



Reweighting of MC sample

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Motivation

Lagrangian

matrix-element

parton events

Showered events

hadronized events

Detector events

FULL SIMULATION
SLOWEST PART

Motivation

Lagrangian

matrix-element

parton events

Showered events

hadronized events

FULL SIMULATION
SLOWEST PART

Detector events

Re-Weighting

- Reuse the sample (Only one Full Sim)
- Change the weight of the events

$$W_{new} = \frac{|M_{new}|^2}{|M_{old}|^2} * W_{old}$$

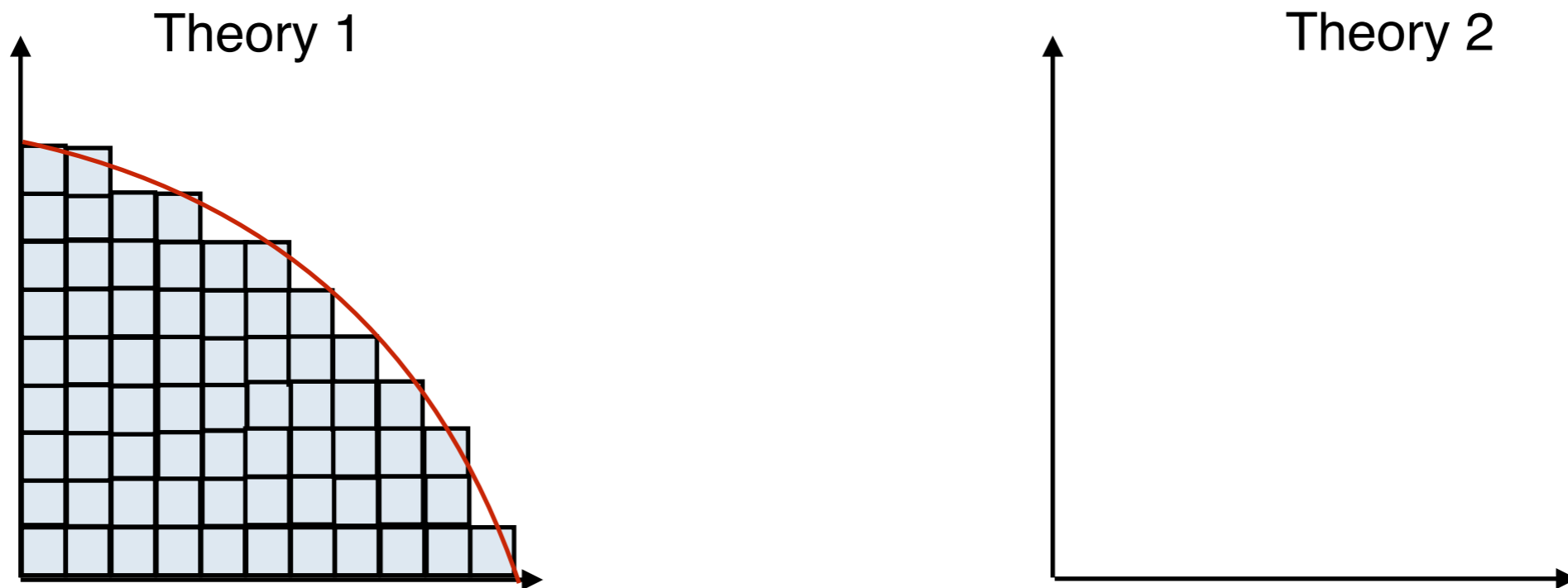
1405.0301

1404.7129

Scan

LHE Events

- Is nothing else than a (efficient) probing of the phase-space

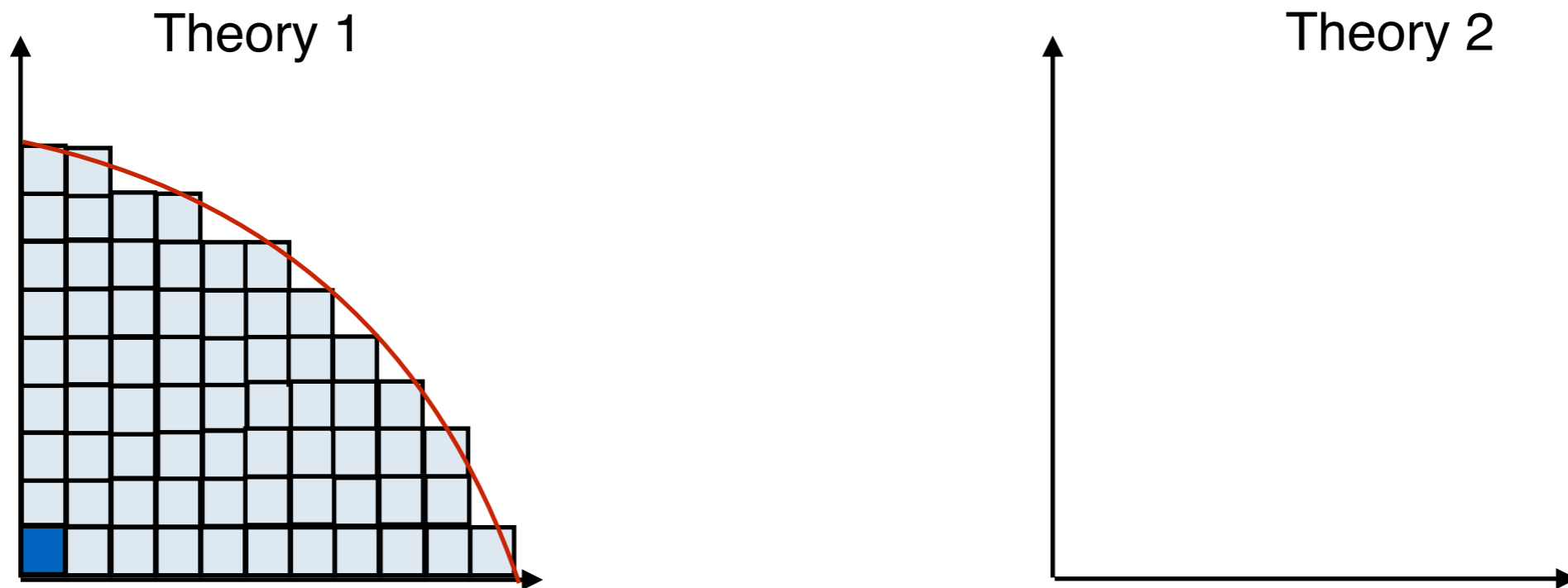


- Fully differential method (not one dimension)

Scan

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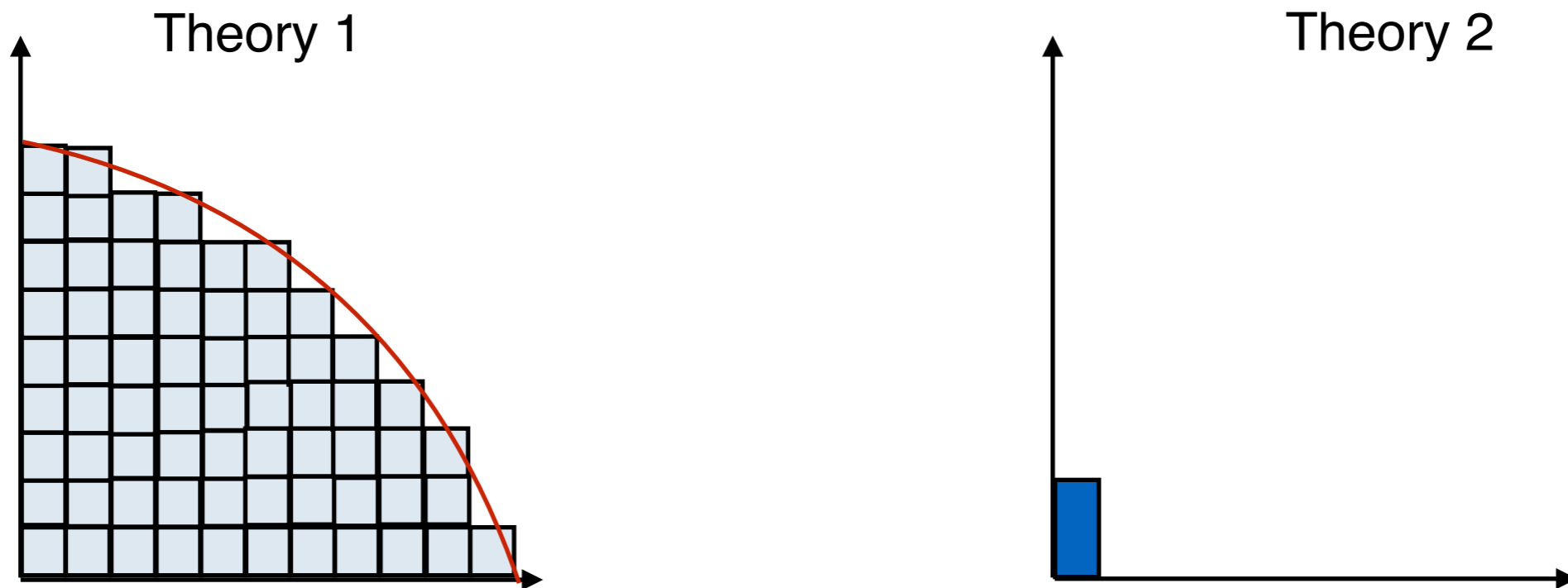


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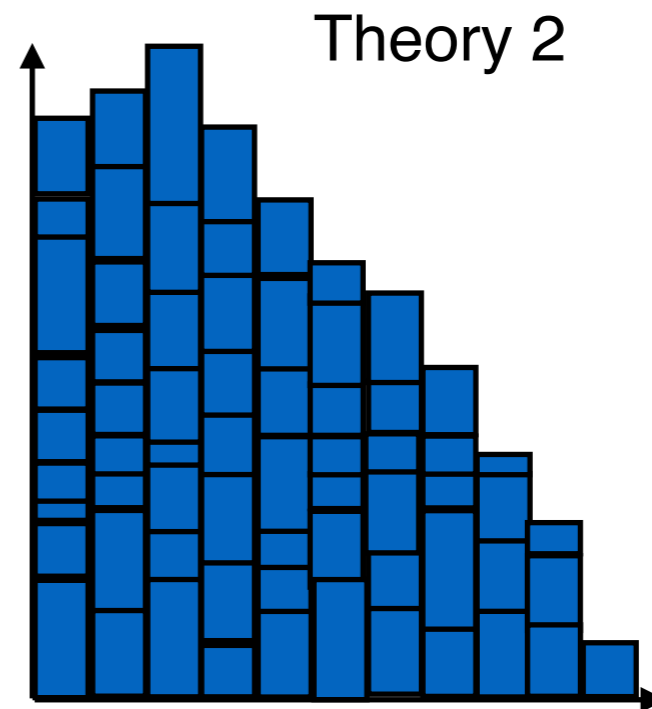
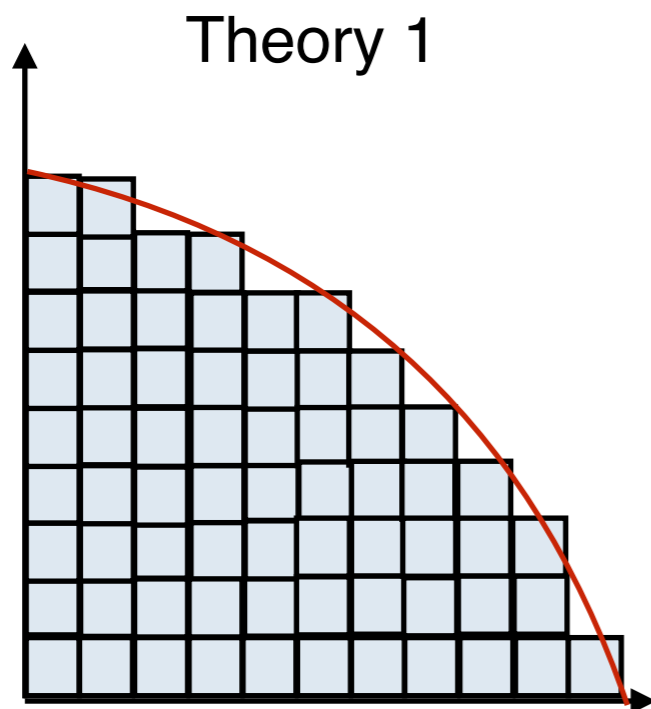


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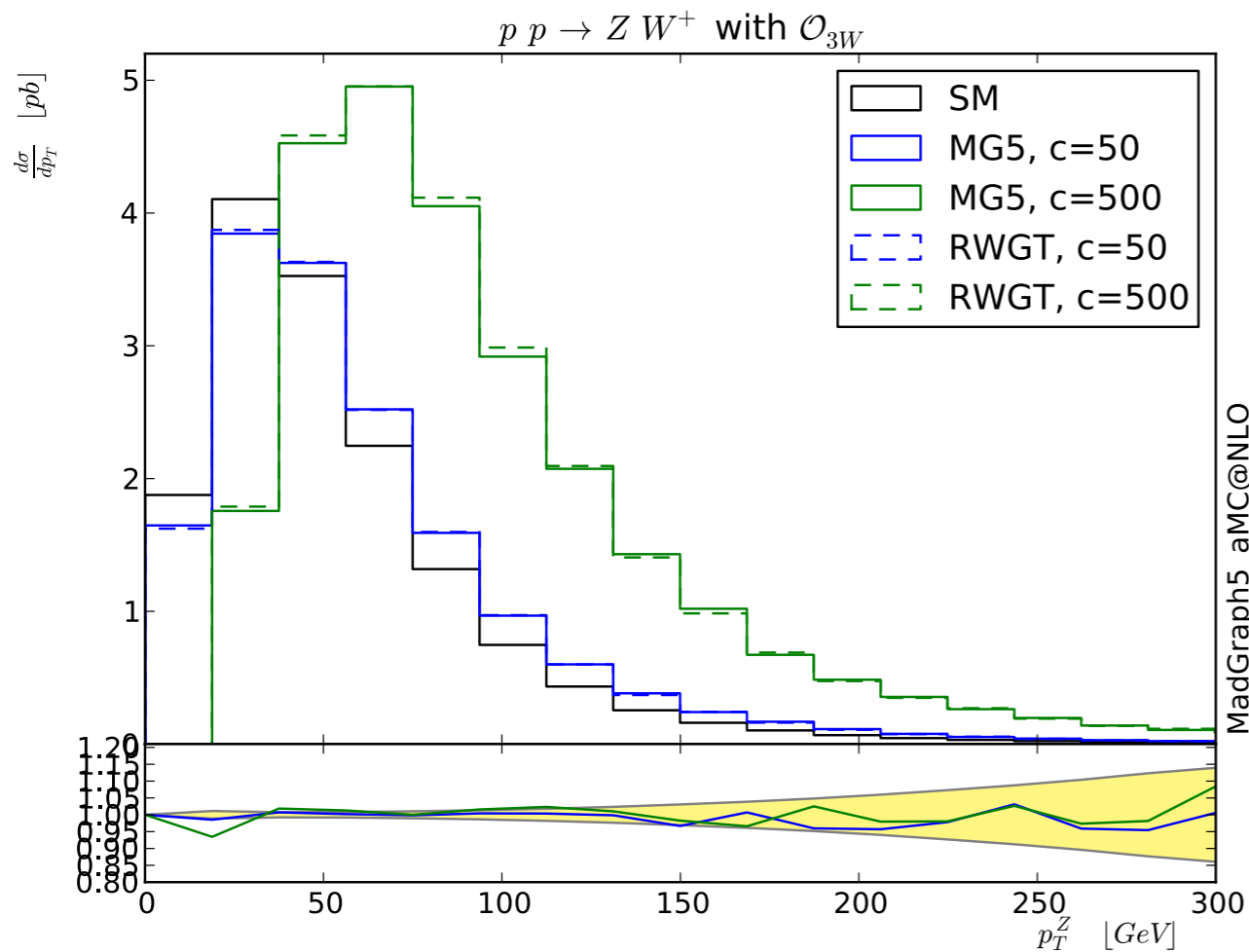
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Re-Weighting usage

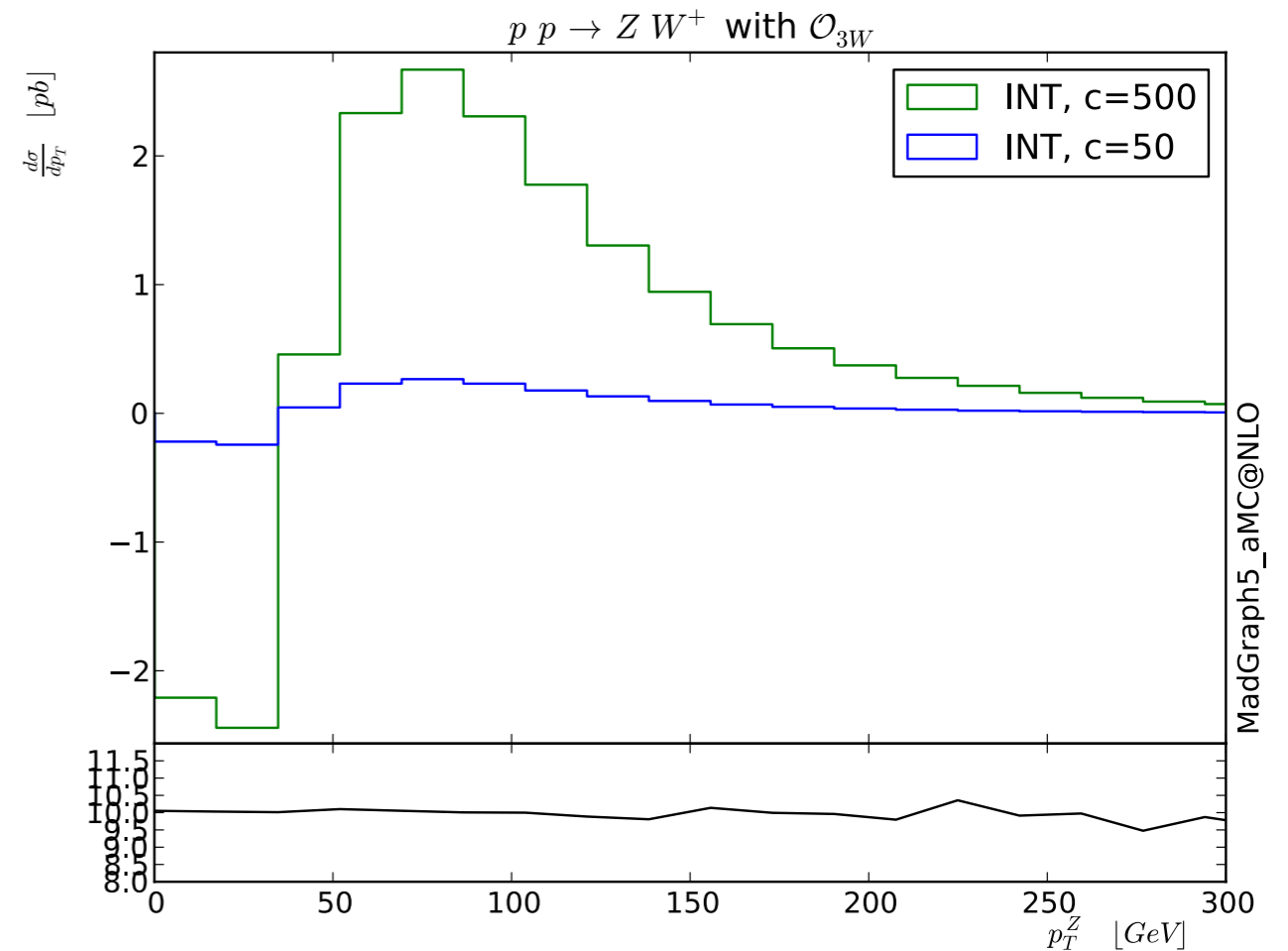
- scale and pdf uncertainties (available both for LO and NLO computation)
- re-introduce top mass effect for Higgs processes
- EFT scan
- Many other application

Examples EFT

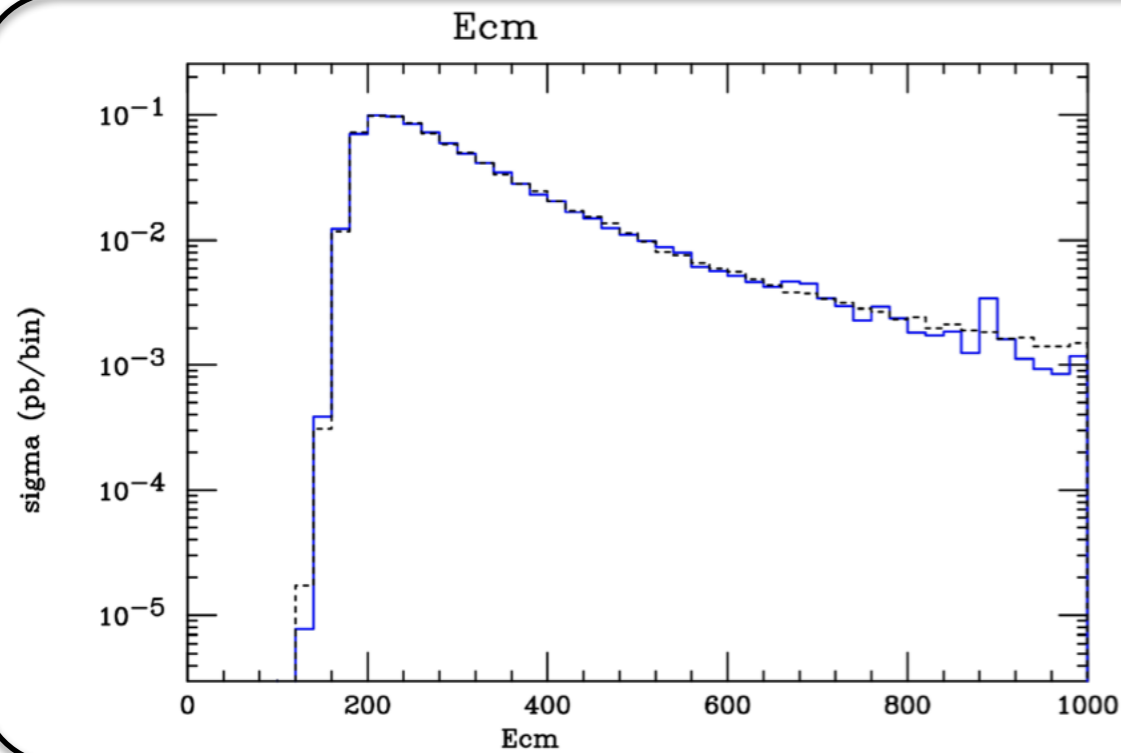
Re-Weighting (by SM+Interference)



Interference contribution

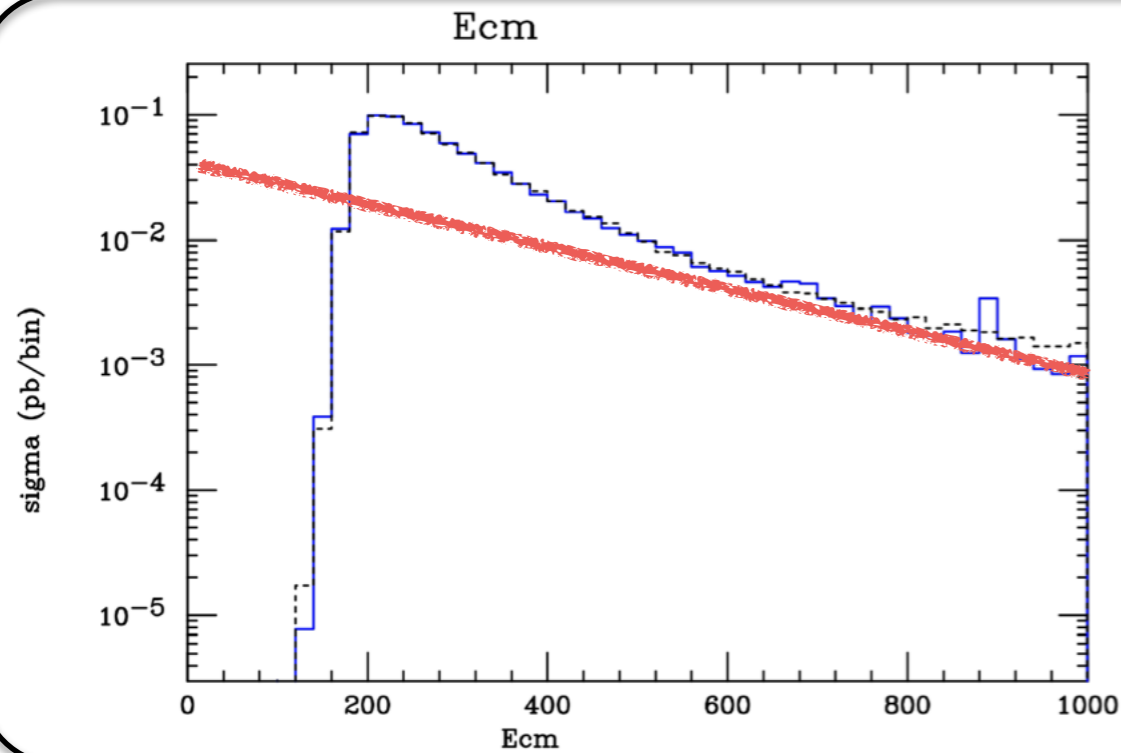


Re-Weighting Limitation



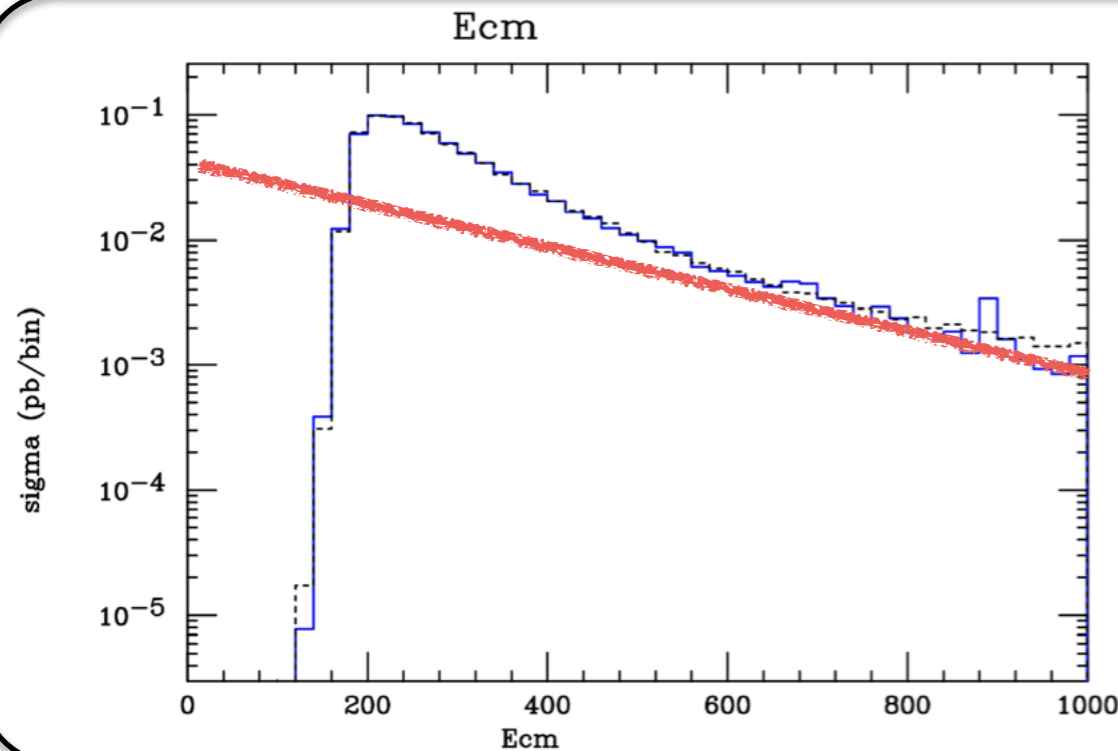
- statistical uncertainty are enhanced by the re-weighting
- better to have $wgt < 1$ and small variance

Re-Weighting Limitation



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Re-Weighting Limitation



- statistical uncertainty are enhanced by the re-weighting
- better to have $wgt < 1$ and small variance

- You need to have the same phase-space (more exactly a subset)

Caution

LHE Additional information

Helicity

Leading color information

Intermediate particle

Caution

LHE Additional information

Helicity

- Partial helicity distribution are not correct with the full re-weighting
- Solution $W_{new} = \frac{|M_{new}^h|^2}{|M_{orig}^h|^2} W_{orig},$
- This is done by default !

Leading color information

Intermediate particle

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Leading color information

- modify the parton-shower so not suitable.

Intermediate particle

- modify the parton-shower so not suitable.

GPU

- Reweighting are massively repetitive task
- Ideal for GPU
 - ➔ Zenny Wettersten
- We are in need of real experimental test case
 - ➔ Number of event in sample
 - ➔ Number of benchmark



NLO Re-Weighting

NLO method

- tracks the dependencies in the various matrix-elements (born, virtual, real)

$$d\sigma^\alpha = f_1(x_1, \mu_F) f_2(x_2, \mu_F) \left[\mathcal{W}_0^\alpha + \mathcal{W}_F^\alpha \log(\mu_F/Q)^2 + \mathcal{W}_R^\alpha \log(\mu_R/Q)^2 \right] d\chi^\alpha,$$

$$\mathcal{W}_\beta^\alpha = \mathcal{B} * \mathcal{C}_{\beta,B}^\alpha + \mathcal{B}_{CC} * \mathcal{C}_{\beta,BCC}^\alpha + \mathcal{V} * \mathcal{C}_{\beta,V}^\alpha + \mathcal{R} * \mathcal{C}_{\beta,R}^\alpha$$

- re-weight each part according to the associated matrix-element

$$\begin{aligned} \mathcal{W}_{\beta,B}^{\alpha,new} &= \frac{\mathcal{B}^{new}}{\mathcal{B}^{old}} * \mathcal{W}_{\beta,B}^{\alpha,old}, \\ \mathcal{W}_{\beta,V}^{\alpha,new} &= \frac{\mathcal{V}^{new}}{\mathcal{V}^{old}} * \mathcal{W}_{\beta,V}^{\alpha,old}, \\ \mathcal{W}_{\beta,R}^{\alpha,new} &= \frac{\mathcal{R}^{new}}{\mathcal{R}^{old}} * \mathcal{W}_{\beta,R}^{\alpha,old}. \end{aligned}$$

NLO ISSUE

- MadGraph use some phase-space trick to avoid to compute the loop as much as possible (and replace it by the born)
 - ➔ Need smarter/complex re-weighting

$$\begin{aligned} \mathcal{W}_{\beta,B}^{\alpha,new} &= \frac{\mathcal{B}^{new}}{\mathcal{B}^{old}} * \mathcal{W}_{\beta,B}^{\alpha,old}, \\ \mathcal{W}_{\beta,V}^{\alpha,new} &= \frac{\mathcal{V}^{new}}{\mathcal{V}^{old}} * \mathcal{W}_{\beta,V}^{\alpha,old}, \\ \mathcal{W}_{\beta,R}^{\alpha,new} &= \frac{\mathcal{R}^{new}}{\mathcal{R}^{old}} * \mathcal{W}_{\beta,R}^{\alpha,old}. \end{aligned}$$



$$\begin{aligned} \mathcal{W}_{\beta,BB}^{\alpha,new} &= \frac{(\mathcal{B}^{new} + \mathcal{V}^{new})}{(\mathcal{B}^{old} + \mathcal{V}^{old})} * \mathcal{W}_{\beta,BB}^{\alpha,old} \\ \mathcal{W}_{\beta,BC}^{\alpha,new} &= \frac{\mathcal{B}^{new}}{\mathcal{B}^{old}} * \mathcal{W}_{\beta,BC}^{\alpha,old} \\ \mathcal{W}_{\beta,V}^{\alpha,new} &= \frac{(\mathcal{B}^{new} + \mathcal{V}^{new})}{(\mathcal{B}^{old} + \mathcal{V}^{old})} * \mathcal{W}_{\beta,V}^{\alpha,old} \\ \mathcal{W}_{\beta,R}^{\alpha,new} &= \frac{\mathcal{R}^{new}}{\mathcal{R}^{old}} * \mathcal{W}_{\beta,R}^{\alpha,old} \end{aligned}$$

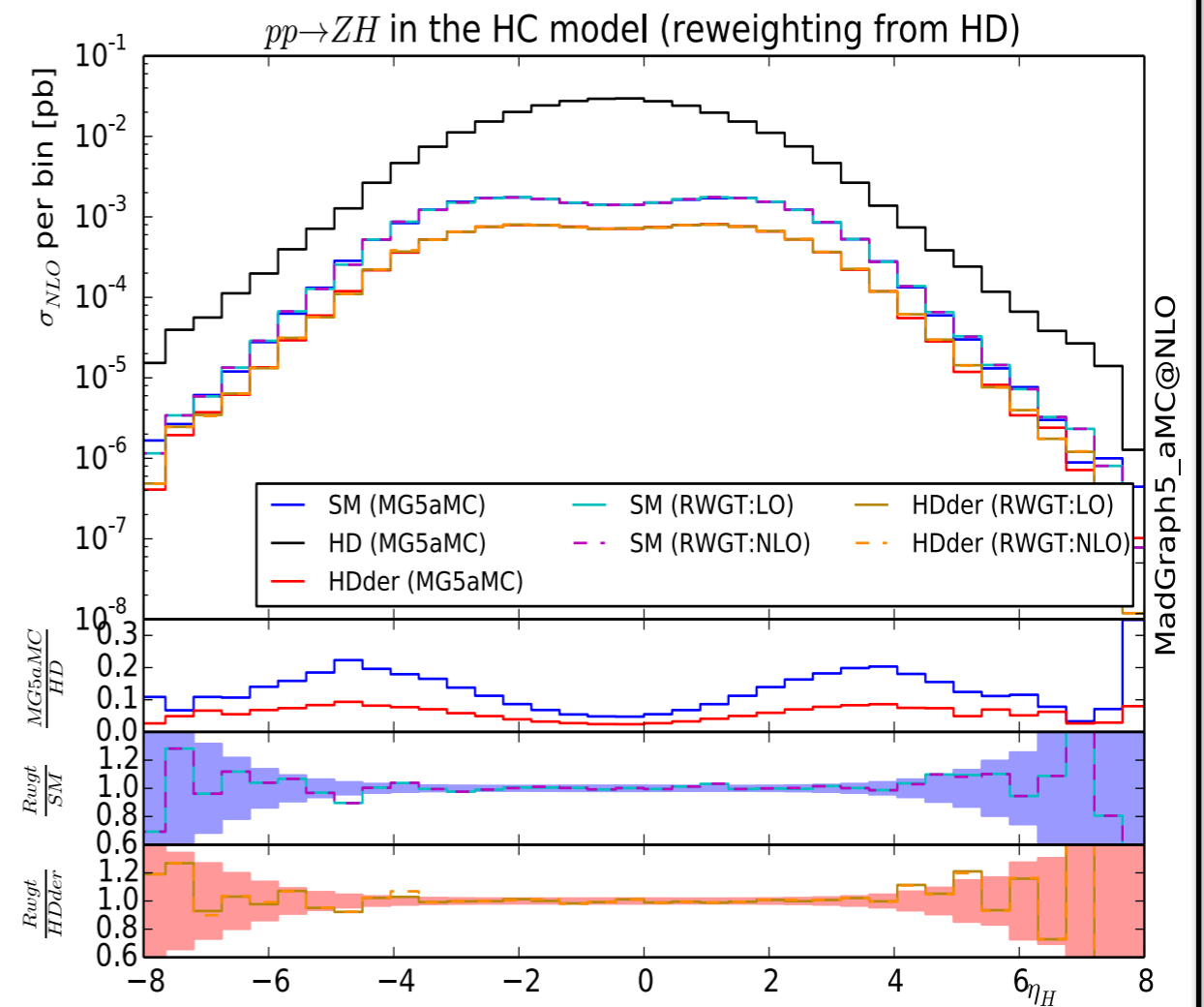
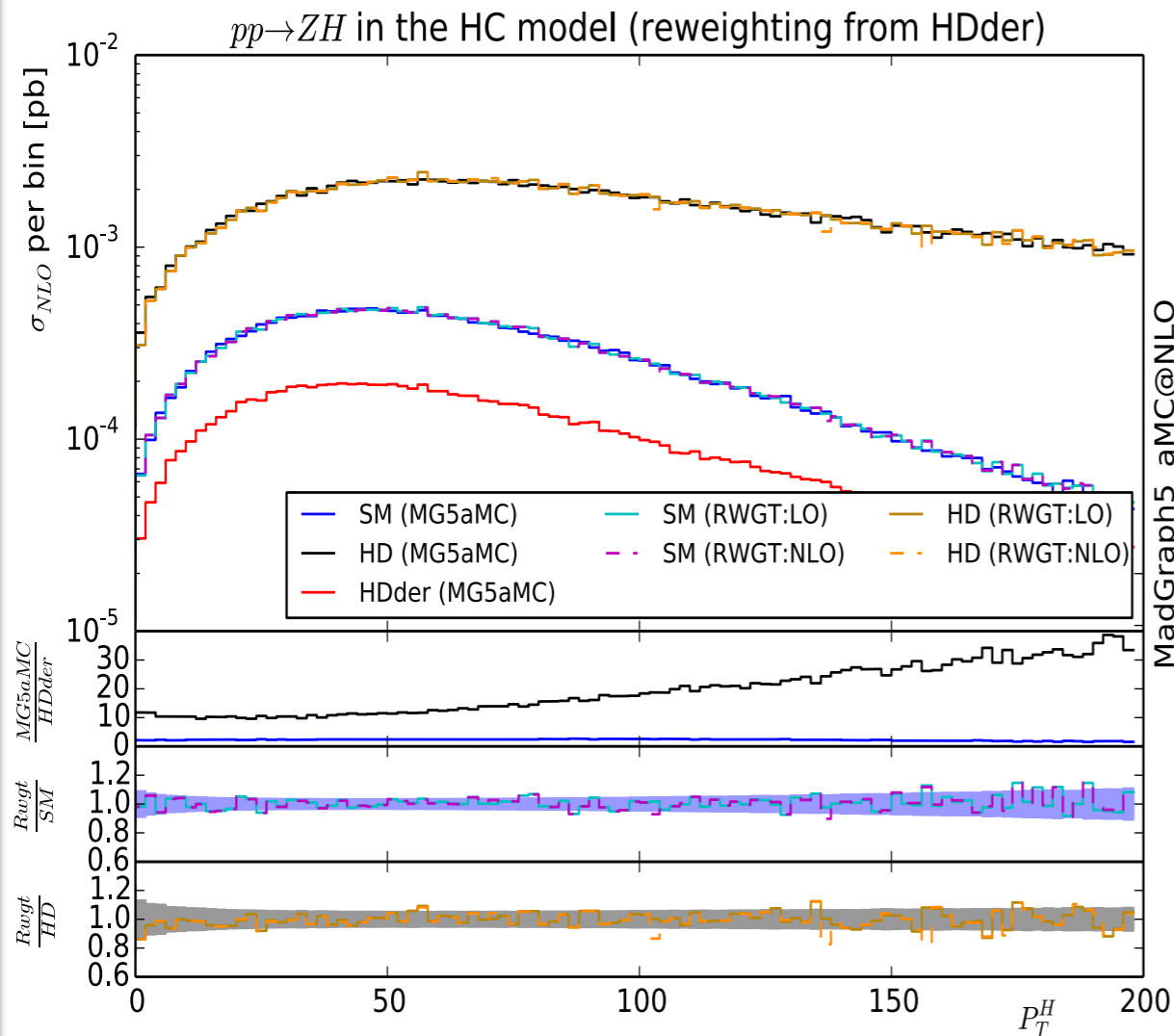
NLO Re-Weighting

EFT Example

$$\mathcal{L}_{HD} = -\frac{1}{4} \frac{1}{\Lambda} \kappa_{HWW} Z_{\mu\nu} Z^{\mu\nu} H$$

$$\mathcal{L}_{HDder} = -\frac{1}{\Lambda} \kappa_{H\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} H +$$

$$\left(-\frac{1}{\Lambda} \kappa_{H\partial W} W_\nu^+ \partial_\mu W^{-\mu\nu} H + h.c. \right),$$



Conclusion

- Re-using previous generation/computation is always a smart move.
- This methods is fully exact but **not bullet proof**
 - Need to check overlap of phase-space/helicity
 - not (really) suitable for mass scanning
 - helicity (need to be careful)
 - leading color information
 - intermediate particle
- NLO is ready
 - Same limitation
 - Issue with numerical precision

Why it works

without un-weighting

$$\begin{aligned}\sigma_{orig} &= \sum_{i=1}^N W_{orig}^i \\ &= \sum_{i=1}^N f_1(x_1^i) \cdot f_2(x_2^i) \cdot |M_{orig}^i|^2 \cdot d\Omega\end{aligned}$$

$$\begin{aligned}\sigma_{new} &= \sum_{i=1}^N W_{new}^i \\ &= \sum_{i=1}^N f_1(x_1^i) \cdot f_2(x_2^i) \cdot |M_{new}^i|^2 \cdot d\Omega\end{aligned}$$

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unweighting case

unweighted sample

$$\begin{aligned}\sigma_{orig} &= \sum_{i=1}^N W_{orig}^i, \\ &= \max_i(W_{orig}^i) \sum_{i=1}^N \frac{W_{orig}^i}{\max_i(W_{orig}^i)}, \\ &\approx \sum_{i=1}^N \max_i(W_{orig}^i) Acc_i\end{aligned}$$

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helicity case

$$\begin{aligned}\sigma_{orig} &= \sum_{i=1}^N W_{orig}^i P_{h,orig}^i \\ &= \sum_{i=1}^N W_{orig}^i \frac{|M_{orig}^h|^2}{\sum_{\tilde{h}} |M_{orig}^{\tilde{h}}|^2},\end{aligned}$$

$$\begin{aligned}\sigma_{new} &= \sum_{i=1}^N W_{new}^i P_{h,new}^i \\ &= \sum_{i=1}^N W_{new}^i \frac{|M_{new}^h|^2}{\sum_{\tilde{h}} |M_{new}^{\tilde{h}}|^2}, \\ &= \sum_{i=1}^N W_{orig}^i \frac{\sum_{\tilde{h}} |M_{new}^{\tilde{h}}|^2}{\sum_{h'} |M_{orig}^{h'}|^2} \frac{|M_{new}^h|^2}{\sum_{\tilde{h}} |M_{new}^{\tilde{h}}|^2}, \\ &= \sum_{i=1}^N W_{orig}^i \frac{1}{\sum_{h'} |M_{orig}^{h'}|^2} \frac{|M_{new}^h|^2}{1}, \\ &= \sum_{i=1}^N W_{orig}^i \frac{|M_{orig}^h|^2}{\sum_{h'} |M_{orig}^{h'}|^2} \frac{|M_{new}^h|^2}{|M_{orig}^h|^2}, \\ &= \sum_{i=1}^N W_{orig}^i P_{h,orig}^i \frac{|M_{new}^h|^2}{|M_{orig}^h|^2}.\end{aligned}$$