

*RECFTA-meeting, Košice, May 27, 2011*

# *Neutrino Physics in Slovakia*

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# *Neutrino Physicists in Slovakia*



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**Participants (experiment):** P. Povinec, K. Holý, I. Sýkora, J. Staníček, M. Pikna  
P. Valko, J. Szarka, J. Vanko, M. Müllerová,  
R. Hodák (PhD), P. Valko (PhD)

**Experiments:**  $0\nu\beta\beta$  (NEMO3, SuperNEMO – 2004/2010  
TGV-2002, COBRA-2005)

$0\nu\varepsilon\varepsilon$  (on  $^{74}\text{Se}$  in Bratislava, proposal for LSM Modane) - 2009  
charge-changing reaction at RCNP Osaka - 2008  
beta beams at ISOLDE -2009

## *OUTLINE*

- *$0\nu\beta\beta$ -decay (theory+experiment)*
- *$0\nu\varepsilon\varepsilon$ -decay (theory+experiment)*
- *$2\nu\beta\beta$ -decay and bosonic neutrinos (theory)*
- *Measuring of mass of  $\nu$  with  $\beta$ -decay of  ${}^3\text{H}$ ,  ${}^{187}\text{Re}$  ... (theory)*
- *Towards the detection of relic neutrinos (theory)*
- *Beta beams (experiment)*
- *Grants and problems*

# *Neutrinoless Double-Beta Decay*

## *(theory and experiment)*

**Comenius University group in collaboration with**

**- NEMO3, SuperNEMO Coll.**

**- Tuebingen, CALTECH, Ioannina, Valparaiso, Dubna, ...**

*Study of the  $0\nu\beta\beta$ -decay  
is one of the highest priority issues  
in particle and nuclear physics*

**What is the nature of neutrinos?**



$\nu$



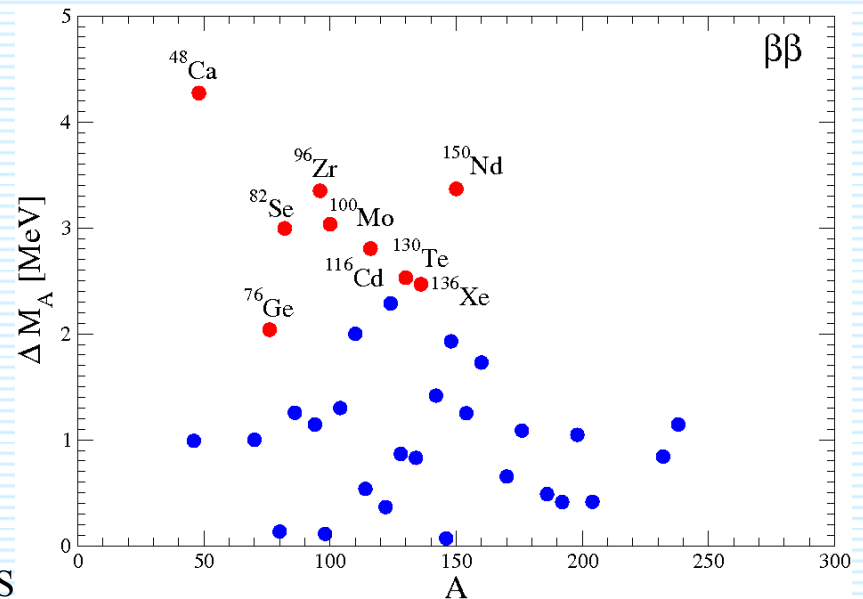
GUT's



**Only the  $0\nu\beta\beta$ -decay can answer this fundamental question  
(plus absolute mass scale of  $\nu$ 's, hierarchy, CP violation)**

# The $0\nu\beta\beta$ -decay is a particle, nuclear and atomic physics problem

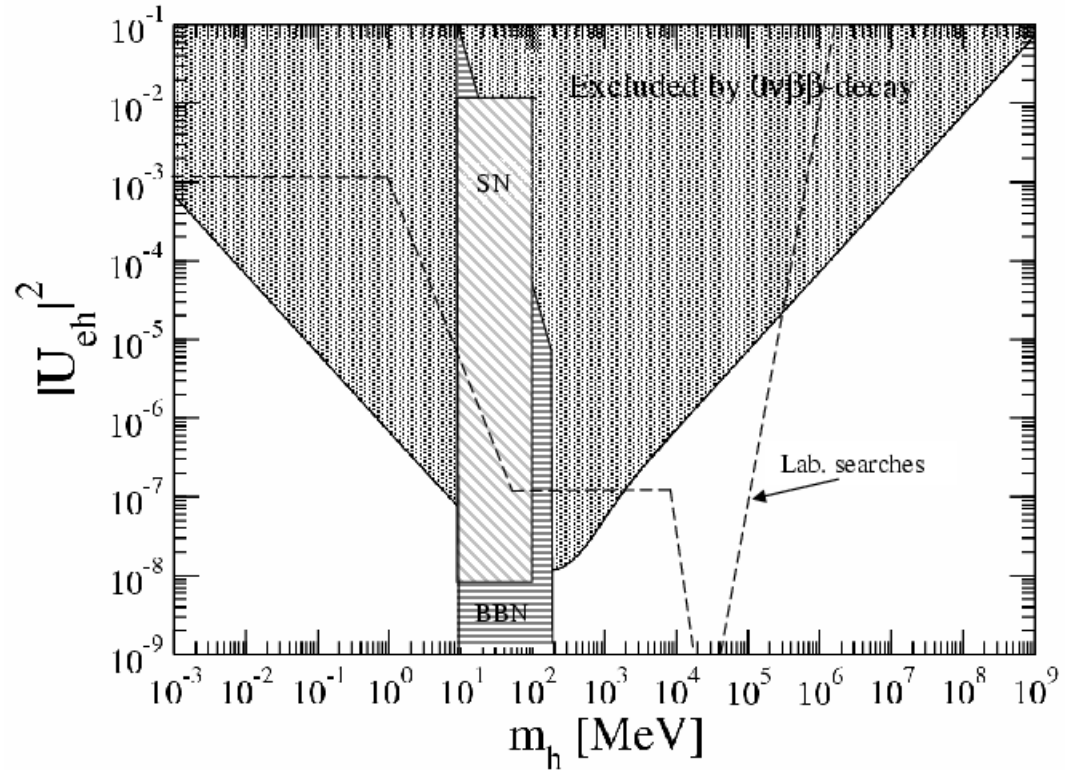
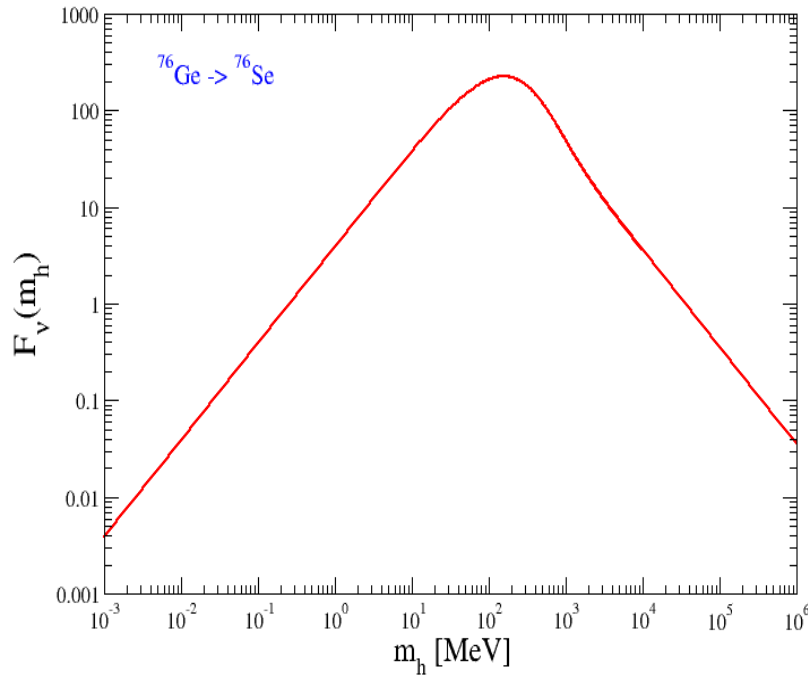
Two basic categories are  
**long-range**  
(exchange of light Majorana  $\nu$ )  
and **short-range**  
(exchange of heavy  $\nu$ , squarks, gluinos ...)  
contributions to the  $0\nu\beta\beta$ -decay



# Sterile neutrino in $0\nu\beta\beta$ -decay

Matrix element  
depends on  
 $\nu$ -mass

$$[T_{1/2}^{0\nu}]^{-1} = G_{01} \left| \frac{\langle m_\nu \rangle_{ee}}{m_e} M_\nu^{light} + U_{eh}^2 \frac{m_h}{m_e} M^{0\nu}(m_h) \right|^2.$$



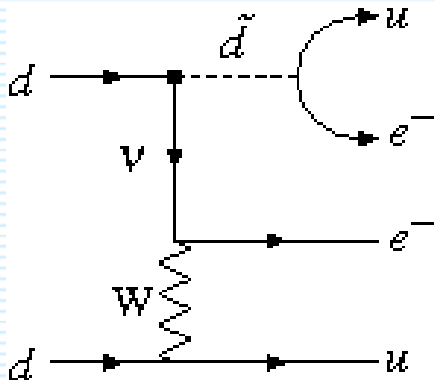
$$F_\nu(m_h) = \frac{m_h}{m_e} M^{0\nu}(m_h)$$

$$|U_{eh}|^2 \leq \frac{1}{|F_\nu(m_h)|} \frac{1}{\sqrt{T_{1/2}^{0\nu-exp} G_{01}}},$$

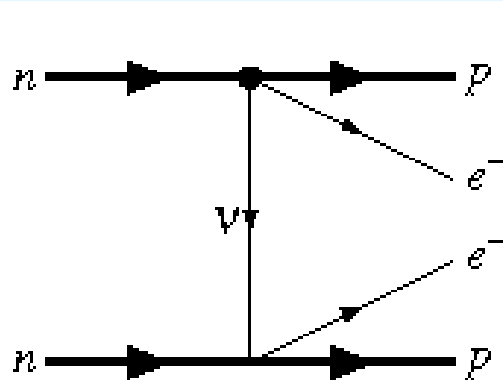
# Squark mixing SUSY mechanism

Mixing between scalar superpartners  
of the **left-** and **right-** handed fermions

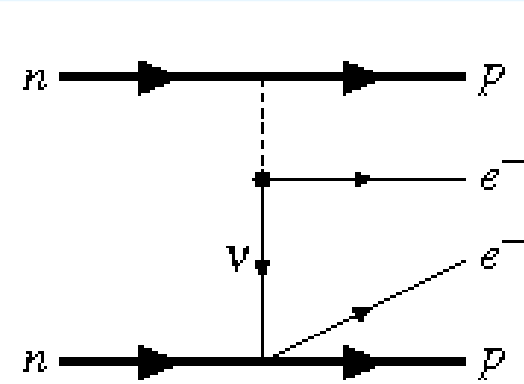
$$M_{\tilde{d}^k}^2 = \begin{pmatrix} m_{\tilde{d}_L^k}^2 + m_{d^k}^2 - \frac{1}{6}(2m_W^2 + m_Z^2) \cos 2\beta & -m_{d^k}((\mathbf{A}_D)_{kk} + \mu \tan \beta) \\ -m_{d^k}((\mathbf{A}_D)_{kk} + \mu \tan \beta) & m_{\tilde{d}_R^k}^2 + m_{d^k}^2 + \frac{1}{3}(m_W^2 - m_Z^2) \cos 2\beta \end{pmatrix}$$



(a)



(b)



(c)

Hirsch,  
Klapdor-Kleingrothaus,  
Kovalenko  
PLB 372 (1996) 181

A. Faessler,  
Th. Gutsche,  
S. Kovalenko,  
F.Š.,  
PRD 77 (2008) 113012

# Co-existence of 2, 3 or more mechanisms of the $0\nu\beta\beta$ -decay

It is well-known that there exist many mechanisms that may contribute to the  $0\nu\beta\beta$ . Let consider **3 mechanisms**: i) light  $\nu$ -mass mechanism, ii) heavy  $\nu$ -mass mechanism, iii) R-parity breaking SUSY mechanism with gluino exchange and **CP conservation**

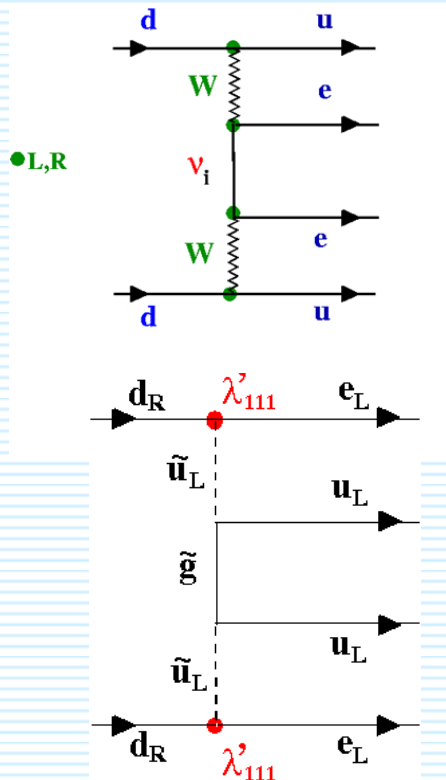
$$\frac{1}{T_{1/2}^{0\nu}} = G^{0\nu}(E_0, Z) \left| \frac{m_{\beta\beta}}{m_e} M_\nu^{0\nu} + \eta_N^L M_N^{0\nu} + \eta_{\lambda'_{111}} M_{\lambda'_{111}}^{0\nu} \dots \right|^2$$

$$m_{\beta\beta} = \sum_k (U_{ek}^L)^2 \xi_k m_k$$

$$\eta_N^L = \sum_{k=4}^6 |U_{ek}^L|^2 \xi'_k \frac{m_p}{M_k},$$

$$\eta_N^R = \sum_{k=4}^6 |U_{ek}^R|^2 \xi'_k \frac{m_p}{M_k}.$$

$$\eta_{\lambda'_{111}} = \frac{\pi\alpha_s}{6} \frac{\lambda'_{111}{}^2}{G_F^2 m_{\tilde{d}_R}^4} \frac{m_p}{m_{\tilde{g}}} \left[ 1 + \left( \frac{m_{\tilde{d}_R}}{m_{\tilde{u}_L}} \right)^2 \right]^2.$$



**Claim of evidence:**  $T_{1/2}^{0\nu}(^{76}\text{Ge}) = 2.23_{-0.31}^{+0.44} \times 10^{25} \text{ y}$

$$T_{1/2}^{0\nu}(^{100}\text{Mo}) \geq 5.8 \times 10^{23} \text{ y}$$

$$T_{1/2}^{0\nu}(^{130}\text{Te}) \geq 3.0 \times 10^{24} \text{ y}$$

Bilenky, Faessler, Potzel, F.Š., arXiv: 1104.1952[hep-ph]

Faessler, Fogli, Lisi, Rotunno, F.Š., arXiv: 1104.3716[hep-ph]

Faessler, Meroni, Petcov, F.Š., Vergados, arXiv: 1103.2334, accepted in PRD

F.Š., Vergados, Faessler, PRD 82, 113015 (2010)





NEMO 3

## Fréjus Underground Laboratory: 4800 m.w.e.

$^{100}\text{Mo}$  (6.914 kg)  $T_{1/2}^{0\nu\beta\beta} > 4.6 \cdot 10^{23}$  years

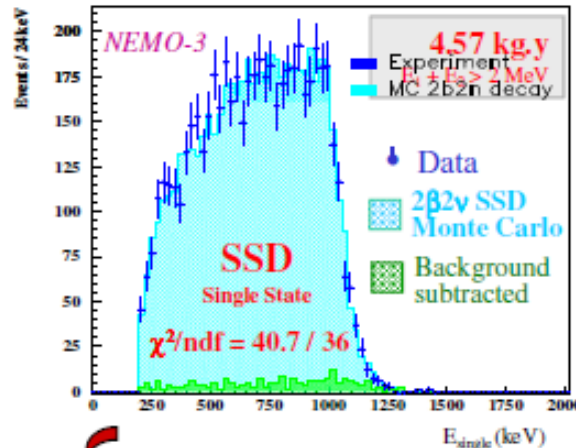
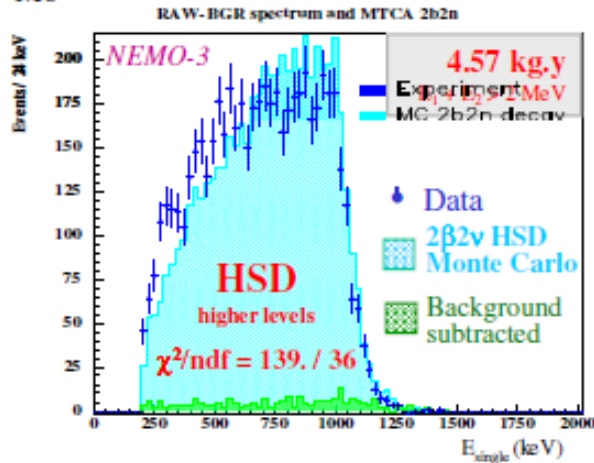
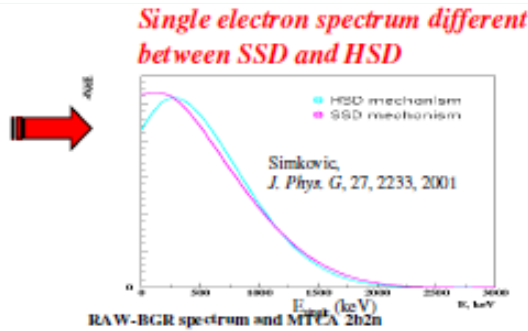
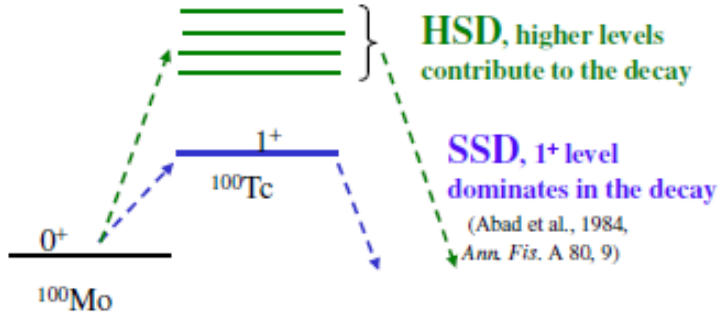
$$Q_{\beta\beta} = 3034 \text{ keV}$$

$$|m_{\beta\beta}| < 2.7 \text{ eV}$$

$^{82}\text{Se}$  (0.932 kg)  $T_{1/2}^{0\nu\beta\beta} > 1.0 \cdot 10^{23}$  y

$$Q_{\beta\beta} = 2995 \text{ keV}$$

$$|m_{\beta\beta}| < 4.1 \text{ eV}$$



**NEMO3  
experiment**

**2 $\nu\beta\beta$ -decay  
~10<sup>6</sup> events**

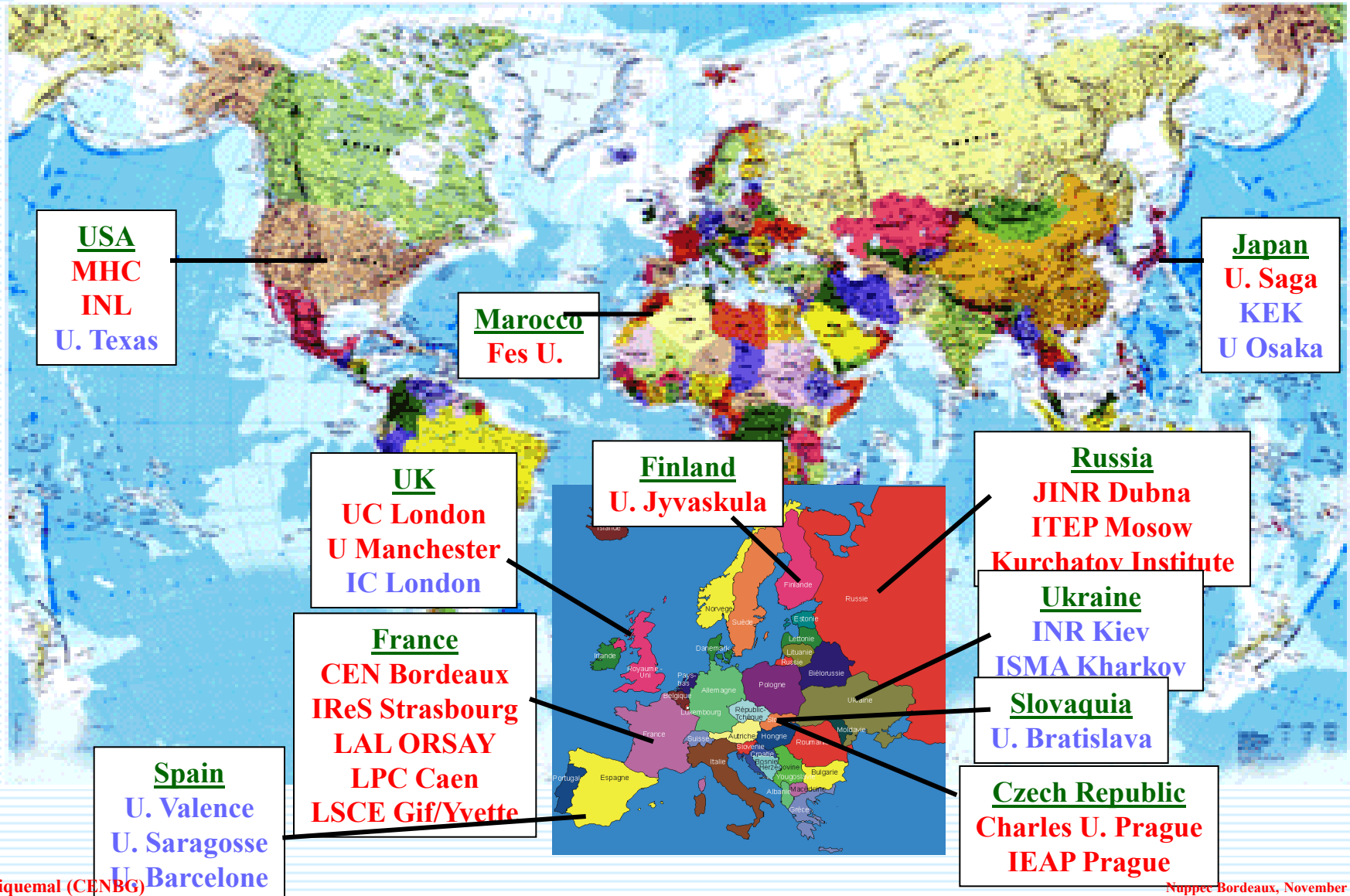
$$\left\{ \begin{array}{l} \text{HSD: } T_{1/2} = 8.61 \pm 0.02 \text{ (stat)} \pm 0.60 \text{ (syst)} \times 10^{18} \text{ y} \\ \text{SSD: } T_{1/2} = 7.72 \pm 0.02 \text{ (stat)} \pm 0.54 \text{ (syst)} \times 10^{18} \text{ y} \end{array} \right.$$

**$^{100}\text{Mo}$  2 $\beta$ 2 $\nu$  single energy distribution in favour of Single State Dominant (SSD) decay**

# SuperNEMO project

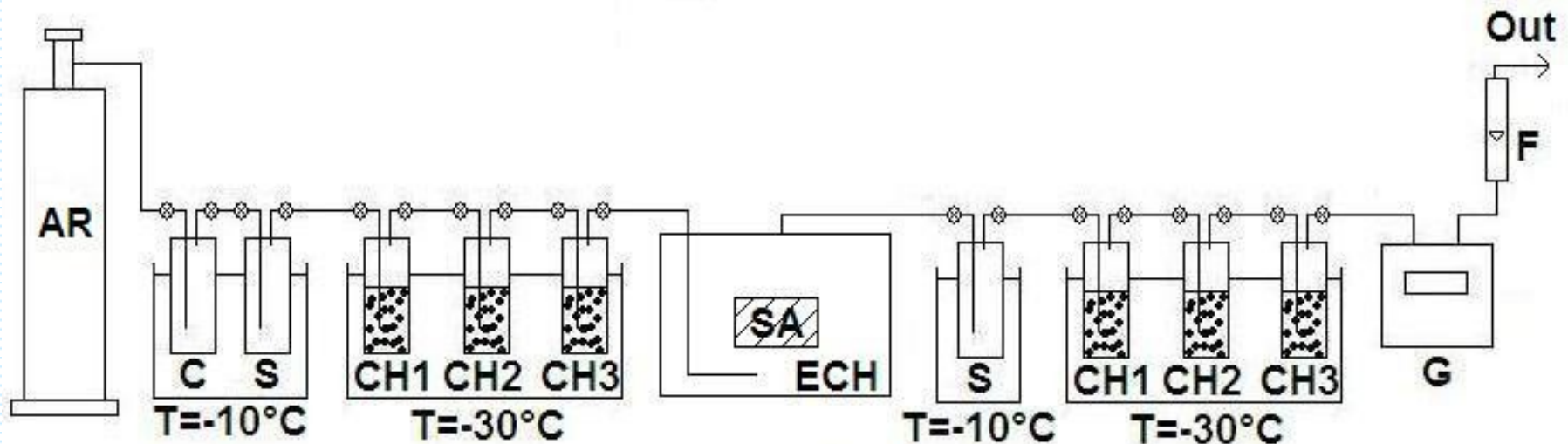
**Objective:** to built a detector sensitive to  $2 \cdot 10^{26}$  y

**Collaboration NEMO** + new labs ~ 70 physicists, **11 countries**, 27 laboratories



# Emanation of $^{222}\text{Rn}$ from the Hamamatsu photomultiplier R6594 (Karol Holý group)

## Scheme of the measurement



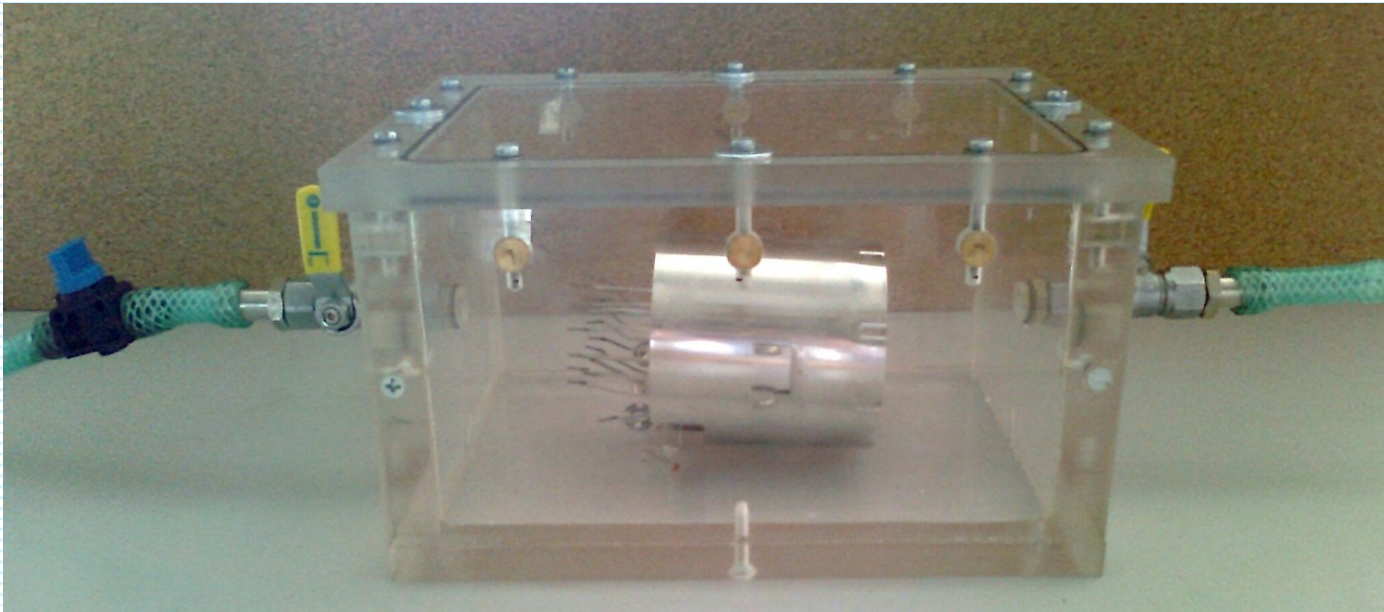
AR – argon reservoir; C – water trap; S – silica gel; CH1 ... CH6 – cooled charcoal columns; SA – sample; ECH – emanation chamber; G – gas meter; F – flow rate meter.

Charcoal columns:

$$V = 10\text{m}\ell; m_{\text{CH}} = 2\text{g}; \text{type} = \text{DB1}; A_{\text{Ra,CH}} = (7.50 \pm 0.02)\text{Bq/kg}$$

# Modulation of the radon emanation measurement

We used small emanation chamber in Bratislava  
 $V = 2.5 \ell$ , Material of walls: plexiglas,  
Thickness of walls: 10 cm

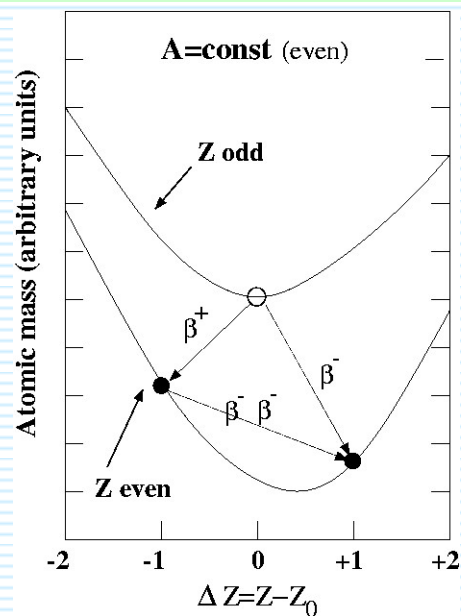


Plexiglass decrease background emanation of radon approximately 10 times. Our detection limit for radon exhalation is now:

$$\sim 3 \cdot 10^{-9} \text{ Bq} \cdot \text{s}^{-1}$$

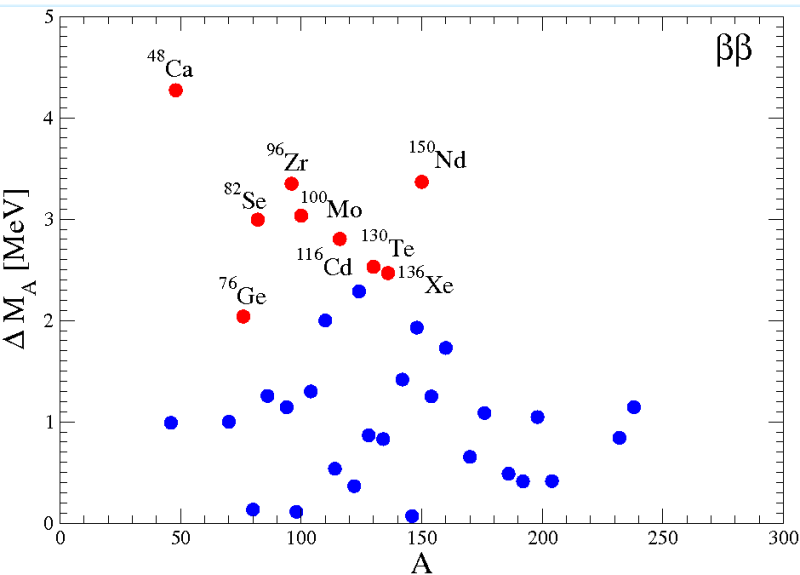
# The double beta decay process can be observed due to nuclear pairing interaction that favors energetically the even-even nuclei over the odd-odd nuclei

AIP



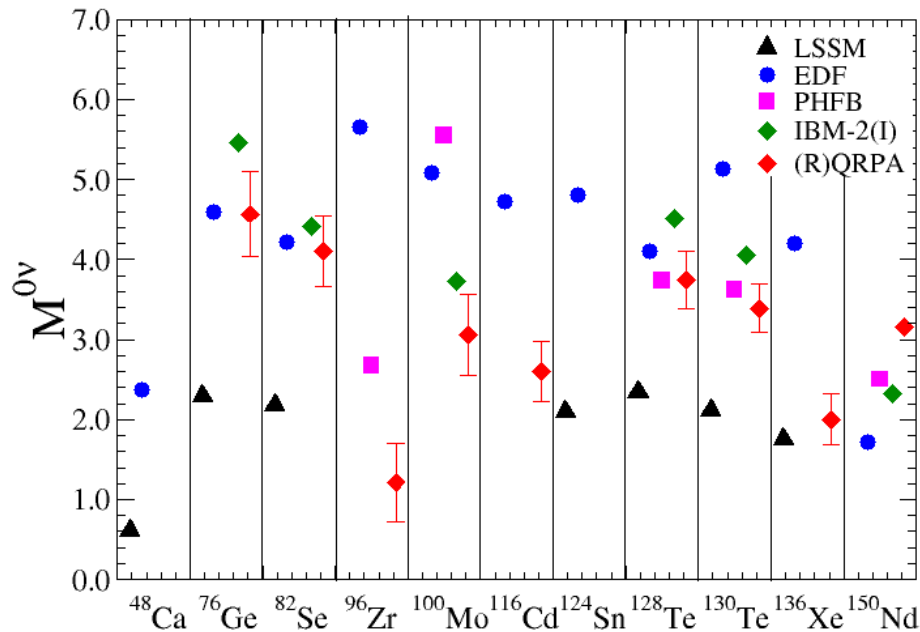
$$\frac{1}{T_{1/2}^{0\nu}} = \left| \frac{m_{\beta\beta}}{m_e} \right|^2 G^{01}(E_0, Z) |M^{0\nu}|^2$$

transition	$G^{01}(E_0, Z)$ $\times 10^{14}y$	$Q_{\beta\beta}$ [MeV]	Abund. (%)	$ M^{0\nu} ^2$
$^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$	26.9	3.667	6	?
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	8.04	4.271	0.2	?
$^{96}\text{Zr} \rightarrow ^{96}\text{Mo}$	7.37	3.350	3	?
$^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$	6.24	2.802	7	?
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	5.92	2.479	9	?
$^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$	5.74	3.034	10	?
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	5.55	2.533	34	?
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	3.53	2.995	9	?
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	0.79	2.040	8	?



*The NMEs for  $0\nu\beta\beta$ -decay must be evaluated using tools of nuclear theory*

## The $0\nu\beta\beta$ -decay NMEs (Status:2010)



## Bratislava contributions

- Role of occupancies of individual orbits
- Brueckner short-range correlations
- Effect of nuclear deformation
- The case of competing of  $0\nu\beta\beta$ -decay mechanisms

## Nuclear structure approaches

**Large Scale Shell Model:** Caurier, Menendez, Nowacki, Poves, PRL 100, 052503 (2008).

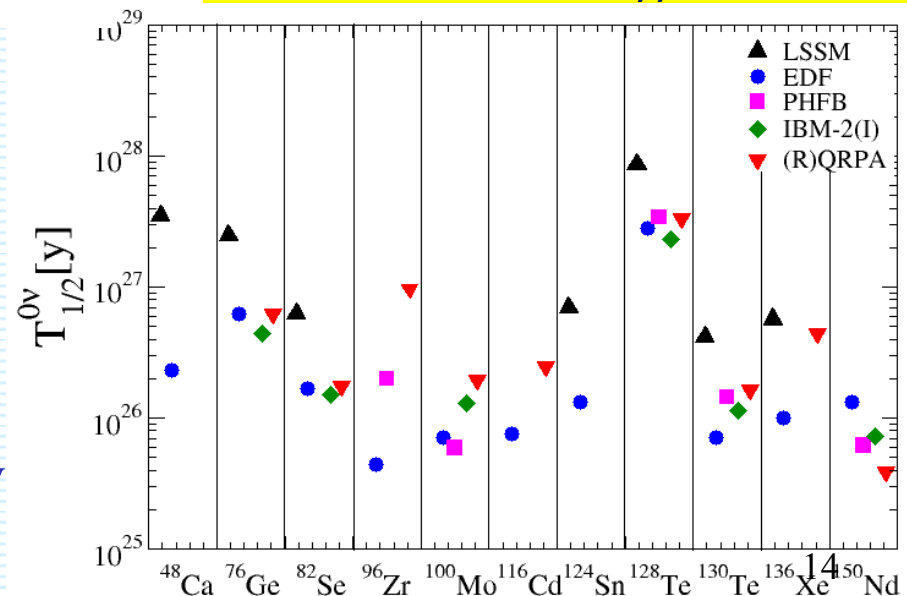
**(Renormalized) QRPA:** Šimkovic, Faessler, Müther, Rodin, Stauf, PRC 79, 055501 (2009).

**Interacting Boson Model:** Barea, Iachello, PRC 79, 044301 (2009).

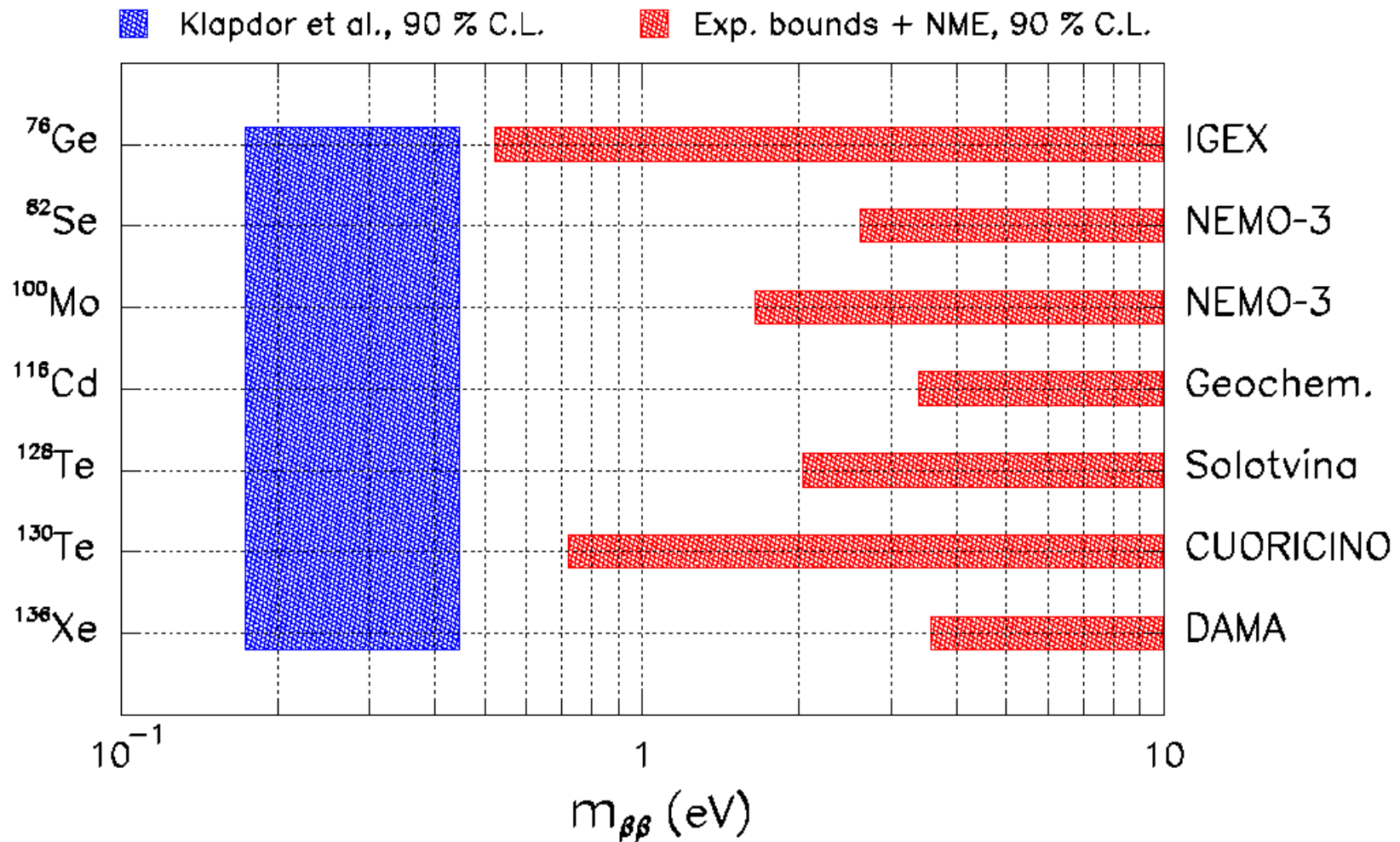
**Projected Hartree-Fock-Bogoliubov:** Rath, Chandra, et al. PRC 82, 064310 (2010).

**Energy Dendity Functional appr.:** Rodríguez, Martínez-Pinedo, arXiv:1008.5260 [nucl-th].

## Half-life $T_{1/2}$ for $m_{\beta\beta} = 50$ meV

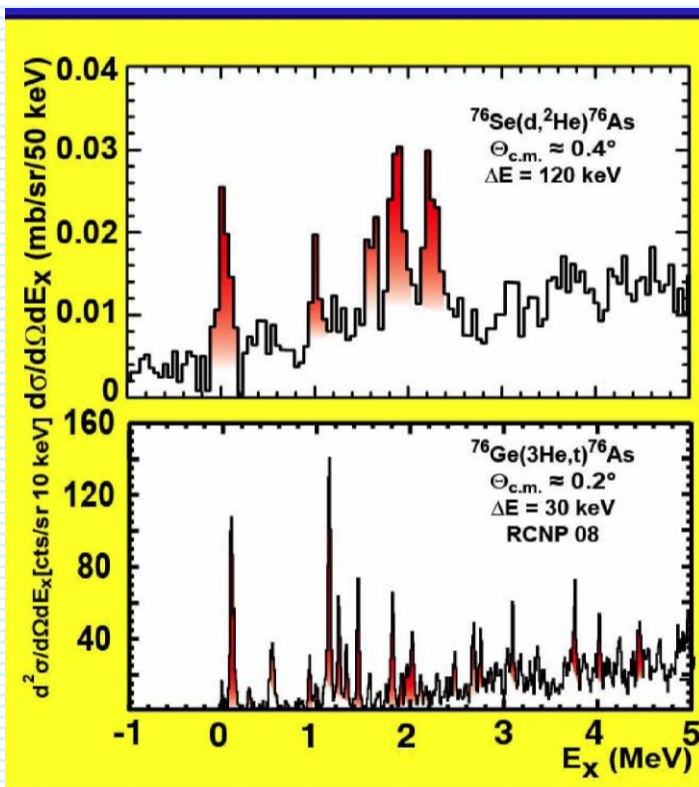
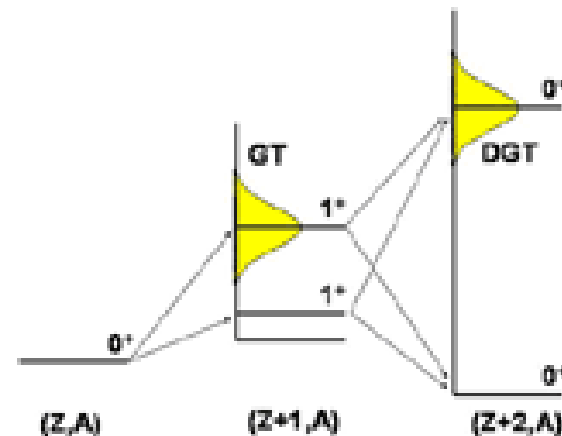


# A claim of evidence and other experiments (current status)



The cross sections of ( $t, {}^3\text{He}$ ) and ( $d, {}^2\text{He}$ ) reactions give  $B(GT^\pm)$  for  $\beta^+$  and  $\beta^-$ , product of the amplitudes ( $B(GT)^{1/2}$ ) entering the numerator of  $M_{GT}^{2\nu}$

$$M_{GT}^{2\nu} = \sum_m \frac{M_{GT}^{(+)}(m) M_{GT}^{(-)}(m)}{Q_{\beta\beta}/2 + m_e + E_x(1_m^+) - E_0}$$



$2\nu\beta\beta$ -matrix element

$$0.16 \pm 0.04 \text{ MeV}^{-1}$$

with  $G(2\nu) = 3.4 \times 10^{-20} \text{ MeV}^2 \text{ a}^{-1}$

$2\nu\beta\beta$  - half-life

$$(1.1 \pm 0.2) \times 10^{21} \text{ a}$$

recommended. exp. value:

$$(1.5 \pm 0.1) \times 10^{21} \text{ a}$$

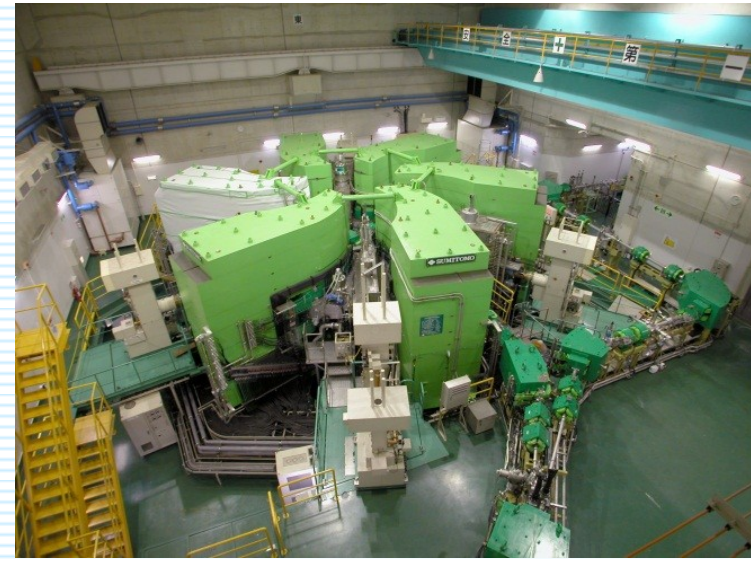
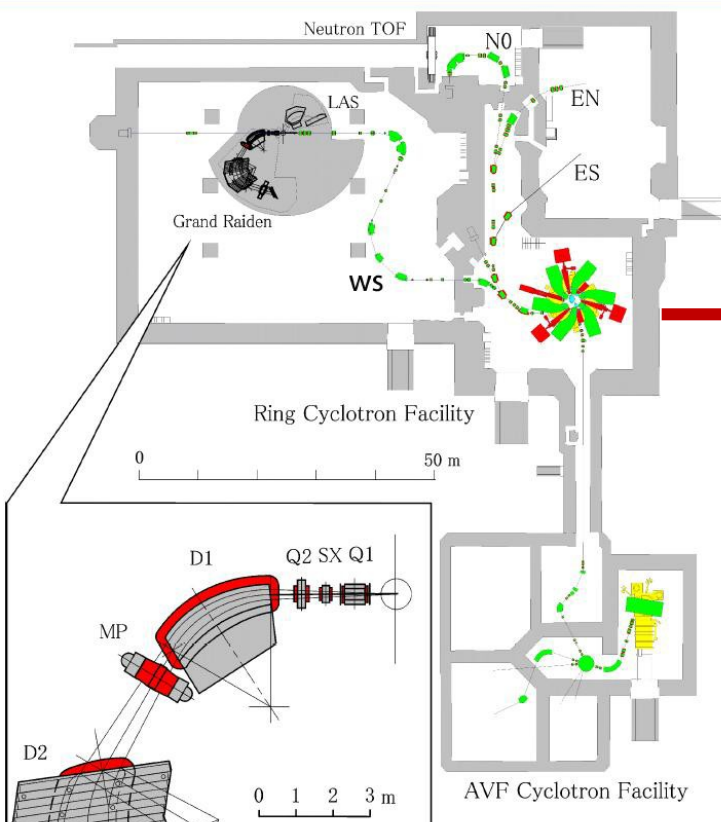
Closure  $2\nu\beta\beta$ -decay  
NME

$$M_{GT-cl}^{2\nu} = \sum_m M_{GT}^{(+)}(m) M_{GT}^{(-)}(m)$$

SSD hypothesis

$$g_A^2 M_{GT-cl}^{2\nu} = \frac{3 D}{\sqrt{ft_{EC} ft_{\beta^-}}}$$

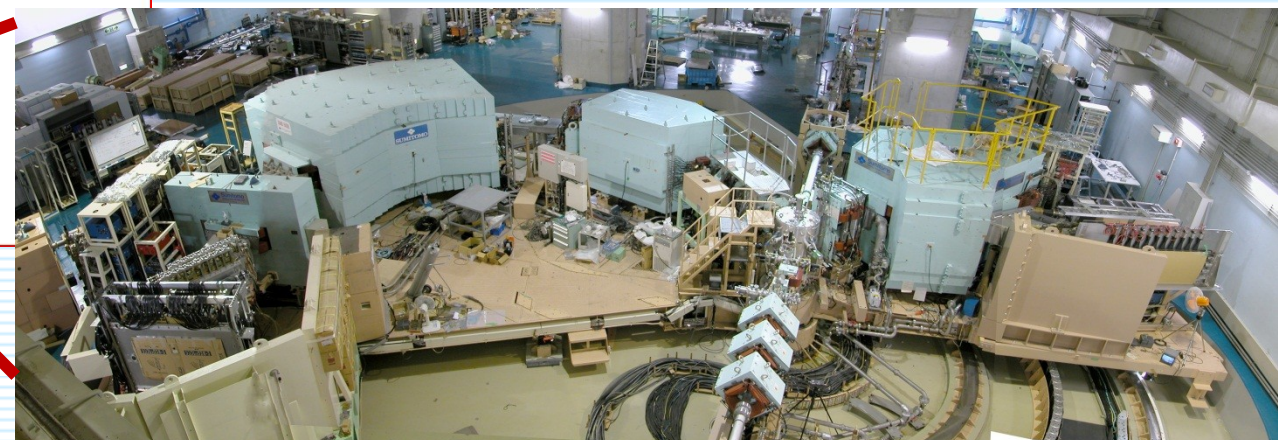




**Facility  
founded  
in 1971**

- Dispersion matching technique
- High resolution - 30 keV
- High intensities  $\sim 10$  pA

**High resolution  
spectrometer Grand  
Raiden**



# Research programs: Nuclear physics, fundamental physics, nuclear chemistry and biology

## Charge exchange reactions for studies of double $\beta$ -decay NME

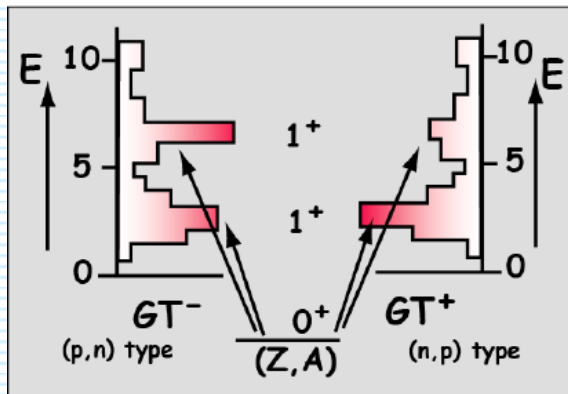
### Beam requirements:

- Type of particle:  ${}^3\text{He}$
- Beam energy: 420 MeV
- Beam intensity: 20 nA
- Energy resolution:  $\Delta E \leq 100$  keV

### Targets:

- ${}^{128,130,\text{nat}}\text{Te}$  ( $\approx 1$  mg/cm $^2$ )
- ${}^{69,71,\text{nat}}\text{Ga}$

- Measure  $B(\text{GT}^+)$  through (n,p)-type reaction
- Measure  $B(\text{GT}^-)$  through (p,n)-type reaction



$$B(GT^\pm) = \frac{1}{2J_i + 1} |M(GT^\pm)|^2$$

$$B(GT) \approx \hat{\sigma}(GT) \frac{d\sigma(q=0)}{d\Omega}$$

- Phase can not be measured
- Simple relation  $\sigma \leftrightarrow B(\text{GT})$

# *Neutrinoless Double-Electron Capture* *(theory and experiment)*

**Povinec, Holý, Sýkora, Staníček, Šimkovic ...  
(Comenius University)**

**TGV collaboration, Štekl group (Prague), Brudanin  
(Dubna)**

**Frekers group (U. Muenster)**

**Blaum (MPI Heidelberg)**

**Krivoruchenko (ITEP Moscow)**

# Oscillations of atoms

$$H_{eff}^{atom} = \begin{pmatrix} M_i & V^{LNV} \\ V^{LNV} & M_f - \frac{i}{2}\Gamma \end{pmatrix}$$

**Oscillation of atoms  
(lepton number violation)**

F.Š., M. Krivoruchenko, Phys.Part.Nucl.Lett. 6 (2009) 485.

**In analogy with oscillations of  
n-anti{n} (baryon number violation)**

$$H_{eff}^{n\bar{n}} = \begin{pmatrix} M & V^{BNV} \\ V^{BNV} & M - \frac{i}{2}\Gamma \end{pmatrix}$$

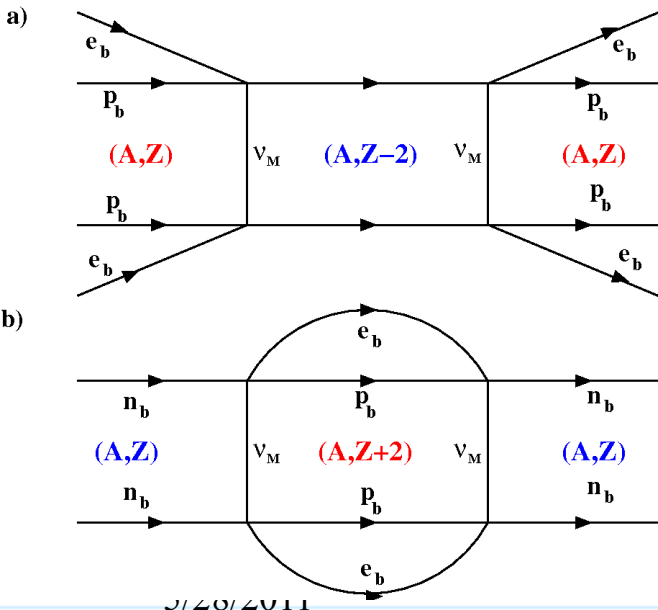
**Oscillations of stable atoms ( $\Gamma=0$ )**

$$| \langle f | e^{-iH_{eff}t} | i \rangle |^2 = \frac{4V^2}{(M_i - M_f)^2} \sin^2 [t (M_i - M_f)/2]$$

$$\begin{matrix} {}^{164}_{68}Er & \rightarrow & {}^{164}_{66}Dy \\ (M_i - M_f) & = & 24.1 \text{ keV} \end{matrix} \quad | \langle f | e^{-iH_{eff}t} | i \rangle |^2 \leq 3 \cdot 10^{-55}$$

**Oscillations of unstable atoms ( $\Gamma \neq 0$ )**

**Double electron capture  
(resonant enhancement)**



# Data analysis of most likely resonant transitions

1 chance of 100 for  $T_{1/2} < 10^{25}$  y  
 10                      100                       $< 10^{27}$  y

## Half-life of a particular isotope

$$\tilde{T}_{1/2} = \tilde{T}_{1/2}^{\min} \frac{\Delta M^2 + \Gamma_\gamma^2/4}{\Gamma_\gamma^2/4}$$

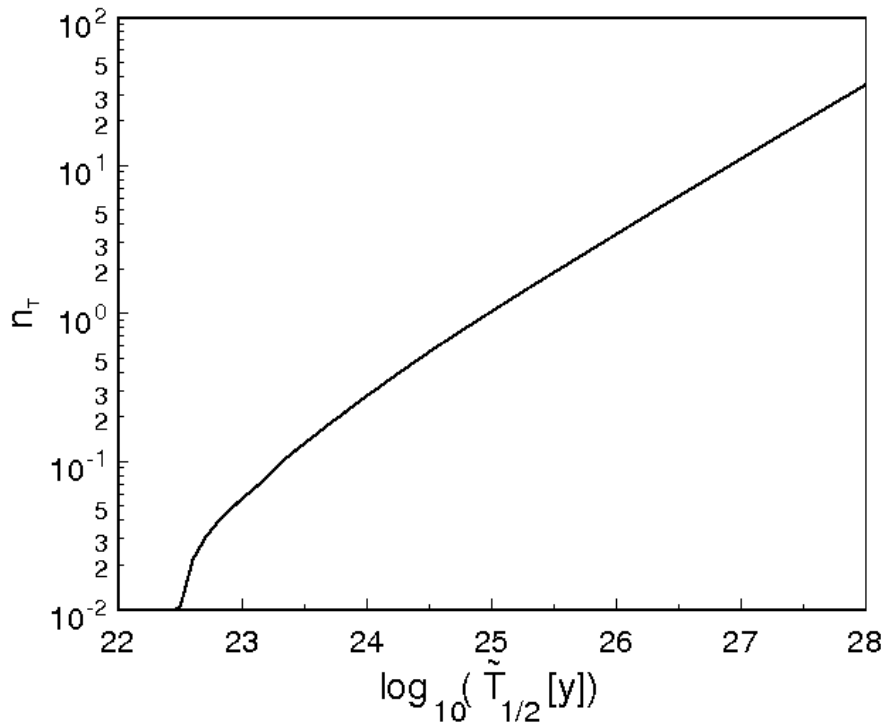


$$\Delta M(\tilde{T}_{1/2}) = \frac{\Gamma_\gamma}{2} \left( \frac{\tilde{T}_{1/2}}{\tilde{T}_{1/2}^{\min}} - 1 \right)^{1/2}$$

Number of transitions **n**  
with half-life

$$T_{1/2}^a < T_{1/2}$$

$$n = \sum_{T_{1/2}^a < T_{1/2}} \frac{\Delta M(\tilde{T}_{1/2}^a)}{\Delta M_{\text{expt}}}$$



## Improved Q-value measurements Klaus Blaum (MPI Heidelberg)

nucl. tr.	$Q_{old}$	$E = B + E_\gamma$	Orbit.	$\Delta = Q(old) - E$	$Q_{new}$	$\Delta = Q(new) - E$
$^{112}\text{Sn} \rightarrow ^{112}\text{Cd}$	1919.5(4.8)	1901.7	$KL_1$	17.8(4.8)	1919.82(16)	18.12(16)
		1924.4	$KK$	-4.9(4.8)		-4.56(16)
$^{152}\text{Gd} \rightarrow ^{152}\text{Sm}$	54.6(3.5)	54.79+0	$KL_1$	-0.19(3.50)	55.70(18)	0.91(18)
$^{164}\text{Er} \rightarrow ^{164}\text{Dy}$	23.3(3.9)	18.09	$l_1L_1$	5.21(3.90)		

**$^{152}\text{Gd} \rightarrow ^{152}\text{Sm}$**  (Eliseev, et al., F.Š., M. Krivoruchenko, PRL 106, 052504 (2011))  
(F.Š., Krivoruchenko, Faessler, PPNP 66, 446 (2011))

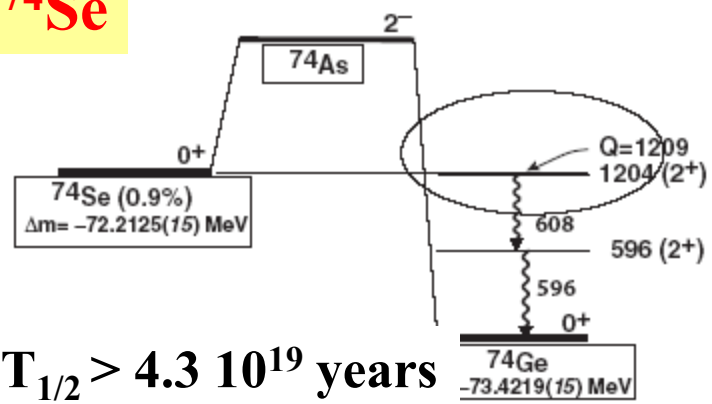
$$\Gamma_{\epsilon\epsilon} = |V_{\epsilon\epsilon}|^2 \frac{\Gamma}{\Delta^2 + \Gamma^2/4}$$

$$= |V_{\epsilon\epsilon}|^2 R$$

$$V_{\epsilon\epsilon} = m_{\beta\beta} \frac{\sqrt{2}g_A^2 G_\beta^2}{(4\pi)^2 R_{nucl}} \bar{f}_a \bar{f}_b M^{0\nu}$$

$$T_{1/2}^{0\nu} = 4 \times 10^{26} \left( \frac{1 \text{ eV}}{m_{\beta\beta}} \right)^2 \text{ years.}$$

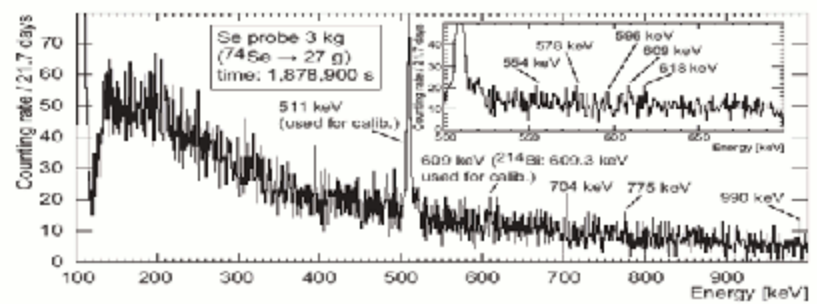
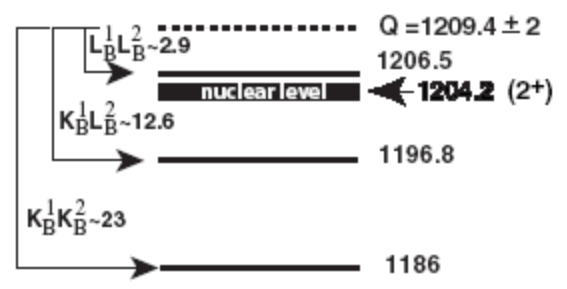
<sup>74</sup>Se



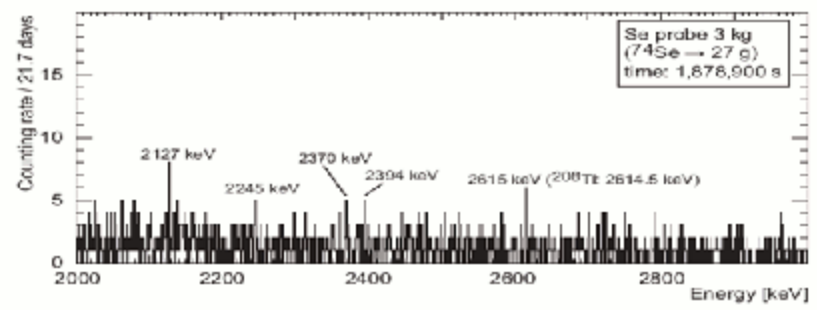
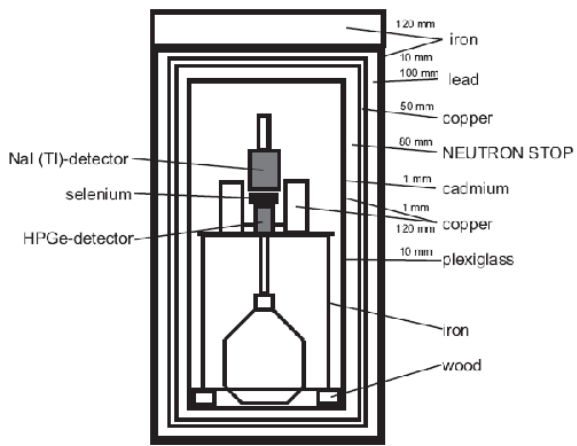
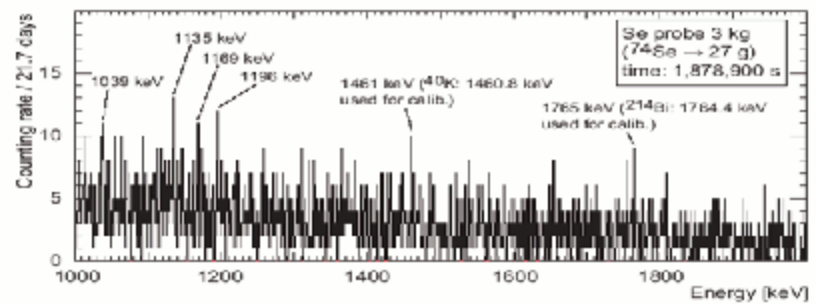
$T_{1/2} > 4.3 \cdot 10^{19}$  years

# Experiment in Bratislava!

Muenster and Bratislava groups

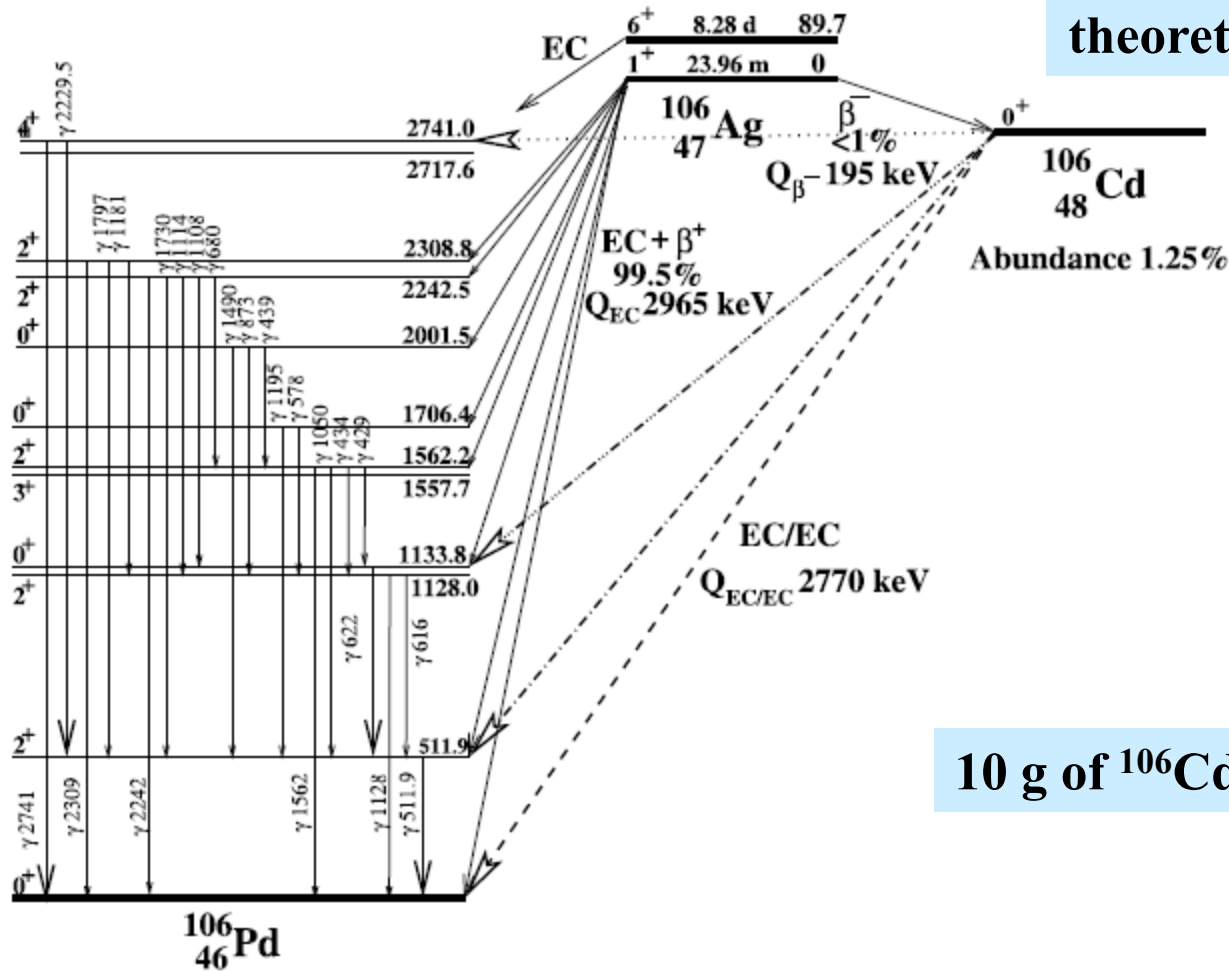


Frekers, Puppe, Thies, Povinec, Šimkovic, Staníček, Sýkora, accepted in NPA



5/28/2011

# TGV experiment in Modane underground laboratory



$$T_{1/2}^{2\nu\epsilon\epsilon} (^{106}\text{Cd}) > 3.6 \cdot 10^{20} \text{ y}$$

TGV Coll, Rukhadze et al., NPA 852, 197 (2011)

$$T_{1/2}^{0\nu\epsilon\epsilon} (^{106}\text{Cd}) > 1.1 \cdot 10^{20} \text{ y}$$

Fedor Simkovic



*Two-neutrino Double-Beta Decay  
and  
statistical properties of  $\nu$   
(theory)*

**Šimkovic, Dvornický (Comenius University)**

**Barabash (ITEP Moscow)**

**Smirnov (ICTP Trieste)**

**Dolgov (U. Ferrara)**

## Mixed statistics for neutrinos

**Definition of mixed state**

$$\begin{aligned} |\nu\rangle &= \hat{a}^\dagger |0\rangle \\ &\equiv \cos\delta \hat{f}^\dagger |0\rangle + \sin\delta \hat{b}^\dagger |0\rangle \\ &= \cos\delta |f\rangle + \sin\delta |b\rangle \end{aligned}$$

**with commutation Relations**

$$\begin{aligned} \hat{f}\hat{b} &= e^{i\phi}\hat{b}\hat{f} & \hat{f}^\dagger\hat{b}^\dagger &= e^{i\phi}\hat{b}^\dagger\hat{f}^\dagger \\ \hat{f}\hat{b}^\dagger &= e^{-i\phi}\hat{b}^\dagger\hat{f} & \hat{f}^\dagger\hat{b} &= e^{-i\phi}\hat{b}\hat{f}^\dagger \end{aligned}$$

**Amplitude for  $2\nu\beta\beta$**

$$\begin{aligned} A^{2\nu} &= [\cos\delta^4 + \cos\delta^2\sin\delta^2(1 - \cos\phi)]A^f + [\cos\delta^4 + \cos\delta^2\sin\delta^2(1 + \cos\phi)]A^b \\ &= \cos\chi^2 A^f + \sin\chi^2 A^b \end{aligned}$$

**Decay rate**

$$\begin{aligned} W^{2\nu} &= \cos\chi^4 W^f + \sin\chi^4 W^b \\ &= (1 - b^2) W^f + b^2 W^b \end{aligned}$$

**Partly bosonic neutrino requires knowing NME or log ft values for HSD or SSD**

**( calculations coming up soon )**

# Looking for a signature of bosonic $\nu$

**$2\nu\beta\beta$ -decay half-lives ( $0^+ \rightarrow 0^+_{\text{g.s.}}$ ,  $0^+ \rightarrow 0^+_1$ ,  $0^+ \rightarrow 2^+_1$ )**

- **HSD – NME needed**
- **SSD –  $\log ft_{\text{EC}}$ ,  $\log ft_{\beta}$  needed**

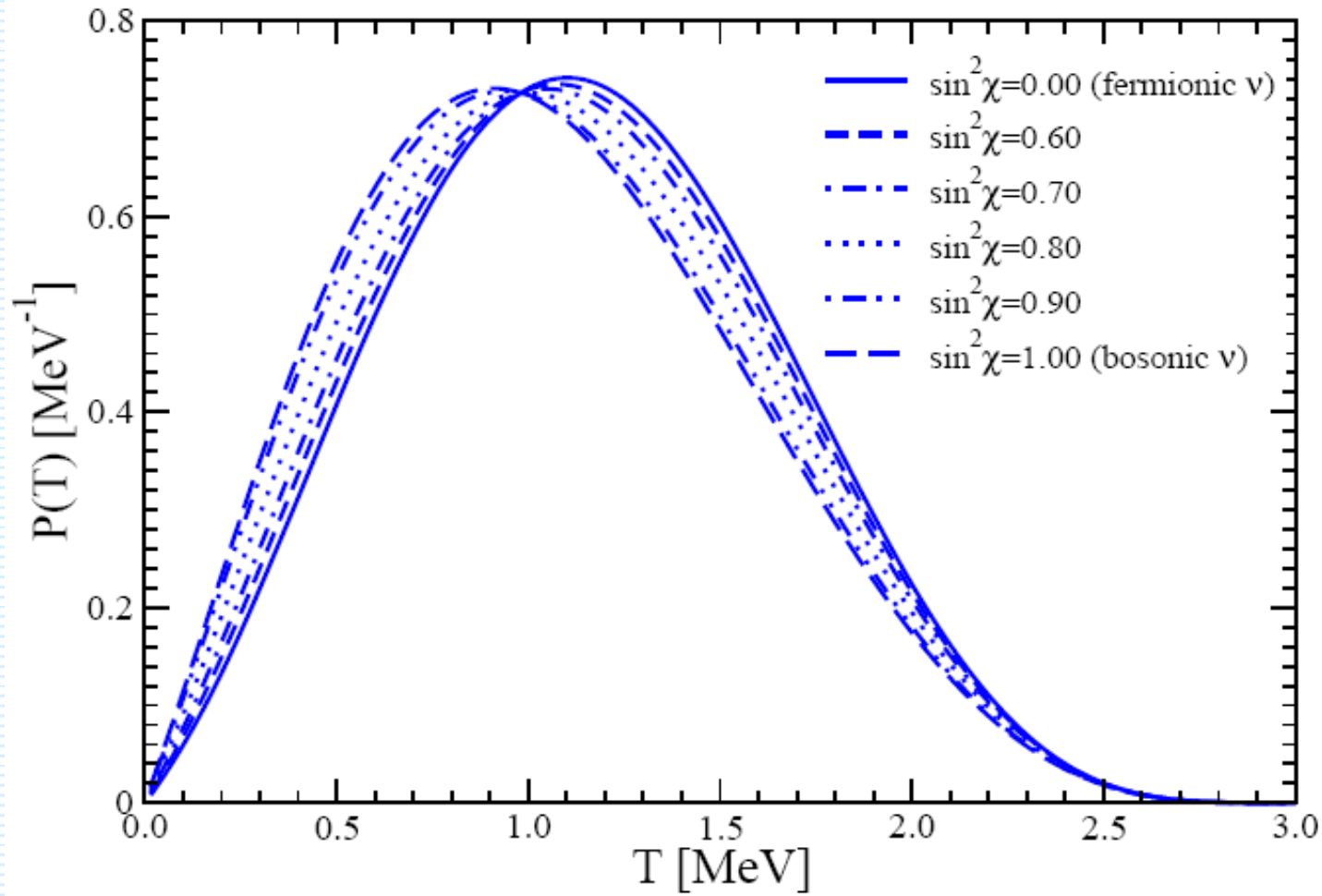
$$\begin{aligned} \frac{T_{1/2}^{2\nu\text{-SSD}}(2^+_f)}{T_{1/2}^{2\nu\text{-SSD}}(0^+_f)} &= 2.41 \times 10^4 & \text{fermionic } \nu & T_{1/2}^{2\nu}(2^+) &= 1.73 \times 10^{23} \text{ years} \\ &= 403 & \text{bosonic } \nu & &= 2.74 \times 10^{21} \text{ years} \\ & & & T_{1/2}^{2\nu\text{-exp}}(2^+) &> 1.6 \times 10^{21} \text{ years} \end{aligned}$$

## Normalized differential characteristics

- The single electron energy distribution
- The distribution of the total energy of two electrons
- Angular correlations of two electrons  
(free of NME and  $\log ft$ )

# Mixed $\nu$ excluded for $\sin^2\chi < 0.6$ (NEMO3 data)

$^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$  (SSD)



*Measuring mass of neutrinos  
with  
 $\beta$ -decays of  ${}^3\text{H}$ ,  ${}^{187}\text{Re}$ ,  ${}^{115}\text{In}$   
and  
electron capture of  ${}^{163}\text{Ho}$   
(theory)*

**Šimkovic, Dvornický (Comenius University)**

**Muto (Tokyo Technical U.)**

**Faessler (Tuebingen)**

# *Relativistic approach to $^3\text{H}$ decay nuclear recoil (3.4 eV) taken into account*

## Standard approach

- non-relativistic nuclear w.f.
- nuclear recoil neglected
- phase space analysis

$$E_e^{\max} = M_i - M_f - m_\nu$$

$$\frac{d\Gamma}{dT} = \frac{(\cos\theta_C G_F)^2}{2\pi^3} |\mathcal{M}|^2 F(E) p E (Q - T) \sqrt{(Q - T)^2 - m_\nu^2}$$

## Relativistic EPT approach (Primakoff)

- Analogy with n-decay  
( $^3\text{H}, ^3\text{He}$ )  $\leftrightarrow$  (n,p)
- nuclear recoil of 3.4 eV by  $E_e^{\max}$
- relevant only phase space

$$E_e^{\max} = \frac{1}{2M_f} [M_i^2 + m_e^2 - (M_f^2 - m_\nu^2)]$$



$$y = E_e^{\max} - E_e$$

$$(m_{12})^2 = M_i^2 - 2M_i E_e + m_e^2$$

$$\begin{aligned} \frac{d\Gamma}{dE_e} &= \frac{1}{(\pi)^3} (G_F \cos\theta_C)^2 F(Z, E_e) p_e \\ &\times \frac{M_i^2}{(m_{12})^2} \sqrt{y \left( y + 2m_\nu \frac{M_f}{M_i} \right)} \\ &\times \left[ (g_V + g_A)^2 y \left( y + m_\nu \frac{M_f}{M_i} \right) \frac{M_i^2 (E_e^2 - m_e^2)}{3(m_{12})^4} \right. \\ &\quad \left. \frac{(g_V + g_A)^2 \left( y + m_\nu \frac{M_f + m_\nu}{M_i} \right) (M_i E_e - m_e^2)}{m_{12}^2} \right. \\ &\quad \left. \times \left( y + M_f \frac{M_f + m_\nu}{M_i} \right) \frac{(M_i^2 - M_i E_e)}{m_{12}^2} \right. \\ &\quad \left. - (g_V^2 - g_A^2) M_f \left( y + m_\nu \frac{(M_f + M_\nu)}{M_i} \right) \right. \\ &\quad \left. \times \frac{(M_i E_e - m_e^2)}{(m_{12})^2} \right. \\ &\quad \left. + (g_V - g_A)^2 E_e \left( y + m_\nu \frac{M_f}{M_i} \right) \right] \end{aligned}$$

## Numerics:

Practically the same dependence of Kurie function on  $m_\nu$  for  $E_e \approx E_e^{\max}$

for Simkovic

F.Š., R. Dvornický, A. Faessler,  
PRC 77 (2008) 055502

# Spectrum of emitted electrons in rhenium $\beta$ -decay

Dvornický, F. Š., Muto, Faessler, PPNP (2009)

$$\frac{d\Gamma}{dE} = \frac{G_F^2 V_{ud}^2}{2\pi^3} |M|^2 pE (E_0 - E) \sqrt{(E_0 - E)^2 - m_\nu^2} \frac{1}{3} R^2 \left( p^2 F_1(Z, E) + k^2 F_0(Z, E) \right)$$

$$k = \sqrt{(E_0 - E)^2 - m_\nu^2}$$

**Electron  $p_{3/2}$  decay channel clearly dominates**

$$\Gamma_S / \Gamma_P = 1.011 \times 10^{-4}$$

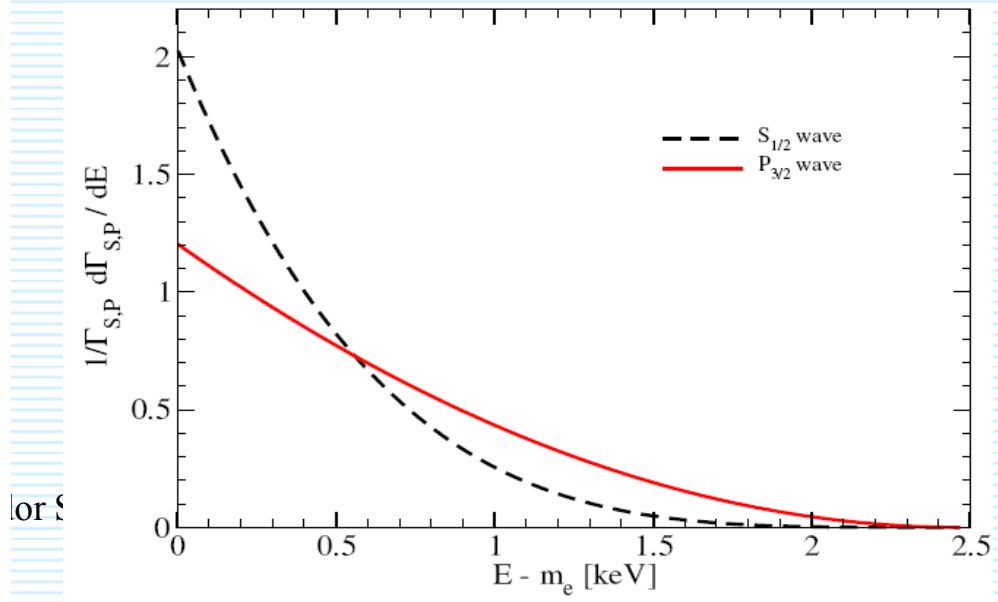
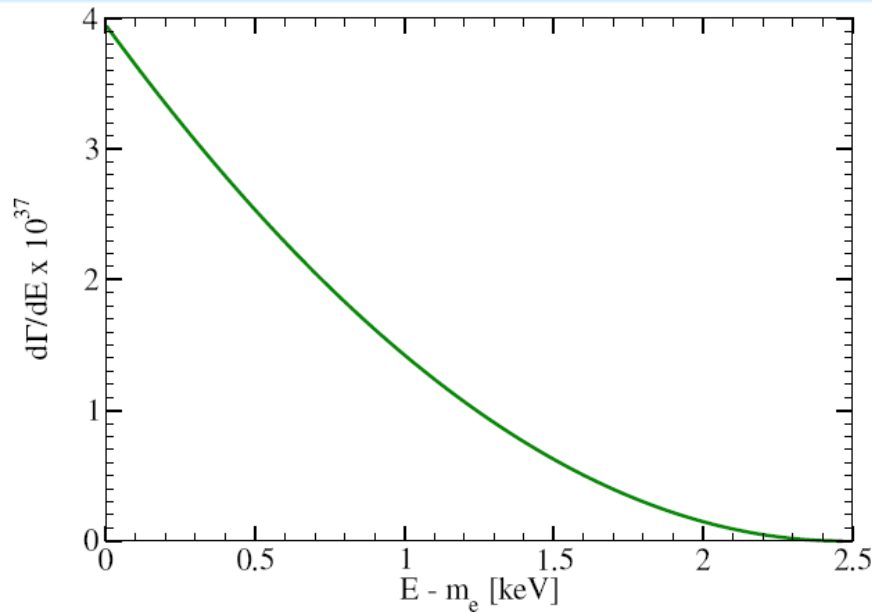
**In agreement with Arnaboldi et al.: PRL 96, 042503 (2006)**

**Electron in the  $p_{3/2}$  state**

$$p^{\max} \cong 50 \text{ keV}$$

**Electron in the  $s_{1/2}$  state**

$$k^{\max} = 2.47 \text{ keV}$$



or

# Kurie plots for rhenium (MARE) and tritium (KATRIN) $\beta$ -decay

## Rhenium

$$B_{\text{Re}} = \frac{G_F V_{ud}}{\sqrt{2\pi^3}} \frac{g_A}{\sqrt{2J_i + 1}} \left| \langle {}^{187}\text{Os} \parallel \sqrt{\frac{4\pi}{3}} \sum_n \tau_n^+ \frac{r_n}{R} \{ \sigma_1 \otimes Y_1 \}_2 \parallel {}^{187}\text{Re} \rangle \right|$$

$$\times \sqrt{\frac{1}{3} R^2 p^2 \frac{F_1(Z, E)}{F_0(Z, E)}}$$

## Tritium

$$B_T = \frac{G_F V_{ud}}{\sqrt{2\pi^3}} \sqrt{g_V^2 + 3g_A^2}$$

$$K(y) / B_T = \left( \sqrt{y(y + 2m_\nu)(y + m_\nu)} \right)^{1/2}$$

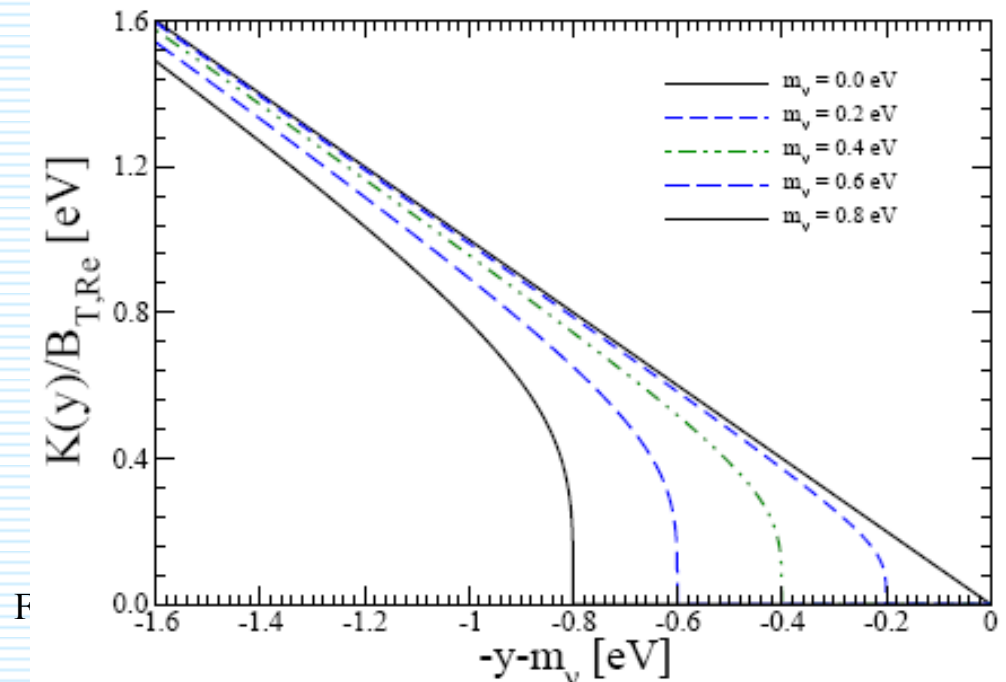
$$K(E_e) / B_{\text{Re}} \cong (E_0 - E_e)^4 \sqrt{1 - \frac{m_\nu^2}{(E_0 - E_e)^2}}$$

$y = E_e \text{max} -$

Properly normalized Kurie functions are practically the same by the endpoint !

$$K(E) / B_{\text{Re}} \cong K(y) / B_T$$

Dvornický, Muto, F.Š., Faessler,  
PRC 83, 045502 (2011)





*Towards laboratory detection of  
relic neutrinos  
(theory)*

**Šimkovic, Hodák (Comenius University)**

**Kovalenko (University Valparaiso)**

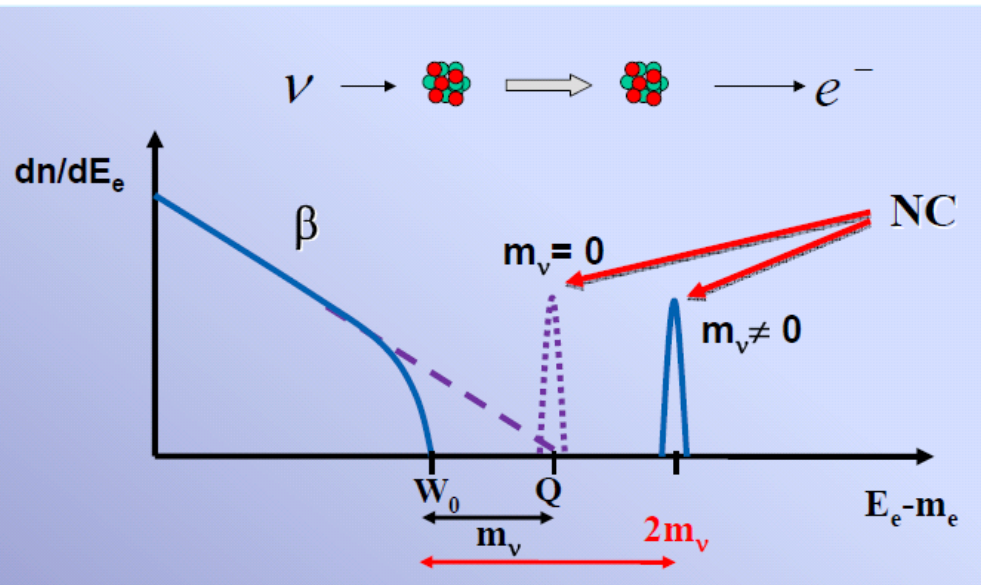
**Krivoruchenko (ITEP Moscow)**

**Faessler (U. Tuebingen)**

# Detection of relic neutrinos by KATRIN experiment



$$\Gamma^\nu({}^3\text{H}) = \frac{1}{\pi} G_\beta^2 F_0(2, p) p p_0 \left( |M_F|^2 + g_A^2 |M_{GT}|^2 \right) \frac{\eta_\nu}{\langle \eta_\nu \rangle} \langle \eta_\nu \rangle$$



Assuming  $M_F=1$ ,  
 $M_{GT}=\sqrt{3}$  and  
 $\eta_\nu = \langle \eta_\nu \rangle$  the capture  
 rate

$$\Gamma^\nu({}^3\text{H}) = 4.2 \cdot 10^{-25} \text{ y}^{-1}$$

KATRIN will use  $\sim 50 \mu\text{g}$  of  ${}^3\text{H}$

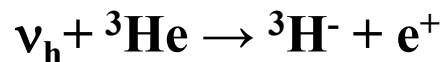
Faessler, Hodák, Kovaenko, F.Š,  
 arXiv: 1102.1799[hep-ph]  
 accepted in J. Phys. G

$$N_{\text{capt}}^\nu(\text{KATRIN}) \approx 4.2 \cdot 10^{-6} \frac{\eta_\nu}{\langle \eta_\nu \rangle} \text{ y}^{-1}$$

Even considering effect of clustering of  $\nu$ ,  $\eta_\nu / \langle \eta_\nu \rangle \sim 10^3 - 10^4$ :

$$N_{\text{capt}}^\nu(\text{KATRIN}) < 1 \text{ y}^{-1}$$

# Sterile relic neutrino detection using $\nu_h$ capture on ${}^3\text{He}$



Mixing of neutrinos

$$\nu_e = \sum_{i=1}^3 U_{ei} \nu_i + U_{eh} \nu_h$$

Capture rate per atom

$$\Gamma^{\nu_h}({}^3\text{He}) = |U_{eh}|^2 \frac{1}{\pi} G_{\beta}^2 \cdot F_0(1, p) \cdot p_{e^+} \cdot p_0 \left( |M_F|^2 + g_A^2 |M_{GT}|^2 \right) \frac{\eta_{\nu}}{\langle \eta_{\nu} \rangle} \langle \eta_{\nu} \rangle$$

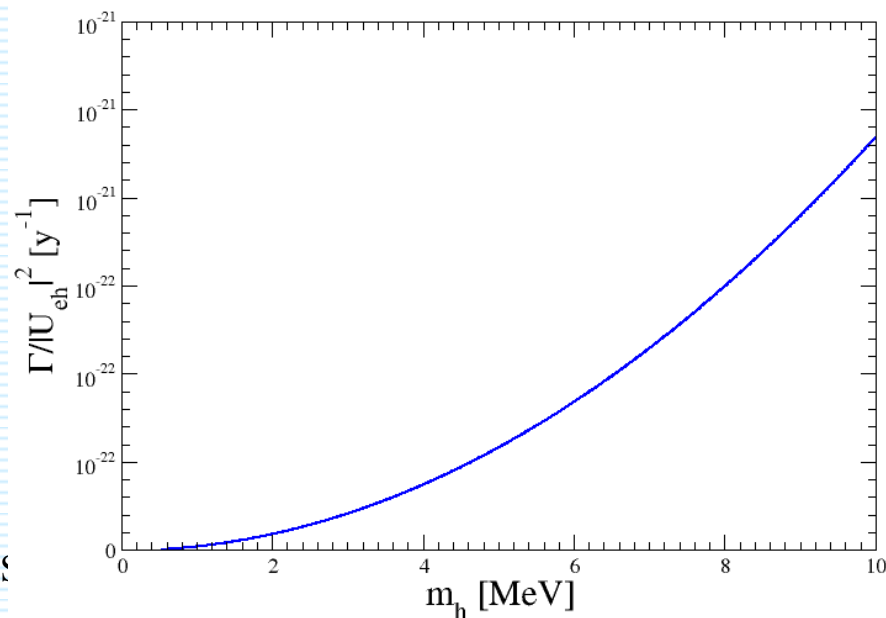
$$p_{e^+} = \sqrt{E_e^2 - m_e^2} = \sqrt{(m_{\nu_h} - 18.6 \text{ keV})^2 - m_e^2}$$

Hodák, F.Š., Kovaenko, Faessler,  
PPNP 66, 452 (2011)

$$m_{\nu_h} > 18.6 \text{ keV} + m_{e^+}$$

Production rate for 1kg of  ${}^3\text{He}$

$m_{\nu_h}$ [MeV]	$N_{\nu_h} / ( U_{eh} ^2 \cdot \frac{\eta_{\nu}}{\langle \eta_{\nu} \rangle})$ [ $\text{y}^{-1}$ ]
1.0	$7.9 \cdot 10^2$
5	$2.3 \cdot 10^4$
10	$9.4 \cdot 10^4$



*Beta Beams at CERN*  
*(experiment)*

**Thierry Stora group (CERN)**

**Rastislav Hodák, Peter Valko  
(Comenius University)**

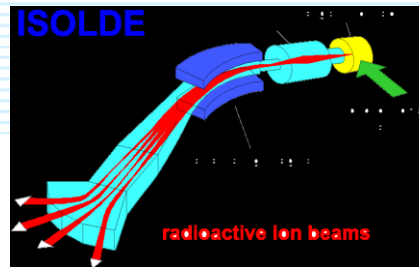
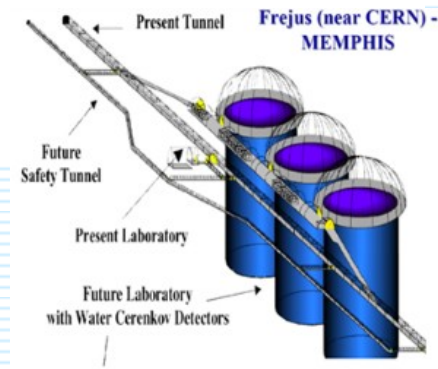
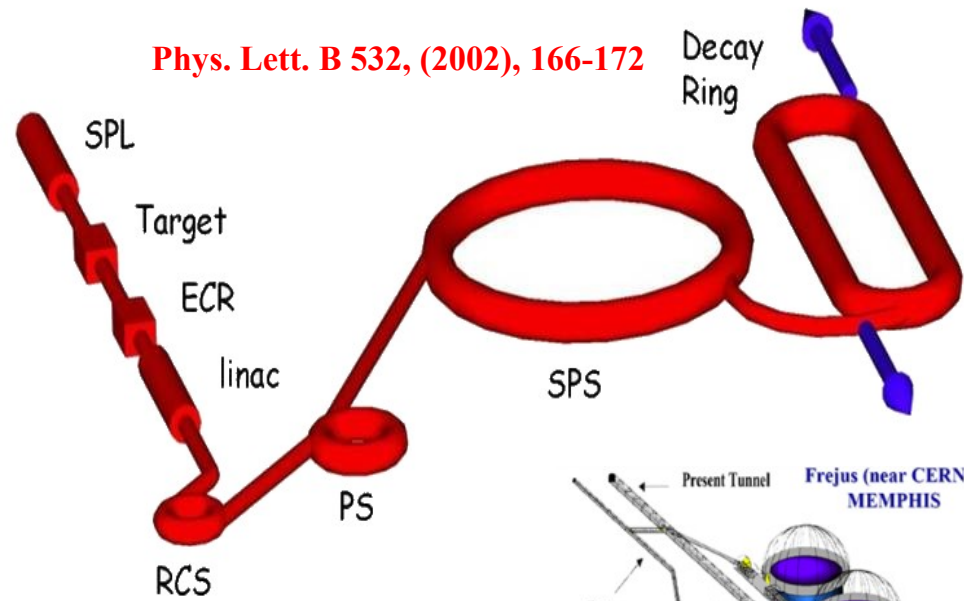
# Beta beams concept

- ❑ Idea by **Piero Zucchelli** (2002)
- ❑ **Aim:** Production of pure and collimated ultra-relativistic (anti)neutrino beams from the beta decay of radioactive ions circulating in a storage ring.

## Physical applications:

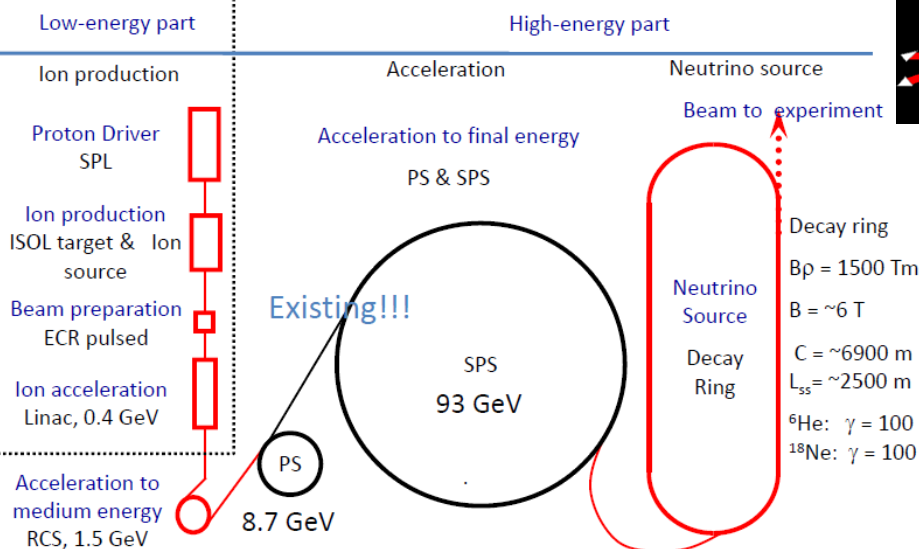
- ❖ **High energy** → **Neutrino oscillation physics** (mixing angle  $\theta_{13}$  and CP violation phase)
- ❖ **Low energy** → **Cross-sections of neutrino-nucleus interaction**

Phys. Lett. B 532, (2002), 166-172



Orme Ch., arXiv:1004.0939v1 (2010)

## Beta beams scenario ${}^6\text{He}/{}^{18}\text{Ne}$

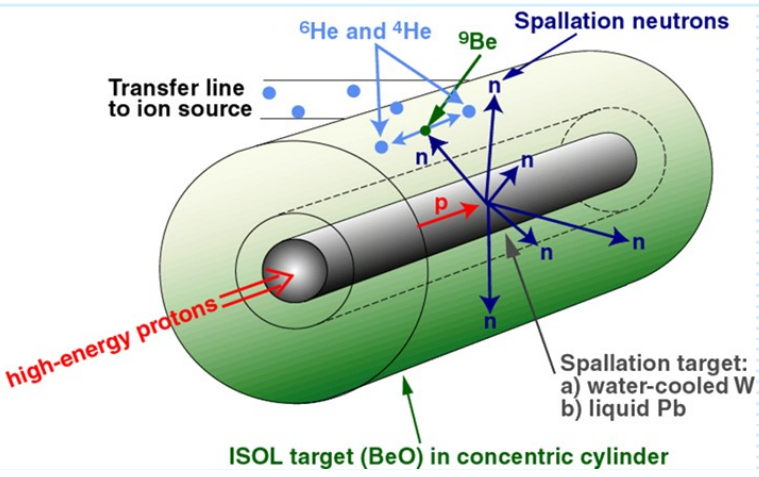


- ❑ Ion choice:  ${}^6\text{He}$  and  ${}^{18}\text{Ne}$

- ❑ Based on existing technology and machines
- ❑ **Production of  $\nu_e$  and anti- $\nu_e$  over 10 years:**

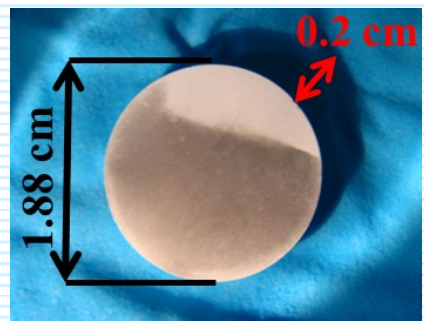
-  $2.9 \times 10^{19}$  anti- $\nu$  from  ${}^6\text{He}$  ( $3.3 \times 10^{13}$   ${}^6\text{He/s}$ )

# ${}^6\text{He}$ production

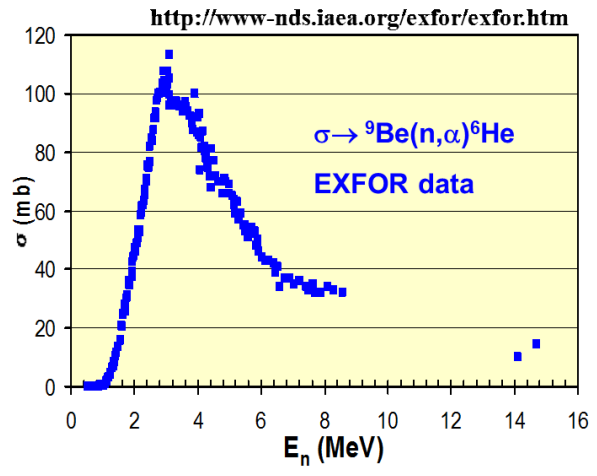


$${}^6_2\text{He}^{2+} (T_{1/2} = 0.8\text{s}) \rightarrow {}^6_3\text{Li} + e^- + \bar{\nu}$$

$$Q_{\beta^-} = 3.51\text{ MeV}$$



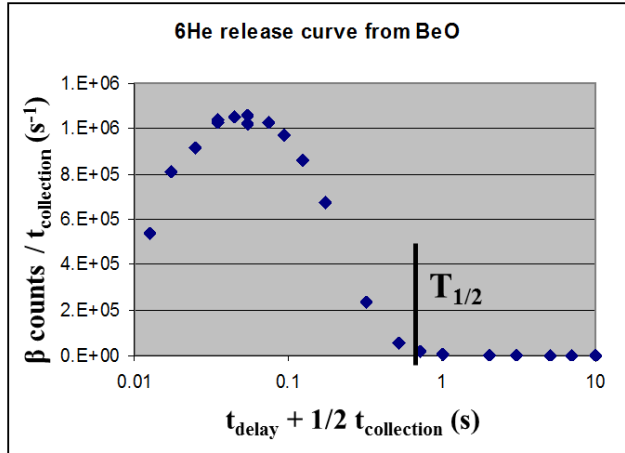
- ❖ **Threshold: 0.6 MeV**
- ❖ **Peak cross-section: 105 mb @ 3MeV**



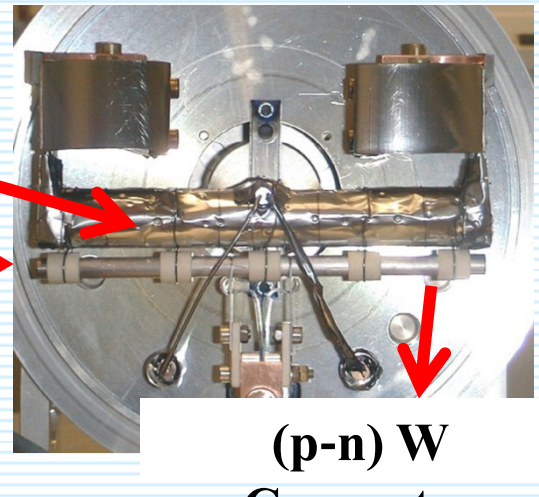
N. Thiolliere et al., EURISOL-DS

## ❖ ${}^6\text{He}$ can be achieved:

- $2 \times 10^{13}$   ${}^6\text{He}/\text{s}$  100kW, 1 GeV proton beam
- $1 \times 10^{14}$   ${}^6\text{He}/\text{s}$  200kW, 2 GeV p beam in-target production



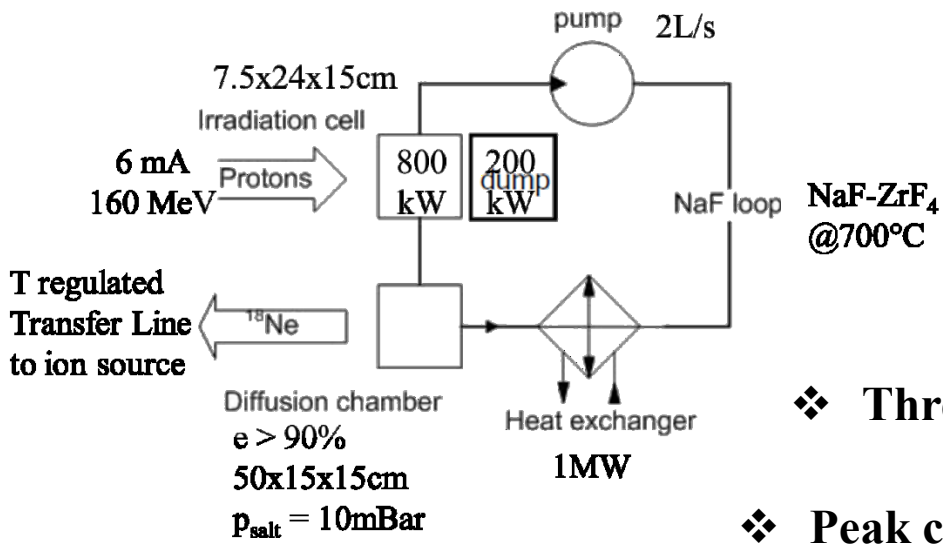
**BeO Target**  
**p (1.4 GeV)**  
**ISOLDE experiment - CERN, GANIL and Weizmann**



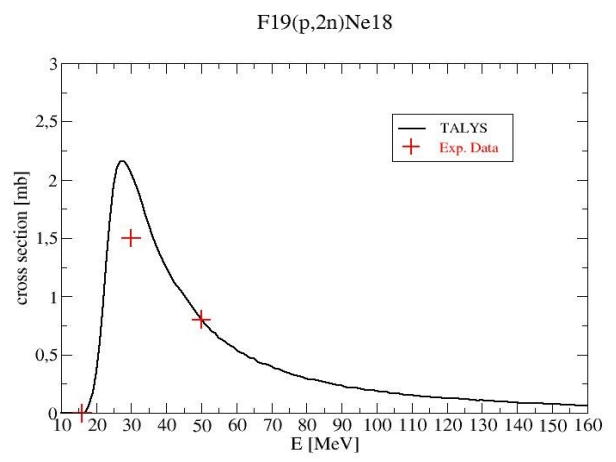
# $^{18}\text{Ne}$ production

$${}_{10}^{18}\text{Ne}^{10+} (T_{1/2} = 1.7\text{ s}) \rightarrow {}_9^{18}\text{F} + e^+ + \nu$$

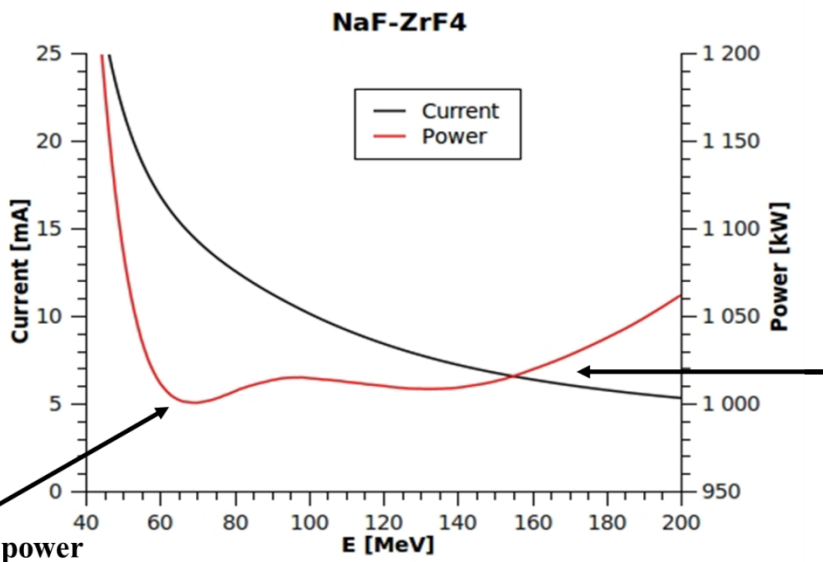
$$Q_{EC} = 4.45\text{ MeV}$$



- ❖ Threshold: 16 MeV
- ❖ Peak cross-section: 1.6 mb @ 30 MeV



## Conceptual target loop ( $^{19}\text{F}(p, 2n)^{18}\text{Ne}$ )



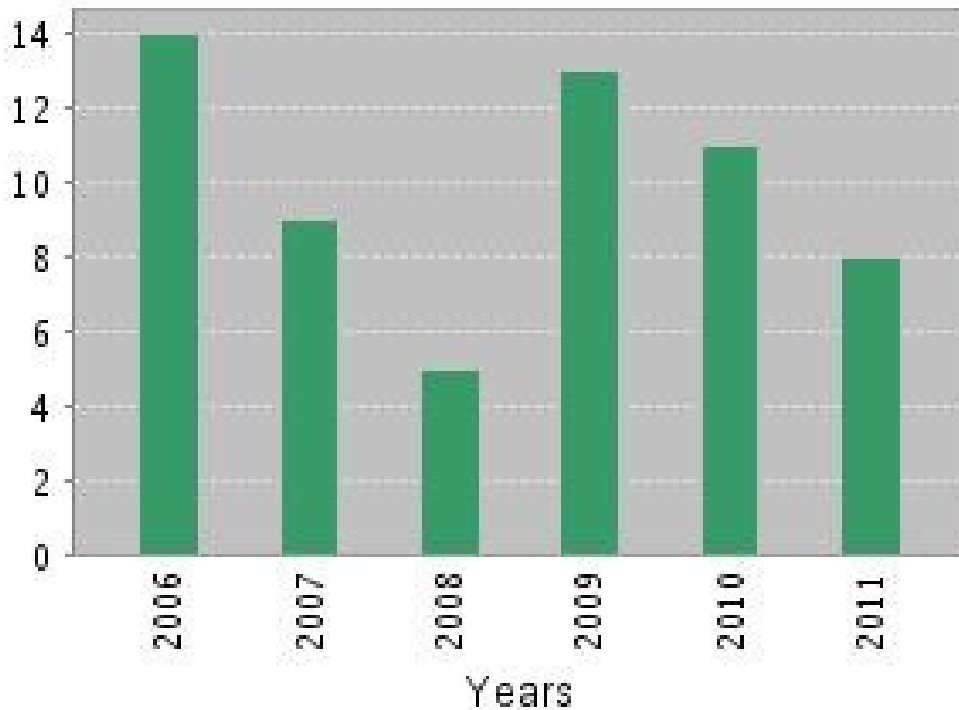
Upgraded  
LINAC 4

- ❑ Melting point of NaF-ZrF<sub>4</sub> ≈ 500°C
- ❑ Hastelloy N alloy (Ni based) – excellent salt corrosion resistance
- ❑ Cooling – by circulating molten salt

# *Publications - Citations*

## *(2006-2011)*

### Published Items in Each Year



**About 60 publications in  
refereed journals  
with about  
700 citations**





## *Grants -Finances*



**EU project:** (2004-09) Integrated Large Infrastructures for Astroparticle Science, RII3-CT-2004-506222 (theory)

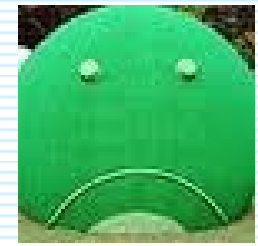
**DFG project:** (2005-11) Nuclei as laboratory to test lepton number/ flavor violation (theory)

**JINR project:** (2005-11) Grand unification, fundamental rare processes and nuclear structure (theory)

**Slovak projects:** VEGA(2006-09) Massive neutrinos and double beta decay  
VEGA(2009-11) Massive neutrinos in astro-, particle and nuclear physics (theory)



## *Can we get some money for experimental activities?*



**EU project ILIAS-next** (theory and experiment), submitted in 2009 and 2010, not approved (twice 13.5 points from 15)

**EU structural funds for Slovakia** (theory and experiment), Project for construction of small underground laboratory, positive referee's reports, not approved - **not enough money allocated for call (2010)?!** But, we need such facility (Fukushima)!

**APVV project SuperNEMO experiment** (theory and experiment), 2011, not approved positive referee's reports, Slovak referees gave not enough points 89/100 and 91/100

Slovak particip. in ASPERA? ASPERA meeting in Bratislava in 2008. Suggestion for the APVV to enter ASPERA within ERANET (34 000 EUR). Answer: **NO**



**Institute for particle and astroparticle physics!**

Can we get support for our astroparticle activities from Slovak-CERN commission?

*We have no end of fun with neutrino physics.*



*Mathematics is Egyptian*



*Neutrino physics is Babylonian*

*We have to communicate more with neutrinos.*