

# Investigation of the Impact of Magnetic Fields on Scattering Muography Images

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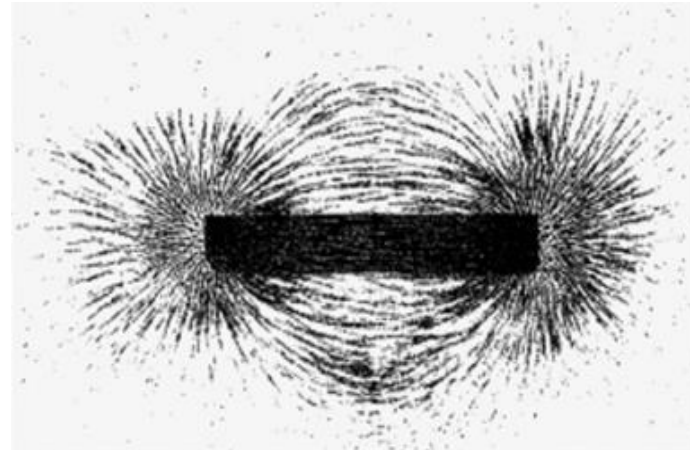
*Basiri.hamid@kyudai.jp*





# ■ Magnet or magnetic field measurement techniques are limited.

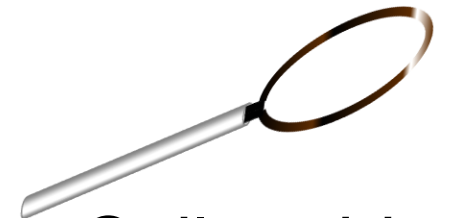
- Magnetic flux can be figured out only where iron sand presents.



- A Hall device probing  
(local measurement)



- Coil probing  
(time dependent one only)





## Cosmic-ray muon has potential!!

- **Charged particle:** Lorentz force deflects muons into specific direction in contrast to scattering.
- **High penetrating power:** Probe insertion is not necessary and we can measure magnetic fields placed inside some targets.
- **Wide field of view** facilitates large-scale measurements.
- **Natural radiation**

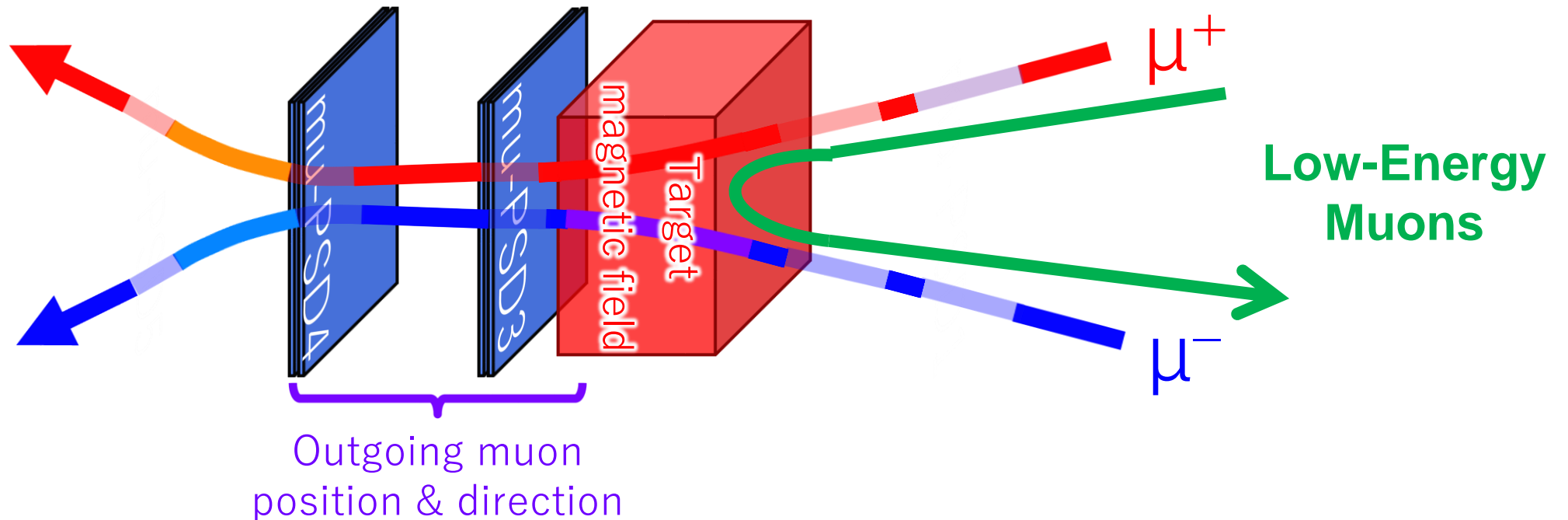
# Magnetic Field Imaging by Cosmic-ray Muon

— Magic- $\mu$  —

Patent: MAGNETIC FIELD STRUCTURE IMAGING USING MUONS, 2022, WO2023031265

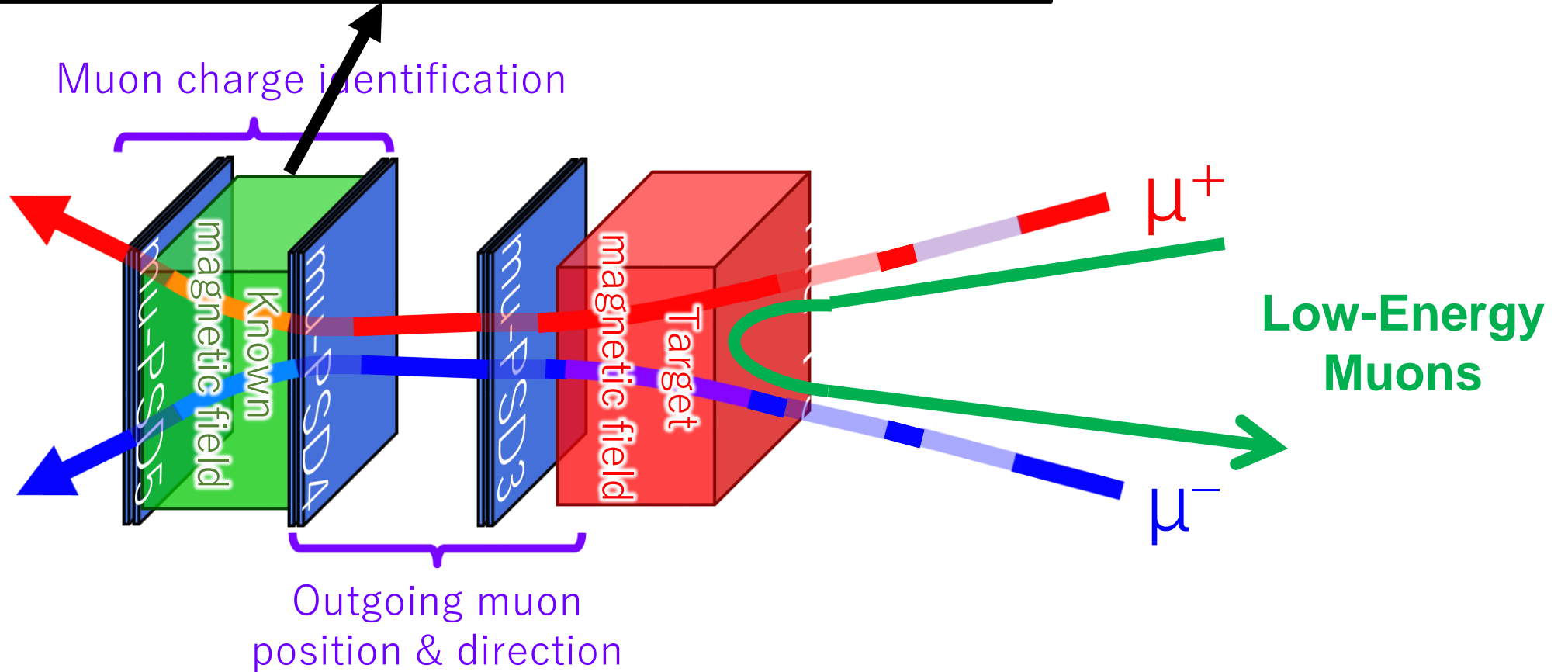
# Conceptual designs

- Huge and strong magnetic fields such as **Fusion reactors**
- Background measurement (Magnet OFF) or precise simulation must be possible.
- We need just qualitative measurement.



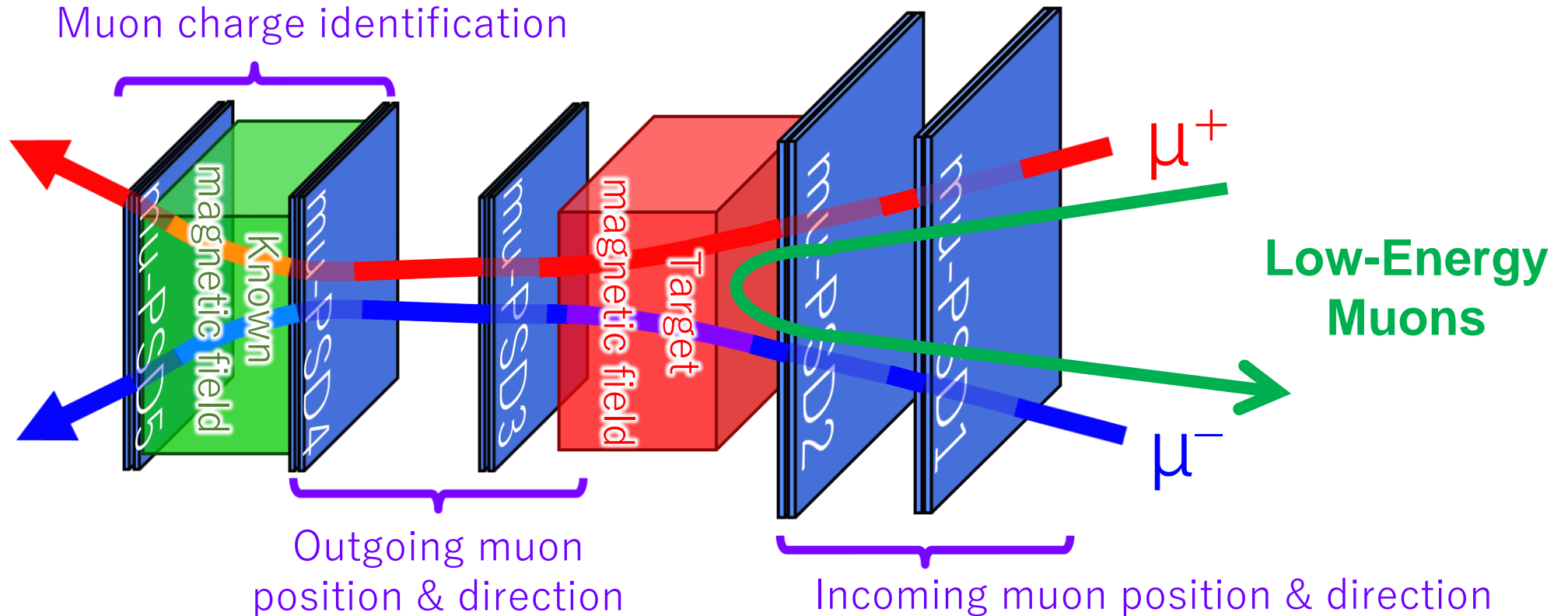
- **1 m** magnetic field of **1 T**, muons up to **180 MeV** will be **completely deflected back**. These constitute **3.5%** of the muon flux.

Addition to the normal muography setup allows for enhanced magnetic field information.



- A 20 cm thick magnet of 0.2 T can distinguish + and - muons of energy of 130 MeV.

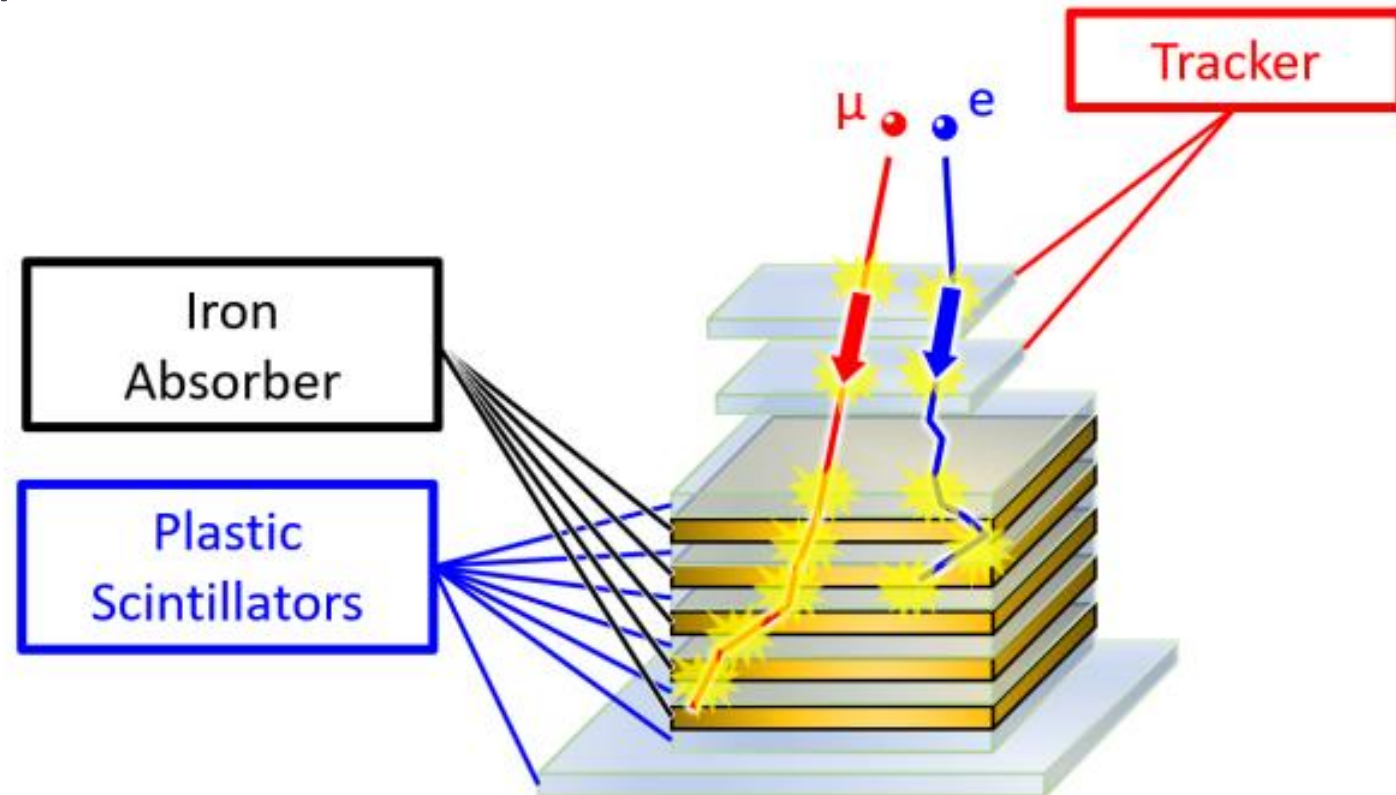
- For small-size targets such as **electric car motor** developments!





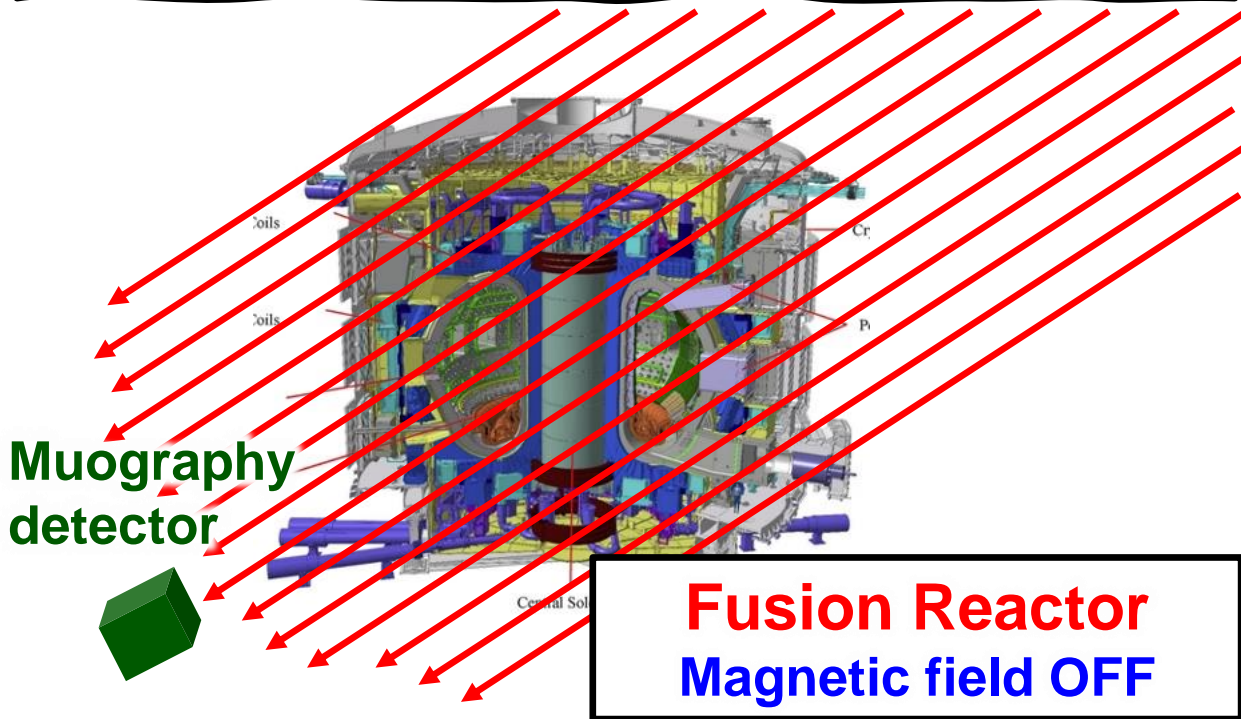
- Composed of layers of **iron plates** and **plastic scintillators**.
- Iron plates interact with muons causing them to **lose energy**.
- Plastic scintillators **detect** these particles, and we can estimate the energy.

Energy up to of 1 GeV  
can be determined using  
multi-layer detector (90  
cm thick) analyzed by  
machine learning



# Effect of magnetic field on muography images

## Absorption

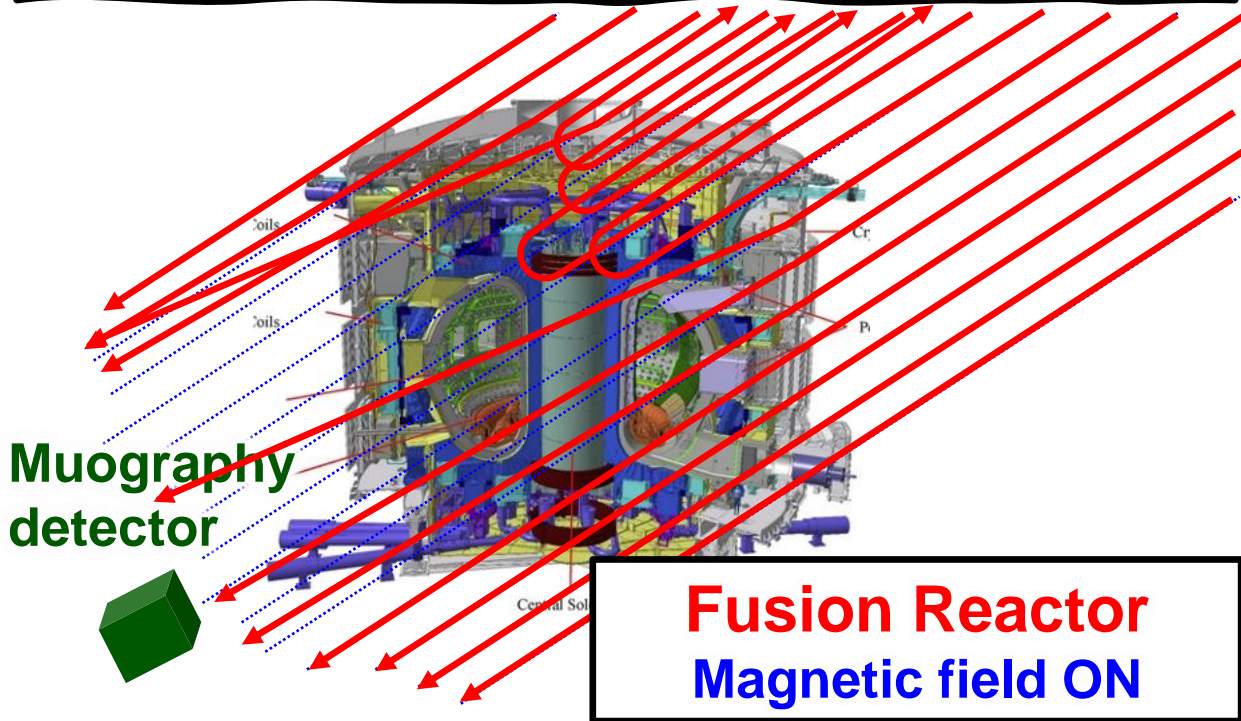


Muon trajectories are almost straight lines if there is no magnetic field

## Scattering

# Effect of magnetic field on muography images

## Absorption

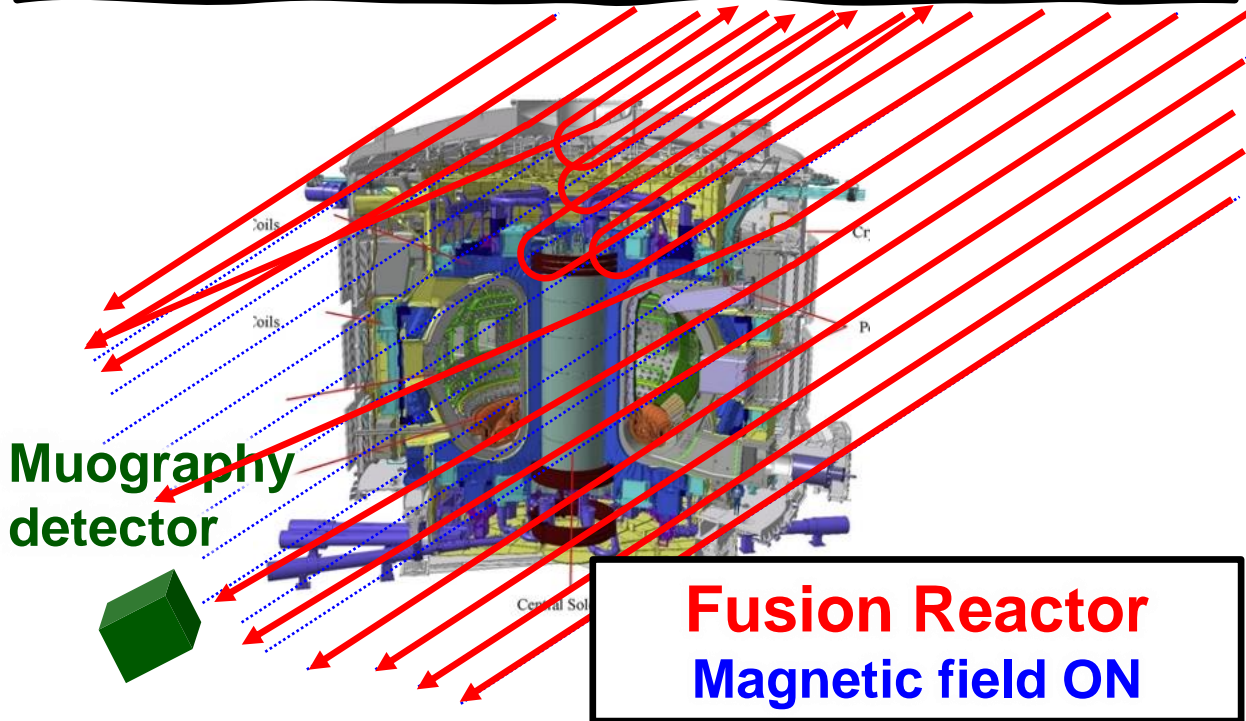


## Scattering

Muography images are **distorted and vanished** by **deflection and reflection** of muon.

# Effect of magnetic field on muography images

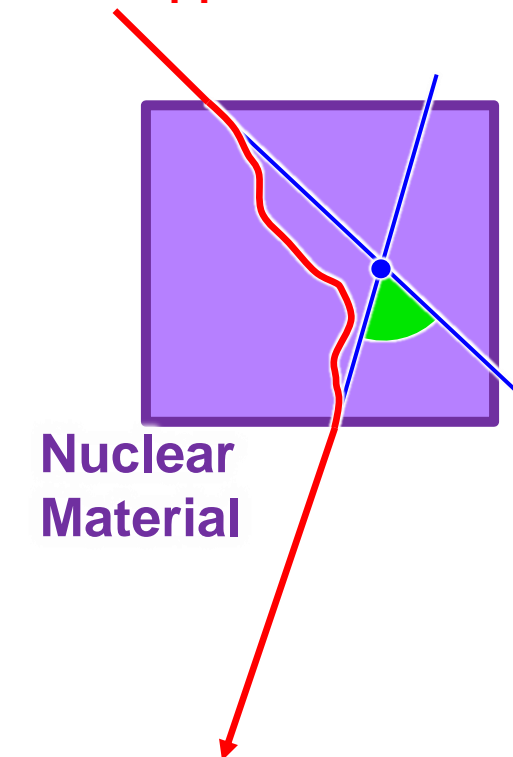
## Absorption



Muography images are **distorted and vanished** by **deflection and reflection** of muon.

## Scattering

Incoming muon from upper tracker



Outgoing muon to lower tracker

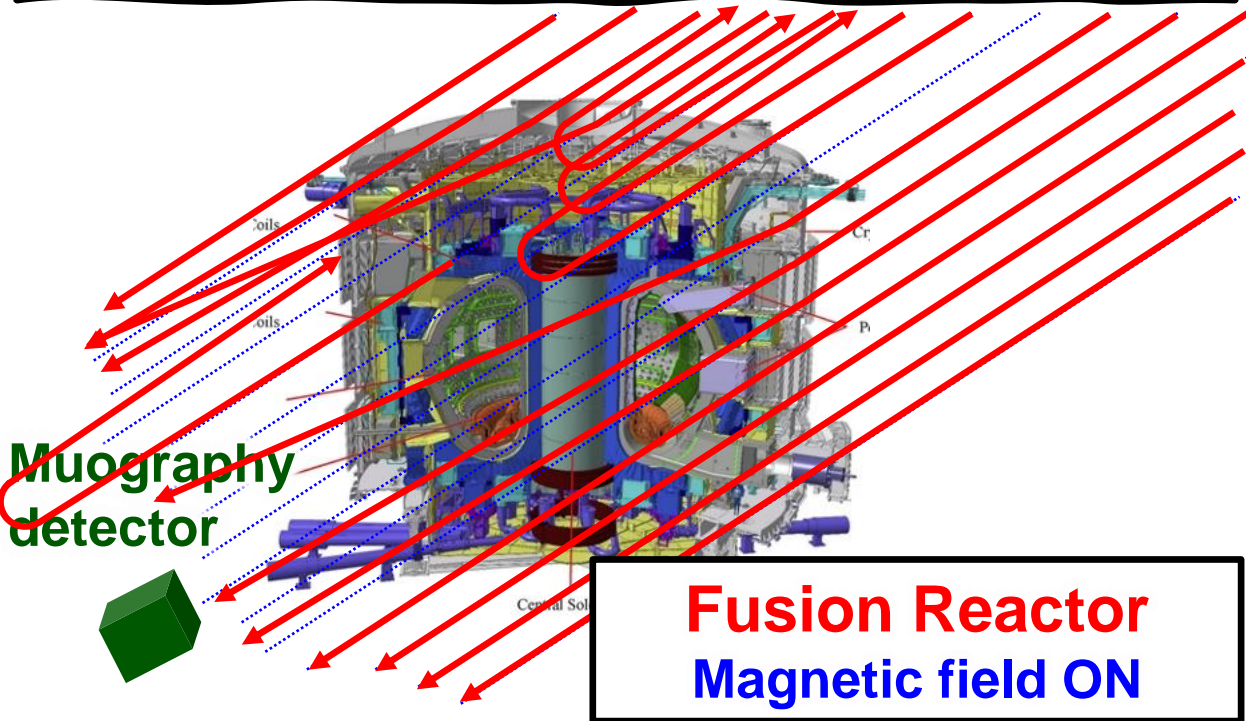
Scattering muography estimates

1. a PoCA position and
2. a scattering angle

by incoming and outgoing muon directions for each event.

# Effect of magnetic field on muography images

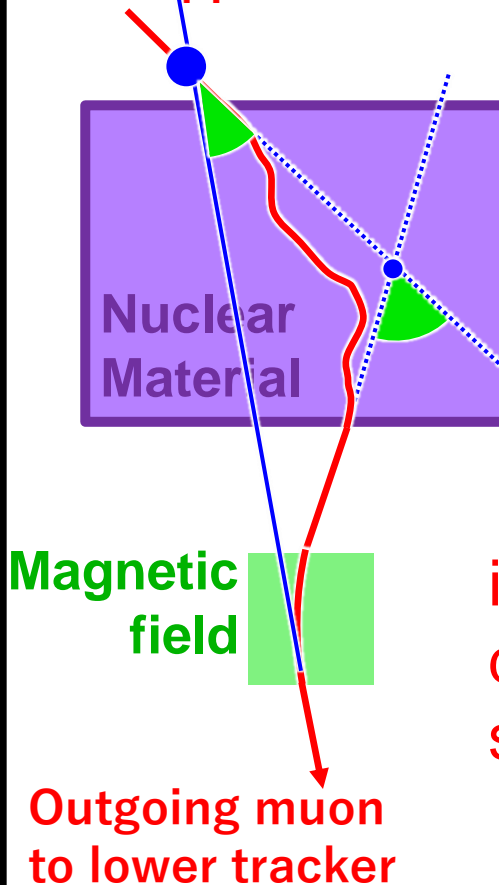
## Absorption



Muography images are **distorted and vanished** by **deflection and reflection** of muon.

## Scattering

Incoming muon from upper tracker



Magnetic field

displaces the PoCA position and shifts the scattering angles

i.e., can be a cause of dummy PoCA position and scattering angle



Made in Japan  
(JAEA)

Capable of transporting nearly all particles over wide energy range using **Monte Carlo** method

- The code and the license is available for **free** upon your request.

<https://phits.jaea.go.jp/howtoget.html>

- There are free online tutorials, and you can invite them for face-to-face tutorials.

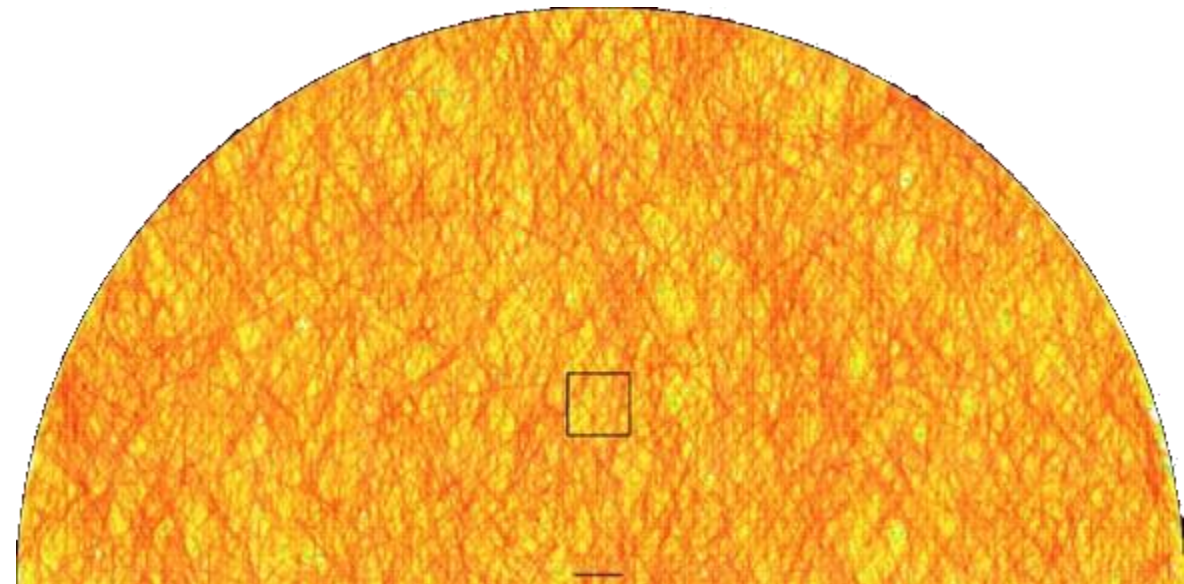


**PHITS**  
Particle and Heavy Ion Transport code System

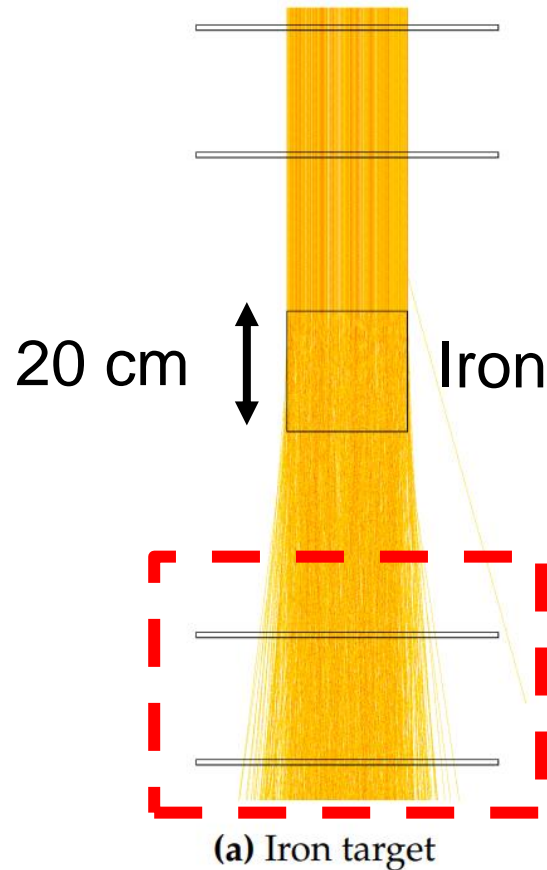


- **PARMA model** (An analytical model) has been implemented for simulation of cosmic-ray.

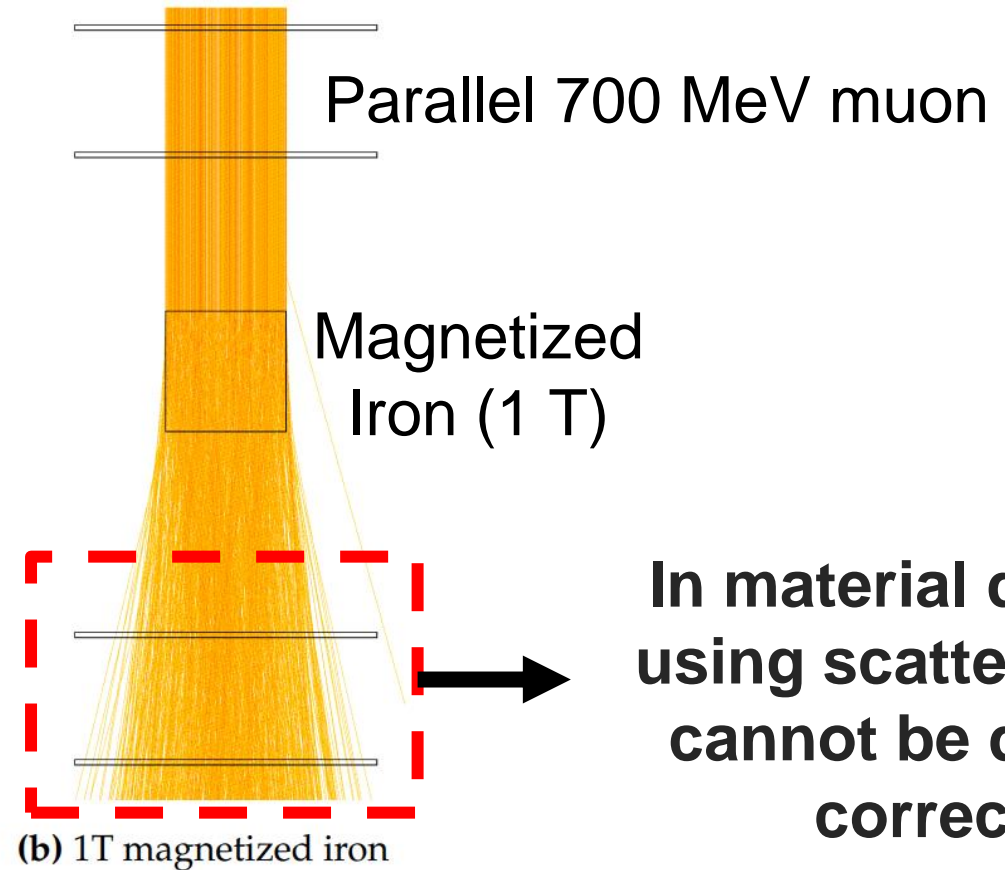
- Parameters such as **Altitude**, **latitude**, **date** and the **radius of hemisphere** can be inputted.



# Effect of magnet on scattering angle distribution



Scattering  
 $(\theta_{\text{RMS}} 4.55^\circ)$



Scattering & Deflection  
 $(\theta_{\text{RMS}} 6.14^\circ)$

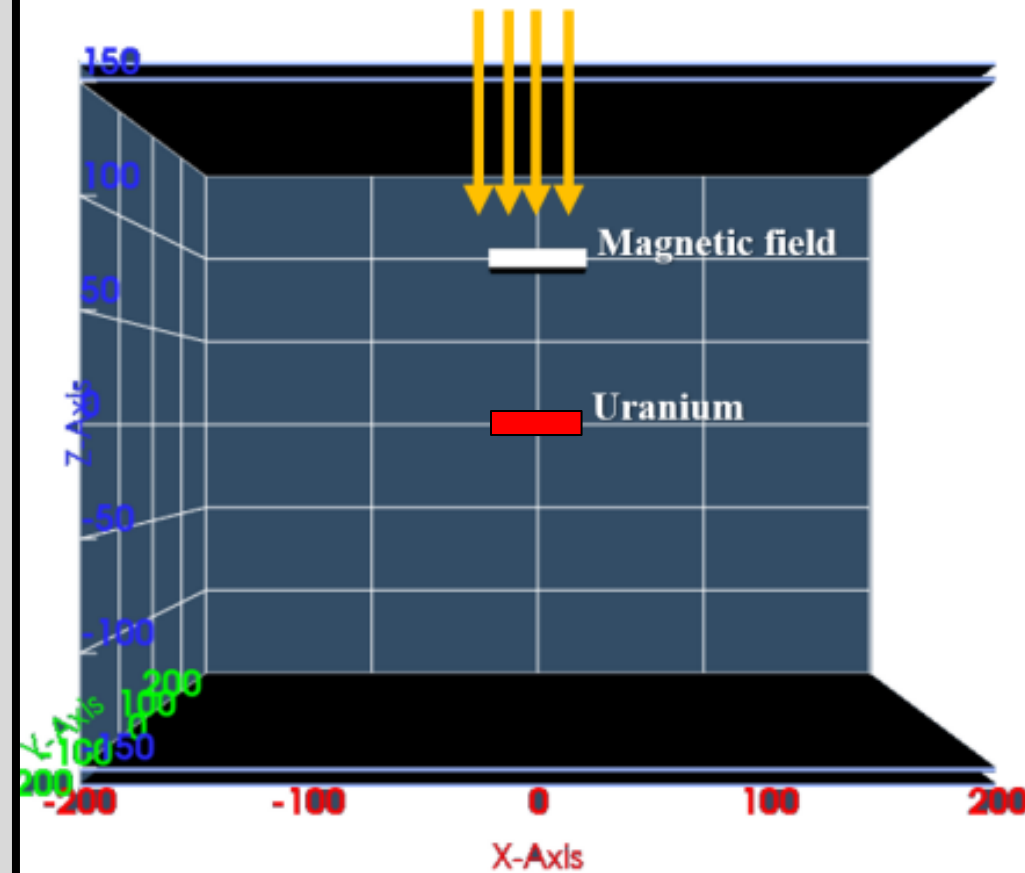
**In material detection using scattering, iron cannot be detected correctly!**



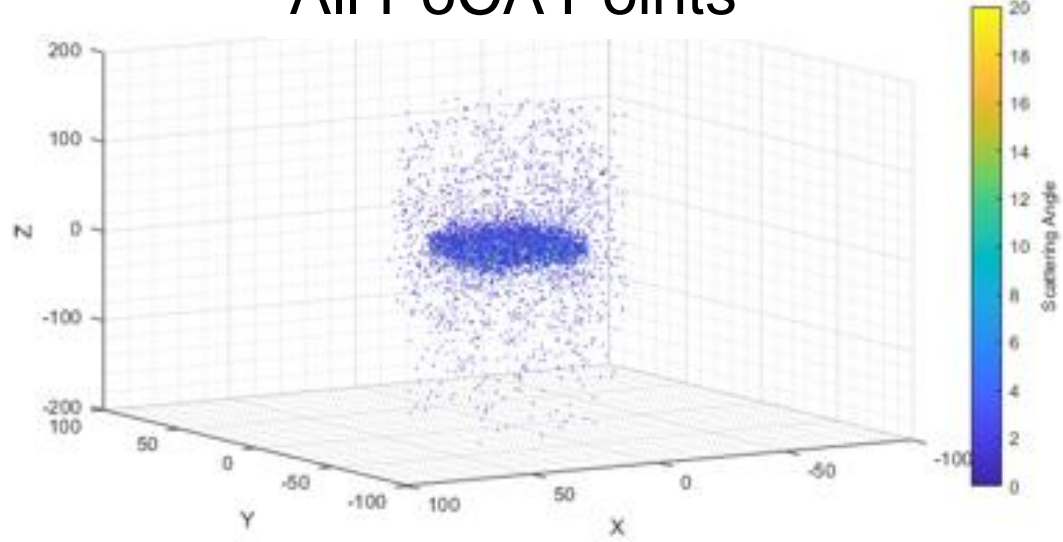
## Effect of magnet on PoCA points

- A parallel beam of positive and negative muons was projected onto a uranium target.
- **Detectors:**
  - plastic scintillators of 2m x 2m x 2mm.
- **Magnetic field region:** 50cm x 50cm x 10cm.
- **Uranium target size:** 40cm x 40cm x 10cm.

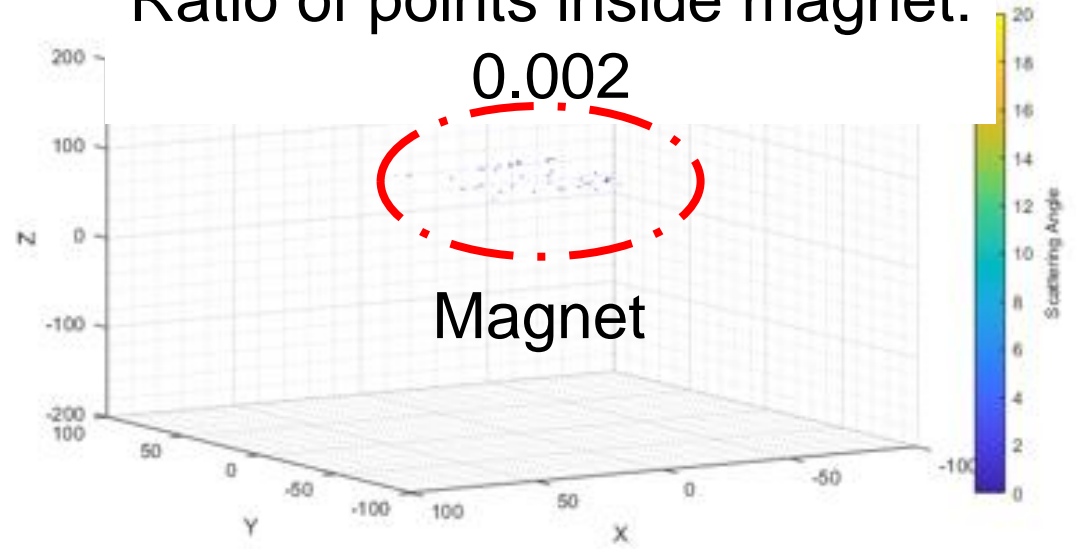
10 cm of magnet in X-Y plane is not covered by uranium target!



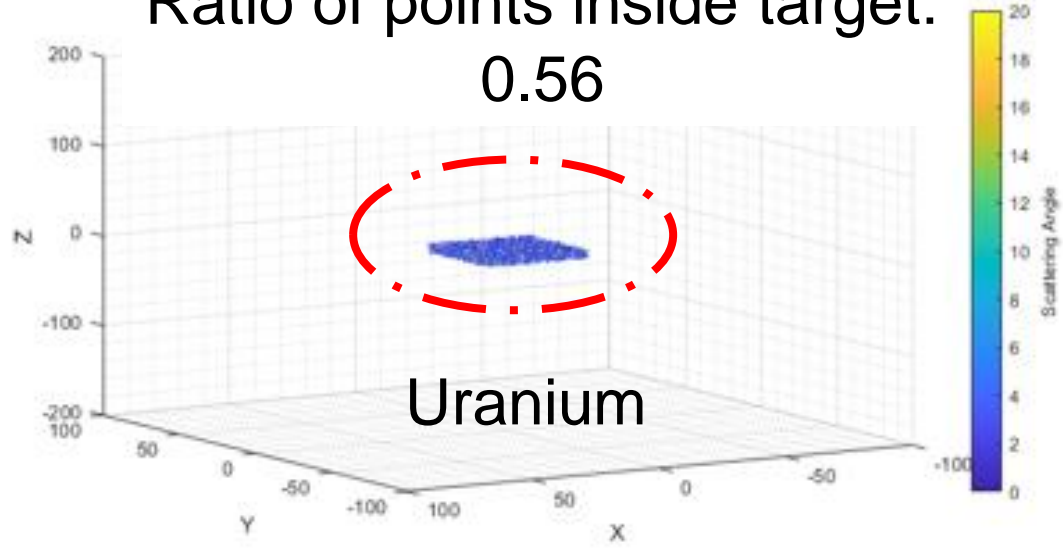
All PoCA Points



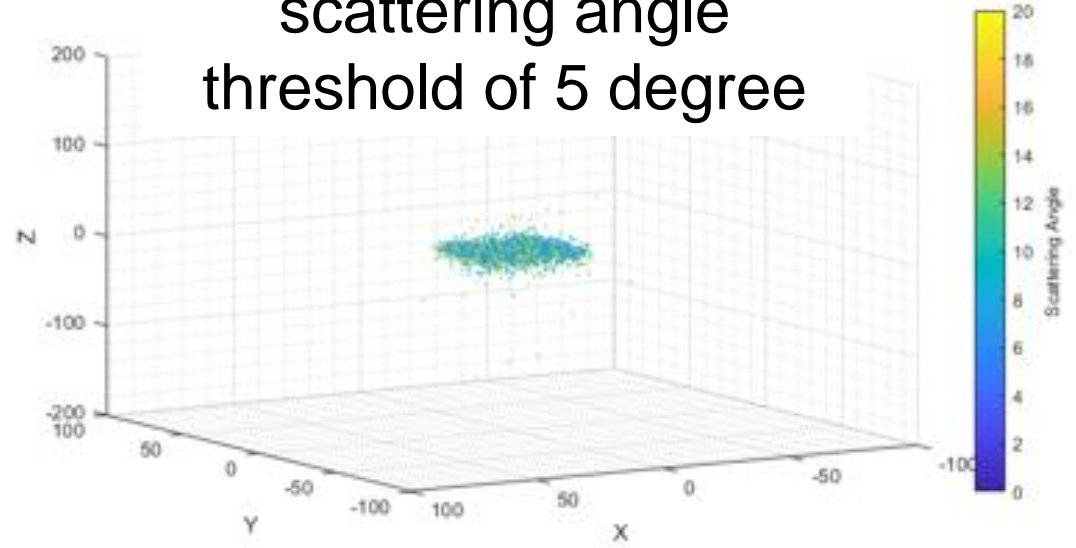
Ratio of points inside magnet:



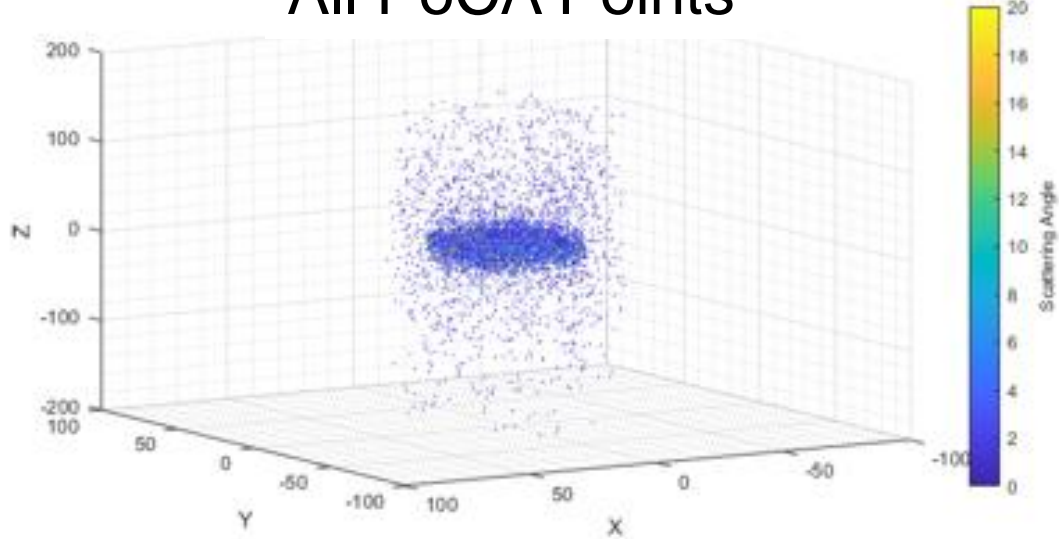
Ratio of points inside target:



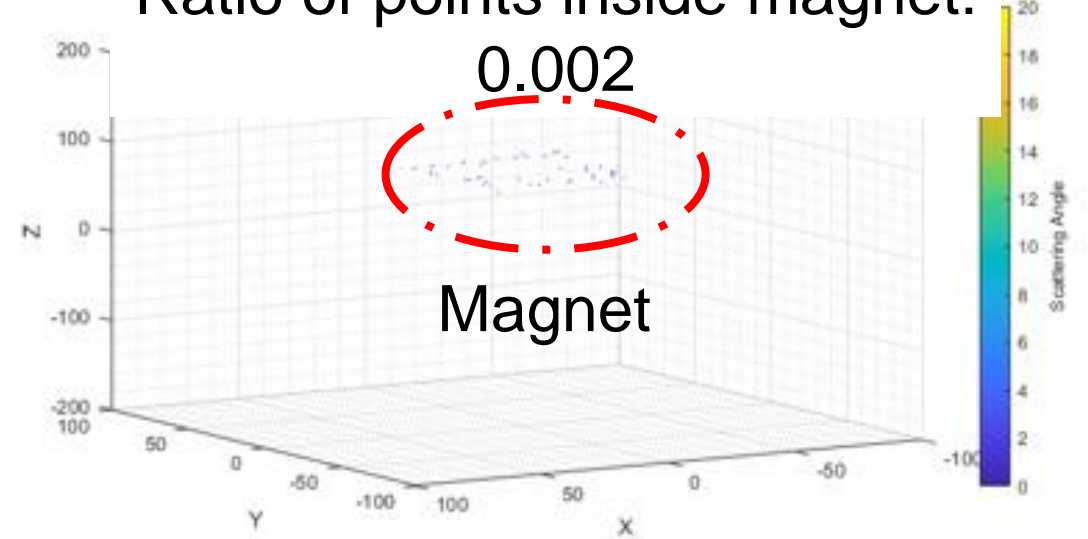
PoCA Points limited by scattering angle threshold of 5 degree



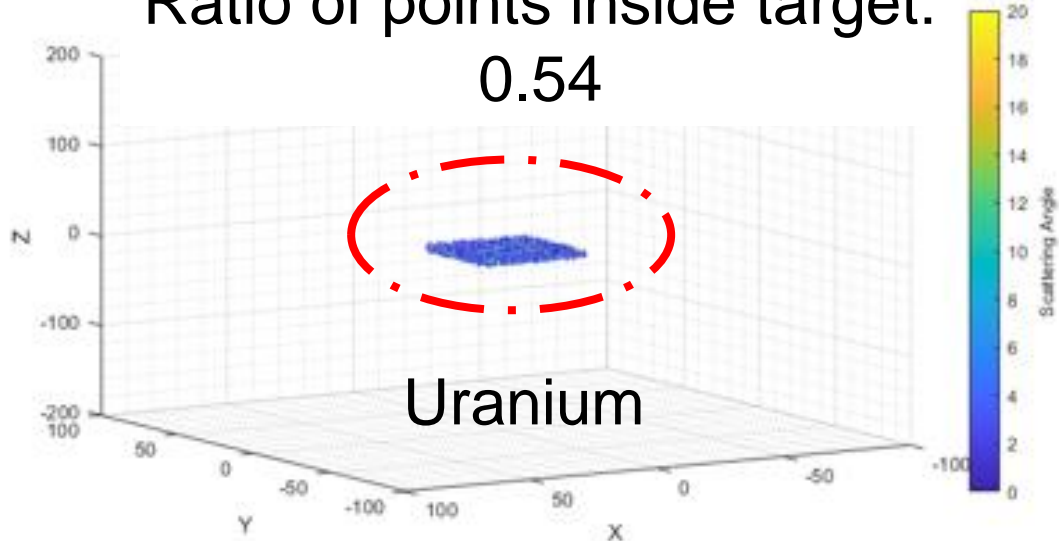
All PoCA Points



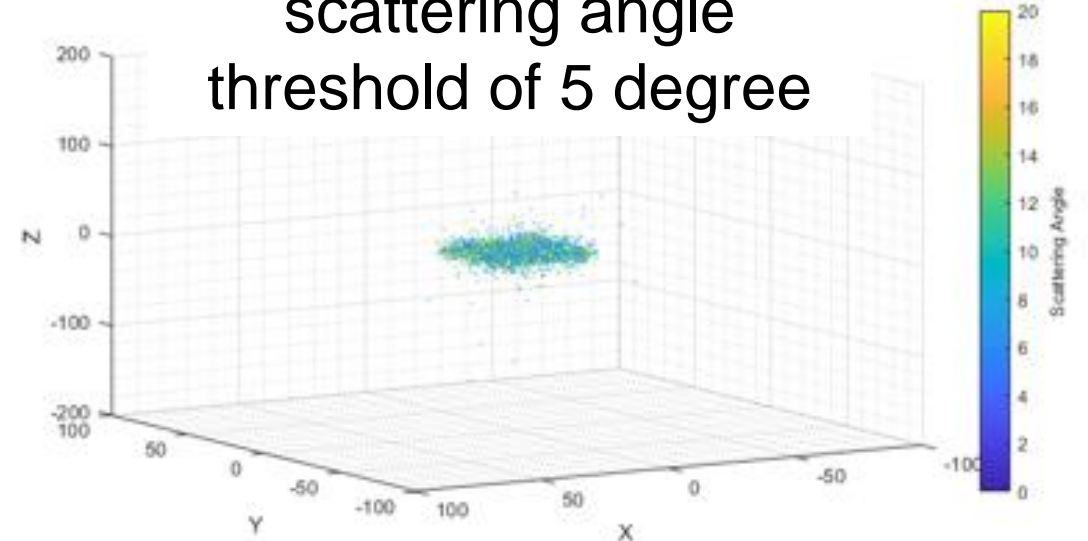
Ratio of points inside magnet:



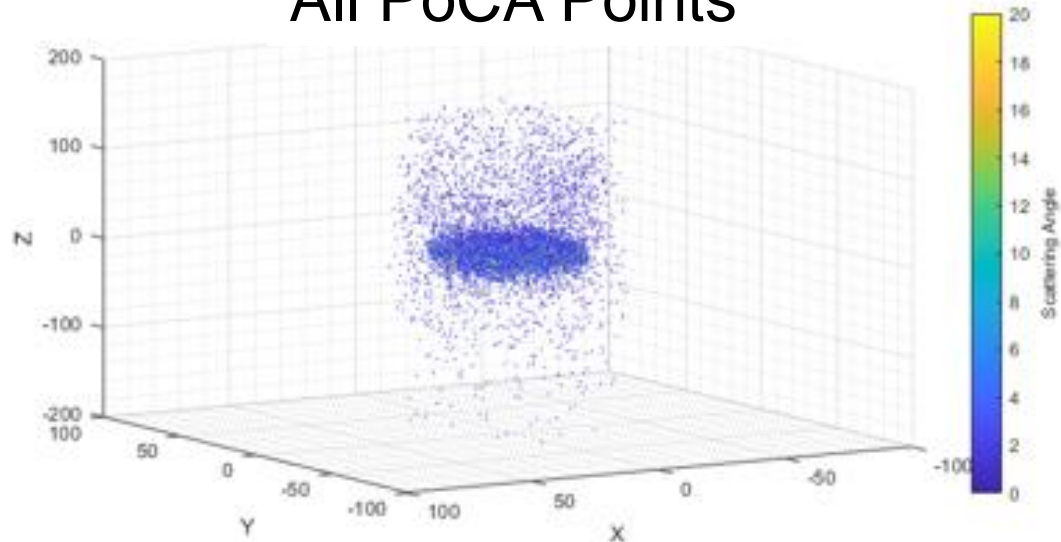
Ratio of points inside target:



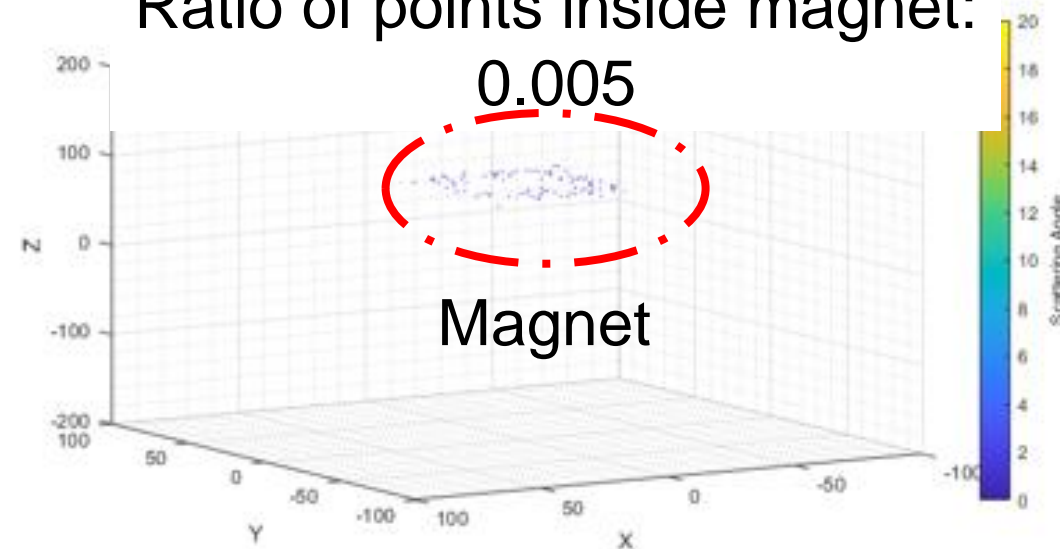
PoCA Points limited by scattering angle threshold of 5 degree



All PoCA Points

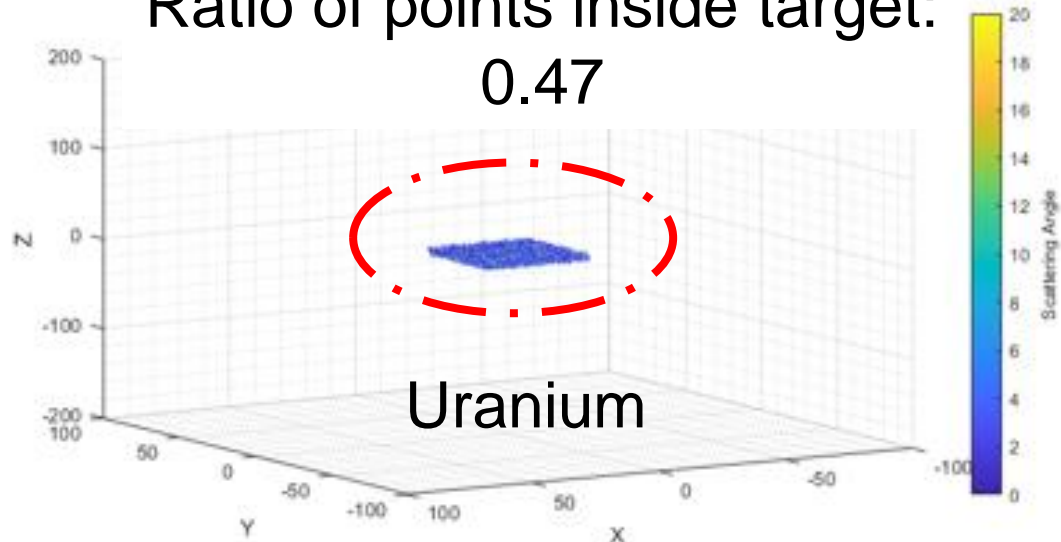


Ratio of points inside magnet:

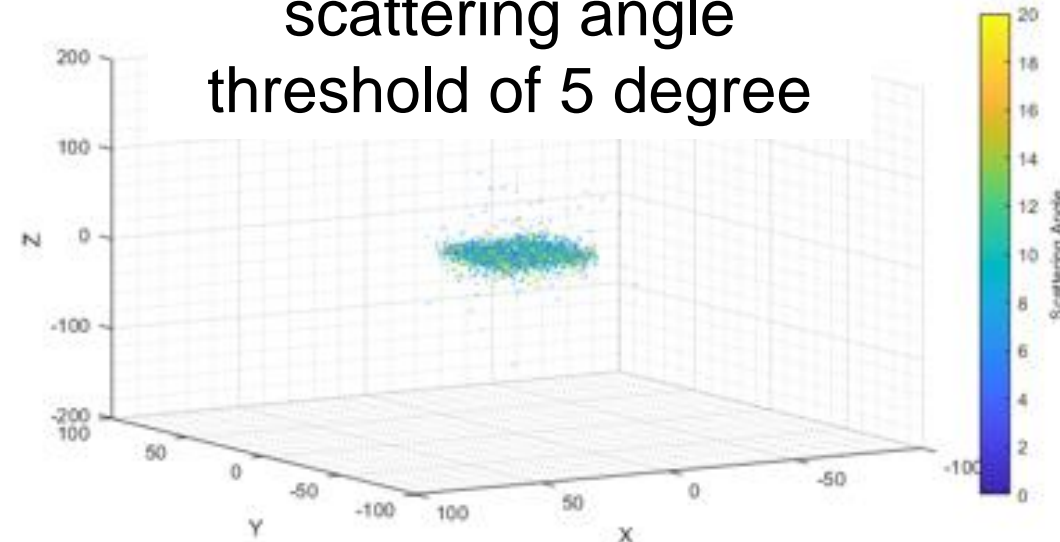


Ratio of points inside target:

0.47

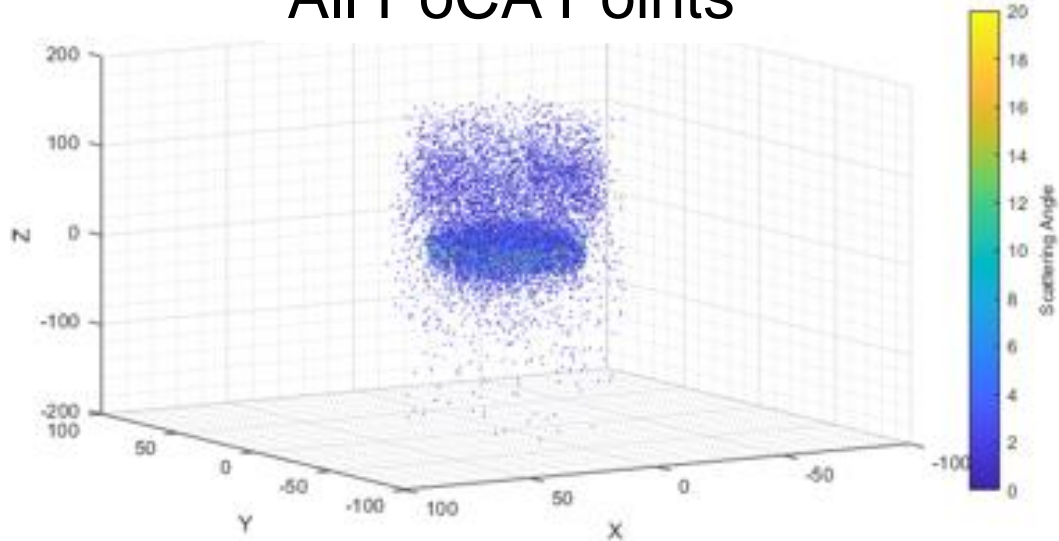


PoCA Points limited by scattering angle threshold of 5 degree

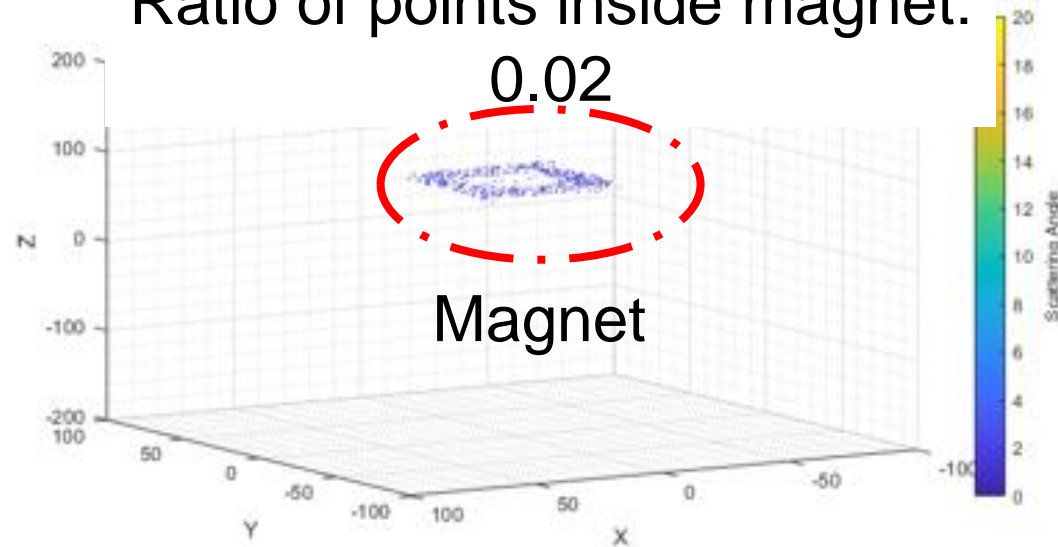




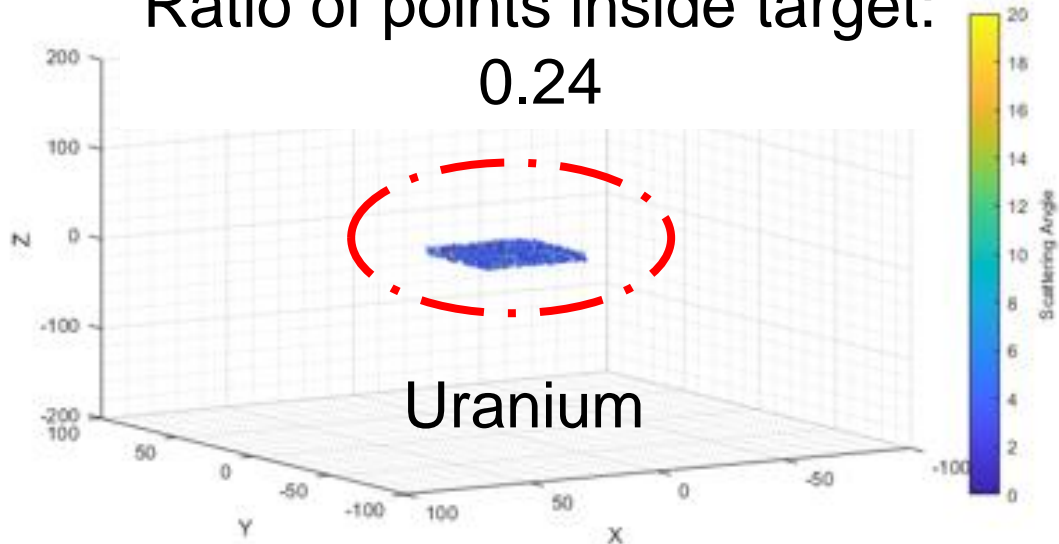
All PoCA Points



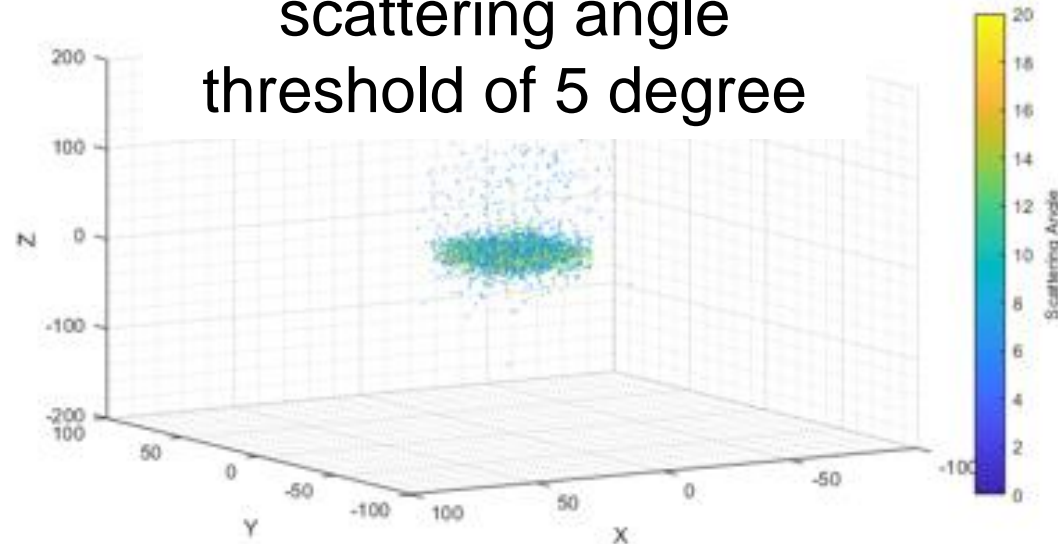
Ratio of points inside magnet:



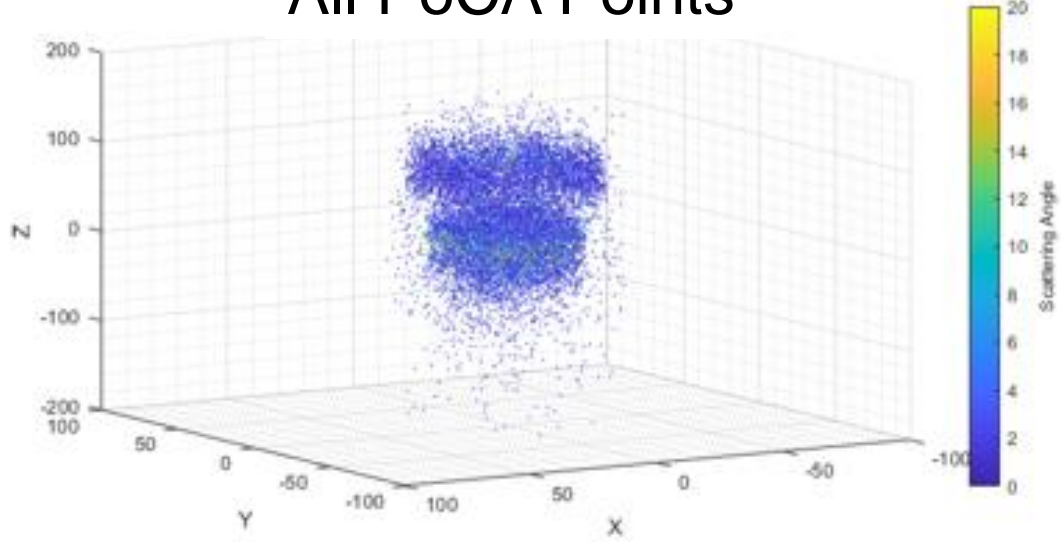
Ratio of points inside target:



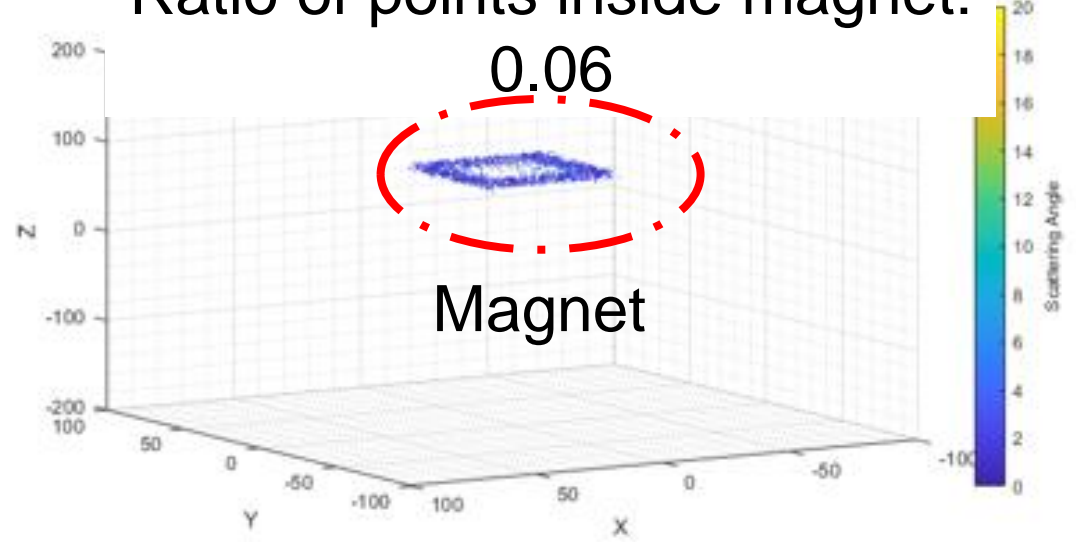
PoCA Points limited by scattering angle threshold of 5 degree



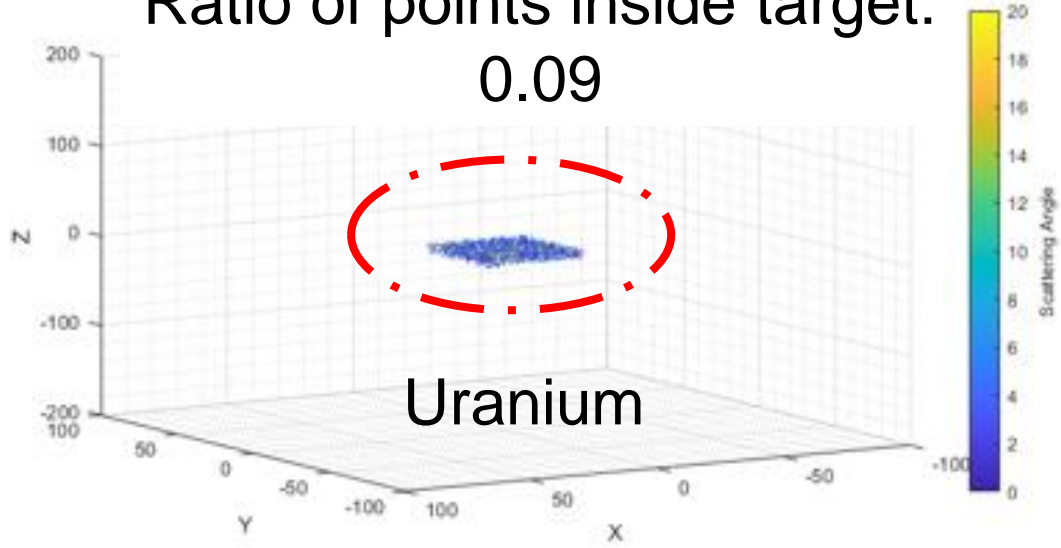
All PoCA Points



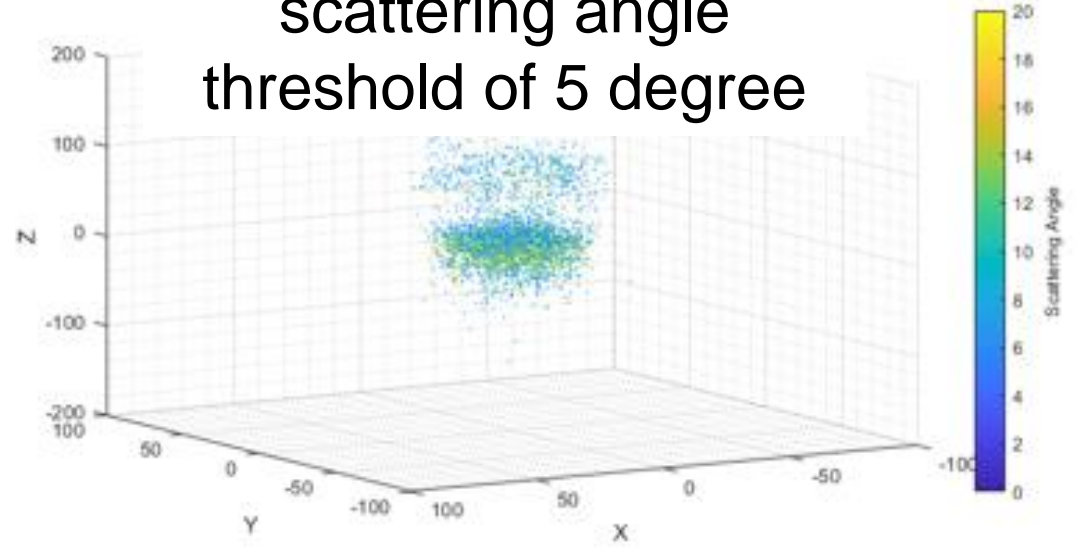
Ratio of points inside magnet:



Ratio of points inside target:



PoCA Points limited by scattering angle threshold of 5 degree



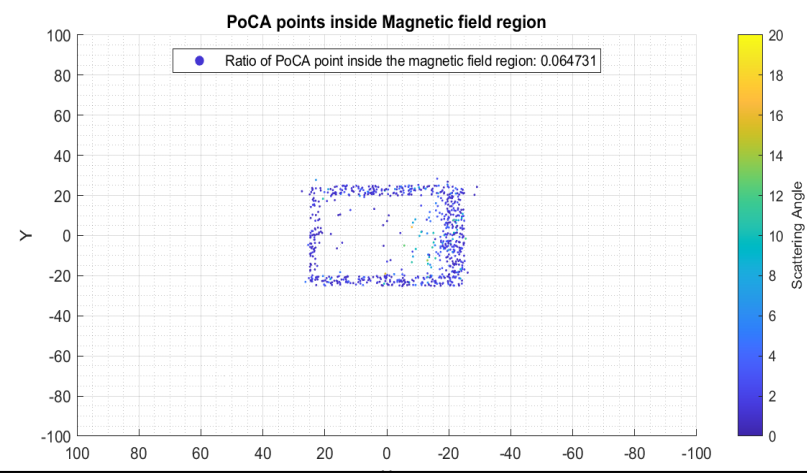
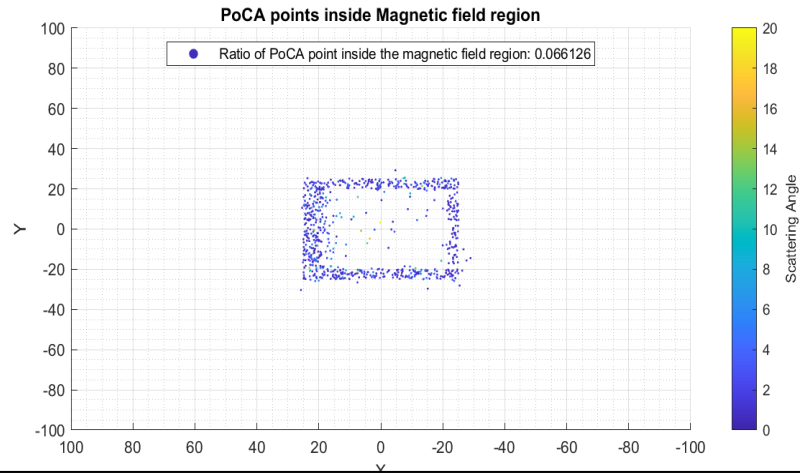


## If we use the charge identification feature in our detector, we can find direction of magnetic field:

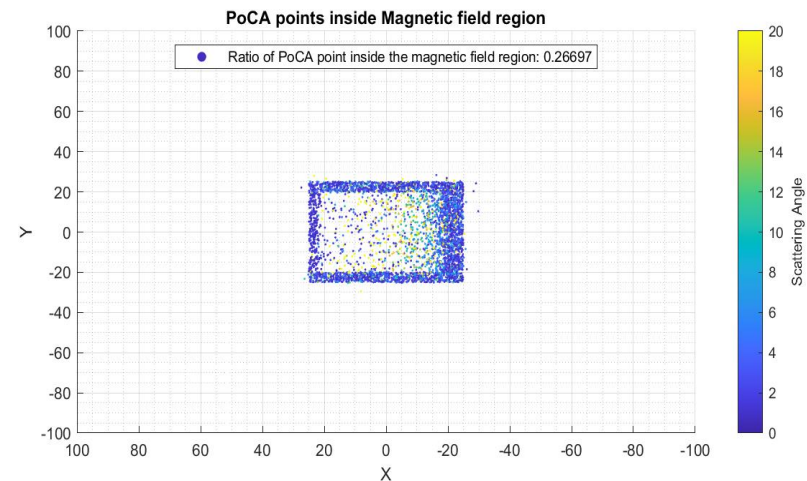
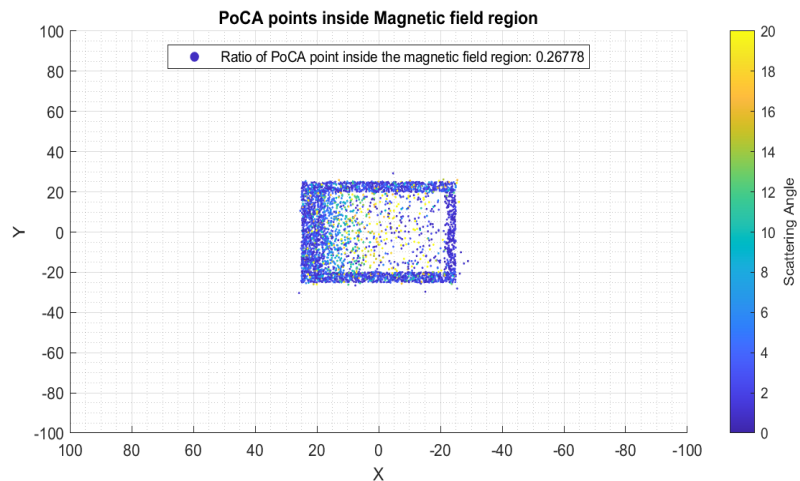
Mu+

Mu-

1 T

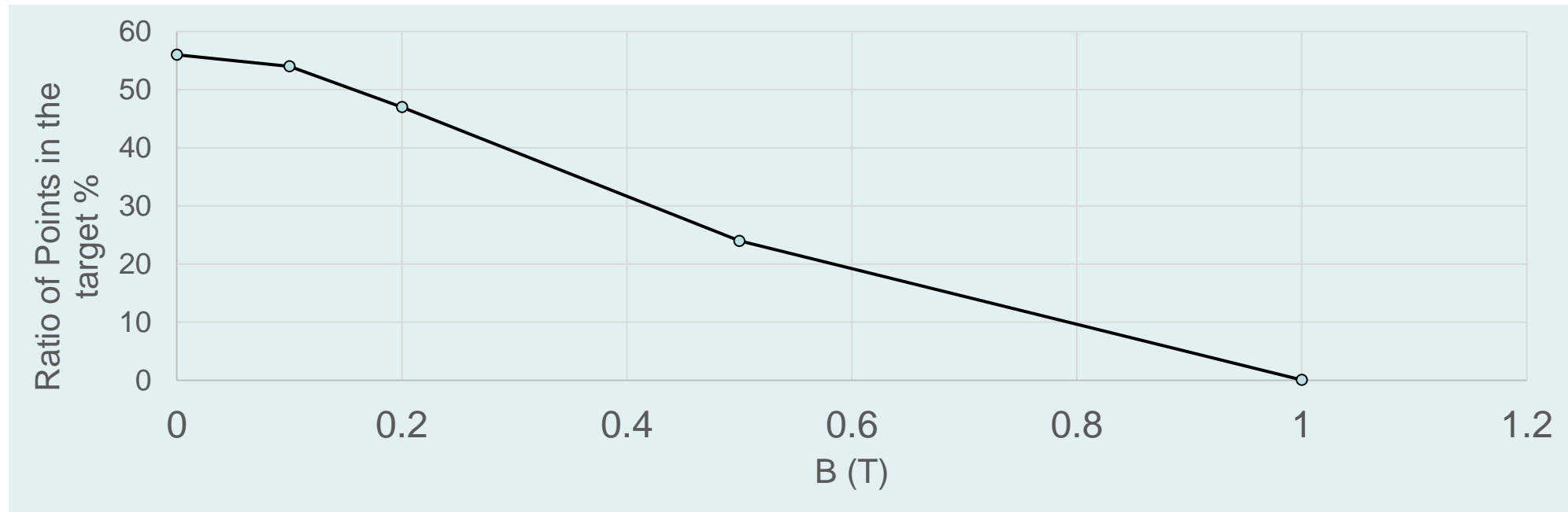


3 T





# PoCA analysis can be used to estimate the magnetic field flux density.

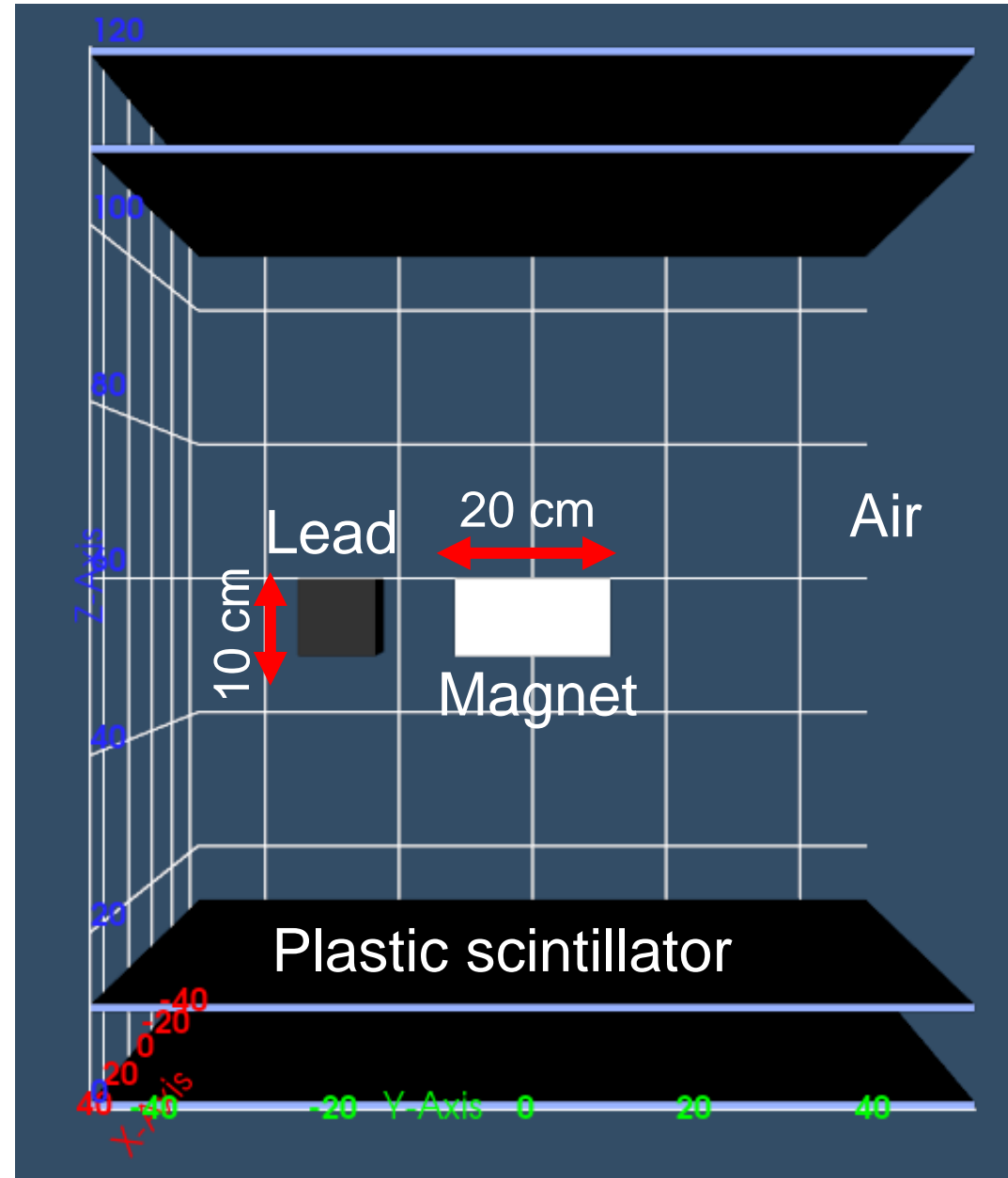


- 1T magnetic field of 10 cm thick cause the ratio of PoCA points inside the target change from 56% to 9%.

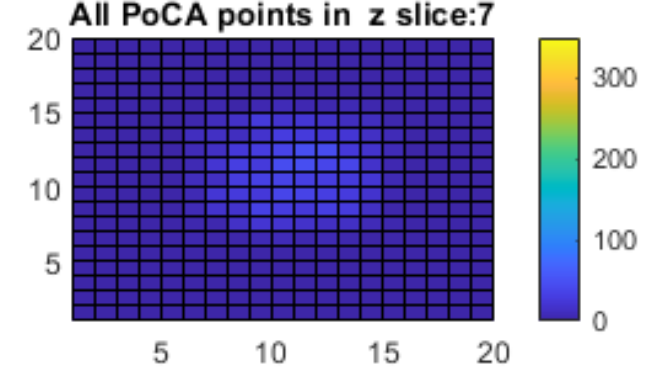
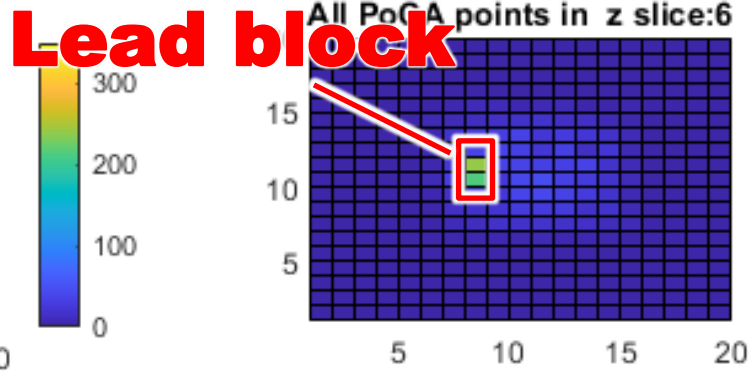
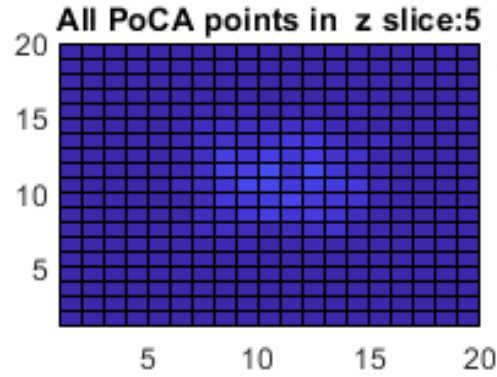


# Magnetic field imaging and magnetic flux estimation using PoCA points

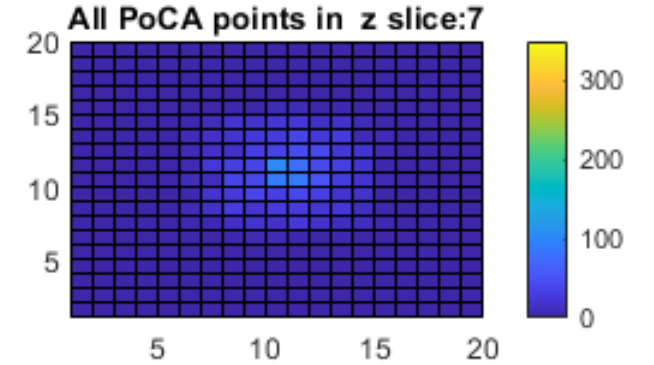
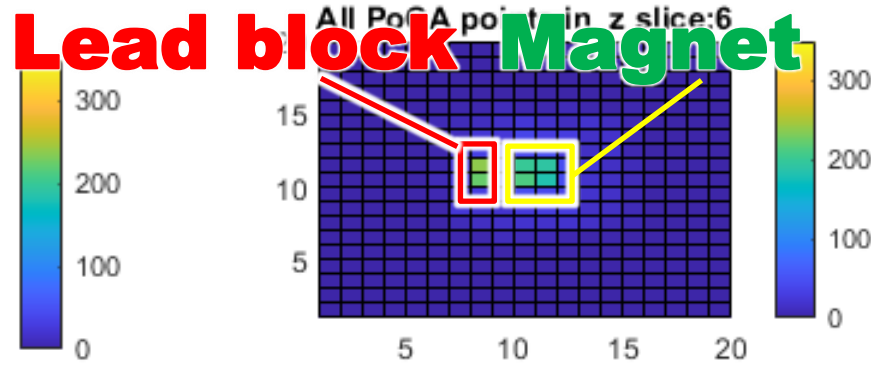
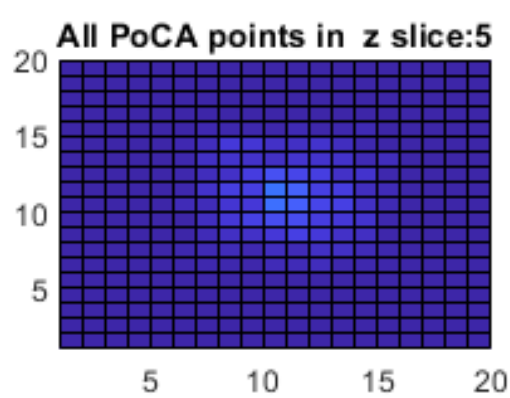
- PARMA Source
- Measurement time: one hour
- Voxel size: 10 cm x 10 cm x 10 cm



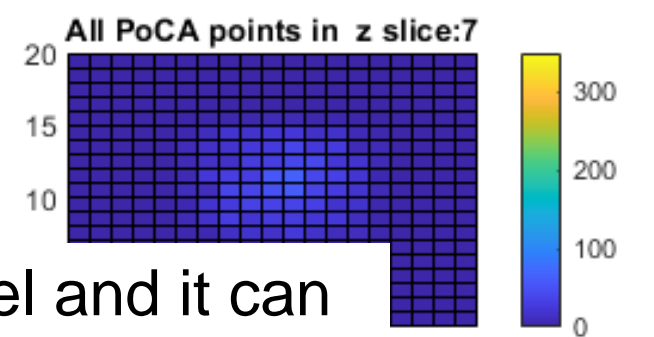
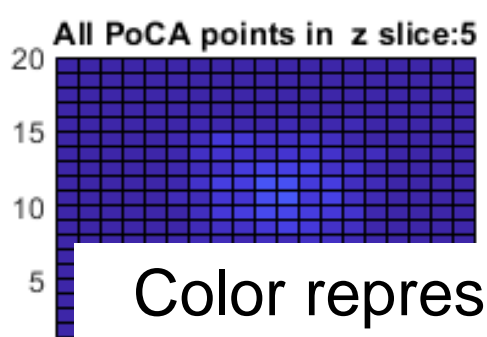
No magnet



0.55 T



1 T

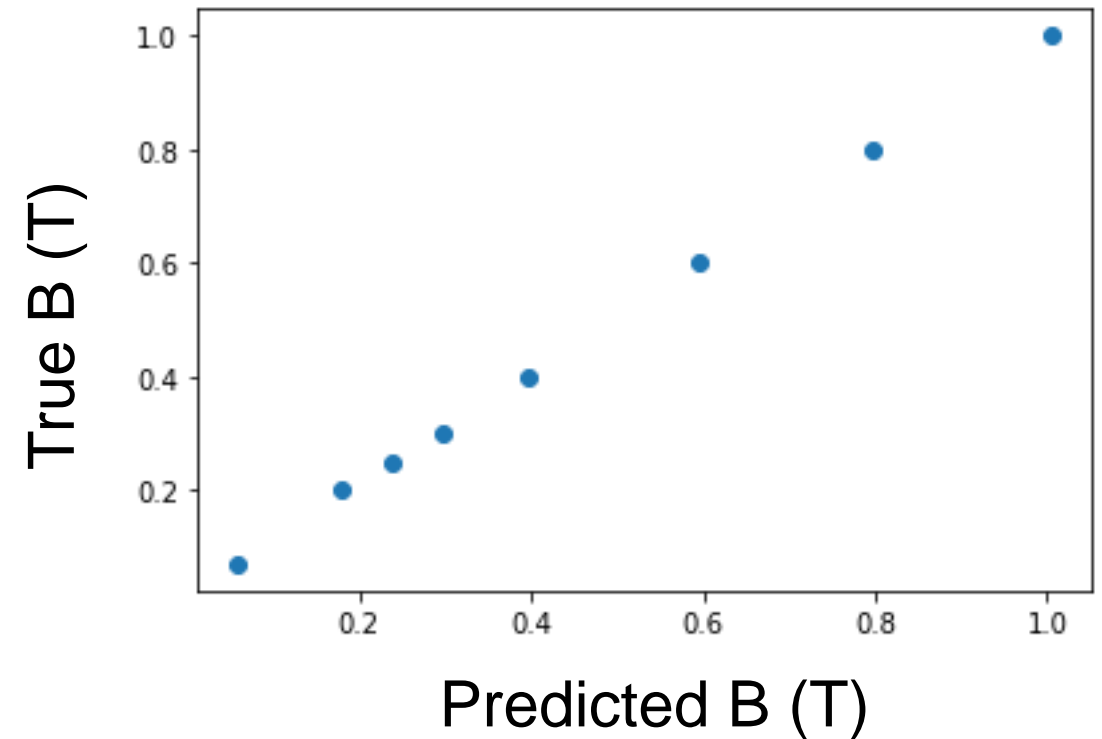


Color represent number of PoCA points per voxel and it can show the strength of magnetic field



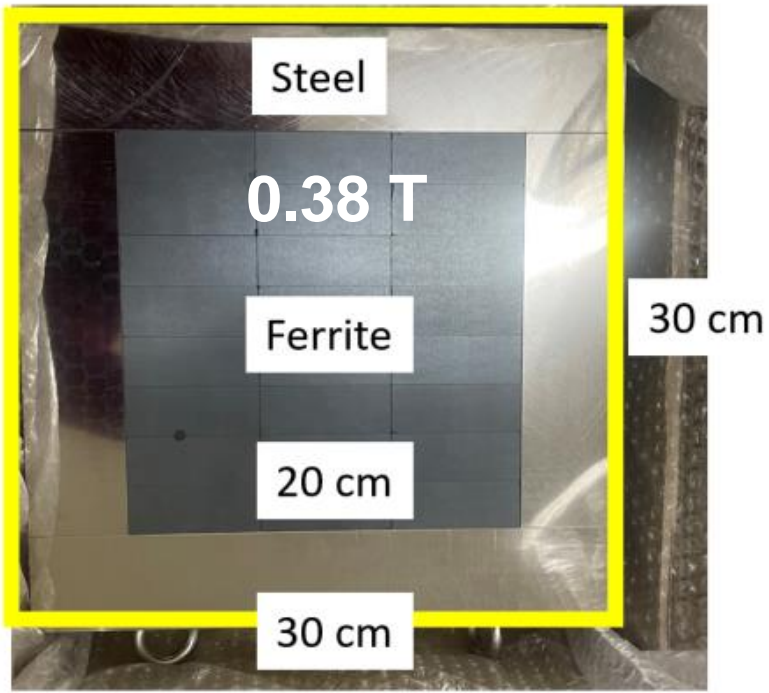
We repeat the simulations with many magnetic field flux densities and extracted some features of PoCA points based on the position of points.

Results showed that using *linear regression* (ordinary least squares) magnetic field can be estimated with a Mean absolute percentage error of 4.1% for magnetic fields within (0.1 T to 1 T).



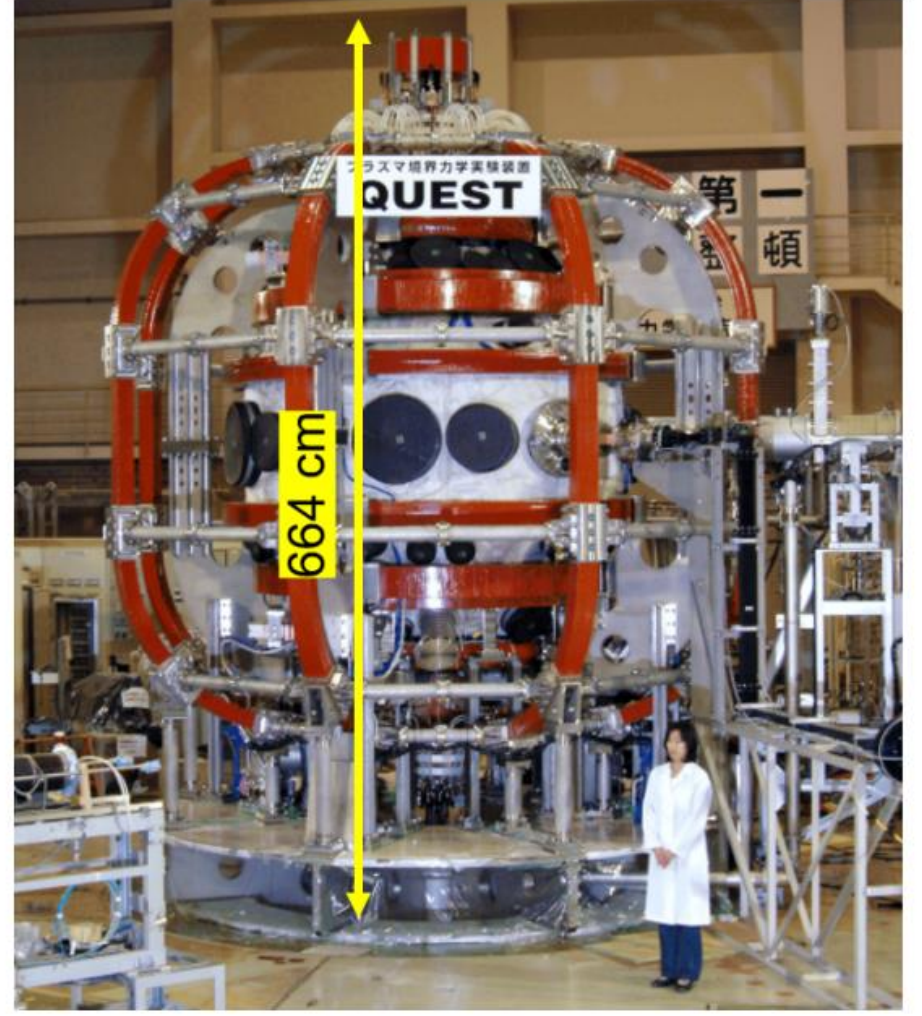
## Targets to be measured

For scattering muography



Magnetized ferrite  
vs.  
Non-magnetized ferrite

For absorption muography



Spherical Tokamak (QUEST)



## Summary

1. Preliminary simulation results showed that cosmic-ray muons have a **potential** to be used for magnetic field imaging.
2. Magnetic fields may have an impact on the **scattering angle distribution** and **imaging** using cosmic-ray muons and this may cause difficulties in material detection!



# Thank you for your attention!

Any feedback, comments, or questions are welcomed!

Please feel free to reach us at:

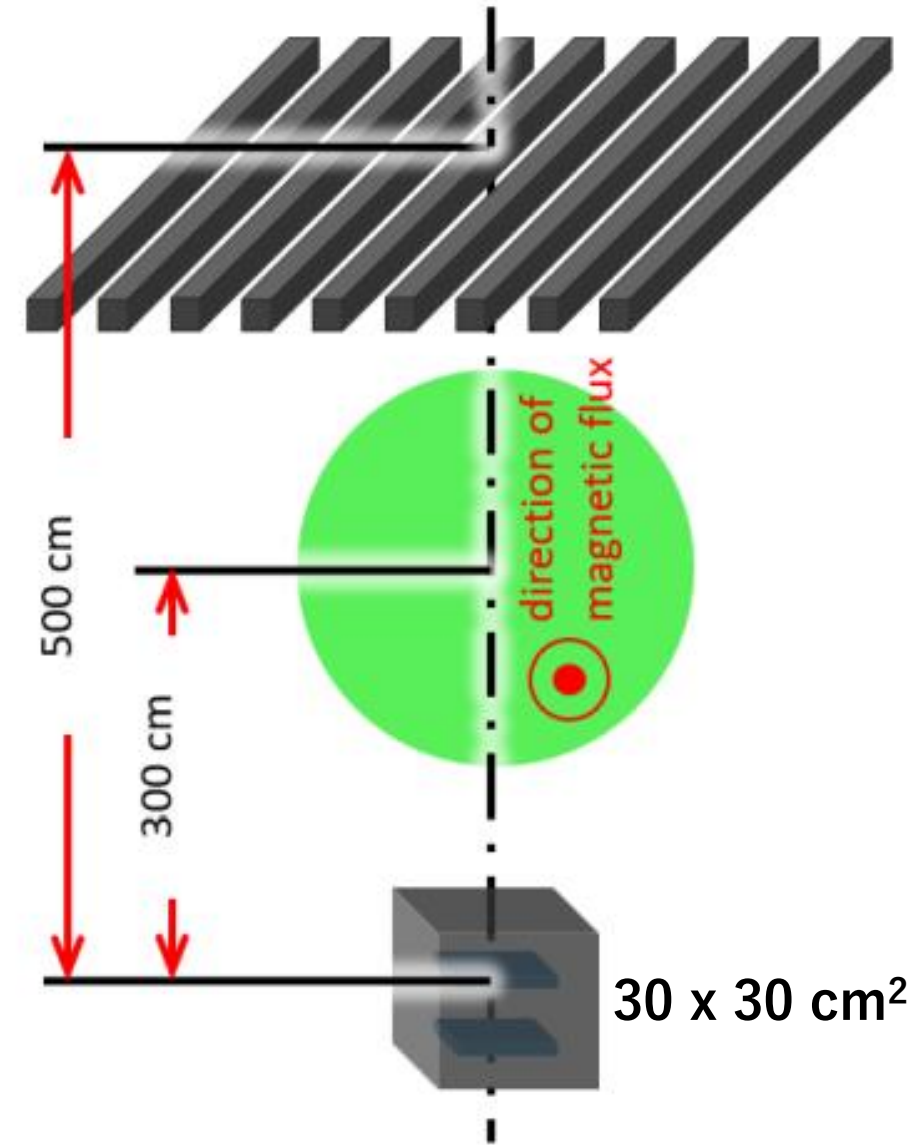
[kin@aees.kyushu-u.ac.jp](mailto:kin@aees.kyushu-u.ac.jp)

[Andrea.Giammanco@cern.ch](mailto:Andrea.Giammanco@cern.ch)

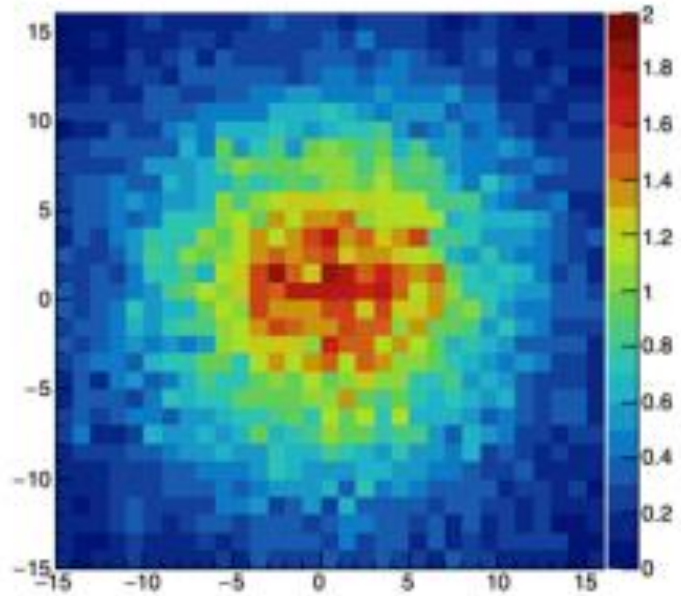
[Basiri.hamid@kyudai.jp](mailto:Basiri.hamid@kyudai.jp)

One-hour cosmic-ray muons by  
PARMA source at Tokyo on Jan. 1, 2020

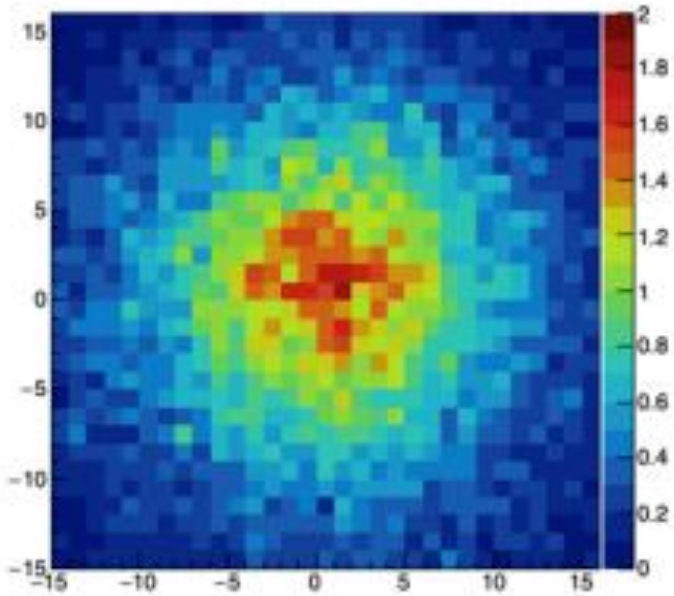
- Lead bars:  $30 \times 30 \times 700 \text{ cm}^3$
- Lead bars placed before the magnetic field to make the background muography image.
- Magnetic field applied is a dipole magnetic field (2T) with a radius of 130 cm spherical shape.



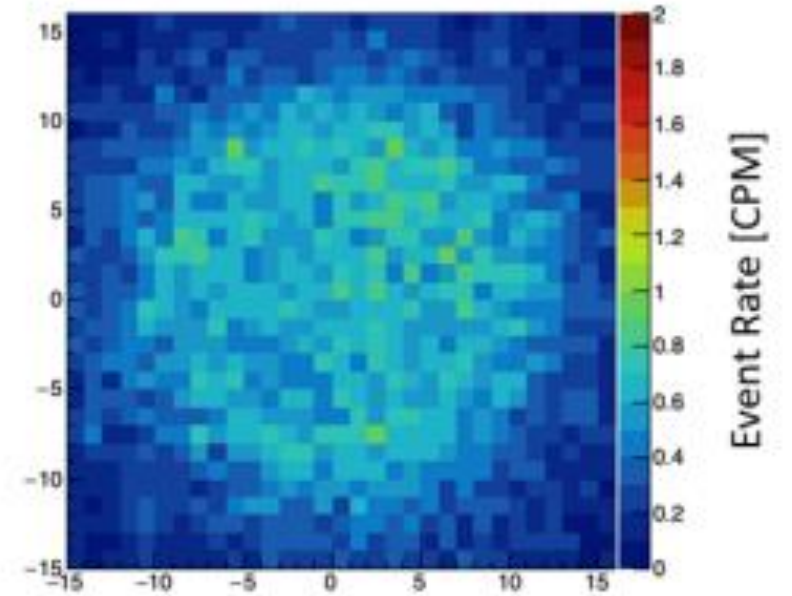
## Count Rate Maps



(a) Open Sky

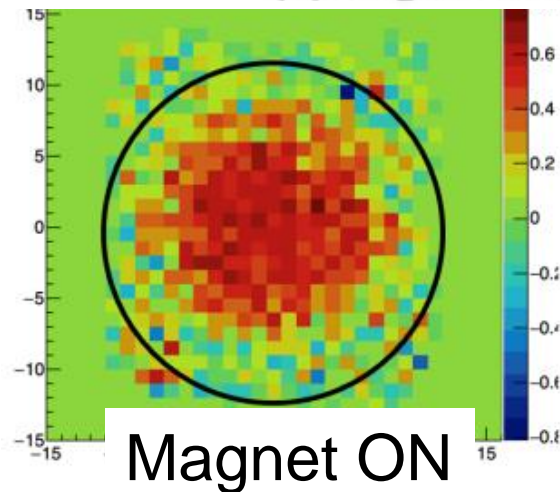


(b) Magnetic Field OFF

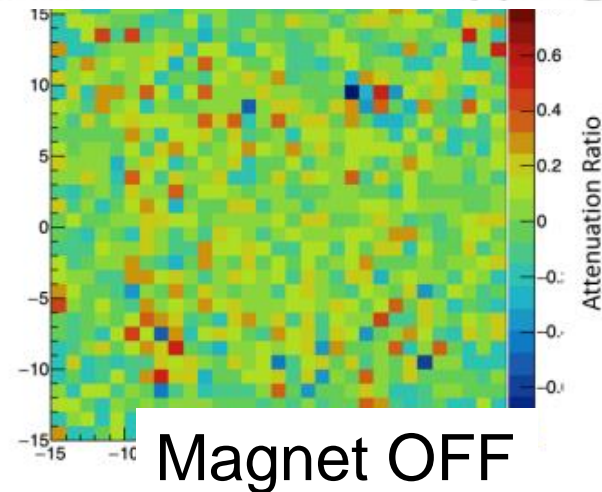


(c) Magnetic Field ON

## Attenuation Ratio Maps



Magnet ON



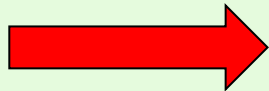
Magnet OFF





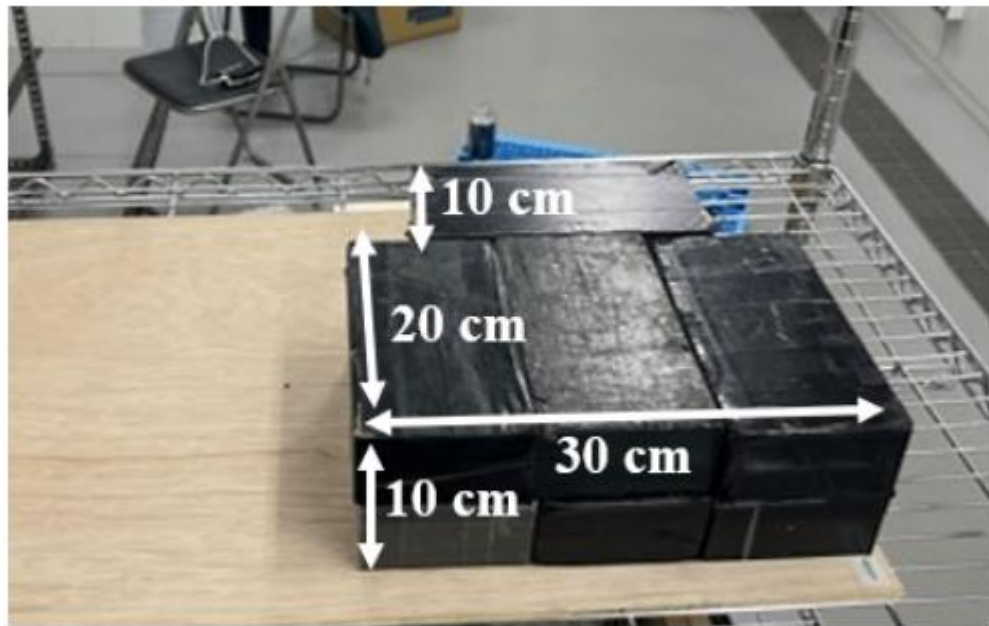
## Muons Deflected back estimation using PARMA model and analytical equations

- Using the derived equations and PARMA model, the threshold energy of muons that cannot penetrate a magnetic field of 2T and a thickness of 1.3m is 556 MeV.
- This threshold corresponds to 13.5% of the total muons, a significant value given that an absorption of a few percent can provide a muography image using the absorption method.

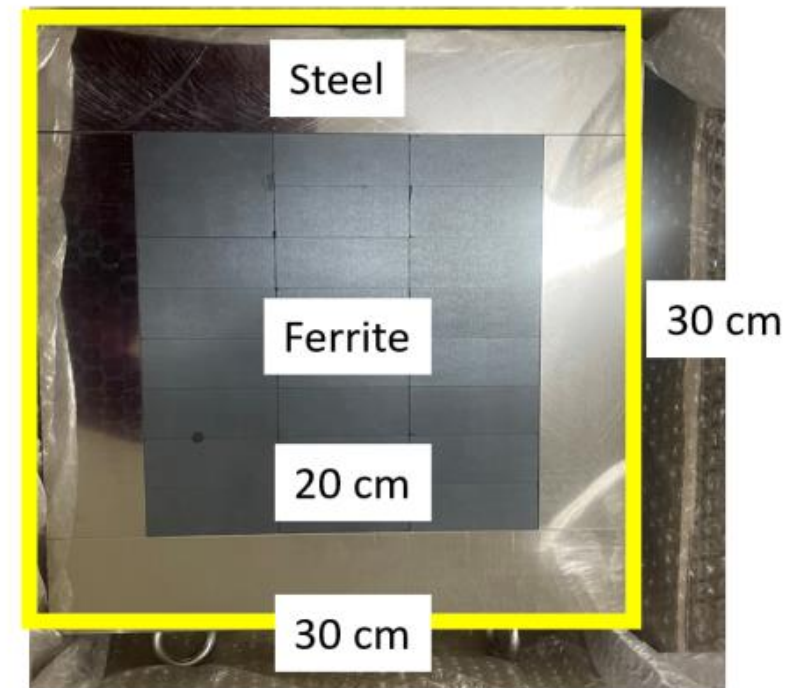
**What is the solution??**  Charge identification!

- ❑ The key point is that the deflection due to the magnet is not random while multiple scattering is random!
- ❑ If images obtained by  $\mu^+$  and  $\mu^-$  are different there is a magnetic field.

- Experiment designed to validate the magnetic field measurement using cosmic-ray muons considering targets such as electric car motor
- Ferrite-based magnet, non-magnetized ferrite for comparison and lead blocks to provide background muography image

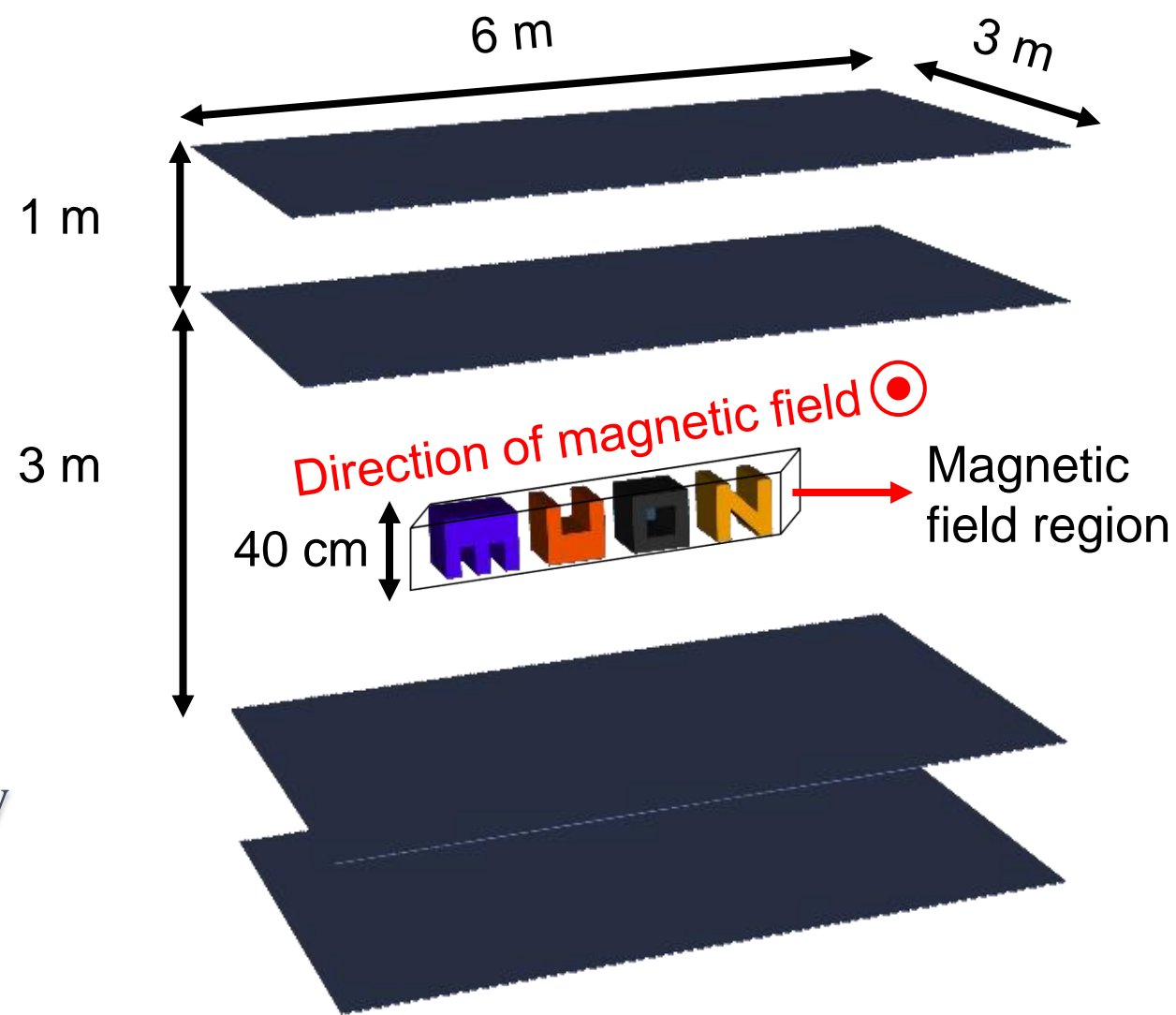


Lead blocks



Permanent magnet

20' Container DC/GP/HD



- **Measurement time:** 13 minutes

- **Source:** PARMA model at Kyushu University Chikushi Campus, January 2020

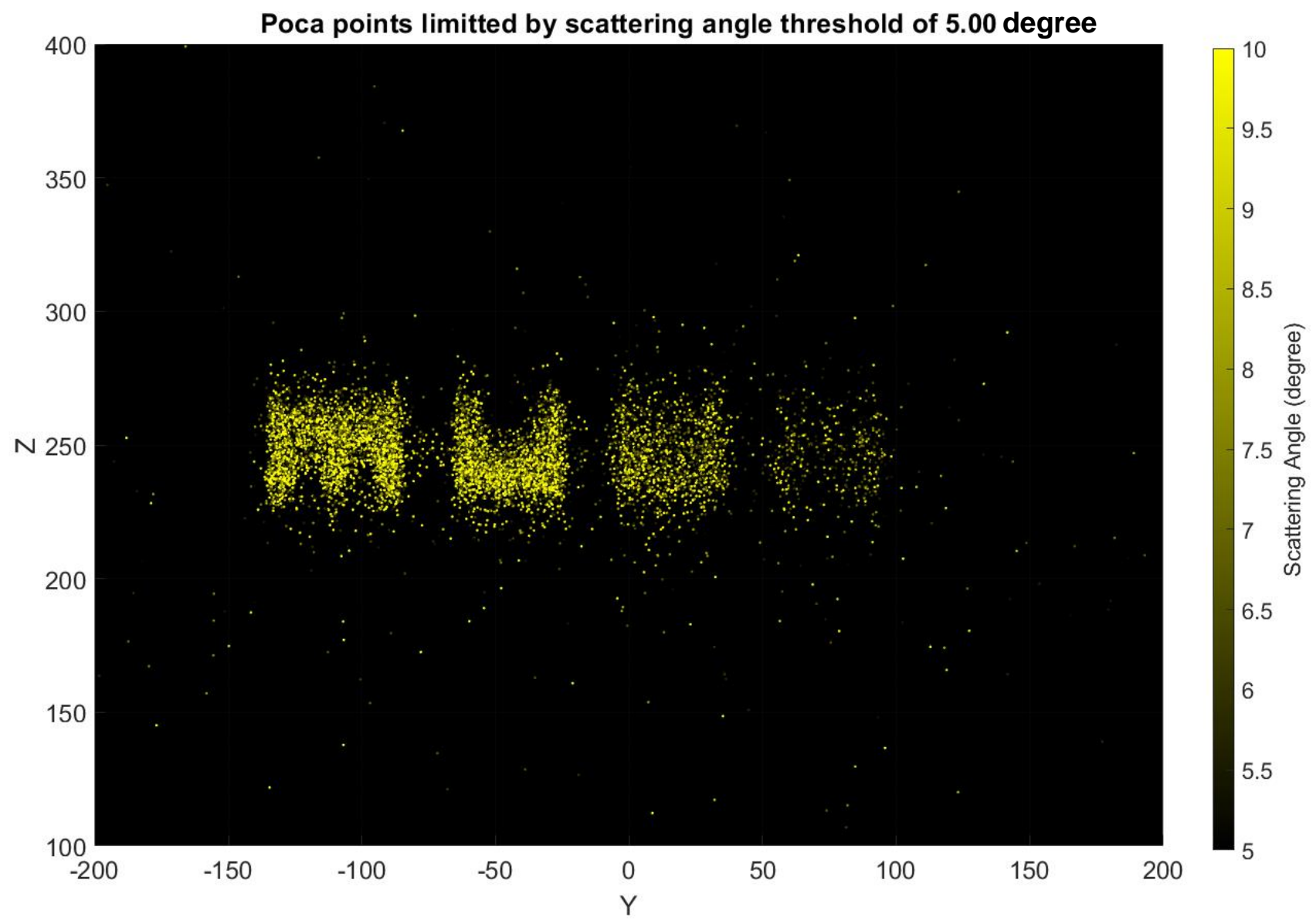
- **Materials:**

**M** : Uranium **U** : Lead **O** : Iron **N** : Aluminum

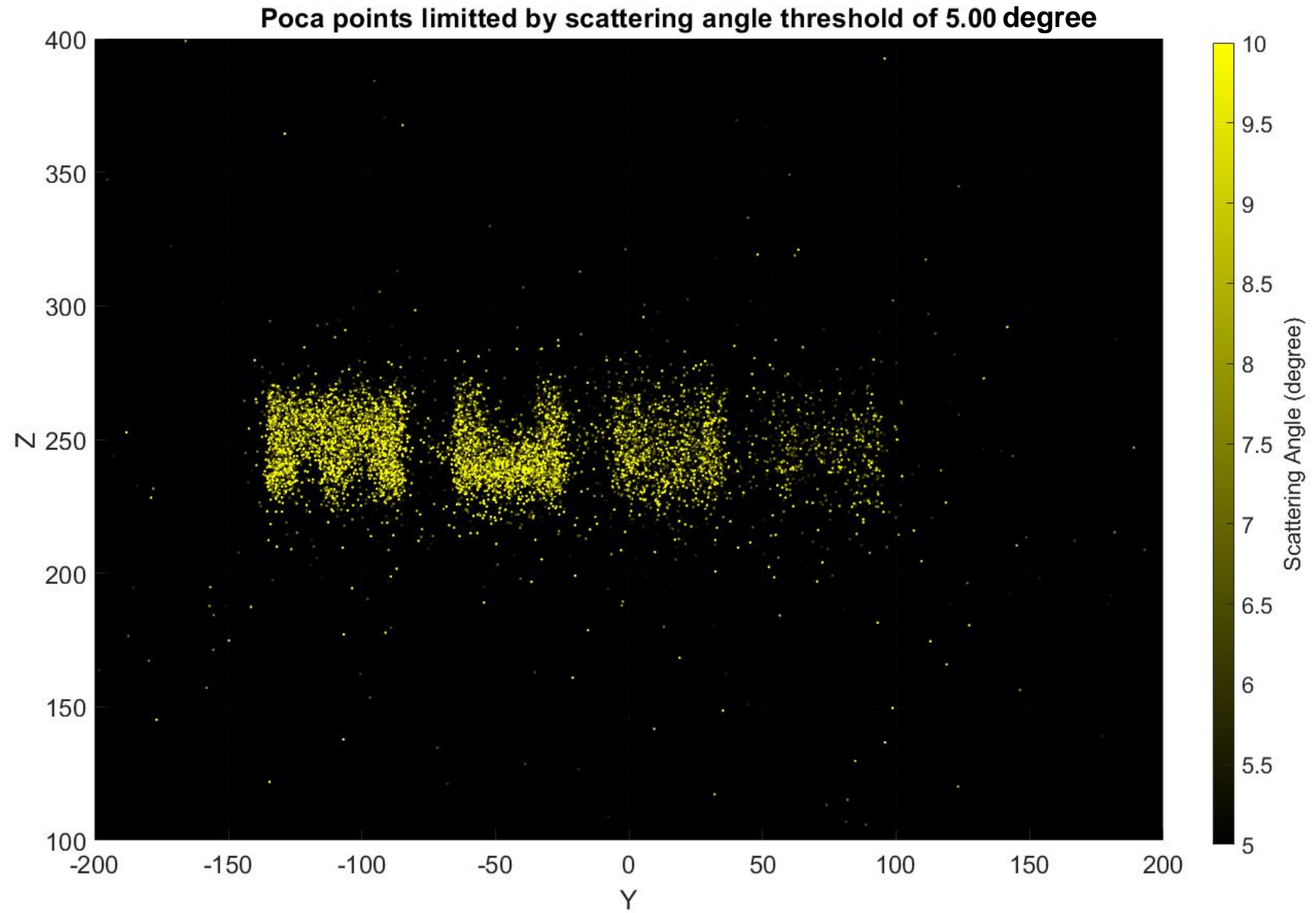
Density of the materials are decreasing from left to right!

- Geometry is similar to "La Rocca, Paola, et al. *Journal of Instrumentation* 9.01 (2014): C01056"

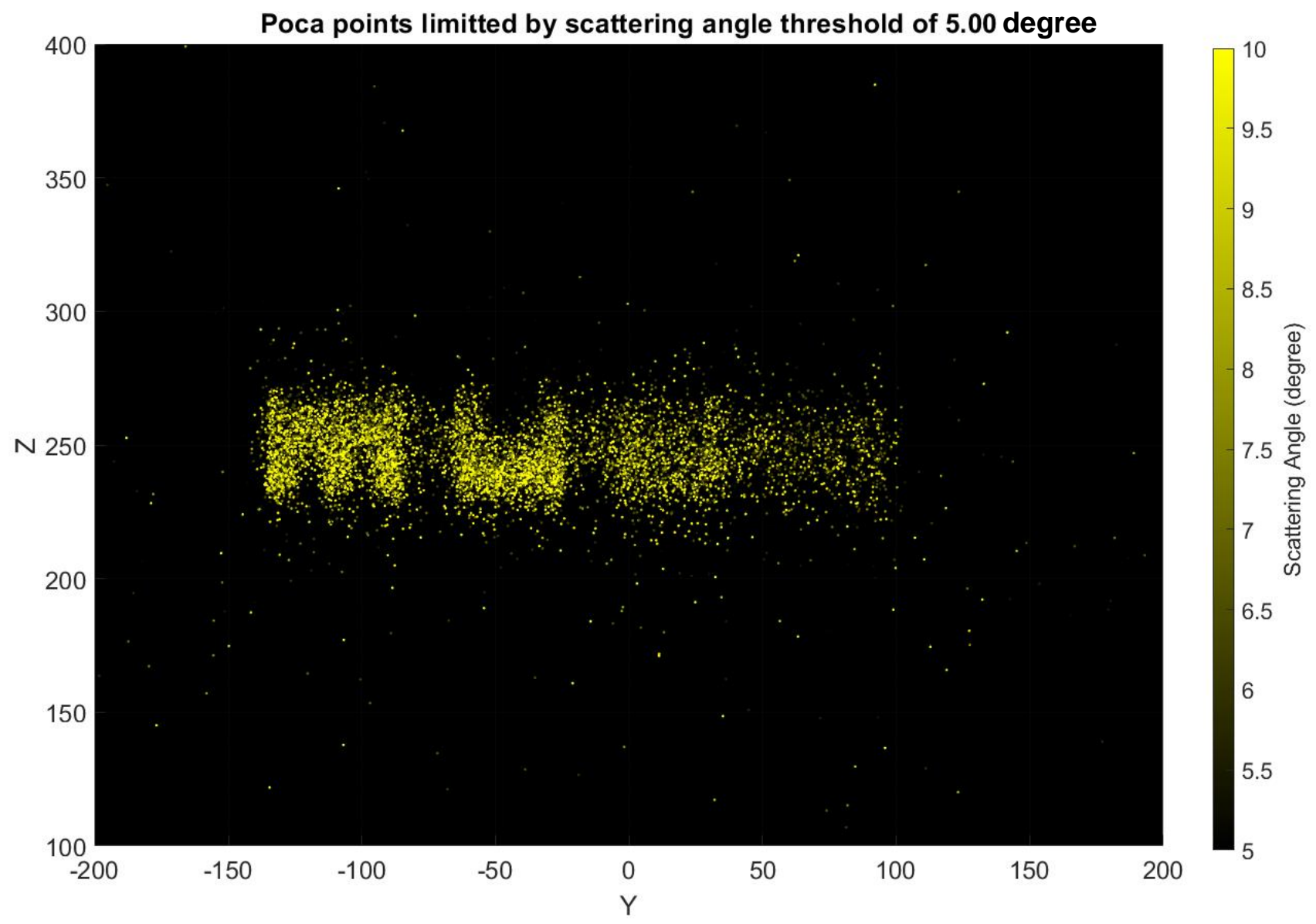
No Magnet



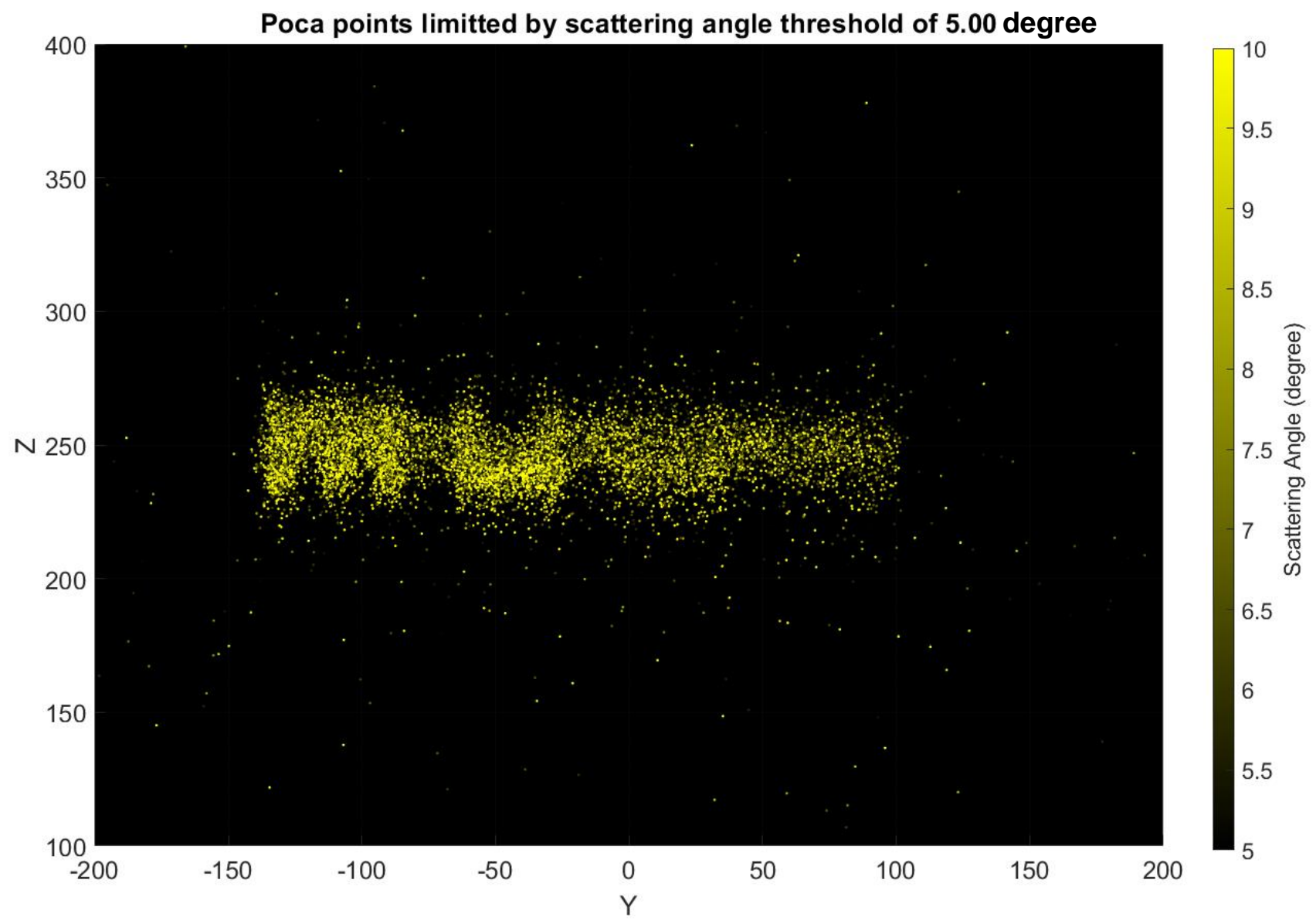
100 mT



200 mT

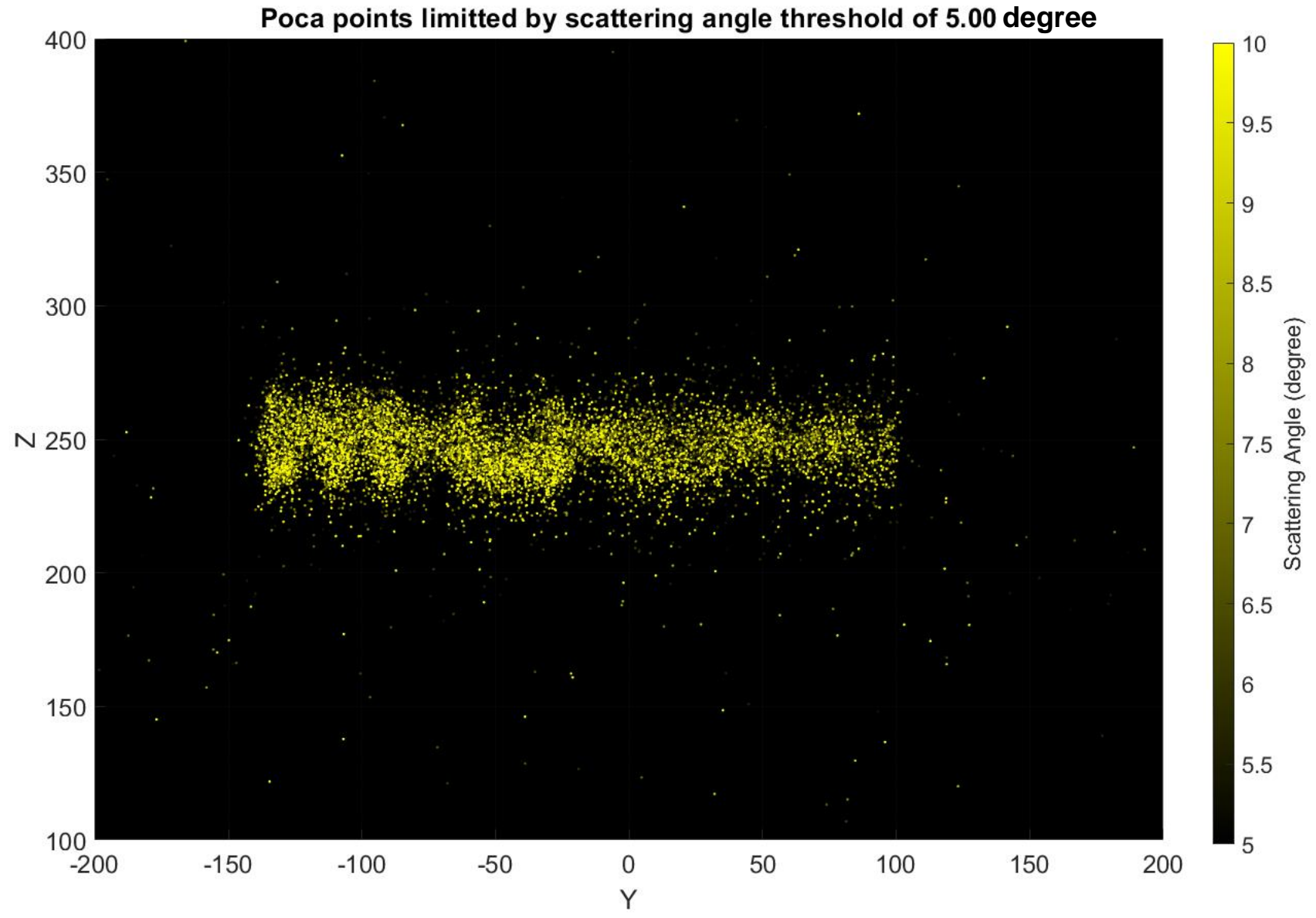


300 mT

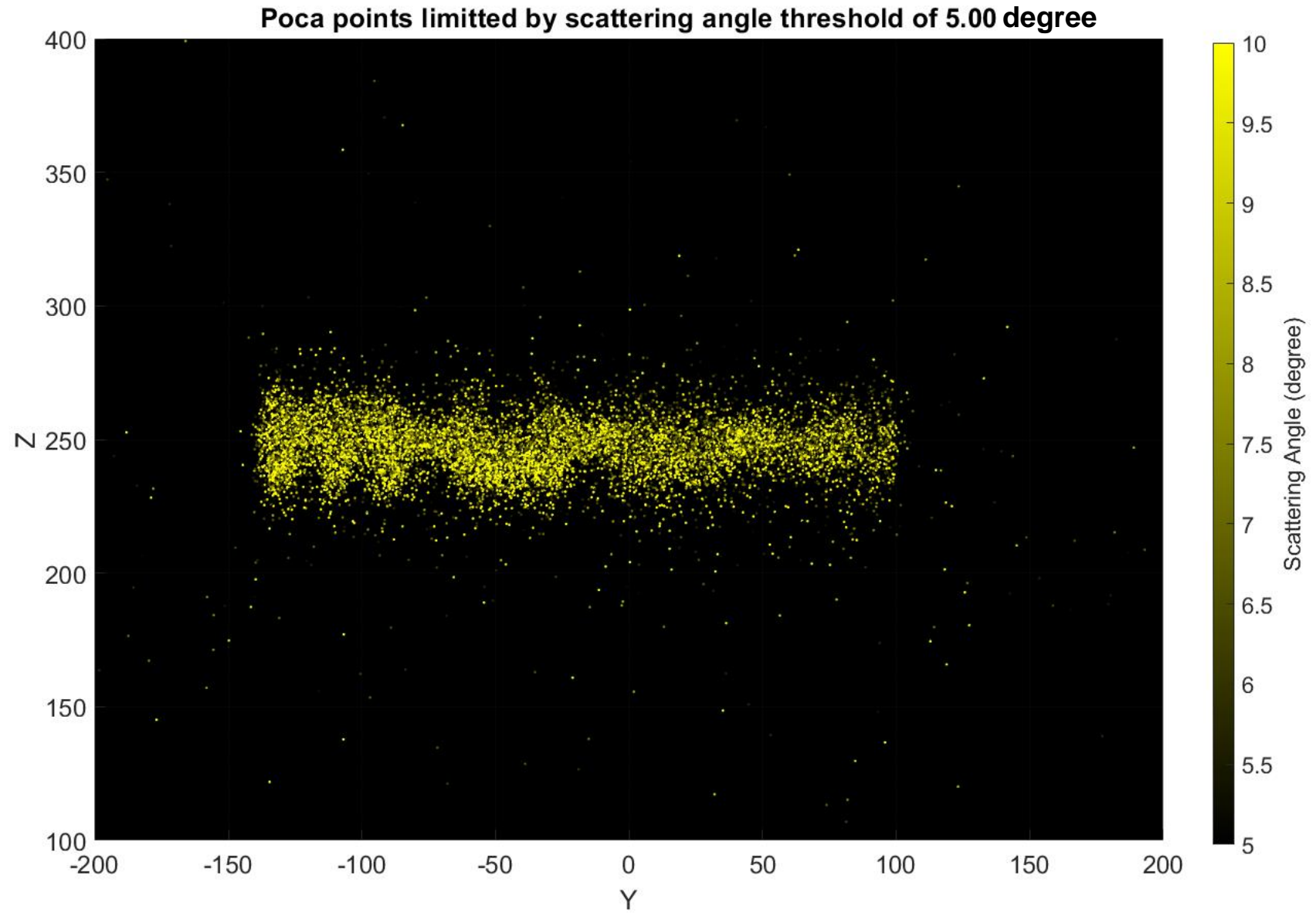




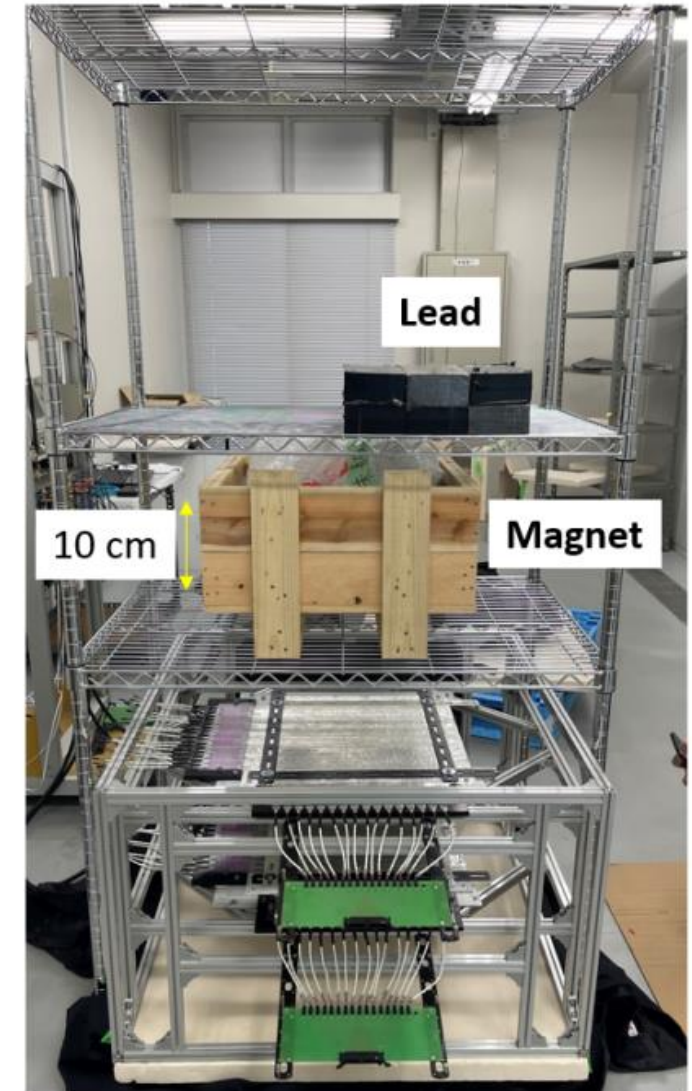
400 mT



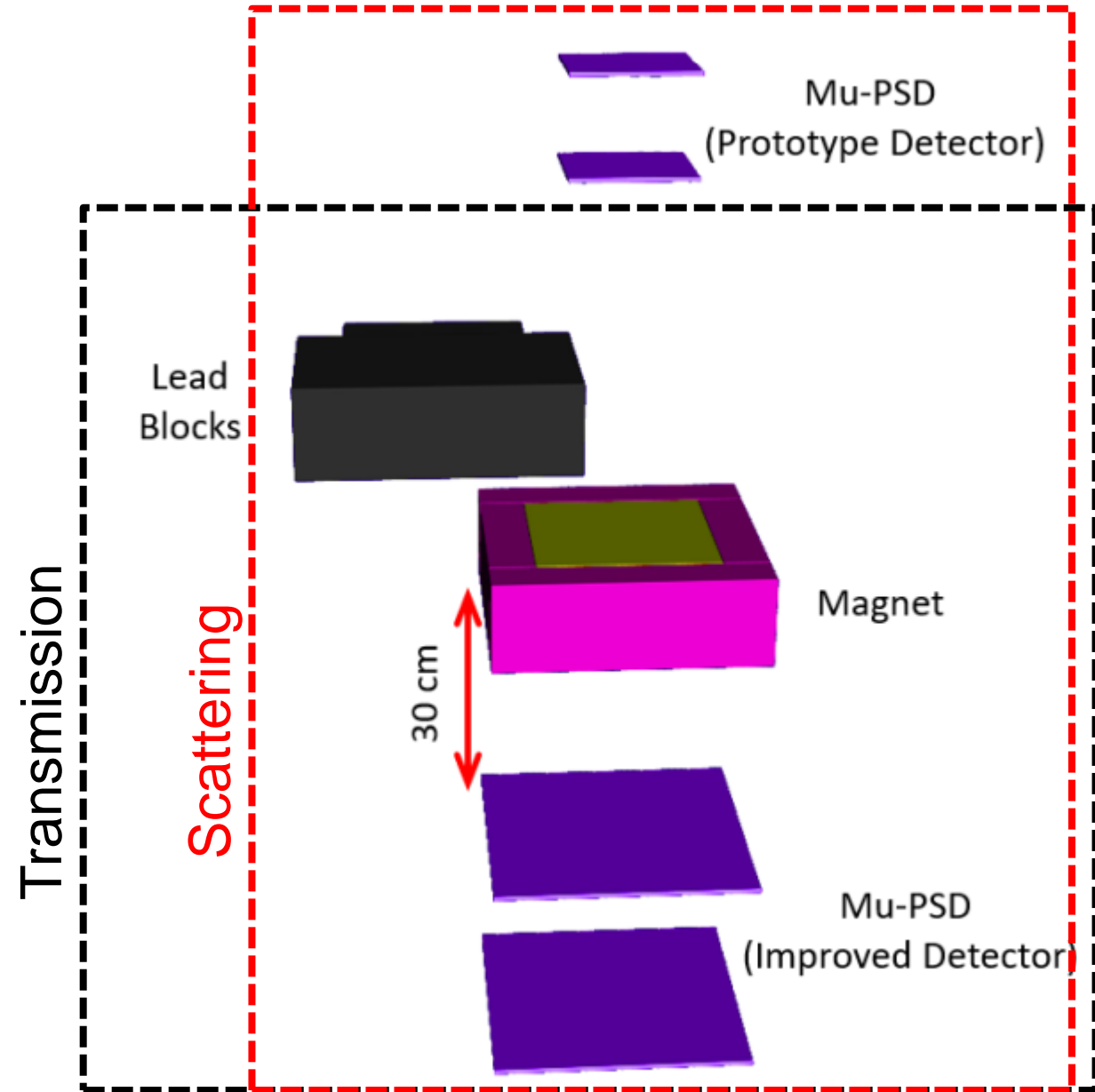
500 mT



- Two-mode experiment to gather data on muon trajectories through targets.
  - Absorption muography
  - Scattering muography

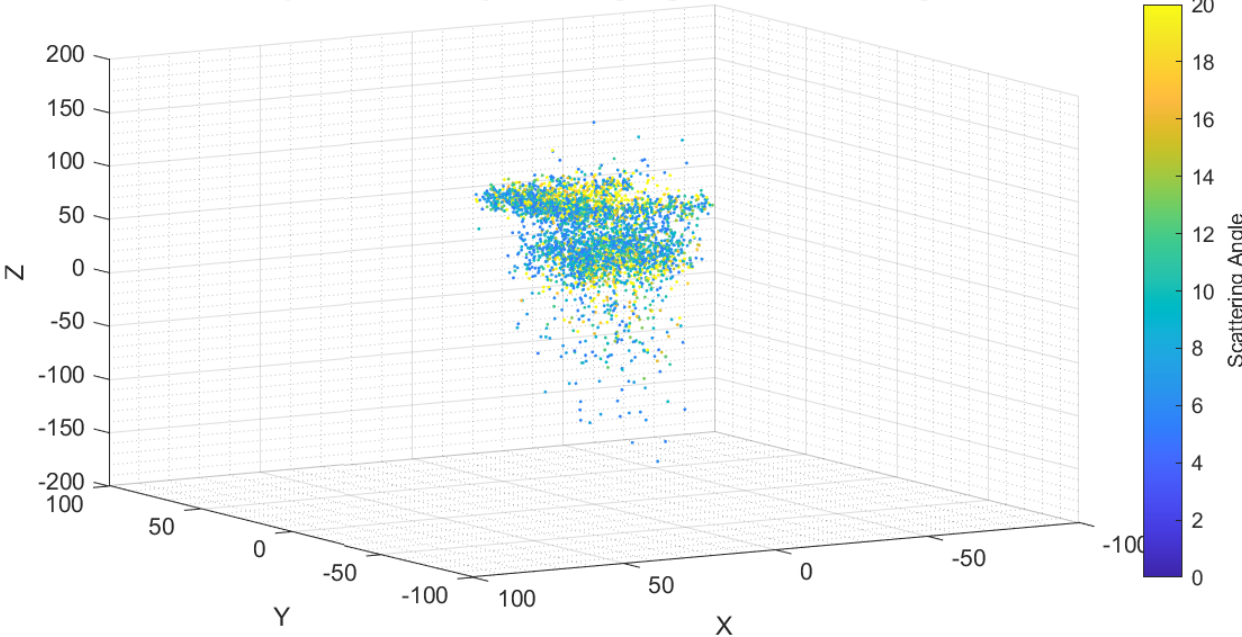


- Simulation for one-week real-time measurement.
- Different detector sizes used on top and bottom. Prototype detector on top and our improved detector in bottom.
- Conditions adjusted to match experiment frame and space limitations

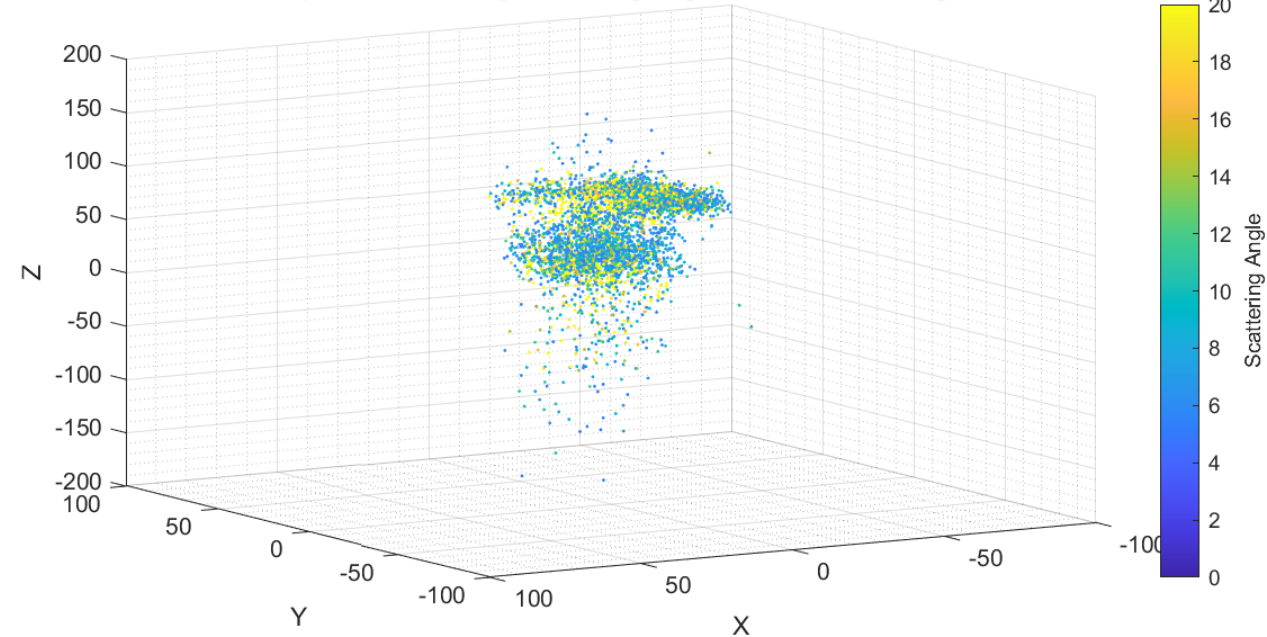


All PoCA points that has scattering angle more than 5 degree while the magnet is 3T

Poca points limited by scattering angle threshold of 5 degree



Poca points limited by scattering angle threshold of 5 degree



Simulations using four different materials  
(uranium, lead, aluminum, and iron)

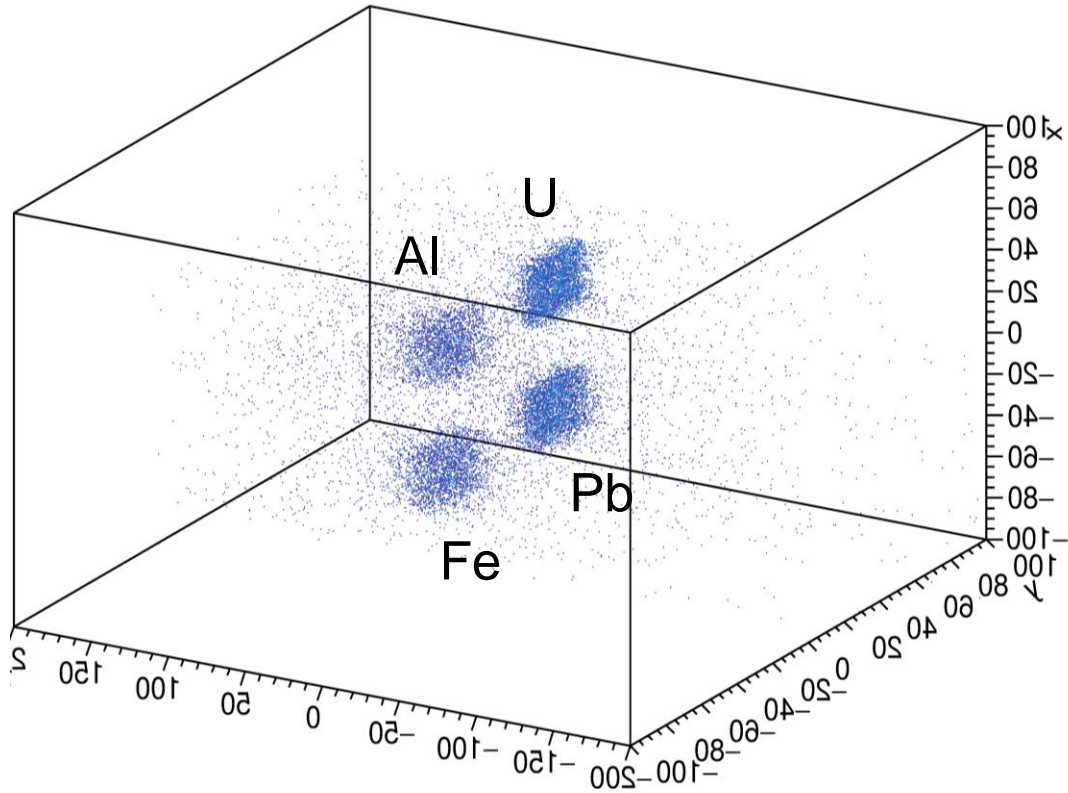
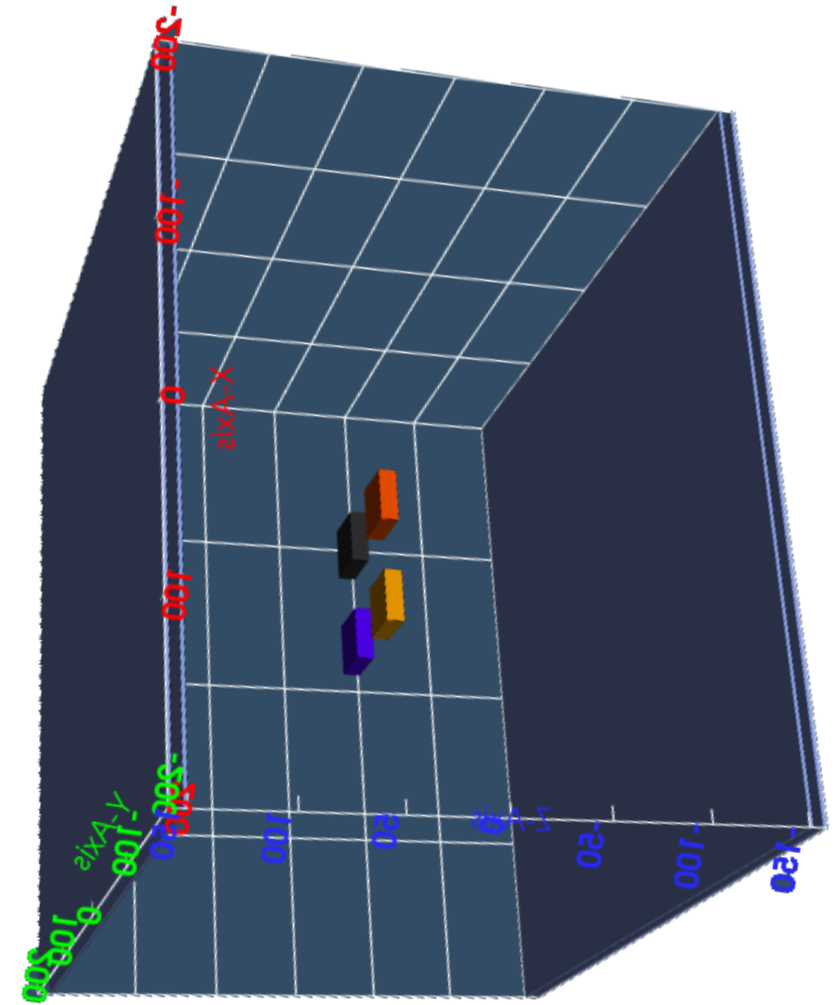
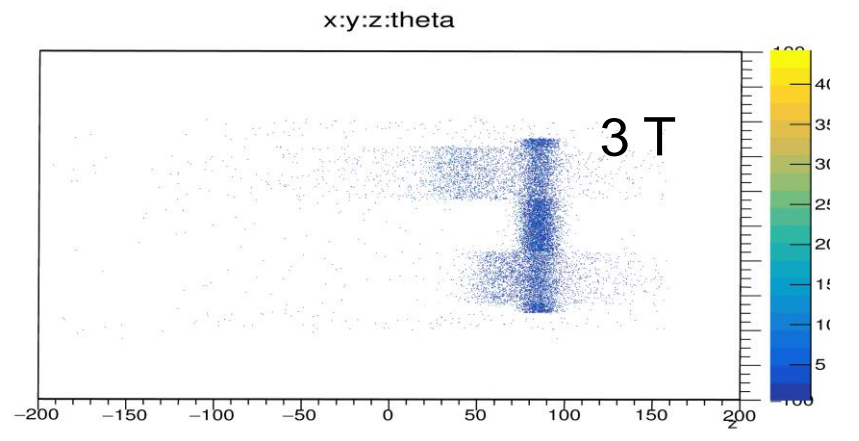
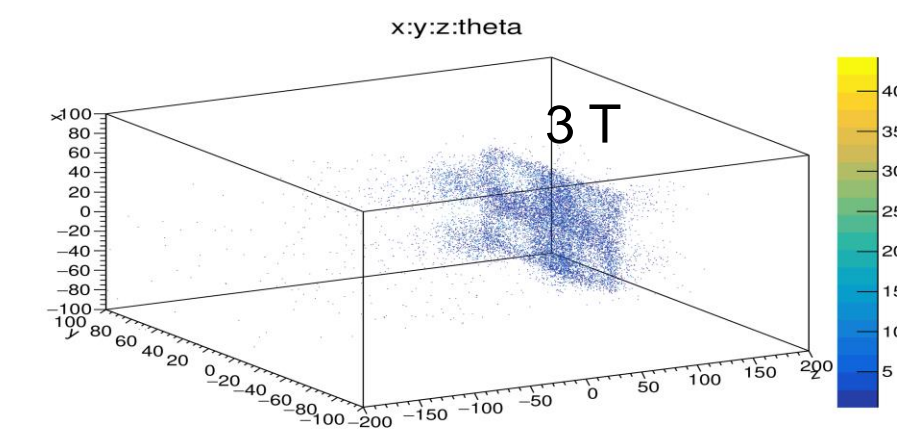
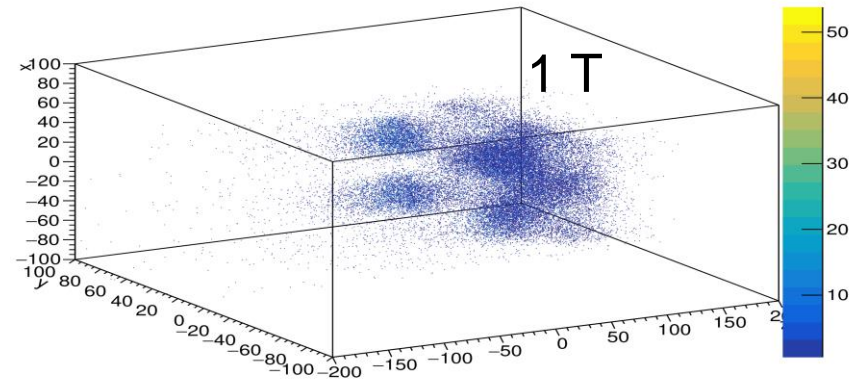
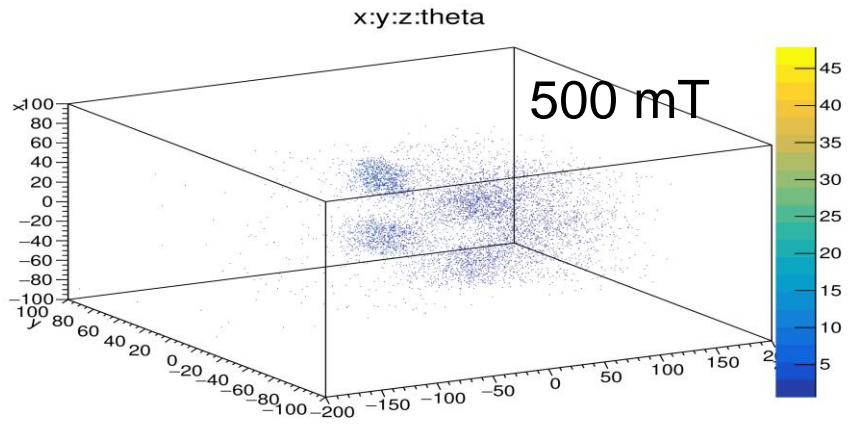
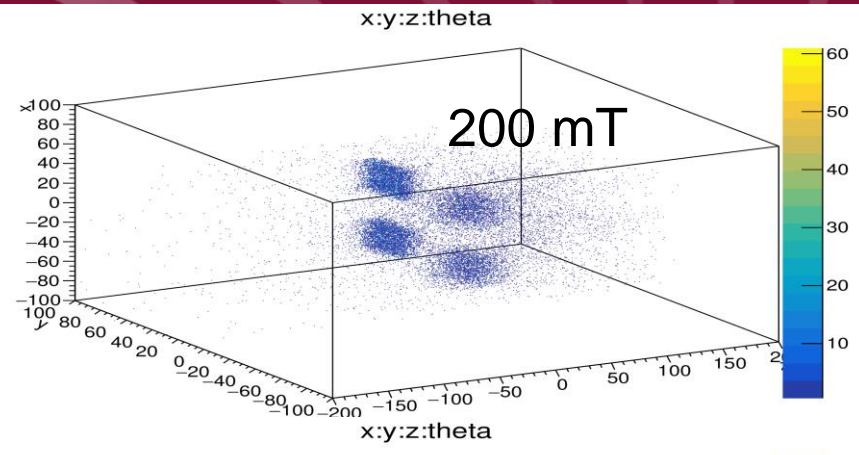
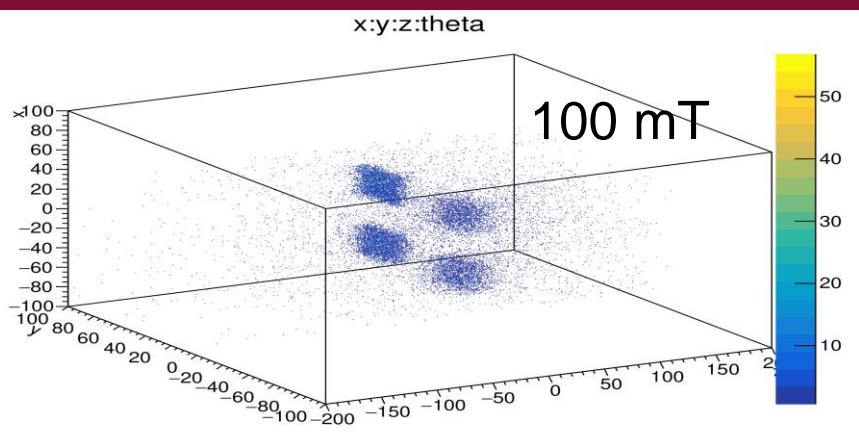


Image without magnetic field

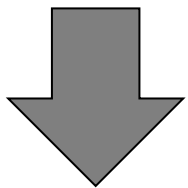


Simulation geometry in PHITS

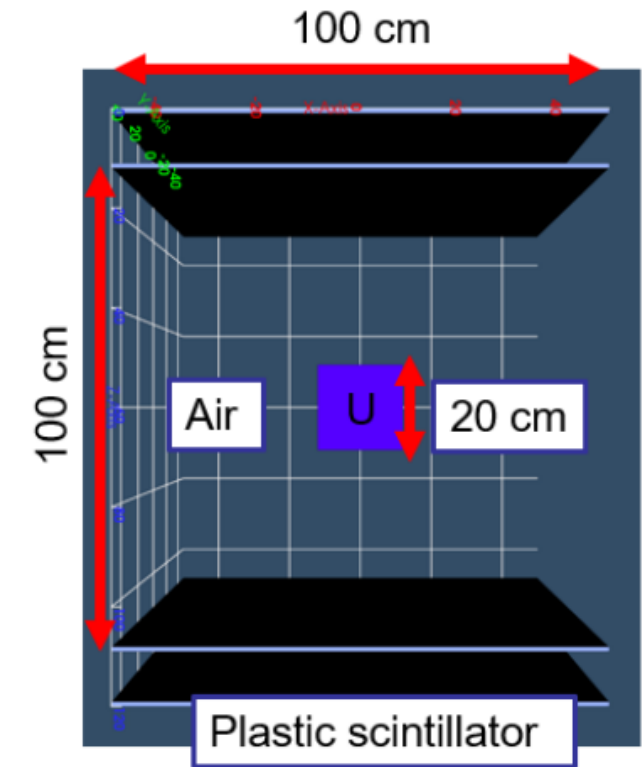
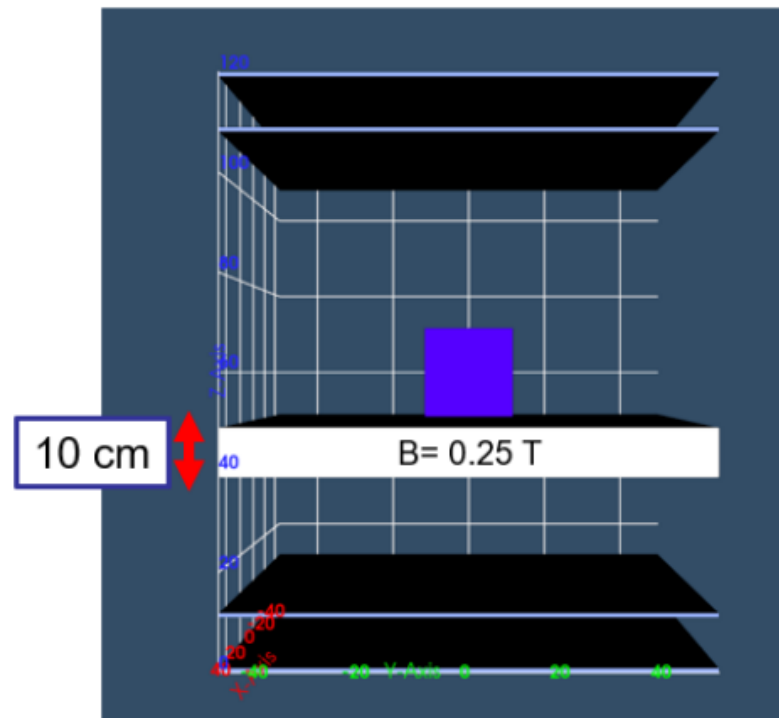


- **One-hour real-time measurement** muons source based on PARMA model.
- The simulation was conducted in two steps, obtaining the muography image of a uranium target and the distribution of PoCA points in a **voxelized** region of interest.

Voxel dimension:  
10 cm \* 10 cm \* 10 cm



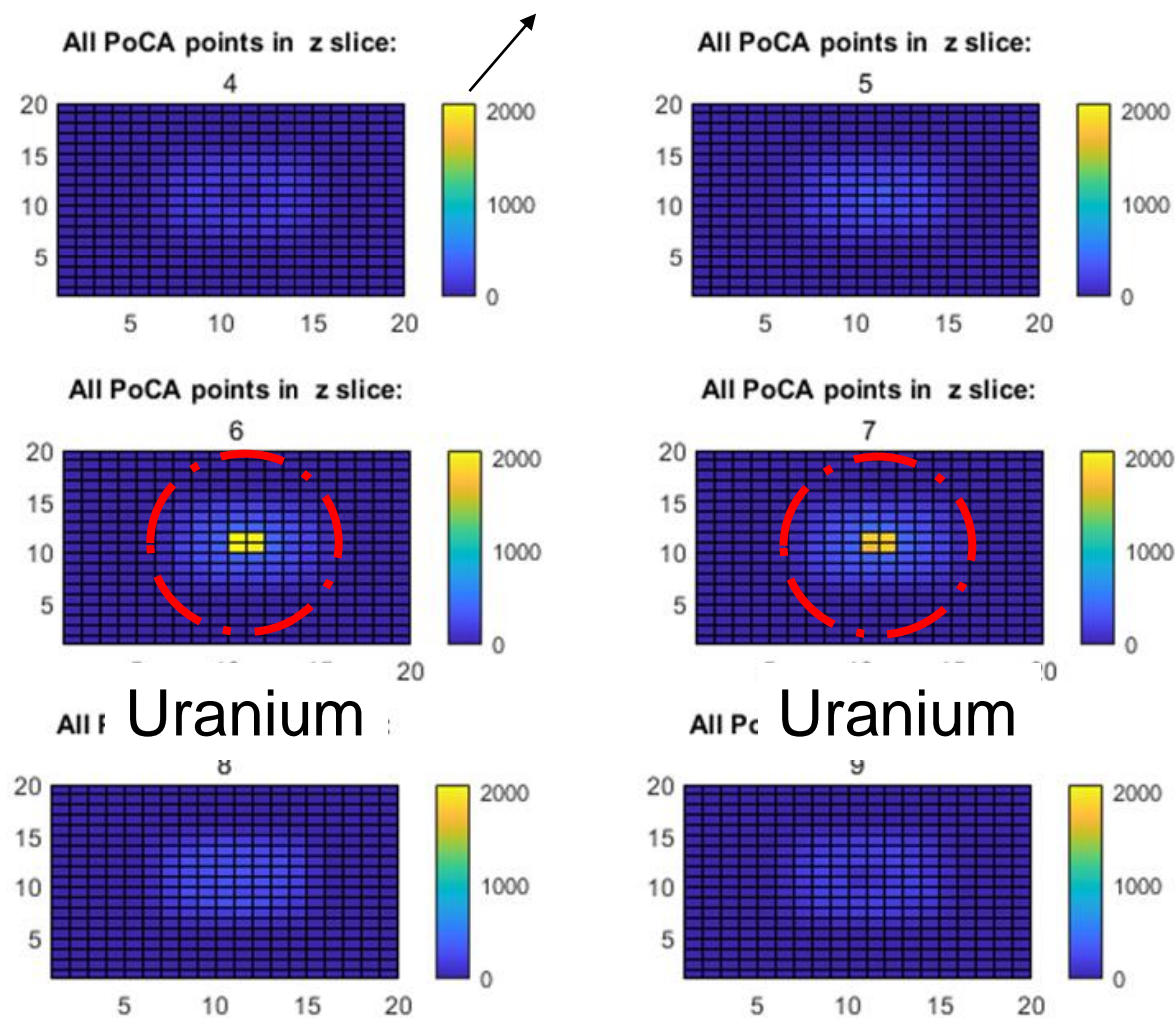
Uranium is made of 8  
voxels.  
(20 cm x 20 cm x 20 cm)



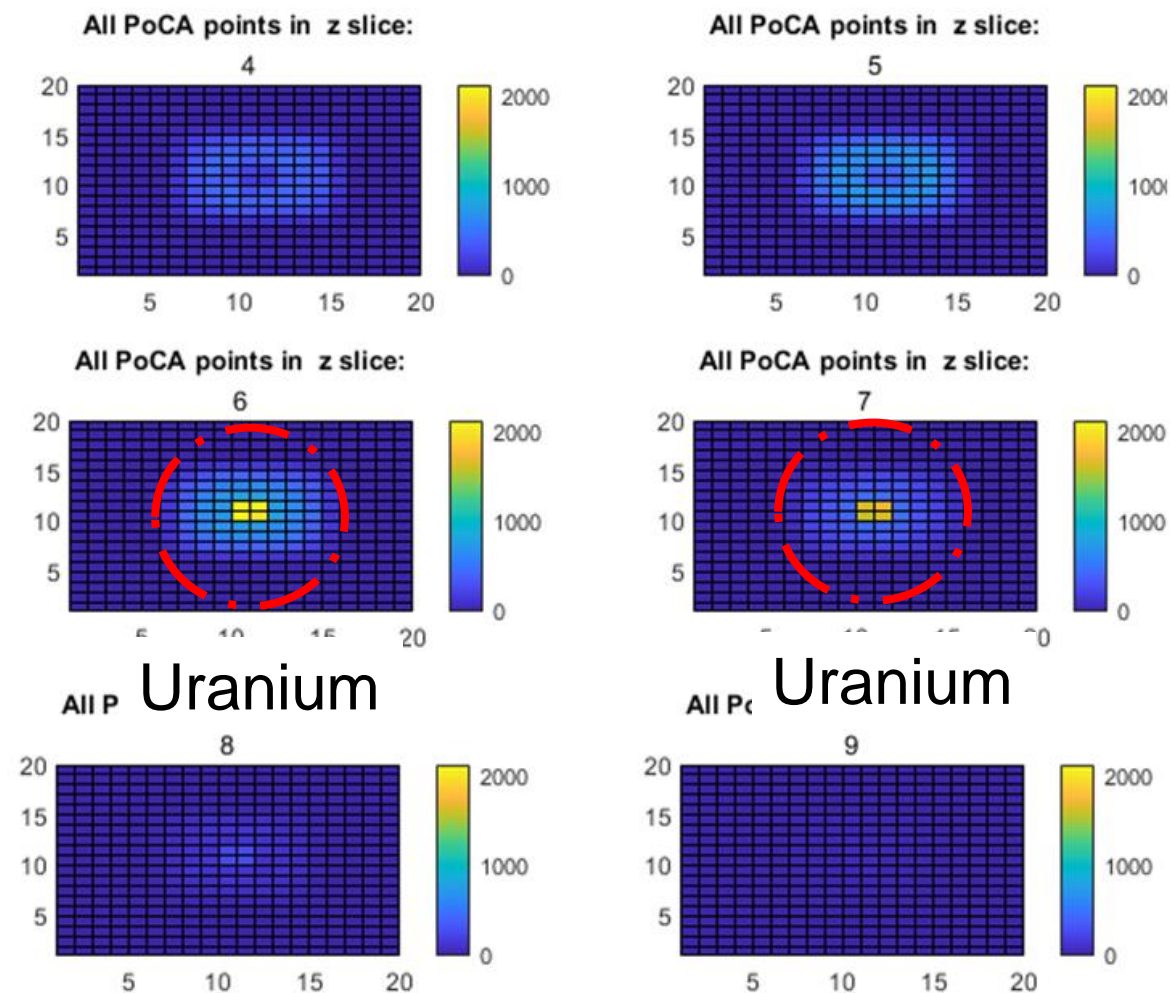


## Magnetic field OFF

Number of points per voxel



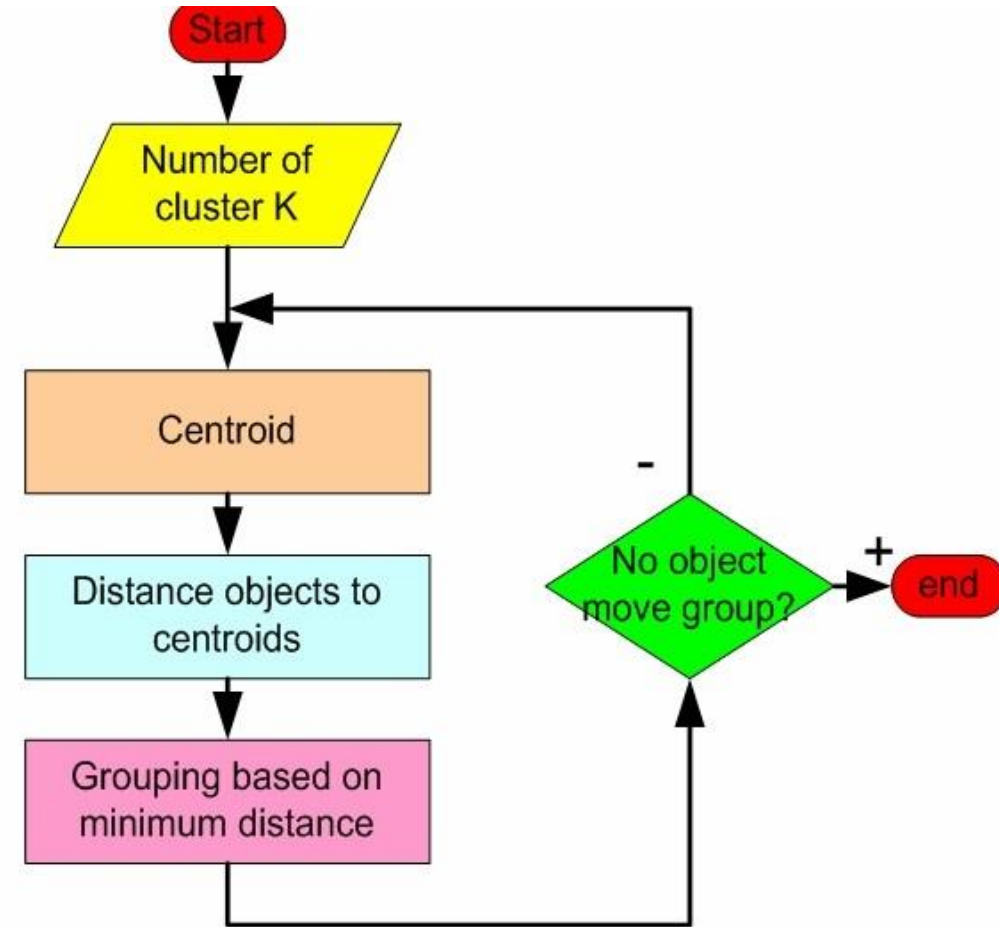
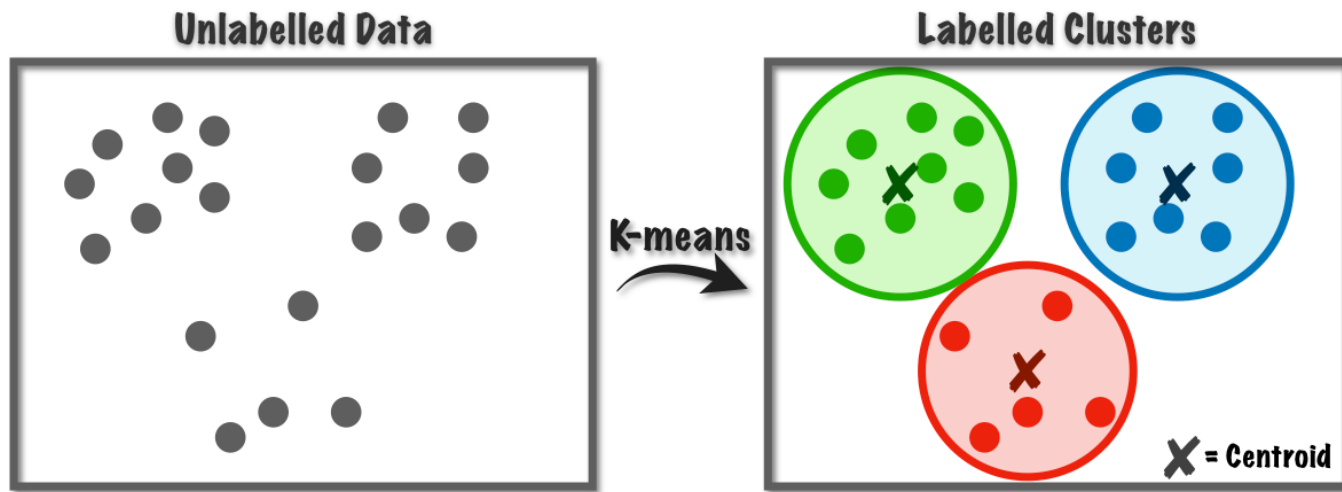
## Magnetic field ON





One method to distinguish nuclear materials in this systems is clustering of voxels

# K-means Clustering:

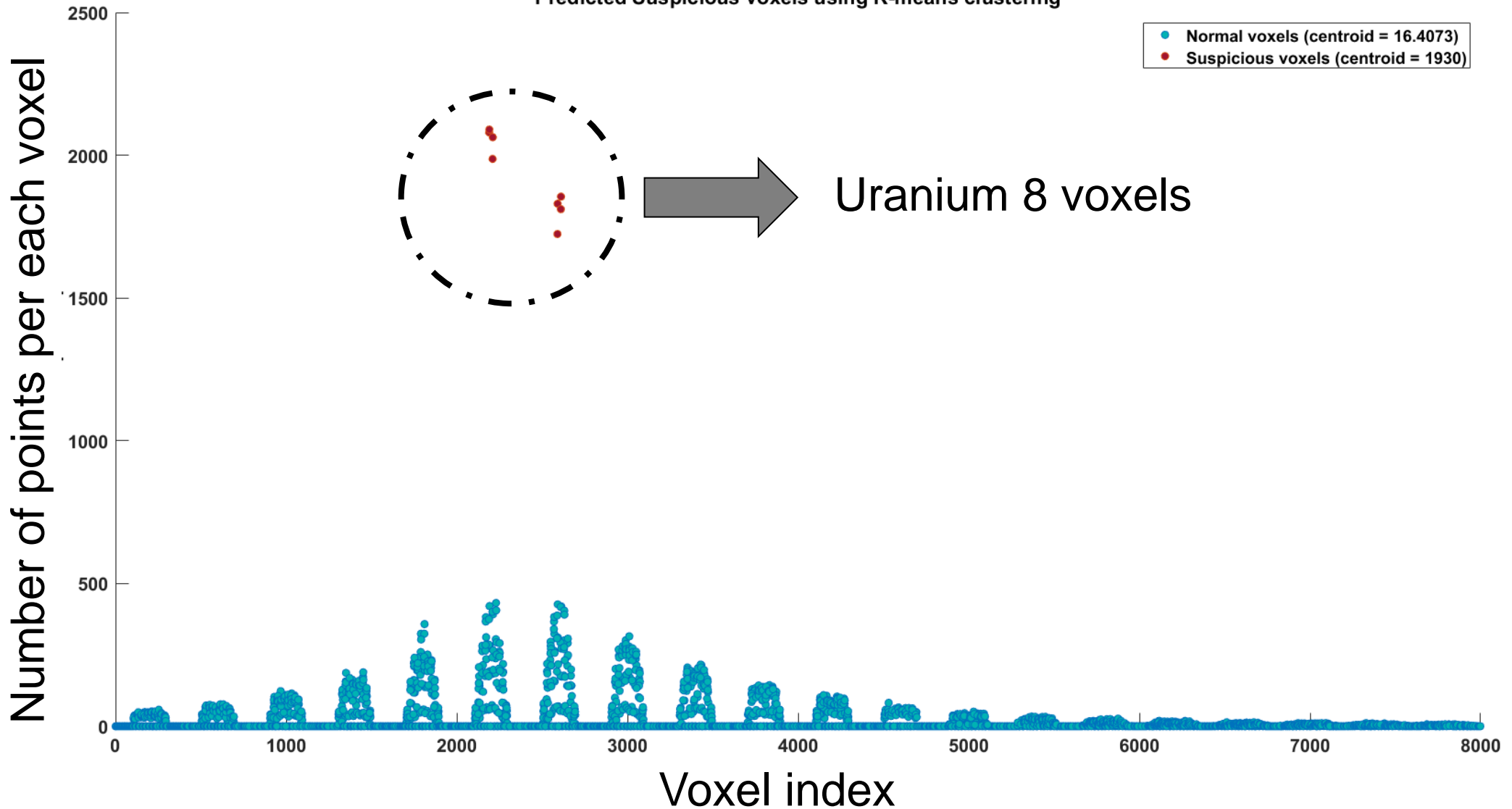


We used two clusters

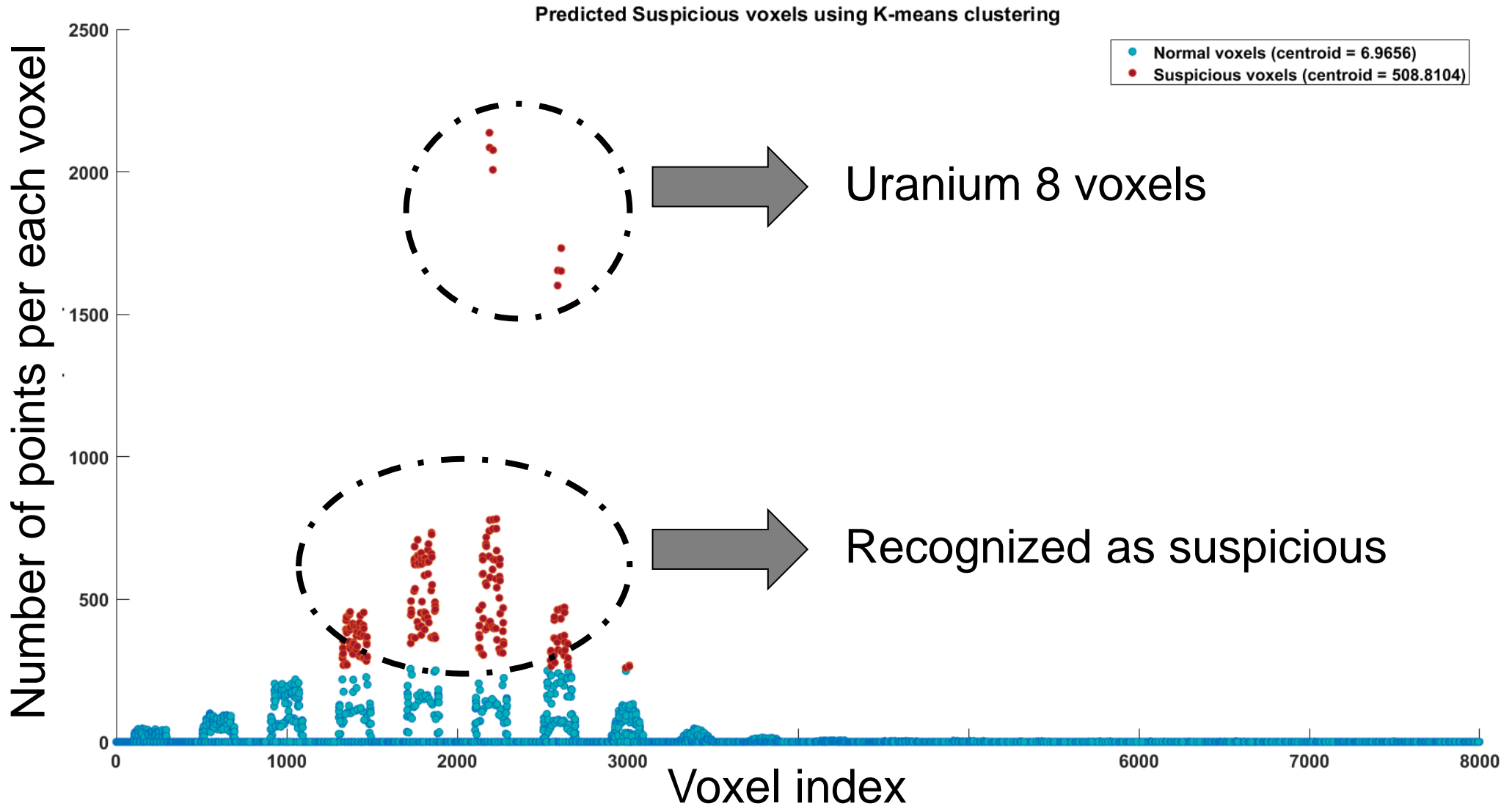
- Suspicious to nuclear material voxels
- Normal voxels

### Magnetic field OFF

Predicted Suspicious voxels using K-means clustering

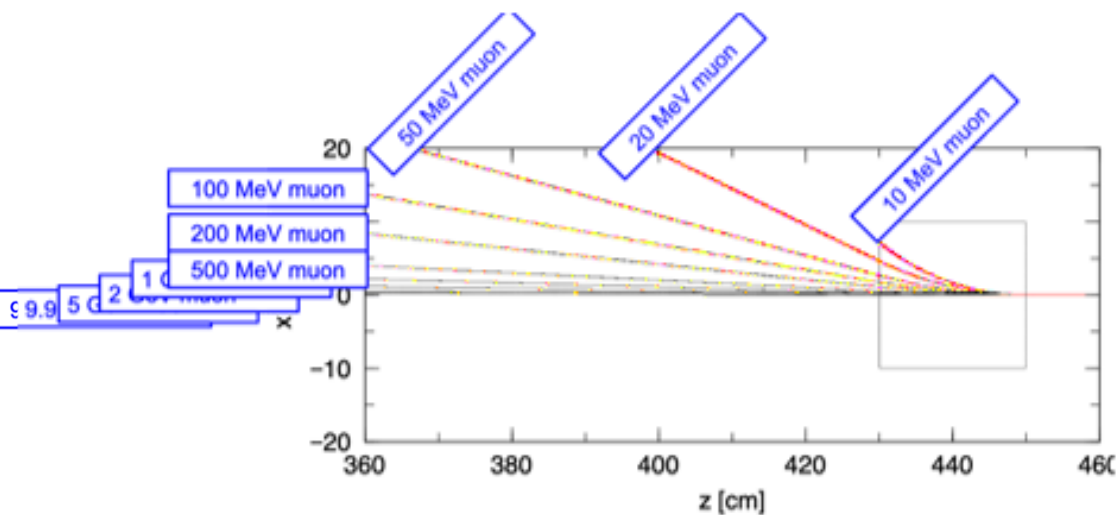


Magnetic field ON

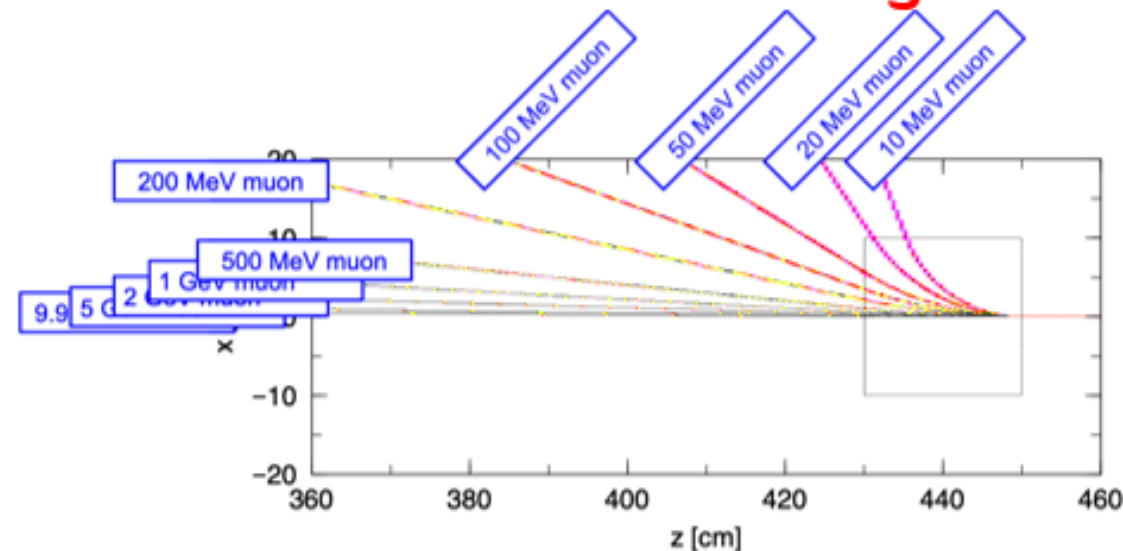


## ■ Cosmic-ray muon can be deflected by magnetic field.

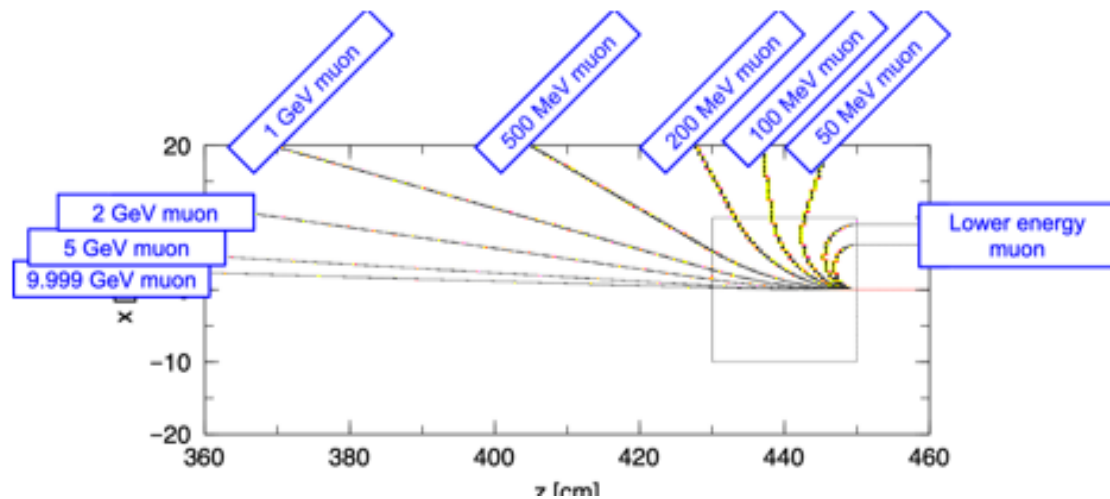
### ■ 0.5 T and 20-cm thick magnetic field



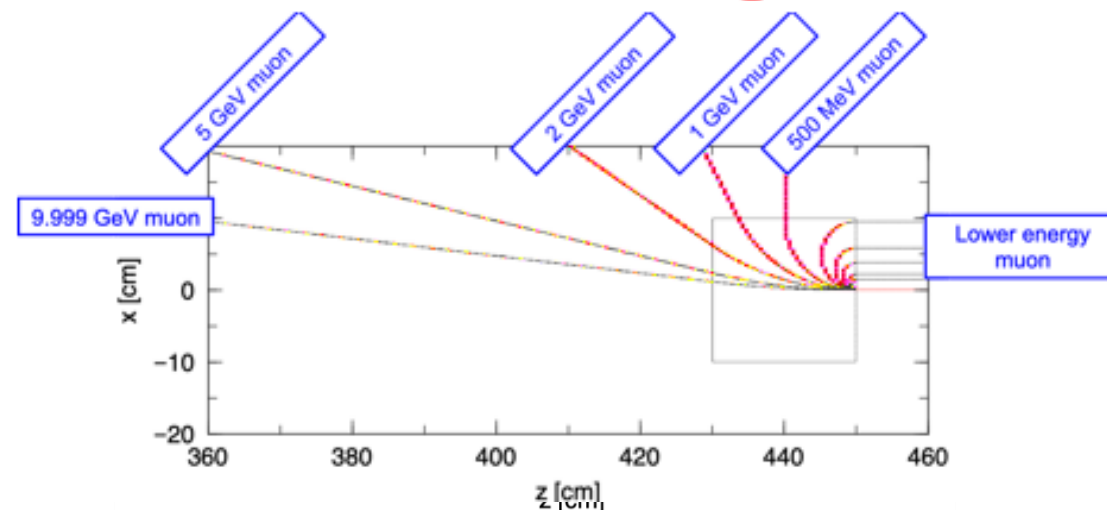
### ■ 1.0 T and 20-cm thick magnetic field



### ■ 5.0 T and 20-cm thick magnetic field



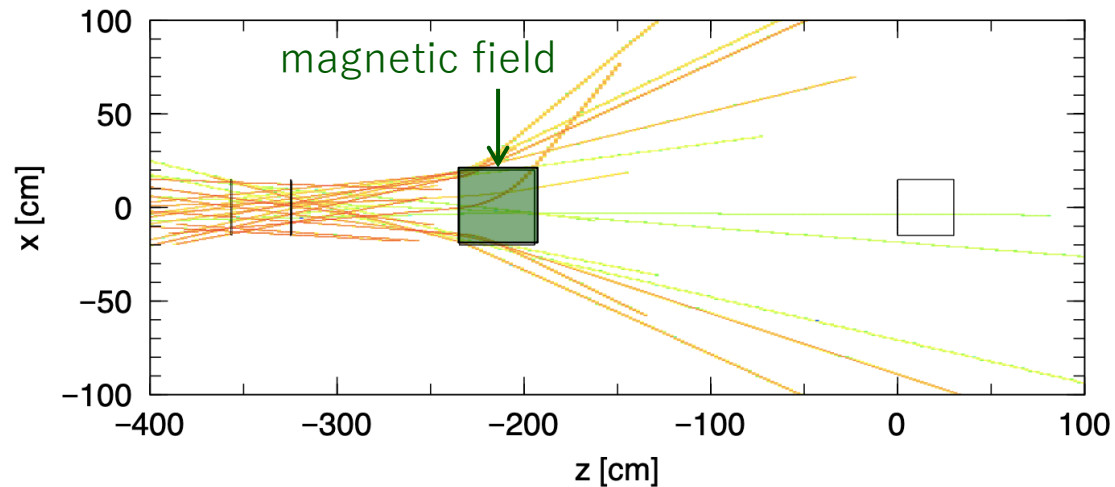
### ■ 20 T and 20-cm thick magnetic field



# Strong magnetic field acts as shielding of muon

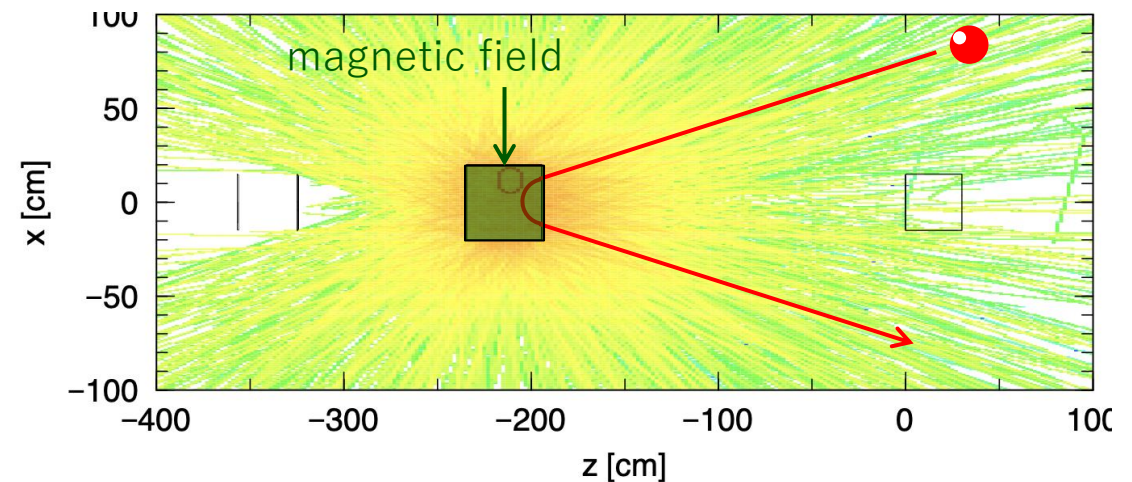
## 20 T and 20-cm thick magnetic field simulation result with realistic cosmic-ray muon flux by PARMA

Detected muons' trajectories that pass through magnetic field.



Very rare events

NOT Detected muons' trajectories that pass through magnetic field.



dominant

**Low energy muons are kicked back to the universe.**

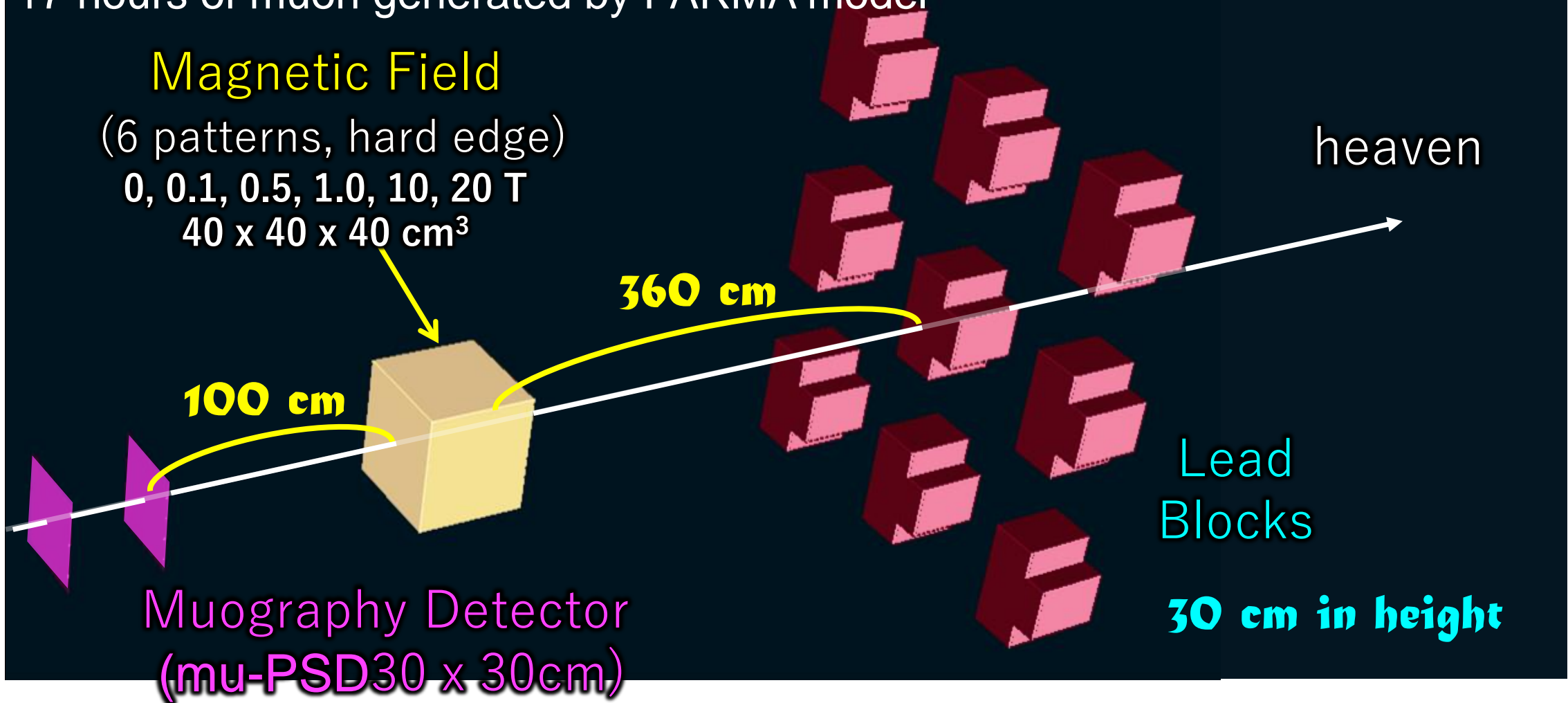
17 hours of muon generated by PARMA model

## Magnetic Field

(6 patterns, hard edge)

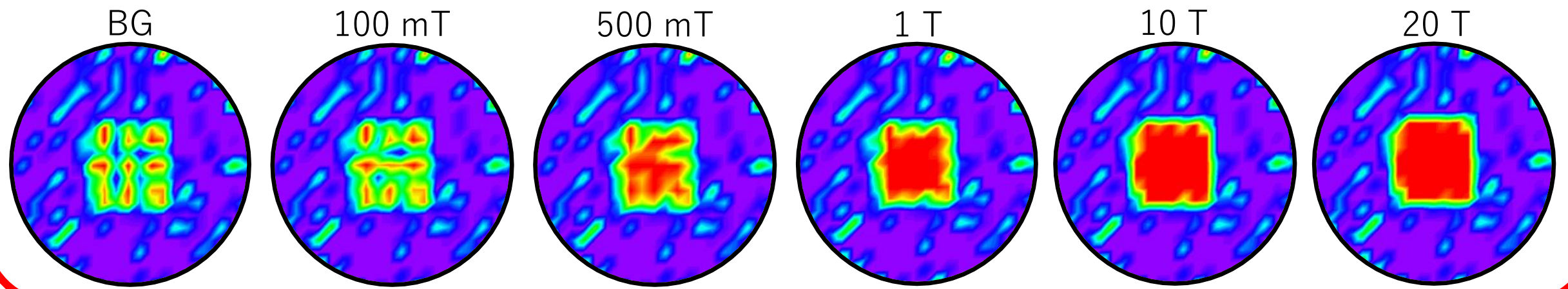
0, 0.1, 0.5, 1.0, 10, 20 T

40 x 40 x 40 cm<sup>3</sup>



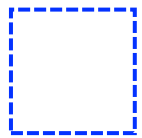
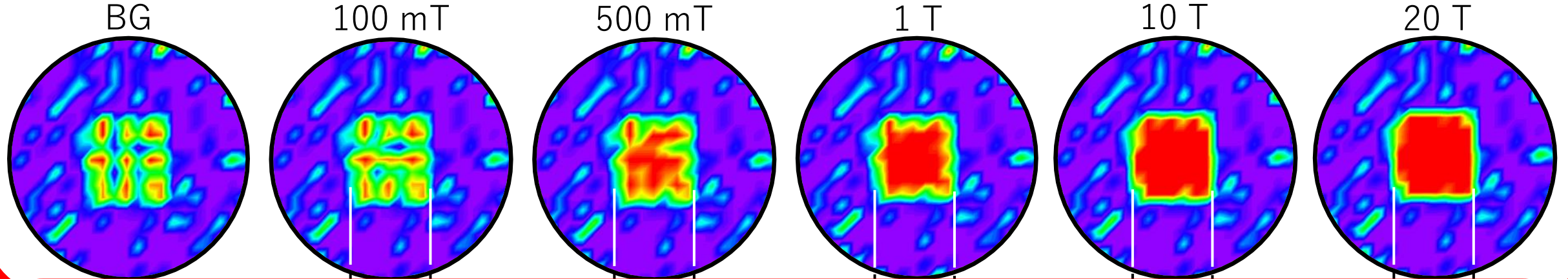
- Muography image calculated for the background (designed to be with in single pixel on muography image).
- Various magnetic flux density applied in the yellow box (have hard edge).

## Muography images / Absorption ratio map

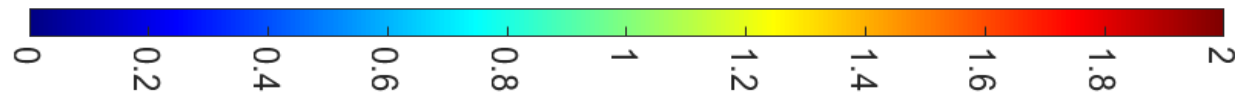
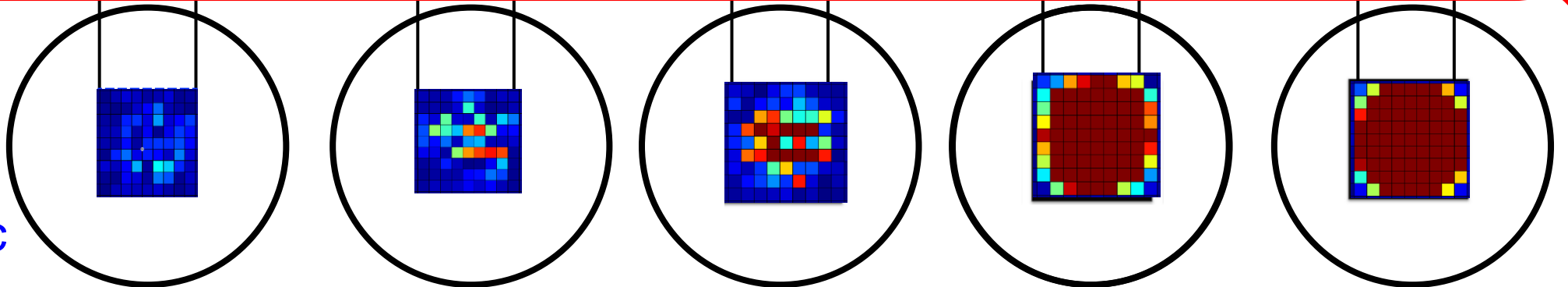




## Muography images / Absorption ratio map



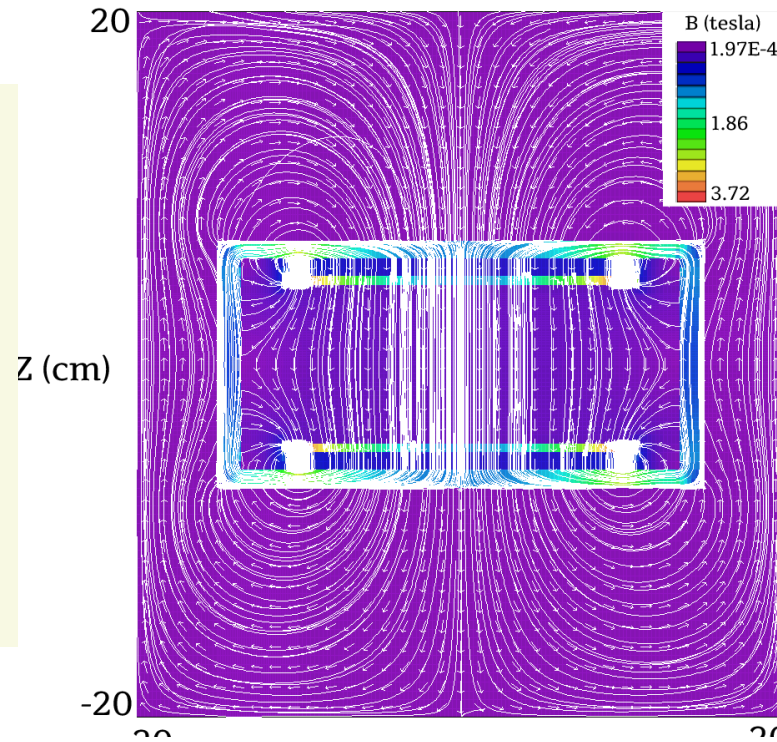
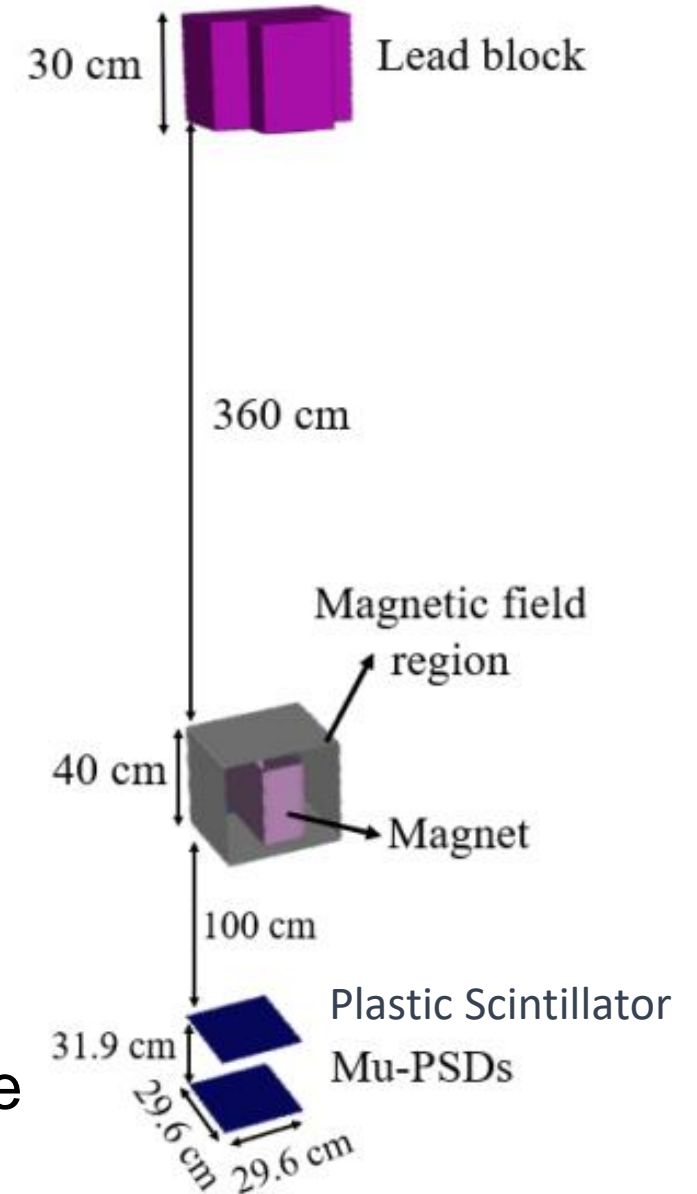
Actual magnetic field region



The difference of BG and FG magnetic

FOM

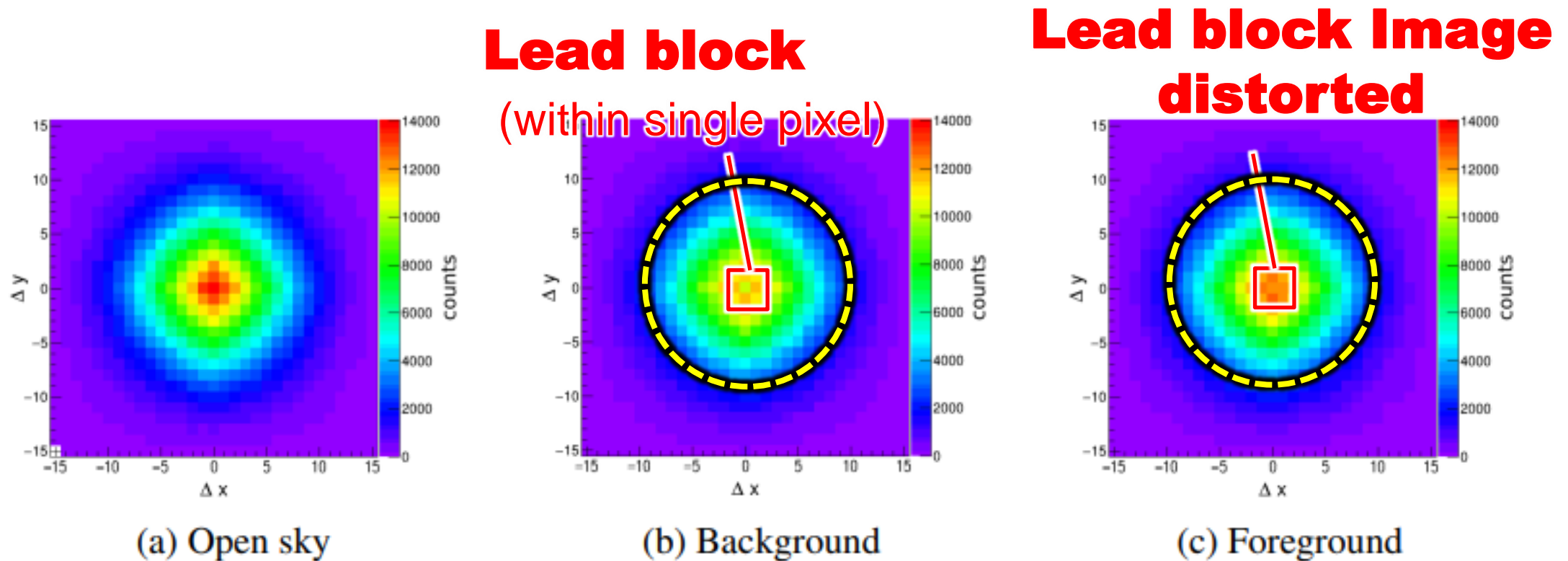
- The 3D distribution of magnetic flux densities calculated using finite element solution package **AMaze** software and implemented in PHITS.



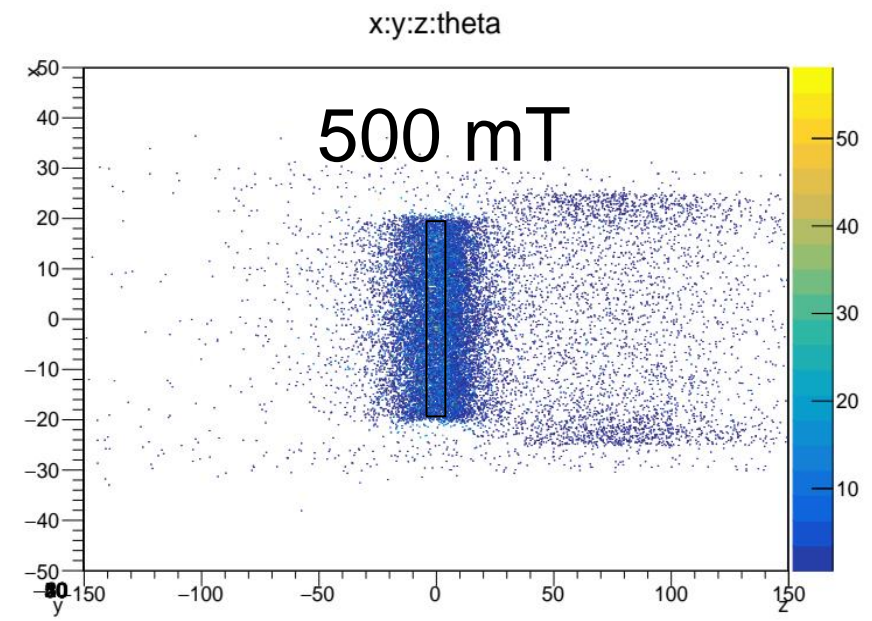
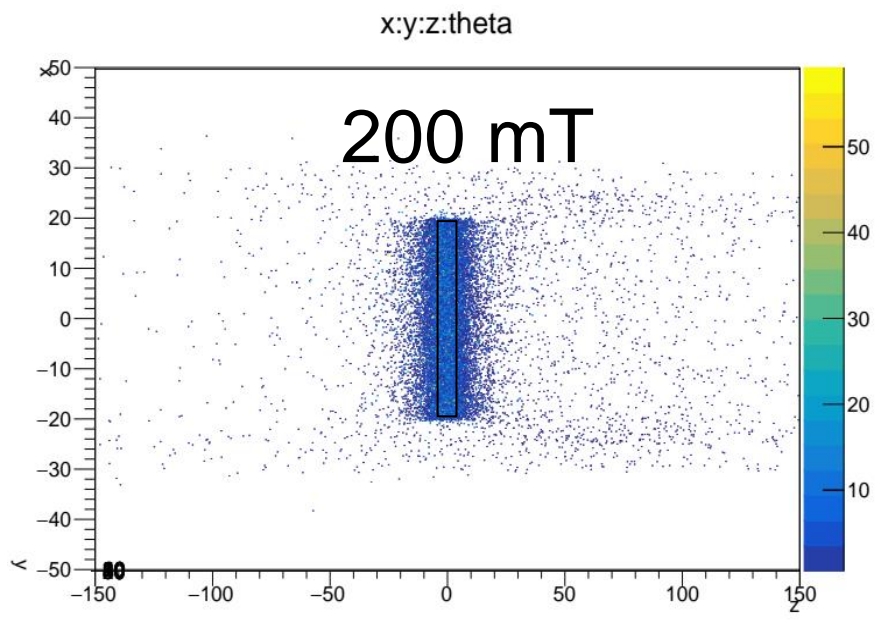
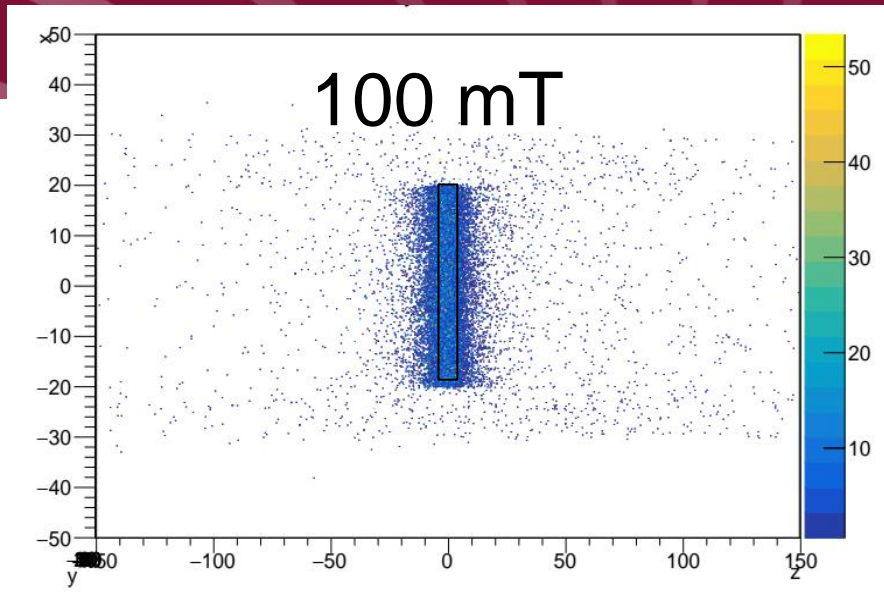
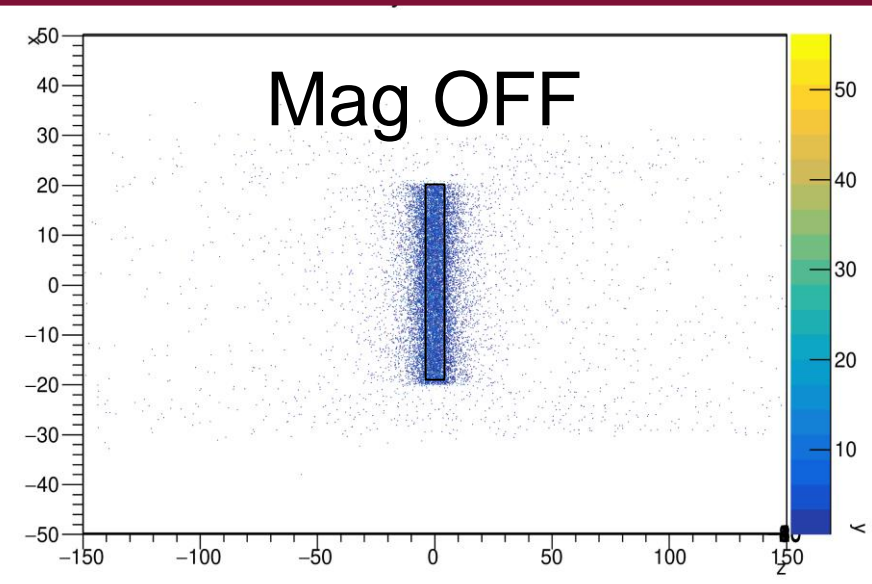
Magnet simulation in Amaze  
Mean (0.2T)

- A lead block was placed above the magnet to represent a **single pixel in the center of the count rate map**, considering the detector resolution.
- 152 hours measurement**

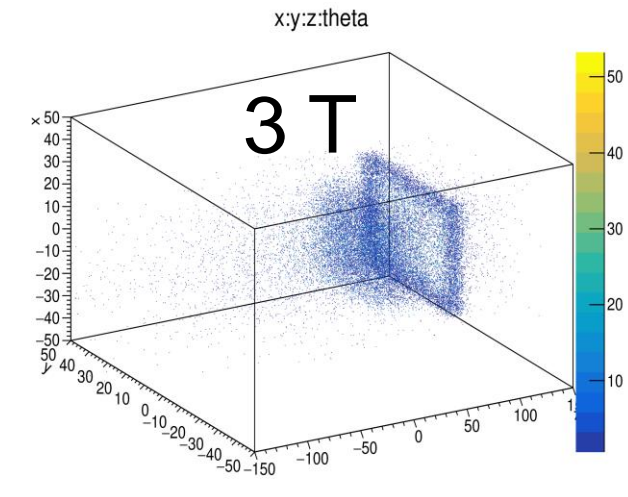
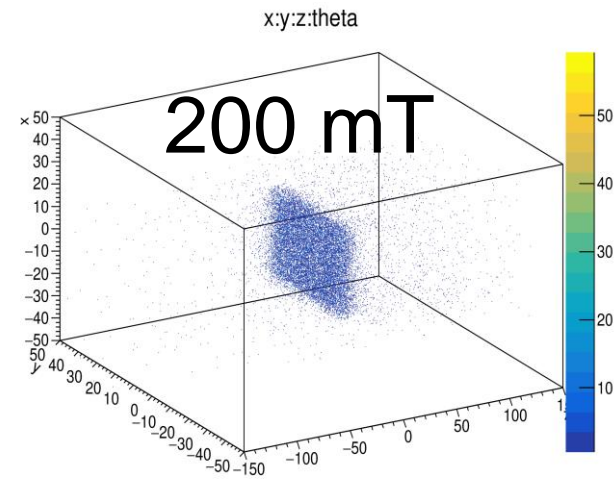
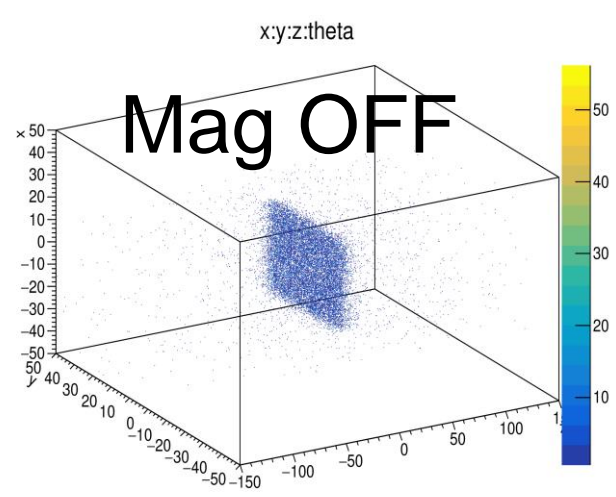
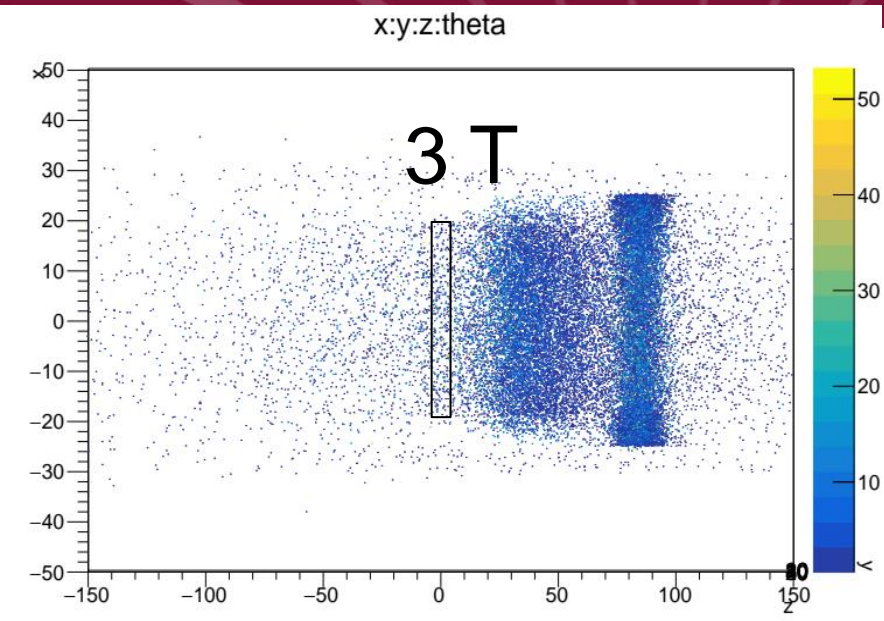
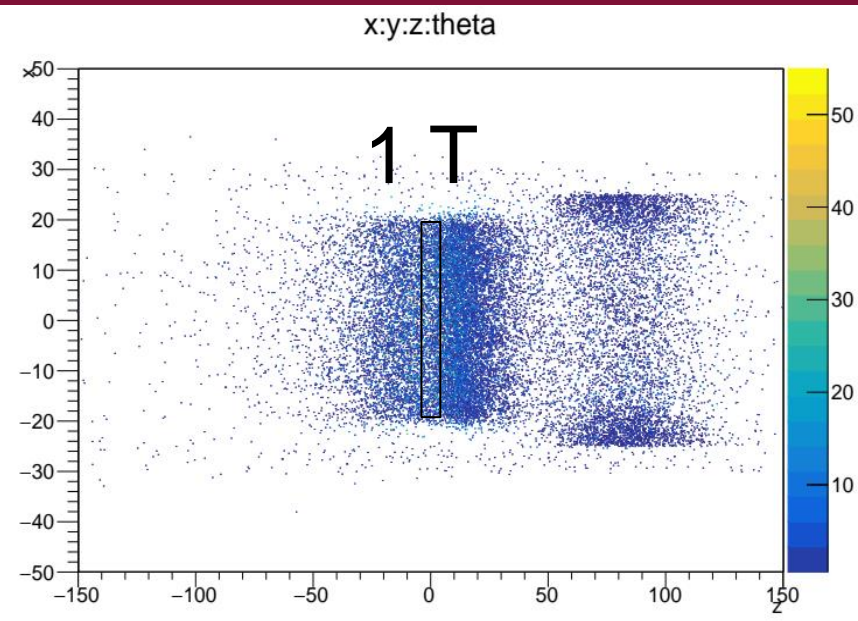
- Three different conditions were simulated: open sky, background (magnet off), and foreground (magnet on).



- The foreground simulation showed *changes in the distribution of counts* due to the magnetic field, with the central pixel blurred and the detection of some muons that would have been missed in the background condition.



Color Represents Scattering angle



Color Represents Scattering angle



## ■ Lorentz Force

Relativistic effect cannot be ignored for cosmic-ray muons

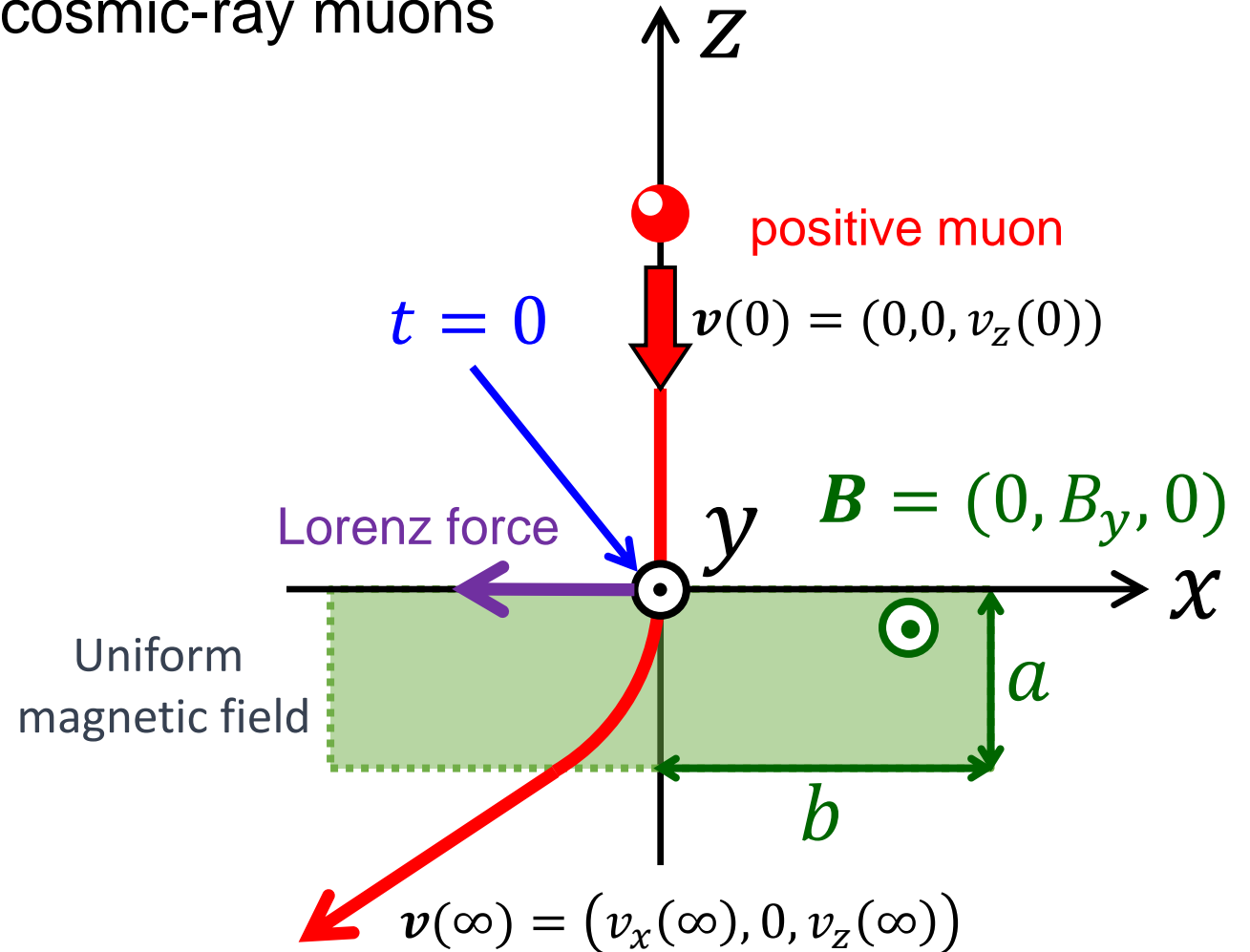
$$\frac{d}{dt} \left\{ \frac{m\mathbf{v}}{\sqrt{1 - \frac{v_z(0)^2}{c^2}}} \right\} = \mathbf{v} \times \mathbf{B}$$

The circular motion is derived as:

$$\begin{aligned} x(t) &= -r \cos \omega t \\ z(t) &= r \sin \omega t \end{aligned}$$

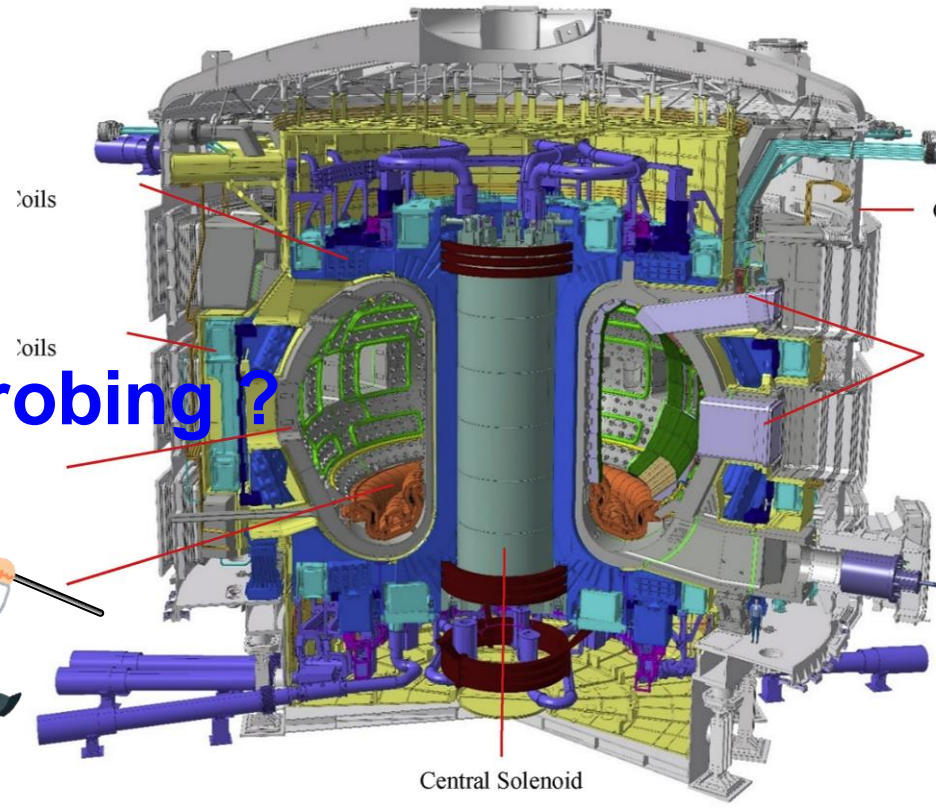
Lamor radius defined as:

$$r \equiv \frac{v_z(0)}{\omega} = \frac{mv_z(0)}{B_y \sqrt{1 - \frac{v_z(0)^2}{c^2}}}$$



# Huge & strong magnetic field

Neutron irradiation induces degradation of superconductive coil.  
→ Many reports say, "it determines the life of fusion reactor."



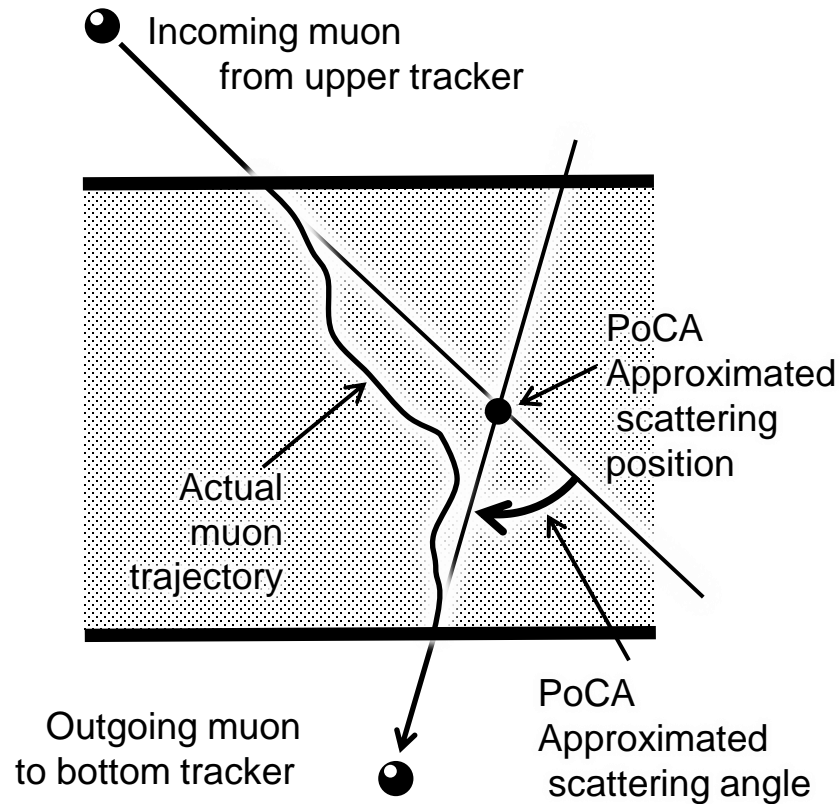
Local probing ?

I found some reports to show the degradation by deviation of the electric current possible to flow to the superconductive coil.

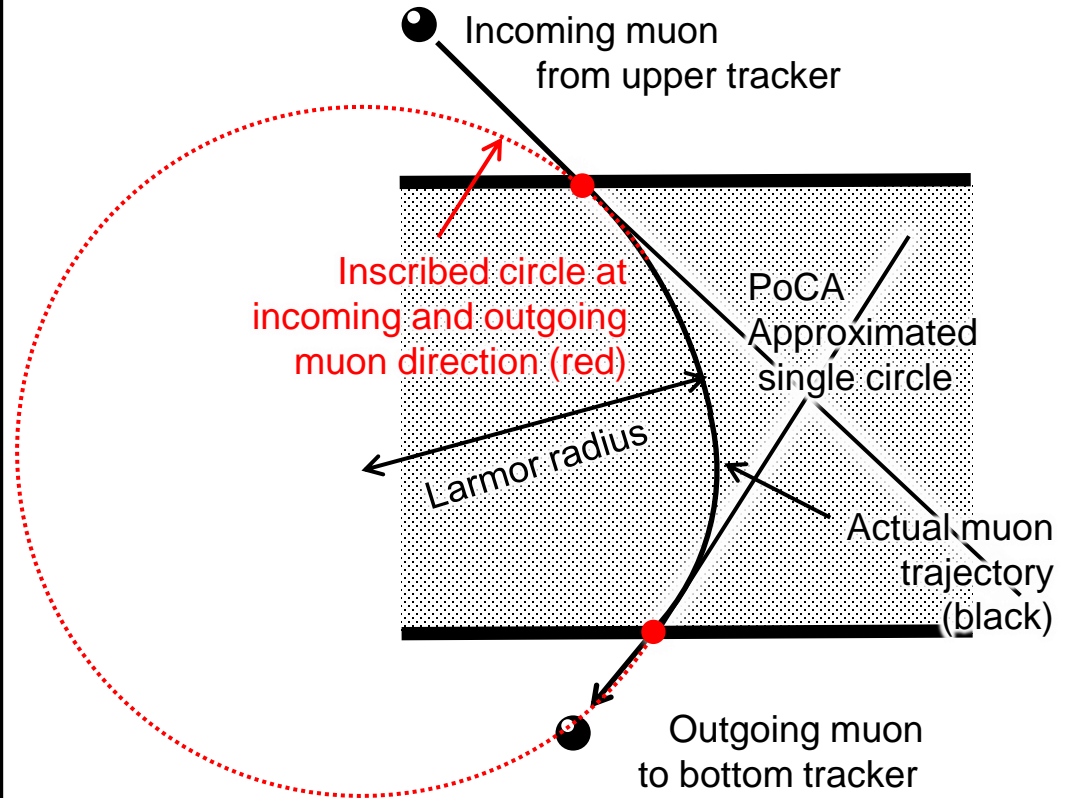
It can predict when the degradation starts, but...

never say "how" and "where".

## Scattering Muography



## Magnetic field measurement by deflection method



$$\sigma \approx \frac{13.6 \text{ MeV}}{pc} \sqrt{\frac{X}{X_0}} + \text{Model (Gaussian)} + \text{MLEM}$$

$$B_y^2 \left( \frac{1}{v_z(0)^2} - \frac{1}{c^2} \right) = \frac{m^2}{r^2} + \text{Model (PARMA)} + \text{MLEM or such}$$



- **Hall device probing**

Measure magnetic field intensity via the Hall effect.

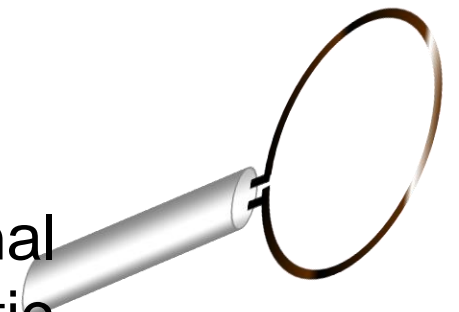
**Primary limitation:** Sensitivity changes due to temperature fluctuations. Only local measurement is possible. Must touch the magnetic field.



- **Coil probing**

Operate based on Faraday's law of electromagnetic induction.

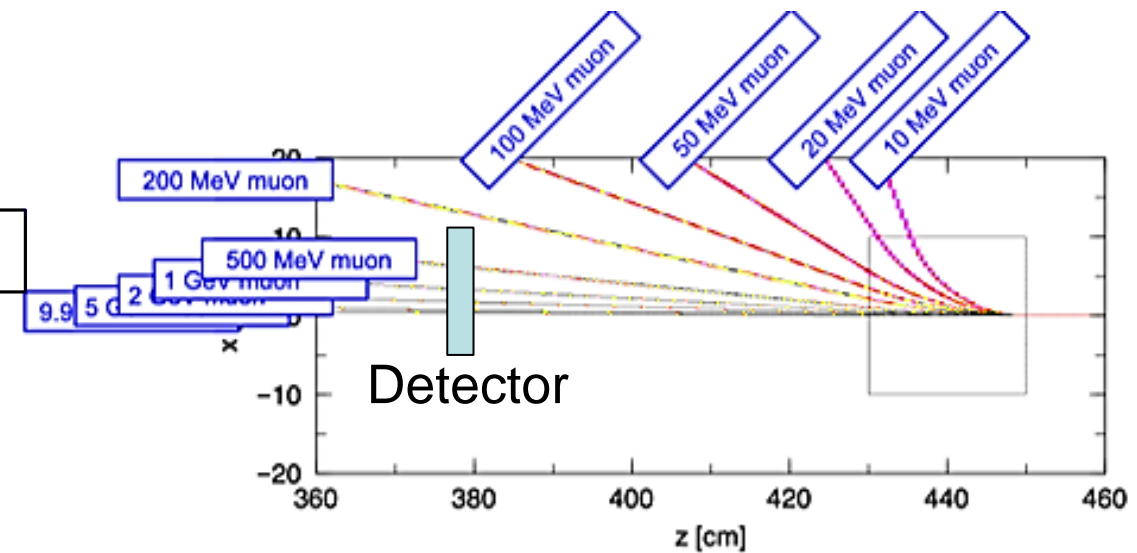
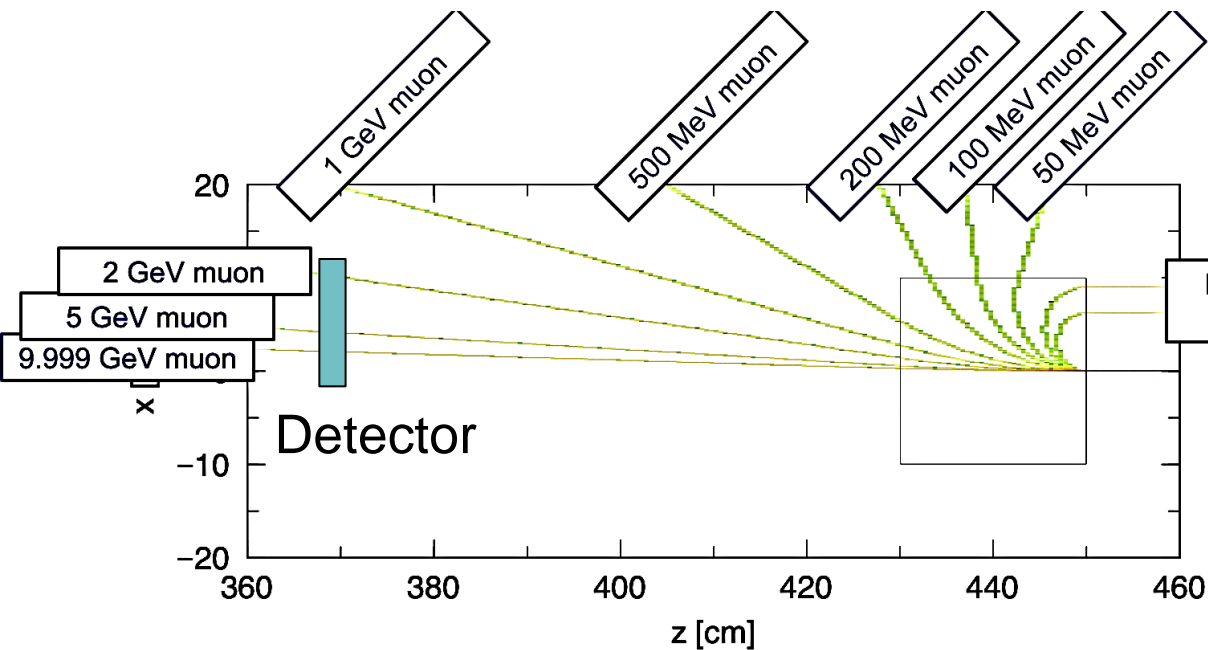
**Primary limitation:** Influenced by temperature variations and external electromagnetic interference. Only showing the difference of magnetic field flux densities (**time dependent one only**)



To have an idea of the effect of magnetic fields on various muon energies

■ 5 T and 20-cm thick magnetic field

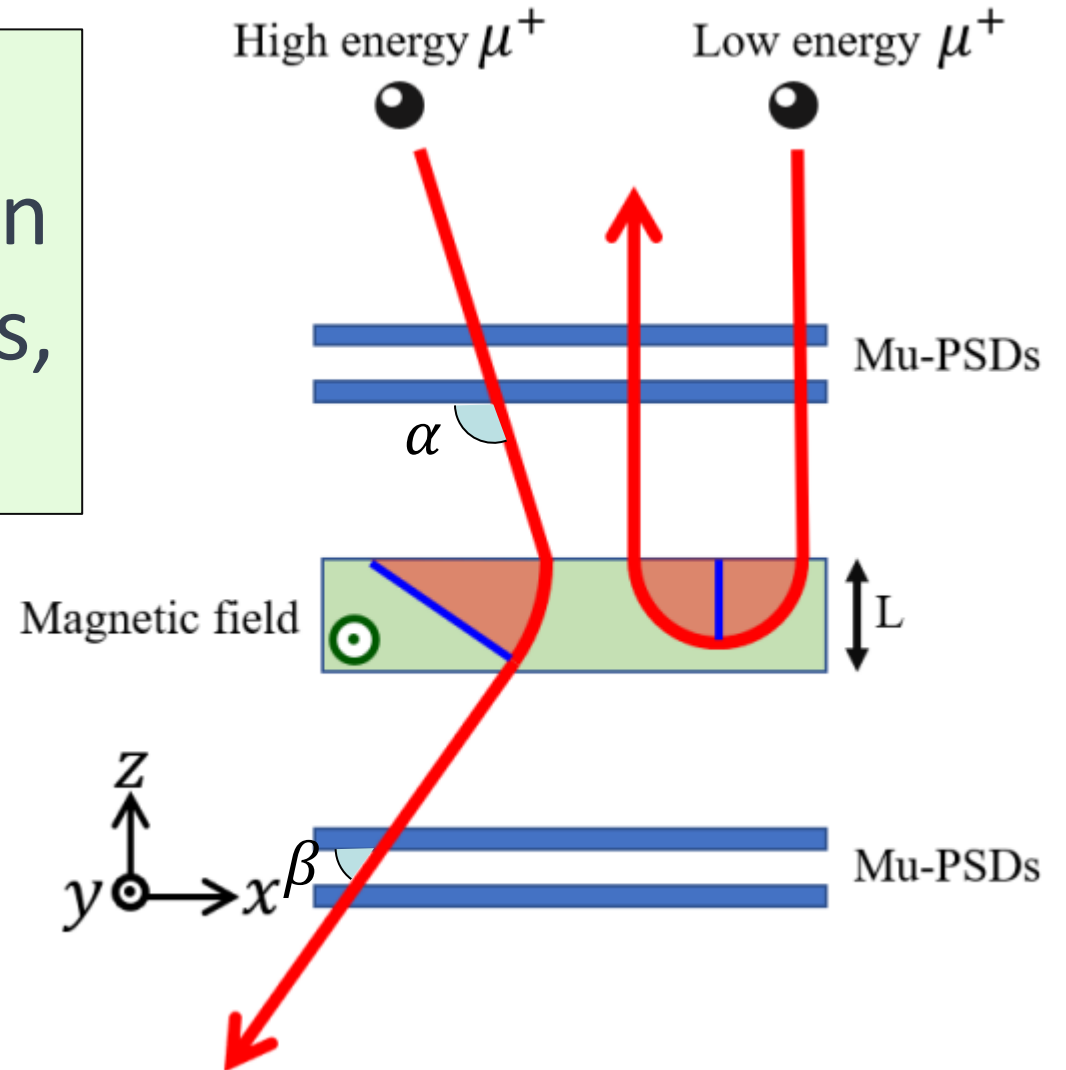
■ 1 T and 20-cm thick magnetic field

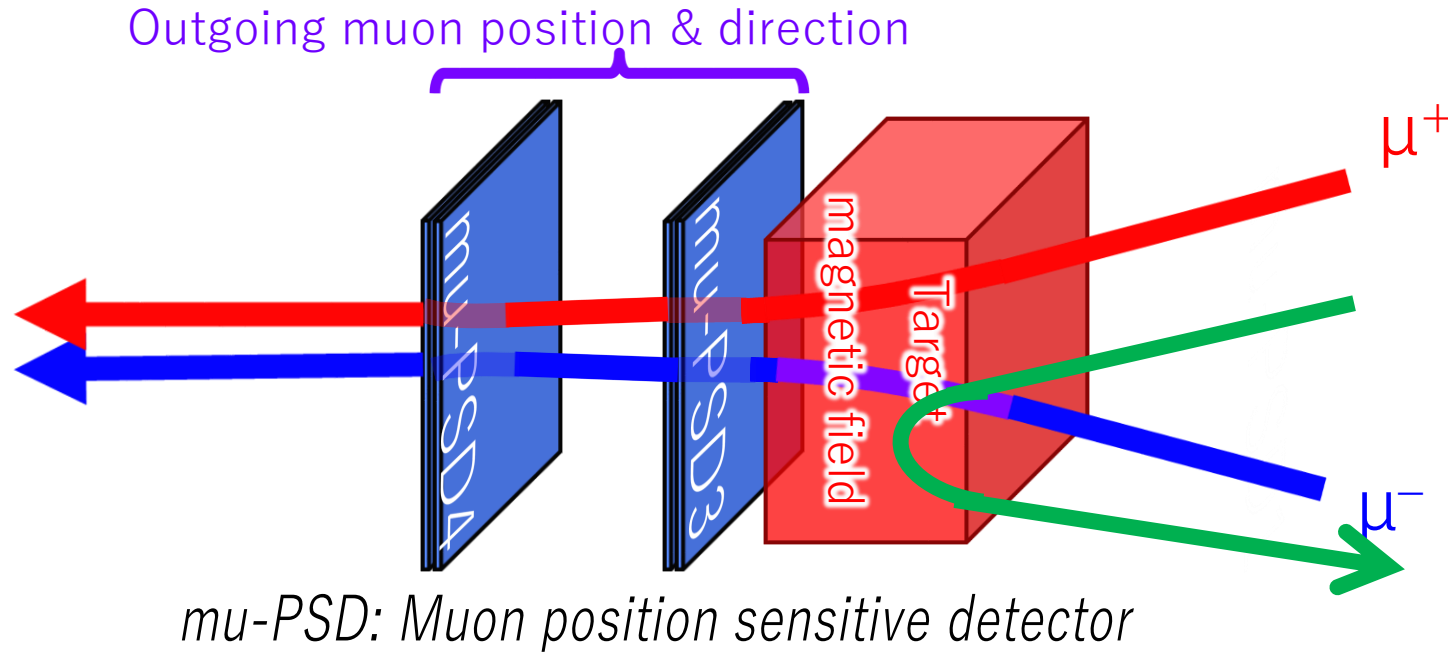


*Muons that cannot reach the detector because of the magnet are important for us!*

- The deflection angle of muons is defined as the difference between the outgoing and incoming angles, and it can be calculated as  $\Delta\theta$ :

$$\alpha - \beta = \Delta\theta = \frac{qBL}{p_{\perp}}$$





Completely the same setup with normal absorption muography detector.

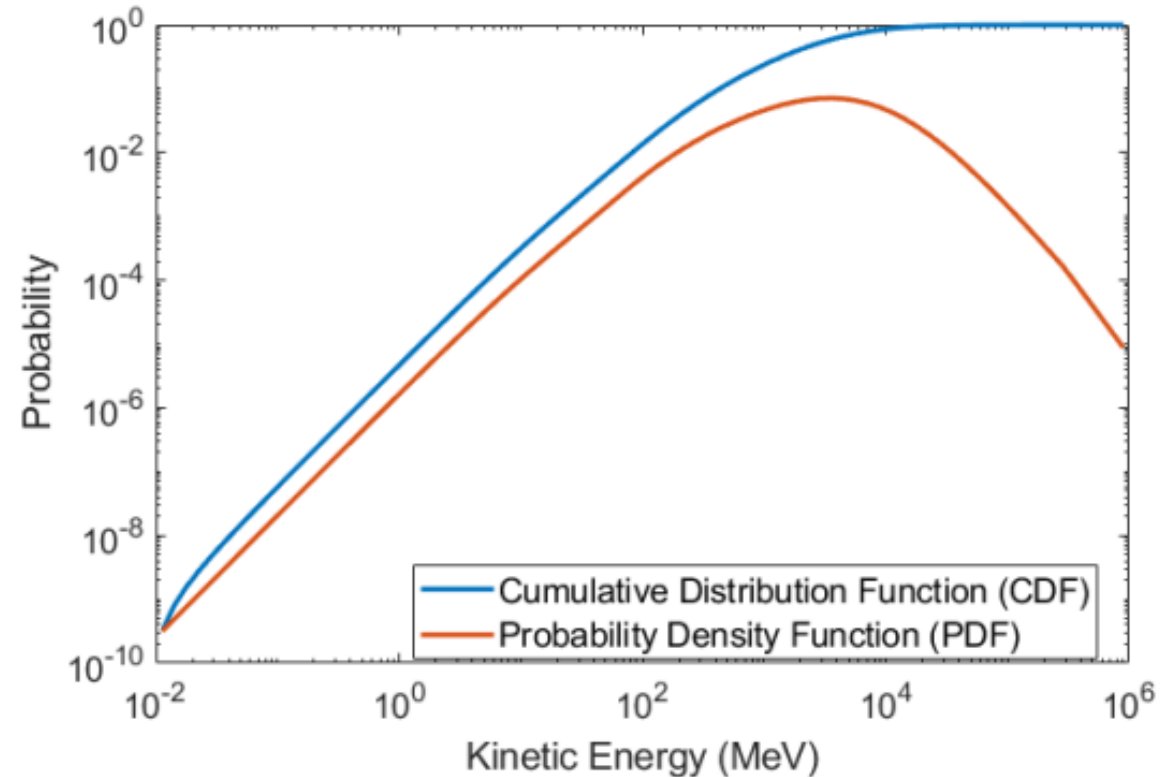
Applicable for:

- Huge and strong magnetic fields
- Background measurement or precise simulation must be possible.

Note: "Background" is NOT an open-sky, but a magnetic field off measurement.

**Low-Energy muons are kicked back to the universe!**

# Are the low-energy muons important?



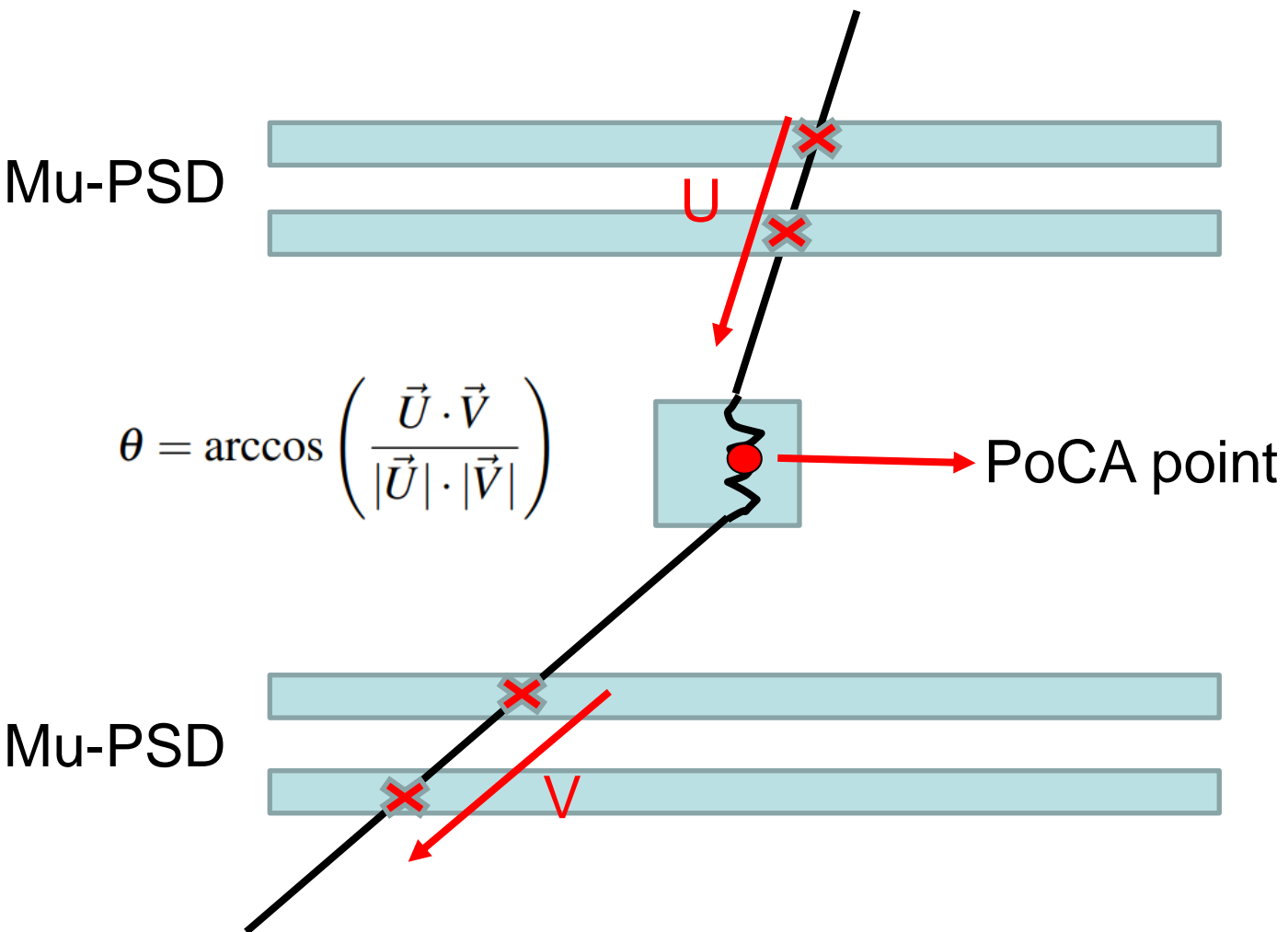
Location of Tokyo using PARMA model

Based on previous equations, in a **1 m** magnetic field of **1 T**, muons up to **180 MeV** will be **completely deflected back**. These constitute **3.5%** of the muon flux.

- **500 MeV** account for **~12%** of the **CDF**

**Lower-energy muons in magnetic field imaging could reveals the information of magnet mainly in strong magnetic field (tesla order)!**

## Point of Closest Approach (PoCA) algorithm



Using precise hit positions, the direction can be calculated

Using position of one point and the direction, PoCA point can be obtained.

By using directions, the scattering angle can be calculated.

- For each incoming muon one PoCA point is calculated