

Apologies for not attending the conference due to sad circumstances.

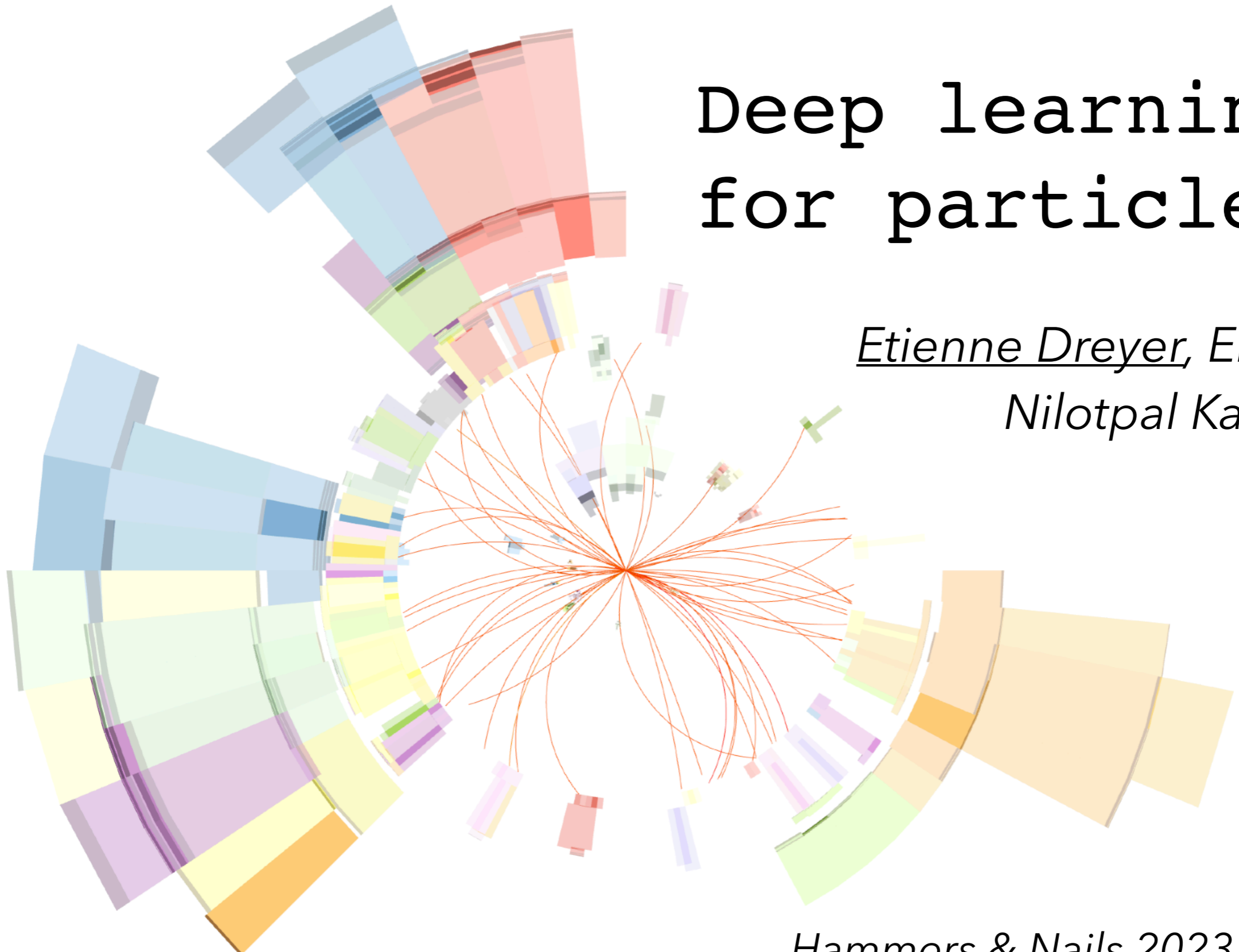
I want to extend my deepest sympathies and express my gratitude to Tobias for his tremendous effort in ensuring the success of the conference, despite it being regrettably interrupted.

Hopefully peace will prevail and we will be able to resume Hammers & Nails in Israel in 2024/2025.

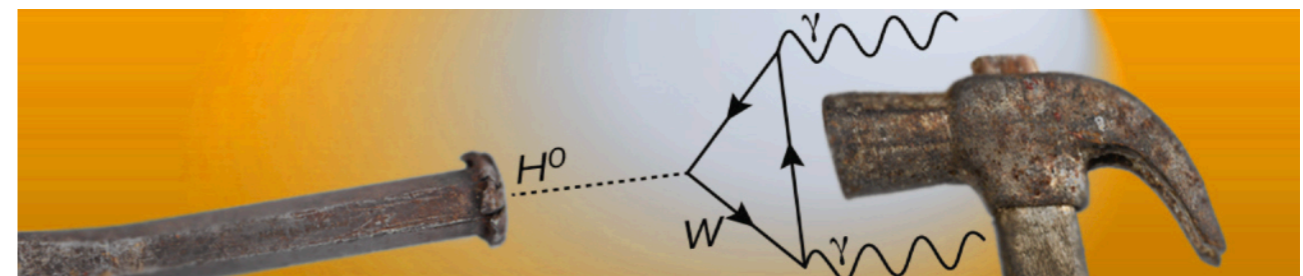


Deep learning for particle flow

*Etienne Dreyer, Eilam Gross
Nilotpal Kakati*



Hammers & Nails 2023 Swiss Edition



"Seeing" particles

BEBC

 1979

Weak neutral current

UA1

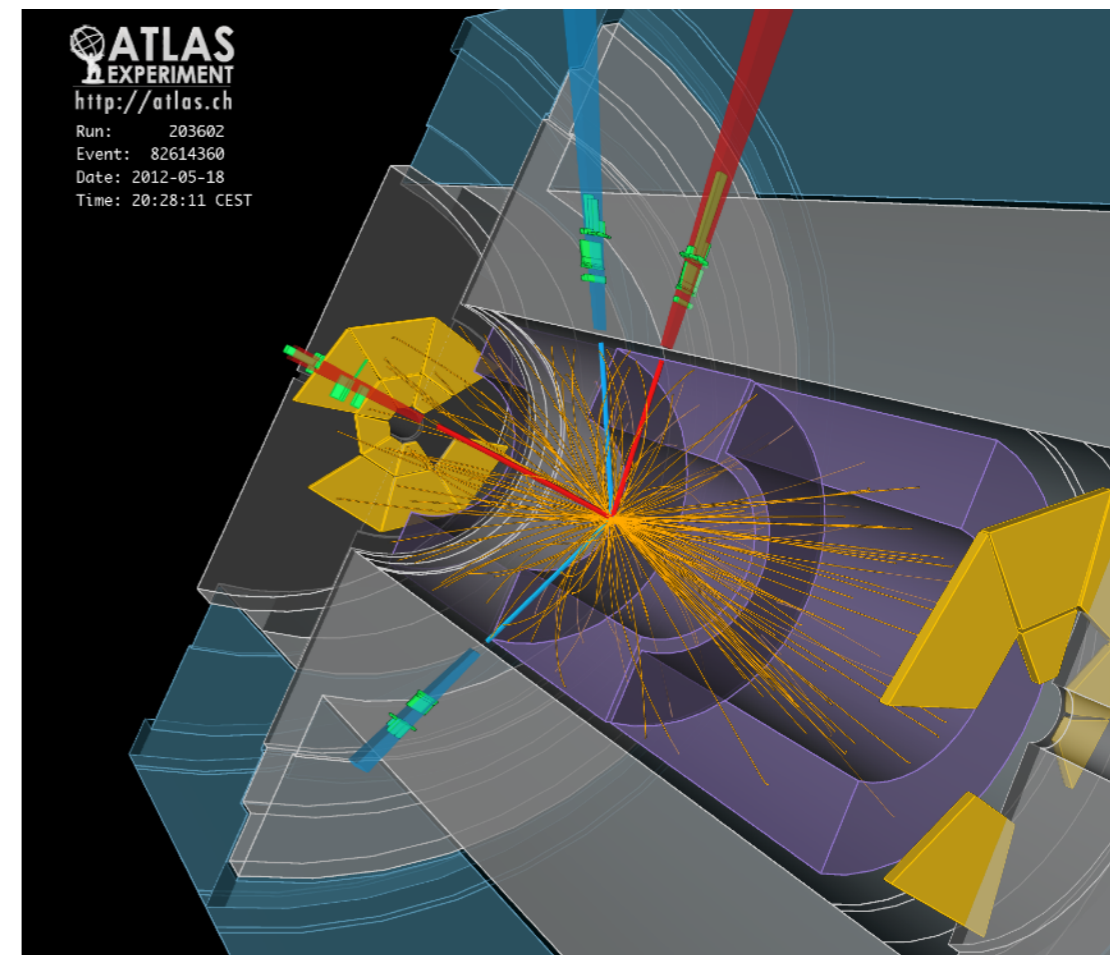
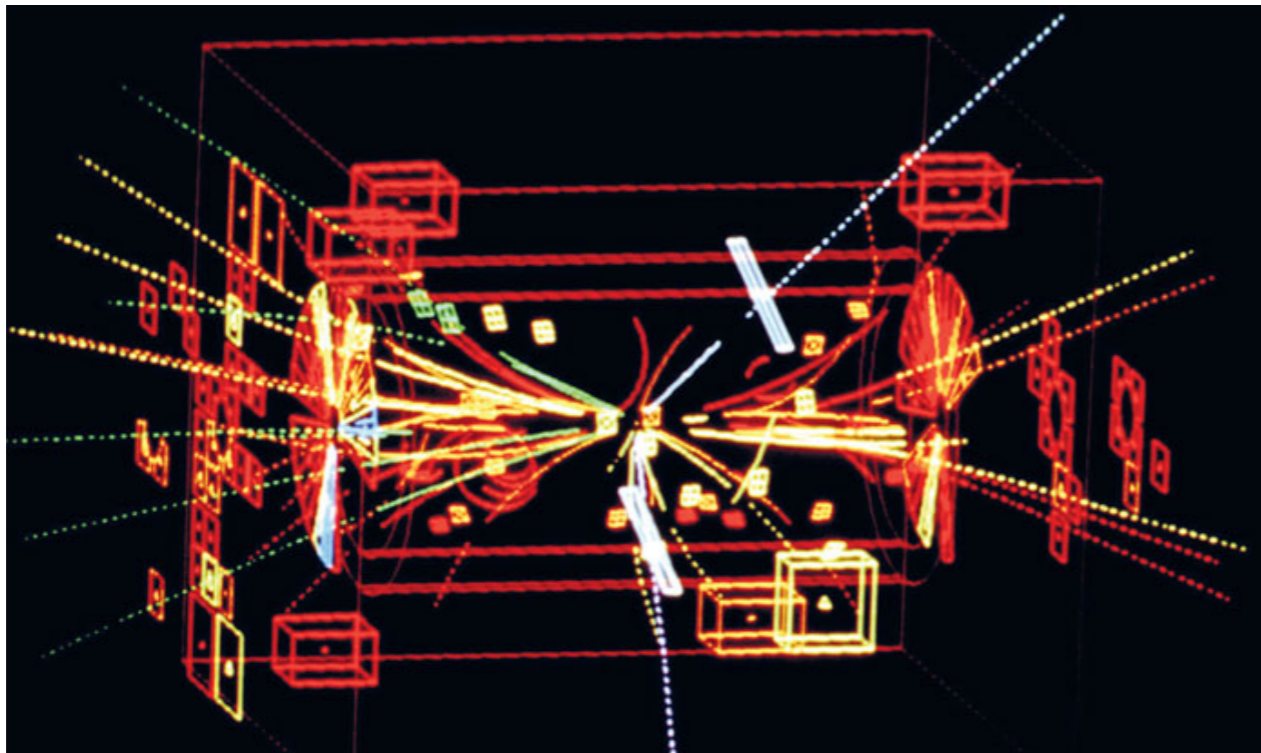
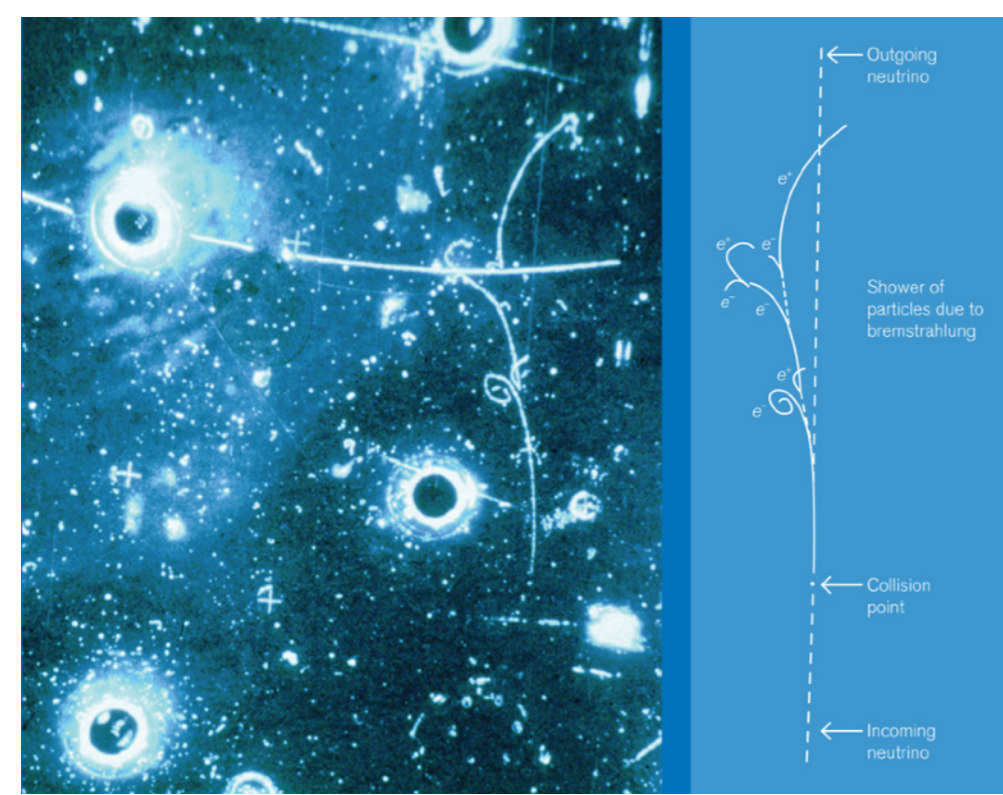
 1984

W, Z bosons

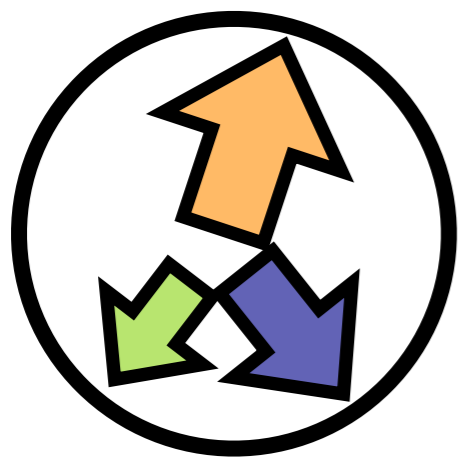
ATLAS

 2013

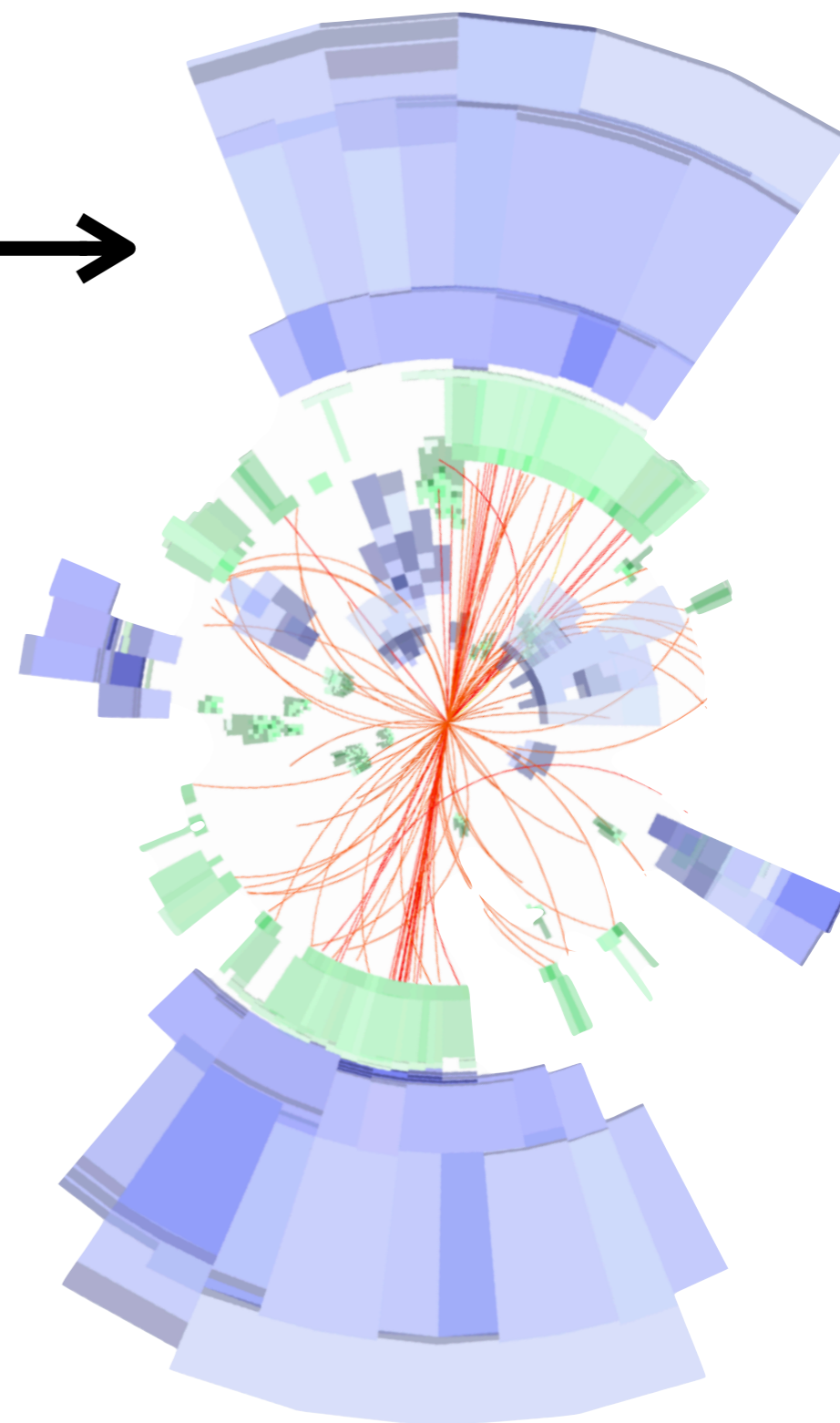
Higgs boson



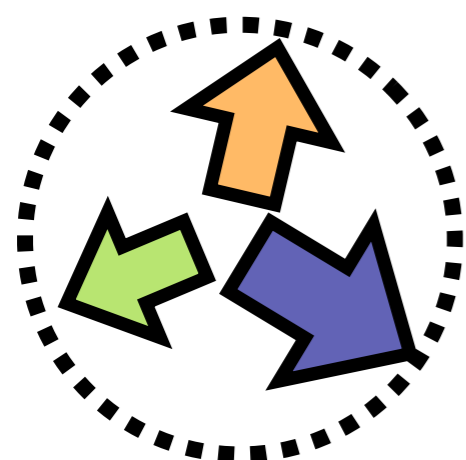
Truth particles



Detector hits



Part 1
The particle
reconstruction
problem



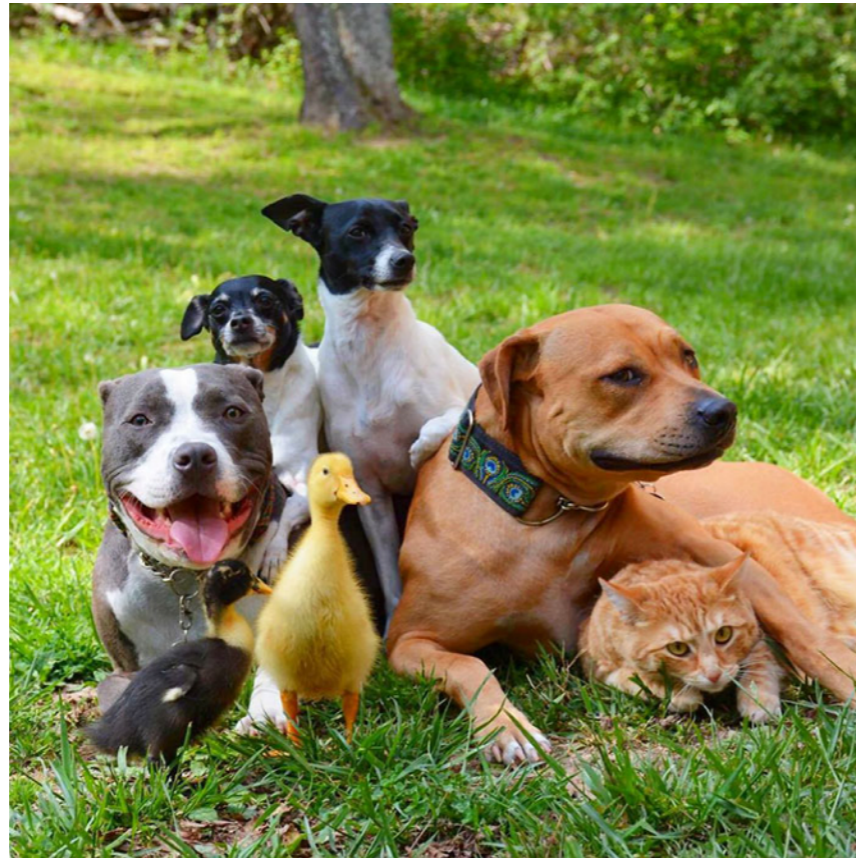
NN
model

Reconstructed particles

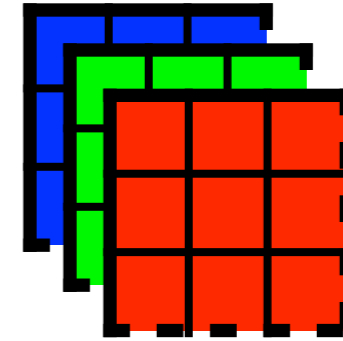
Classic object detection

Input

BoredPanda



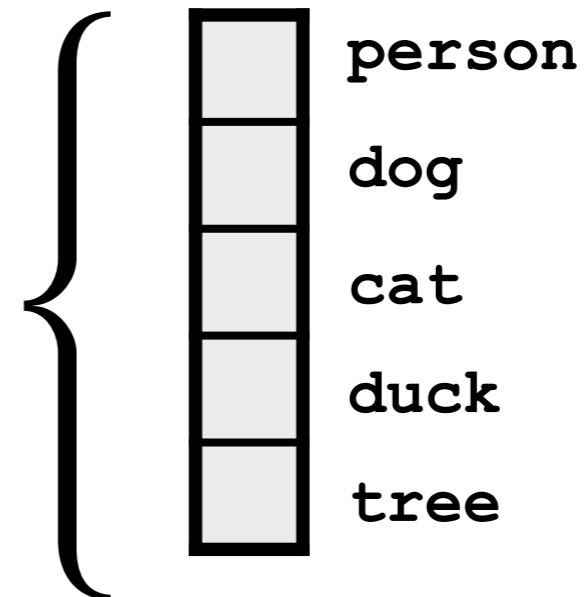
Features: RGB value array



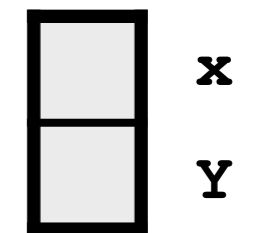
Cardinality



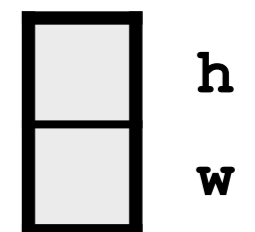
Class



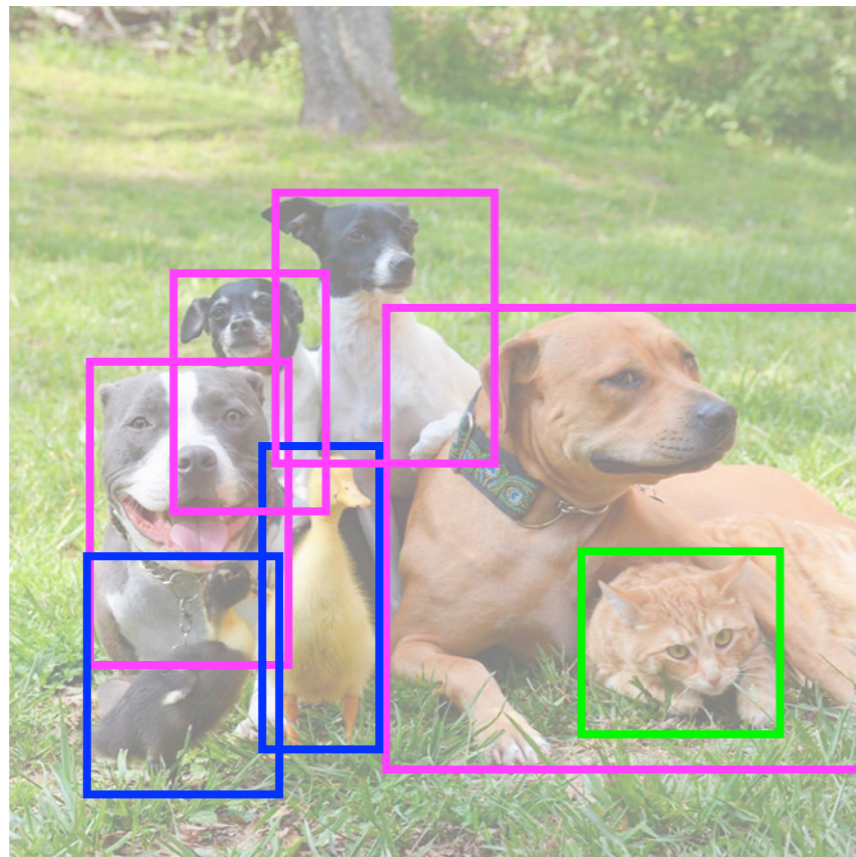
Position



Size

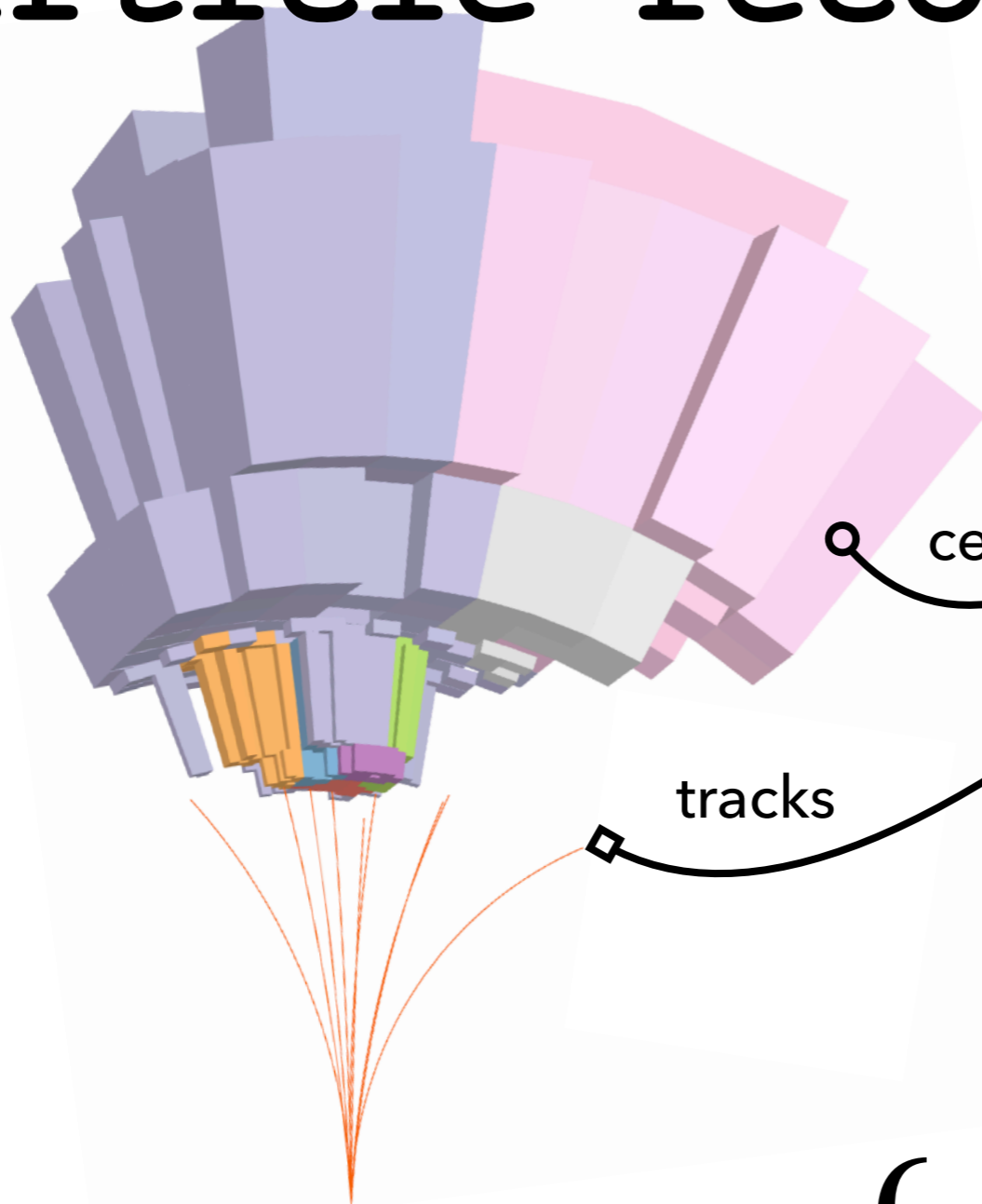


Output

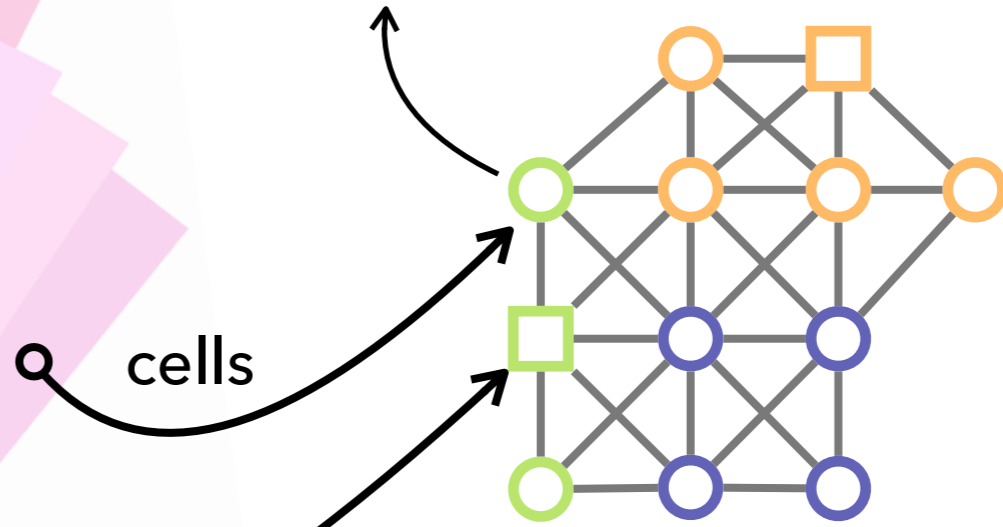


Particle reconstruction

Input



Features: [energy, location, ...]

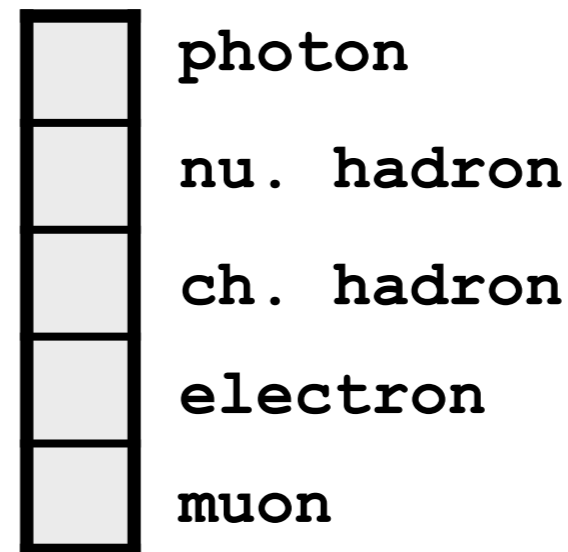


tracks

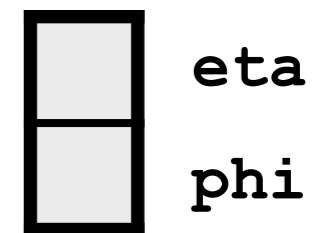
Cardinality



Class



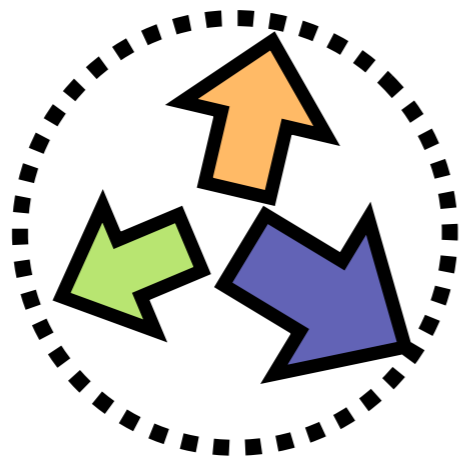
Direction



Momentum



Output

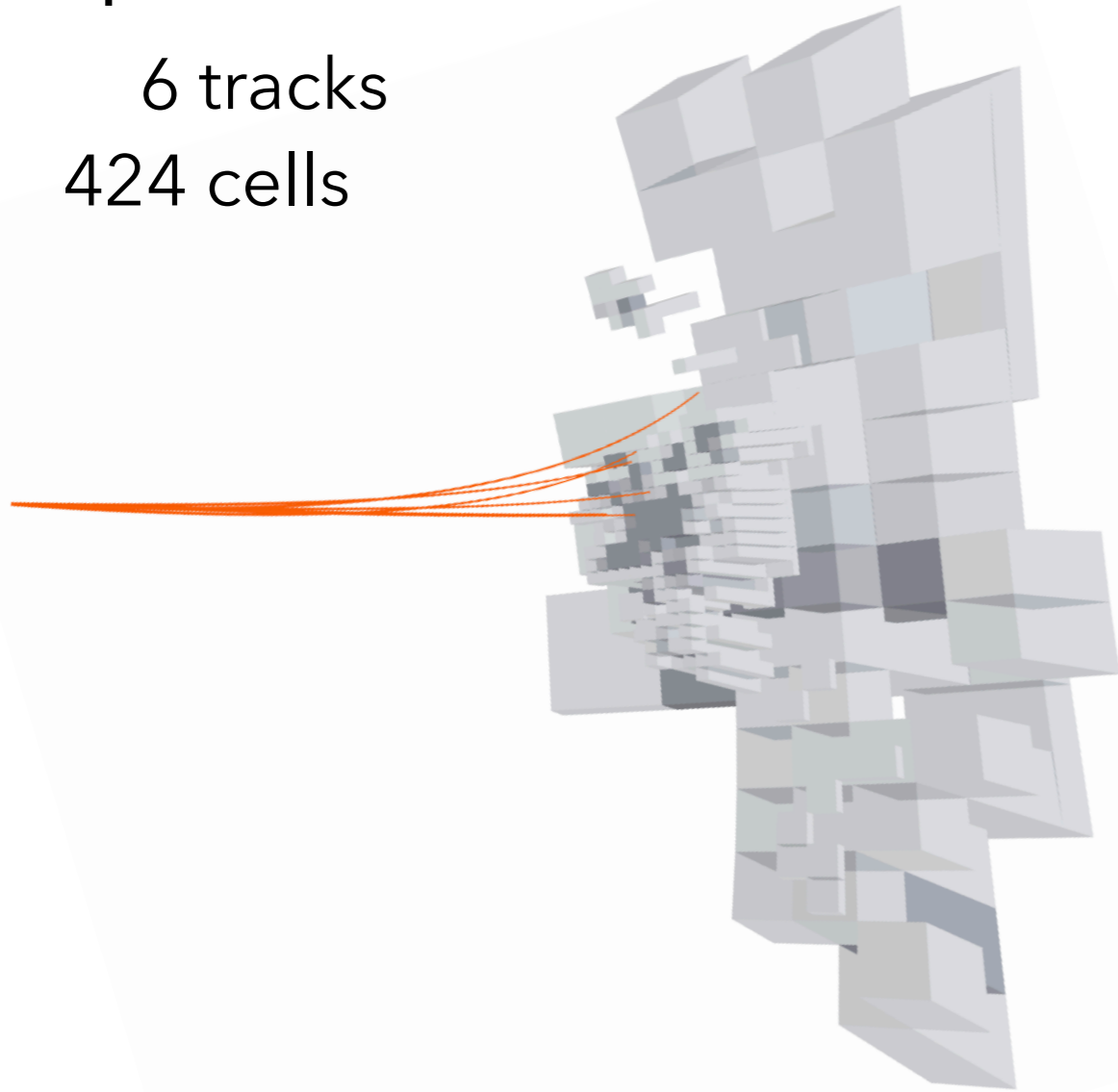


Cardinality prediction

Ex: single jet

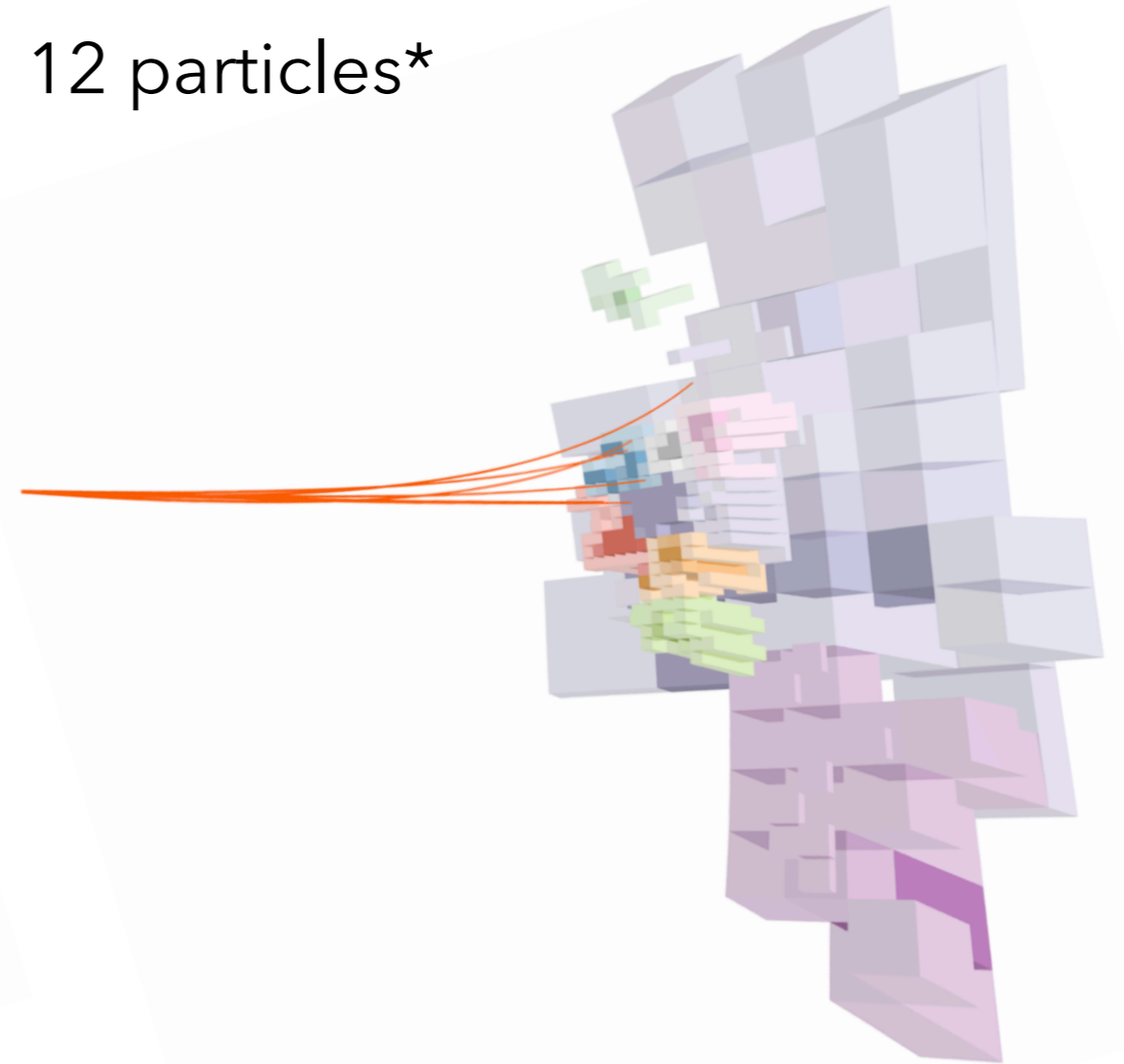
Input

6 tracks
424 cells



Ground truth (colored by particle index)

12 particles*



*Some particles are not dominant in any one of the cells (i.e. no dedicated color)

Particle classification

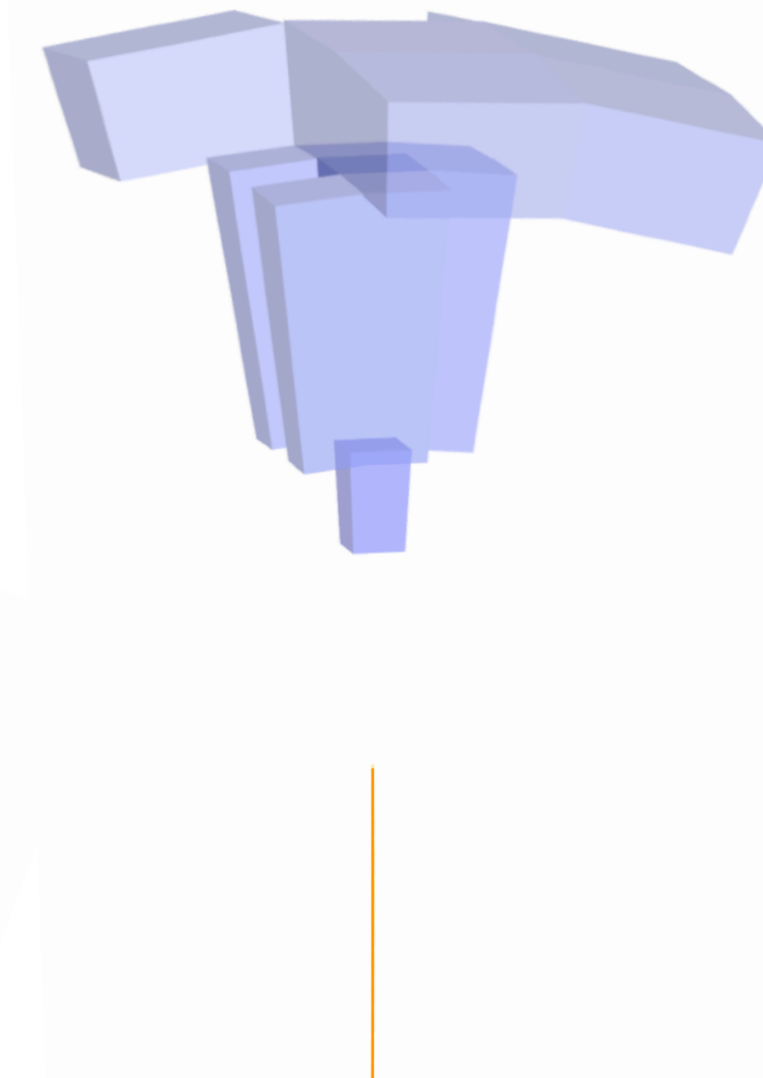
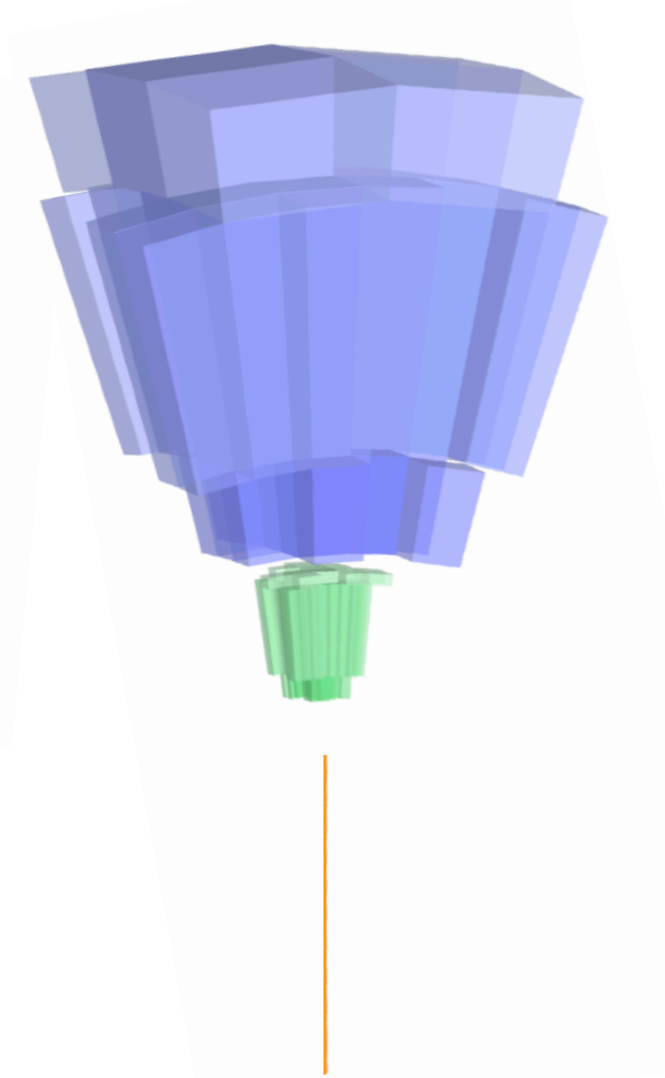
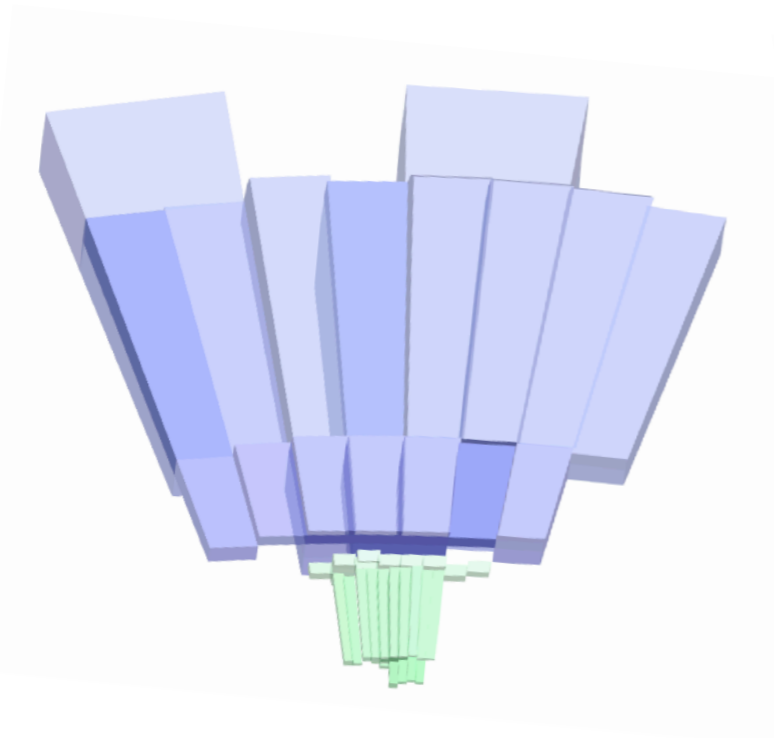
(0)
photon

(1)
neutral
hadron

(2)
charged
hadron

(3)
electron

(4)
muon



γ

K_L^0

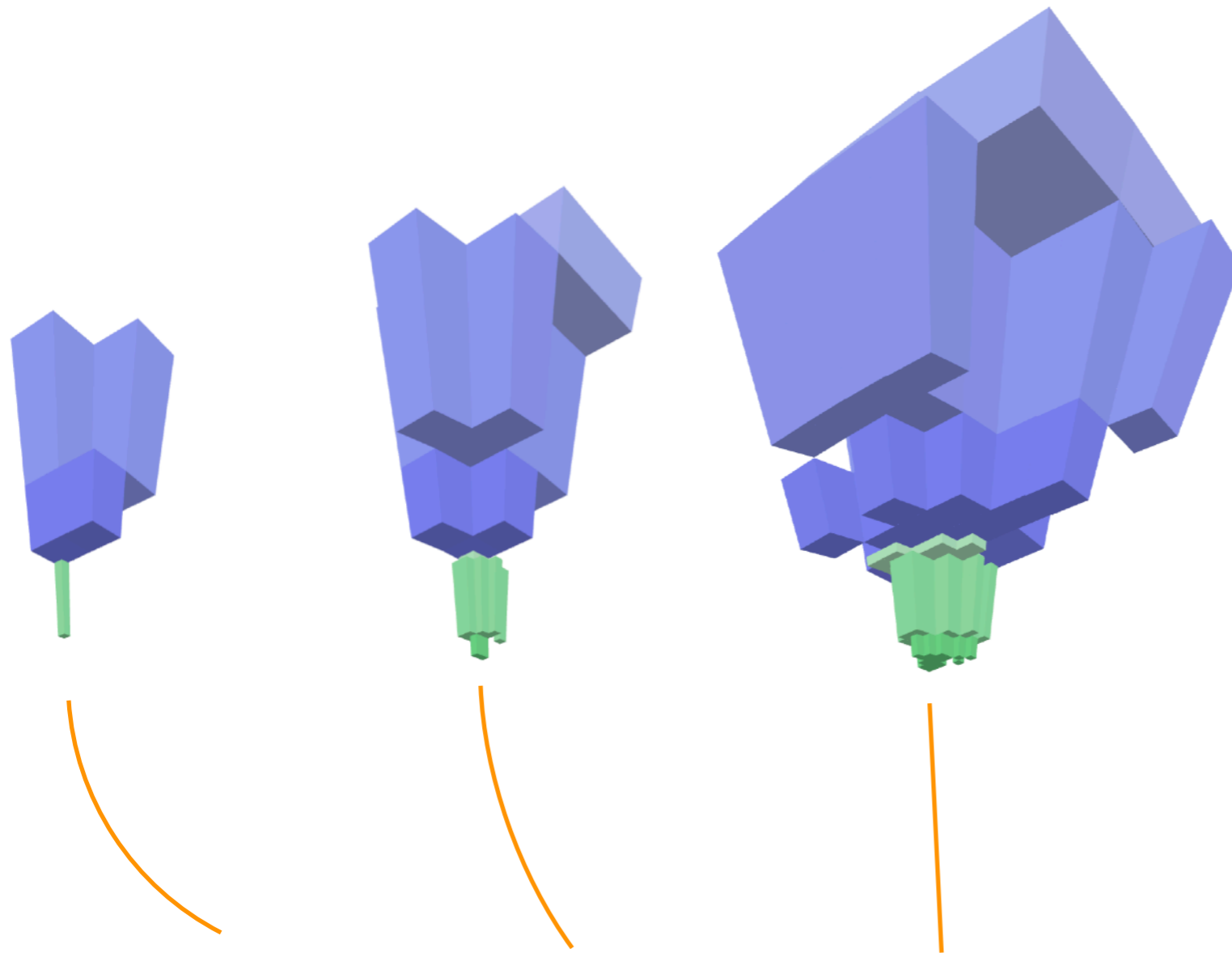
π^+

e^-

μ^-

All examples: ($E = 50$ GeV, $\eta = 0$)

Particle momentum regression

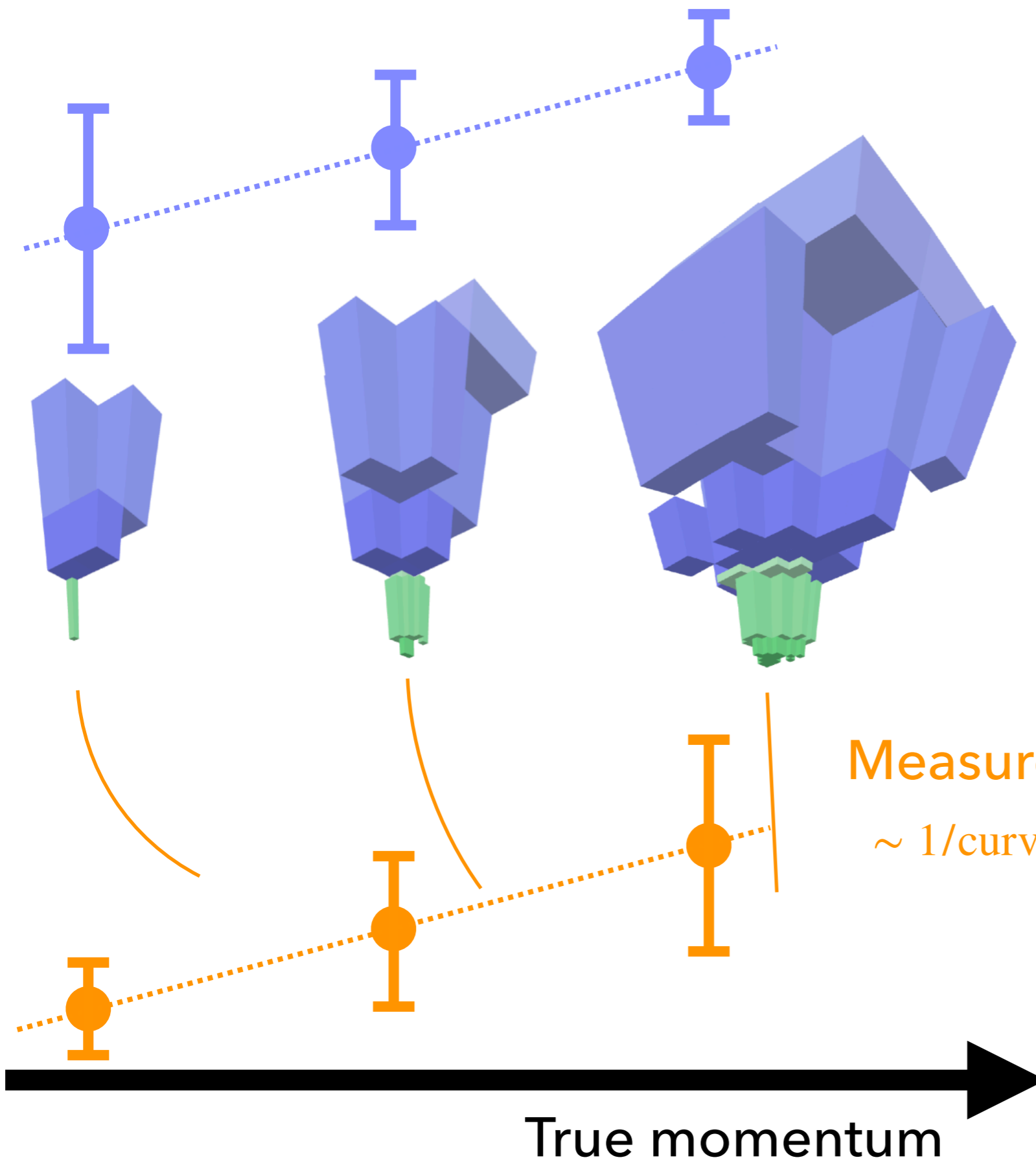


“Particle flow”

An algorithm that combines the information from both tracker and calorimeter to optimize the momentum prediction

True momentum 

Particle momentum regression



Measured momentum

$$\sim \sum_{\text{cells}} E_i$$

“Particle flow”

An algorithm that combines the information from both tracker and calorimeter to optimize the momentum prediction

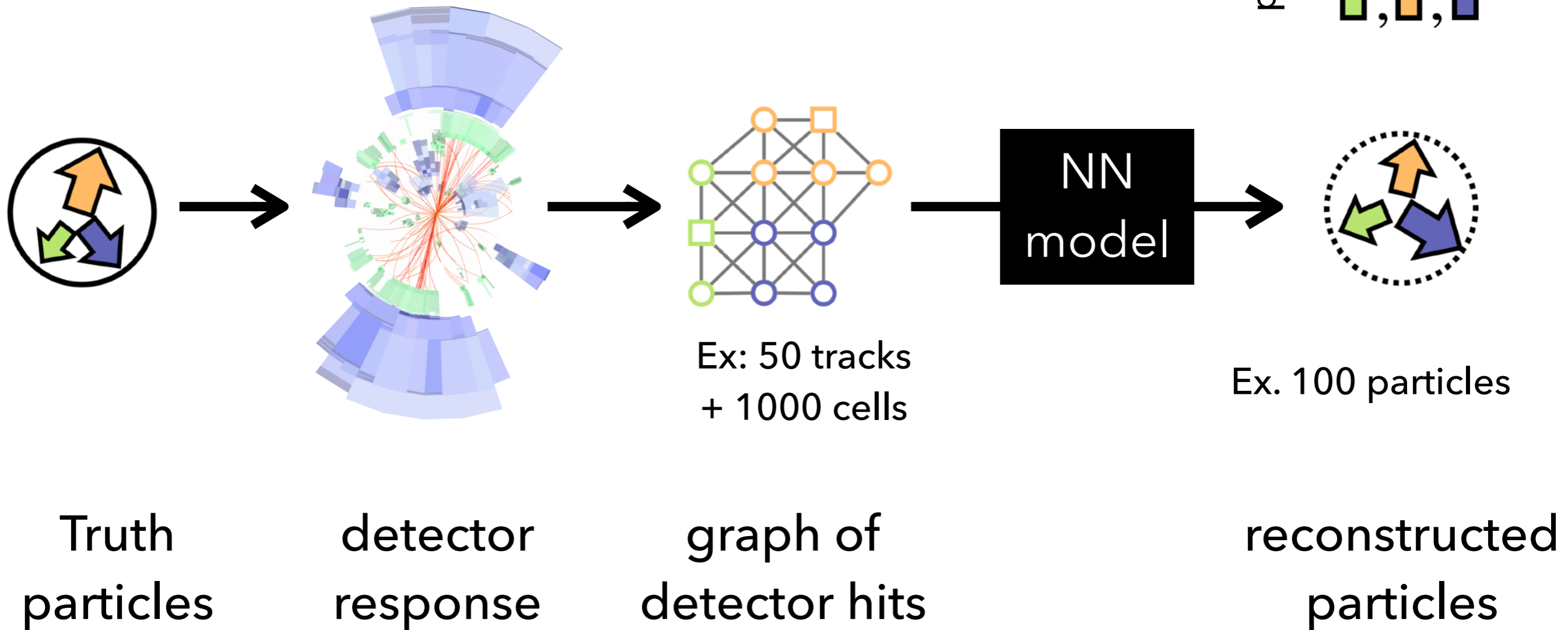
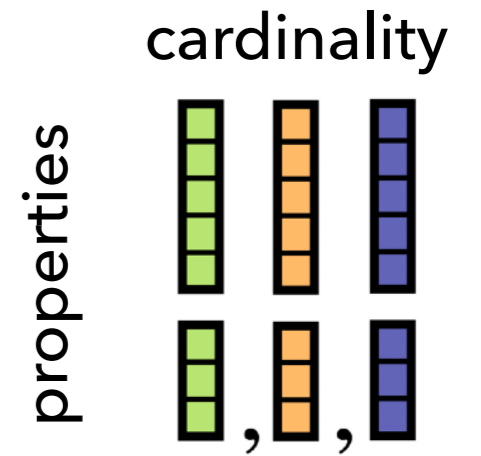
Measured momentum

$$\sim 1/\text{curvature}$$

True momentum

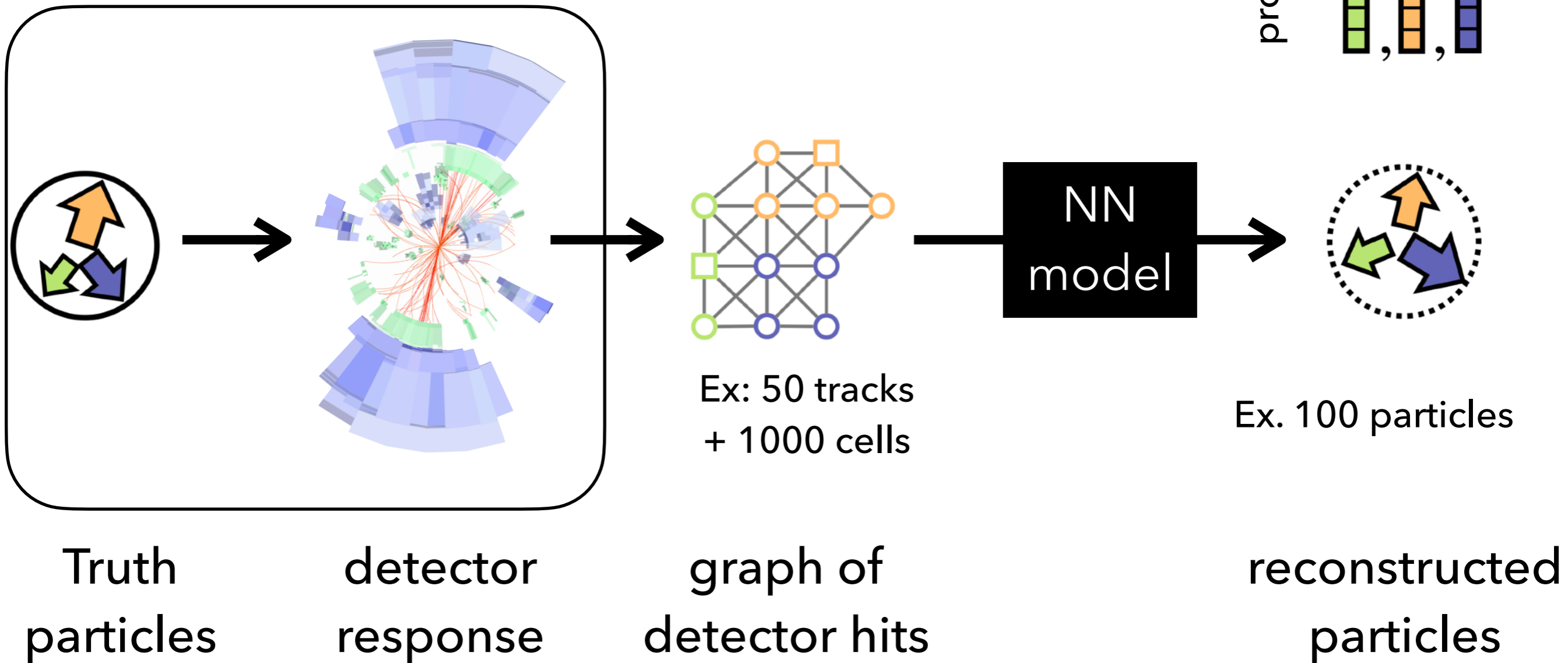
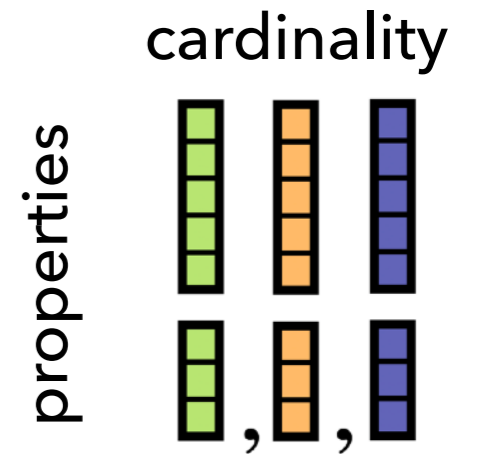
Part 2

Recent deep learning approaches



Part 2

Recent deep learning approaches



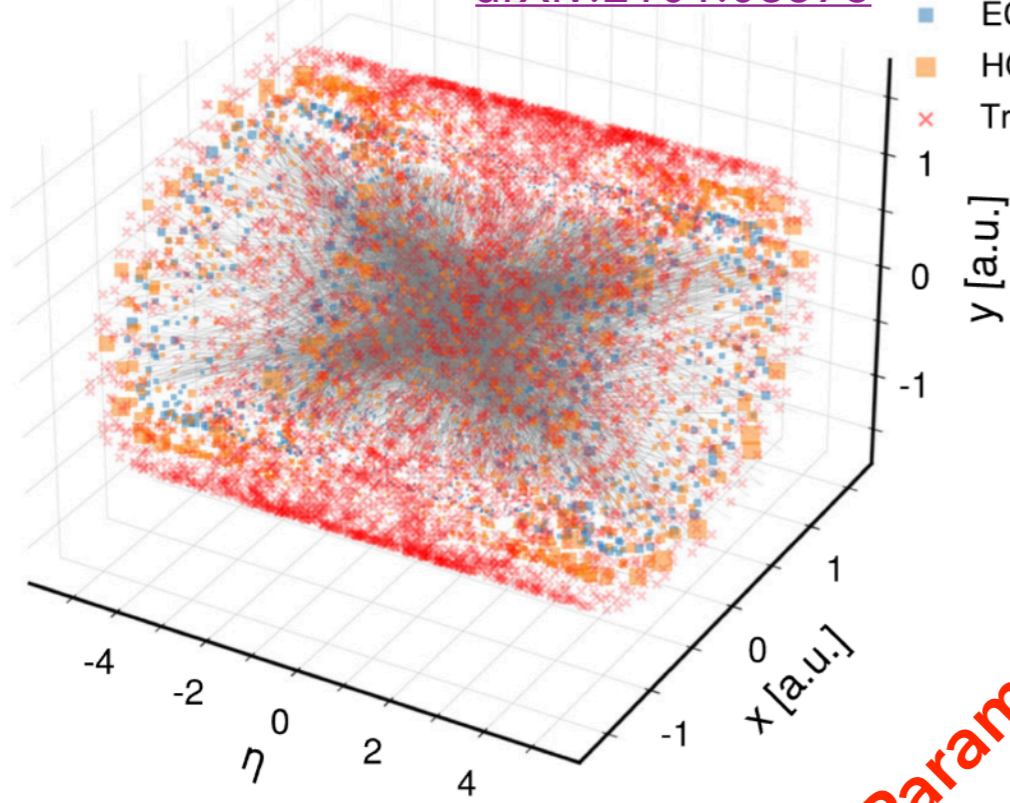
Delphes

[arXiv:1307.6346](https://arxiv.org/abs/1307.6346)

[arXiv:2101.08578](https://arxiv.org/abs/2101.08578)

$t\bar{t}$, 14 TeV, 200 PU

- Tracks
- ECAL clusters
- HCAL clusters
- × Truth particles



Parameterized

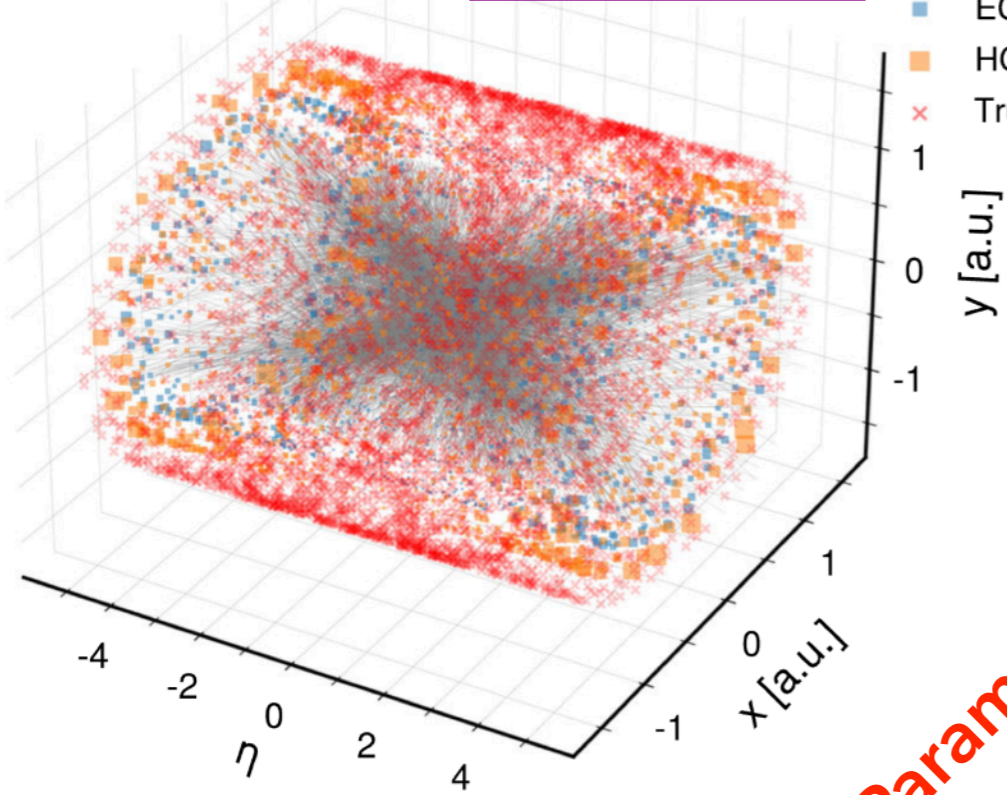
Datasets

[arXiv:2204.01681](https://arxiv.org/abs/2204.01681)

Delphes

[arXiv:1307.6346](https://arxiv.org/abs/1307.6346)
[arXiv:2101.08578](https://arxiv.org/abs/2101.08578)

$t\bar{t}$, 14 TeV, 200 PU
— Tracks
■ ECAL clusters
■ HCAL clusters
× Truth particles



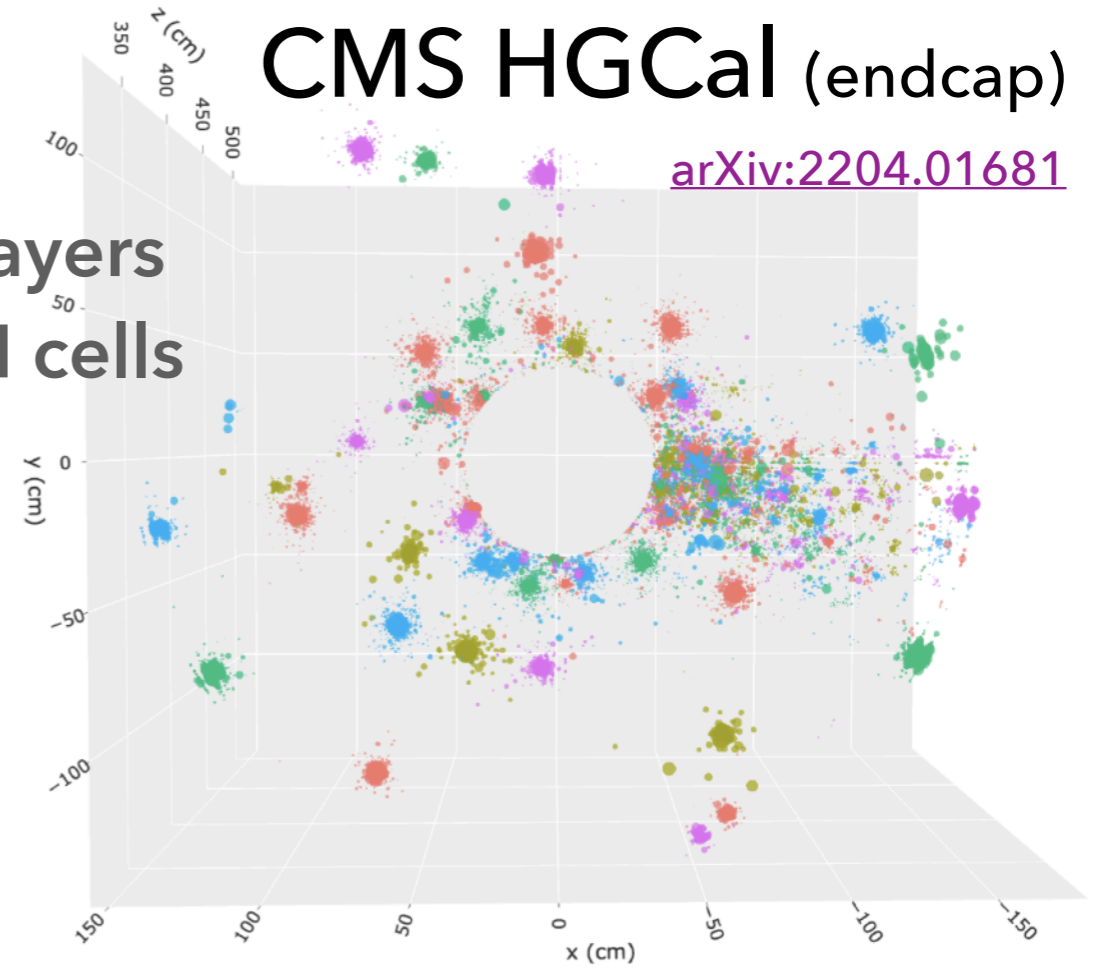
Parameterized
GEANT4

Datasets

CMS HGCal (endcap)

[arXiv:2204.01681](https://arxiv.org/abs/2204.01681)

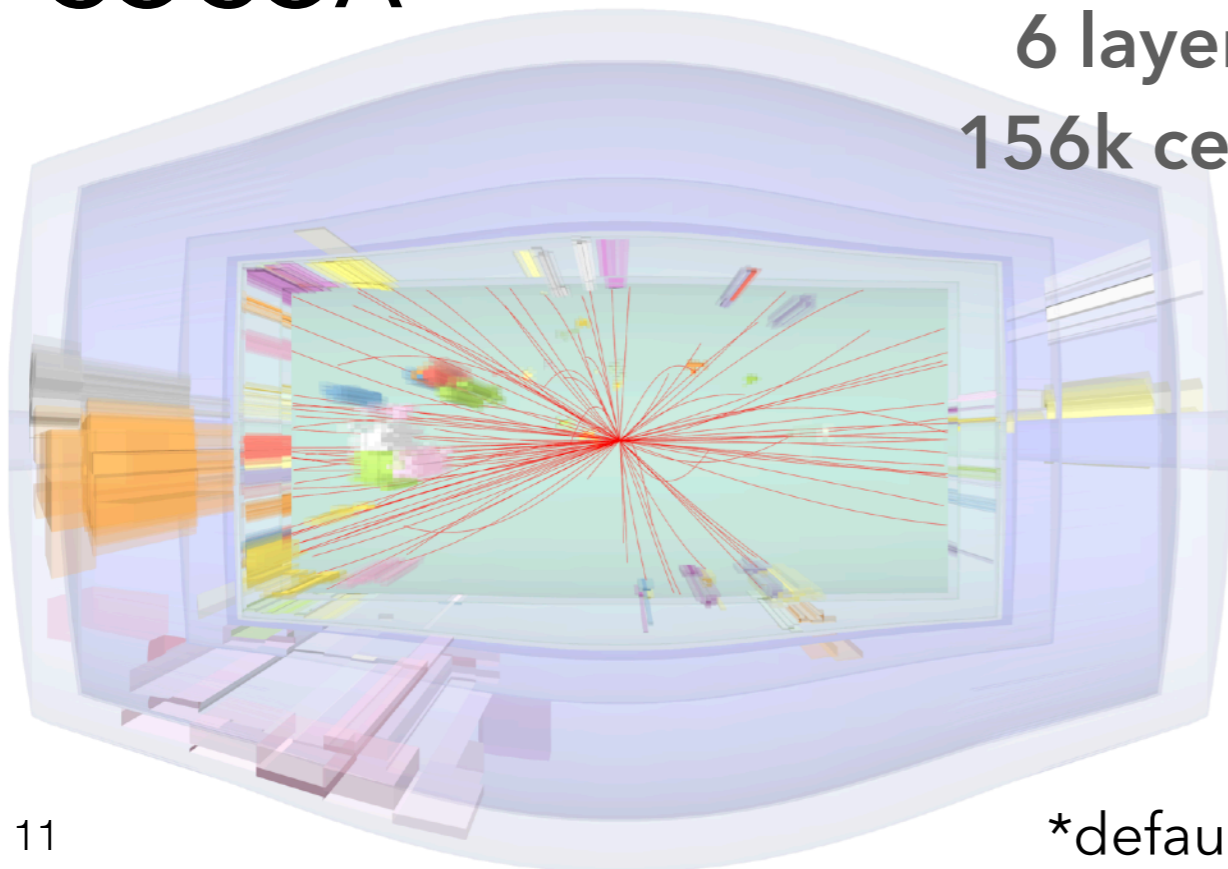
42 layers
1.5M cells



COCOA

[arXiv:2303.02101](https://arxiv.org/abs/2303.02101)

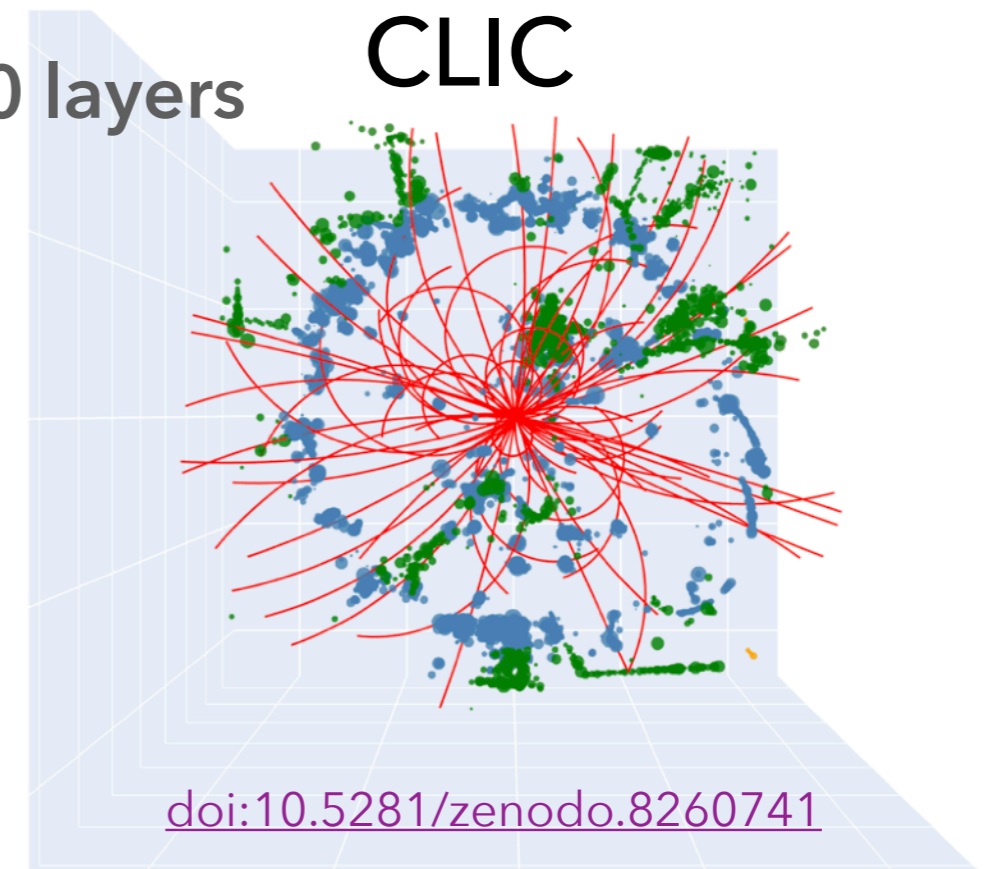
6 layers
156k cells*



100 layers

CLIC

[doi:10.5281/zenodo.8260741](https://doi.org/10.5281/zenodo.8260741)



Dimensionality reduction

Credit:

Example: topological clustering using ratio of signal to noise threshold

Marco Valente

		0		0					
		0	1	0	0	0			
			0	0	2	1	1		
		0	0	0	2	2	0	0	
	1	2	2	2	3	3	2	2	0
	0	2	2	3	6	2	2	1	0
		0	0	3	2	2	3	0	0
			0	0	2	2	2	2	1
				0	1	0	2	0	0
				0	0	0	0	0	

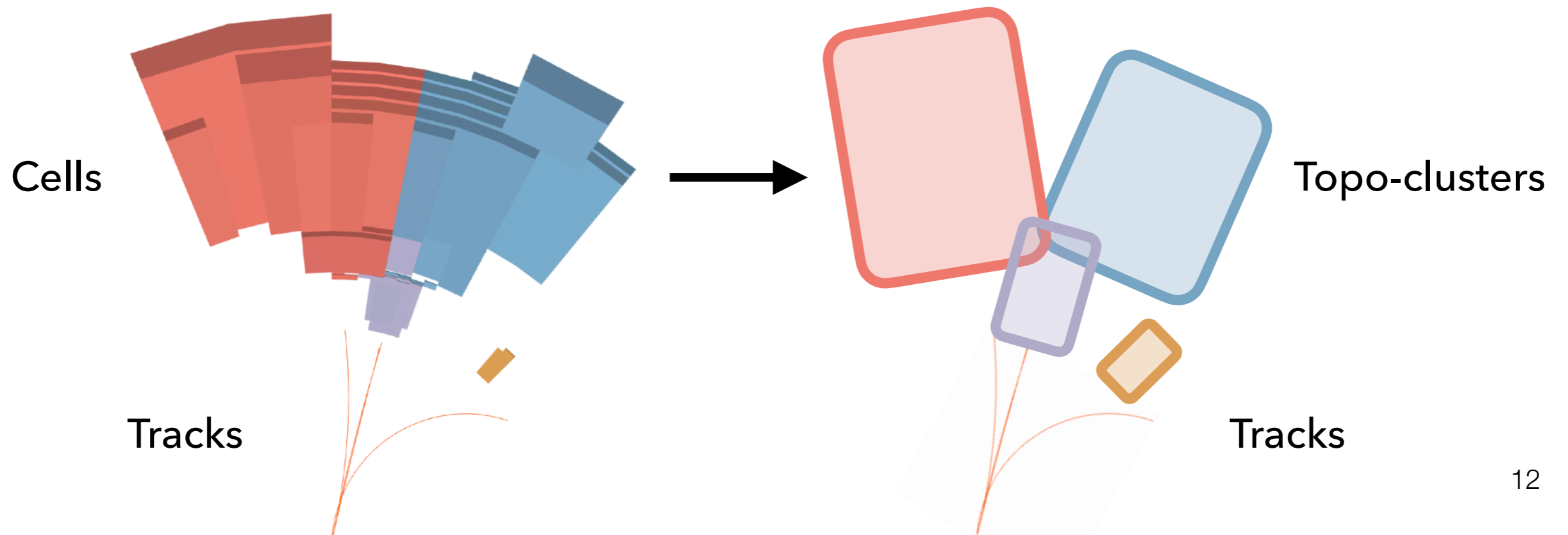
(a) Clustering of $|e_{\text{cell}}^{\text{EM}}| > 4$ cells.

		0		0					
		0	1	0	0	0			
			0	0	2	1	1		
		0	0	0	2	2	0	0	
	1	2	2	2	3	3	2	2	0
	0	2	2	3	6	2	2	1	0
		0	0	3	2	2	3	0	0
			0	0	2	2	2	2	1
				0	1	0	2	0	0
				0	0	0	0	0	

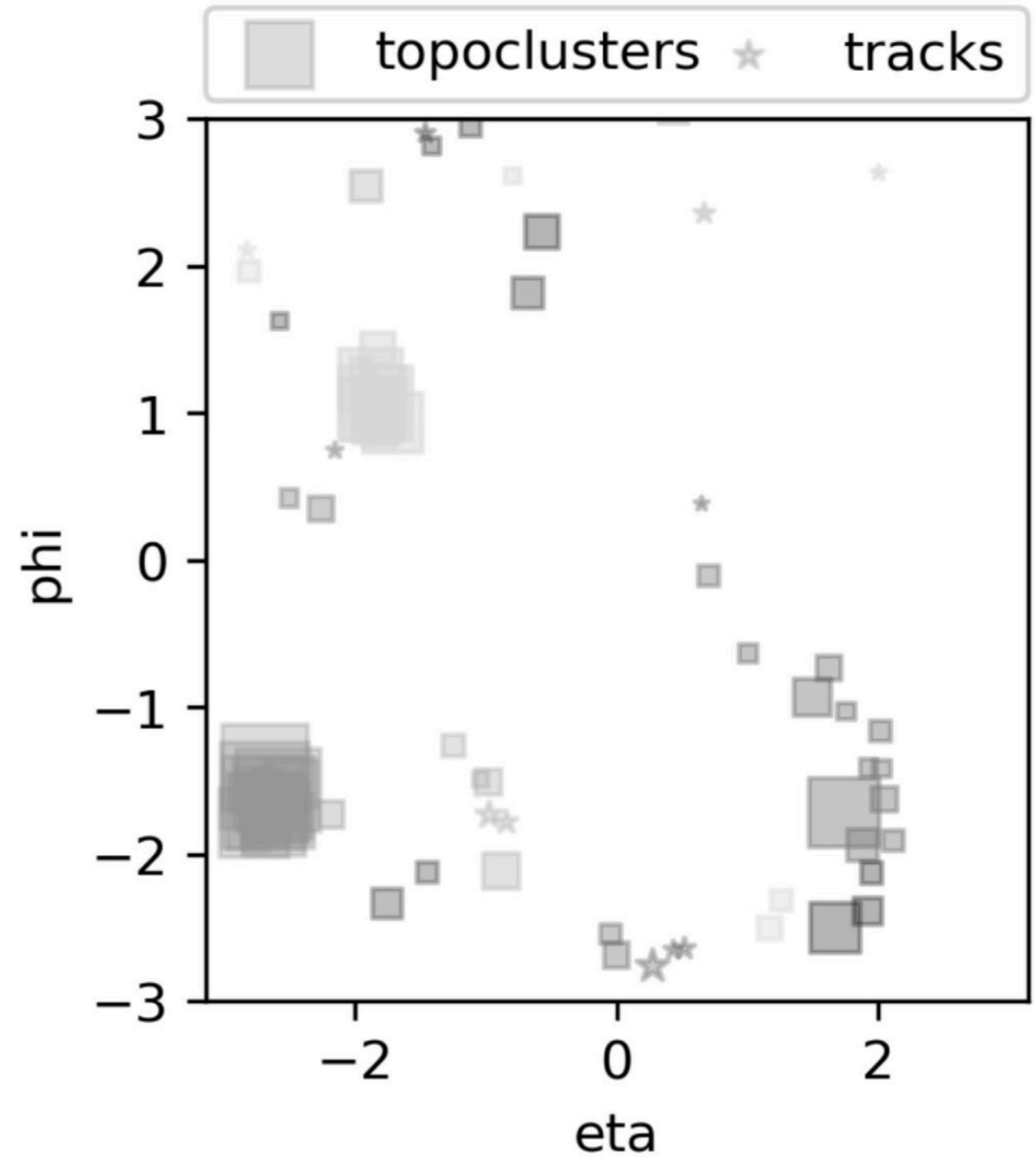
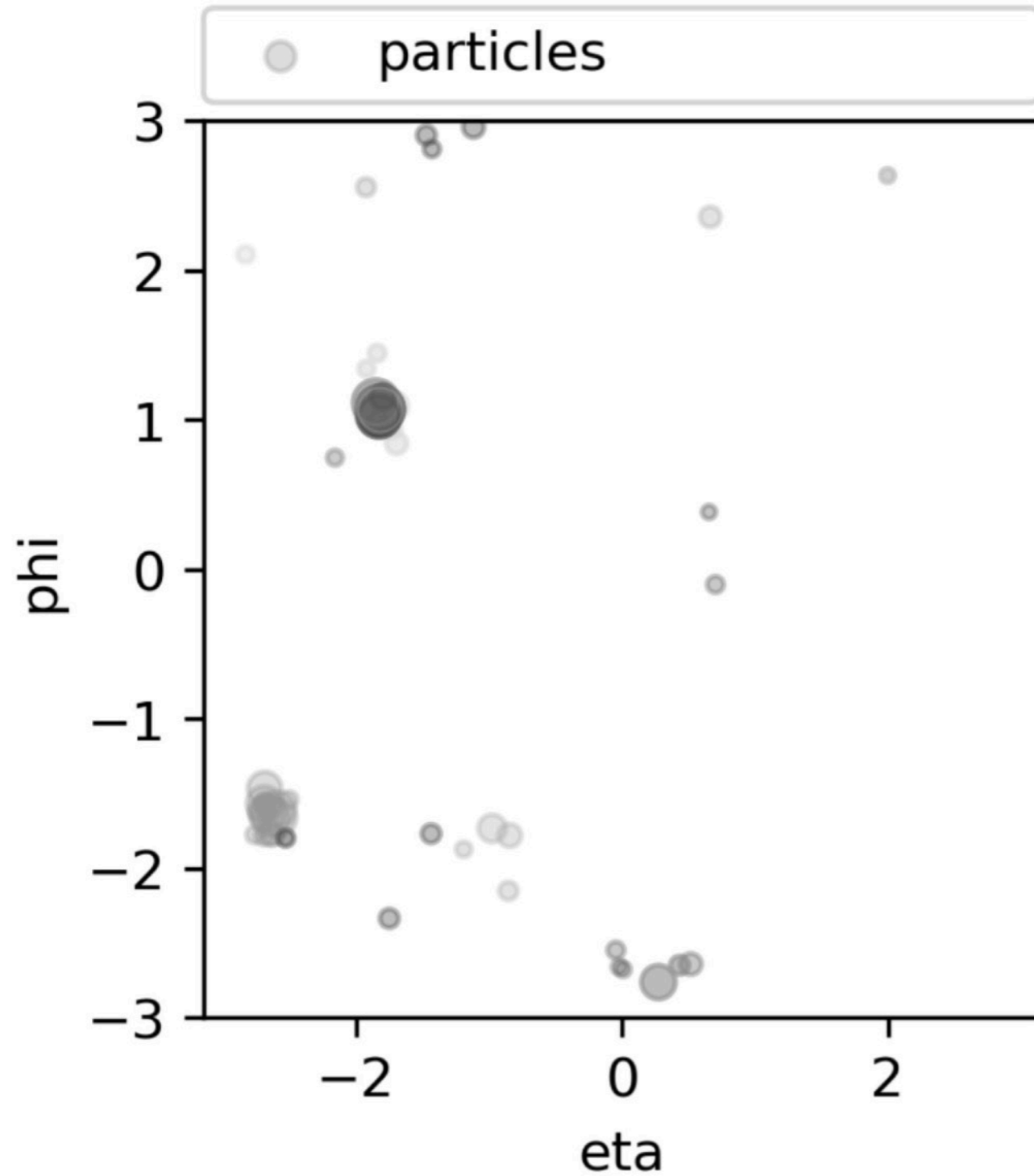
(b) Clustering of $|e_{\text{cell}}^{\text{EM}}| > 2$ cells.

			0		0					
			0	1	0	0	0			
				0	0	2	1	1		
			0	0	0	2	2	0	0	
			0	0	0	2	2	0	0	
	1	2	2	2	3	3	2	2	0	
	0	2	2	3	6	2	2	1	0	
			0	0	3	2	2	3	0	0
				0	0	2	2	2	2	1
					0	1	0	2	0	0
					0	0	0	0	0	

(c) Clustering of $|e_{\text{cell}}^{\text{EM}}| > 0$ cells.

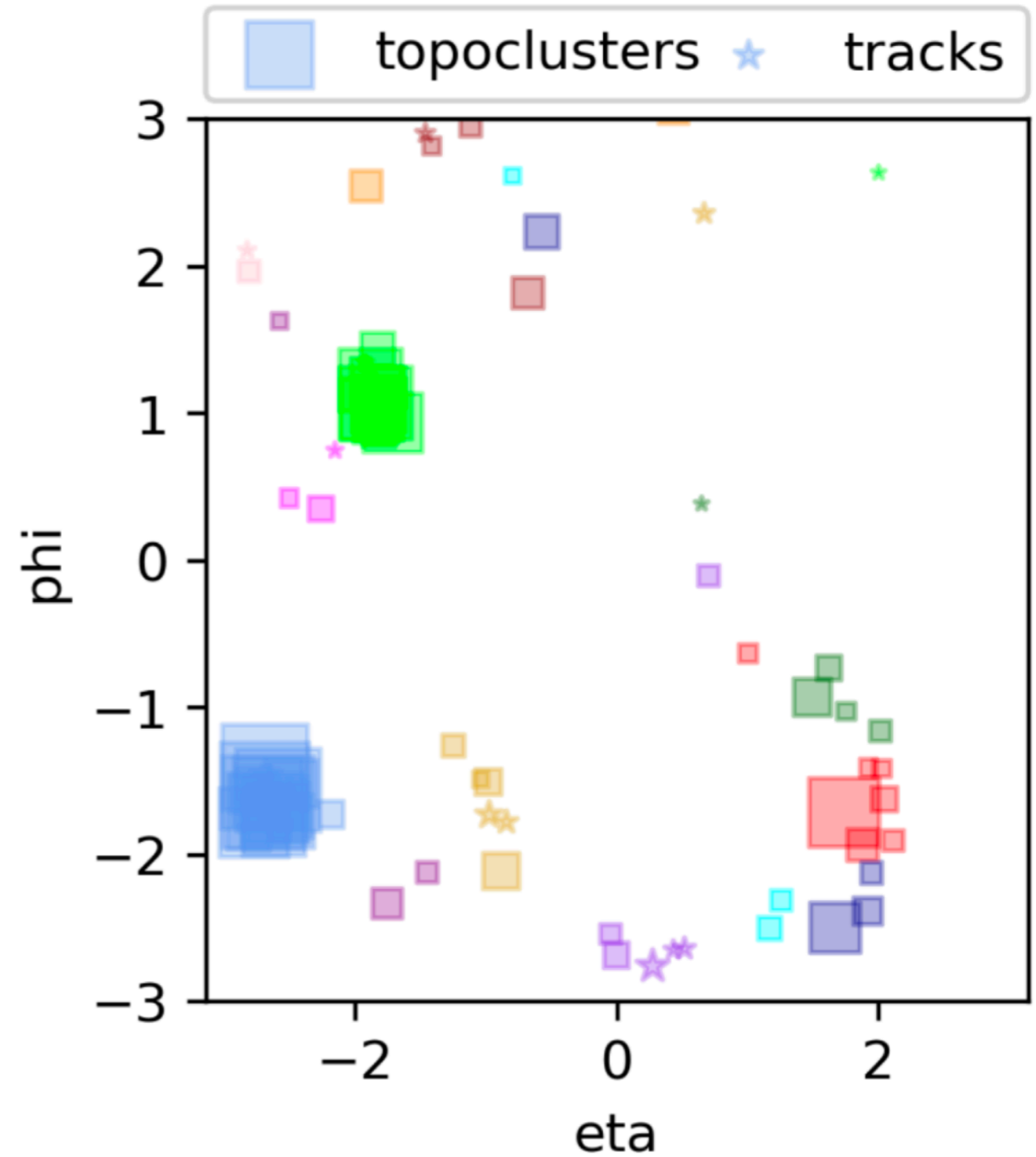
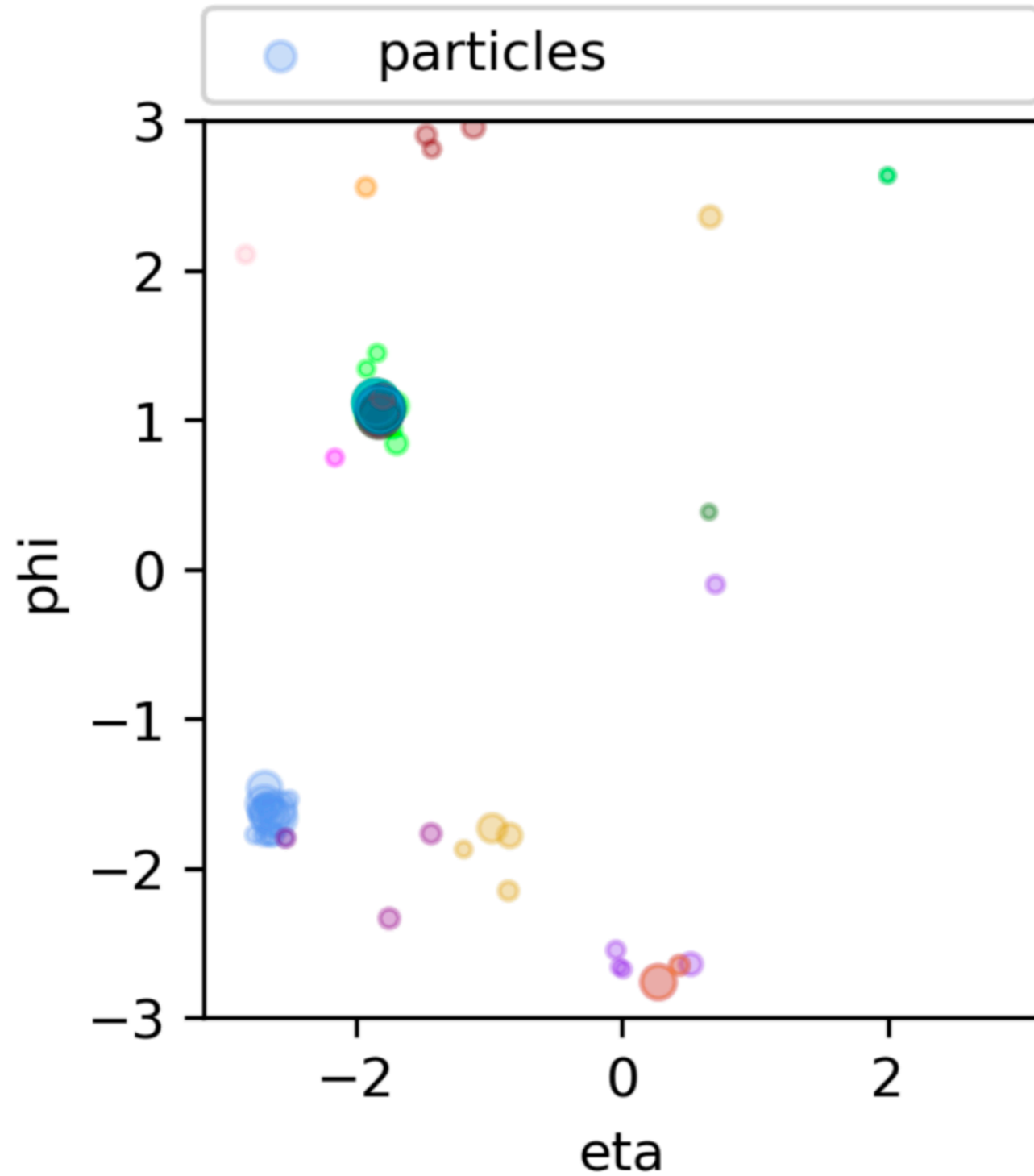


Aside: Event partitioning



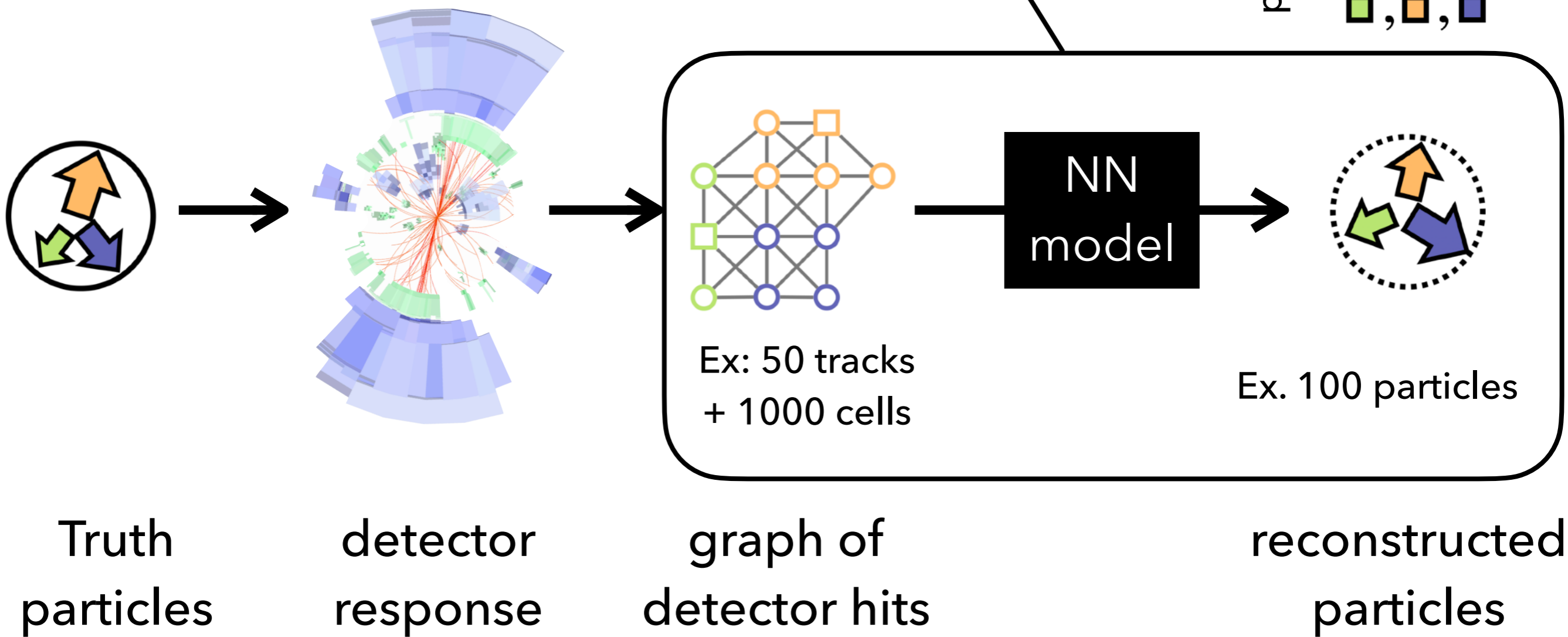
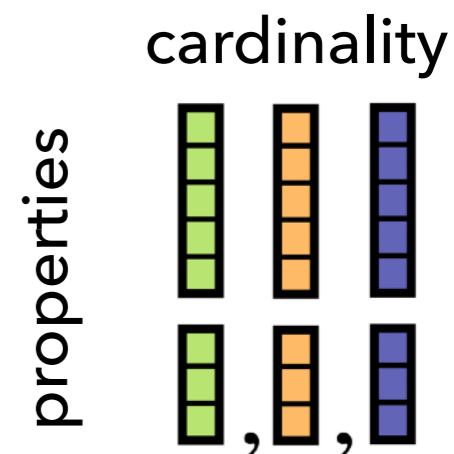
Credit: Nilotpall Kakati (more details next week at ML4Jets)

Aside: Event partitioning



Credit: Nilotpal Kakati (more details next week at ML4Jets)

Set-to-set (graph) problem



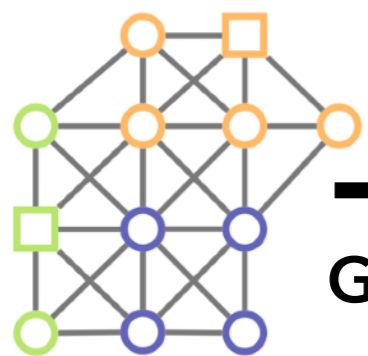
Set-to-set approaches

(graph)



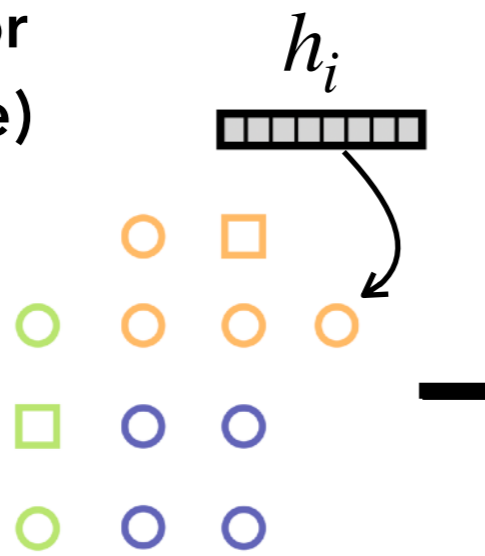
Truth particles

(Detector response)



GNN

graph of
detector hits



set of node
representations

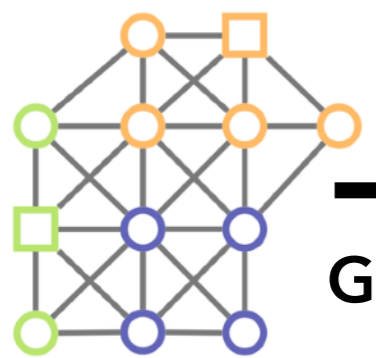
Set-to-set approaches (graph)

approaches



Truth particles

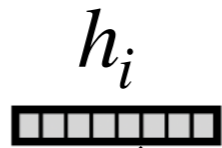
(Detector response)



GNN

graph of detector hits

set of node representations

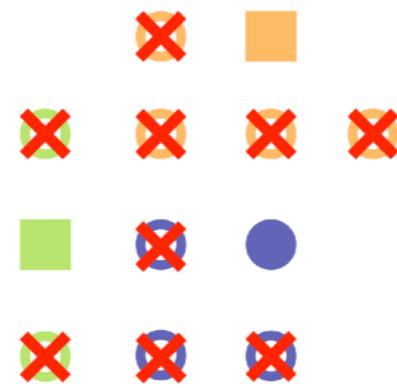


[1] [arXiv:2101.08578](https://arxiv.org/abs/2101.08578)

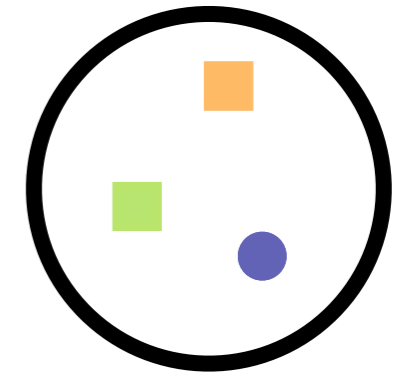
[2] [arXiv:2002.03605](https://arxiv.org/abs/2002.03605)

[3] [arXiv:2212.01328](https://arxiv.org/abs/2212.01328)

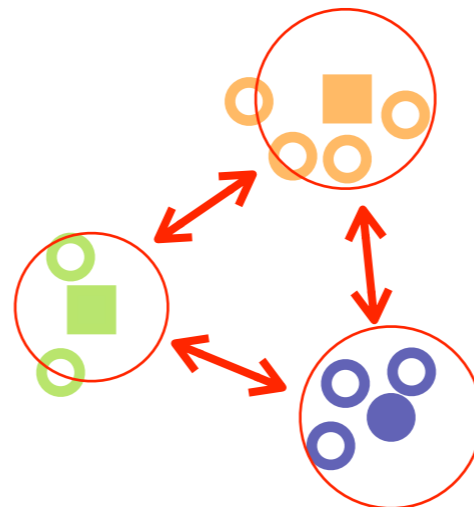
MLPF [1]



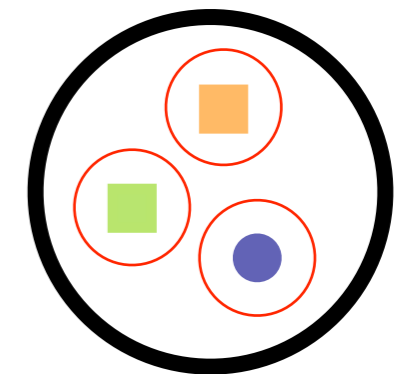
Nodes classified as particles



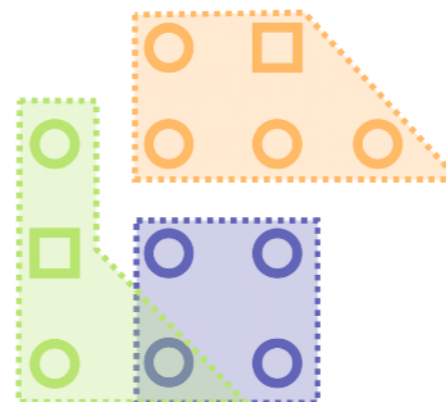
Object condensation [2]



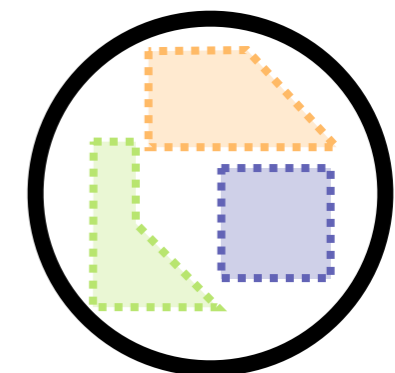
Cluster centers & neighbors



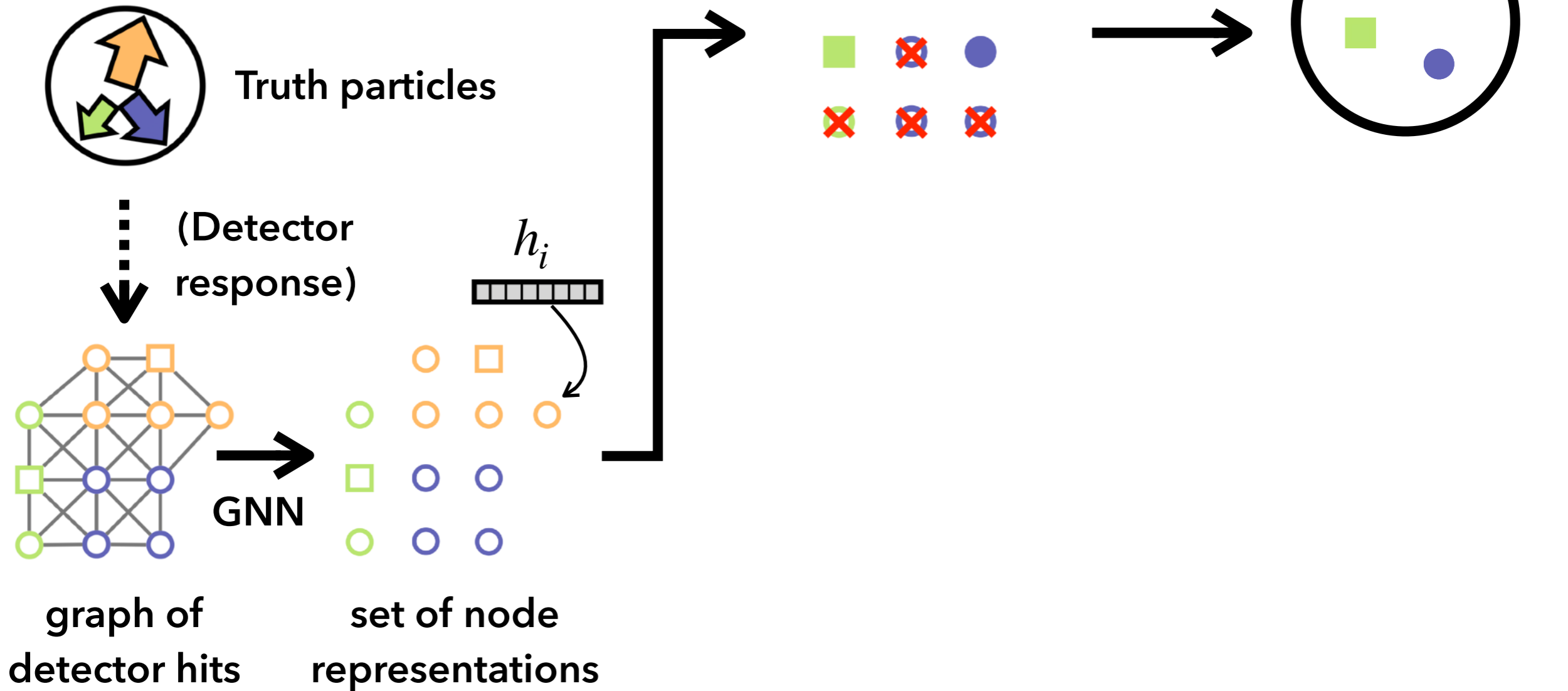
HGPflow [3]



Hyperedges with score > threshold



Set-to-set approaches (graph) approaches



[1] [arXiv:2101.08578](https://arxiv.org/abs/2101.08578)

[2] [arXiv:2002.03605](https://arxiv.org/abs/2002.03605)

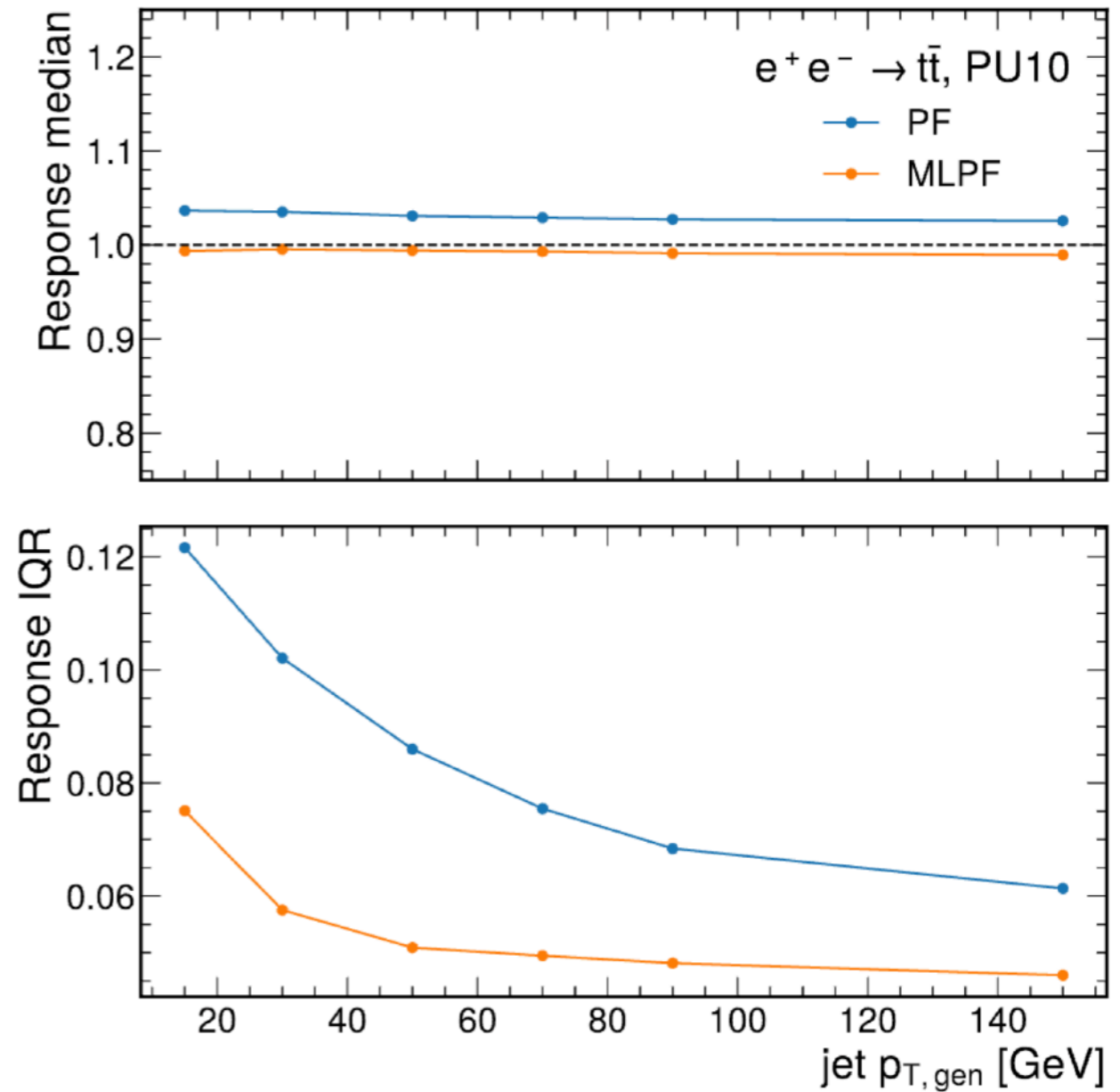
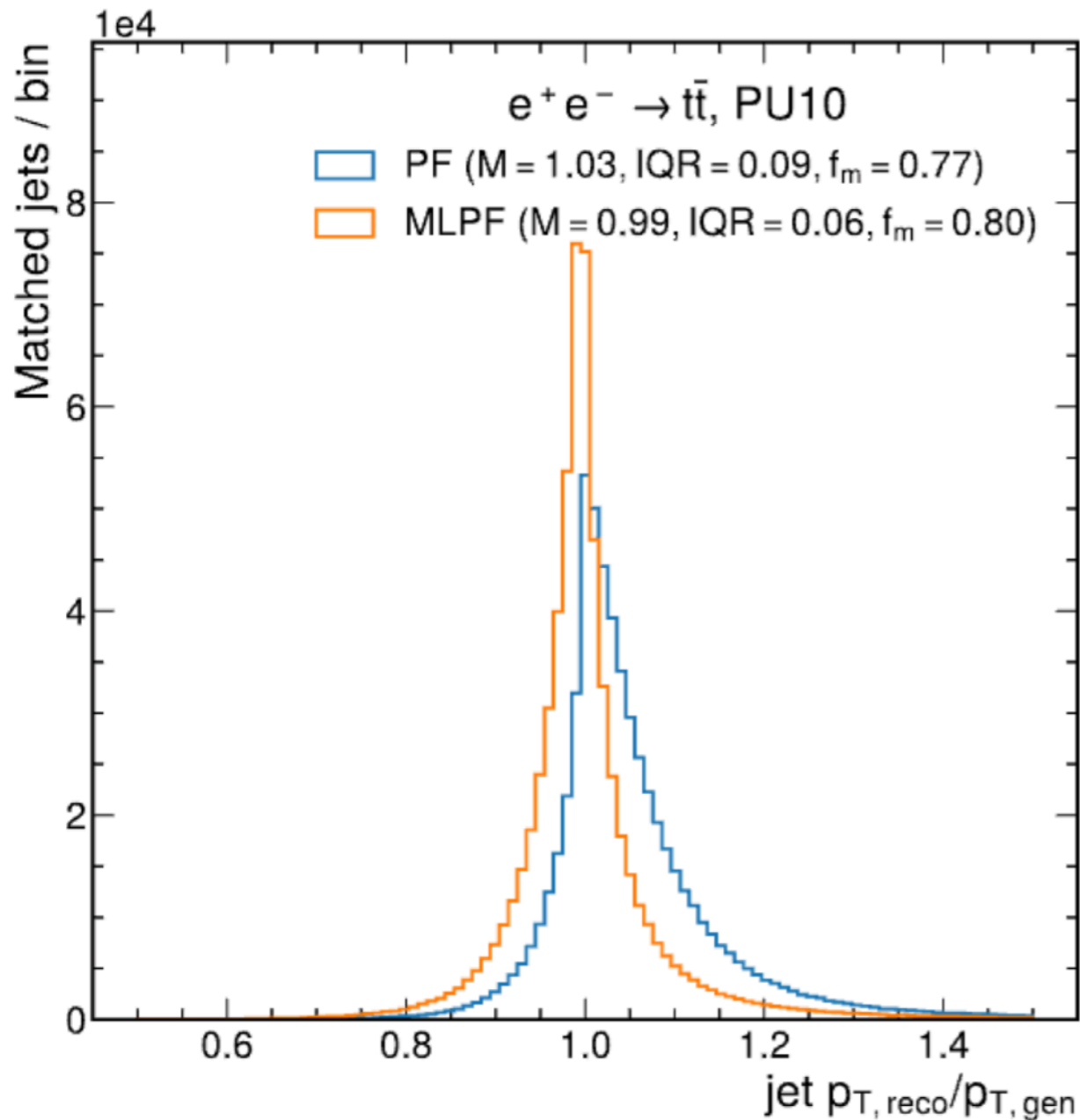
[3] [arXiv:2212.01328](https://arxiv.org/abs/2212.01328)

MLPF jet-level improvement

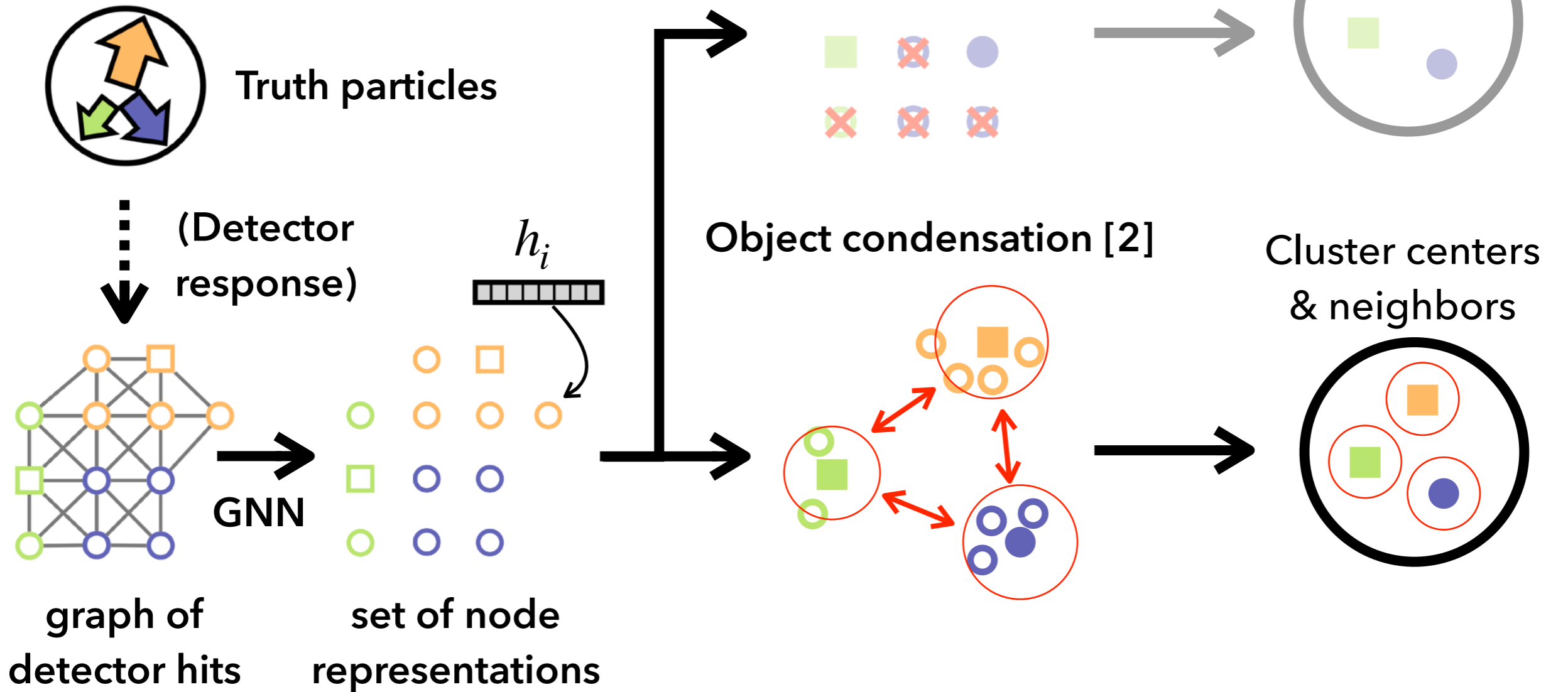
[arXiv:2309.06782](https://arxiv.org/abs/2309.06782)

Jet (transverse) momentum ratio

Median, IQR of distribution vs. momentum



Set-to-set approaches (graph) approaches



[1] [arXiv:2101.08578](https://arxiv.org/abs/2101.08578)

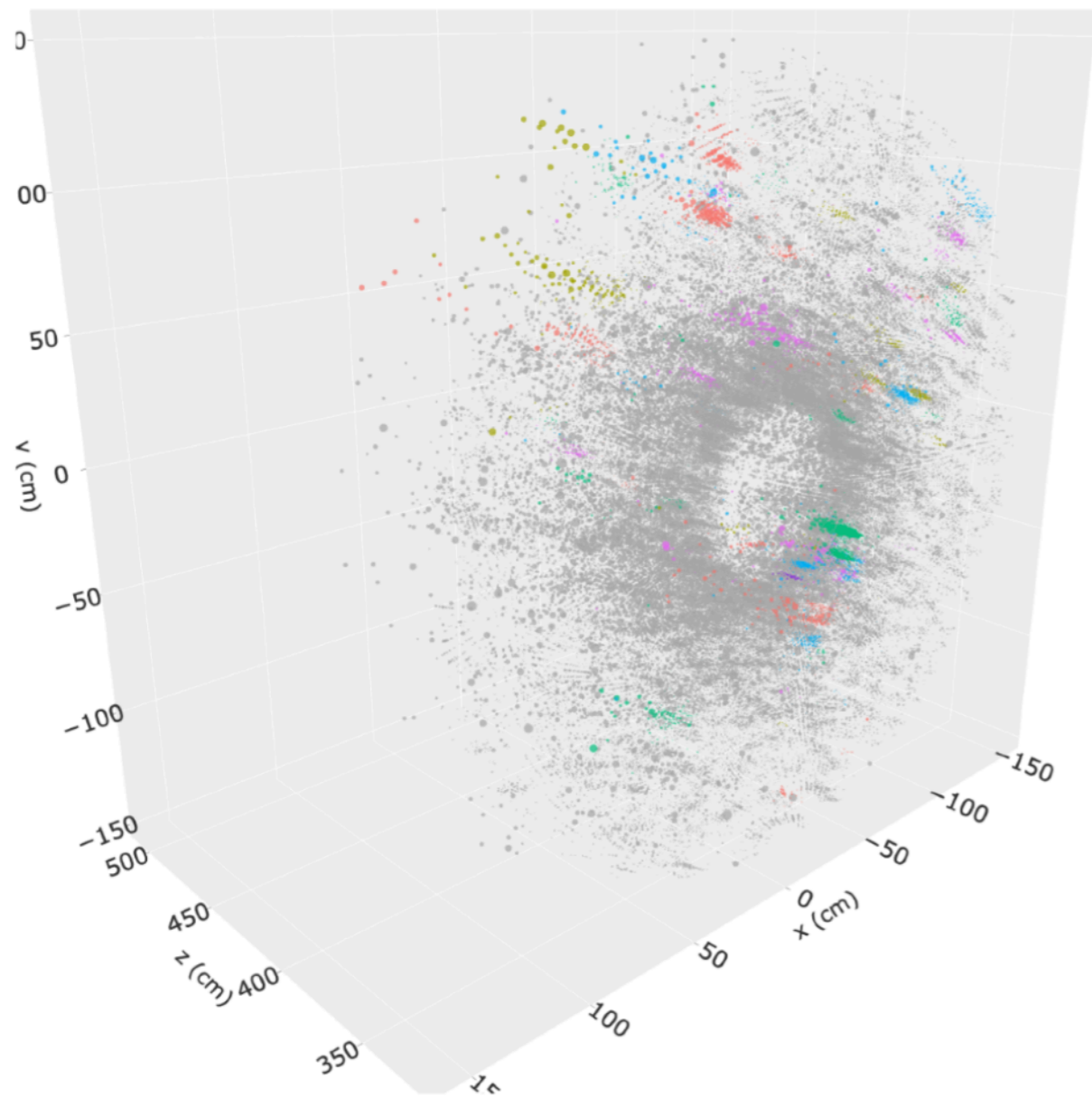
[2] [arXiv:2002.03605](https://arxiv.org/abs/2002.03605)

[3] [arXiv:2212.01328](https://arxiv.org/abs/2212.01328)

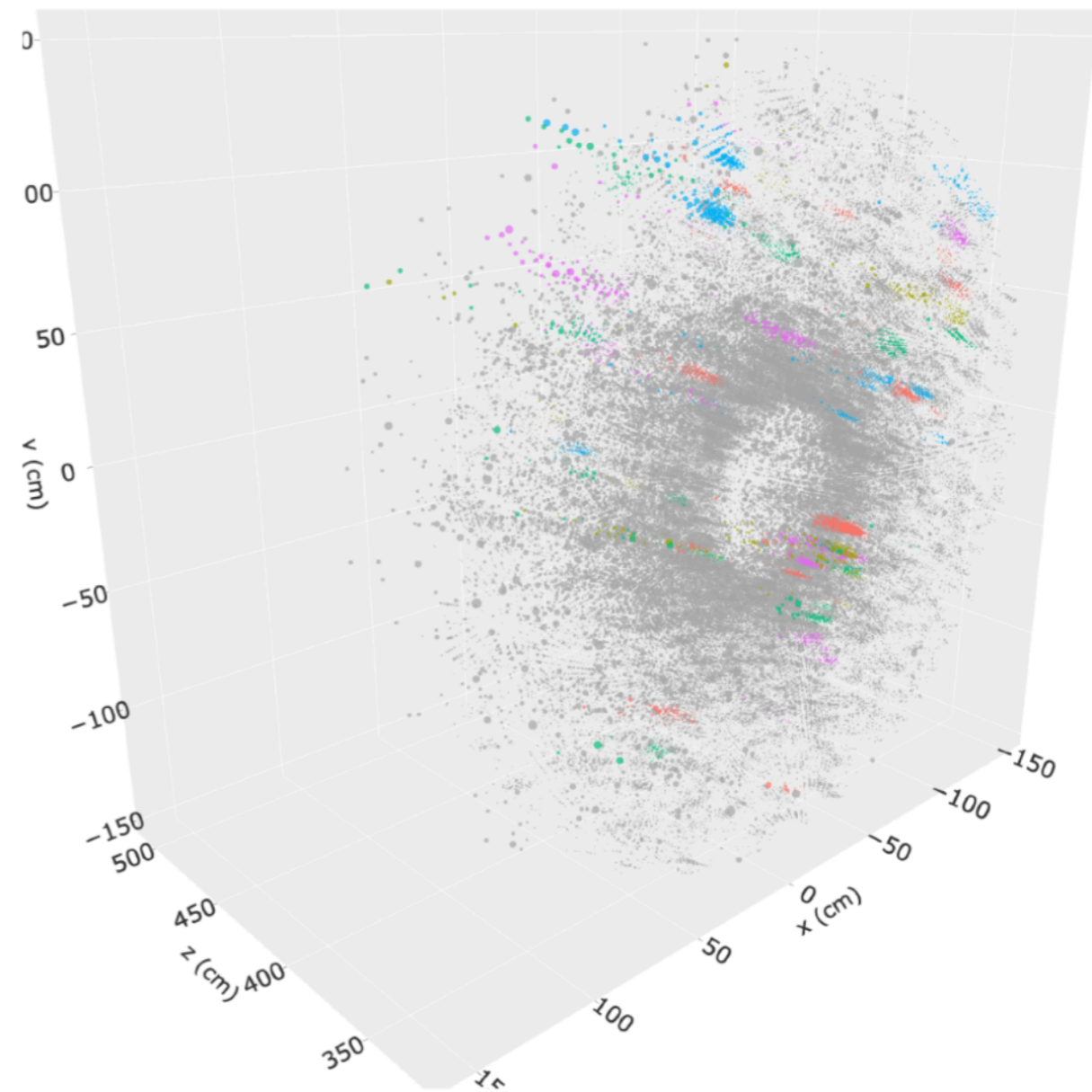
Showers in CMS HGCAL (endcap)

[arXiv:2204.01681](https://arxiv.org/abs/2204.01681)

**Truth particle showers (color)
+ 200 pileup**



**Reconstructed showers
using Object Condensation**



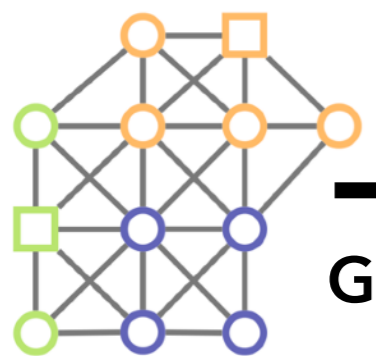
Set-to-set approaches (graph)

approaches



Truth particles

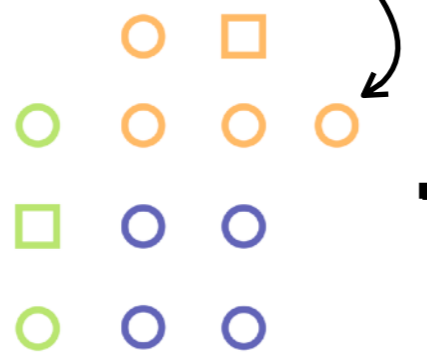
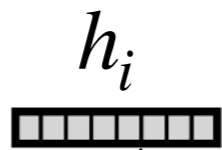
(Detector response)



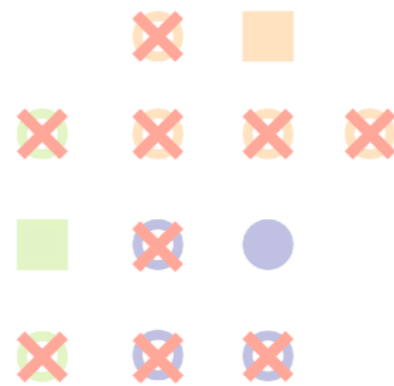
GNN

graph of detector hits

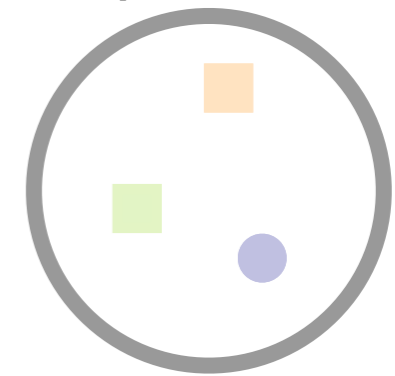
set of node representations



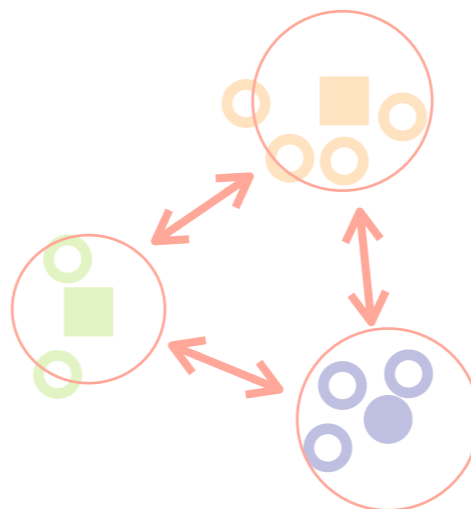
MLPF [1]



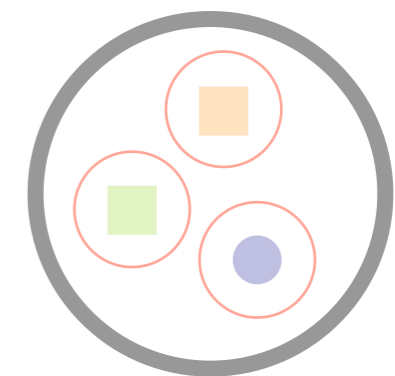
Nodes classified as particles



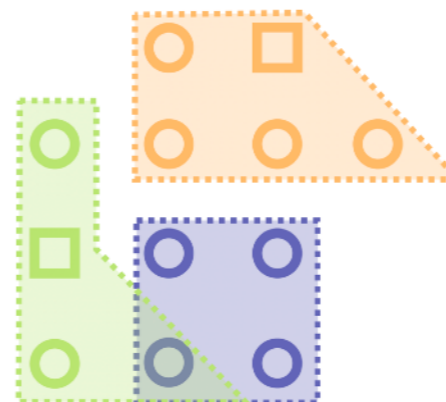
Object condensation [2]



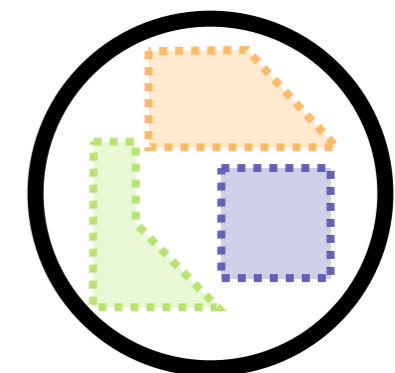
Cluster centers & neighbors



HGPflow [3]



Hyperedges with score > threshold



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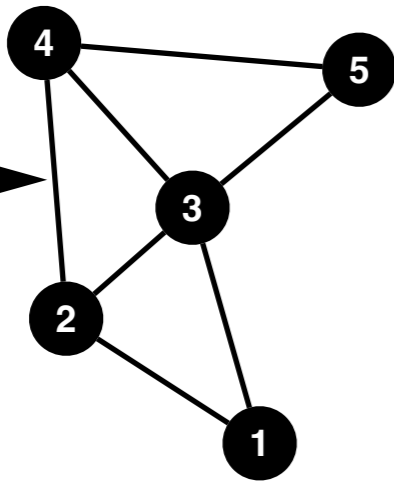
[2] [arXiv:2002.03605](https://arxiv.org/abs/2002.03605)

[3] [arXiv:2212.01328](https://arxiv.org/abs/2212.01328)

What is a hypergraph?

Graph

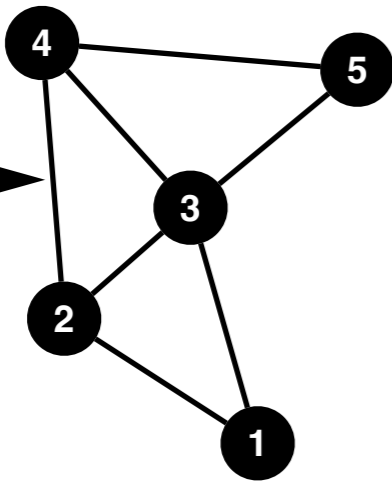
edges
connect
2 nodes



What is a hypergraph?

Graph

edges
connect
2 nodes

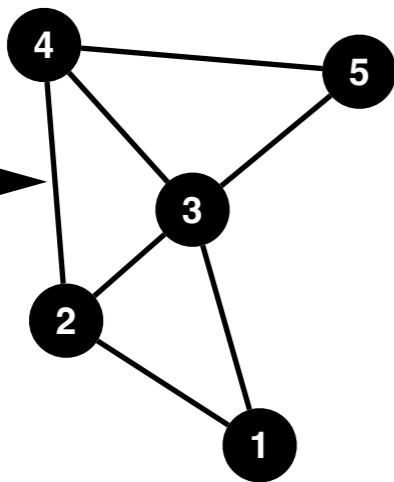


Adjacency matrix

$$\begin{matrix} & \begin{matrix} \textcircled{1} & \textcircled{2} & \textcircled{3} & \textcircled{4} & \textcircled{5} \end{matrix} \\ \begin{matrix} \textcircled{1} \\ \textcircled{2} \\ \textcircled{3} \\ \textcircled{4} \\ \textcircled{5} \end{matrix} & \begin{pmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{pmatrix} \end{matrix} \quad (N \times N)$$

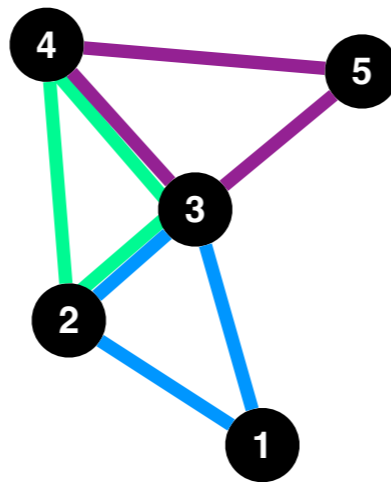
What is a hypergraph?

Graph



edges
connect
2 nodes

Hypergraph

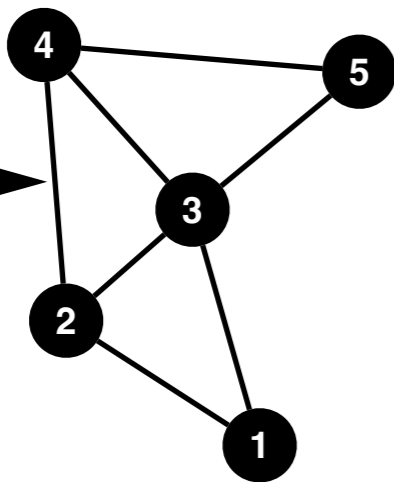


Adjacency matrix

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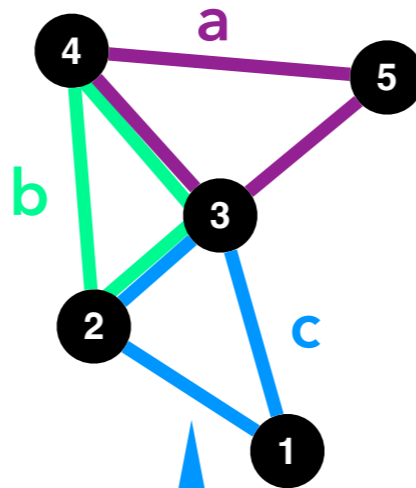
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Graph



edges connect 2 nodes

Hypergraph



hyperedges connect ≥ 1 nodes

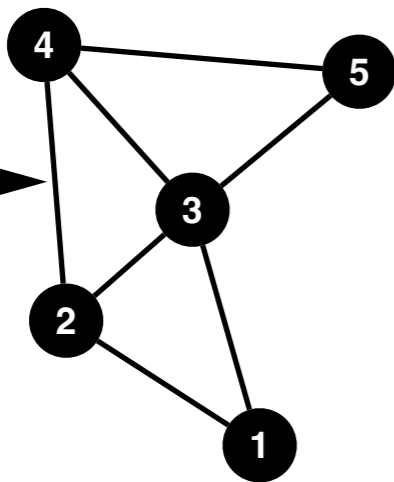
Adjacency matrix

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$(N \times N)$

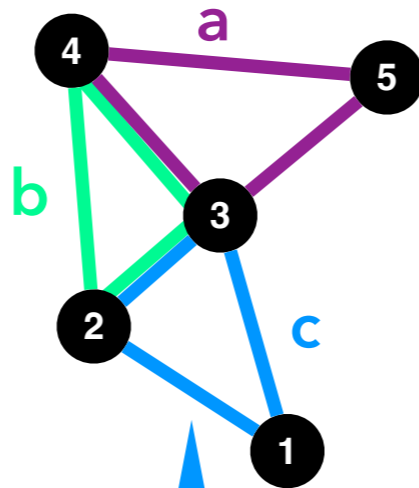
What is a hypergraph?

Graph



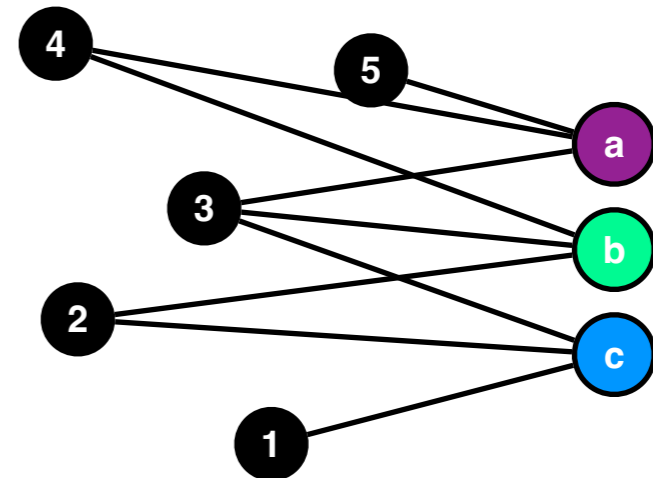
edges connect 2 nodes

Hypergraph



hyperedges connect ≥ 1 nodes

Bipartite graph



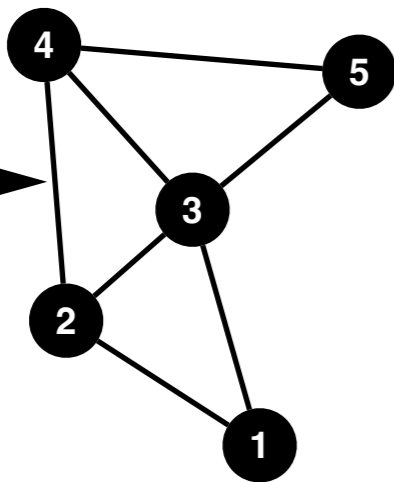
Adjacency matrix

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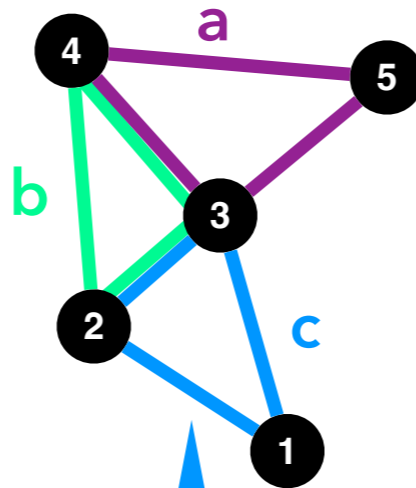
What is a hypergraph?

Graph



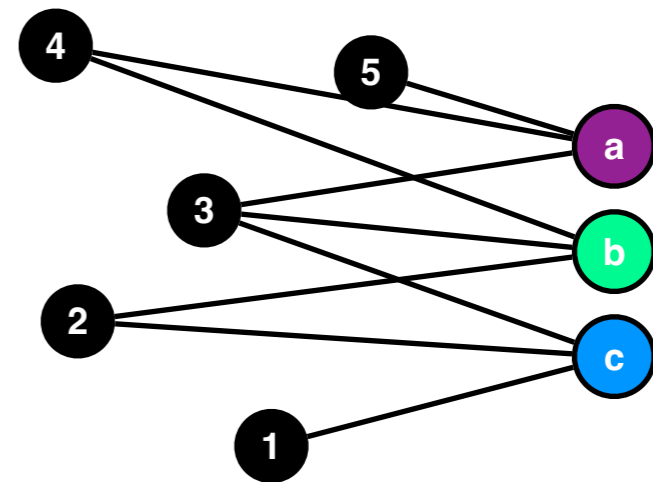
edges connect 2 nodes

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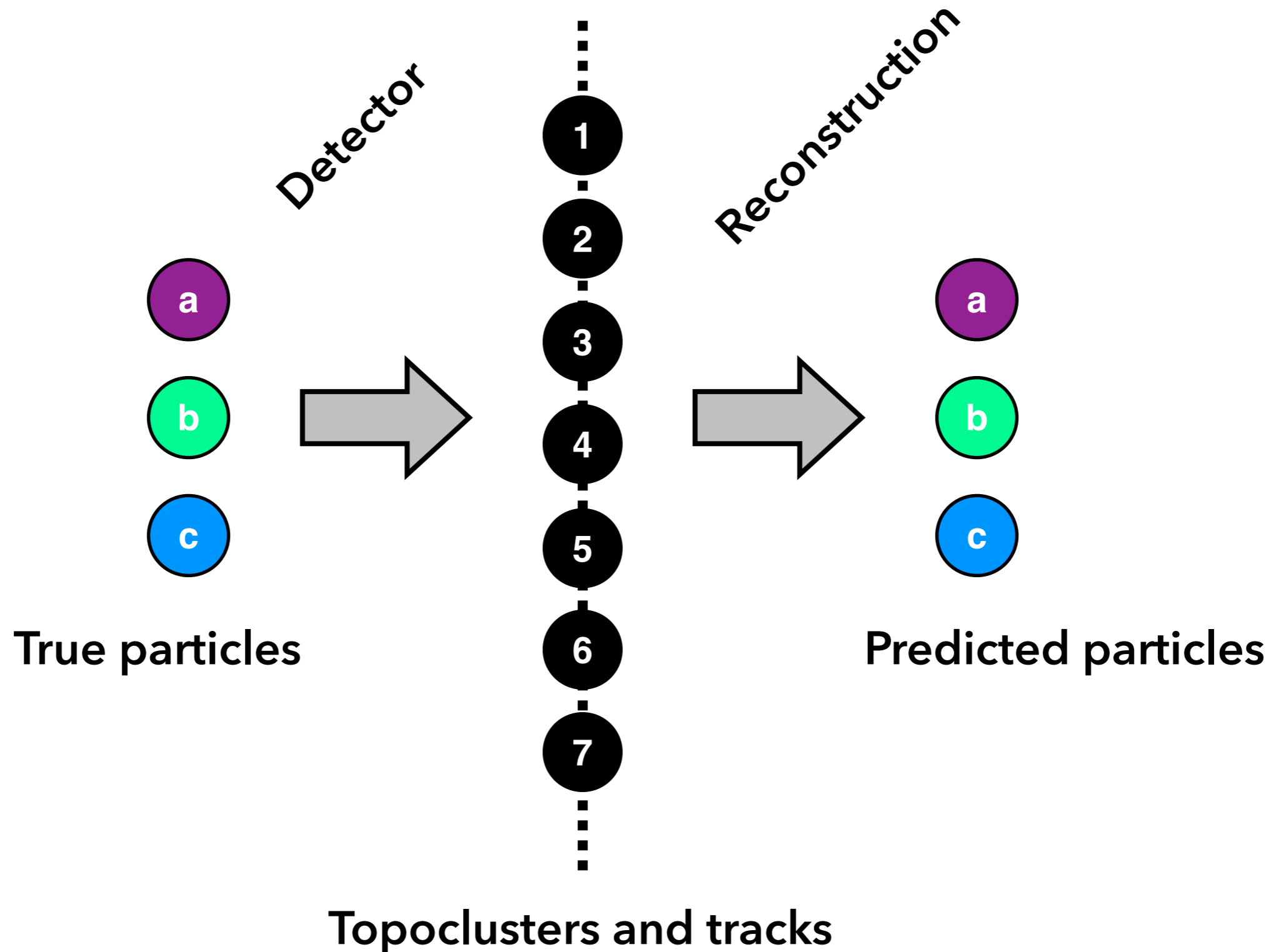
Incidence matrix

$$\begin{matrix} & \begin{matrix} \textcircled{a} & \textcircled{b} & \textcircled{c} \end{matrix} \\ \begin{matrix} \textcircled{1} \\ \textcircled{2} \\ \textcircled{3} \\ \textcircled{4} \\ \textcircled{5} \end{matrix} & \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix} \end{matrix}$$

$(N \times H)$

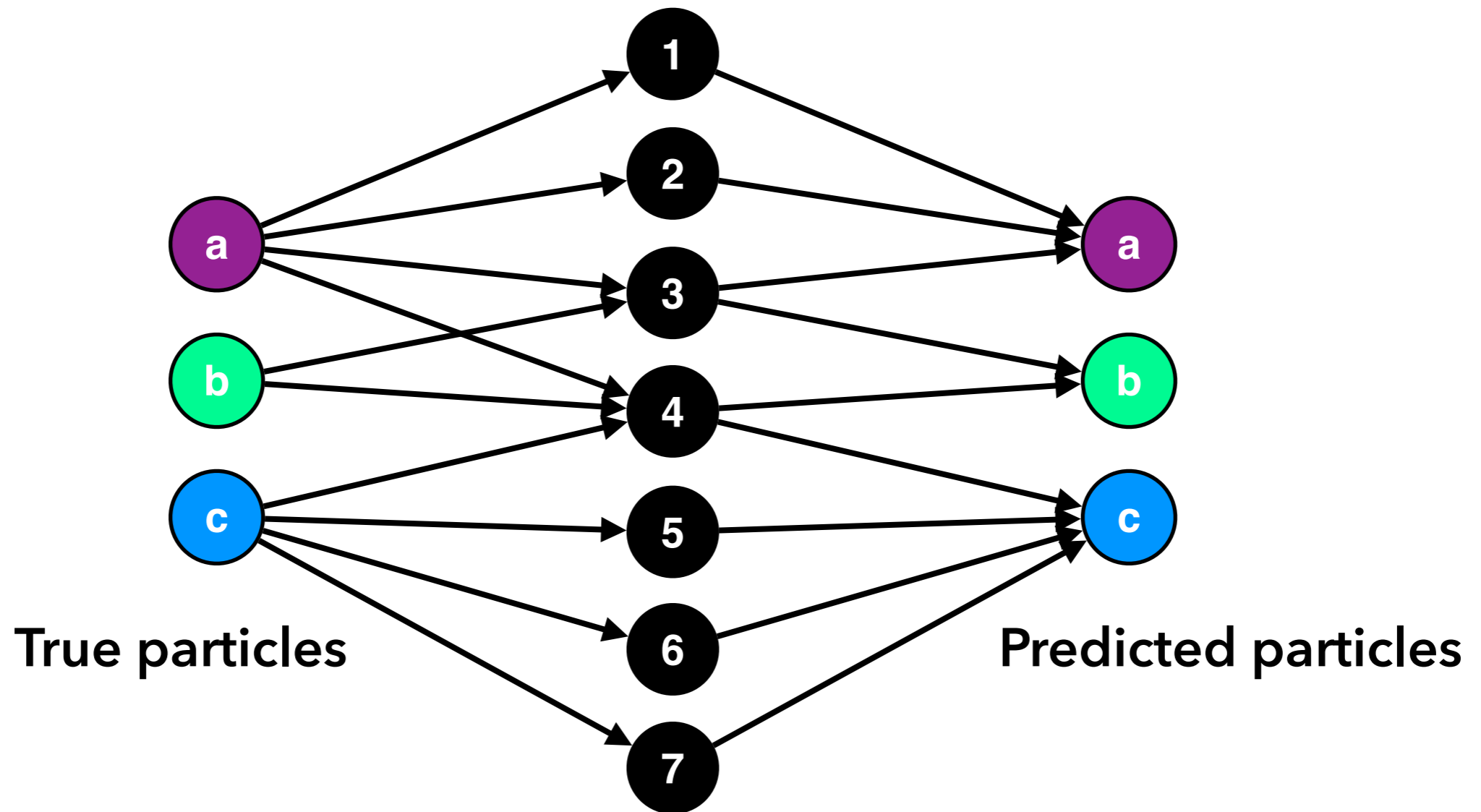
Why use a hypergraph?

cartoon from [Nilotpal Kakati](#)



Why use a hypergraph?

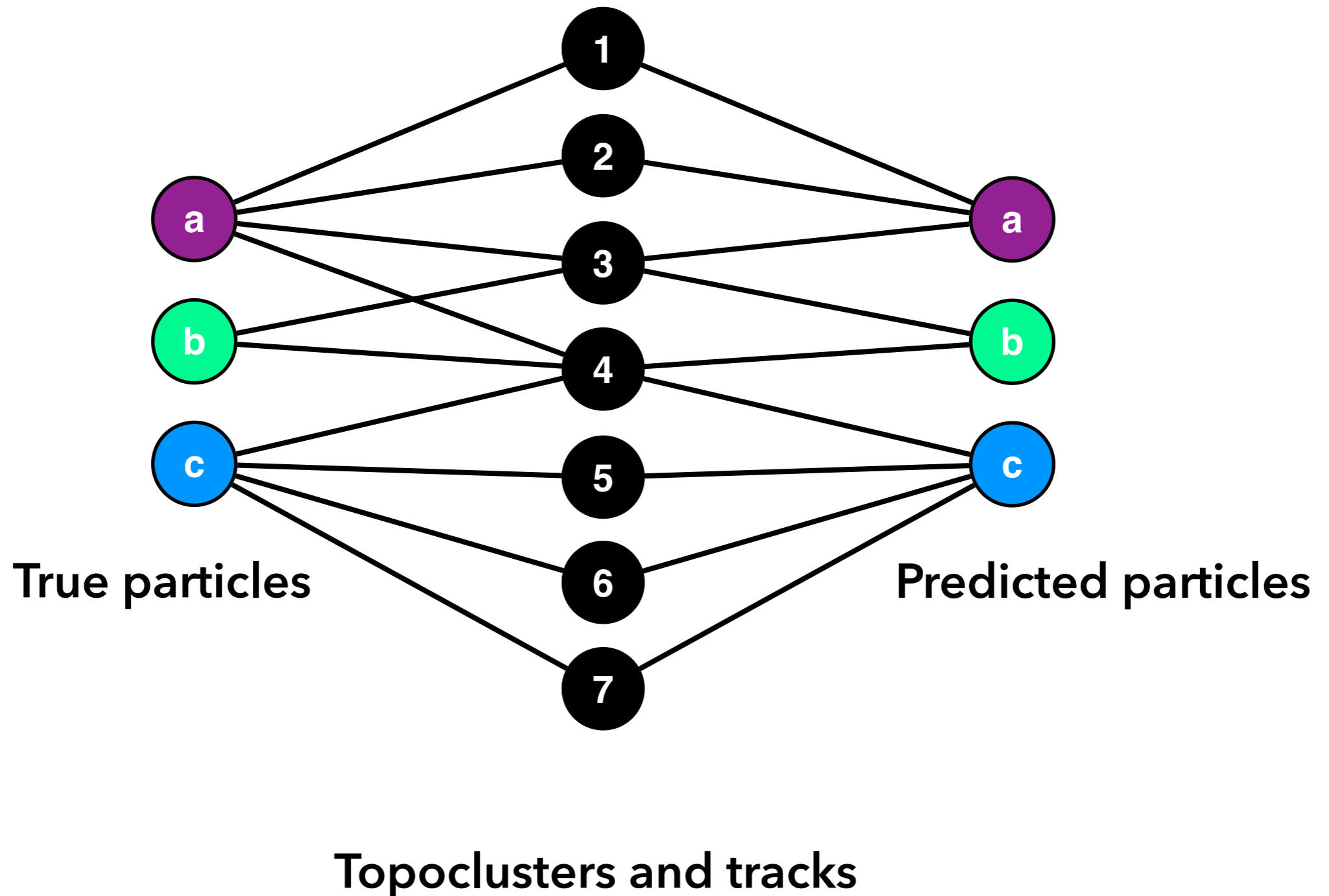
cartoon from [Nilotpal Kakati](#)



Topoclusters and tracks

Why use a hypergraph?

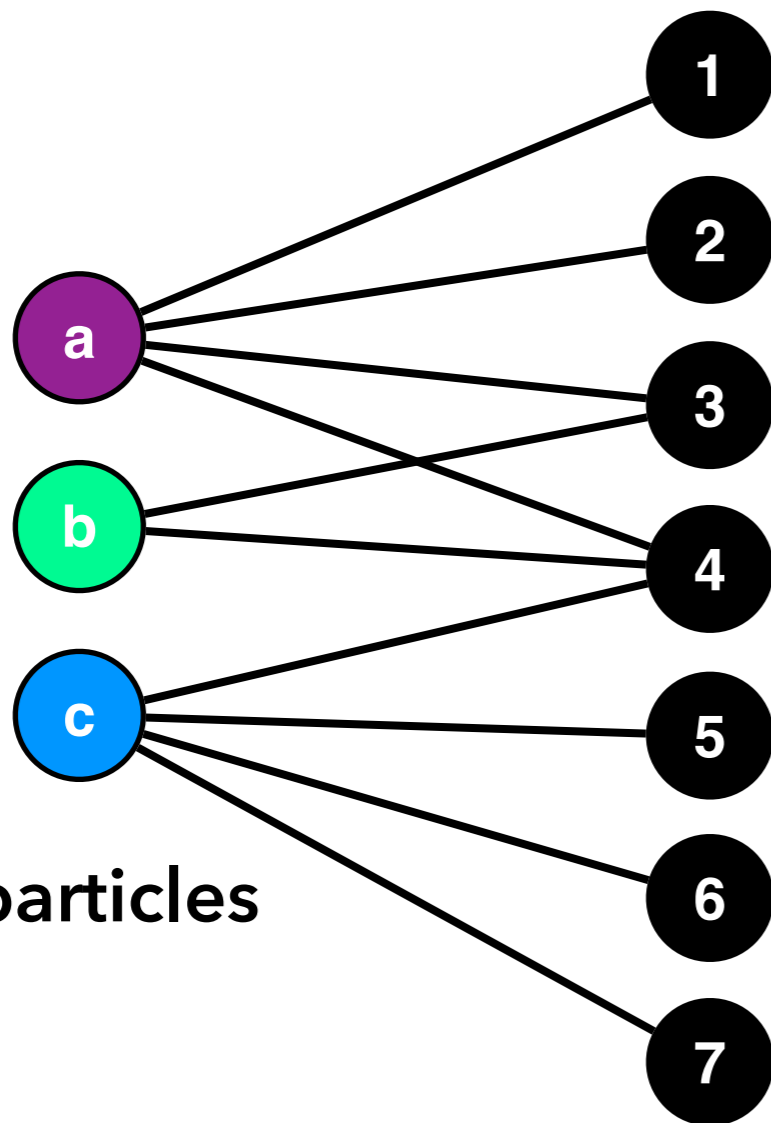
cartoon from [Nilotpal Kakati](#)



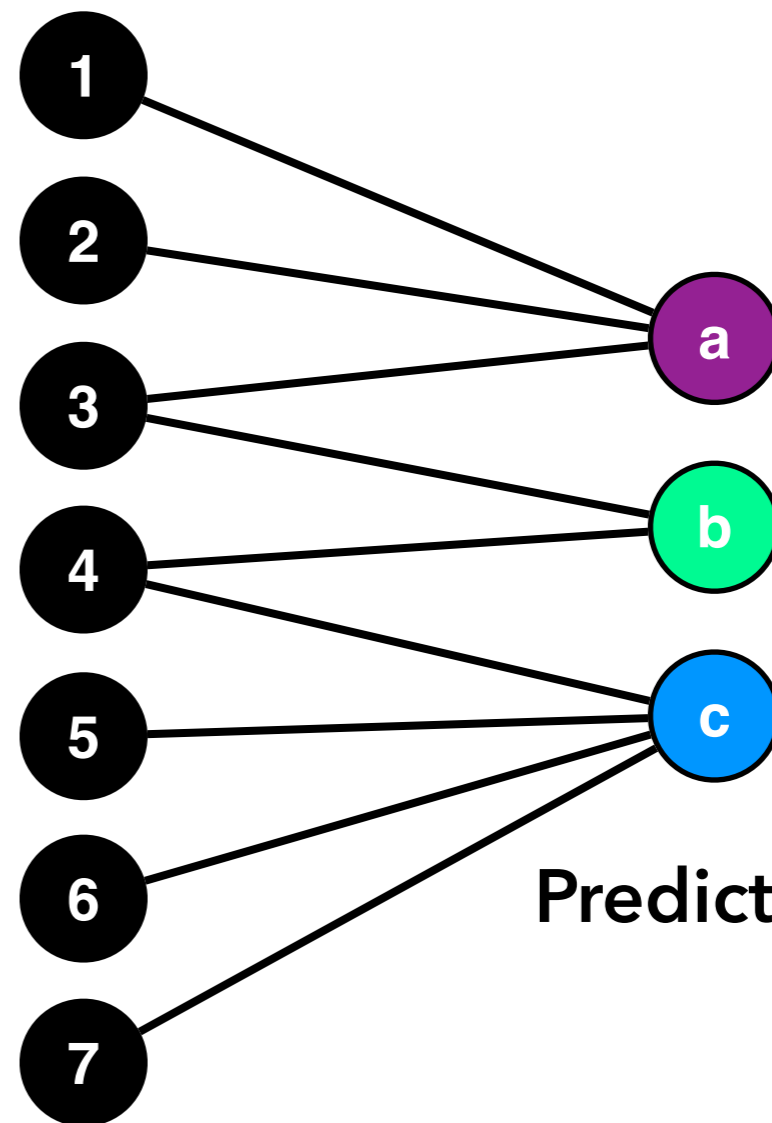
Why use a hypergraph?

cartoon from Nilotpal Kakati

Target hypergraph



Predicted hypergraph

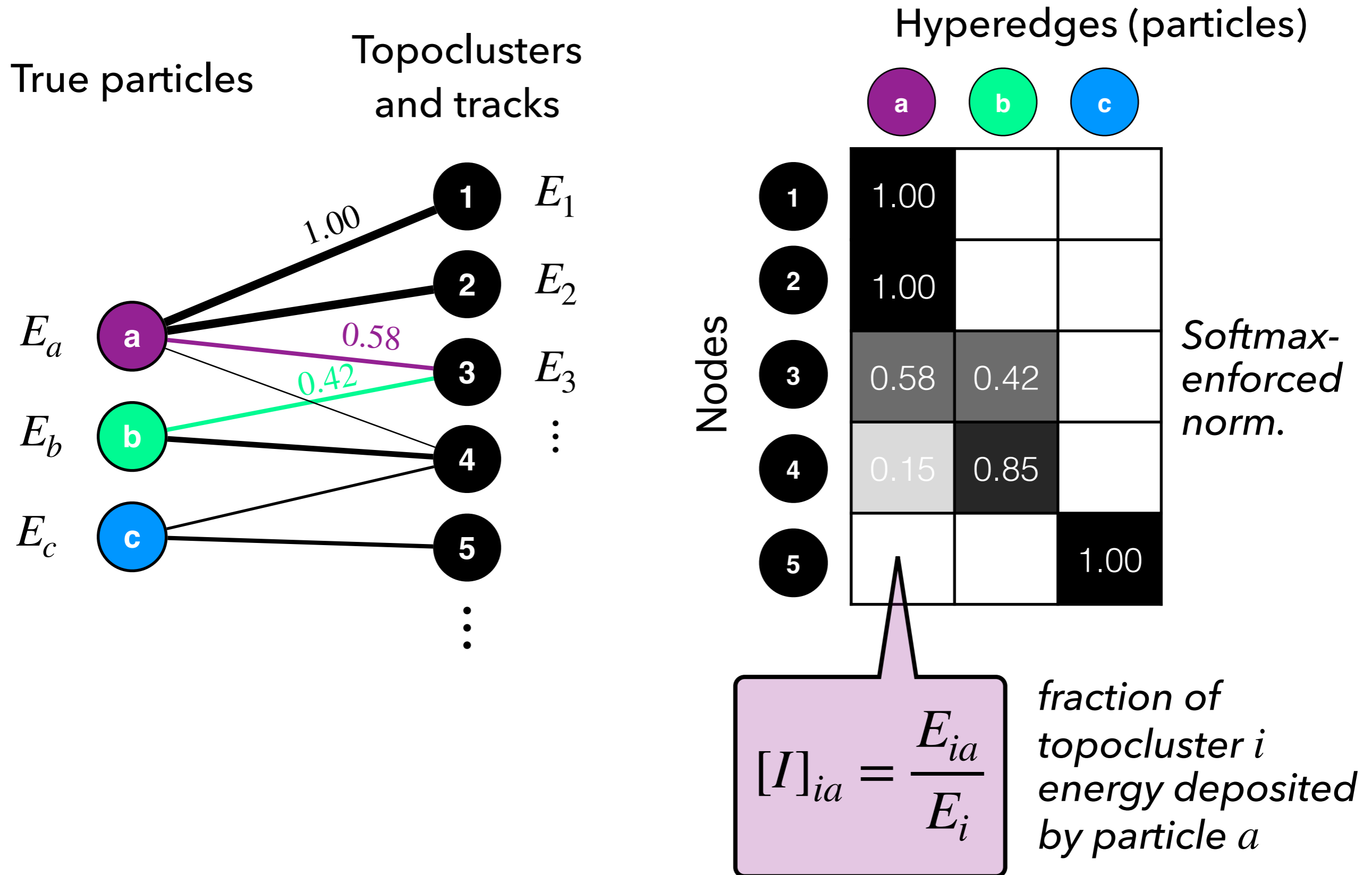


True particles

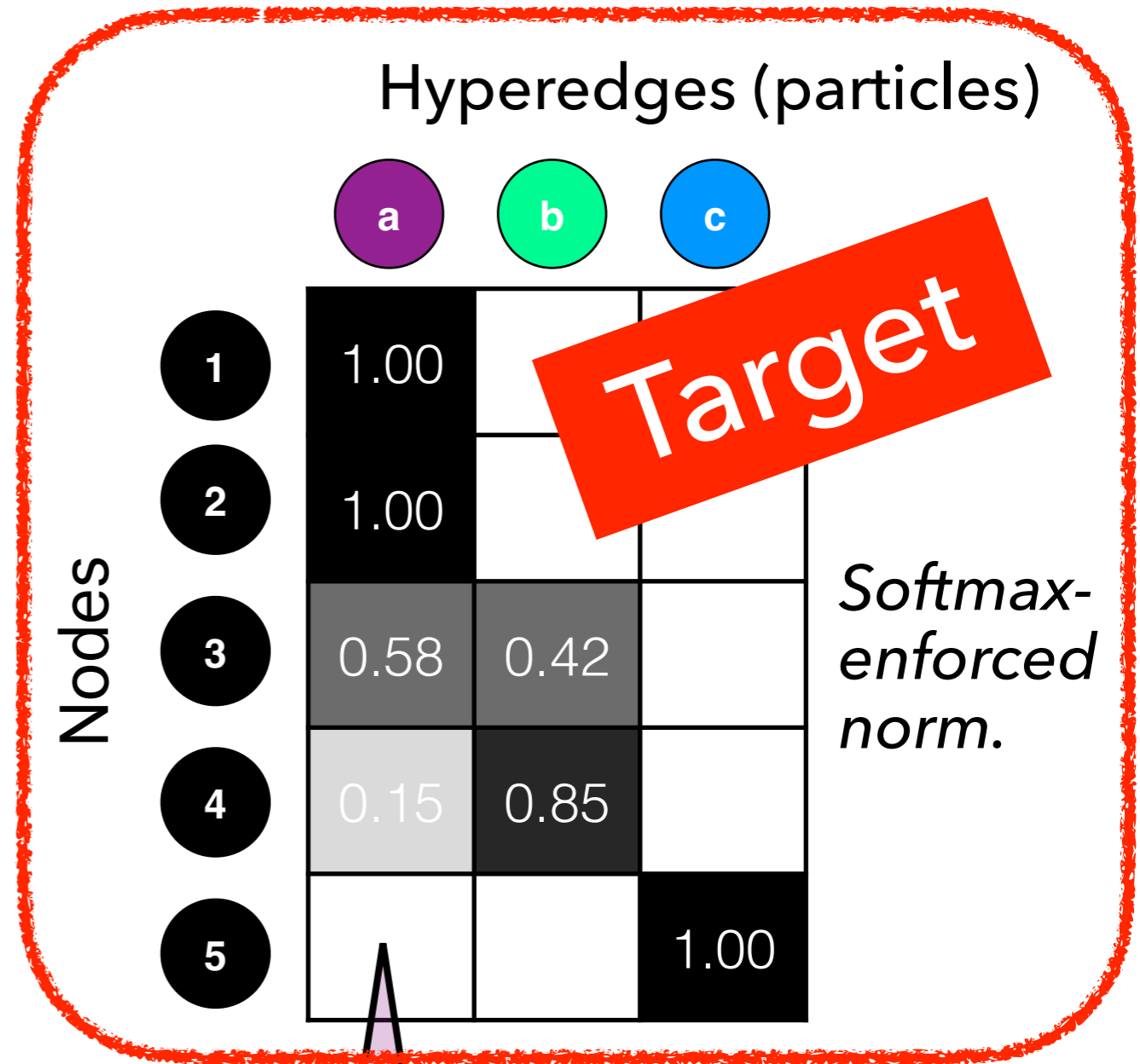
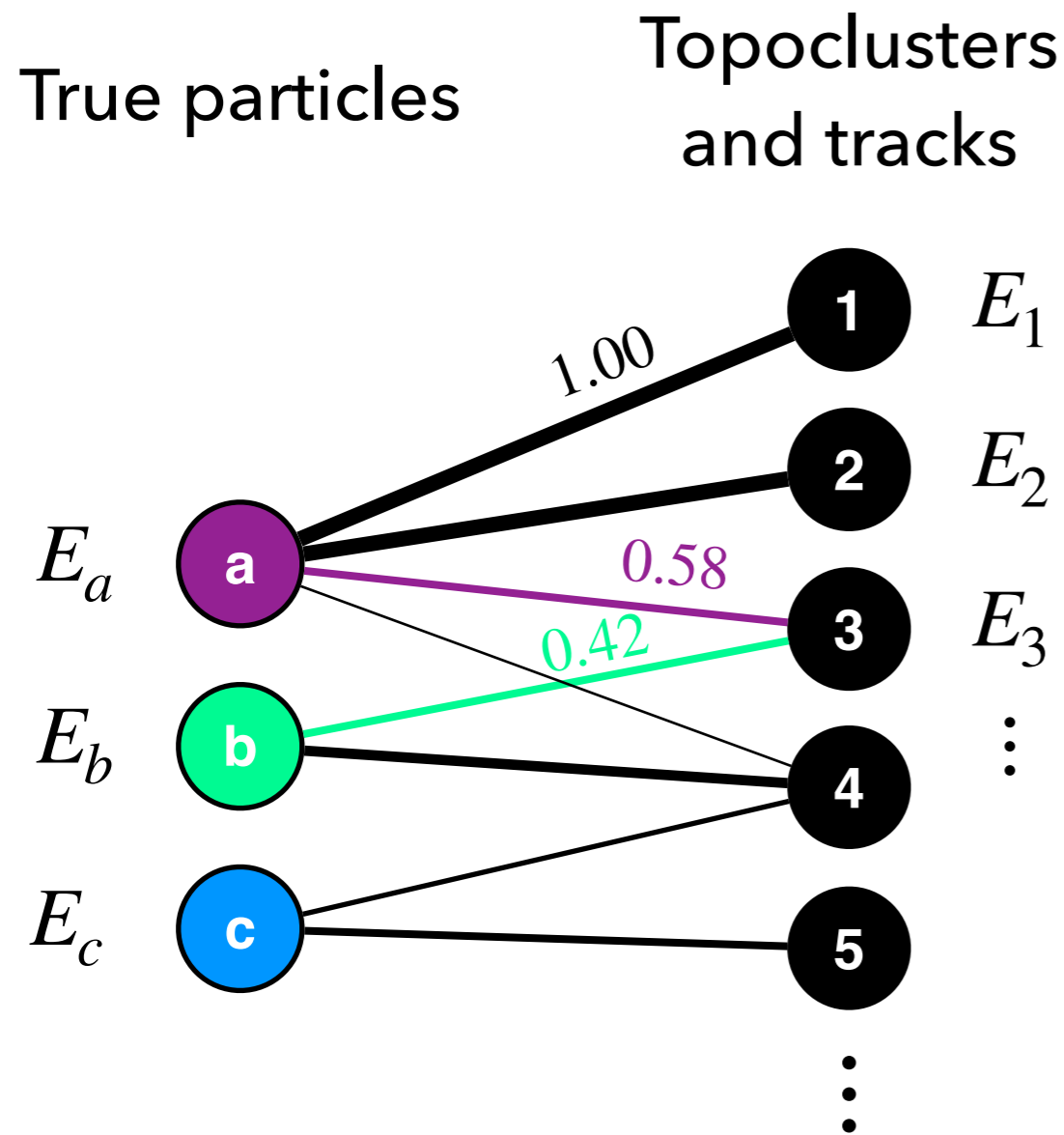
Predicted particles

Topoclusters and tracks

Energy-based incidence matrix



Energy-based incidence matrix

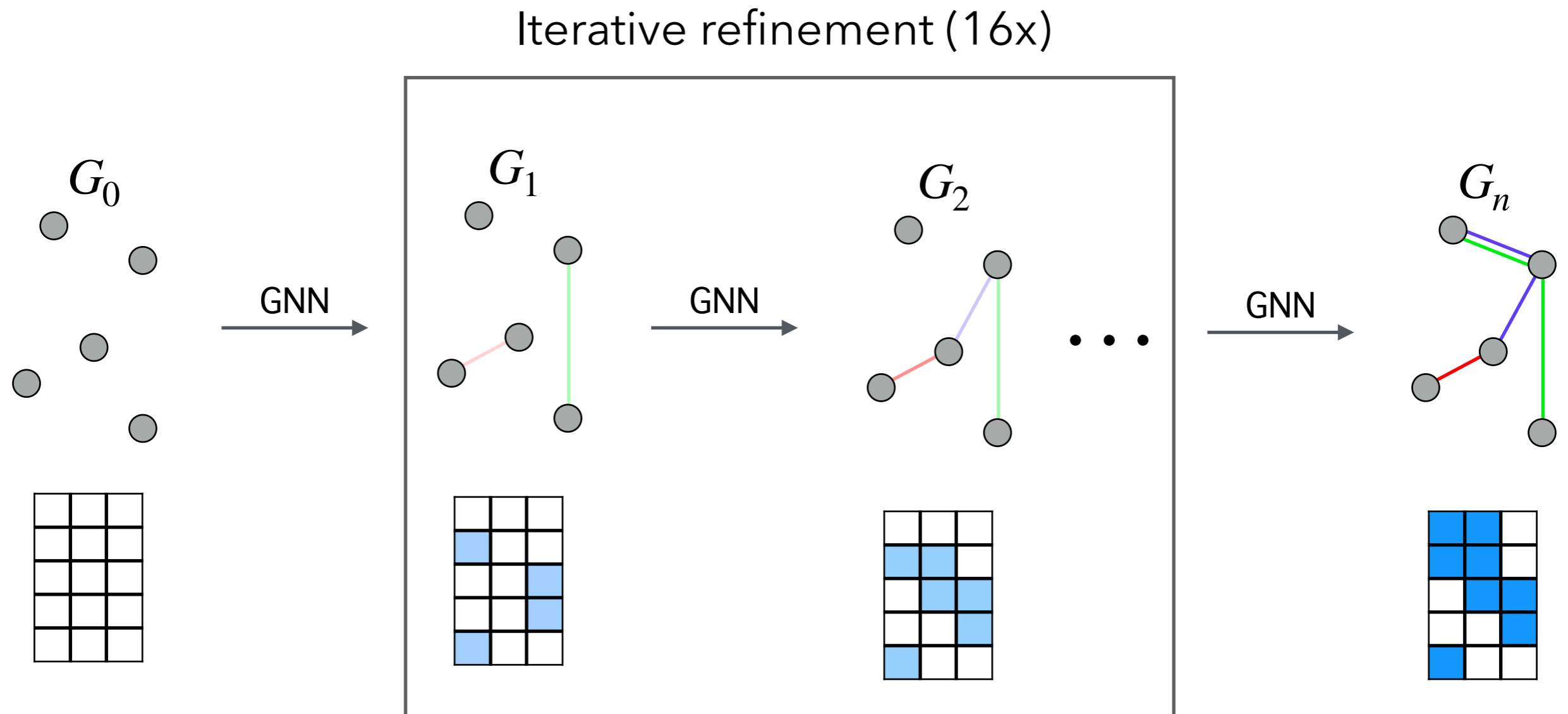


$$[I]_{ia} = \frac{E_{ia}}{E_i}$$

fraction of topocluster i energy deposited by particle a

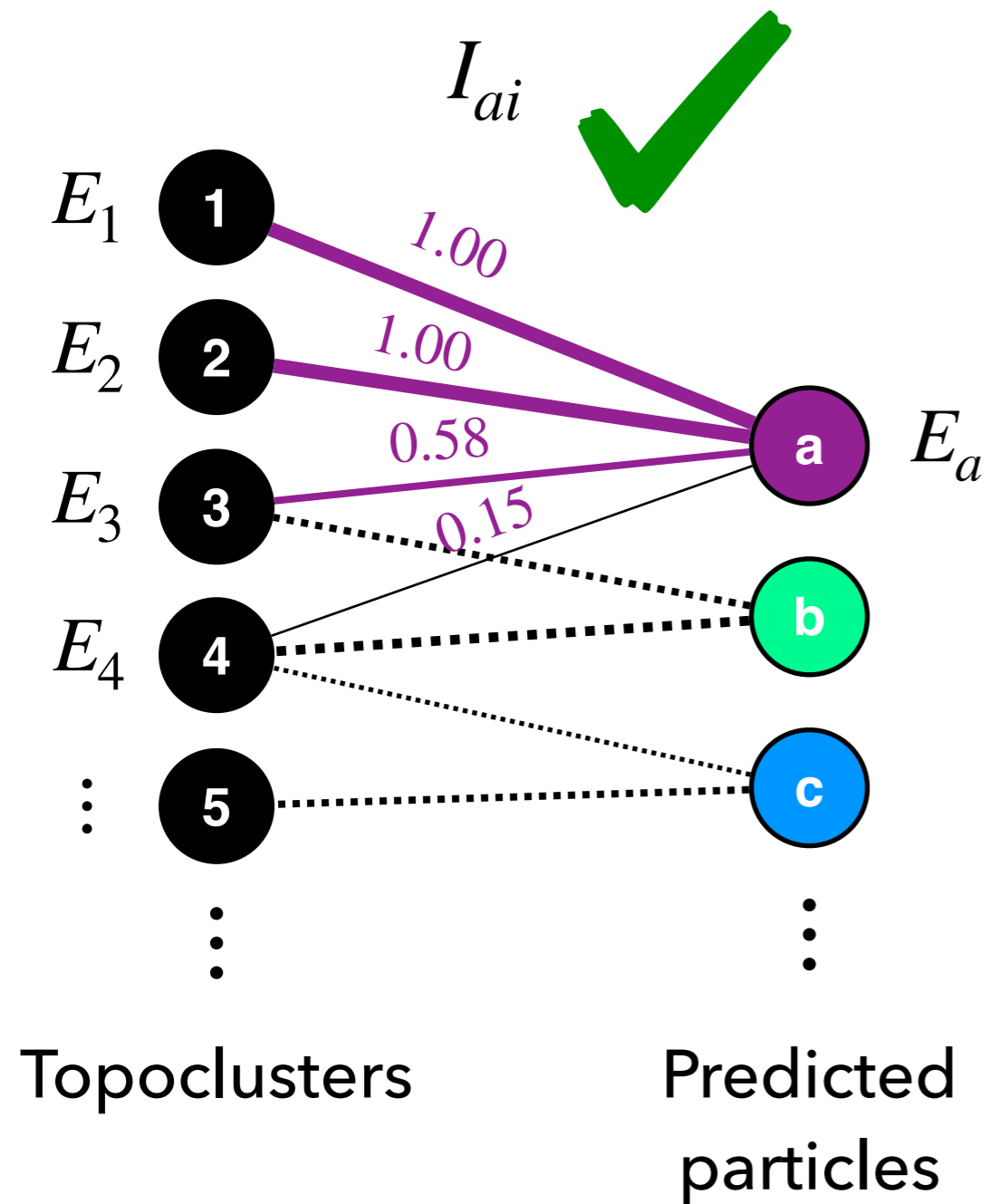
Recurrently predicting hypergraphs

Following Zhang, Burghouts and Snoek ([arXiv:2106.13919](https://arxiv.org/abs/2106.13919))



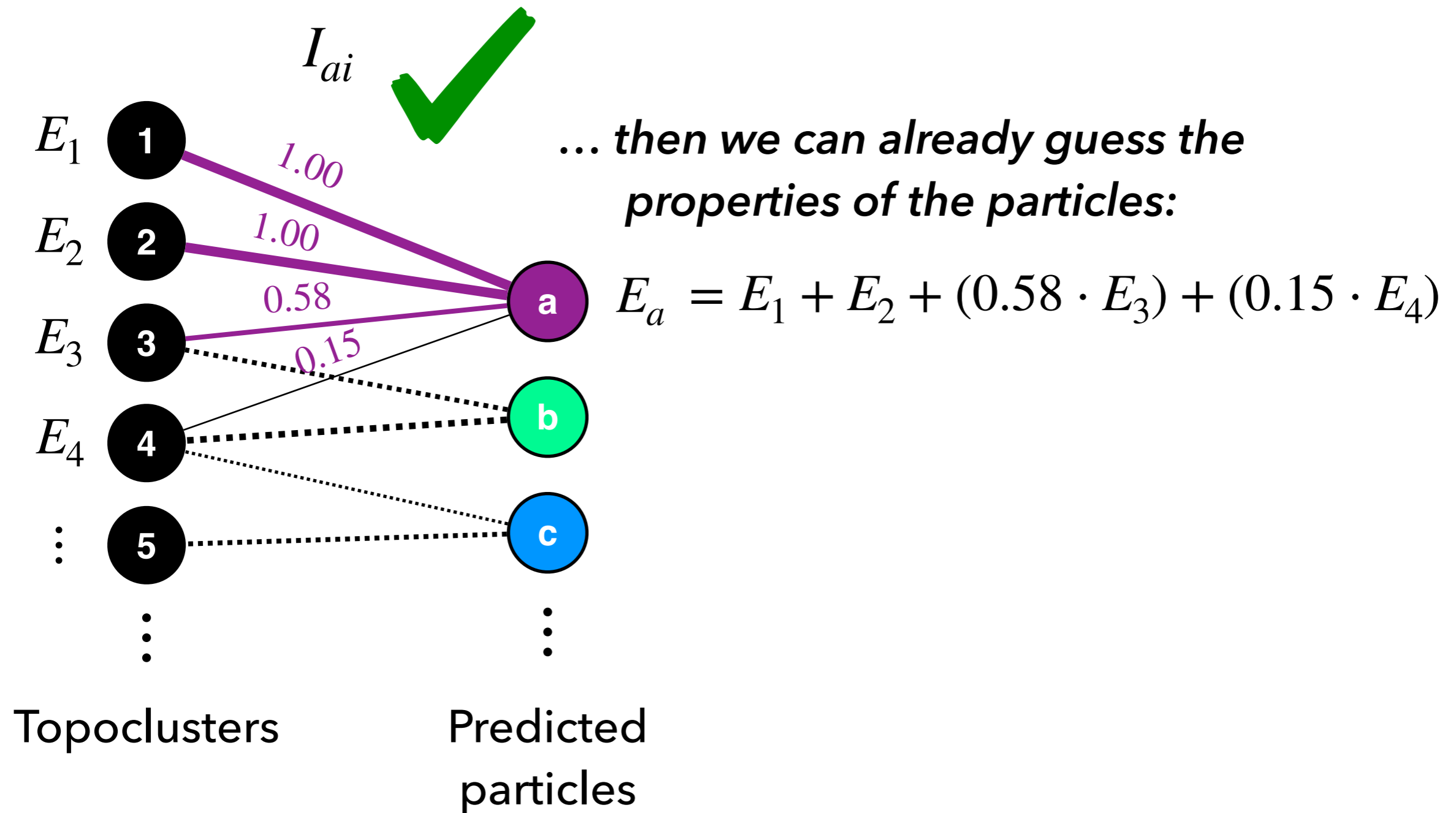
Perks of learning incidence matrix

Assuming we predicted the incidence matrix correctly...



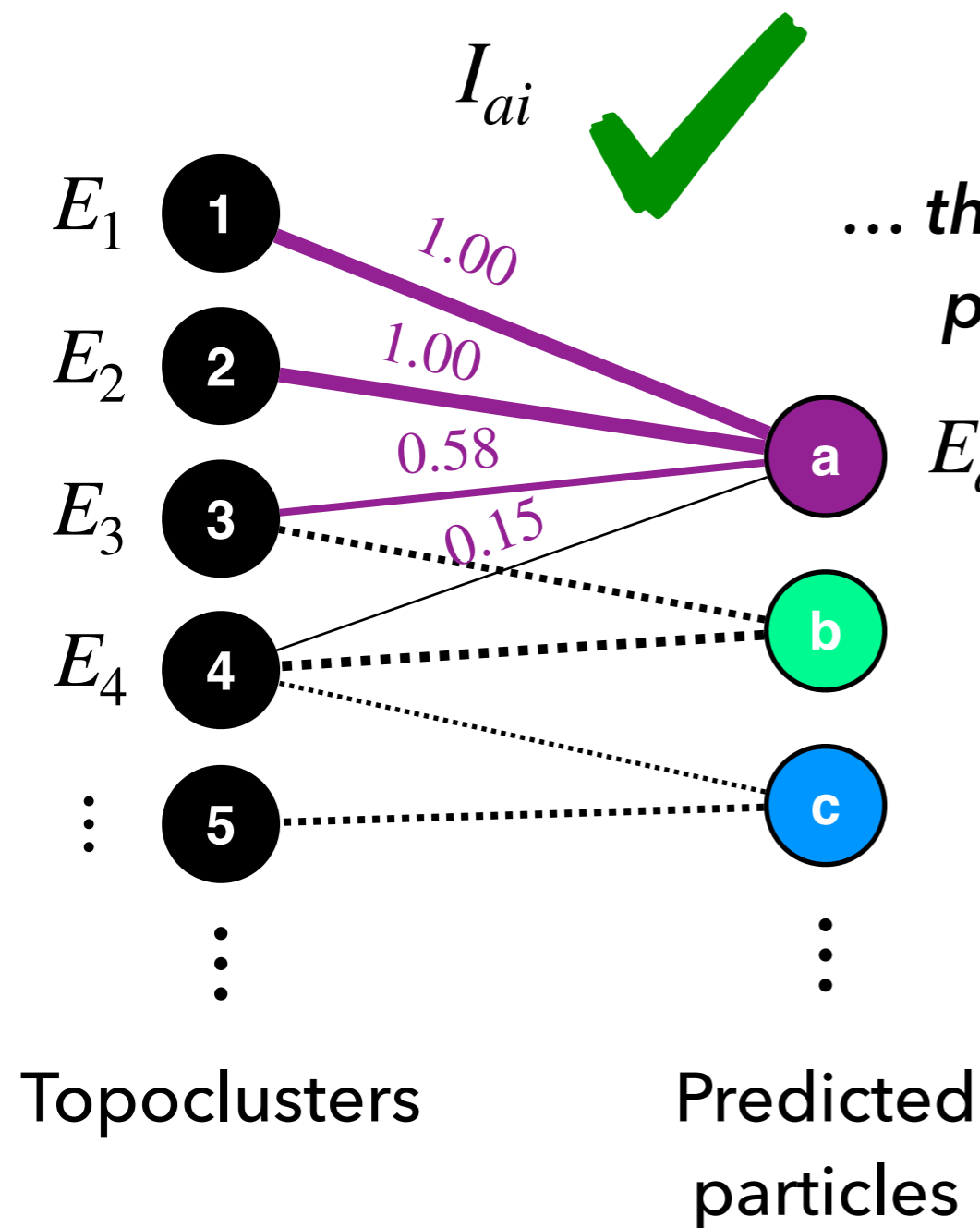
Perks of learning incidence matrix

Assuming we predicted the incidence matrix correctly...



Perks of learning incidence matrix

Assuming we predicted the incidence matrix correctly...



... then we can already guess the properties of the particles:

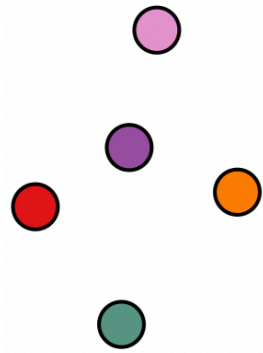
$$E_a = E_1 + E_2 + (0.58 \cdot E_3) + (0.15 \cdot E_4)$$

Learning the energy-based incidence matrix is an inductive bias that aids both prediction of particle properties and interpretability

HGPflow algorithm

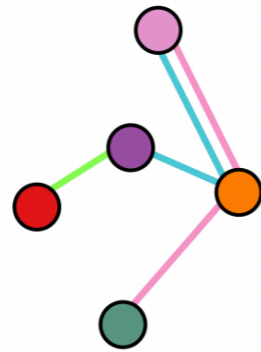
1) predict incidence matrix

input nodes



Recursive learning
→
16 refinement
blocks

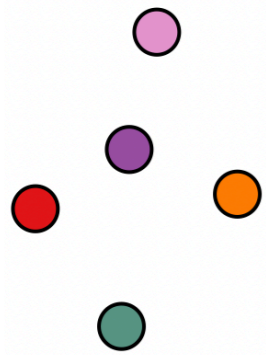
hyperedges



HGPflow algorithm

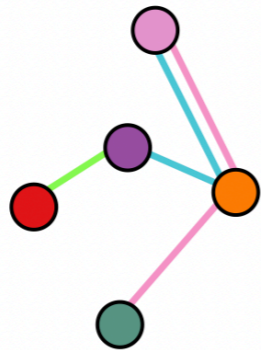
1) predict incidence matrix

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Recursive learning
→
16 refinement
blocks

hyperedges



Energy-fraction
incidence matrix

$$I_{ia} =$$

		Hyperedges		
Nodes		0.4	0.6	
			0.7	0.3
		0.6	0.4	
		1		
				1

Incidence matrix

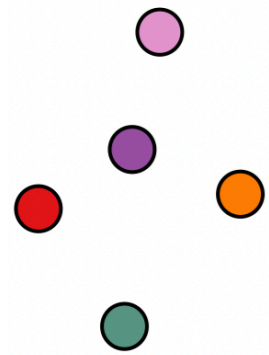
Recurrently predicting hypergraphs

[arXiv:2106.13919](https://arxiv.org/abs/2106.13919)

HGPflow algorithm

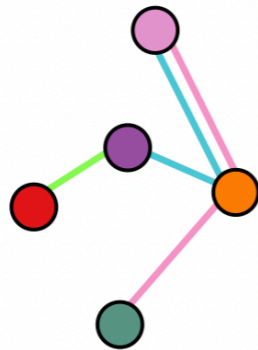
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Energy-fraction
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Incidence matrix

Recurrently predicting hypergraphs

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2) predict particle properties

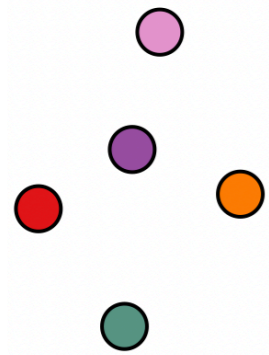
hyperedge rep.



HGPflow algorithm

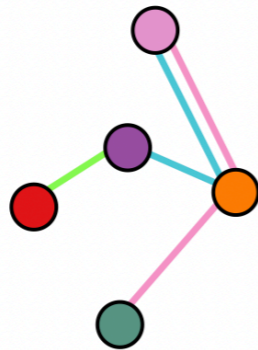
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Recursive learning
16 refinement
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hyperedges



Energy-fraction
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$$I_{ia} =$$

		Hyperedges		
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		1		
				1

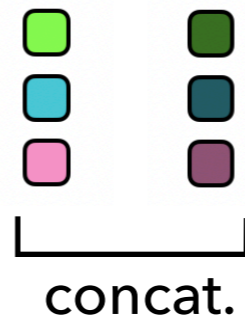
Incidence matrix

Recurrently predicting hypergraphs

[arXiv:2106.13919](https://arxiv.org/abs/2106.13919)

2) predict particle properties

hyperedge rep.
proxy quantity



Energy-weighted
proxy quantities:

$$\hat{E}_a = \sum_{\text{nodes } i} E_i \cdot I_{ia}$$

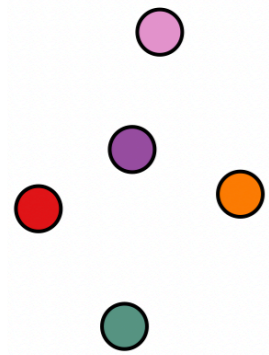
$$\hat{\eta}_a = \sum_{\text{nodes } i} \eta_i \cdot \frac{E_{ia}}{E_a}$$

$$\hat{\phi}_a = \sum_{\text{nodes } i} \phi_i \cdot \frac{E_{ia}}{E_a}$$

HGPflow algorithm

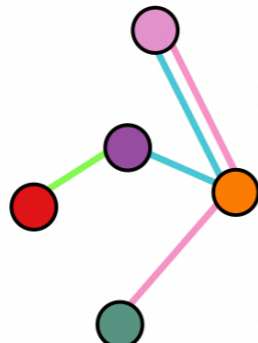
1) predict incidence matrix

input nodes



Recursive learning
16 refinement
blocks

hyperedges



Energy-fraction
incidence matrix

$$I_{ia} =$$

		Hyperedges		
		pink	blue	green
Nodes	pink	0.4	0.6	
	purple		0.7	0.3
	orange	0.6	0.4	
	teal	1		
	red			1

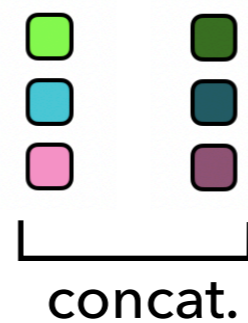
Incidence matrix

Recurrently predicting hypergraphs

[arXiv:2106.13919](https://arxiv.org/abs/2106.13919)

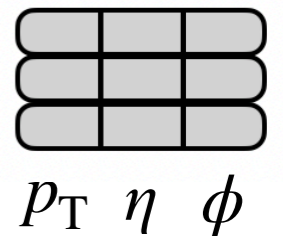
2) predict particle properties

hyperedge rep.
proxy quantity



$$\eta_a^{\text{pred}} = \hat{\eta}_a + \Delta\eta_a^{\text{net}}$$

predict
offsets



Energy-weighted
proxy quantities:

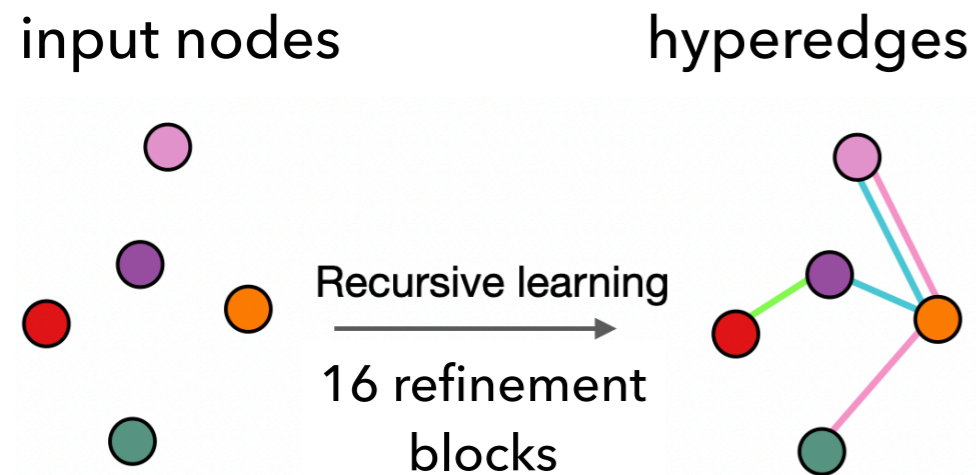
$$\hat{E}_a = \sum_{\text{nodes } i} E_i \cdot I_{ia}$$

$$\hat{\eta}_a = \sum_{\text{nodes } i} \eta_i \cdot \frac{E_{ia}}{E_a}$$

$$\hat{\phi}_a = \sum_{\text{nodes } i} \phi_i \cdot \frac{E_{ia}}{E_a}$$

HGPflow algorithm

1) predict incidence matrix



Energy-fraction incidence matrix

$$I_{ia} =$$

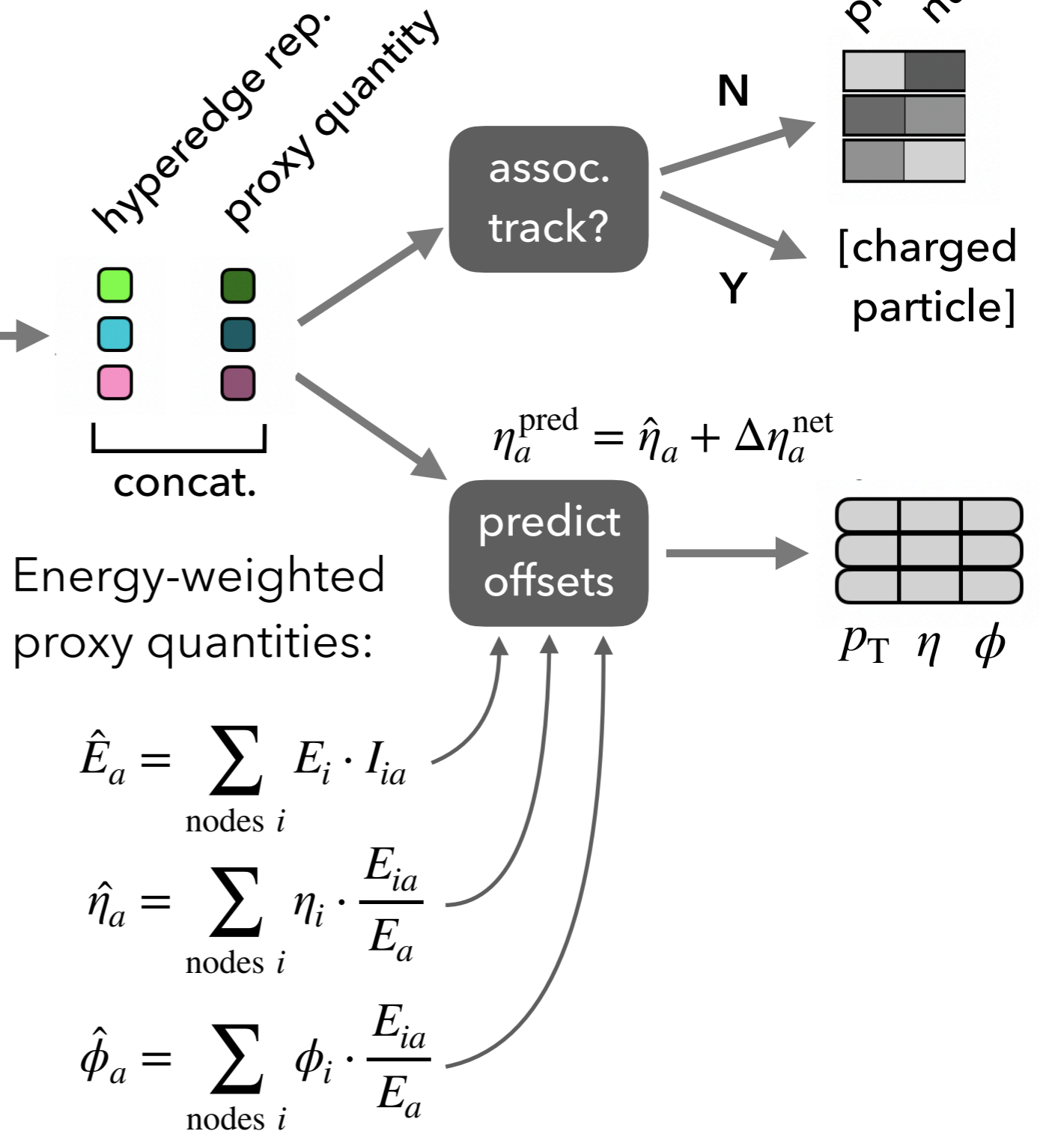
Nodes	Hyperedges		
	0.4	0.6	
		0.7	0.3
	0.6	0.4	
	1		
			1

Incidence matrix

Recurrently predicting hypergraphs

[arXiv:2106.13919](https://arxiv.org/abs/2106.13919)

2) predict particle properties



HGPflow jet-level improvement

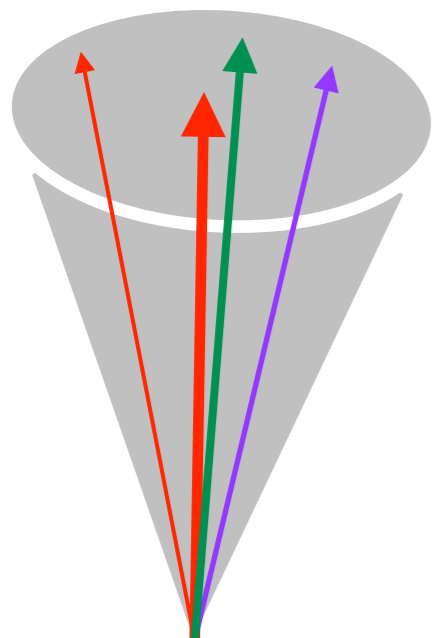
Dataset of single jets

$\frac{\text{target} - \text{predicted}}{\text{target}}$

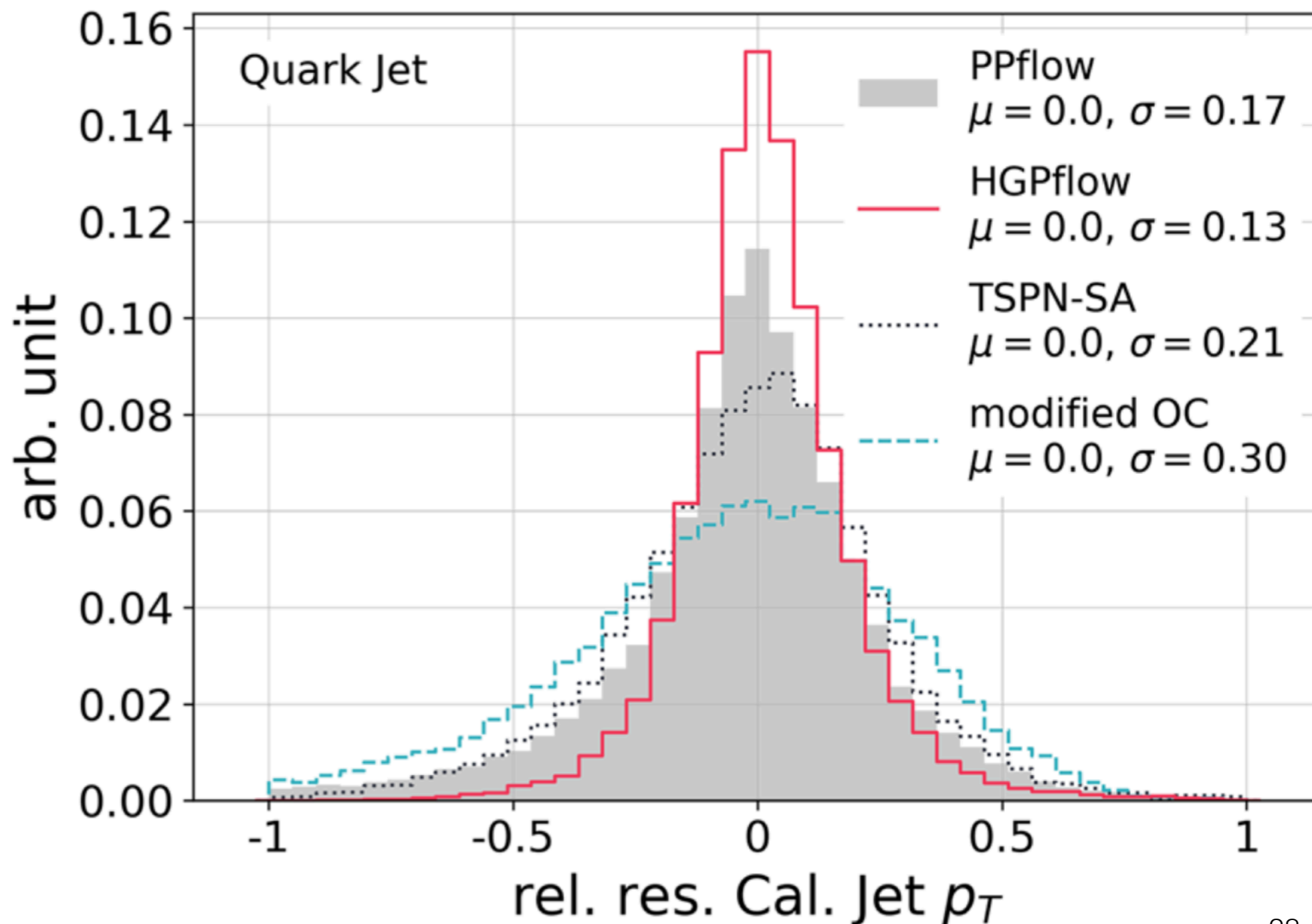
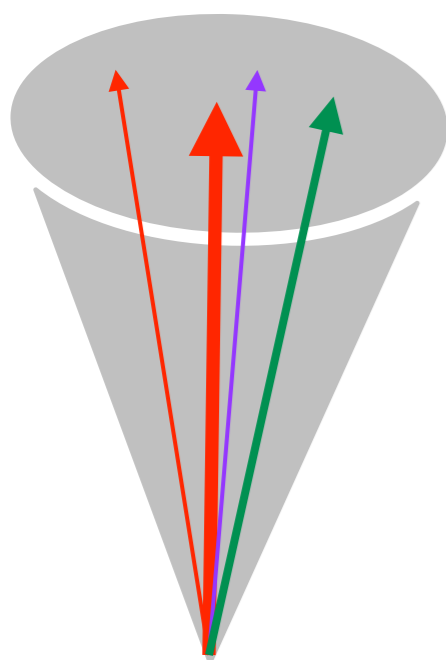
[arXiv:2212.01328](https://arxiv.org/abs/2212.01328)

target

Truth



Reco



Summary & outlook



Particle reconstruction is foundational to experimental HEP

Deep learning models are the future for particle reconstruction

Recent GNN-based approaches show prospects to:

- * optimally exploit the set-valued, heterogeneous input space
- * predict set of particles and their properties in one shot
- * improve over traditional parameterized algorithms

Hypergraph learning suits the problem well and aids interpretability

Summary & outlook



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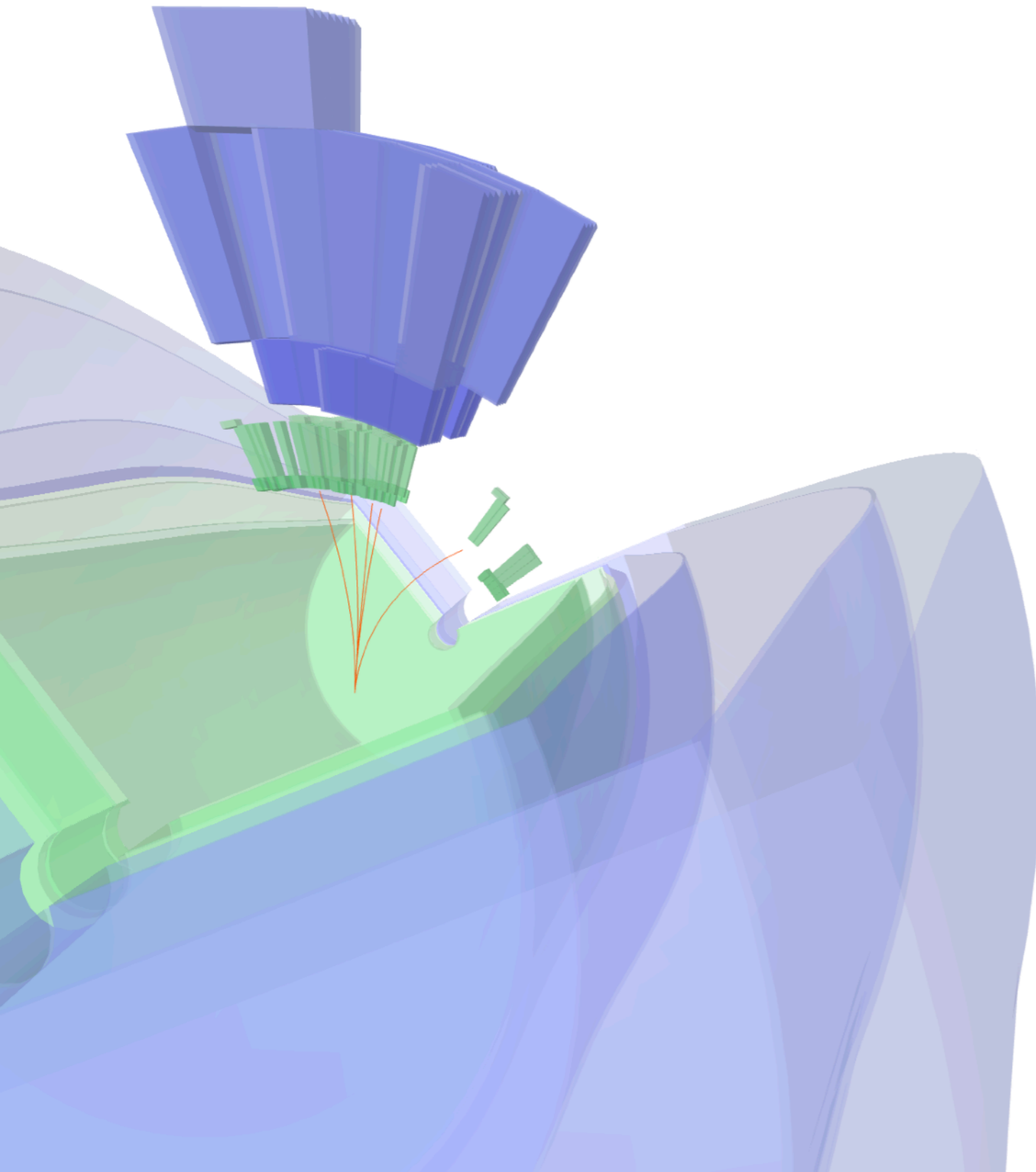
Outlook:

- * performance studies on common datasets* will help compare and improve the current SOTA models (MLPF, OC, HGPflow)
- * CMS and ATLAS are both pursuing ML algorithms in their core reconstruction software targeting the HL-LHC timeframe (or earlier)

Backup

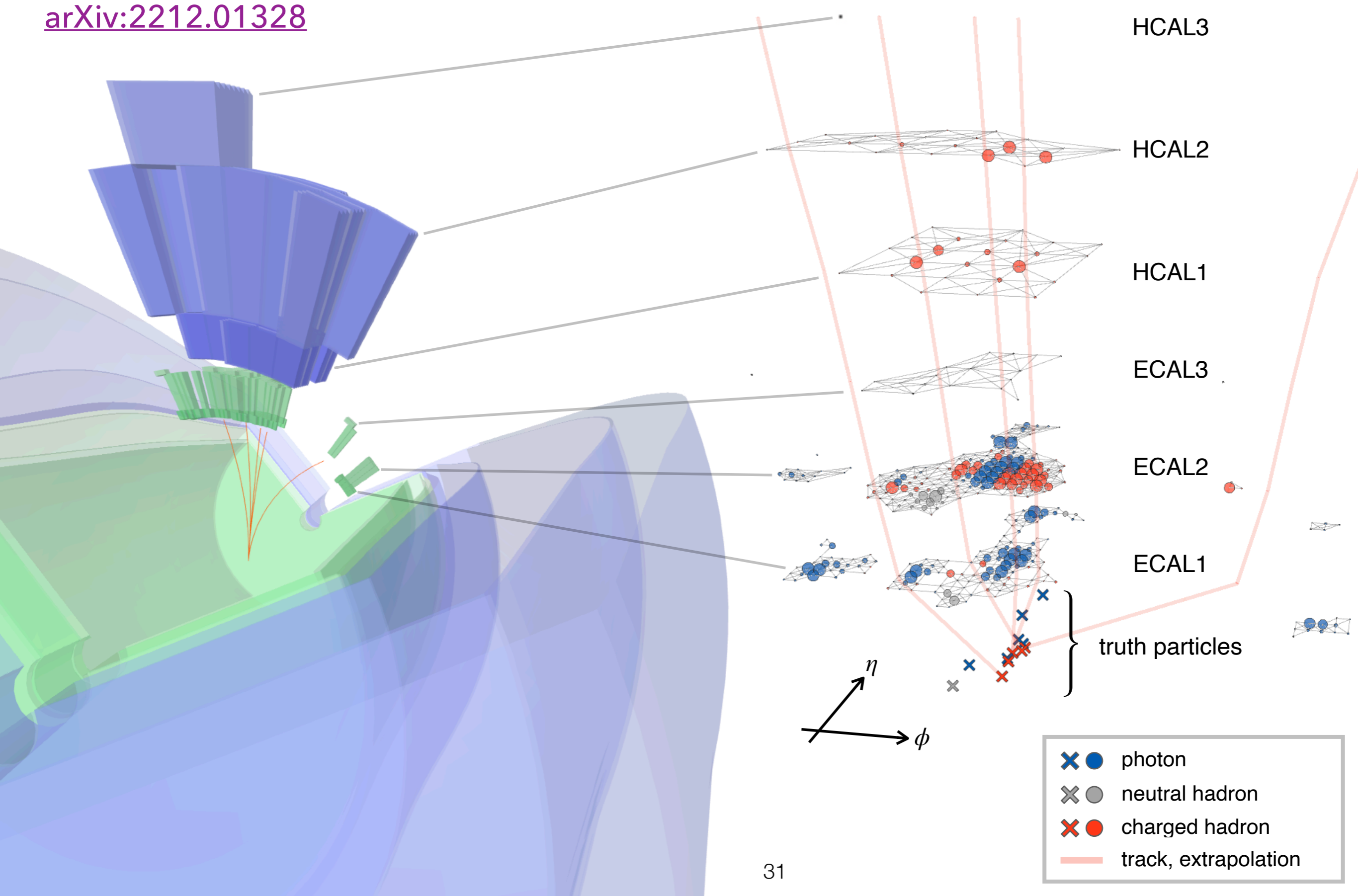
Example of a single jet

[arXiv:2212.01328](https://arxiv.org/abs/2212.01328)



Example of a single jet

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