

# Combined effect of Beam-Beam and Impedance

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# Outline

- Overview of Study with Longitudinal Impedance (ZL)
- Simulation(Analysis) with Transverse Impedance (ZT)
  - FCCee
  - Other Machines (CEPC/SuperKEKB)
  - Mitigation
- Summary

# Crab-waist collision

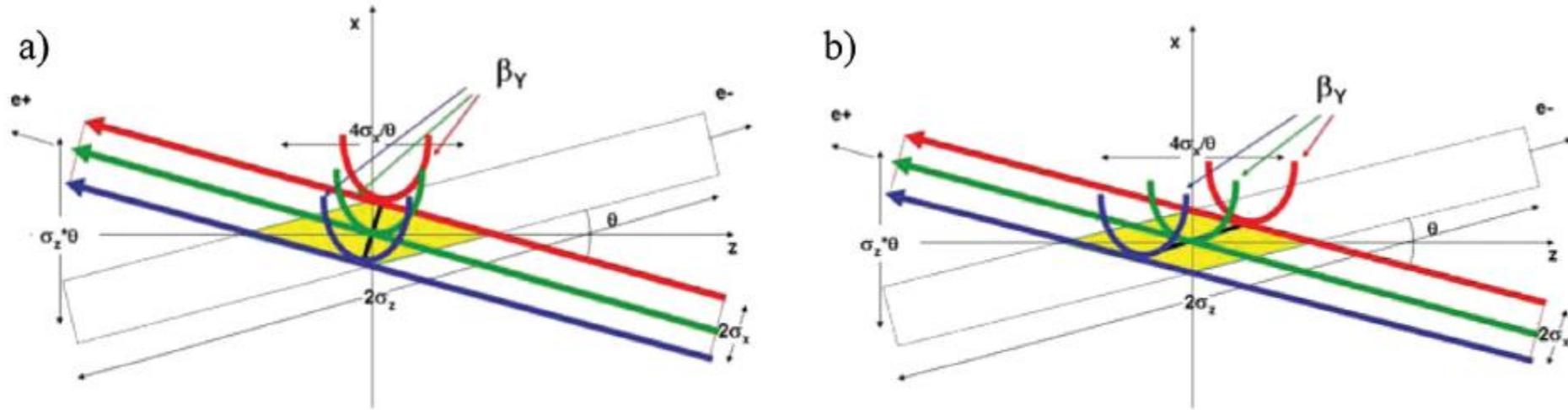


FIG. 1 (color). Crab-waist collision scheme. The color straight lines show directions of motion for particles with different horizontal deviations from the central orbit. The arrows indicate the corresponding  $\beta$  function variations along these trajectories.

$$L \propto \frac{N \xi_y}{\beta_y^*}; \quad \xi_y \propto \frac{N \sqrt{\beta_y^*/\epsilon_y}}{\sigma_z \theta}; \quad \xi_x \propto \frac{N}{(\sigma_z \theta)^2},$$

$$\varphi = \frac{\sigma_z}{\sigma_x} \tan\left(\frac{\theta}{2}\right) \approx \frac{\sigma_z}{\sigma_x} \frac{\theta}{2}.$$

$$\beta_y^* \approx \frac{\sigma_x}{\theta} \ll \sigma_z.$$

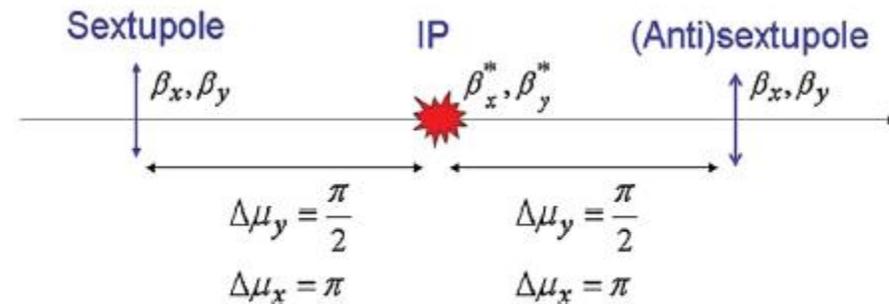
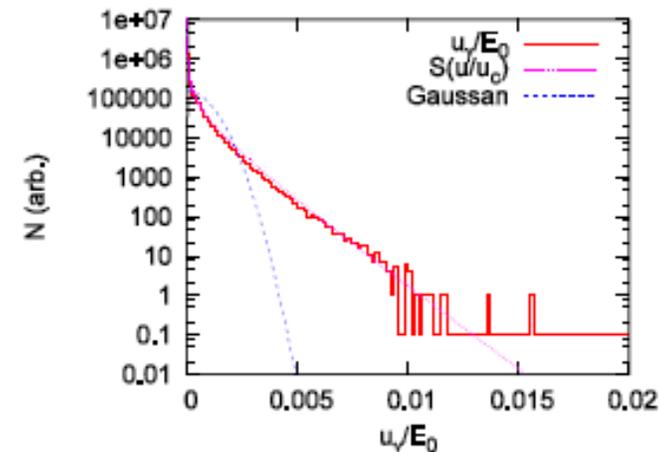
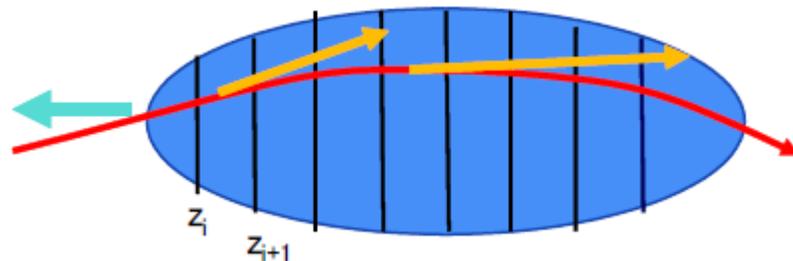


FIG. 2 (color). Crab sextupole locations.

# Beamstrahlung Effect & 3D flip-flop

- Synchrotron radiation during beam-beam interaction
- High energy photon  $\rightarrow$  Momentum acceptance  $\rightarrow$  Lifetime
- Longer bunch length and Higher energy spread
- Beam blowup: 3D flip-flop



# Coherent Beam-Beam Instability with a Large Crossing Angle

K. Ohmi, Int. J. Mod. Phys. A, 31, 1644014 (2016).

K. Ohmi and et al., PRL 119, 134801 (2017)

N. Kuroo et al, PHYS. REV. ACCEL. BEAMS 21, 031002 (2018)

K. Ohmi, eeFACT 2018

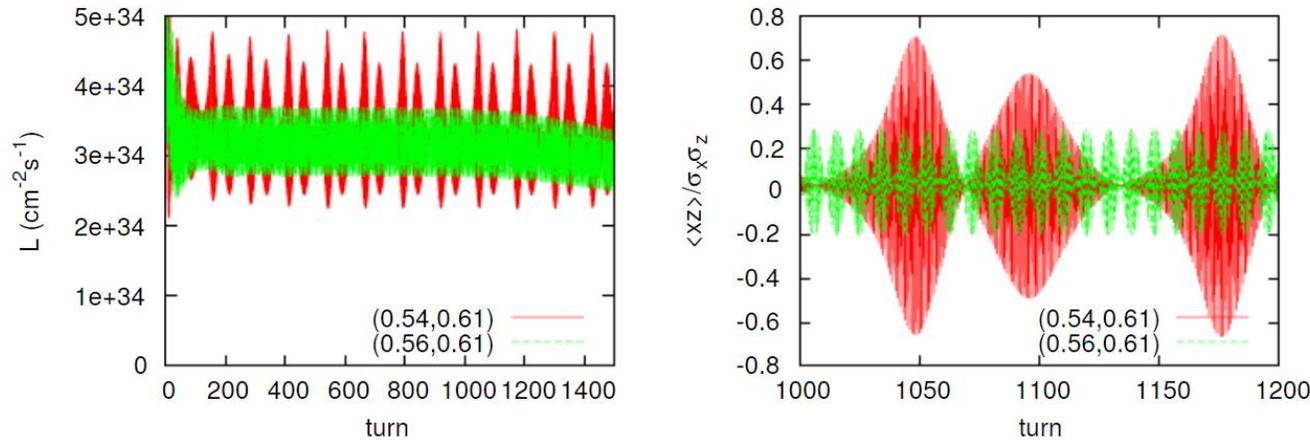


Fig. 5. Luminosity and  $\langle xz \rangle$  evolutions given by a strong-strong simulation using BBSS code.

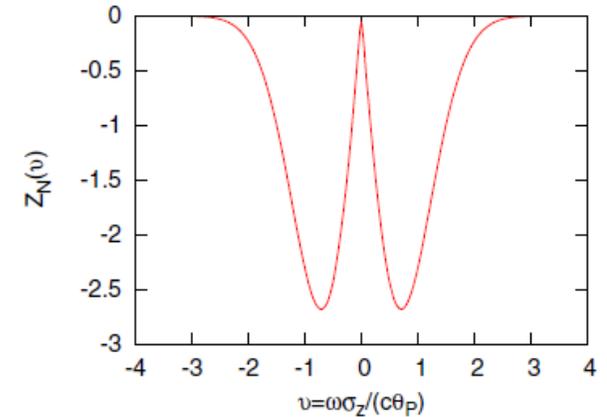


FIG. 3. Imaginary part of normalized cross impedance, where  $v = \omega \sigma_z / (c \theta_p)$ .

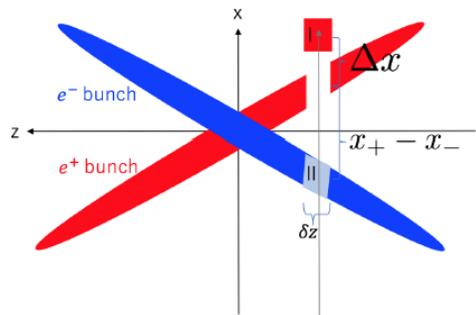


FIG. 1. Illustrative representation of the evaluation of the cross-wake force.

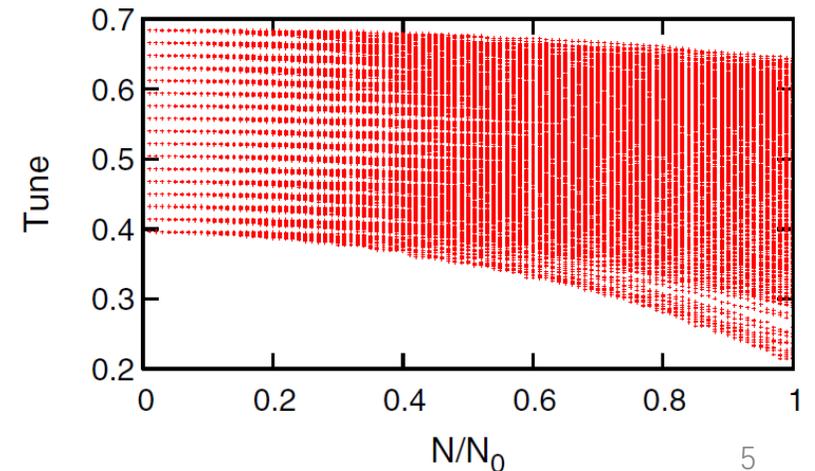
- Usual wake force gives correlation between bunch head to tail. Head-tail instability is induced by synchrotron motion

$$\Delta p_x(z) = - \int_z^\infty W(z - z') \rho_x(z') dz'$$

- **Cross wake field** gives correlation of two colliding beam by convolution of each dipole moment.

$$\Delta p_{x,\mp}(z_\mp) = - \int_{-\infty}^\infty W_x^{(\mp)}(z_\mp - z'_\pm) \rho_x^{(\pm)}(z'_\pm) dz'_\pm$$

- Cross wake force induced by the beam-beam interaction is localized at IP.



# Why have we started with the longitudinal impedance and transverse impedance?

1. In the collision scheme with Crab Waist and Large Piwinski Angle the luminosity and tune shifts **strongly depend on the bunch length**

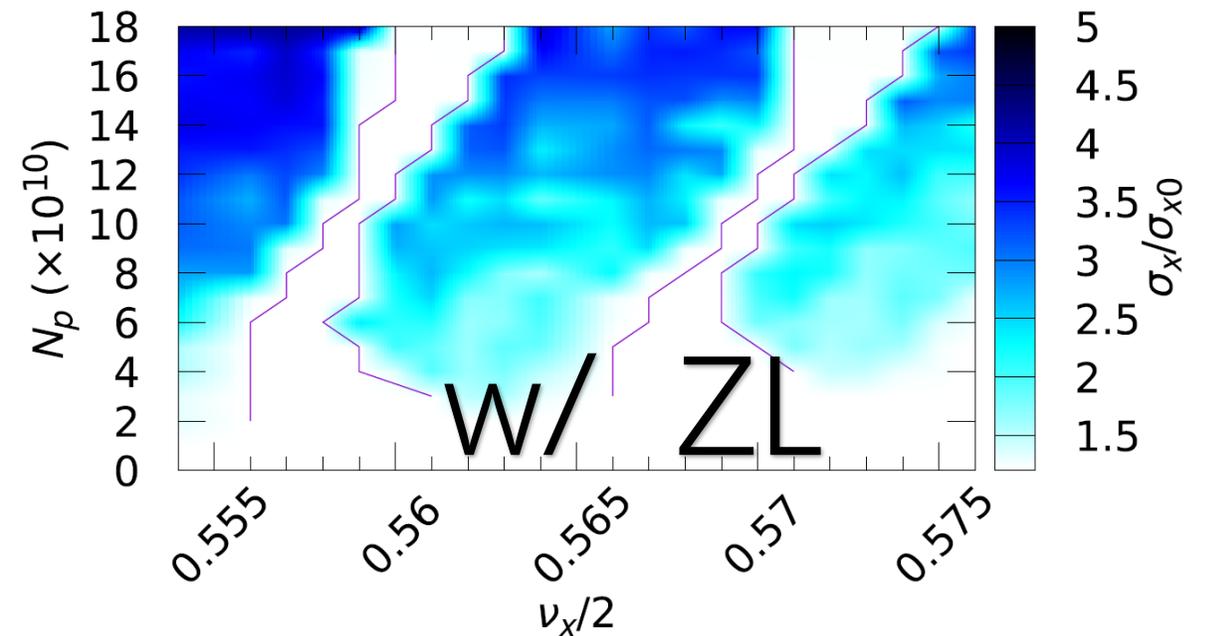
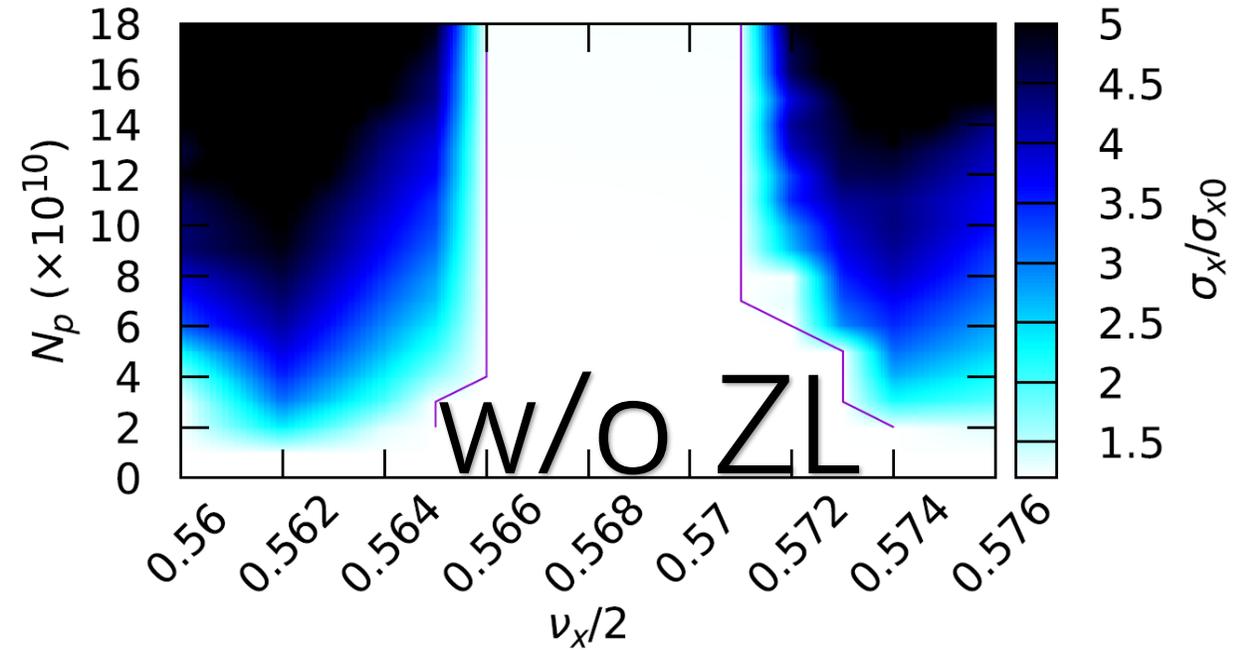
$$L \propto \frac{N\xi_y}{\beta_y^*}, \quad \xi_y \propto \frac{N\sqrt{\beta_y/\varepsilon_y}}{\sigma_z\theta}, \quad \xi_x \propto \frac{N}{(\sigma_z\theta)^2}$$

2. For the future circular colliders with extreme beam parameters in collision several **new effects** become important such as beamstrahlung, coherent X-Z instability and 3D flip-flop. **The longitudinal beam dynamics plays an essential role for these effects**

3. Considering transverse impedance is very natural:

- Why not transverse impedance, since longitudinal impedance is included
- Transverse impedance change the coherent betatron tune

	Z
Circumference (km)	97.75 km
Beam energy (GeV)	45.6
Bunch population ( $10^{11}$ )	1.7
Bunches per beam	16640
RF frequency (MHz)	400
RF Voltage (GV)	0.1
Energy loss per turn (GeV)	0.036
Longitudinal damping time (turns)	1273
Momentum compaction factor $10^{-6}$	14.8
Horizontal tune	269.139
Vertical tune	269.219
Synchrotron tune	0.025
Horizontal emittance (nm)	0.27
Vertical emittance (pm)	1.0
IP number	2
Nominal bunch length (mm) (SR/BS)*	3.5/12.1
Nominal energy spread (%) (SR/BS)*	0.038/0.132
Piwnski angle (SR/BS)*	8.2/28.5
$\xi_x/\xi_y$	0.004/0.133
Horizontal $\beta^*$ (m)	0.15
Vertical $\beta^*$ (mm)	0.8
Luminosity/IP ( $10^{34}/\text{cm}^2\text{s}$ )	230



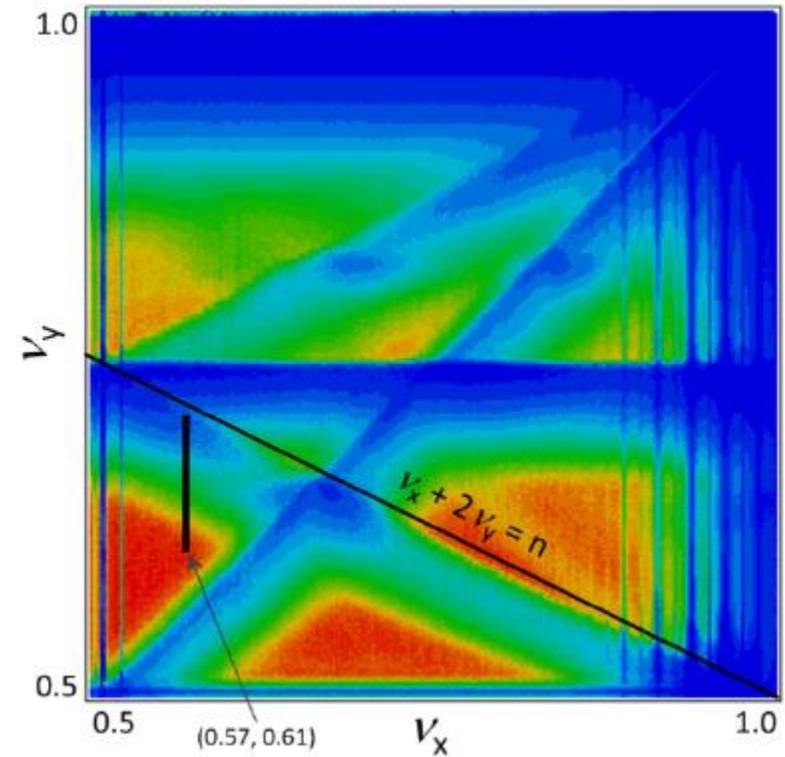
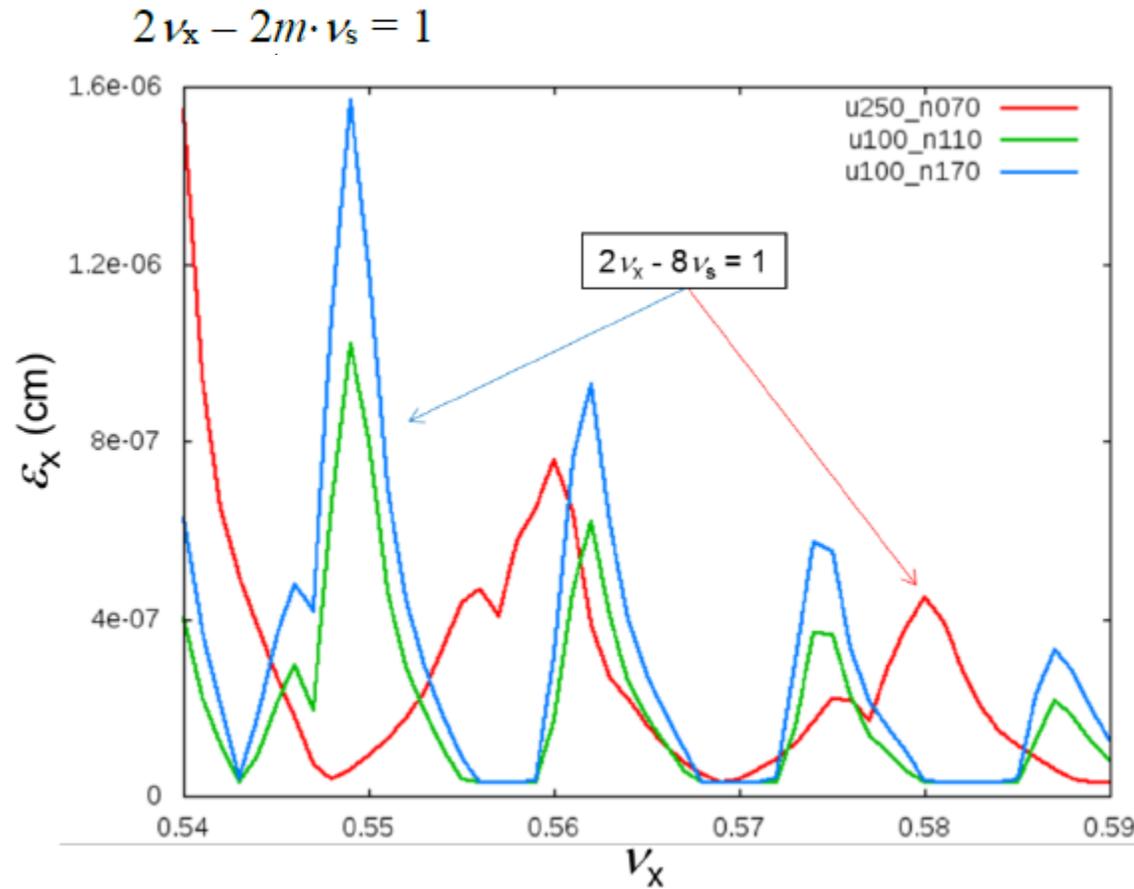
# Parameter Optimization

$$N_{th} \propto \frac{\alpha_p \sigma_\delta \sigma_z}{\beta_x^*}$$

$$\alpha_p \sigma_\delta \propto v_s \sigma_z$$

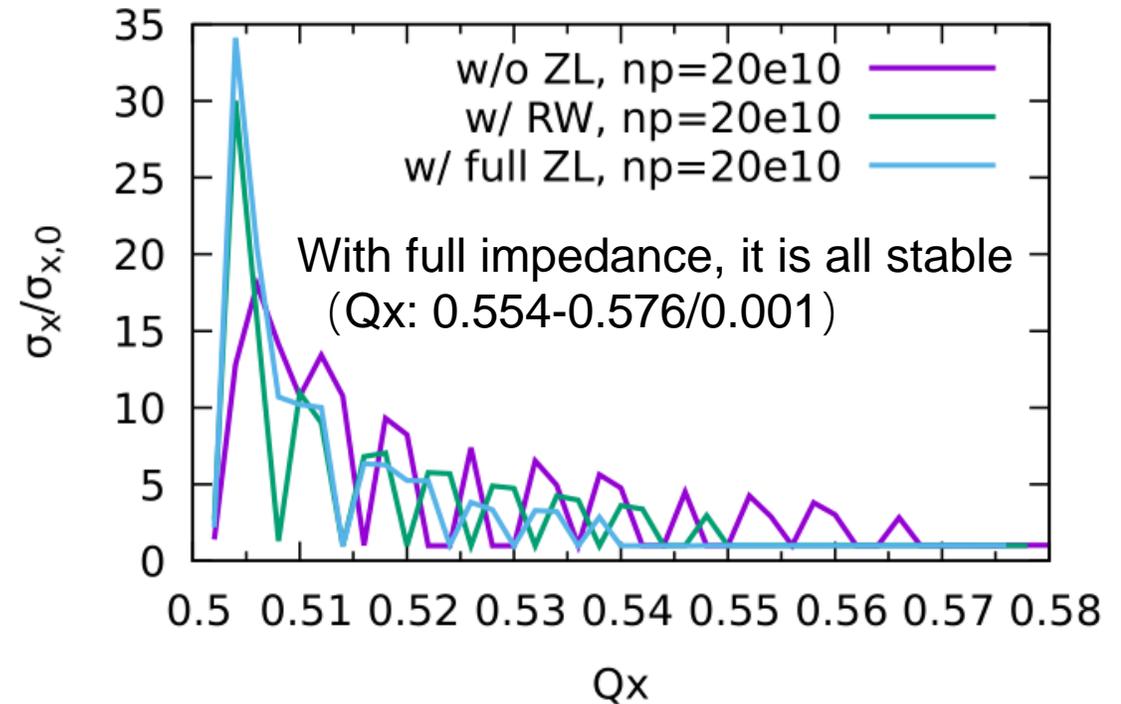
$$\xi_x \propto N_p \beta_x^* / \sigma_z^2$$

Larger  $v_s / \xi_x$  is preferred!



# Idea of using harmonic cavities

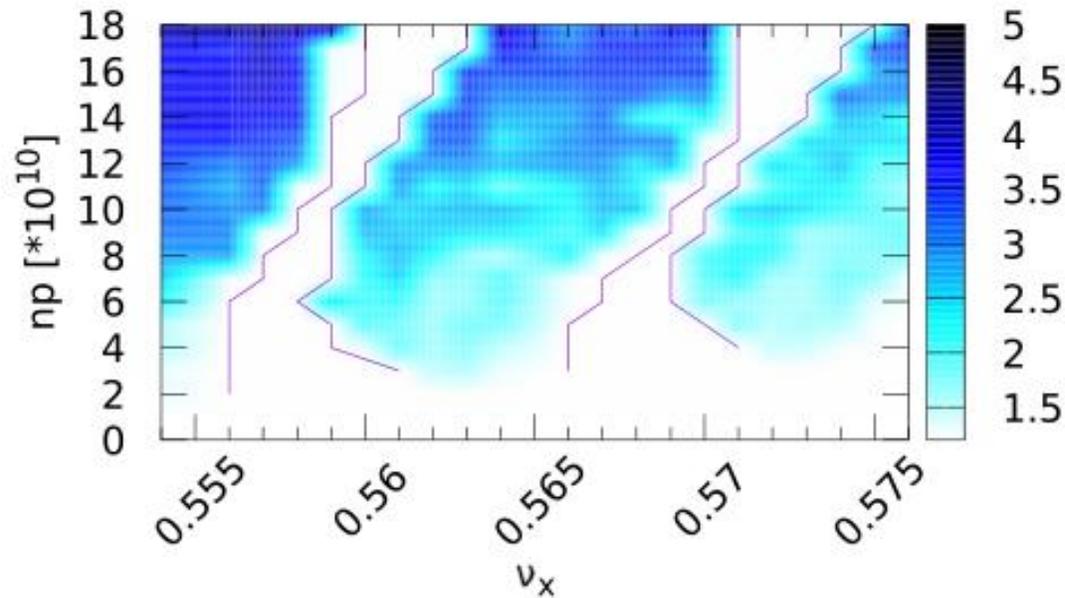
- Lower synchrotron tune
- Higher order X-Z resonances
- Landau damping due to higher synchrotron frequency spread
- Longer bunches reduce the horizontal tune shift, which helps in suppressing the X-Z instability.
- Longer bunches in collision result in a smaller energy spread due to beamstrahlung.



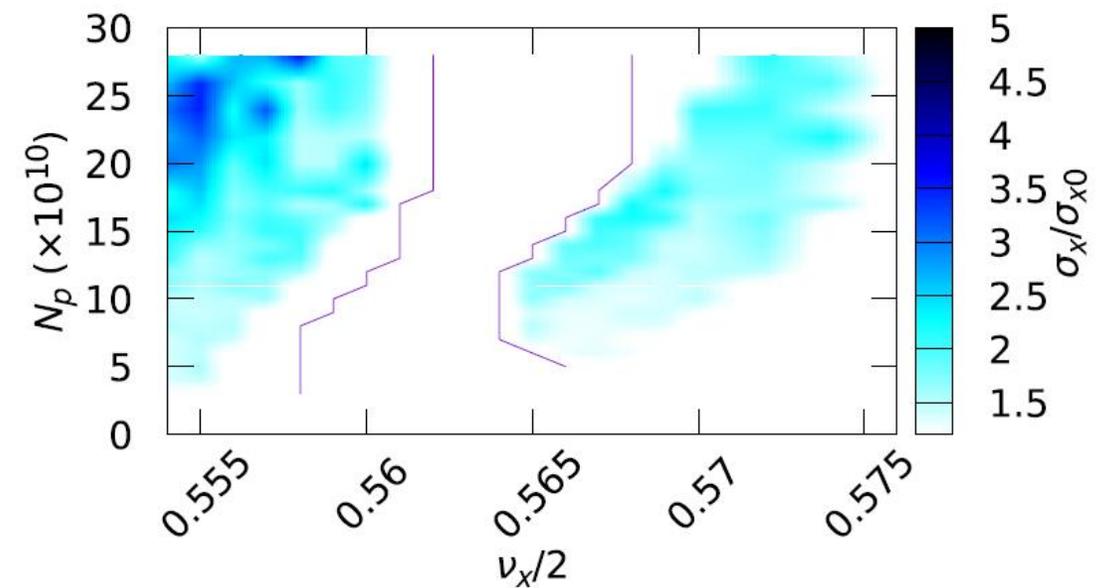
$$\sigma_z = 18 \text{ mm (CDR: 12 mm)}$$
$$\sigma_p = 9.2e-4 \text{ (CDR: 13e-4)}$$

# Higher Momentum Compaction

- Switching from  $60^\circ/60^\circ$  to  $45^\circ/45^\circ$  for arc cell lattice has been proposed for FCC-ee Z. To restore the luminosity of CDR, higher bunch population ( $28e10$ ) has been proposed.

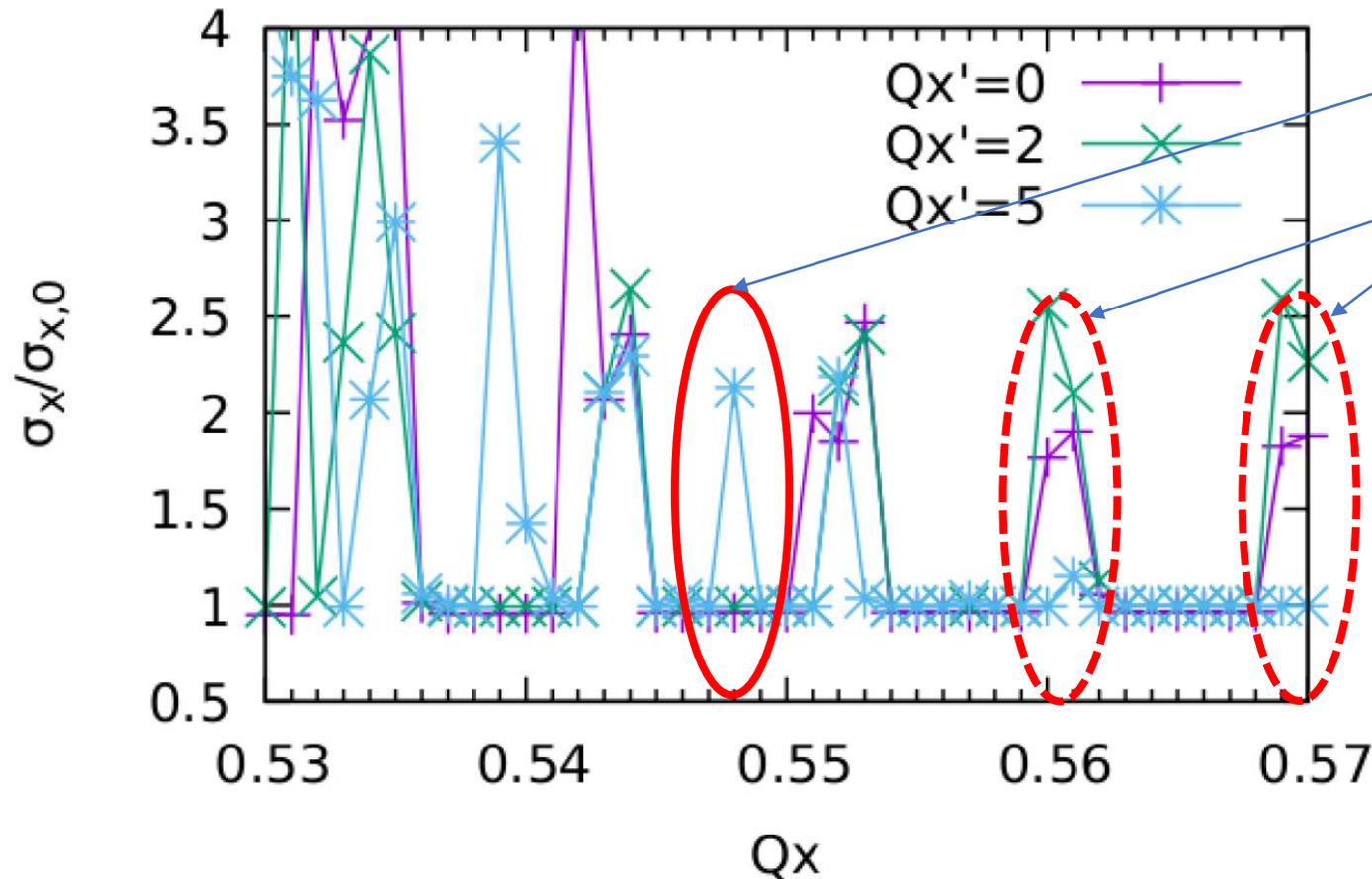


FODO CELL:  $60^\circ/60^\circ$



FODO CELL:  $45^\circ/45^\circ$

# Effect of Chromaticity on X-Z instability



- Non-zero tune chromaticity bring new resonance
- In the high order resonance region ( $0.5+n*\nu_s$ ), some resonance may be suppressed or weakened

### Future work:

- Analysis work considering linear tune chromaticity
- Simulation work considering realistic chromaticity (from lattice model)

# Analysis with PWD

- Azimuthal Mode Expansion

$$x(J, \phi) = \sum_{l=-\infty}^{\infty} x_l(J) e^{il\phi}, \quad p_x(J, \phi) = \sum_{l=-\infty}^{\infty} p_l(J) e^{il\phi}$$

- Synchro-betatron motion in Arc

$$\begin{pmatrix} x_l(J) \\ p_l(J) \end{pmatrix} = e^{-2\pi i l \nu_s(J)} \begin{pmatrix} \cos \mu_x & \sin \mu_x \\ -\sin \mu_x & \cos \mu_x \end{pmatrix} \begin{pmatrix} x_l(J) \\ p_l(J) \end{pmatrix} \equiv M_0 \begin{pmatrix} x_l(J) \\ p_l(J) \end{pmatrix}$$

- Action Discretization

we truncate  $l$  at  $\pm l_{\max}$ , and discretize  $J$  at  $J_1, J_2, \dots, J_{n_J}$ .

For example,

$$\begin{pmatrix} x_l(J_i) \\ p_l(J_i) \end{pmatrix} = e^{-2\pi i l \nu_s(J_i)} \begin{pmatrix} \cos \mu_x & \sin \mu_x \\ -\sin \mu_x & \cos \mu_x \end{pmatrix} \begin{pmatrix} x_l(J_i) \\ p_l(J_i) \end{pmatrix} \equiv M_0 \begin{pmatrix} x_l(J_i) \\ p_l(J_i) \end{pmatrix}$$

$n_J = 40$ ,  $l_{\max} = 8$

- Momentum Kick due to localized Wake force (beam-beam)

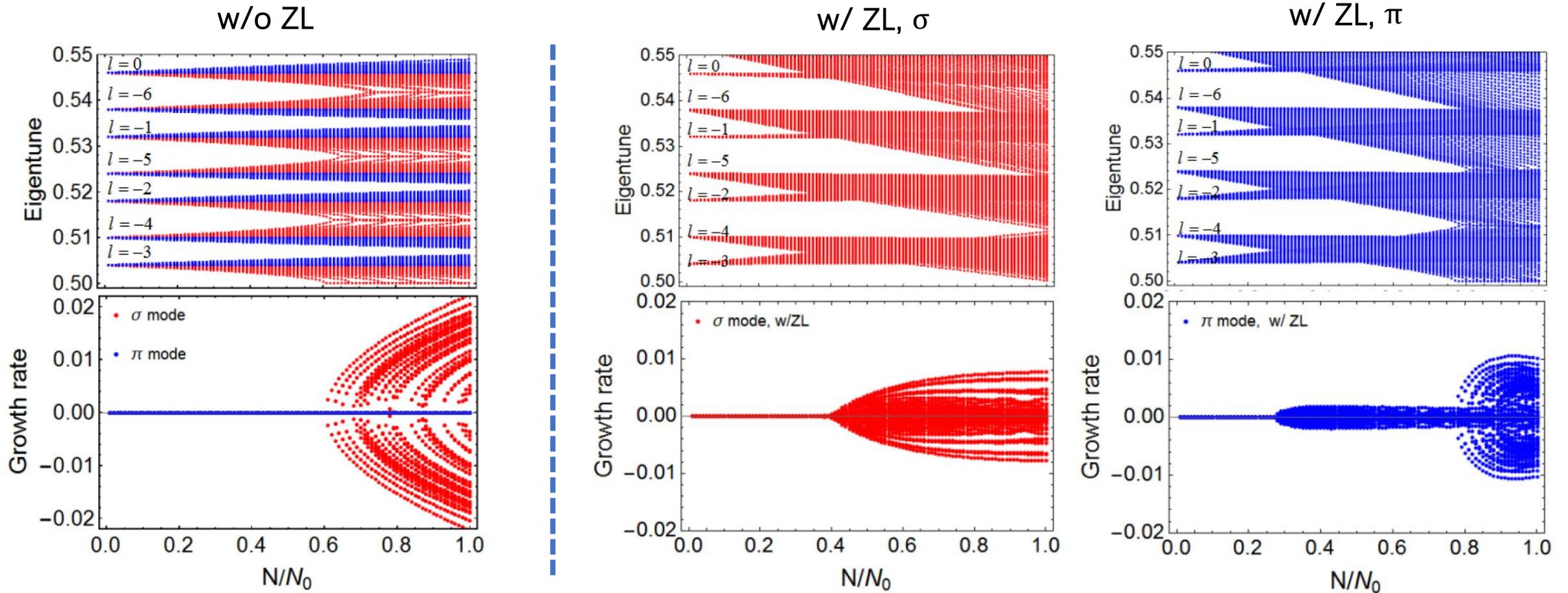
$$M_W = \begin{pmatrix} 1 & 0 \\ \beta_x M_{lil'i'} & 1 \end{pmatrix}.$$

$$\begin{aligned} \Delta p_l(J_i) &= \mp \frac{\beta_x}{2\pi} \sum_{l'} \sum_{i'} \Delta J_{i'} W_{ll'}(J_i, J_{i'}) \psi(J_{i'}) x_{l'}(J_{i'}) \\ &\equiv \beta_x M_{lil'i'} x_{l'}(J_{i'}). \end{aligned}$$

- Stability analysis of  $M_0 M_W$

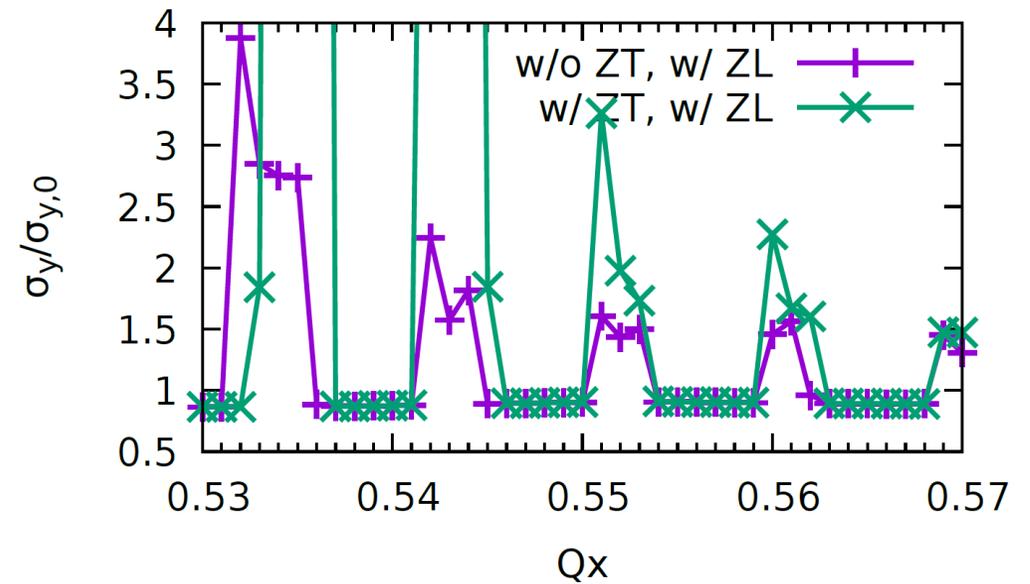
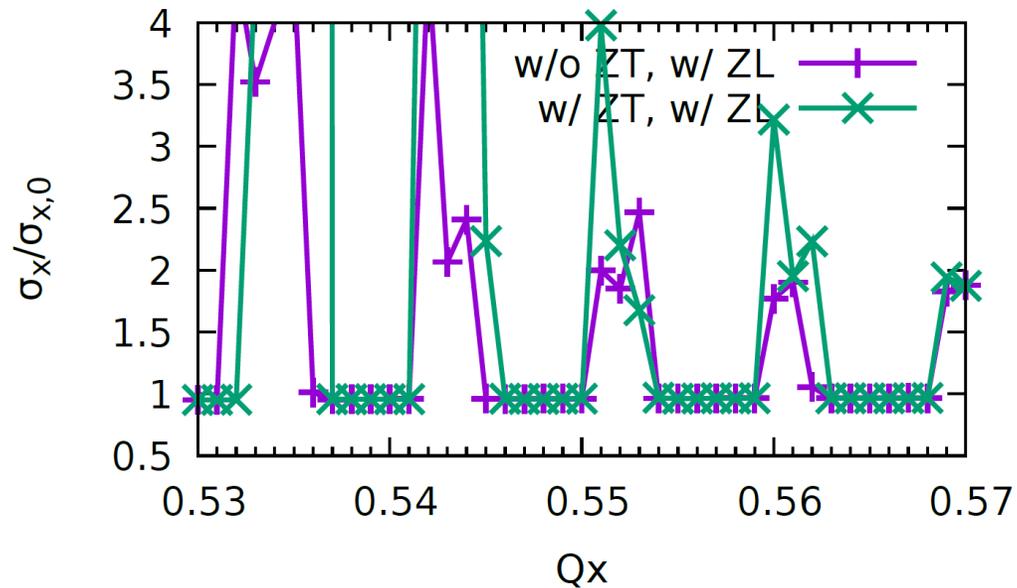
$$W_{ll'}(J_i, J_{i'}) = \sum_j \sum_{j'} e^{-il\phi_j + il'\phi_{j'}} W_x(z(J_i, \phi_j) - z(J_{i'}, \phi_{j'})) \Delta\phi_j \Delta\phi_{j'}.$$

# Eigen-Mode Analysis w/o and w/ ZL

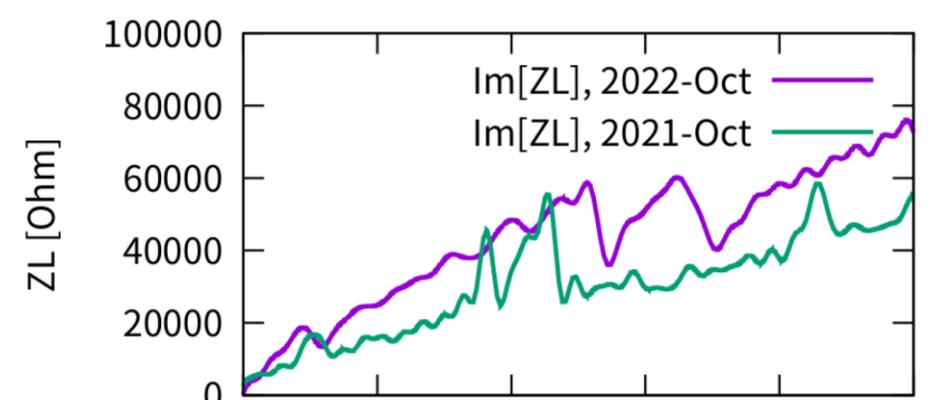
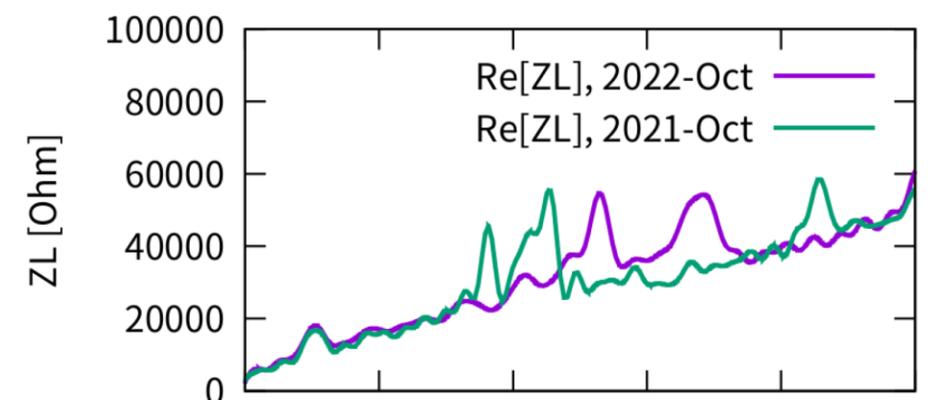


# Collision considering ZT (2022-Mar)

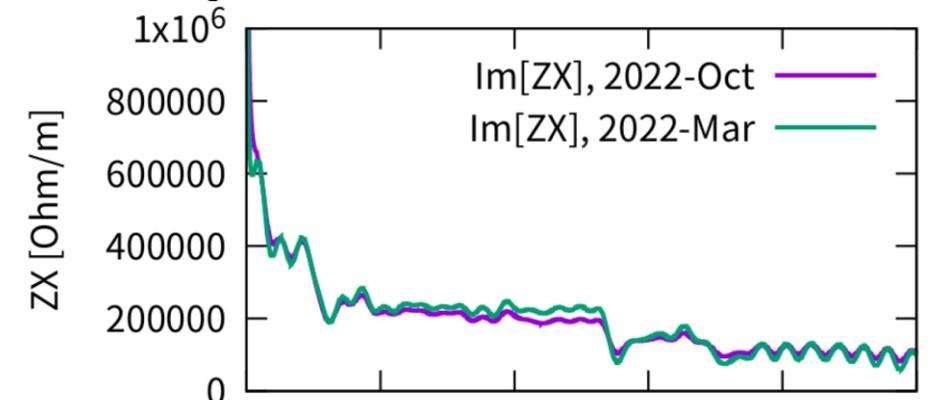
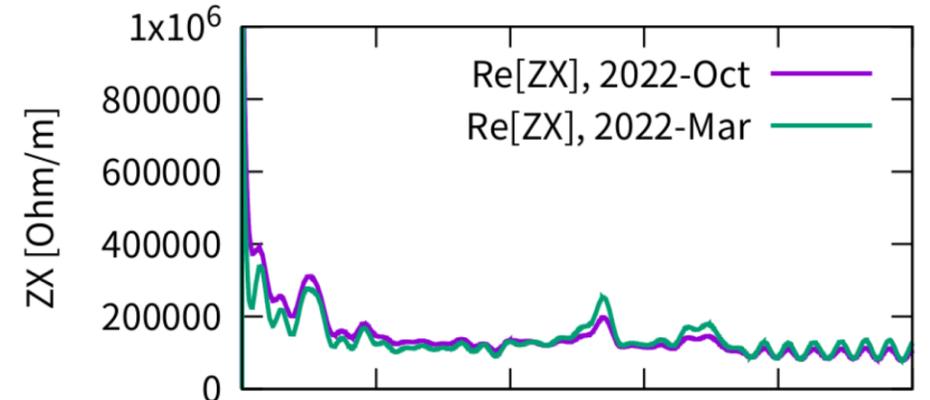
- no clear effect in stability region considering transverse impedance (2022-Mar)



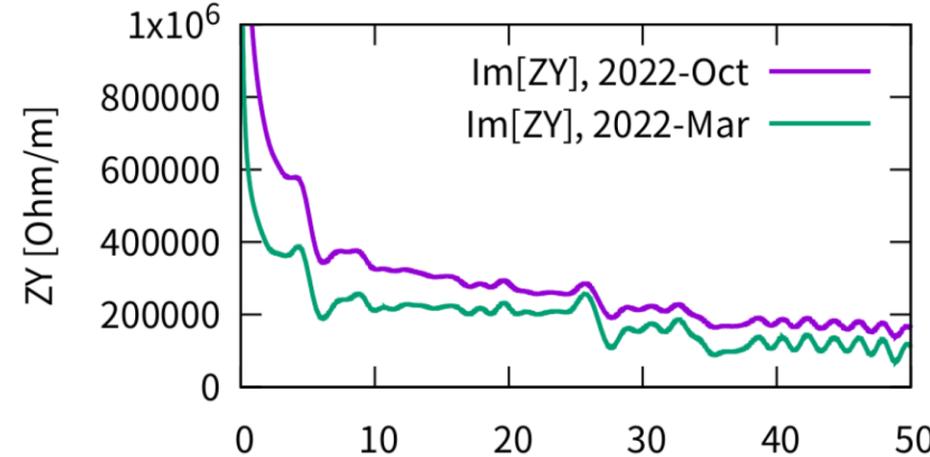
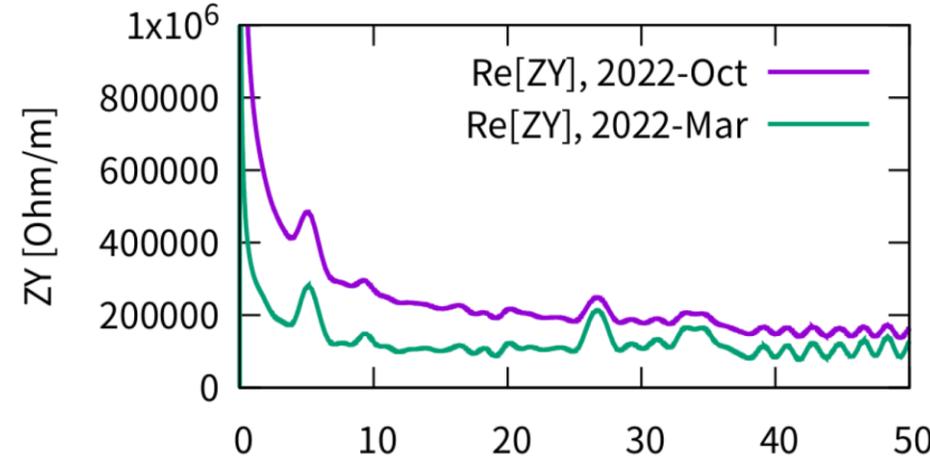
ZL



ZX

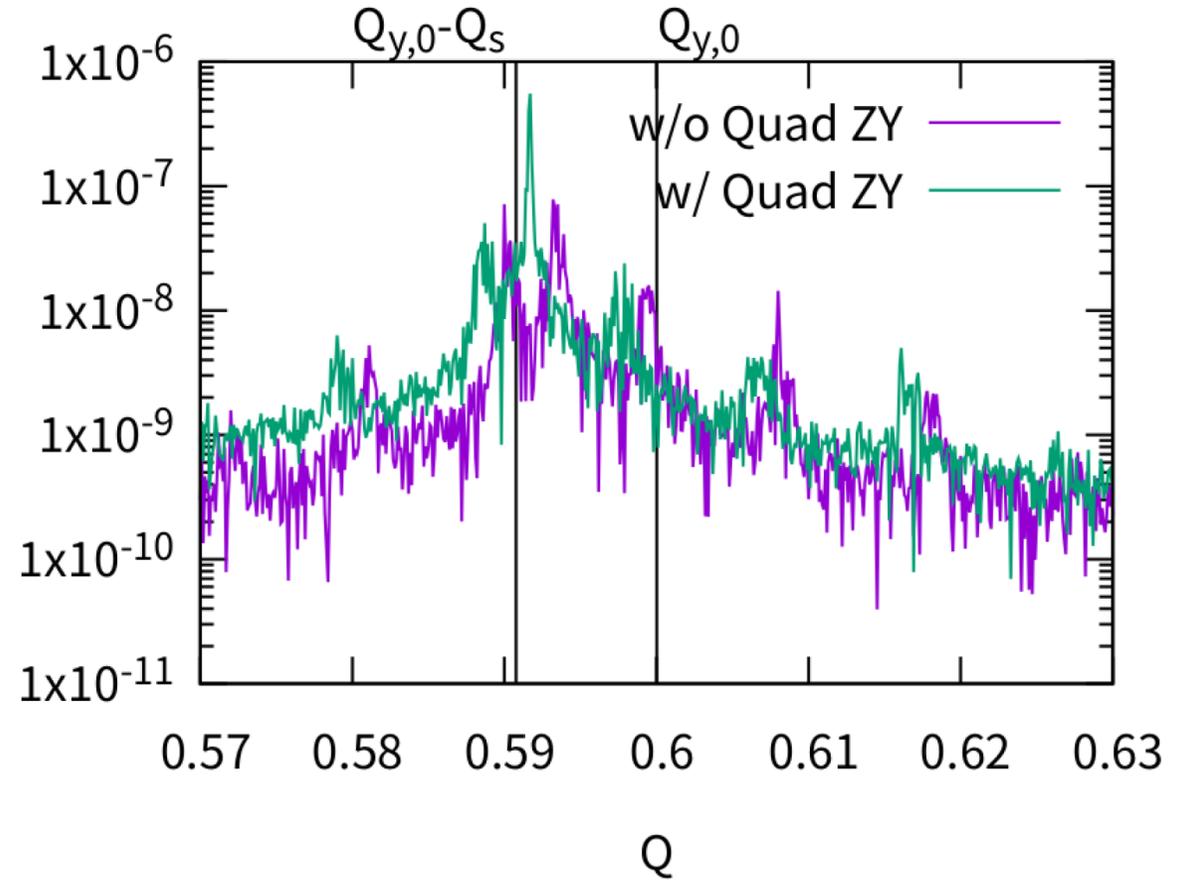
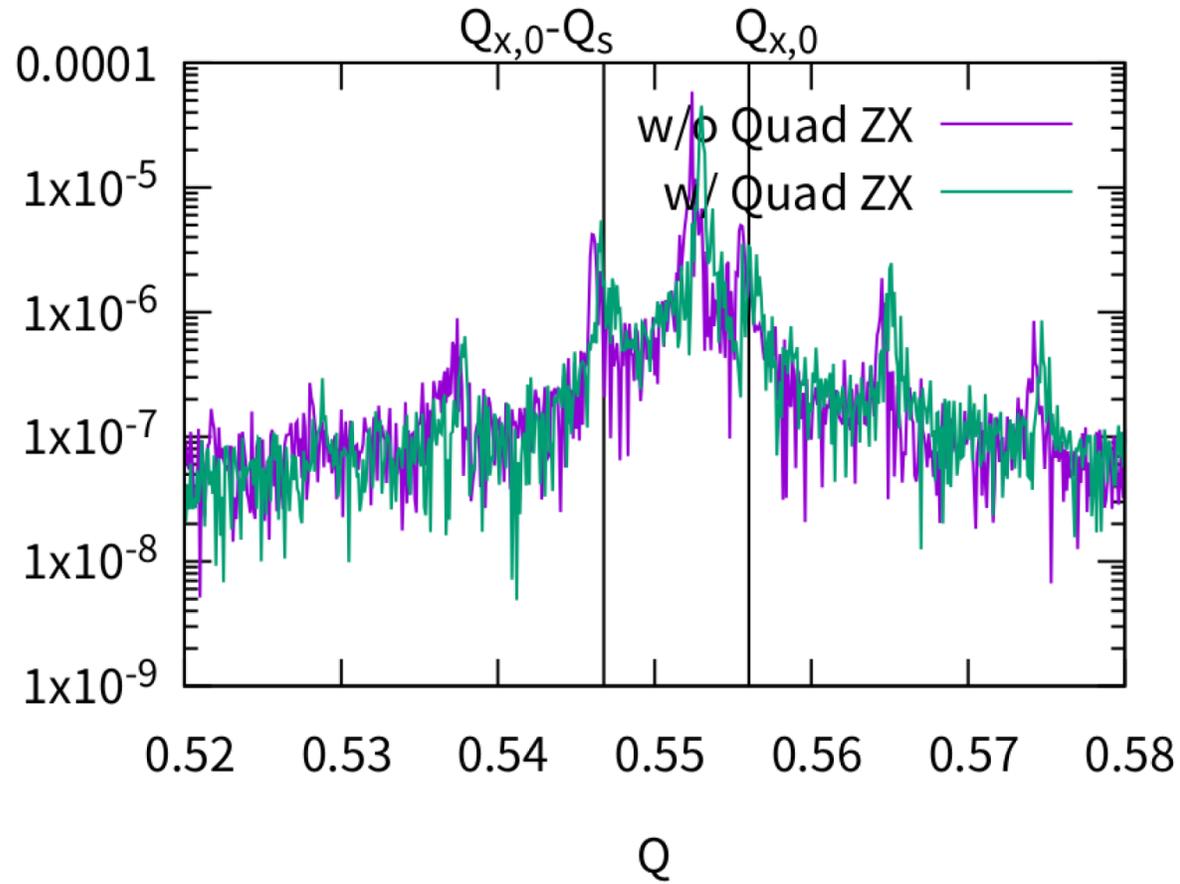


ZY



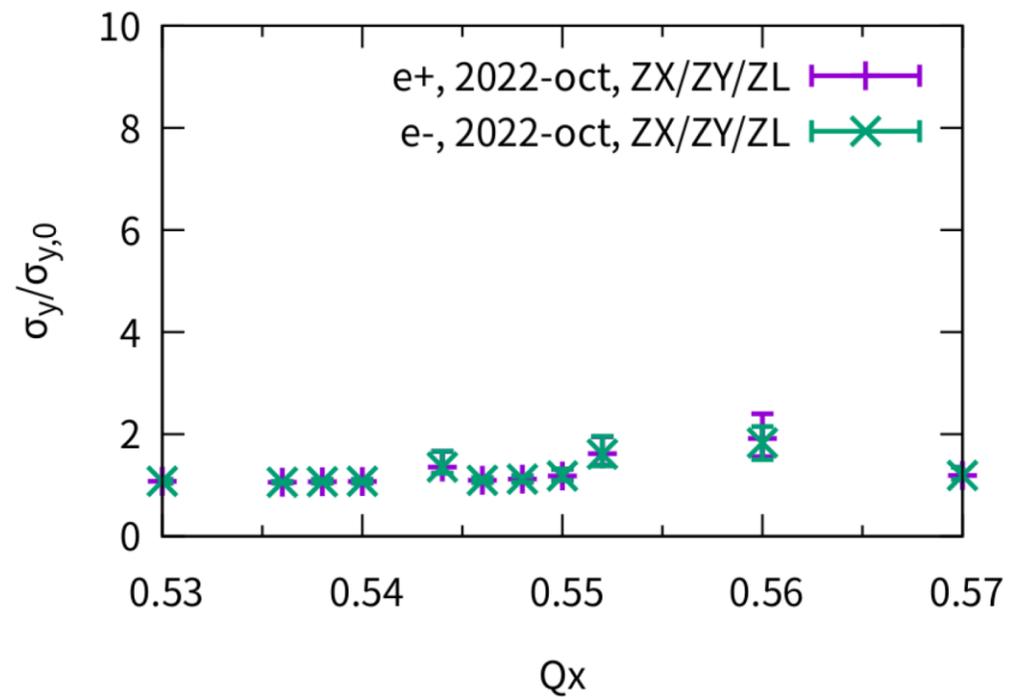
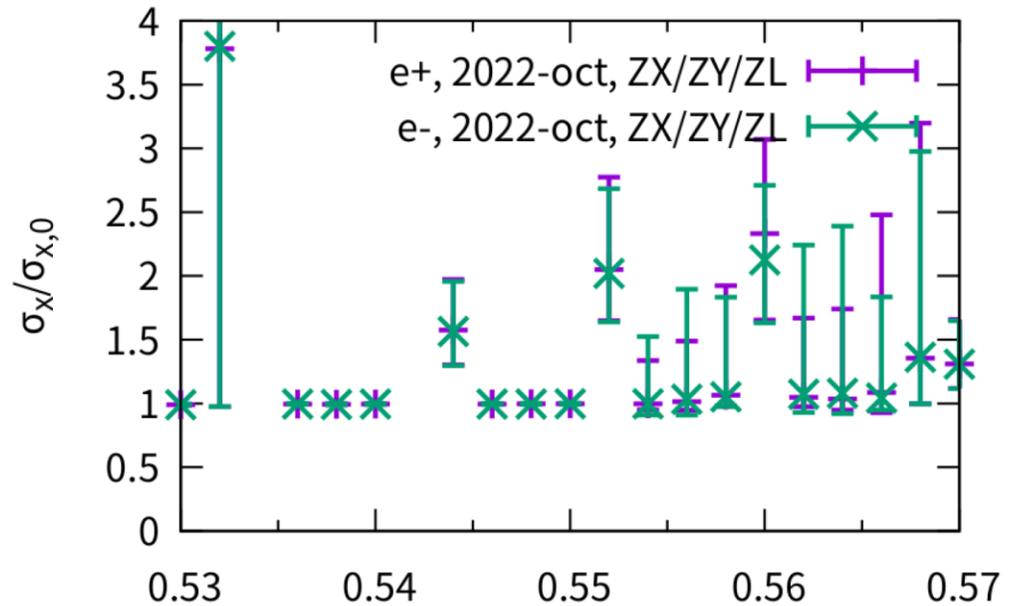
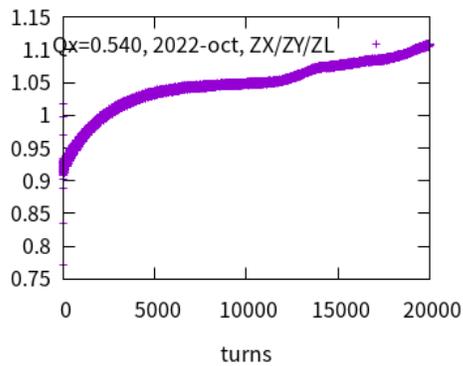
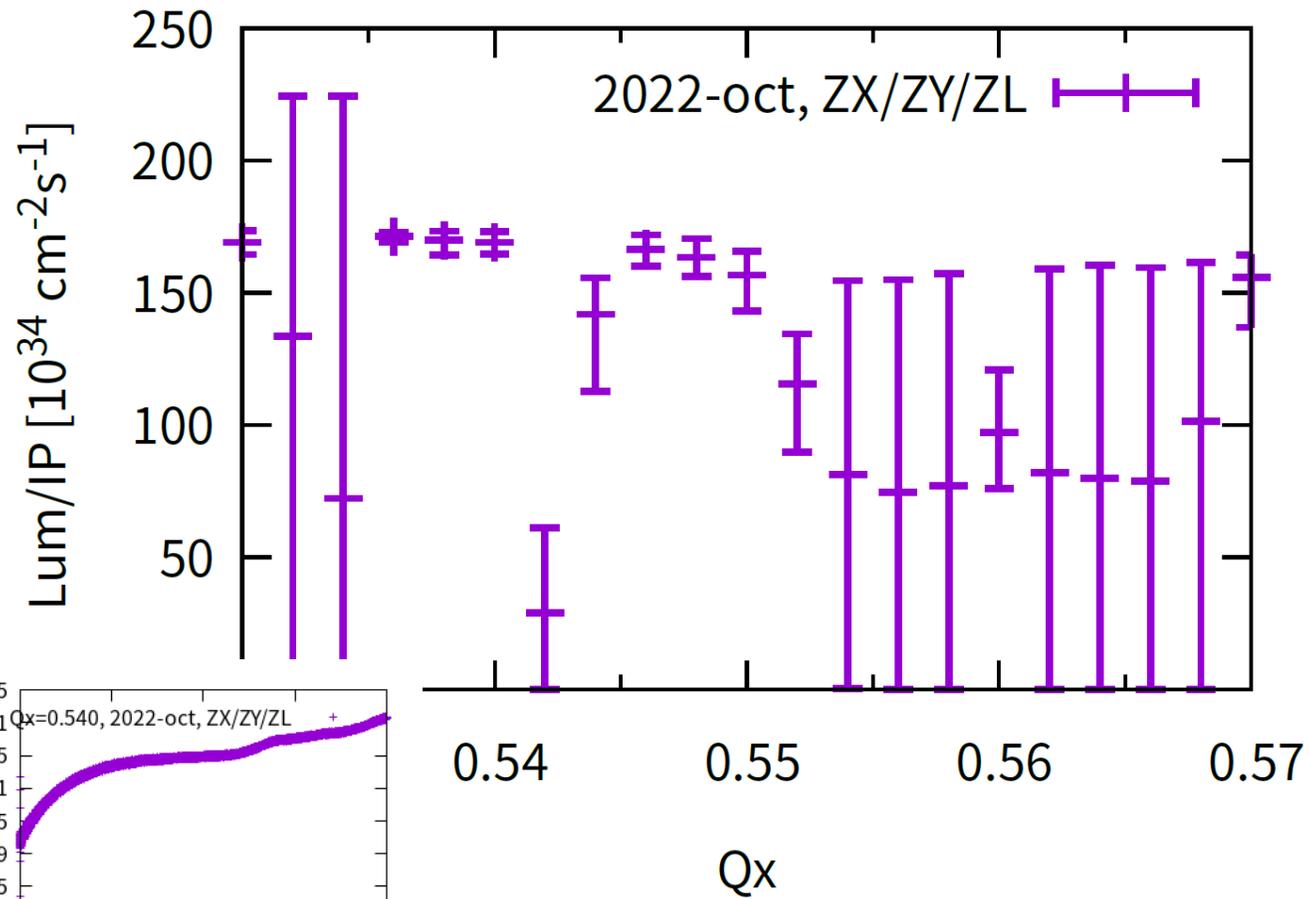
# Evolving Impedance

# Collision off, but with Beamstrahlung Length



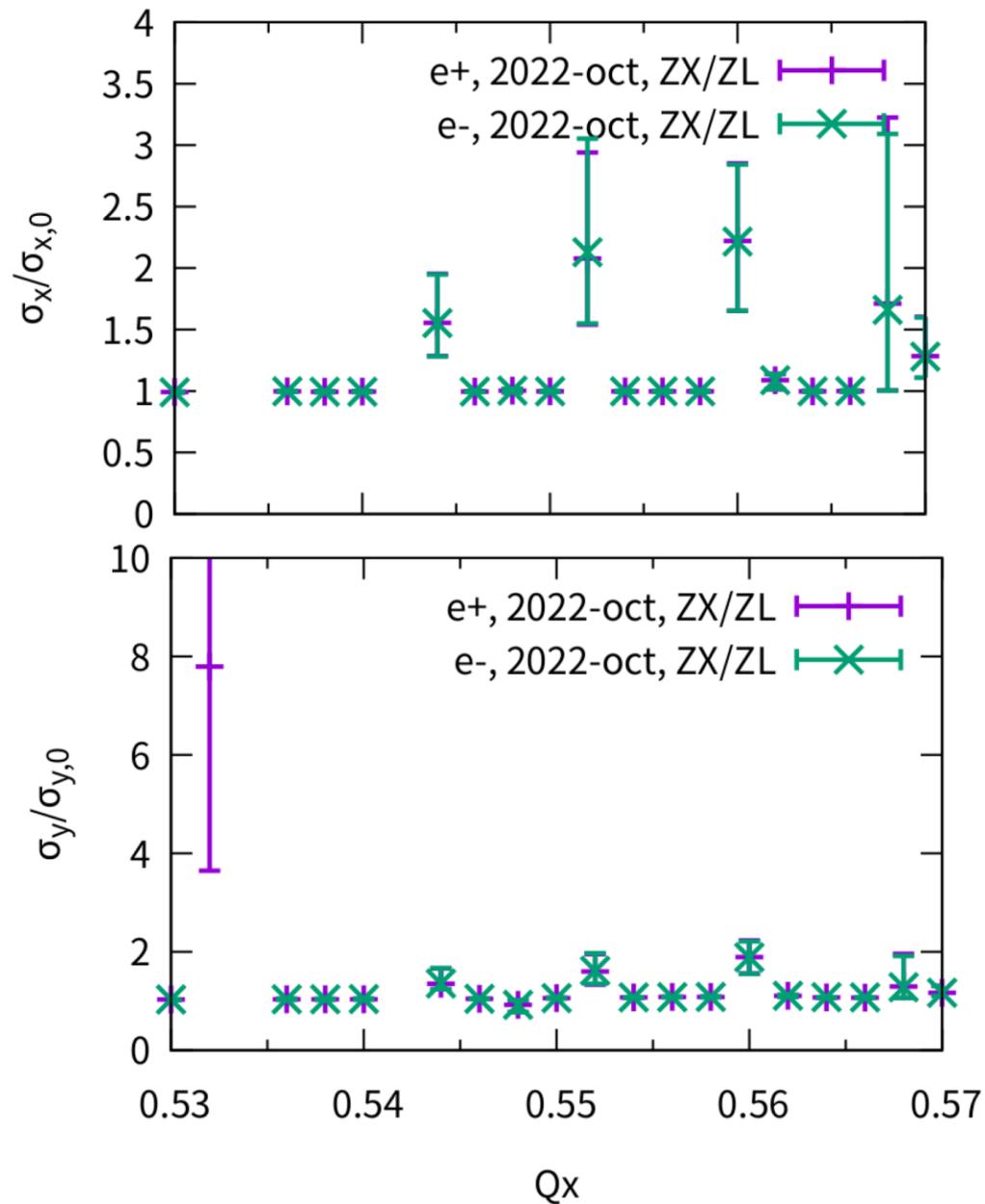
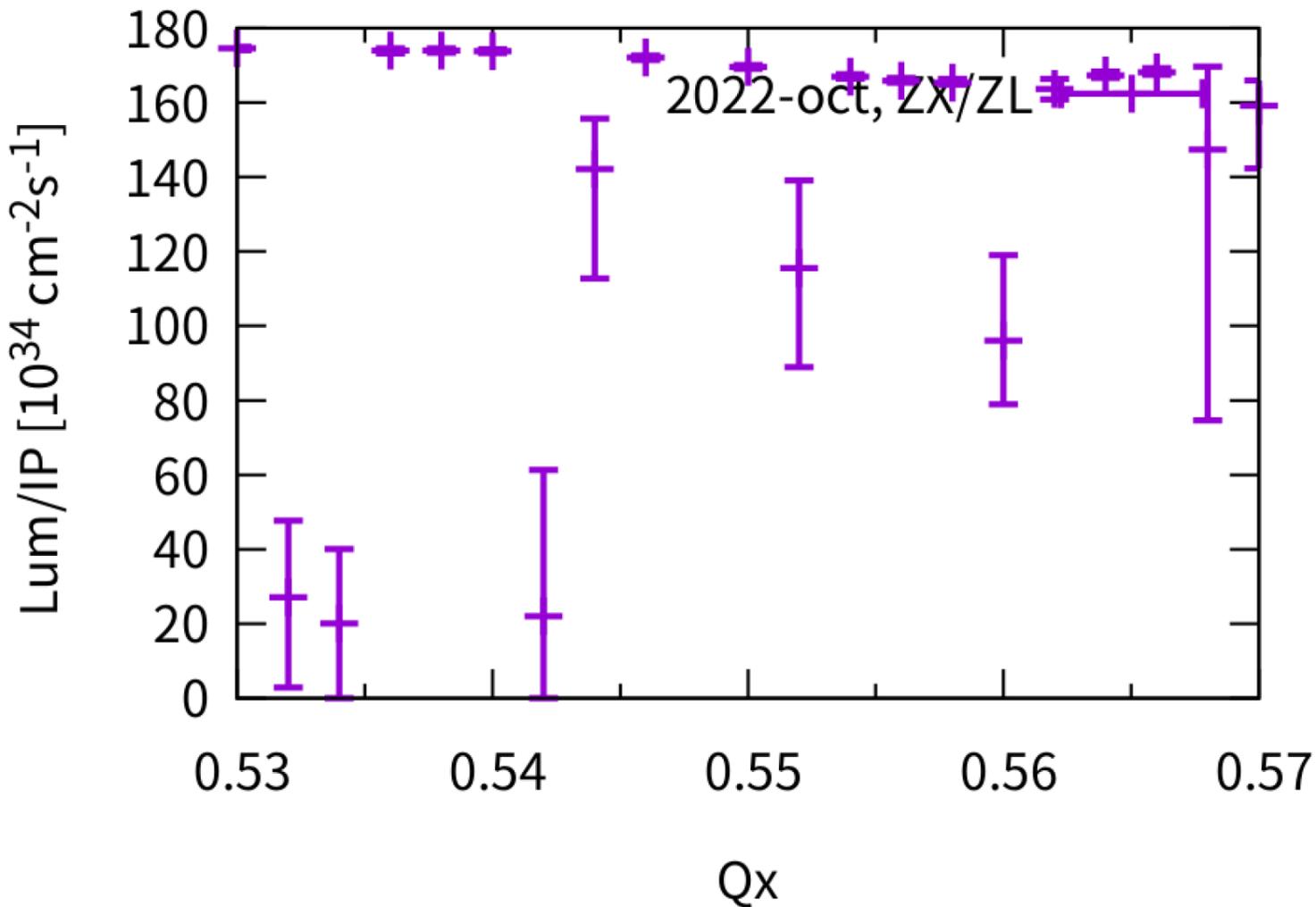
$Q_y=0.600$

# Horizontal tune scan



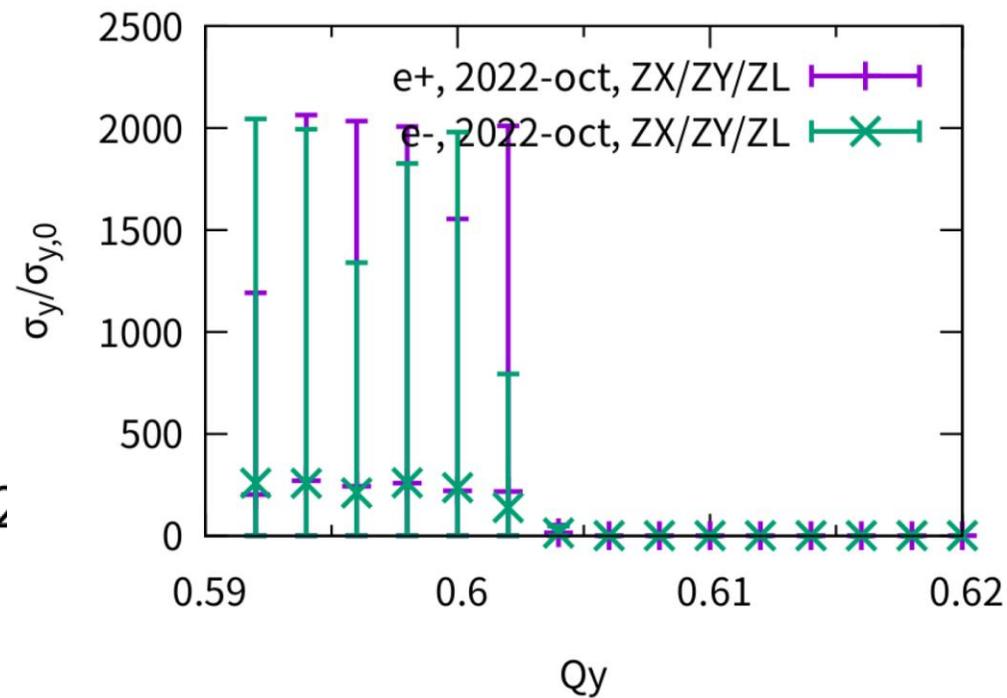
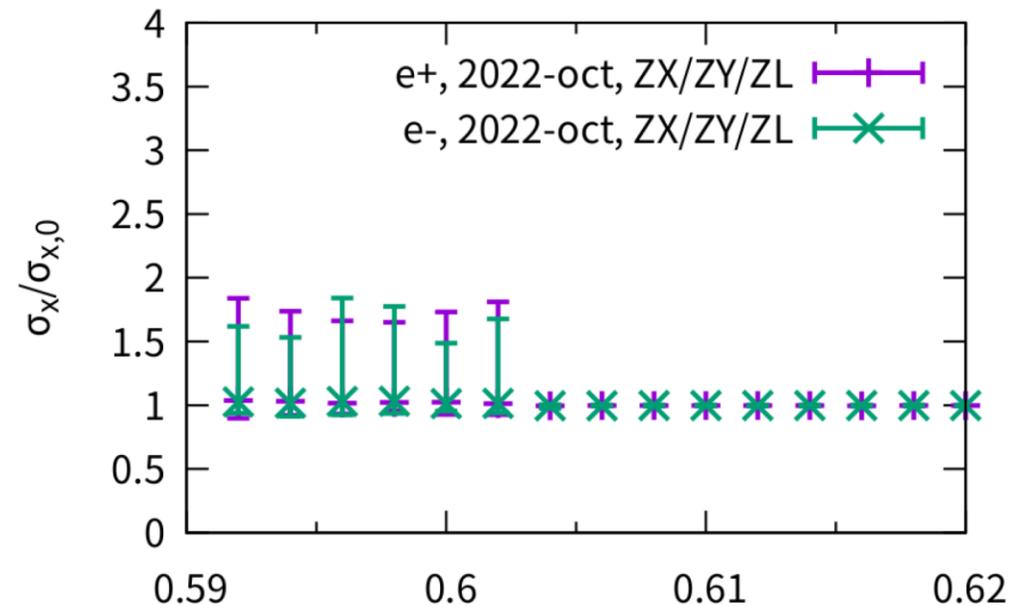
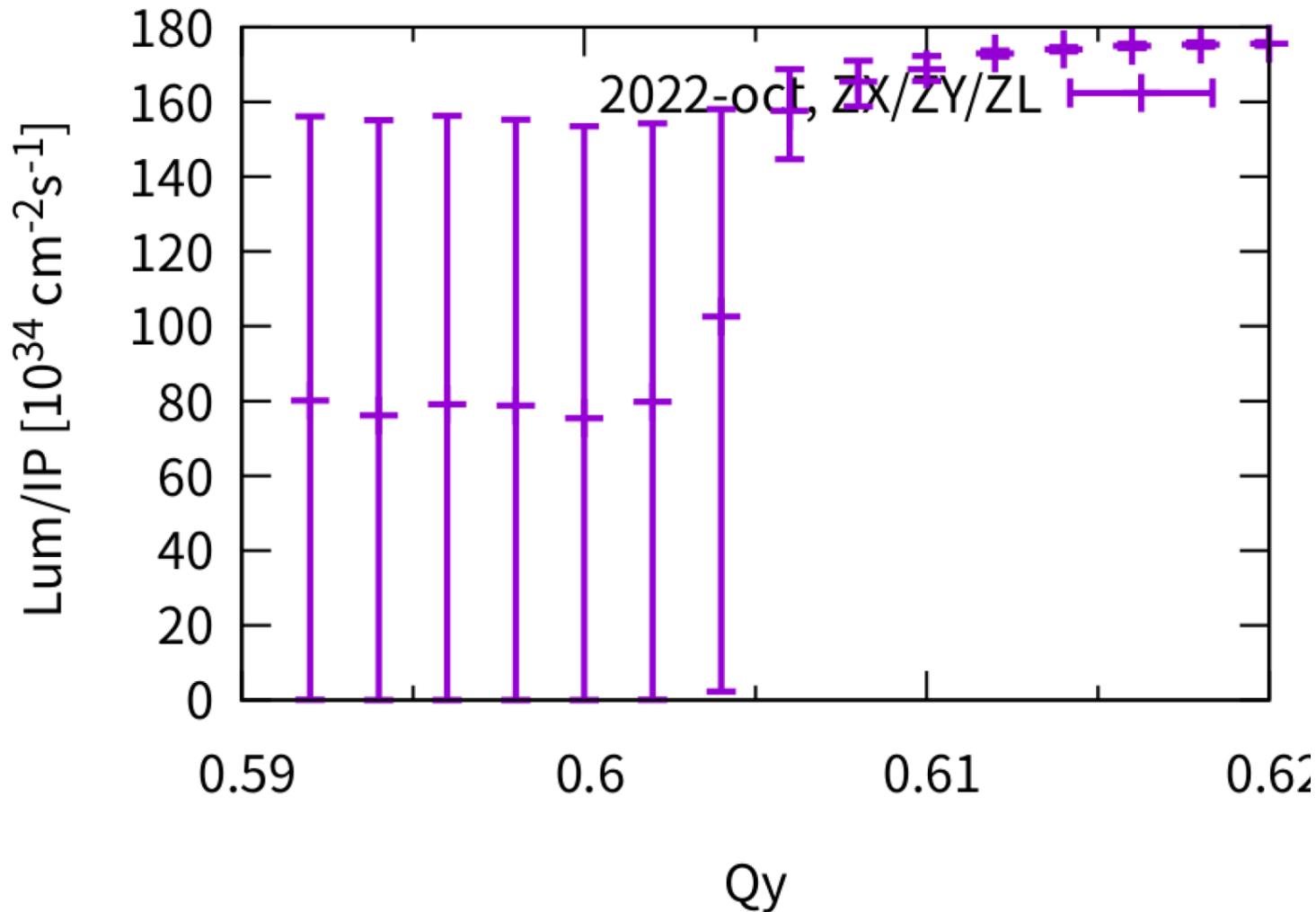
$Q_y=0.600$

# Only horizontal impedance



$Q_x=0.556$

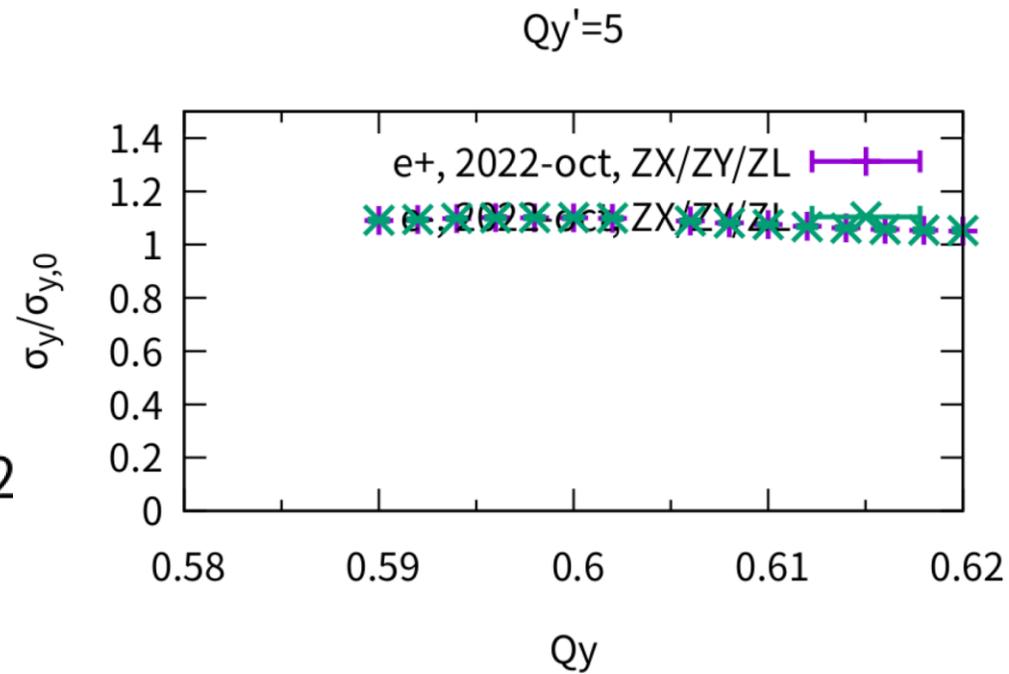
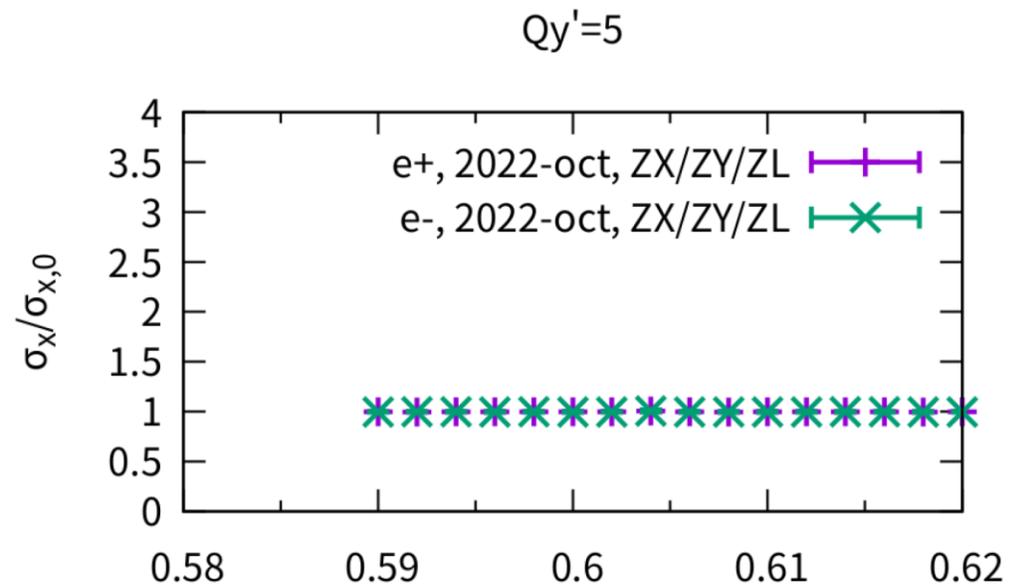
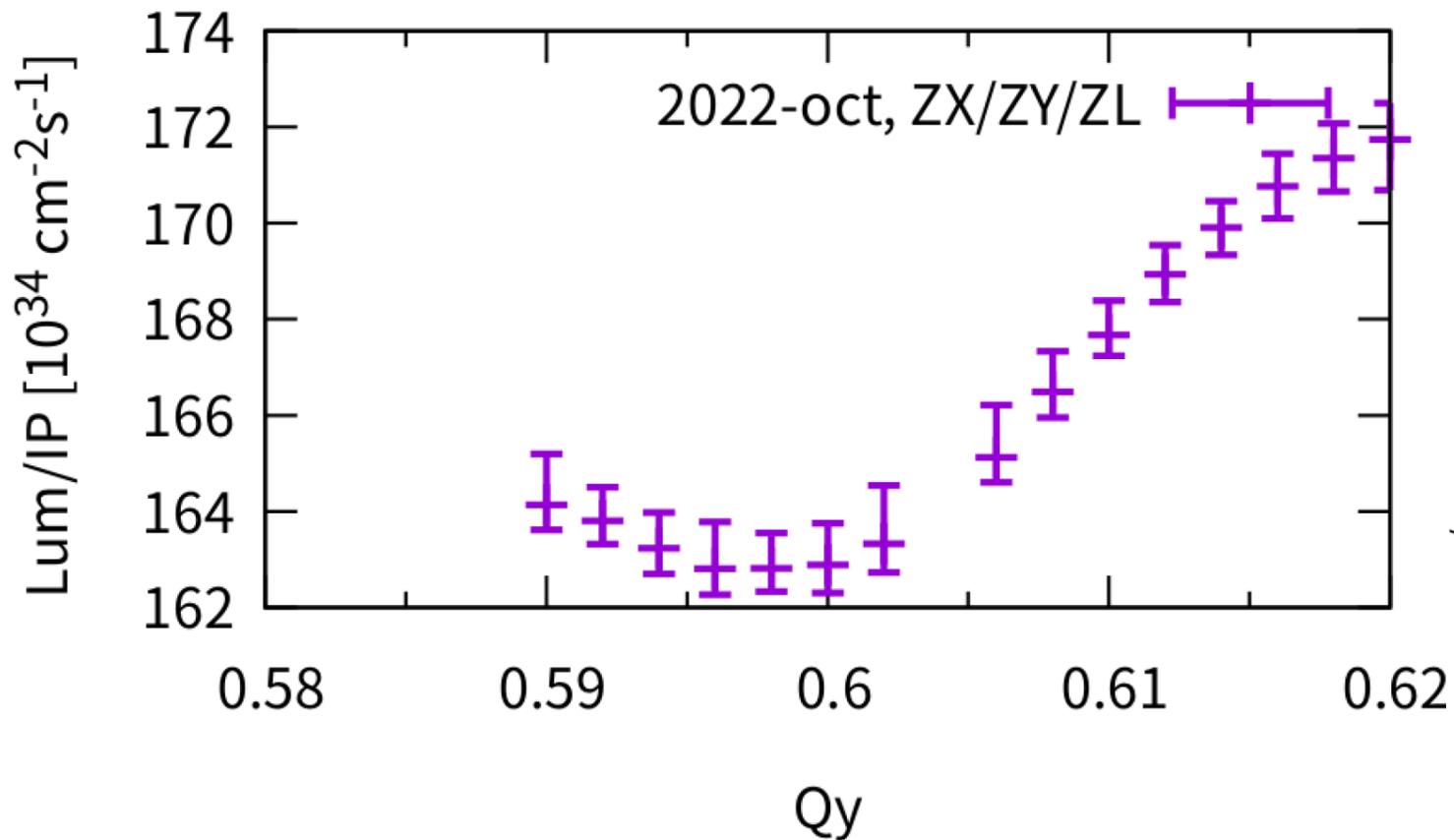
# Vertical tune scan



$Q_x=0.556$

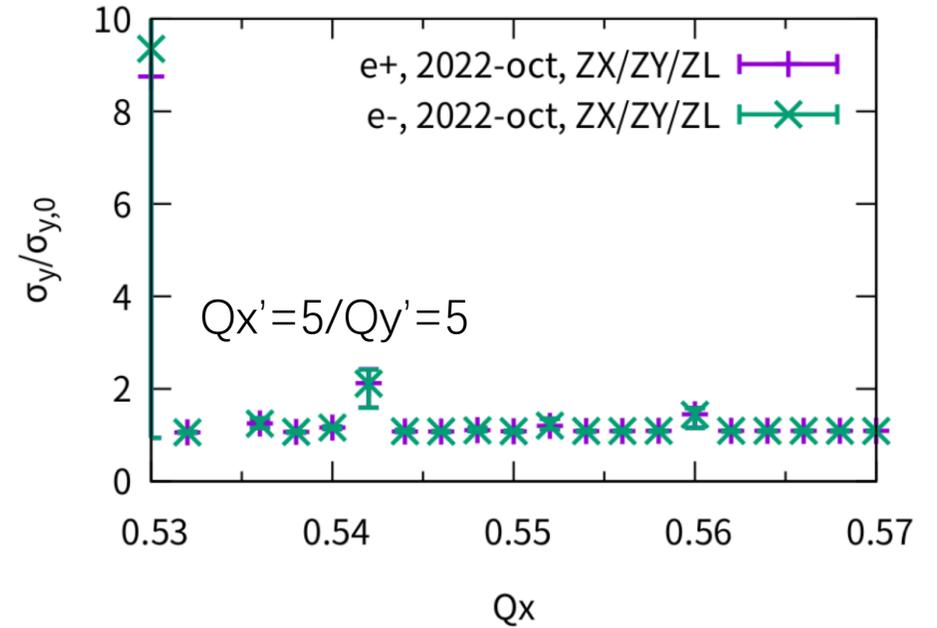
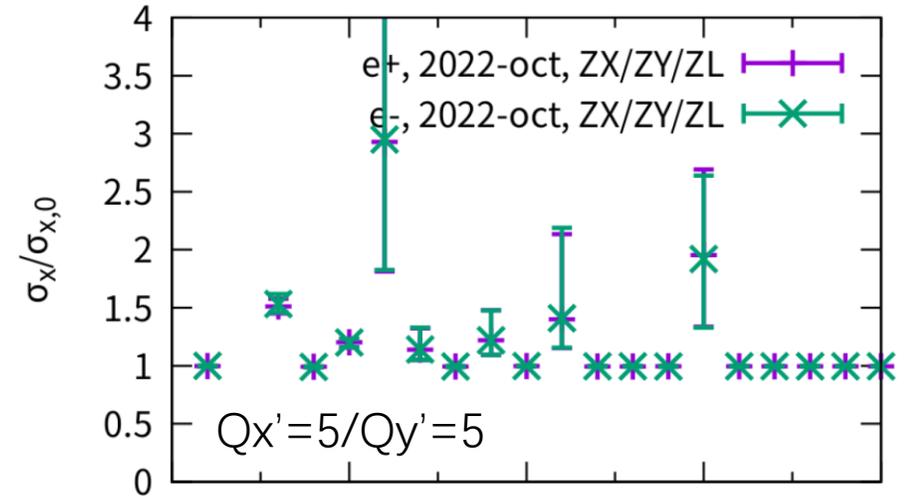
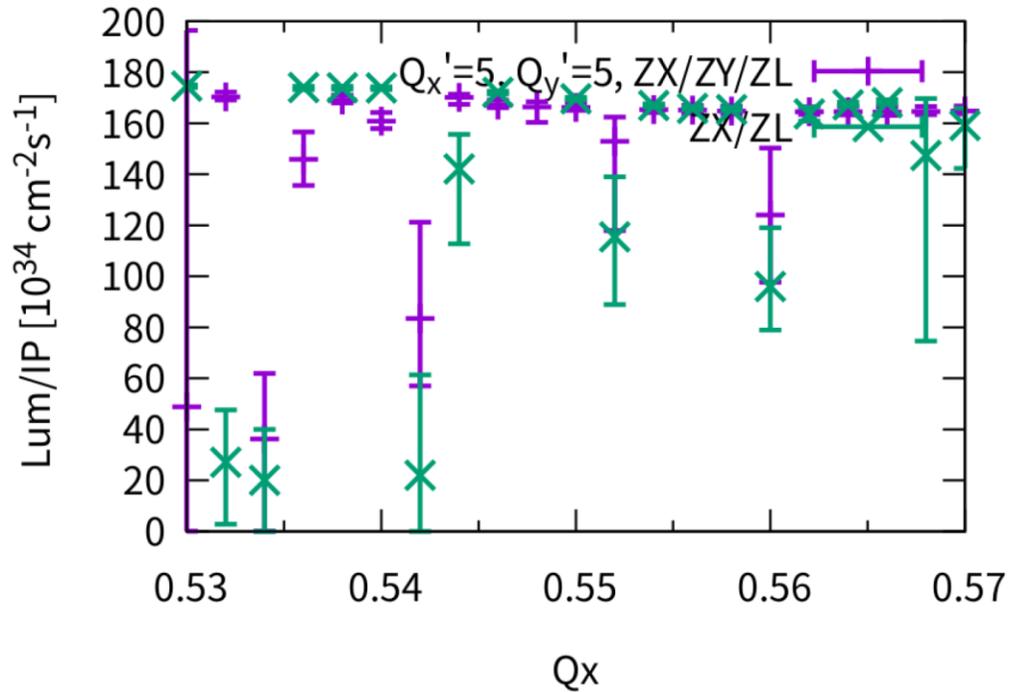
# Vertical Chromaticity

$Q_y'=5$



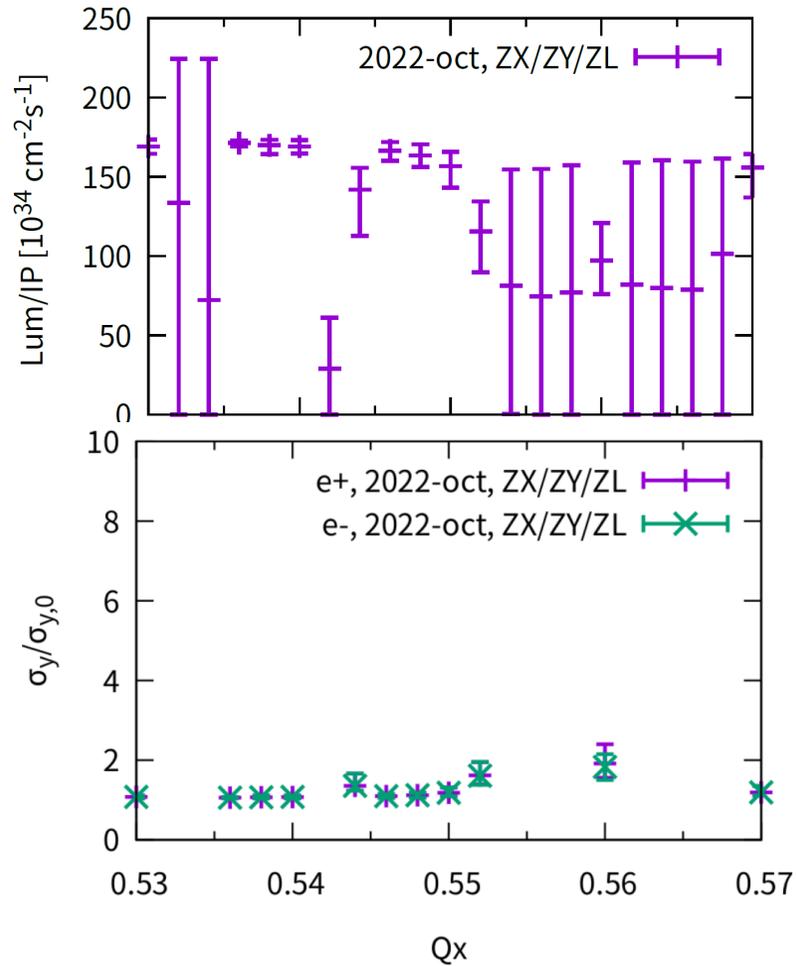
$$Qx' = 5 / Qy' = 5 \quad (Qy = 0.60)$$

Enlarge stable tune area in (0.56-0.57)

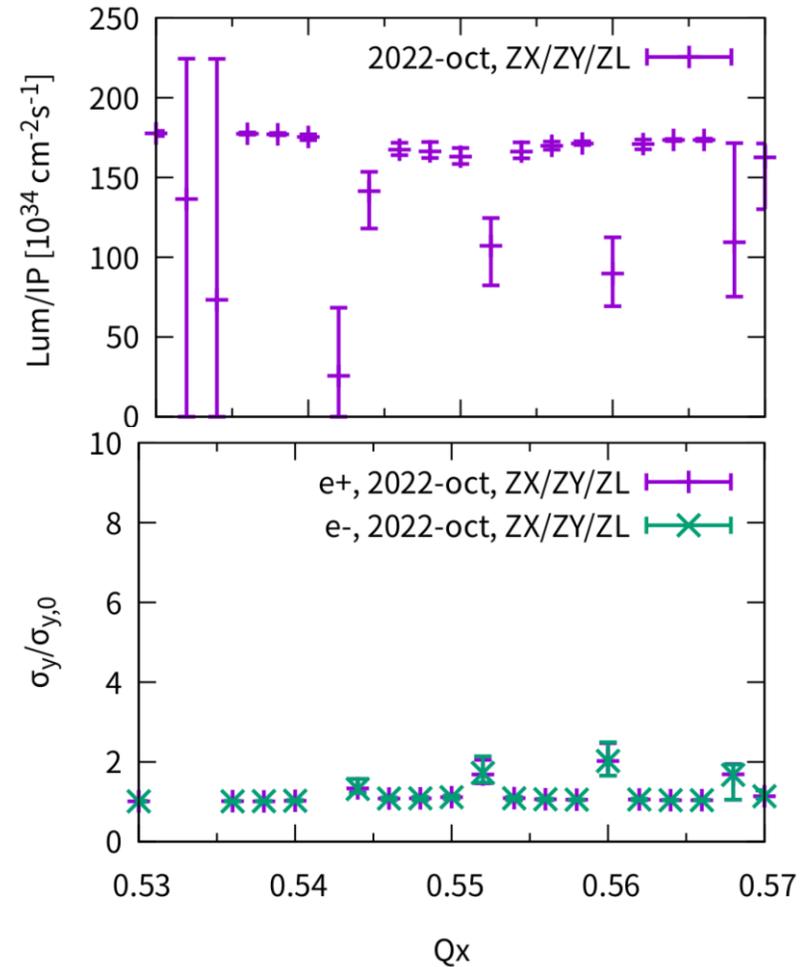


# Horizontal scan at different $Q_y$

$Q_y=0.60$



$Q_y=0.61$

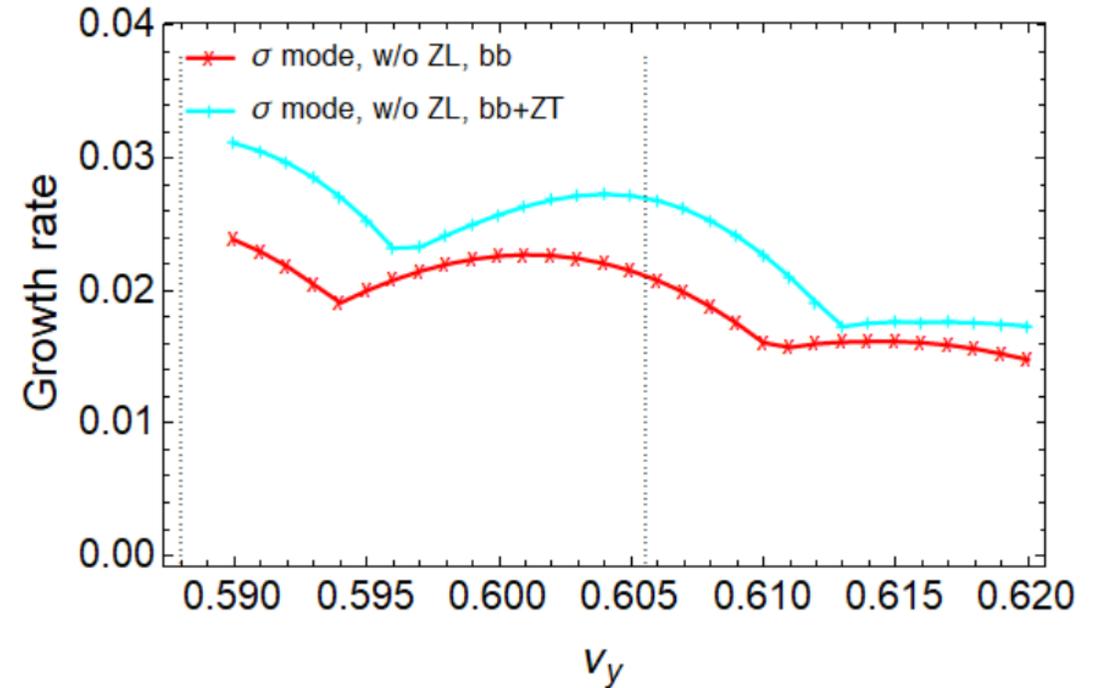
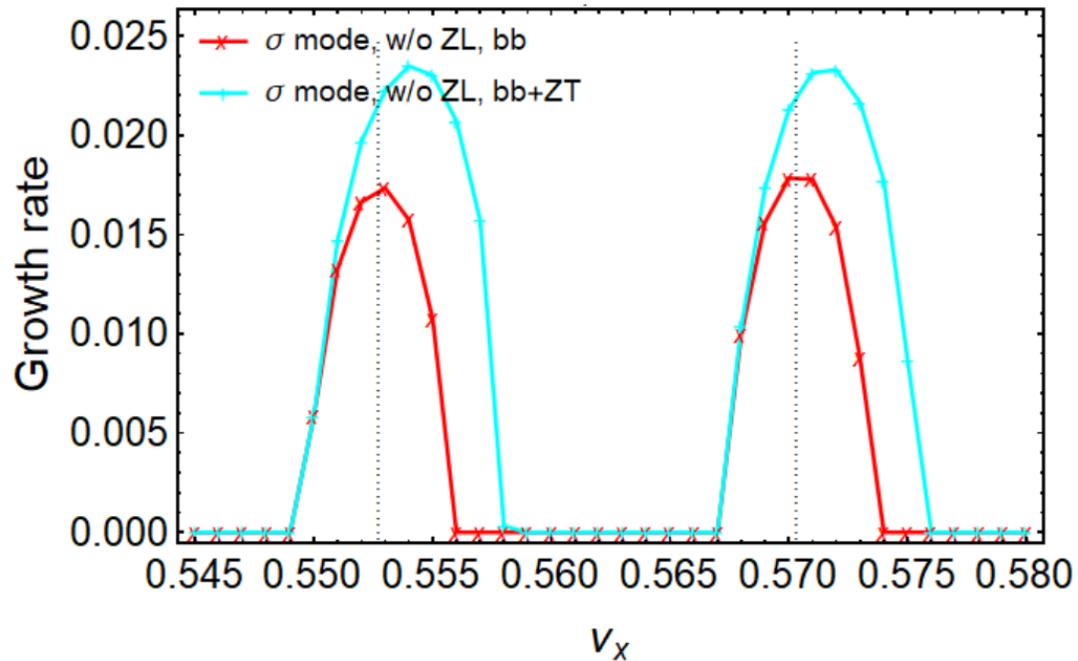


# Some Analysis - Local Beam-Beam Model

- In horizontal direction, considering ZX
  - the instability growth rate is faster,
  - unstable tune area increases
- In vertical direction,
  - pure beam-beam is unstable due to ignorance of strong nonlinearity
  - It is also found enhance of instability when considering ZY

CEPC

Pi mode is not sensitive to ZT

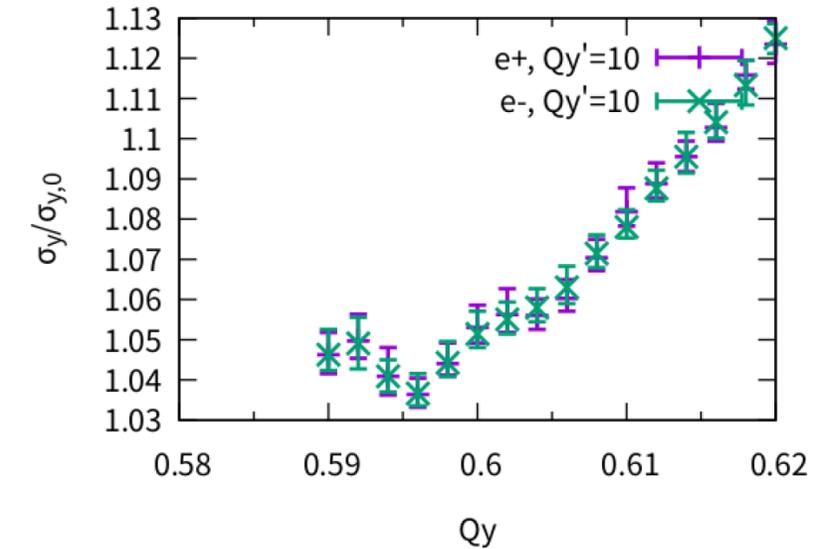
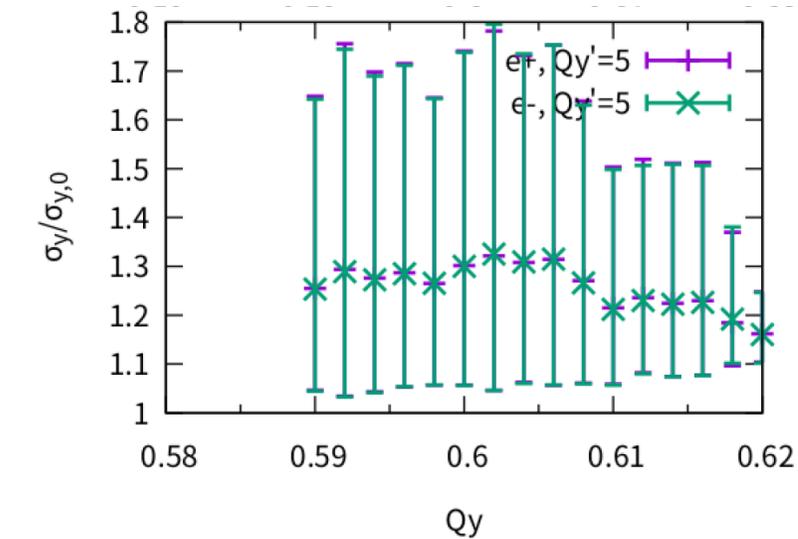
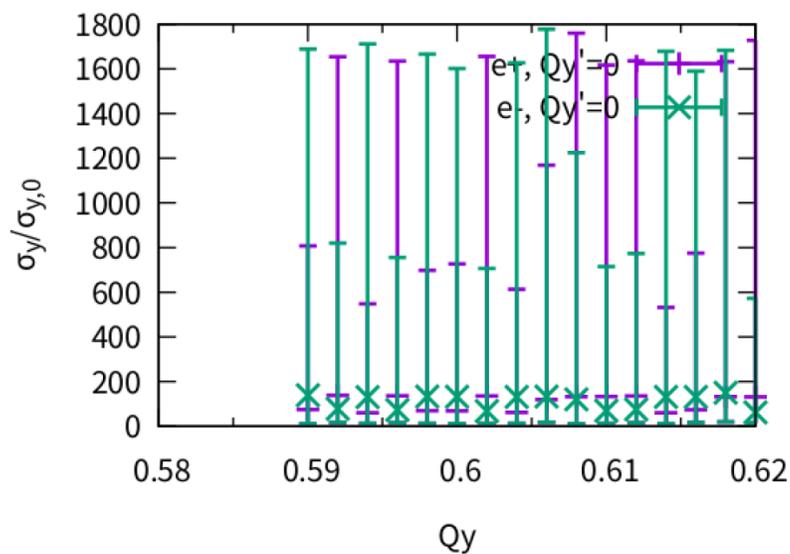
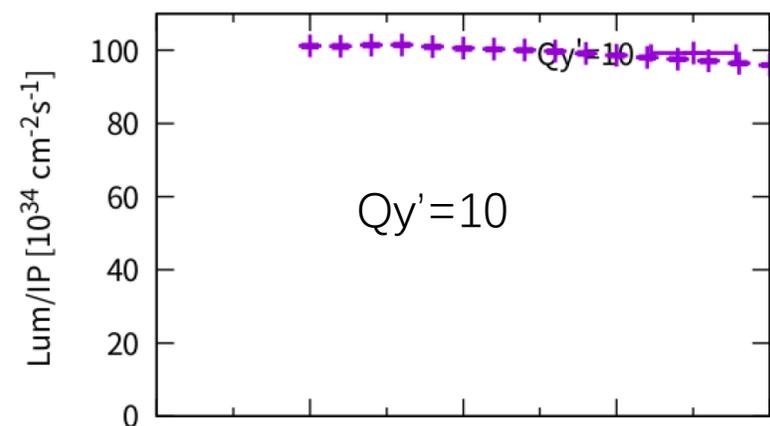
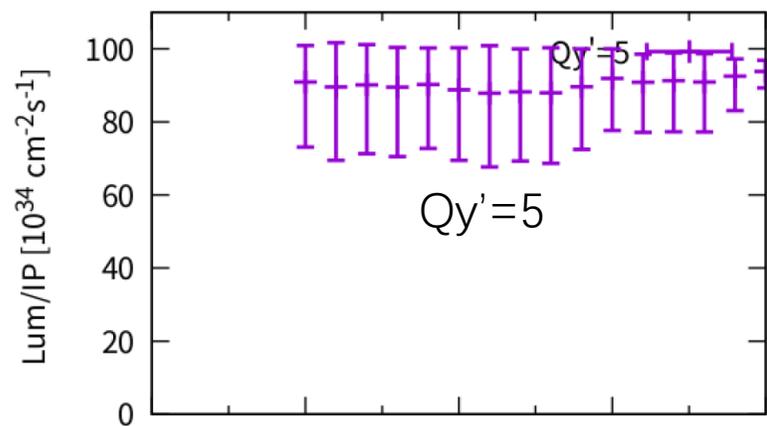
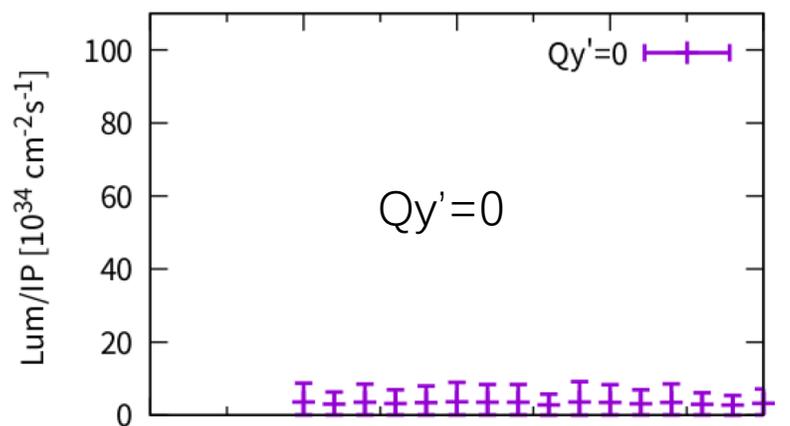


$Qy' \sim 10$  could help suppress the strong TMCI-like instability induced by BB+ZT

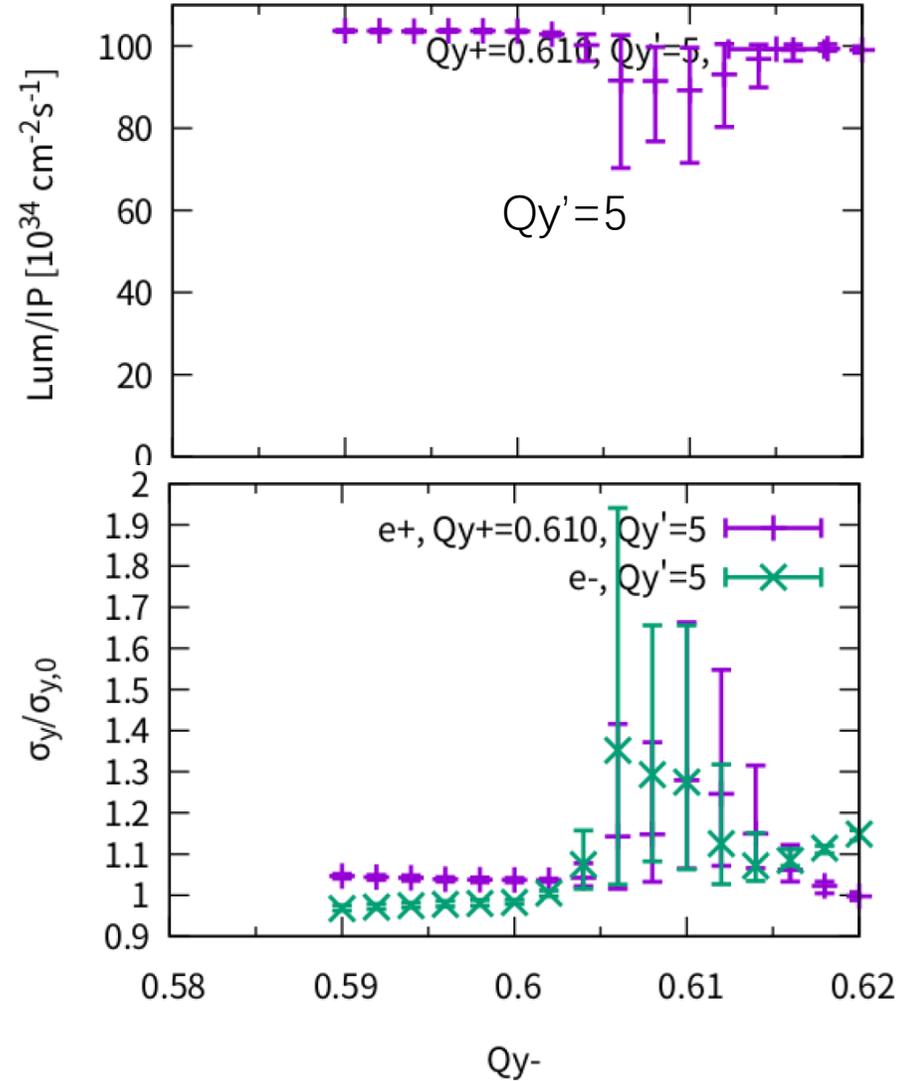
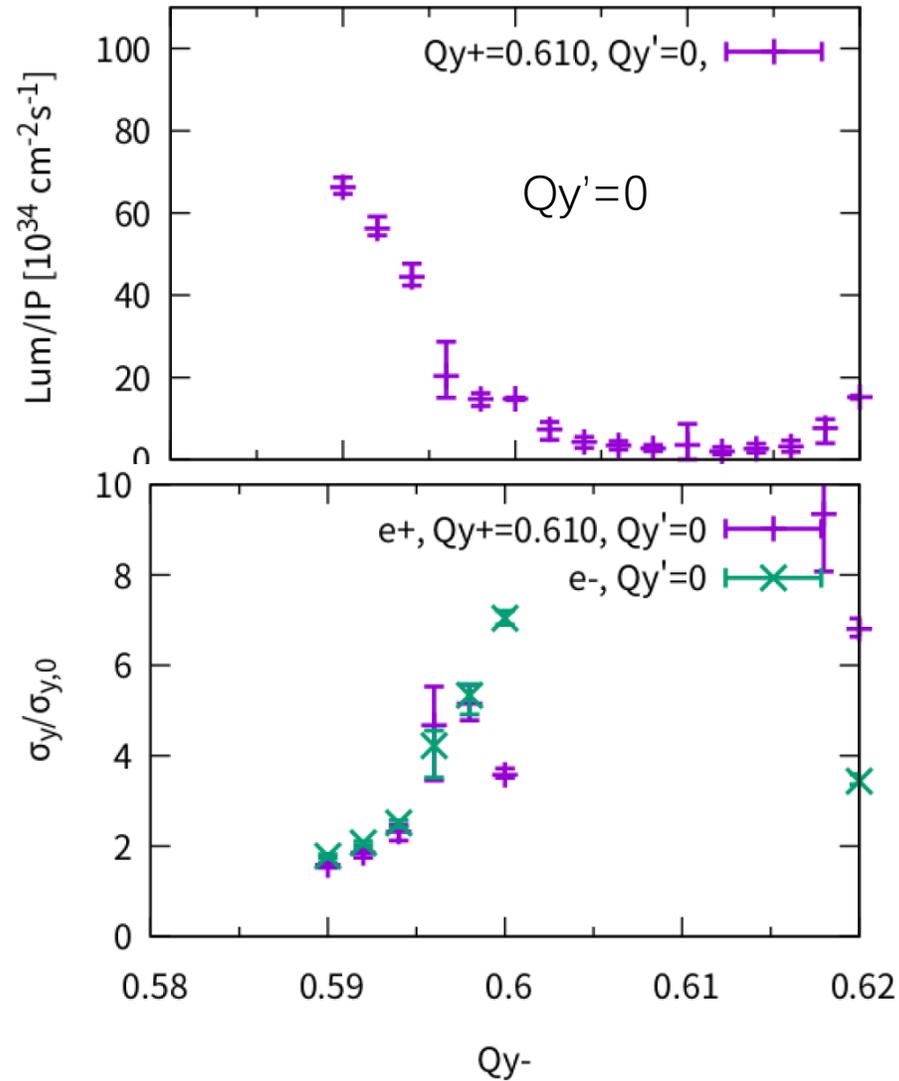
# Effect of Vertical Chromaticity ( $Lum$ & $\sigma_y$ )

CEPC

ZX+ZY+ZL,  $Q_x=0.567$

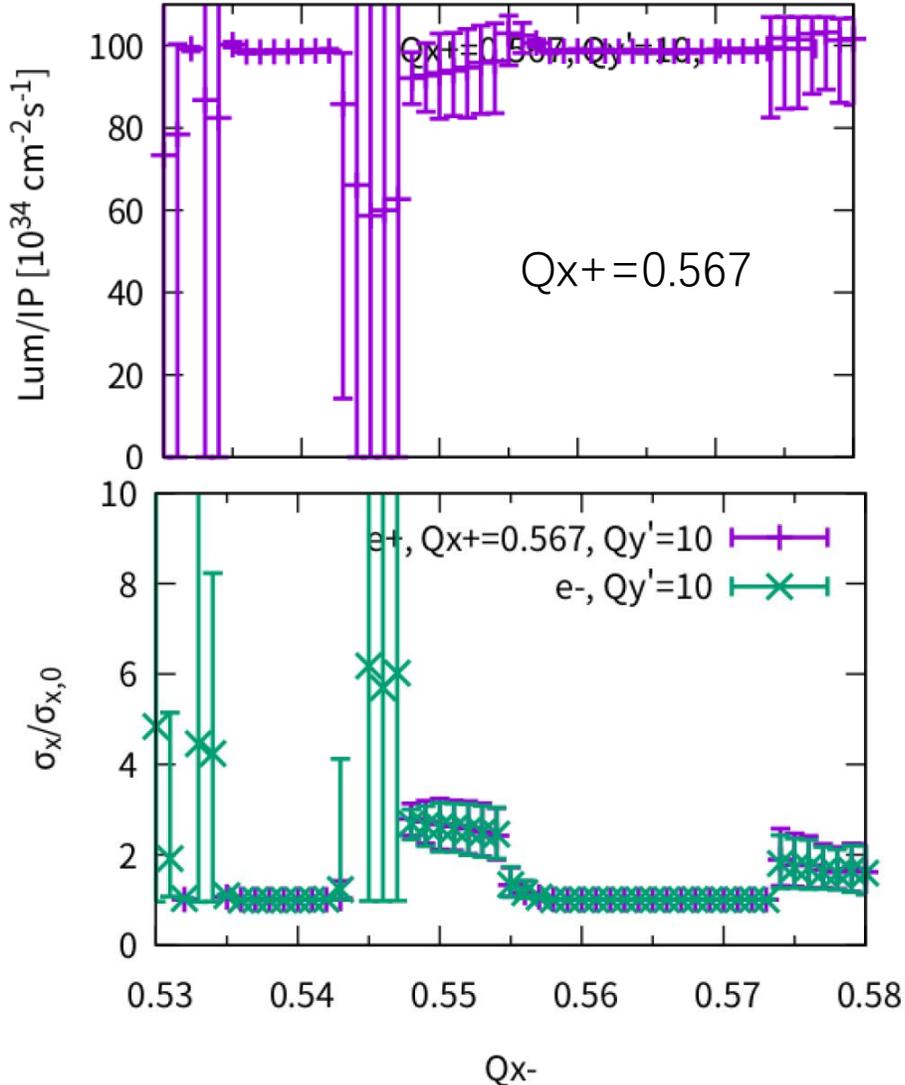


# Effect of different vertical tune ( $Q_{y+}=0.610$ ) <sup>CEPC</sup>

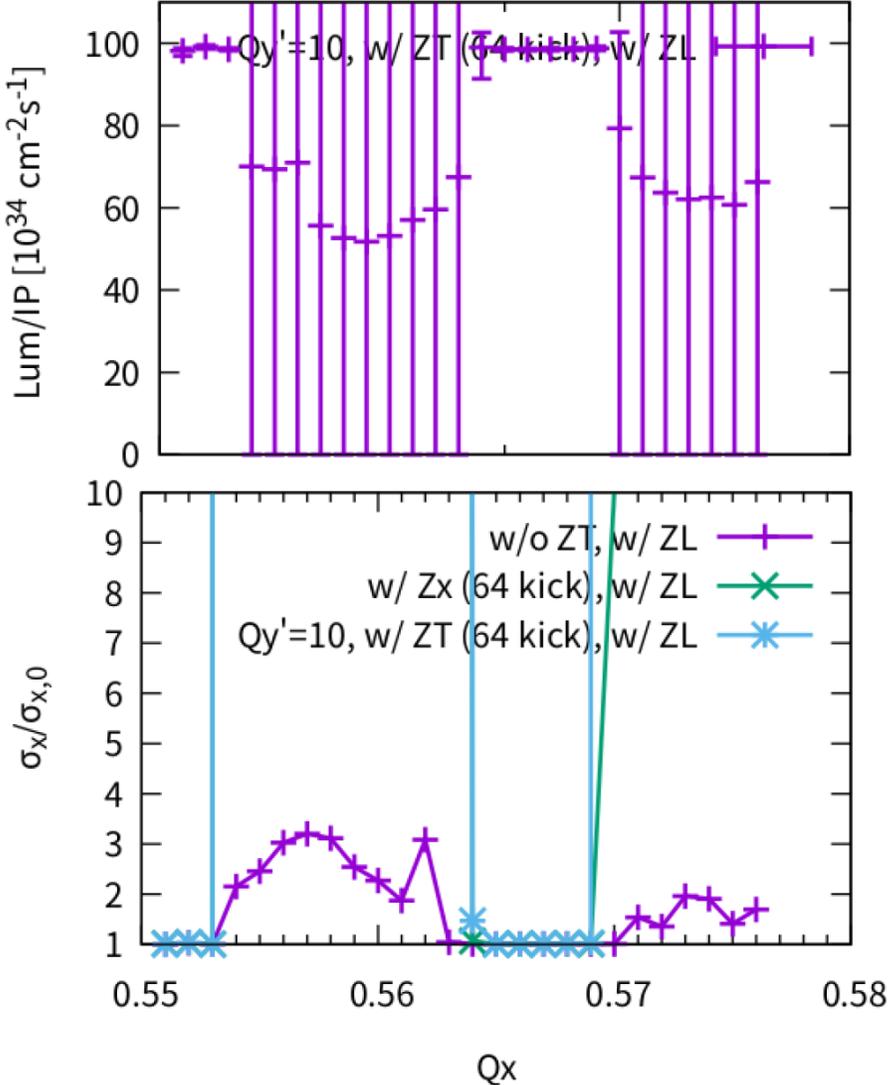


# Different Horizontal tune

Asymmetric



Symmetric



# SKEKB: Machine Parameters & Impedance

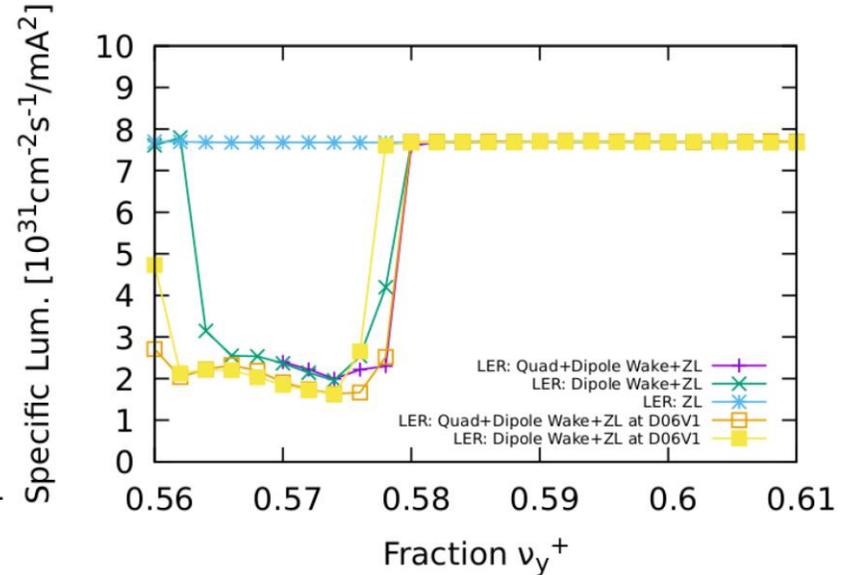
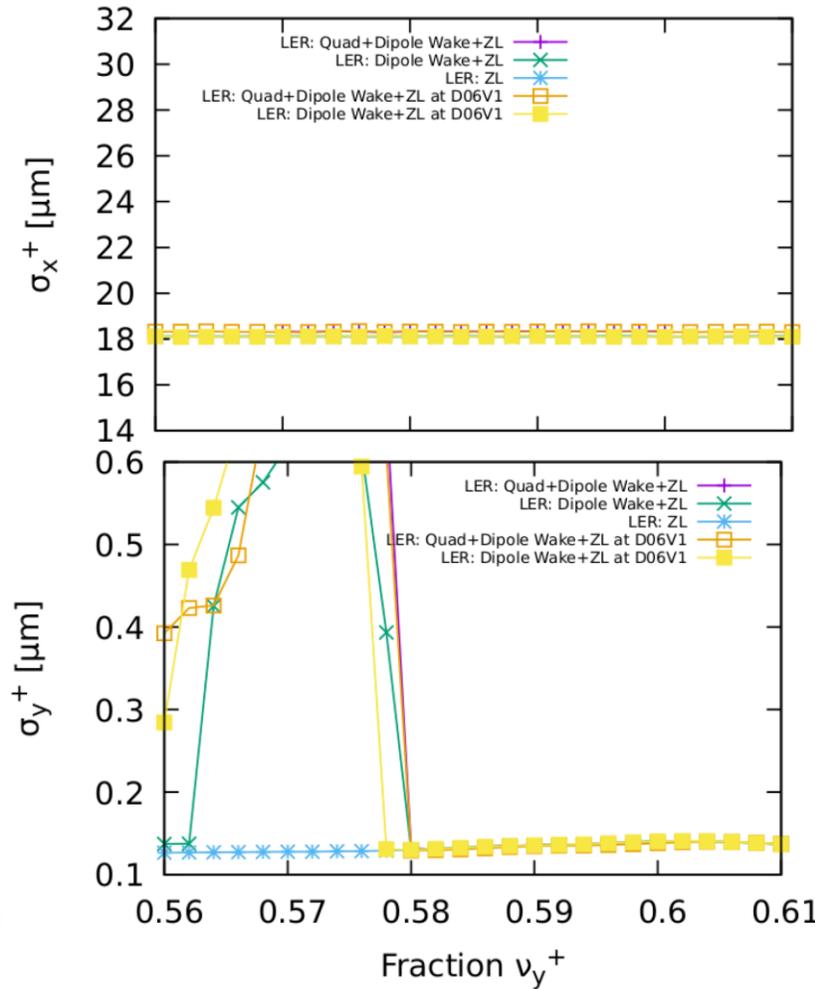
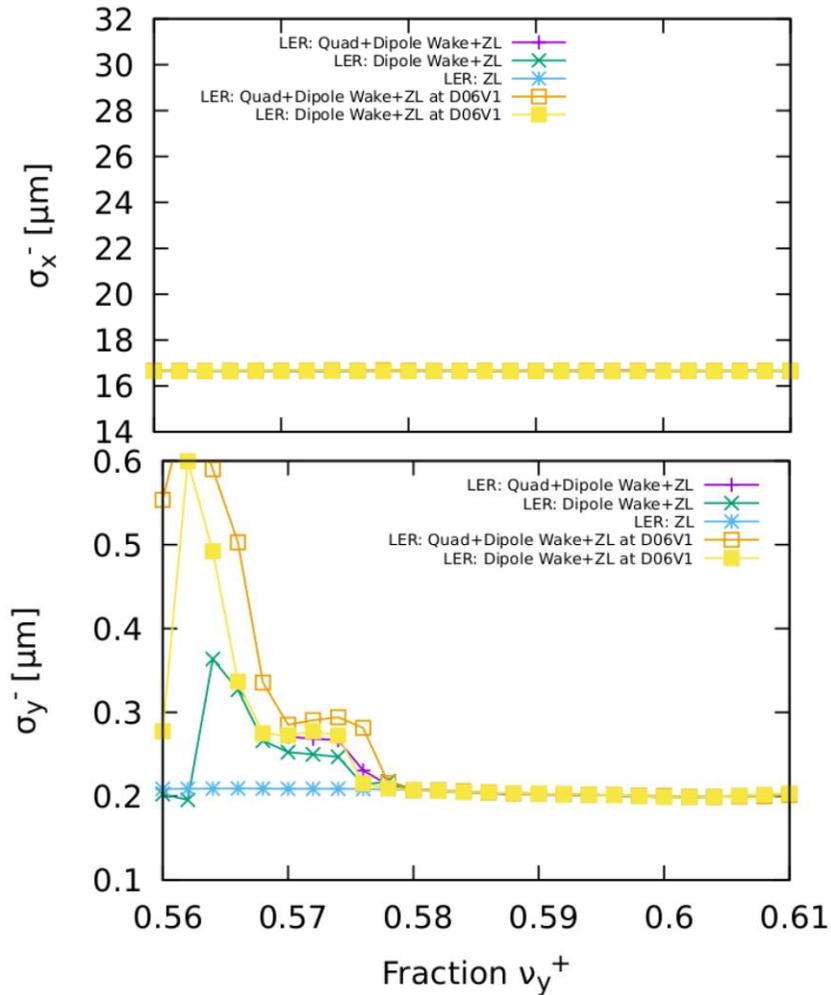
	2021.12.21		Comments
	HER	LER	
$I_{\text{bunch}}$ (mA)	$I_e$	$1.25 * I_e$	
# bunch	393		Assumed value
$\epsilon_x$ (nm)	4.6	4.0	w/ IBS
$\epsilon_y$ (pm)	35	20	Estimated from XRM data
$\beta_x$ (mm)	60	80	Calculated from lattice
$\beta_y$ (mm)	1	1	Calculated from lattice
$\sigma_{z0}$ (mm)	5.05	4.60	Natural bunch length (w/o MWI)
$\nu_x$	45.53	44.524	Measured tune of pilot bunch
$\nu_y$	43.572	46.589	Measured tune of pilot bunch
$\nu_s$	0.0272	0.0233	Calculated from lattice
Crab waist	40%	80%	Lattice design

- Wake data for TMCI study of 2021.12
- CSR are not included
- **Only LER transverse wake is considered. HER transverse wake not considered.**
- The impedance instead of original wake data is used in simulation

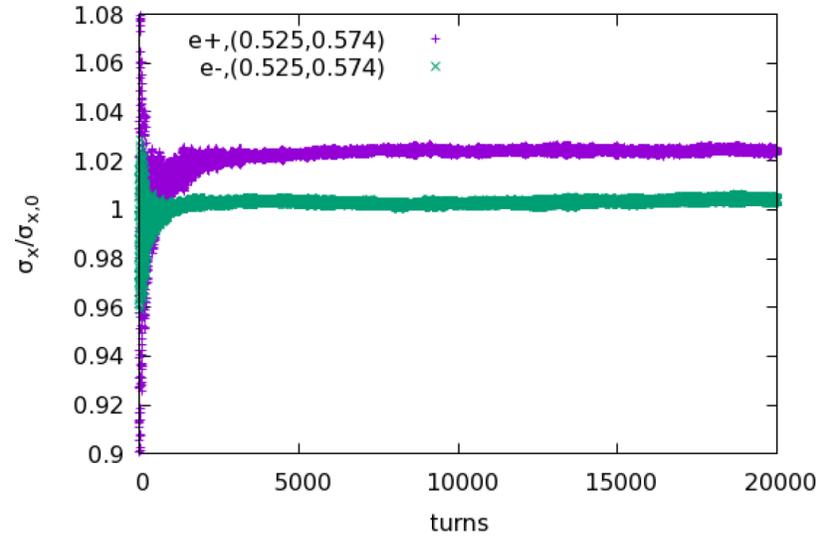
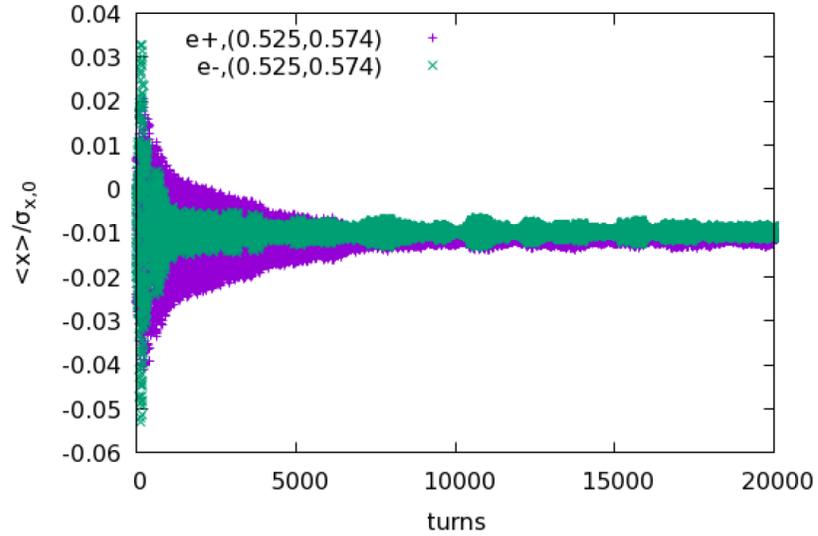
$$v_{x,0}^+ = 0.525$$

# SKEKB Collision versus $v_{y,0}^+$

- There exist vertical instability when we consider transverse wake.
- It does not matter that the local transverse is put at IP or D06V1.

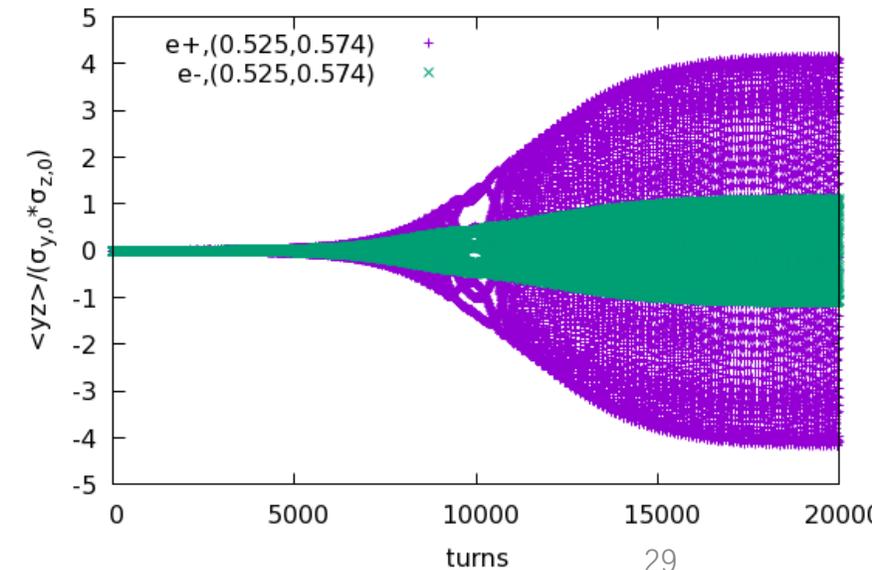
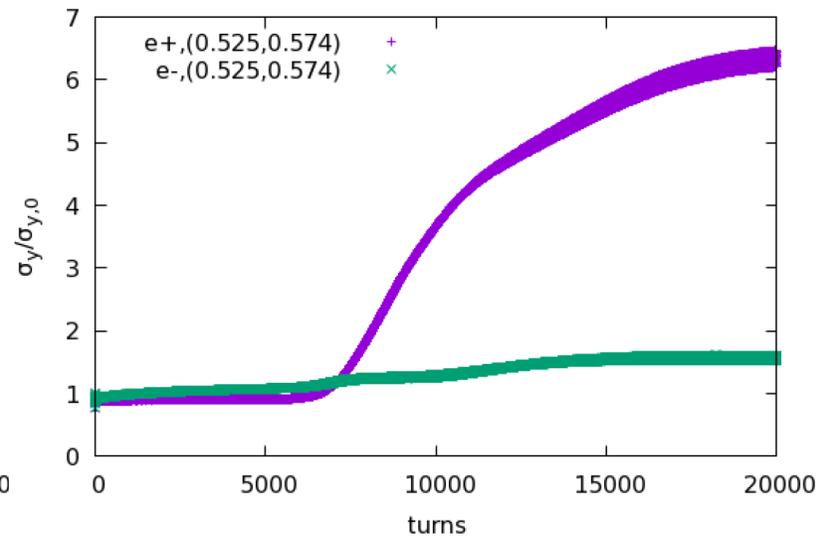
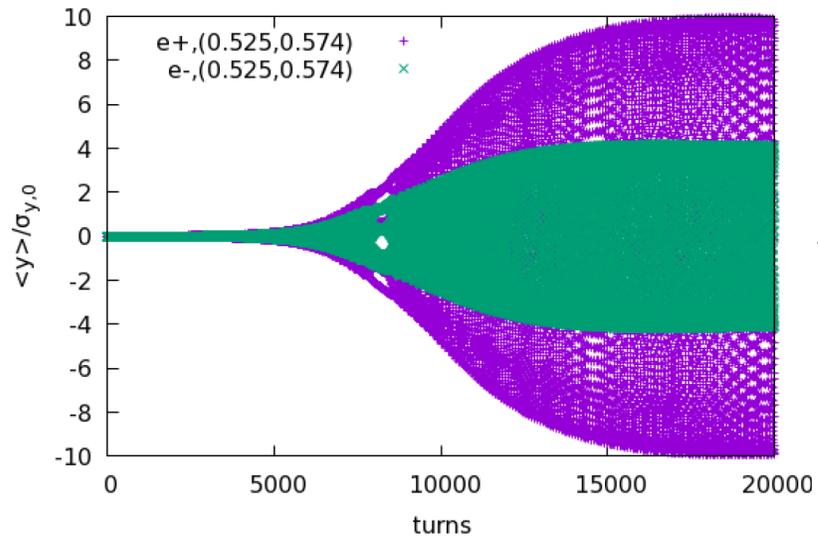


# Moment evolution: LER: dipole+quad wake + ZL, HER: ZL



There exist:

- Vertical Dipole oscillation
- Vertical Beam Blowup
- $\langle yz \rangle$  head-tail oscillation



# Summary

- The FCCee (Z) parameters is evolving, and the combined effect of beam-beam and impedance has been studied by simulation.
- The simulation results show that the present parameter could work when both  $Z_L$  and  $Z_T$  is considered
- Some mitigation schemes has been studied
- Some analysis work has been done to help understand the physics
- **The interplay between beam-beam and other dynamics effect must be considered in future high performance e+e-colliders**