

Integration of neural networks on FPGAs

Giulio Bianchini

Referent teacher: Santocchia Attilio
Tutors: Mirko Mariotti, Daniele Spiga

Research Doctoral programs PON for the academic year 2021/2022 - XXXVII cycle

Outline

1 Introduction

- Project recap
- Expected results

2 An accelerated system

- System overview
- Tests
- Benchmark

3 Machine Learning inference with BondMachine

- ML inference on FPGA
- The BondMachine inference
- Tests

Introduction

1 Introduction

Project recap
Expected results

2 An accelerated system

System overview
Tests
Benchmark

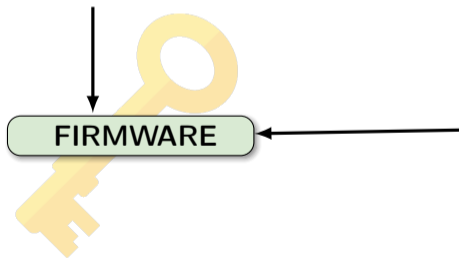
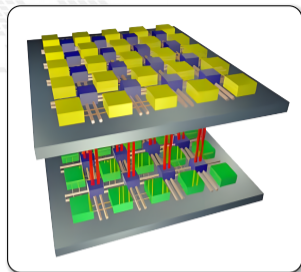
3 Machine Learning inference with BondMachine

ML inference on FPGA
The BondMachine inference
Tests

FPGA accelerator

A field programmable gate array (FPGA) is an integrated circuit whose logic is re-programmable.

- Parallel computing
- Highly specialized
- Energy efficient



- Array of programmable logic blocks
- Logic blocks configurable to perform complex functions
- The configuration is specified with the hardware description language

Integration of neural networks on FPGA

FPGAs are playing an increasingly important role in the industry sampling and data processing.



Deep Learning



In the industrial field

- Intelligent vision;
- Financial services;
- Edge devices;
- Life science and medical data analysis;

In the scientific field

- Real time deep learning in particle physics;
- Hardware trigger of LHC experiments;
- And many others ...

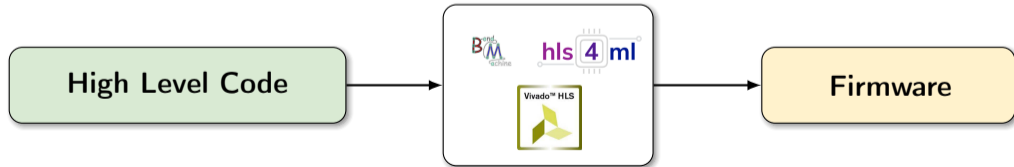
How FPGA are programmed?

Programming an FPGA is not an easy task...

```
1 library IEEE;
2 use IEEE.Std_logic_1164.all;
3 use IEEE.Std_logic_arith.all;
4
5 entity signed_adder is
6     port
7     (
8         a : in  std_logic;
9         b : in  std_logic;
10        n : in  std_logic_vector;
11        h : in  std_logic_vector;
12        q : out std_logic_vector
13    );
14 end signed_adder;
15
16 architecture signed_adder_arch of signed_adder is
17     signal q_n : signed(n'highest_order-1); -- extra bit wide
18
19 begin -- architecture
20     power_of_two_n = n'length;
21     report "The n must be the longer vector if different sizes!"
22     when (n'length < h'length);
23     q <= std_logic_vector(q_n);
24
25     adding_proc:
26     process (a,b,n)
27     begin
28         if (a'len = n'len) then
29             q_n <= (a+b) <> "0";
30         else if (n'length < h'length) then
31             q_n <= ("0" & a+b) <> ("0" & h);
32         end if; -- case'd
33     end process;
34
35 end signed_adder_arch;
```

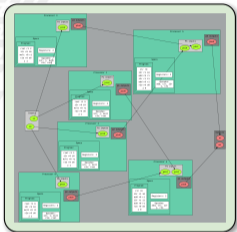
Hardware description language (HDL) represents the biggest barrier to using this device.

For this reason so many HLS (High Level Synthesis) tools has been developed.



BondMachine

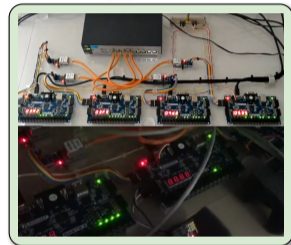
The BondMachine is a software ecosystem for the dynamical generation of computer architectures that can be synthesized on FPGA.



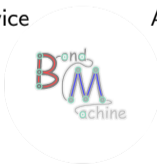
The main feature of the BondMachine is that processors form a heterogeneous set of computing units.



As a standalone device



As clustered devices



Expected results and achieved results

- Build of a system to use standard neural network models on FPGAs using BondMachine;
- Registry of pre-trained neural network models to perform a specific task that can be used through cloud services;
- Development of an accelerated system on hybrid processor;
- Benchmark of the proposed systems;

An accelerated system

1 Introduction

Project recap
Expected results

2 An accelerated system

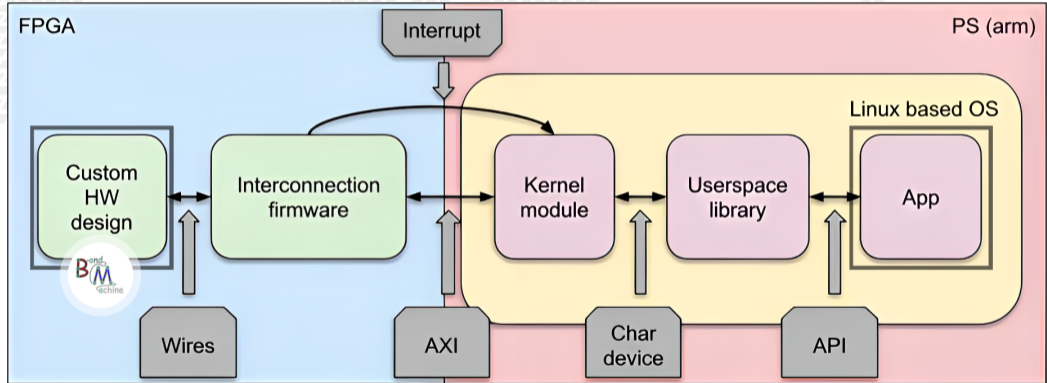
System overview
Tests
Benchmark

3 Machine Learning inference with BondMachine

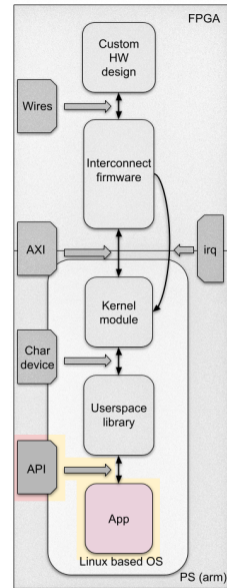
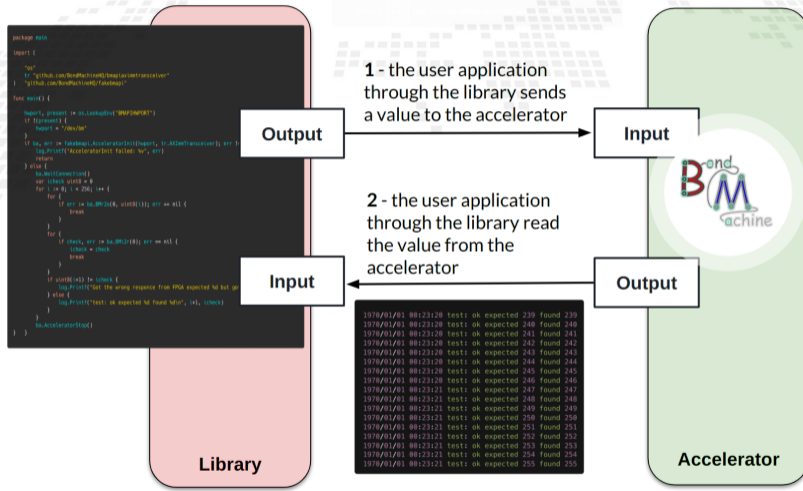
ML inference on FPGA
The BondMachine inference
Tests

The whole accelerated system overview

Worked on the development of an accelerated system, starting from firmware up to the high level application.



Accelerated application: an example



An example

- Definition of an example
- Benchmark of the execution

Squared Matrix-vector multiplication

$$\begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{bmatrix} \times \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_n \end{bmatrix} = [c_i]_{i=1}^n = [\sum_{k=1}^n a_{ik} b_k]_{i=1}^n$$

Squared Matrix-vector multiplication

$$\begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{bmatrix} \times \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_n \end{bmatrix} = [c_i]_{i=1}^n = [\sum_{k=1}^n a_{ik} b_k]_{i=1}^n$$

```
"A": [  
    [6,5],  
    [1,2]  
],  
"B": [  
    [3,1,1],  
    [6,7,2],  
    [7,1,4]  
],  
"C": [  
    [6,3,7,1],  
    [1,6,4,2],  
    [3,2,1,7],  
    [5,3,1,7]  
],
```

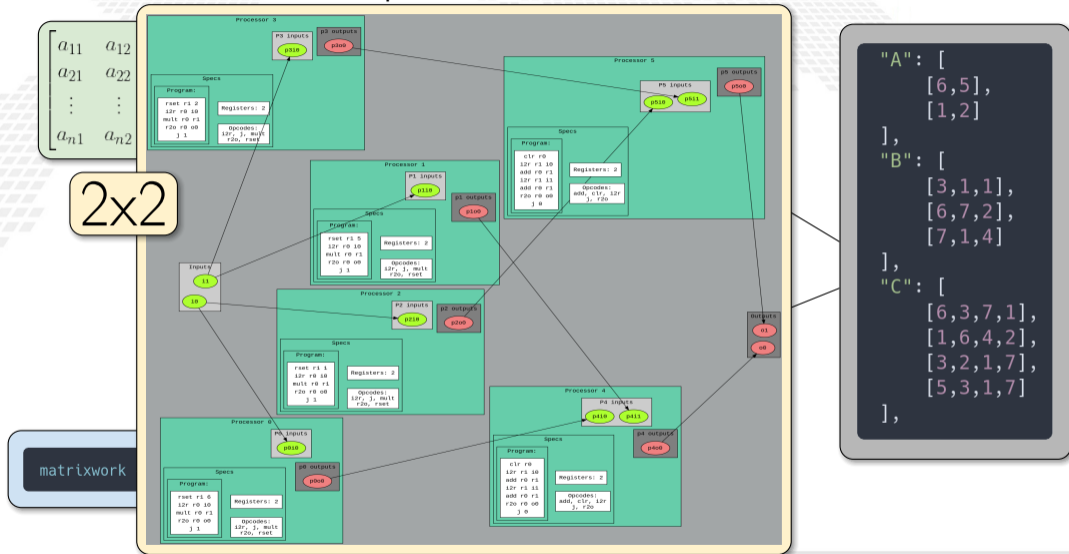
Squared Matrix-vector multiplication

$$\begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{bmatrix} \times \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_n \end{bmatrix} = [c_i]_{i=1}^n = \left[\sum_{k=1}^n a_{ik} b_k \right]_{i=1}^n$$

```
"A": [  
  [6,5],  
  [1,2]  
],  
"B": [  
  [3,1,1],  
  [6,7,2],  
  [7,1,4]  
],  
"C": [  
  [6,3,7,1],  
  [1,6,4,2],  
  [3,2,1,7],  
  [5,3,1,7]  
],
```

```
matrixwork -constants constants.json -constant-matrix A -numerical-type uint8 ...
```

Squared Matrix-vector multiplication

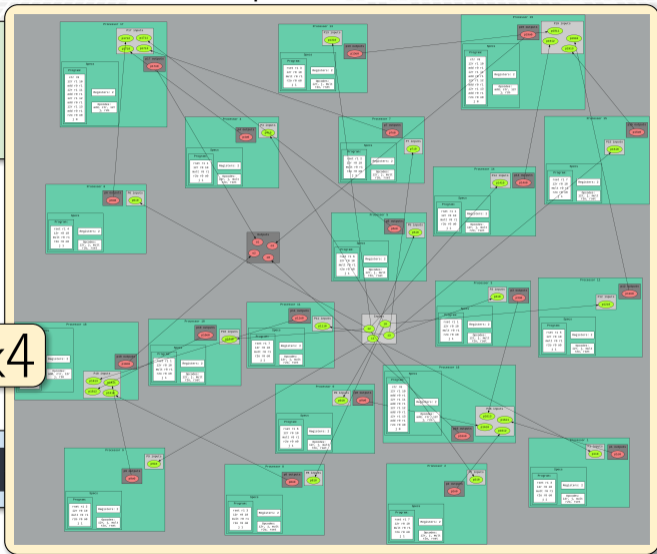


Squared Matrix-vector multiplication

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ \vdots & \vdots \\ a_{n1} & a_{n2} \end{bmatrix}$$

4x4

matrixwork



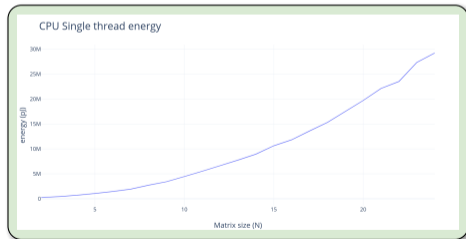
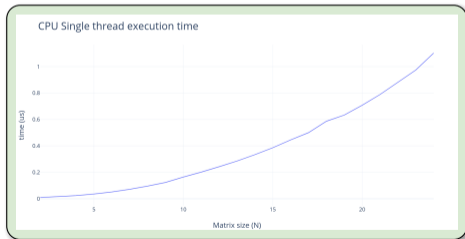
```
"A": [  
  [6,5],  
  [1,2]  
],  
"B": [  
  [3,1,1],  
  [6,7,2],  
  [7,1,4]  
],  
"C": [  
  [6,3,7,1],  
  [1,6,4,2],  
  [3,2,1,7],  
  [5,3,1,7]  
],
```

Benchmark: the CPU (Golang)

```
func matrixtest(n int, lter int64) float32 {  
    //...  
    start := time.Now()  
    for k := 0; lter64[k] < lter; k++ {  
        for l := 0; l < n; l++ {  
            output[l] = uint8(0)  
        }  
        for i := 0; i < n; i++ {  
            for j := 0; j < n; j++ {  
                output[l] += input[j] * matrix[i+j*n]  
            }  
        }  
        return float32(time.Since(start).Microseconds()) / float32(lter)  
    }  
} func main() {  
    for i := 2; i <= 32; i++ {  
        fmt.Println(i, " ", matrixtest(i, 100000000))  
    }  
}
```

- Time measures: built-in golang facilities
- Energy measures: perf
- Intel(R) Xeon(R) CPU E3-1270 v5 @ 3.60GHz
- Go 1.18.2

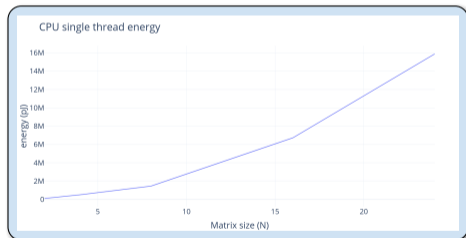
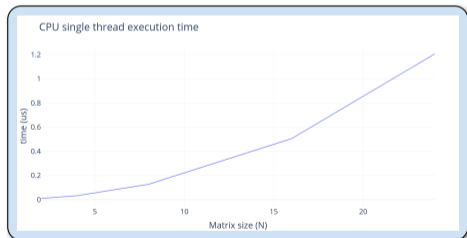
| N | single vs time (us) | single vs energy (J) | energy eff |
|----|---------------------|----------------------|-------------|
| 2 | 0.0042009 | 250200 | 0.000000-00 |
| 3 | 0.0041868 | 384200 | 2.302479-00 |
| 4 | 0.0209964 | 722200 | 1.304000-00 |
| 5 | 0.0042009 | 1479400 | 0.340000-01 |
| 6 | 0.0019983 | 1471400 | 0.796200-01 |
| 7 | 0.0730911 | 1839000 | 0.308000-01 |
| 8 | 0.0050720 | 2707000 | 0.000000-00 |
| 9 | 0.0221912 | 3400000 | 2.888000-01 |
| 10 | 0.0040078 | 4488000 | 2.200000-01 |
| 11 | 0.0217000 | 5530000 | 1.800000-01 |
| 12 | 0.0200000 | 6600000 | 1.300000-01 |
| 13 | 0.0080000 | 7700000 | 0.200000-01 |
| 14 | 0.0040000 | 8800000 | 1.100000-01 |
| 15 | 0.0011716 | 10000000 | 0.000000-00 |
| 16 | 0.0000000 | 11000000 | 0.000000-00 |
| 17 | 0.0000000 | 13004700 | 7.000000-08 |
| 18 | 0.0000000 | 15104000 | 0.000000-00 |
| 19 | 0.0019800 | 17000000 | 0.000000-00 |
| 20 | 0.0000000 | 18100000 | 0.000000-00 |
| 21 | 0.0000000 | 22000000 | 0.000000-00 |
| 22 | 0.0000000 | 25000000 | 0.000000-00 |
| 23 | 0.0000000 | 27000000 | 0.000000-00 |
| 24 | 1.0011716 | 28000000 | 0.000000-00 |



Benchmark: the CPU (C)

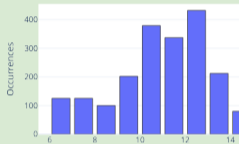
- Time measures: time
- Energy measures: perf
- Intel(R) CPU I5-8500 v5 @ 3GHz
- gcc with -O0

| | n | single op energy (pJ) | single op time (us) | energy eff |
|---|----|-----------------------|---------------------|---------------------|
| 1 | 2 | 100000 | 0.01 | 0.000006333333333 |
| 2 | 4 | 500000 | 0.033 | 0.00000702702703 |
| 3 | 8 | 1490000 | 0.127 | 0.0000009524861878 |
| 4 | 16 | 6720000 | 0.505 | 0.0000001326059947 |
| 5 | 24 | 19880000 | 1.205 | 0.00000008854009596 |

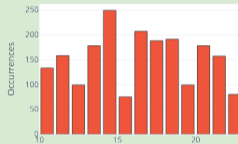


Benchmark of the accelerated system

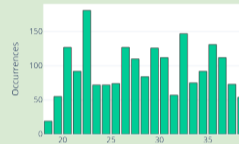
Clock cycles distributions



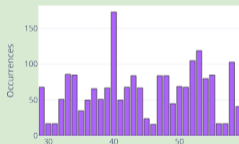
Clock cycles



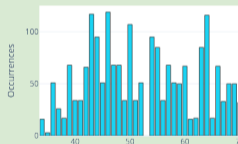
Clock cycles



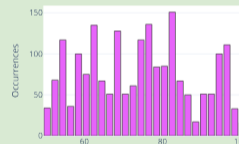
Clock cycles



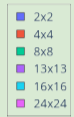
Clock cycles



Clock cycles



Clock cycles

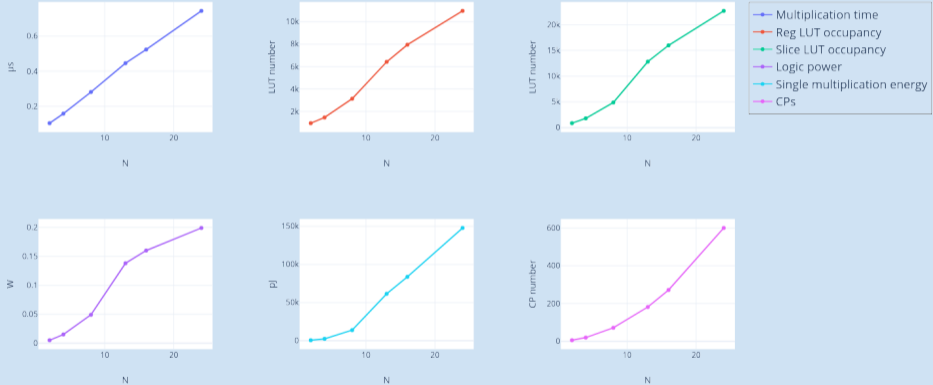


FPGA benchmark summary

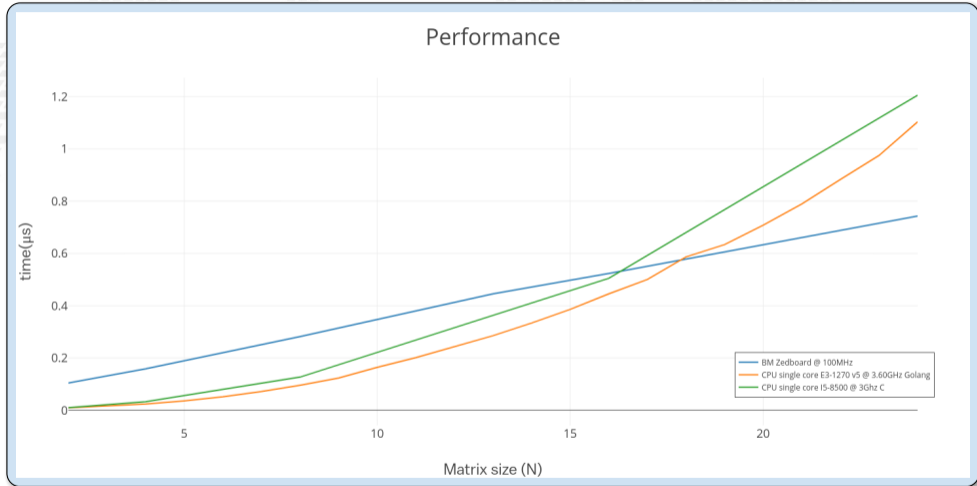
| | N | single op time (us) | Register LUTs | Slice LUTs | Power | single op energy (pJ) | CPs |
|---|----|---------------------|---------------|------------|-------|-----------------------|-----|
| 1 | 2 | 0.1044 | 947 | 875 | 0.005 | 522 | 6 |
| 2 | 4 | 0.1587 | 1457 | 1813 | 0.015 | 2380.5 | 20 |
| 3 | 8 | 0.2819 | 3131 | 4897 | 0.049 | 13813.1 | 72 |
| 4 | 13 | 0.4456 | 6422 | 12819 | 0.138 | 61492.8 | 182 |
| 5 | 16 | 0.5234 | 7950 | 15979 | 0.160 | 83744 | 272 |
| 6 | 24 | 0.7432 | 10974 | 22669 | 0.199 | 147896.8 | 600 |

Benchmark FPGA

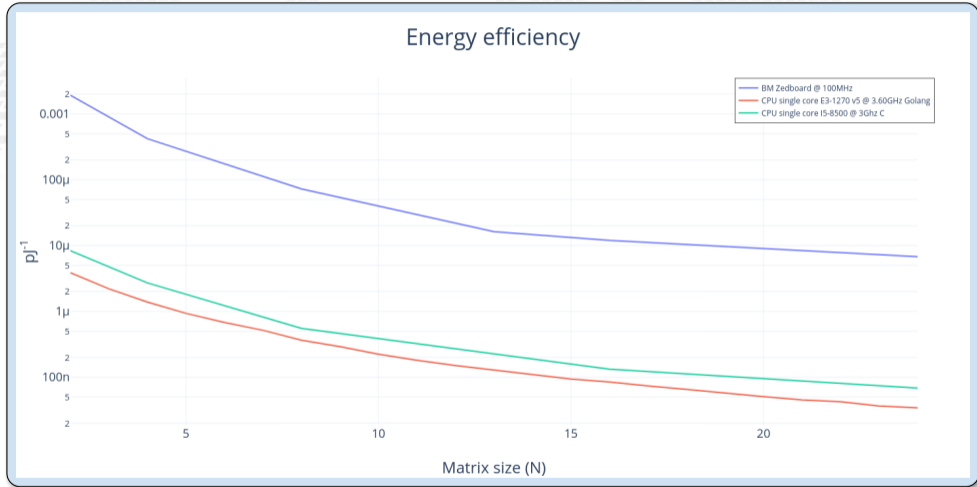
BondMachine NxN matrix-vector multiplication



Comparisons: Performance



Comparisons: Energy



Machine Learning inference with BondMachine

1 Introduction

- Project recap
- Expected results

2 An accelerated system

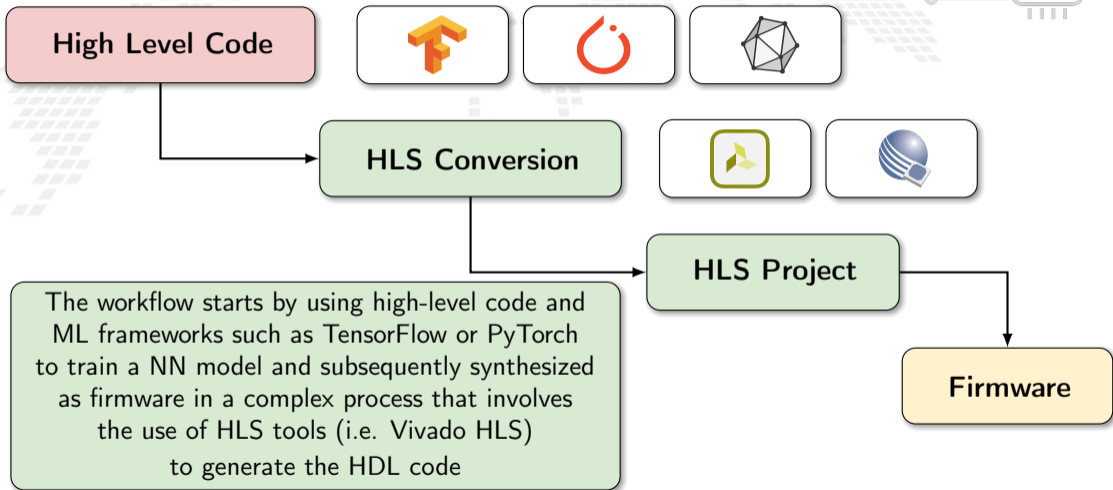
- System overview
- Tests
- Benchmark

3 Machine Learning inference with BondMachine

- ML inference on FPGA
- The BondMachine inference
- Tests

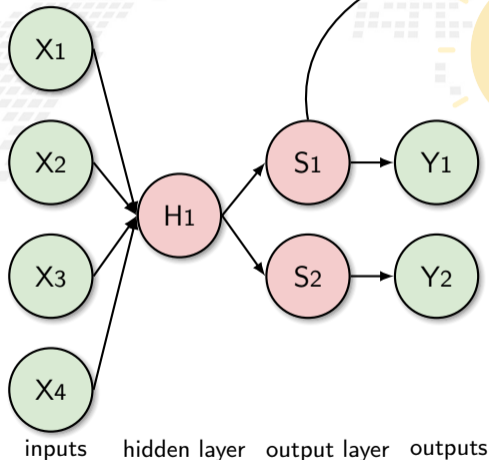
Converting NN to HDL

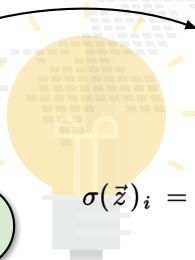
What is the typical process for making FPGA inference?

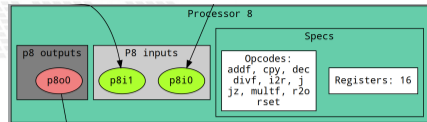
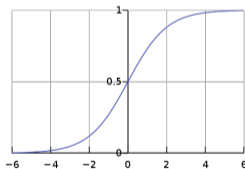


BM inference: the idea

A neuron of a neural network can be seen as Connecting Processor of BM




$$\sigma(\vec{z})_i = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}}$$



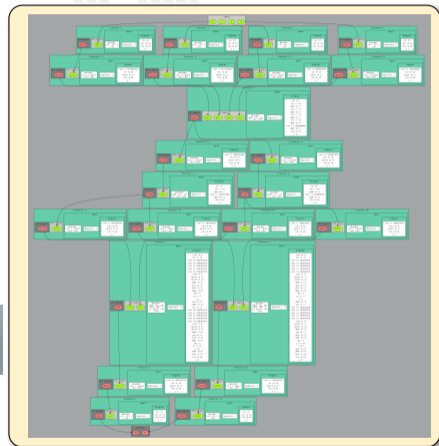
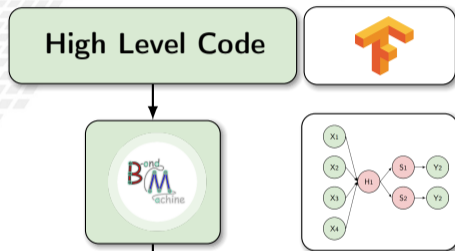
```
%section softmax .romtext iomode:sync
entry_start ; Entry point
_start:
mov r8, 0f0.0
{{range $y := intRange "0" .Params.inputs}}
{{printf "%2r r1,%d\n" $y}}
mov r0, 0f1.0
mov r2, 0f1.0
mov r3, 0f1.0
mov r4, 0f1.0
mov r5, 0f1.0
mov r7, {{{.Params.exprec}}
loop{{printf "%d" $y}}:
multf r2, r1
multf r3, r4
addf r4, r5
mov r6, r2
divf r6, r3

addf r0, r6

dec r7
jz r7,exit{{printf "%d" $y}}
j loop{{printf "%d" $y}}
exit{{printf "%d" $y}}:
{{Sz := atoi $.Params.pos}}
{{if eq $y $z}}
mov r9, r0
%endsection
```


From idea to implementation

Starting from High Level Code, a NN model trained with **TensorFlow** and exported in a standard interpreted by **neuralbond** that converts nodes and weights of the network into a set of heterogeneous processors.



A simple example

- A first example
- Check correctness of predictions
- Analysis of the main metrics

First test

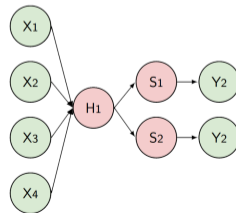
Dataset info:

- **Dataset name:** Banknote Authentication
- **Description:** Dataset on the distinction between genuine and counterfeit banknotes. The data was extracted from images taken from genuine and fake banknote-like samples.
- **N. features:** 4
- **Classification:** binary
- **Samples:** 1097

Neural network info:

- **Class:** Multilayer perceptron fully connected
- **Layers:**
 - 1 An hidden layer with 1 **linear** neuron
 - 2 One output layer with 2 **softmax** neurons

Graphic representation:



Make predictions and check correctness

Thanks to PYNQ we can easily load the bitstream and program the FPGA in real time.

With their APIs we interact with the memory addresses of the BM IP to send data into the inputs and read the outputs

Dump output results for future analysis

```
In [138]: from pynq import Overlay
         from pynq import MMIO
         import os
         import numpy as np
         import struct
         import time

In [148]: # SETTING
         project_name = "proj_0ba2205_neuralnet_expanded"
         firmware_name = project_name + ".bit"
         n_input = 4
         n_output = 2
         benchmark = True

In [153]: # LOAD OVERLAY
         overlay = Overlay(os.getcwd()+"/"+firmware_name)

In [154]: # GET MEMORY ADDRESS OF IP
         bm_starting_address = (overlay.ip_dict["bondmachine_0"]+"phys_addr")
         print(" Starting memory address of Bondmachine IP is (in dec): ", bm_starting_address)
         print(" Starting memory address of Bondmachine IP is (in hex): ", hex(bm_starting_address))

         Starting memory address of Bondmachine IP is (in dec): 1136658384
         Starting memory address of Bondmachine IP is (in hex): 0x43c05000

In [155]: # GET THE OBJECT NECESSARY TO INTERACT WITH AN IP
         sgi0 = MMIO(bm_starting_address, 128)

In [156]: # LOAD BENCHMARK TESTSET
         x_test = np.load('bondmate-authentication_x_test.npy')
         y_test = np.load('bondmate-authentication_y_test.npy')
         # get the first 20 samples
         x_test = x_test[:10]
         y_test = y_test[:10]
         print(" Example of first two input: ", x_test[:1])
         print(" Example of first two output: ", y_test[:1])

         Example of first two input: [[ 0.39886742  0.76609776 -0.39093127 -0.58781728]]
         Example of first two output: [[ 1.  0.]]

In [157]: # IN THIS CASE I WANT TO SEND ONLY THE FIRST X INPUT SAMPLE
         idx = 0
         results_to_dump = []
         for example in x_test:
             offset = 0
             for feature in list(example):
                 binToSend = get_binary_from_float(feature)
                 declen0 = len(binToSend) // 2
                 sgi0.write_mem_of_float(declen0) # WRITE THE FEATURE TO THE CORRESPONDING INPUT
                 offset = offset + 4 # 4 BYTES = 32 BIT
             time.sleep(1)
             out = np.asarray(read_output())
             #print(" sgi0.idx = ", classification, ", np.argmax(out[0:2])")
             classification = np.argmax(out[0:2])
             if (benchmark == True):
                 results_to_dump.append([out[0], out[1], classification, out[2]])
             else:
                 results_to_dump.append([out[0], out[1], classification])
             idx = idx + 1
             #break
         print(results_to_dump)

[[ 0.6895708225193222, 0.3104250833507913, 0, 10462.0], [ 0.57489191702511108, 0.42517088317758535, 0, 10522.0], [ 0.4009186220845402, 0.5990818701385406, 0, 8758.0], [ 0.78591807591222078], [ 0.21988888028310509, 0, 5448.0], [ 0.48210493584605713, 0.307895066435394287, 0, 14992.0], [ 0.152358591899642844, 0.3675418108357938, 0, 12287.0], [ 0.6057641530398263, 0.33423587478662878, 0, 8191.0], [ 0.69289423393248612, 0.307095176646288611, 0, 10592.0], [ 0.63776418830871582, 0.3622578188896179, 0, 11627.0], [ 0.4755048195648929, 0.32444518845450171, 0, 19076.0]]

In [158]: import csv
         f = ["probability_0", "probability_1", "classification", "clock_cycles"]
         with open(project_name + ".csv", "w") as f:
             write = csv.writer(f)
             write.writerow(f)
             write.writerow(results_to_dump)
```

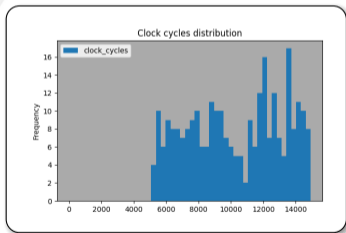
| Software | | | BondMachine | | |
|----------|--------|-------|-------------|--------|-------|
| prob0 | prob1 | class | prob0 | prob1 | class |
| 0.6895 | 0.3104 | 0 | 0.6895 | 0.3104 | 0 |
| 0.5748 | 0.4251 | 0 | 0.5748 | 0.4251 | 0 |
| 0.4009 | 0.5990 | 1 | 0.4009 | 0.5990 | 1 |

The output of the bm corresponds to the software output: **it works!**

Inference evaluation

Evaluation metrics used:

- **Inference speed:** time taken to predict a sample i.e. time between the arrival of the input and the change of the output measured with the **benchcore**;
- **Resource usage:** luts and registers in use;
- **Accuracy:** as the average percentage of error on probabilities.



- σ : 2875.94
- Mean: 10268.45
- Latency: 102.68 μ s

Resource usage

| resource | value | occupancy |
|----------|-------|-----------|
| regs | 15122 | 28.42% |
| luts | 11192 | 10.51% |

Is it possible to **optimize** this solution? (Yes)

Tons of ways for optimizations

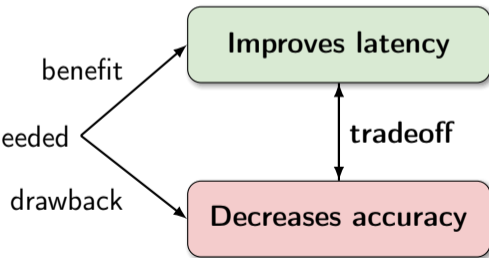
BondMachine is highly customizable and a lot of optimizations can be made. For example, you can scale the size of the registers (32,16,8 .. bit), choose whether to collapse processors up to customize the single neuron (and these are just some examples).

Customizing neurons

Remember the **softmax** function?

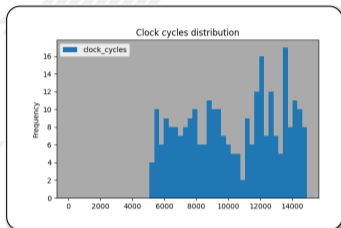
$$\sigma(\vec{z})_i = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}}$$

K can be customize as needed



Results of optimization

Changing number of K iterations of the softmax function...

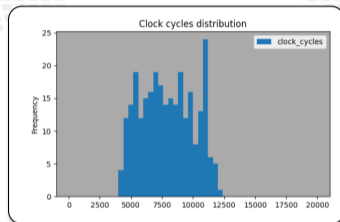


- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|



- K : 16
- σ : 2106.32
- Mean: 7946.16
- Latency: 79 μ s
- Prediction: 100%

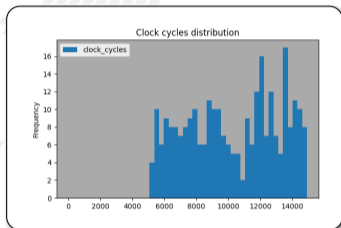
| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|

Results of optimization

Changing number of K iterations of the softmax function...

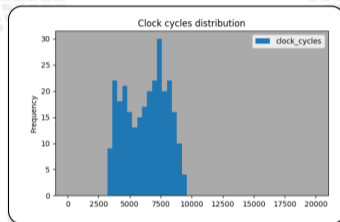


- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|



- K : 13
- σ : 1669.88
- Mean: 6312.26
- Latency: 63 μ s
- Prediction: 100%

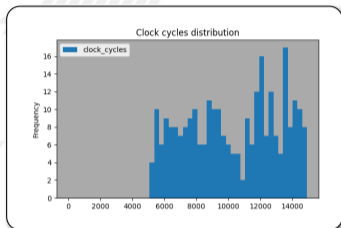
| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|

Results of optimization

Changing number of K iterations of the softmax function...

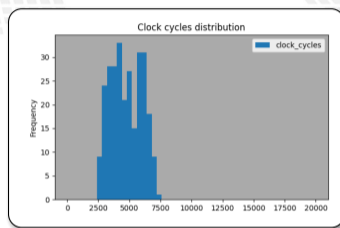


- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|



- K : 10
- σ : 1232.47
- Mean: 4766.75
- Latency: 47 μ s
- Prediction: 100%

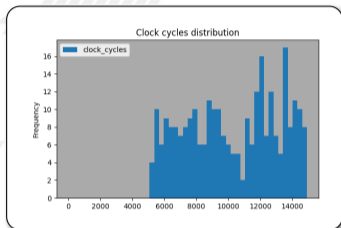
| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6162e^{-07}$ | $1.1013e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6525e^{-07}$ | $1.1831e^{-07}$ |
|-------|-----------------|-----------------|

Results of optimization

Changing number of K iterations of the softmax function...

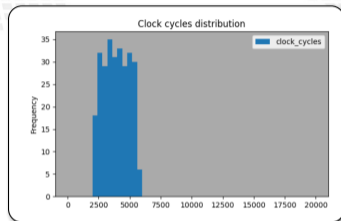


- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|



- K : 8
- σ : 1015.50
- Mean: 3913.66
- Latency: 39 μ s
- Prediction: 100%

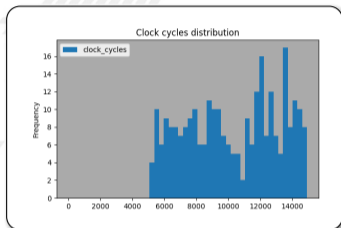
| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $6.5562e^{-05}$ | $1.7607e^{-05}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $6.6098e^{-05}$ | $1.7609e^{-05}$ |
|-------|-----------------|-----------------|

Results of optimization

Changing number of K iterations of the softmax function...

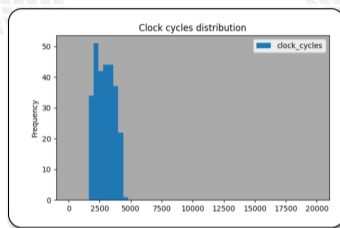


- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|



- K : 5
- σ : 740
- Mean: 2911
- Latency: 29 μ s
- Prediction: 100%

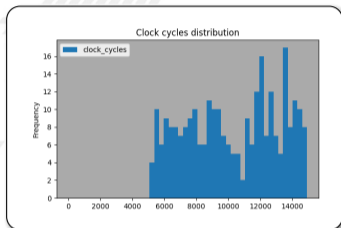
| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $3.1070e^{-05}$ | $7.5290e^{-05}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $3.1070e^{-05}$ | $7.5290e^{-05}$ |
|-------|-----------------|-----------------|

Results of optimization

Changing number of K iterations of the softmax function...

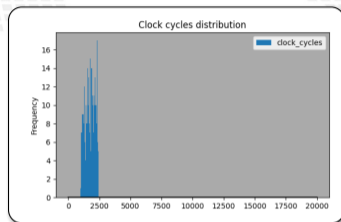


- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|



- K : 3
- σ : 394.10
- Mean: 1750.93
- Latency: 17 μ s
- Prediction: 100%

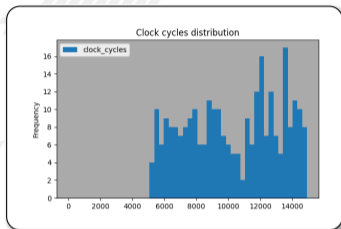
| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|--------|--------|
| prob0 | 0.0053 | 0.0090 |
|-------|--------|--------|

| | | |
|-------|--------|--------|
| prob1 | 0.0053 | 0.0090 |
|-------|--------|--------|

Results of optimization

Changing number of K iterations of the softmax function...

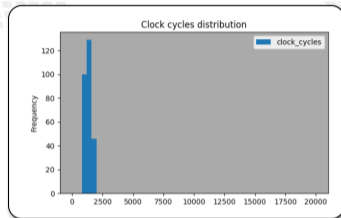


- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
|-------|-----------------|-----------------|

| | | |
|-------|-----------------|-----------------|
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |
|-------|-----------------|-----------------|



- K : 2
- σ : 268.69
- Mean: 1311.11
- Latency: 13.11 μ s
- Prediction: 100%

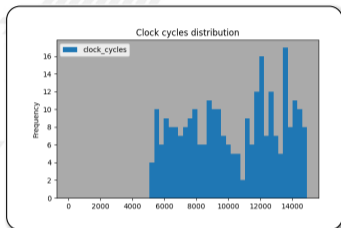
| | mean | σ |
|--|------|----------|
|--|------|----------|

| | | |
|-------|--------|--------|
| prob0 | 0.0193 | 0.0232 |
|-------|--------|--------|

| | | |
|-------|--------|--------|
| prob1 | 0.0193 | 0.0232 |
|-------|--------|--------|

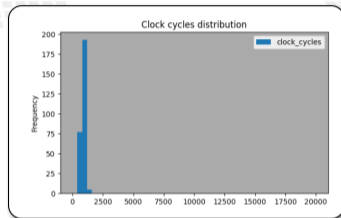
Results of optimization

Changing number of K iterations of the softmax function...



- K : 20
- σ : 2875.94
- Mean: 10268.45
- Latency: 102 μ s
- Prediction: 100%

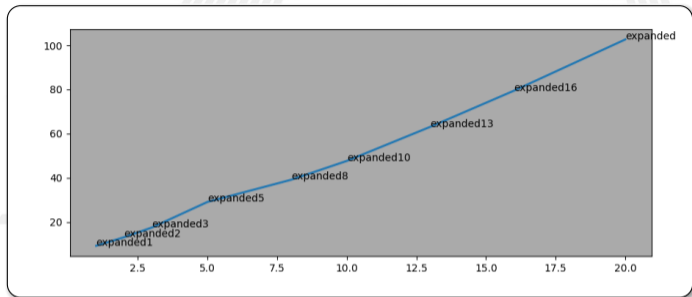
| | mean | σ |
|-------|-----------------|-----------------|
| prob0 | $1.6470e^{-07}$ | $1.2332e^{-07}$ |
| prob1 | $1.6623e^{-07}$ | $1.2142e^{-07}$ |



- K : 1
- σ : 173.25
- Mean: 923.71
- Latency: 9.23 μ s
- Prediction: 100%

| | mean | σ |
|-------|--------|----------|
| prob0 | 0.0990 | 0.1641 |
| prob1 | 0.0990 | 0.1641 |

Results of optimization



| K | Inference time |
|----|----------------|
| 1 | 9.23 μ s |
| 2 | 13.11 μ s |
| 3 | 17.50 μ s |
| 5 | 29.11 μ s |
| 8 | 39.13 μ s |
| 10 | 47.66 μ s |
| 13 | 63.12 μ s |
| 16 | 79.46 μ s |
| 20 | 102.68 μ s |

Reduced inference times by a factor of 10 ... only by decreasing the number of iterations.



Next steps...

We are still at the beginning ...

- **More datasets:** test on other datasets with more features and multiclass classification;
- **Optimizations:** optimize the solution trying to reduce the use of resources while maintaining accuracy and inference time;
- **Integrations with existing tools:** combine the advantages of the proposed solution with other tools that make inference on FPGAs such as HLS4ML;
- **Neurons:** increase the library of neurons to support other activation functions;
- **Boards:** make the solution heterogeneous and vendor independent;
- **Evaluate results:** compare the results obtained with other technologies (CPU and GPU) in terms of inference speed and energy efficiency;
- **Training on FPGA:** train a neural network on FPGA.

Schools and courses, conferences and docs

Courses and schools:

- Machine Learning Techniques With FPGA Devices For Particle Physics Experiments (11/2022)
- SOSC2022 (11/2022)
- Third ML-INFN Hackathon: Advanced Level (11/2022)

Papers:

- Work in progress: BM Machine Learning Paper 2022

Documentation:

- <https://github.com/BondMachineHQ/ml-ebaz4205>
- https://github.com/BondMachineHQ/bondmachine_ebaz4205_buildroot_example
- <https://github.com/BondMachineHQ/ml-zedboard>
- https://github.com/BondMachineHQ/bondmachine_ebaz4205_buildroot

