

Study of $B^0 \rightarrow K^{*0} \tau \tau$ at FCC-ee

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FUTURE
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- 1 Context
- 2 $B^0 \rightarrow K^{*0} \tau^+ \tau^-$ reconstruction method and vertexing emulation
- 3 Backgrounds and selection
- 4 IDEA vertexing emulation
- 5 Results & outlook

- Third generation couplings in quark transitions are the less-well known.
- Specific models addressing the Flavour problem(s) often provide $b \rightarrow \tau$ enhancements or modifications w.r.t. the SM $\Rightarrow b \rightarrow s\tau\tau$ ($m_\tau \sim 20m_\mu$) is a must do to sort out the BSM models [1, 2]. Problem : measuring the ν 's.
- Thanks to its clear experimental environment and its ability to produce boosted b -hadrons, FCC-ee looks like the right place to reconstruct the ν 's.
- SM : the $b \rightarrow s\tau\tau$ transition proceeds through an electroweak penguin diagram.
- Study of the rare heavy-flavoured decay $B^0 \rightarrow K^* \tau^+ \tau^-$ at FCC-ee[3]. SM prediction : $\text{BR} = \mathcal{O}(10^{-7}) \rightarrow$ not observed yet (present limit : $\mathcal{O}(10^{-3} - 10^{-4})$ [4]).

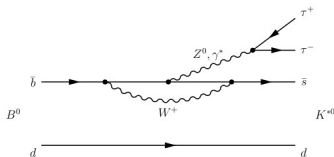


Figure – EW penguin quark-level transition

- The $B^0 \rightarrow K^* \tau \tau$ decay topology is driven by the tau decay multiplicity.
- There are from 2 to 4 neutrinos (not detected) and at least 4 charged particles in the final state and one, two or three decay vertices.
- We focus on the 3-prongs tau decays ($\tau \rightarrow \pi \pi \pi \nu$) for which the decay vertex can be reconstructed in order to solve fully the kinematics.
- 10 particles in the final state ($K, 7\pi, \nu, \bar{\nu}$), 3 decay vertices and 2 undetected neutrinos.

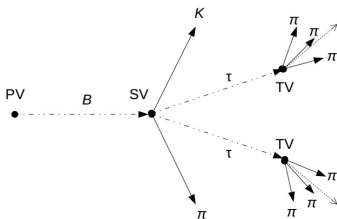


Figure – Decay topology

Goal : explore the feasibility of the search for $B^0 \rightarrow K^* \tau^+ \tau^-$ and give the corresponding detector requirements.

- The events used in this work are generated with Pythia [5] ($Z \rightarrow b\bar{b}$ and hadronisation) and EvtGen [6] (forcing the decay with adequate models).
- The reconstruction is performed with the FCC Analyses sw using Delphes [7] simulation (featuring the IDEA [8] detector).
- The simulated data use particles reconstructed with the momentum resolution given by the IDEA drift chamber tracking system.
- The vertex resolutions drives the feasibility of the measurement (Krakow) \rightarrow the main goal of the study is to address the precision of the BF as function of the vertex resolution.
- State of the art IDEA vertexing performance will be determined and compared to other working points.

- To fully reconstruct the kinematics of the decay \rightarrow neutrinos momenta must be resolved.
- Enough constraints are available in order to determine the missing coordinates.
- Energy momentum conservation at τ decay vertex \Rightarrow gives the neutrino momentum at the cost of a quadratic ambiguity :

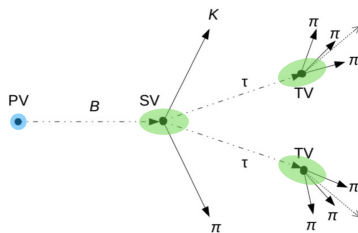
$$\begin{cases} p_{\nu\tau}^{\perp} = -p_{\pi_t}^{\perp} \\ p_{\nu\tau}^{\parallel} = \frac{((m_{\tau}^2 - m_{\pi_t}^2) - 2p_{\pi_t}^{\perp,2})}{2(p_{\pi_t}^{\perp,2} + m_{\pi_t}^2)} \cdot p_{\pi_t}^{\parallel} \pm \frac{\sqrt{(m_{\tau}^2 - m_{\pi_t}^2)^2 - 4m_{\tau}^2 p_{\pi_t}^{\perp,2}}}{2(p_{\pi_t}^{\perp,2} + m_{\pi_t}^2)} \cdot E_{\pi_t} \end{cases}$$

- A selection rule has to be build in order to solve the ambiguities.
- Practically energy-momentum conservation at the B decay vertex gives a condition between τ 's and K^* :

$$p_{\tau_{-}^{+}} = -\frac{\vec{p}_{K^{*}} \cdot \vec{e}_{\tau_{-}^{+}}}{1 - (\vec{e}_{\tau_{-}^{+}} \cdot \vec{e}_B)^2} - p_{\tau_{+}^{+}} \cdot \frac{\vec{e}_{\tau_{-}^{+}} \cdot \vec{e}_{\tau_{+}^{-}} - (\vec{e}_{\tau_{-}^{+}} \cdot \vec{e}_B)(\vec{e}_{\tau_{+}^{-}} \cdot \vec{e}_B)}{1 - (\vec{e}_{\tau_{+}^{-}} \cdot \vec{e}_B)^2}$$

- Method validated at MC truth level.

- PV : 3D normal law including Beam Spot Constraints.
- SV & TV \rightarrow ellipsoidal (decaying particle direction as reference) :
 - longitudinal,
 - transverse.
- Several working points examined (Longitudinal-Transverse configuration denoted as L-T in the following) :
 - 5 μm to 20 μm longitudinal,
 - 1 μm to 8 μm transverse.
- 20-3 (L-T) smearing used as reference in the following.
- Experimental vertexing efficiency is conservatively taken as 80% for the time beingⁱ.



i. Due to the large multiplicity of the decay FCCAnalyses vertexing failed to estimate efficiency by itself.

The considered backgrounds

- The relevant backgrounds are the ones with a similar final state than the signal ($K7\pi$).
- Several possible modes in $b \rightarrow c\bar{c}s$ and $b \rightarrow cT\nu$ transitionsⁱⁱⁱ but often not observed to date \Rightarrow guesstimate of the branching fraction from phase space computation and use of analogies.
- Determination of the dominant backgrounds for the measurement by building per track efficiencies from already generated ones.

iii. More details on backgrounds choices in appendix.

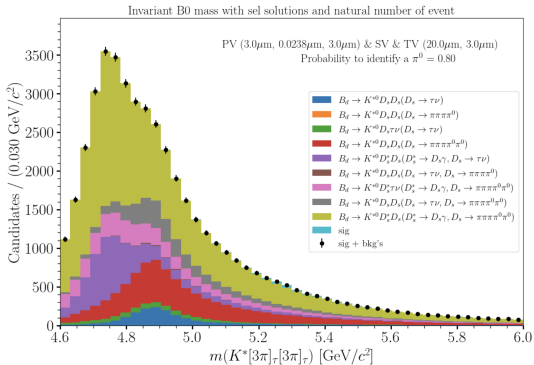
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- Determination of the dominant backgrounds for the measurement by building per track efficiencies from already generated ones.

Decay	BF (SM/meas.)	Intermediate decay	BF_had	Additional missing particles
Signal : $B^0 \rightarrow K^* \tau \tau$	1.30×10^{-7}	$\tau \rightarrow \pi \pi \pi \nu, K^* \rightarrow K \pi$	9.57×10^{-11}	
Backgrounds $b \rightarrow c\bar{c}s$: $B^0 \rightarrow K^{*0} D_s D_s$	2.78×10^{-4}	$D_s \rightarrow \tau \nu$ $D_s \rightarrow \tau \nu, \pi \pi \pi \pi^0$ $D_s \rightarrow \pi \pi \pi \pi^0$	5.79×10^{-10} 6.52×10^{-10} 7.35×10^{-10}	2ν ν, π^0 $2\pi^0$
$B^0 \rightarrow K^{*0} D_s D_s^*$	8.78×10^{-4}	$D_s \rightarrow \tau \nu, \pi \pi \pi \pi^0 \pi^0$ $D_s \rightarrow \pi \pi \pi 2\pi^0$ $D_s \rightarrow \tau \nu$ $D_s \rightarrow \pi \pi \pi \pi^0 \pi^0$	5.47×10^{-9} 5.17×10^{-8} 1.83×10^{-9} 1.63×10^{-7}	$\nu, 2\pi^0$ $4\pi^0$ $2\nu, \gamma/\pi^0$ $4\pi^0, \gamma/\pi^0$
Backgrounds $b \rightarrow cT\nu$: $B^0 \rightarrow K^{*0} D_s T \nu$ $B^0 \rightarrow K^{*0} D_s^* T \nu$	9.17×10^{-6} 2.03×10^{-5}	$D_s \rightarrow \tau \nu$ $D_s \rightarrow \pi \pi \pi \pi^0 \pi^0$	3.59×10^{-10} 7.51×10^{-9}	2ν $\nu, \gamma, 2\pi^0$

iii. More details on backgrounds choices in appendix.

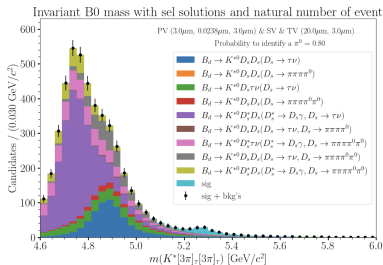
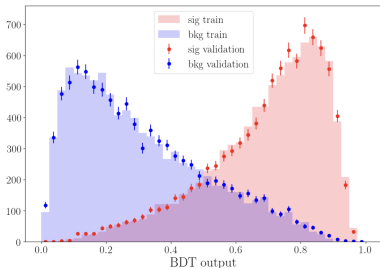
- The B^0 mass has been reconstructed for all our modes.
- Calorimeter PID performances : π^0 detection rate of 80% is assumed in order to reduce the π^0 backgrounds.
- Backgrounds are overwhelming^{iv}.
- Additional selection is required. We played a Multivariate selection (XGBoost [9]).



^{iv}. Reconstruction performances for all modes in appendix.

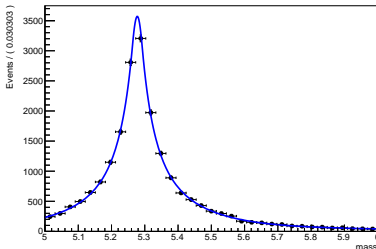
- Training dataset generated with signal and the collection of available backgrounds.
- The backgrounds are considered in natural proportion (after the preselection).
- 50/50 split train/validation.
- Previous variables are given as inputs as well as the reconstructed p_{τ} of each τ candidate.
- XGB parameters optimised on AUC.
- Overtraining plot in order to check the validity of the training \rightarrow OK.
- Use of the MVA^{vi} to perform the selection (cut at 0.5 on the BDT output).

vi. Feature importance plot in appendix.

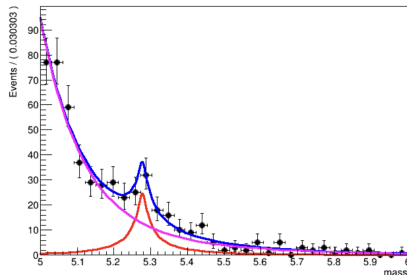


- Same selection applied to other vertex resolution emulations.
- Unbinned ML fit of the data with :
 - signal \rightarrow double CB + a Gaussian,
 - background \rightarrow two decreasing exponential.
- Baseline : fit of the simulated signal then fit of the signal and background rescaled together.
- Extraction of the signal yield N and the associated error σ_N .
- Plot of the naive precision σ_N/N of the BF measurement of $B^0 \rightarrow K^{*0} \tau\tau$ as function of the resolution ^{vii}.

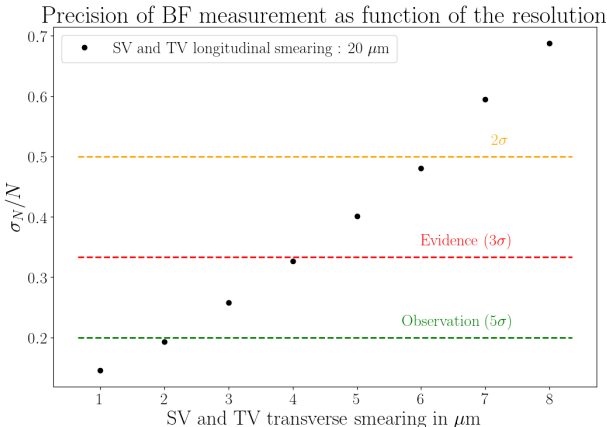
A RooPlot of "mass"



A RooPlot of "mass"



vii. Points from other longitudinal resolutions in appendix.



- Precision on BF measurement for fully emulated vertexing working points have been determined.
- Let's confront this to an actual state of the art vertex detector we have at hand → the IDEA vertex detector.

- Resolutions determined from 10^6 signal events.
- Reconstructed PV position fitted from reconstructed tracks with the FCCAnalyses VertexFitterSimple tools (Beam Spot Constraints set at (4.5, $20e^{-3}$, 300)mm).
- Displacement of the reconstructed PV w.r.t. the MC truth PV is build in cartesian coordinates.
- The IDEA resolution is determined for each coordinate by a fit of the displacement :
 - double gaussian model on (x,z) ^{viii},
 - simple gaussian model on y.
- Resolutions $\mathcal{O}(3 \mu\text{m})$ for (x,z).
- Resolution $\mathcal{O}(20 \text{nm})$ for y.

viii. In appendix.

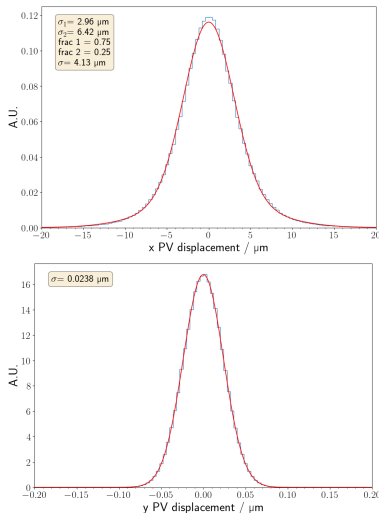


Figure – PV displacement and fit of the resolution for x (top) and y (bottom).

- Reconstructed SV ($K^{*0} \rightarrow K\pi$) and TV ($\tau \rightarrow 3\pi$) positions fitted from MC matched reconstructed tracks via FCCAnalyses VertexFitterSimple tools.
- Displacement of the reconstructed SV and TV w.r.t. to the MC truth projected on decay plan (L-T).
- The IDEA resolution is determined for each coordinate by a fit of the displacement :
 - triple gaussian model on L,
 - simple CB model on T.
- The performances are a bit better^{ix} on the TV (3 tracks) comparing to the SV (2 tracks) despite the lower daughters momenta on average.

ix. In appendix.

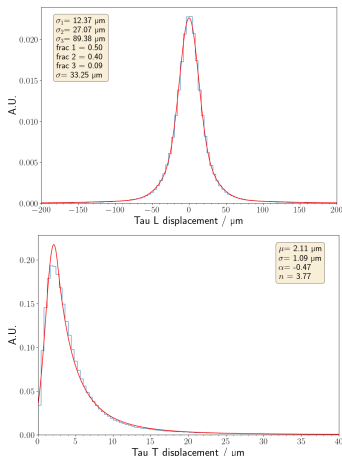


Figure – TV displacement and fit of the resolution for L (top) and T (bottom), T not signed because there is no reference T direction (not as it is in our smearing).

- Emulation of the PV resolutions with 3D-gaussian smearing that follow the combined σ of the fits among each axis.
- SV and TV smearing via the IDEA fitted resolutions.
- Smearing emulated on each direction via accept/reject algorithms.
- SV and TV L smeared from there respective pdf's.
- SV and TV T smeared from an opportunistic 3 gaussians pdf ($\mu = 0, \sigma_1 = 2.7 \mu\text{m}, f_1 = 50\%, \sigma_2 = 7 \mu\text{m}, f_2 = 40\%, \sigma_3 = 20 \mu\text{m}, f_3 = 10\%$), which reproduce approximately the IDEA T displacement distribution when emulated in 2D on the transverse plan.

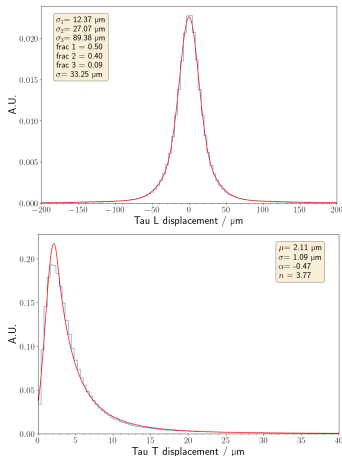
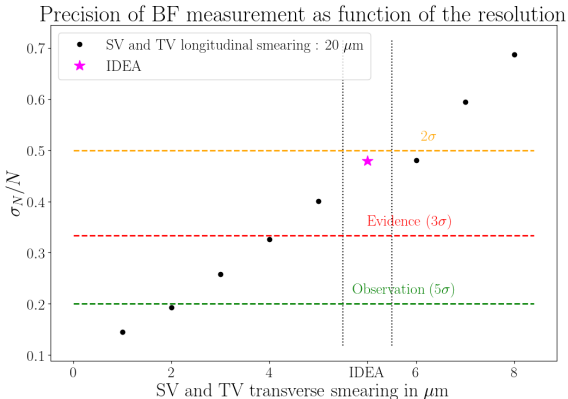


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Emulation of the vertex resolution performances in order to look for the feasibility of the search of $B^0 \rightarrow K^{*0} \tau\tau$ at FCC-ee :

- we can't make that mode with the state-of-the-art vertex^x detector,
- we are not that far neither.

x. Because of a previous bug, the performance shown for IDEA has changed comparing to the one presented by Michele on Monday.

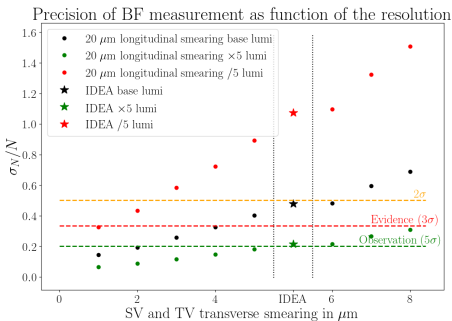


Figure – Precision on the BF measurement as function of the vertex resolution. Previous points are shown with the baseline luminosity and two other luminosity hypothesis are tested. Increasing the data taking period by a factor 5 could bring us near the observation with IDEA as it is.

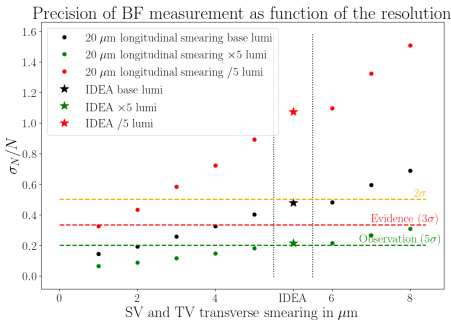


Figure – Precision on the BF measurement as function of the vertex resolution. Previous points are shown with the baseline luminosity and two other luminosity hypothesis are tested. Increasing the data taking period by a factor 5 could bring us near the observation with IDEA as it is.

- Analysis aimed at assessing the required vertexing performances to measure $B^0 \rightarrow K^{*0} \tau \tau$ from the two $\tau \rightarrow 3\pi$ self-contained method only.
- Considering τ leptonic decays on one branch of the B^0 decay brings a factor 7 in statistics. Less experimental handles but still way out to get out the signal.
- Considering fully τ leptonic decays in both branches brings a factor 14 in statistics (Impact Parameter resolution will be instrumental here)

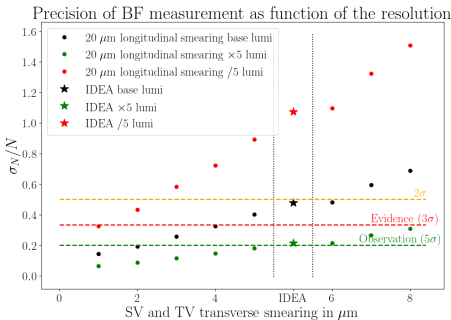


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- Considering fully τ leptonic decays in both branches brings a factor 14 in statistics (Impact Parameter resolution will be instrumental here)

Thanks!

To fully reconstruct the kinematics of the decay (B invariant-mass observable for instance) we need :

- Momentum of all final particles including not detected neutrinos.
- The decay lengths (6 constraints) together with the tau mass (2 constraints) can be used to determine the missing coordinates (6 degrees of freedom).
- We use energy-momentum conservation at tertiary (or τ decay) vertex with respect to τ direction^{xi}.

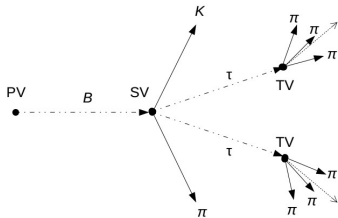


Figure – The dotted lines represent the non-reconstructed particles. The plain lines are the particles that can be reconstructed in the detector.

$$\begin{cases} p_{\nu_\tau}^\perp = -p_{\pi_t}^\perp \\ p_{\nu_\tau}^\parallel = \frac{((m_\tau^2 - m_{\pi_t}^2) - 2p_{\pi_t}^{\perp,2})}{2(p_{\pi_t}^{\perp,2} + m_{\pi_t}^2)} \cdot p_{\pi_t}^\parallel \pm \frac{\sqrt{(m_\tau^2 - m_{\pi_t}^2)^2 - 4m_\tau^2 p_{\pi_t}^{\perp,2}}}{2(p_{\pi_t}^{\perp,2} + m_{\pi_t}^2)} \cdot E_{\pi_t} \end{cases}$$

xi. Another way to do this computation is given by [10].

There is a quadratic ambiguity on each neutrino momentum !

→ The ambiguities propagate to τ and B reconstructions

→ 4 possibilities by taking all +/- combination for the two neutrinos

⇒ A selection rule is needed to choose the right possibility

→ From the energy-momentum conservation at the B decay vertex, we have a condition between the 2 taus and the K^* with respect to the B direction :

$$p_{\tau_-^+} = -\frac{\vec{p}_{K^*}^\perp \cdot \vec{e}_{\tau_-^+}}{1 - (\vec{e}_{\tau_-^+} \cdot \vec{e}_B)^2} - p_{\tau_+^-} \cdot \frac{\vec{e}_{\tau_-^+} \cdot \vec{e}_{\tau_+^-} - (\vec{e}_{\tau_-^+} \cdot \vec{e}_B)(\vec{e}_{\tau_+^-} \cdot \vec{e}_B)}{1 - (\vec{e}_{\tau_+^-} \cdot \vec{e}_B)^2}$$

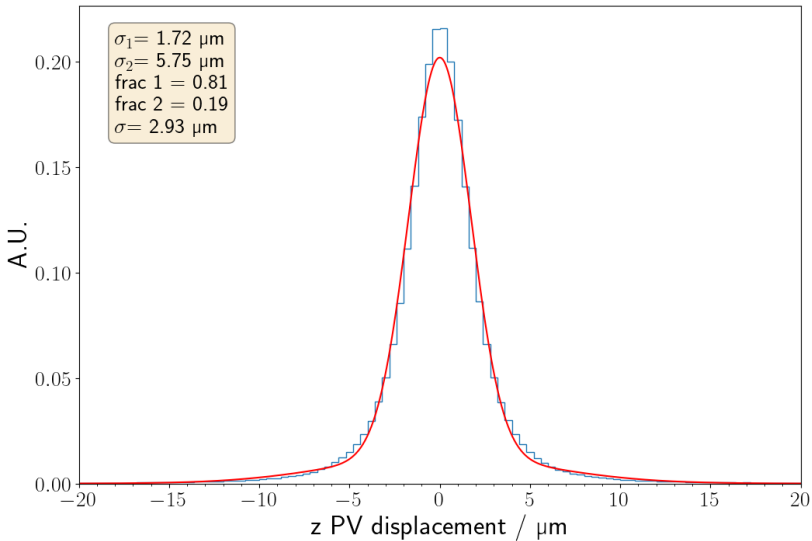


Figure – PV displacement and fit of the resolution for z

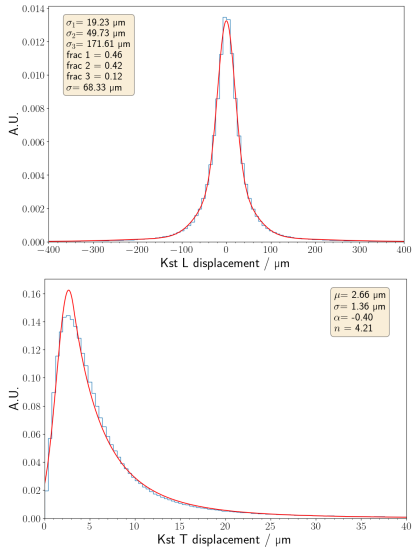


Figure – SV displacement and fit of the resolution for L (top) and T (bottom).

The knowledge of the reconstruction efficiency allows us to compute the expected number of B^0 decays fully reconstructed at FCC-ee :

$$\mathcal{N}_{K^*\tau\tau \rightarrow K7\pi2\nu} = \mathcal{N}_Z \cdot BR(Z \rightarrow b\bar{b}) \cdot 2f_d \cdot BR(K^*\tau\tau) \cdot BR(\tau \rightarrow \pi\pi\pi\nu)^2 \cdot BR(K^* \rightarrow K\pi) \cdot \epsilon_{reco} \cdot \epsilon_{vertex}$$

Where :

- $\mathcal{N}_Z = 8 \times 10^{12}$ the expected number of Z produced,
- $BR(Z \rightarrow b\bar{b}) = 0.1512 \pm 0.0005$,
- $f_d = 0.407 \pm 0.007$ the hadronisation term,
- $BR(K^*\tau\tau) = 1.30 \times 10^{-7} \pm 10\%$ the SM predicted branching fraction,
- $BR(\tau \rightarrow \pi\pi\pi\nu) = 0.0931 \pm 0.0005$,
- $BR(K^* \rightarrow K\pi) = 0.69$,
- $\epsilon_{reco} = 0.3840 \pm 0.0007$ for a smearing $3 \mu\text{m} - 20 \mu\text{m}$,
- $\epsilon_{reco} = 0.2850 \pm 0.0005$ for a smearing that follows IDEA performances,
- $\epsilon_{vertex} = 0.8$,

$$\Rightarrow \mathcal{N}_{K^*\tau\tau \rightarrow K7\pi2\nu} \approx 235 \pm 24 \text{ for } 20 - 3$$

$$\Rightarrow \mathcal{N}_{K^*\tau\tau \rightarrow K7\pi2\nu} \approx 175 \pm 18 \text{ for IDEA}$$

- $B^0 \rightarrow K^{*0} D_s D_s$ from analogy game :

$$BF(B^0 \rightarrow K^{*0} D_s D_s) = BF(B^0 \rightarrow DD_s) \times \frac{BF(B^0 \rightarrow D_s \pi K^0)}{BF(B^0 \rightarrow D\pi)}$$

where $B^0 \rightarrow DD_s$ is the equivalent mode without $s\bar{s}$ from vacuum, $B^0 \rightarrow D\pi$ is the equivalent mode without $s\bar{s}$ from vacuum and with $W \rightarrow \bar{u}d$, $B^0 \rightarrow D_s \pi K^0$ is the equivalent mode with $W \rightarrow \bar{u}d$.

- $B^0 \rightarrow K^{*0} D_s^* D_s$ and $B^0 \rightarrow K^{*0} D_s^* D_s^*$ w.r.t. $B^0 \rightarrow K^{*0} D_s D_s$ from $B_s^0 \rightarrow D_s^{(*)} D_s^{(*)}$ hierarchy.
- $B^0 \rightarrow K^{*0} D_s^{(*)} \tau \nu$ from analogy via phase space computation[10] :

$$BF(B^0 \rightarrow K^{*0} D_s^{(*)} \tau \nu) = BF(B^+ \rightarrow KD_s^{(*)} \ell \nu) \times \frac{PS(B^0 \rightarrow K^{*0} D_s^{(*)} \tau \nu)}{PS(B^+ \rightarrow KD_s^{(*)} \ell \nu)}$$

where PS denotes the Phase Space computed numerically (three body decay hypothesis used conservatively) and $B^+ \rightarrow KD_s^{(*)} \ell \nu$ is a reference mode with a known BF.

- $B^0 \rightarrow K^{*0} D_s \tau \nu$ and $B^0 \rightarrow K^{*0} D_s^* \tau \nu$ w.r.t. $B^0 \rightarrow K^{*0} D_s^{(*)} \tau \nu$ from $B^0 \rightarrow D^{(*)} \ell \nu$ hierarchy.

- $B_s^0 \rightarrow K^{*0} D^{(*)} \tau \nu$ from analogy via phase space computation[10] :

$$BF(B_s^0 \rightarrow K^{*0} D^{(*)} \tau \nu) = BF(B_s^0 \rightarrow D_{s1} \mu \nu) \times \frac{PS(B_s^0 \rightarrow K^{*0} D^{(*)} \tau \nu)}{PS(B_s^0 \rightarrow D_{s1} \mu \nu)}$$

where PS denotes the Phase Space computed numerically (three body decay hypothesis used conservatively) and $B_s^0 \rightarrow D_{s1} \mu \nu$ is a reference mode with a known BF.

- $B_s^0 \rightarrow K^{*0} D \tau \nu$ and $B_s^0 \rightarrow K^{*0} D^* \tau \nu$ w.r.t. $B_s^0 \rightarrow K^{*0} D^{(*)} \tau \nu$ from $B^0 \rightarrow D^{(*)} \ell \nu$ hierarchy.

Decay	BF (SM/meas.)	Intermediate decay	BF _{had}	Additional missing particles
Signal : $B^0 \rightarrow K^* \tau \tau$	1.30×10^{-7}	$\tau \rightarrow \pi \pi \pi \nu, K^* \rightarrow K \pi$	9.57×10^{-11}	
Backgrounds $b \rightarrow c \bar{c} s$: $B^0 \rightarrow K^{*0} D_s D_s$	2.78×10^{-4}	$D_s \rightarrow \tau \nu$ $D_s \rightarrow \tau \nu, \pi \pi \pi \pi^{0 \text{ xii}}$ $D_s \rightarrow \pi \pi \pi \pi^{0 \text{ xii}}$ $D_s \rightarrow \tau \nu, \pi \pi \pi \pi^0 \pi^0$ $D_s \rightarrow \pi \pi \pi 2\pi^{0 \text{ xii}}$	5.79×10^{-10} 6.52×10^{-10} 7.35×10^{-10} 5.47×10^{-9} 5.17×10^{-8}	2ν ν, π^0 $2\pi^0$ $\nu, 2\pi^0$ $4\pi^0$
$B^0 \rightarrow K^{*0} D_s D_s^*$	8.78×10^{-4}	$D_s \rightarrow \tau \nu$ $D_s \rightarrow \tau \nu, \pi \pi \pi \pi^0$ $D_s \rightarrow \pi \pi \pi \pi^0$ $D_s \rightarrow \pi \pi \pi \pi^0 \pi^0$	1.83×10^{-9} 2.06×10^{-9} 2.32×10^{-9} 1.63×10^{-7}	$2\nu, \gamma/\pi^0$ $\nu, \pi^0, \gamma/\pi^0$ $2\pi^0, \gamma/\pi^0$ $4\pi^0, \gamma/\pi^0$
$B^0 \rightarrow K^{*0} D_s^* D_s^*$	9.10×10^{-4}	$D_s \rightarrow \tau \nu$ $D_s \rightarrow \tau \nu, \pi \pi \pi \pi^0$ $D_s \rightarrow \pi \pi \pi \pi^0 \pi^0$	1.90×10^{-9} 2.14×10^{-9} 2.41×10^{-9}	$2\nu, 2\gamma/\pi^0$ $\nu, \pi^0, 2\gamma/\pi^0$ $2\pi^0, 2\gamma/\pi^0$
Backgrounds $b \rightarrow c \tau \nu$: $B_s \rightarrow K^{*0} D \tau \nu$ $B_s \rightarrow K^{*0} D^* \tau \nu$	7.27×10^{-5} 2.03×10^{-4}	$D \rightarrow \pi \pi \pi \pi^0$ $D^* \rightarrow D^0 \pi, D \pi^0$ $D \rightarrow \pi \pi \pi \pi^0$ $D^0 \rightarrow 2\pi 2\pi \pi^0$	1.65×10^{-9} 1.12×10^{-9} 8.98×10^{-10}	ν, π^0 $\nu, 2\pi^0$ $\nu, 2\pi^0, 2\pi^\pm$
$B^0 \rightarrow \bar{K}^{*0} D_s \tau \nu$	9.17×10^{-6}	$D_s \rightarrow \tau \nu$ $D_s \rightarrow \pi \pi \pi \pi^0$	3.68×10^{-10} 4.15×10^{-10}	2ν ν, π^0
$B^0 \rightarrow K^{*0} D_s^* \tau \nu$	2.03×10^{-5}	$D_s \rightarrow \tau \nu$ $D_s \rightarrow \pi \pi \pi \pi^0$ $D_s \rightarrow \pi \pi \pi \pi^0 \pi^0$	8.07×10^{-10} 9.09×10^{-10} 7.51×10^{-9}	$2\nu, \gamma/\pi^0$ $\nu, \pi^0, \gamma/\pi^0$ $\nu, \gamma, 2\pi^0$

xii. $D_s \rightarrow 3\pi n \pi^0$ modes involves η/ω intermediate states (see appendix).

Better simulations for $D_s \rightarrow \pi\pi\pi\pi^0$

- Previously this decay has been generated in the Phase Space \rightarrow a more accurate simulation of the decay is needed \Rightarrow new samples which include η/ω (saturating the inclusive BF) intermediate states are in order.
- Replacement of the previous samples.
- $B^0 \rightarrow K^{*0} D_s D_s (D_s \rightarrow \pi\pi\pi\pi^0)$ is now $B^0 \rightarrow K^{*0} D_s D_s$ where $D_s \rightarrow \eta/\omega\pi$ and $\eta/\omega \rightarrow \pi\pi\pi^0$.
- $B^0 \rightarrow K^{*0} D_s D_s (D_s \rightarrow \pi\pi\pi\pi^0\pi^0)$ is now $B^0 \rightarrow K^{*0} D_s D_s$ where $D_s \rightarrow \eta/\omega\pi\pi^0$ and $\eta/\omega \rightarrow \pi\pi\pi^0$.

Momentum and transverse momentum distributions of the π^0

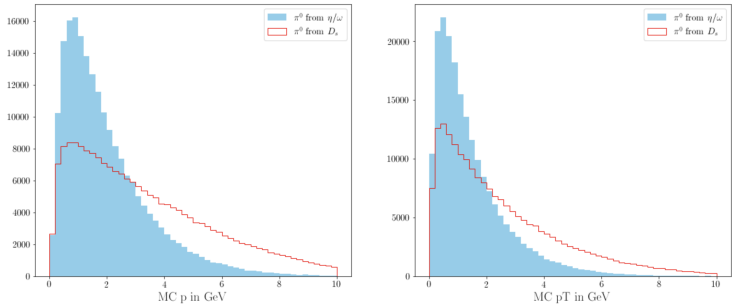
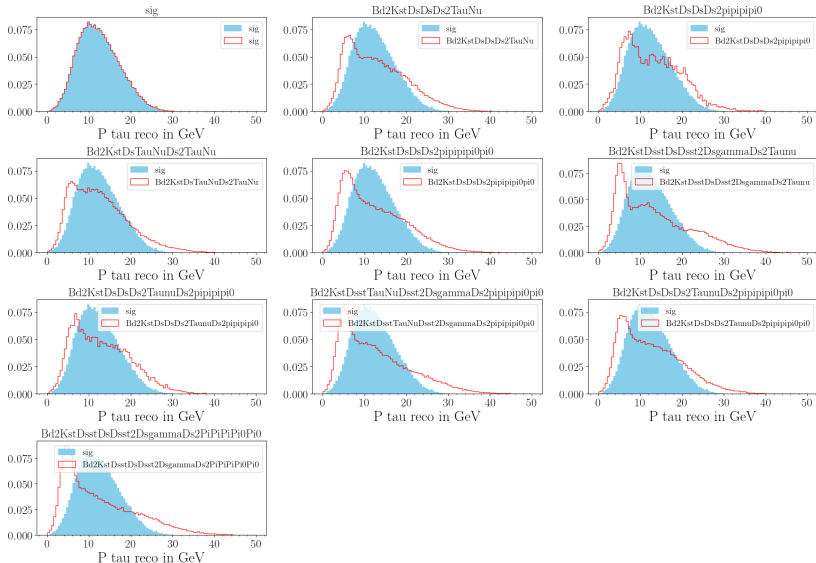


Figure – Distribution of π^0 momentum from $D_s \rightarrow 3\pi^2\pi^0$.

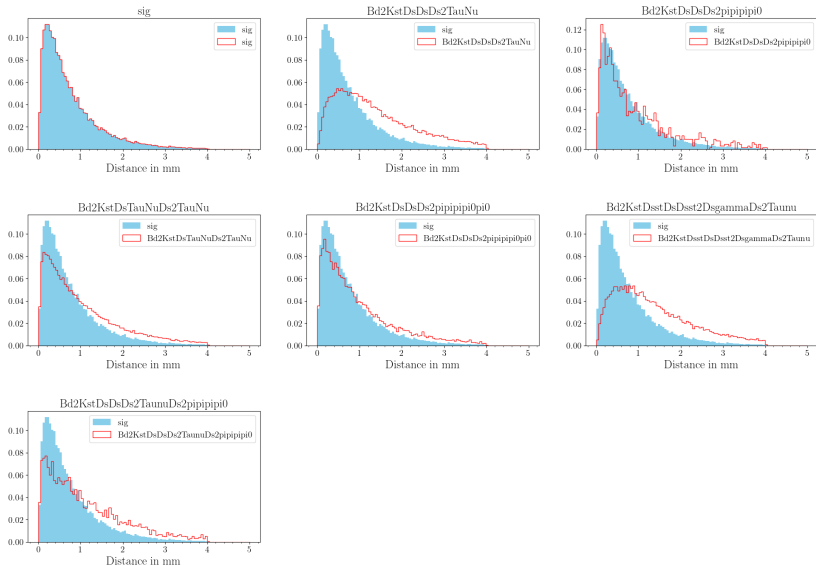
- $B^0 \rightarrow K^{*0} D_s D_s$ with the two D_s decaying as $D_s \rightarrow \tau \nu$, $D_s \rightarrow \pi \pi \pi \pi^0$ and $D_s \rightarrow \pi \pi \pi \pi^0 \pi^0$ already generated.
- $B^0 \rightarrow K^{*0} D_s^* D_s$ with the two D_s decaying as $D_s \rightarrow \tau \nu$ already generated.
- $B^0 \rightarrow K^{*0} D_s D_s$ with both $D_s \rightarrow \tau \nu$ and $D_s \rightarrow \pi \pi \pi \pi^0$ already generated.
- Construction of a "per track" efficiency by taking the square root of the reconstruction efficiency of the four first modes $\Rightarrow \epsilon(D_s \rightarrow \tau \nu)$, $\epsilon(D_s^* \rightarrow \tau \nu)$, $\epsilon(D_s \rightarrow \pi \pi \pi \pi^0)$ and $\epsilon(D_s \rightarrow \pi \pi \pi \pi^0 \pi^0)$.
- Cross check : $\epsilon(D_s \rightarrow \tau \nu) \times \epsilon(D_s \rightarrow \pi \pi \pi \pi^0) \simeq \epsilon(B^0 \rightarrow K^{*0} D_s D_s, D_s \rightarrow \tau \nu, D_s \rightarrow \pi \pi \pi \pi^0)$.
- Construction of an $\epsilon(*) = \epsilon(D_s^* \rightarrow \tau \nu) / \epsilon(D_s \rightarrow \tau \nu)$.
- Computation of an estimated efficiency for the possible background from these per track efficiencies.
- Ranking of the backgrounds via $BF \times \epsilon$.
- Choice of the biggest one for each type of specific topology.

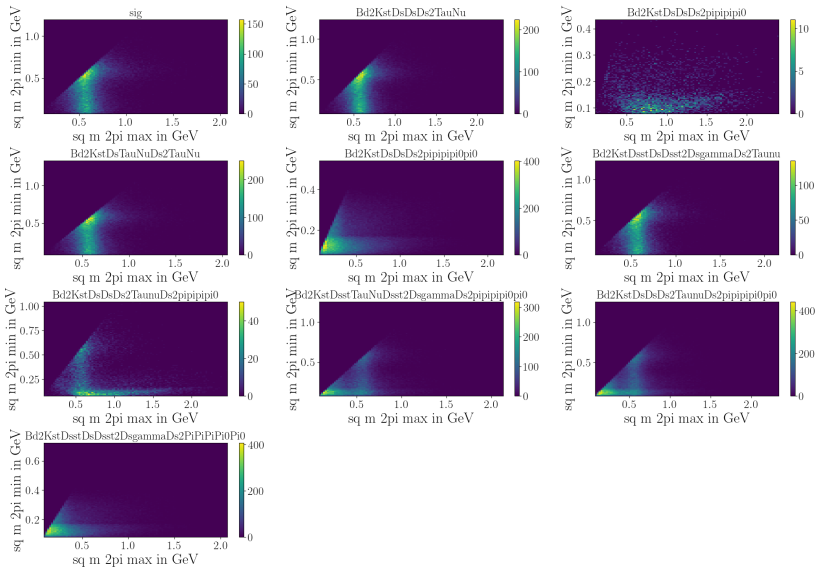
Data	Reconstruction 20 – 3
$B^0 \rightarrow K^{*0} \tau \tau (\tau \rightarrow \pi \pi \pi \nu)$	0.3840 ± 0.0007
$B^0 \rightarrow K^{*0} D_s D_s (D_s \rightarrow \tau \nu)$	0.4749 ± 0.0004
$B^0 \rightarrow K^{*0} D_s D_s (D_s \rightarrow \pi \pi \pi \pi^0)$	0.02190 ± 0.00002
$B^0 \rightarrow K^{*0} D_s D_s (D_s \rightarrow \pi \pi \pi \pi^0, \tau \nu)$	0.1014 ± 0.0001
$B^0 \rightarrow K^{*0} D_s D_s (D_s \rightarrow \pi \pi \pi \pi^0 \pi^0)$	0.5630 ± 0.0005
$B^0 \rightarrow K^{*0} D_s \tau \nu (D_s \rightarrow \tau \nu)$	0.4285 ± 0.0004
$B^0 \rightarrow K^{*0} D_s^* D_s (D_s^* \rightarrow D_s \gamma, D_s \rightarrow \tau \nu)$	0.4827 ± 0.0004
$B^0 \rightarrow K^{*0} D_s^* \tau \nu (D_s^* \rightarrow D_s \gamma, D_s \rightarrow \pi \pi \pi \pi^0 \pi^0)$	0.4726 ± 0.0004
$B^0 \rightarrow K^{*0} D_s D_s (D_s \rightarrow \tau \nu, \pi \pi \pi \pi^0 \pi^0)$	0.5164 ± 0.0004
$B^0 \rightarrow K^{*0} D_s^* D_s (D_s^* \rightarrow D_s \gamma, D_s \rightarrow \pi \pi \pi \pi^0 \pi^0)$	0.5730 ± 0.0004

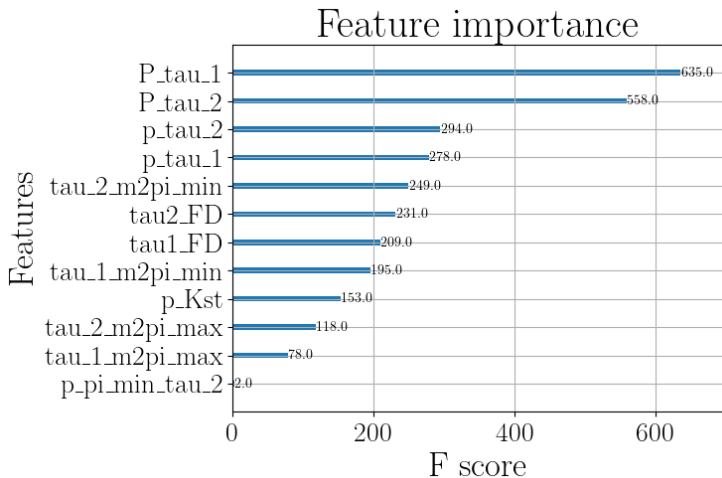
sel 20-3 P tau



sel 20-3 tau FD







Precision of BF measurement as function of the resolution

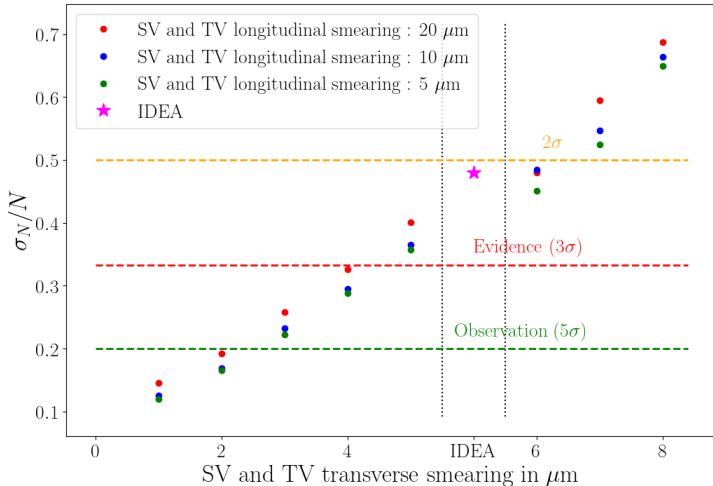


Figure – Precision on the BF measurement as function of the vertex resolution with 3 longitudinal configurations. Observed hierarchy issue comes from the interplay between the smearing of the vertexing and the fit model.



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