

LHC EW WG General Meeting - CERN

15-17 November 2022

# WZ at NNLO QCD and NLO EW matched to parton showers

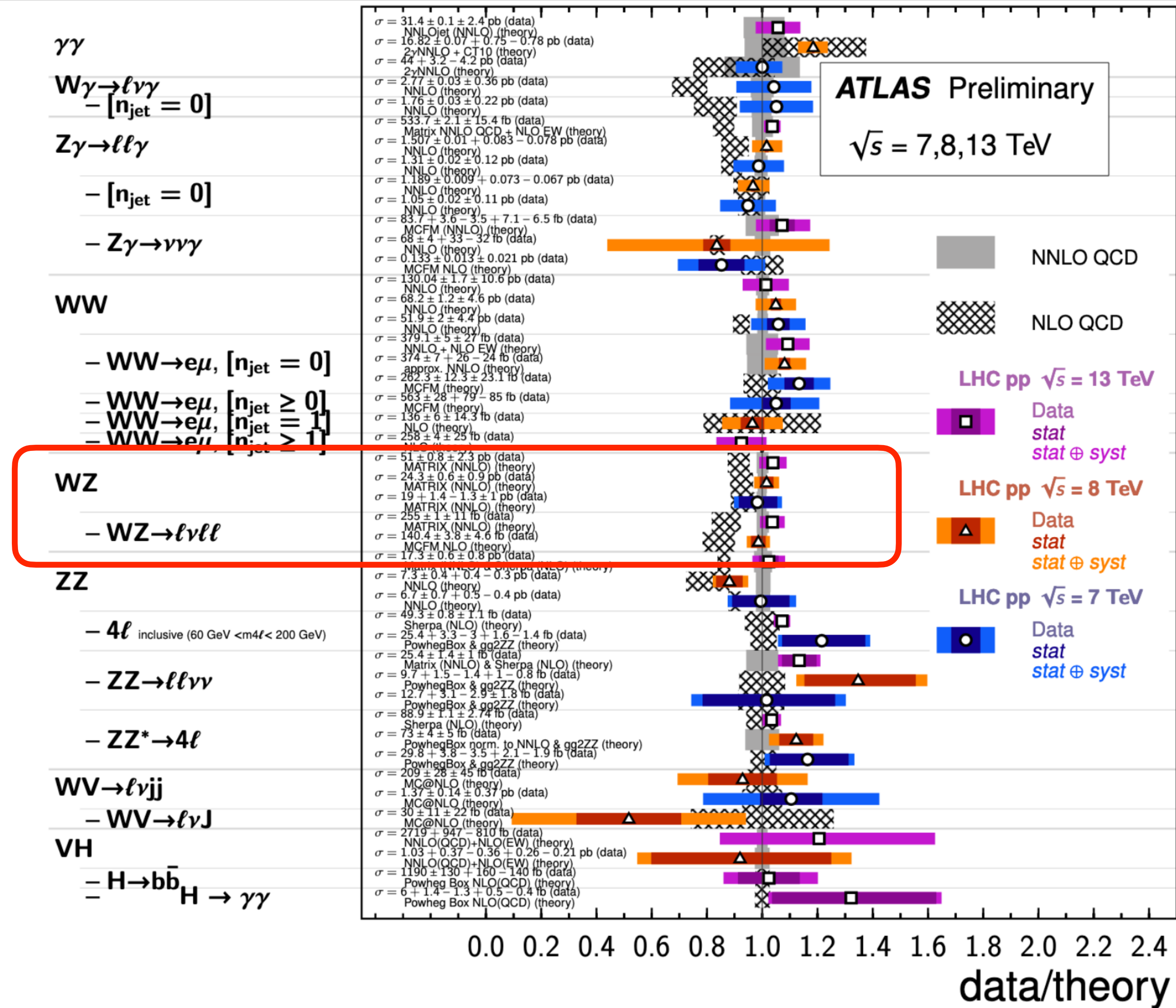
Based on [2208.12660] J. Lindert, D. Lombardi, M. Wiesemann, G. Zanderighi, S.Z.

MAX PLANCK INSTITUTE  
FOR PHYSICS



Silvia Zanolì  
Max Planck Institute for Physics

# WZ production



## CURRENT STATE OF THE ART:

NLO EW calculation

[Bierweiler, Kasprzik, Kühn (2013), Baglio, Ninh, Weber (2013)]  
[Biedermann, Denner, Hofer (2017)]

NNLO QCD calculation

[Grazzini, Kallweit, Rathlev, Wiesemann (2016), (2017)]

NLO QCD + NLO EW matched to Parton Showers

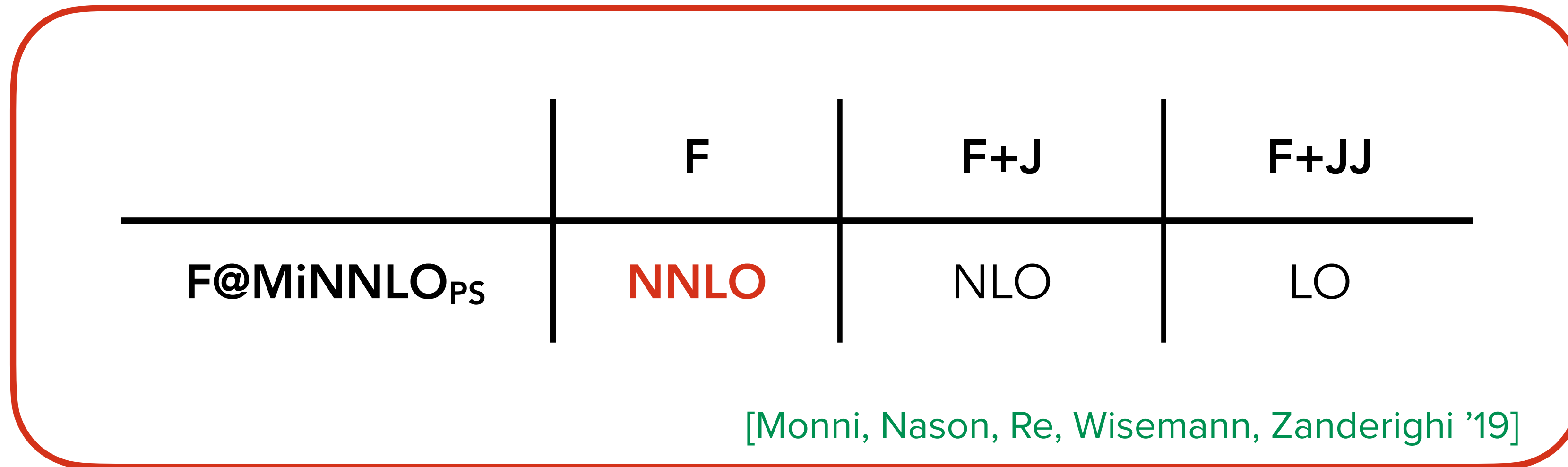
[Chiesa, Oleari, Re (2020)]

NNLO QCD + NLO EW combination

[Grazzini, Kallweit, Lindert, Pozzorini, Wiesemann (2020)]

## THIS TALK:

- NNLO+PS (QCD) calculation using MiNNLO<sub>PS</sub>
- Combination of NNLO+PS (QCD) with NLO+PS (EW) computations



- No computationally intense reweighting
- No unphysical merging scale
- LL accuracy of the shower preserved
- Numerically efficient

MiNNLO<sub>PS</sub> starting point : analytic all order formula

$$\frac{d\sigma}{d\Phi_F dp_T} = \frac{d}{dp_T} \left\{ e^{-\tilde{S}(p_T)} \mathcal{L}(p_T) \right\} + R_f(p_T) = e^{-\tilde{S}(p_T)} \left[ D(p_T) + \frac{R_f(p_T)}{e^{-\tilde{S}(p_T)}} \right] = \dots =$$

$$D(p_T) \equiv -\frac{d\tilde{S}(p_T)}{dp_T} \mathcal{L}(p_T) + \frac{d\mathcal{L}(p_T)}{dp_T}$$

## MiNNLO<sub>PS</sub> starting point : analytic all order formula

$$\begin{aligned}
 \frac{d\sigma}{d\Phi_F dp_T} &= \frac{d}{dp_T} \left\{ e^{-\tilde{S}(p_T)} \mathcal{L}(p_T) \right\} + R_f(p_T) = e^{-\tilde{S}(p_T)} \left[ D(p_T) + \frac{R_f(p_T)}{e^{-\tilde{S}(p_T)}} \right] = \dots = \\
 &= e^{-\tilde{S}(p_T)} \left\{ \frac{\alpha_s(p_T)}{2\pi} \left[ \frac{d\sigma_{FJ}}{d\Phi_{FJ} dp_T} \right]^{(1)} \left( 1 + \frac{\alpha_s(p_T)}{2\pi} [\tilde{S}]^{(1)} \right) + \left( \frac{\alpha_s(p_T)}{2\pi} \right)^2 \left[ \frac{d\sigma_{FJ}}{d\Phi_{FJ} dp_T} \right]^{(2)} + \left( D(p_T) - D^{(1)}(p_T) - D^{(2)}(p_T) \right) + reg \right\}
 \end{aligned}$$

$D(p_T) \equiv -\frac{d\tilde{S}(p_T)}{dp_T} \mathcal{L}(p_T) + \frac{d\mathcal{L}(p_T)}{dp_T}$

$\int \frac{dp_T}{p_T} \alpha_s^m(p_T) \ln^n \frac{p_T}{Q} e^{-\tilde{S}(p_T)} \approx \mathcal{O}(\alpha_s^{m-\frac{n+1}{2}})$

## MiNNLO<sub>PS</sub> starting point : analytic all order formula

$$\begin{aligned}
 \frac{d\sigma}{d\Phi_F dp_T} &= \frac{d}{dp_T} \left\{ e^{-\tilde{S}(p_T)} \mathcal{L}(p_T) \right\} + R_f(p_T) = e^{-\tilde{S}(p_T)} \left[ D(p_T) + \frac{R_f(p_T)}{e^{-\tilde{S}(p_T)}} \right] = \dots = \\
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 \end{aligned}$$

$D(p_T) \equiv -\frac{d\tilde{S}(p_T)}{dp_T} \mathcal{L}(p_T) + \frac{d\mathcal{L}(p_T)}{dp_T}$   
 $\int \frac{dp_T}{p_T} \alpha_s^m(p_T) \ln^n \frac{p_T}{Q} e^{-\tilde{S}(p_T)} \approx \mathcal{O}(\alpha_s^{m-\frac{n+1}{2}})$

## Calculation embedded in the POWHEG formalism:

$$d\sigma_F^{\text{MiNNLO}_{\text{PS}}} = d\Phi_{\text{FJ}} \bar{\text{B}}^{\text{MiNNLO}_{\text{PS}}} \times \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{\text{T,rad}}) \frac{\text{R}_{\text{FJ}}}{\text{B}_{\text{FJ}}} \right\}$$

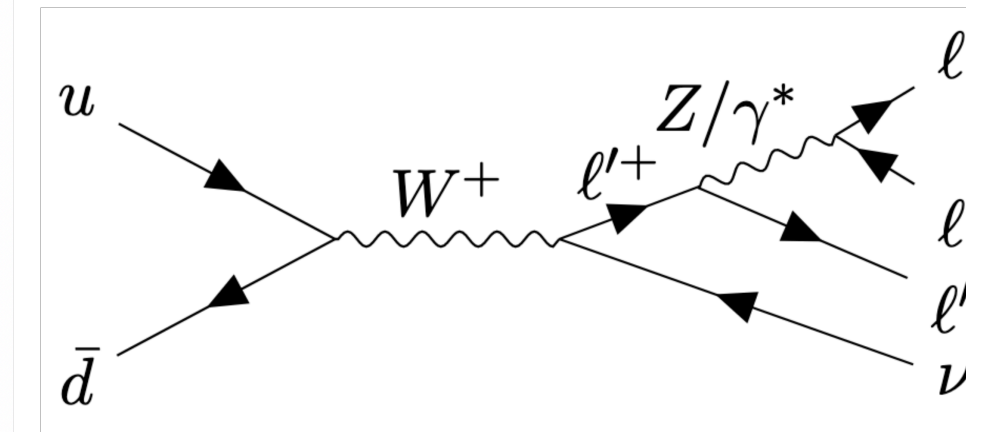
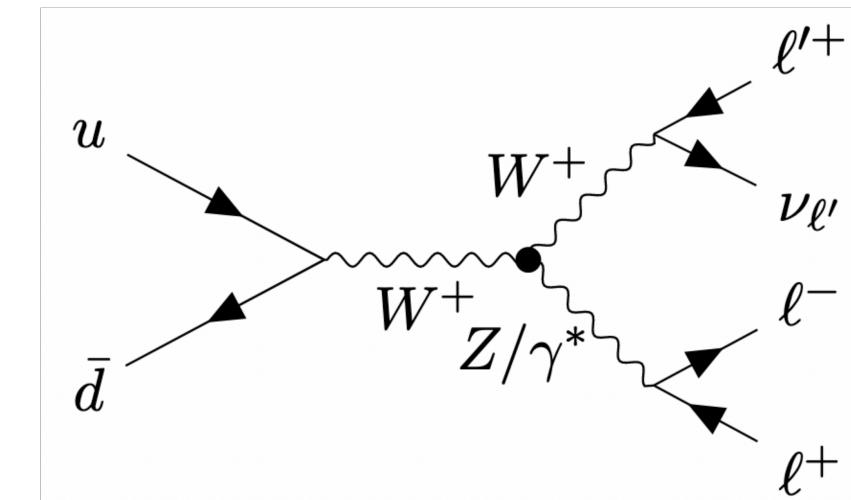
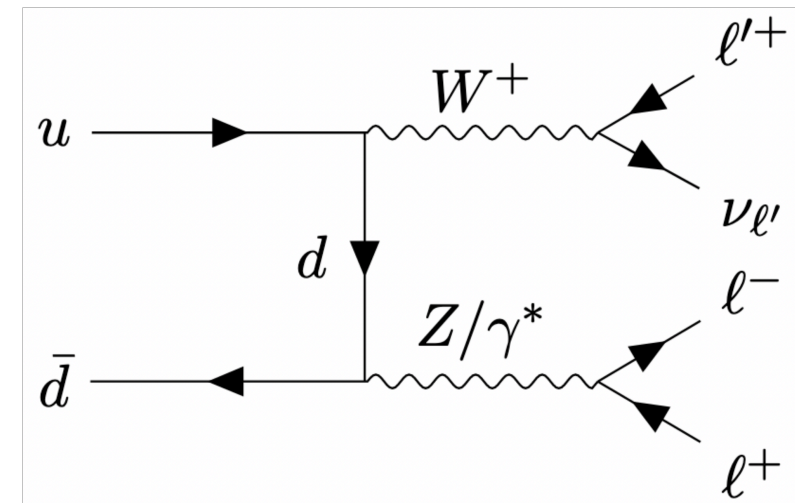
POWHEG Sudakov for the emission of the first (hardest) radiation

NNLO accurate in F

$$\bar{\text{B}}^{\text{MiNNLO}_{\text{PS}}} \sim e^{-S} \left\{ d\sigma_{\text{FJ}}^{(1)} (1 + S^{(1)}) + d\sigma_{\text{FJ}}^{(2)} + (D - D^{(1)} - D^{(2)}) \right\}$$

*Simplified notation!*

$$pp \rightarrow l'^{\pm} \nu_{l'} l^+ l^- + X$$



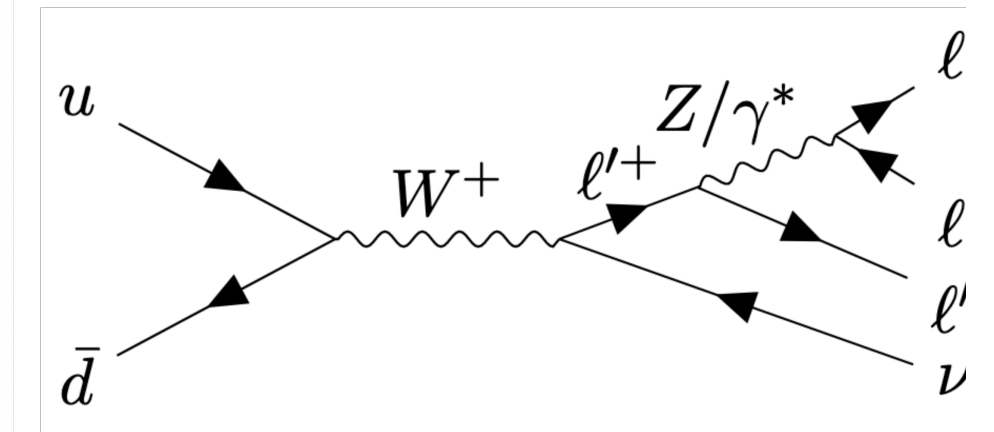
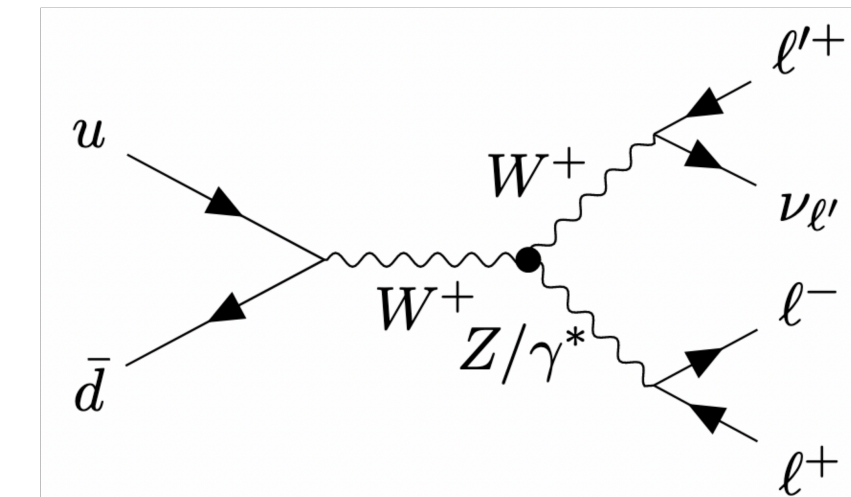
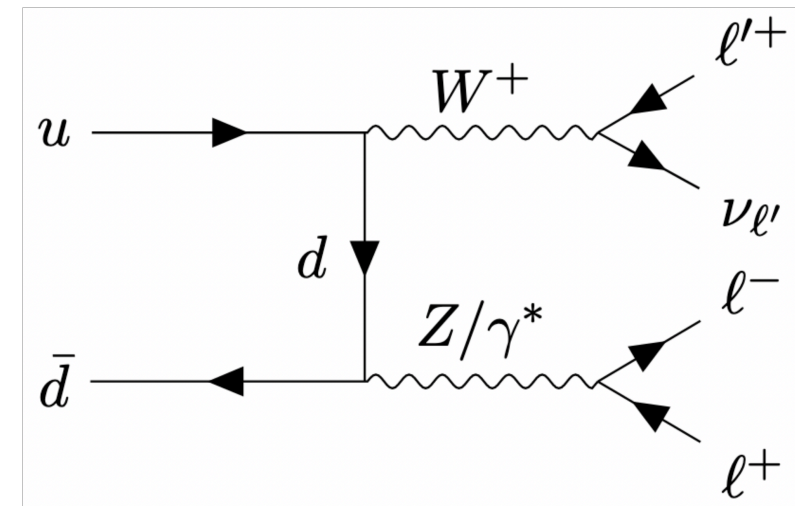
## 1) Generation of NNLO+PS (QCD) results using MiNNLO<sub>PS</sub>

$$d\sigma_{\text{F}}^{\text{MiNNLO}_{\text{PS}}} = d\Phi_{\text{FJ}} \bar{\text{B}}^{\text{MiNNLO}_{\text{PS}}} \times \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(\mathbf{p}_{\text{T,rad}}) \frac{\text{R}_{\text{FJ}}}{\text{B}_{\text{FJ}}} \right\}$$

$$\bar{\text{B}}^{\text{MiNNLO}_{\text{PS}}} \sim e^{-S} \left\{ d\sigma_{\text{FJ}}^{(1)} (1 + S^{(1)}) + d\sigma_{\text{FJ}}^{(2)} + (D - D^{(1)} - D^{(2)}) \right\}$$

- Order  $\mathcal{O}(\alpha^4 \alpha_s^2)$ .
- No loop-induced gluon-fusion contributions.
- Important NNLO corrections (10-15%), due to radiation zero effect at LO (= vanishing of the leading helicity amplitudes in some kinematic regions).

$$pp \rightarrow l'^{\pm} \nu_{l'} l^+ l^- + X$$



## 2) Generation of NLO+PS (EW) results using POWHEG

$$d\sigma_F^{\text{pwg}} = d\Phi_F \bar{B}^{\text{pwg}} \times \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R_F}{B_F} \right\}$$

$$\bar{B}^{\text{pwg}} = d\sigma_F^{(1)} + d\sigma_F^{(2)}$$

- Order  $\mathcal{O}(\alpha^5)$ .
- Real radiation corresponds to photon radiation.
- No photon-photon contribution at this order.
- Photon-quark contributions are not considered (formally, they are  $\mathcal{O}(\alpha^6 L)$ ).

## 3) Combination of NNLO<sub>QCD</sub>+PS and NLO<sub>EW</sub>+PS: MATCHING SCHEMES

### ADDITIVE SCHEME

$$\text{NNLO}_{\text{QCD}} + \text{NLO}_{\text{EW}} - \text{LO}$$

$$\mathcal{O}(\alpha^4), \mathcal{O}(\alpha^4\alpha_s), \mathcal{O}(\alpha^4\alpha_s^2), \mathcal{O}(\alpha^5)$$

### MULTIPLICATIVE SCHEME

$$\text{NNLO}_{\text{QCD}} \times \text{NLO}_{\text{EW}}/\text{LO}$$

$$\mathcal{O}(\alpha^4), \mathcal{O}(\alpha^4\alpha_s), \mathcal{O}(\alpha^4\alpha_s^2), \mathcal{O}(\alpha^5), \mathcal{O}(\alpha^5\alpha_s), \mathcal{O}(\alpha^5\alpha_s^2)$$

- The **multiplicative scheme is preferable** in the high energy limit, where EW Sudakov-logs are dominant and dominant QCD effects arise at scales below the hard scale. —> **QCD factorizes**.
- This assumption is **violated when giant K-factors are present** (= hard vector-boson+jet topologies, with a soft second vector boson).
- The **average** of the two schemes can give a **pragmatic estimate** in these regions.

## 4) Combination of NNLO<sub>QCD</sub>+PS and NLO<sub>EW</sub>+PS: TREATMENT OF THE SHOWER

1. The **formal accuracy** of the calculation **must not be spoilt**.
2. We must **avoid double counting**.

We let the QCD and/or QED showers radiate in whole the phase space and then we apply the following **veto procedure**:

**NNLO<sub>QCD</sub>+PS** :

- **QCD** shower is **restricted** by the transverse momentum of the hardest QCD emission generated at Les Houches level (as commonly done in POWHEG).

- **QED** shower is **unconstrained**.

**NLO<sub>EW</sub>+PS** :

- **QCD** shower is **unconstrained**.
- **QED** shower is **restricted** by the transverse momentum of the hardest QED emission generated at Les Houches level (POWHEG multiple-radiation scheme → **three different starting scales** for ISR, FSR from W decay, FSR from Z decay).

**ADDITIVE:** 1.  $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} - \text{LO}^{(\text{QCD}, \text{QED})_{\text{PS}}} = \text{NNLO}_{\text{QCD+EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$

2.  $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QED})_{\text{PS}}} - \text{LO}^{(\text{QED})_{\text{PS}}}$

3.  $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} - \text{LO}^{(\text{QCD})_{\text{PS}}}$

**MULTIPLICATIVE:** 4.  $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} \times \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} / \text{LO}^{(\text{QCD}, \text{QED})_{\text{PS}}} = \text{NNLO}_{\text{QCD} \times \text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$

5.  $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} \times \text{NLO}_{\text{EW}}^{(\text{QED})_{\text{PS}}} / \text{LO}^{(\text{QED})_{\text{PS}}}$

6.  $\text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} \times \text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} / \text{LO}^{(\text{QCD})_{\text{PS}}}$

7.  $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} \times \text{NLO}_{\text{EW}}^{\text{f.o.}} / \text{LO}^{\text{f.o.}}$

**NOTATION:**

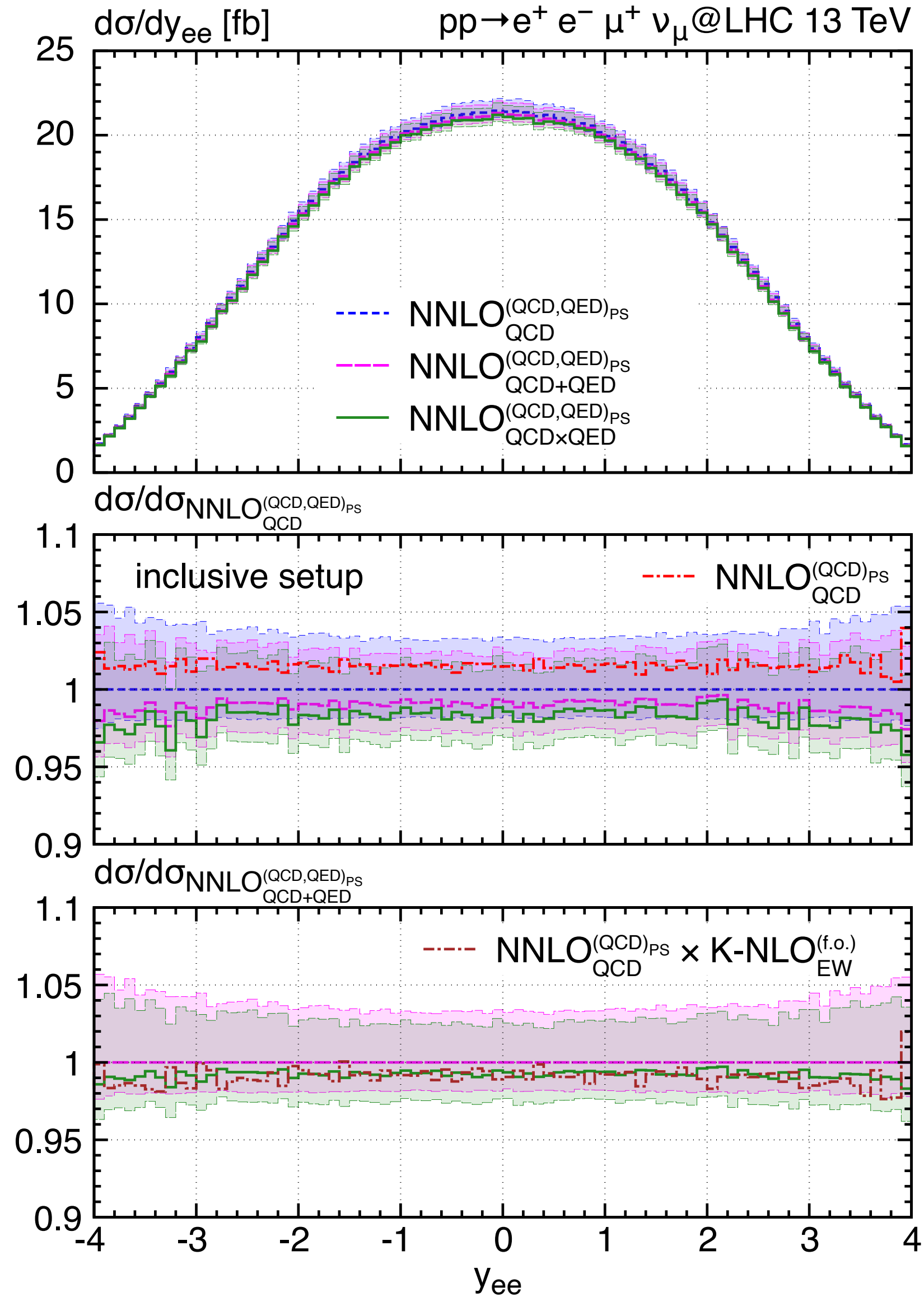
$$(\text{N})\text{NLO}_{\text{X}}^{(\text{Y})_{\text{PS}}}$$

X = QCD,EW calculation

Y = QCD,QED showers (PY8)

# Phenomenological results (1)

Rapidity of the Z boson - inclusive setup



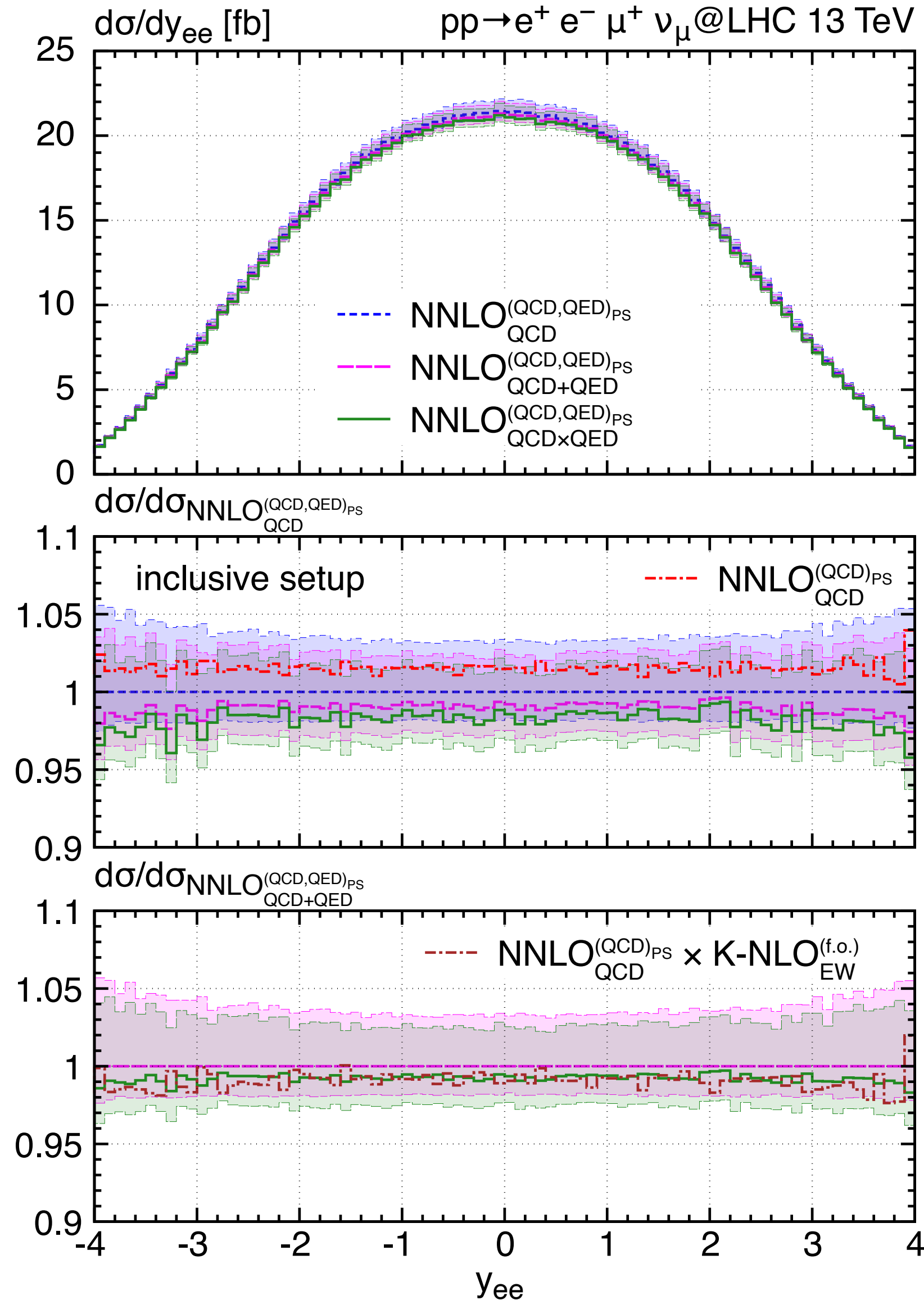
## LEGEND:

- $\text{NNLO}_{\text{QCD}}^{(\text{QCD},\text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD+EW}}^{(\text{QCD},\text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}\times\text{EW}}^{(\text{QCD},\text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} \times K_{\text{EW}}^{\text{f.o.}}$

# Phenomenological results (1)

## Rapidity of the Z boson - inclusive setup

- Almost no shape effect
- EW corrections are 2-3%
- Additive ● and multiplicative ● schemes are almost identical
- Fixed-order K-factor ● is in excellent agreement  $\rightarrow$  effects of secondary photon emissions are negligible for this observable



## LEGEND:

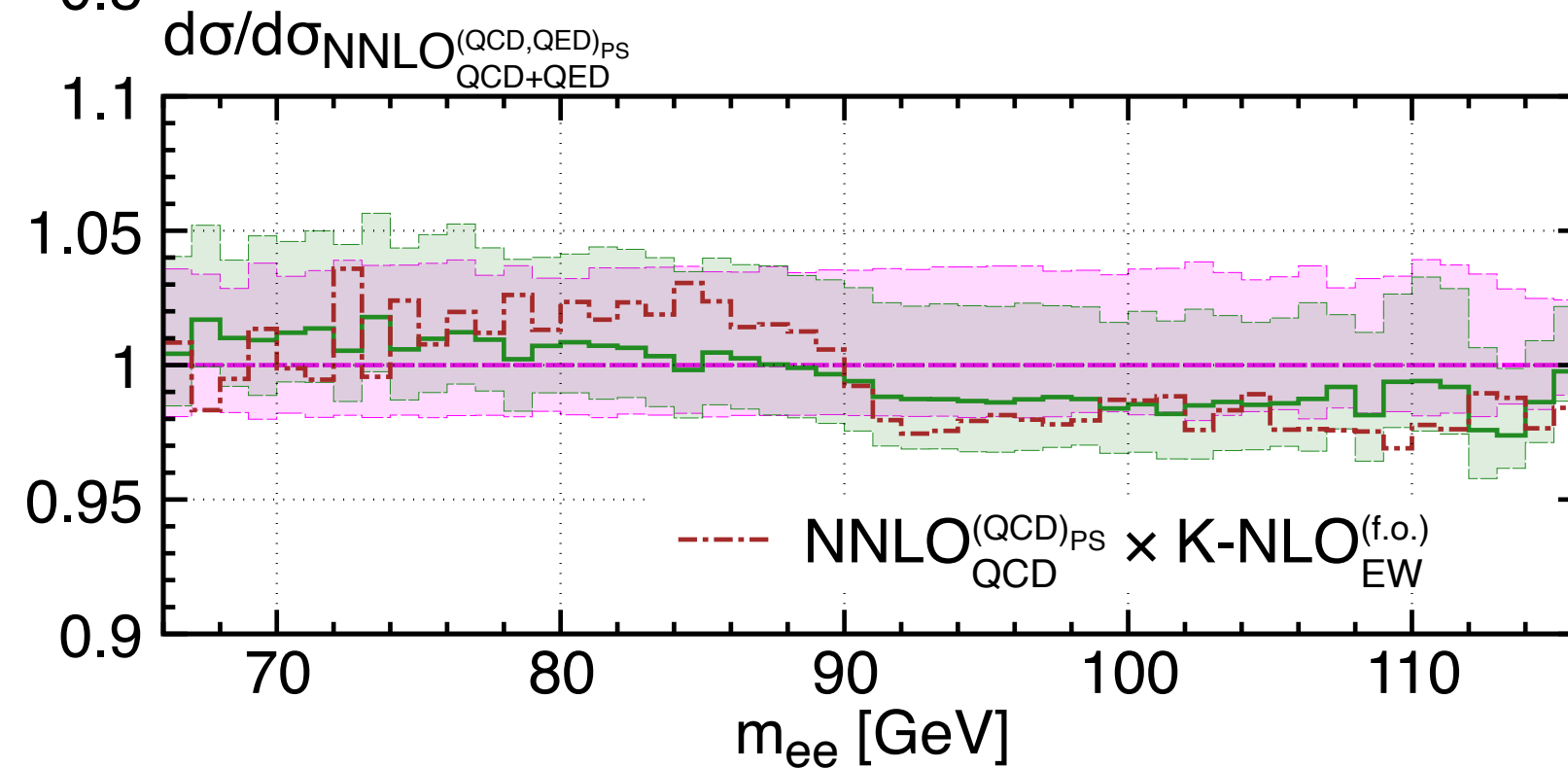
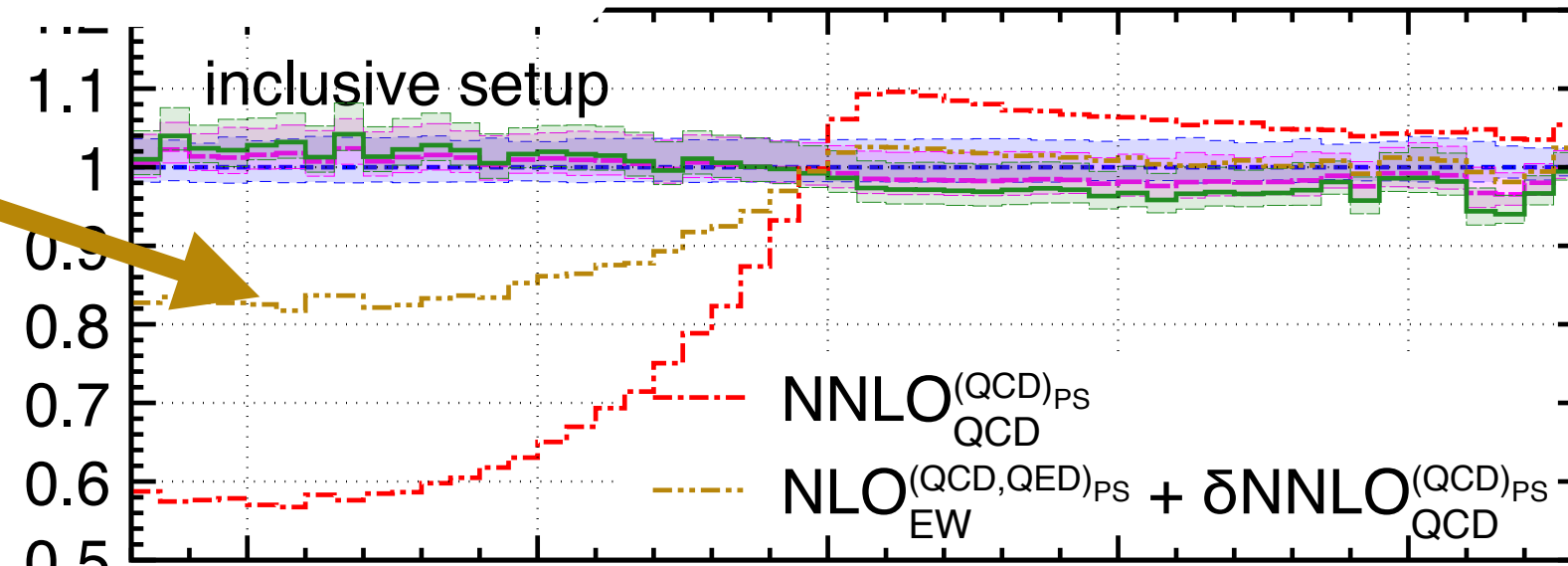
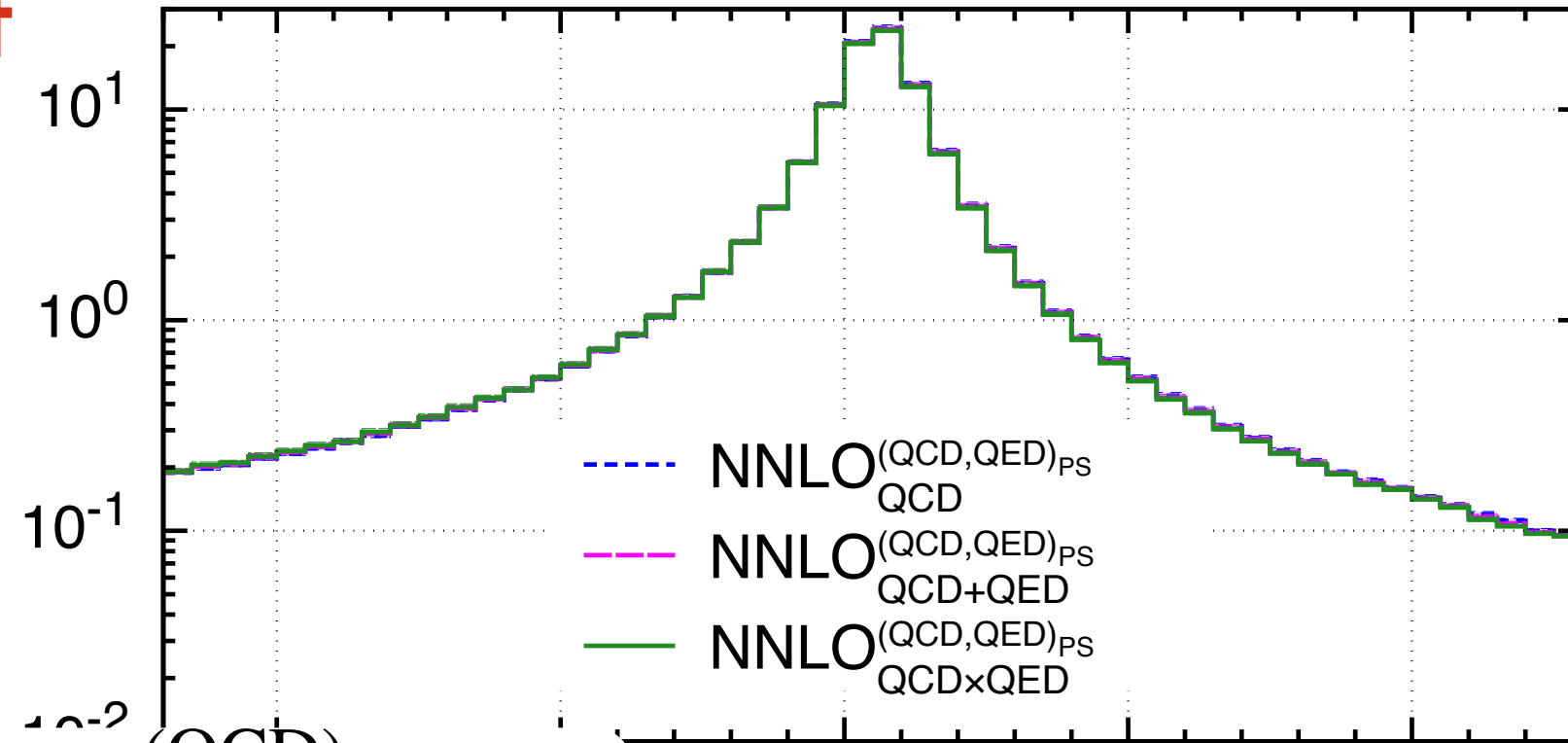
- NNLO<sup>(QCD,QED)</sup><sub>PS QCD</sub>
- NNLO<sup>(QCD,QED)</sup><sub>PS QCD+EW</sub>
- NNLO<sup>(QCD,QED)</sup><sub>PS QCD×EW</sub>
- NNLO<sup>(QCD)</sup><sub>PS QCD</sub>
- NNLO<sup>(QCD)</sup><sub>PS QCD</sub> × K<sup>f.o.</sup><sub>EW</sub>

# Phenomenological results (2)

Invariant mass of the Z boson - inclusive setup

●  $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} - \text{LO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$

$d\sigma/dm_{ee}$  [fb/GeV]  $pp \rightarrow e^+ e^- \mu^+ \nu_\mu$  @LHC 13 TeV



## LEGEND:

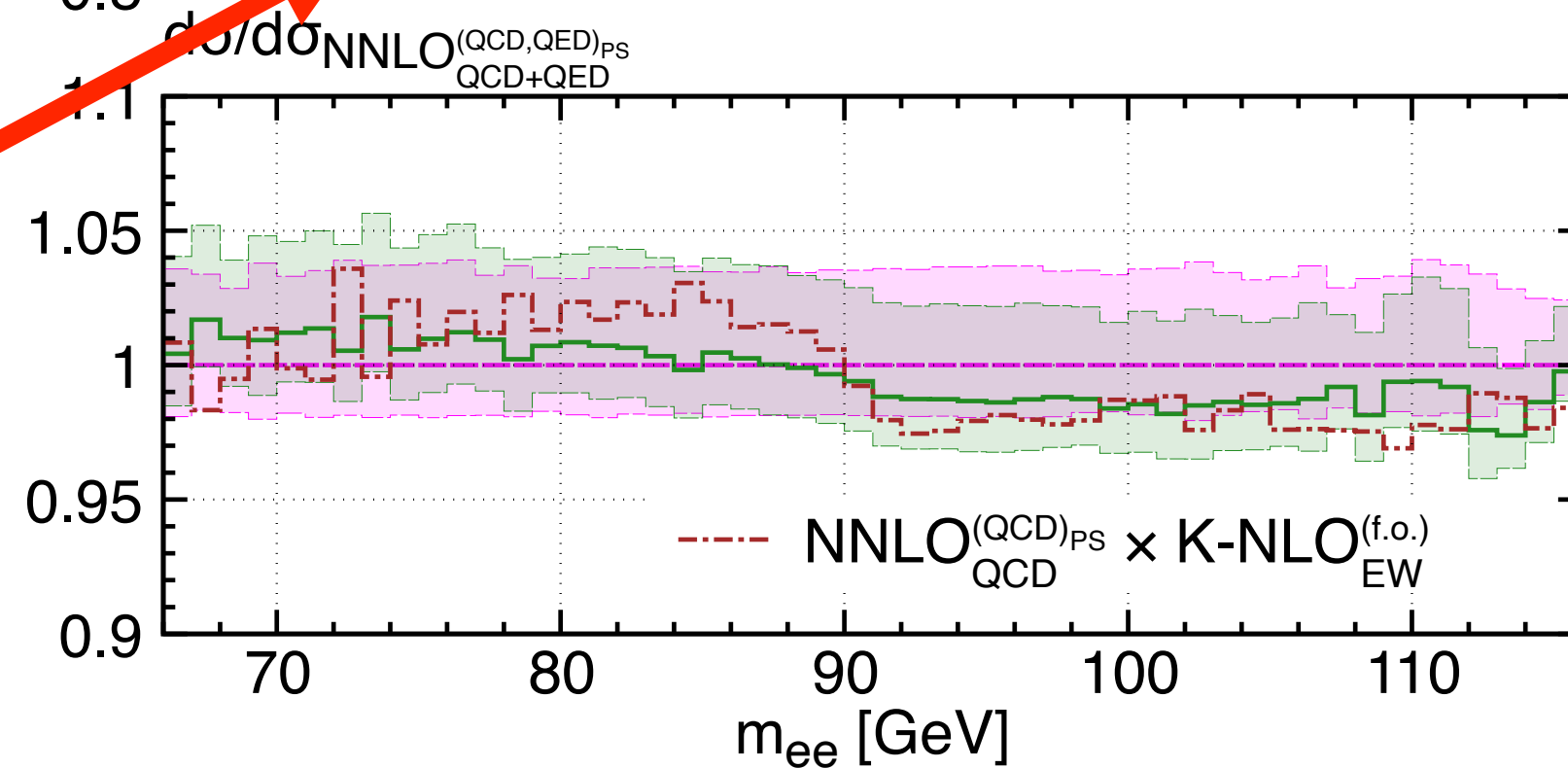
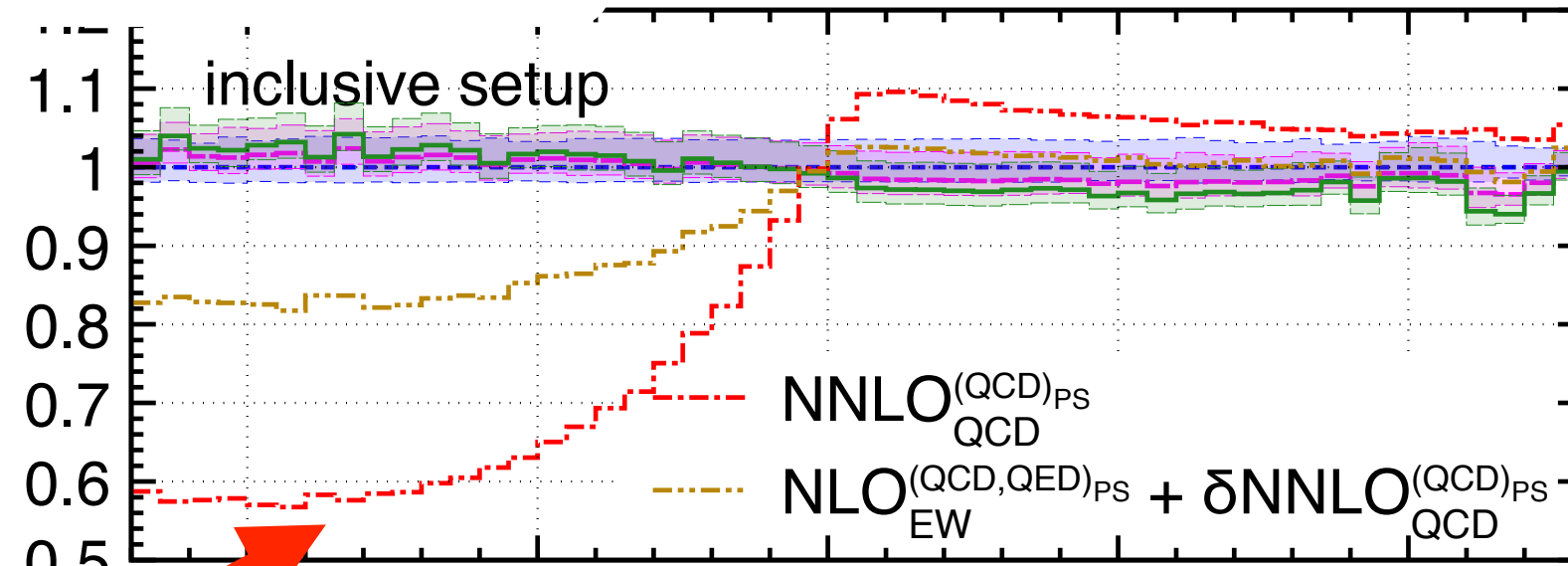
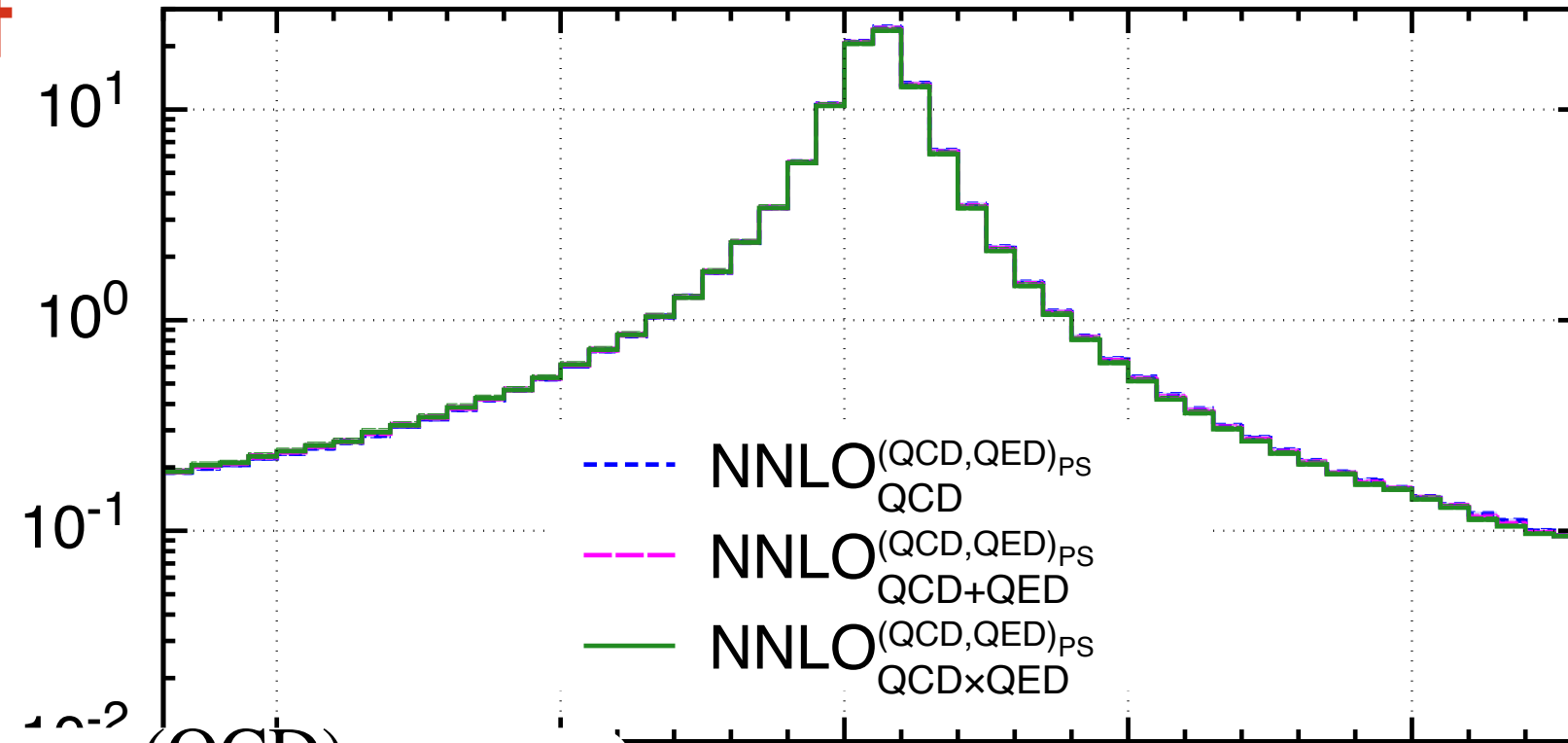
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}+\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD} \times \text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$
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$d\sigma/dm_{ee}$  [fb/GeV]  $pp \rightarrow e^+ e^- \mu^+ \nu_\mu$  @LHC 13 TeV



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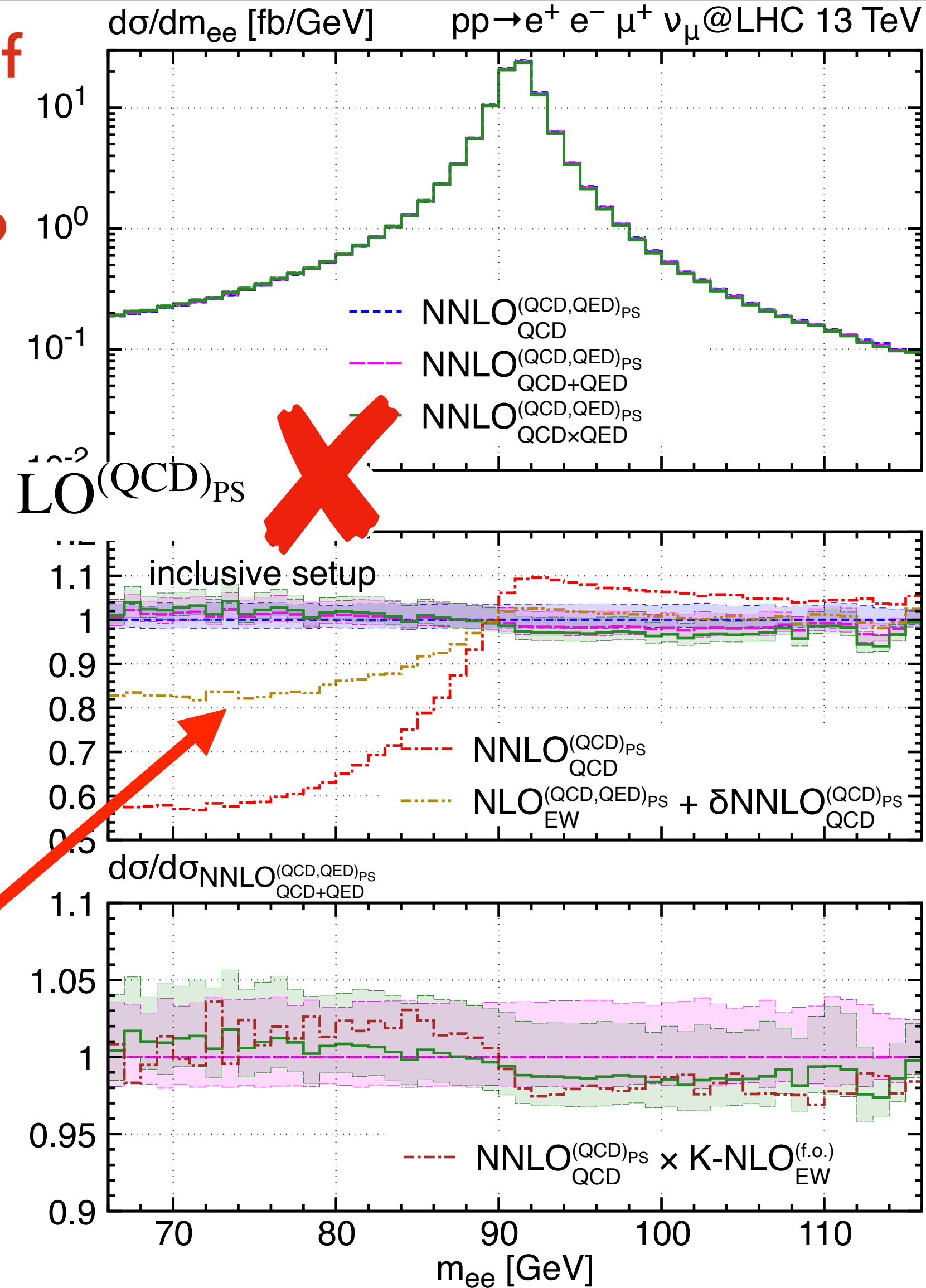
Large effects from collinear QED radiations (~40%), which are absent in ●

# Phenomenological results (2)

Invariant mass of the Z boson - inclusive setup

●  $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} + \text{NLO}_{\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}} - \text{LO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$

● misses important QED-QCD effects originating from QED emissions on top of the NNLO calculation —> **DISCARDED**



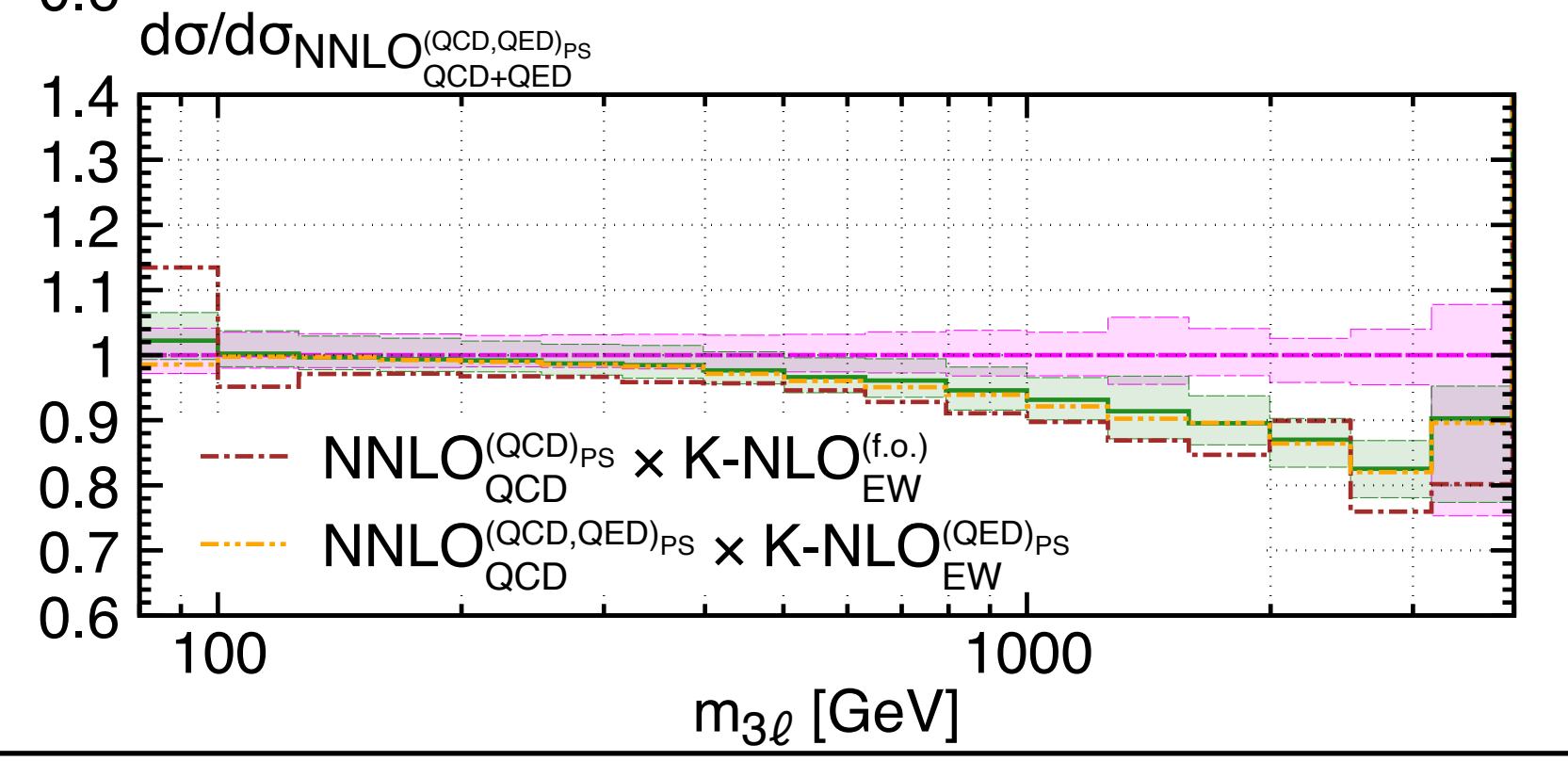
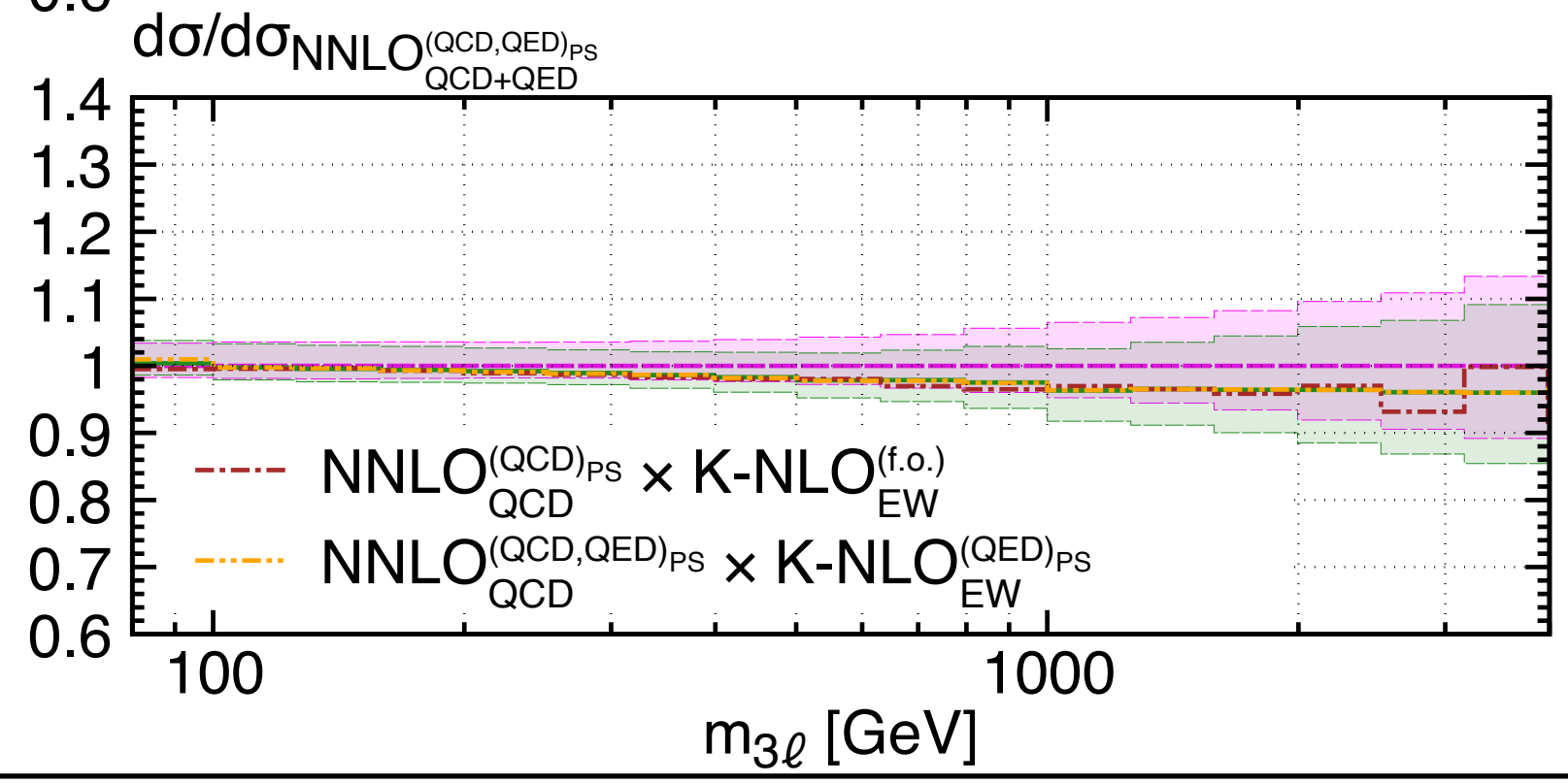
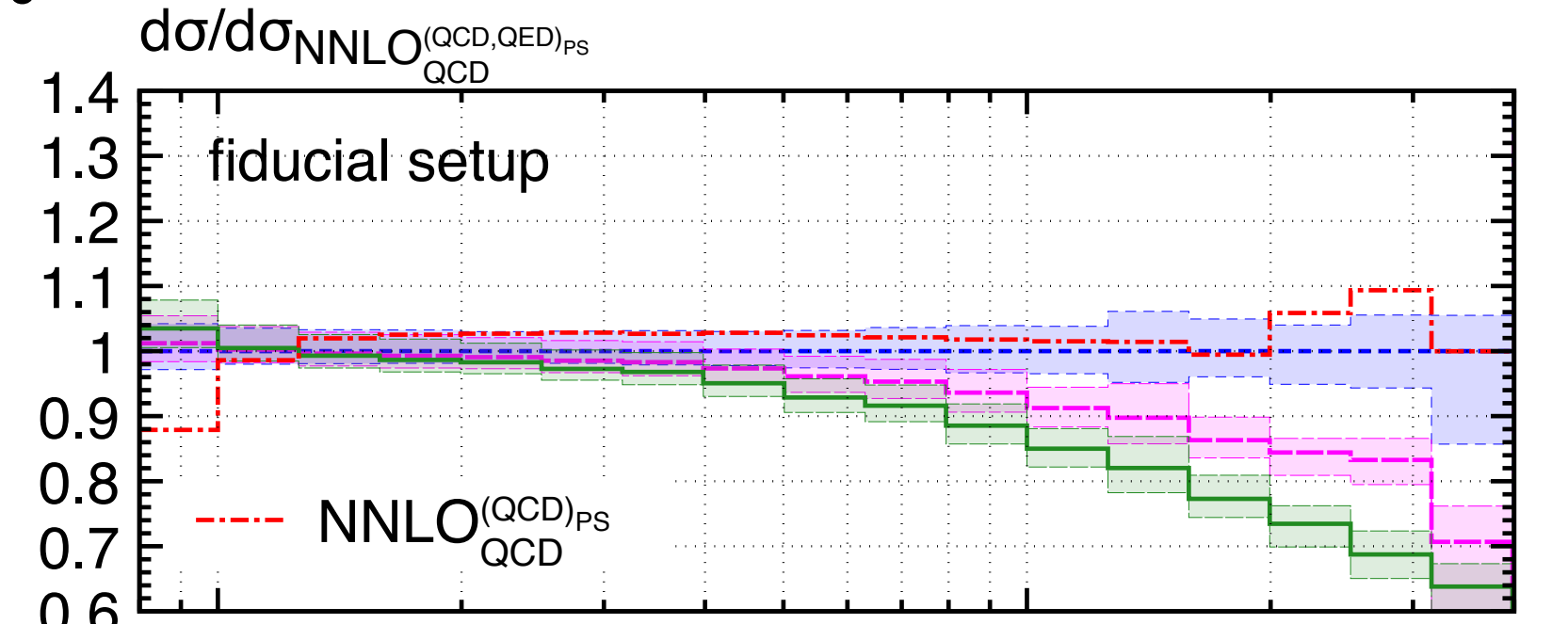
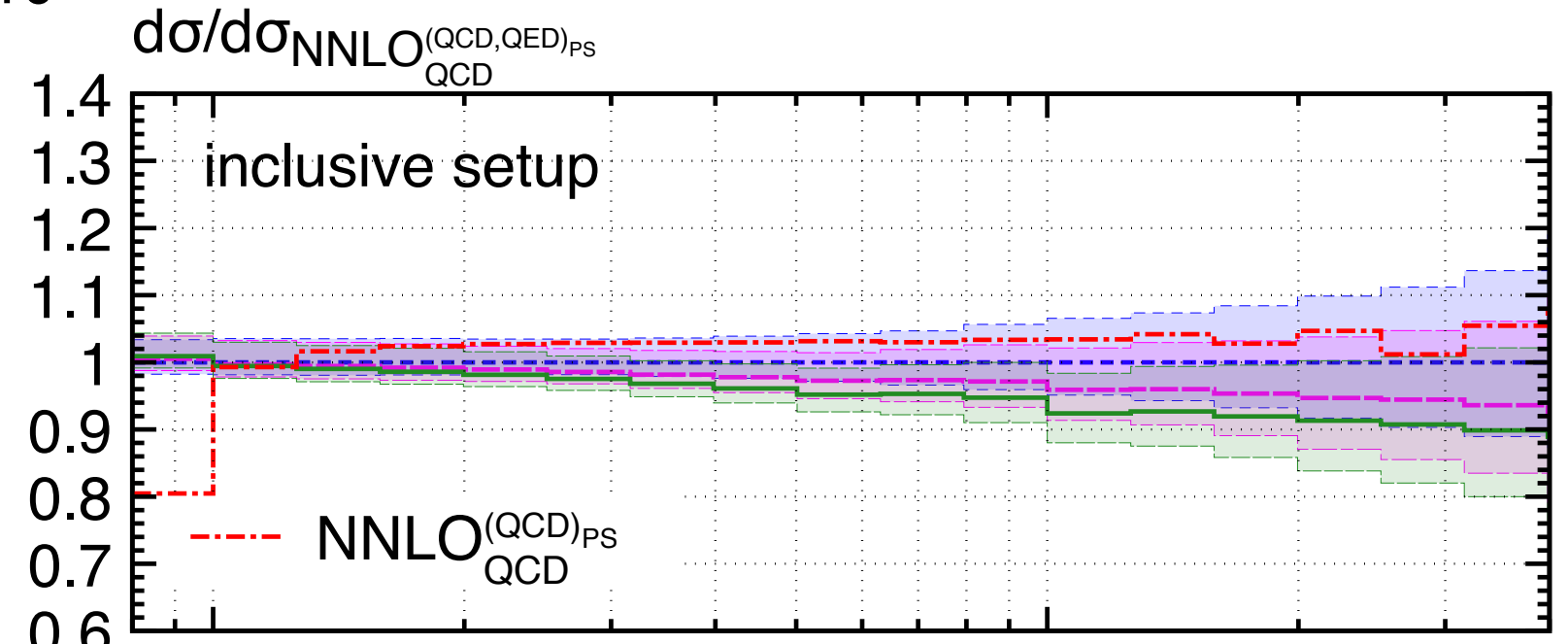
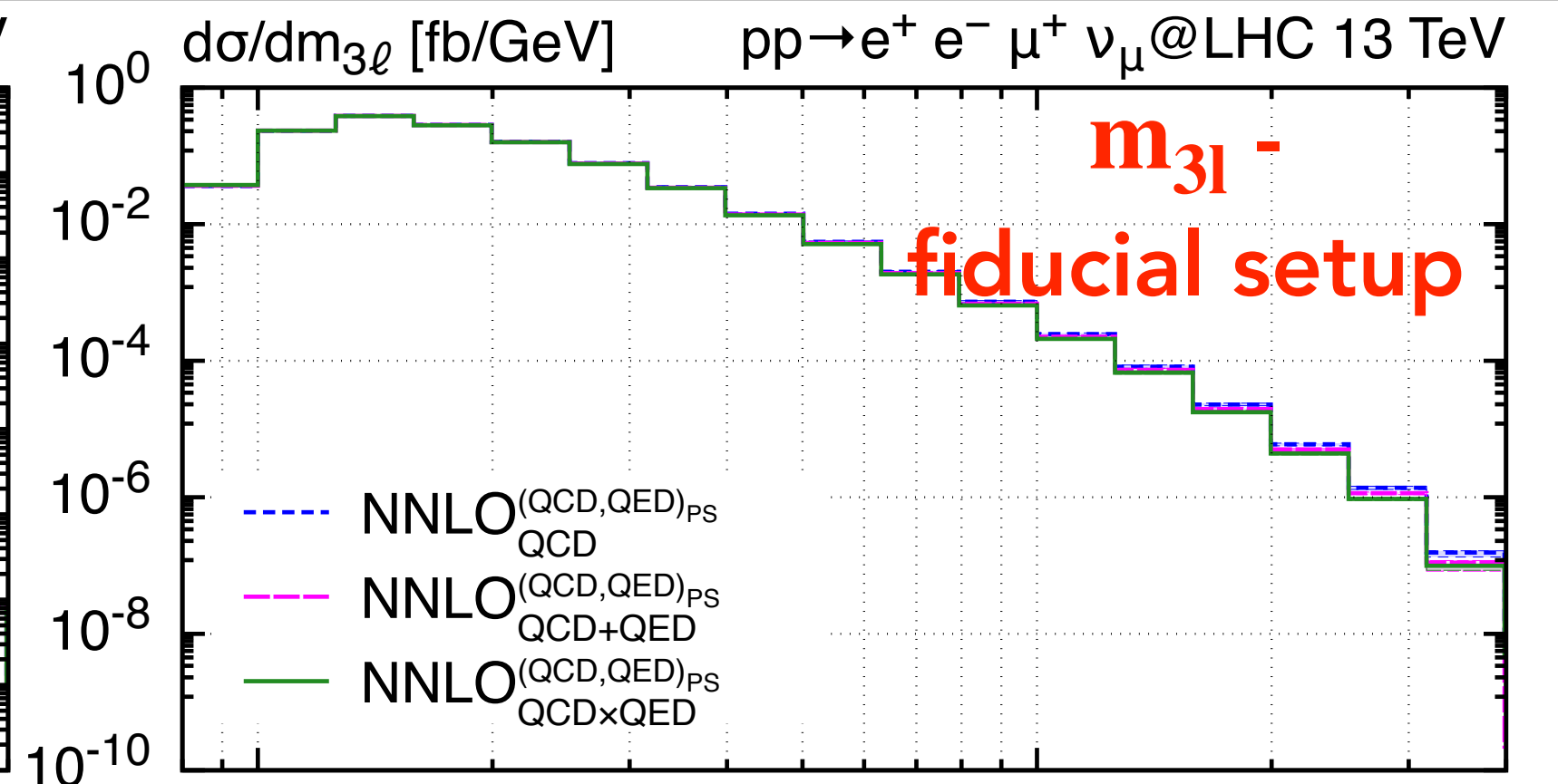
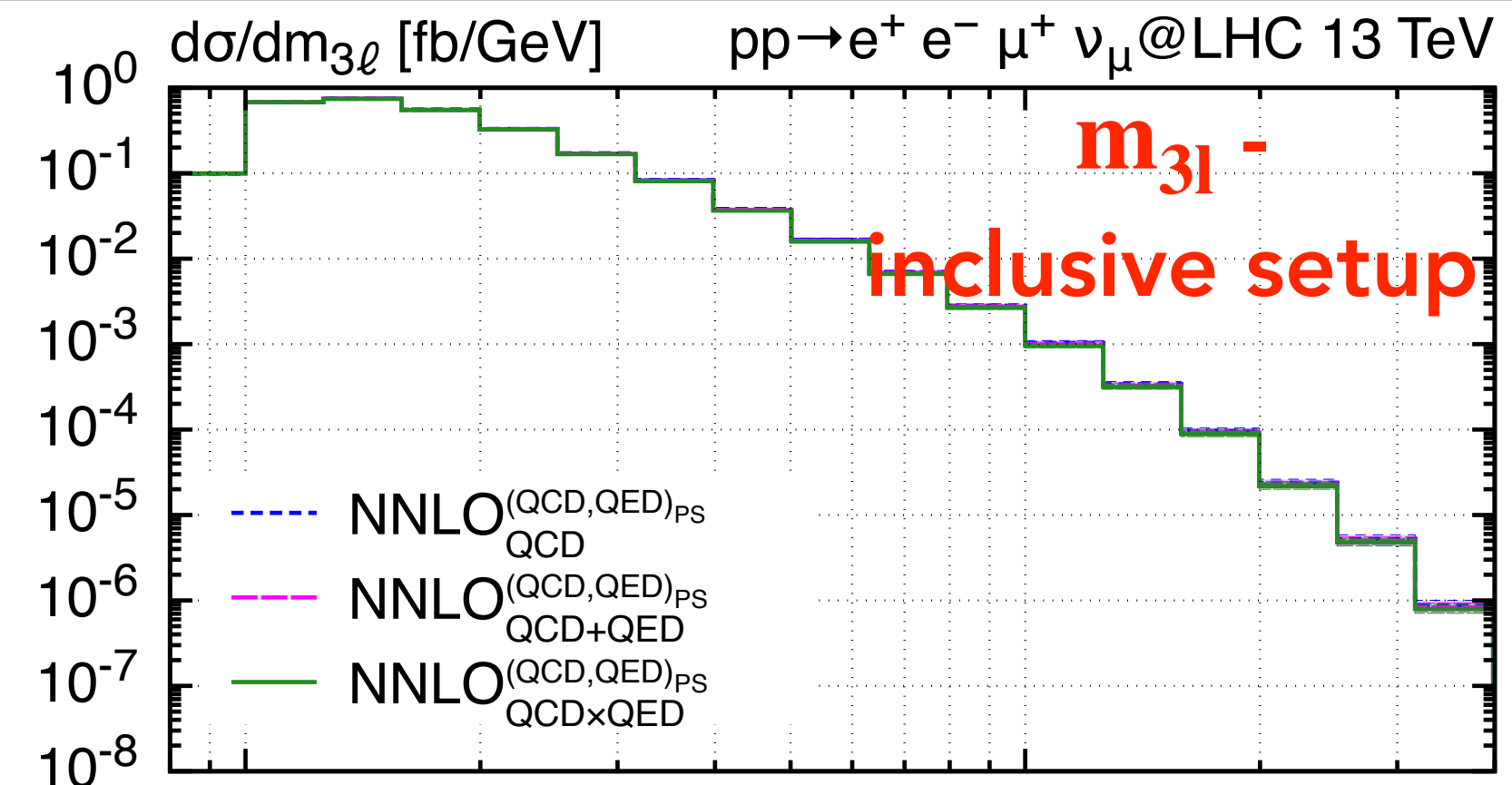
## LEGEND:

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- $\text{NNLO}_{\text{QCD} \times \text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$
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# Phenomenological results (3)

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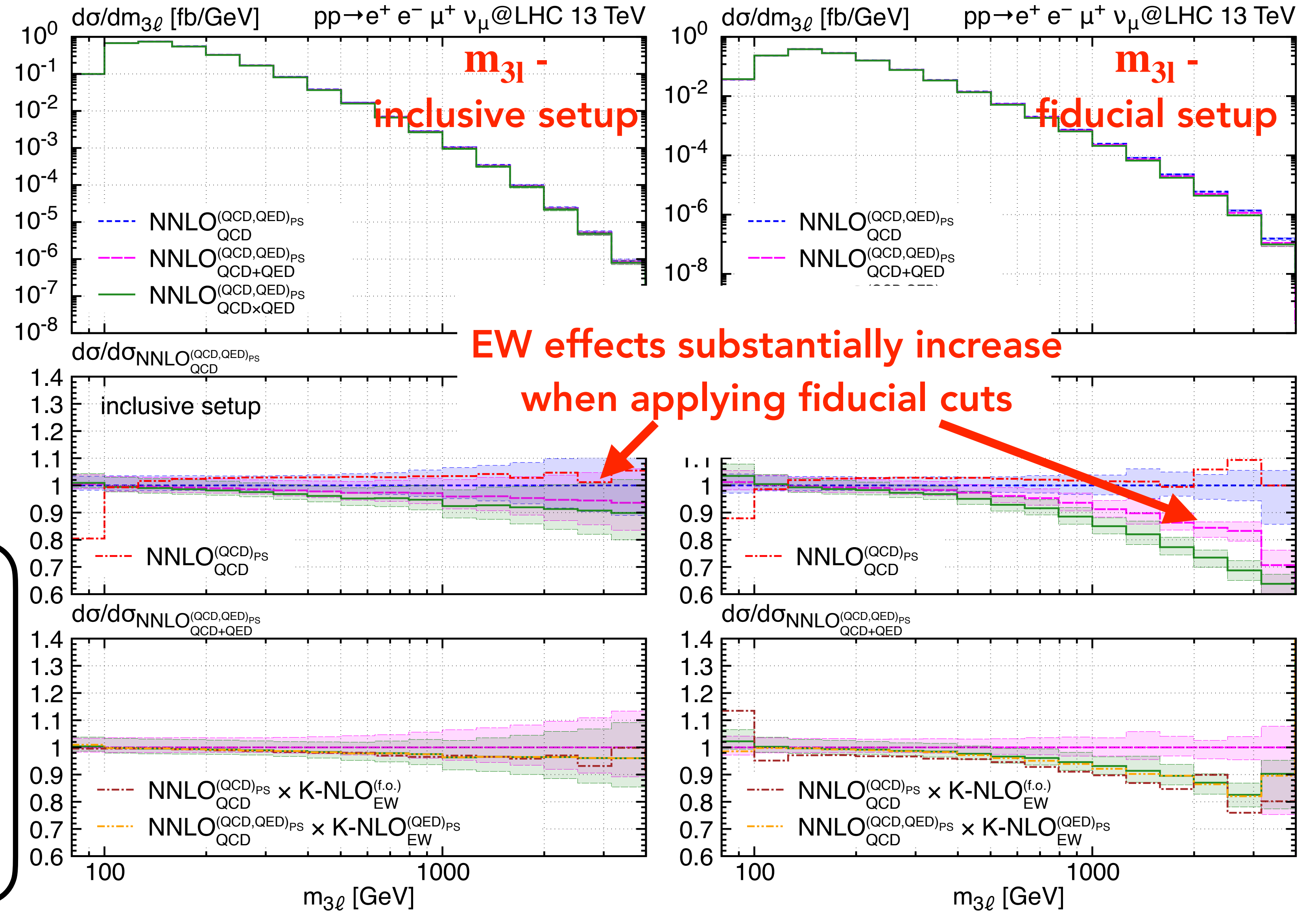


# Phenomenological results (3)

## LEGEND:

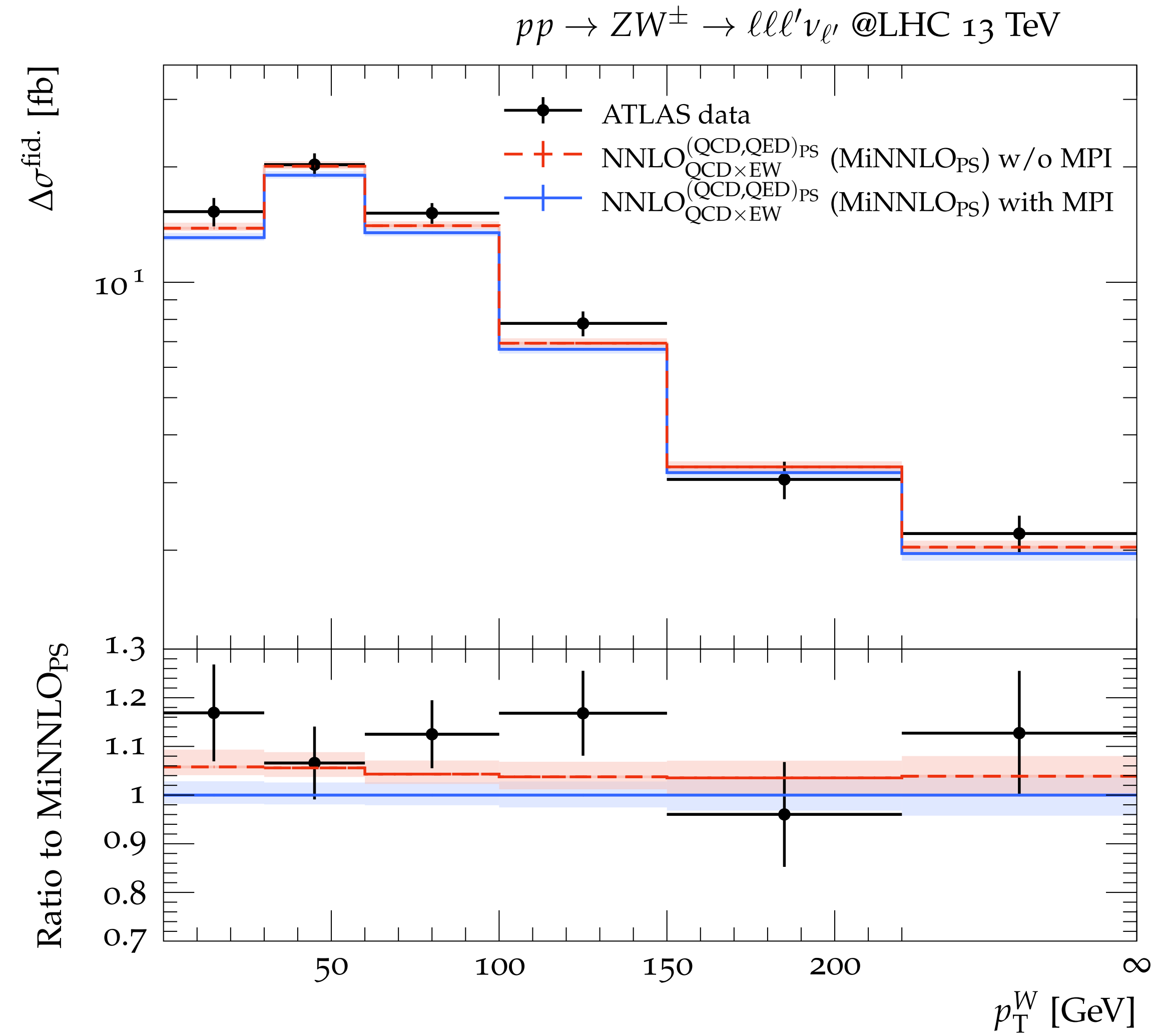
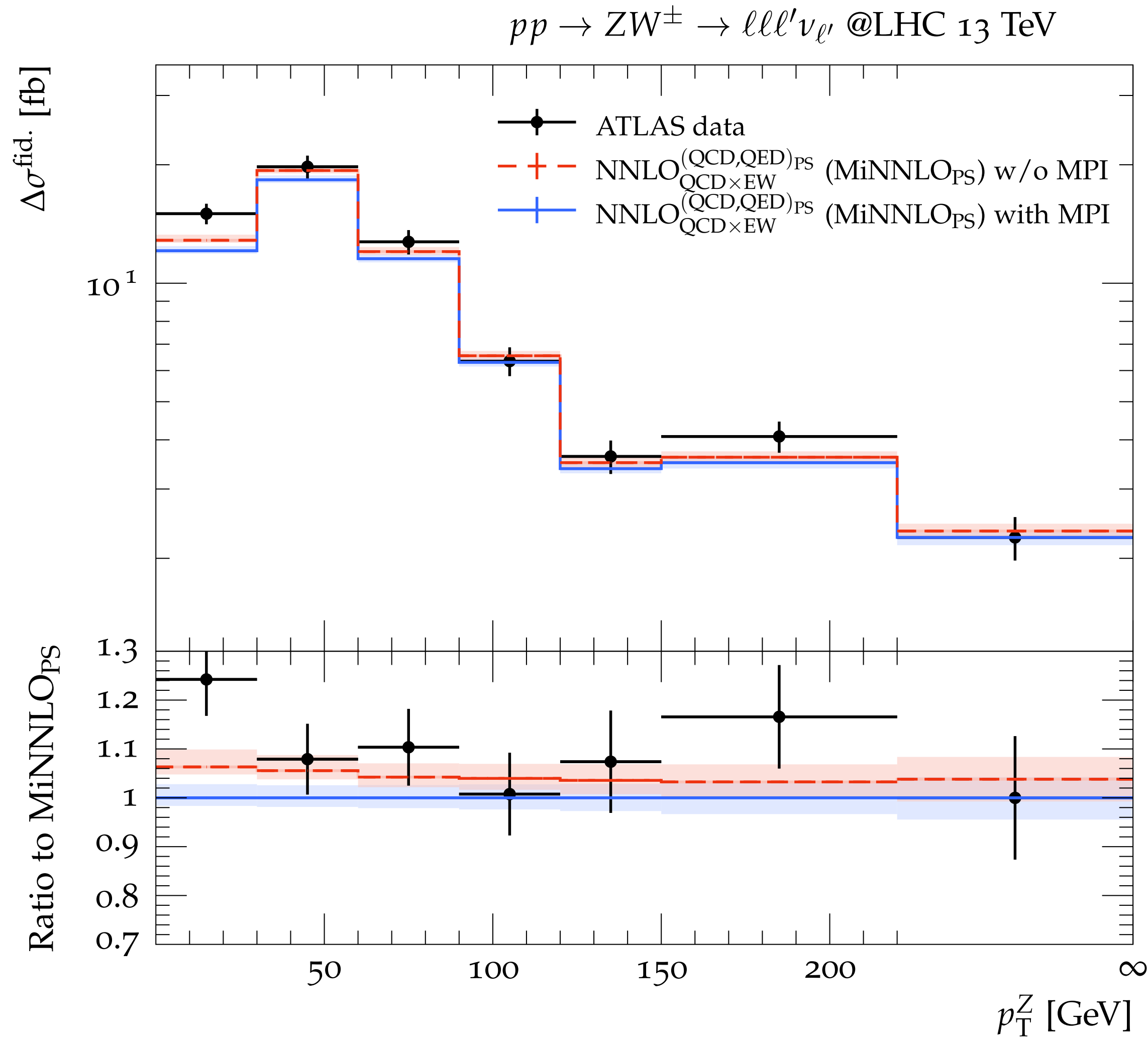
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- $\text{NNLO}_{\text{QCD+EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
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- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} \times K_{\text{EW}}^{\text{f.o.}}$

In the inclusive case, Sudakov-logs are suppressed because not all the Mandelstam invariants are large in the very forward regime. These regions are removed when applying fiducial cuts.



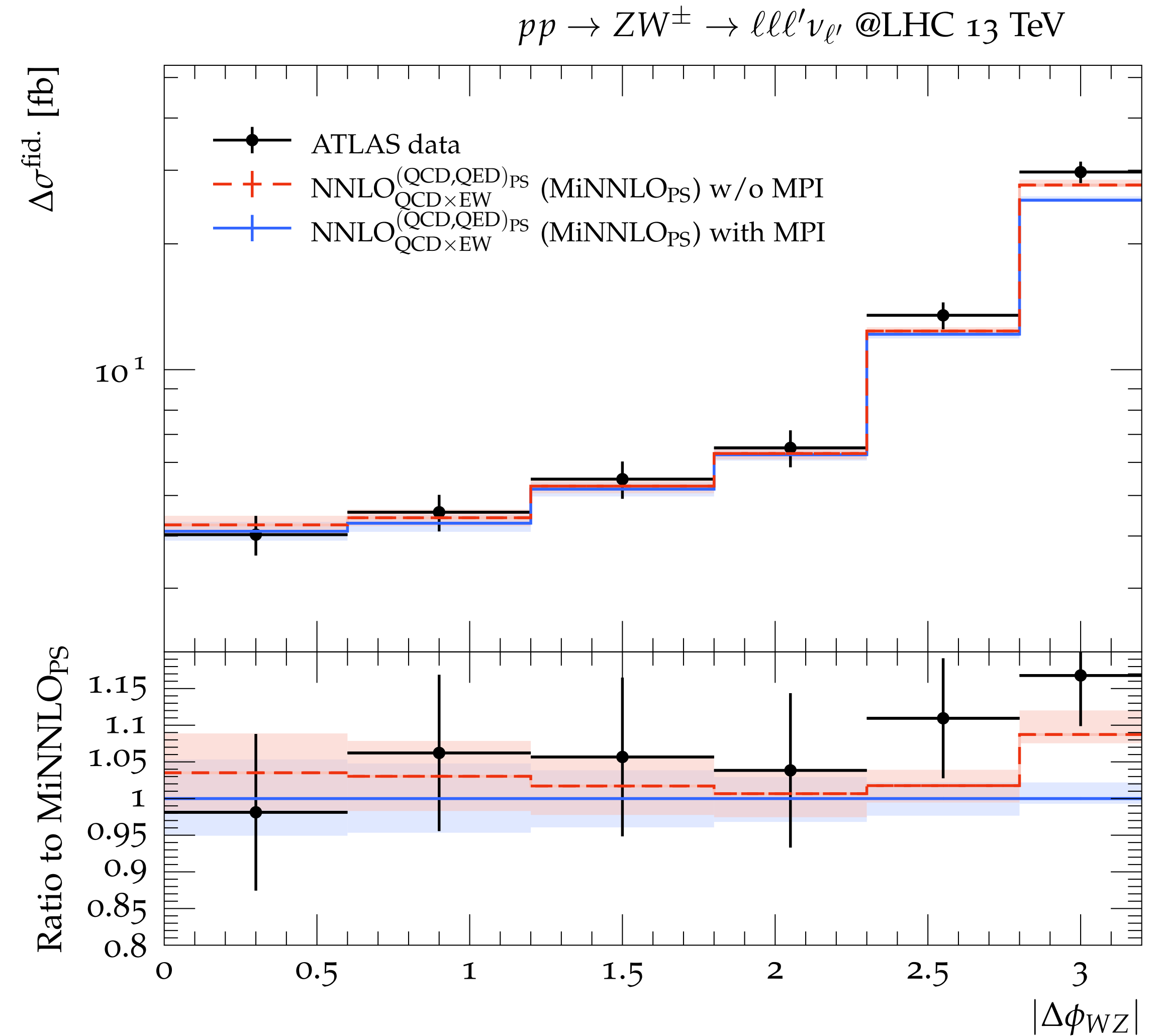
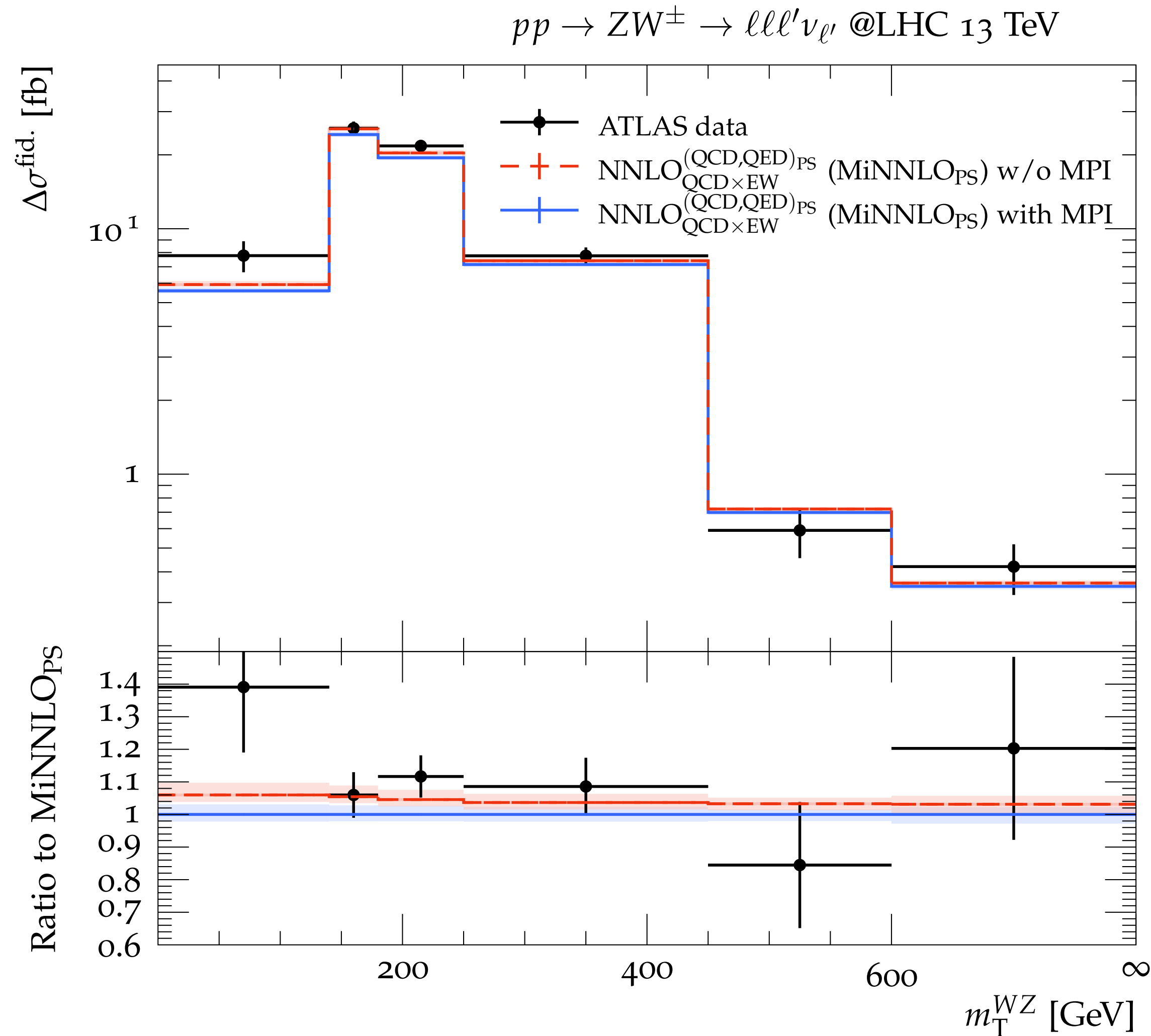
# Comparison against data

ATLAS data from Eur. Phys. J. C 79 (2019)



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- **NNLO+PS (QCD)** predictions are strongly needed for a realistic description of LHC events and the **MiNNLO<sub>PS</sub> method** is a powerful tool for reaching this accuracy.
- In the context of precision physics, the inclusion of **NLO EW corrections** on top of the NNLO calculations is particularly important.
- I showed and discuss results for **WZ production** at NNLO (QCD) and NLO (EW) accuracy matched to parton showers for 13 TeV LHC collisions.
- The natural next step is the implementation of the combined generation of NNLO QCD and NLO EW accurate events, rather than an a posteriori recombination.

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Thank you!

# BACKUP

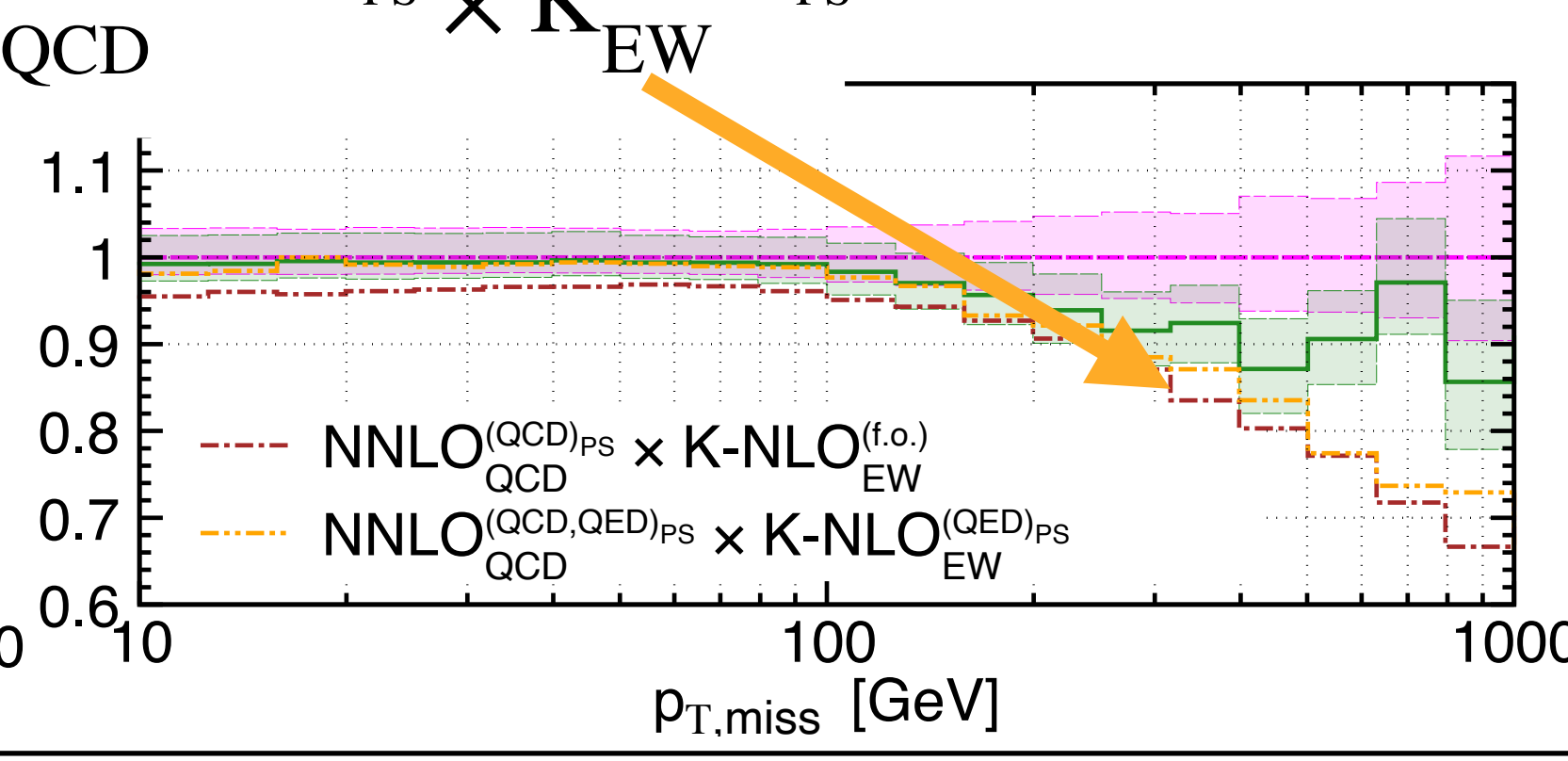
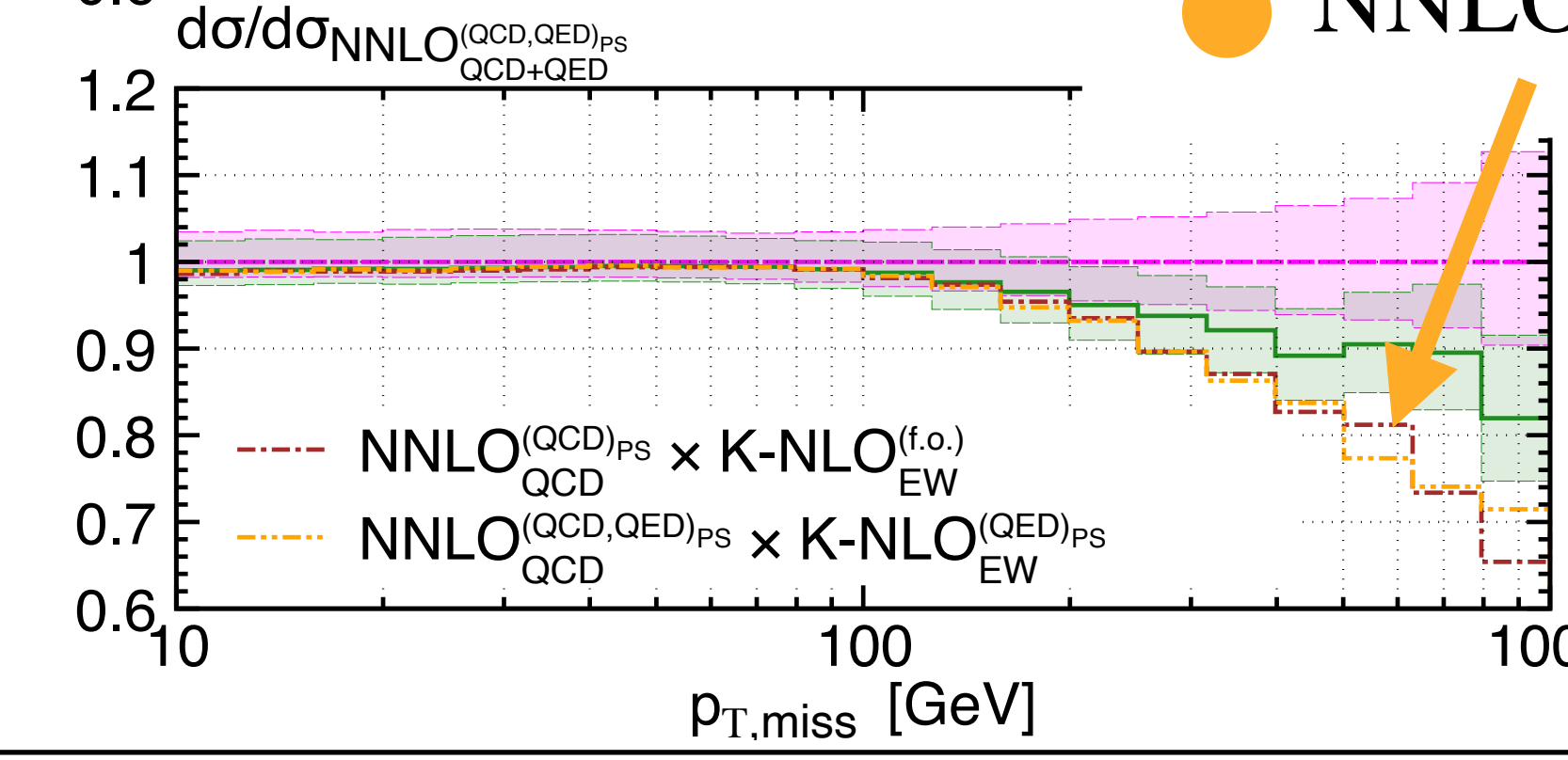
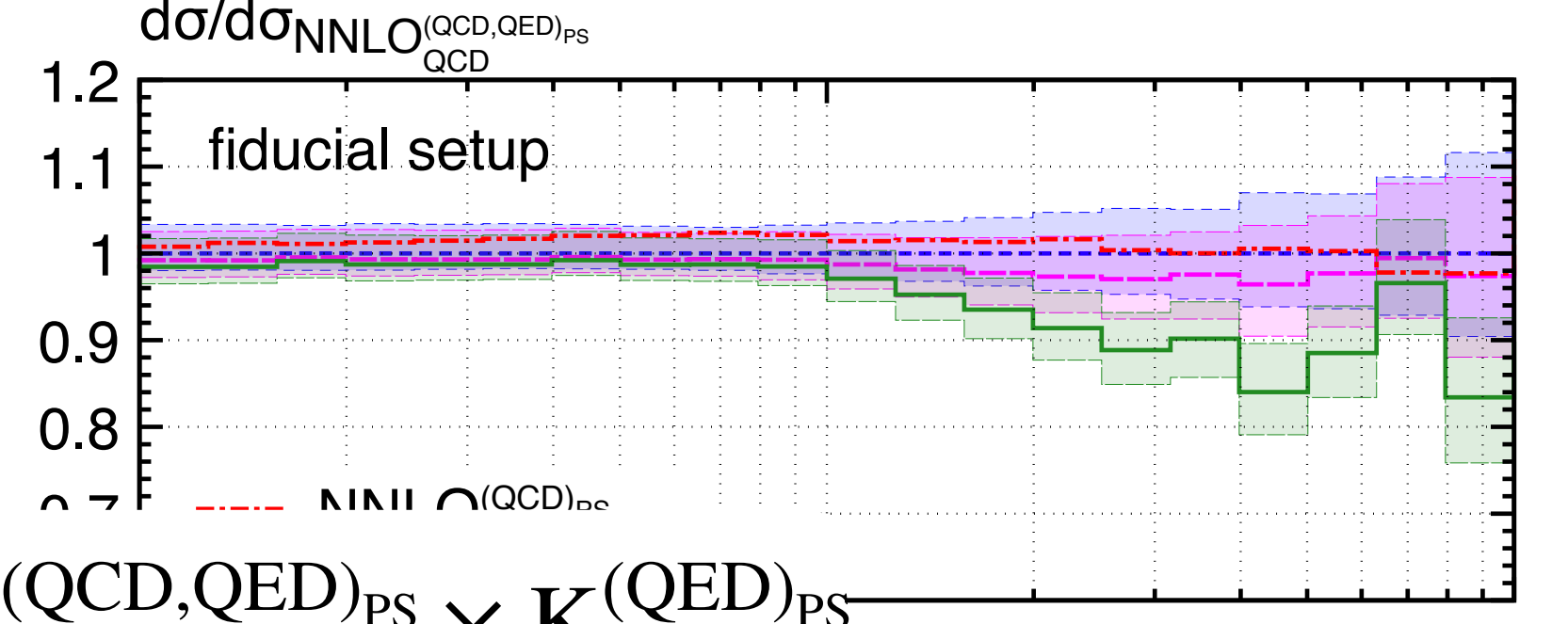
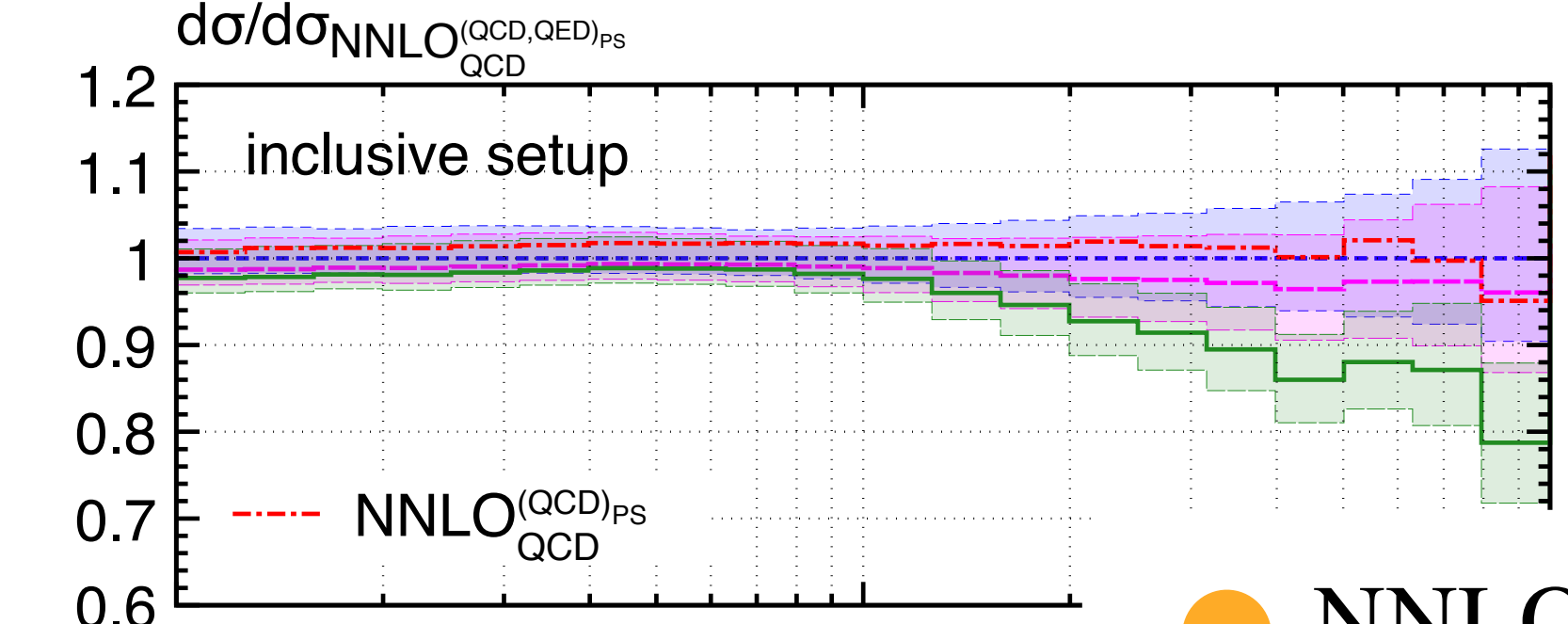
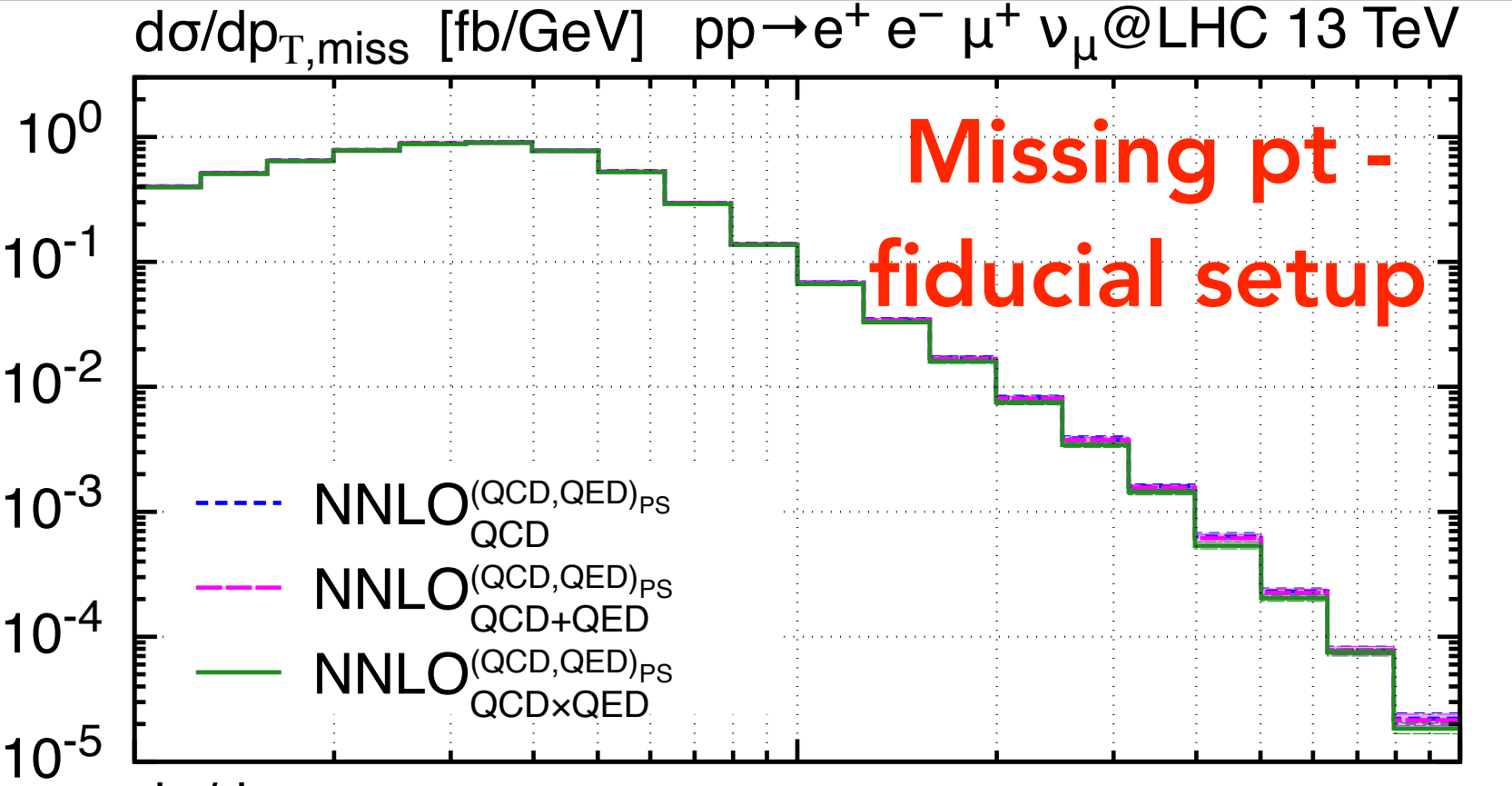
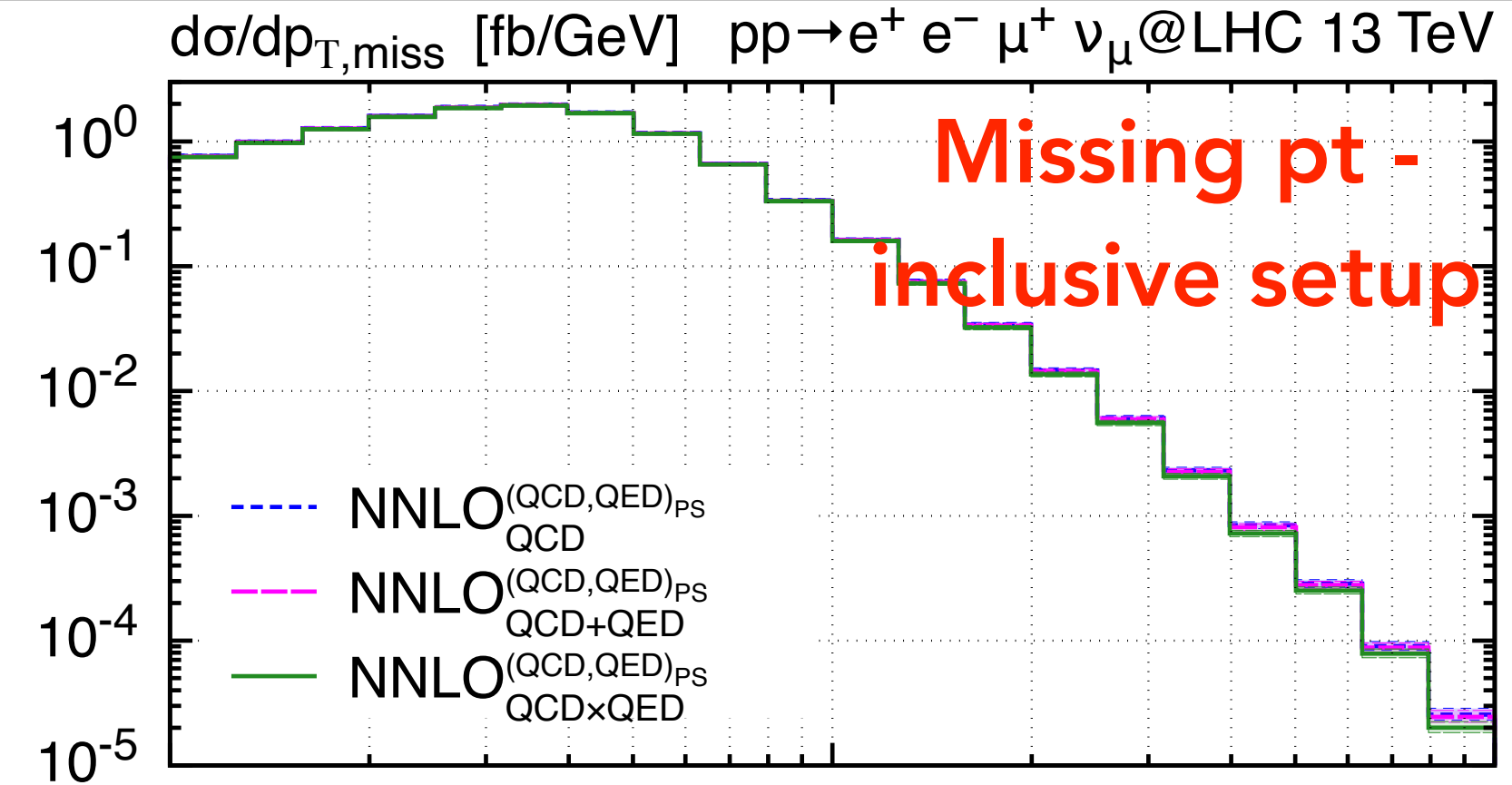
	F	F+J	F+JJ
<b>F@POWHEG</b> [Nason '04]	NLO	LO	LL
<b>F@MiNLO'</b> [Hamilton, Nason, Oleari, Zanderighi '12]	NLO	NLO	LO
<b>F@MiNNLO<sub>PS</sub></b> [Monni, Nason, Re, Wisemann, Zanderighi '19]	<b>NNLO</b>	<b>NLO</b>	<b>LO</b>

- No computationally intense reweighting
- No unphysical merging scale
- LL accuracy of the shower preserved
- Numerically efficient

# Phenomenological results (3)

**LEGEND:**

- $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD+EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}\times\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} \times K_{\text{EW}}^{\text{f.o.}}$

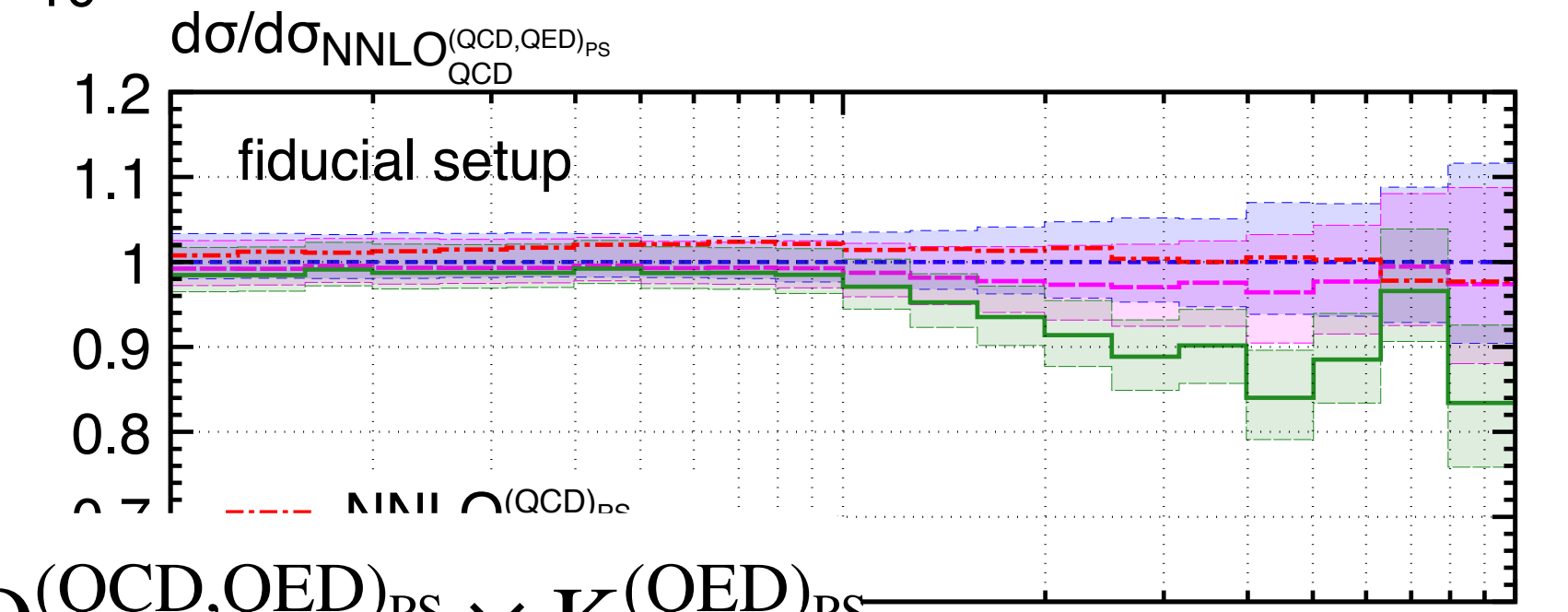
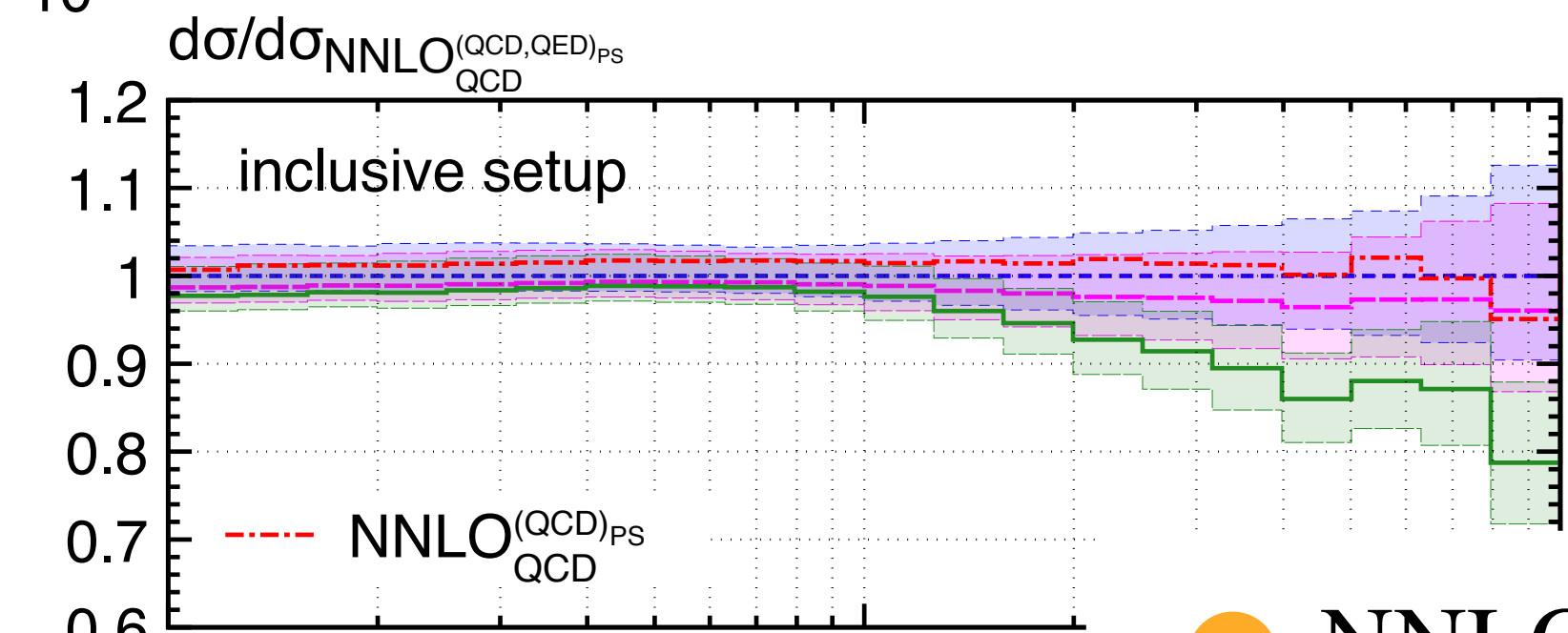
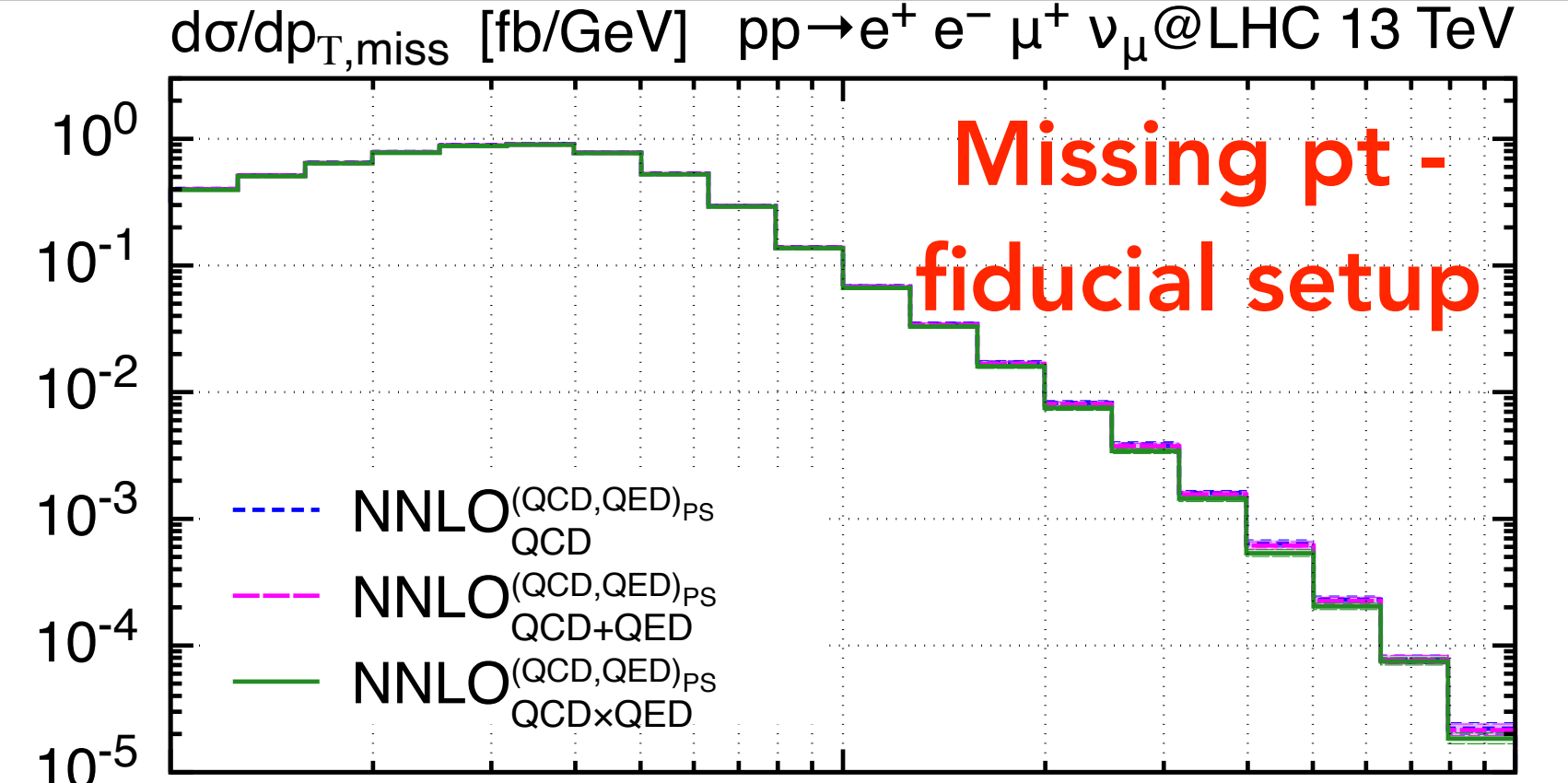
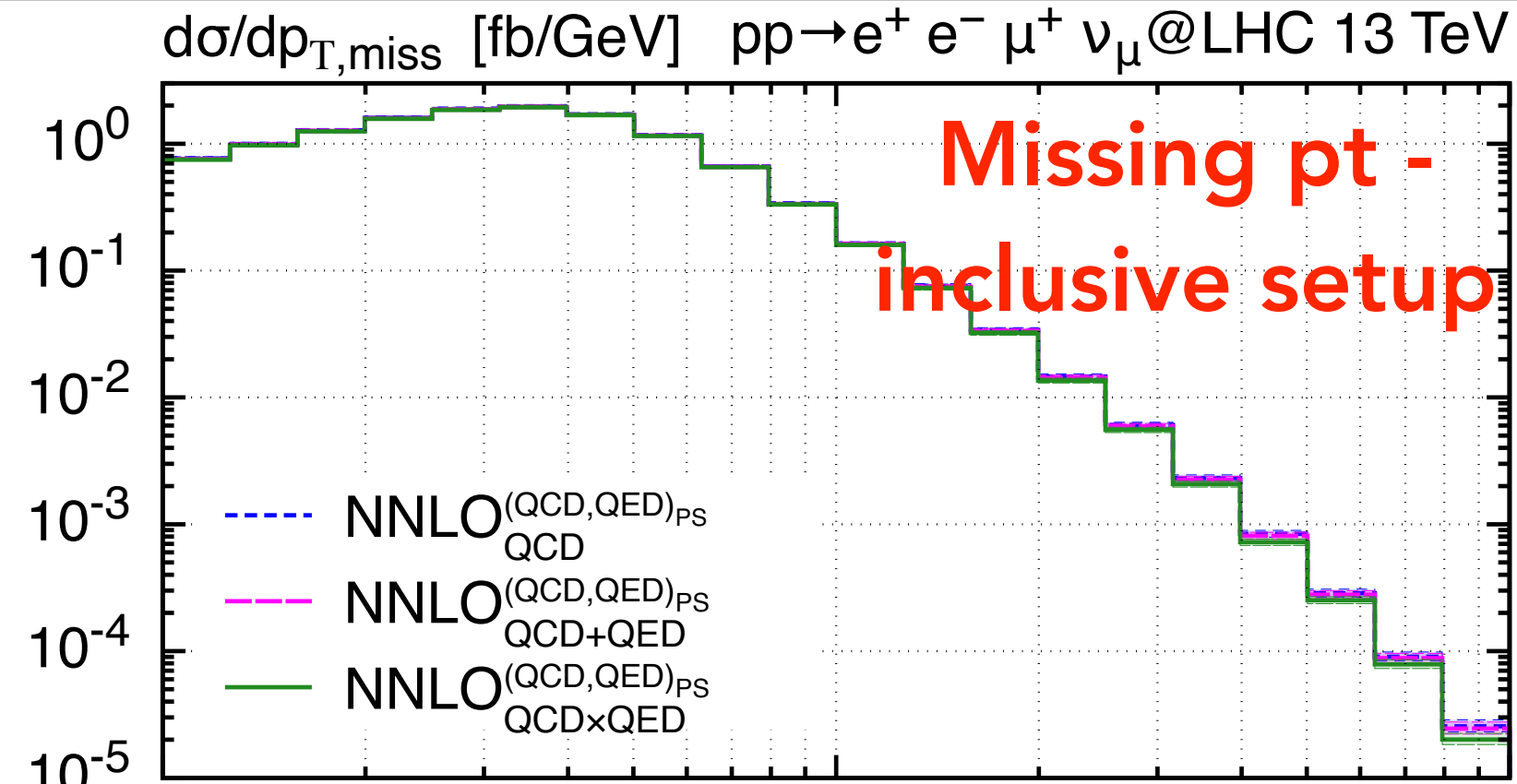


# Phenomenological results (3)

## LEGEND:

- $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD+EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}\times\text{EW}}^{(\text{QCD}, \text{QED})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}}$
- $\text{NNLO}_{\text{QCD}}^{(\text{QCD})_{\text{PS}}} \times K_{\text{EW}}^{\text{f.o.}}$

● is affected by giant K-factors



●  $\text{NNLO}_{\text{QCD}}^{(\text{QCD}, \text{QED})_{\text{PS}}} \times K_{\text{EW}}^{(\text{QED})_{\text{PS}}}$

