frac{4i\bar{g}'^2 v}{\bar{g}^2 + \bar{g}'^2} C^{\varphi \tilde{W}} p_1^{\alpha_1} p_2^{\beta_1} \epsilon_{\mu_1 \mu_2 \alpha_1 \beta_1} + \frac{4i\bar{g}^2 v}{\bar{g}^2 + \bar{g}'^2} C^{\varphi \tilde{B}} p_1^{\alpha_1} p_2^{\beta_1} \epsilon_{\mu_1 \mu_2 \alpha_1 \beta_1} \\
 & - \frac{4i\bar{g}\bar{g}' v}{\bar{g}^2 + \bar{g}'^2} C^{\varphi \tilde{W} B} p_1^{\alpha_1} p_2^{\beta_1} \epsilon_{\mu_1 \mu_2 \alpha_1 \beta_1}
 \end{aligned}$$

[arXiv:1704.03888](https://arxiv.org/abs/1704.03888)

- In the end relate to observables \vec{x}_{reco}

— kinematic effects
 — experimental choice

} affect sensitivity to EFT parameters $\vec{\theta}$

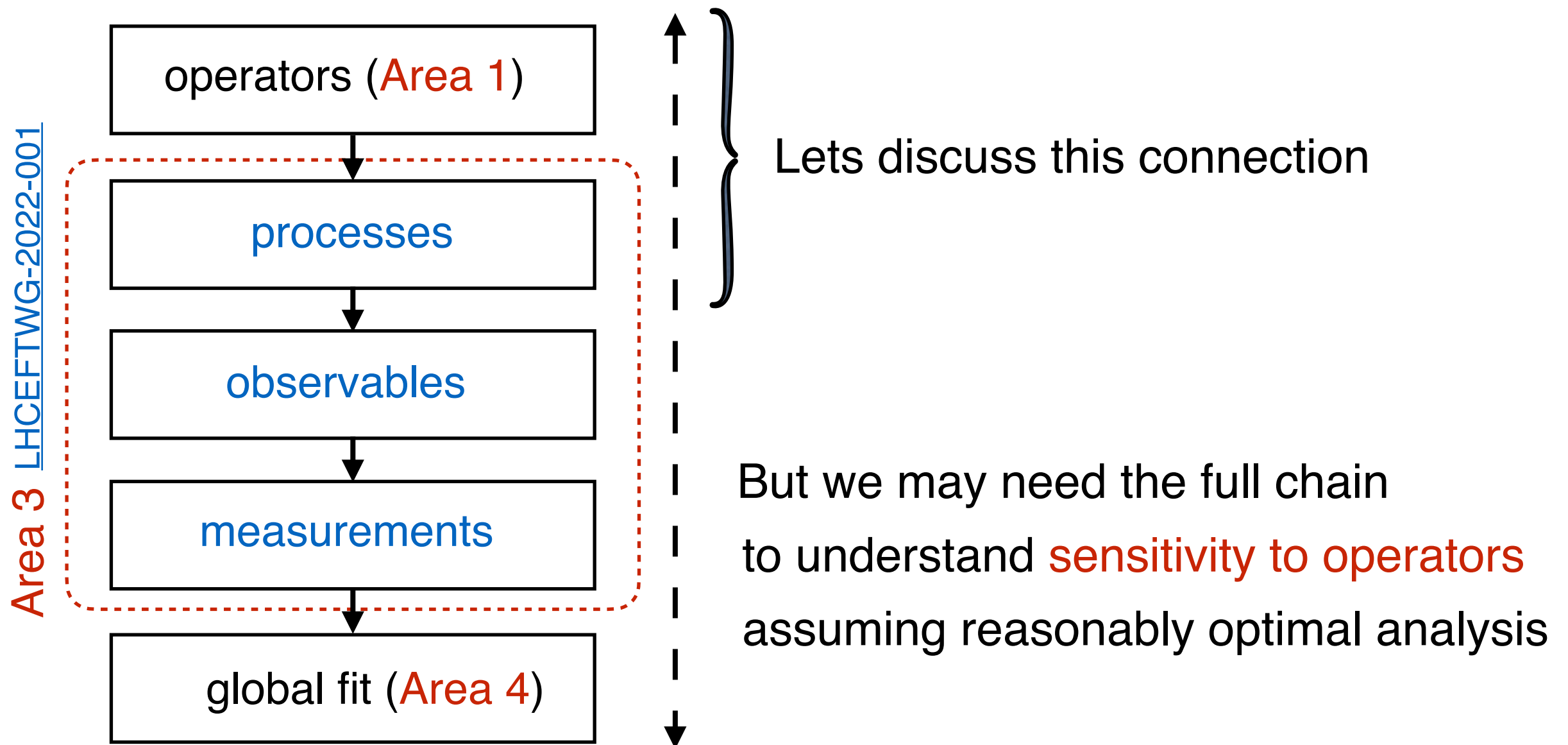
$$\mathcal{P}(\vec{x}_{\text{reco}} | \vec{\theta}) \propto \mathcal{P}_0(\vec{x}_{\text{reco}}) + \sum_k \left(\frac{2\theta_k}{\theta_0} \right) \mathcal{P}_{0k}(\vec{x}_{\text{reco}}) + \sum_k \left(\frac{\theta_k}{\theta_0} \right)^2 \mathcal{P}_k(\vec{x}_{\text{reco}}) + \sum_{i < j} \left(\frac{2\theta_i \theta_j}{\theta_0^2} \right) \mathcal{P}_{ij}(\vec{x}_{\text{reco}})$$

SM

linear terms

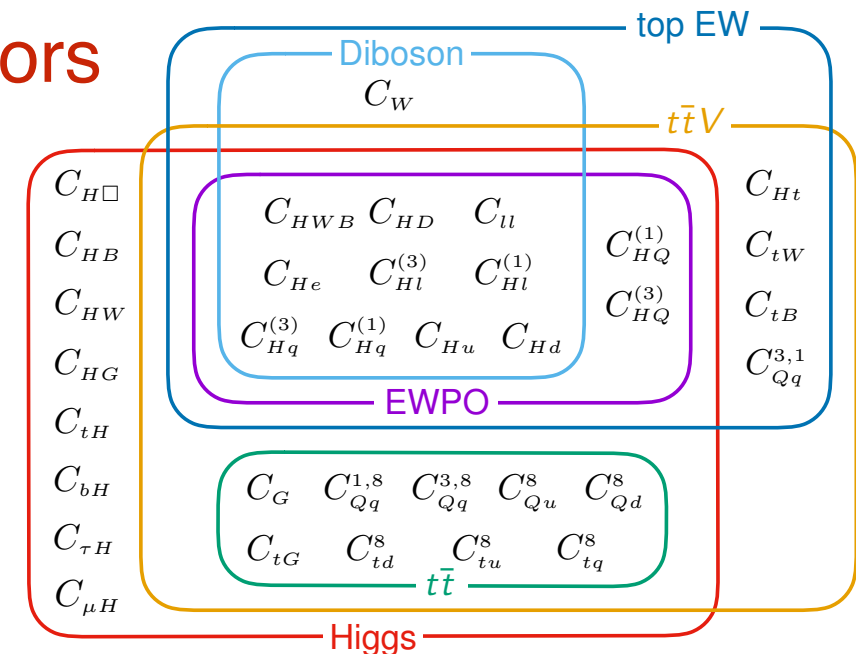
quadratic terms

Part 2 (Chapter III)



(III) Operators and Measurements

- Which **measurements** are sensitive to which **operators** based on **SMEFiT** and **Fitmaker** global fits
 - **limited to the choice of 20–50 operators** (e.g. only heavy flavor Yukawa couplings)
 - Note: separate note on flavor assumptions...



- **limited to the choice of ATLAS+CMS inclusive and differential measurements**

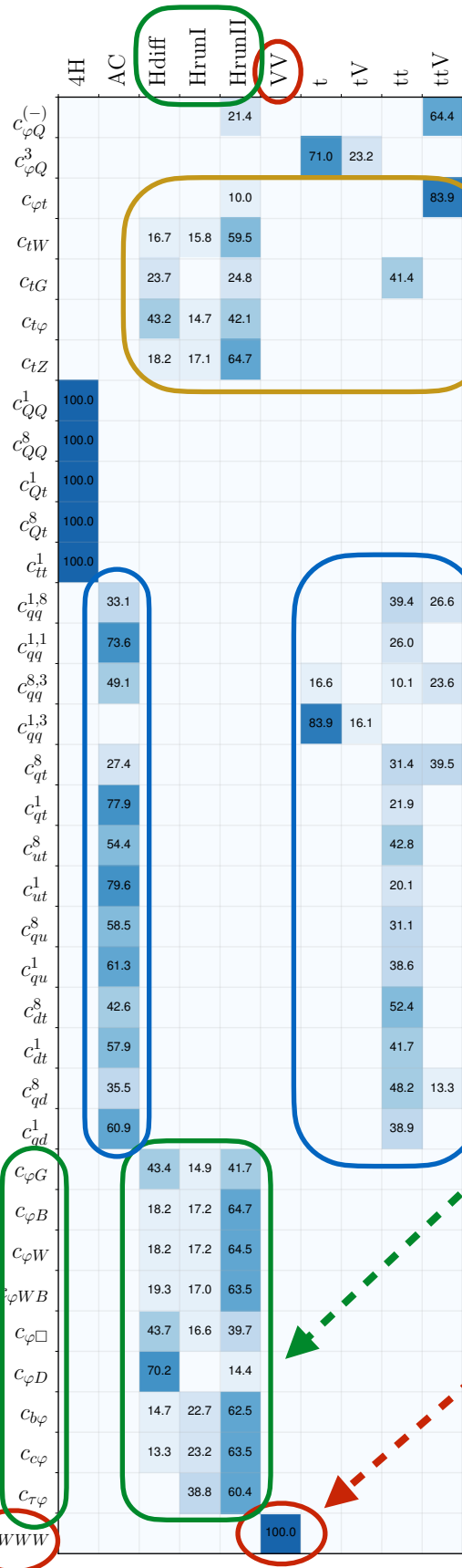
- Extract sensitivity:
 - **Linear dependence** on operators
 - **Fisher information matrix**
 - Global fit with **one operator**

Category	Processes	n_{dat}
Top quark production	$t\bar{t}$ (inclusive)	94
	$t\bar{t}Z, t\bar{t}W$	14
	single top (inclusive)	27
	tZ, tW	9
	$t\bar{t}t\bar{t}, t\bar{t}b\bar{b}$	6
	Total	150
Higgs production and decay	Run I signal strengths	22
	Run II signal strengths	40
	Run II, differential distributions & STXS	35
	Total	97
Diboson production	LEP-2	40
	LHC	30
	Total	70
Baseline dataset	Total	317

(III) Operators and Measurements

- Fisher information matrix (SMEFiT approach)

$$I_{ij}(\mathbf{c}) = -\mathbb{E} \left[\frac{\partial^2 \ln f(\boldsymbol{\sigma}_{\text{exp}} | \mathbf{c})}{\partial c_i \partial c_j} \right]$$

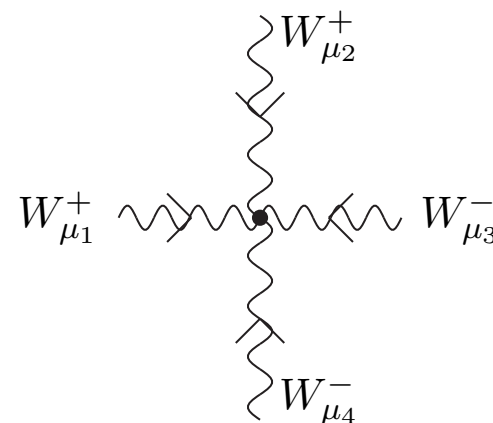


two-fermion operators from Higgs / top data

four-fermion operators from top data

Higgs operators

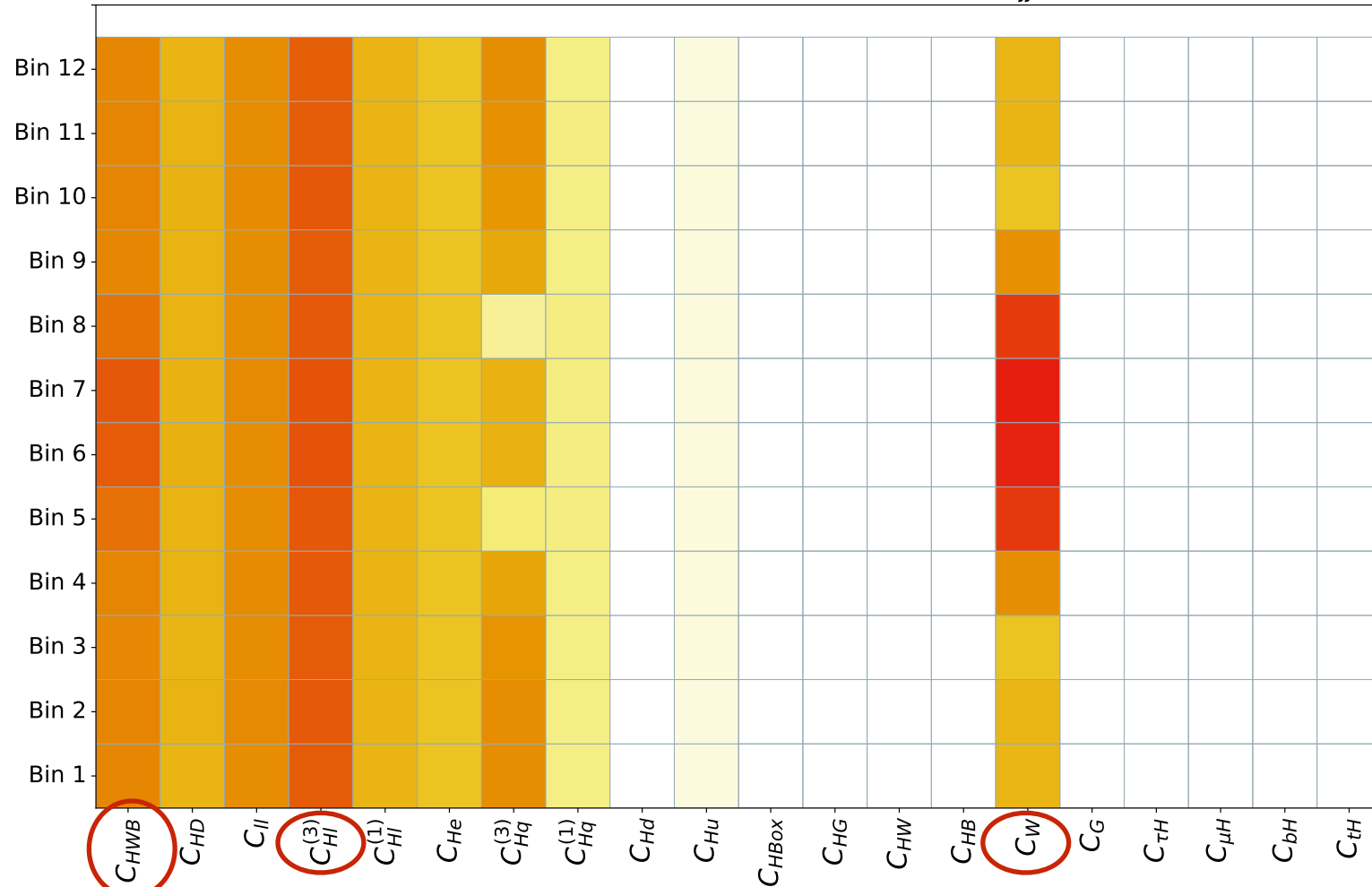
VV data



$$\begin{aligned}
 & -i\bar{g}^2 (\eta_{\mu_1\mu_4}\eta_{\mu_2\mu_3} + \eta_{\mu_1\mu_3}\eta_{\mu_2\mu_4} - 2\eta_{\mu_1\mu_2}\eta_{\mu_3\mu_4}) \\
 & + 6i\bar{g}C^W (\eta_{\mu_1\mu_3}(p_3^{\mu_2}p_1^{\mu_4} - p_1^{\mu_2}p_3^{\mu_4} - p_4^{\mu_2}p_1^{\mu_4} - p_3^{\mu_2}p_2^{\mu_4}) \\
 & + \eta_{\mu_1\mu_4}(p_4^{\mu_2}p_1^{\mu_3} - p_1^{\mu_2}p_4^{\mu_3} - p_3^{\mu_2}p_1^{\mu_3} - p_4^{\mu_2}p_2^{\mu_3}) \\
 & + \eta_{\mu_2\mu_3}(p_3^{\mu_1}p_2^{\mu_4} - p_2^{\mu_1}p_3^{\mu_4} - p_4^{\mu_1}p_2^{\mu_4} - p_3^{\mu_1}p_1^{\mu_4}) \\
 & + \eta_{\mu_2\mu_4}(p_4^{\mu_1}p_2^{\mu_3} - p_2^{\mu_1}p_4^{\mu_3} - p_3^{\mu_1}p_2^{\mu_3} - p_4^{\mu_1}p_1^{\mu_3}) \\
 & - \eta_{\mu_1\mu_2}(p_4^{\mu_3}(p_3 + p_4)^{\mu_4} + (p_3 + p_4)^{\mu_3}p_3^{\mu_4}) \\
 & - \eta_{\mu_3\mu_4}(p_2^{\mu_1}(p_1 + p_2)^{\mu_2} + (p_1 + p_2)^{\mu_1}p_1^{\mu_2}) \\
 & + \eta_{\mu_1\mu_3}\eta_{\mu_2\mu_4}(p_1 \cdot p_4 + p_2 \cdot p_3) + \eta_{\mu_1\mu_4}\eta_{\mu_2\mu_3}(p_1 \cdot p_3 + p_2 \cdot p_4) \\
 & - \eta_{\mu_1\mu_2}\eta_{\mu_3\mu_4}(p_1 \cdot p_3 + p_1 \cdot p_4 + p_2 \cdot p_3 + p_2 \cdot p_4)
 \end{aligned}$$

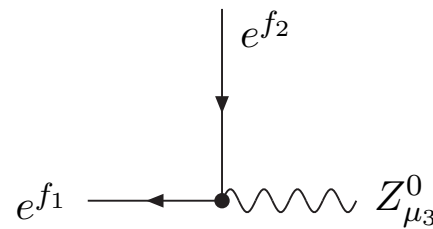
(III) Operators and Measurements

log(Linear C dependencies): $Z_{jj} \Delta\phi_{jj}$



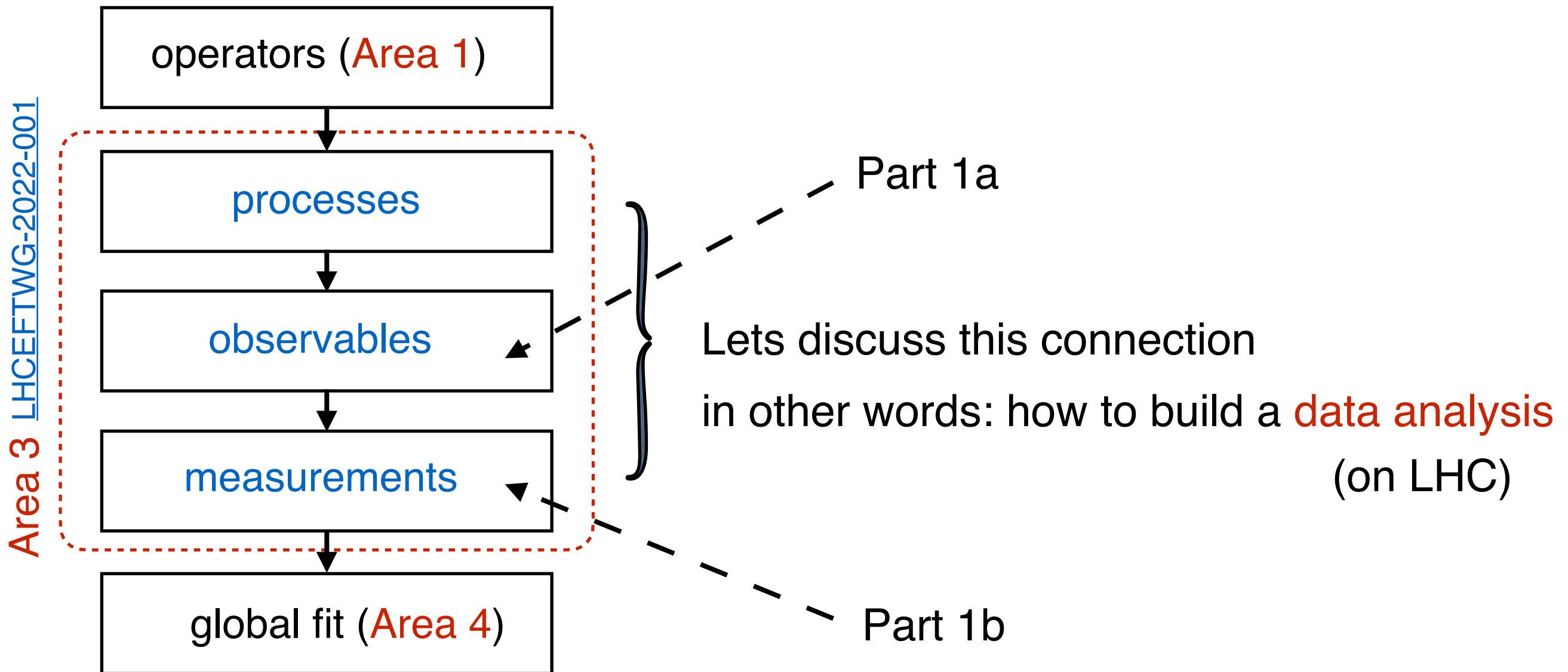
- Linear dependence (Fitmaker approach)

$$\mu_X \equiv \frac{X}{X_{SM}} = 1 + \sum_i a_i^X \frac{C_i}{\Lambda^2} + \mathcal{O}\left(\frac{1}{\Lambda^4}\right)$$



$$\begin{aligned} & -\frac{i}{2\sqrt{\bar{g}^2 + \bar{g}'^2}} \delta_{f_1 f_2} \left((\bar{g}'^2 - \bar{g}^2) \gamma^{\mu 3} P_L + 2\bar{g}'^2 \gamma^{\mu 3} P_R \right) \\ & + \frac{i\bar{g}\bar{g}'v^2}{2(\bar{g}^2 + \bar{g}'^2)^{3/2}} \delta_{f_1 f_2} C^{\varphi WB} \left((\bar{g}'^2 - \bar{g}^2) \gamma^{\mu 3} P_L - 2\bar{g}^2 \gamma^{\mu 3} P_R \right) \\ & + \frac{\sqrt{2}\bar{g}v}{\sqrt{\bar{g}^2 + \bar{g}'^2}} p_3^\nu \left(C_{f_2 f_1}^{eW*} \sigma^{\mu 3 \nu} P_L + C_{f_1 f_2}^{eW} \sigma^{\mu 3 \nu} P_R \right) \\ & + \frac{\sqrt{2}\bar{g}'v}{\sqrt{\bar{g}^2 + \bar{g}'^2}} p_3^\nu \left(C_{f_2 f_1}^{eB*} \sigma^{\mu 3 \nu} P_L + C_{f_1 f_2}^{eB} \sigma^{\mu 3 \nu} P_R \right) \\ & + \frac{1}{2} i v^2 \sqrt{\bar{g}^2 + \bar{g}'^2} C_{f_1 f_2}^{\varphi l 1} \gamma^{\mu 3} P_L + \frac{1}{2} i v^2 \sqrt{\bar{g}^2 + \bar{g}'^2} C_{f_1 f_2}^{\varphi l 3} \gamma^{\mu 3} P_L \\ & + \frac{1}{2} i v^2 \sqrt{\bar{g}^2 + \bar{g}'^2} C_{f_1 f_2}^{\varphi e} \gamma^{\mu 3} P_R \end{aligned}$$

Part 1 (Chapter II)



(II) Observables (1a)

$$\mathcal{P}(\vec{x}_{\text{reco}} | \vec{\theta}) = \int d\vec{x}_{\text{part}} p(\vec{x}_{\text{reco}} | \vec{x}_{\text{part}}) \mathcal{P}(\vec{x}_{\text{part}} | \vec{\theta})$$

reco
observables
Part 1a

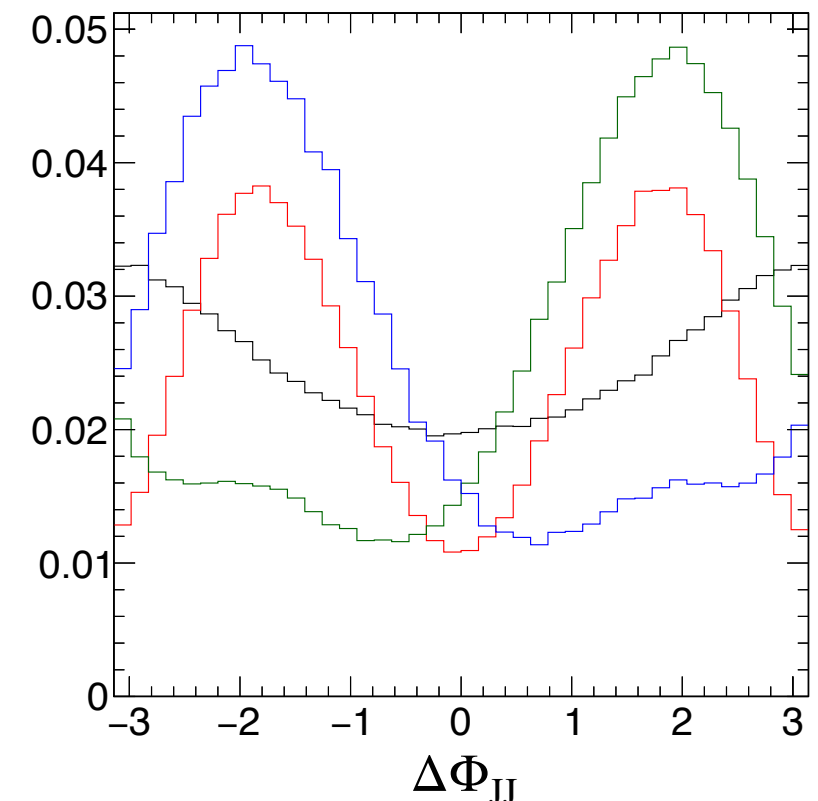
- typical **SM observables** (to suppress background)
- **EFT-sensitive** observables (e.g. angular, q^2 , etc)
- **optimized observables** (matrix element, machine learning)
- **full accessible information** $\vec{x}_{\text{reco}}^{\text{full}}$ (e.g. all four-vectors)

Example: VBF $\Delta\Phi_{JJ}$ (**EFT-sensitive**)

EFT:

- new tensor structures
- higher q dimensions

SM	—	$(\theta_0, 0)$
CP-odd	—	$(0, \theta_1)$
+mix	—	$(\theta_0, +\theta_1)$
-mix	—	$(\theta_0, -\theta_1)$



(II) Observables (1a)

$$\mathcal{P}(\vec{x}_{\text{reco}} | \vec{\theta}) = \int d\vec{x}_{\text{part}} p(\vec{x}_{\text{reco}} | \vec{x}_{\text{part}}) \mathcal{P}(\vec{x}_{\text{part}} | \vec{\theta})$$



reco
observables
Part 1a

- typical **SM observables** (to suppress background)
- **EFT-sensitive** observables (e.g. angular, q^2 , etc)
- **optimized observables** (matrix element, machine learning)
- **full accessible information** $\vec{x}_{\text{reco}}^{\text{full}}$ (e.g. all four-vectors)

- **full information** is the best, but hard to deal with $ND, N \gg 1$
- **optimized observables**: pack **full information** in $1D$ optimal for **one target** works if the number of targets is small
- **observable** choice does not limit its usage
(e.g. **differential measurement** of an **optimized observable** is an option)

(II) Optimized Observables

$$\mathcal{P}(\vec{x}_{\text{reco}} | \vec{\theta}) \propto \mathcal{P}_0(\vec{x}_{\text{reco}}) + \sum_k \left(\frac{2\theta_k}{\theta_0} \right) \mathcal{P}_{0k}(\vec{x}_{\text{reco}}) + \sum_k \left(\frac{\theta_k}{\theta_0} \right)^2 \mathcal{P}_k(\vec{x}_{\text{reco}}) + \sum_{i<j} \left(\frac{2\theta_i\theta_j}{\theta_0^2} \right) \mathcal{P}_{ij}(\vec{x}_{\text{reco}})$$

- Two types from first principles: (matrix elements for models θ_0, θ_1)

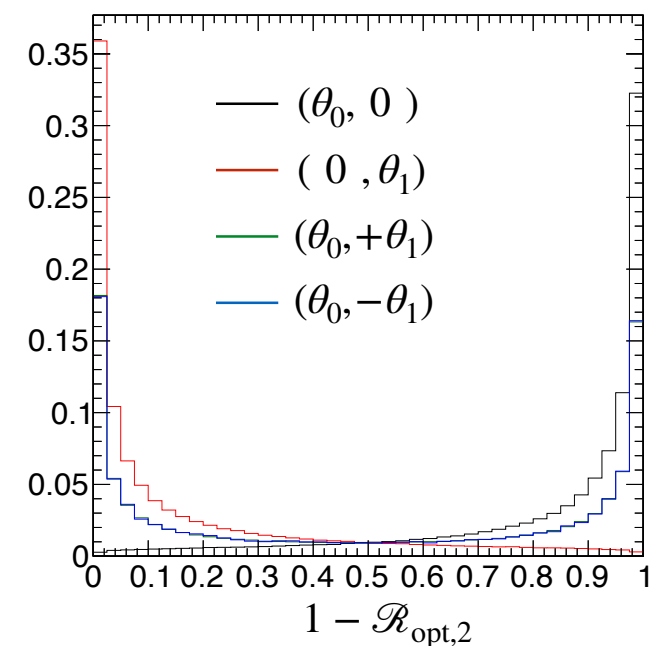
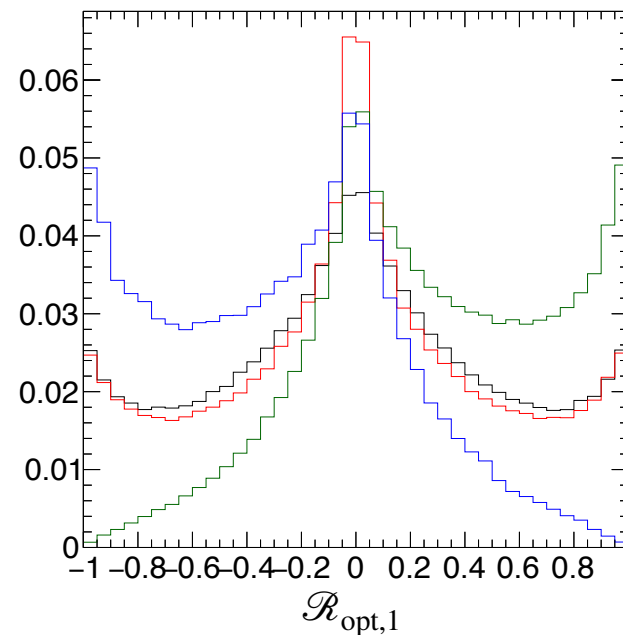
$$\mathcal{R}_{\text{opt},1} = \frac{2\mathcal{P}_{01}(\vec{x}_{\text{reco}}^{\text{full}})}{\mathcal{P}_0(\vec{x}_{\text{reco}}^{\text{full}}) + c \cdot \mathcal{P}_1(\vec{x}_{\text{reco}}^{\text{full}})}$$

$$\mathcal{R}_{\text{opt},2} = \frac{\mathcal{P}_1(\vec{x}_{\text{reco}}^{\text{full}})}{\mathcal{P}_0(\vec{x}_{\text{reco}}^{\text{full}}) + c \cdot \mathcal{P}_1(\vec{x}_{\text{reco}}^{\text{full}})}$$

- Machine learning equivalent (parton shower, detector effects)

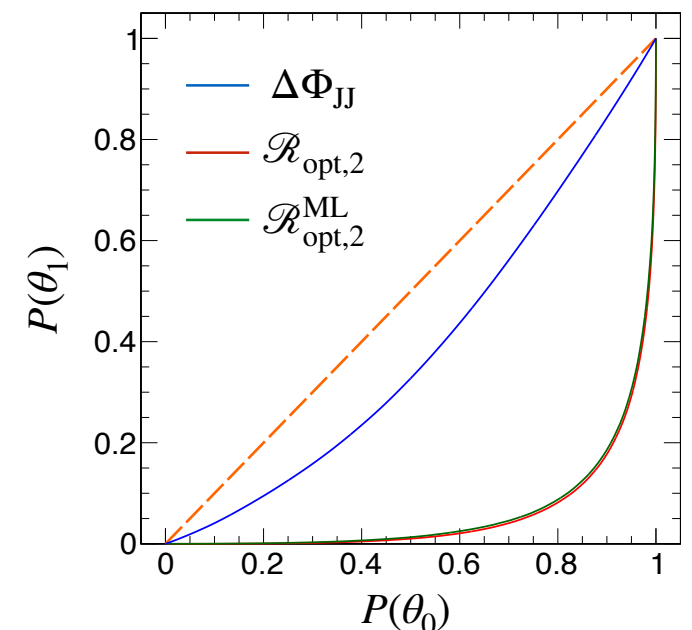
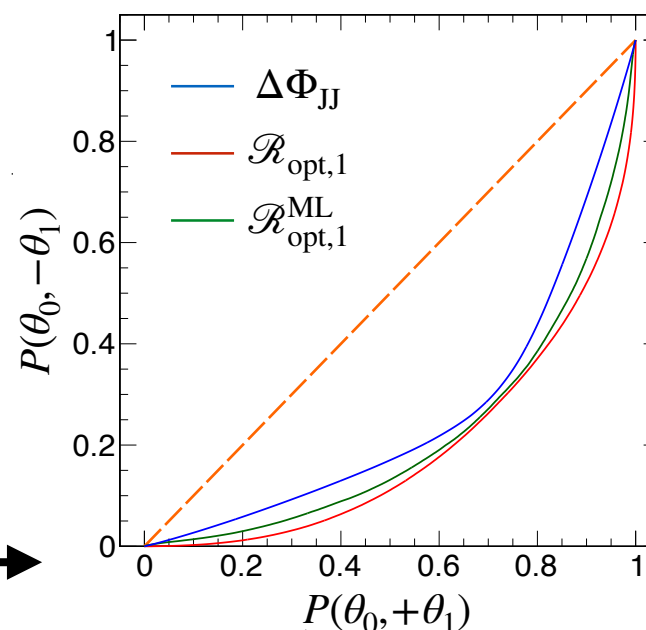
$\mathcal{R}_{\text{opt},1}$: train +mix vs -mix

$\mathcal{R}_{\text{opt},2}$: train θ_1 vs θ_0 (SM)



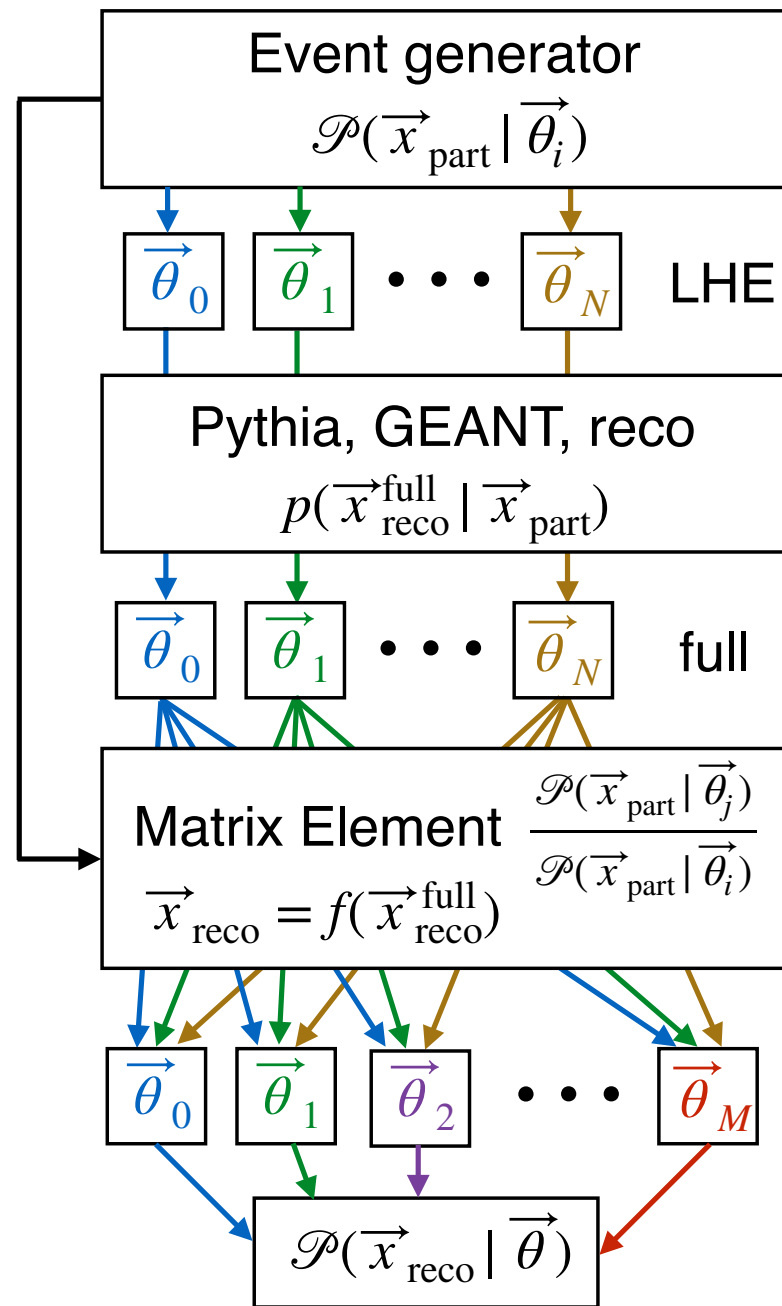
- Essential to limit the set of θ_i
 - determine sensitive θ_i in advance
 - rotate basis to remove flat directions

e.g. in VBF: rotate to $\theta_1 = \tilde{c}_{zz}$



(II) Two Types of Measurements (2b)

- **Single-step** approach (folded)



- **Two-step** approach (unfolded)

— step 1: “unfold” to **parton-level distribution**

$$\mathcal{P}(\vec{x}_{\text{reco}}|\vec{\theta}) = \int d\vec{x}'_{\text{part}} p'(\vec{x}_{\text{reco}}|\vec{x}'_{\text{part}};\vec{\theta}) \mathcal{P}(\vec{x}'_{\text{part}}|\vec{\theta})$$

usually assume **SM** θ_0

$\vec{x}'_{\text{part}} \subset \vec{x}_{\text{part}}$

— step 2: (re)**interpretation** - global fit

- **Single-step** (folded)

— can be **optimal** and **unbiased**

— most **difficult** and **no re-interpretation**

- **Two-step** (unfolded)

— **easier** and open for **re-interpretation**

— **not full information**, **SM assumption**

$$\mathcal{P}(\vec{x}_{\text{reco}}|\vec{\theta}) \propto \mathcal{P}_0(\vec{x}_{\text{reco}}) + \sum_k \left(\frac{2\theta_k}{\theta_0} \right) \mathcal{P}_{0k}(\vec{x}_{\text{reco}}) + \sum_k \left(\frac{\theta_k}{\theta_0} \right)^2 \mathcal{P}_k(\vec{x}_{\text{reco}}) + \sum_{i<j} \left(\frac{2\theta_i\theta_j}{\theta_0^2} \right) \mathcal{P}_{ij}(\vec{x}_{\text{reco}})$$

(II) Differential cross sections (unfolding)

unfolding:
$$\frac{d\sigma_{t\bar{t}}}{dX^i} = \frac{1}{\mathcal{L} \cdot \Delta X^i \cdot \epsilon_{eff}^i} \cdot \sum_j R_{ij}^{-1} \cdot f_{acc}^j \cdot (N_{obs}^j - N_{bkg}^j)$$

Response Matrix
Data Events
Expected Background Events

Integrated luminosity
bin width

reverse

$$\mathcal{P}(\vec{x}_{reco}|\vec{\theta}) = \int d\vec{x}'_{part} p'(\vec{x}_{reco}|\vec{x}'_{part};\vec{\theta})\mathcal{P}(\vec{x}'_{part}|\vec{\theta})$$

- Differential cross sections — detector corrected measurement
 - historically **tools for theorists** to test calculations and MC tuning
 - more recently **EFT applications** — shape dependence
- Potential concerns:
 - **unfolding** procedure — best with **diagonal response matrix**
 - **biased to SM** in unfolding — often small, best with **flat acceptance effects**
 - EFT effect in **background** — best with **high S/B**
- STXS: “sort-of” differential measurement, likelihood-based fits (may use OO)
 - unique to Higgs: multiple production, multiple decay modes

(II) MEM and ML likelihood inference

- not the same as **optimized observables** (though can be used to compute):
 - ME or ML **observables** can be used in any approach (e.g. differential)
- Matrix Element Method (**MEM**) — compute the likelihood from first principles

$$\mathcal{P}(\vec{x}_{\text{reco}} | \vec{\theta}) = \int d\vec{x}_{\text{part}} p(\vec{x}_{\text{reco}} | \vec{x}_{\text{part}}) \mathcal{P}(\vec{x}_{\text{part}} | \vec{\theta})$$

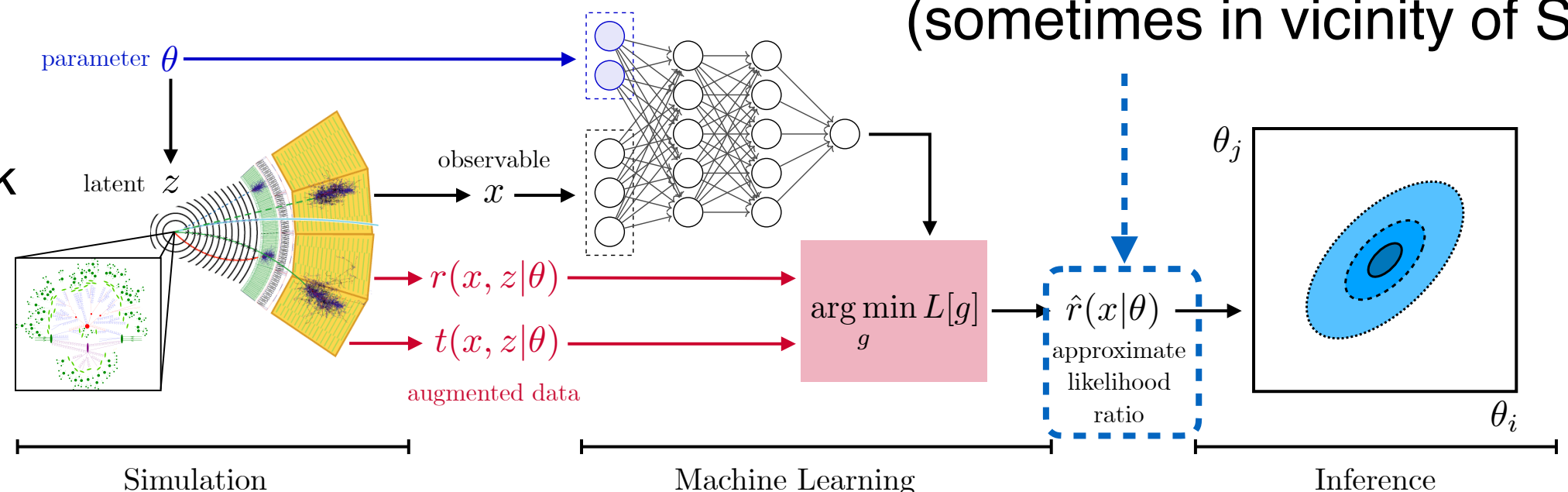
← full info

ideal for EFT, but: **hard to model** transfer function p , **ME not available** for all processes...
 few examples in Higgs, top, EW (e.g. backgrounds)

- Machine Learning (**ML**) inference

— learn the full likelihood ratio (sometimes in vicinity of SM)

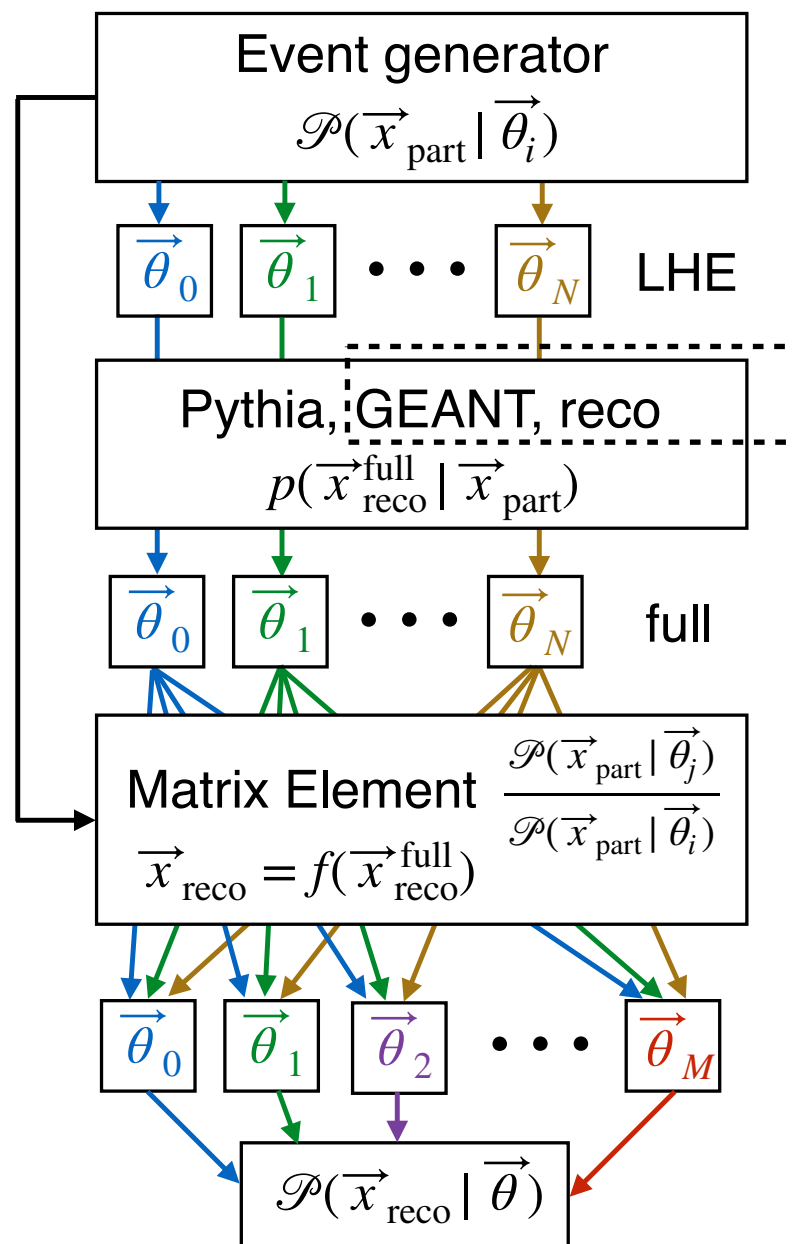
see next talk by Robert Schoefbeck



(II) Template likelihood fit

- Most common fit approach is based on “templates”

$$\mathcal{P}(\vec{x}_{\text{reco(part)}} | \vec{\theta}) \propto \mathcal{P}_0(\vec{x}_{\text{reco}}) + \sum_k \left(\frac{2\theta_k}{\theta_0} \right) \mathcal{P}_{0k}(\vec{x}_{\text{reco(part)}}) + \sum_k \left(\frac{\theta_k}{\theta_0} \right)^2 \mathcal{P}_k(\vec{x}_{\text{reco(part)}}) + \sum_{i < j} \left(\frac{2\theta_i\theta_j}{\theta_0^2} \right) \mathcal{P}_{ij}(\vec{x}_{\text{reco(part)}})$$



— templates in **bins of observables** / measurements

two-step: first **SM templates** with full simulation

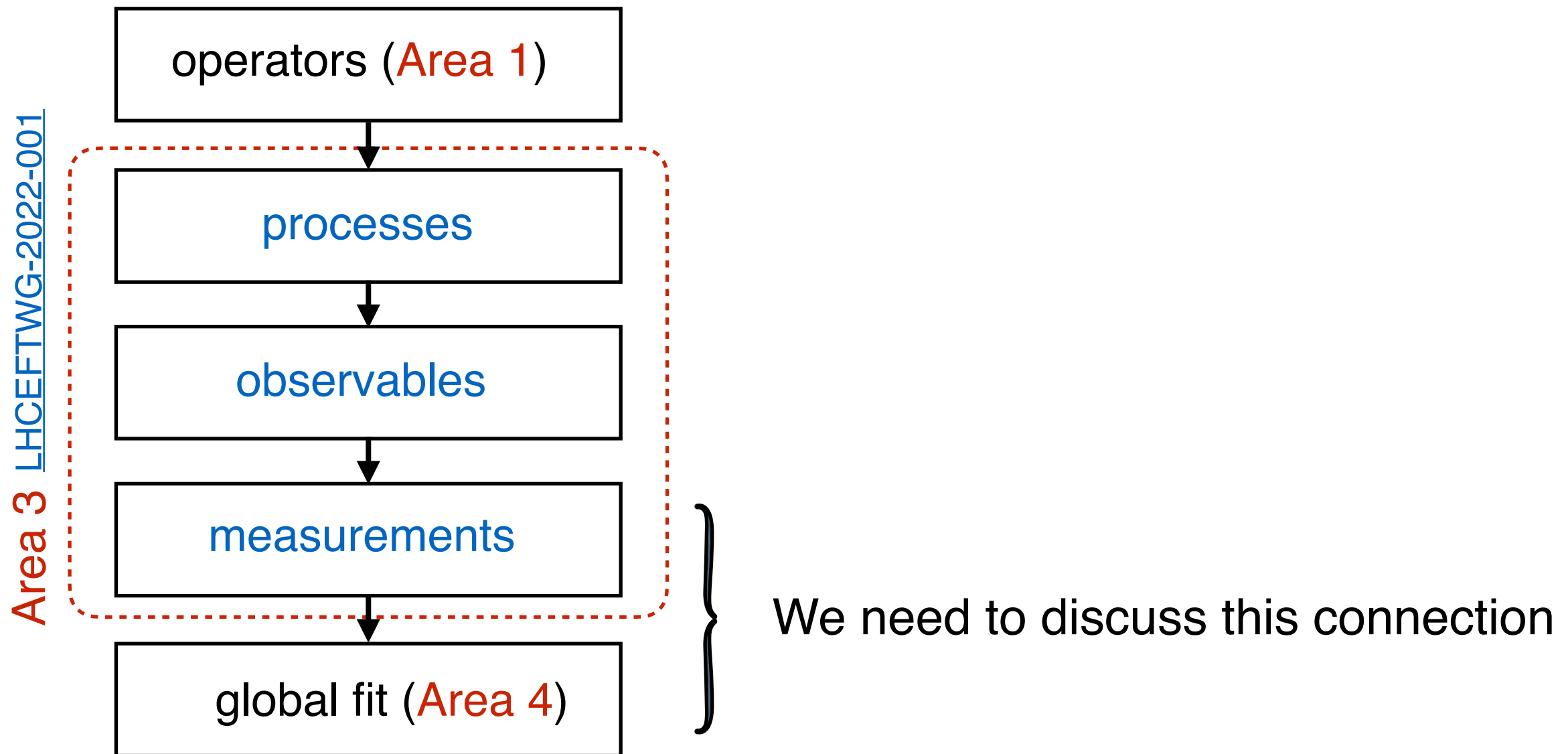
skip second **EFT templates** without detector

(e.g. globals fits in **Area 4**)

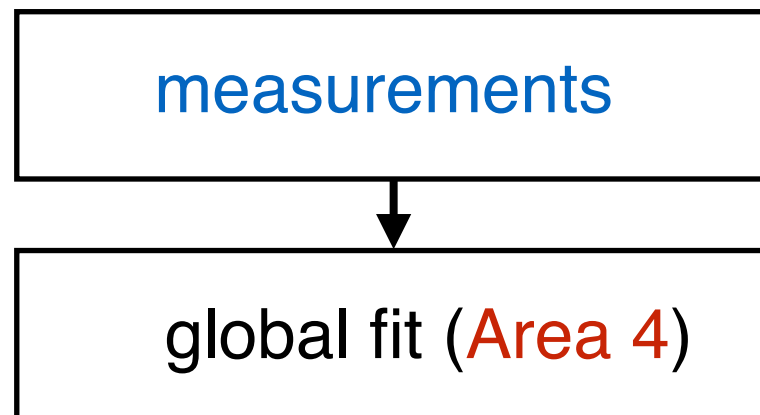
single-step: make **EFT templates** with full simulation

- Bottom line: variety of **approaches**
no unique **recommendation**
awareness of pros / cons, tools
practical choices

Final step in measurements: communicate results



Final step in measurements: communicate results



} We need to discuss this connection

- How to communicate **systematics, bias**, and with all **correlations**
- How to communicate **dedicated measurements** (**single-step**)
 - **approximate likelihood** (Gaussian assumptions break, correlations lost...)
 - direct fits **by LHC collaborations** (+ theorists, activity by this WG)
 - report “**full likelihood**” — no practical EFT examples yet, but works in exotica
 - HEPData supports HistFactory model (full-blown workspaces)
 - limited to **template** fits currently, **equivalent to fits by collaborations**
 - report experimental **EFT templates** with full simulation + observation
(kind of “STXS” at detector level)

Summary: EFT Measurements and Observables

- Observables for EFT LHC EFT WG Area 3
 - from “**simple**” to **optimized** observables [LHCEFTWG-2022-001](#)
 - clear prescription if optimization is desired
needed: clear shared target

- Measurements for EFT global fits
 - unfolded (**two-step**) $\left\{ \begin{array}{l} \text{easier and open for re-interpretation} \\ \text{not full information, SM assumption} \end{array} \right.$

inclusive, differential, and STXS used in global EFT fits
challenges: uncertainties, correlations, EFT in backgrounds...

- folded (**single-step**) $\left\{ \begin{array}{l} \text{can be optimal and unbiased} \\ \text{most difficult and no re-interpretation} \end{array} \right.$

MEM, ML inference, template fit with OO

we are still to successfully **interface** these to the global EFT fits...