

On exclusive $b \rightarrow c \ell \nu$ decay modes

Damir Bečirević

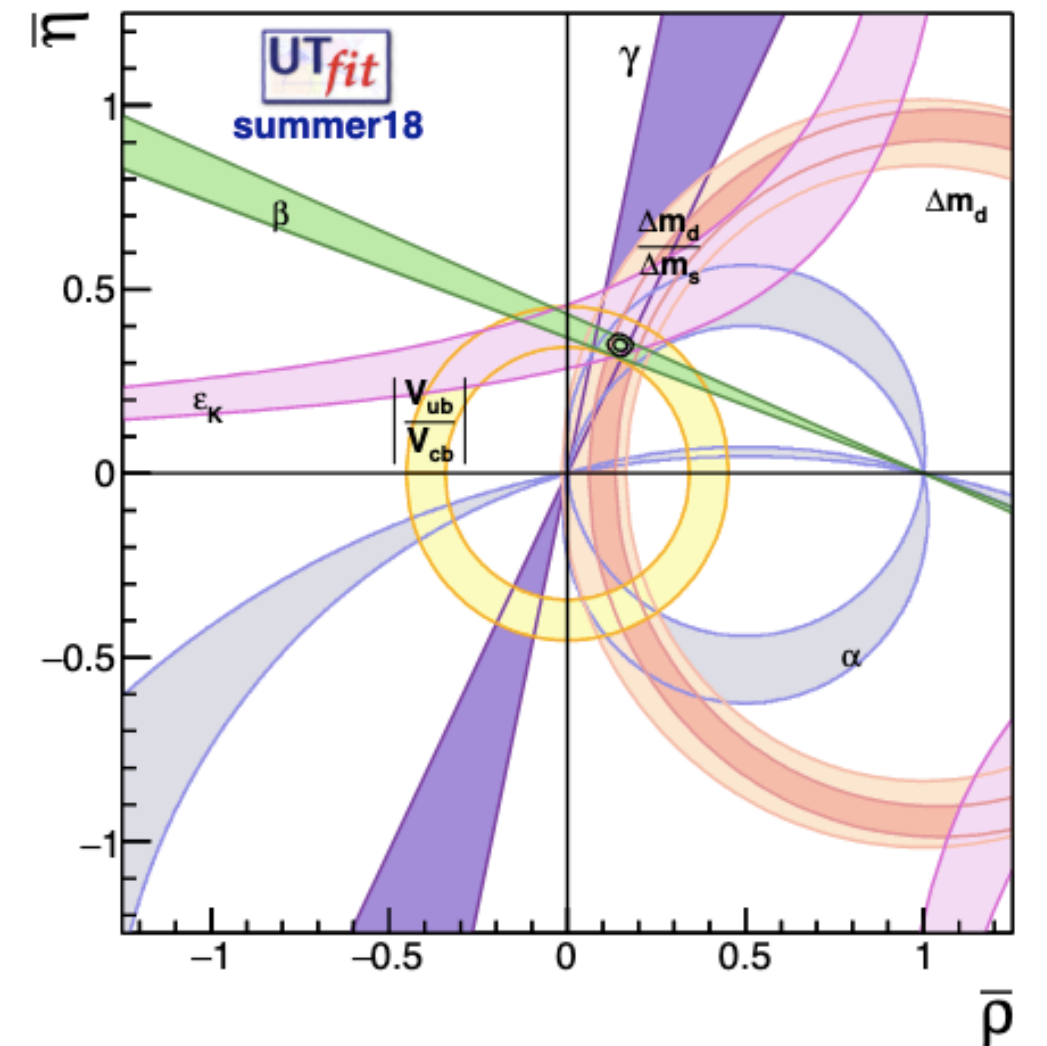
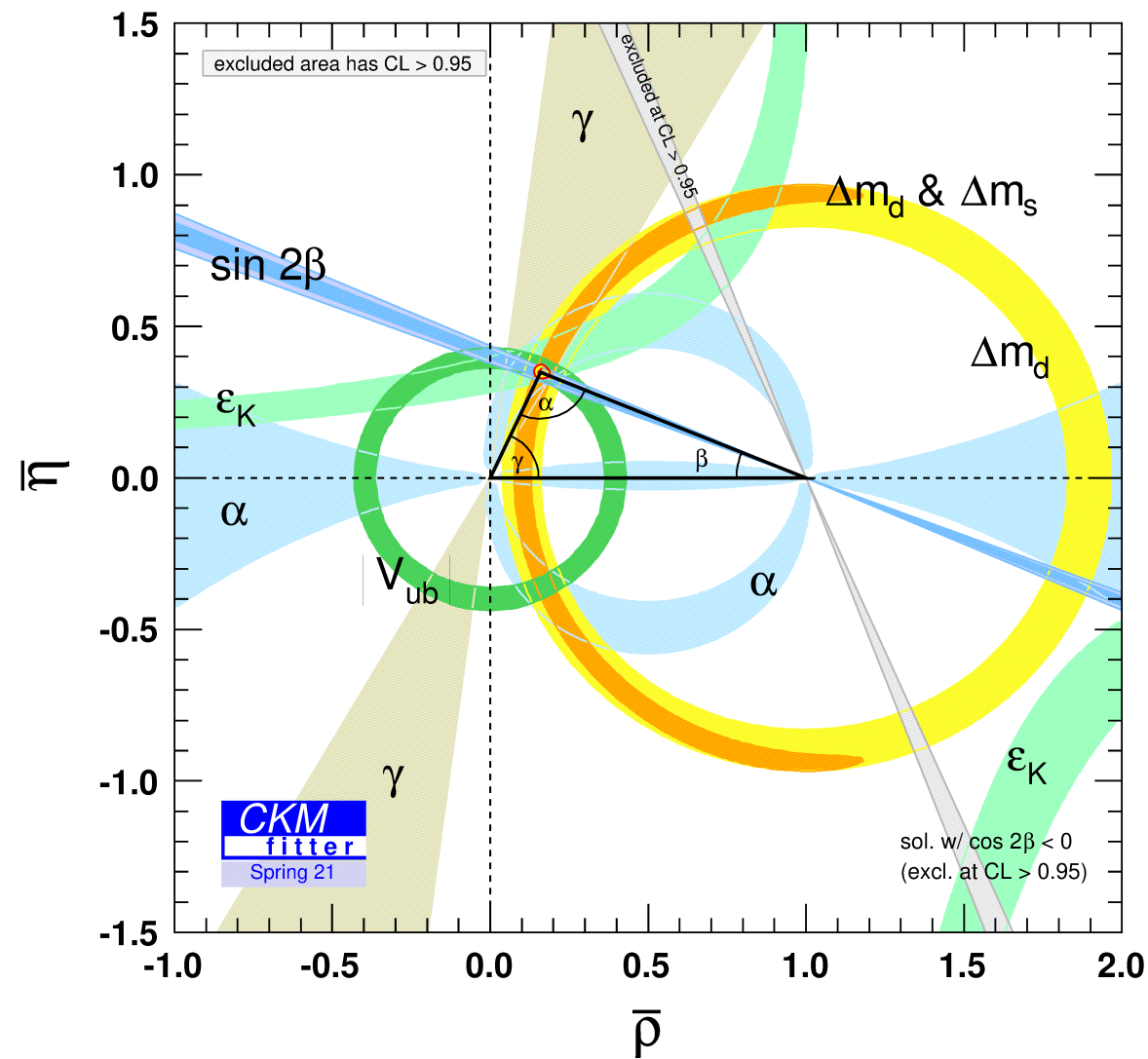
Pôle Théorie, IJCLab

CNRS et Université Paris-Saclay

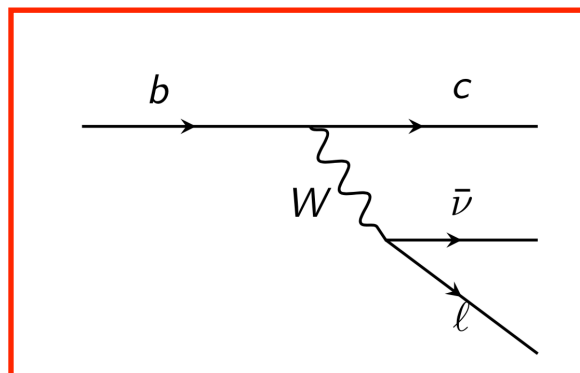


based on works with F. Jaffredo, A. Le Yaouanc, and O. Sumensari

CKM-ology

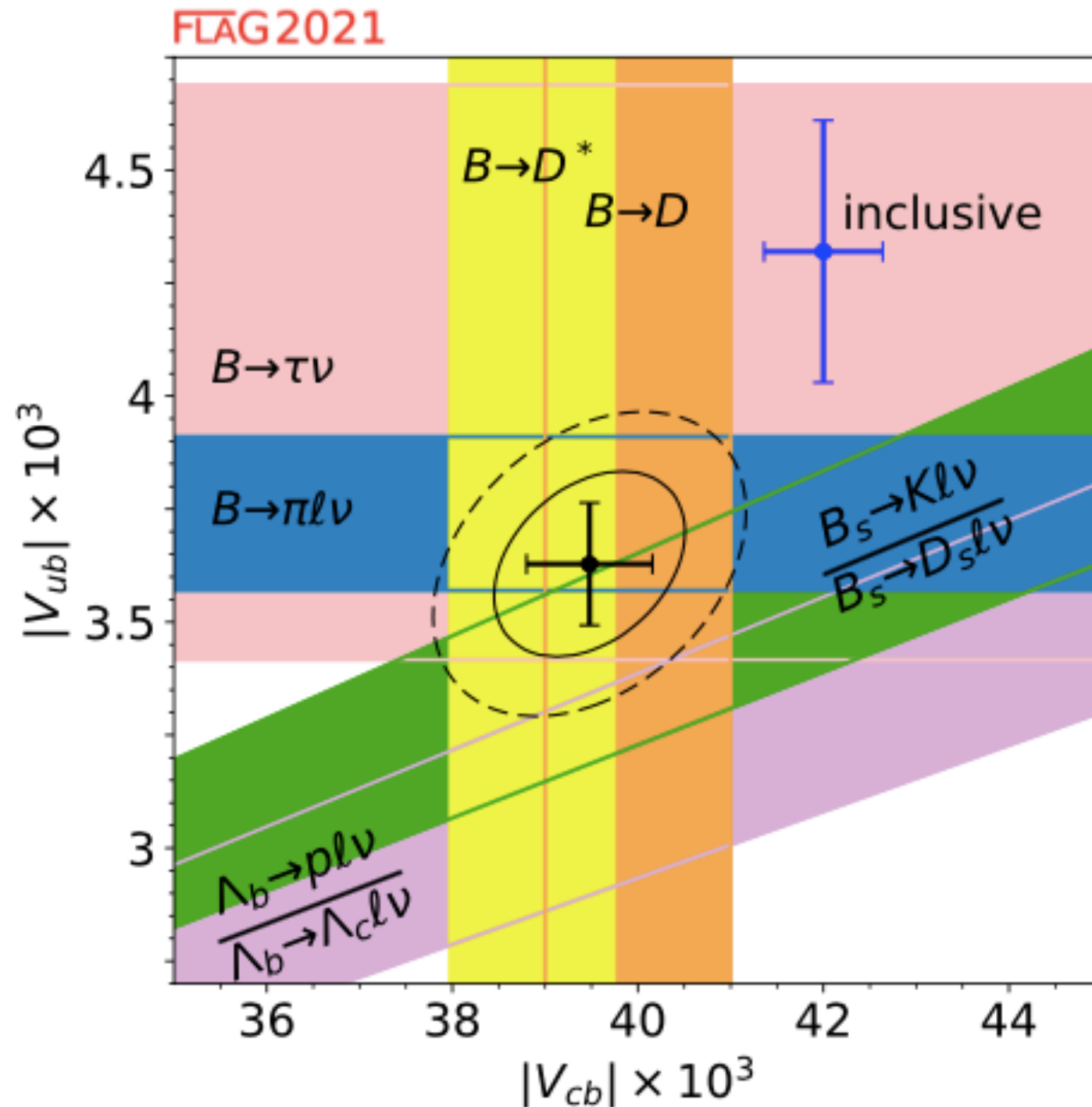


- ✗ Still open: inclusive v exclusive V_{ub} and V_{cb} ?
- Is V_{ud} well controlled? V_{us} keeps coming back (EM)...



CKM-ology - Small flavor 'anomaly'

✗ Still open: inclusive v exclusive V_{ub} and V_{cb} ?



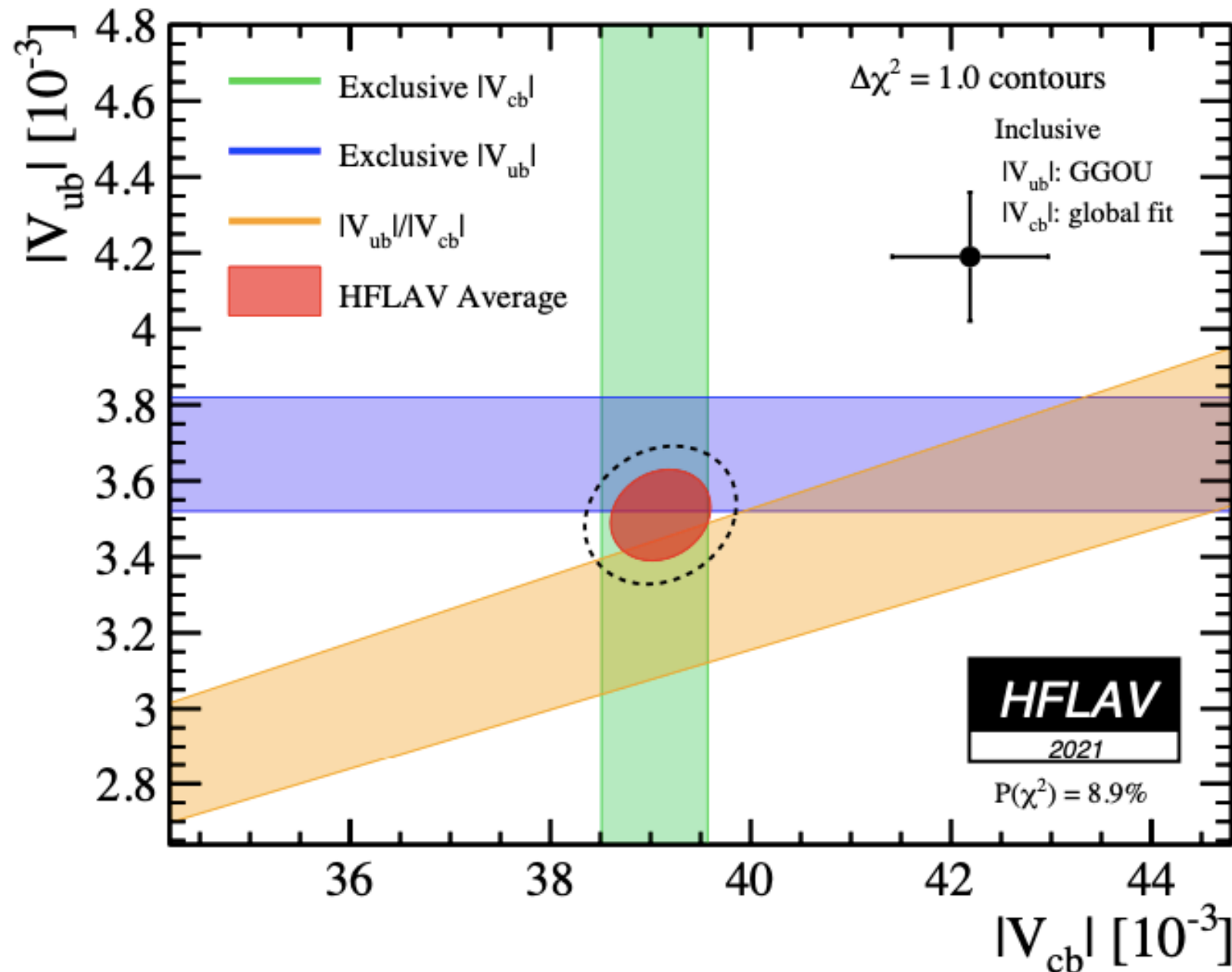
✗ Belle II (excl + incl), LHCb (excl)

✗ QCD on very fine lattices
 $B \rightarrow D$ and $B \rightarrow D^*$ at $w=1$

✗ Nowadays probed *non-zero recoil*

CKM-ology - Small flavor 'anomaly'

✗ Still open: inclusive v exclusive V_{ub} and V_{cb} ?



✗ Lattice, best way to go
 $B \rightarrow D$ at various small w ,
but for w accessible from
LQCD, a huge phase space
suppression

✗ Experimentally appealing
 $B \rightarrow D^*$ (also *Luke theorem*)

HQE

$$\hat{h}_V = 1 + \hat{\alpha}_s C_{V_1} + \varepsilon_c [\hat{L}_2^{(c)} - \hat{L}_5^{(c)}] + \varepsilon_b [\hat{L}_1^{(b)} - \hat{L}_4^{(b)}] + \varepsilon_c \varepsilon_b \hat{M}_9$$

$$\hat{h}_{A_1} = 1 + \hat{\alpha}_s C_{A_1} + \varepsilon_c \left(\hat{L}_2^{(c)} - \hat{L}_5^{(c)} \frac{w-1}{w+1} \right) + \varepsilon_b \left(\hat{L}_1^{(b)} - \hat{L}_4^{(b)} \frac{w-1}{w+1} \right) + \varepsilon_c \varepsilon_b \hat{M}_9$$

$$\hat{h}_{A_2} = \hat{\alpha}_s C_{A_2} + \varepsilon_c [\hat{L}_3^{(c)} + \hat{L}_6^{(c)}] - \varepsilon_c \varepsilon_b \hat{M}_{10}$$

$$\hat{h}_{A_3} = 1 + \hat{\alpha}_s (C_{A_1} + C_{A_3}) + \varepsilon_c [\hat{L}_2^{(c)} - \hat{L}_3^{(c)} + \hat{L}_6^{(c)} - \hat{L}_5^{(c)}] + \varepsilon_b [\hat{L}_1^{(b)} - \hat{L}_4^{(b)}] + \varepsilon_c \varepsilon_b [\hat{M}_9 + \hat{M}_{10}]$$

$$q^2 = m_B^2 + m_{D^*}^2 - 2m_B m_{D^*} w$$

2206.11281

✗ tricky part - shapes...

$$\hat{h}(w) = h(w)/\xi(w)$$

$$\bullet \quad h_{A_1}(w) = 1 - \rho^2(w-1) + \frac{c}{2}(w-1)^2 + \dots$$

$$\bullet \quad h_{A_1}(w) = \left(\frac{2}{w+1} \right)^{2\rho^2} \quad c = \rho^2 \left(\rho^2 + \frac{1}{2} \right)$$

$$\bullet \quad h_{A_1}(w) = 1 - 8\rho^2 z + (53\rho^2 - 15)z^2 - (231\rho^2 - 91)z^3 \quad z = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}}$$

$$c = \frac{3}{32} \rho^2 (23\rho^2 - 5)$$

CLN or BGL or...

$$\frac{d\Gamma(\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell)}{dw} = \frac{G_F^2 m_{D^*}^3}{48\pi^3} (m_B - m_{D^*})^2 \chi(w) \eta_{EW}^2 \mathcal{F}^2(w) |V_{cb}|^2$$

$$\chi(w) \mathcal{F}^2(w) = h_{A_1}^2(w) \sqrt{w^2 - 1} (w + 1)^2 \left\{ 2 \left[\frac{1 - 2wr + r^2}{(1 - r)^2} \right] \left[1 + R_1^2(w) \frac{w - 1}{w + 1} \right] + \left[1 + (1 - R_2(w)) \frac{w - 1}{1 - r} \right]^2 \right\}$$

$$q^2 = m_B^2 + m_{D^*}^2 - 2m_B m_{D^*} w$$

$$r = m_{D^*}/m_B$$

$$h_{A_1}(w) = h_{A_1}(1) [1 - 8\rho^2 z + (53\rho^2 - 15)z^2 - (231\rho^2 - 91)z^3]$$

$$R_1(w) = R_1(1) - 0.12(w - 1) + 0.05(w - 1)^2 \quad \text{CLN} \quad 9712417$$

$$R_2(w) = R_2(1) + 0.11(w - 1) - 0.06(w - 1)^2 \quad \text{BGL} \quad 9705252$$

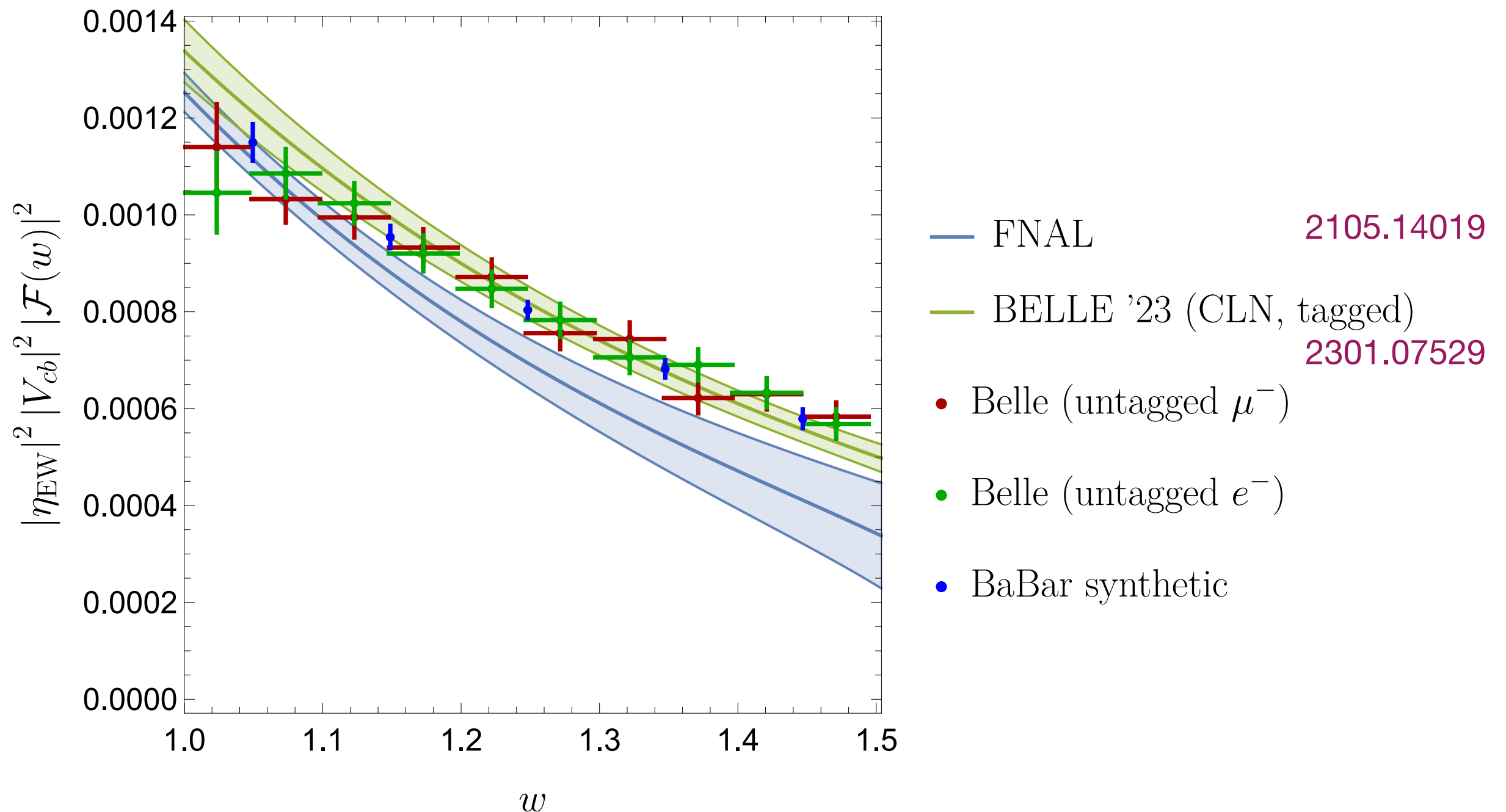
$$z = \frac{\sqrt{w + 1} - \sqrt{2}}{\sqrt{w + 1} + \sqrt{2}}$$

these should be fit too
and not fixed as in CLS

- ✗ Exp data fit very well with CLN, but eventually [with ever better precision] BGL should be the ultimate choice, **IF** you decide to follow this route...

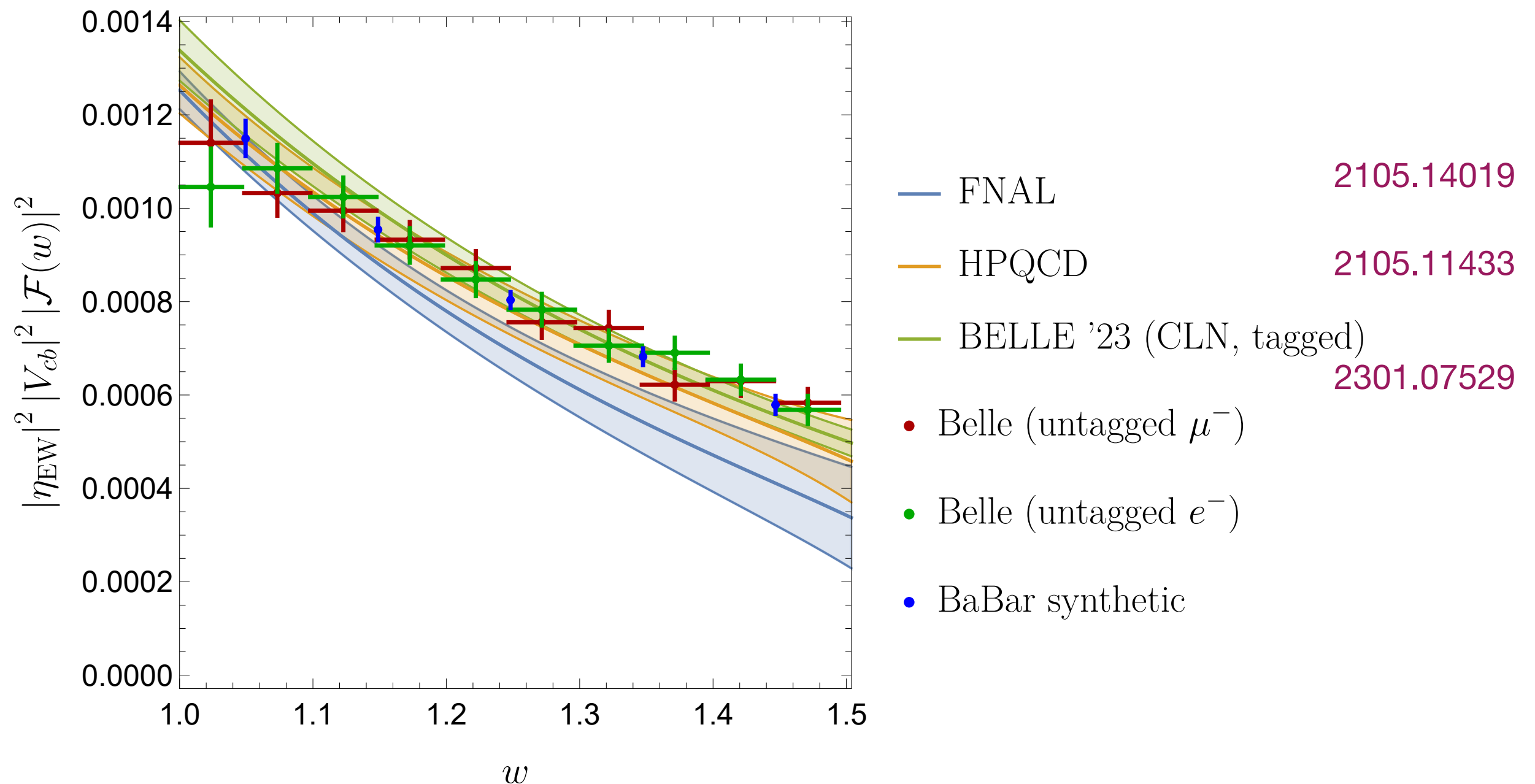
We still do not have a control over hadronic uncertainties with

$$\frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dq^2} = \frac{1}{2m_B m_{D^*}} \frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dw} \propto |V_{cb}|^2 |\mathcal{F}(w)|^2$$



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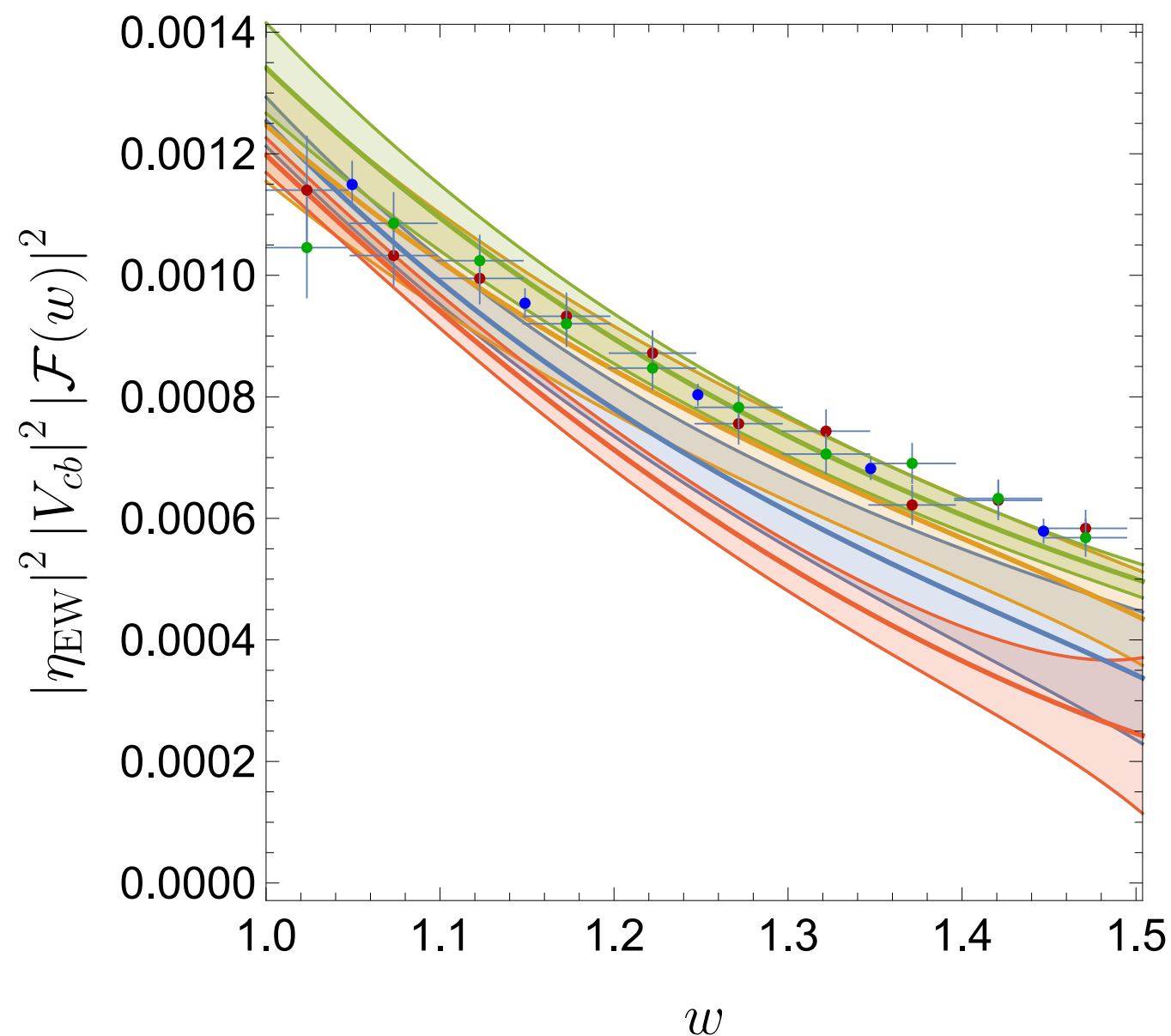
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• Assuming with HPQCD that $\mathcal{F}(w)^{B_s \rightarrow D_s^*} = \mathcal{F}(w)^{B \rightarrow D^*}$

We still do not have a control over hadronic uncertainties with

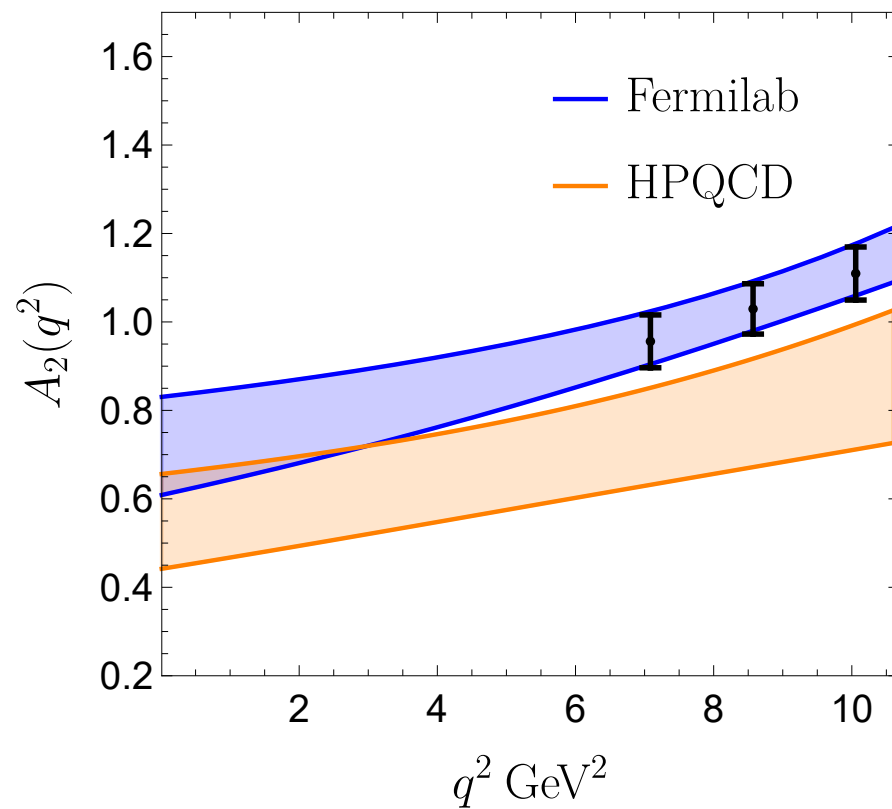
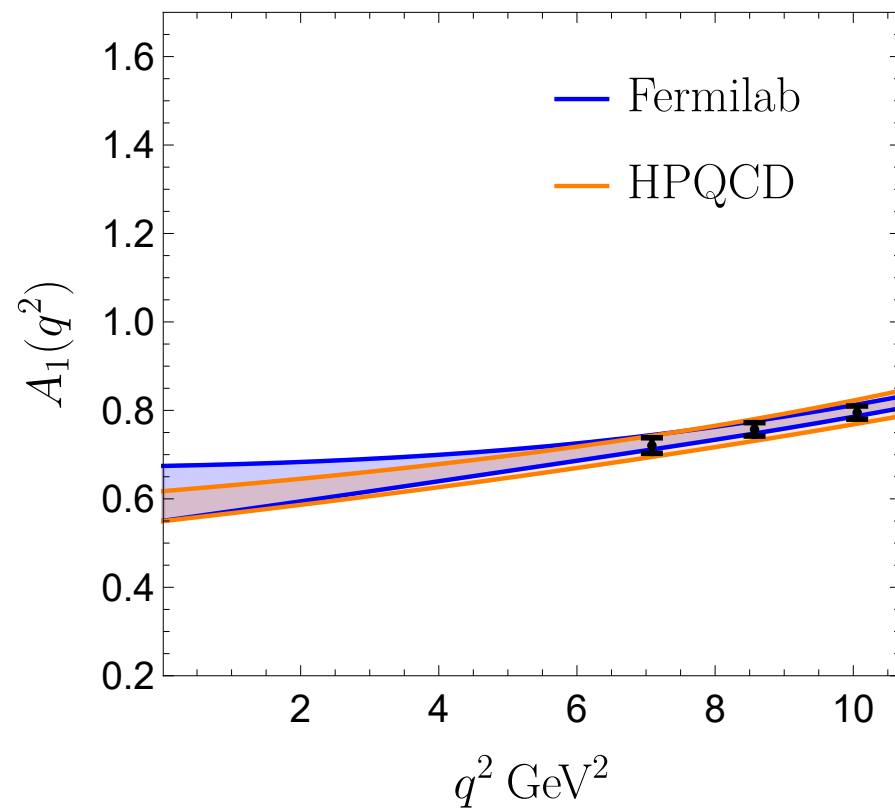
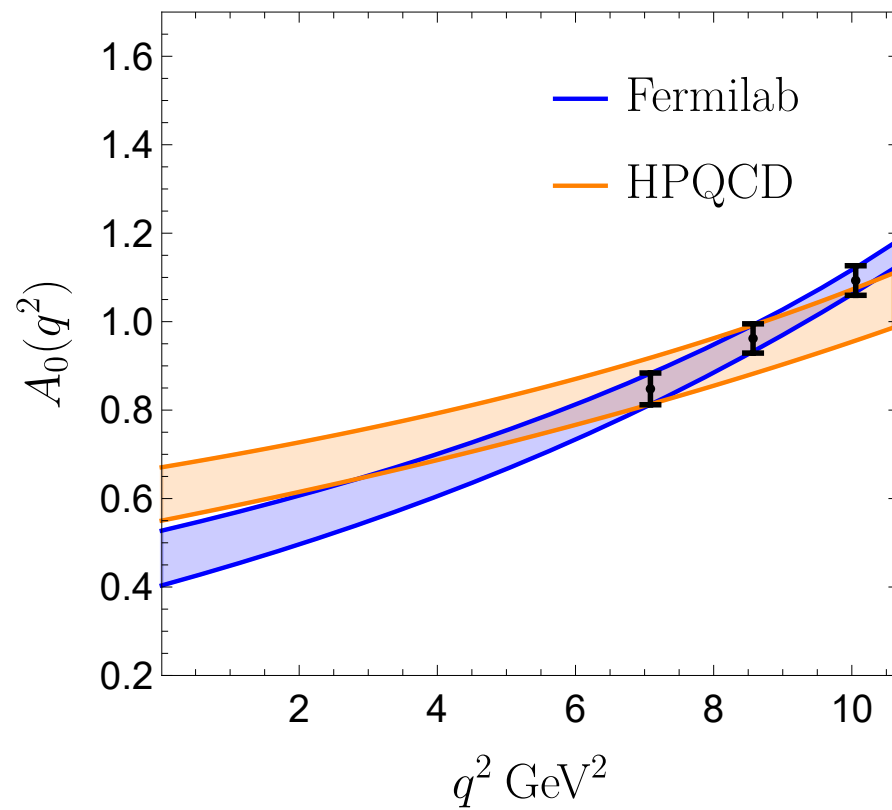
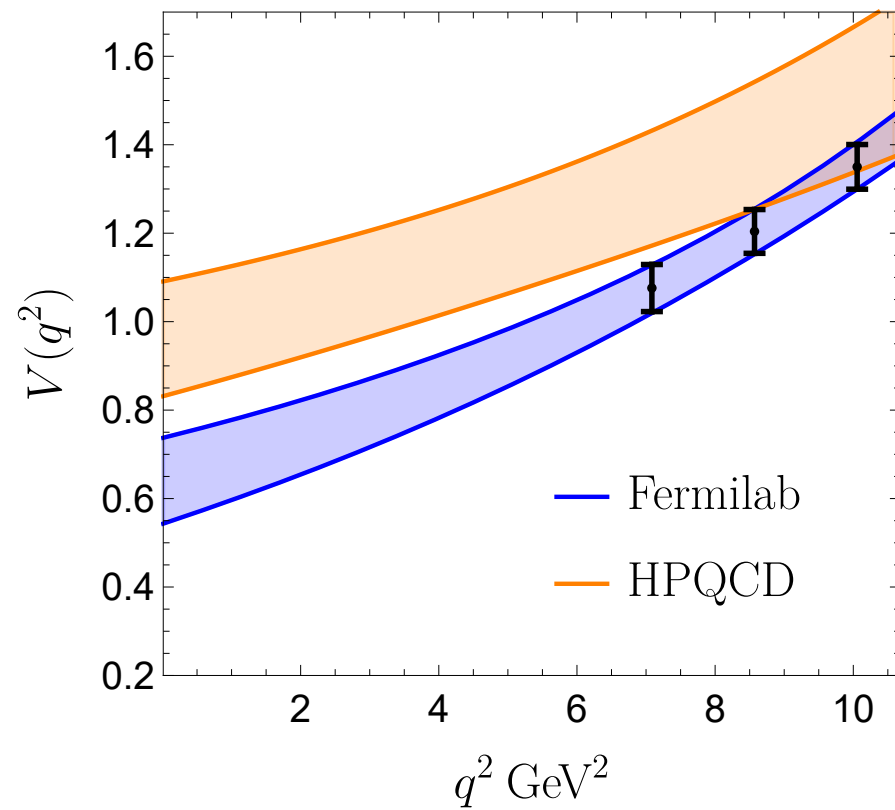
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- Fermilab 2105.14019
- Previous HPQCD $B_s \rightarrow D_s^*$ 2105.11433
- BELLE (CLN, tagged) 2301.07529
- New HPQCD $B \rightarrow D^*$ 2304.03137
- Belle (untagged μ^-)
- Belle (untagged e^-)
- BaBar synthetic

• Assuming with HPQCD that $\mathcal{F}(w)^{B_s \rightarrow D_s^*} = \mathcal{F}(w)^{B \rightarrow D^*}$

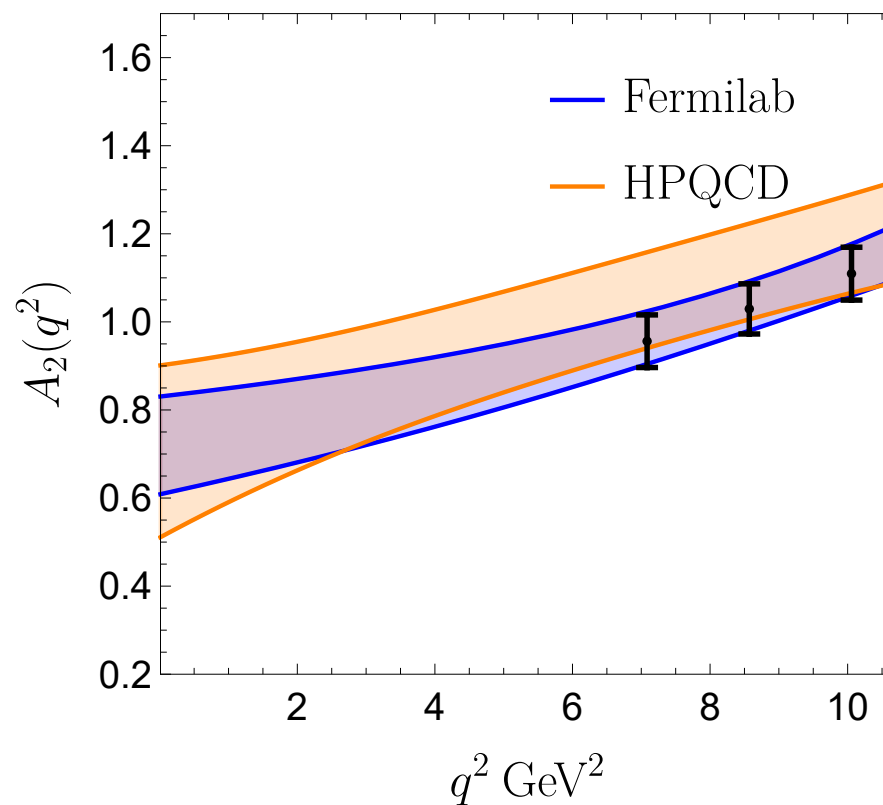
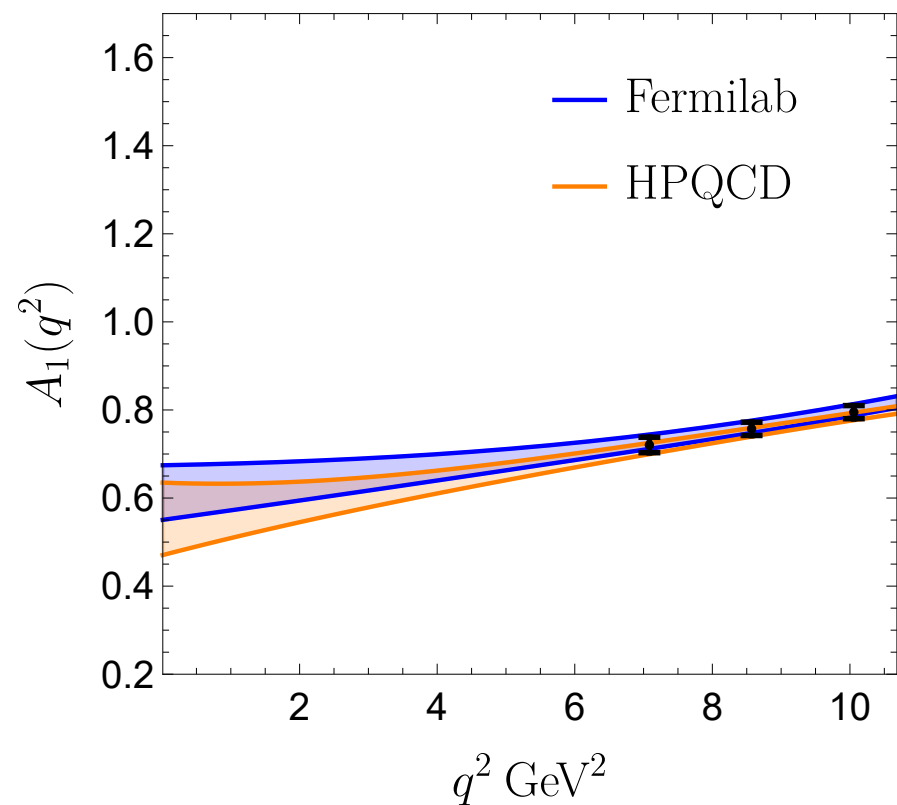
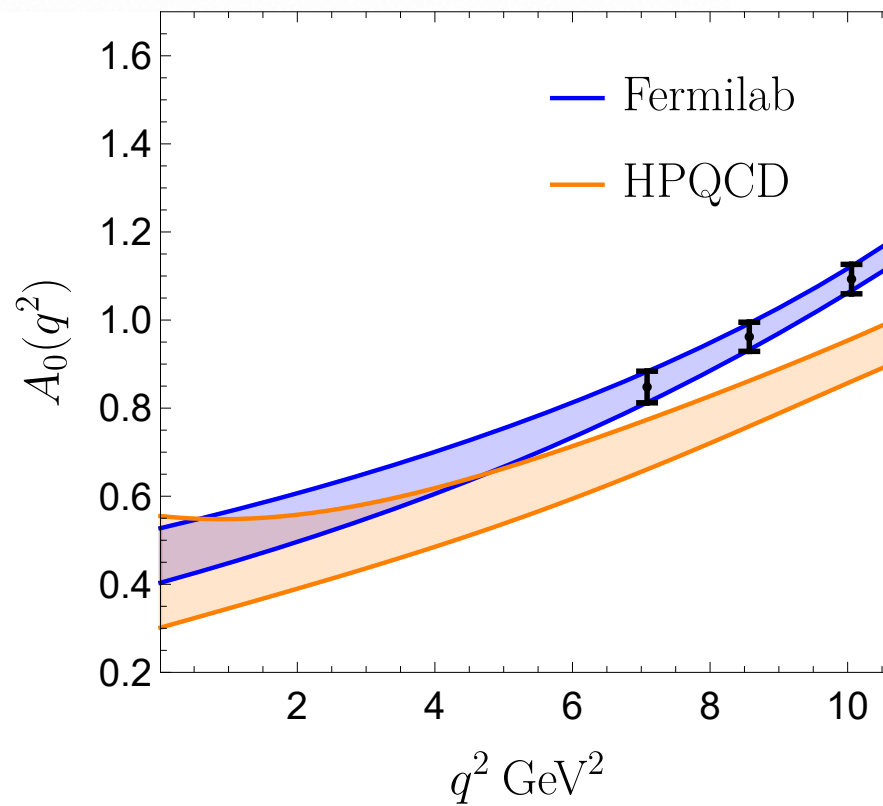
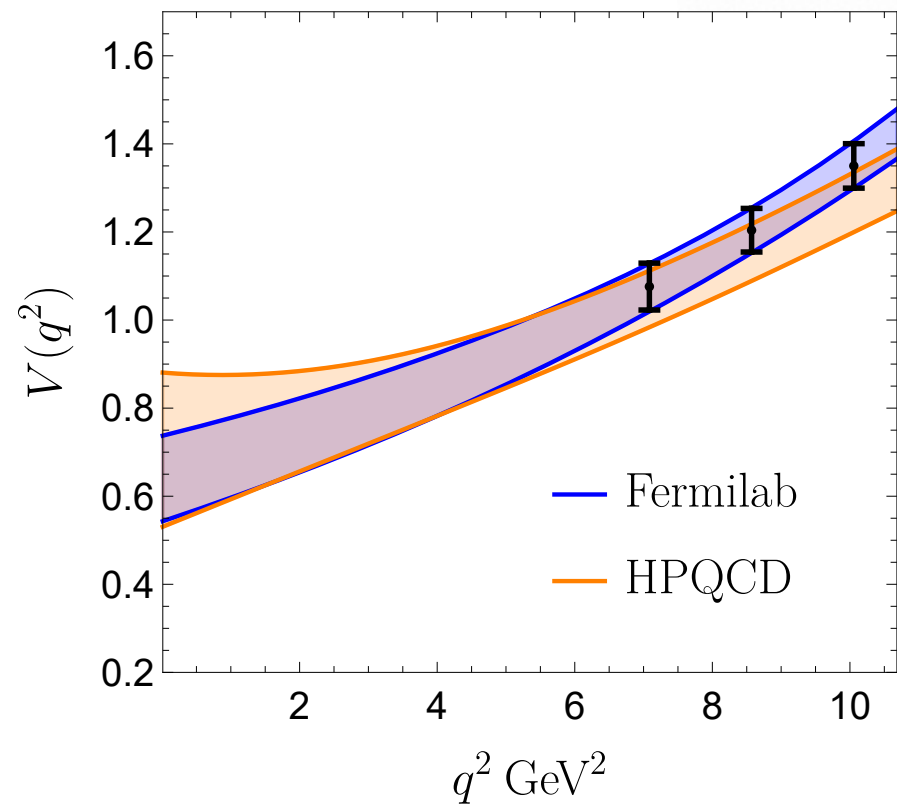
$$B \rightarrow D^* \ell \bar{\nu}$$



2105.14019

2105.11433

$$B \rightarrow D^* \ell \bar{\nu}$$



2105.14019

2304.03137

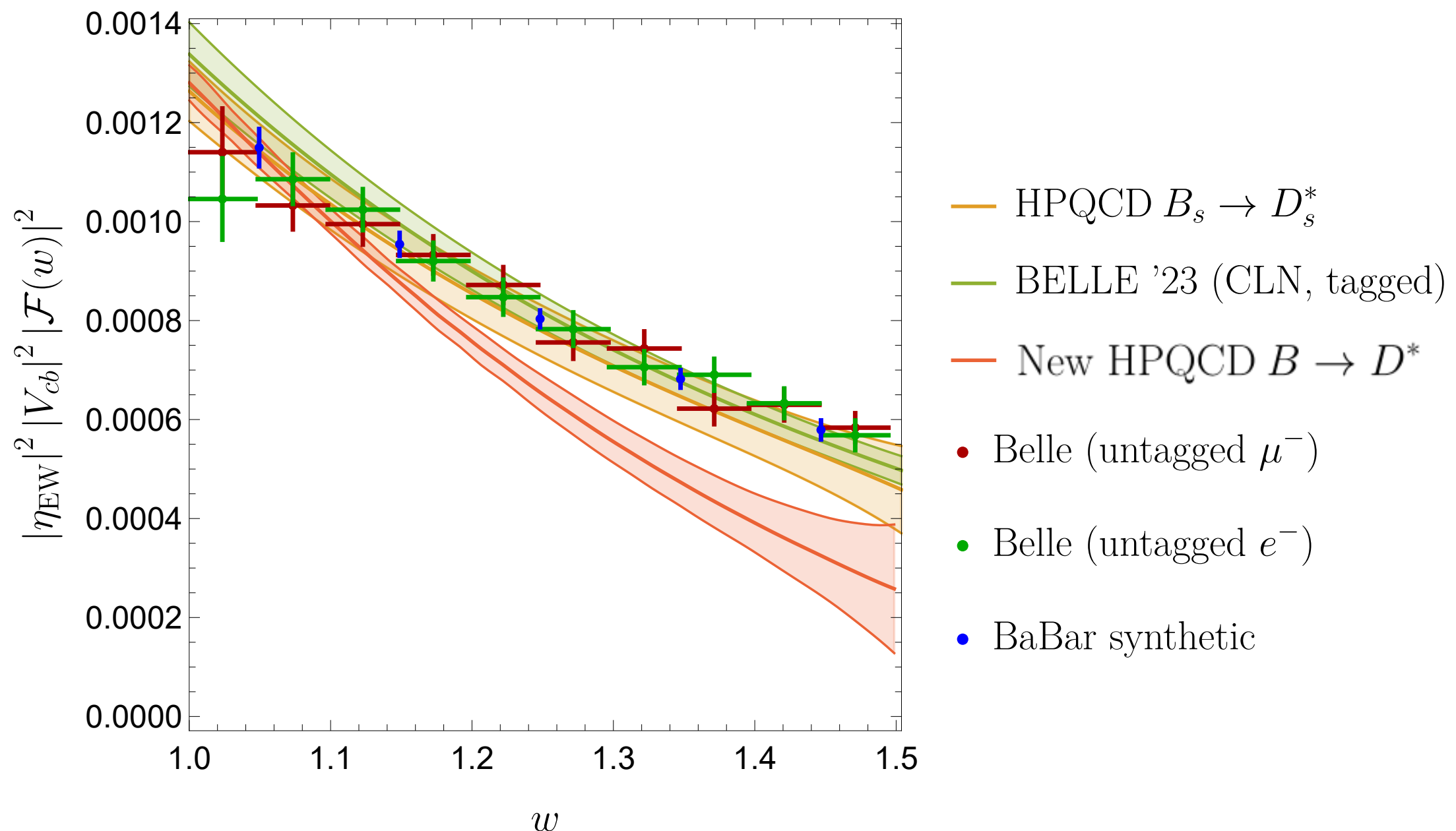
New HPQCD

- ✗ One more lattice spacing
- ✗ Chiral extrapolation

New HPQCD results suggest spectator light quark mass dependence

How can we understand that?

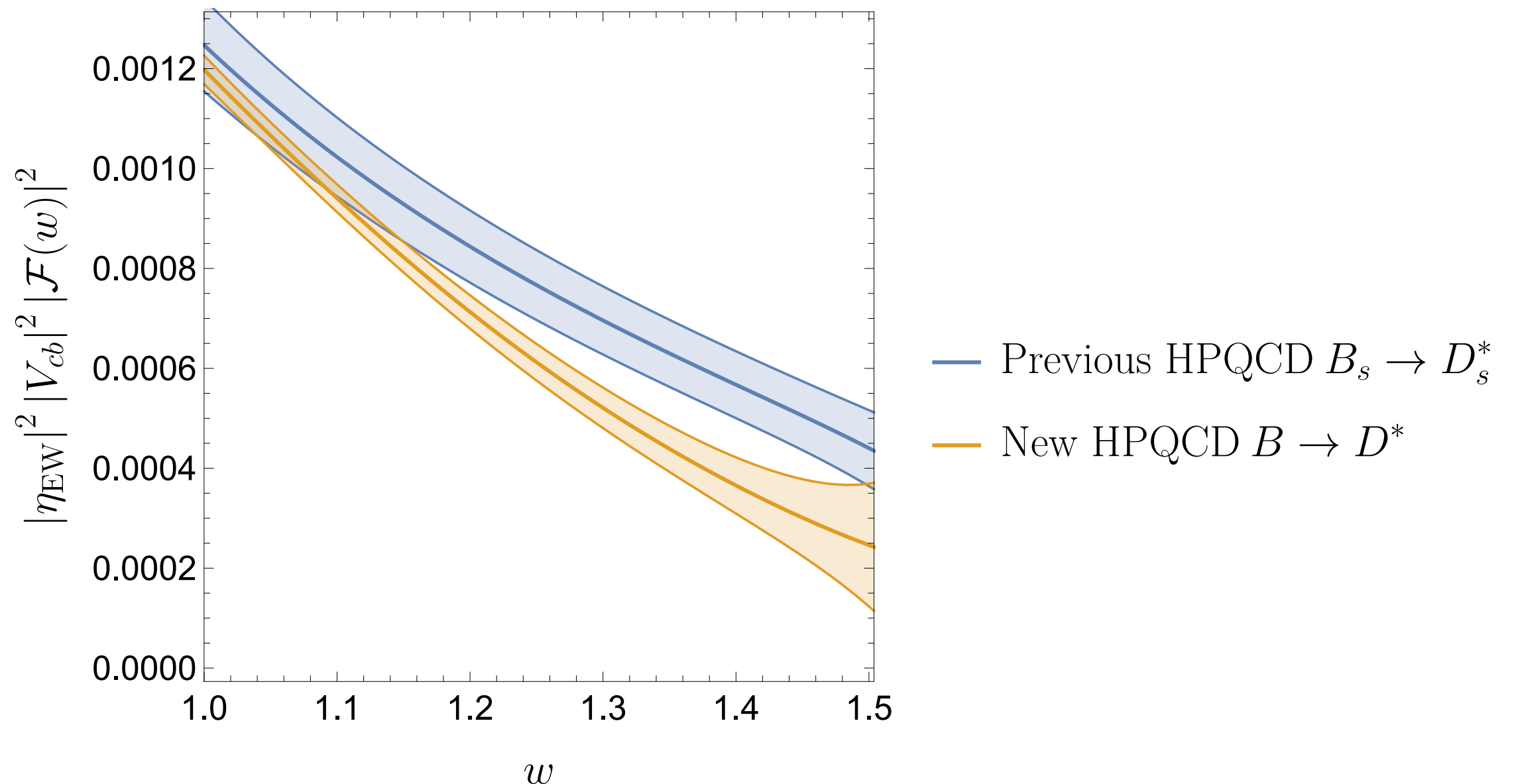
$$\frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dq^2} = \frac{1}{2m_B m_{D^*}} \frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dw} \propto |V_{cb}|^2 |\mathcal{F}(w)|^2$$



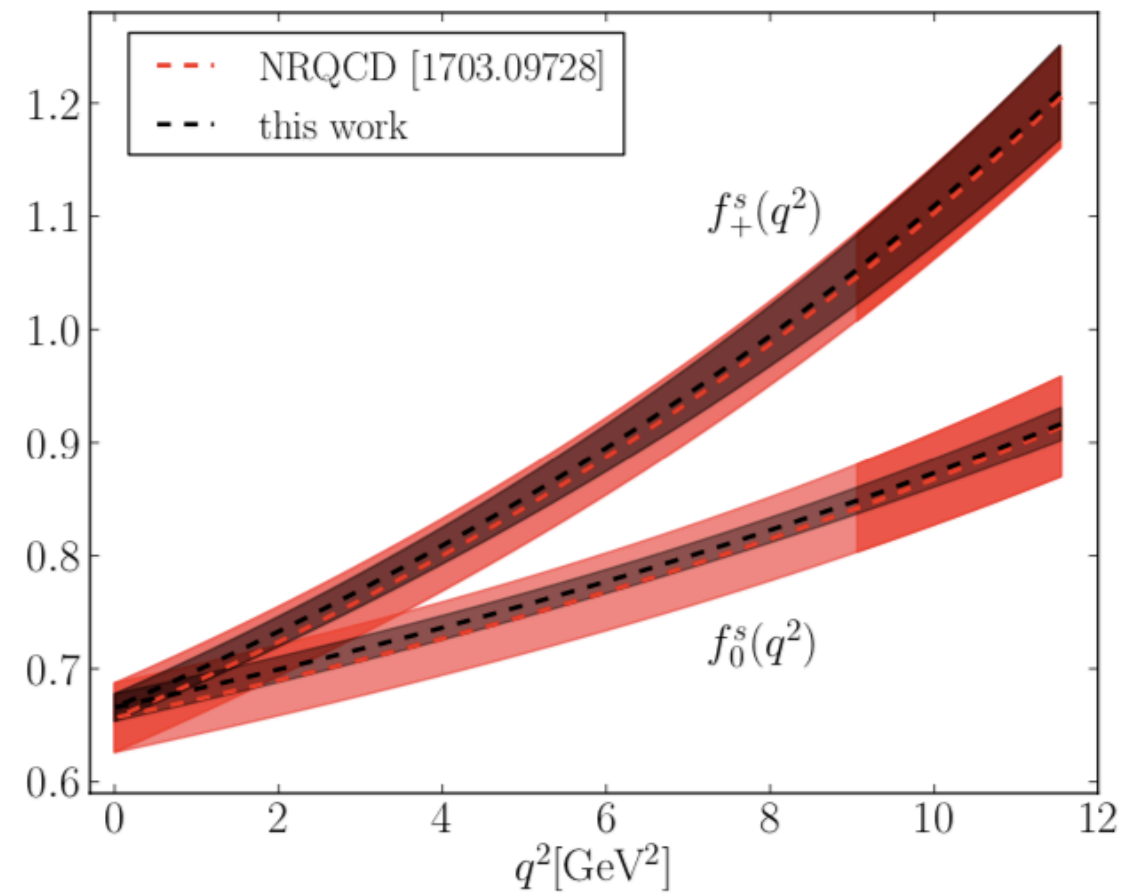
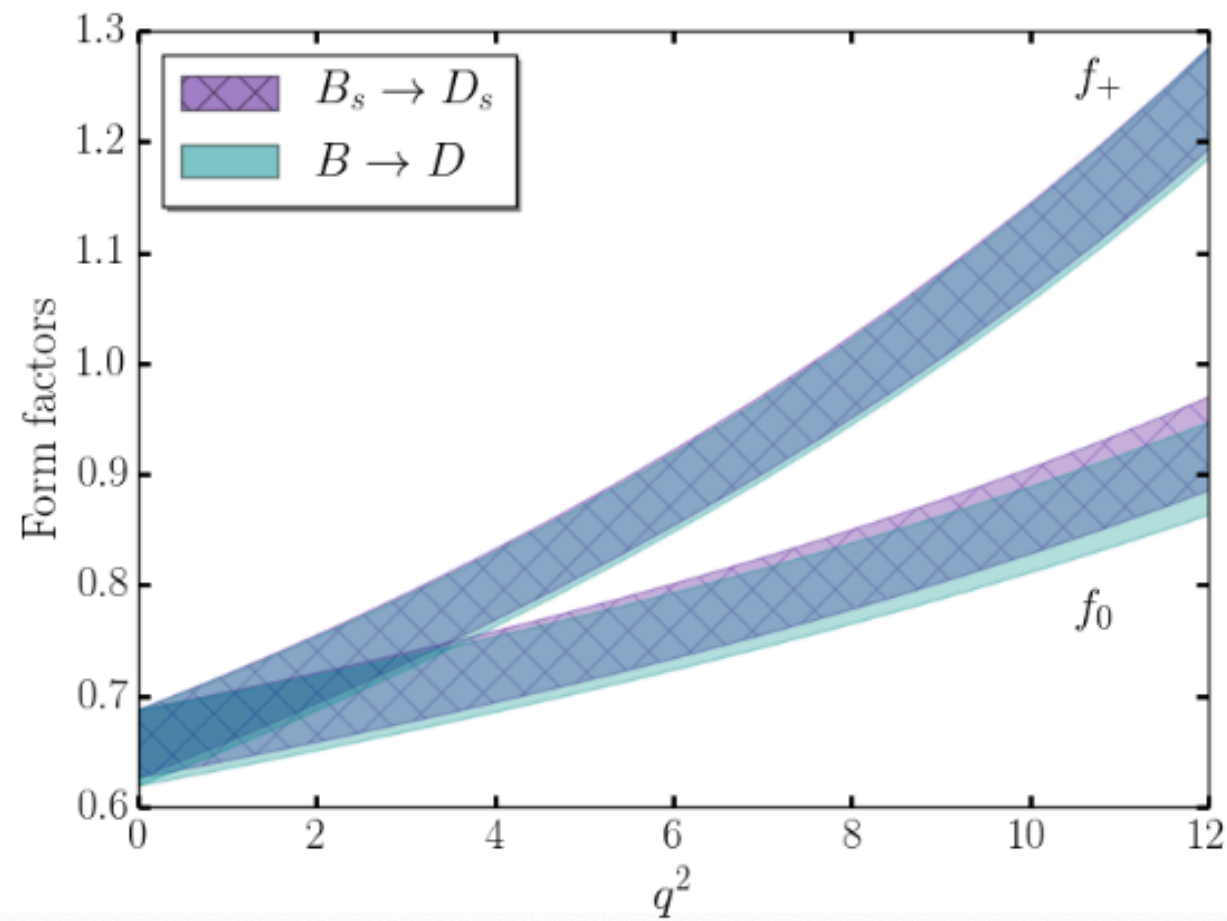
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Light spectator quark mass dependence?



$$B \rightarrow D^* \ell \bar{\nu}$$

Do we understand well $B \rightarrow D^$ at $w=1$?*

$$\mathcal{F}(1) = 0.906(4)(12) \quad (N_f = 2 + 1) \quad 1403.0635$$

$$\mathcal{F}(1) = 0.895(10)(24) \quad (N_f = 2 + 1 + 1) \quad 1711.1103$$

- The value of $\mathcal{F}(1)$ seems to be too large when comparing the exclusive and inclusive semileptonics at $w = 1$.
- As if all the other $B \rightarrow D(n)$ semileptonic modes were tiny or negligible - “oversaturation”. 1206.2296
- Since $|V_{cb}|\mathcal{F}(1)$ comes from fit with exp. data, a lower $\mathcal{F}(1)$ would lead to larger $|V_{cb}|$.
- Necessary to double check with $B \rightarrow D\ell\nu$.
- Lattice results for $\mathcal{F}(1)$ with different regularization would be highly welcome.

Side remark: Never ending problem $|V_{cb}|$

There is no canonical way/parametrization that would lead to reliable $|V_{cb}|$.

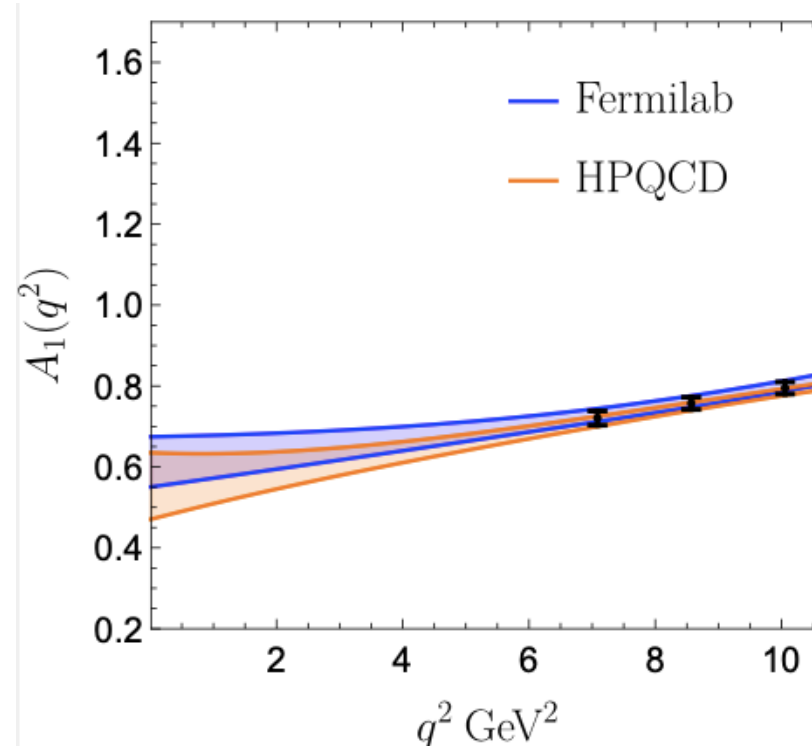
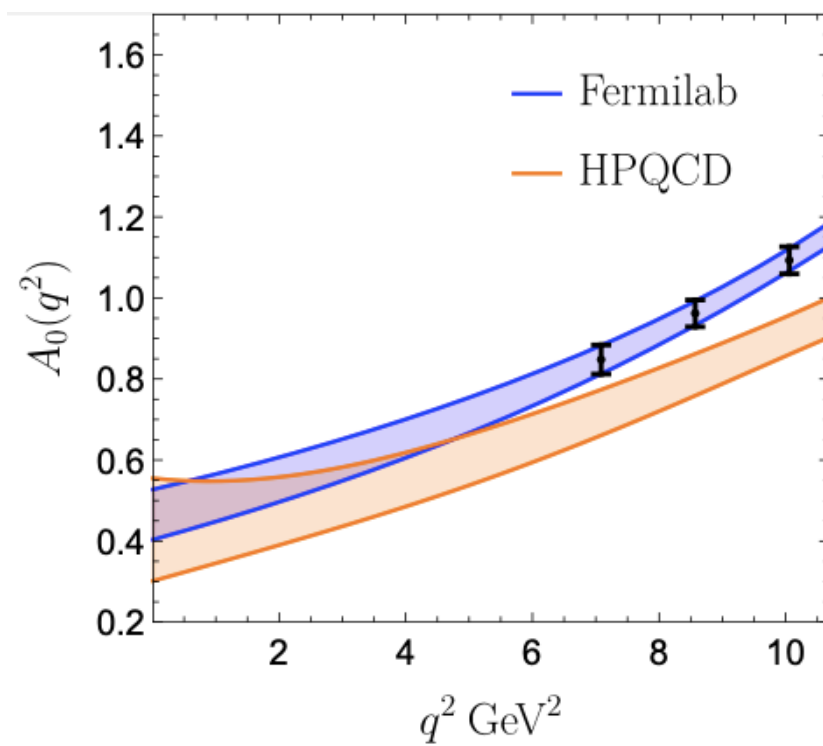
Never forget that we need dynamical QCD information! Changing variables ain't gonna do it!

At least TRY various options - and cross check!

Eg1. Can we measure the slowly varying scalar helicity amplitude? (!)

Eg2. Try this!

$$\lim_{m_\ell \rightarrow 0} \frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dq^2} \bigg|_{q^2=0} = \tau_B \frac{G_F^2 m_B^3 |V_{cb}|^2}{192\pi^3} \left(1 - \frac{m_{D^*}^2}{m_B^2}\right)^3 |A_0(0)|^2$$



2105.14019

2304.03137

Side remark: Never ending problem $|V_{cb}|$

$$\lim_{m_\ell \rightarrow 0} \left. \frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dq^2} \right|_{q^2=0} = \tau_B \frac{G_F^2 m_B^3 |V_{cb}|^2}{192\pi^3} \left(1 - \frac{m_{D^*}^2}{m_B^2}\right)^3 |A_0(0)|^2$$

$$0.44(12)^{\text{HPQCD-23}}$$

- $A_0(0) = 0.47(6)^{\text{FNAL}}, 0.61(6)^{\text{HPQCD}}, 0.78(23)^{\text{“LCSR”}}$

0809.0222

- Use HFLAV results with e.g. CLN: $R_2(1) = 0.853(17) \Rightarrow R_2(w_{\text{max}})$

2206.07501

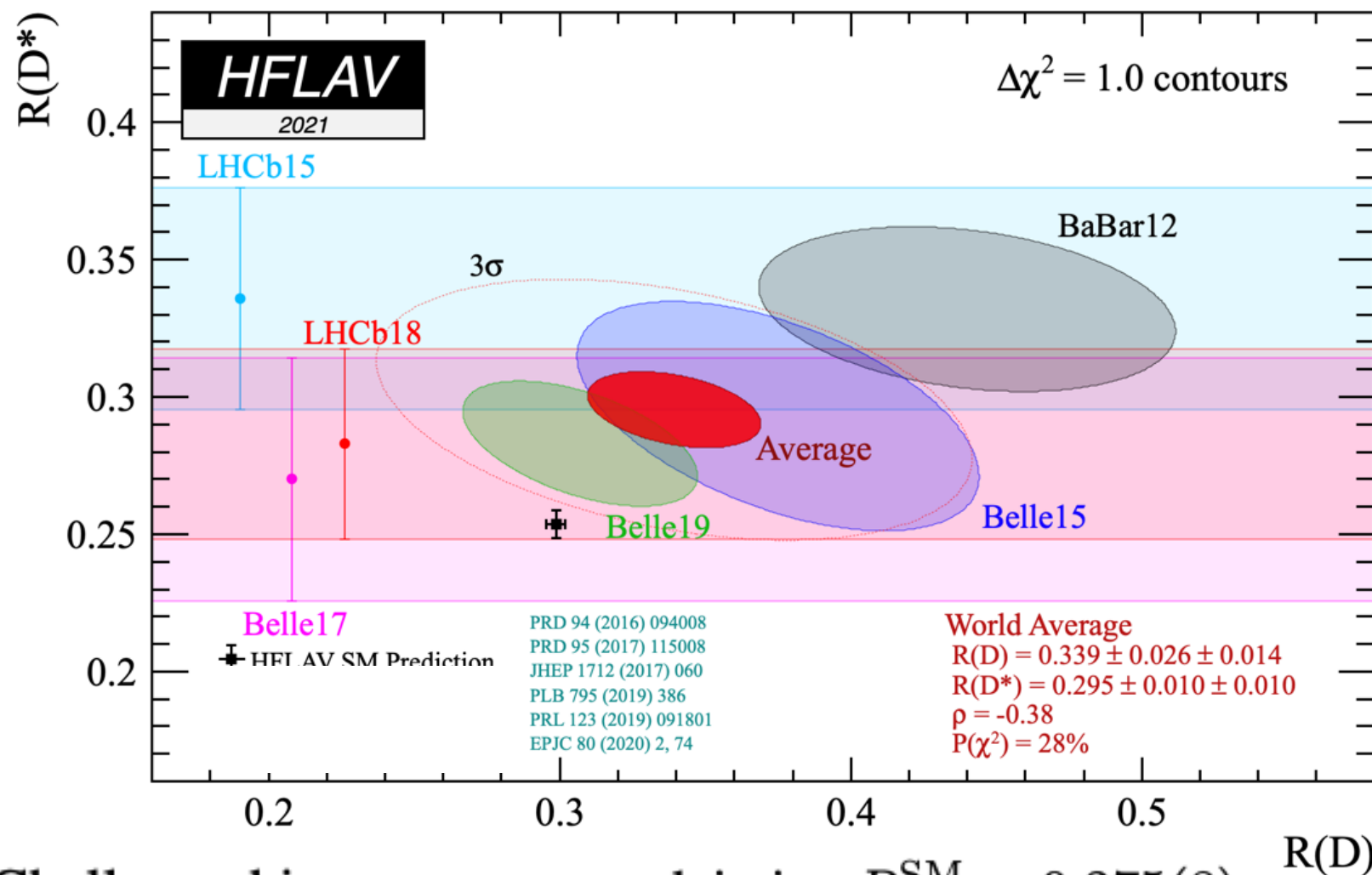
$$\left. \frac{A_0(0)}{A_1(0)} \right|_{\text{HFLAV}}^{\text{CLN}} = 1.087(14) \rightarrow A_0(0) = 0.66(7)^{\text{FNAL}}, 0.63(8)^{\text{HPQCD}}, 0.79(22)^{\text{“LCSR”}}$$

- Use measured $\mathcal{B}(B \rightarrow D\pi^\pm)$ and $\mathcal{B}(B \rightarrow D^*\pi^\pm)$ to either check whether or not $a_1^{D\pi} = a_1^{D^*\pi}$ or to extract $A_0(m_\pi^2)/f_0(m_\pi^2)$
More in the paper to come.

Hint of LFUV ['scare' or 'joy'] possibility to study NP effects

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})_{\ell \in (e, \mu)}} \quad \& \quad R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}}$$

$$R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}} \Rightarrow \Lambda_{\text{NP}} \lesssim 3 \text{ TeV}$$



LHCb

- $B_c \rightarrow J/\psi \ell \bar{\nu}$

$$R_{J/\psi}^{\text{exp}} > R_{J/\psi}^{\text{SM}}$$

- $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

$$R_{\Lambda_c}^{\text{exp}} \approx R_{\Lambda_c}^{\text{SM}}$$

NEW and can be improved... a lot

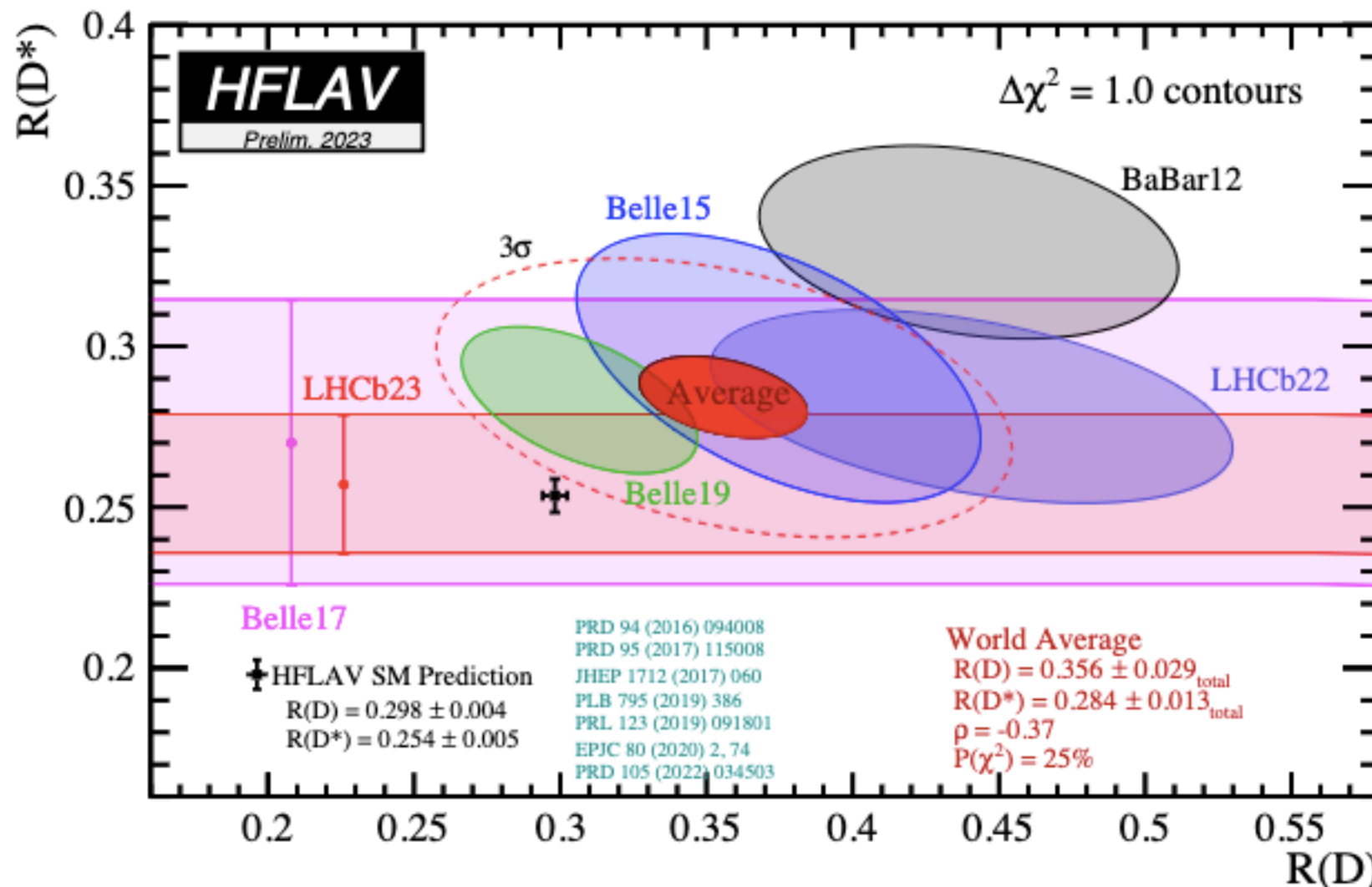
2201.03497

Challenged in 2109.15248 claiming $R_{D^*}^{\text{SM}} = 0.275(8)$

Hint of LFUV ['scare' or 'joy'] possibility to study NP effects

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})_{\ell \in (e, \mu)}} \quad \& \quad R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}}$$

2302.02886



LHCb

- $B_c \rightarrow J/\psi \ell \bar{\nu}$

$$R_{J/\psi}^{\text{exp}} > R_{J/\psi}^{\text{SM}}$$

- $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

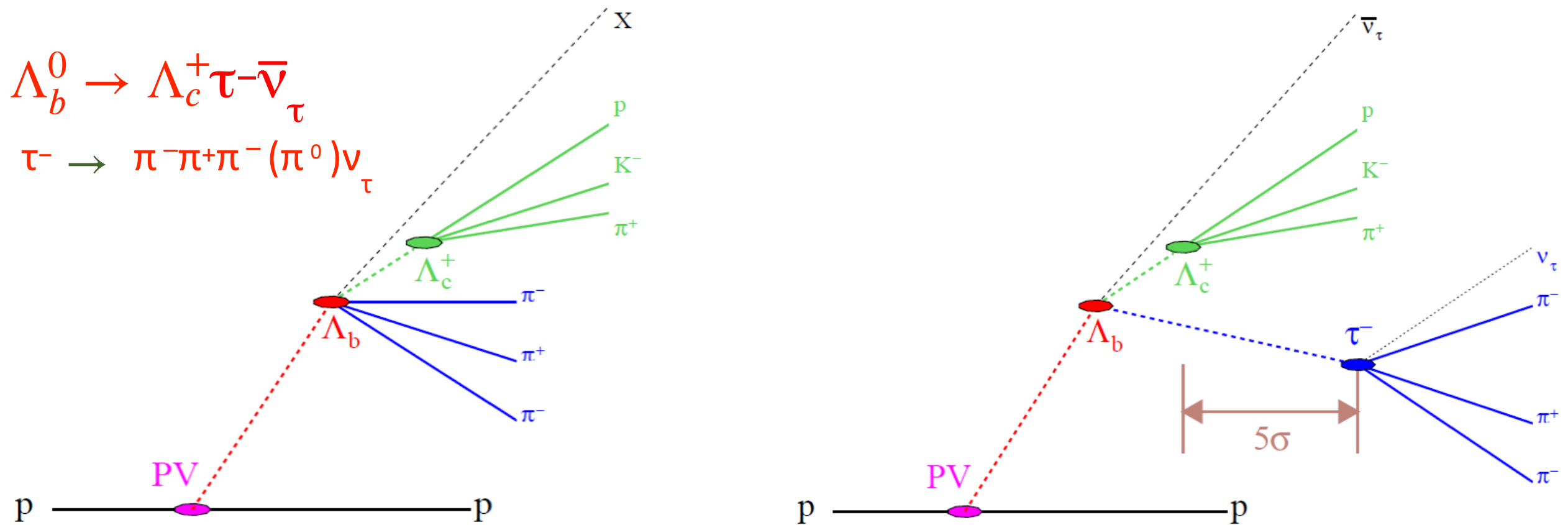
$$R_{\Lambda_c}^{\text{exp}} \approx R_{\Lambda_c}^{\text{SM}}$$

NEW and can be improved... a lot

2201.03497

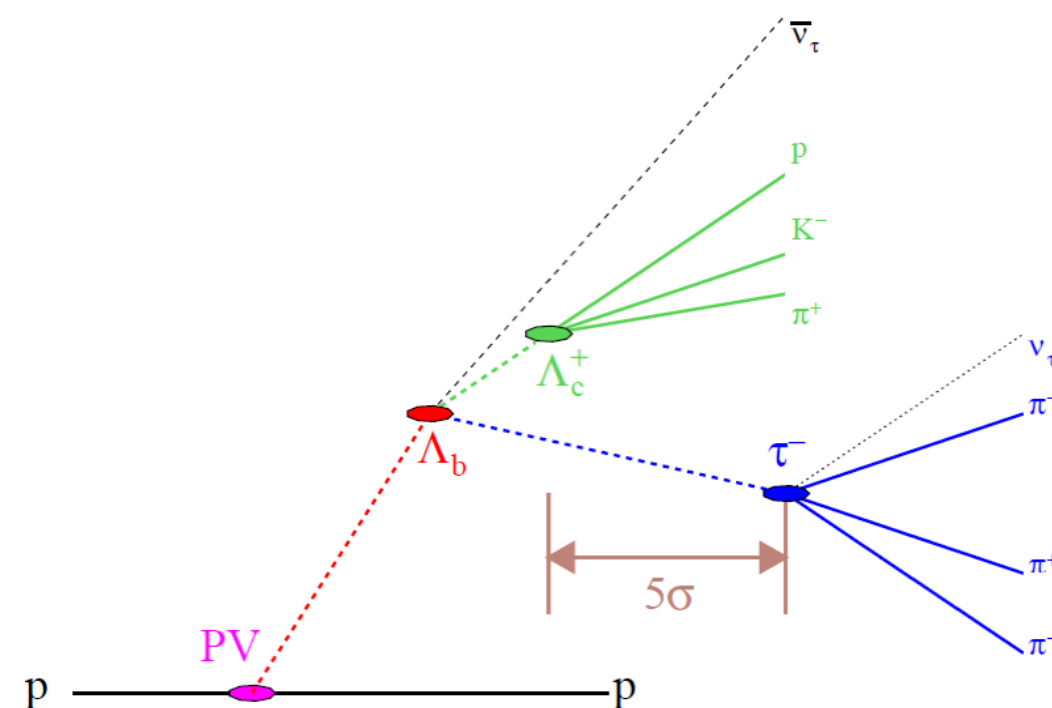
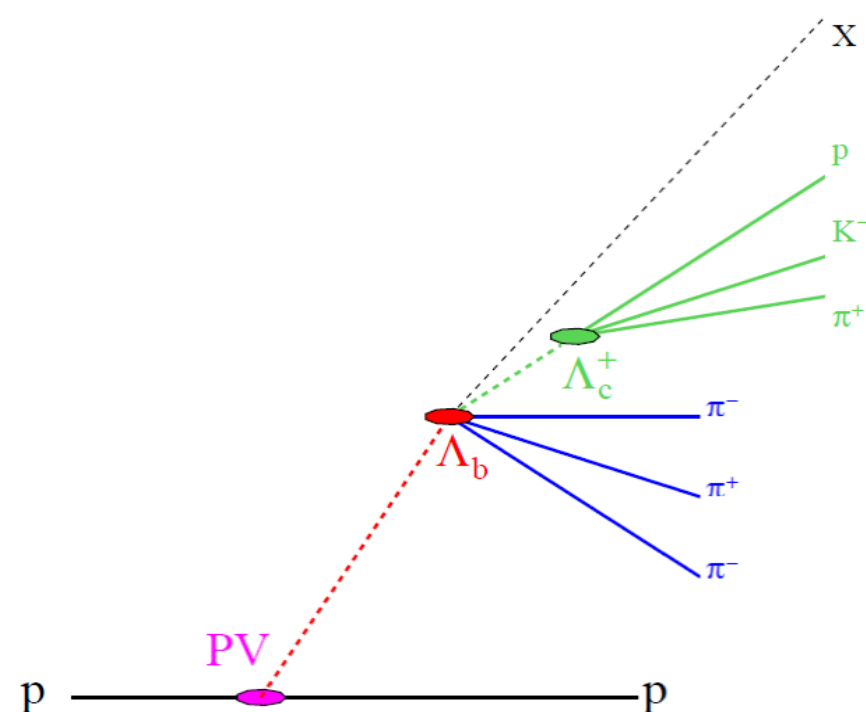
A comment on R_{Λ_c}

2201.03497



$$K_{\Lambda_c} = \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^- \pi^+ \pi^-)} = 2.46(27)(40)$$

A comment on R_{Λ_c}



$$K_{\Lambda_c} = \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^- \pi^+ \pi^-)} = 2.46(27)(40)$$

20%

 $\Gamma(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^+ \pi^- \pi^-) / \Gamma_{\text{total}}$
 Γ_{35}/Γ

VALUE (10^{-3}) 14%

EVTS

DOCUMENT ID

TECN

COMMENT

 7.6 ± 1.1 **OUR FIT** Error includes scale factor of 1.1. $14.8^{+3.8}_{-3.1} \pm 1.1$ ¹ AALTONEN

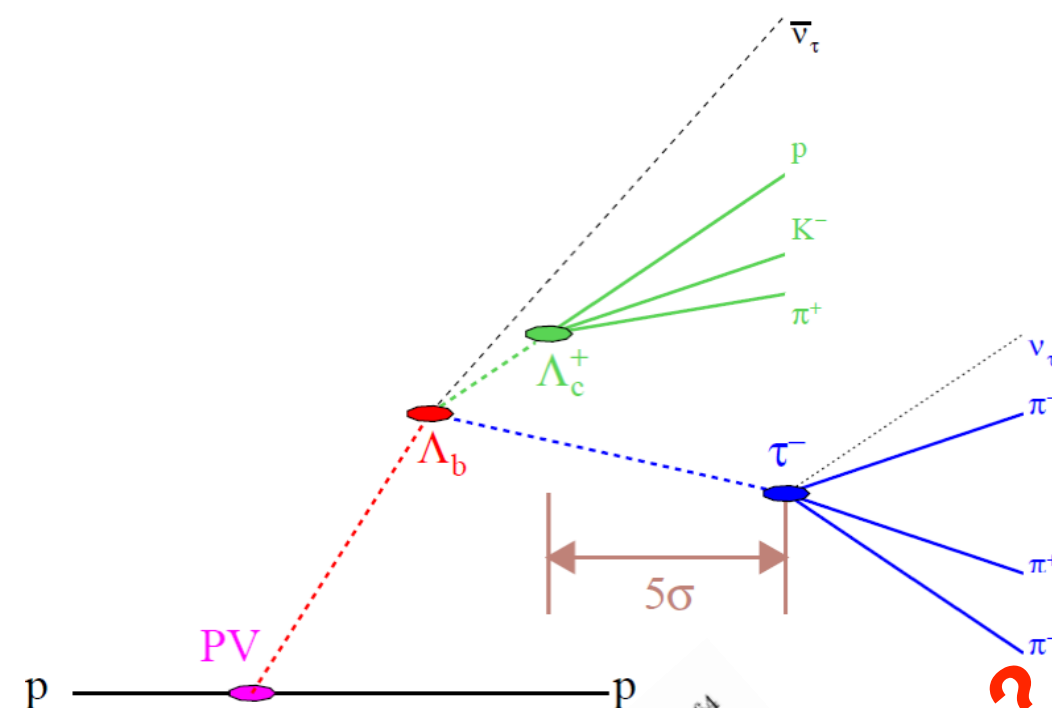
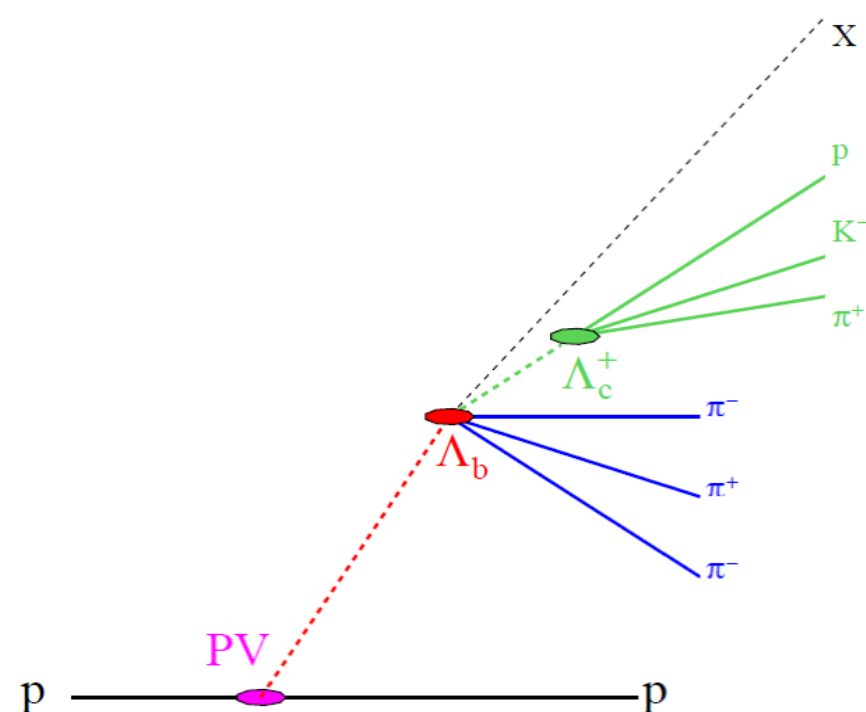
2012A

CDF

 $p\bar{p}$ at 1.96 TeV

• • We do not use the following data for averages, fits, limits, etc. • •

A comment on R_{Λ_c}



$$K_{\Lambda_c} = \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^- \pi^+ \pi^-)} = 2.46(27)(40)_{20\%}$$

CERN-EP-2017-164
LHCb-PAPER-2017-016
January 25, 2018

$\Gamma(\Lambda_b^0 \rightarrow \Lambda_c^+ \ell^- \bar{\nu}_\ell) / \Gamma_{\text{total}}$

VALUE **22%**

DOCUMENT ID

TECN

CC

0.062^{+0.014}_{-0.013} OUR FIT

0.050^{+0.011}_{-0.008} ^{+0.016}_{-0.012}

¹ ABDALLAH

2004A

DLPH

$e^+ e^- \rightarrow Z$

¹ Derived from a combined likelihood and event rate fit to the distribution of the Isgur-Wise variable and using HQET. The form factor is measured to be $\rho^2 = 2.03 \pm 0.46$ ^{+0.72}_{-1.00}.

Why not working with 1709.01920?

Measurement of the shape of the $\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu$ differential decay rate

The LHCb collaboration

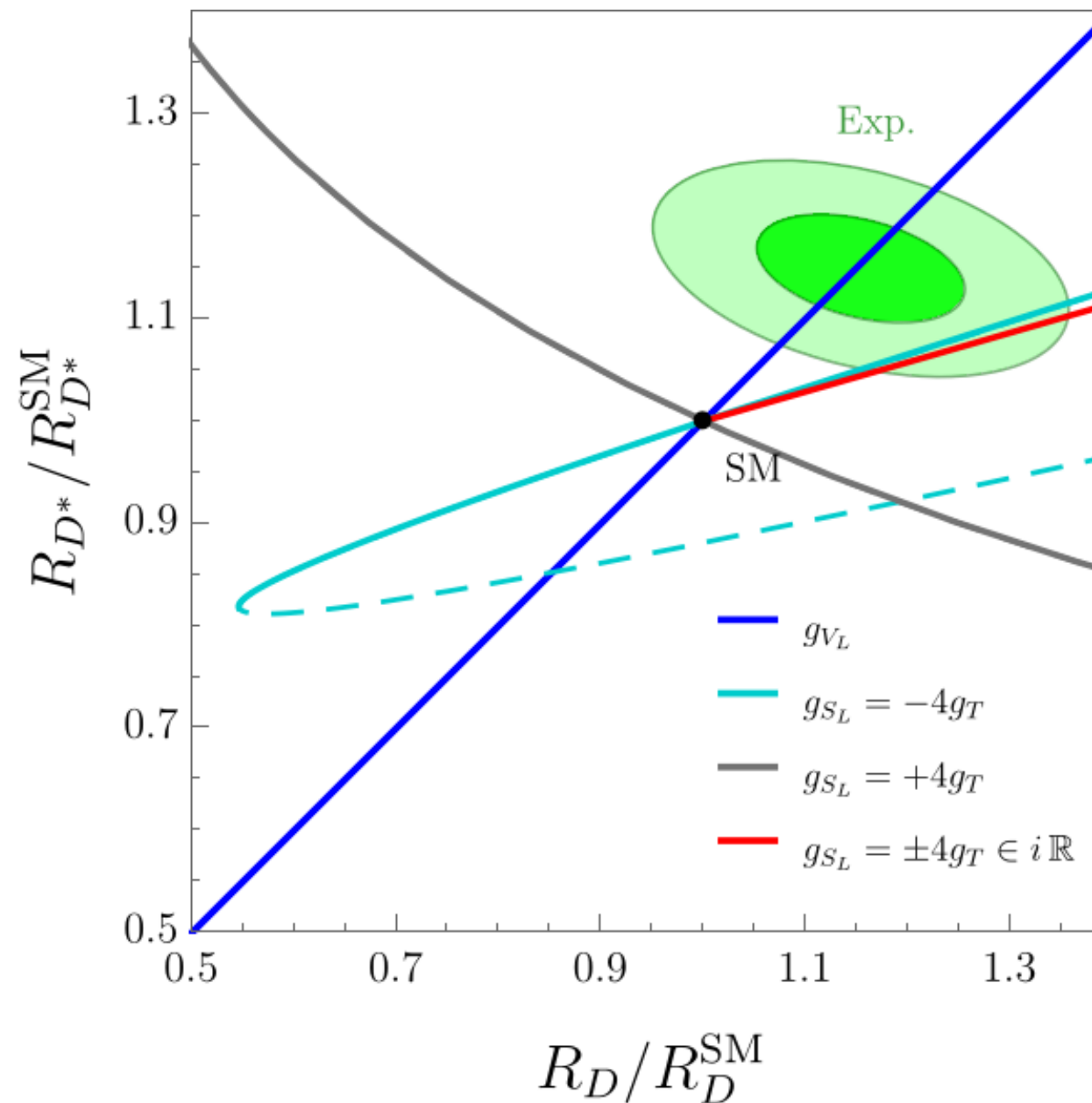
Abstract
Differential decay rate and
is reported, using
on-proton

EFT - exclusive $b \rightarrow c \ell \nu$

$$\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F V_{cb} \left[(1 + g_{V_L})(\bar{c}_L \gamma_\mu b_L)(\bar{\ell}_L \gamma^\mu \nu_L) + g_{V_R}(\bar{c}_R \gamma_\mu b_R)(\bar{\ell}_L \gamma^\mu \nu_L) \right. \\ \left. + g_{S_R}(\bar{c}_L b_R)(\bar{\ell}_R \nu_L) + g_{S_L}(\bar{c}_R b_L)(\bar{\ell}_R \nu_L) + g_T(\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\ell}_R \sigma^{\mu\nu} \nu_L) \right] + \text{h.c.}$$

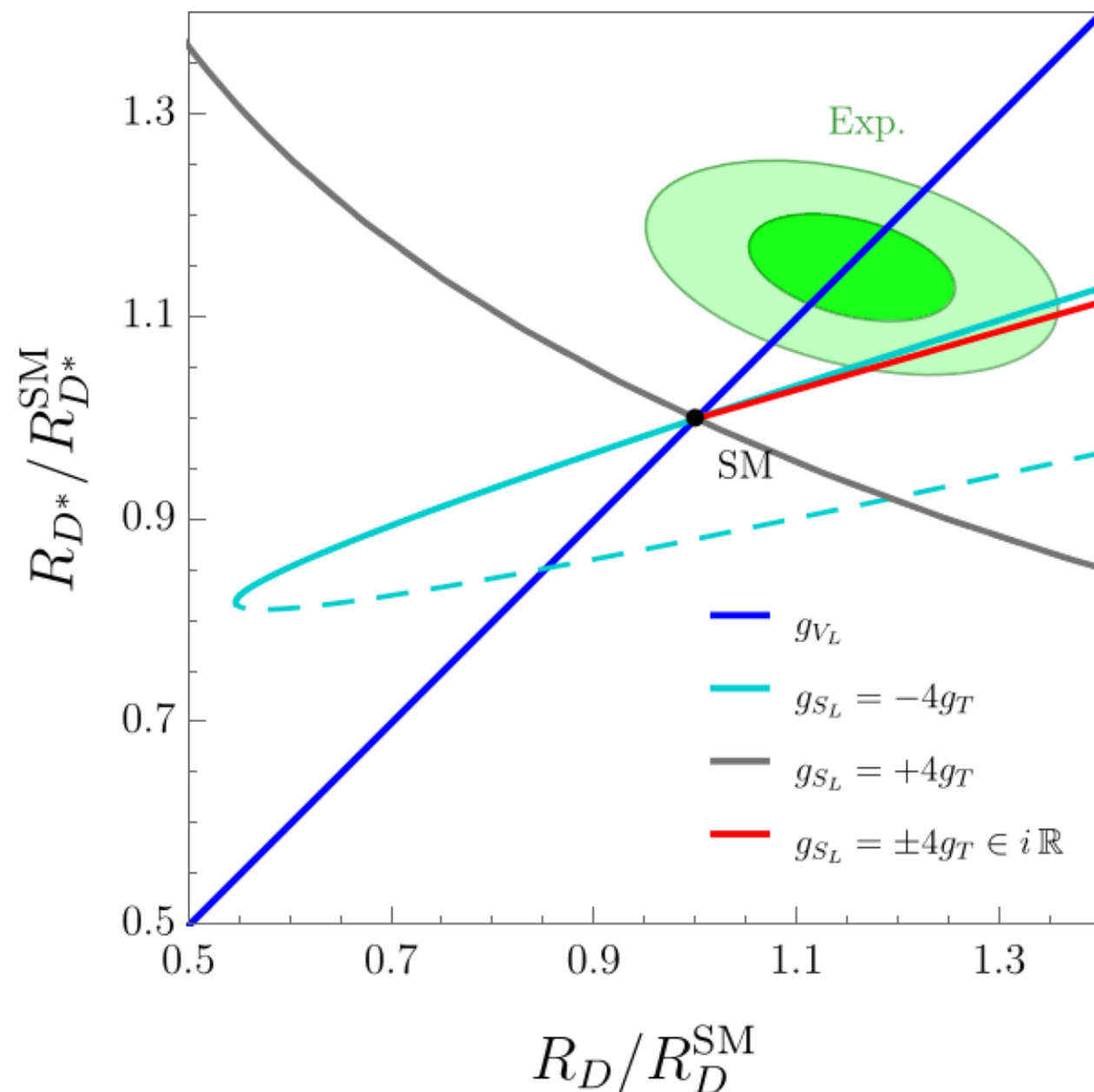
EFT - exclusive $b \rightarrow c \ell \nu$

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EFT - exclusive $b \rightarrow c \ell \nu$

$$\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F V_{cb} \left[(1 + g_{V_L})(\bar{c}_L \gamma_\mu b_L)(\bar{\ell}_L \gamma^\mu \nu_L) + g_{V_R}(\bar{c}_R \gamma_\mu b_R)(\bar{\ell}_L \gamma^\mu \nu_L) \right. \\ \left. + g_{S_R}(\bar{c}_L b_R)(\bar{\ell}_R \nu_L) + g_{S_L}(\bar{c}_R b_L)(\bar{\ell}_R \nu_L) + g_T(\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\ell}_R \sigma^{\mu\nu} \nu_L) \right] + \text{h.c.}$$



Need better data and more observables to discriminate among various possibilities.

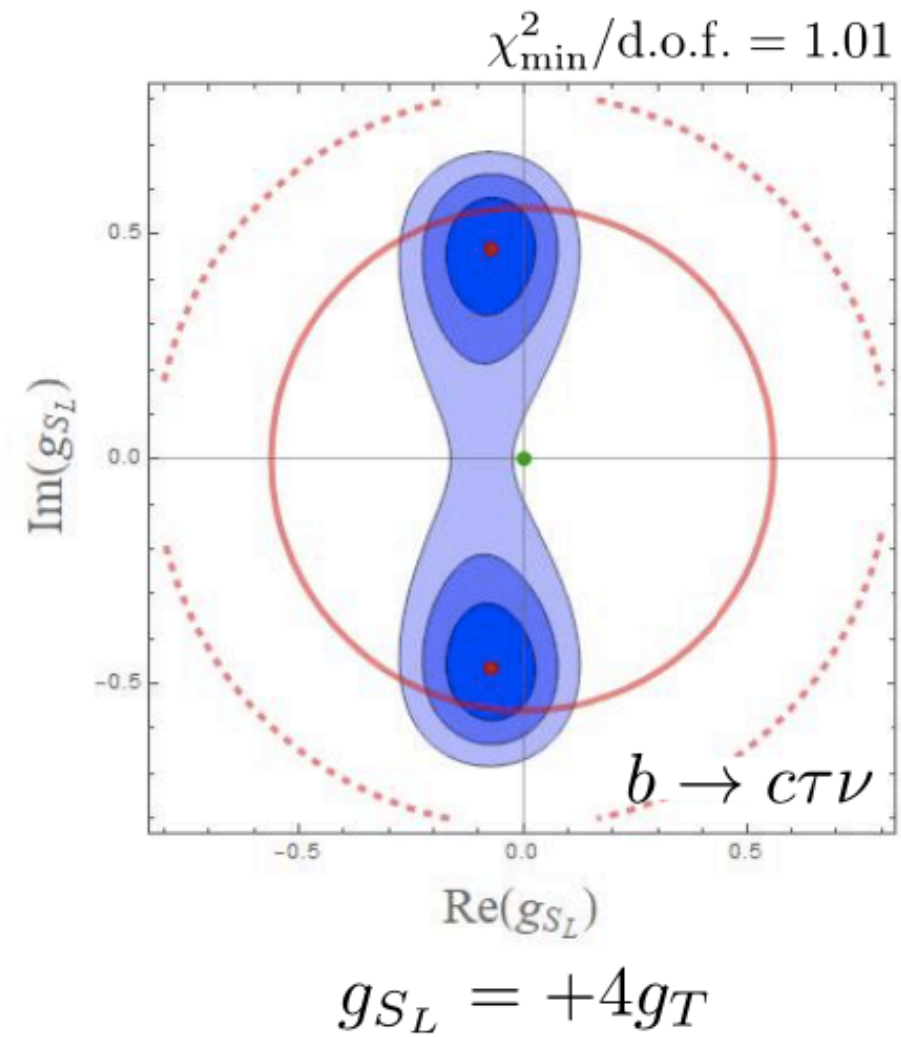
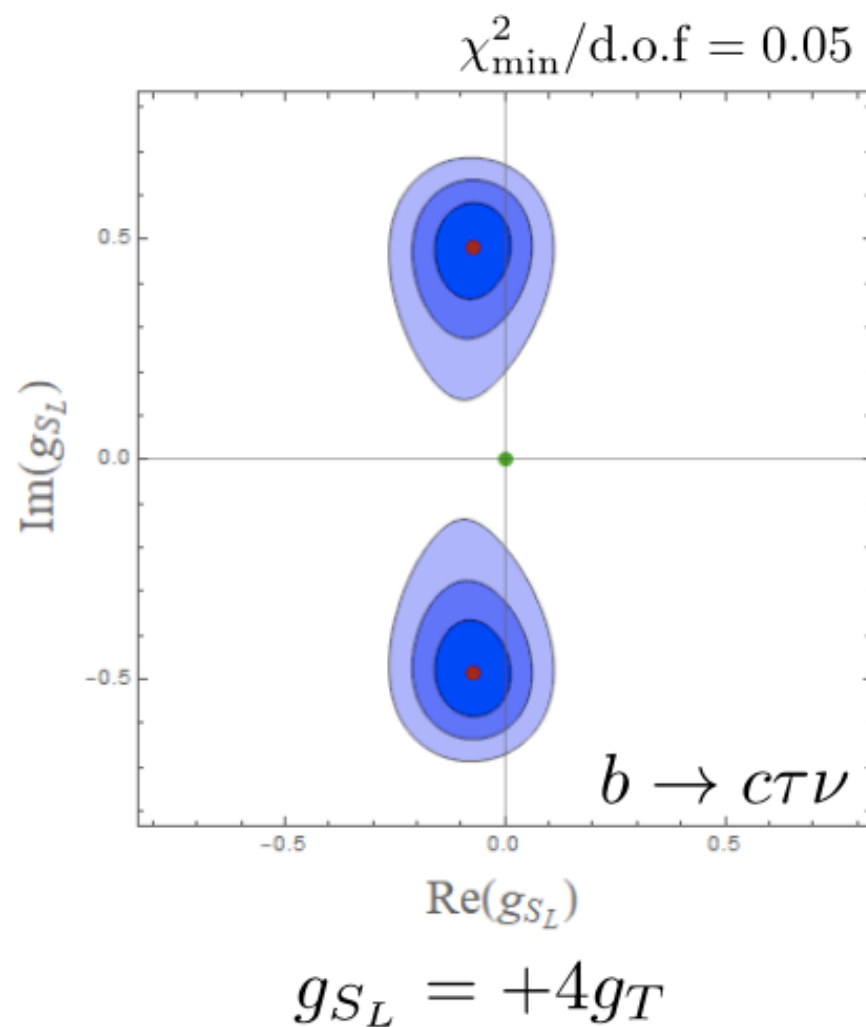
Dream goal is to confidently & simultaneously determine all NP cplgs from fit with the data.

Angular distributions can help!

vast literature...

Impact of R_{Λ_c}

Wilson Coefficient	$R(D)$ and $R(D^*)$	$R(\Lambda_c)$	Combined	$\chi^2_{\min}/\text{d.o.f}$
g_{V_L}	0.084 ± 0.029	-0.15 ± 0.14	0.077 ± 0.035	$0.06 \rightarrow 1.3$
g_{S_L}	-1.47 ± 0.08	-0.53 ± 0.54	-1.45 ± 0.11	$0.5 \rightarrow 2.1$
g_T	-0.027 ± 0.011	0.13 ± 0.14	-0.026 ± 0.013	$1.2 \rightarrow 1.7$
$g_{S_L} = +4g_T \in i\mathbb{R}$	$\pm 0.49 \pm 0.10$	0.0 ± 0.39	$\pm 0.47 \pm 0.13$	$0.9 \rightarrow 1.6$
$g_{S_L} = -4g_T$	0.16 ± 0.06	0.0 ± 0.39	0.15 ± 0.07	$0.7 \rightarrow 1.0$



We still do not have a full/good control over hadronic uncertainties

Mode	$B \rightarrow D\ell\bar{\nu}$	$B \rightarrow D^*\ell\bar{\nu}$	$\Lambda_b \rightarrow \Lambda_c\ell\bar{\nu}$
$\langle V_\mu \rangle$	2 ✓	1 ✓	3 ✓
$\langle A_\mu \rangle$		3 ✓	3 ✓
$\langle T_{\mu\nu} \rangle$	1 ✗	3 ✓	4 ✓

1503.07237

1505.03925

2105.14019

2304.03137

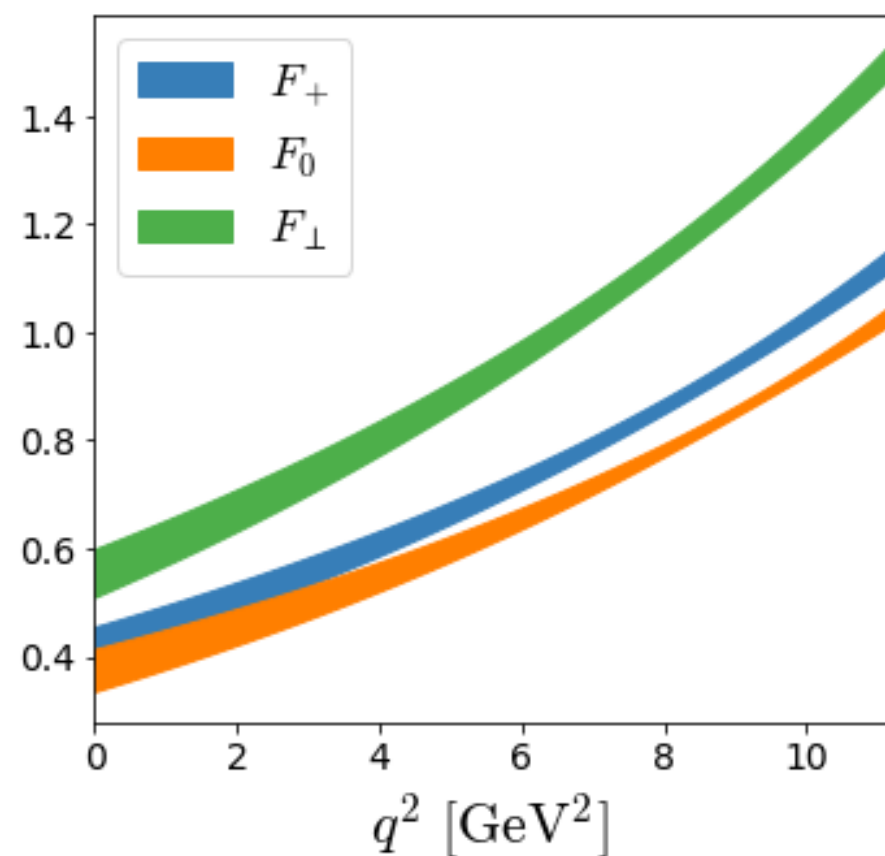
1503.01421

1702.02243

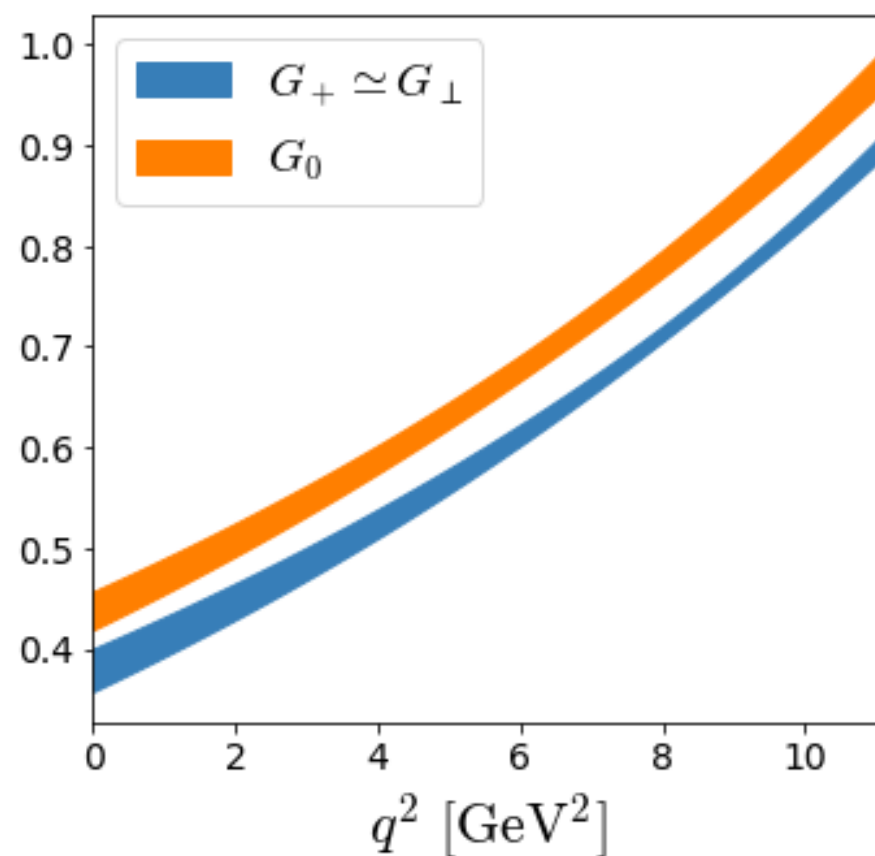
$$\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$$

Form factors

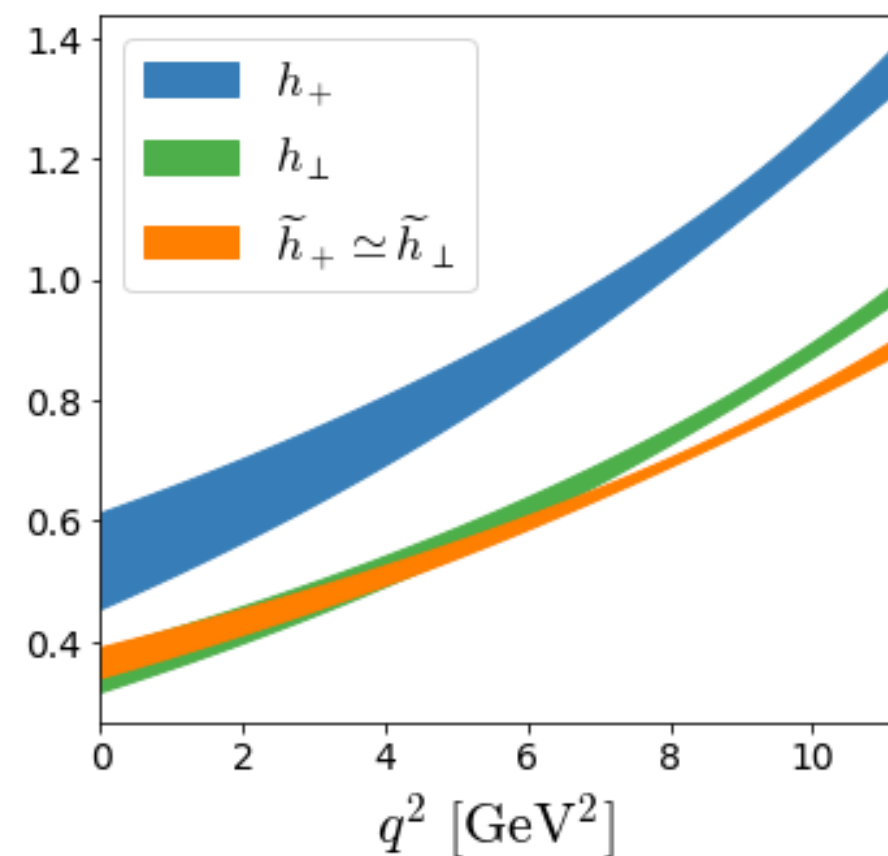
$$\langle \Lambda_c | \bar{c} \gamma_\mu b | \Lambda_b \rangle$$



$$\langle \Lambda_c | \bar{c} \gamma_\mu \gamma_5 b | \Lambda_b \rangle$$



$$\langle \Lambda_c | \bar{c} \sigma_{\mu\nu} b | \Lambda_b \rangle$$



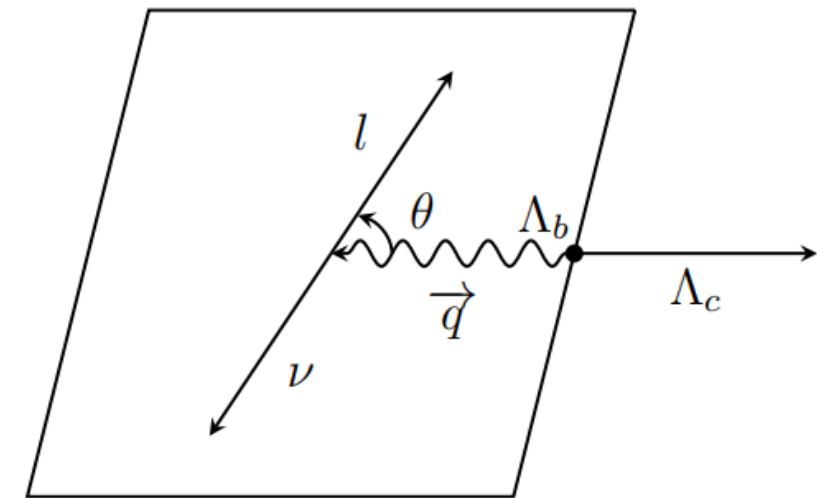
1503.01421

1702.02243

Keep in mind: Less than a half of available q^2 's computed on the lattice. Otherwise “z-parametrization”.

Angular observables can help disentangling among various NP scenarios

Many works with mesons: $\mathbf{B} \rightarrow \mathbf{D}\ell\bar{\nu}$ $\mathbf{B} \rightarrow \mathbf{D}^*\ell\bar{\nu}$



Let us now play with baryons:

$$\frac{d^2\Gamma}{dq^2 d\cos\theta} = \frac{\sqrt{\lambda_{\Lambda_b\Lambda_c}(q^2)}}{1024\pi^3 M_{\Lambda_b}^3} \left(1 - \frac{m_l^2}{q^2}\right) \sum_{\lambda_l \lambda_b \lambda_c} \left| \mathcal{M}_{\lambda_c}^{(3)\lambda_b\lambda_l} \right|^2$$

$$\frac{d^2\Gamma(\Lambda_b \rightarrow \Lambda_c^{\lambda_c} \ell^{\lambda_l} \nu)}{dq^2 d\cos\theta} = a_{\lambda_c}^{\lambda_l}(q^2) + b_{\lambda_c}^{\lambda_l}(q^2)\cos\theta + c_{\lambda_c}^{\lambda_l}(q^2)\cos^2\theta$$

Each $a_{\lambda_c}^{\lambda_l}(q^2)$, $b_{\lambda_c}^{\lambda_l}(q^2)$, $c_{\lambda_c}^{\lambda_l}(q^2)$ is a function of kinematics, form factors and the NP couplings g_{V_L} , g_{S_L} , g_{S_R} , g_T .

12-2=10 observables

Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

1907.12554 1908.02328 1909.10769 1702.02243 1502.04864 2209.13409

Three powerful observables:

$$\circ \quad \mathcal{A}_{\text{fb}}(q^2) = \frac{1}{\Gamma} \left[\int_0^1 - \int_{-1}^0 \right] \frac{d\Gamma}{d \cos \theta} d \cos \theta$$

$$\circ \quad \mathcal{A}_{\pi/3}(q^2) = \frac{1}{\Gamma} \left[\int_0^{\pi/3} + \int_{2\pi/3}^{\pi} - \int_{\pi/3}^{2\pi/3} \right] \frac{d\Gamma}{d \cos \theta} \sin \theta d\theta$$

$$\circ \quad \mathcal{A}_{\lambda}(q^2) = \frac{1}{\Gamma} \left[\frac{d\Gamma^+}{dq^2} - \frac{d\Gamma^-}{dq^2} \right]$$

Examples:

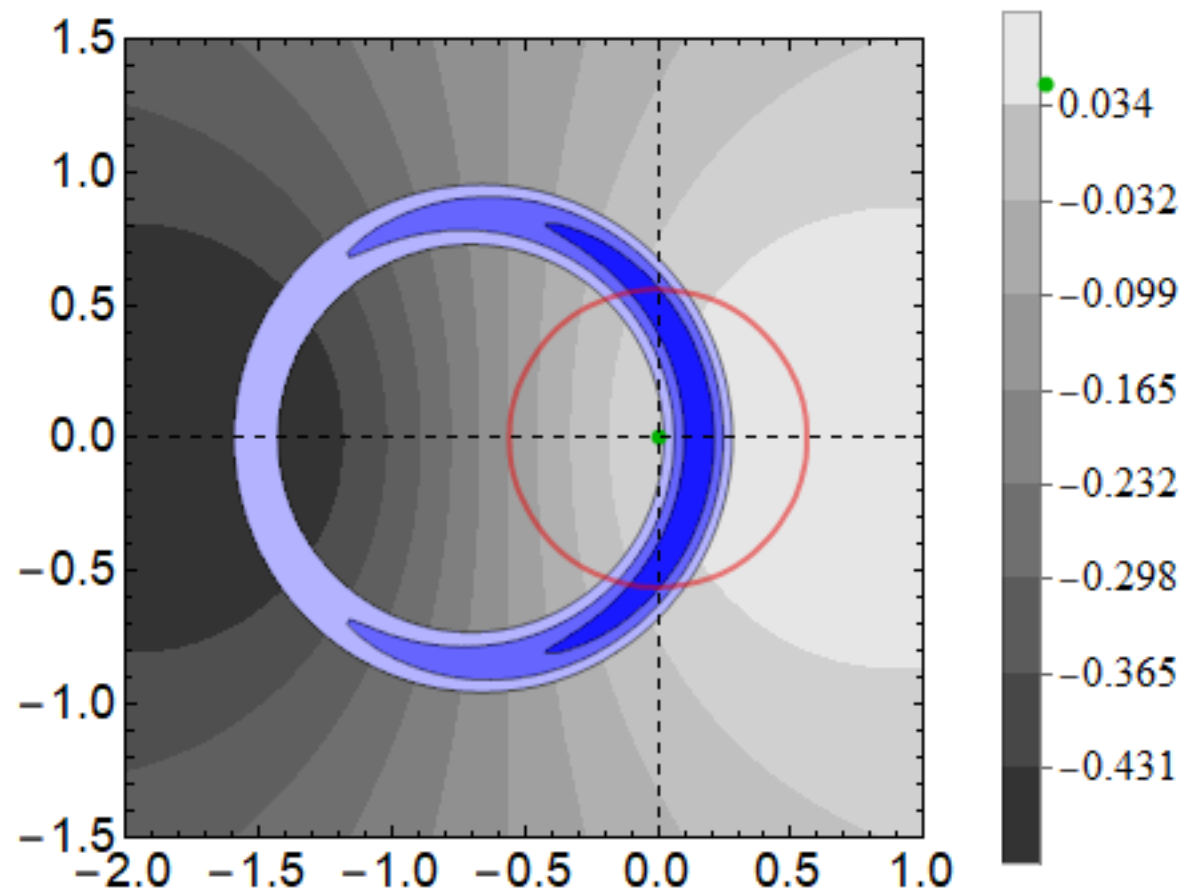
$$U_1 : g_{V_L} \quad R_2 : g_{S_L} = 4 g_T \quad S_1 : g_{S_L} = -4 g_T$$

Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

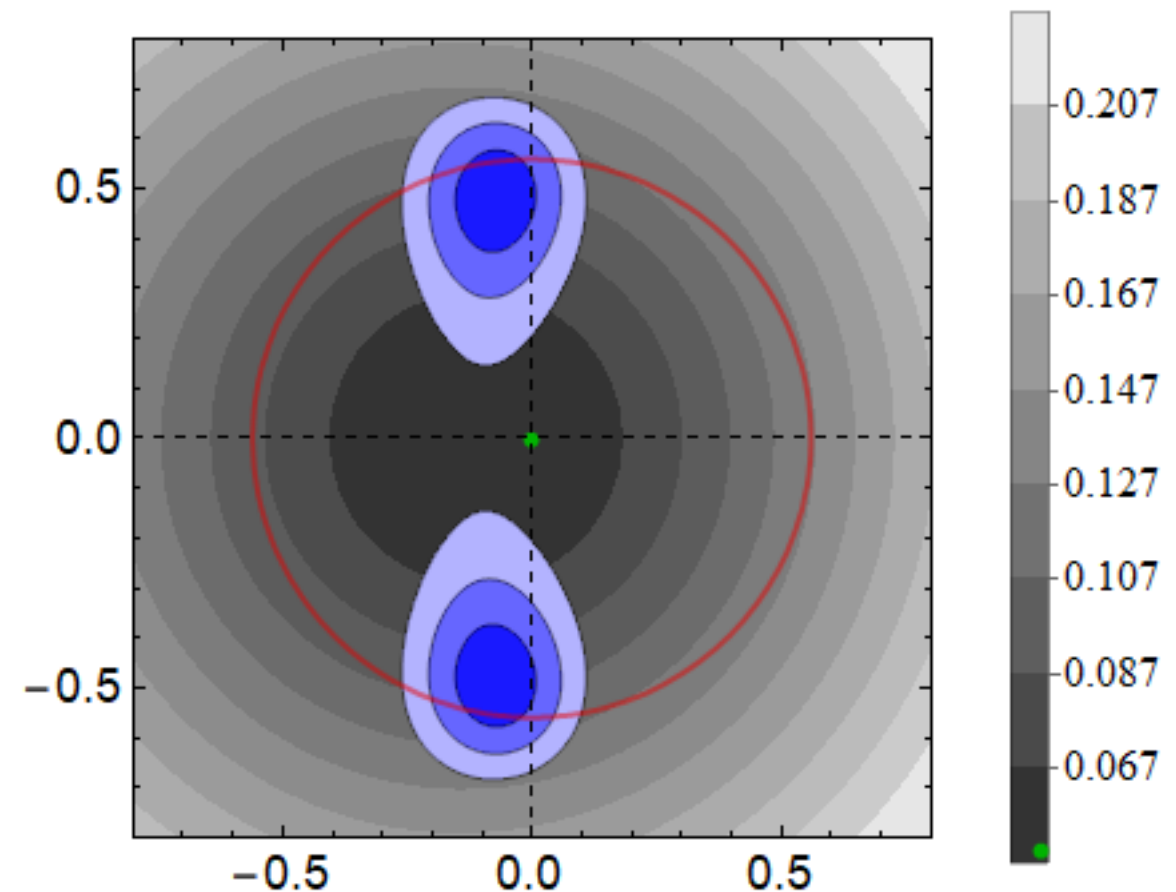
2209.13409

(At least) Three powerful observables:

$$\langle \mathcal{A}_{\text{fb}}^\tau \rangle$$



S_1



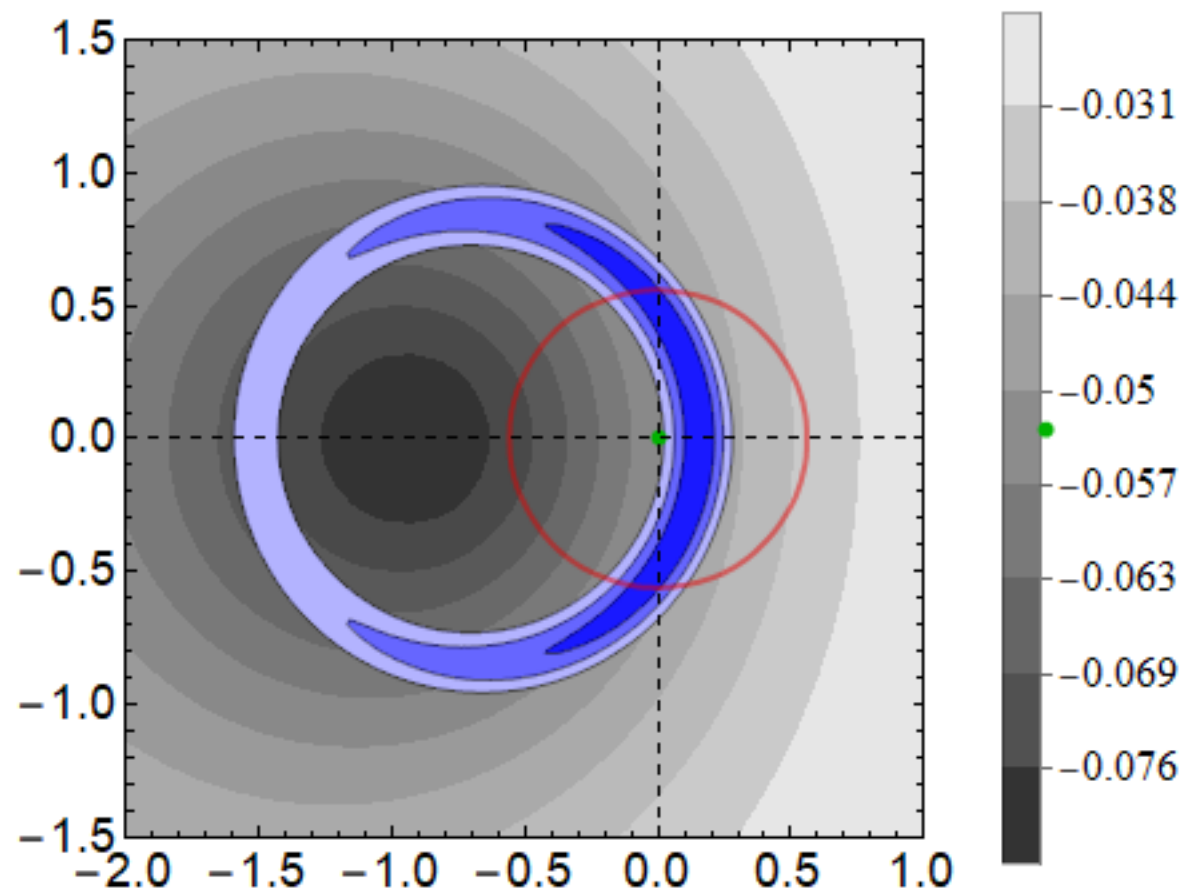
R_2

Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

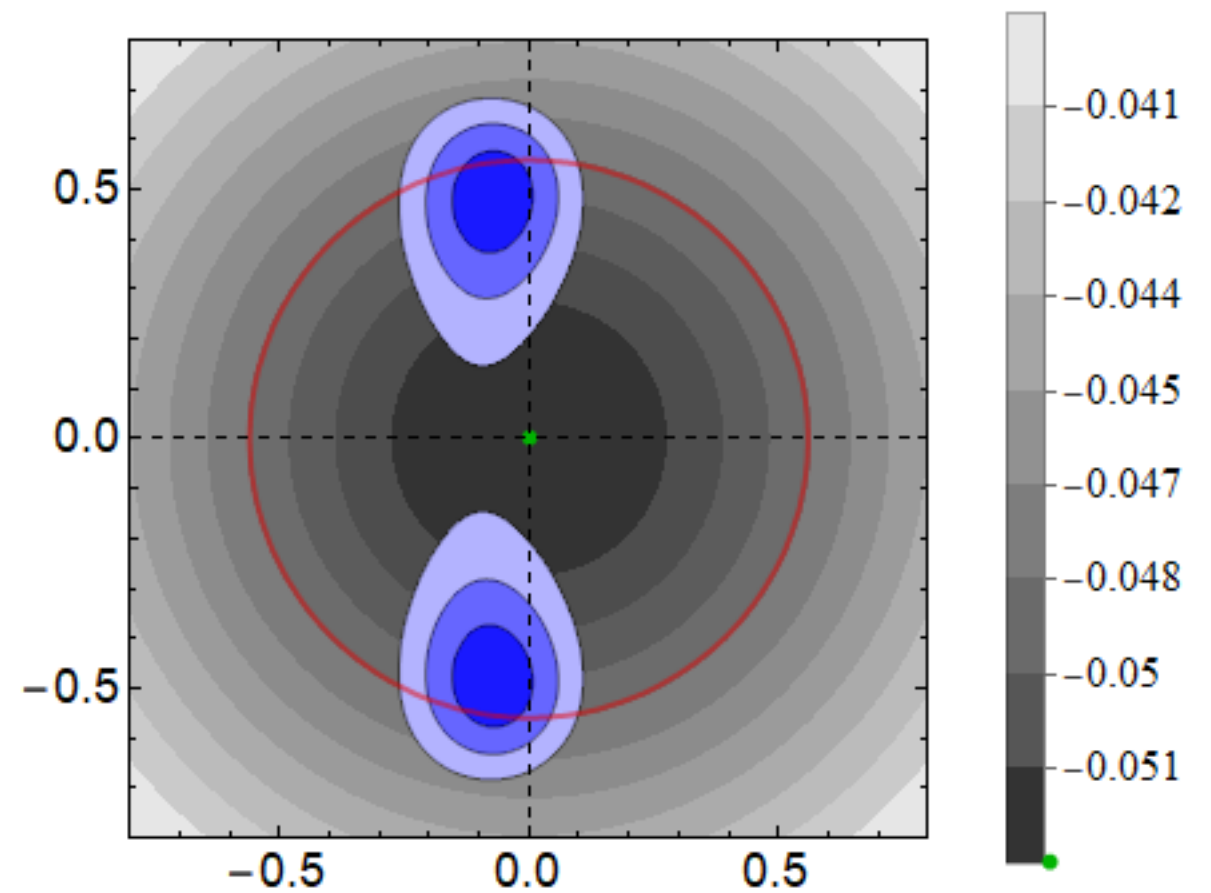
2209.13409

Three powerful observables:

$$\langle \mathcal{A}_{\pi/3}^\tau \rangle :$$



S_1



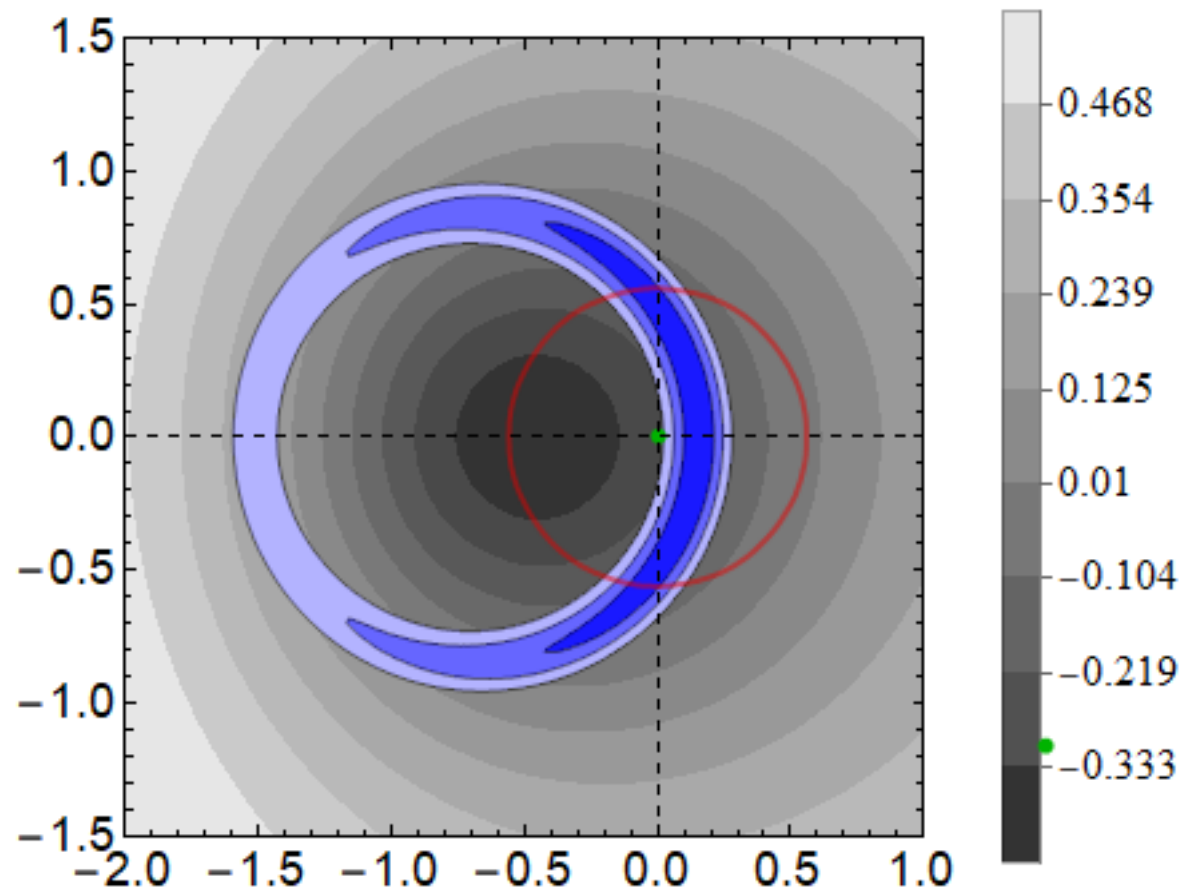
R_2

Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

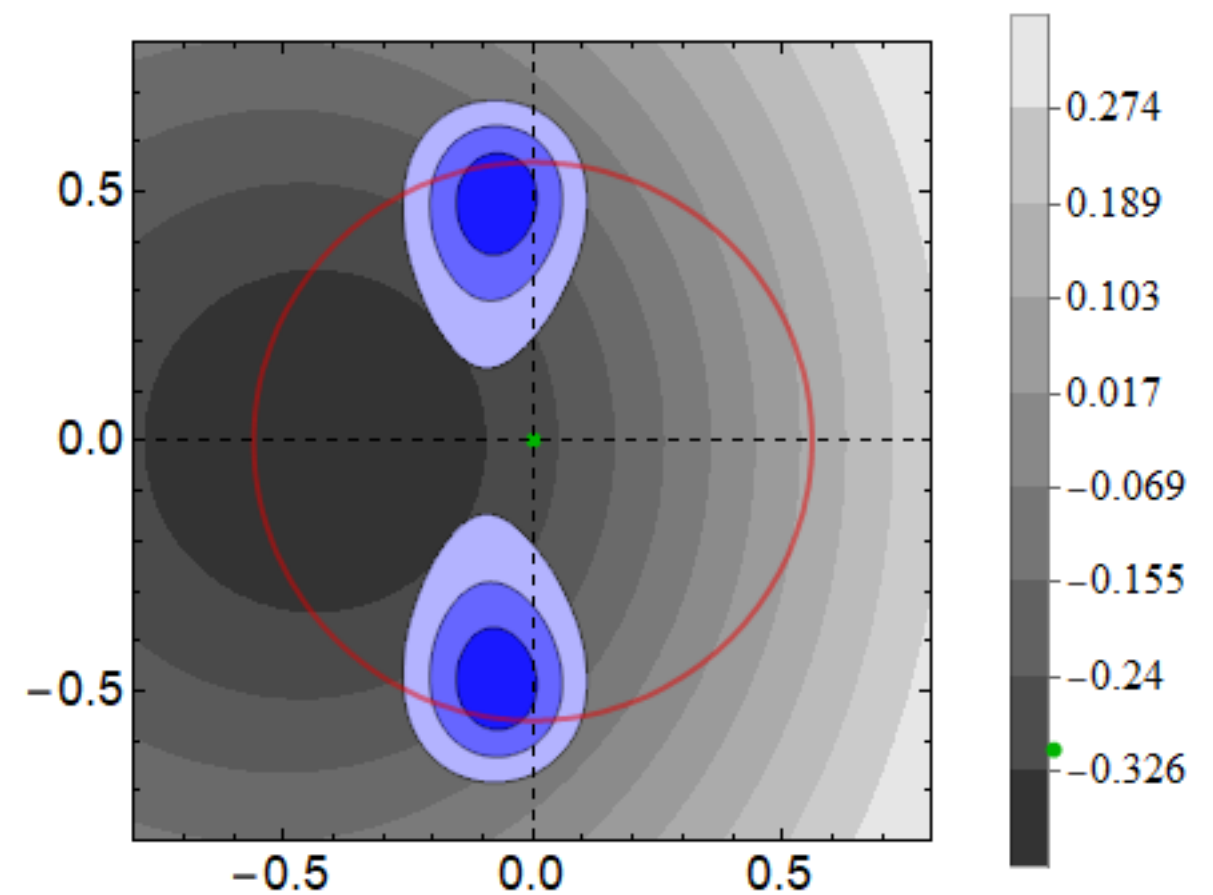
2209.13409

Three powerful observables:

$$\langle \mathcal{A}_\lambda^\tau \rangle$$



S_1



R_2

$$\Lambda_b \longrightarrow \Lambda_c (\rightarrow \Lambda \pi) \ell \nu$$

2209.13409

NB: $\mathcal{B}(\Lambda_c \rightarrow \Lambda \pi) = 1.30(7)\%$ or $\mathcal{B}(\Lambda_c \rightarrow p K_S) = 1.59(8)\%$

Many more angular observables and checking on $\text{Im}[g_x] \neq 0$

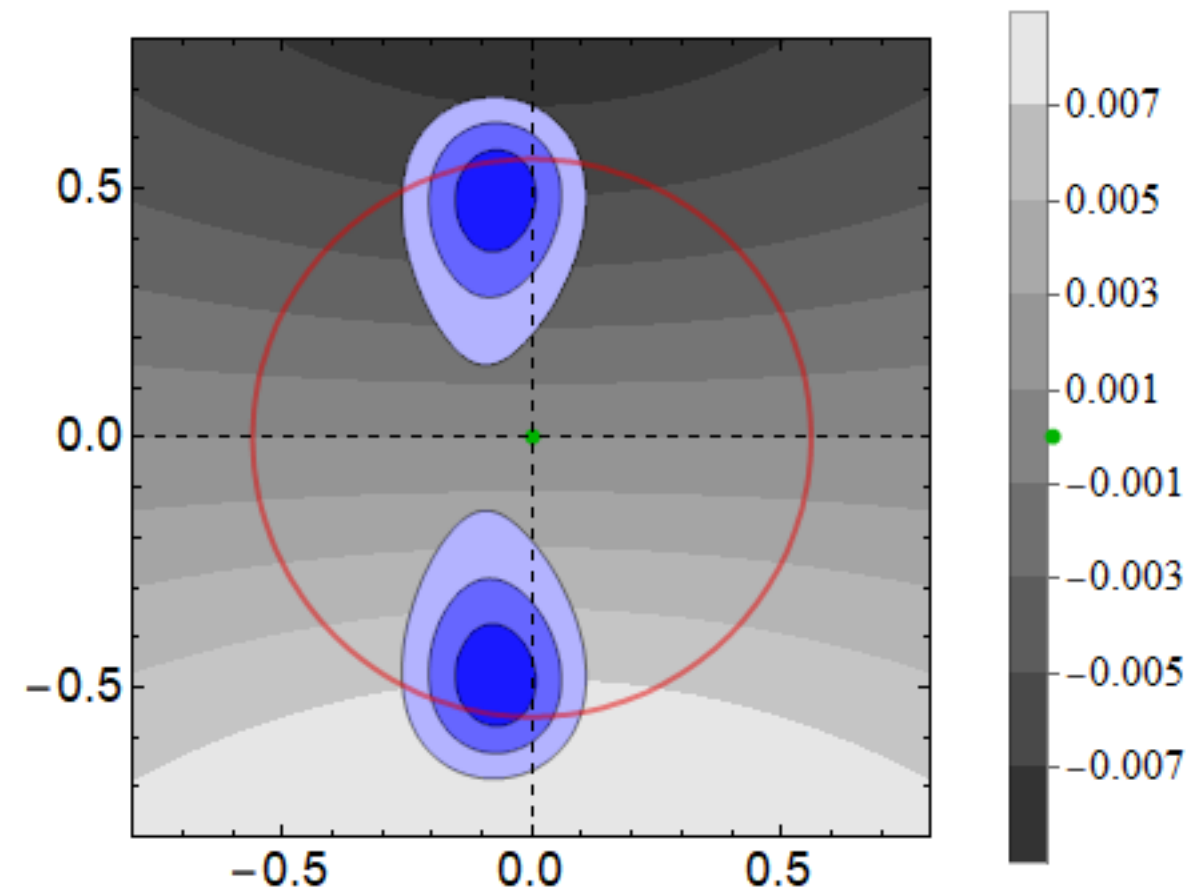
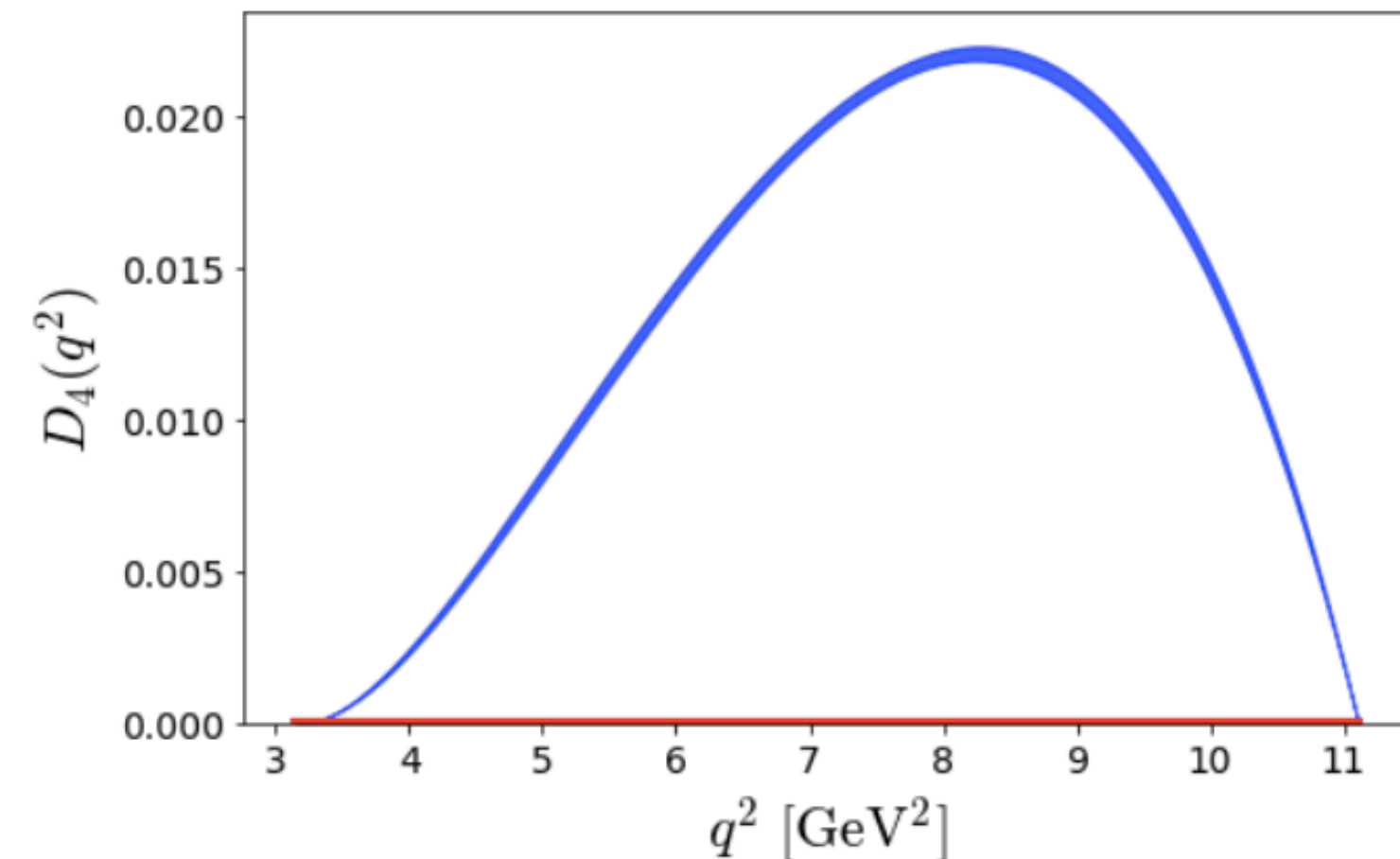
$$\begin{aligned} \dots \\ \frac{d^4 \Gamma^{\lambda_\ell}}{dq^2 d \cos \theta d \cos \theta_\Lambda d \phi} = & A_1^{\lambda_\ell} + A_2^{\lambda_\ell} \cos \theta_\Lambda \\ & + \left(B_1^{\lambda_\ell} + B_2^{\lambda_\ell} \cos \theta_\Lambda \right) \cos \theta \quad \mathcal{A}_{\text{fb Baryon}} \\ & + \left(C_1^{\lambda_\ell} + C_2^{\lambda_\ell} \cos \theta_\Lambda \right) \cos^2 \theta \\ & + \left(D_3^{\lambda_\ell} \sin \theta_\Lambda \cos \phi + D_4^{\lambda_\ell} \sin \theta_\Lambda \sin \phi \right) \sin \theta \quad \mathcal{A}_{\text{fb Lepton}} \\ & + \left(E_3^{\lambda_\ell} \sin \theta_\Lambda \cos \phi + E_4^{\lambda_\ell} \sin \theta_\Lambda \sin \phi \right) \sin \theta \cos \theta \end{aligned}$$

$$\Lambda_b \longrightarrow \Lambda_c(\rightarrow \Lambda\pi)\ell\nu$$

NB: $\mathcal{B}(\Lambda_c \rightarrow \Lambda\pi) = 1.30(7)\%$ or $\mathcal{B}(\Lambda_c \rightarrow pK_S) = 1.59(8)\%$

Many more angular observables and checking on $\text{Im}[g_x] \neq 0$

$$\langle D_4^\tau \rangle$$

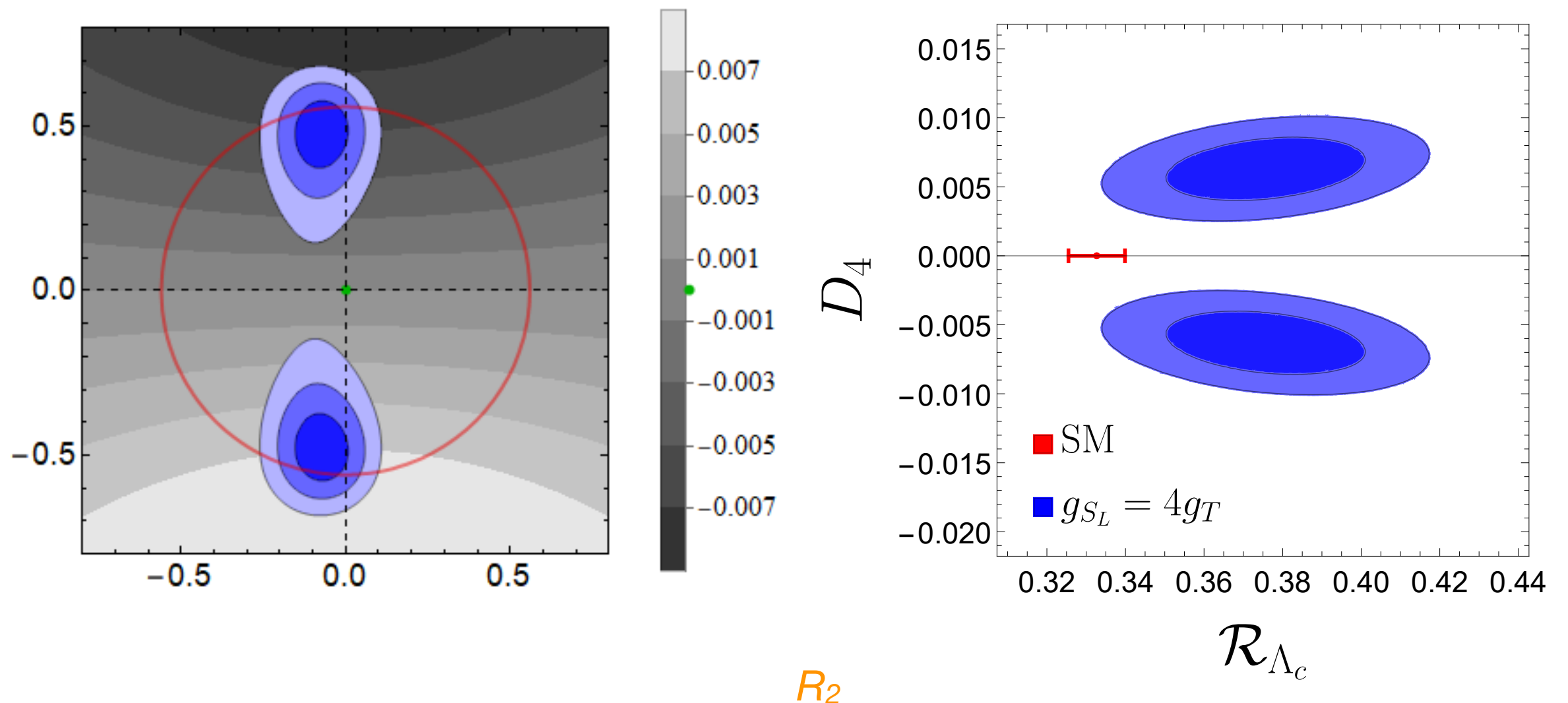


R_2

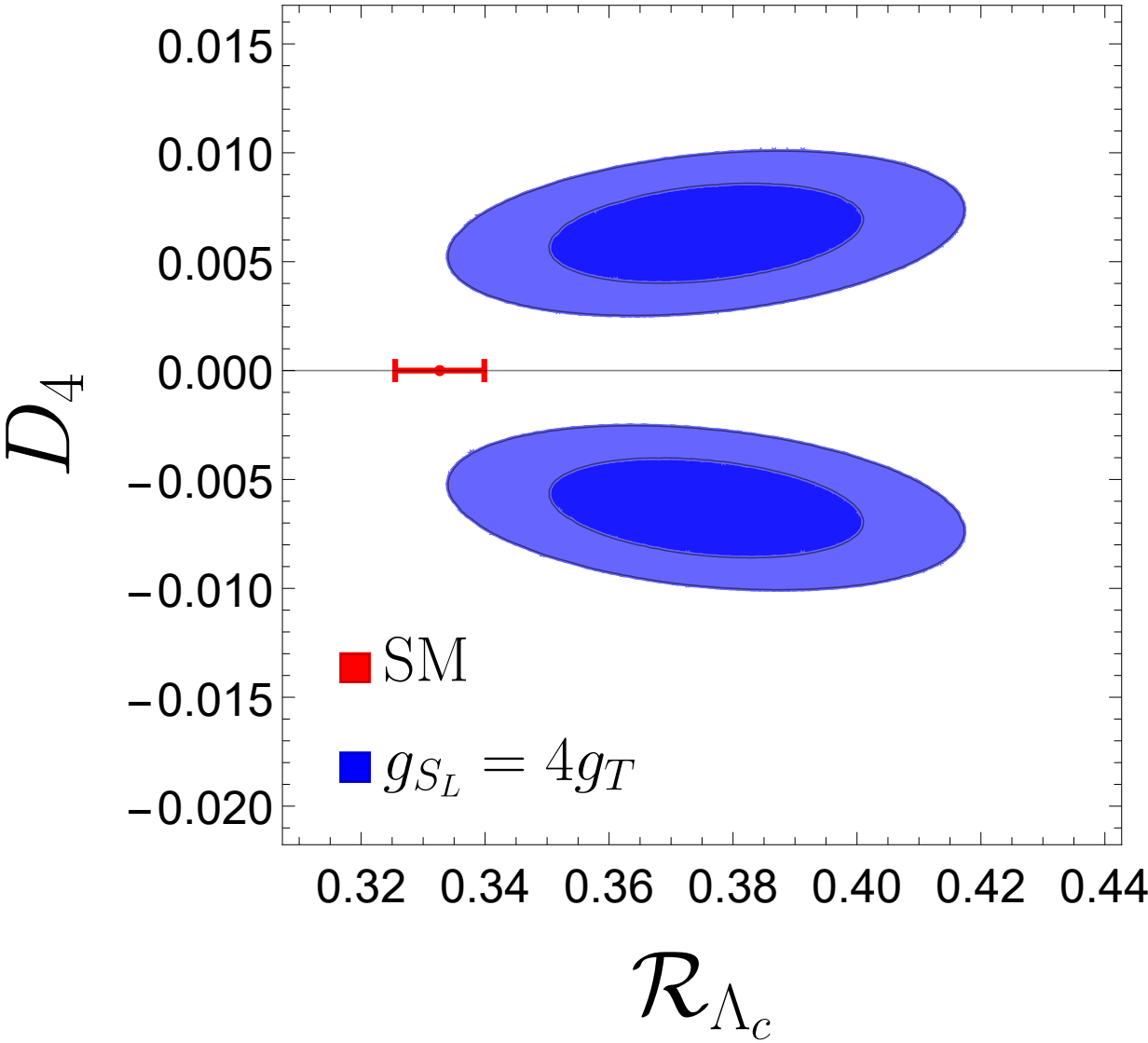
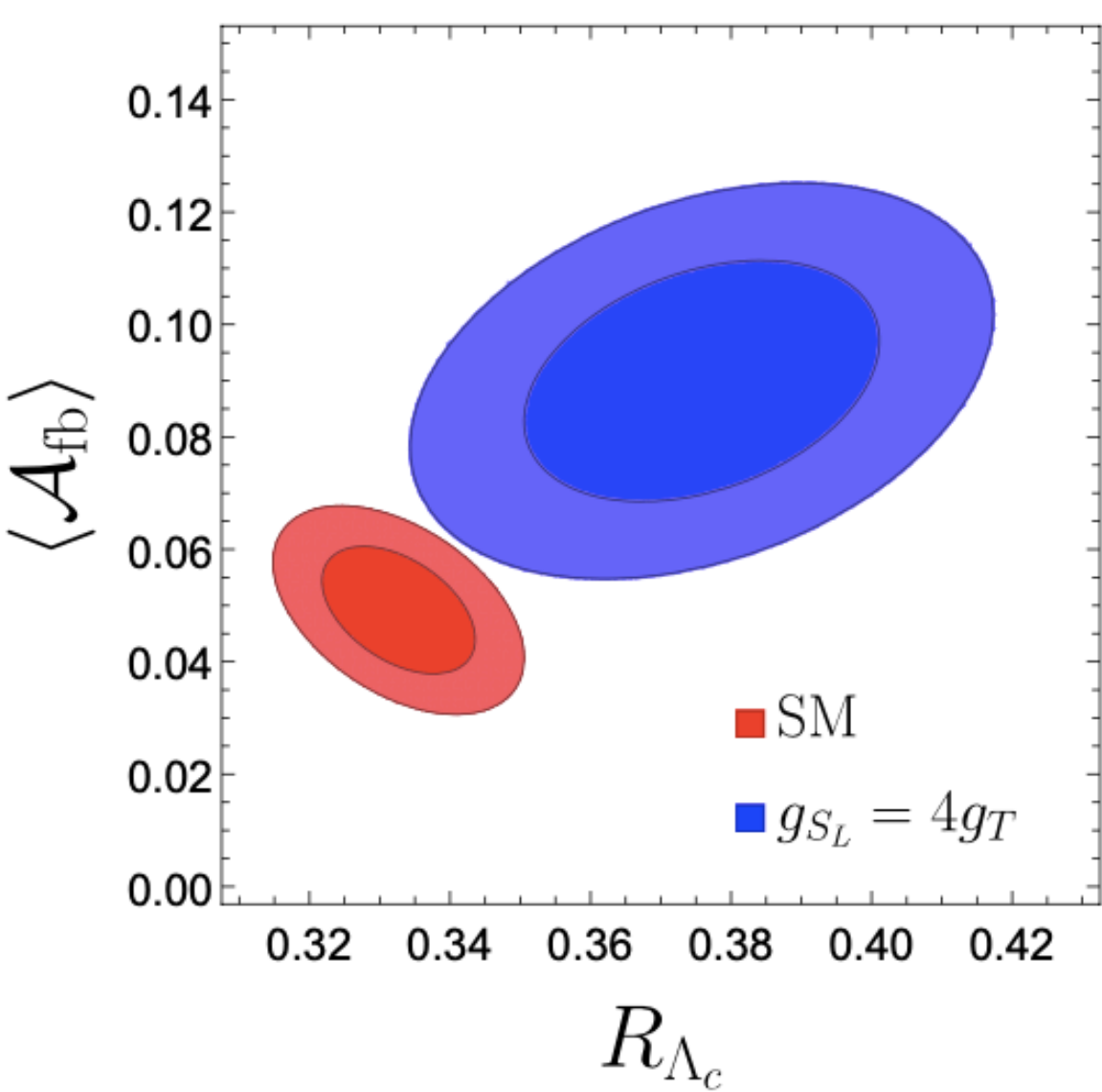
$$\Lambda_b \longrightarrow \Lambda_c (\longrightarrow \Lambda \pi) \ell \nu$$

Many more angular observables and checking on $\text{Im}[g_x] \neq 0$

$$\langle D_4^\tau \rangle$$

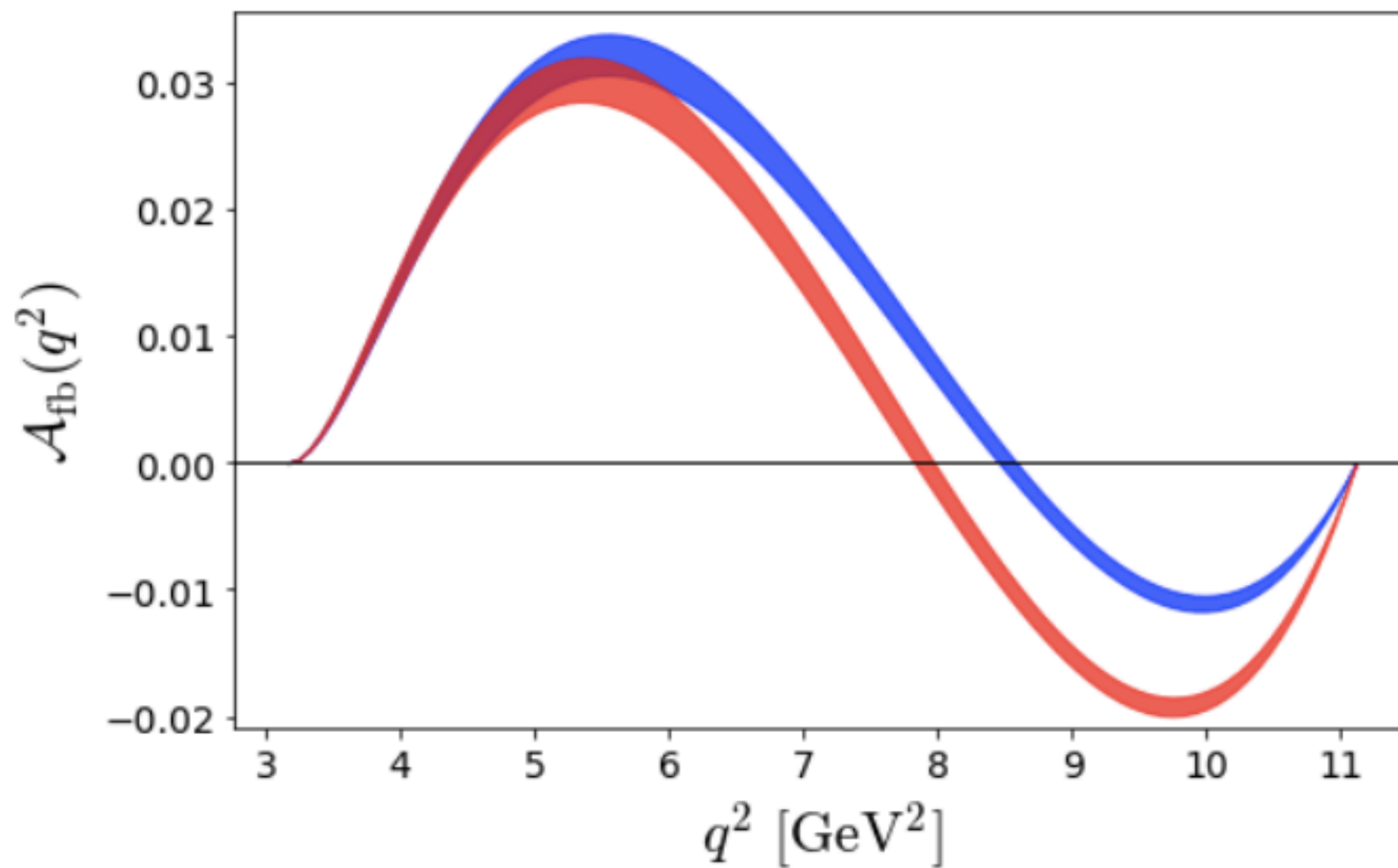


$$\Lambda_b \longrightarrow \Lambda_c(\rightarrow \Lambda\pi)\ell\nu$$



$$\Lambda_b \longrightarrow \Lambda_c (\rightarrow \Lambda \pi) \ell \nu$$

And there is also this...



- Hadronic uncertainties are with us and one should always keep in mind that nonperturbative QCD is not solved.
- Results from various models and SR suffer from systematics that is next-to-impossible to estimate.
- LQCD is the only good way to go but the situation is unsatisfactory for a reliable fit with data to extract $|V_{cb}|$ and/or NP parameters.
- Exclusive V_{cb} should be checked on in several possible ways. [Sanity check and can be helpful for testing other ideas - e.g. factorization.]
- R_D and R_{D^*} are too few observables to understand the source of LFUV. Too many NP solutions exist and could be filtered by angular $B \rightarrow D^{(*)} \tau \nu$ and $\Lambda_b \rightarrow \Lambda_c \tau \nu$ observables. Should revisit $B \rightarrow D^{(*)} \ell \nu$ too.
- All of the $\Lambda_b \rightarrow \Lambda_c \ell \nu$ form factors are known from LQCD in SM and BSM. LHCb showed it is possible to measure $B(\Lambda_b \rightarrow \Lambda_c \tau \nu)$. A partial angular is doable.
- There are 18 observables that can be extracted from $\Lambda_b \rightarrow \Lambda_c (\rightarrow \Lambda \pi) \tau \nu$. Even a small subset would be very helpful to discriminate among various scenarios.
- There are observables allowing to check whether or not there is a nonzero NP phase!