

10/3@BUE

Complete vectorlike fourth family and new $U(1)'$ for muon anomalies

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2205.10480 (PRD), 2104.04461 (PRD), 1911.11075 (PRD), 1906.11297 (PRD)

in collaboration with

S.Raby [Ohio State U.], A.Trautner [Max Planck Inst.]

Outline

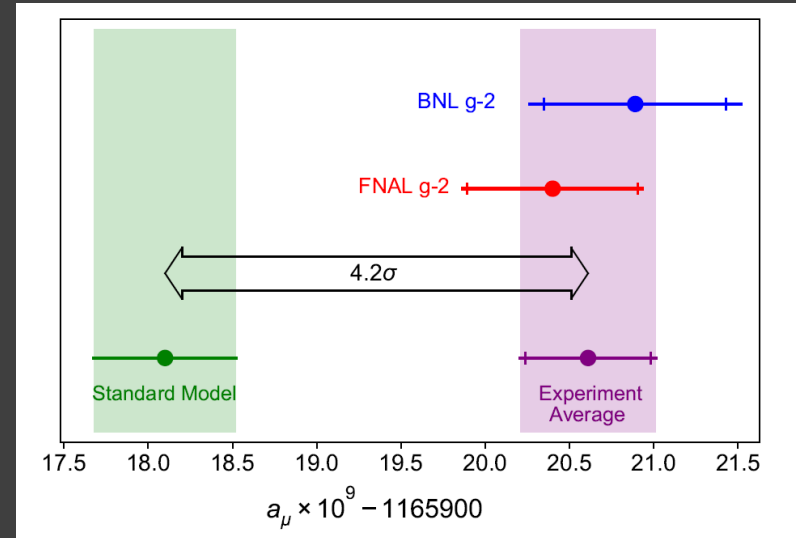
1. Muon anomalies
2. Vector-like $U(1)'$ model
3. High multiplicity muon signals from Z' and VL lepton
4. W mass anomaly
5. Summary

muon g-2

➤ muon g-2

$$\begin{aligned}\Delta a_\mu &= a_\mu^{\text{exp}} - a_\mu^{\text{SM}} \\ &= (2.51 \pm 0.59) \times 10^{-9}\end{aligned}$$

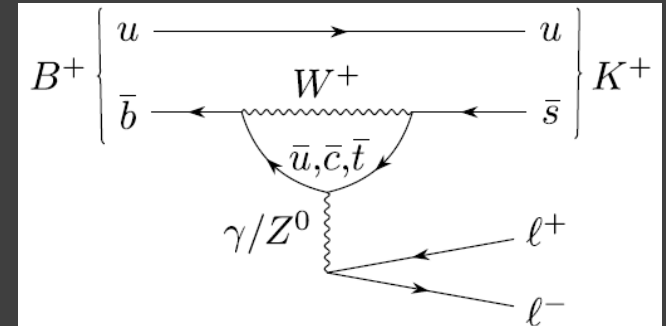
4.2 σ discrepancy



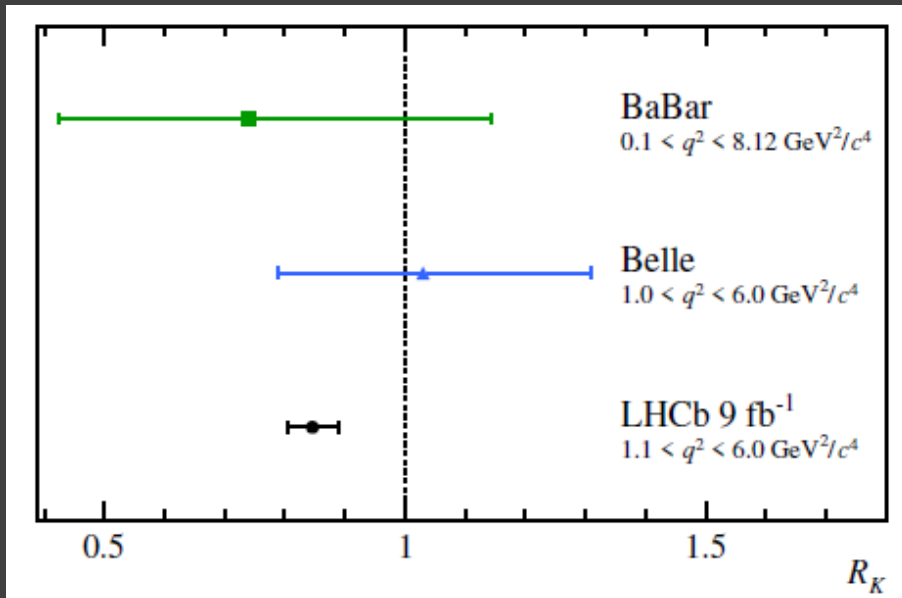
- EW-size corrections are necessary
- lattice results are more consistent with the Exp. value

R_K anomaly

$$R_K = \frac{\Gamma(B \rightarrow K \mu^+ \mu^-)}{\Gamma(B \rightarrow K e^+ e^-)}$$



SM holds lepton universality: $R_K = 1$



➤ Moriond 2021

$$R_K = 0.846^{+0.042}_{-0.039} \pm 0.013$$

$\sim 3.1 \sigma$ below

$b \rightarrow s \mu^+ \mu^-$ anomalies

➤ Lepton Non-Universality

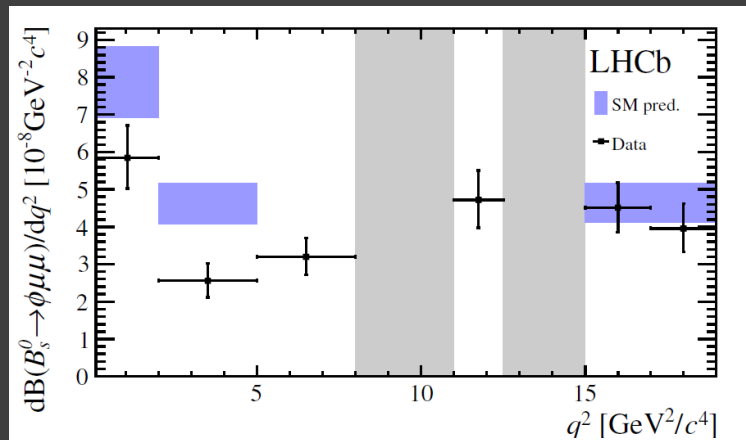
$$R_K = 0.846_{-0.039}^{+0.042} \pm 0.013$$

below $R_K^{SM} = 1.0 \sim 3.1 \sigma$

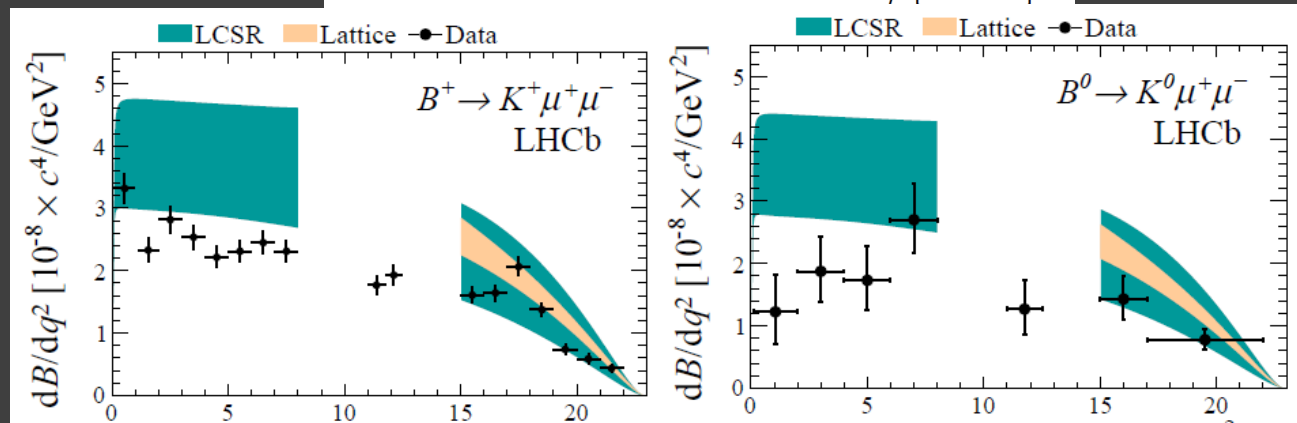
➤ Branching ratio $B \rightarrow \phi \mu^+ \mu^-, K \mu^+ \mu^-$

+ angular observables

3.3 σ discrepancy



below SM pred.
 $\sim 3.0 \sigma$



below SM pred.

$b \rightarrow s\mu\mu$ anomaly

$$\mathcal{H}_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha}{4\pi} \sum_{j=9,10} (C_j \mathcal{O}_j + C'_j \mathcal{O}'_j) + h.c.$$

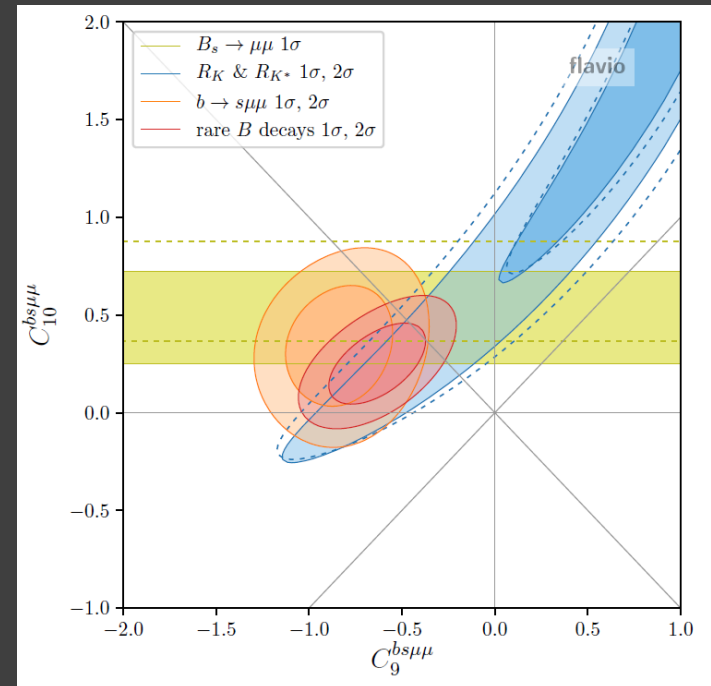
$$\mathcal{O}_9^{(l)\mu} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{l}\gamma^\mu l) \quad \mathcal{O}'_{10}{}^{(l)\mu} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{l}\gamma^\mu \gamma_5 l)$$

➤ global fit of (C_9^{NP}, C_{10}^{NP})

fit the Wilson coefficients to all observable related to $b \rightarrow s\mu\mu$

➔ $C_9^{NP} = -0.80 \pm 0.14$

➔ 5.7σ improvement from SM



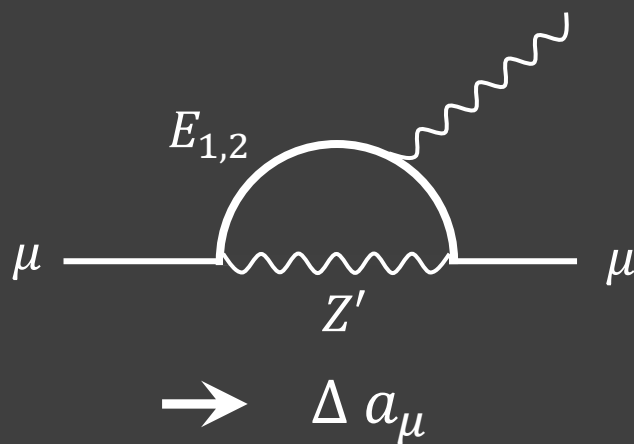
Outline

1. Muon anomalies
2. **Vector-like $U(1)'$ model** ✓ Can both anomalies be explained?
3. High multiplicity muon signals from Z' and VL lepton
4. W mass anomaly
5. Summary

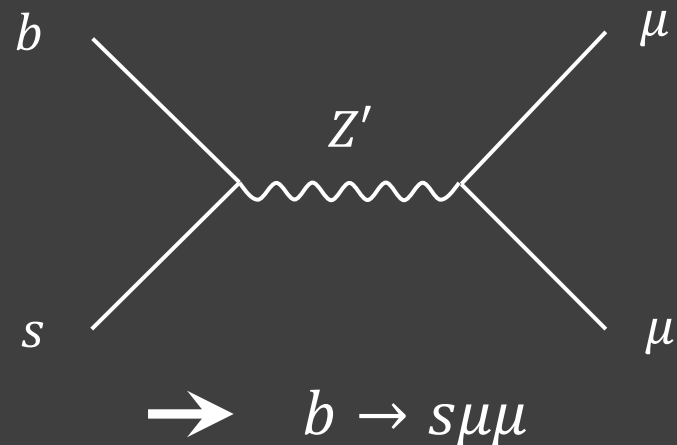
Vector-Like [VL] fermion + $U(1)'$

simultaneous explanation for muon anomalies

➤ $U(1)'$ + VL-leptons



+ VL-quarks



➤ Models

- $U(1)_{L_\mu - L_\tau}$ + VL-lepton + VL-quark W.Altmannshofer et.al 1604.08221
- $U(1)_{3-4}$ + VL 4th family S. Raby, A.Trautner 1712.09360
- e.t.c. Allanach, Queiroz et.al 1511.07447, Megias, Quiros et.al 1701.05072

Our Model

➤ Complete Vector-Like 4th Family + $U(1)'$

	Q_L	\bar{U}_R	\bar{D}_R	L_L	\bar{E}_R	\bar{N}_R	\bar{Q}_R	U_L	D_L	\bar{L}_R	E_L	N_L	ϕ	Φ
$SU(3)_C$	3	$\bar{3}$	$\bar{3}$	1	1	1	$\bar{3}$	3	3	1	1	1	1	1
$SU(2)_L$	2	1	1	2	1	1	2	1	1	2	1	1	1	1
$U(1)_Y$	$\frac{1}{3}$	$-\frac{4}{3}$	$\frac{2}{3}$	-1	2	0	$-\frac{1}{3}$	$\frac{4}{3}$	$-\frac{2}{3}$	1	-2	0	0	0
$U(1)'$	-1	+1	+1	-1	+1	+1	+1	-1	-1	+1	-1	-1	0	-1

VL fermions

$\langle\phi\rangle\sim\langle\Phi\rangle\sim\text{TeV}$

*similar setup:

A. Falkowski, S. F. King et.al
1803.04430

- Only the VL-family have $U(1)'$ charge
- Z' - SM particle couplings appear in mass basis
- Unwanted new physics contributions may be evaded

Mass Matrix and Couplings

- Yukawa interactions and mass matrix

$$-\mathcal{L}_{\text{Yukawa}} = \bar{e}_{R_i} Y_e^{ij} l_{L_j} H + \lambda_e \bar{E}_R L_L H - \lambda'_e \bar{L}_R \tilde{H} E_L \\ + \lambda_V^L \phi \bar{L}_R L_L - \lambda_V^E \phi \bar{E}_R E_R + \lambda_i^L \Phi \bar{L}_R l_{L_i} - \lambda_i^E \Phi^* \bar{e}_{R_i} E_L$$

$$\longrightarrow \bar{\hat{E}}_R M_e \hat{E}_L = \begin{pmatrix} \bar{e}_{R_i} & \bar{E}_R & \bar{E}'_R \end{pmatrix} \begin{pmatrix} Y_e^{ij} H & 0 & \lambda_i^L \Phi \\ 0 & \lambda_e H & \lambda_V^E \phi \\ \lambda_j^L \Phi & \lambda_V^L \phi & \lambda'_e H \end{pmatrix} \begin{pmatrix} e_{L_j} \\ E'_L \\ E_L \end{pmatrix}$$

* similar for quarks/neutrino

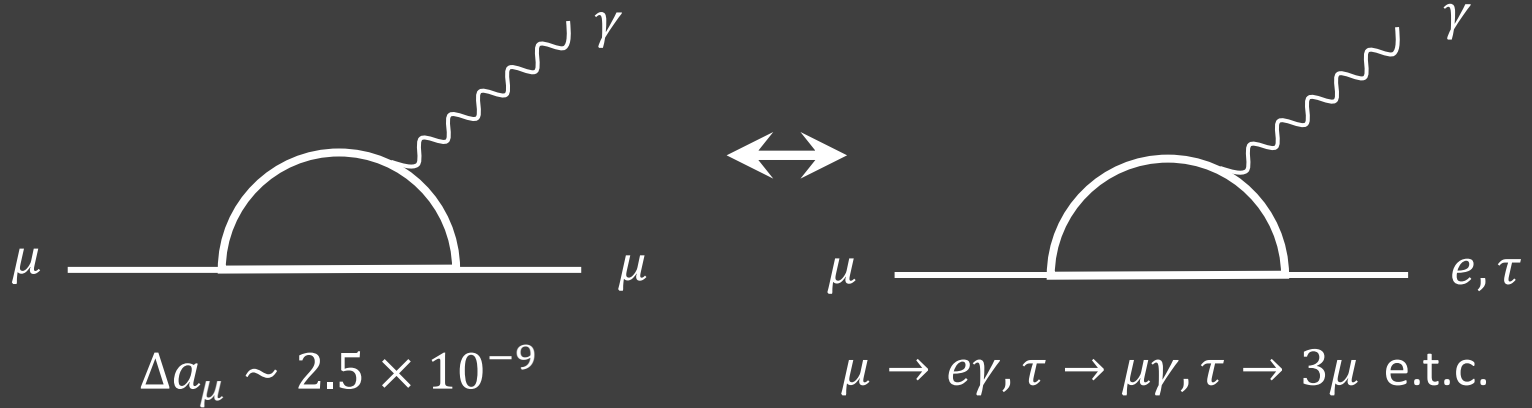
- Z' -coupling in mass basis : $U_R^{e\dagger} M_e U_L^e = \text{diag}(m_e, m_\mu, m_\tau, m_{E_1}, m_{E_2})$

$$g_{e_L}^{Z'} = g' U_L^{e\dagger} \begin{pmatrix} 0_{3 \times 3} & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} U_L^e \quad g_{e_R}^{Z'} = g' U_R^{e\dagger} \begin{pmatrix} 0_{3 \times 3} & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} U_R^e$$

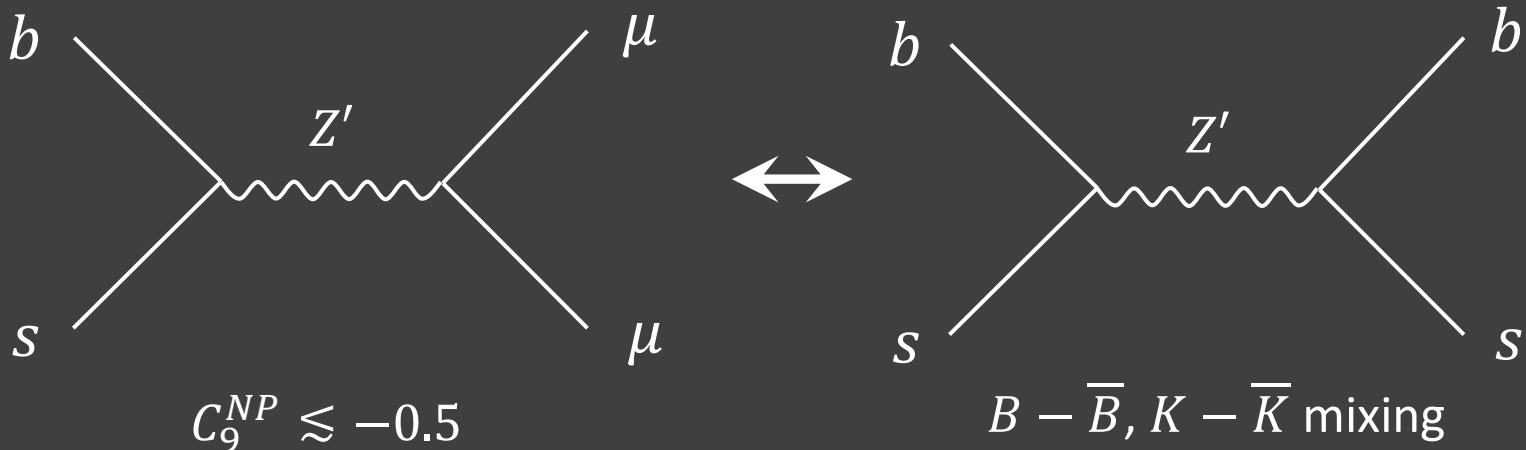
➔ Z' -couplings to the SM families

Possible Flavor Violations

➤ Lepton flavor violation



➤ Quark flavor violation



CKM Matrix

5 × 5 “CKM” matrix $\hat{V}_{CKM} = U_u^\dagger \begin{pmatrix} 1_{3 \times 3} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & \boxed{0} \end{pmatrix} U_d$

CKM matrix is **NOT** unitary

➤ Non-Unitarity

$$\sum_{k=1}^3 [V_{CKM}]_{ik} [V_{CKM}]_{kj} = \delta_{ij} + \mathcal{O} \left(\epsilon_{t_R}^2 \frac{m_t^2}{M_Q^2} \right) \quad \begin{array}{l} M_Q: \text{VL quark [VLQ] mass} \\ \epsilon_{t_R}: \text{mixing bet. top and VLQ} \end{array}$$

$$\epsilon_{t_R}^2 \frac{m_t^2}{M_Q^2} \sim 7.2 \times 10^{-7} \times \left(\frac{\epsilon_{t_R}}{0.01} \right)^2 \left(\frac{2 \text{ TeV}}{M_Q} \right)^2$$

CKM is approximately unitary as far as $\epsilon_{t_R} \lesssim 0.01$

Benchmark Points

$$\chi^2 = 22.6, \quad 25.0, \quad 23.3, \quad 23.8 \quad N_{dof} = 33$$

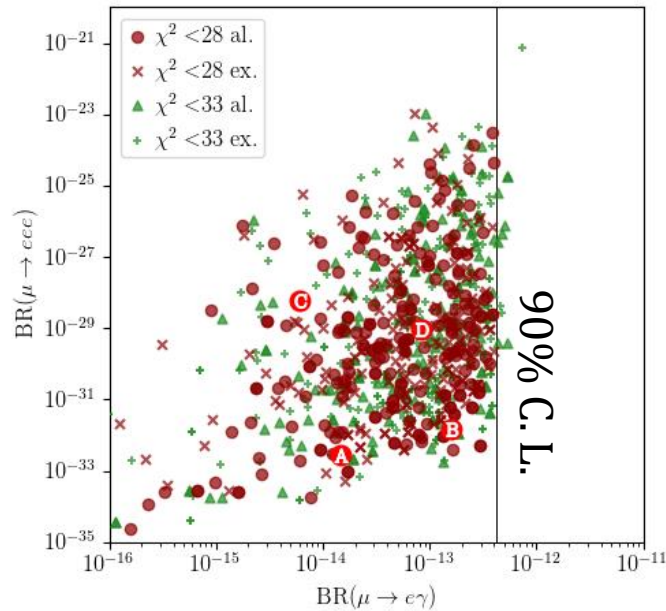
Observables	Point A	Point B	Point C	Point D	Exp.
$\Delta a_\mu \times 10^9$	2.62	2.52	2.52	2.45	2.68 ± 0.76
$\text{BR}(\mu \rightarrow e\gamma) \times 10^{13}$	0.147	1.597	0.061	0.822	< 4.2
$\text{BR}(\tau \rightarrow \mu\gamma) \times 10^8$	3.34×10^{-4}	3.62×10^{-4}	3.27×10^{-6}	8.45×10^{-7}	< 4.4
$\text{BR}(\tau \rightarrow \mu\mu\mu) \times 10^8$	6.96×10^{-3}	4.77×10^{-4}	6.55×10^{-5}	4.36×10^{-7}	< 2.1
$\text{Re } C_9^\mu$	-0.548	-0.806	-0.838	-0.808	-0.7 ± 0.3
$\text{Re } C_{10}^\mu$	0.370	0.252	0.347	0.322	0.4 ± 0.2
$\Delta M_d [\text{ps}^{-1}]$	0.561	0.610	0.598	0.590	0.506 ± 0.081
$\Delta M_s [\text{ps}^{-1}]$	19.6	19.8	19.4	20.0	17.76 ± 2.5
$S_{\psi K_s}$	0.697	0.696	0.692	0.695	0.695 ± 0.019
$S_{\psi\phi}$	0.0366	0.0374	0.0373	0.0379	0.021 ± 0.031
$R_{B_s \rightarrow \mu\mu}^{\text{th}}$	0.841	0.890	0.850	0.861	0.75 ± 0.16

$$\text{best } m_{E_1} > 1.2 \text{ TeV} \quad m_\chi > 750 \text{ GeV} \quad m_{Z'} > 750 \text{ GeV}$$

Most observables are explained within 1σ

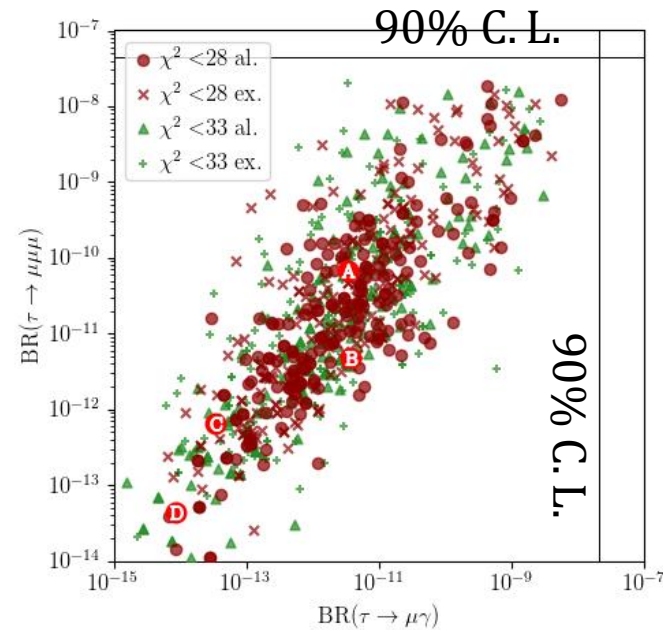
LFV decays

muon decays



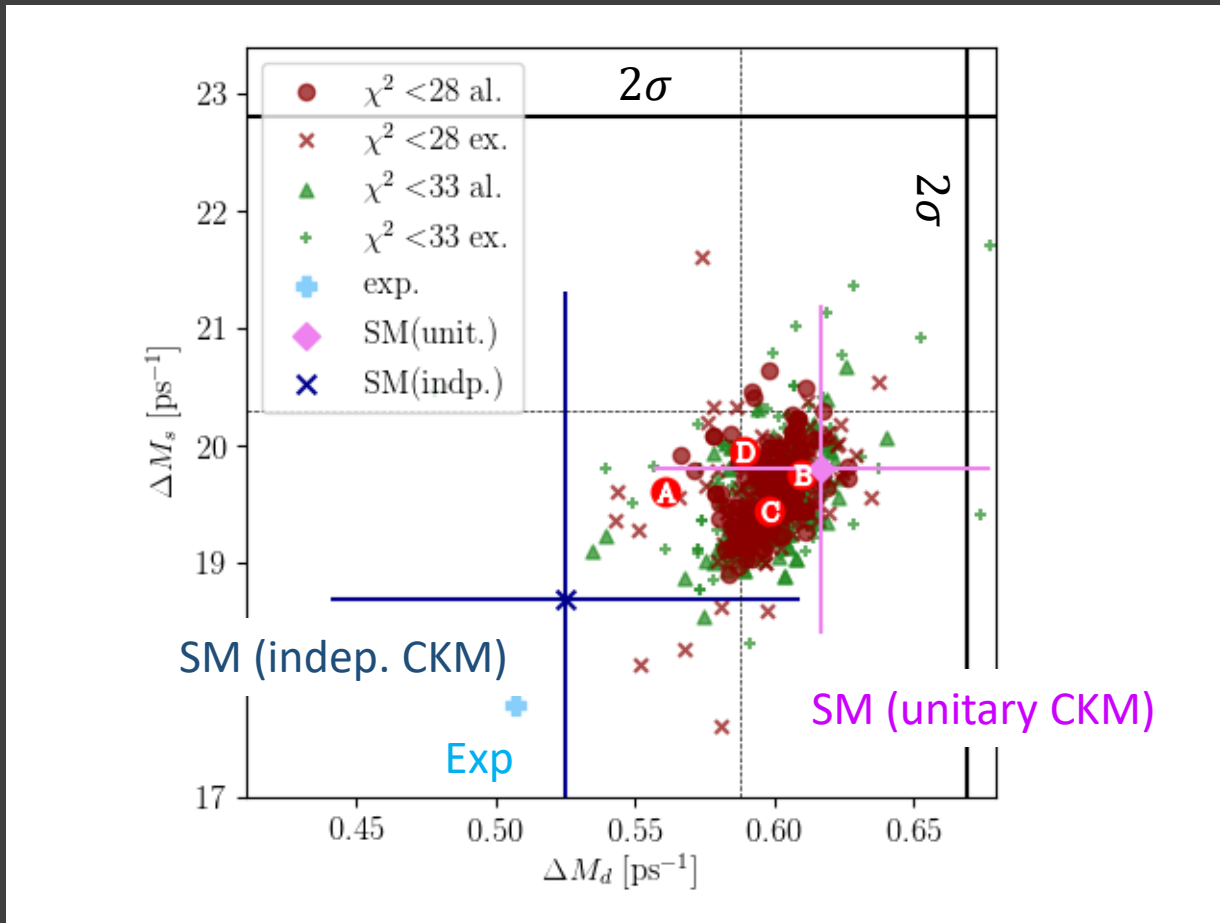
$$Br(\mu \rightarrow e\gamma) \gg Br(\mu \rightarrow eee)$$

tau decays



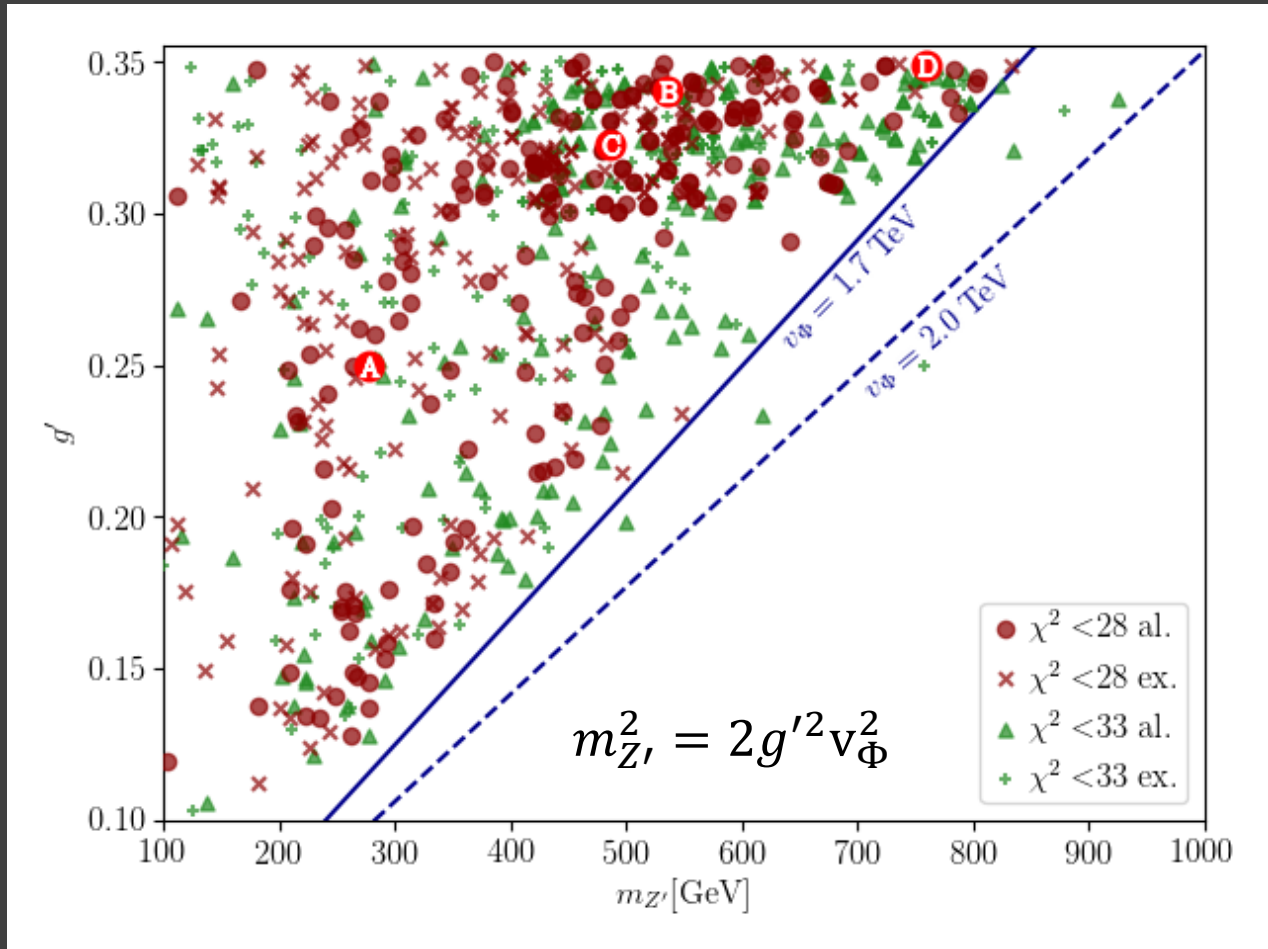
$$Br(\tau \rightarrow \mu\gamma) \lesssim Br(\tau \rightarrow \mu\mu\mu)$$

B-meson mixing



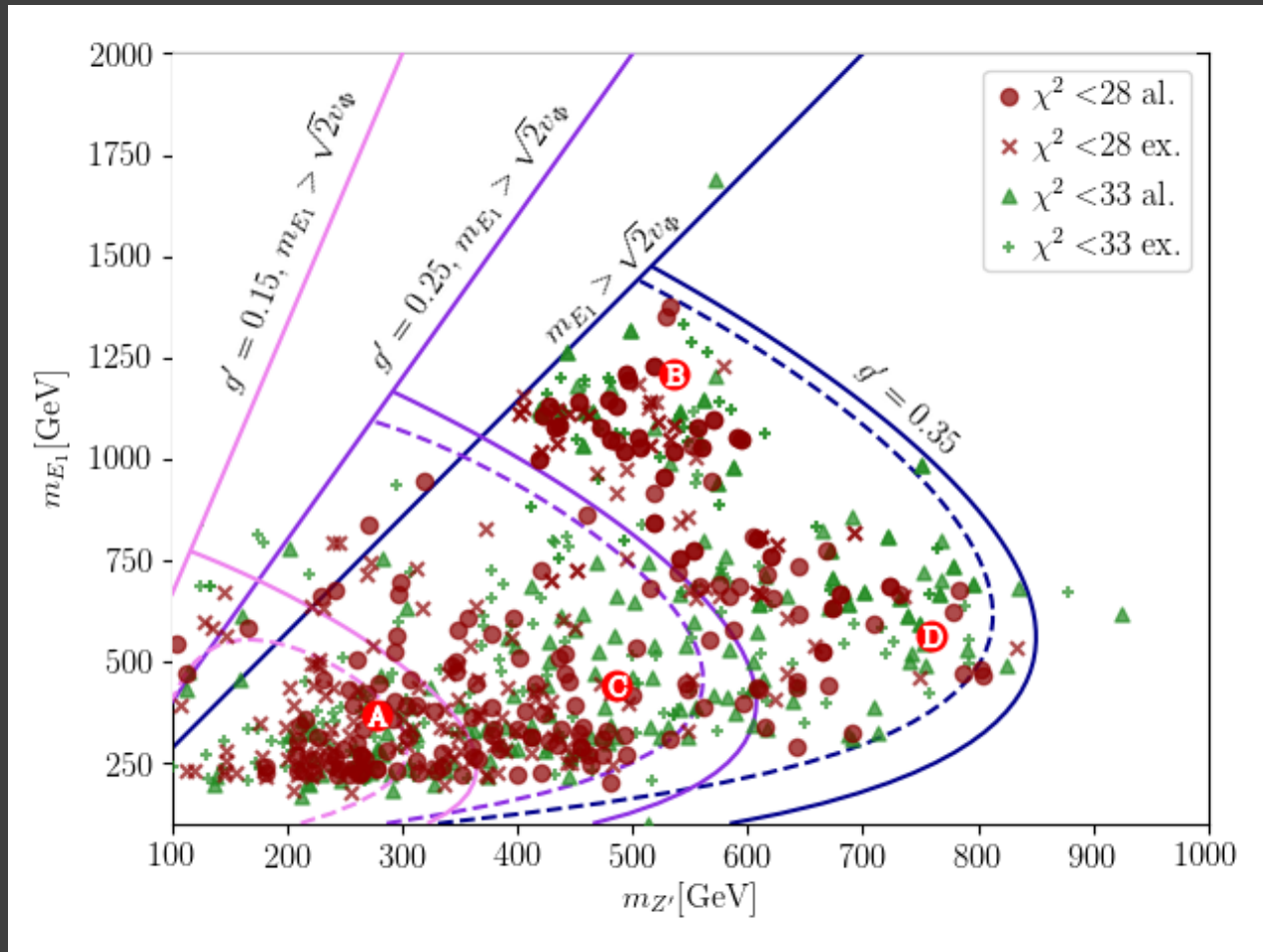
- B meson mixing is consistent with SM
- NP contributions are smaller than CKM uncertainties

Upper bound on Z' mass



$m_{Z'} < 800$ GeV is required for $\chi^2 < 28$

Upper bound on VL lepton mass



- Δa_μ is explained inside the contours
- VL lepton should be lighter than 1.4 TeV even if $m'_{Z'} \sim 500$ GeV

Summary

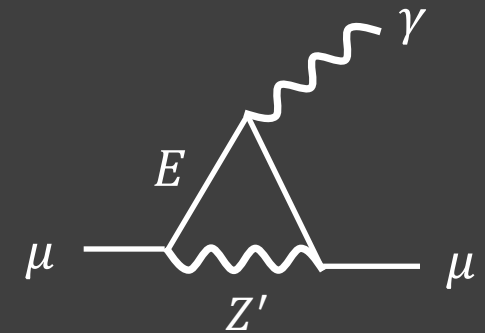
JK, S.Raby, A.Trautner, 1906.11297, 1911.11075

both anomalies are explained in models with Z' and vector-like [VL] lepton

➤ muon g-2

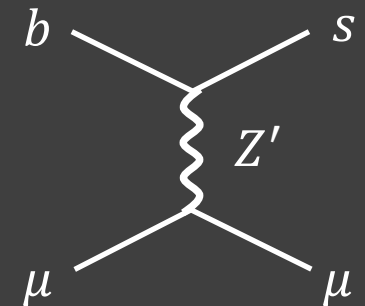
$$\Delta a_\mu \sim 5 \times 10^{-9} \times \left(\frac{500 \text{ GeV}}{m_{Z'}} \right)^2 \left(\frac{g_{\mu E}^L g_{\mu E}^R}{0.09} \right)$$

$g_{fF}^{L/R}$: $f - F - Z'$ coupling in L/R current



➤ $b \rightarrow s\mu\mu$ anomaly c.f. $C_9 \sim [-1, -0.5]$ is favored

$$C_9 \sim -0.83 \times \left(\frac{500 \text{ GeV}}{m_{Z'}} \right)^2 \left(\frac{g_{sb}^L}{0.0006} \right) \left(\frac{g_{\mu\mu}^L + g_{\mu\mu}^R}{0.6} \right)$$



$m_{Z'} \sim m_E \sim \mathcal{O}(500 \text{ GeV})$ is predicted

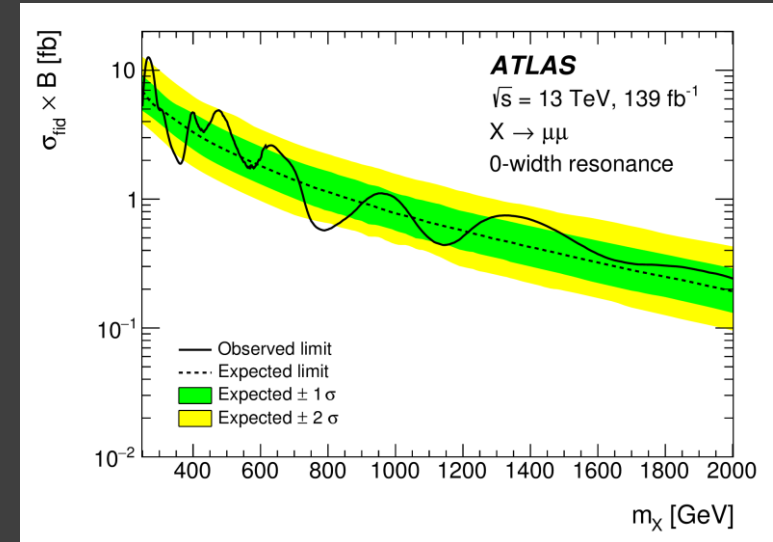
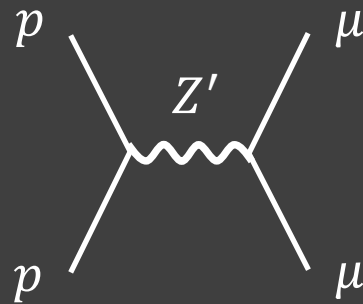
Outline

1. Muon anomalies
2. Vector-like $U(1)'$ model
3. High multiplicity muon signals from Z' and VL lepton
4. W mass anomaly
 - ✓ How to confirm the model ?
use LHC
5. Summary

Z' search

- dimuon search at LHC

$$pp \rightarrow Z' \rightarrow \mu^+ \mu^-$$



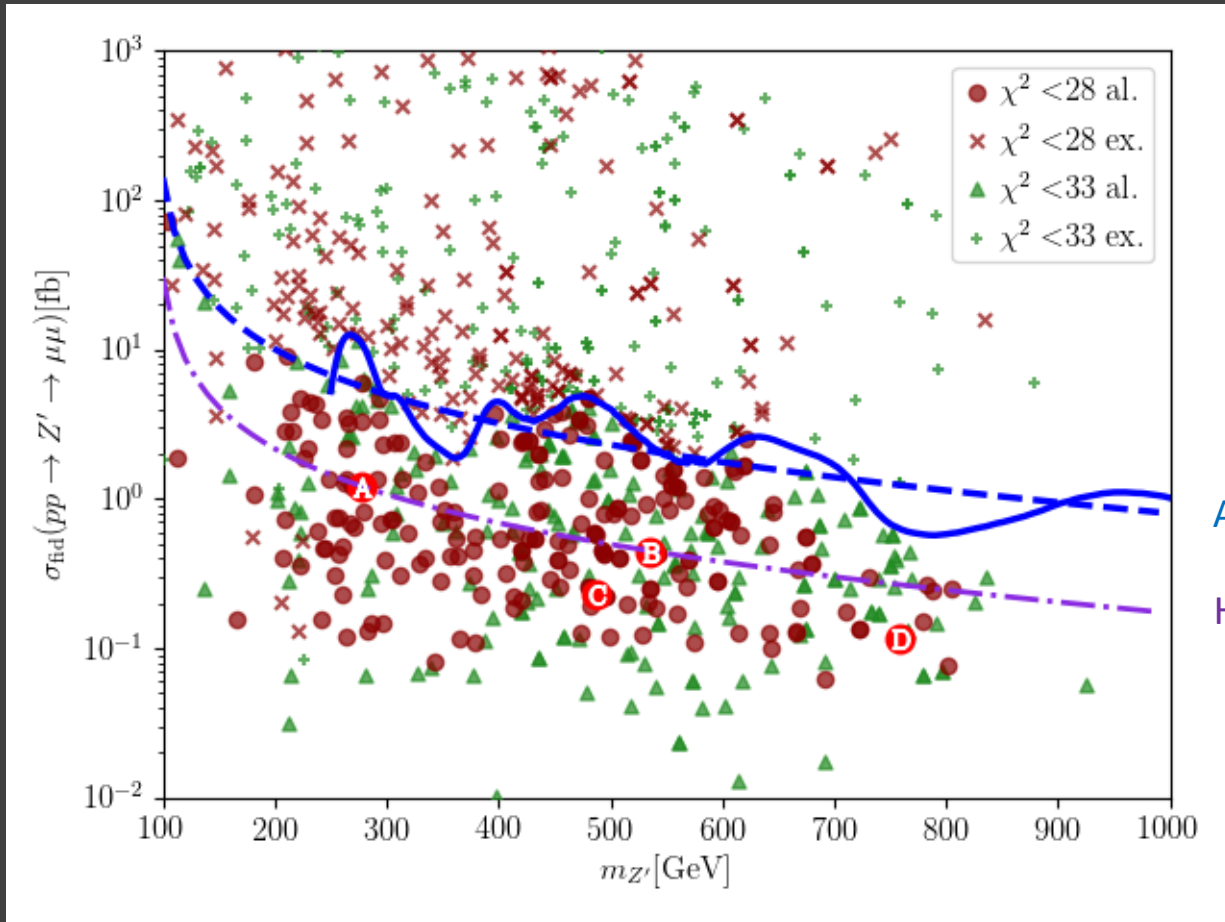
- muon anomalies, $B_s - \bar{B}_s$ mixing

$$C_9 \sim -0.83 \times \left(\frac{500 \text{ GeV}}{m_{Z'}} \right)^2 \left(\frac{g_{sb}^L}{0.0006} \right) \left(\frac{g_{\mu\mu}^L + g_{\mu\mu}^R}{0.6} \right)$$

Z' may strongly couple to leptons, but weakly to quarks

$$\Rightarrow \sigma_{\text{fid}}(pp \rightarrow Z' \rightarrow \mu^+ \mu^-) < 1 \text{ fb}$$

Dimuon Z' Search at LHC



MadGraph5
FeynRules

arXiv: 1903.06248

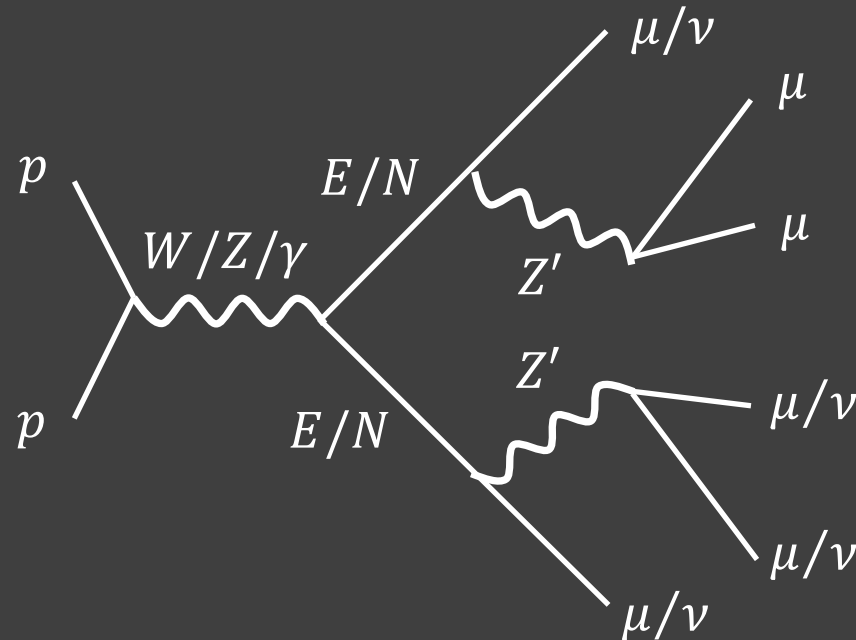
ATLAS limit

HL-LHC expected

- Cross sections can be smaller than current limits
- HL-LHC is sensitive to not all, but many points

$\geq 4\mu$ signal

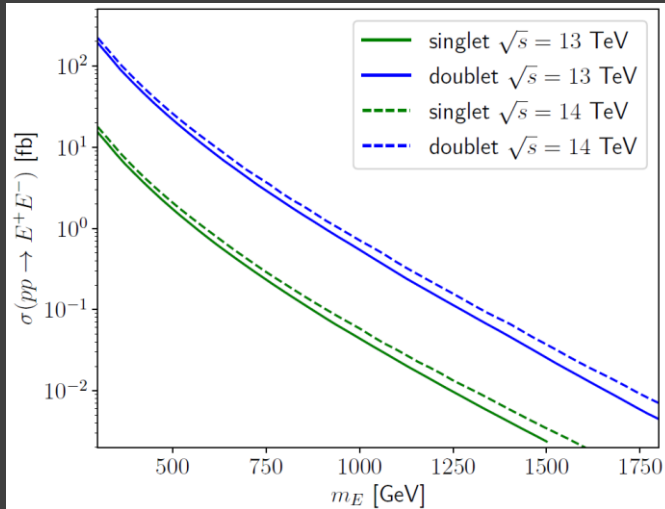
➤ VL-lepton pair production: $pp \rightarrow \bar{L}L$ $L = E/N$



- 6 muons are produced if both $Z' \rightarrow \mu\mu$ from $pp \rightarrow \bar{E}E \rightarrow \mu^- \mu^+ Z' Z'$
- 4 muons are produced if one $Z' \rightarrow \mu\mu$
- 4 muons are also produced from VL neutrino production

Assumptions

- VL leptons are assumed to be $SU(2)_L$ singlet or doublet



production cross section

$m_E = m_N$ for doublet case

Madgraph5

- Z' boson decays to muon or neutrino

$$\text{BR}(Z' \rightarrow \mu\mu) = \frac{\Gamma(Z' \rightarrow \mu\mu)}{\Gamma(Z' \rightarrow \nu\nu) + \Gamma(Z' \rightarrow \mu\mu)} \simeq \frac{|g_{\mu\mu}^L|^2 + |g_{\mu\mu}^R|^2}{2|g_{\mu\mu}^L|^2 + |g_{\mu\mu}^R|^2} = \frac{2}{3}$$

$|g_{\mu\mu}^L| = |g_{\mu\mu}^R|$ is predicted in C_9 -only or C_{10} -only scenario

Recasting ATLAS analysis 2103.11684

➤ Signal regions

$$*p_T^\mu > 5 \text{ GeV}$$

SR	$N_{e,\mu}$	N_τ	N_b	Z boson	selection
SR0 ^{loose} _{bveto}	≥ 4	≥ 0	$= 0$	veto	$m_{\text{eff}} > 600 \text{ GeV}$
SR0 ^{tight} _{bveto}	≥ 4	≥ 0	$= 0$	veto	$m_{\text{eff}} > 1250 \text{ GeV}$
SR5L	≥ 5	≥ 0	≥ 0	-	-

+ trigger condition

$$m_{\text{eff}} = E_T^{\text{miss}} + \sum_{\ell=e,\mu} p_T^\ell + \sum_{j(p_T > 40 \text{ GeV})} p_T^j$$

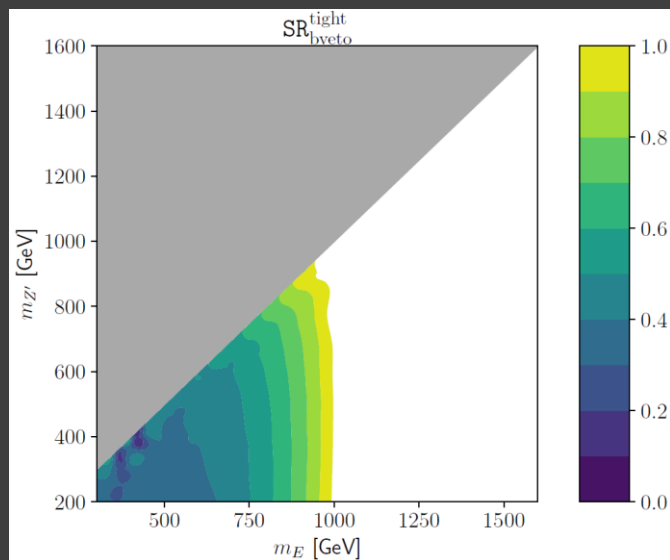
➤ Experimental result

	SR0 ^{loose} _{bveto}	SR0 ^{tight} _{bveto}	SR5L
data	11	1	21
SM	$11.5^{+2.9}_{-2.2}$	$3.5^{+2.0}_{-2.2}$	12.4 ± 2.3
S^{95}	9.79	3.87	17.88

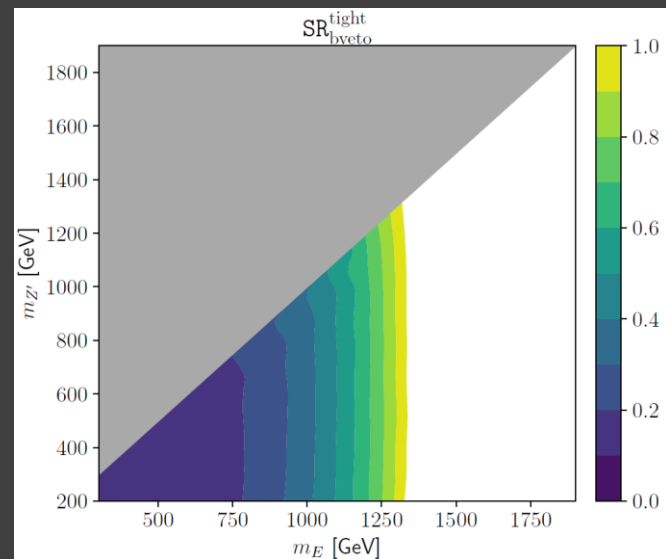
- no evidence of new physics
- 1.9σ excess in SR5L

95%C.L. limits on $\text{Br}(E \rightarrow Z' \mu)$

➤ $SU(2)_L$ singlet



➤ $SU(2)_L$ doublet



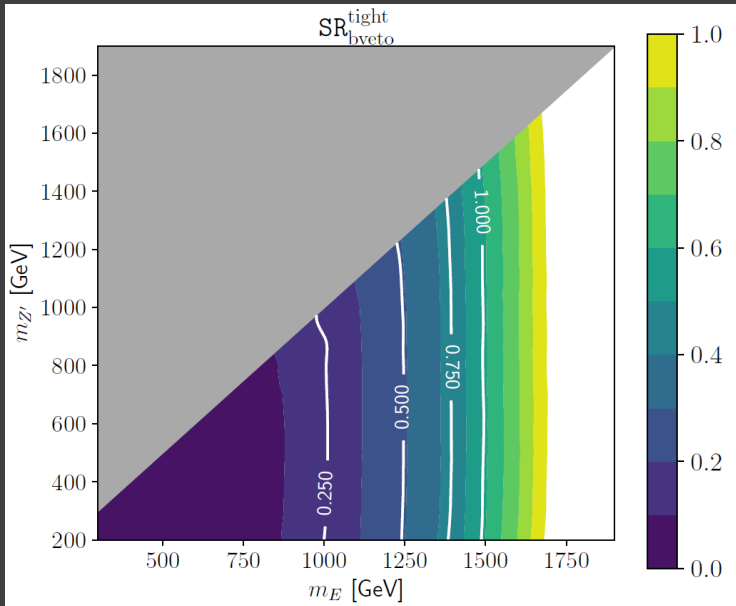
Madgraph5+pythia8+Delphes3

- $\text{SR}_{\text{bveto}}^{\text{tight}}$ gives the strongest bound for $\text{Br}(E \rightarrow Z' \mu)$
- limit is 1 (1.3) TeV for $\text{Br}(E \rightarrow Z' \mu) = 1$ for singlet (doublet)
- SR5L limit is weaker because of the excess

Future limits at HL-LHC: $L = 3\text{ab}^{-1}$

➤ $SR0_{\text{bveto}}^{\text{tight}}$

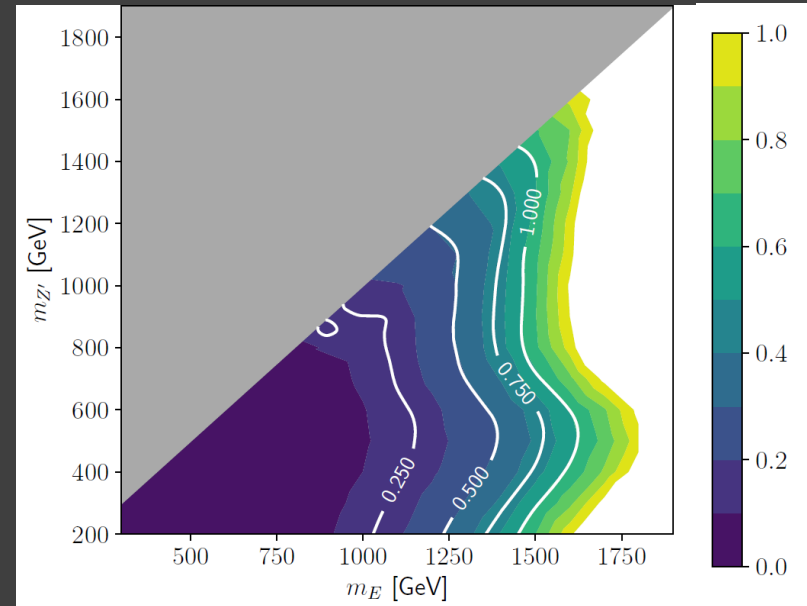
*doublet VL lepton



$$\text{bkg} = 3000/139 \ b^{13\text{TeV}} = 76.6$$

➤ $SR0_{\text{bveto}}^{\text{tight}}$

+ $|m_{OS} - 500| < 100$ (250) GeV



$$\text{bkg} = 10$$

Madgraph5+pythia8+Delphes3

- background colors are exclusion upper bounds
- white lines are discovery potential for a given $\text{Br}(E \rightarrow Z'\mu)$ attached on the line
- if $\text{Br}(E \rightarrow Z'\mu) = 1$, exclusion (discovery) limit is 1.7 (1.5) TeV by $SR0_{\text{bveto}}^{\text{tight}}$

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W mass anomaly ?

CDF, Science '22

➤ CDF measurement

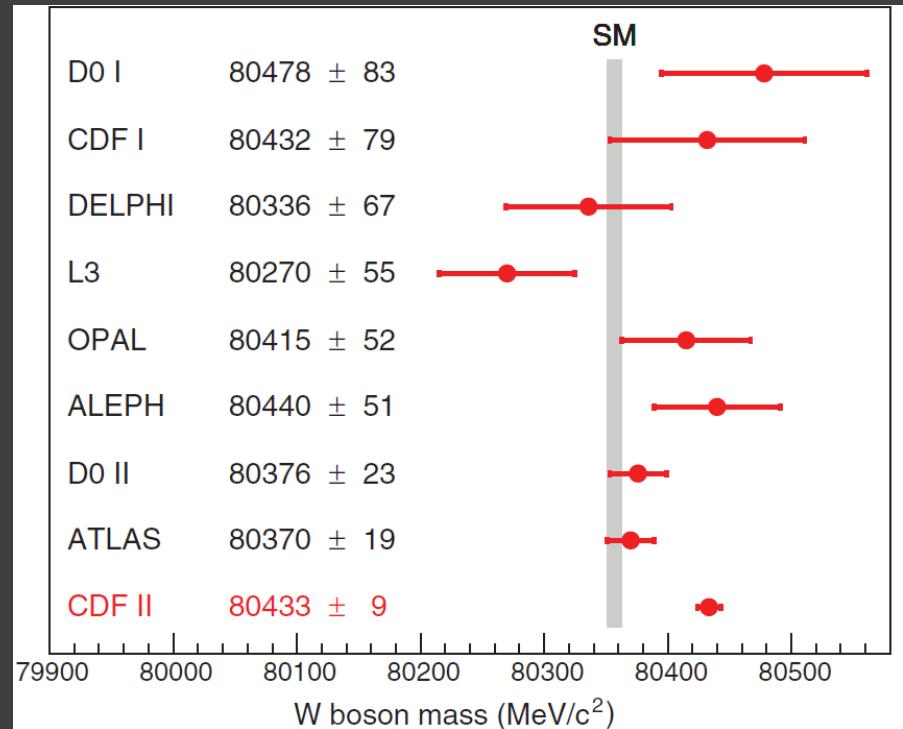
$$m_W = 80.4335 (94) \text{ GeV}$$

➤ PDG average

$$m_W = 80.379 (12) \text{ GeV}$$

➤ SM value _{PDG}

$$m_W = 80.361 (6) \text{ GeV}$$

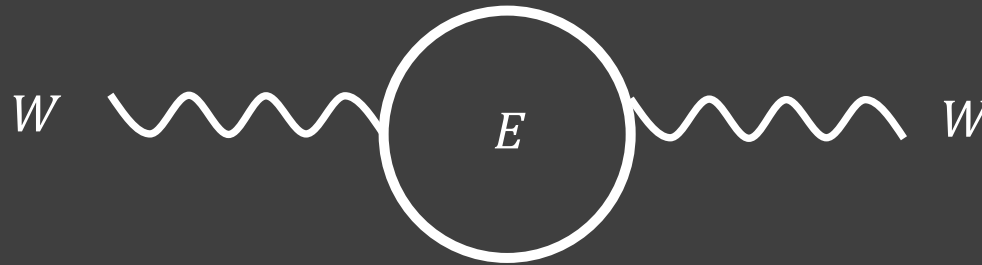


new value is 7σ larger than the SM expectation

Vector-like lepton explanation

* VL quark may be possible

J.Cao et.al. 2204.09477



- W mass shift by VL leptons $L^- (L^0)$: charged (neutral) doublet

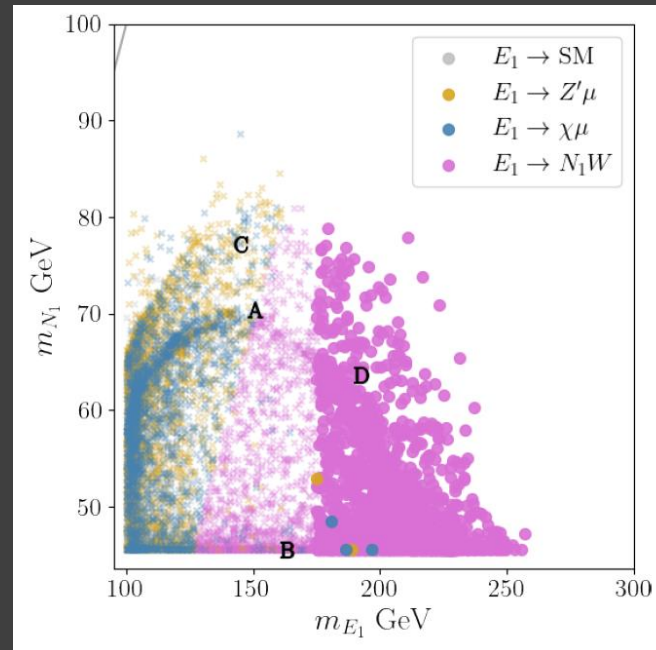
$$\frac{\delta m_W^2}{m_W^2} \sim 0.0014 \times \left(\frac{250 \text{ GeV}}{m_L} \right)^2 \left(\frac{m_{L^-}^2 - m_{L^0}^2}{(100 \text{ GeV})^2} \right)^2$$

- m_W is explained for $\mathcal{O}(200 \text{ GeV})$ VL lepton with $\mathcal{O}(10 \text{ GeV})$ mass diff.
- large singlet-doublet mixing is required as for muon g-2

Vector-like lepton explanation

2205.10480, JK, S.Raby

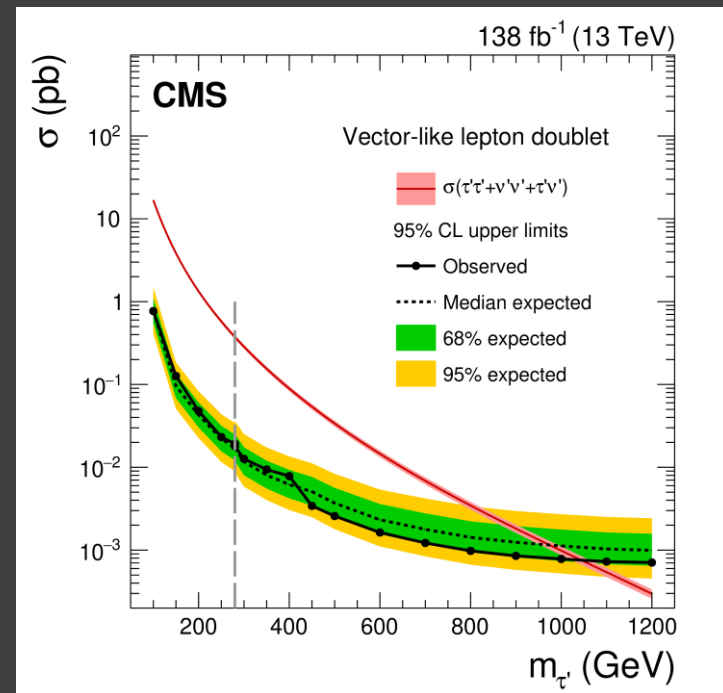
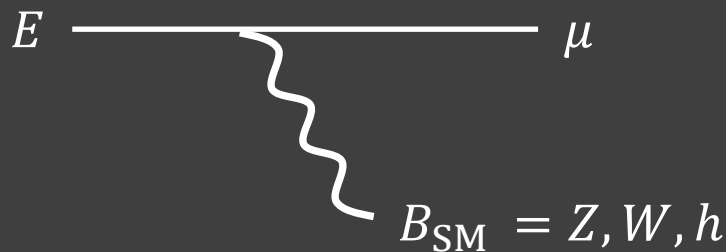
➤ with singlet VL neutrino



- VLL is lighter than 200 (250) GeV with (without) singlet VL lepton
- muon g-2 can be explained in both cases

LHC limits ?

➤ doublet VL lepton



* VLL decaying to tau

- Run1 limit for VL lepton decaying to muon is about 300 GeV

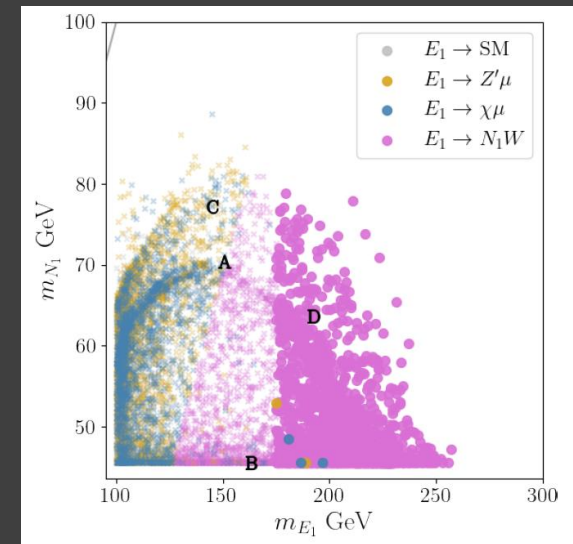
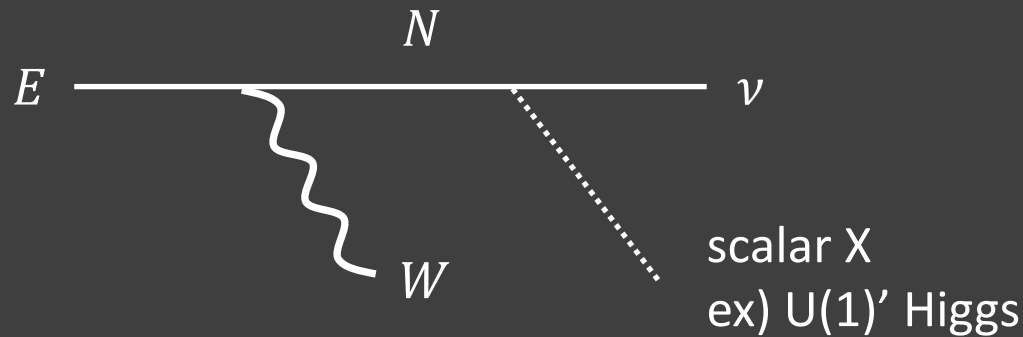
1408.3123, R.Dermisek, J.P.Hall et.al

- Run2 limit may be stronger than 800 GeV

LHC limits ? 2205.10480, JK, S.Raby

possible way to relax LHC limits

➤ VL lepton + VL neutrino + X



- VL neutrino can be singlet-like
- scalar X may decay hadronically
- complicated signals

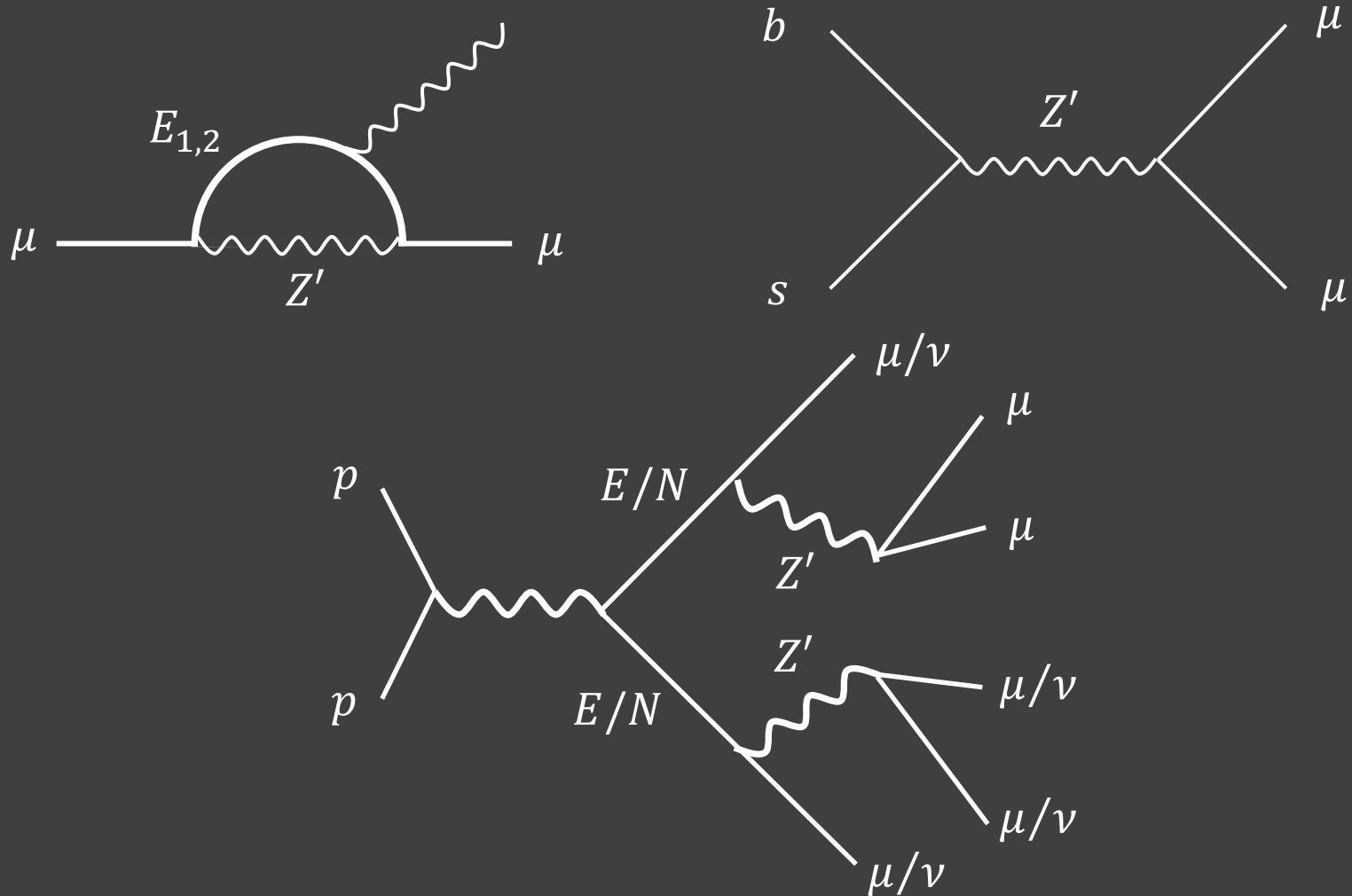
Summary

- Δa_μ and $b \rightarrow s\mu\mu$ anomalies are explained in the VL family + $U(1)'$ model
- $\geq 4\mu$ signals are expected in models with muon-philic VL leptons and Z'
- new CDF value of W mass can be explained by 200 GeV VL leptons
- LHC limits may be evaded if VL lepton decays to VL neutrino + X

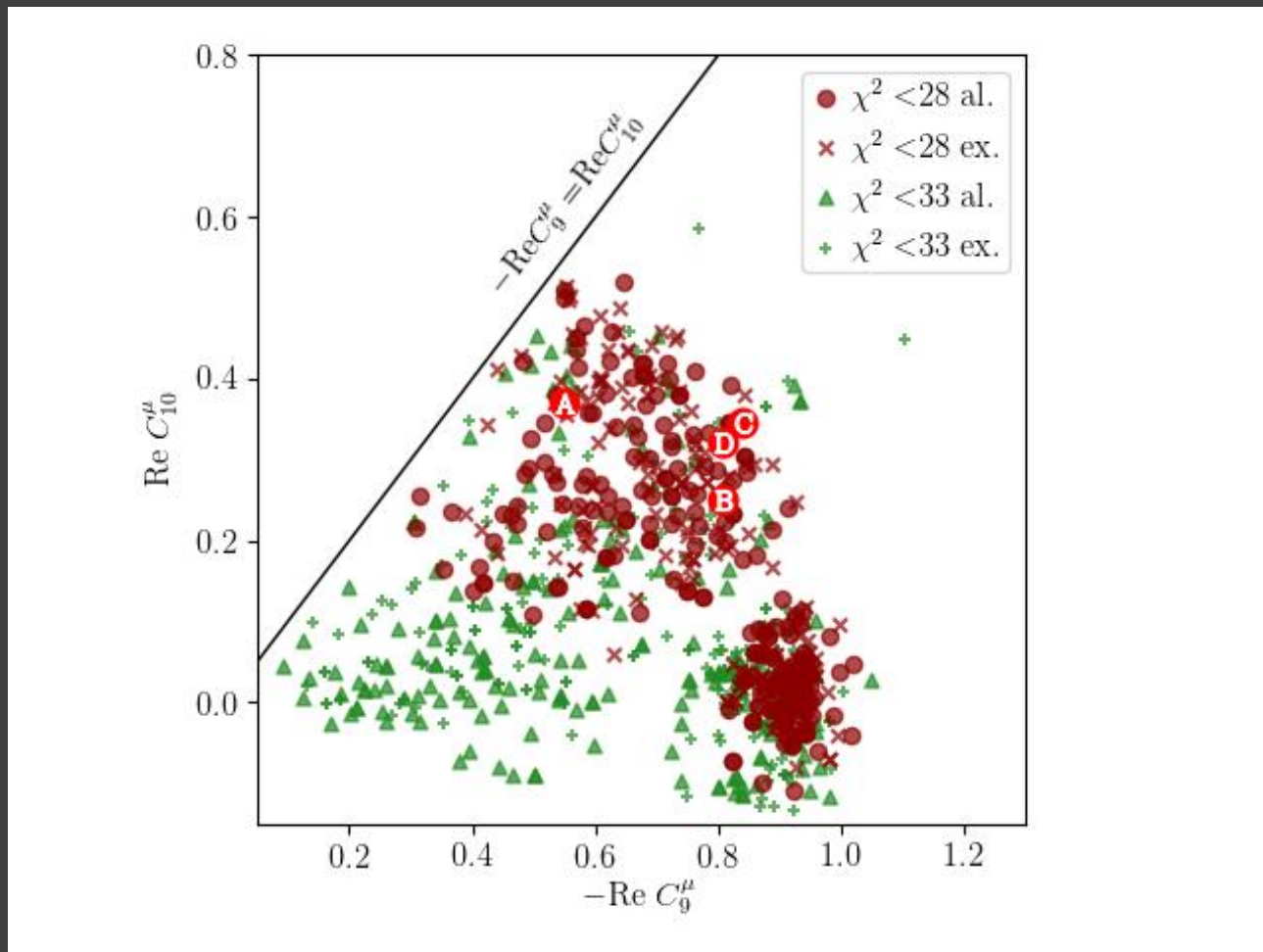
Thank you !

Backup

Complete vectorlike fourth family and new $U(1)'$ for muon anomalies

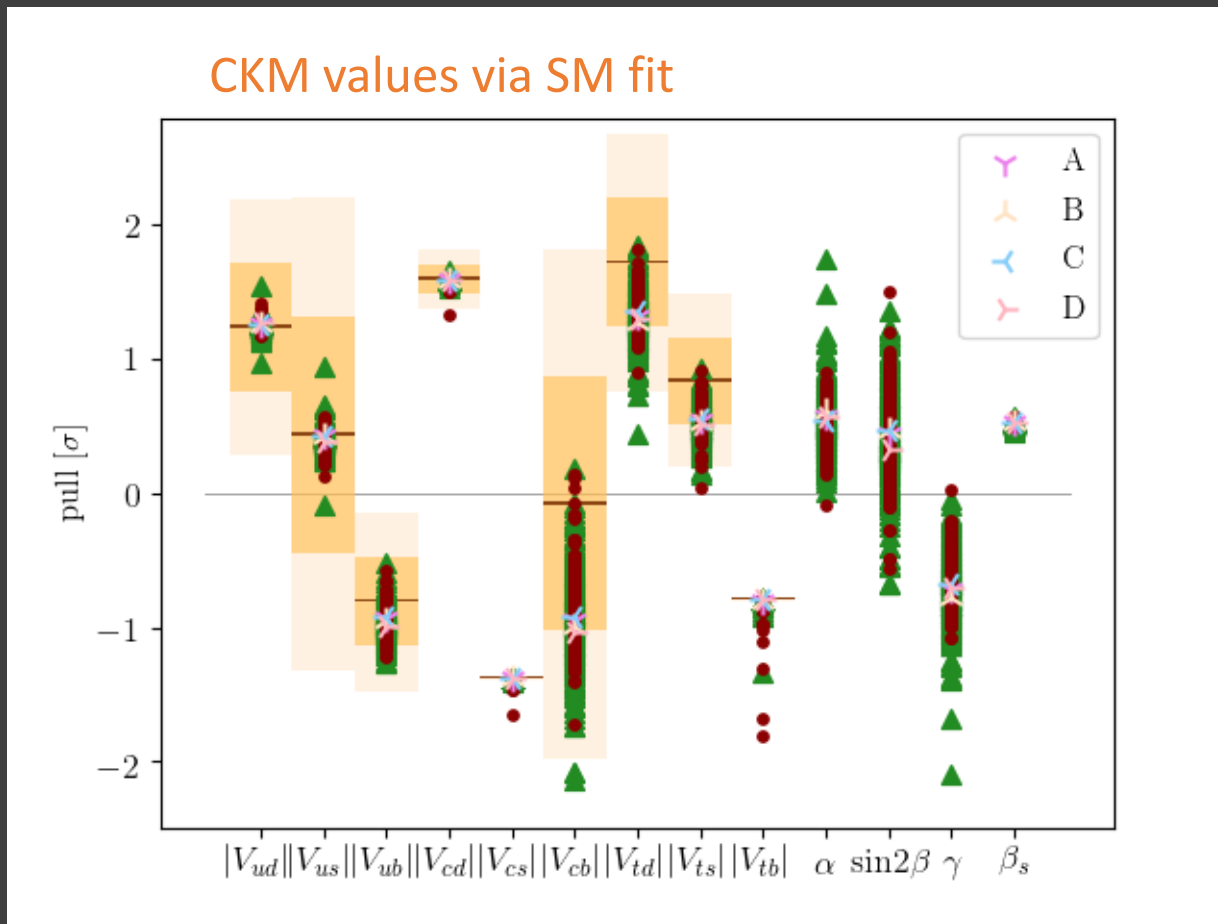


Patterns of C_9, C_{10}



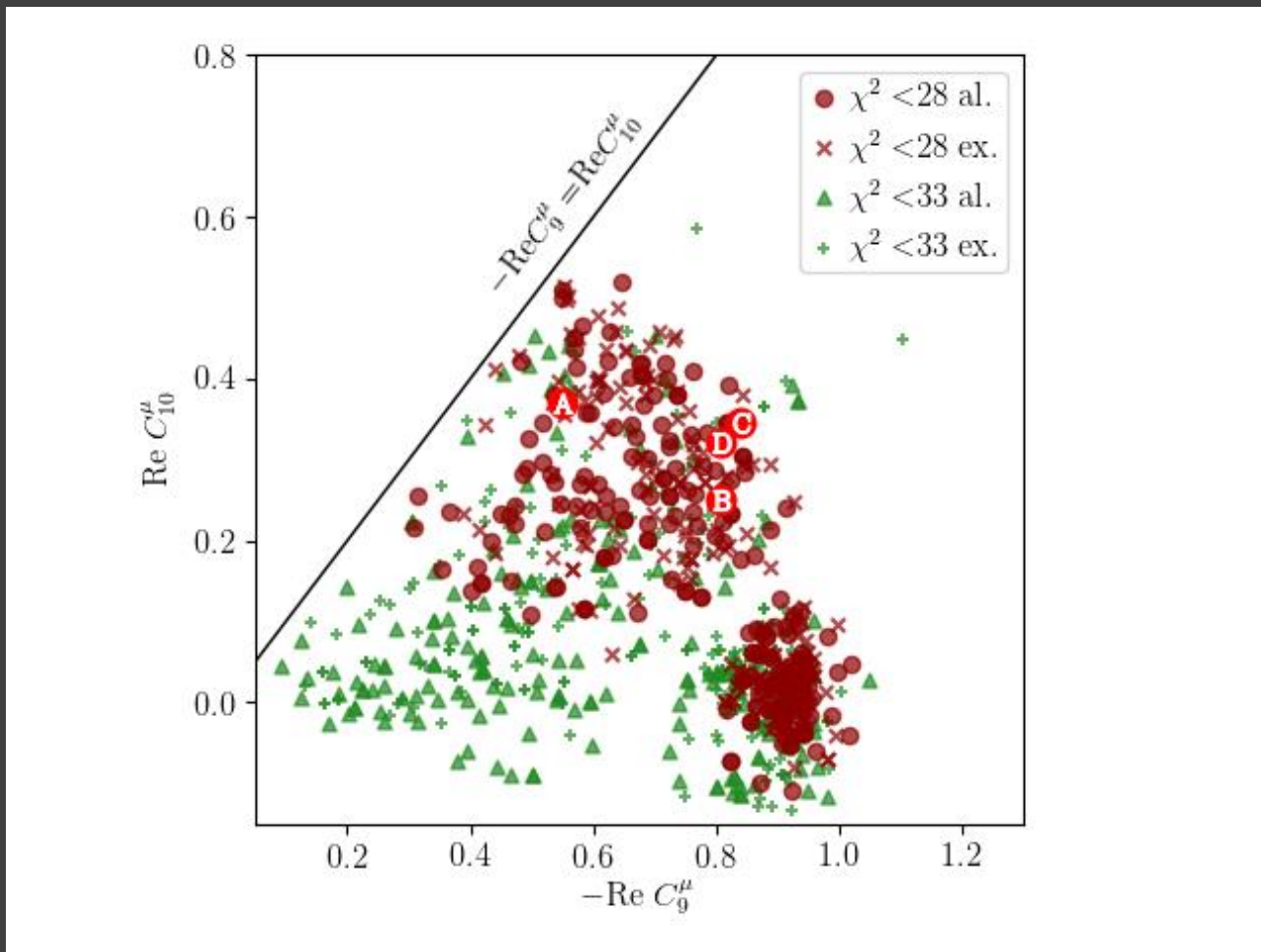
This model predicts $-C_9 > C_{10}$ to explain Δa_μ

CKM elements



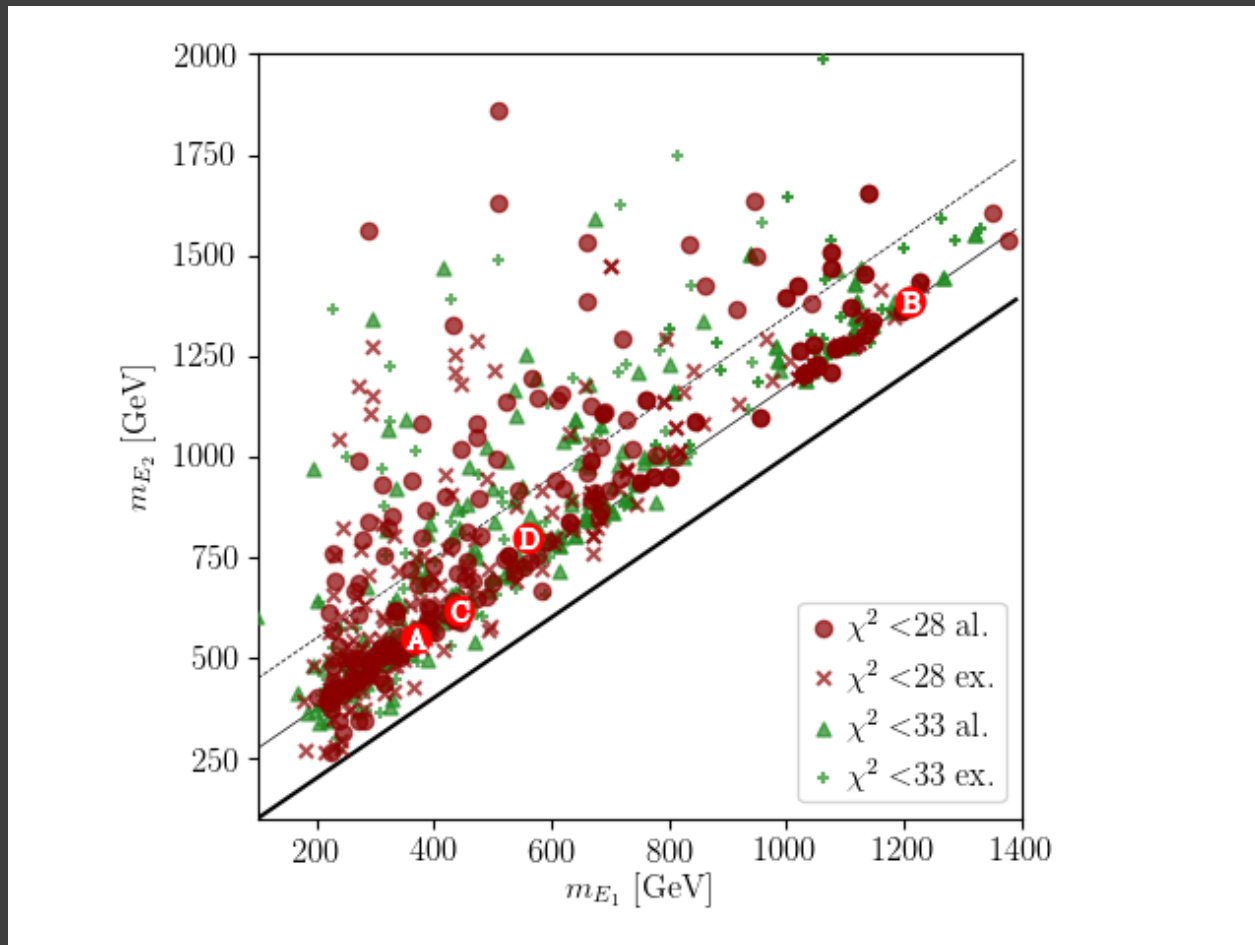
CKM values are consistent with SM fit

Patterns of C_9, C_{10}



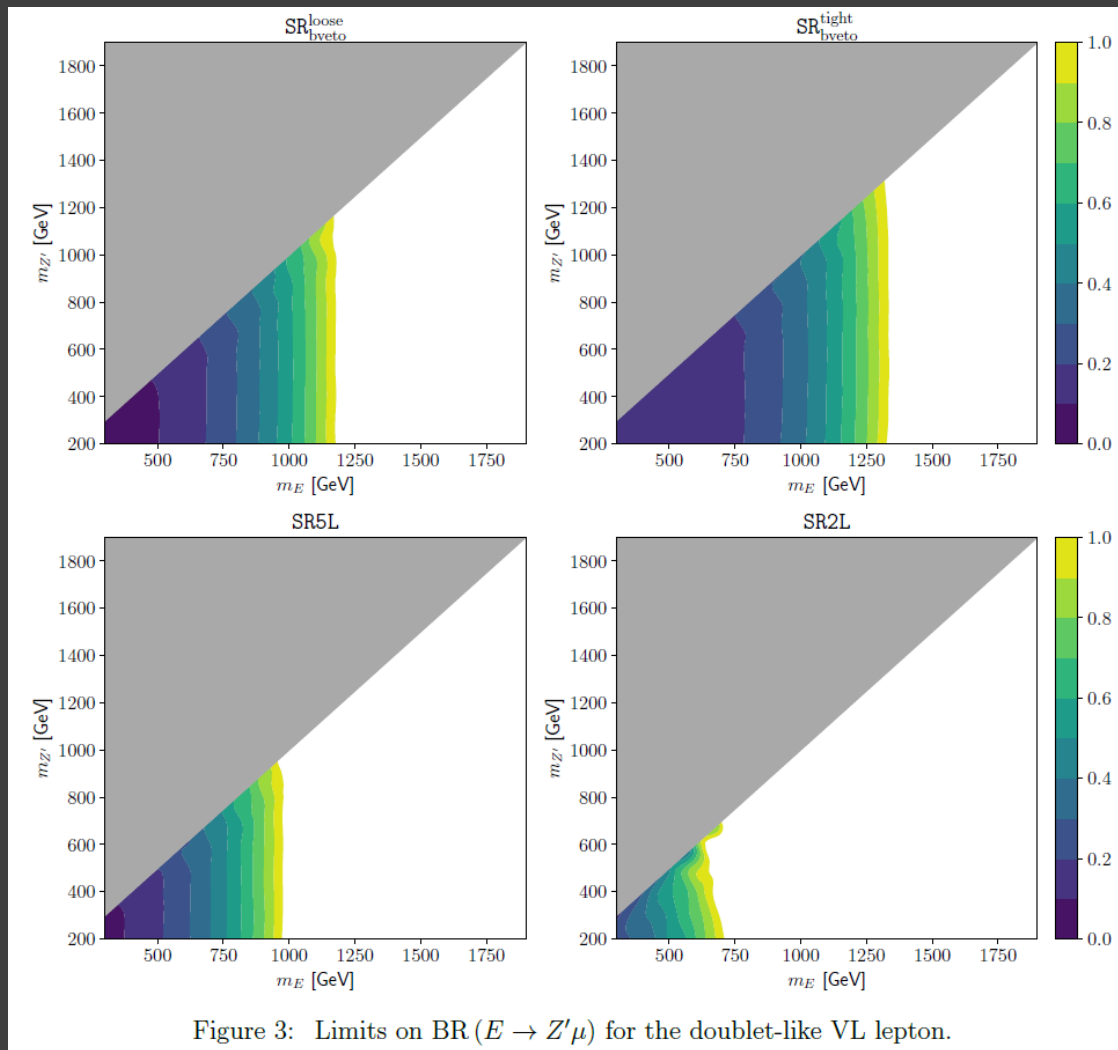
This model predicts $-\text{Re } C_9 > \text{Re } C_{10}$ to explain Δa_μ

Heavier VL-lepton



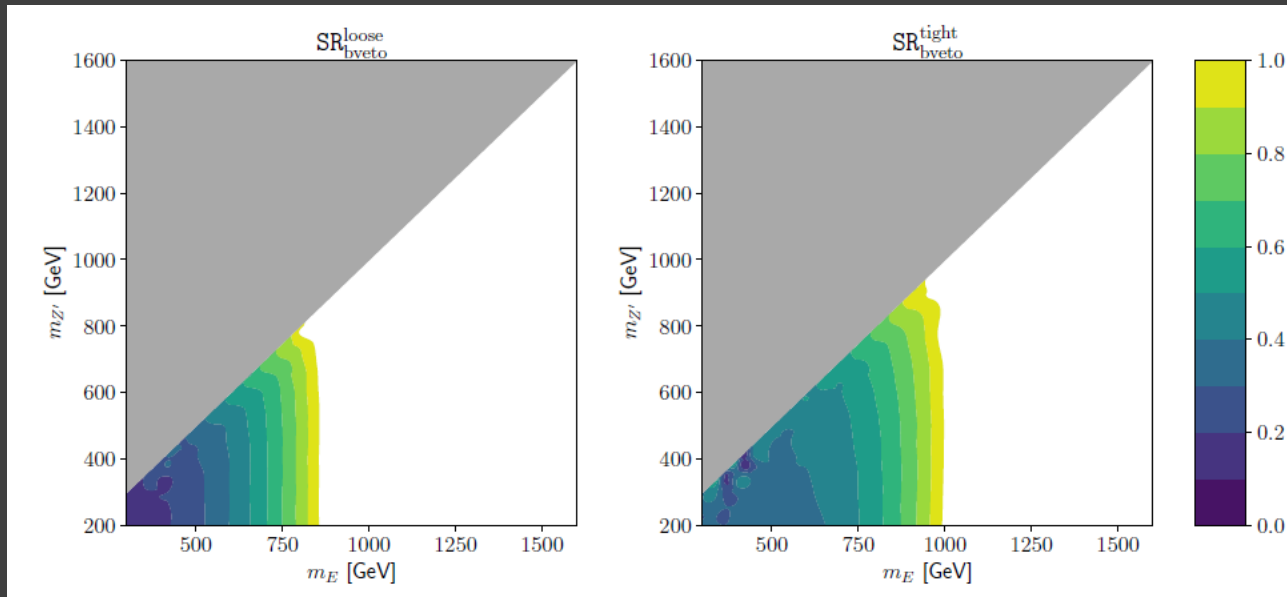
$m_{E_2} \lesssim 1.7 \text{ TeV}$ for $\Delta a_\mu \sim 2.68 \times 10^{-9}$ since LR-effect is crucial

Current limits on doublet-like VL lepton



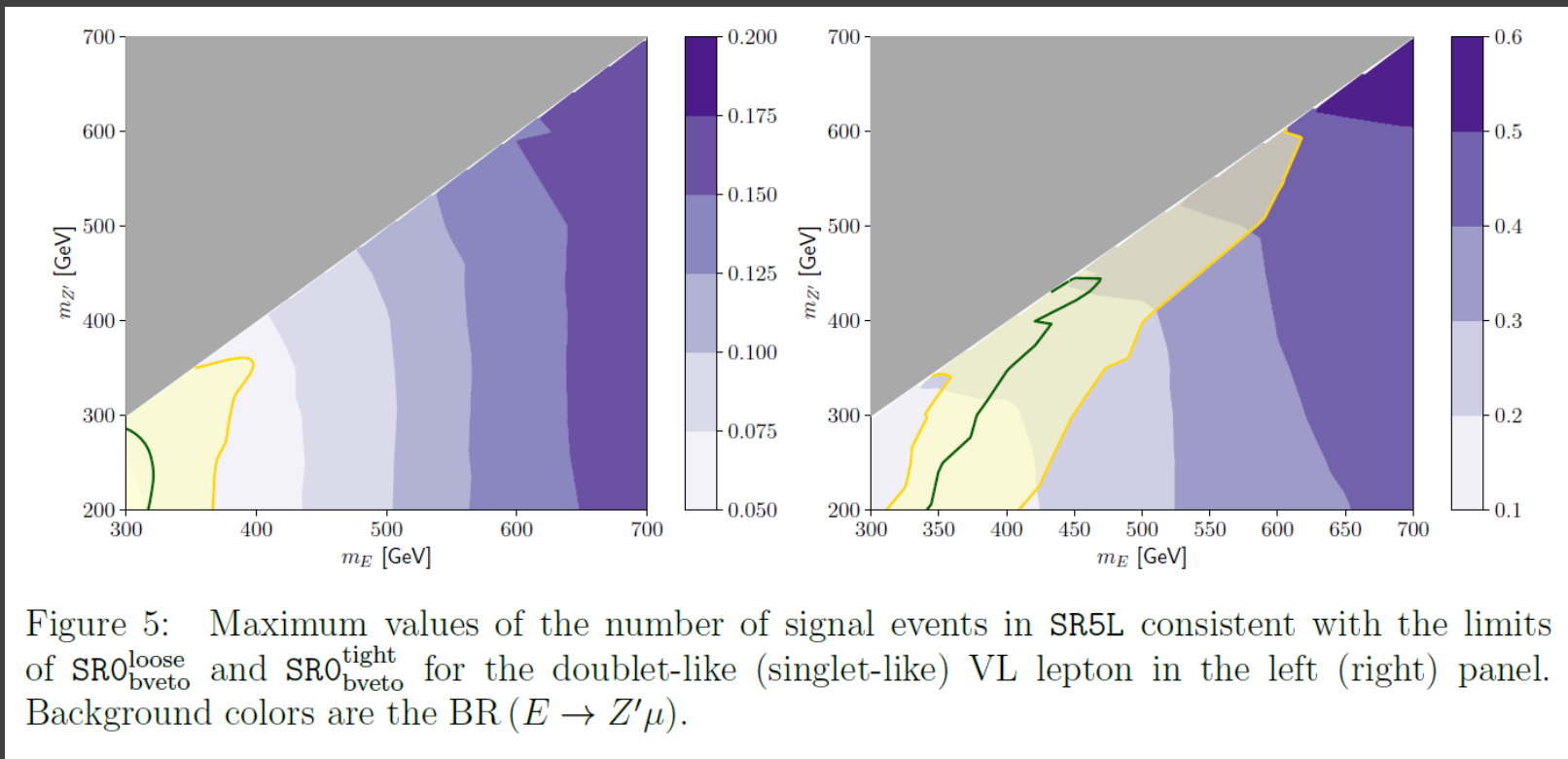
Upper limits on $\text{Br}(E \rightarrow Z' \mu)$

Current limits on singlet-like VL lepton



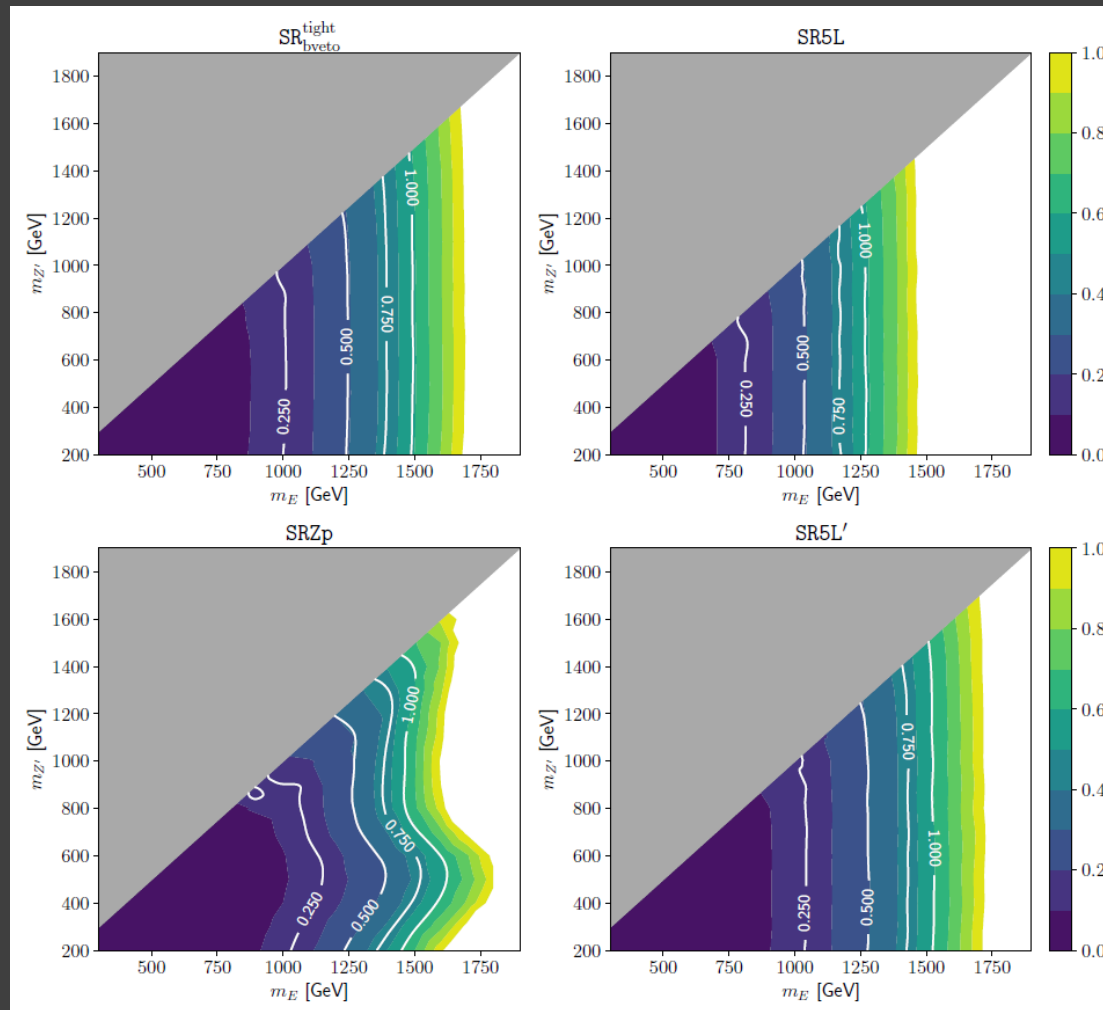
Upper limits on $\text{Br}(E \rightarrow Z' \mu)$

Maximum number of signals in SR5L



The excess is explained in yellow region

Future limits for doublet-like VL leptons

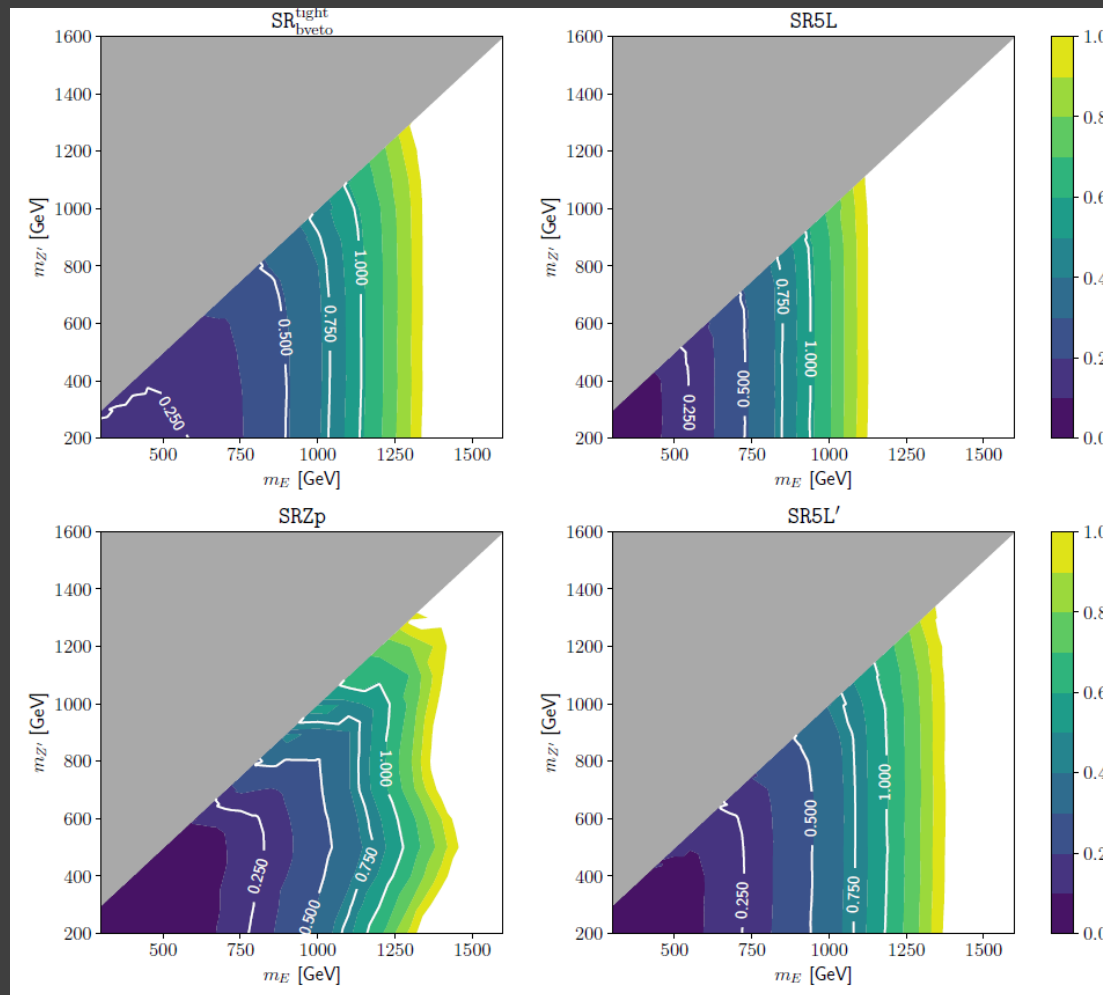


Future limits on $\text{Br}(E \rightarrow Z' \mu)$

SRZp : SR_{bveto}^{tight} + $|m_{OS} - 500| < 100$ (250) GeV

SR5L' : SR5L+Z-veto + $m_{\text{eff}} > 1000$ GeV

Future limits for singlet-like VL leptons

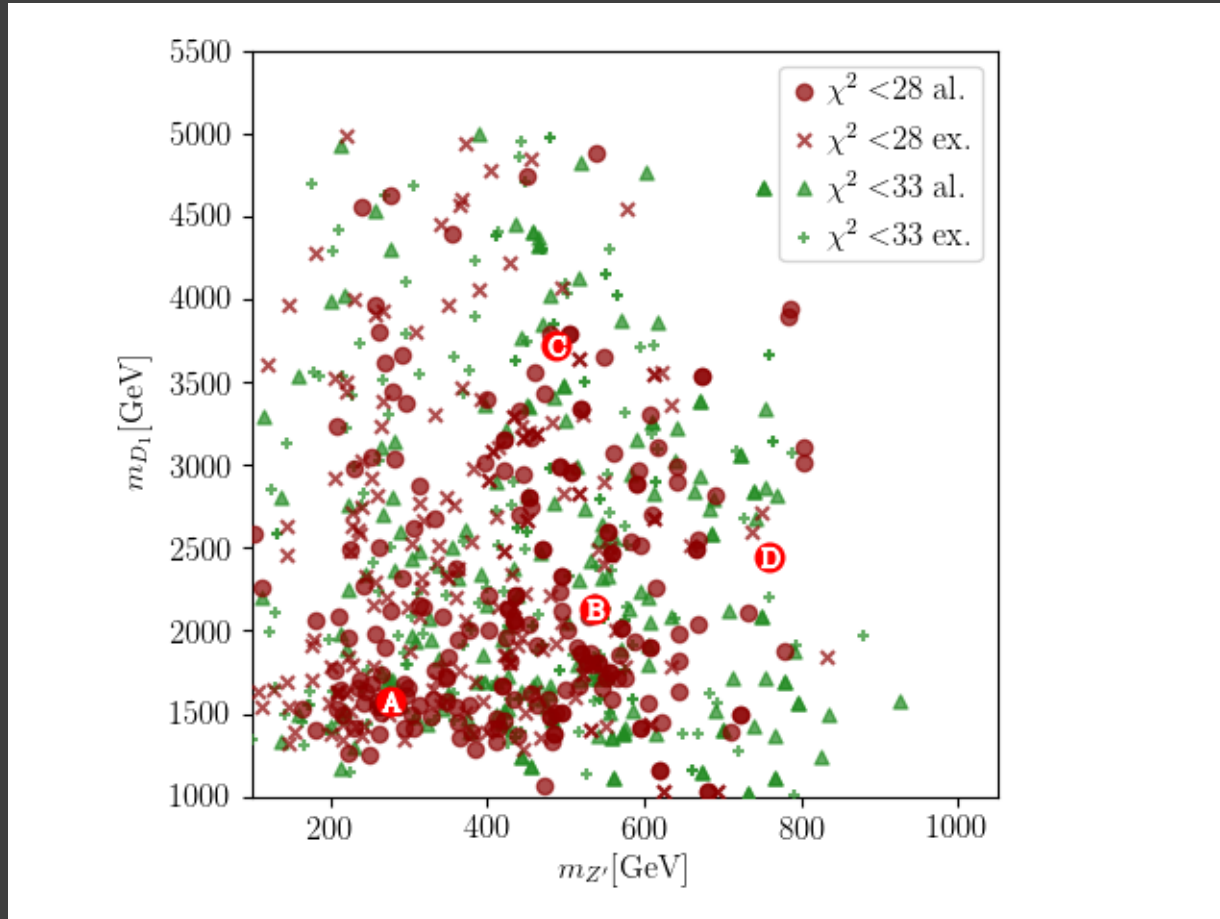


Future limits on $\text{Br}(E \rightarrow Z' \mu)$

SR_{Zp} : $\text{SR}_{\text{bveto}}^{\text{tight}} + |m_{\text{OS}} - 500| < 100$ (250) GeV

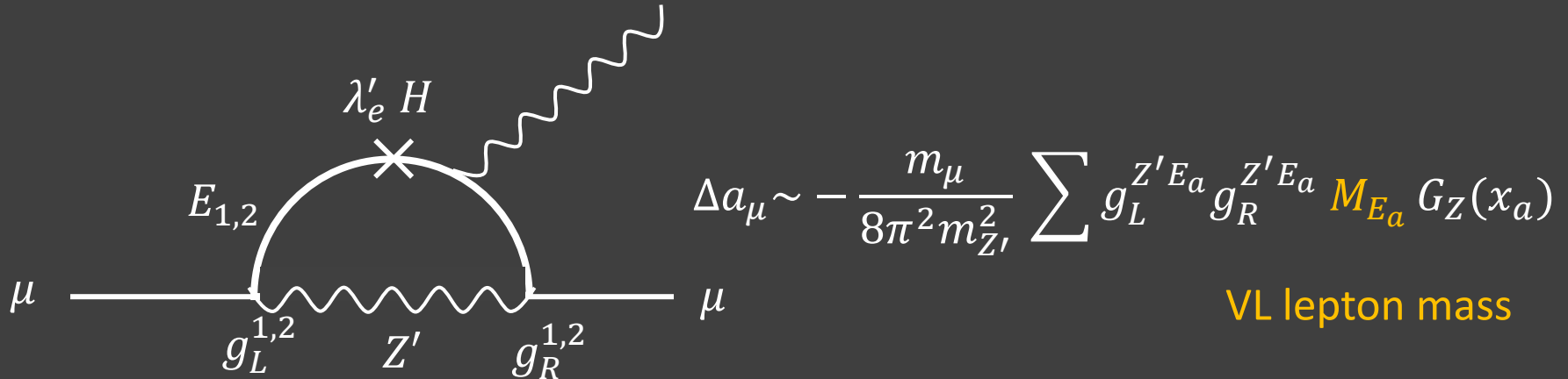
SR_{5L}' : $\text{SR}_{5L} + \text{Z-veto} + m_{\text{eff}} > 1000$ GeV

Masses of VL quarks



There is no stringent upper bound on VL quark

Muon $g - 2$



➤ Δa_μ is proportional to Higgs coupling: $\lambda'_e \bar{L}_R \tilde{H} E_L$

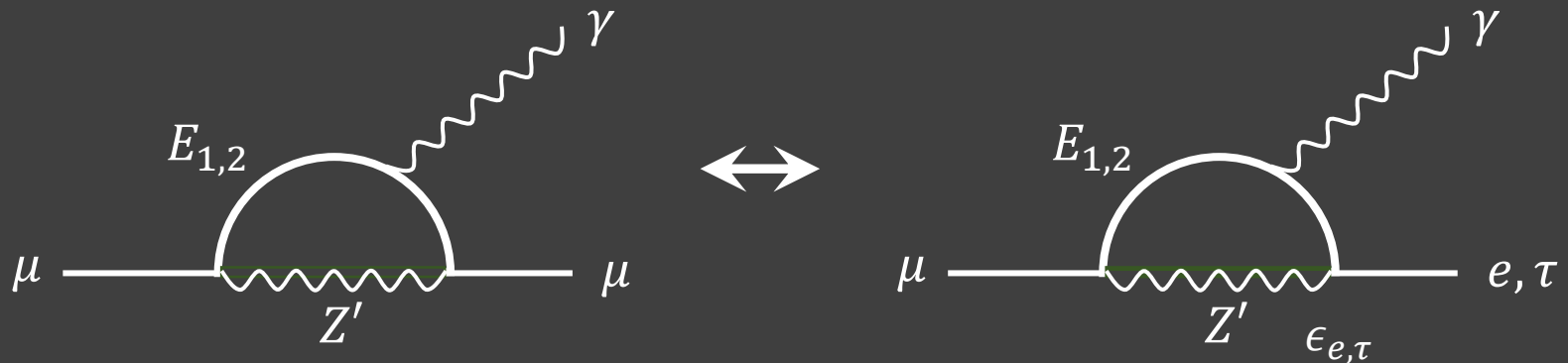
$$\Delta a_\mu \lesssim 2.9 \times 10^{-9} \times \left(\frac{c_{LE}}{0.1} \right) \left(\frac{\lambda'_e H}{174 \text{ GeV}} \right) \left(\frac{1 \text{ TeV}}{\Phi} \right)^2 \quad c_{LE} = M_L M_E \frac{G_Z(x_L) - G_Z(x_E)}{M_L^2 - M_E^2}$$

$\lambda'_e H / \Phi \gtrsim 0.1$ are needed

Lepton Flavor Violation (I)

➤ $\mu \rightarrow e\gamma, \tau \rightarrow \mu\gamma$

$\epsilon_{e_{L,R}}, \epsilon_{\tau_{L,R}}$: mixing bet. VL-lepton and e, τ



similar diagrams as Δa_μ induce $\mu \rightarrow e\gamma, \tau \rightarrow \mu\gamma$

Exp. limits

$$\text{Br}(\mu \rightarrow e\gamma) \sim 2.3 \times 10^{-14} \times \left(\frac{\lambda'_e}{1.0}\right)^2 \left(\frac{\epsilon_e}{10^{-6}}\right)^2 \left(\frac{1.0 \text{ TeV}}{\Phi}\right)^4 < 4.2 \times 10^{-13} \text{ (90\%C.L.)}$$

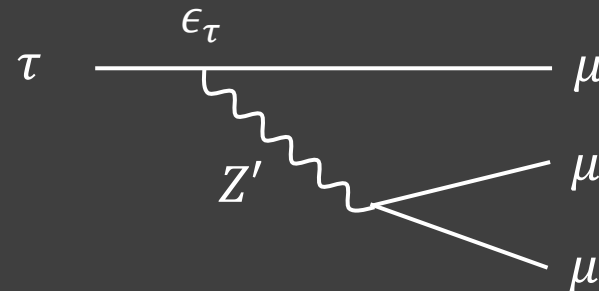
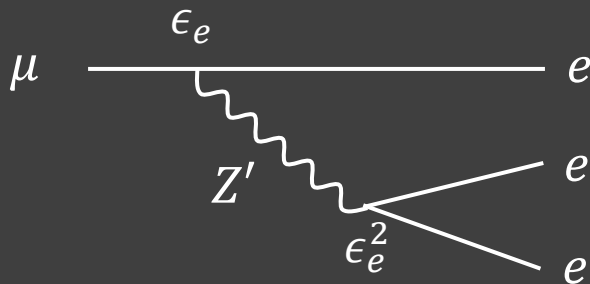
$$\text{Br}(\tau \rightarrow \mu\gamma) \sim 1.5 \times 10^{-9} \times \left(\frac{\lambda'_e}{1.0}\right)^2 \left(\frac{\epsilon_\tau}{10^{-2}}\right)^2 \left(\frac{1.0 \text{ TeV}}{\Phi}\right)^4 < 4.4 \times 10^{-8} \text{ (90\%C.L.)}$$

Lepton Flavor Violation (II)

- Z' coupling to SM families $\epsilon_{e_{L,R}}, \epsilon_{\tau_{L,R}}$: mixing bet. VL-lepton and e, τ

$$\sim g' Z'_\mu (\bar{e}_L \quad \bar{\mu}_L \quad \bar{\tau}_L) \gamma^\mu \begin{pmatrix} \epsilon_{e_L}^2 & \epsilon_{e_L} S_{\theta_{\mu L}} & \epsilon_{e_L} \epsilon_{\tau_L} \\ \epsilon_{e_L} S_{\theta_{\mu L}} & S_{\theta_{\mu L}}^2 & \epsilon_{\tau_L} S_{\theta_{\mu L}} \\ \epsilon_{e_L} \epsilon_{\tau_L} & \epsilon_{\tau_L} S_{\theta_{\mu L}} & \epsilon_{\tau_L}^2 \end{pmatrix} \begin{pmatrix} e_L \\ \mu_L \\ \tau_L \end{pmatrix}$$

- $\mu \rightarrow eee, \tau \rightarrow \mu\mu\mu$ e.t.c.



$$\text{Br}(\mu \rightarrow eee) \sim 2.3 \times 10^{-40} \times \left(\frac{\epsilon_e}{10^{-6}}\right)^6 \left(\frac{1.0 \text{ TeV}}{\Phi}\right)^4 < 1.0 \times 10^{-12} \text{ (90\%C.L.)}$$

$$\text{Br}(\tau \rightarrow \mu\mu\mu) \sim 1.0 \times 10^{-9} \times \left(\frac{\epsilon_\tau}{10^{-2}}\right)^2 \left(\frac{1.0 \text{ TeV}}{\Phi}\right)^4 < 2.1 \times 10^{-8} \text{ (90\%C.L.)}$$

Neutrino Mass

➤ Majorana mass for $\nu_{R_{1,2,3}}$, $M_R \sim 10^{14}$ GeV

$$M_{Dirac} = \begin{pmatrix} Y_\nu^{ij} H & 0_i & \lambda_i^N \Phi \\ 0_j & \lambda_\nu H & \lambda_V^N \phi \\ \lambda_j^L \Phi & \lambda_V^L \phi & \lambda'_\nu H \end{pmatrix} \xrightarrow{V_L} \tilde{M}_{Dirac} = \begin{pmatrix} \tilde{Y}_\nu^{ij} H & \tilde{\lambda}^N_i H & \lambda_i^N \Phi \\ 0_j & 0 & \lambda_V^N \phi \\ 0 & \tilde{M}_L & \tilde{m}_5 \end{pmatrix}$$

ν_R N_R N'_R $\tilde{\nu}_L$ \tilde{N}'_L \tilde{N}_L

Majorana mass

$$M_{10 \times 10} = \begin{pmatrix} M_R & 0 & 0 & \tilde{Y}_\nu^{ij} H & \tilde{\lambda}^N_i H & \lambda_i^N \Phi \\ 0 & 0 & 0 & 0_j & 0 & \lambda_V^N \phi \\ 0 & 0 & 0 & 0 & \tilde{M}_L & \tilde{m}_5 \\ \tilde{Y}_\nu^{ij} H & 0_i & 0 & 0_{3 \times 3} & 0 & 0 \\ \tilde{\lambda}^N_i H & 0 & \tilde{M}_L & 0 & 0 & 0 \\ \lambda_i^{NT} \Phi & \lambda_V^N \phi & \tilde{m}_5 & 0 & 0 & 0 \end{pmatrix}$$

decoupled by M_R

Dirac neutrino \sim TeV

SM neutrino $\sim H^2/M_R$

SM and VL neutrinos are secluded by Majorana mass

Benchmark point A

$$m_{Z'} = 277.608, \quad v_\phi = 4079.3, \quad g' = 0.250042, \quad \lambda_\chi = 0.689454, \quad \lambda_\sigma = 0.210518$$

$M_e =$

$$\begin{pmatrix} 0.000486575 & 0.000000322078 & -0.0000009971 & 0 & 0.000201232 \\ 0.0000000453521 & 0.159775 & 0.00162206 & 0 & -153.074 \\ -0.0000614248 & -0.00512644 & -1.74616 & 0 & -0.0409467 \\ 0 & 0 & 0 & 0.0000361209 & 448.074 \\ -0.00000237863 & -312.626 & 0.0547758 & 289.432 & -174.104 \end{pmatrix},$$

$M_n =$

$$\begin{pmatrix} 0. & 0. & 0. & 0 & 0 \\ -15.7947 & 28.3788 \cdot e^{-0.0735218i} & 15.4093 \cdot e^{0.107535i} & 0 & 0 \\ 10.4292 \cdot e^{1.19397i} & 67.3777 \cdot e^{0.0000000228655i} & -53.4556 & 0 & 0 \\ 0 & 0 & 0 & 1.54426 & -454.964 \\ -0.00000237863 & -312.626 & 0.0547758 & 289.357 & -21.7762 \end{pmatrix}$$

$M_u =$

$$\begin{pmatrix} 0.000893504 & 0.00562655 & 0.688382 \cdot e^{1.52313i} & 0 & -0.0228009 \\ -0.000172924 & 0.631189 & -0.119538 & 0 & -40.8575 \\ 0.535431 \cdot e^{1.72288i} & 4.4472 & -171.657 & 0 & -8.7671 \\ 0 & 0 & 0 & -0.000301965 & -3596.52 \\ 0.0051151 & 214.302 & -96.8583 & 3445.76 & 5.50646 \end{pmatrix},$$

$M_d =$

$$\begin{pmatrix} 0.0121338 & 0.0527148 & 0.0199472 \cdot e^{-3.08081i} & 0 & -0.0254167 \\ -0.00528222 & -0.0409769 & -2.58755 & 0 & -41.2307 \\ 0.00189847 \cdot e^{-1.62491i} & -0.0198056 & -1.21195 & 0 & 6.1041 \\ 0 & 0 & 0 & -0.122713 & -1571.54 \\ 0.0051151 & 214.302 & -96.8583 & 3445.76 & -1.99223 \end{pmatrix}.$$

inputs

mass and widths

	Mass [GeV]	Width [GeV]	Decay 1	BR	Decay 2	BR
Z'	277.6	0.1361	$\mu\mu$	0.5091	$\nu\nu$	0.4907
χ	651.9	0.669538	$E_1\mu$	0.4391	$N_1\nu$	0.4227
σ	1871.7	0.9049	N_2N_2	0.2988	E_2E_2	0.1473
E_1	367.9	0.0354639	$Z'\mu$	1.	$h\mu$	0.
N_1	422.2	0.0817534	$Z'\nu$	0.9995	$W\mu$	0.0003
N_2	459.	0.113389	WE_1	0.8792	$Z'\nu$	0.1179
E_2	548.3	4.07452	WN_1	0.4799	ZE_1	0.4415
D_1	1572.1	0.0371	$Z'b$	0.4117	χb	0.2831
U_1	3453.7	3.0221	$Z'c$	0.4117	χc	0.3829
D_2	3453.8	3.0228	$Z's$	0.4063	χs	0.3779
U_2	3596.8	0.1085	$Z'c$	0.4504	χc	0.4213

Angular observables

from talk slides at 10th LHCb IW by D.Gerick

angular differential decay rate:

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \left. \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\Omega} \right|_P =$$

$$\frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right.$$

$$+ \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell$$

$$- F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi$$

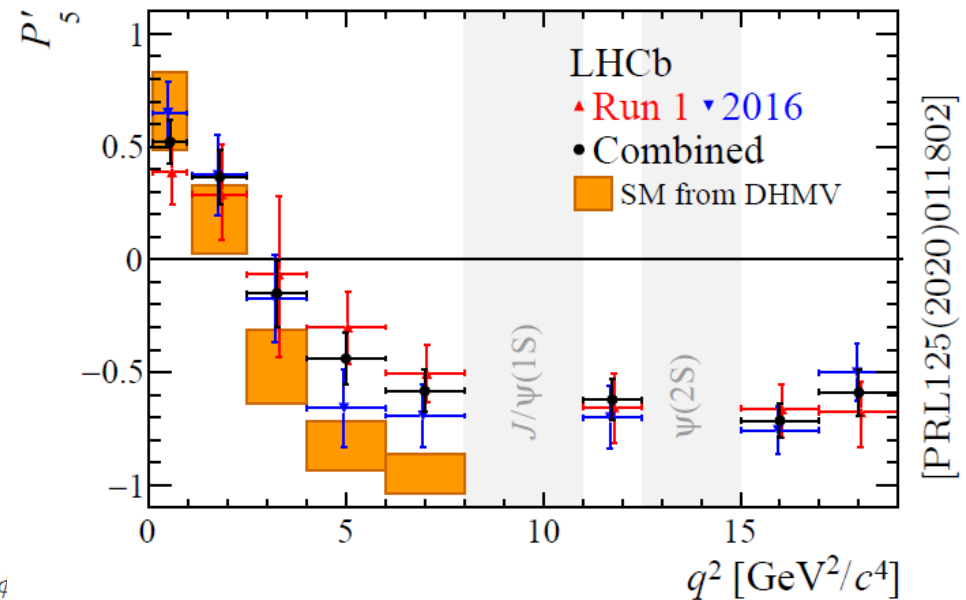
$$+ S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi$$

$$+ S_{6s} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi$$

$$\left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

plus S-wave contribution and P-/S-wave-interference terms.

- $A_{FB} = \frac{3}{4} S_{6s}$
- $P_1 = \frac{2S_3}{1-F_L}$, $P_2 = \frac{S_{6s}}{2(1-F_L)}$ and $P_3 = \frac{-S_9}{1-F_L}$
- $P'_{4,5,6,8} = \frac{S_{4,5,7,8}}{\sqrt{F_L(1-F_L)}}$

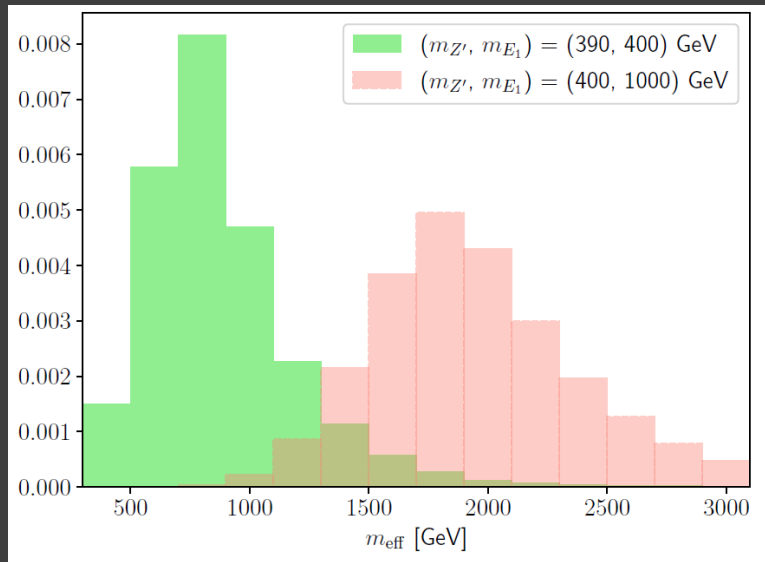


3.3 σ discrepancy

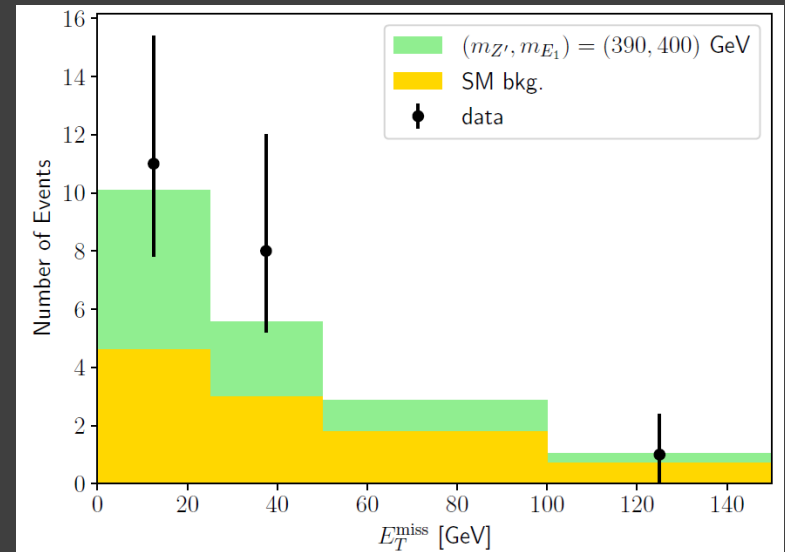
Explanation of excess in $\geq 5\ell$ signal

explain the excess in SR5L and null excess in $SR0_{bveto}^{tight}$, $SR0_{bveto}^{loose}$

➤ m_{eff} distribution



➤ E_T^{miss} distribution $Br(Z' \rightarrow E\mu) = 0.25$



Madgraph5+pythia8+Delphes3

- limits from $SR0_{bveto}^{tight(loose)}$ are weaker for light spectra
- excess explained by singlet VL lepton if $(m_{Z'}, m_E) = (390, 400)$ GeV
- Our model only has muons, but the experiment also counts electrons