

# DATA-DRIVEN STRONG GRAVITATIONAL LENSING ANALYSIS IN THE ERA OF LARGE SKY SURVEYS

Laurence Perreault-Levasseur

Ciela Institute

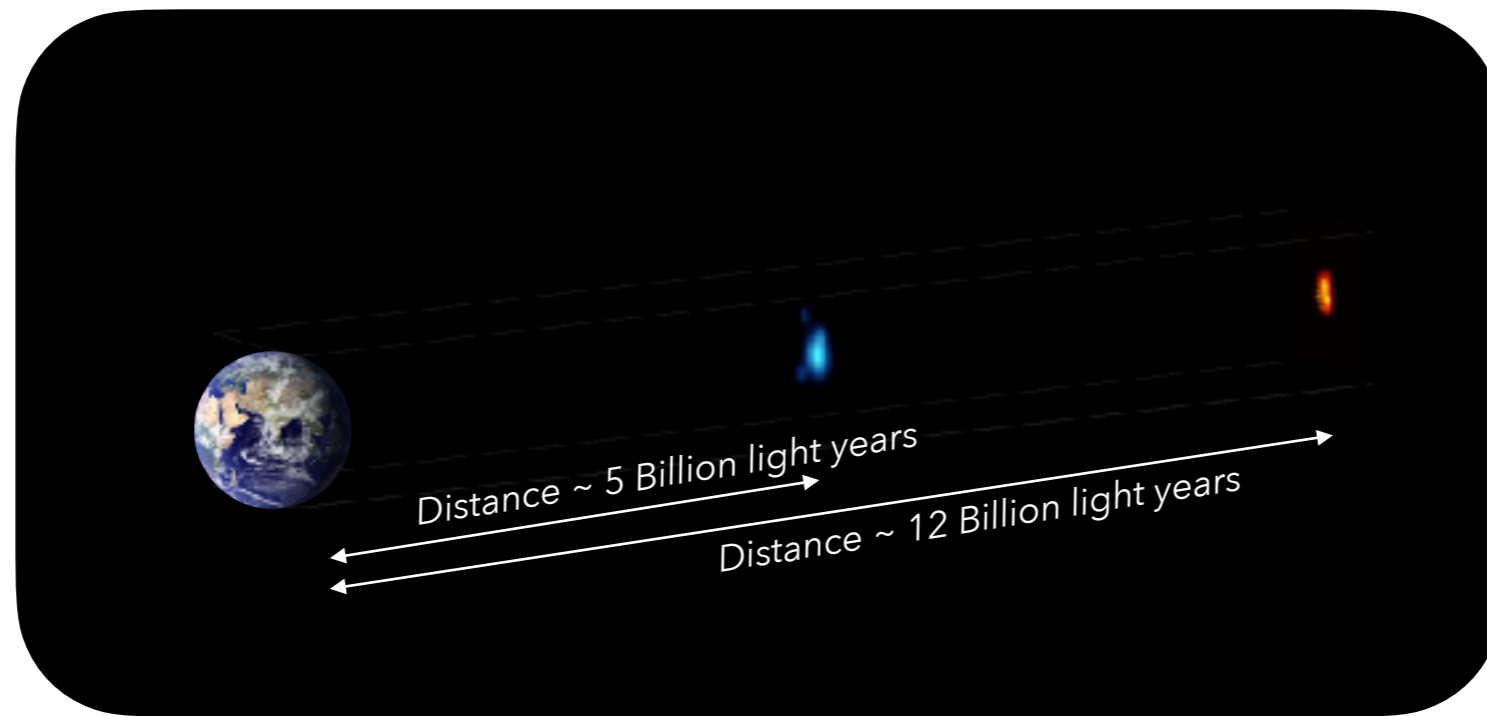
Université   
de Montréal

 Mila

 FLATIRON  
INSTITUTE  
Center for Computational  
Astrophysics

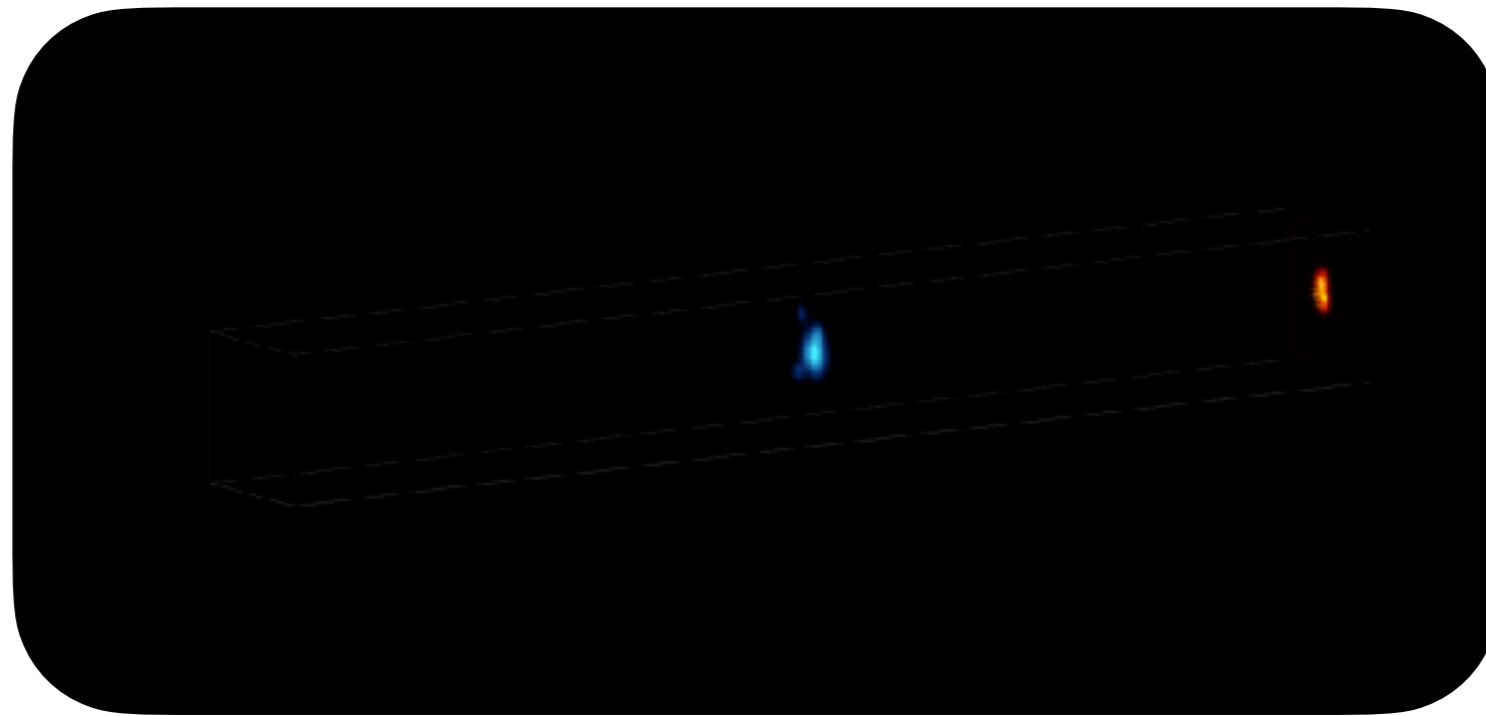
# STRONG GRAVITATIONAL LENSING

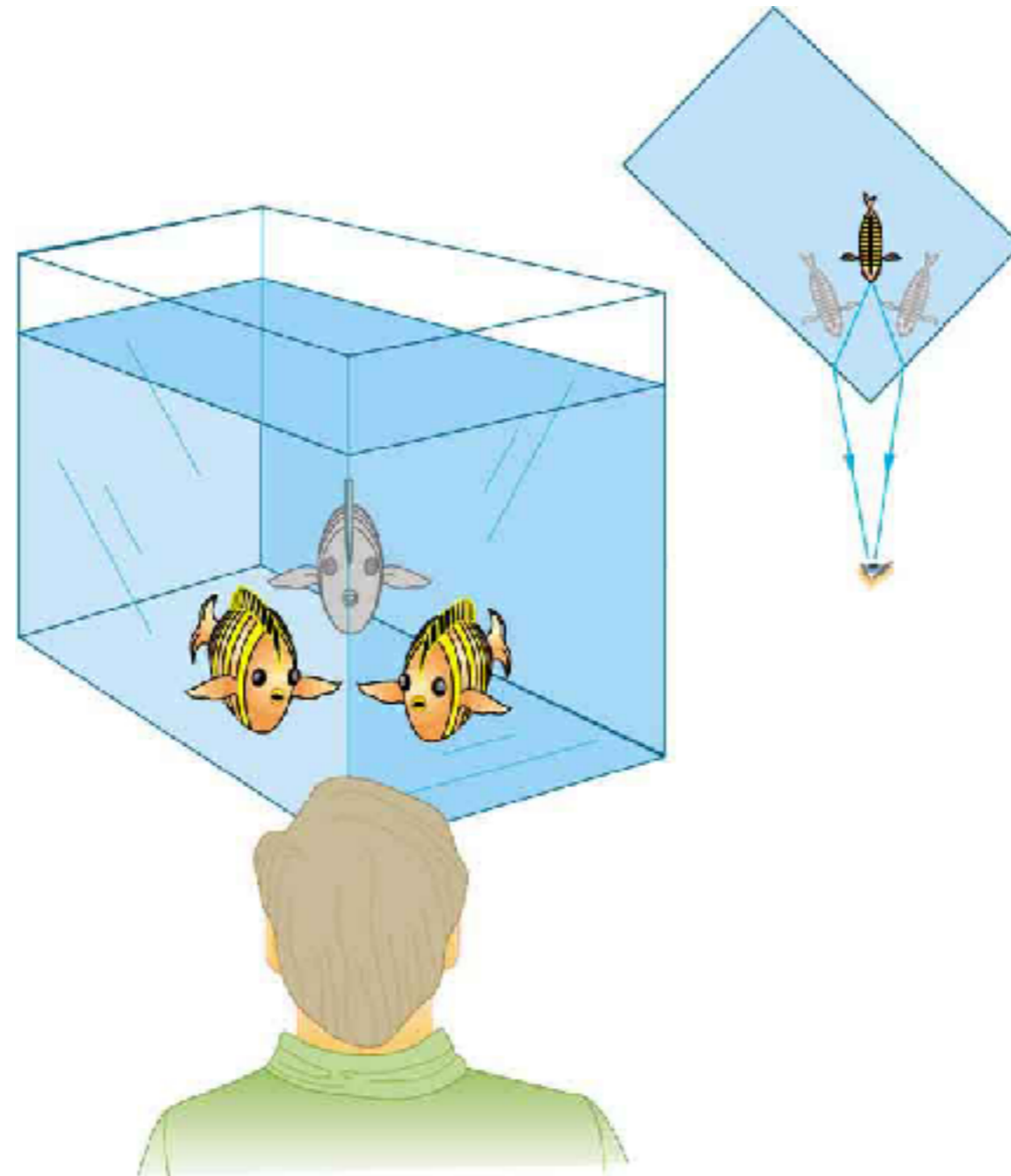
Formation of **multiple images** of a single distant object due to the **deflection of its light** by the **gravity** of intervening structures.



# STRONG GRAVITATIONAL LENSING

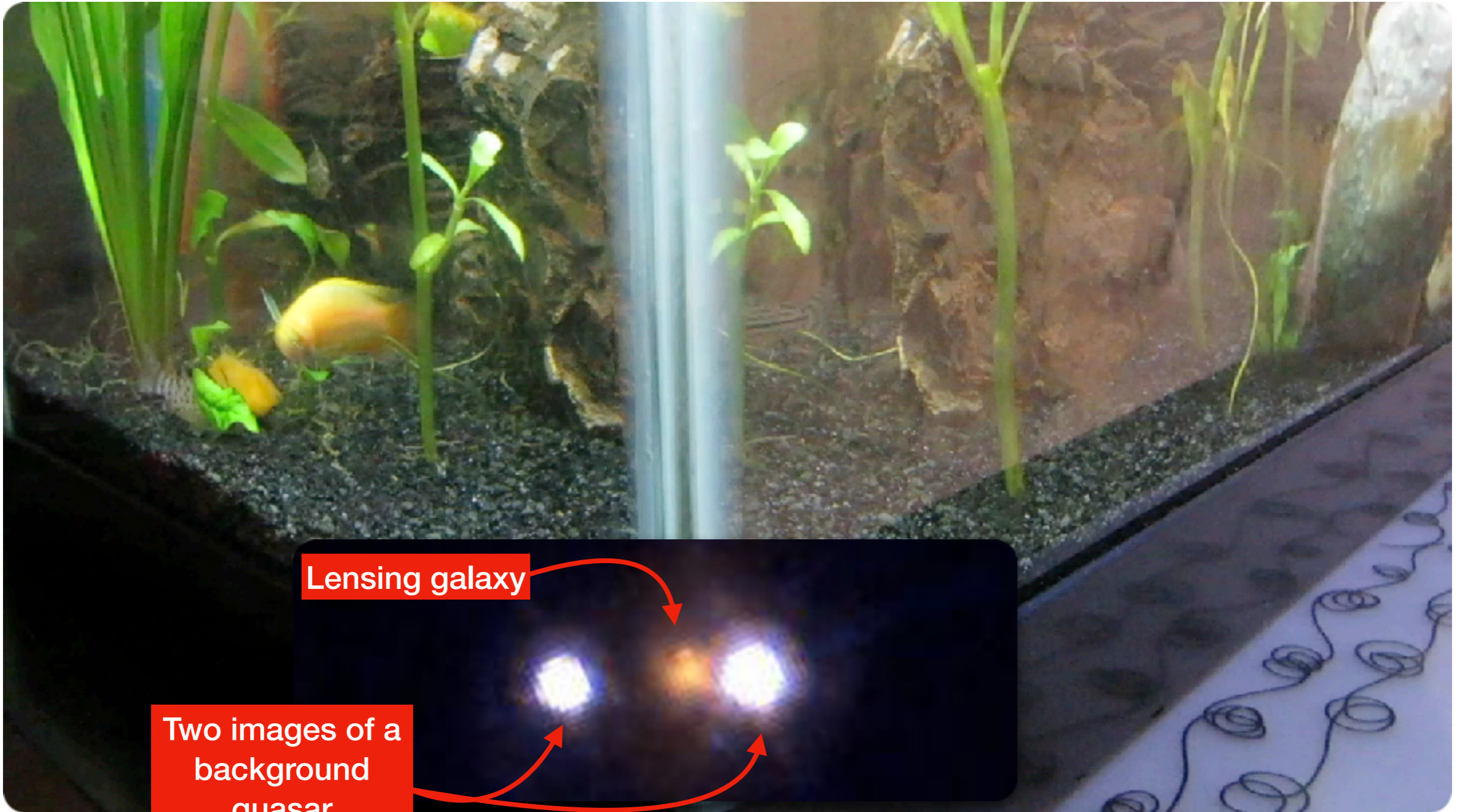
Formation of **multiple images** of a single distant object due to the **deflection of its light** by the **gravity** of intervening structures.











Lensing galaxy

Two images of a background quasar





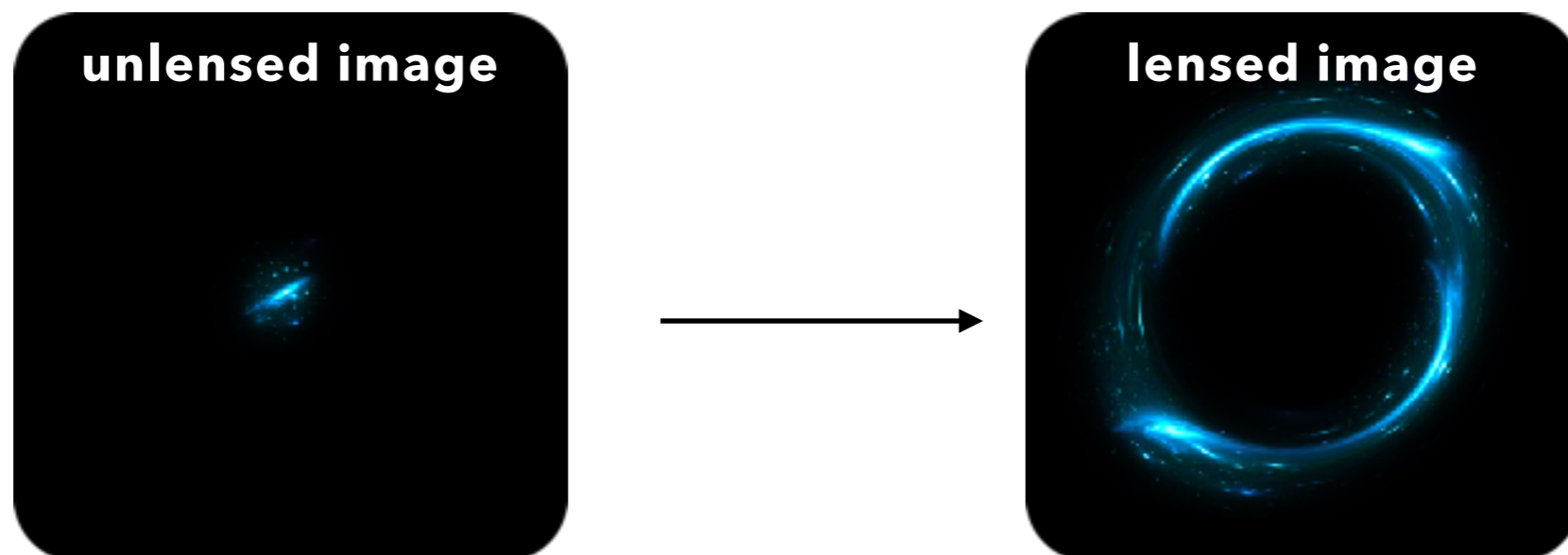






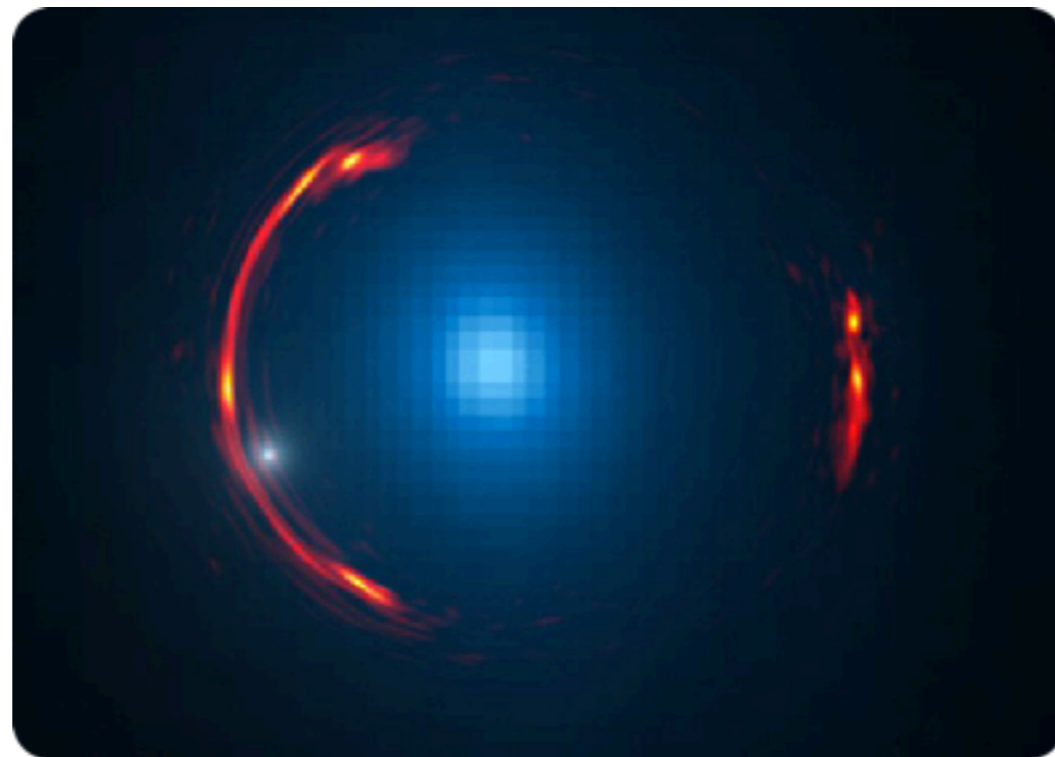
# SCIENCE MOTIVATIONS FOR STRONG LENSING

- 1 - Use strong lensing as a **cosmic telescope**.
  - Lensing **magnifies** the images of sources and makes them appear **brighter**.
  - This allows us to study some of the most distant galaxies of the universe that would have been otherwise below our sensitivity or resolution limits.

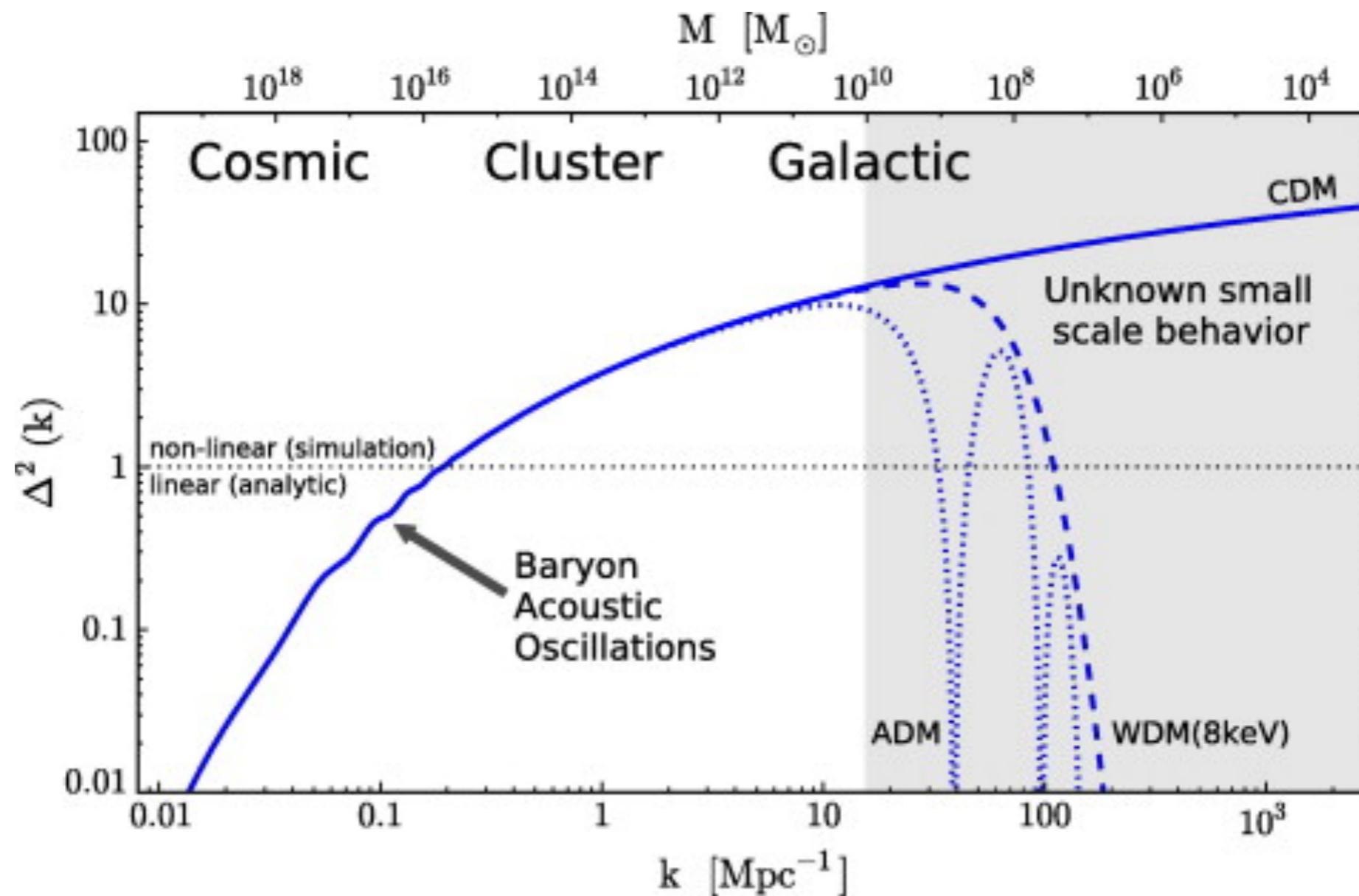


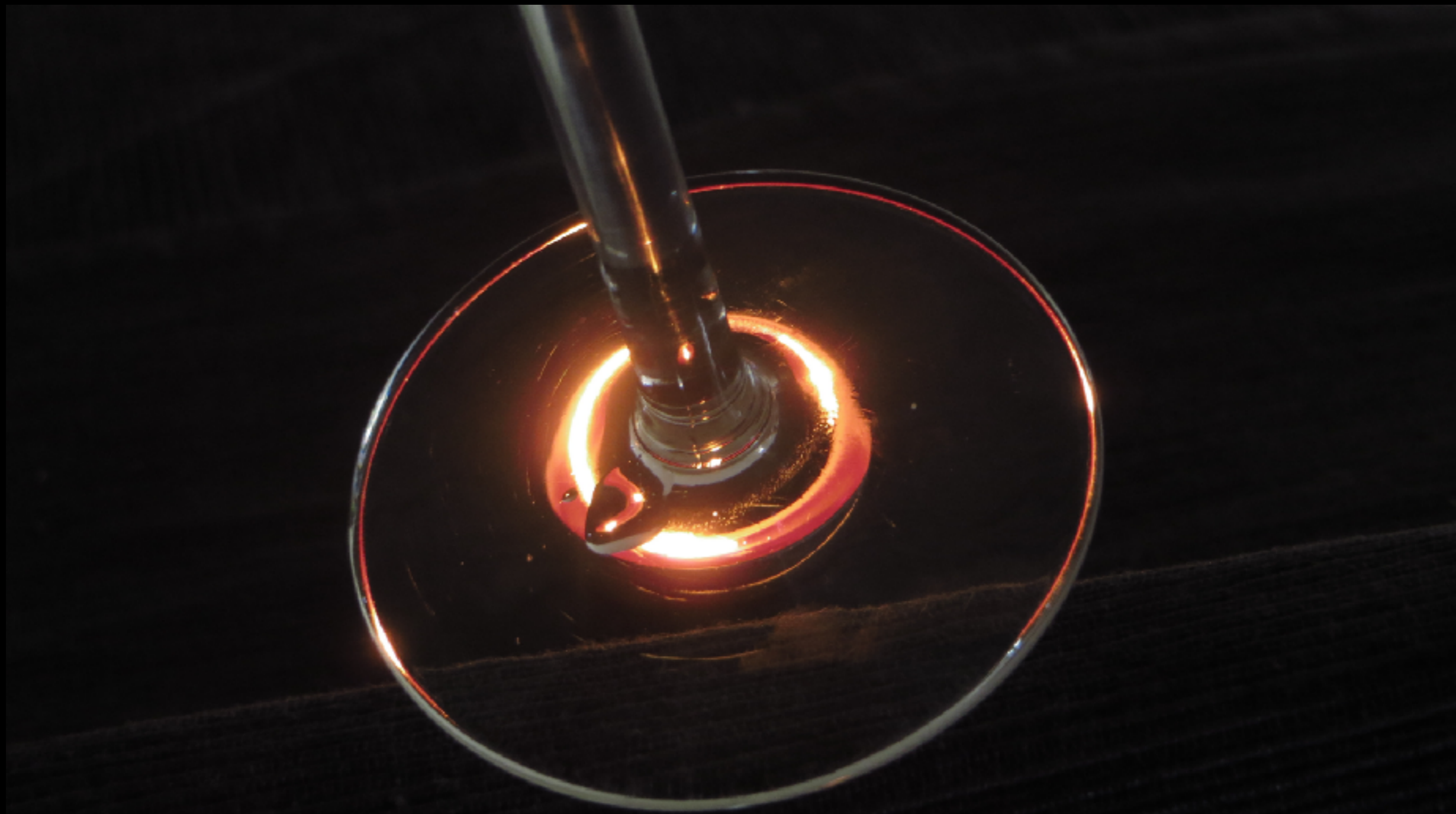
# SCIENCE MOTIVATIONS FOR STRONG LENSING

- 2 - Use lensing to probe the **distribution of matter** in the lensing structures.
- Distortions in images are caused by **gravity**.
  - They can be used to map the **distribution of matter** in the lens.
  - Particularly useful for studying **dark matter**.



# Matter power spectrum





# SCIENCE MOTIVATIONS FOR STRONG LENSING

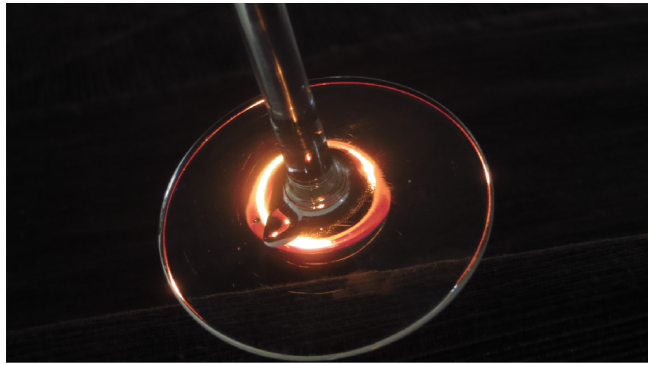
3 - Measure **comological parameters** ( $H_0$ ).

- Different images are produced because light follows **different paths**.
- These paths are of **different lengths**.
- If the source has time variability, this will cause **time delays** between different images.

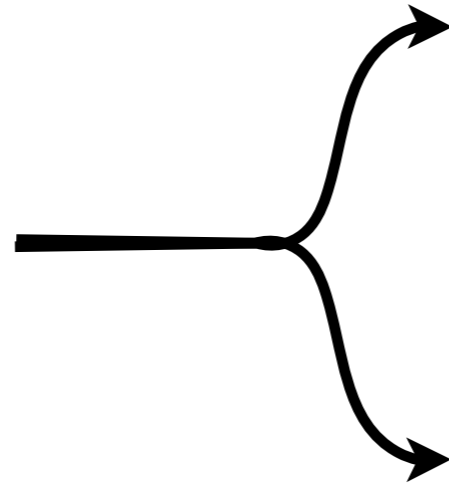




# LENSING ANALYSIS



Data

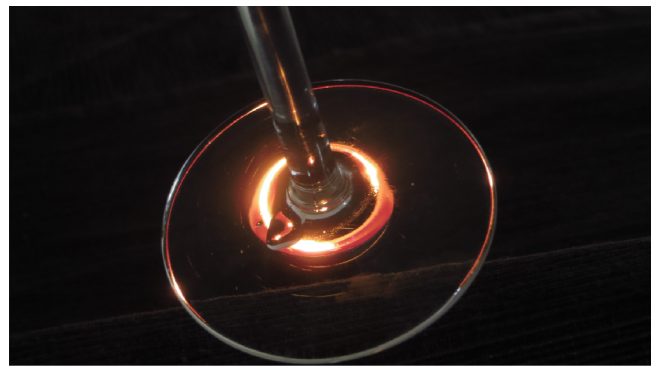


1: Morphology of the background source  
(the true, undistorted image of the candle)

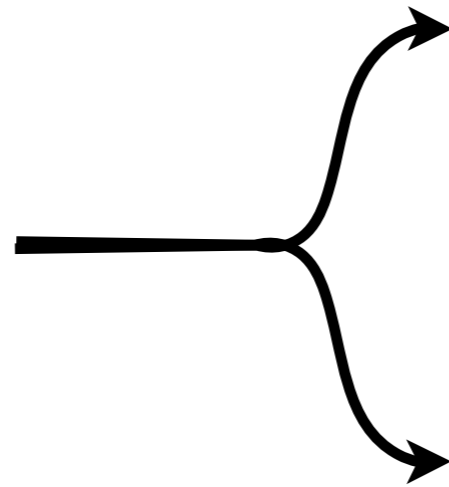


2: Matter distribution in the lens  
(the shape of the wineglass)

# LENSING ANALYSIS



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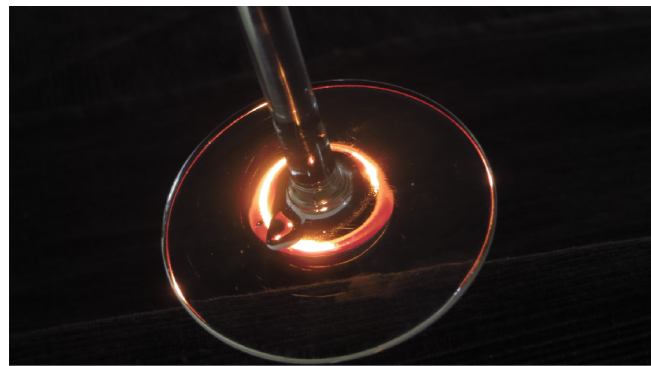
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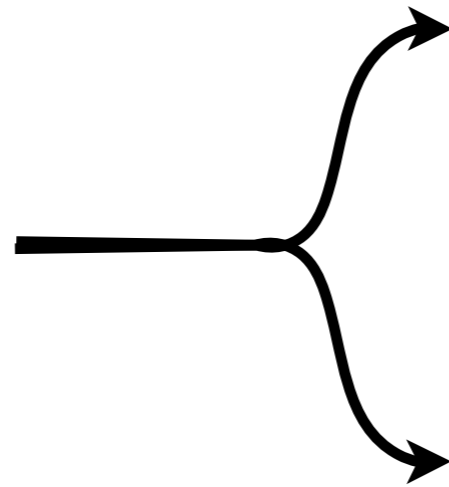
2: Matter distribution in the lens (the shape of the wineglass)

$$y = L(p)x + n$$

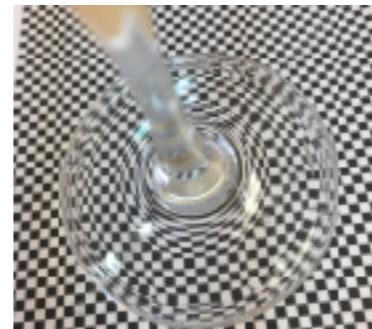
# LENSING ANALYSIS



Data



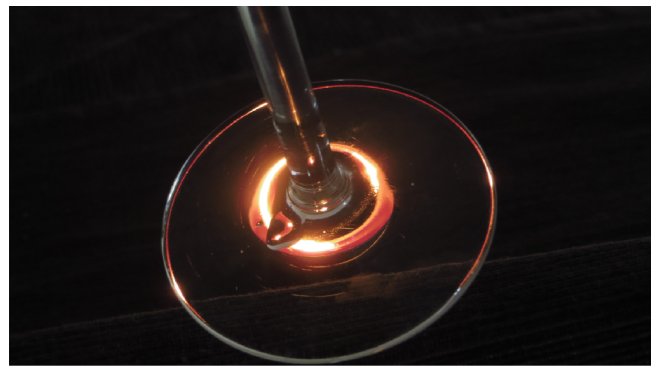
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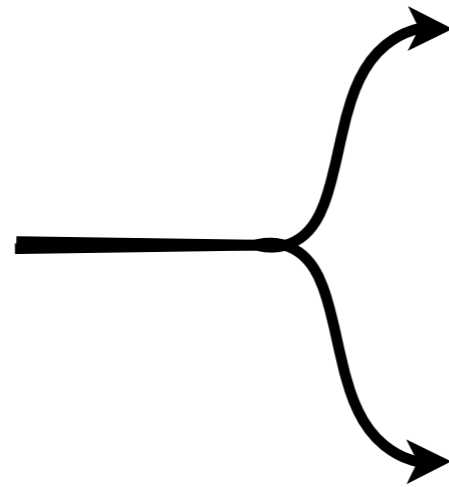
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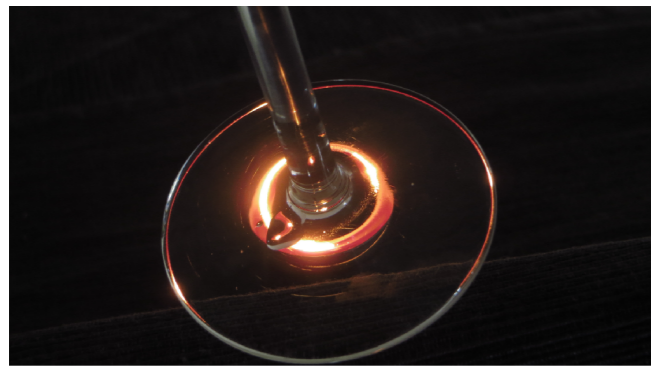


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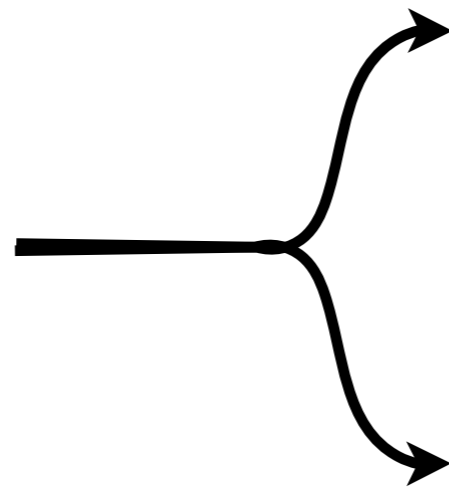
Source Parameters (linear)

Data  $\longrightarrow y = L(p)x + n$

# LENSING ANALYSIS



Data



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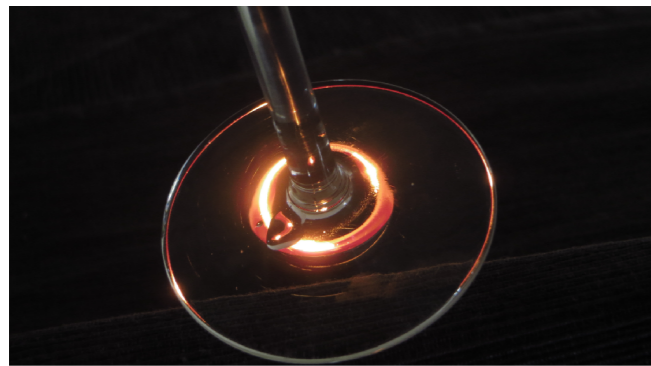
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Source Parameters (linear)

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Lens Parameters (non-linear)

# LENSING ANALYSIS



Data



1: Morphology of the background source  
(the true, undistorted image of the candle)



2: Matter distribution in the lens  
(the shape of the wineglass)

Source Parameters (linear)

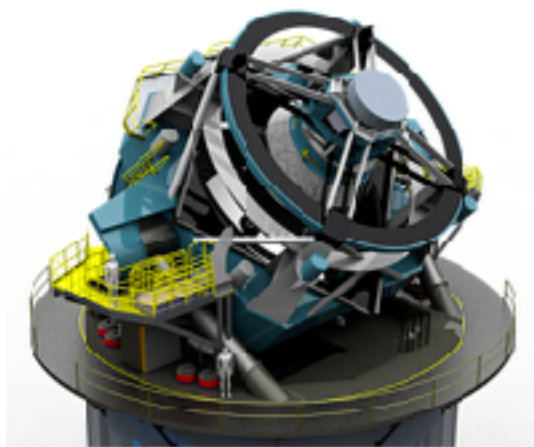
$$\text{Data} \longrightarrow y = L(p)x + n$$

Lens Parameters (non-linear)

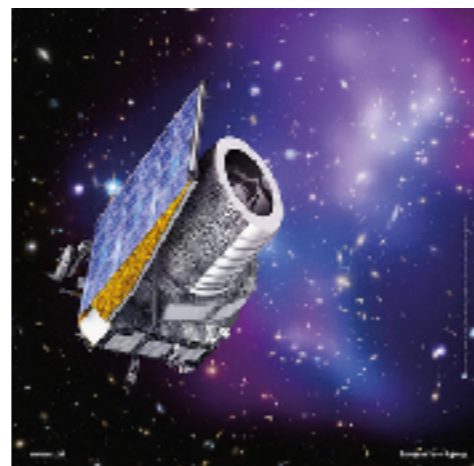
Noise

# LOOKING INTO THE FUTURE

In the next few years, we're expecting to discover more than 170,000 new lenses.



**LSST**



**euclid**  
consortium



NANCY GRACE  
**ROMAN**  
SPACE TELESCOPE

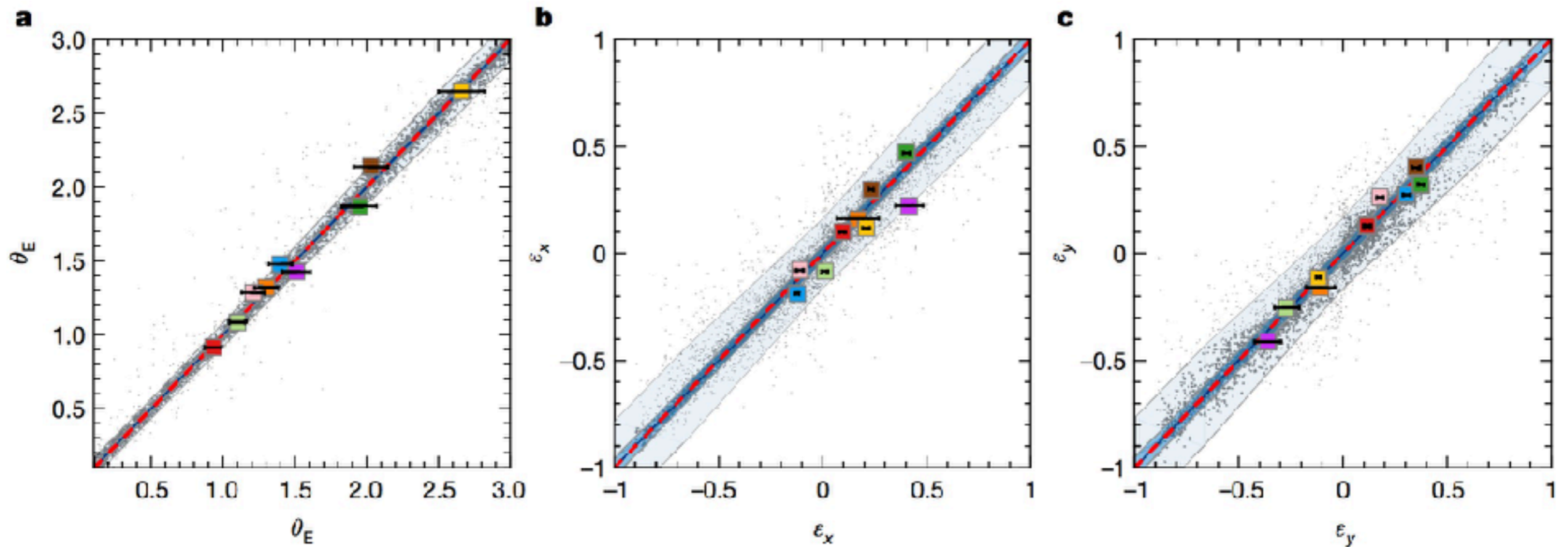
## Methods for the future:

How are we going to analyze 170,000 lenses?

- Lens modeling is **very slow**.
- Simple lens model takes ~3 days  
=> **1,400 years !**



# ESTIMATING THE MATTER DISTRIBUTION PARAMETERS WITH CNNs



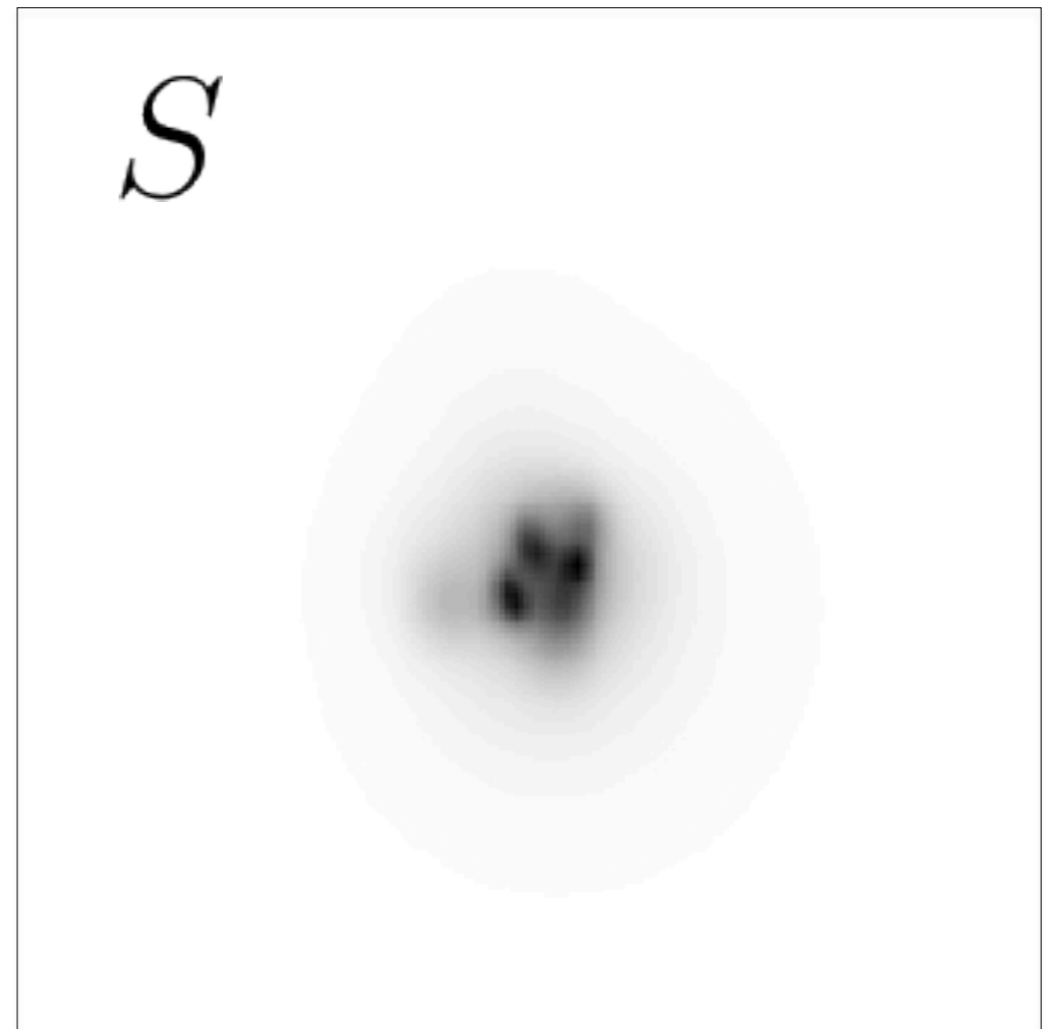
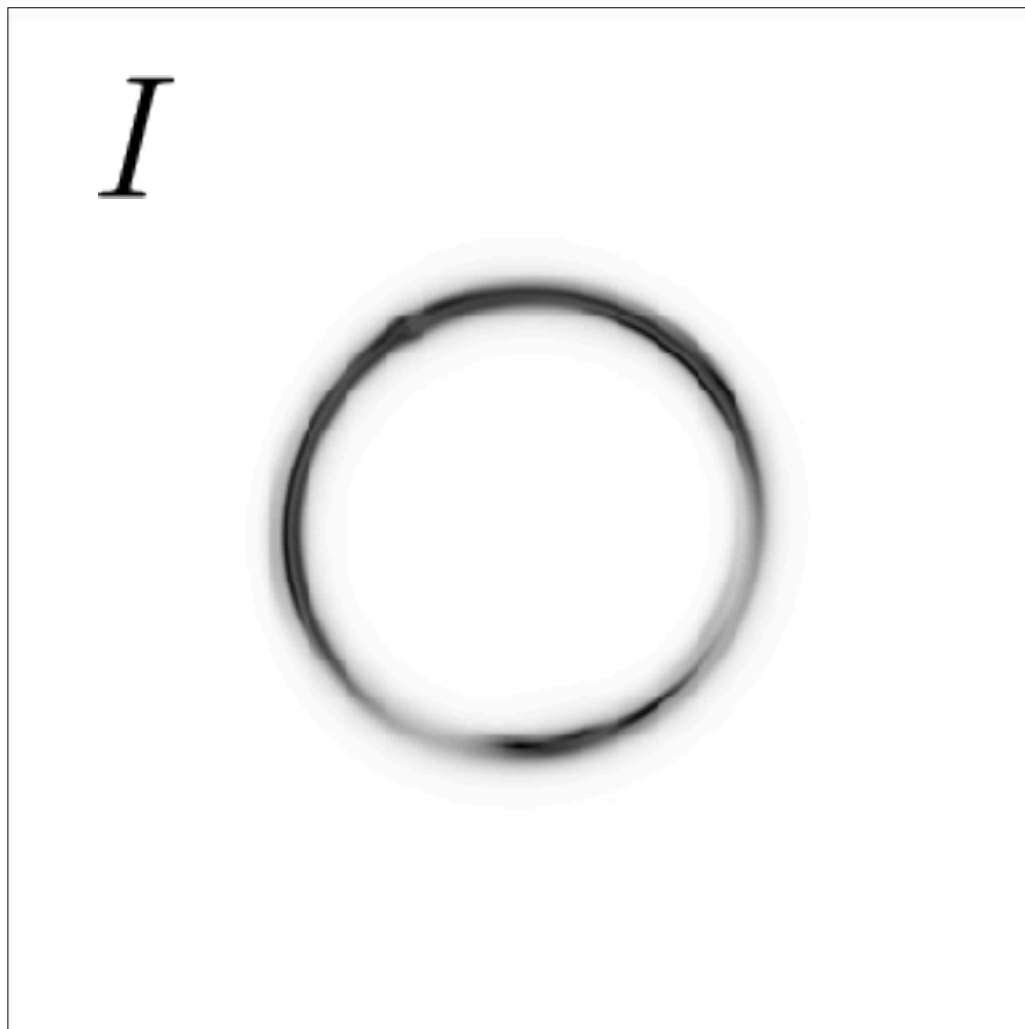
**10 million** times faster than traditional lens modeling.

**0.01 seconds** on a **single GPU**

# UNDISTORTED IMAGE OF THE BACKGROUND SOURCE

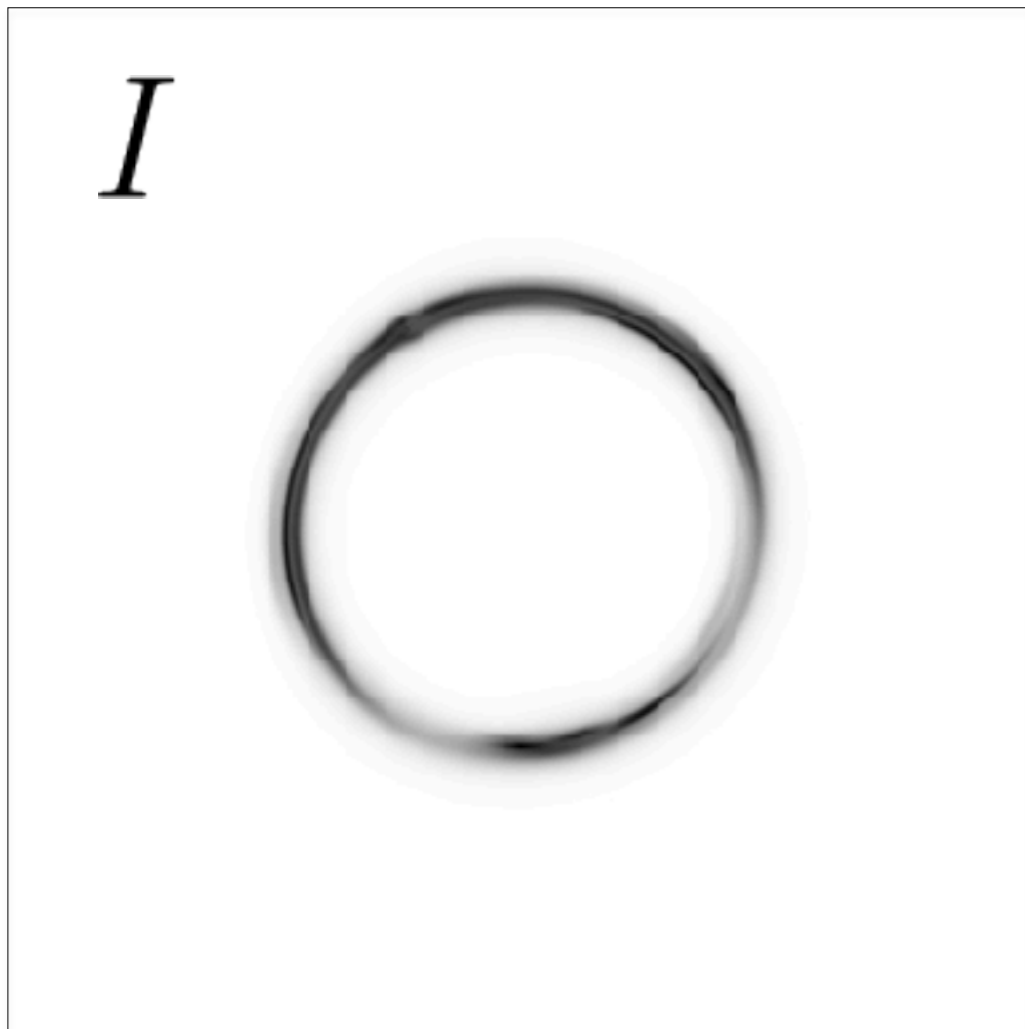


PIXEL VALUES OF THE BACKGROUND SOURCE ARE LINEAR  
PARAMETERS



$$I = L(p)S$$

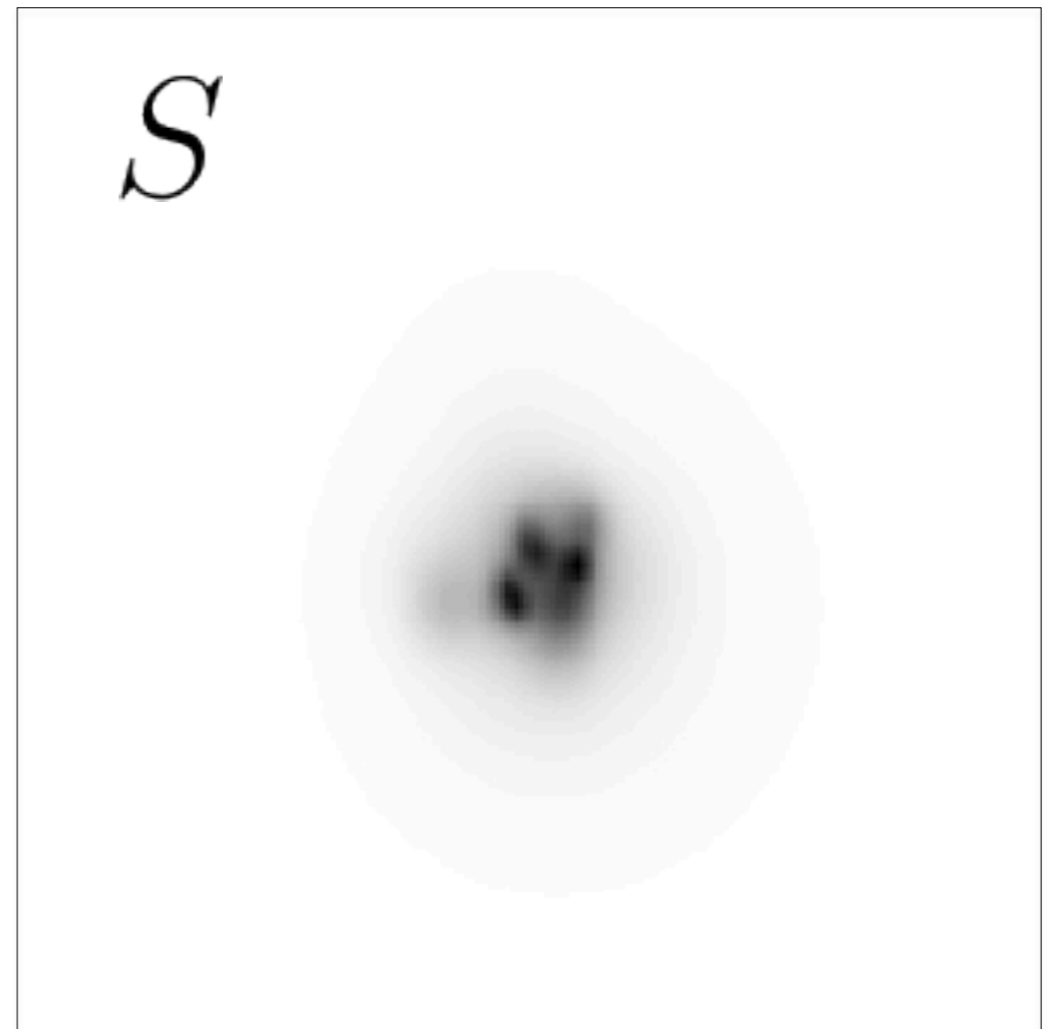
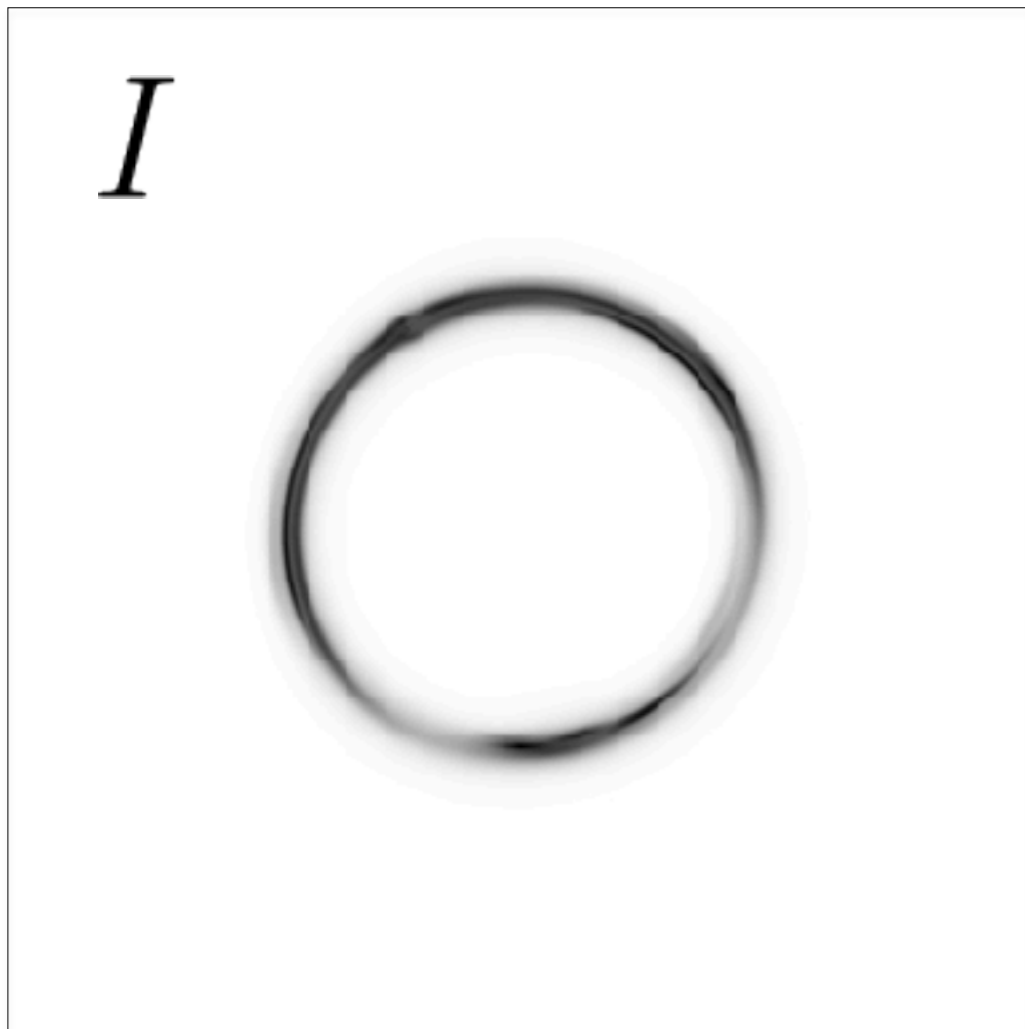
PIXEL VALUES OF THE BACKGROUND SOURCE ARE LINEAR  
PARAMETERS



$$I = L(p)S$$

$$S = (L^T C_N^{-1} L)^{-1} L^T C_N^{-1} D$$

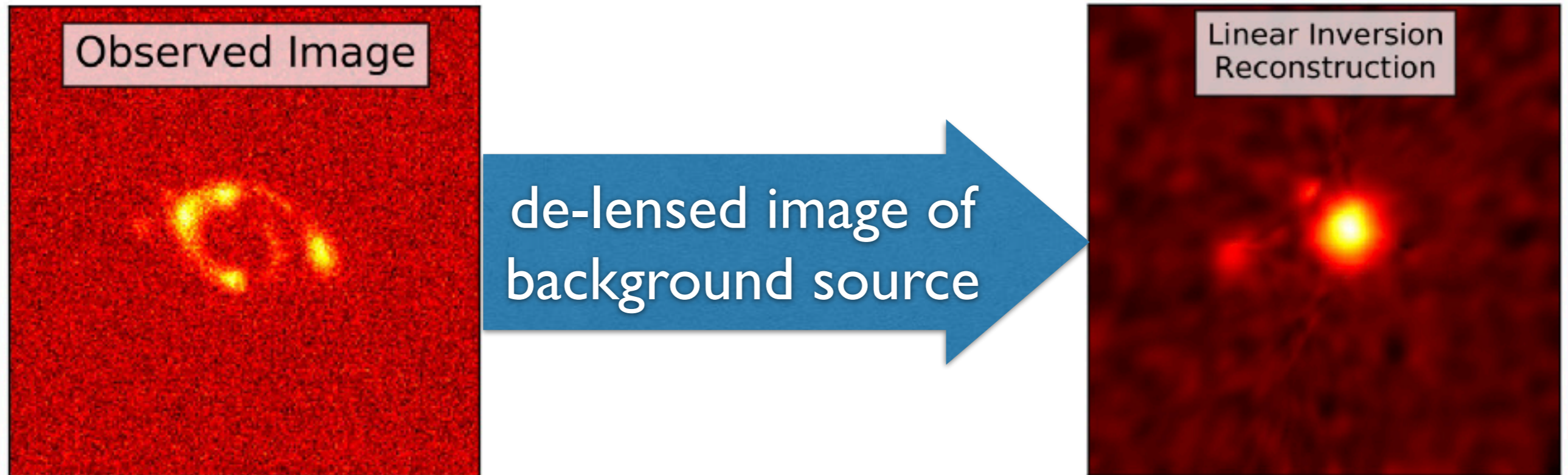
PIXEL VALUES OF THE BACKGROUND SOURCE ARE LINEAR  
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$$I = L(p)S$$

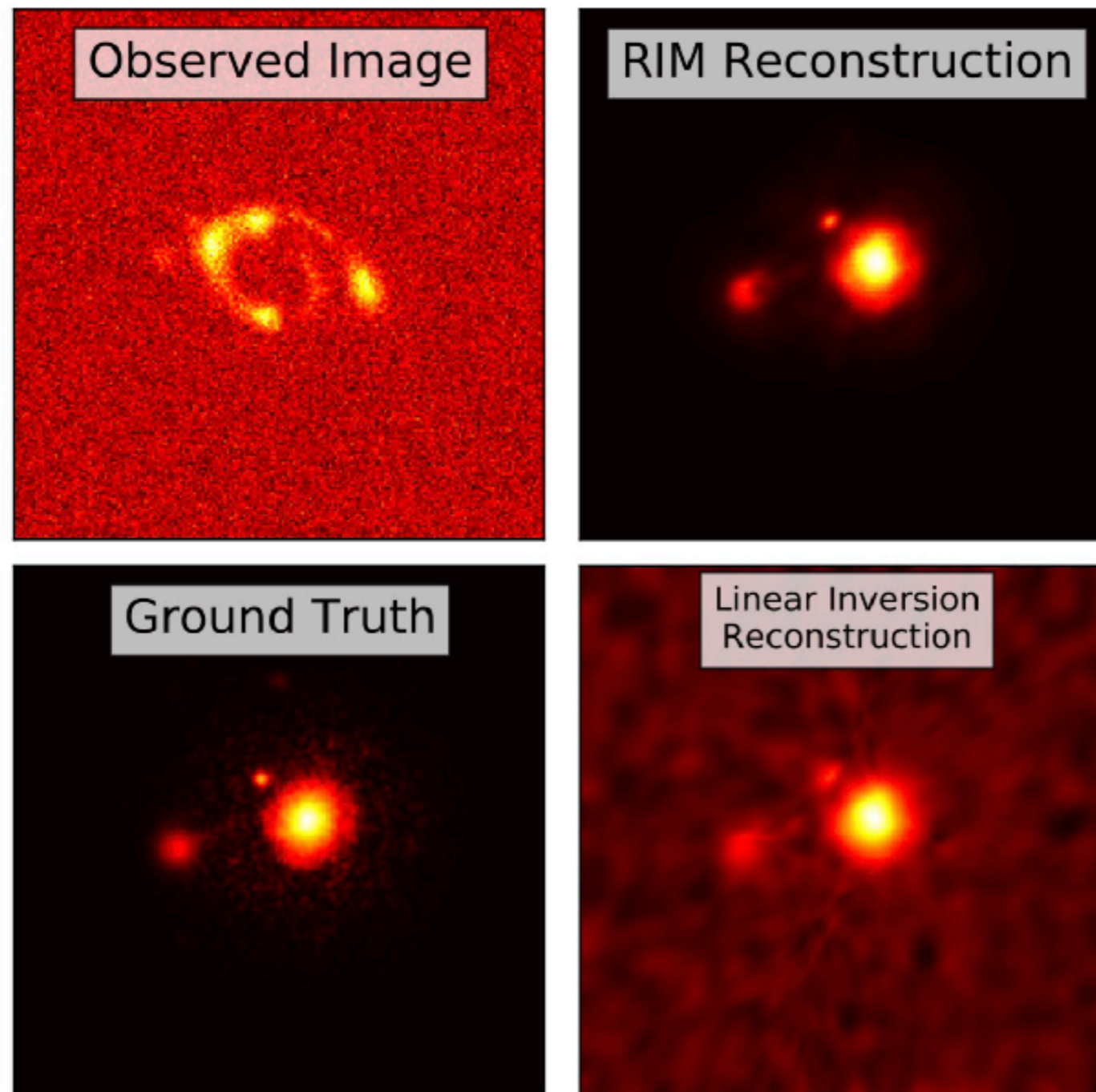
$$S = (L^T C_N^{-1} L + C_p^{-1})^{-1} L^T C_N^{-1} D$$

# UNDISTORTED IMAGE OF THE BACKGROUND SOURCE

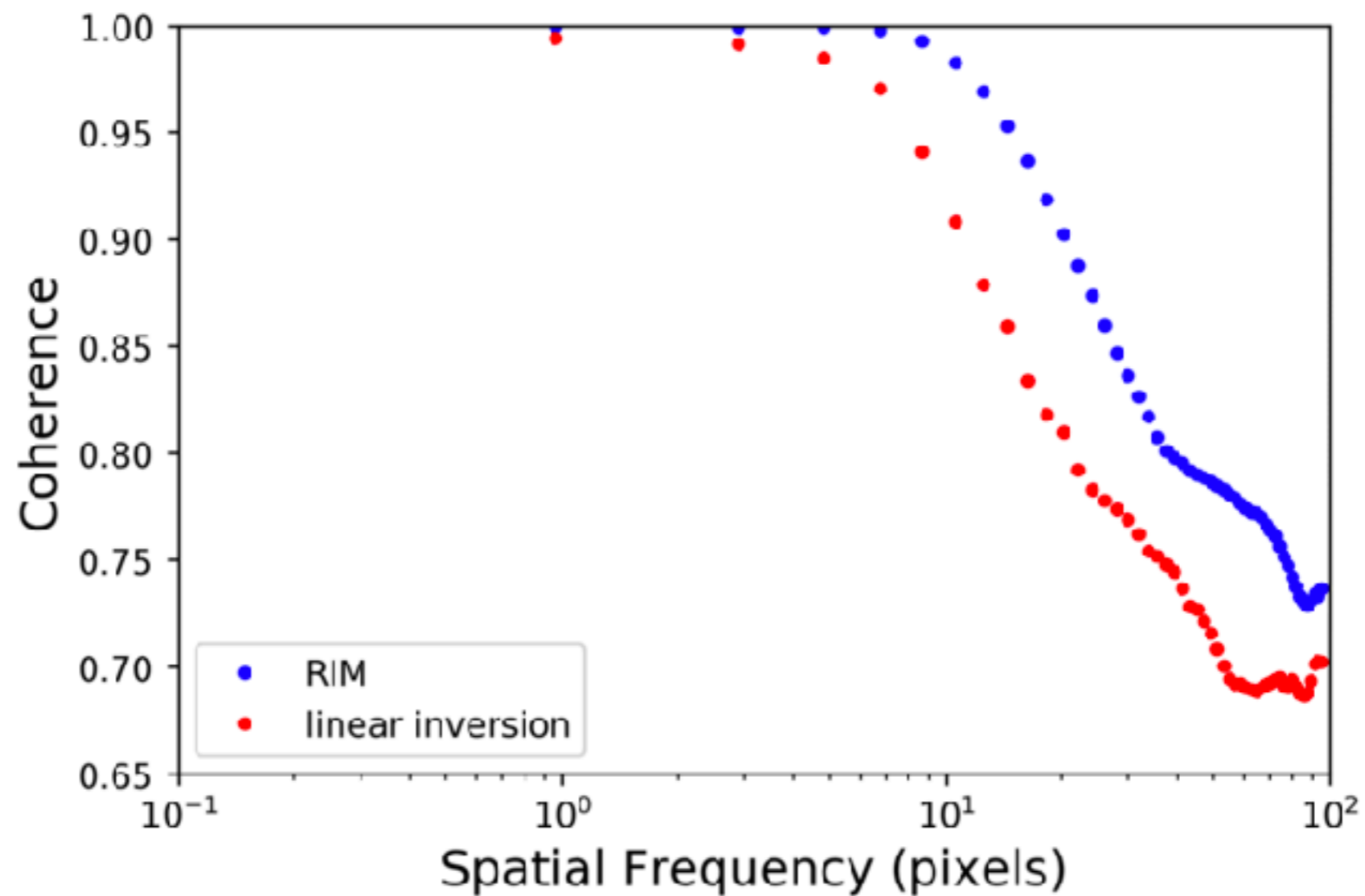


$$S = (L^T C_N^{-1} L + C_p^{-1})^{-1} L^T C_N^{-1} D$$

# UNDISTORTED IMAGE OF THE BACKGROUND SOURCE WITH THE RECURRENT INFERENCE MACHINE (RIM)



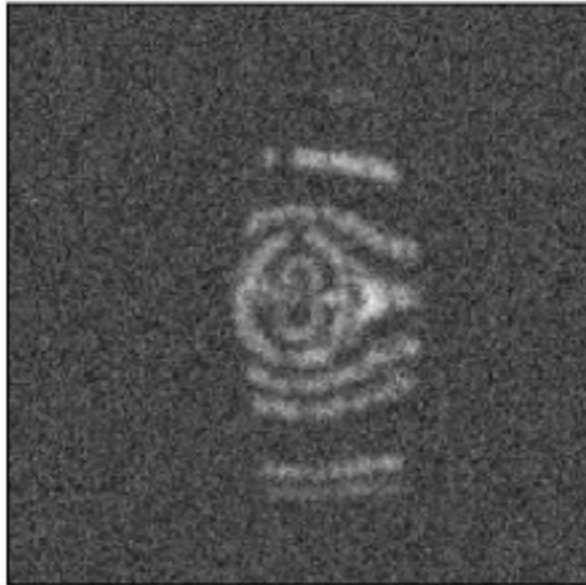
# BACKGROUND SOURCE RECONSTRUCTION: COMPARISON TO MAXIMUM LIKELIHOOD METHODS



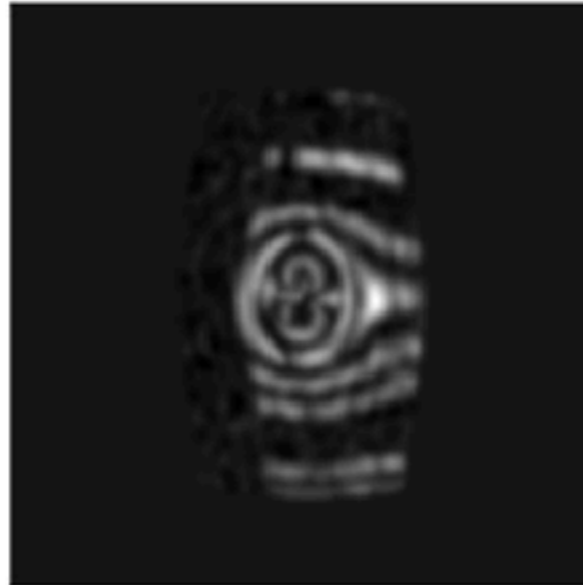


# EXAMPLES OUTSIDE THE TRAINING DATA

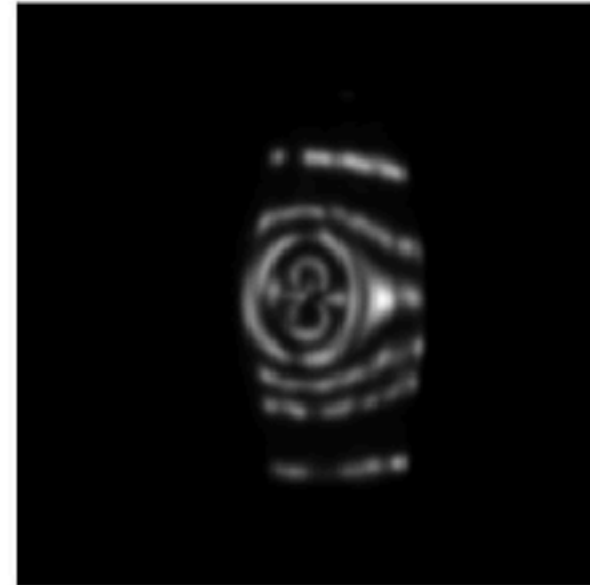
Data



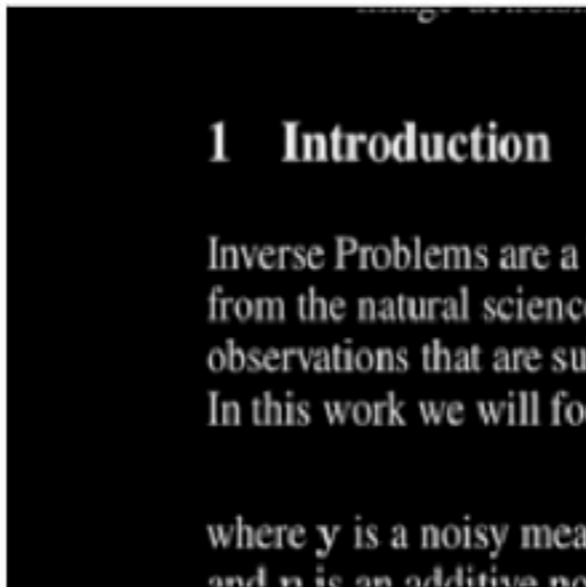
Linear Model



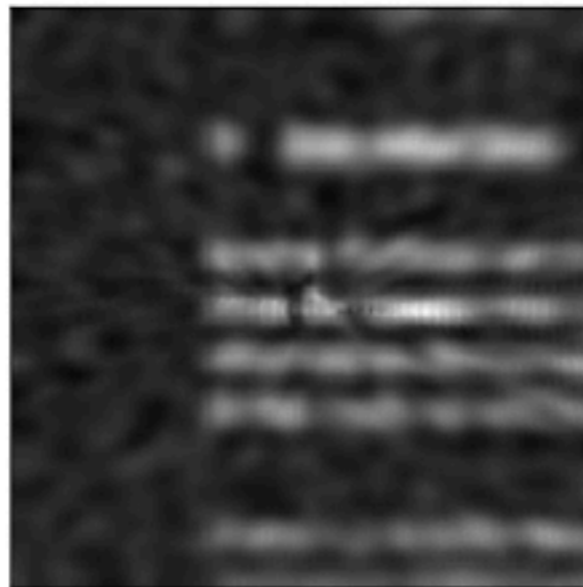
RIM Model



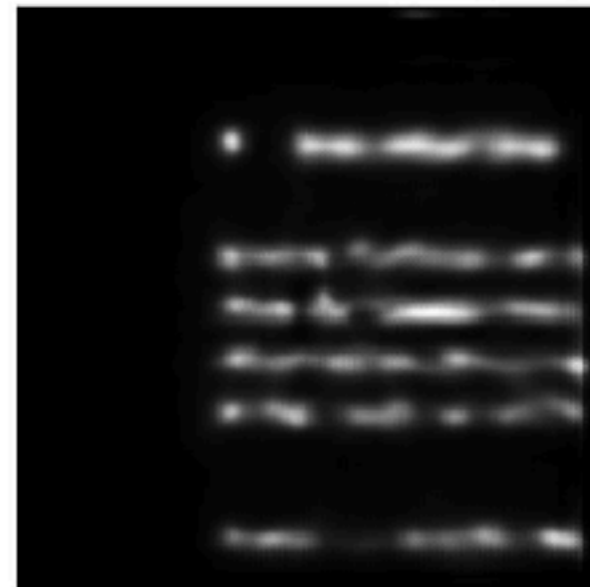
True Source

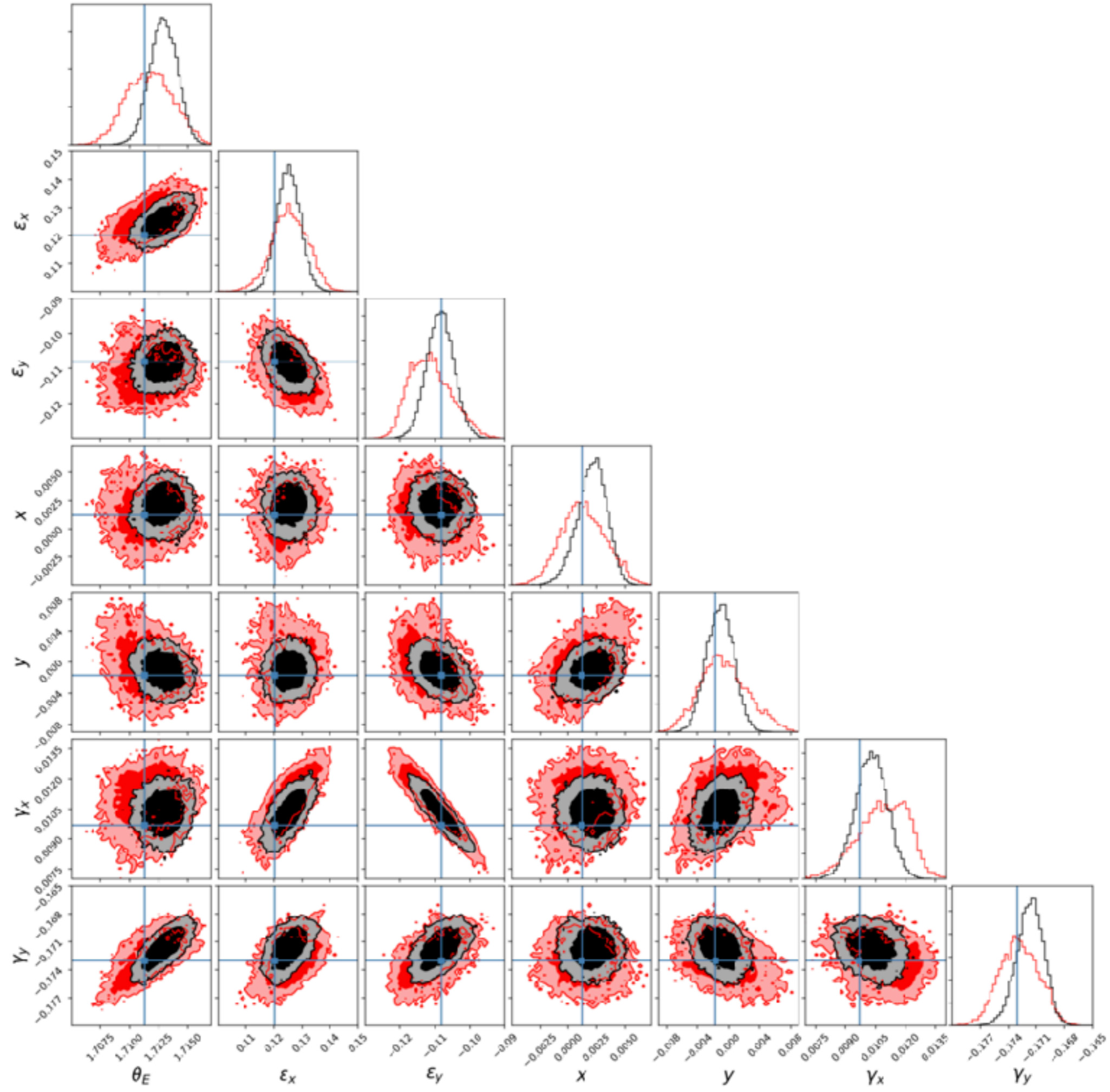


Reconstructed Source (Linear)



Reconstructed Source (RIM)





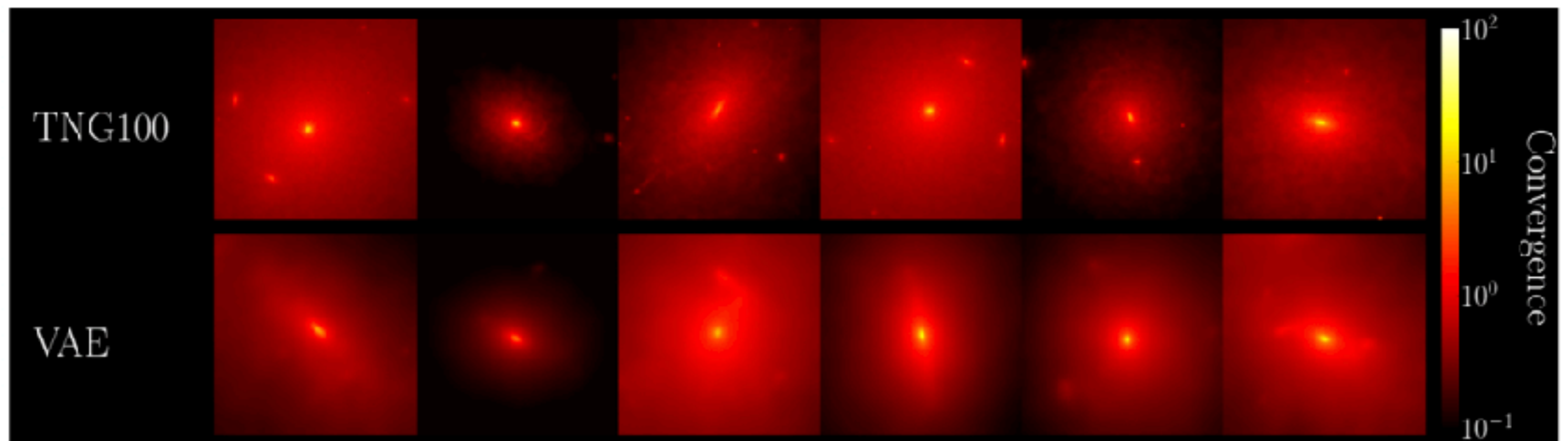
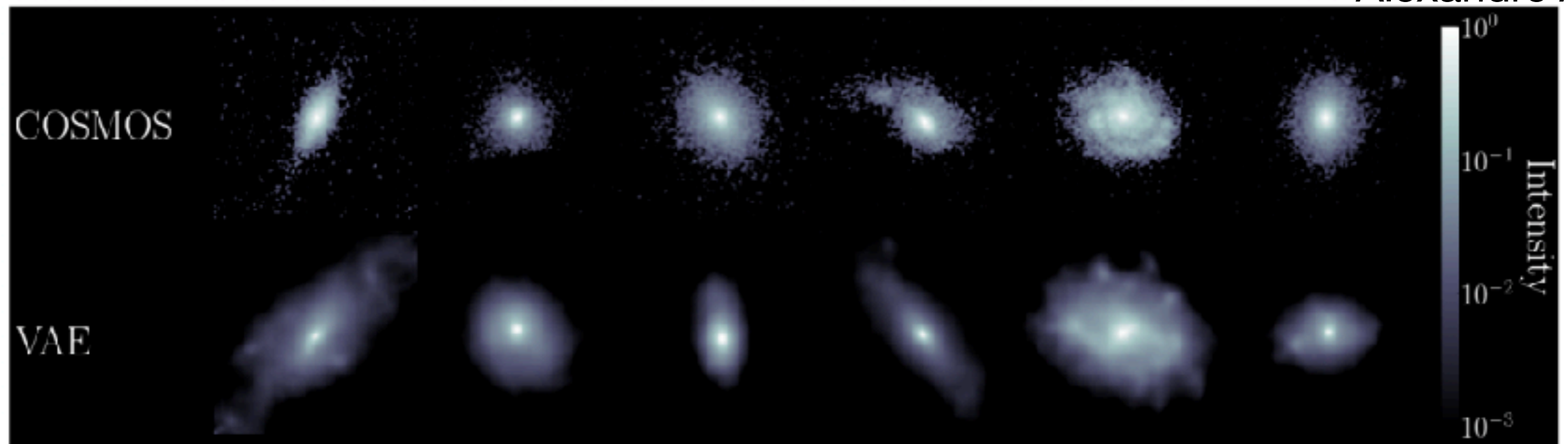




# SIMULATED GALAXIES GENERATED WITH A VARIATIONAL AUTOENCODER



Alexandre Adam



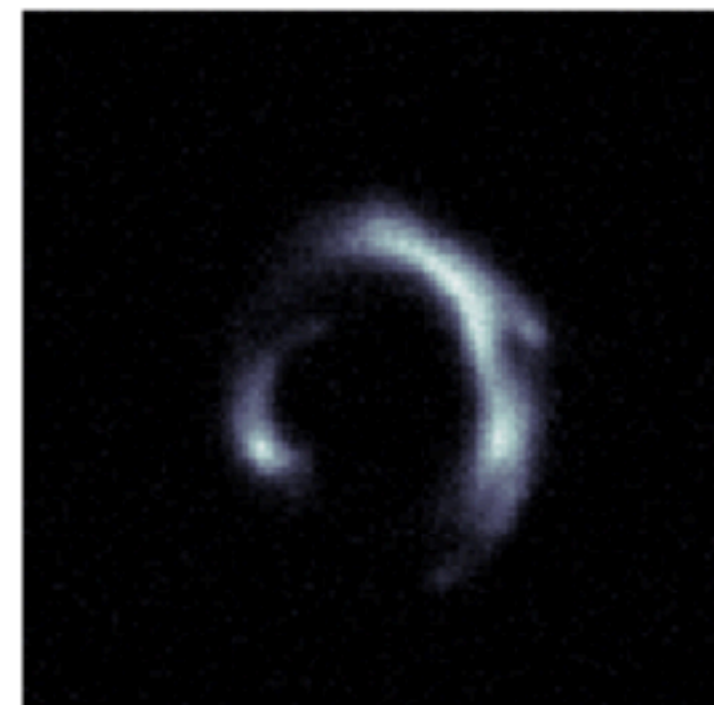
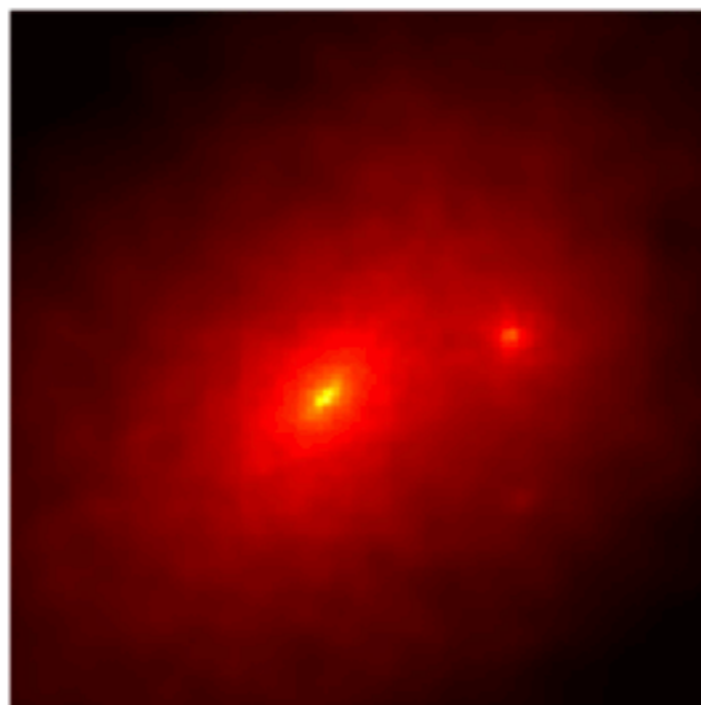
# TRAINING ON HYDRODYNAMICAL SIMULATIONS

Background

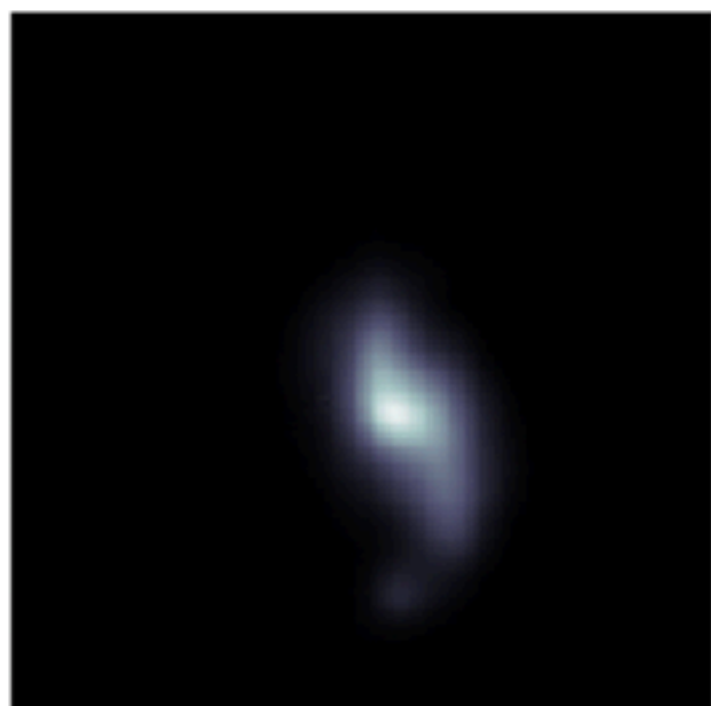
Foreground

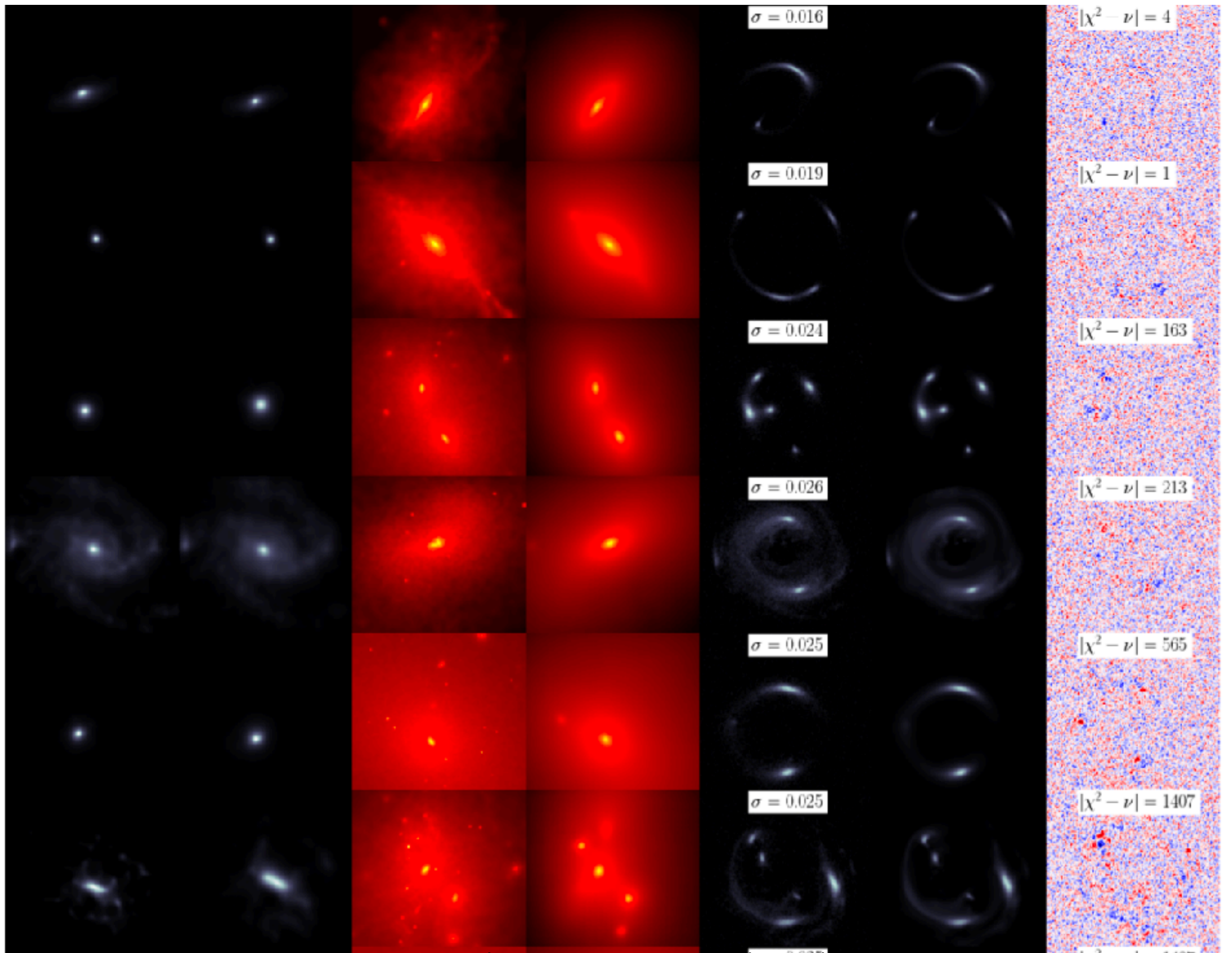
Lensed Image

Ground Truth

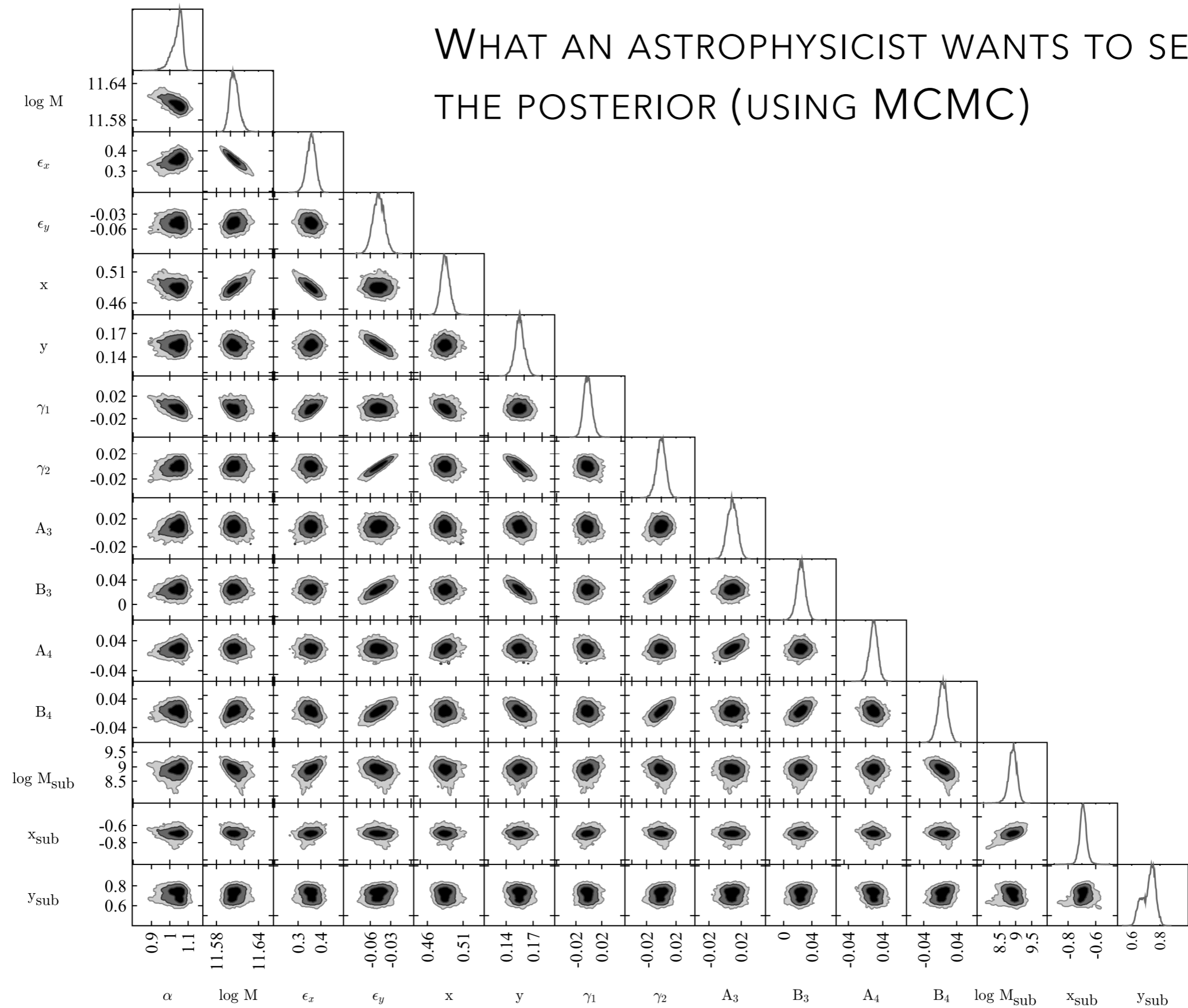


Prediction



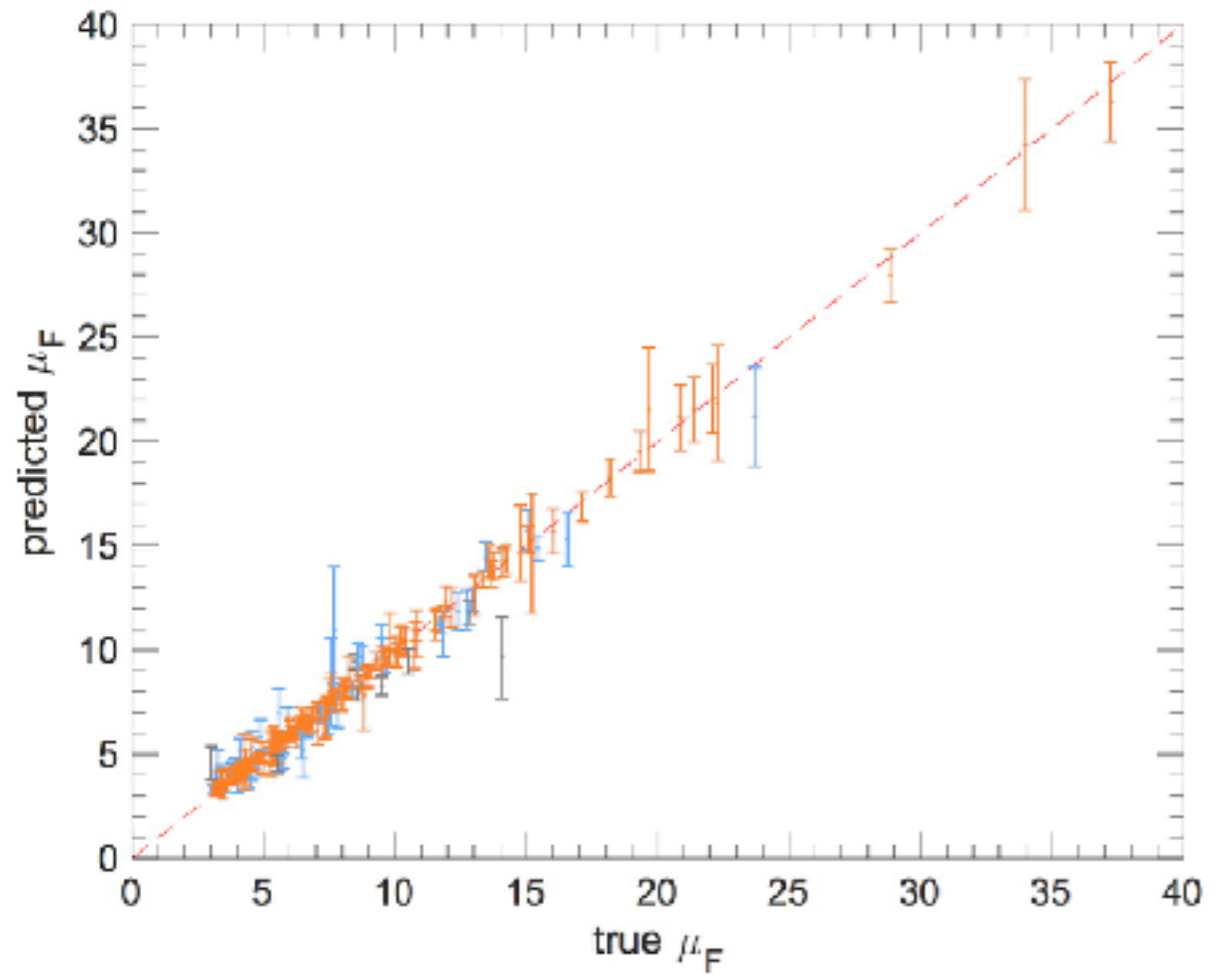


# WHAT AN ASTROPHYSICIST WANTS TO SEE: THE POSTERIOR (USING MCMC)

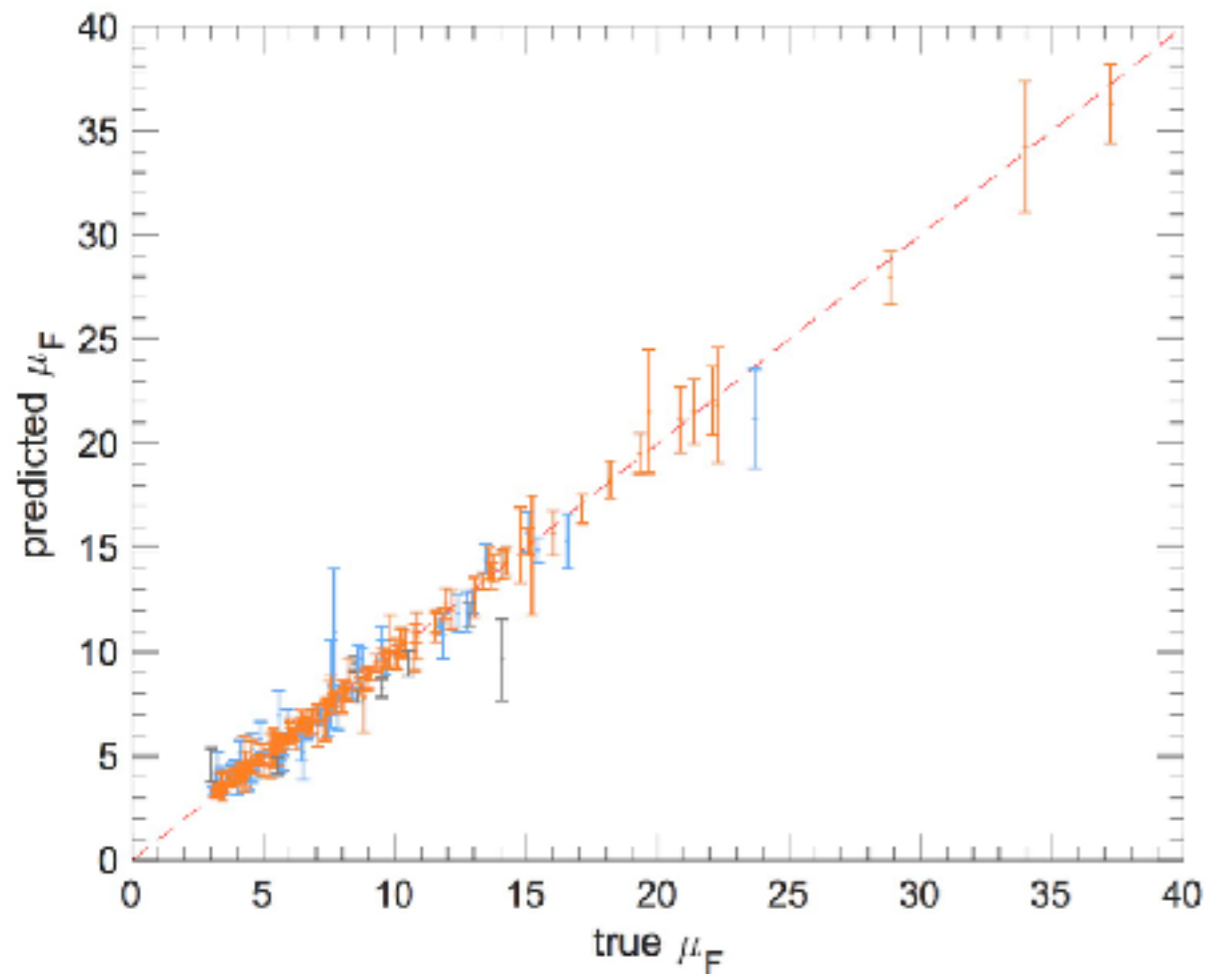




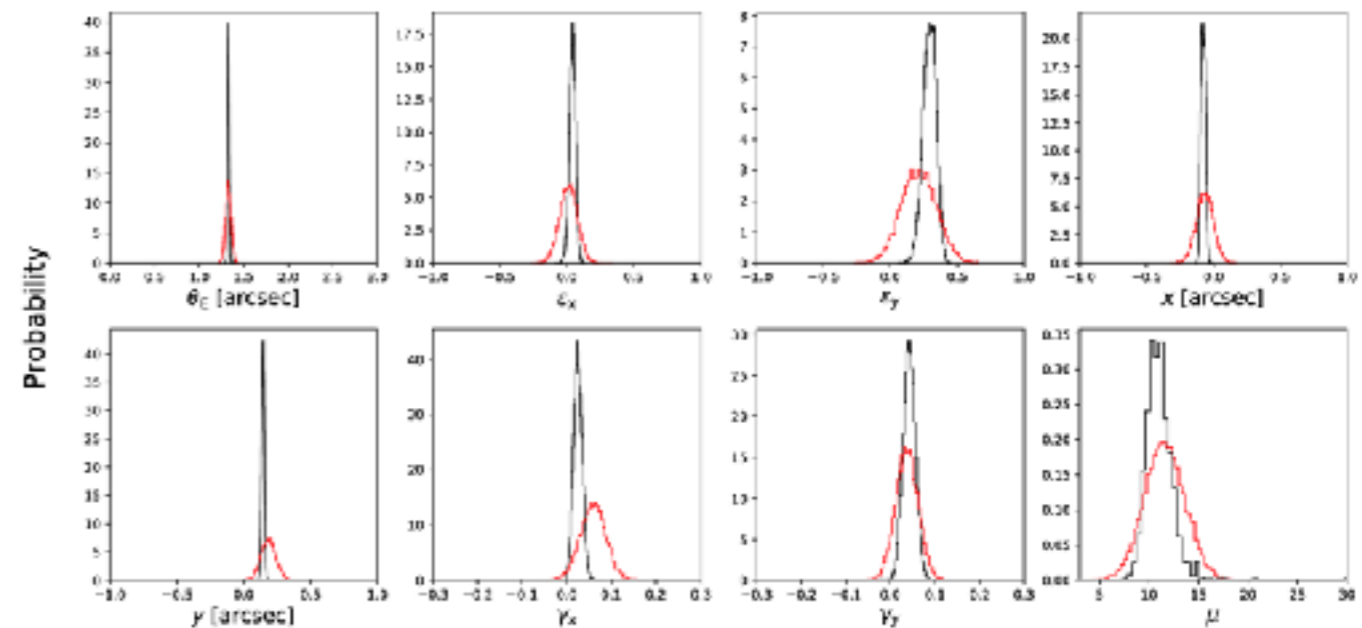
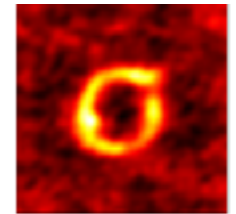
# UNCERTAINTY ESTIMATION WITH APPROXIMATE BAYESIAN NEURAL NETWORKS



# UNCERTAINTY ESTIMATION WITH APPROXIMATE BAYESIAN NEURAL NETWORKS



Max-likelihood lens modeling (black)  
Neural Networks (red)

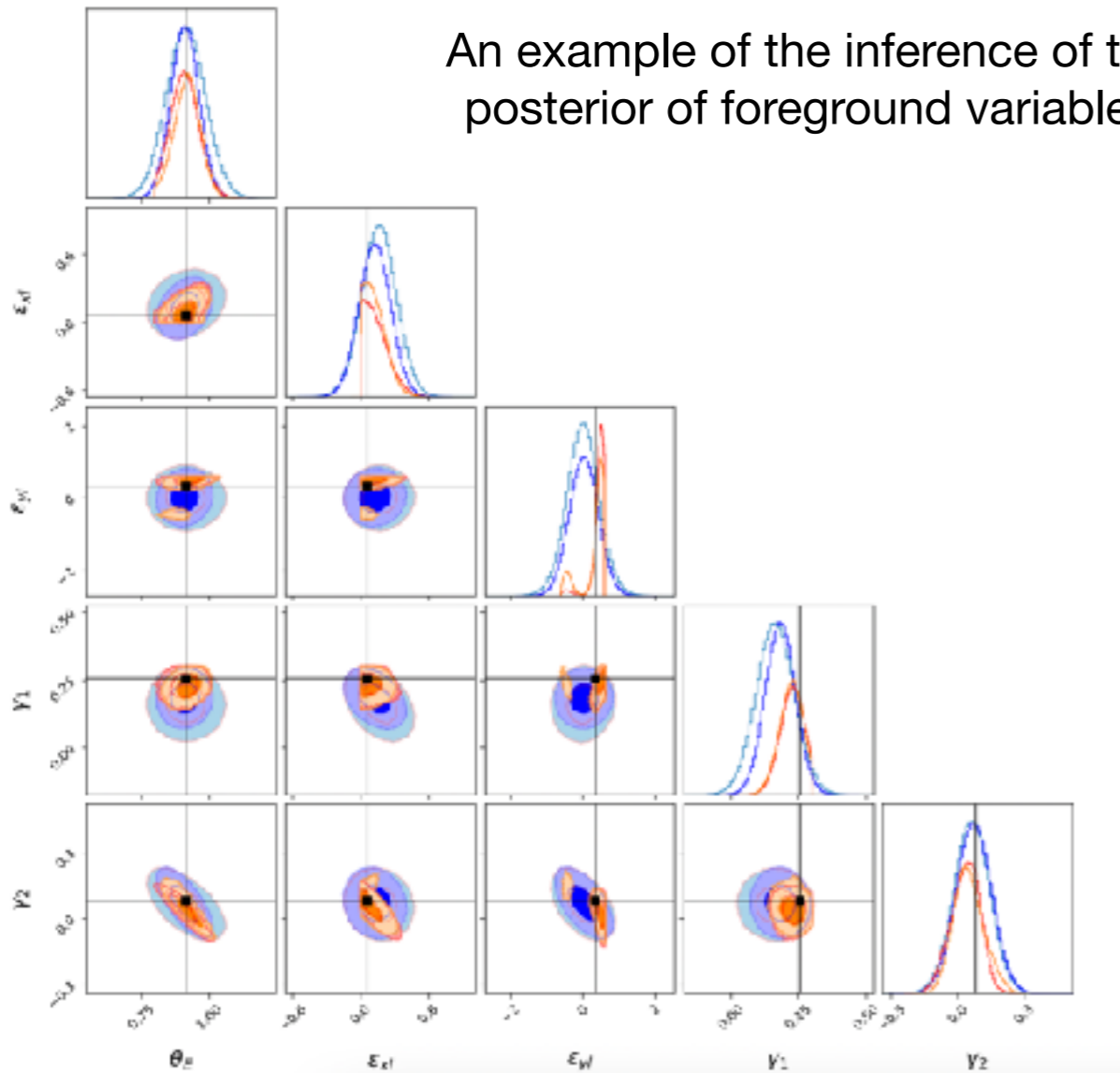


# UNCERTAINTY ESTIMATION WITH SIMULATION-BASED INFERENCE METHODS

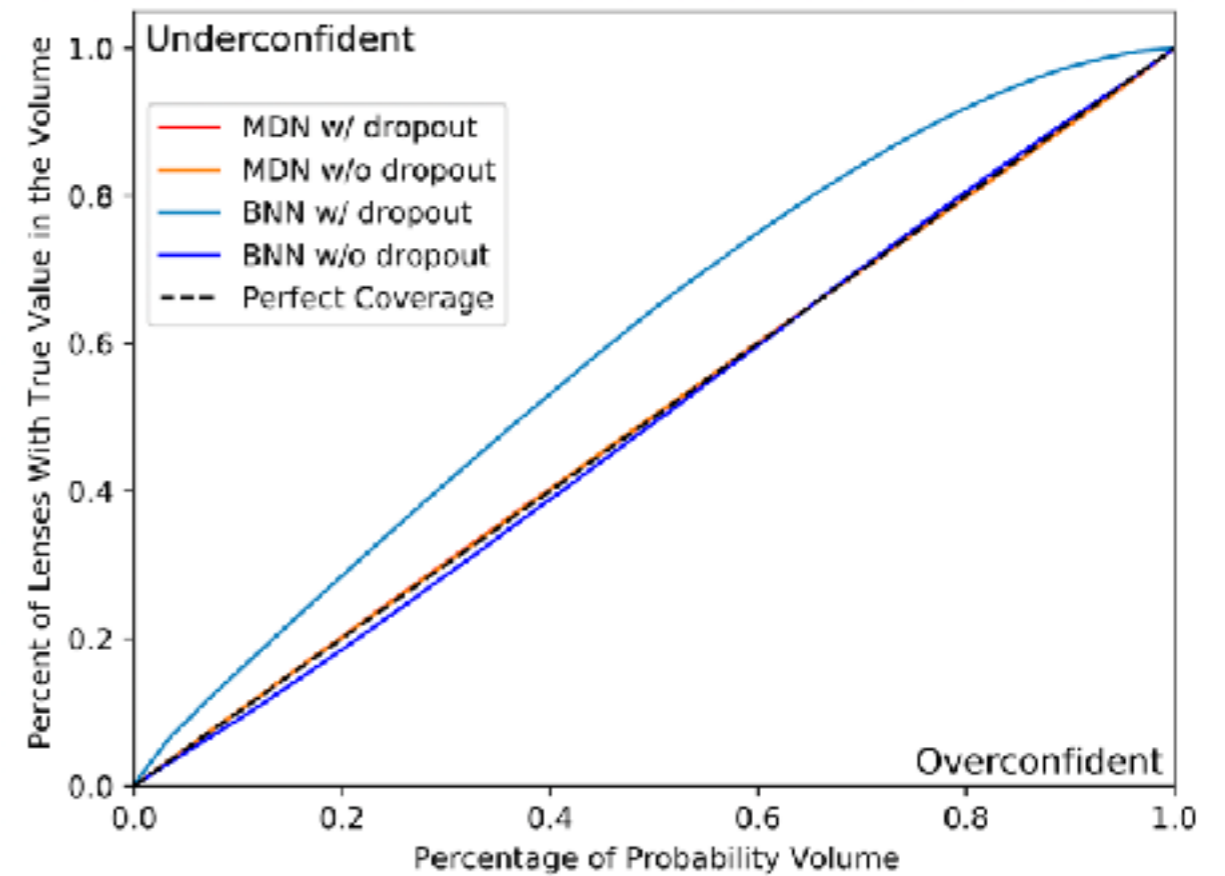


Ronan Legin

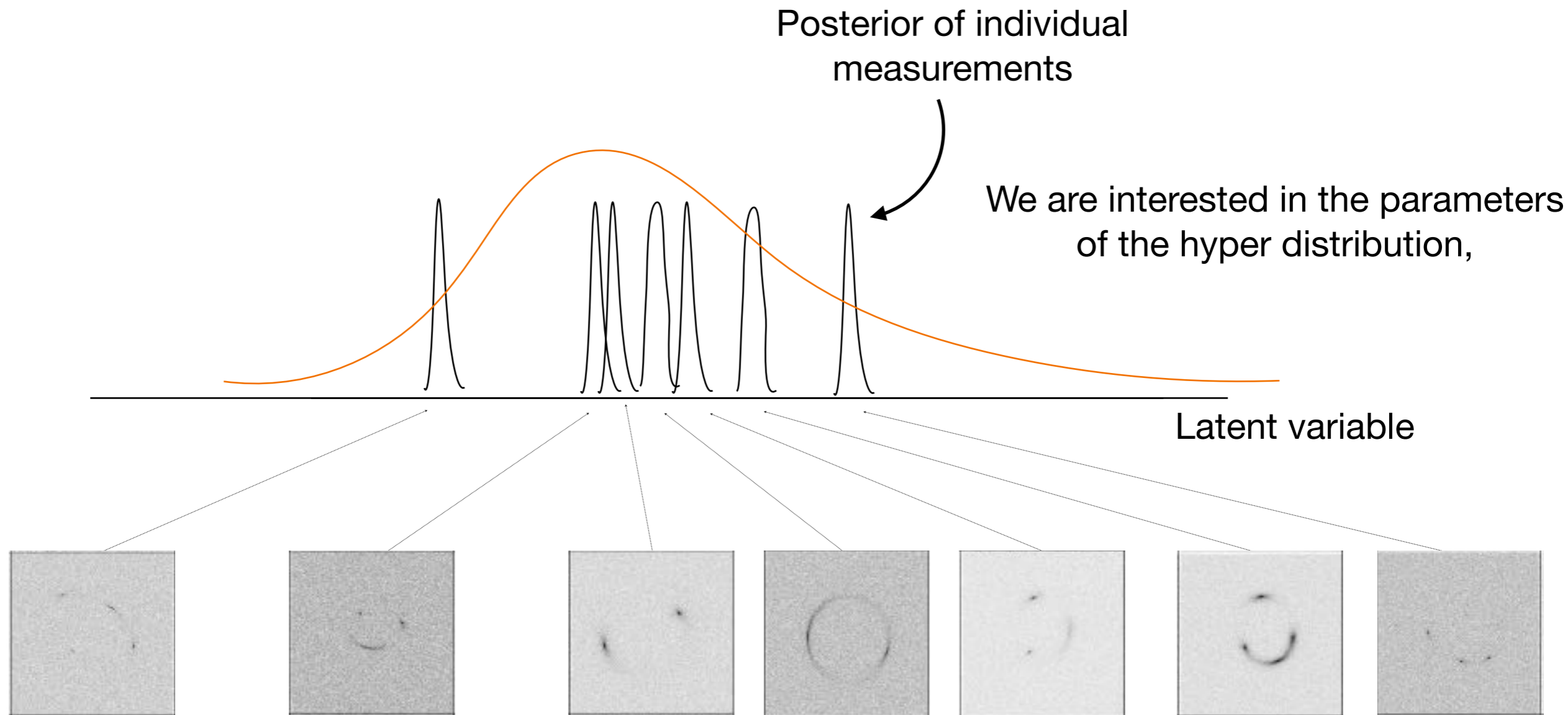
An example of the inference of the posterior of foreground variables



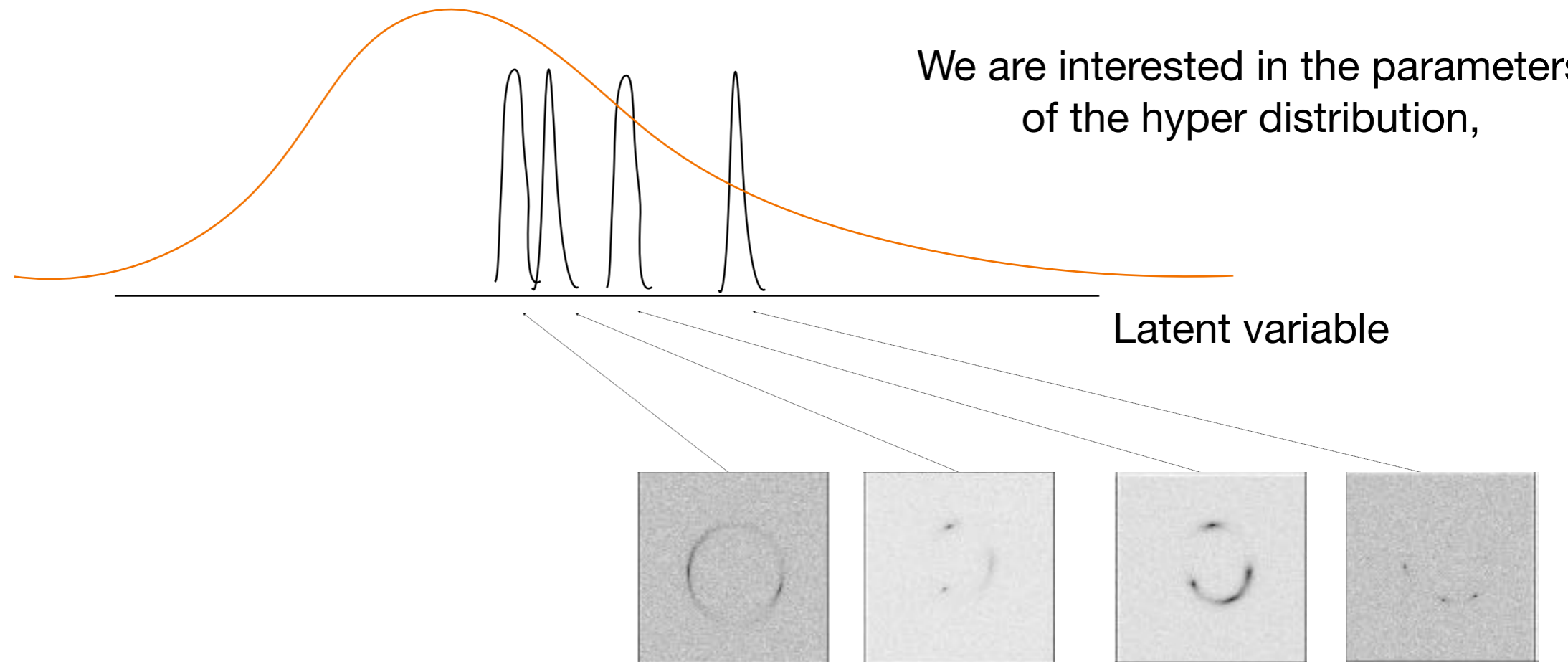
Coverage probabilities



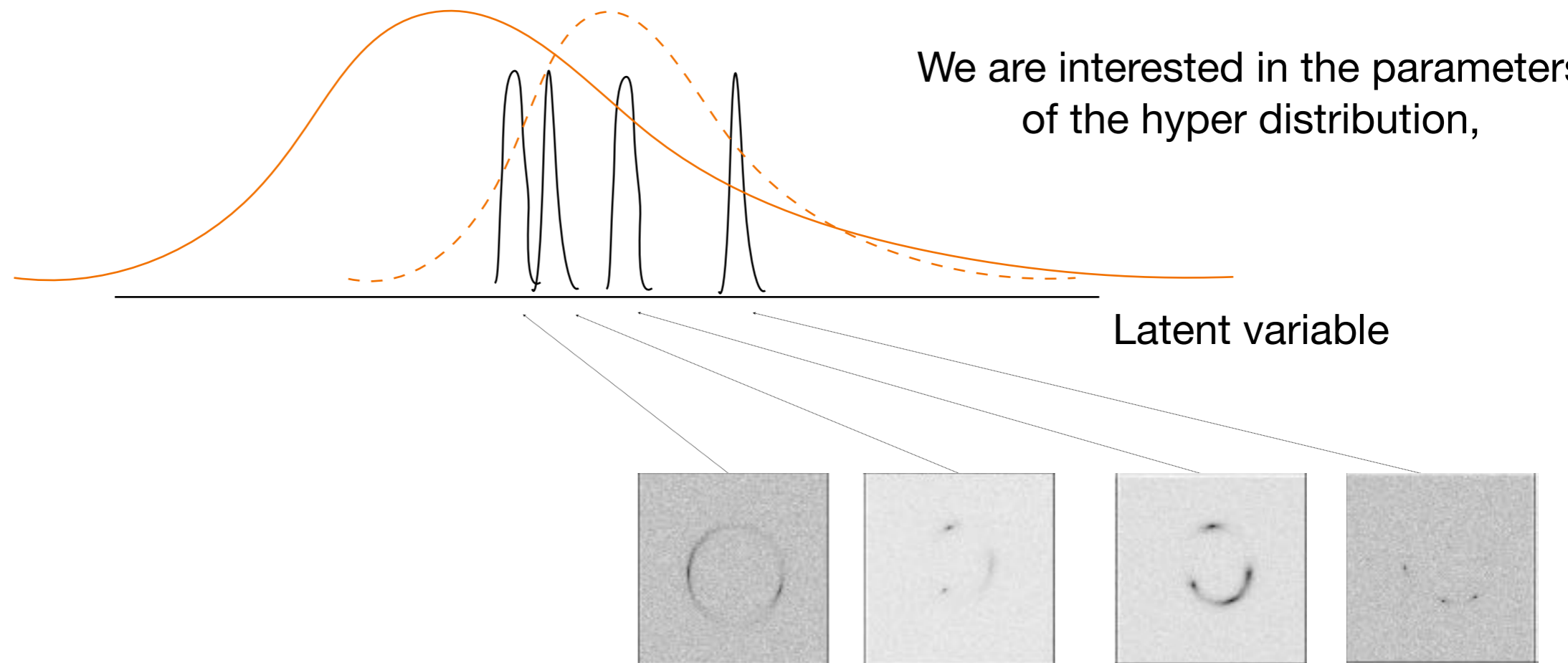
# Hierarchical Bayesian inference



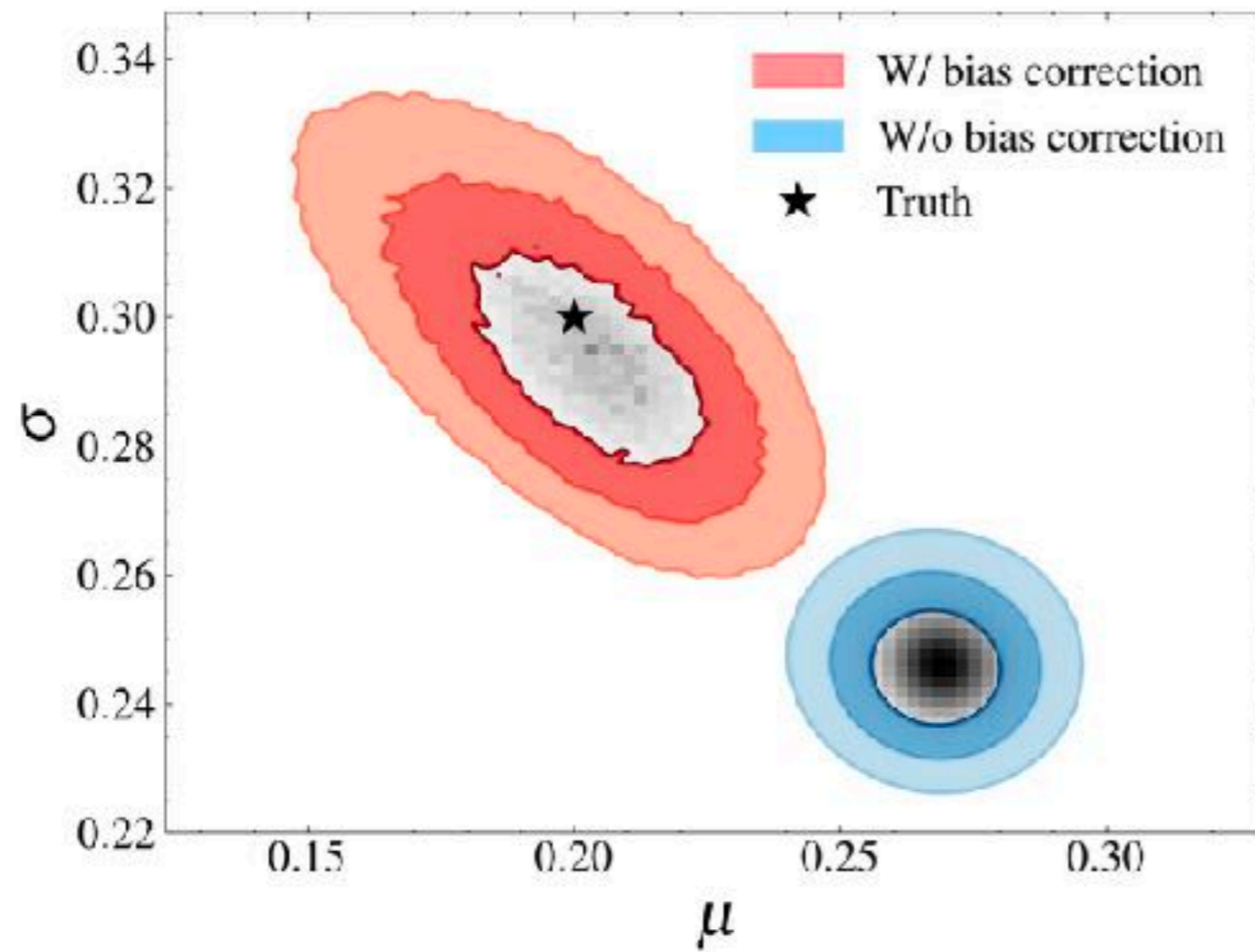
# Hierarchical Bayesian inference



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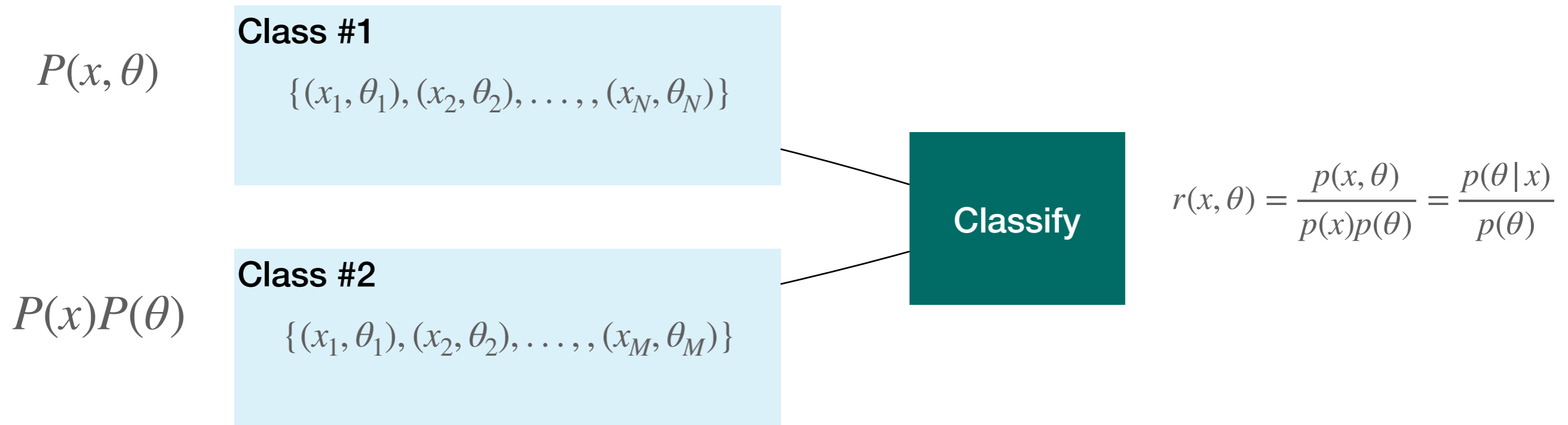


Ronan  
Legin



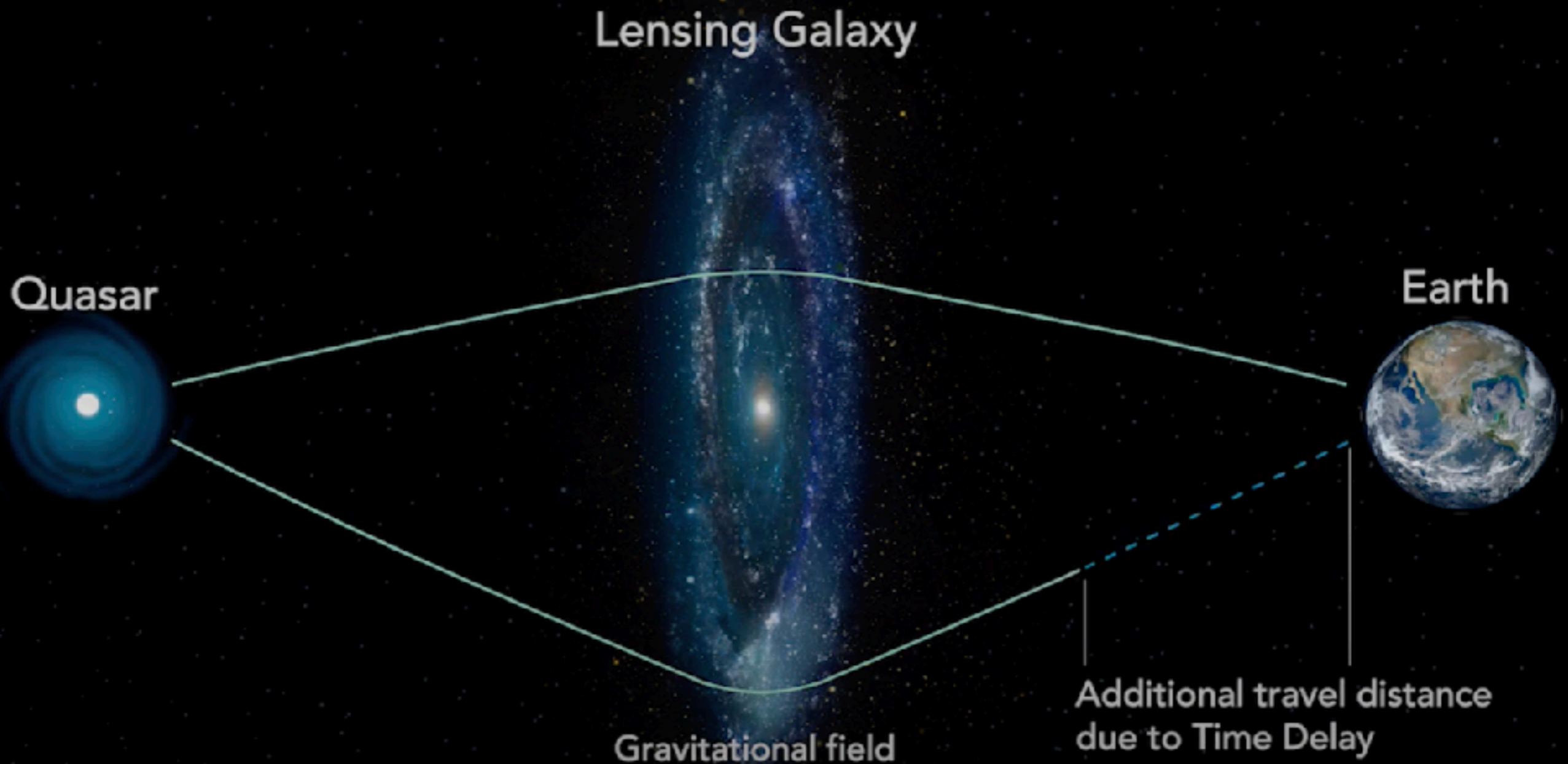
Connor  
Stone

# NEURAL RATIO ESTIMATORS



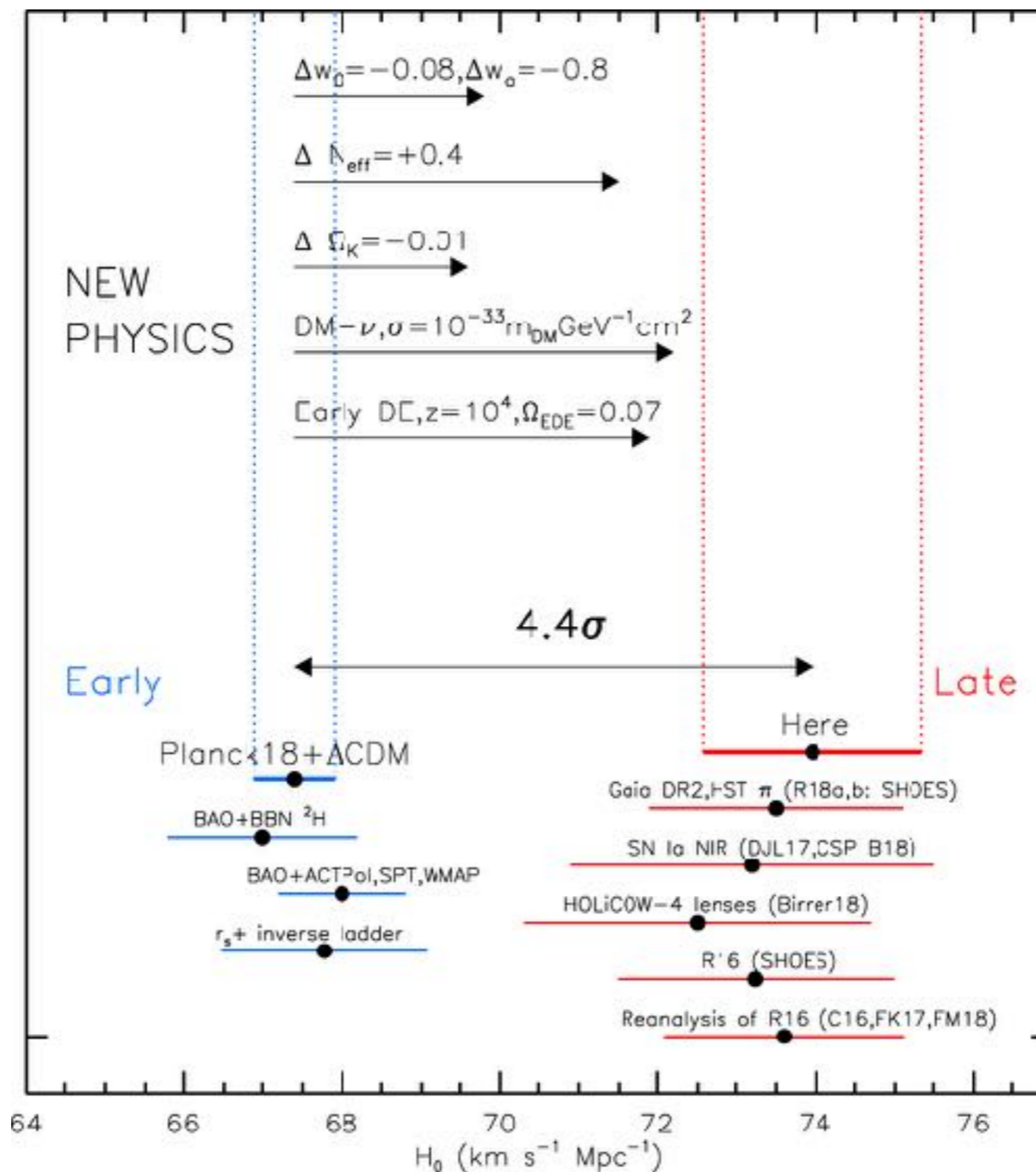


# H0 INFERENCE WITH TIME DELAY COSMOGRAPHY



# THE HUBBLE CONSTANT

## DISCREPANCY BETWEEN MEASUREMENTS



# H0 INFERENCE WITH NEURAL RATIO ESTIMATORS

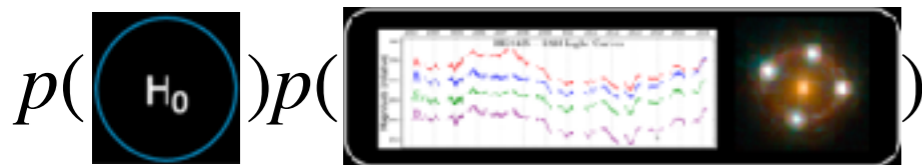
$P(\theta, x)$



**Class #1**

$\{(x_1, \theta_1), (x_2, \theta_2), \dots, (x_N, \theta_N)\}$

$P(\theta)P(x)$



**Class #2**

$\{(x_1, \theta_1), (x_2, \theta_2), \dots, (x_M, \theta_M)\}$

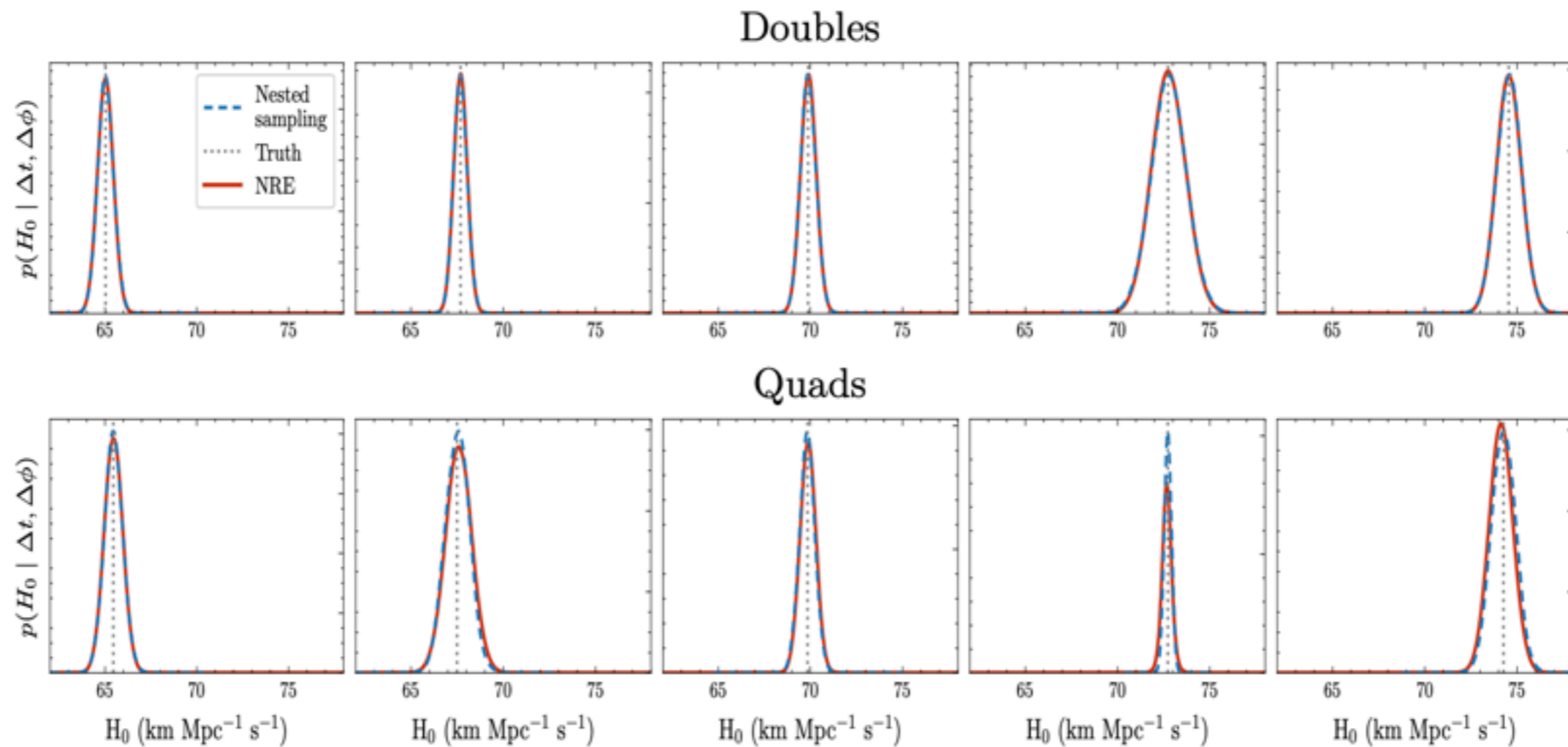
**Classify**

$$r(x, \theta) = \frac{p(x, \theta)}{p(x)p(\theta)} = \frac{p(\theta | x)}{p(\theta)}$$



# H0 INFERENCE WITH NEURAL RATIO ESTIMATORS

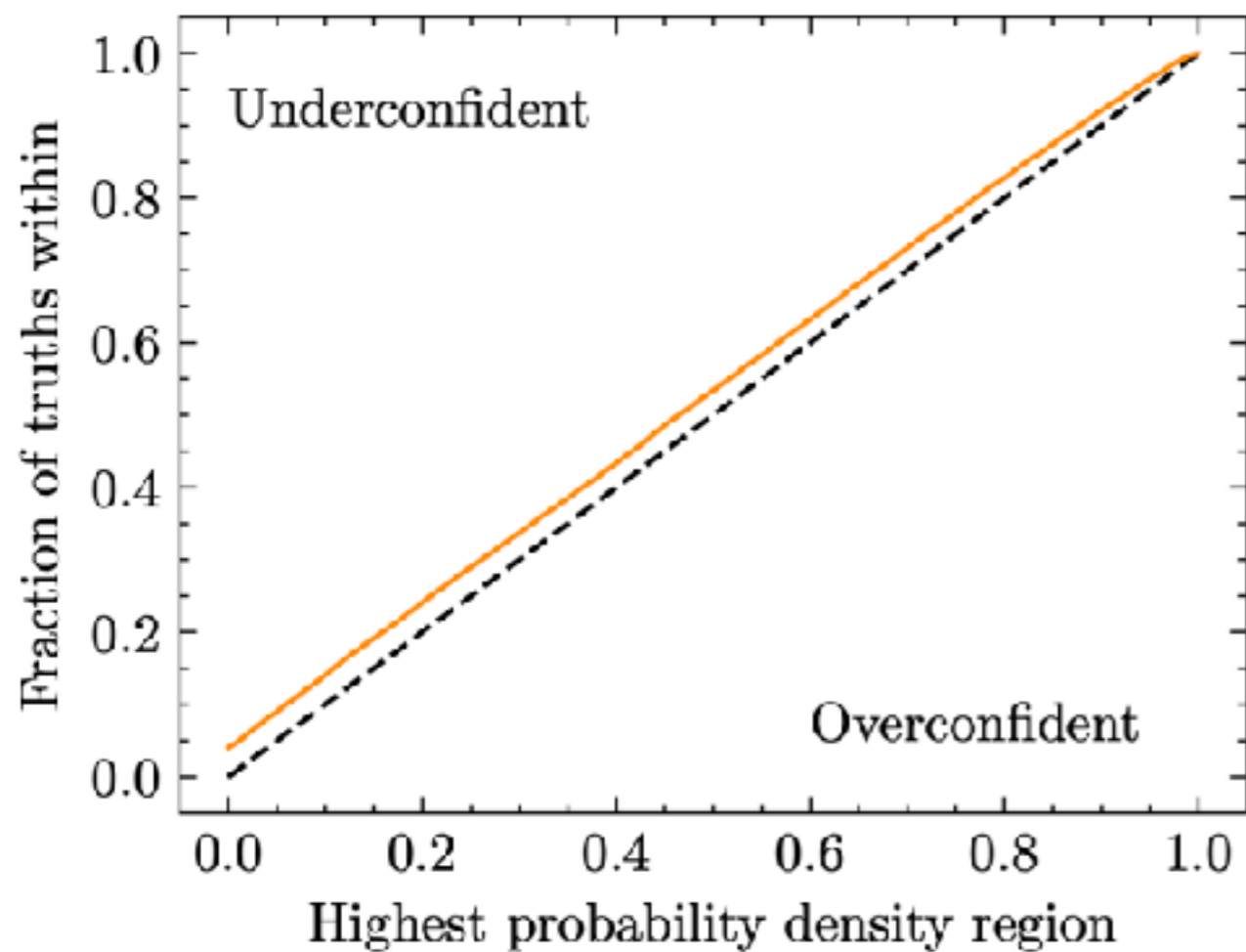
Ève Campeau-Poirier



# H0 INFERENCE WITH NEURAL RATIO ESTIMATORS



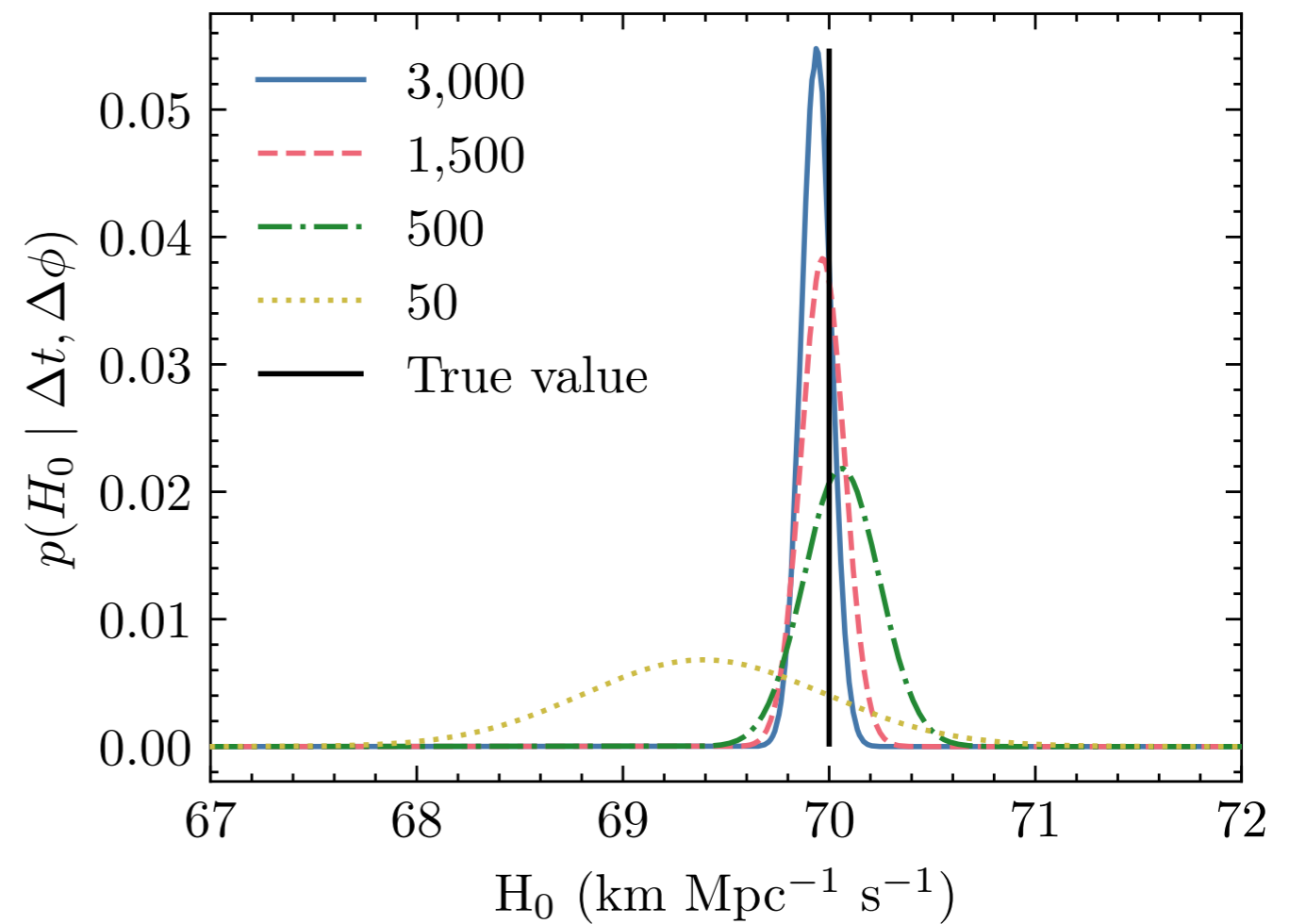
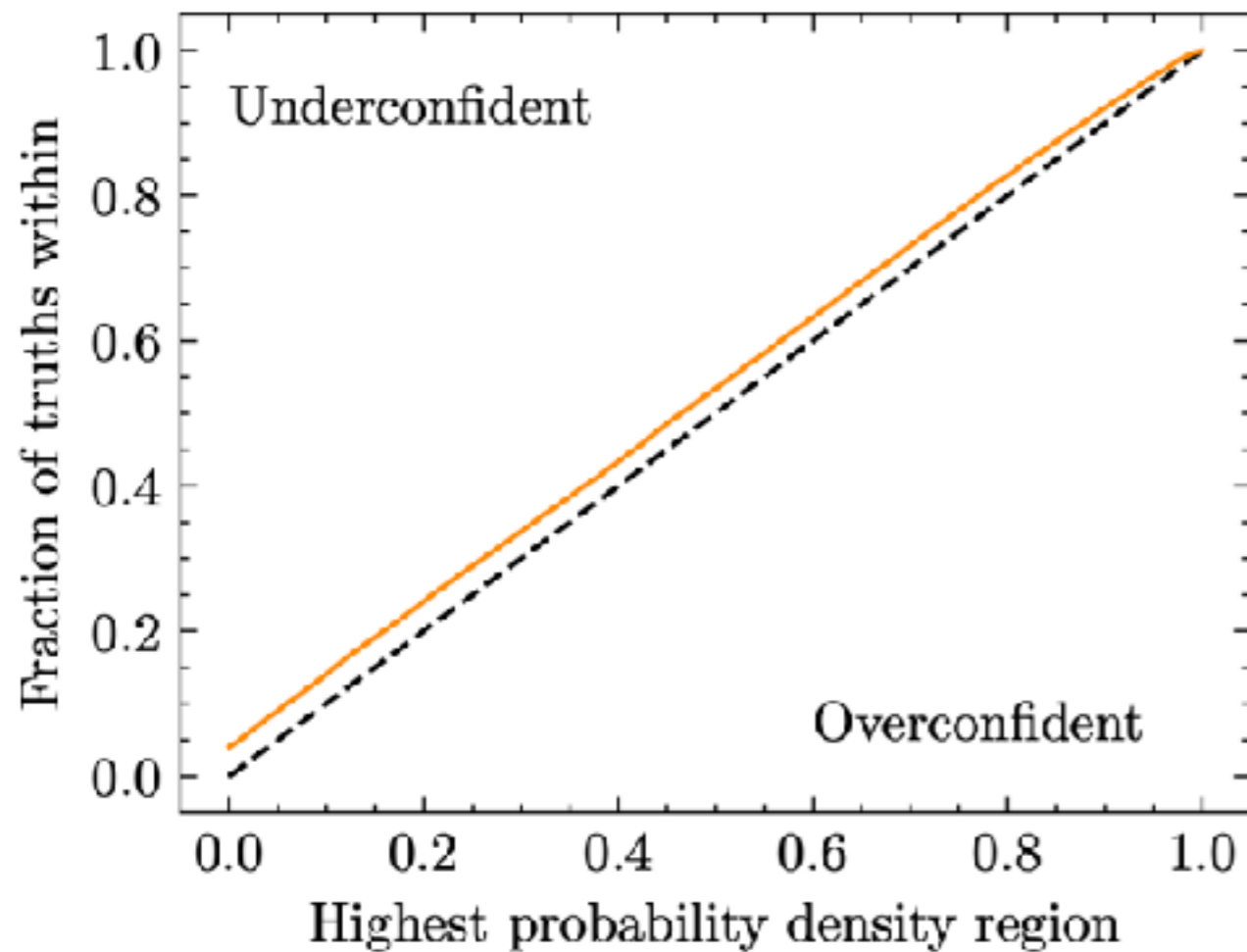
Ève Campeau-Poirier



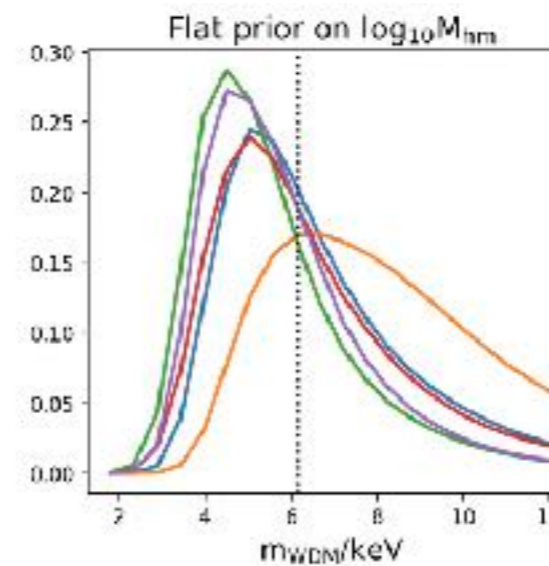
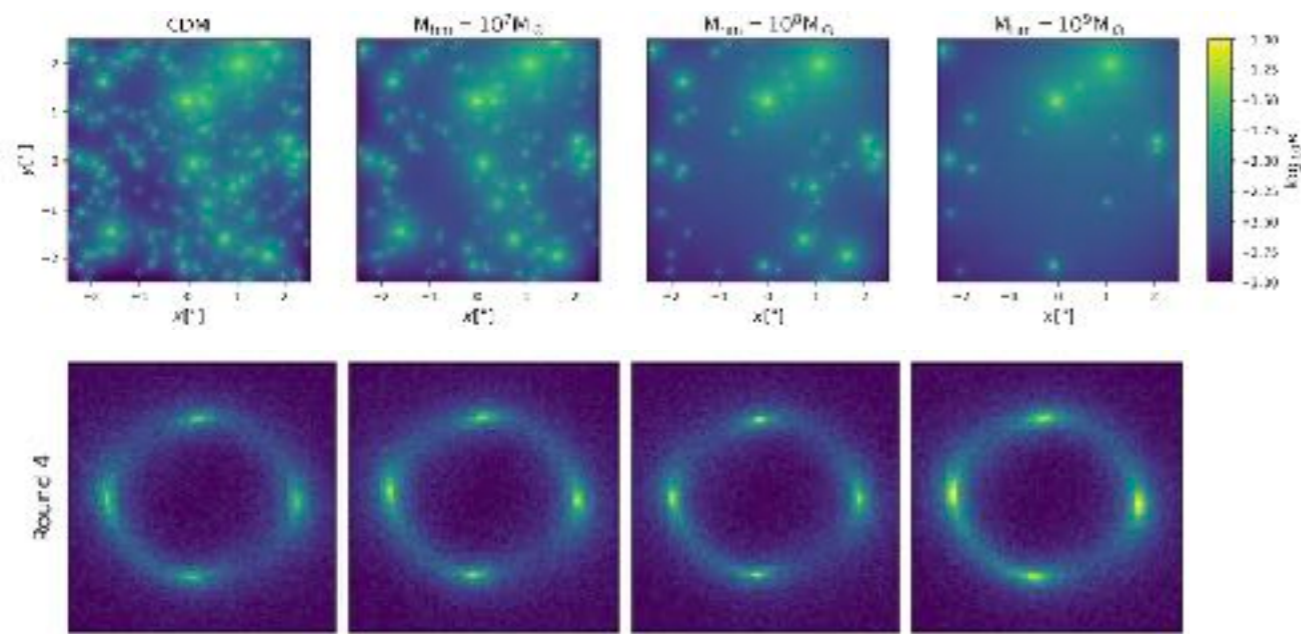
# H0 INFERENCE WITH NEURAL RATIO ESTIMATORS



Ève Campeau-Poirier



# Estimating the dark matter particle temperature with Neural Ratio Estimators



Adam  
Coogan

Anau Montel, Coogan et al. 2022, arXiv:2205.09126  
Coogan et al. , NeurIPS 2020 ML4PS Workshop

# TACKLING AN UNSOLVED PROBLEM: HIGH DIMENSIONAL INFERENCE

How do we infer the posteriors of high-dimensional parameters (e.g., an image or spectra)?

Obstacles:

- 1) How do we encode complex priors
- 2) How we sample such high-dimensional posteriors (even if we could compute them)



# LEARNING THE PRIOR EXPLICITLY

Can we learn our high-dimensional prior explicitly from data?  
i.e. can we learn a generative model that will produce samples from that distribution?

# LEARNING THE PRIOR EXPLICITLY

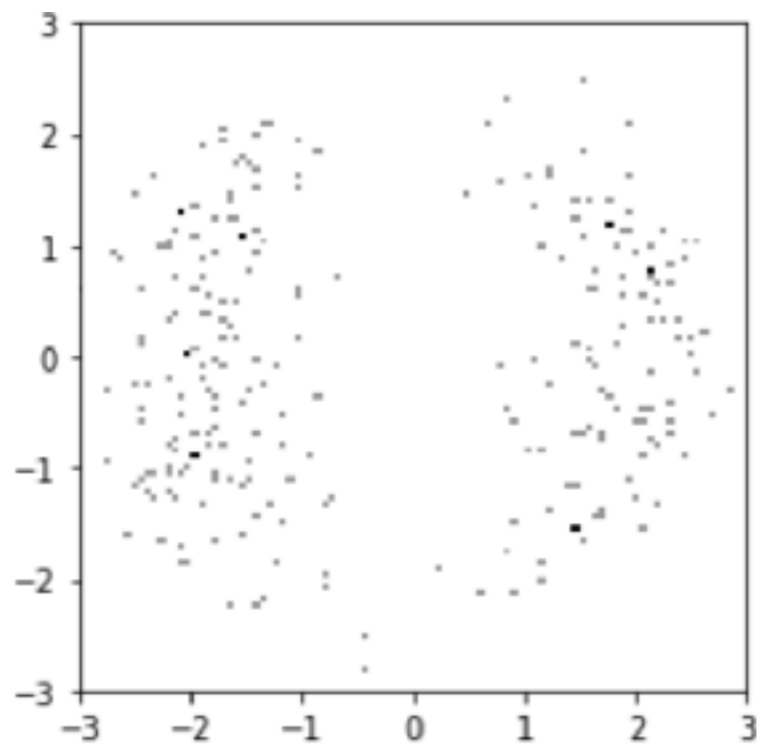
Can we learn our high-dimensional prior explicitly from data?  
i.e. can we learn a generative model that will produce samples from that distribution?

How can we do this from samples (e.g. data)? Modeling the density?

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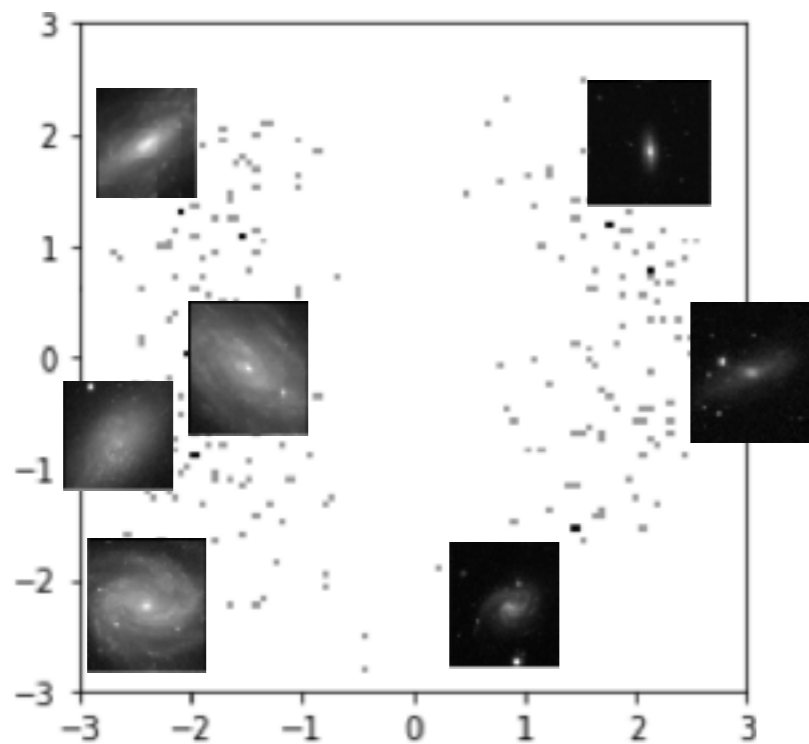
Training data

$$\{\mathbf{x}_1, \dots, \mathbf{x}_n\} \stackrel{iid}{\sim} \pi_{data}(\mathbf{x})$$

# LEARNING THE PRIOR EXPLICITLY

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i.e. can we learn a generative model that will produce samples from that distribution?

How can we do this from samples (e.g. data)? Modeling the density?



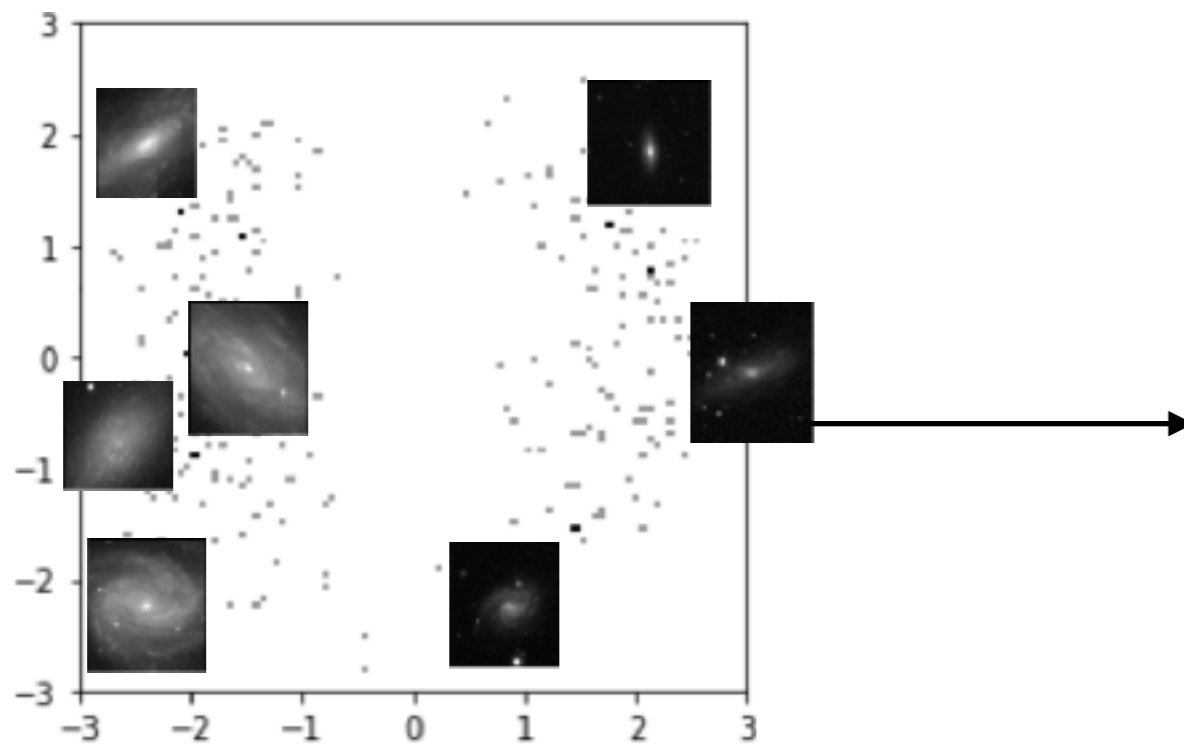
Training data

$$\{\mathbf{x}_1, \dots, \mathbf{x}_n\} \stackrel{iid}{\sim} \pi_{data}(\mathbf{x})$$

# LEARNING THE PRIOR EXPLICITLY

Can we learn our high-dimensional prior explicitly from data?  
i.e. can we learn a generative model that will produce samples from that distribution?

How can we do this from samples (e.g. data)? Modeling the density?



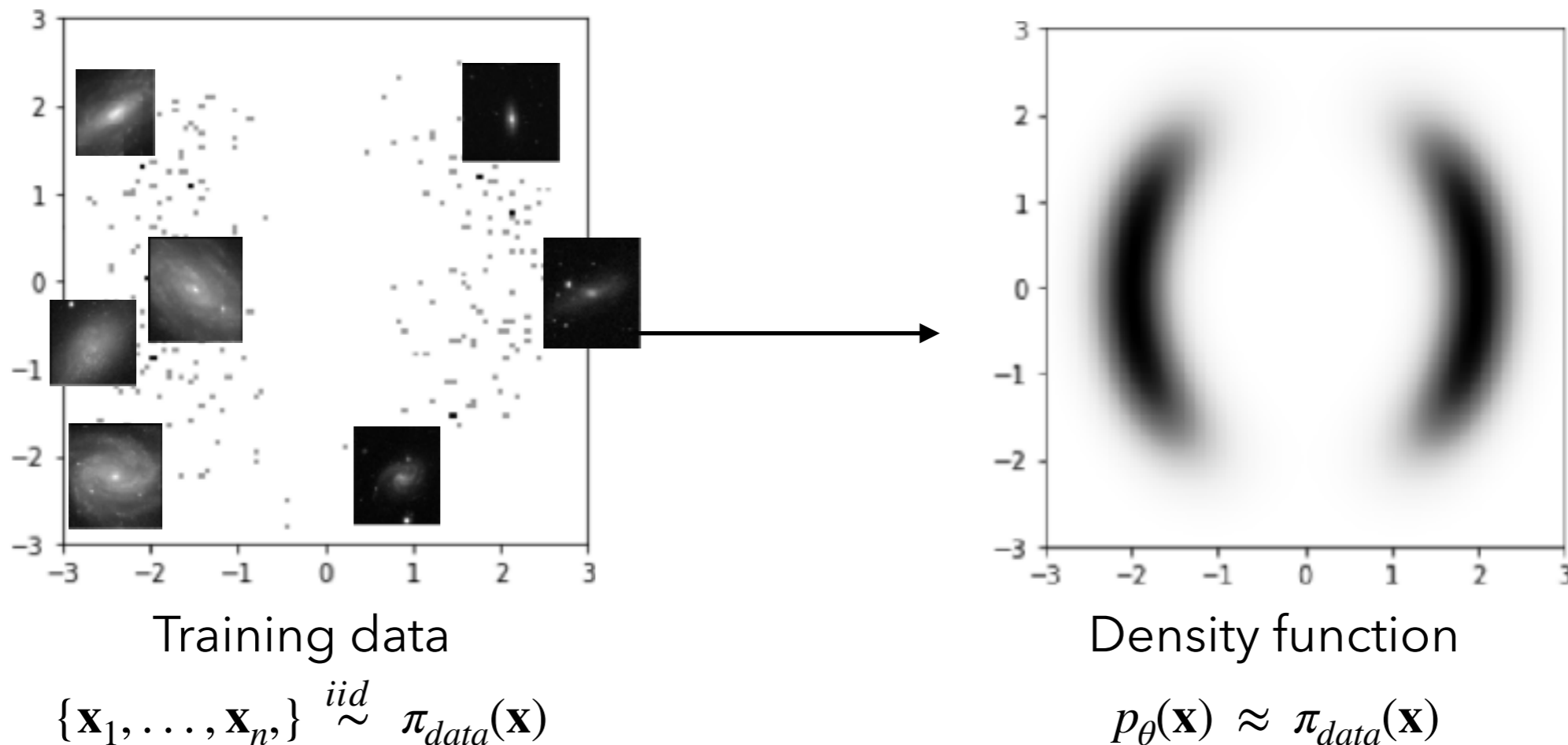
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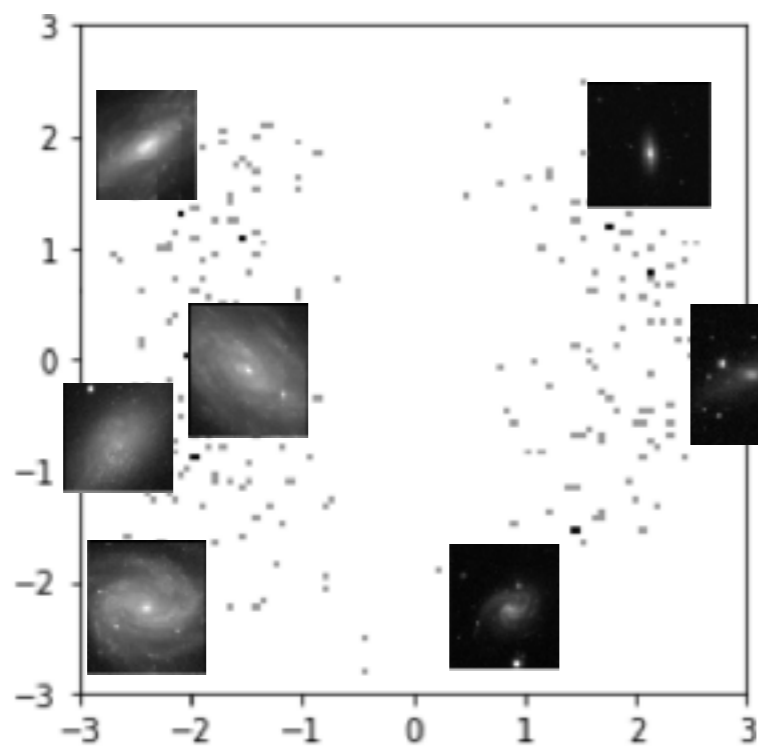
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# SCORE MODELING

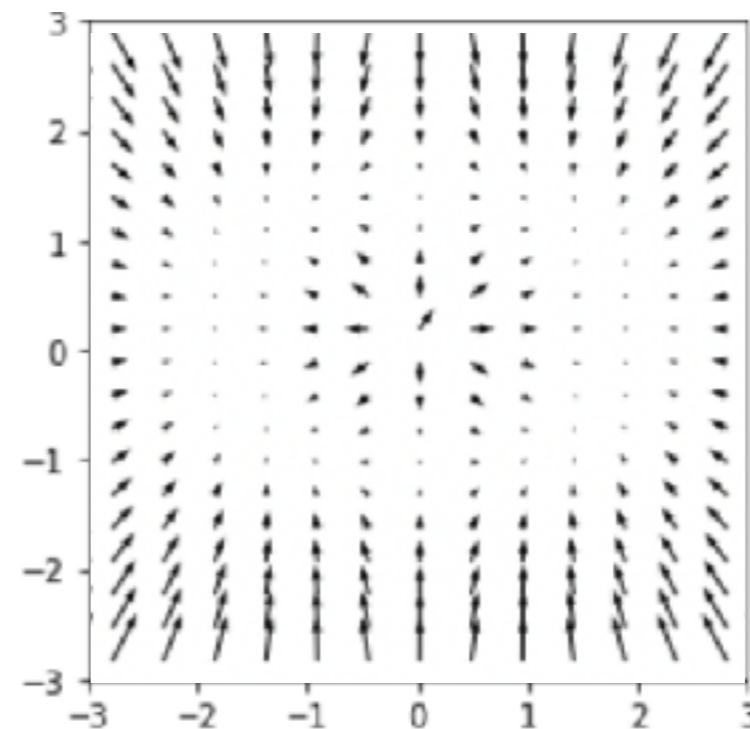
Turns out that if I want to sample a distribution, the only thing I need to learn is its **score**, which does not include the normalization constant and only uses local information

$$\mathbf{s}(\mathbf{x}) = \nabla_{\mathbf{x}} \log(\pi(\mathbf{x}))$$



Training data

$$\{\mathbf{x}_1, \dots, \mathbf{x}_n\} \stackrel{iid}{\sim} \pi_{data}(\mathbf{x})$$



Score function

$$\mathbf{s}_{\theta}(\mathbf{x}) \approx \nabla \log(\pi(\mathbf{x}))$$

# SCORE-BASED MODELING



Alexandre Adam

We model the score of the prior

$$s_{\theta}(x) \equiv \nabla_x \log p_{\theta}(x)$$



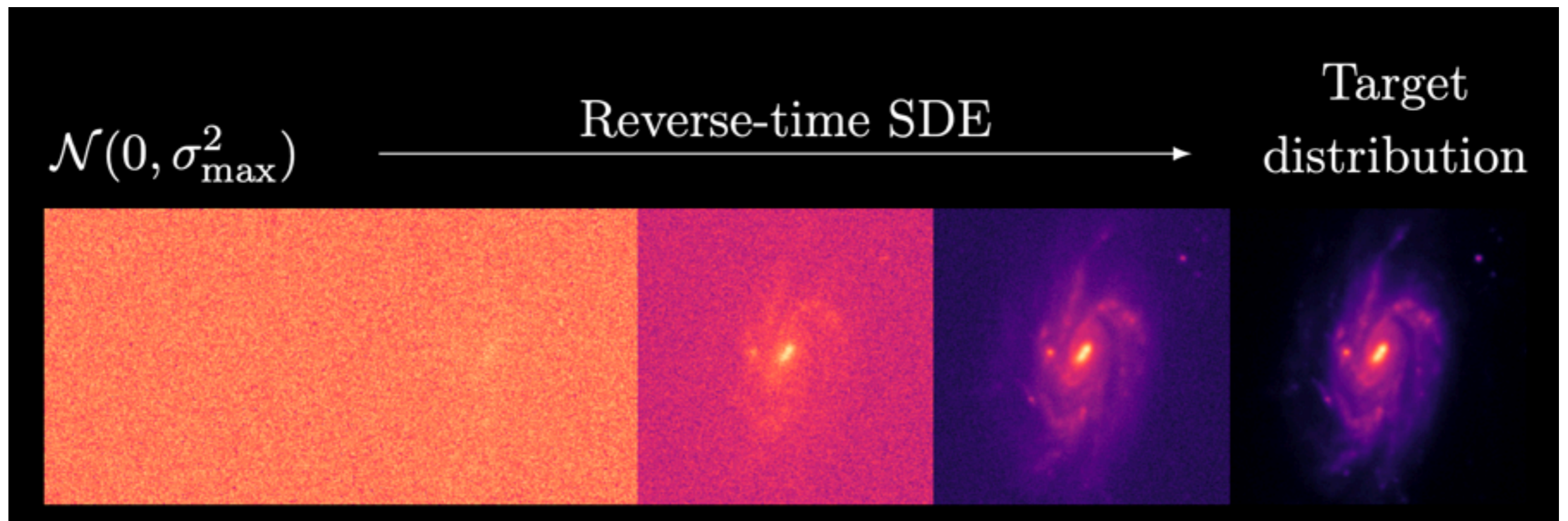
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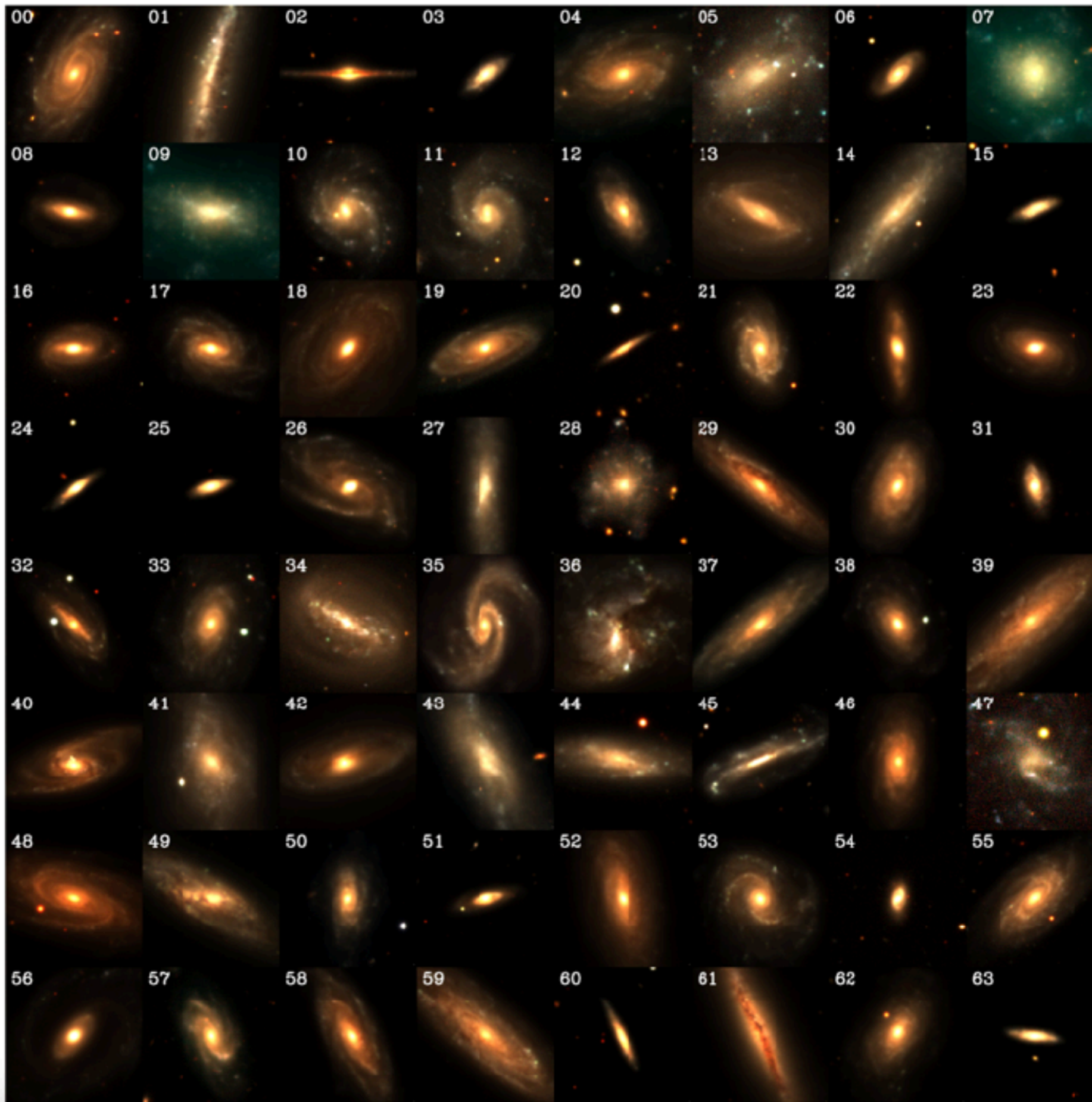


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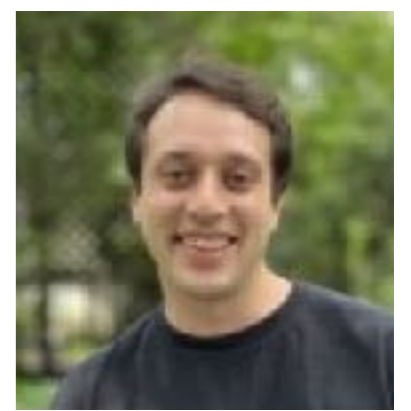




Connor  
Stone

<http://www.mjjsmith.com/thisisnotagalaxy/>

# SCORE-BASED MODELING



**Alexandre Adam**

Now if we want to sample from the posterior, its score is all we need:

$$\nabla_x \log p(x | y)$$

# SCORE-BASED MODELING



Alexandre Adam

Now if we want to sample from the posterior, its score is all we need:

$$\nabla_x \log p(x|y) = \nabla_x \log p(y|x) + \nabla_x \log p_\theta(x)$$

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# SCORE-BASED MODELING



Alexandre Adam

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To a good approximation, we can calculate the likelihood score analytically if we assume it's Gaussian and we know the lensing matrix.

This is the prior score we learnt from the training data

# SCORE-BASED MODELING



Alexandre Adam

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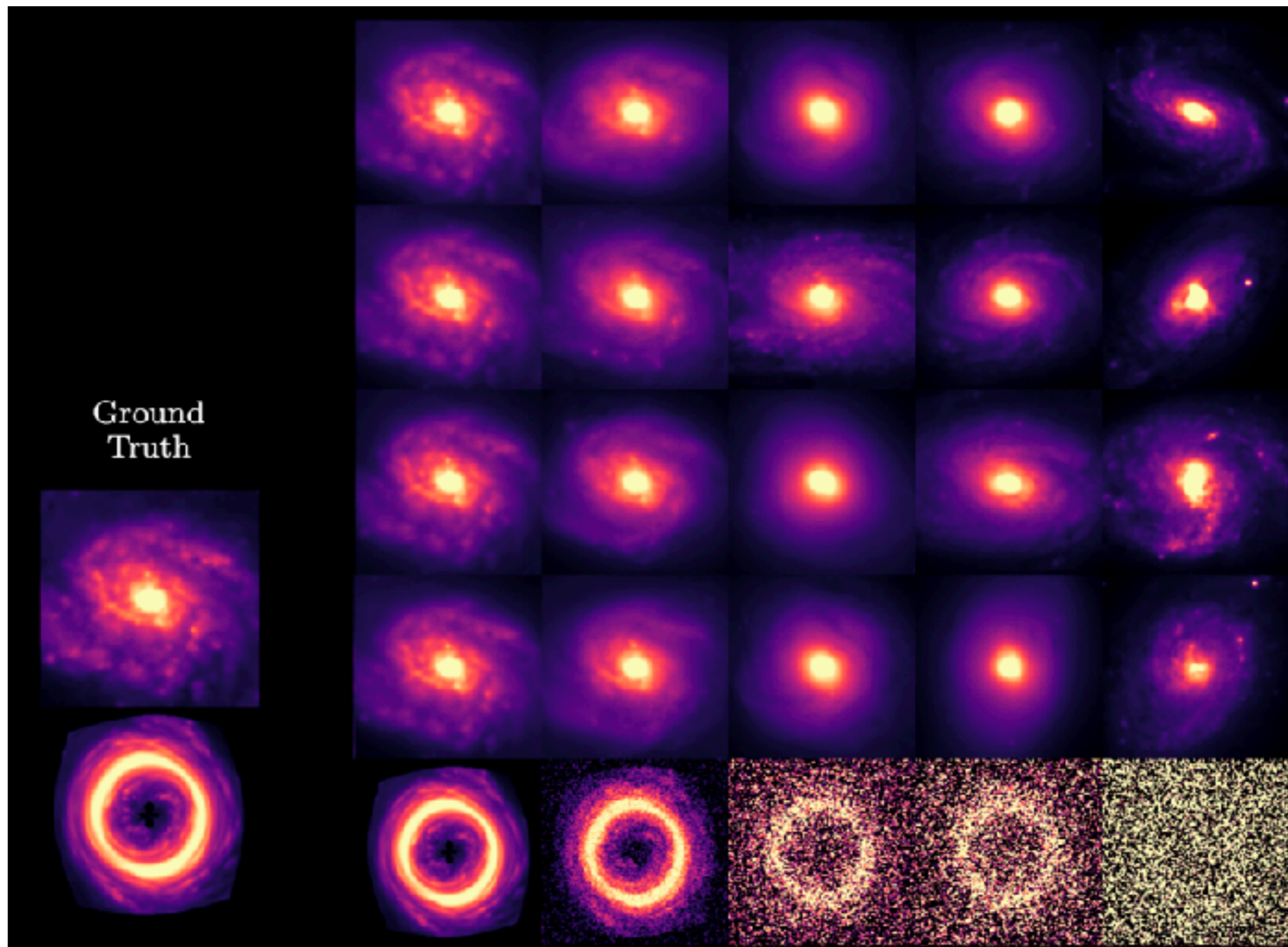
# SCORE-BASED MODELING



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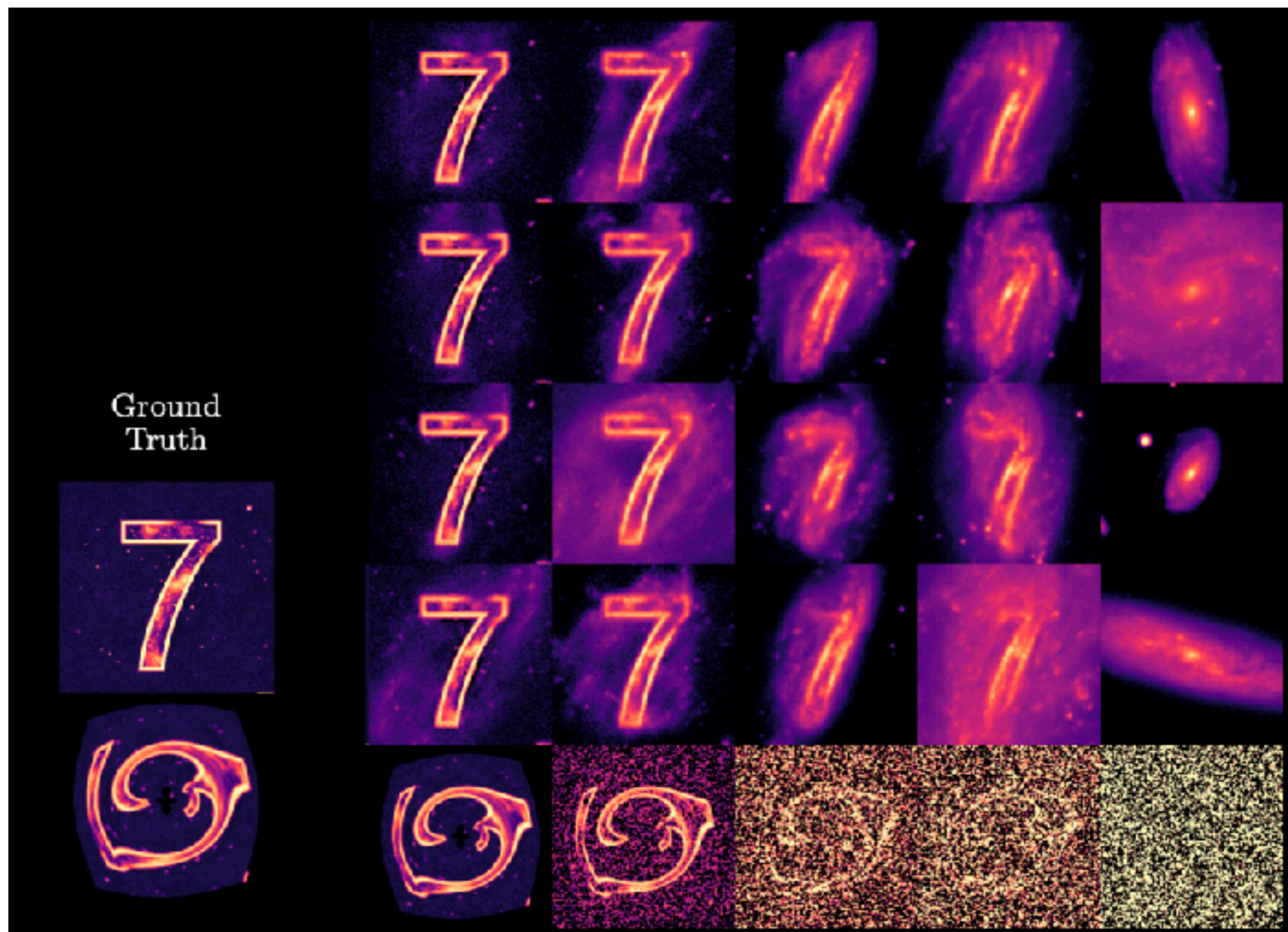
# OUT OF DISTRIBUTION TESTS



Alexandre Adam

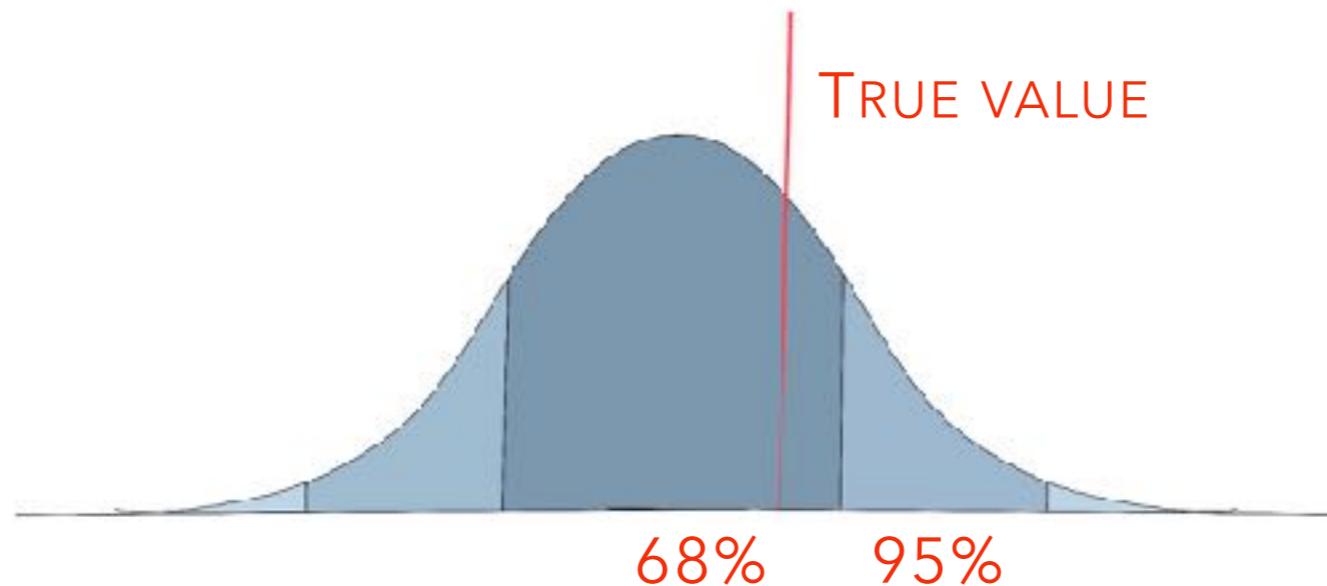
Now if we want to sample from the posterior, its score is all we need:

$$\nabla_x \log p(x|y) = \nabla_x \log p(y|x) + \nabla_x \log p_\theta(x)$$



## ARE THESE UNCERTAINTIES ACCURATE?

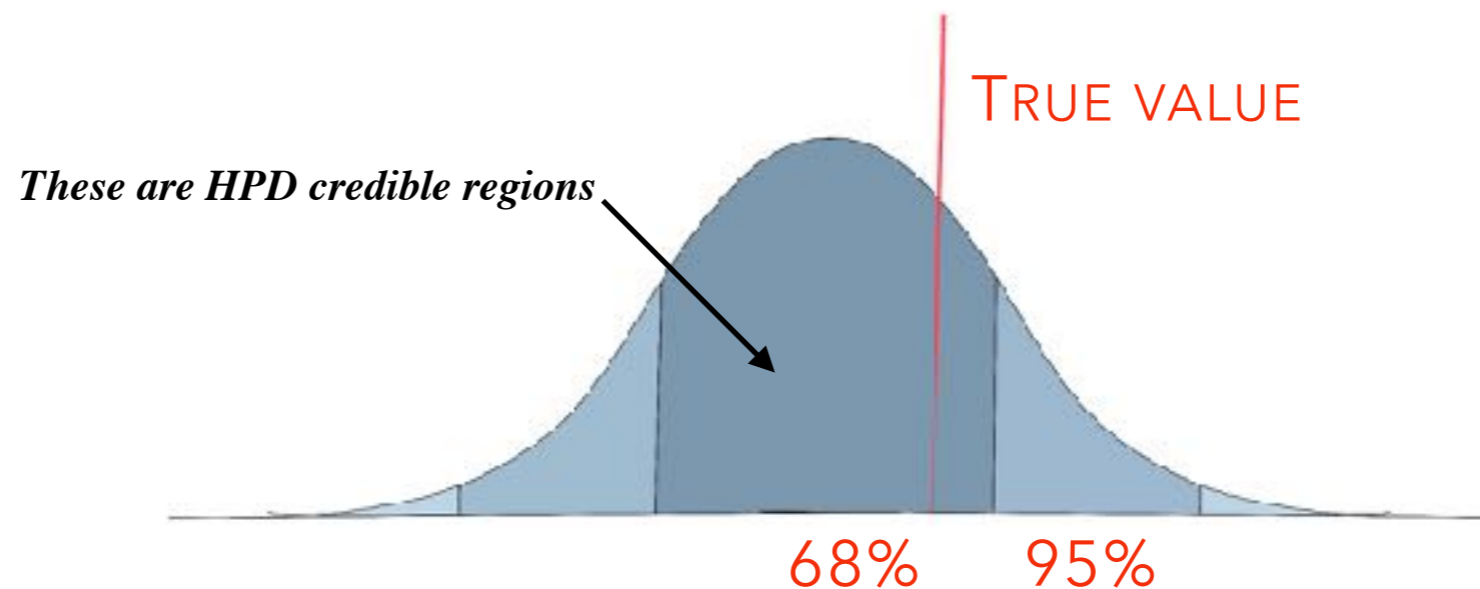
The expected coverage probability of a credible region is the proportion of the time that the region contains the true value of interest.



For an accurate posterior estimator, the expected coverage probability is equal to the probability mass of the credible region.

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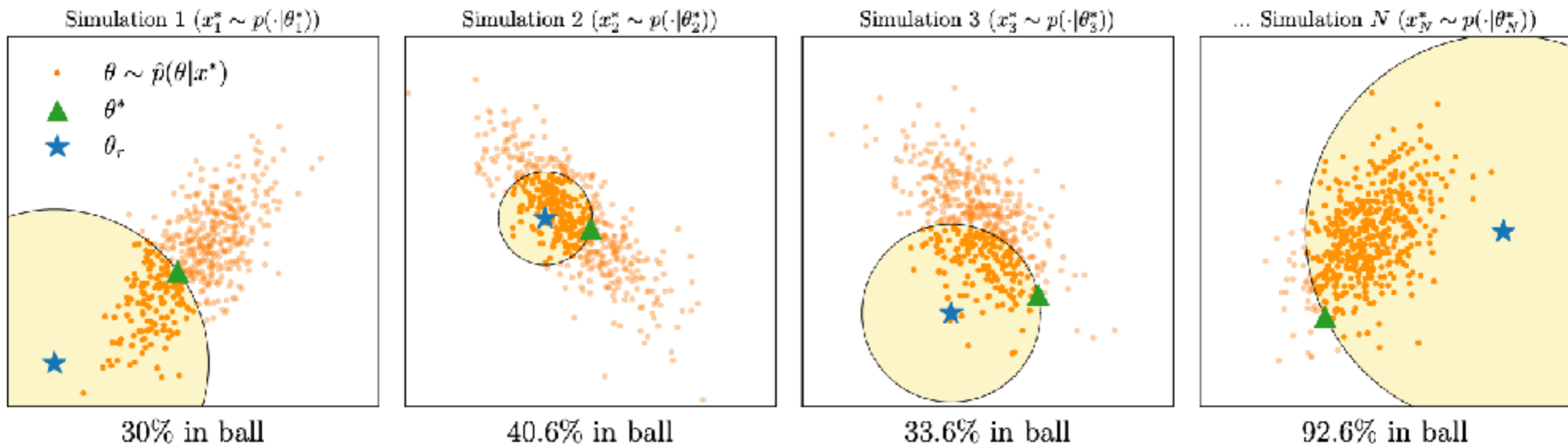


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# COVERAGE TEST FOR ACCURACY



Pablo Lemos

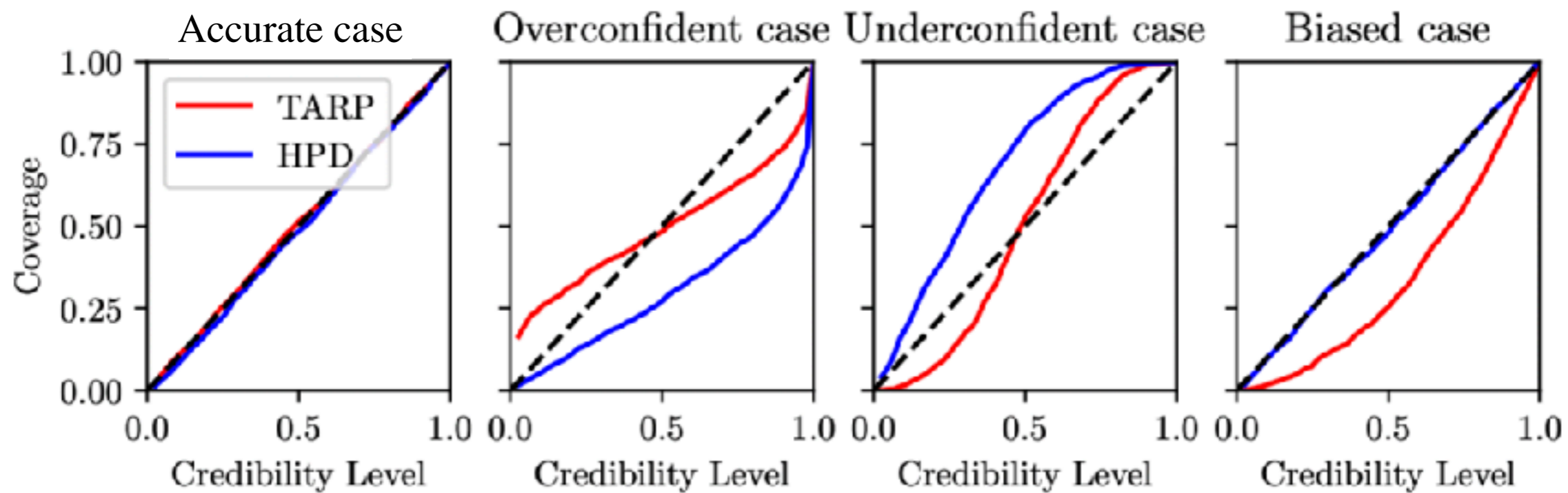


**pip install tarp**

# COVERAGE TEST FOR ACCURACY



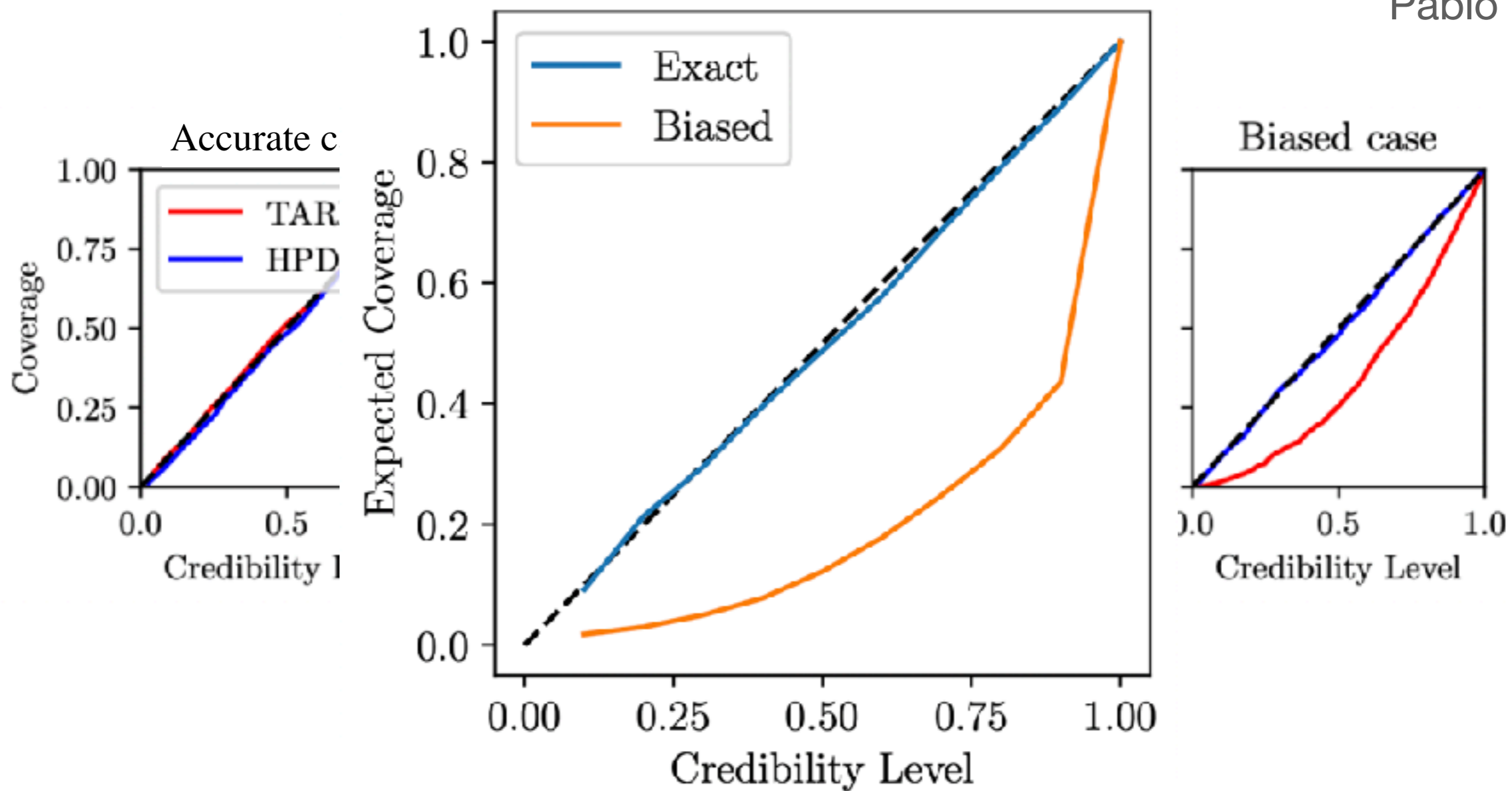
Pablo Lemos



# COVERAGE TEST FOR ACCURACY



Pablo Lemos



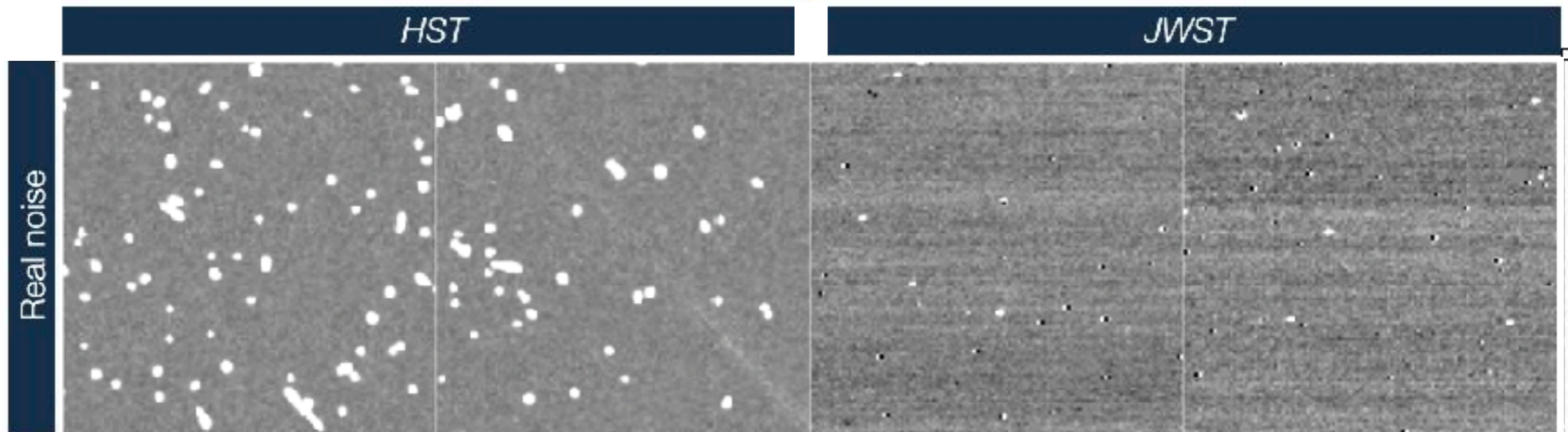
# DEALING WITH REALISTIC NOISE: BEYOND GAUSSIANITY



Alexandre Adam



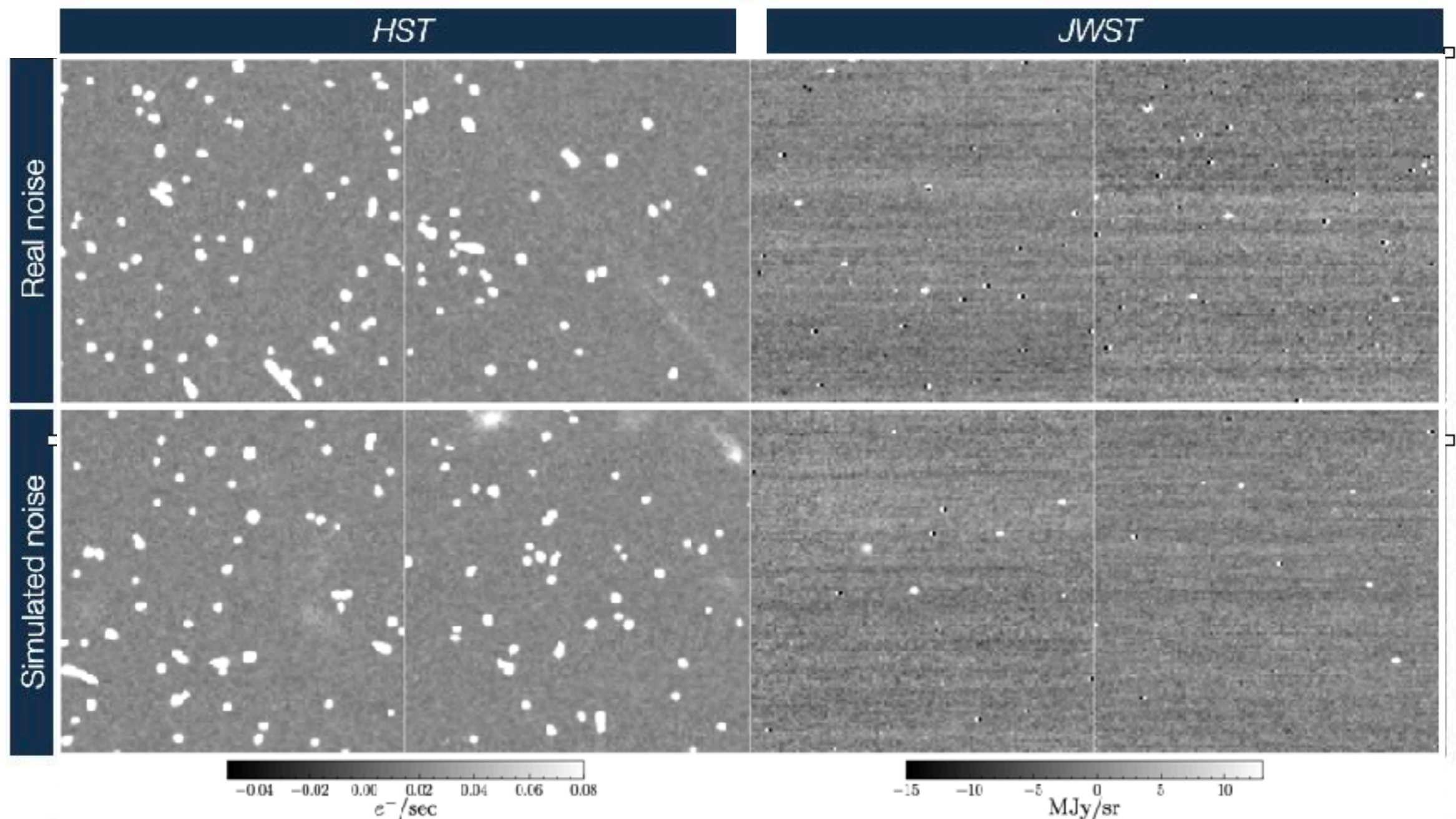
Ronan Legin



# DEALING WITH REALISTIC NOISE: BEYOND GAUSSIANITY

## SLIC: SCORE-BASED LIKELIHOOD CHARACTERIZATION

Since we have learnt a generative model of the additive noise, it can now be used in a simulation pipeline to get new, independent realizations of noise:



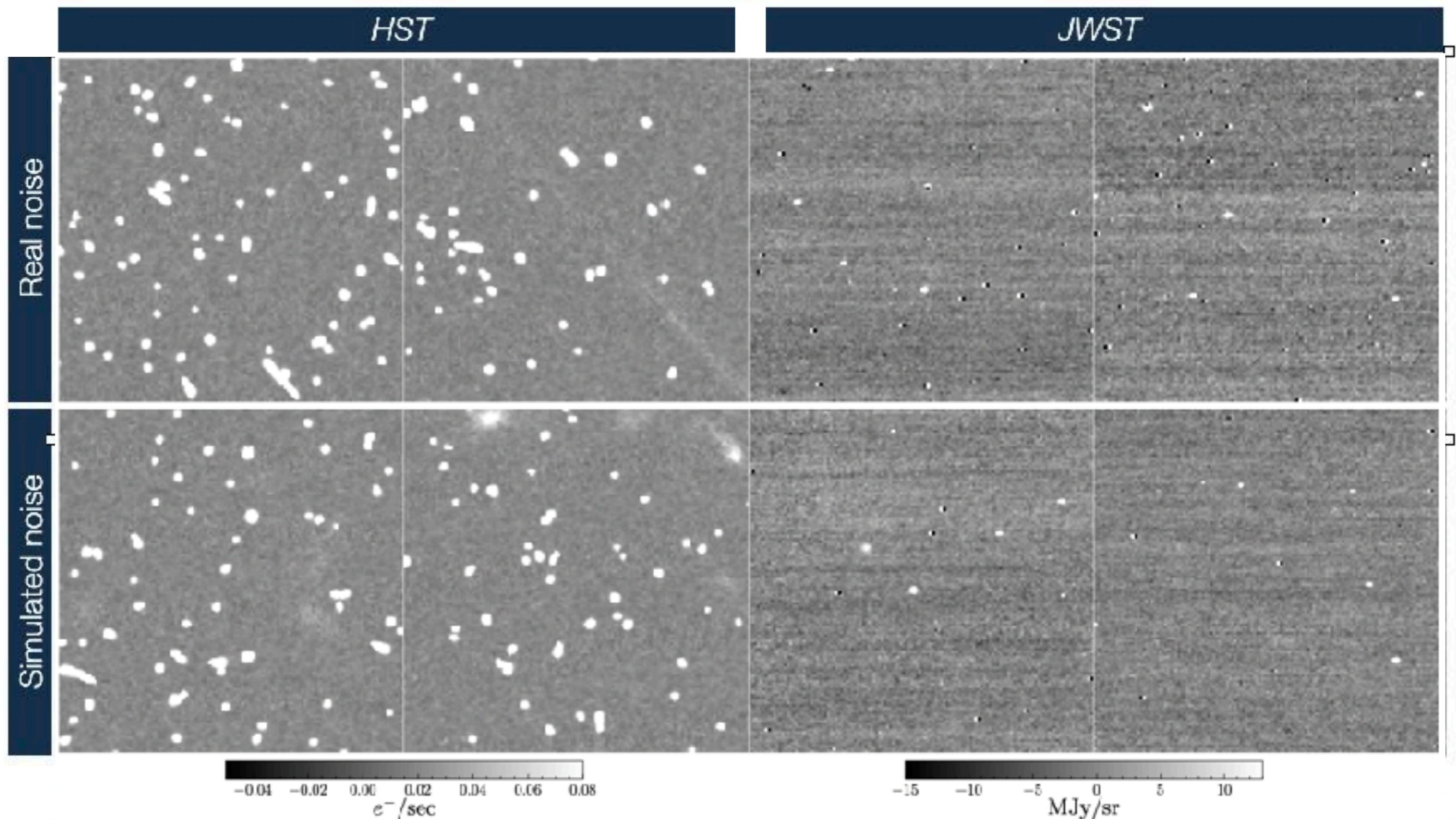


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# DEALING WITH REALISTIC NOISE: BEYOND GAUSSIANITY

## SLIC: SCORE-BASED LIKELIHOOD CHARACTERIZATION

# DEALING WITH REALISTIC NOISE: BEYOND GAUSSIANITY

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$$\mathbf{s}(\mathbf{x}_0) = \partial \log Q(\mathbf{x}_0) / \partial \mathbf{x}$$

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$$\eta_{l+1} = \eta_l + \tau \nabla_{\eta} \log Q(\mathbf{x}_0 - \mathbf{M}(\eta)) + \sqrt{2\tau} \xi_l$$

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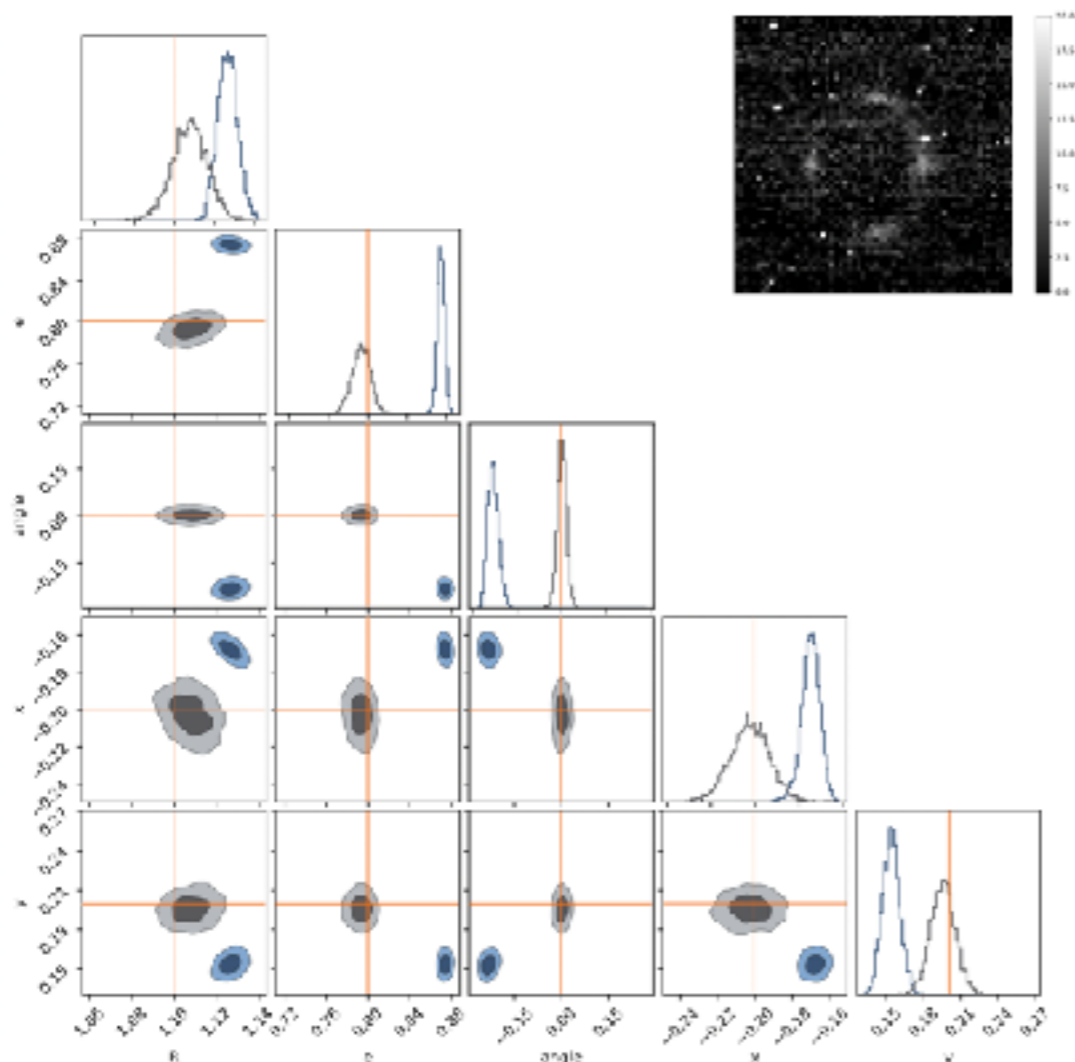
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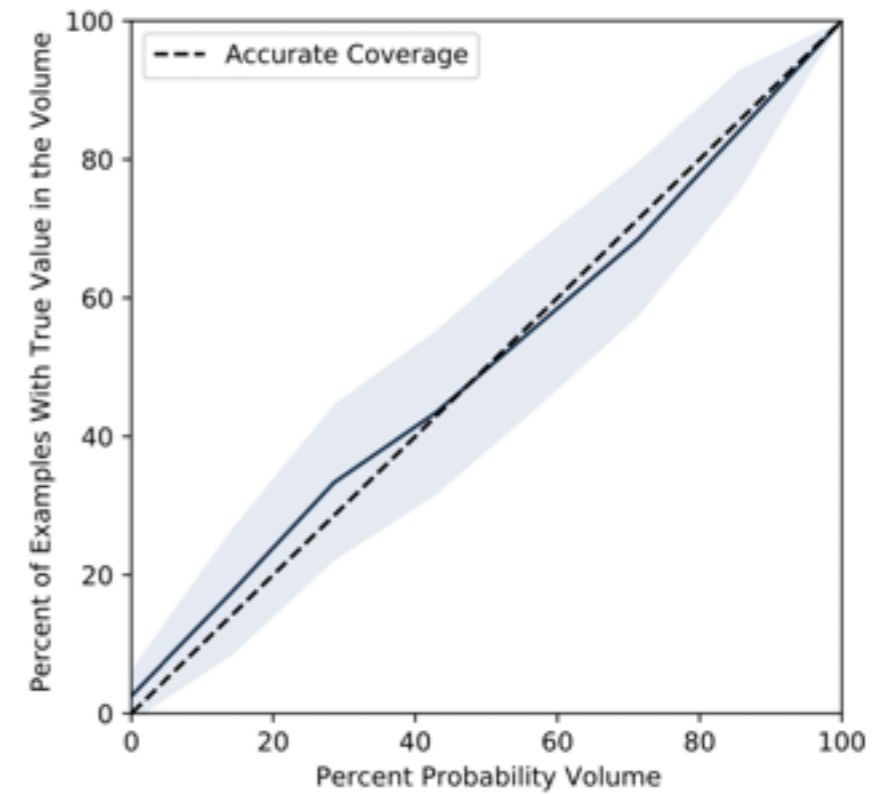
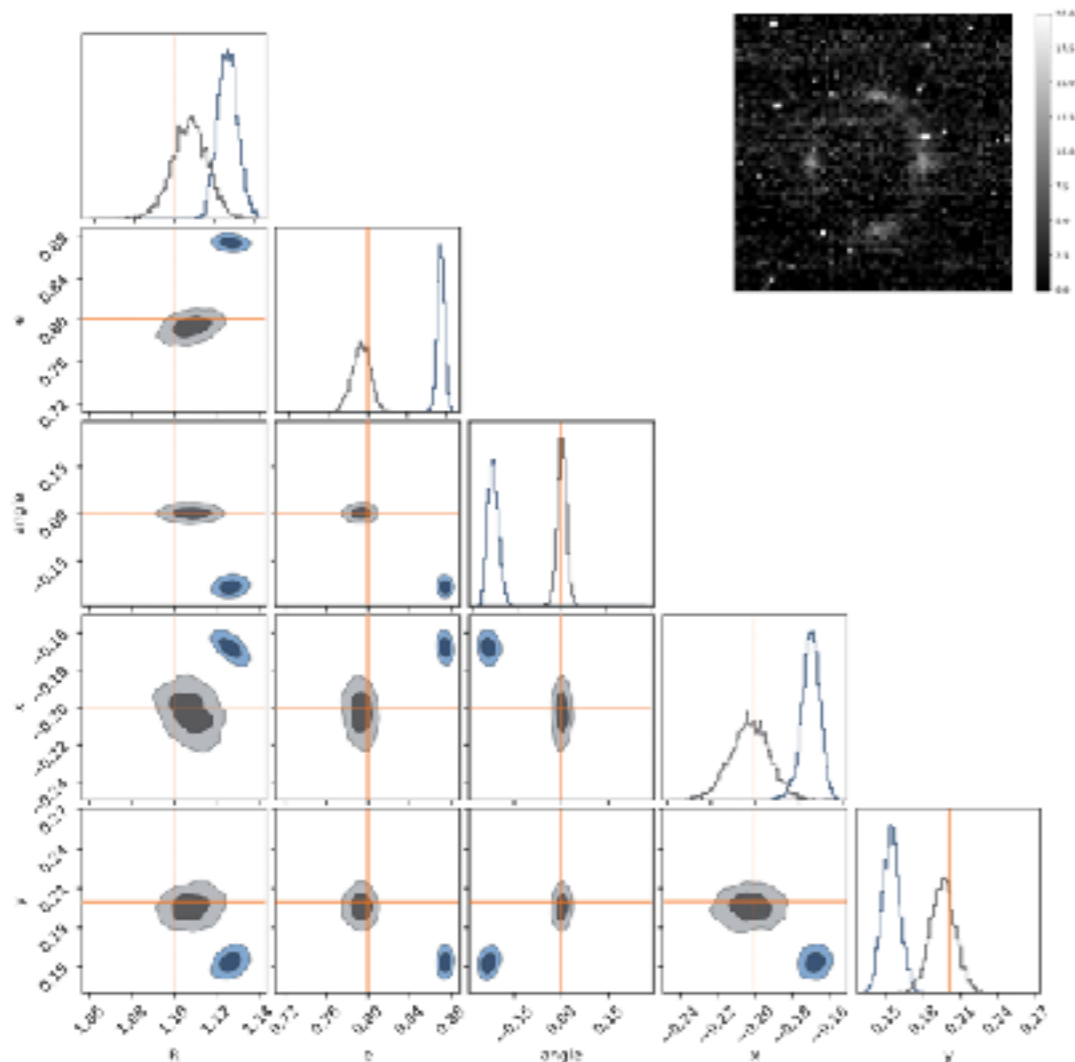
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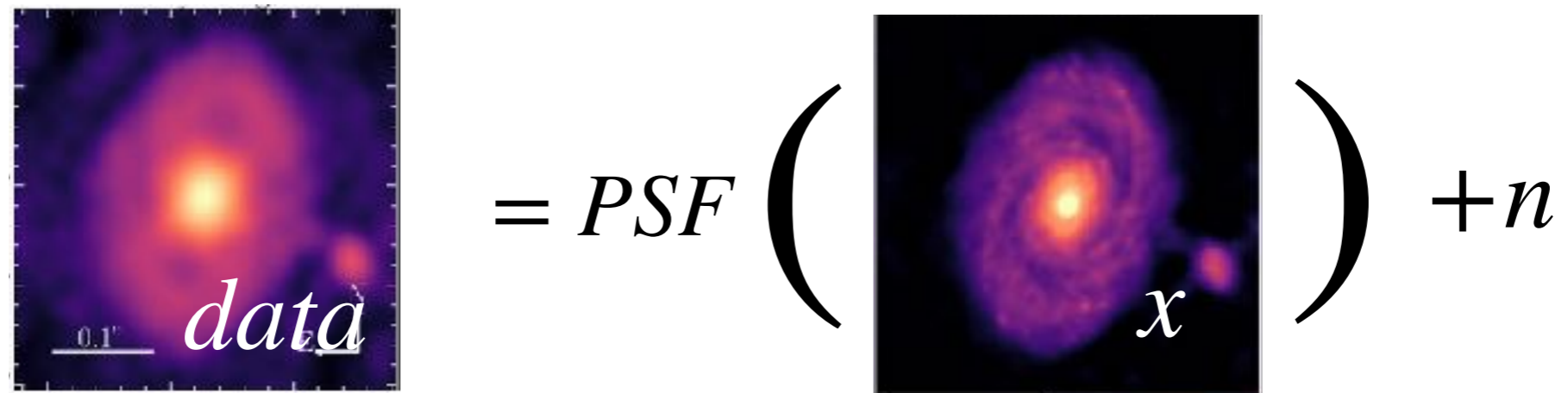




# PSF-DECONVOLUTION



Alexandre Adam



The diagram illustrates the PSF deconvolution equation. On the left is a blurred image of a galaxy labeled 'data' with a scale bar of 0.1". In the center is the equation  $= PSF \left( \text{image} \right) + n$ . The image inside the parentheses is a sharper version of the galaxy labeled 'x'. On the right is the noise term '+n'.

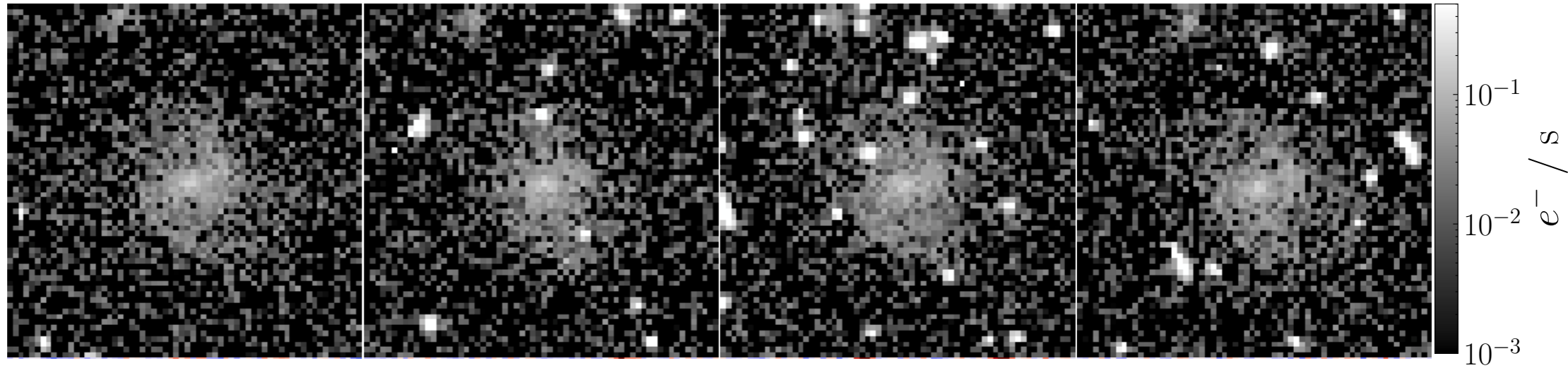
$$data = PSF \left( x \right) + n$$

# PSF-DECONVOLUTION (FOR HST)



Alexandre Adam

Observations ( $\mathbf{y}$ ), *HST* ACS/F814W

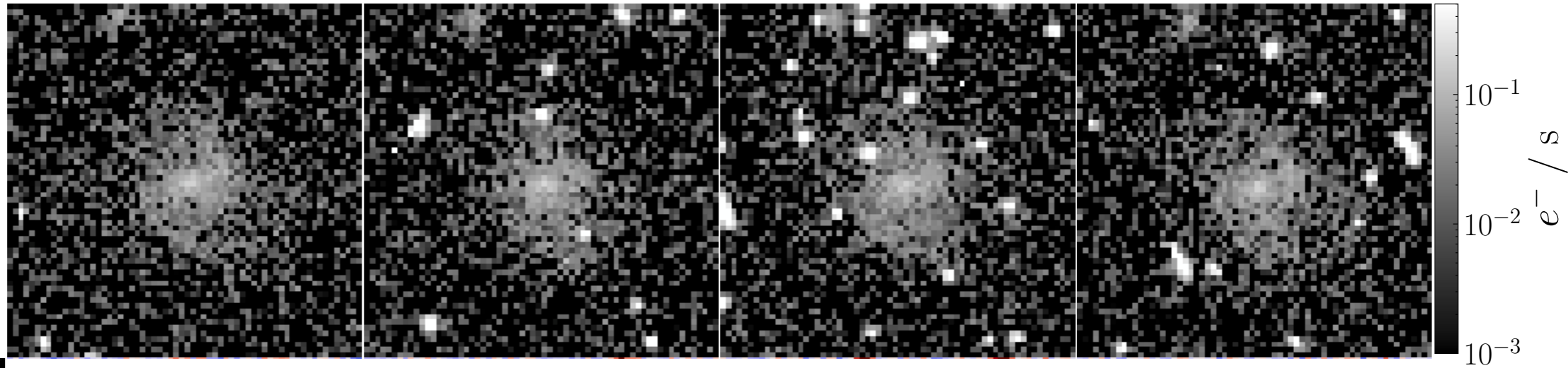


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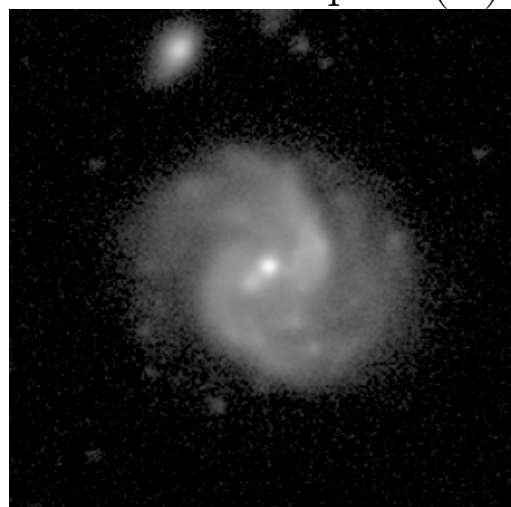


Alexandre Adam

Observations ( $\mathbf{y}$ ), *HST* ACS/F814W



Posterior samples ( $\mathbf{x}$ )

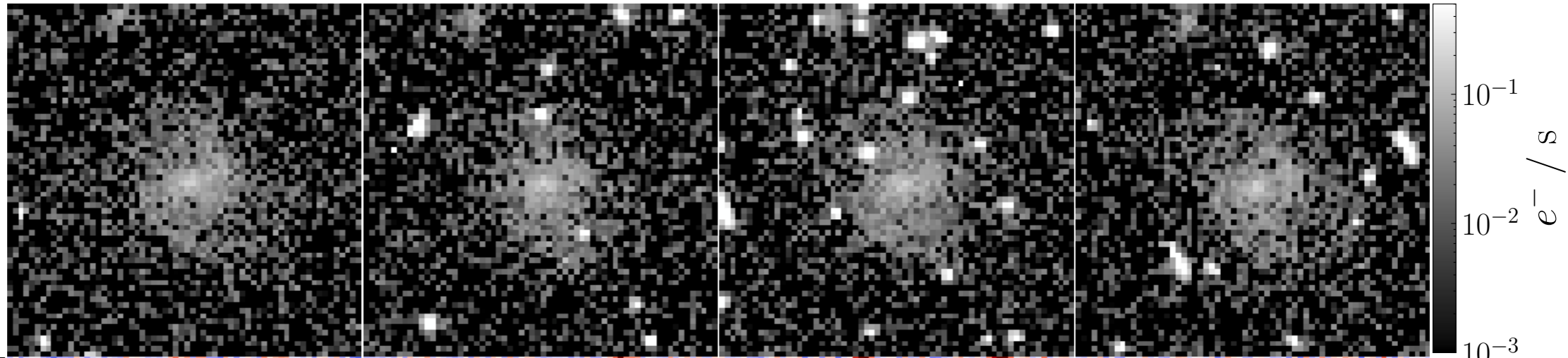


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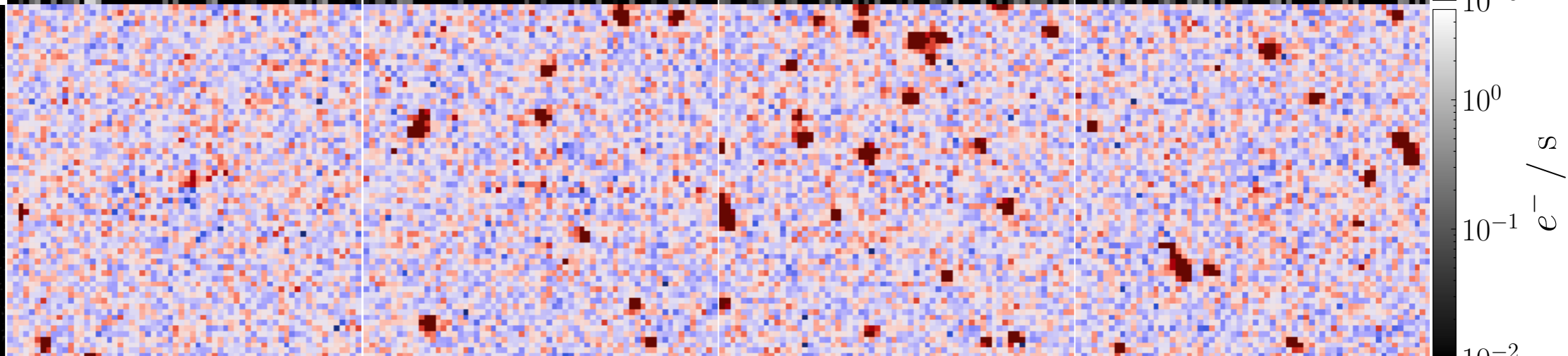
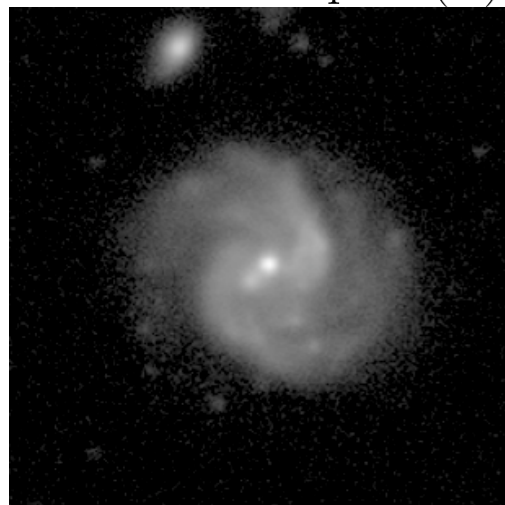


Alexandre Adam

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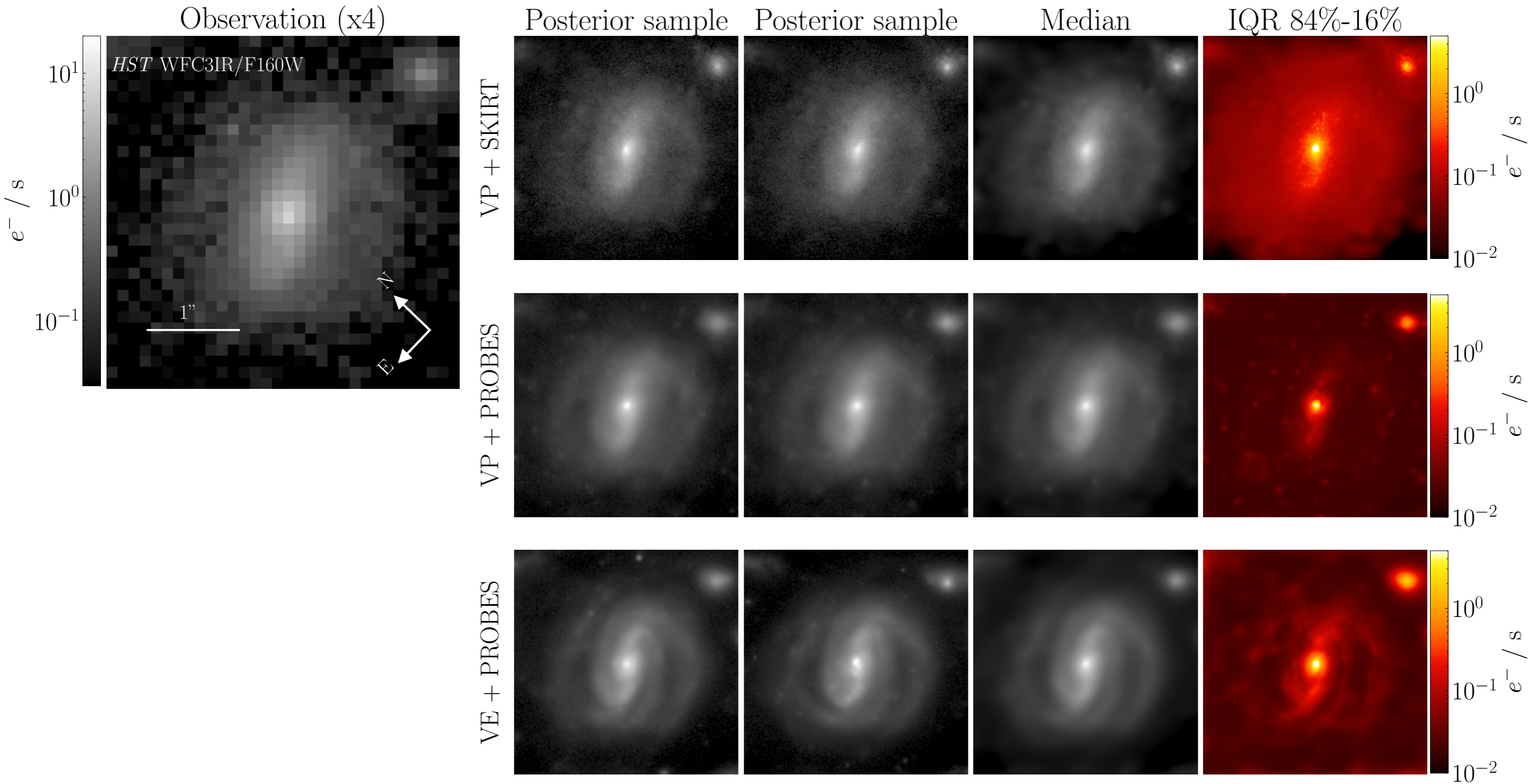


Residuals ( $\mathbf{y} - A\mathbf{x}$ )

# PSF-DECONVOLUTION (FOR HST)



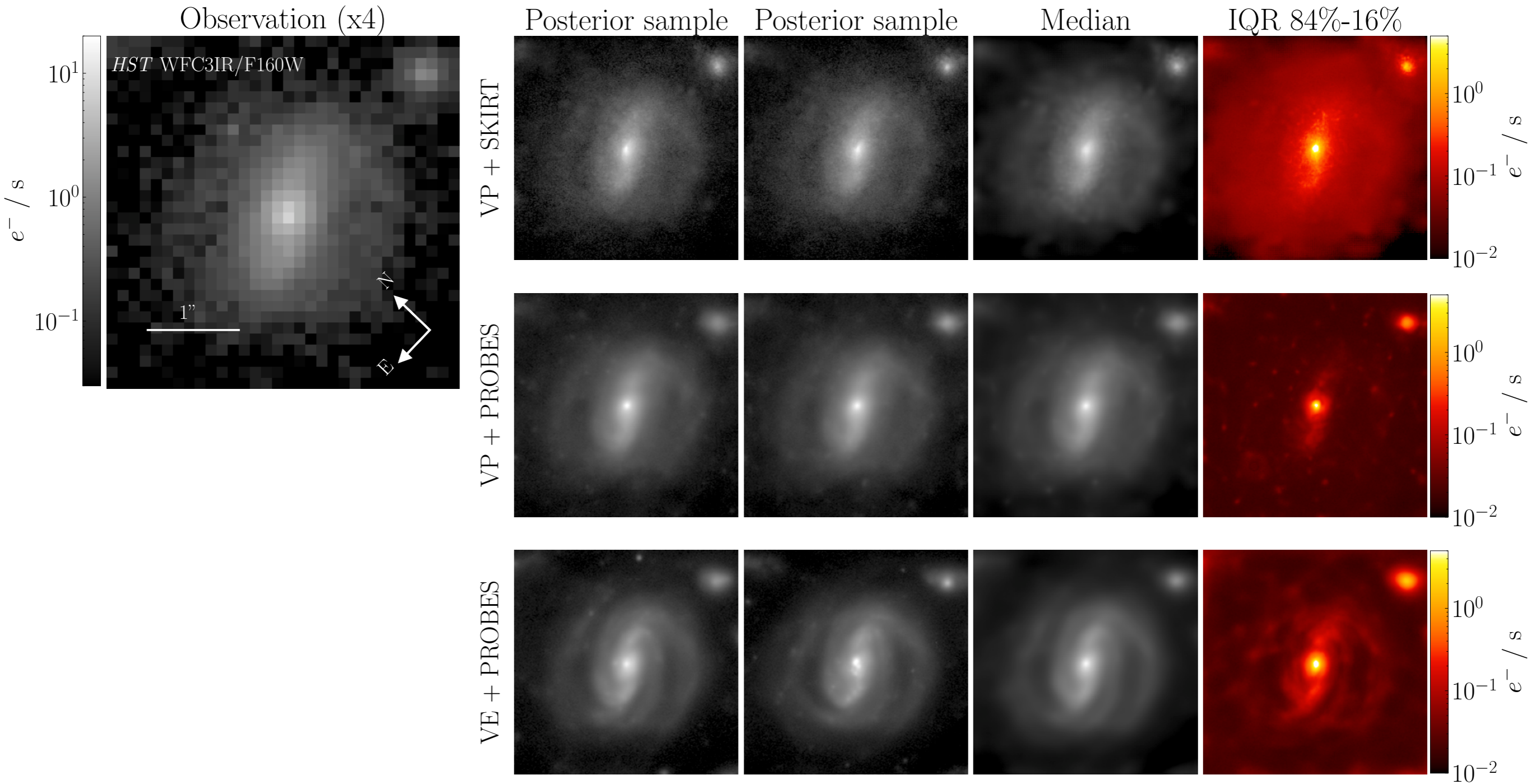
Alexandre Adam



# PSF-DECONVOLUTION (FOR HST)



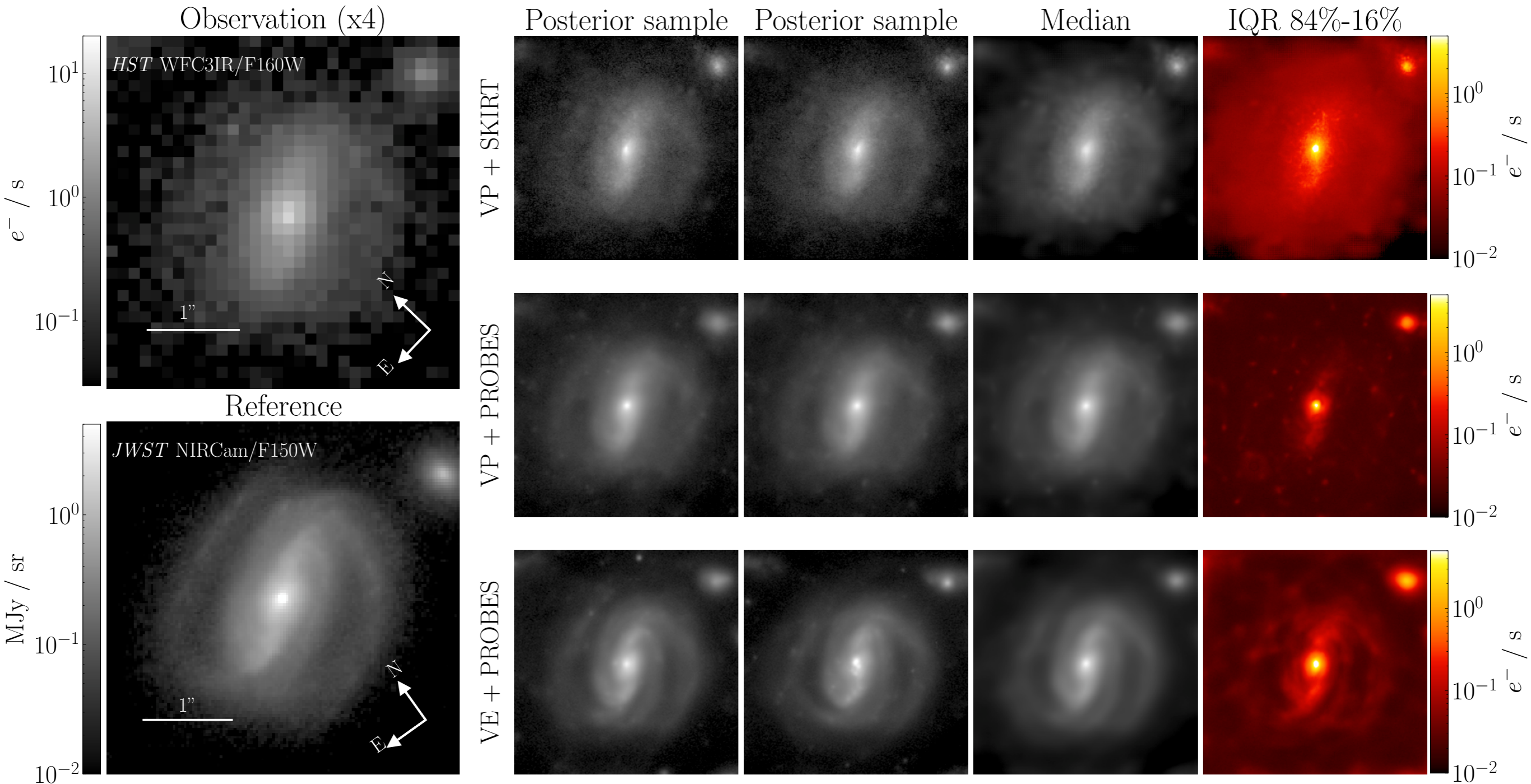
Alexandre Adam



# PSF-DECONVOLUTION (FOR HST)



Alexandre Adam



# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models



# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models

$$\mathcal{V} = \mathcal{SFP}_{\text{beam}}\mathbf{x} + \boldsymbol{\eta}$$

# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models

$$\mathcal{V} = S\mathcal{F}P_{\text{beam}}\mathbf{x} + \eta$$



Sky emission

# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models

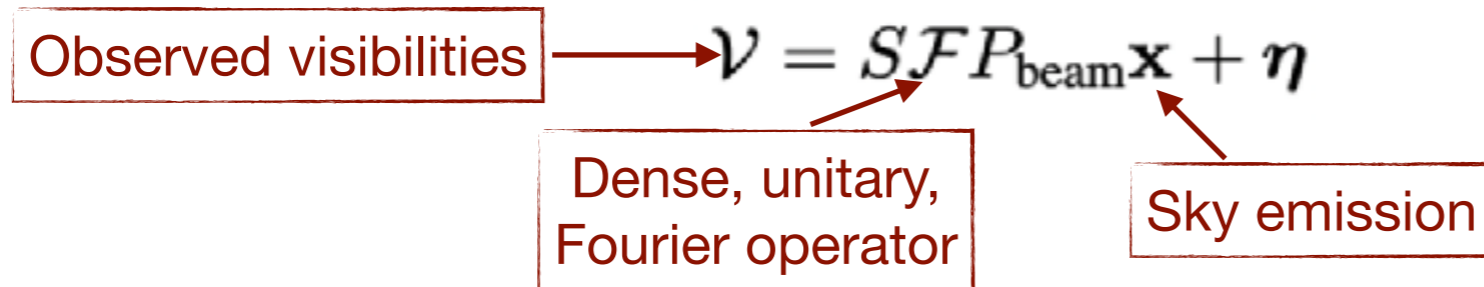
Observed visibilities  $\rightarrow \mathcal{V} = S\mathcal{F}P_{\text{beam}}\mathbf{x} + \eta$

Sky emission  $\rightarrow$

The diagram illustrates the relationship between observed visibilities, sky emission, and the PSF-deconvolution equation. A box labeled "Observed visibilities" has an arrow pointing to the left side of the equation  $\mathcal{V} = S\mathcal{F}P_{\text{beam}}\mathbf{x} + \eta$ . A box labeled "Sky emission" has an arrow pointing to the  $\mathbf{x}$  term in the equation.

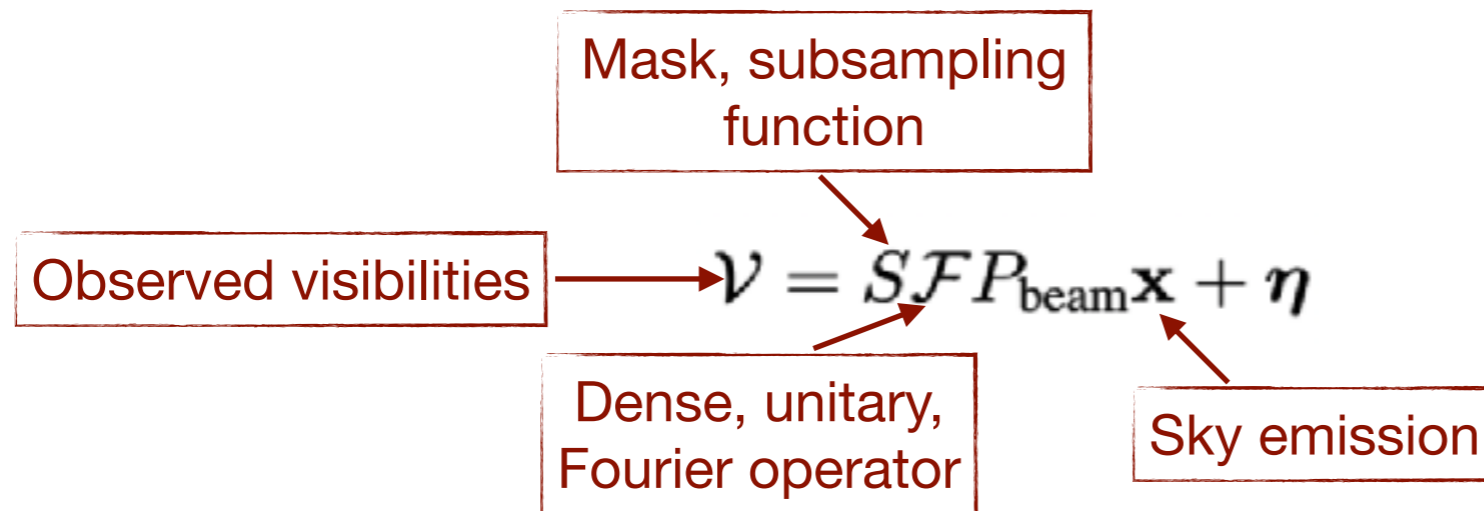
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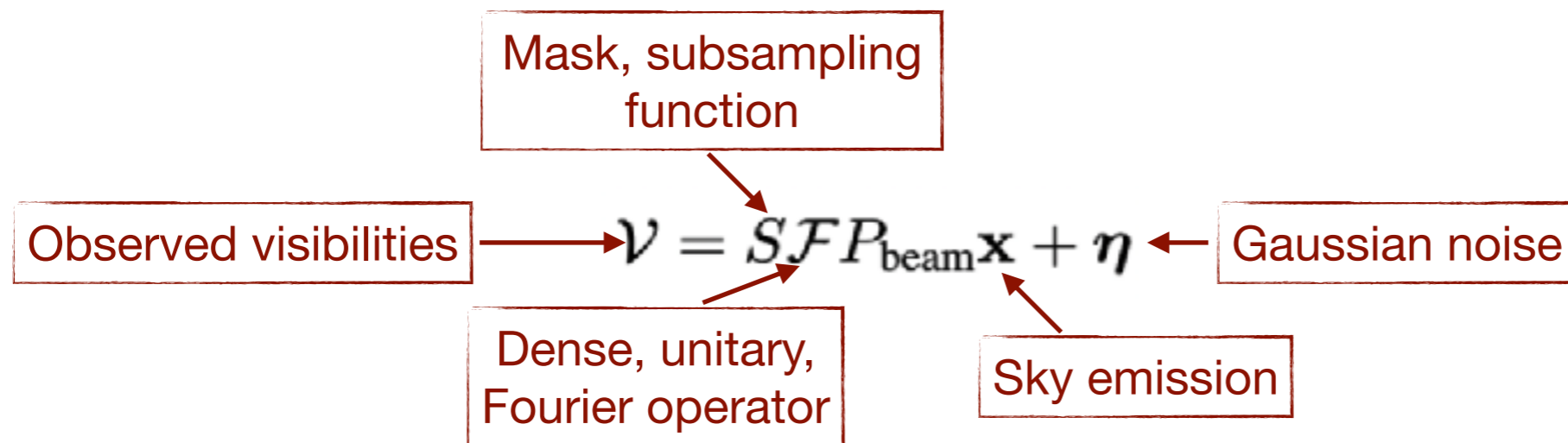
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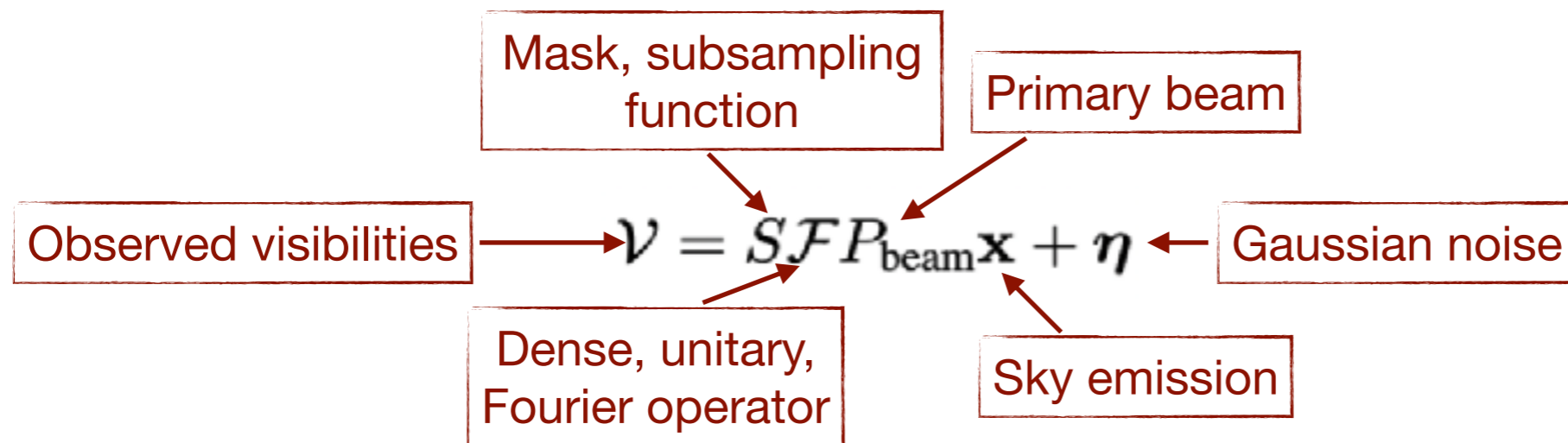
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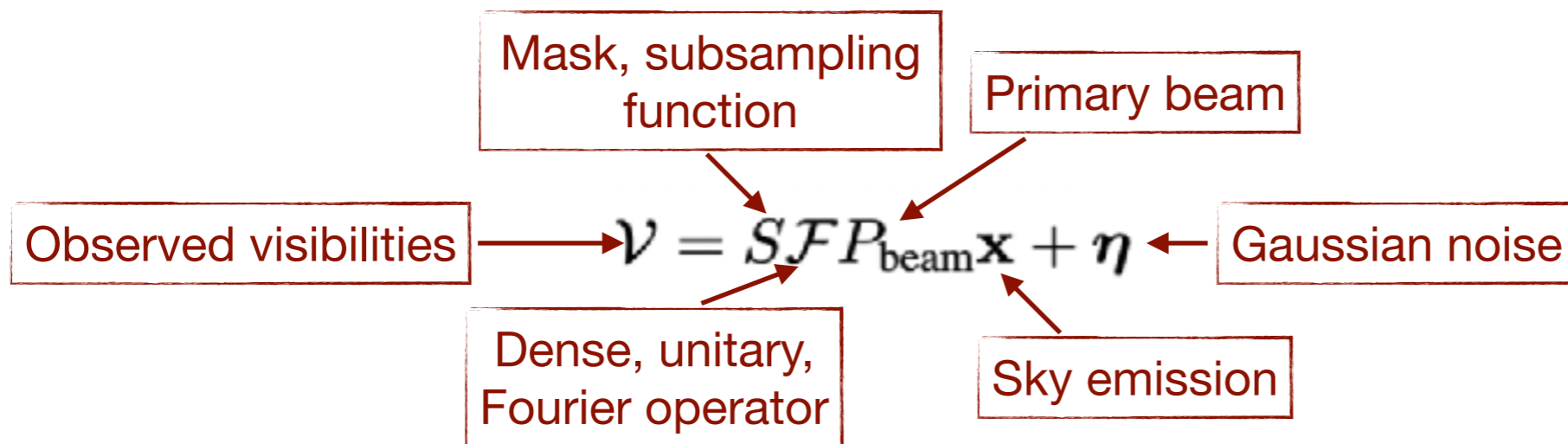
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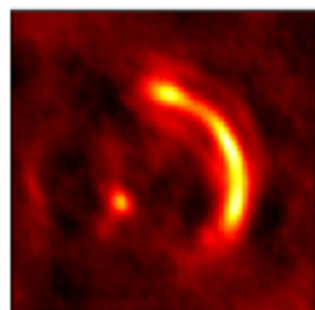
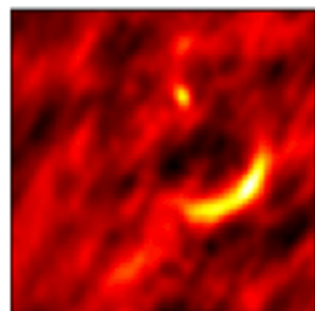
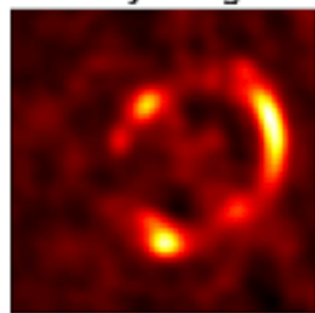


# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models



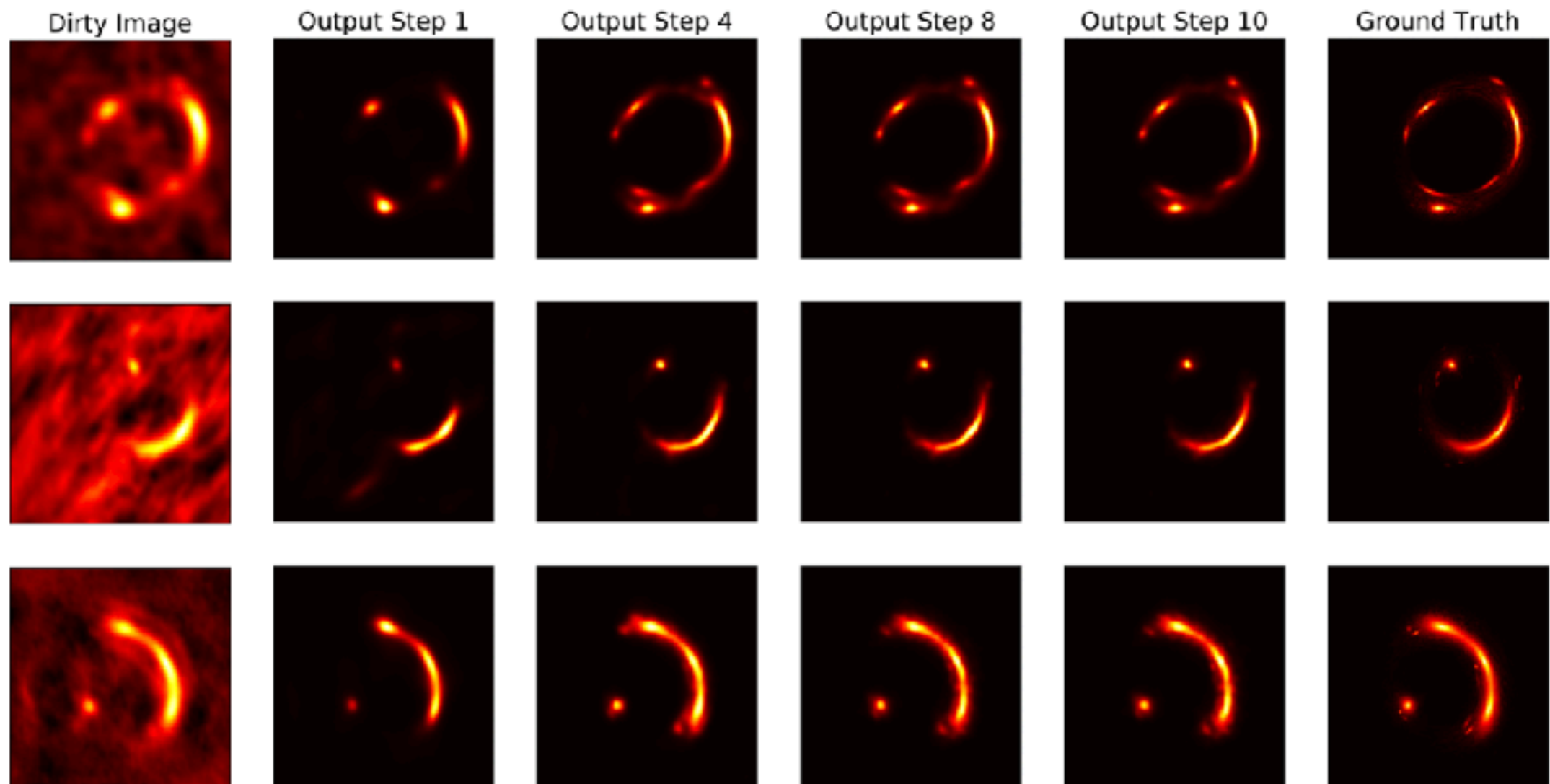
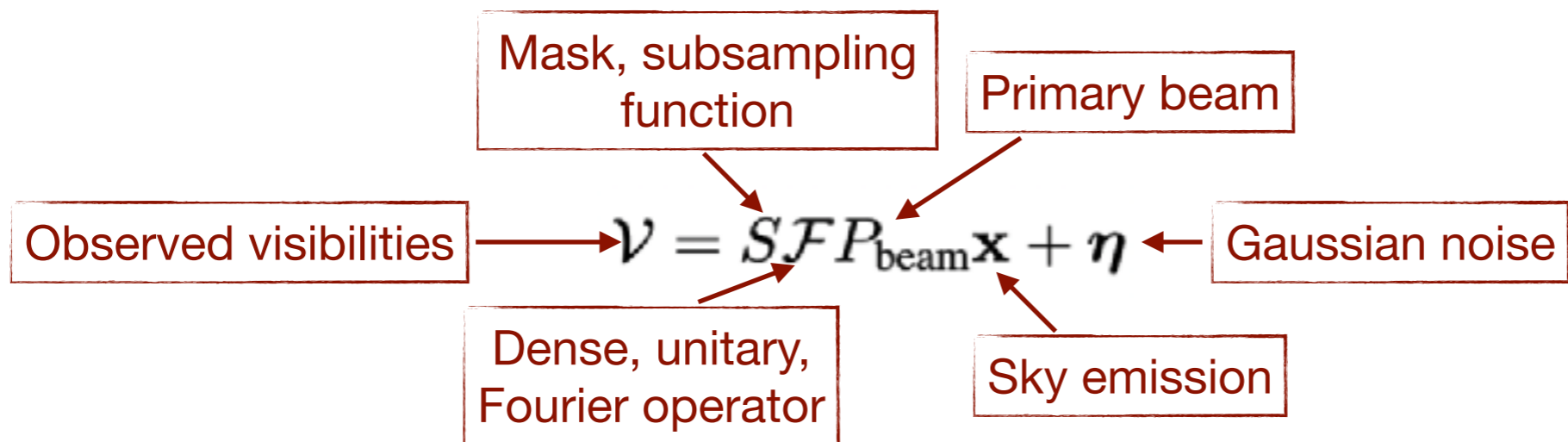
Dirty Image





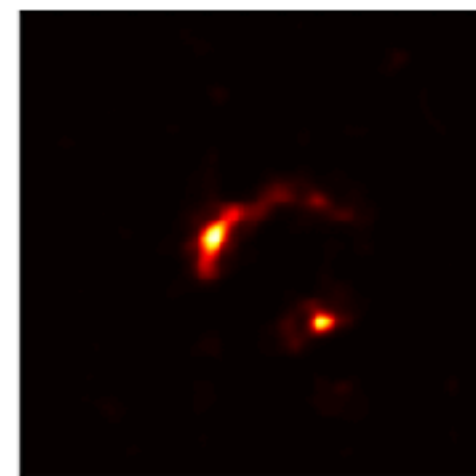
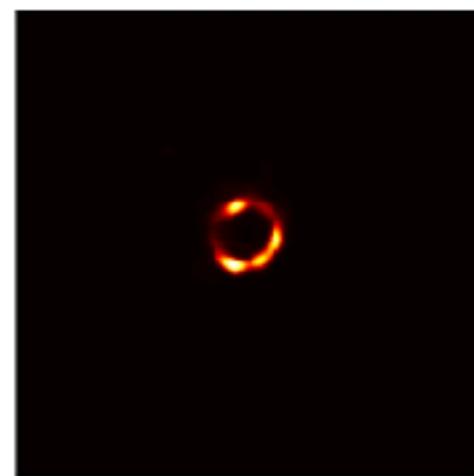
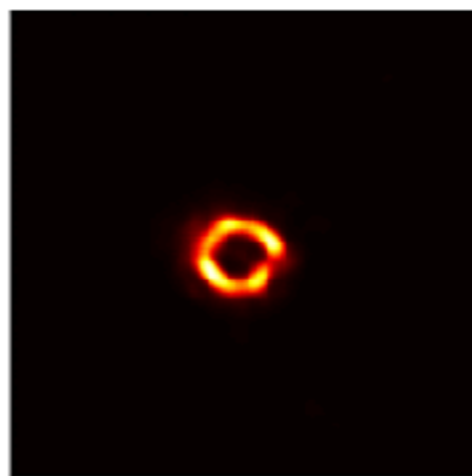
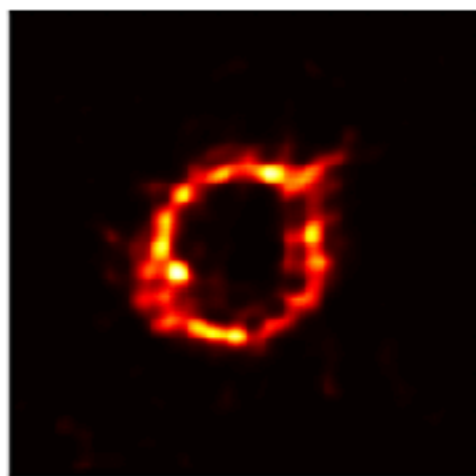
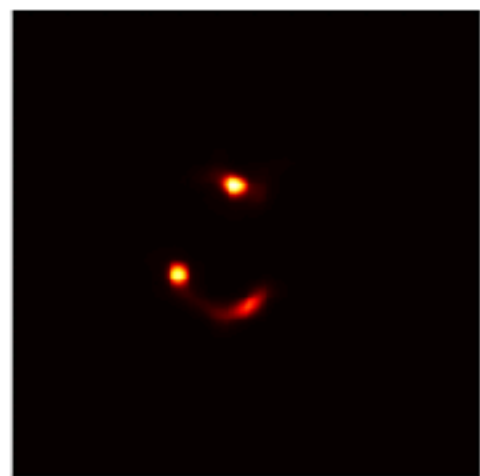
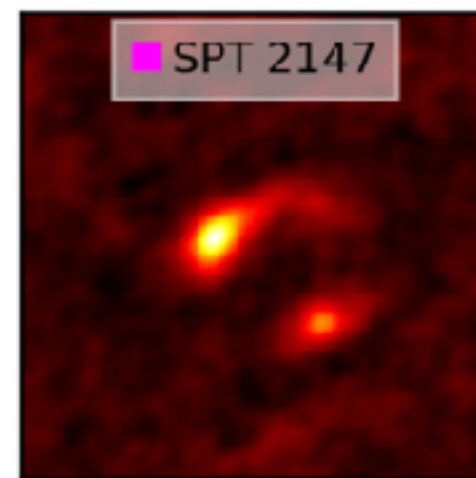
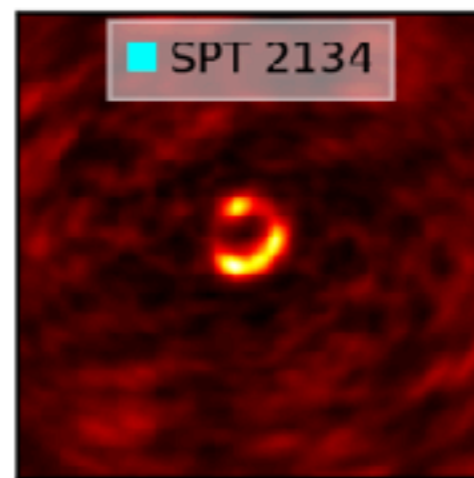
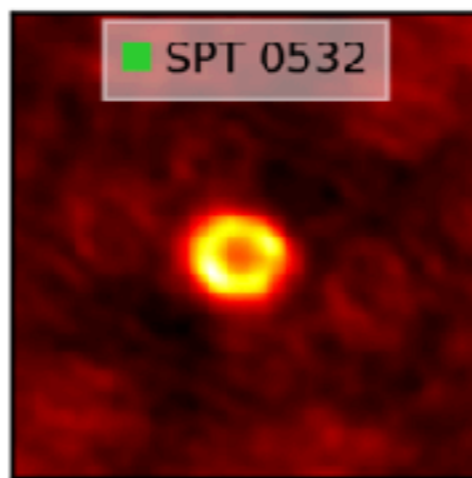
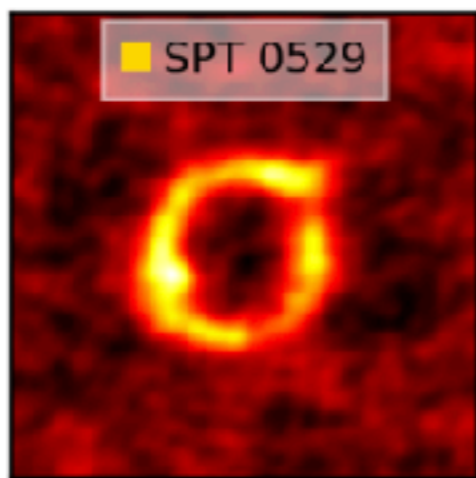
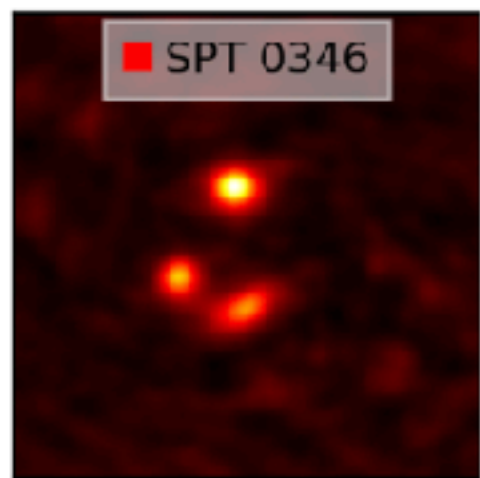
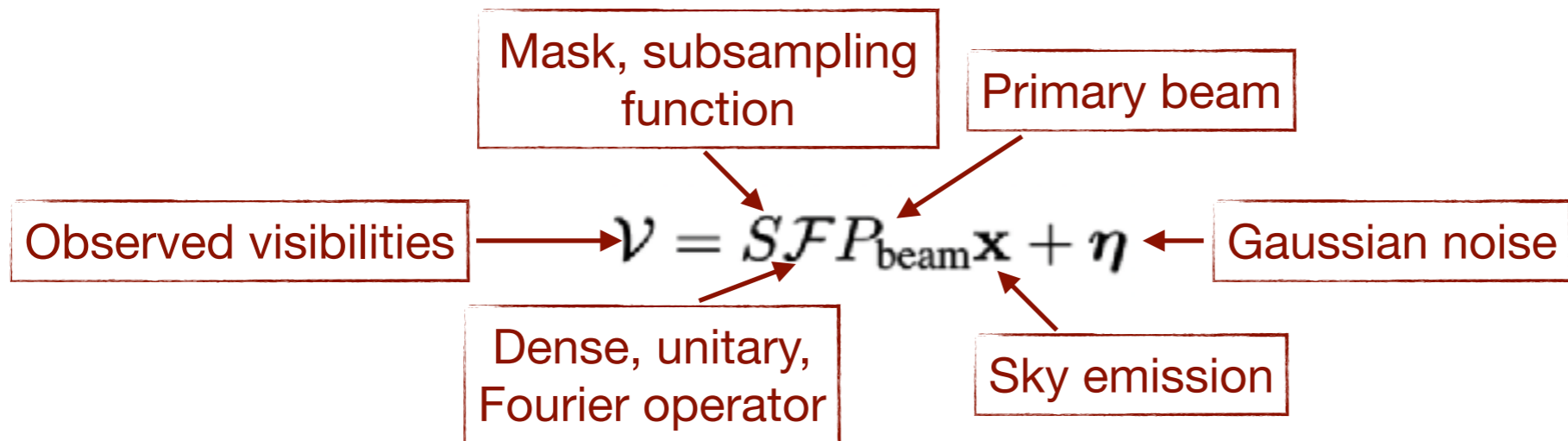
# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models



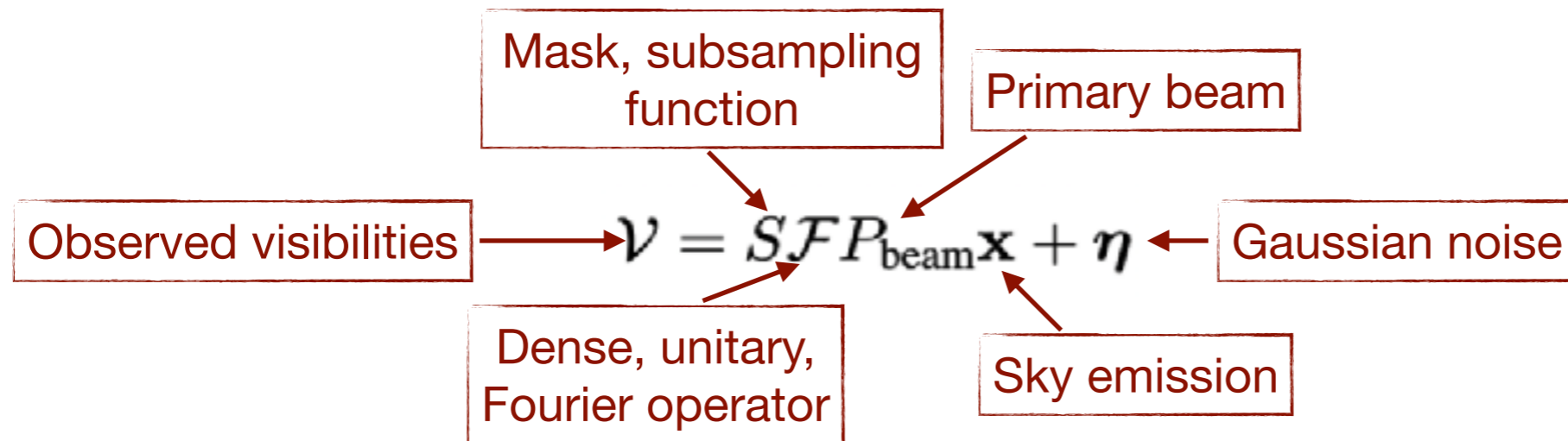
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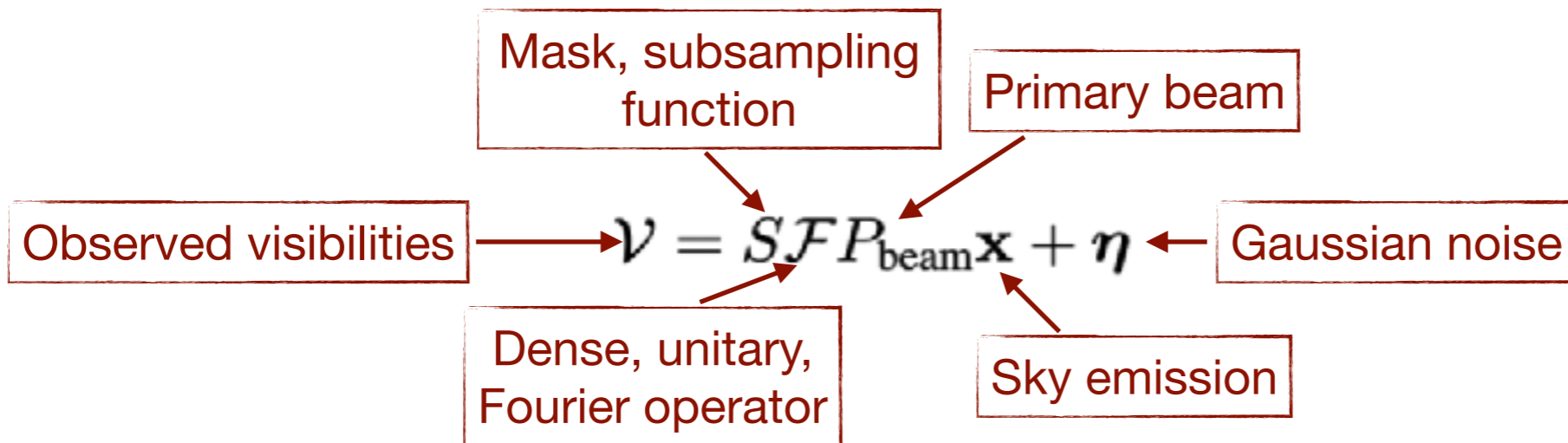
With Score-Based Diffusion Models



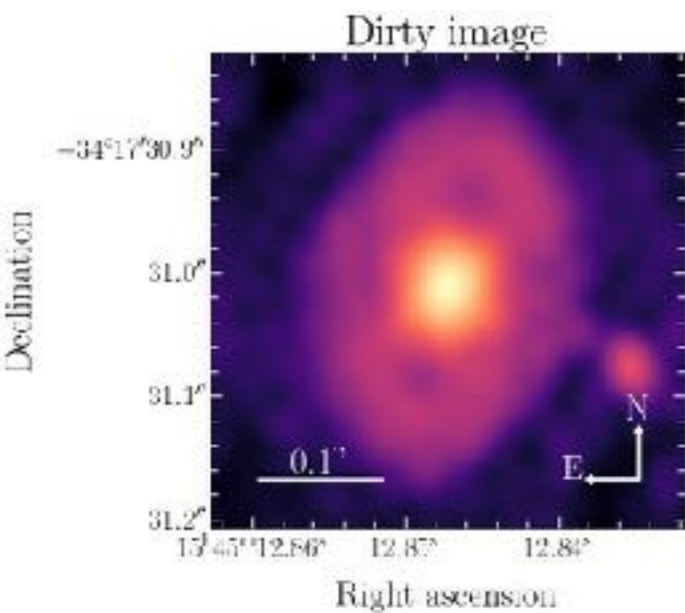
Noé Dia

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With Score-Based Diffusion Models

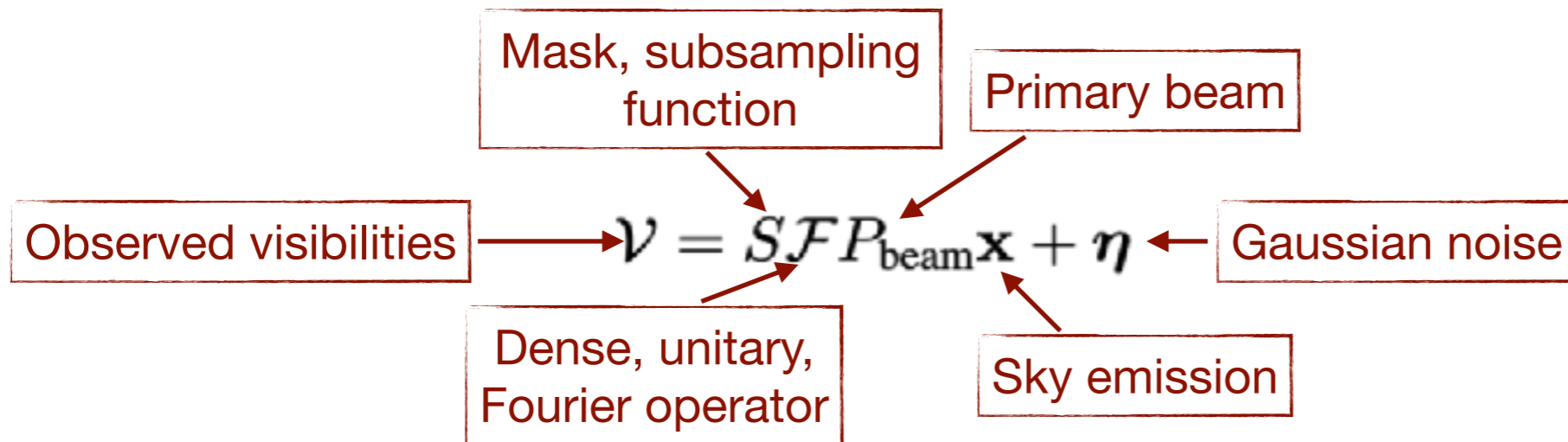


Noé Dia

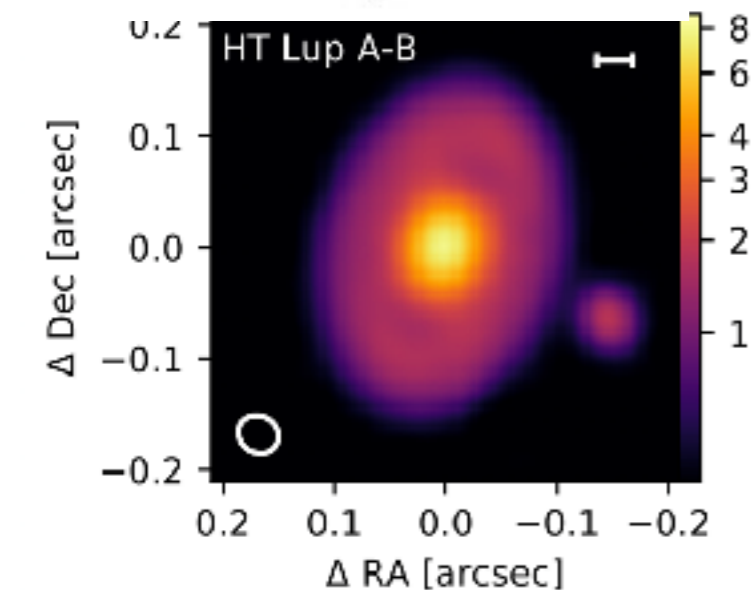
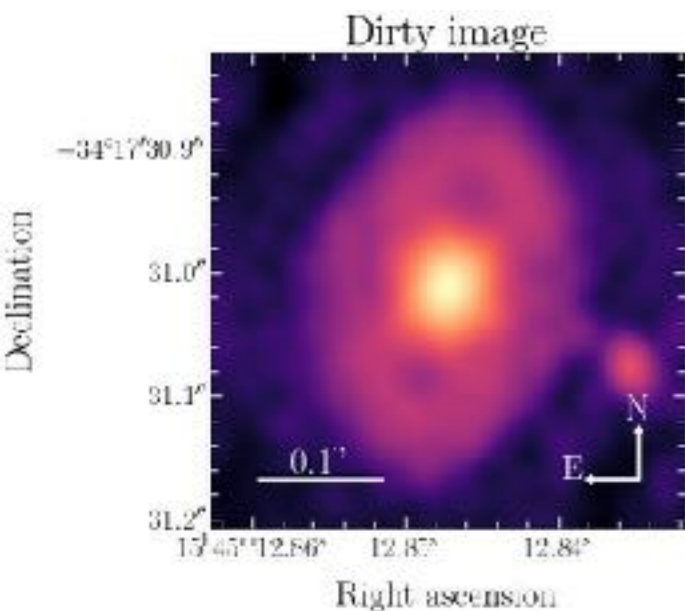


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With Score-Based Diffusion Models

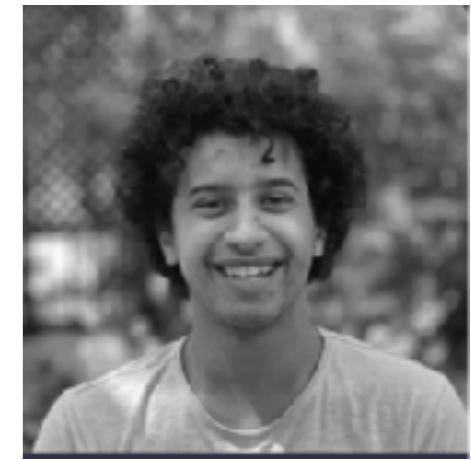


Noé Dia

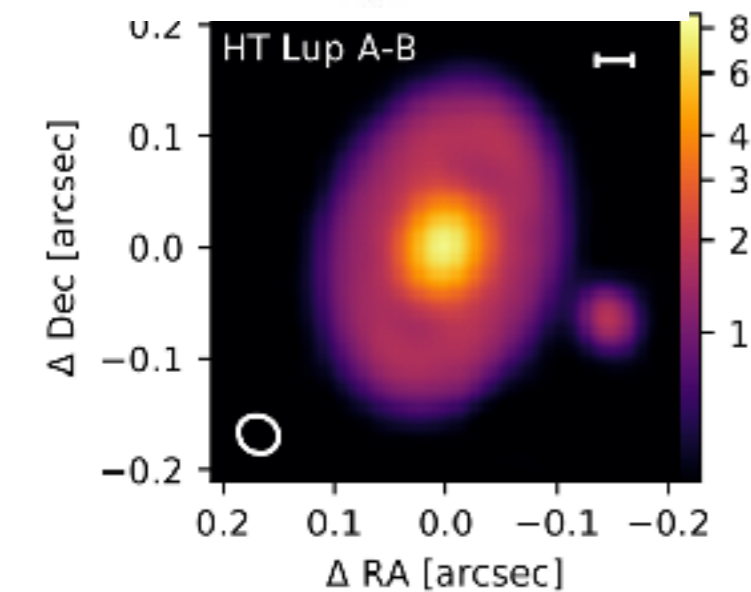
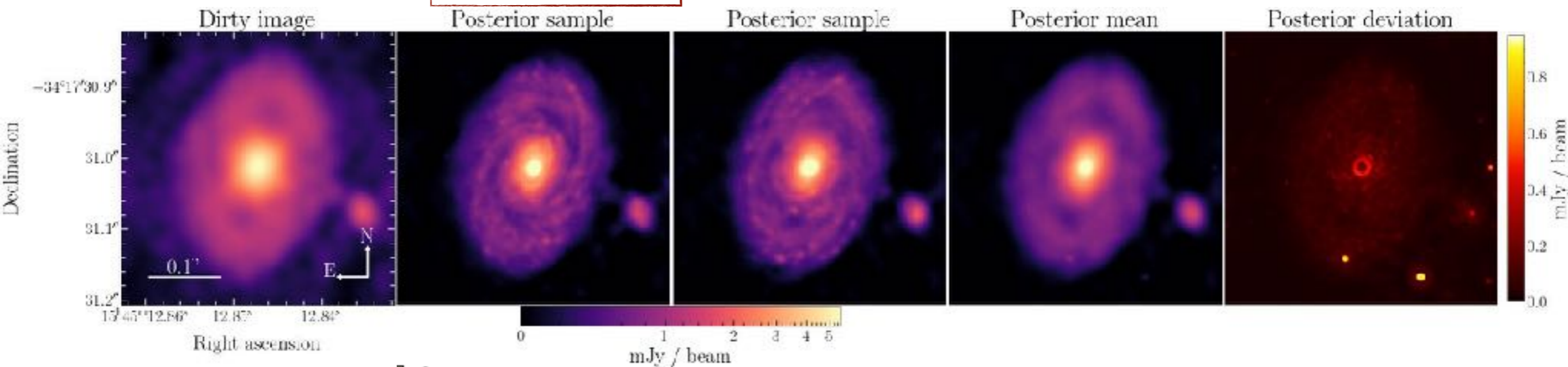
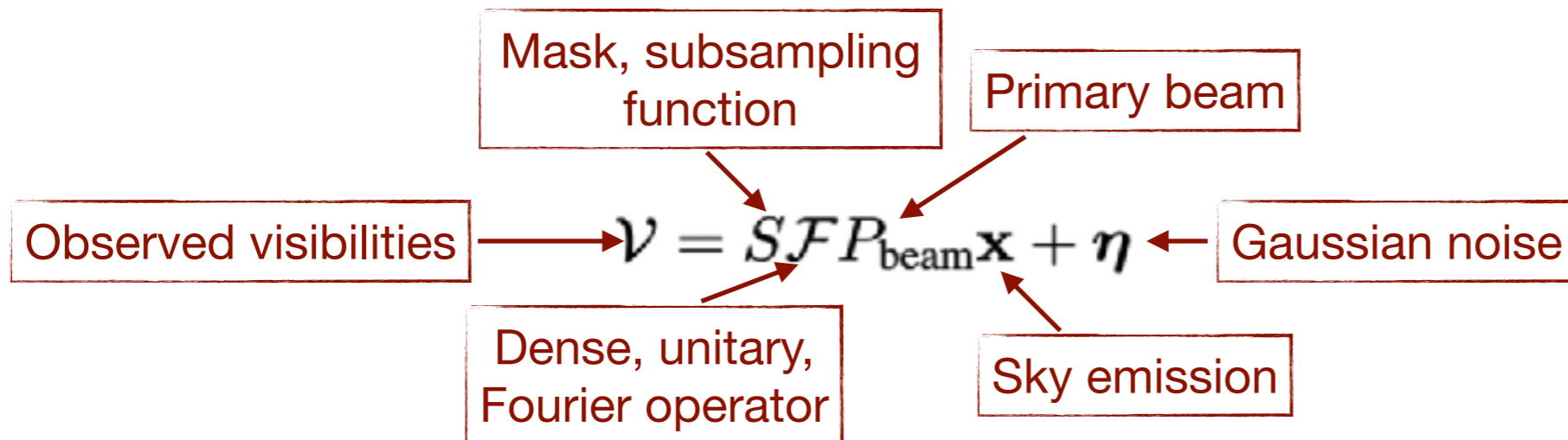


# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models

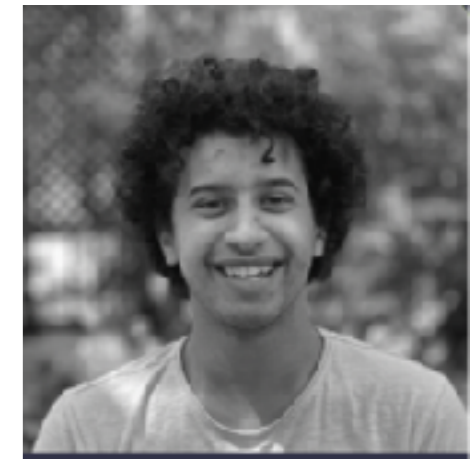


Noé Dia

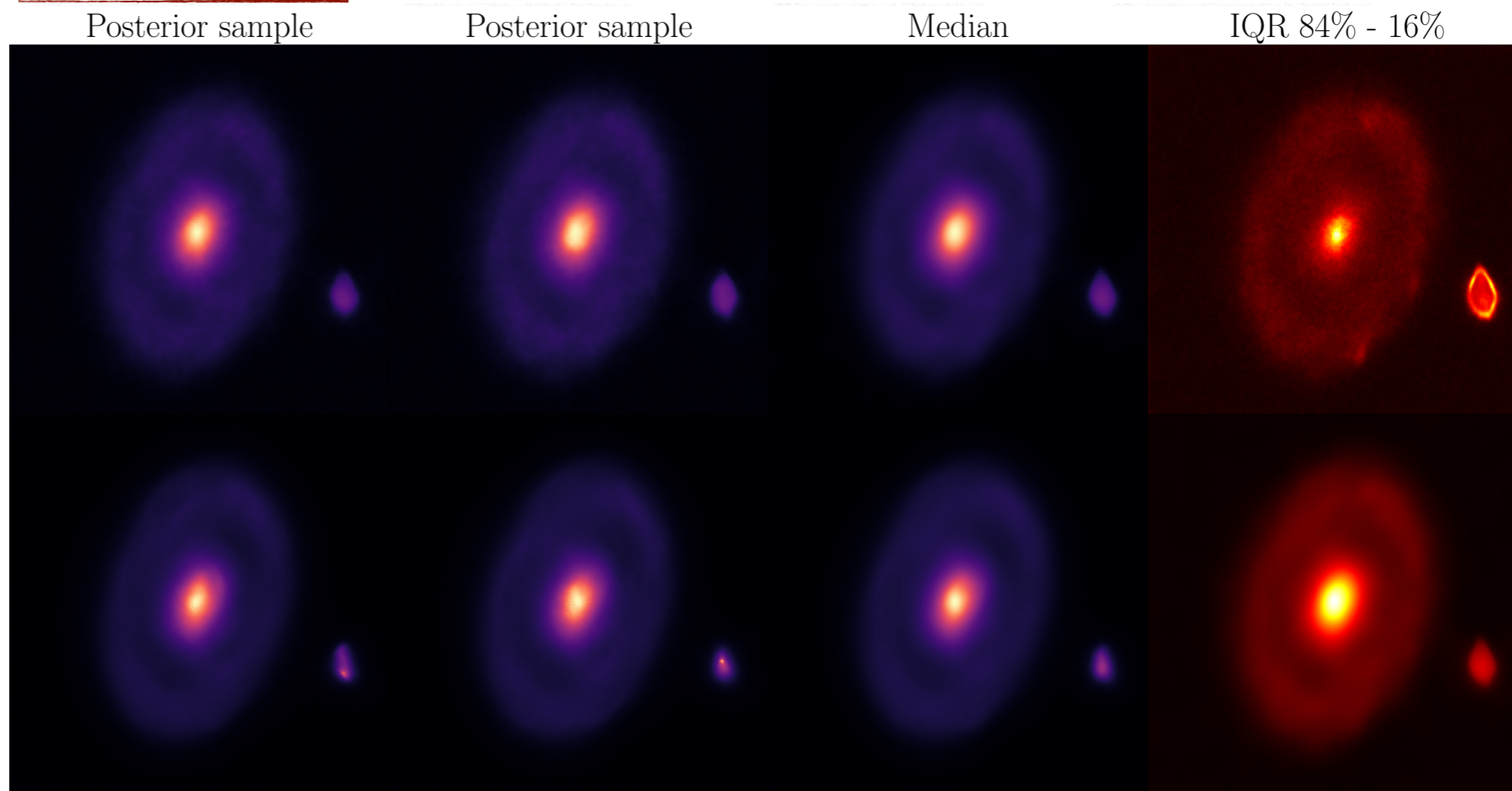
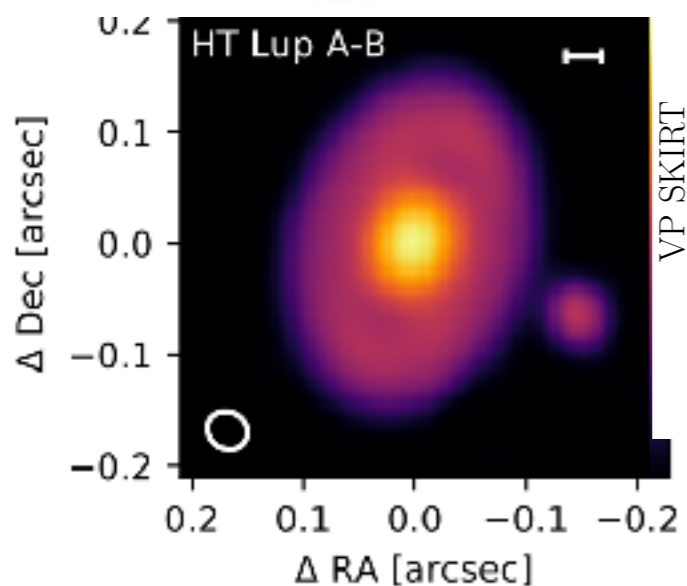
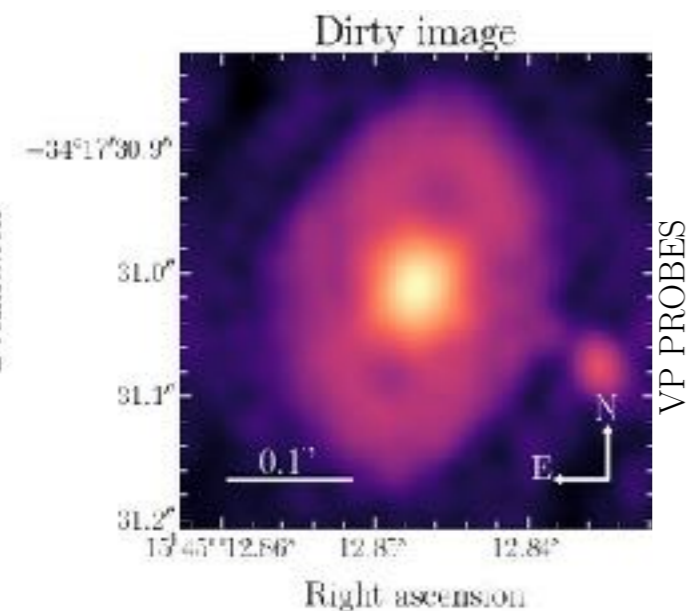
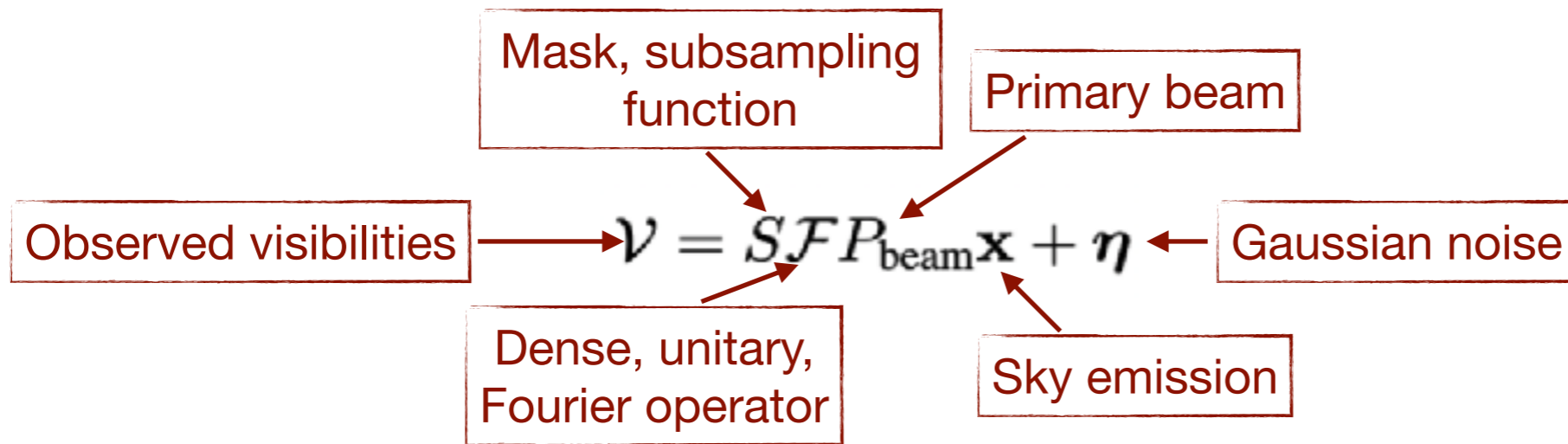


# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models



Noé Dia



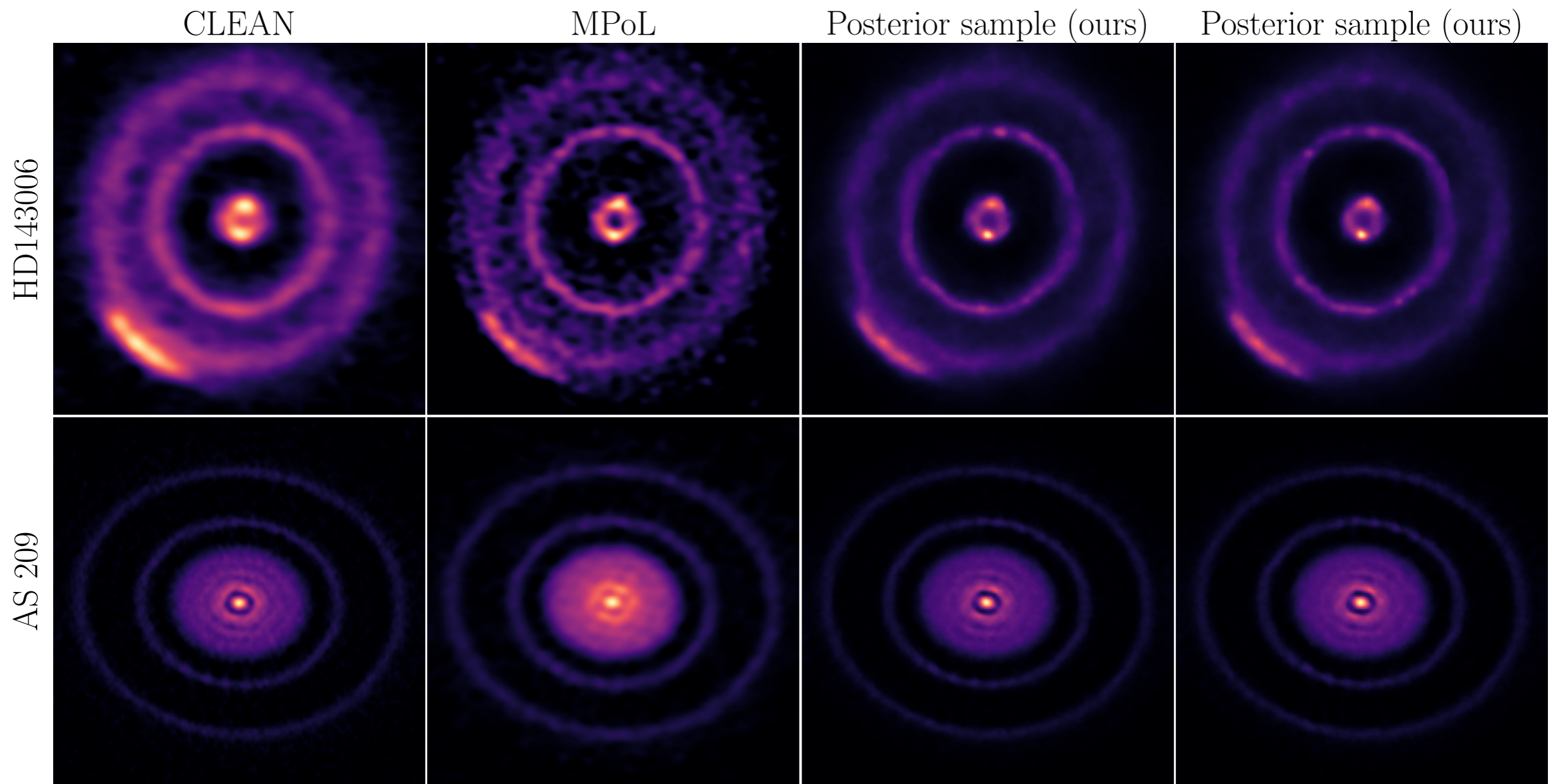
# PSF-DECONVOLUTION FOR INTERFEROMETRIC DATA

With Score-Based Diffusion Models

$$\mathcal{V} = \mathcal{SFP}_{\text{beam}}\mathbf{x} + \boldsymbol{\eta}$$



Noé Dia

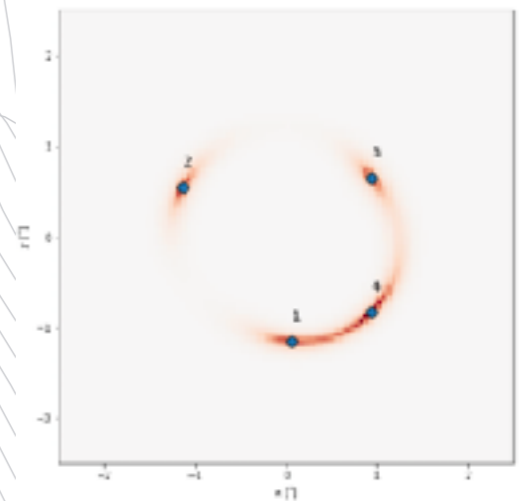




# STRONG LENSING SIMULATION PIPELINE: CAUSTIC

**A fast, AI-empowered, differentiable, extremely modular simulation pipeline for all your strong lensing needs.**

- 1) Lens and source from analytic profiles or pixelated images/densities
- 2) Multiplane lensing
- 3) Line of sight mass distributions
- 4) Fast microlensing simulations
- 5) Time-delays



Connor  
Stone



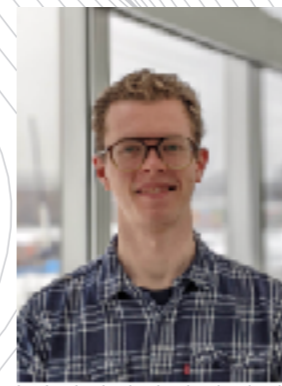
Adam  
Coogan



Andi  
Filipp



Alex  
Adam



Misha  
Barth



Charles  
Wilson

<https://github.com/Ciela-Institute/caustic>

<https://ciela-institute.github.io/caustic/BasicIntroduction.html>

