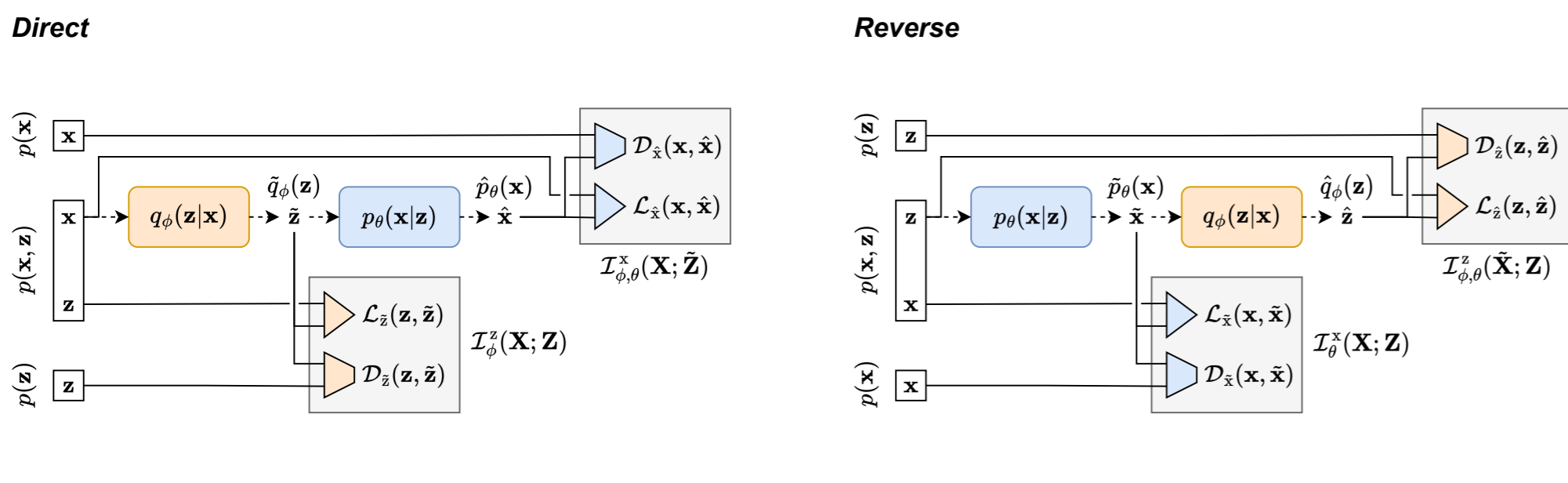


Introduction
A rigorous interpretation of the concepts and principles behind machine learning methods, unifying as many models as possible. Two complementary methods:

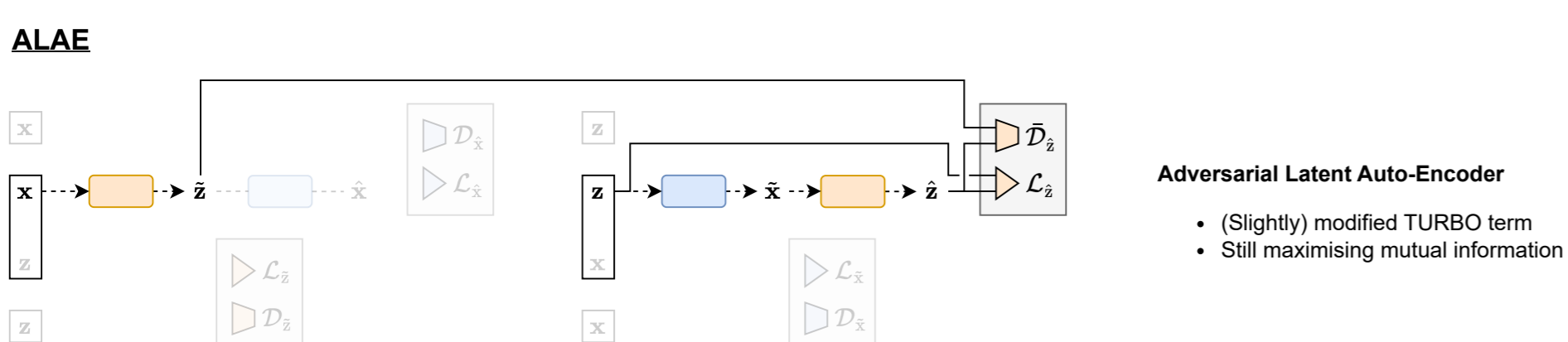
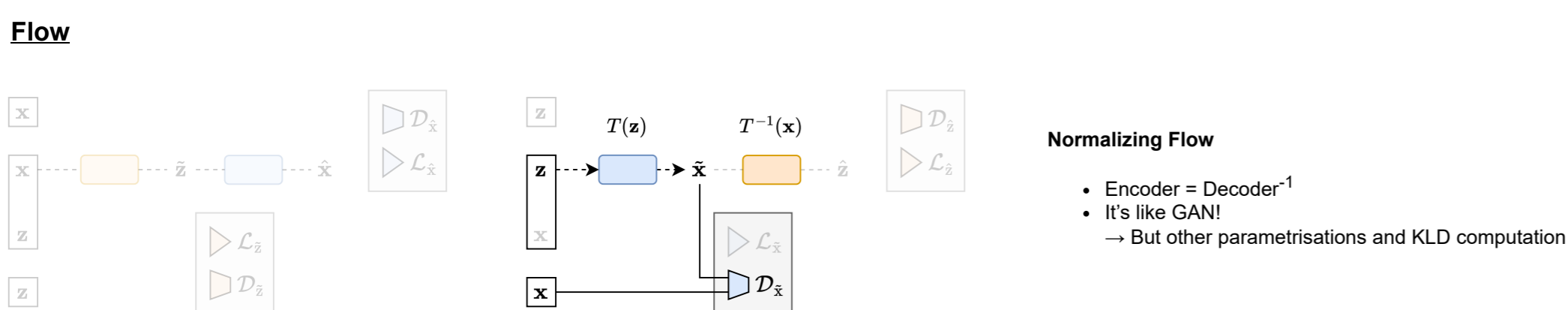
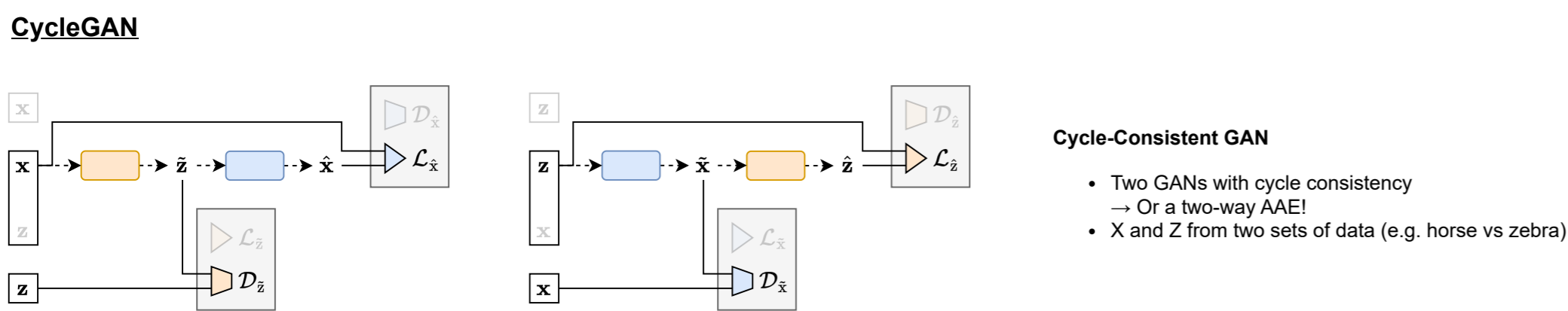
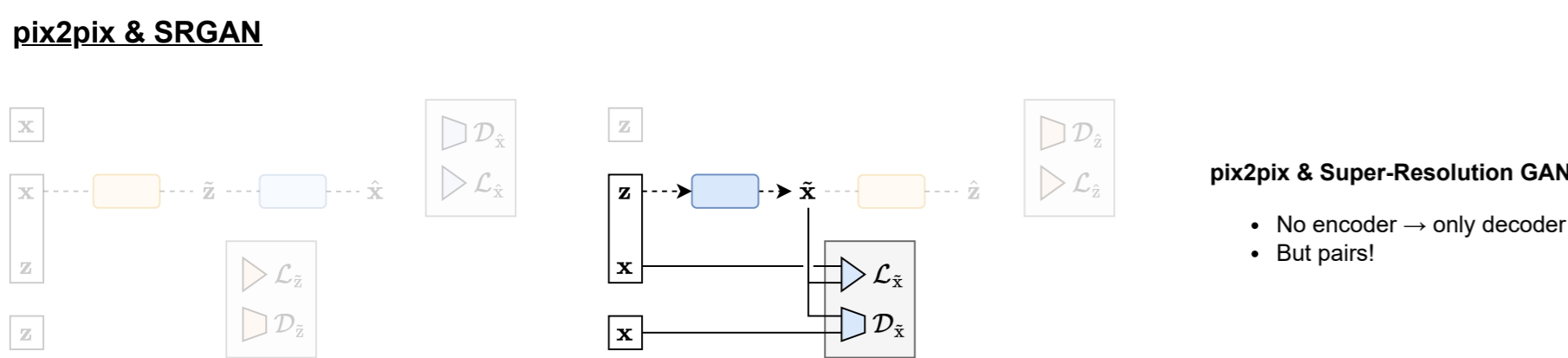
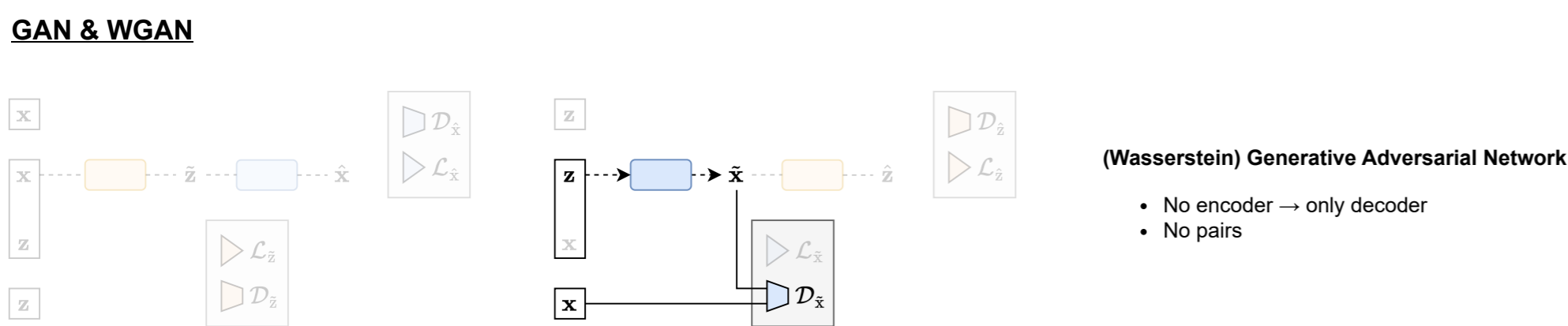
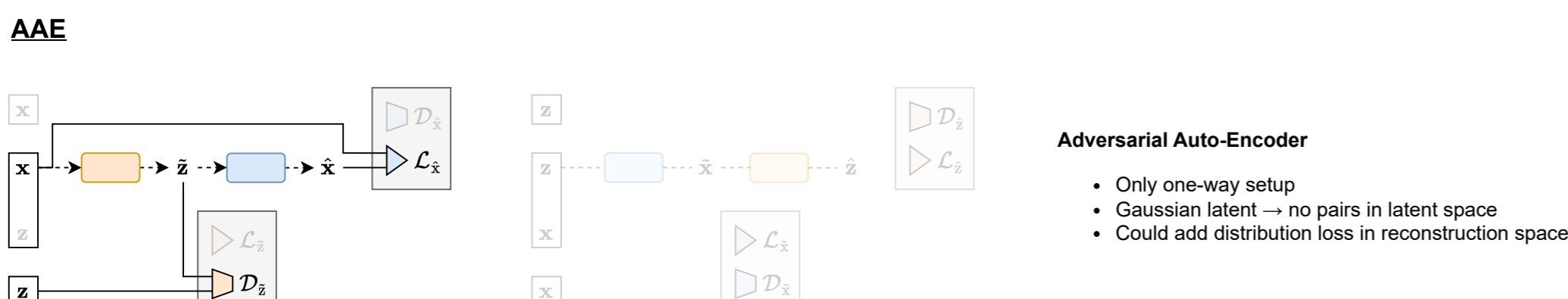
- Bounded Information Bottleneck Auto-Encoder (BIB-AE)
- Two-way Uni-directional Representations by Bounded Optimisation (TURBO)

	BIB-AE	TURBO
Paradigm	<p>Minimising the mutual information between the input space and the latent space, while maximising the mutual information between the latent space and the output space</p> <p>One-way encoding</p> <p>Data and latent space distributions are considered independently</p>	<p>Maximising the mutual information between the input space and the latent space, and maximising the mutual information between the latent space and the output space</p> <p>Two-way encoding</p> <p>Data and latent space distributions are considered jointly</p>
Targeted tasks	<ul style="list-style-type: none"> Data compression, privacy, classification Representation learning 	<ul style="list-style-type: none"> Linking relevant modalities Transcoding/translation between modalities
Advantages	<ul style="list-style-type: none"> Theoretical basis for both supervised and unsupervised tasks Allows for easy sampling 	<ul style="list-style-type: none"> Interpretable latent space Seamlessly handles paired, unpaired and partially paired data The encoder can represent a physical system, while the decoder can represent a learnable model
Drawbacks	<ul style="list-style-type: none"> Not suited for data translation Enforces a distribution for the latent space Struggles to map discontinuous data distributions to continuous latent space distributions 	<ul style="list-style-type: none"> More hyperparameters to tune More modules increases training complexity
Particular cases	VAE, GAN, VAE/GAN	AAE, GAN, pix2pix, SRGAN, CycleGAN, Flows
Related models	InfoVAE, CLUB	ALAE

TURBO
Maximising four lower bounds to mutual information gives rise to the following two-way auto-encoder setup.

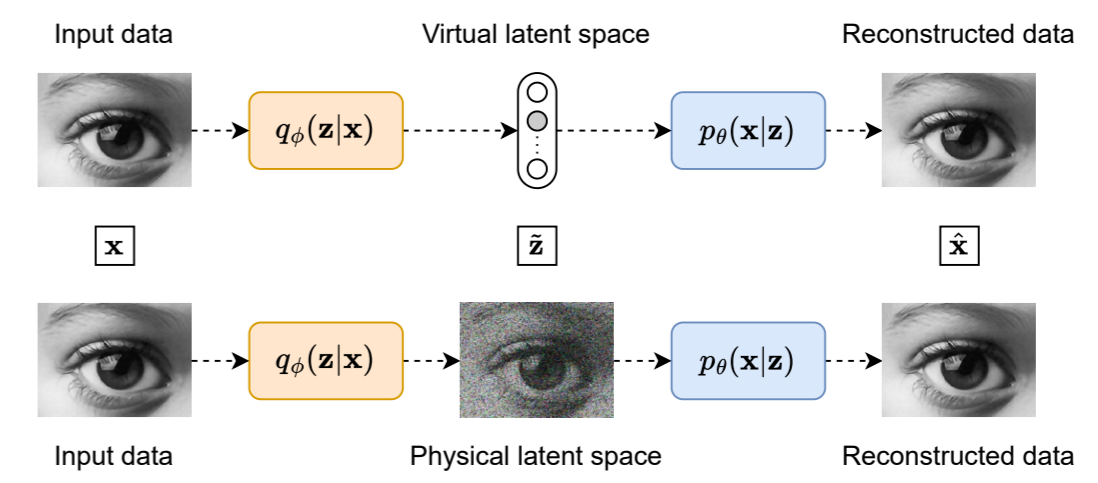


Generalisation of Many Models
Turning on and off the TURBO loss terms lead to many well-known machine learning models.



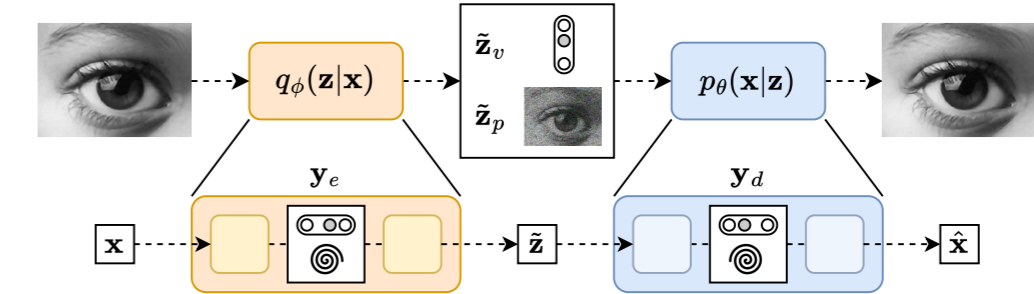
Physical Latent Space
Auto-encoders with a *virtual* latent space or a *physical* latent space.

- In the virtual setting, the latent variable does not have any physical meaning (e.g. random noise, category, etc.).
- In the physical setting, the latent variable represents a part of the physical observation or measurement chain.



Composition of different latent space settings and several auto-encoder-like networks as internal components of a global auto-encoder architecture.

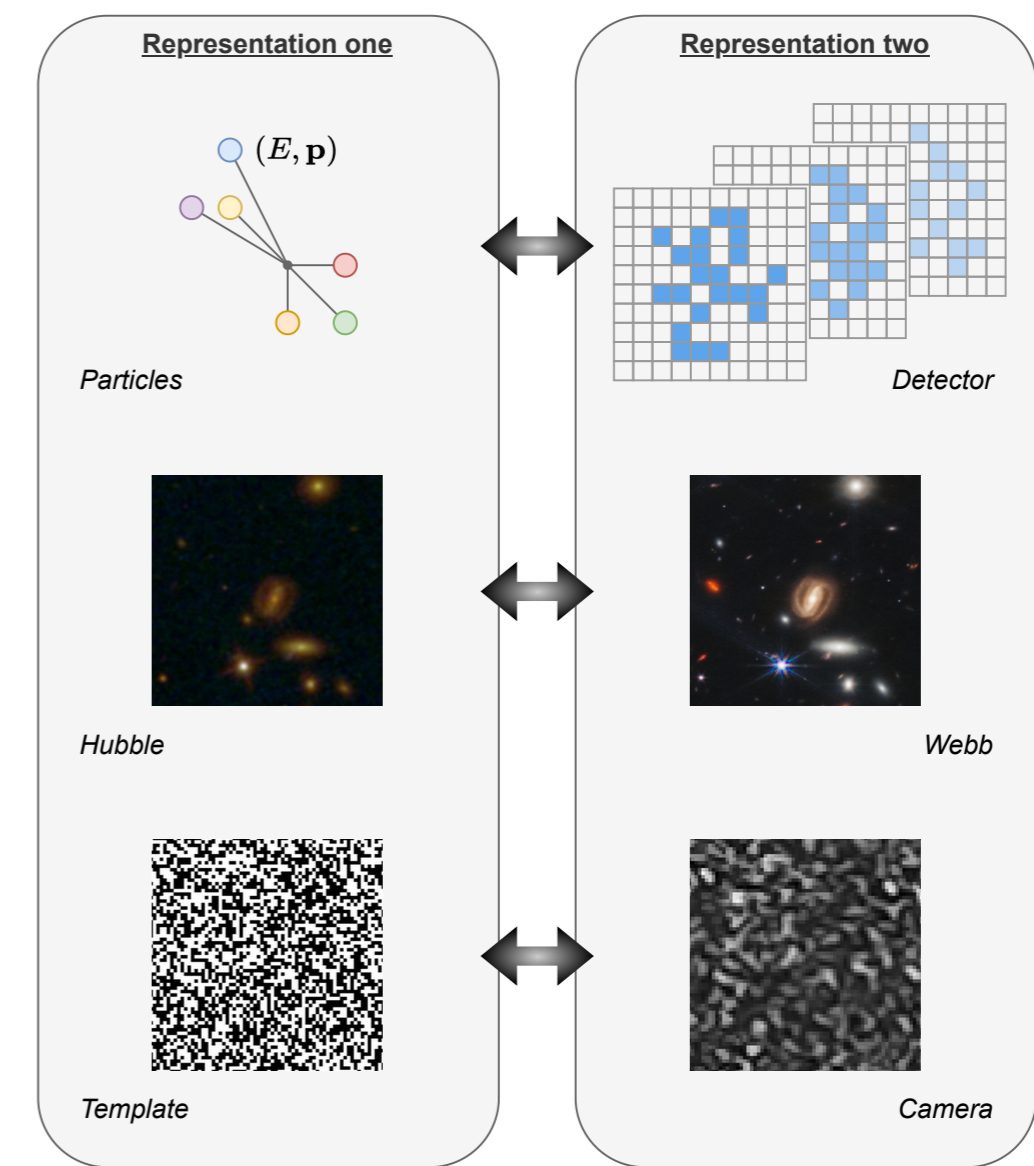
- The global latent variable can contain both a virtual and a physical parts.
- The global encoder and decoder can be nested auto-encoders with internal latent variables of any kind.



Applications

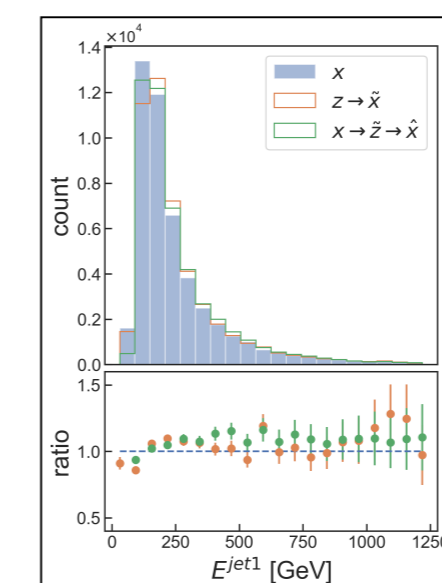
Highlights of three practical applications where TURBO shows interoperability, superior performance with respect to the models compared, more stable and efficient training.

- The top row shows a high-energy physics example, where particles with given four-momenta are created in a collider experiment and detected by a detector.
- The middle row shows a galaxy imaging example, where two pictures of the same portion of the sky are taken by two different telescopes.
- The bottom row shows a counterfeiting detection example, where a digital template is acquired by a phone camera.



TURBO in High-Energy Physics: Turbo-Sim

Transform the real four-momenta of a set of particles created by the collision of two protons in a collider experiment into the observed four-momenta of the particles captured by detectors, and vice versa. A clever interpretation of the problem is to think of the real and the observed spaces as two different representations of the same physical system.

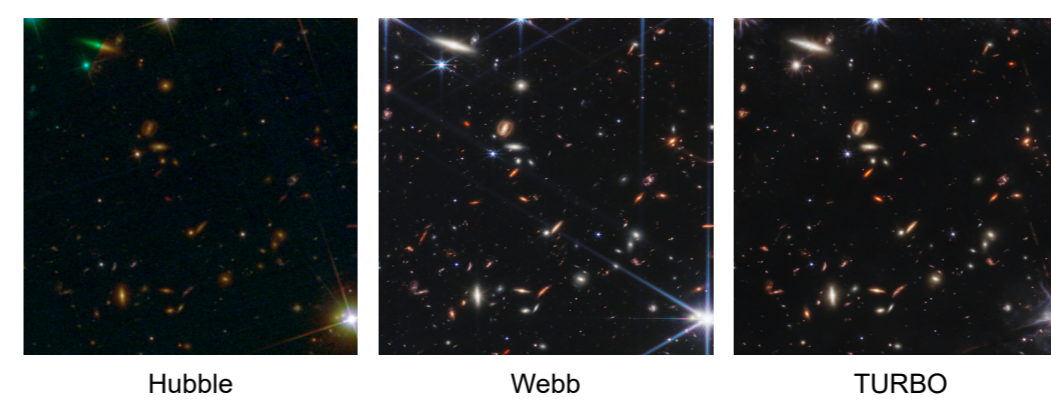


The Kolmogorov-Smirnov distance between the original data simulation and samples generated by the model. The energy of a real particle, a b-quark and the energy of the leading jet are shown, as well as the invariant mass of the top-quarks pair, which are unstable particles decaying into the real ones before flying through the detectors to be observed.

	Z space	X space	Rec. space
Model	E^b	E^{jet1}	m_{tt}
OTUS	2.76	5.75	15.8
Turbo-Sim	3.96	4.43	2.97

TURBO in Astronomy: Hubble-to-Webb

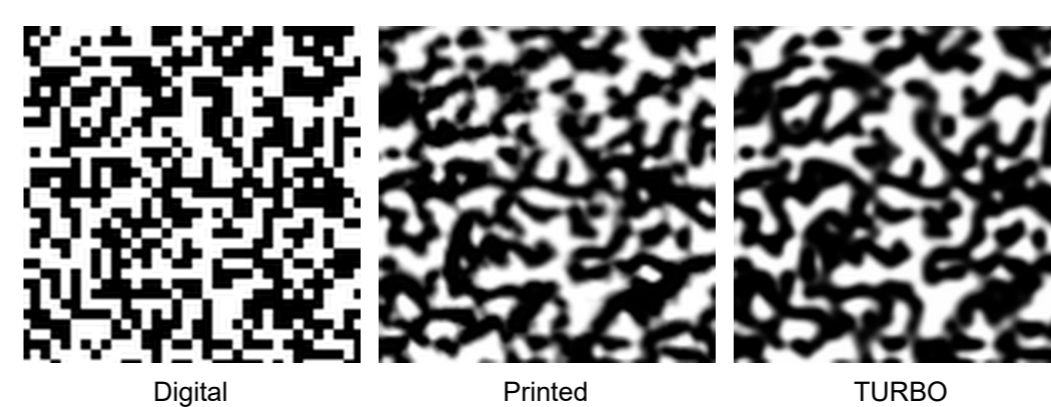
Using TURBO as an image-to-image translation framework to generate simulated images of the James Webb Space Telescope from observed images of the Hubble Space Telescope and vice versa.



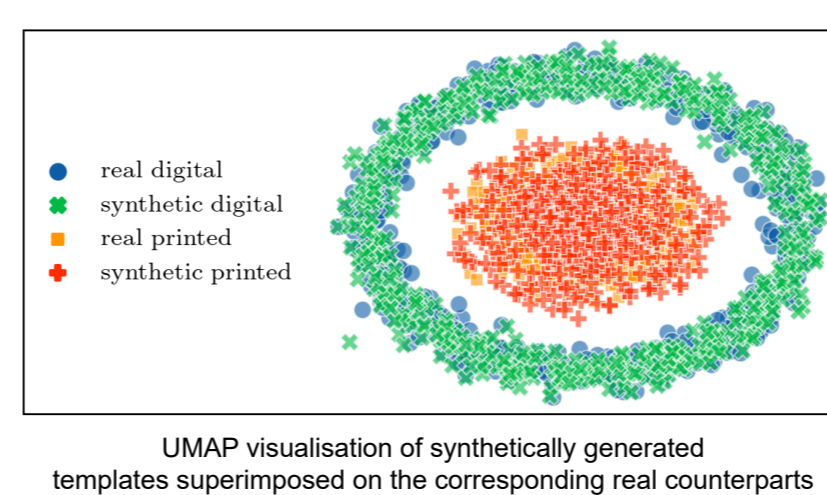
Model	MSE ↓	SSIM ↑	PSNR ↑	LPIPS ↓	FID ↓
CycleGAN	0.0097	0.83	20.11	0.48	128.1
pix2pix	0.0021	0.93	26.78	0.44	54.58
TURBO	0.0026	0.92	25.88	0.41	43.36

TURBO in Anti-Counterfeiting: Digital Twin

Accurately estimate the complex stochastic process of printing and generate predictions of how a digital template would appear once printed, as well as reversing the process and predict the original digital template from the printed one.



Model	FID _{x-z} ↓	FID _{z-x} ↓	Hamming ↓	MSE ↓	SSIM ↑
w/o processing	304	304	0.24	0.18	0.48
CycleGAN	3.87	4.45	0.15	0.05	0.73
pix2pix	3.37	8.57	0.11	0.05	0.76
TURBO	3.16	6.60	0.09	0.04	0.78



References

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- Quéant G., Drozdova M., Kinakh V., Golling T., Voloshynovskiy S. *Turbo-Sim: A generalised generative model with a physical latent space*. In Proceedings of the Workshop on Machine Learning and the Physical Sciences, NeurIPS, 2021. <https://arxiv.org/abs/2112.10629>
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