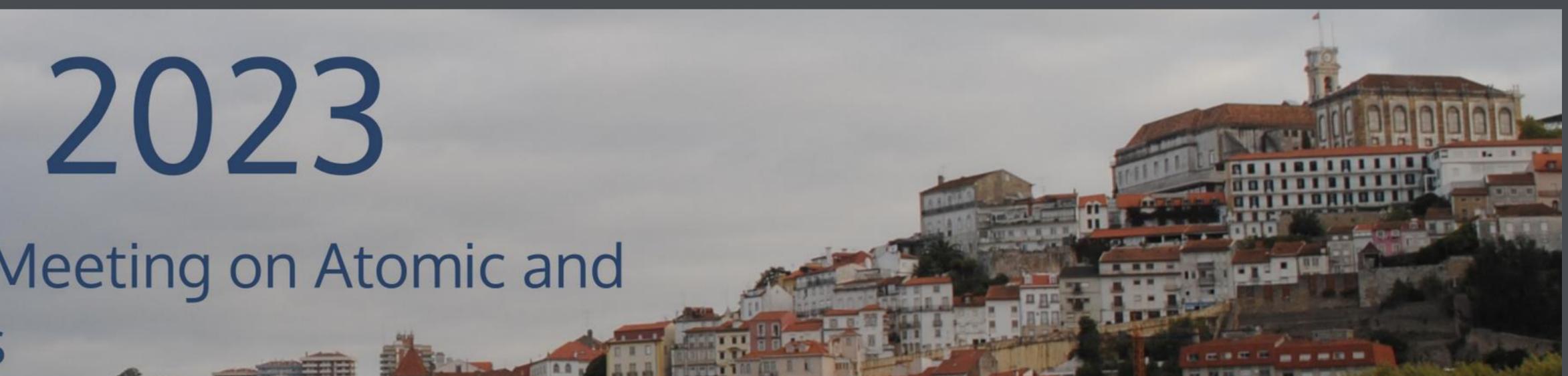


# Laser excitation of the ground-hyperfine transition in muonic hydrogen

 **IBER 2023**

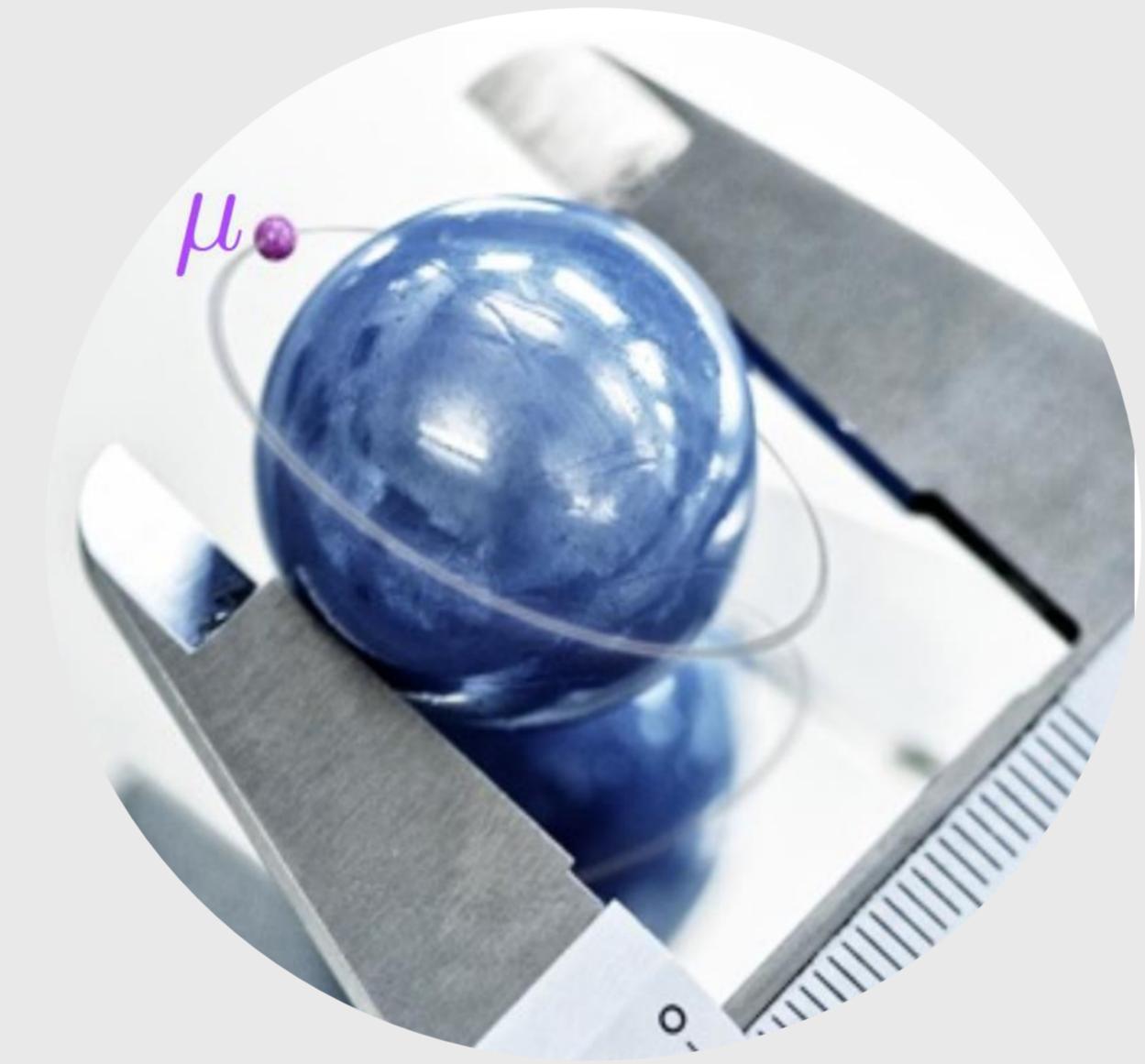
XVII Iberian Joint Meeting on Atomic and  
Molecular Physics



# Outline

	CREMA Charge Radius Experiments with Muonic Atoms
	Past $\mu\text{H}$ Lamb shift
	Present $\mu\text{He}$ Lamb shift
	Future $\mu\text{H}$ hyperfine structure



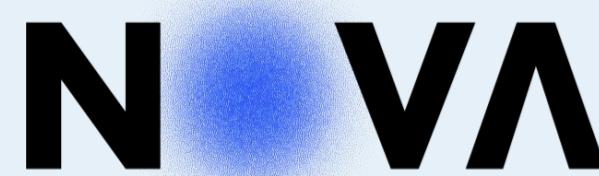


# CREMA Collaboration

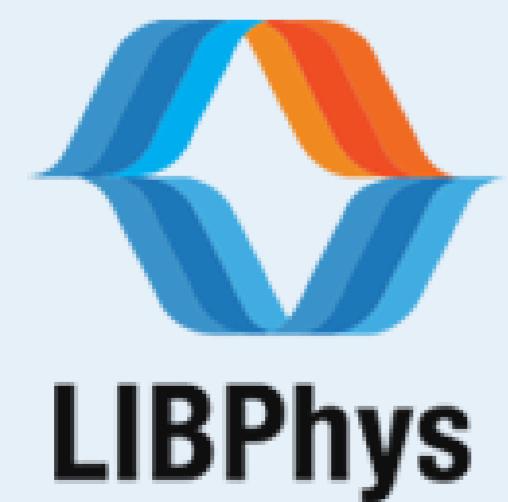
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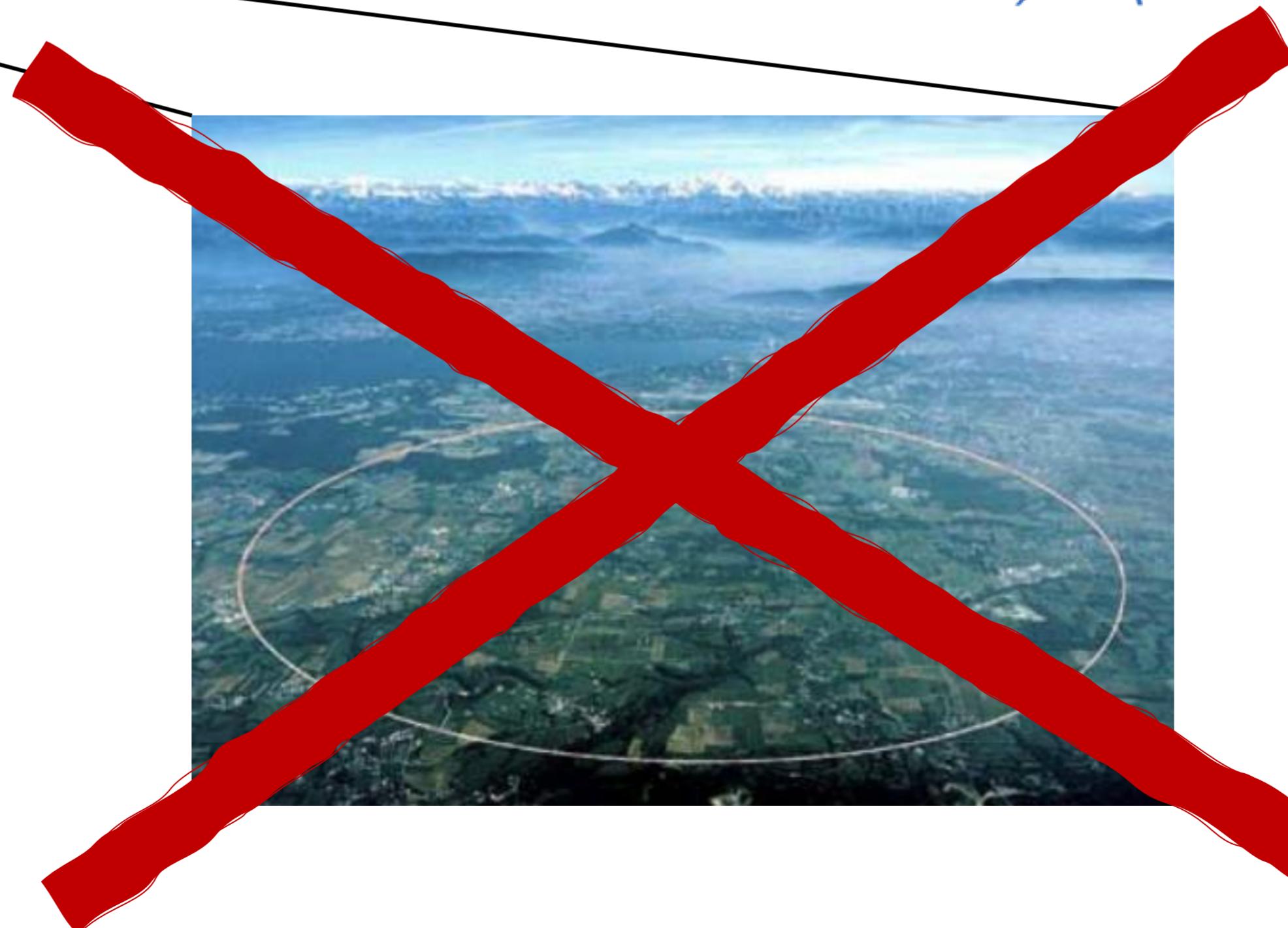
## IFJ

A. Adamczak

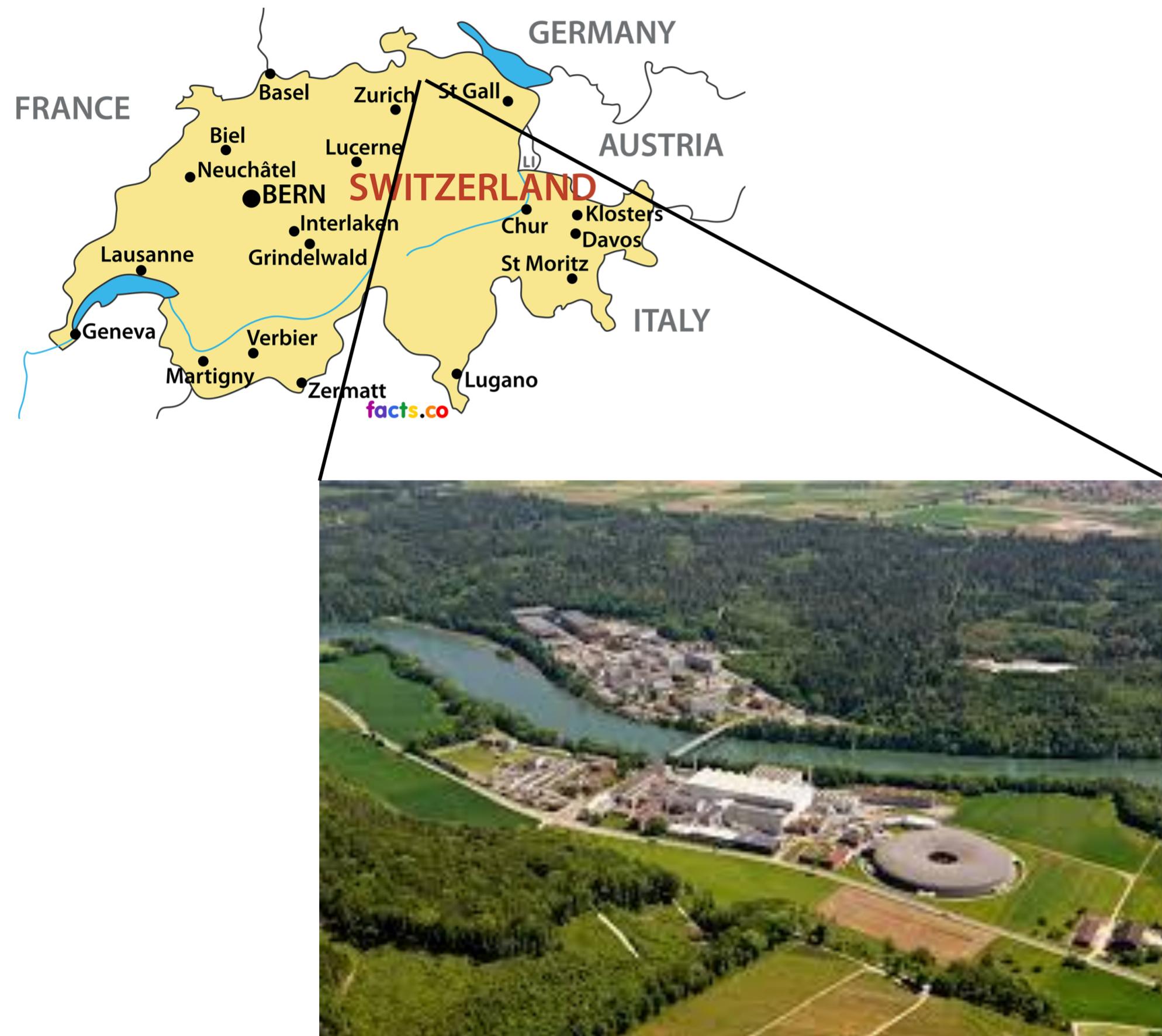


# CREMA COLLABORATION

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# CREMA COLLABORATION

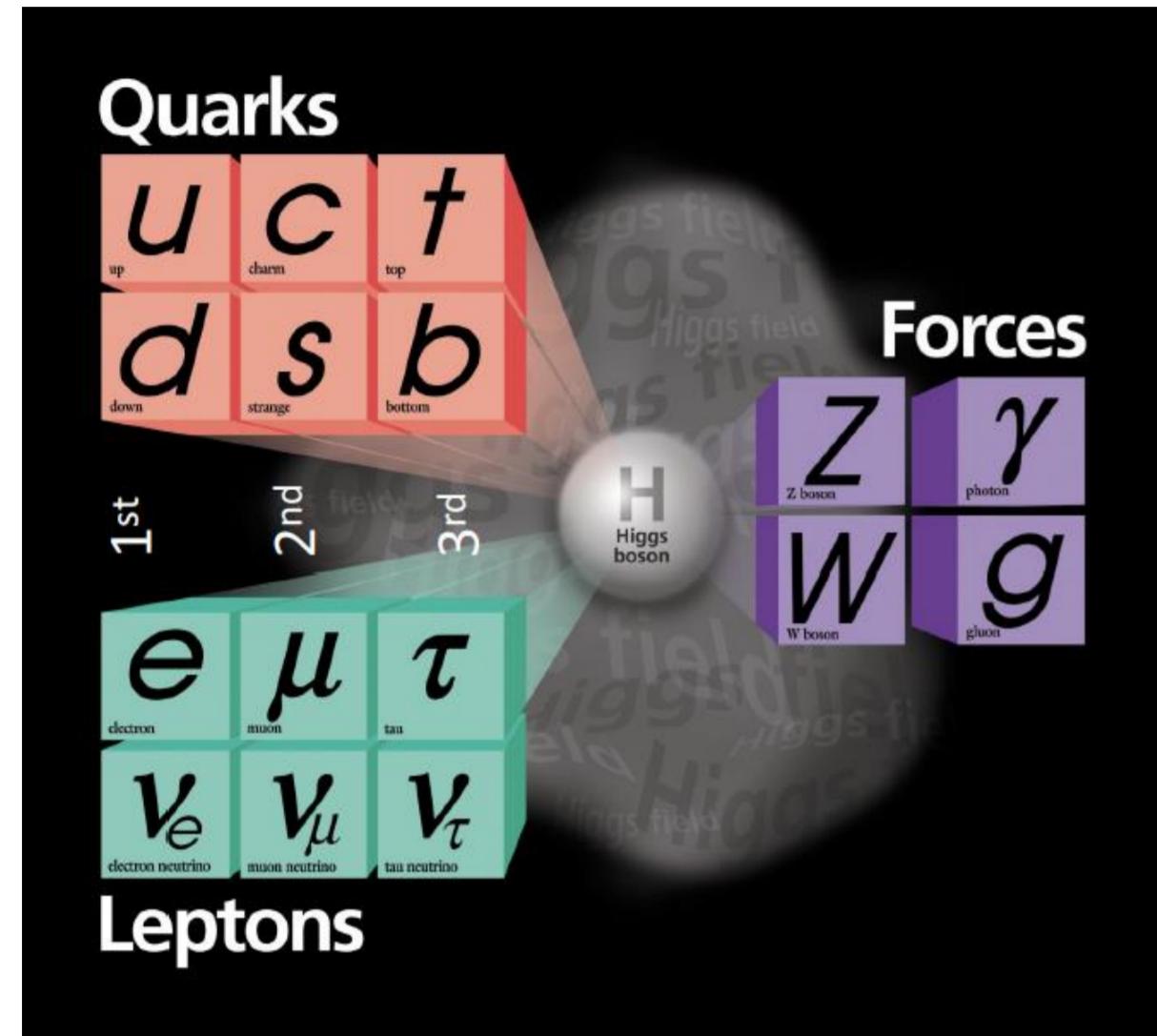


PAUL SCHERRER INSTITUT  
**PSI**



World's highest intensities of:  
Mesons:  $\pi^+$ ,  $\pi^-$ ,  $\pi^0$   
Leptons:  $\mu^+$ ,  $\mu^-$

# MUONIC ATOMS



$$r_\mu \approx \frac{r_e}{200}$$

$$V_\mu (\text{inside the proton}) \approx 200^3 V_e$$

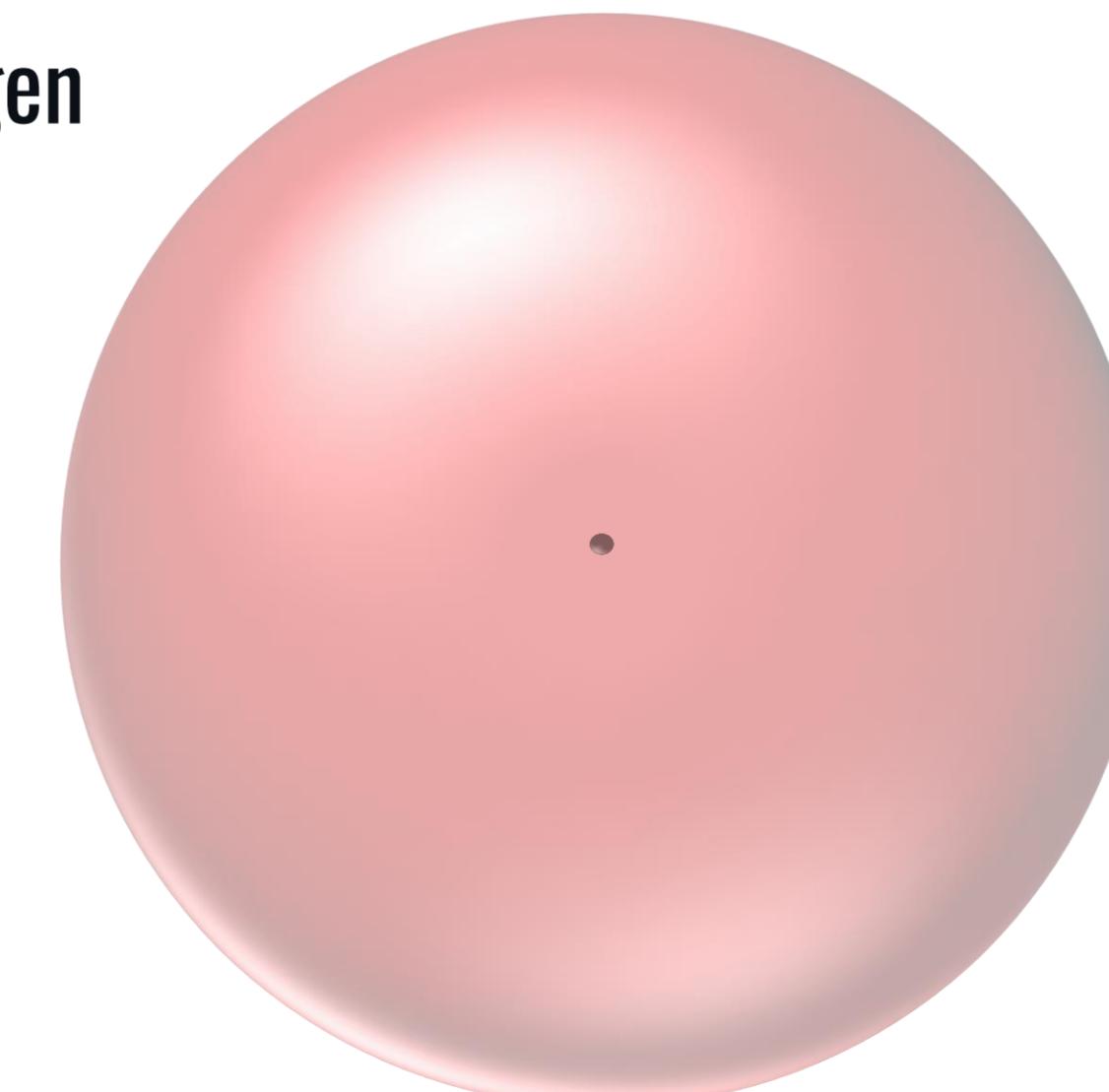
- **Muon**
  - heavy “cousin” of the electron:

$$m_\mu \approx 200 m_e$$

- short lifetime

$$\tau_\mu = 2.2 \mu\text{s}$$

hydrogen

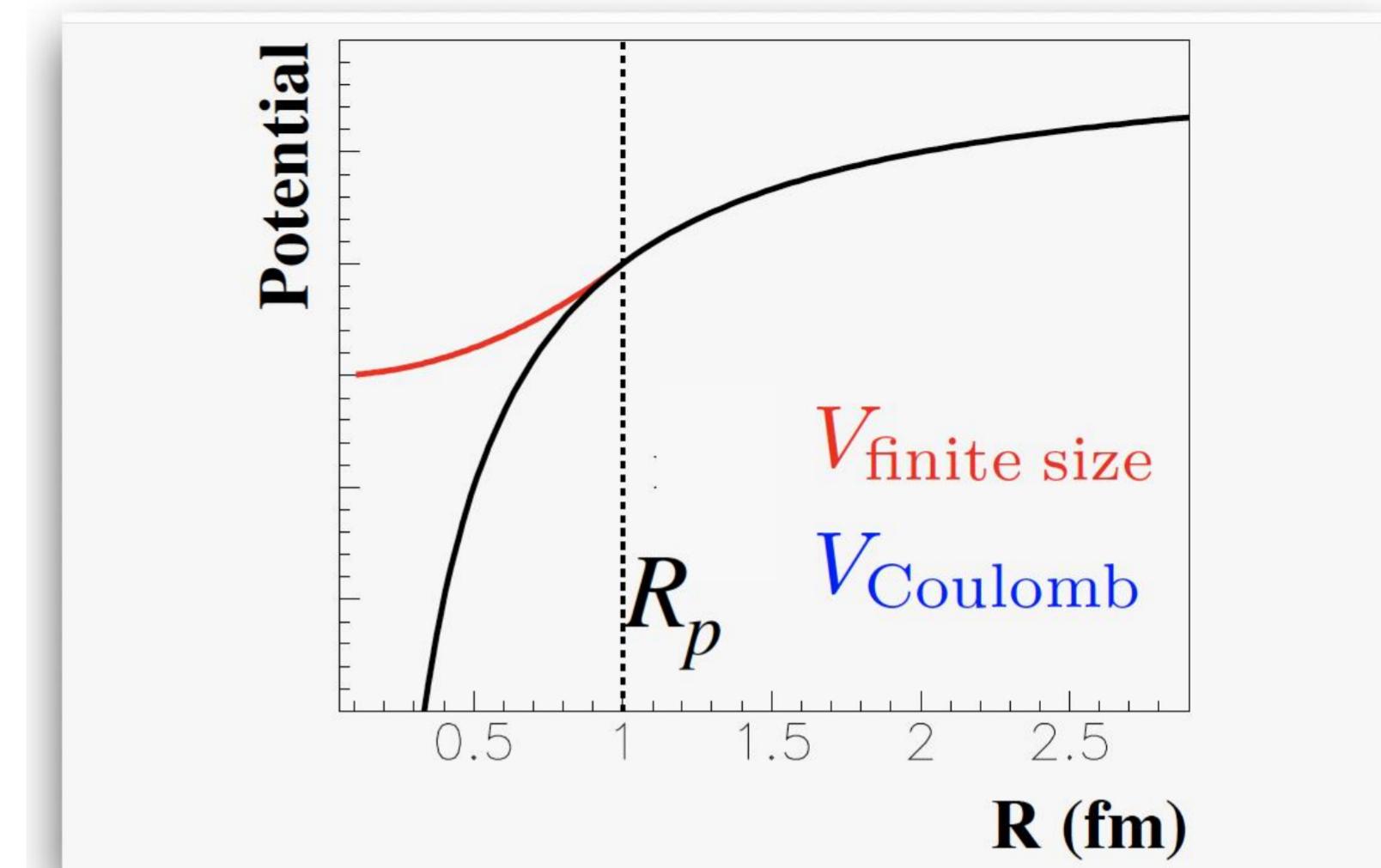
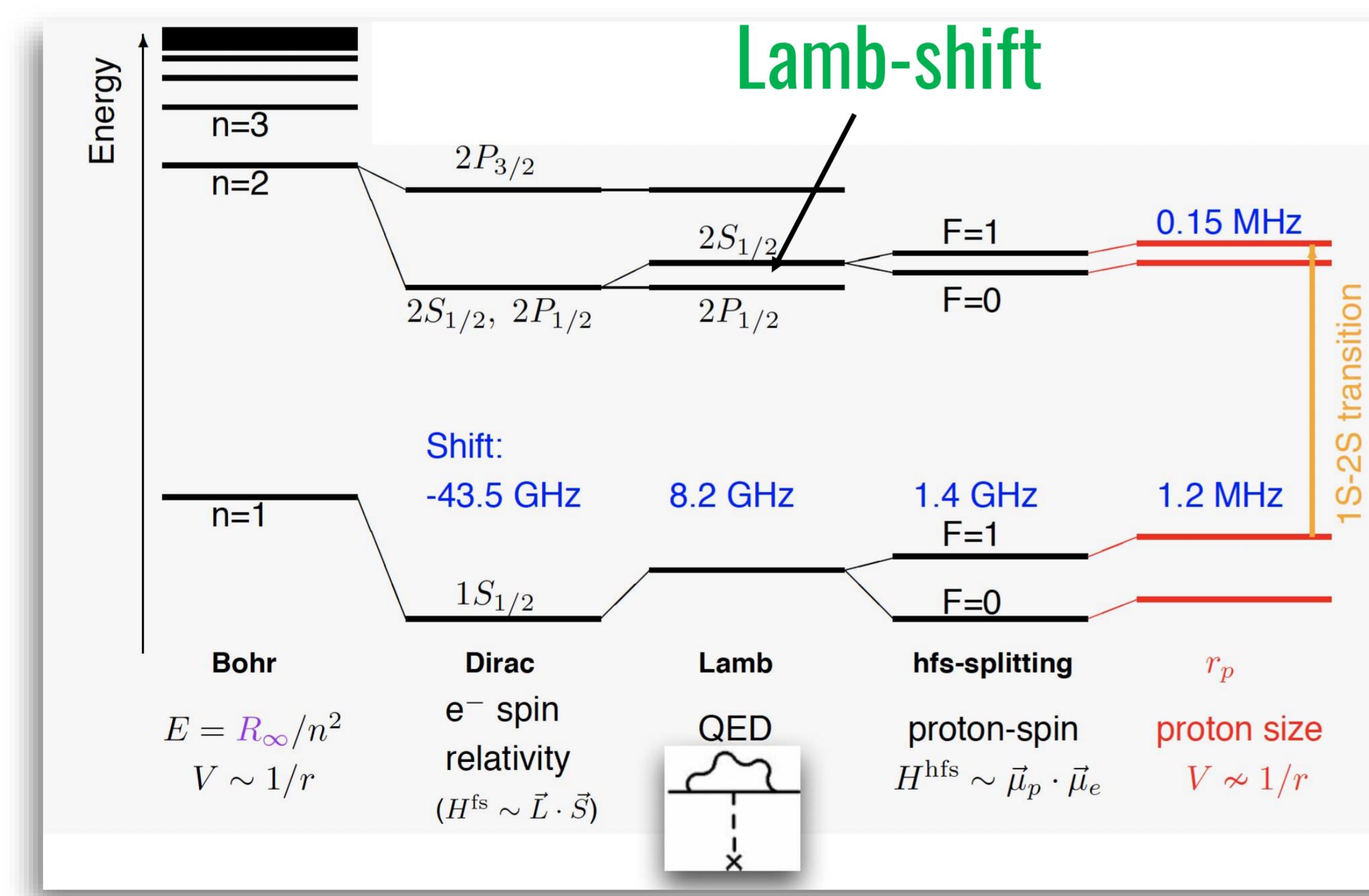


Muonic hydrogen



# MUONIC ATOMS

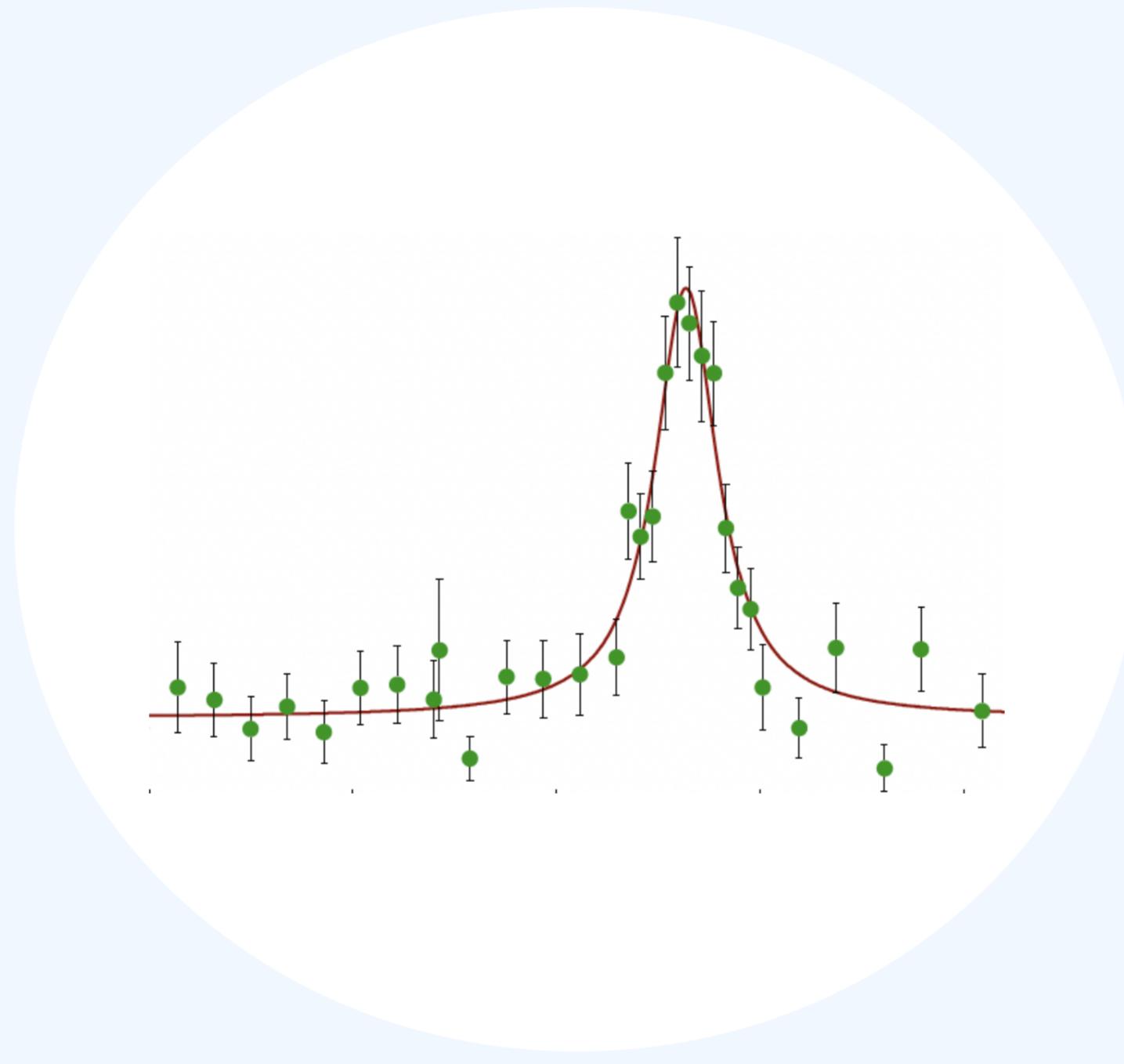
## Hydrogen energy levels



$$\Delta E_{\text{size}} = \langle \bar{\Psi} | V_{\text{Coulomb}} - V_{\text{finite size}} | \Psi \rangle$$

$$\Delta E_{\text{size}} = \langle \bar{\Psi}(r) | \Delta V(r) | \Psi(r) \rangle$$

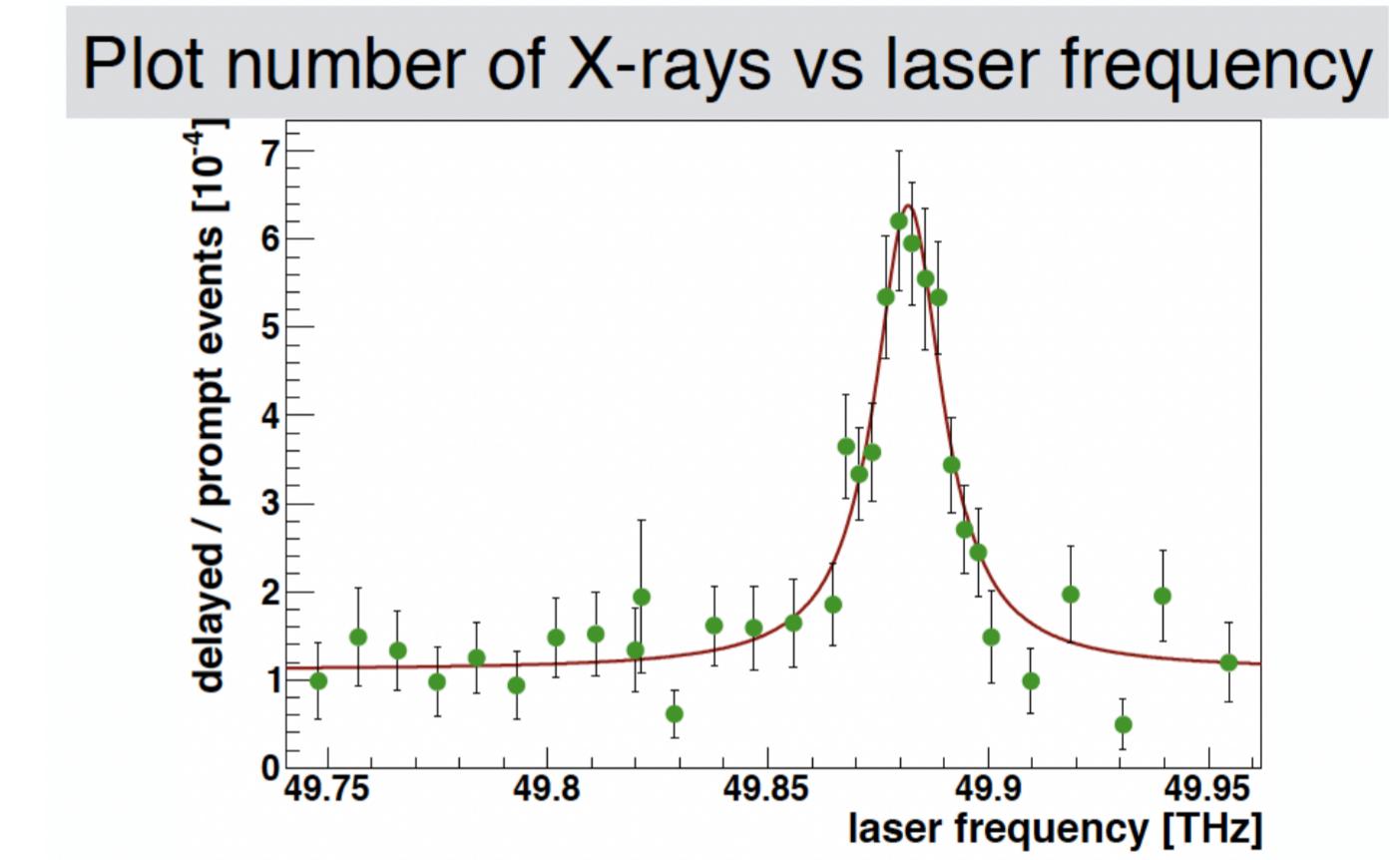
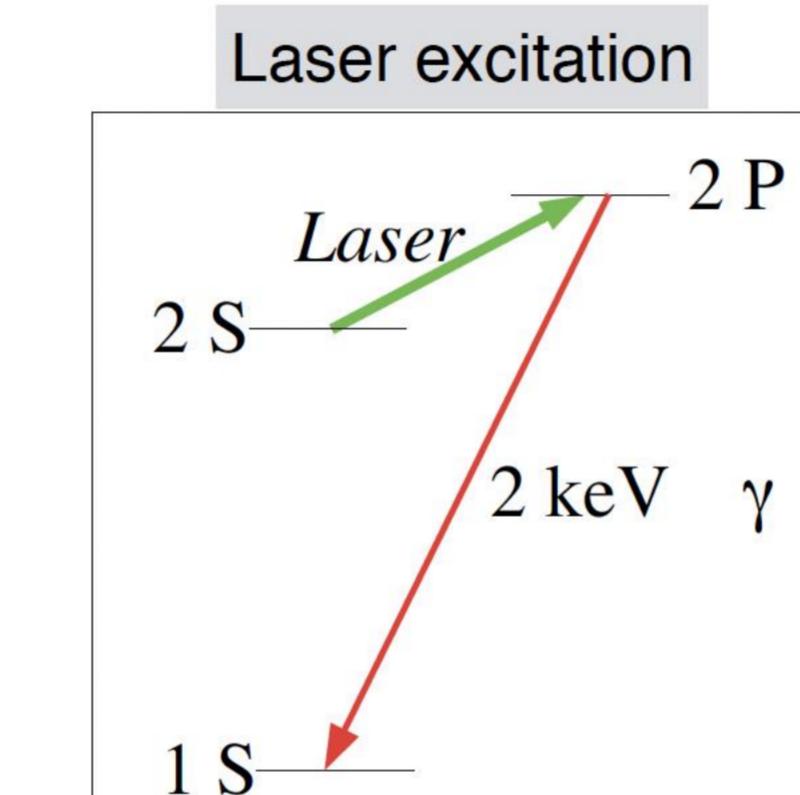
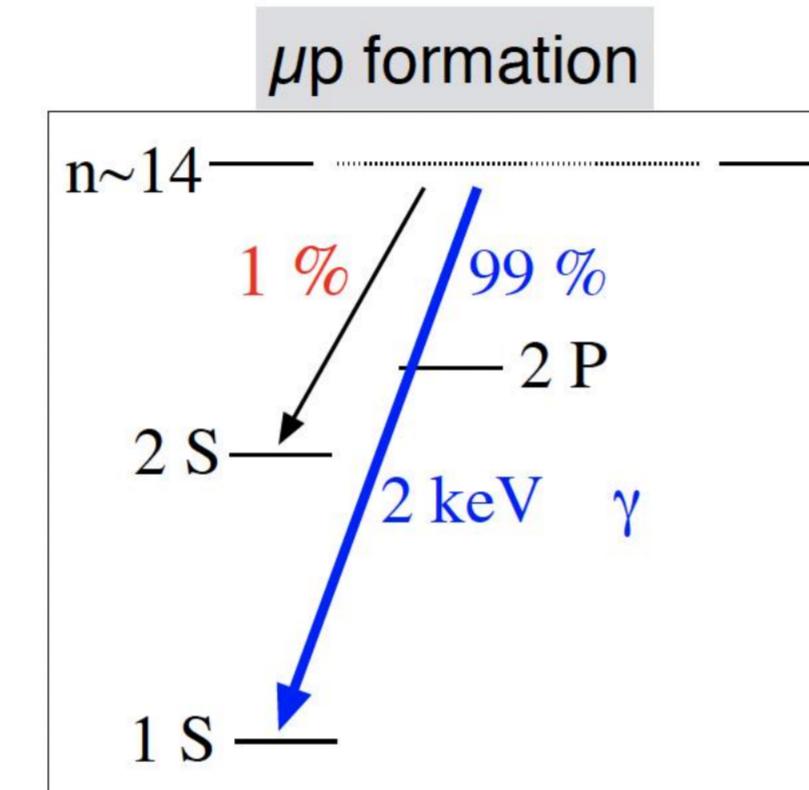
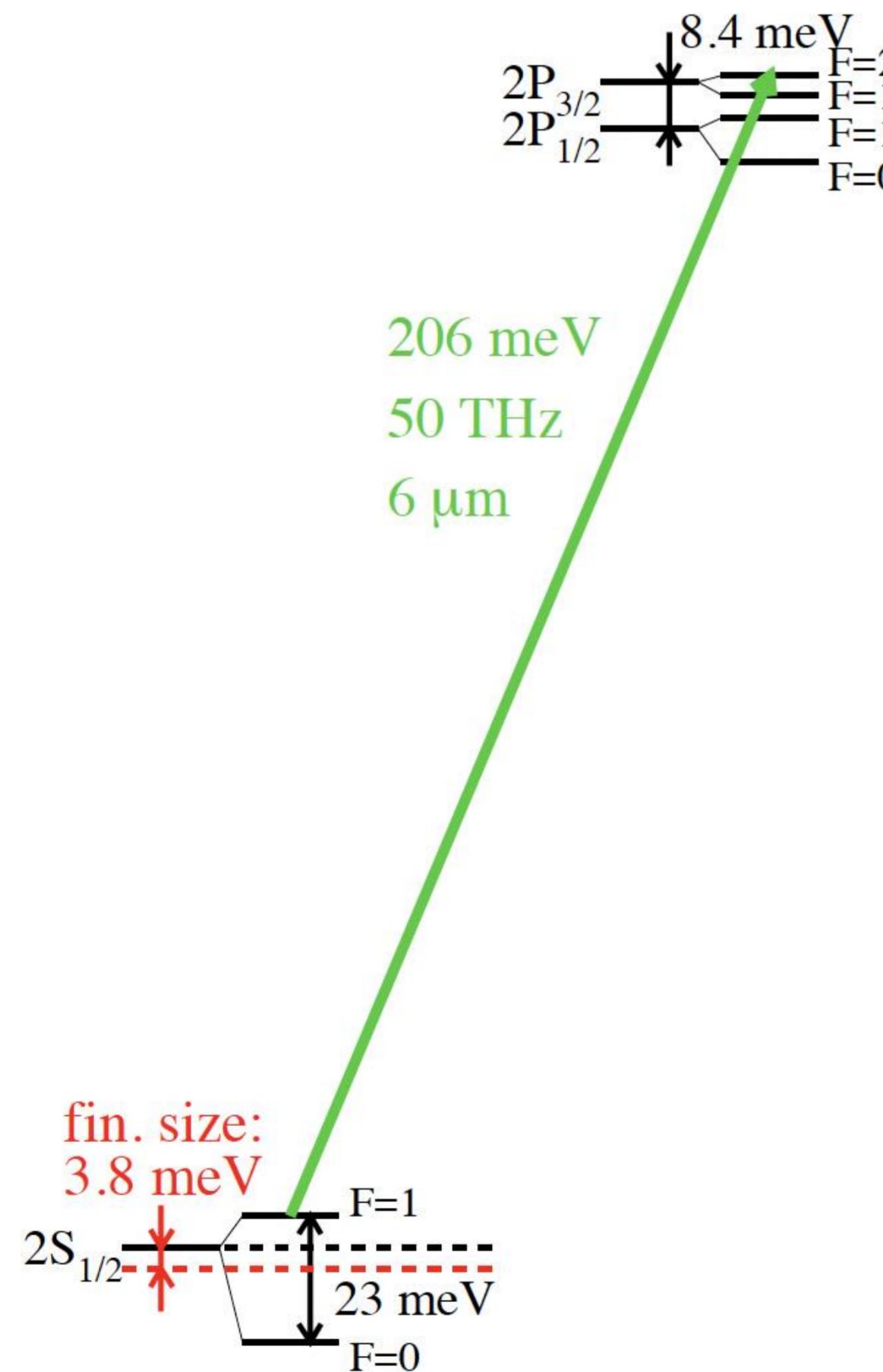
$$\begin{aligned}\Delta E_{\text{size}} &= \frac{2\pi(Z\alpha)}{3} R_p^2 |\Psi_{nl}(0)|^2 \\ &= \frac{2(Z\alpha)^4}{3n^3} m_r^3 R_p^2 \delta_{l0}\end{aligned}$$



$\mu\text{H}$  Lamb shift

# Extracting the proton radius

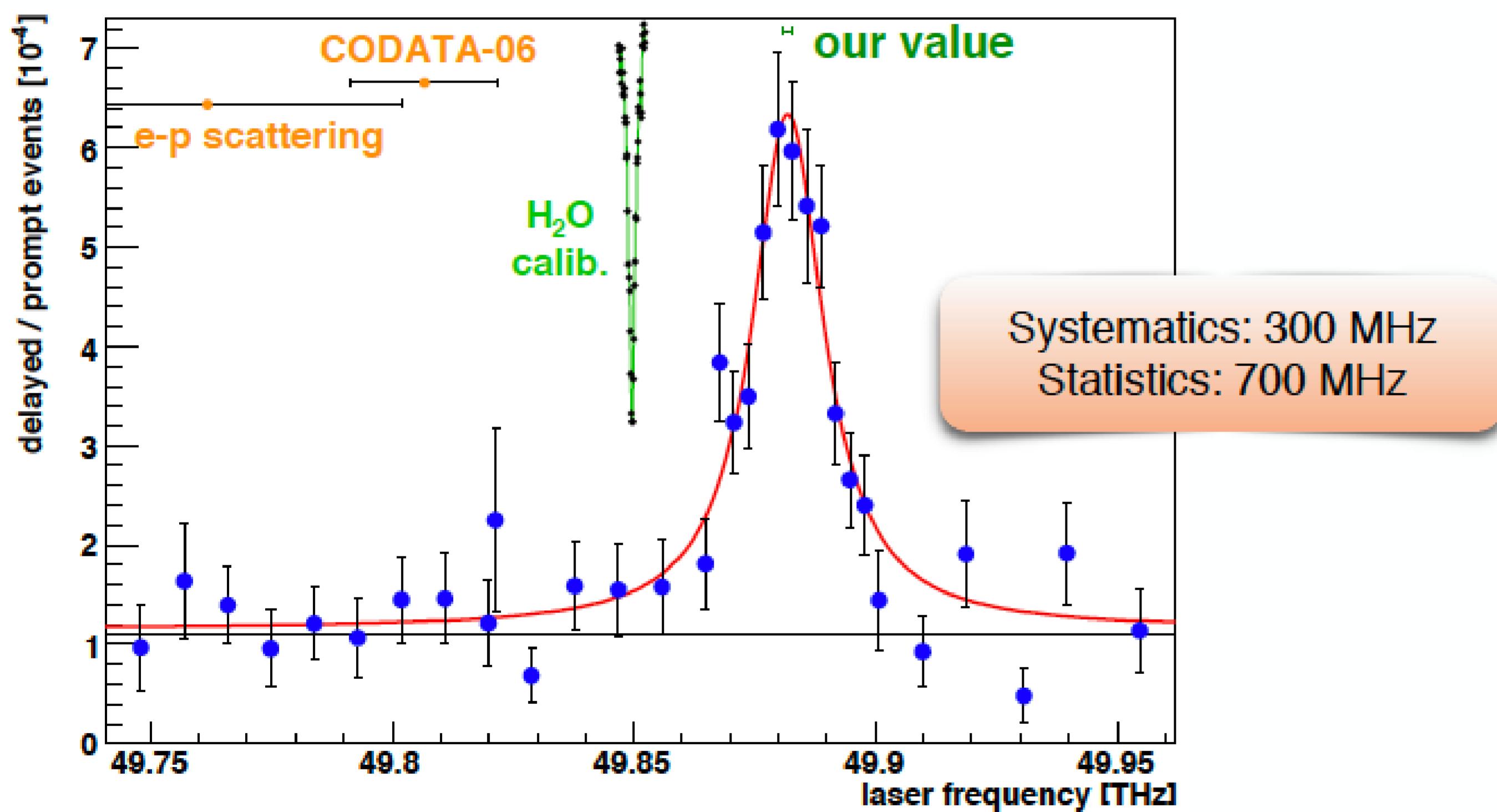
## Lamb-shift (2s-2p)



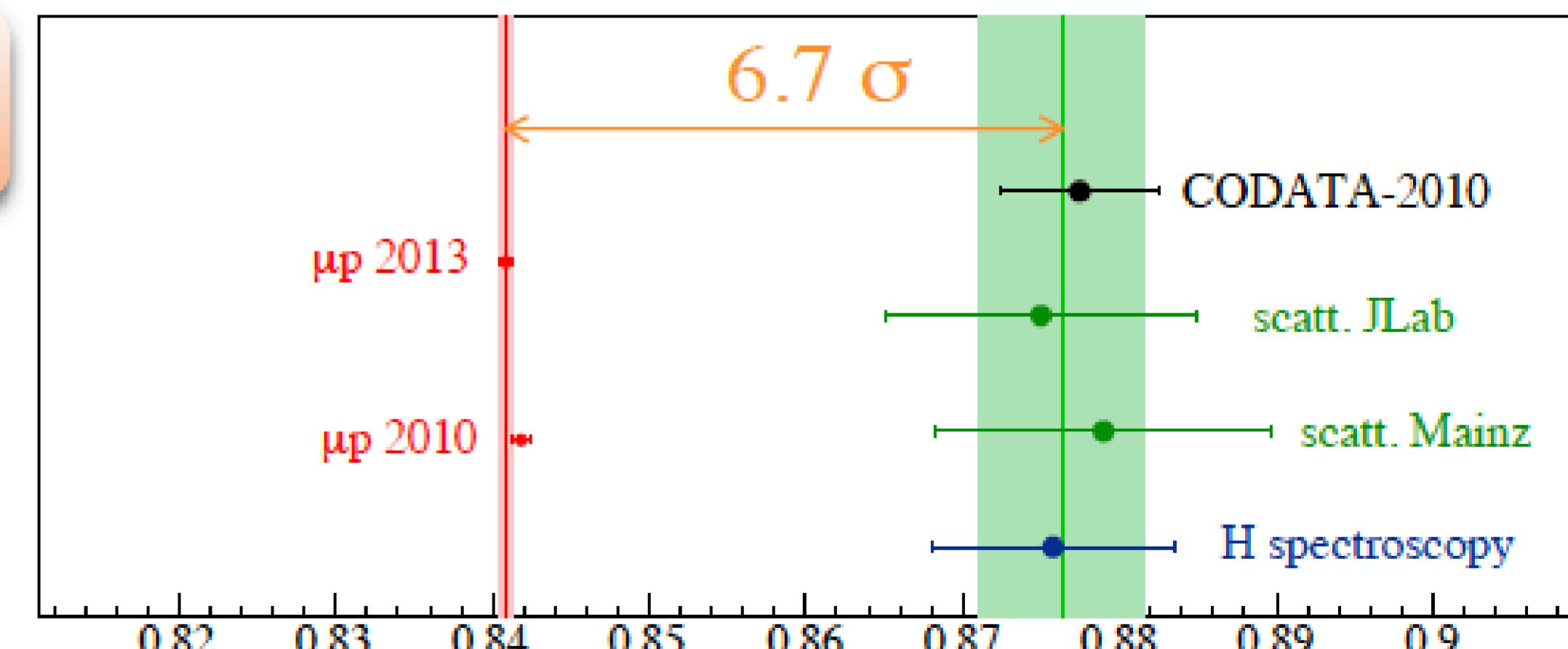
$$\Delta E_{2P-2S}^{\text{th}} = 206.0336(15) - 5.2275(10) R_p^2 + 0.0332(20) \text{ [meV]}$$

# Proton radius extracted

- Charge radius with **0.1%** uncertainty
- **10x** more accurate than the average of all combined measurements
- Yet was  **$6.7\sigma$**  smaller than recommended value



Pohl et al., Nature 466, 213 2010



Pohl et al., Nature 466, 213 2010  
Antognini et al., Science 339, 417 2013

# Proton radius puzzle

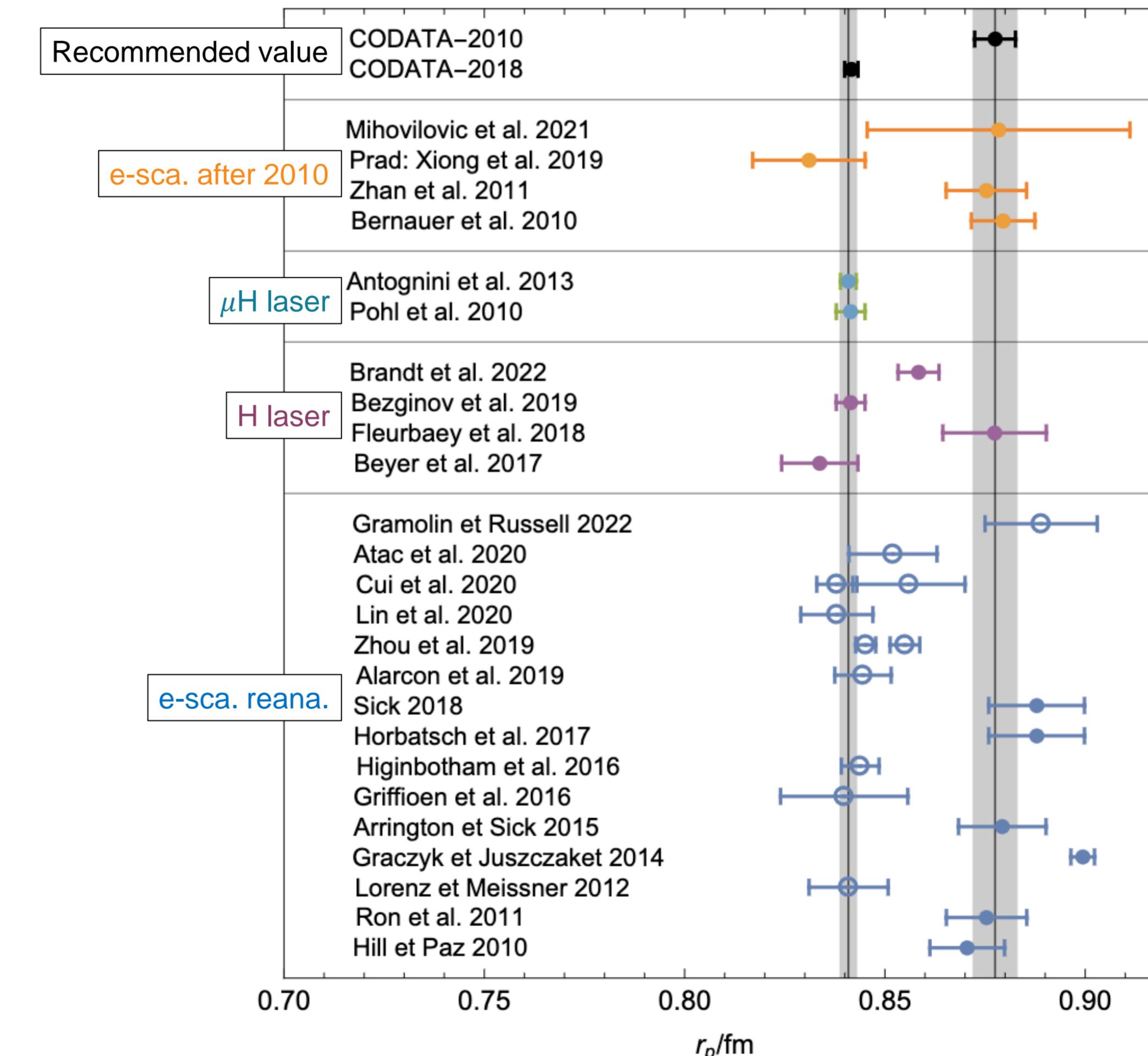
$$E_{2P-2S}^{\text{exp}} = E_{2P-2S}^{\text{th}}$$

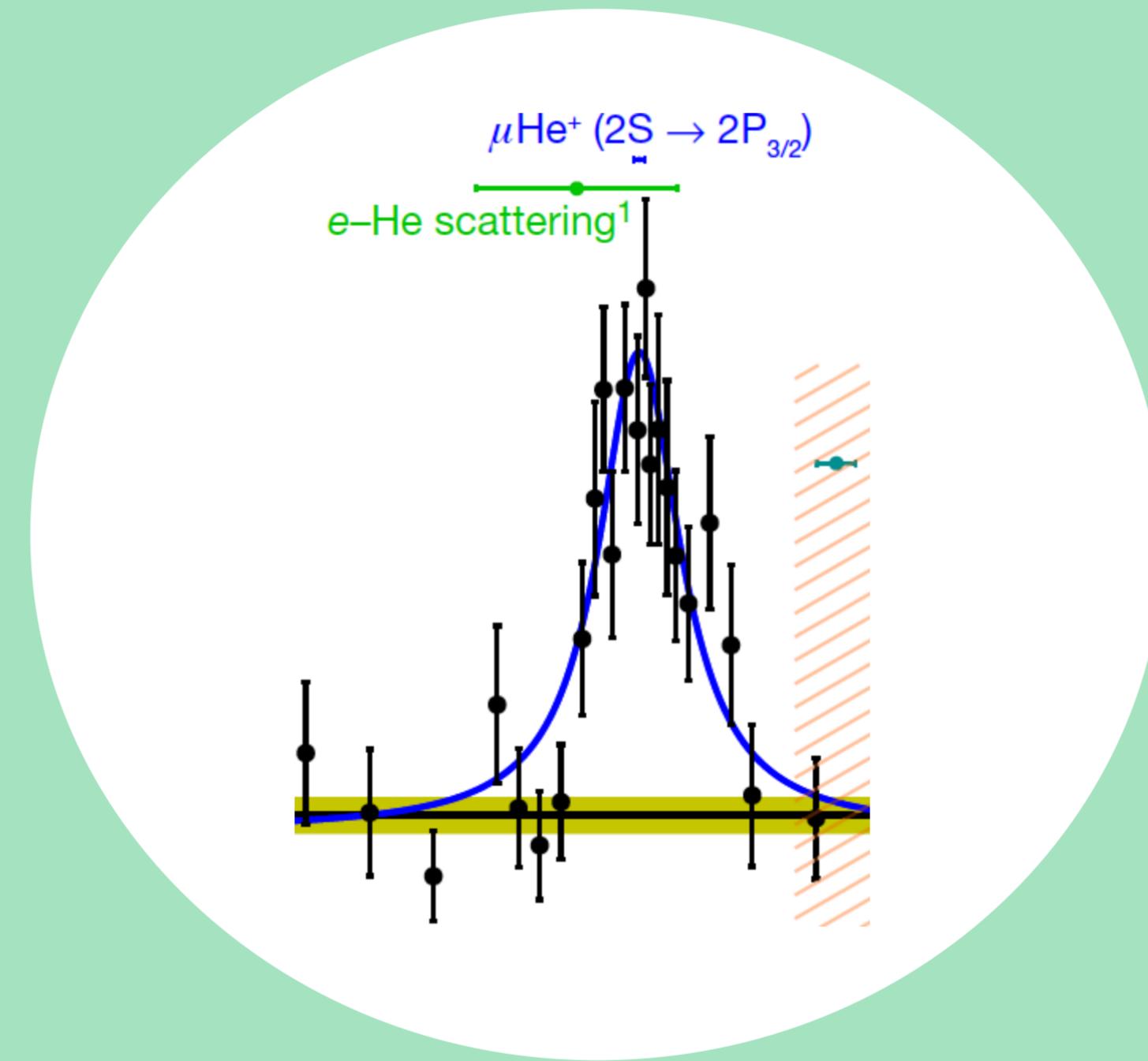
$$E_{2P-2S}^{\text{exp}} = \text{QED} + \text{TPE} + kR_p^2$$

↑ measure  
know (calculated)  
extract

- Experiment is **wrong?**
- QED prediction is **wrong?**
- Proton structure **not well understood?**
- The radii as determined from other experiments are **wrong?**
- other?

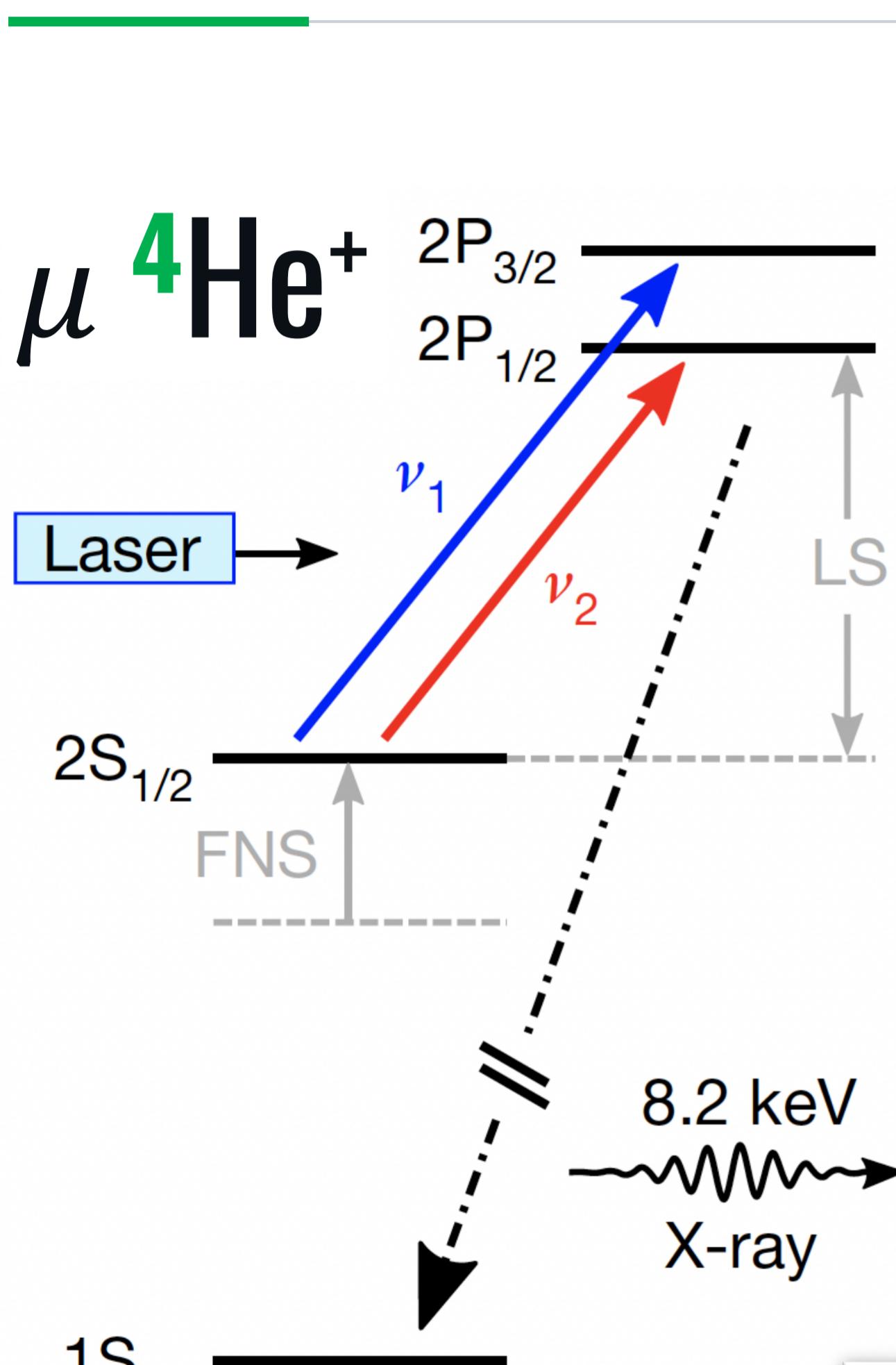
Antognini, Annual Reviews, 2022  
Walcher, ArXiv 2304.07035, 2023





## $\mu$ He Lamb shift

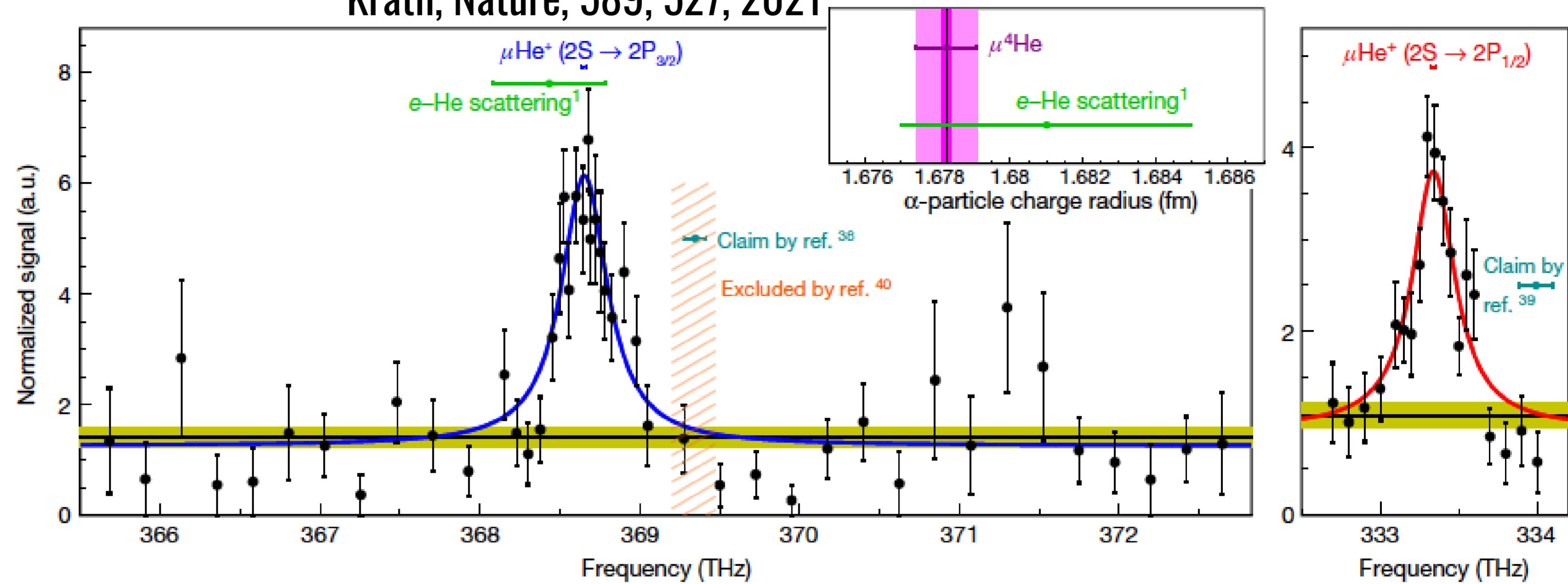
# Alpha radius extracted



alpha particle radius

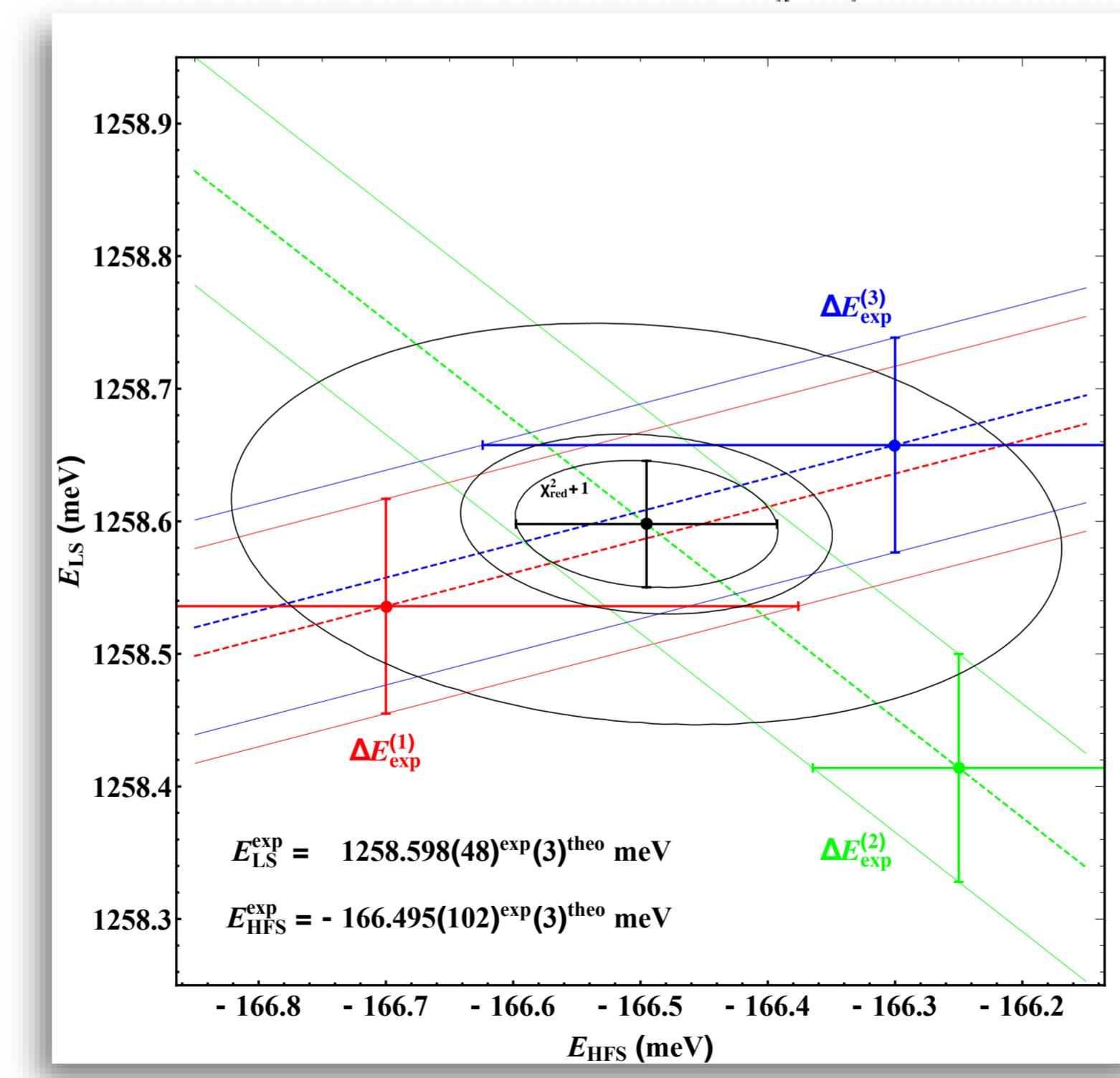
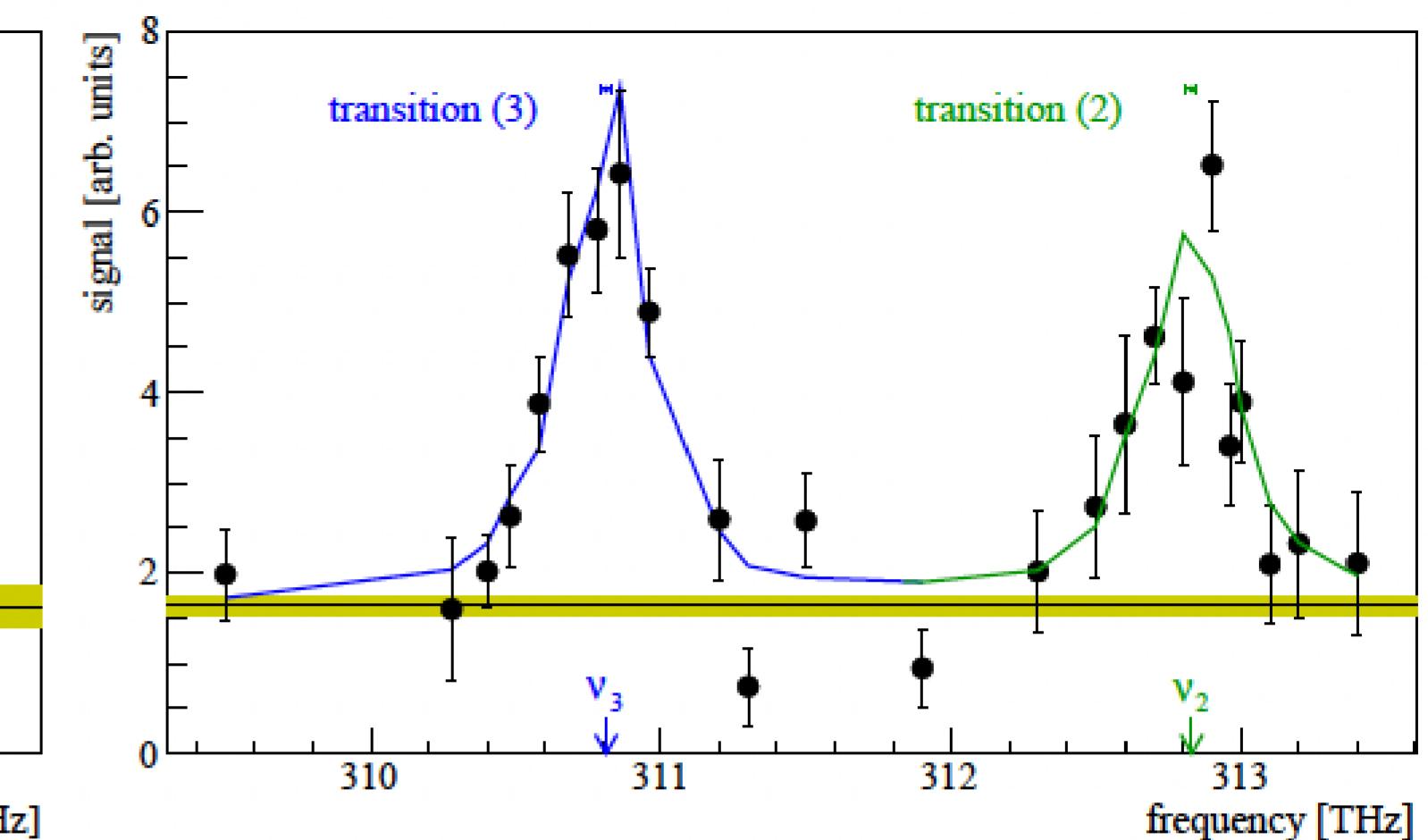
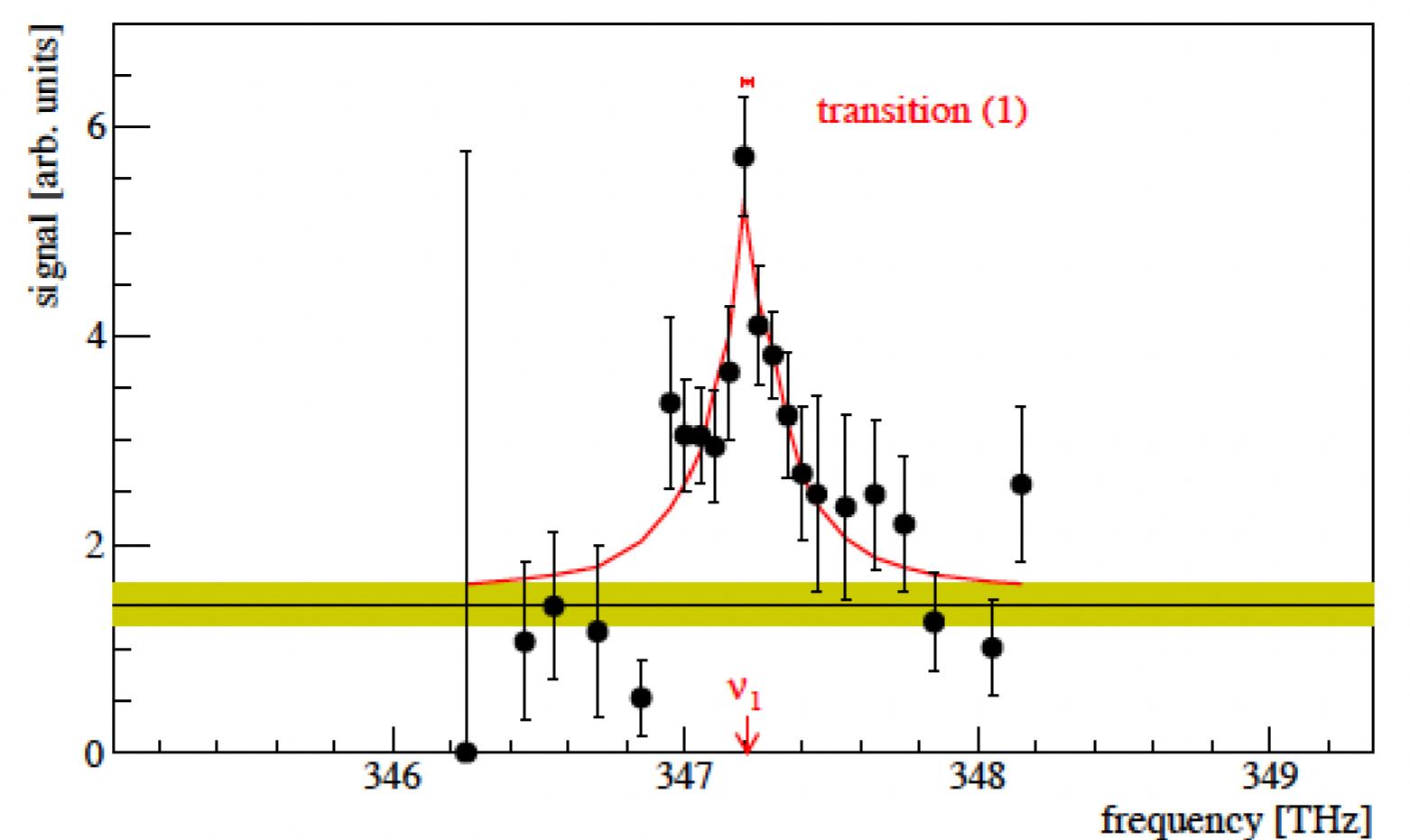
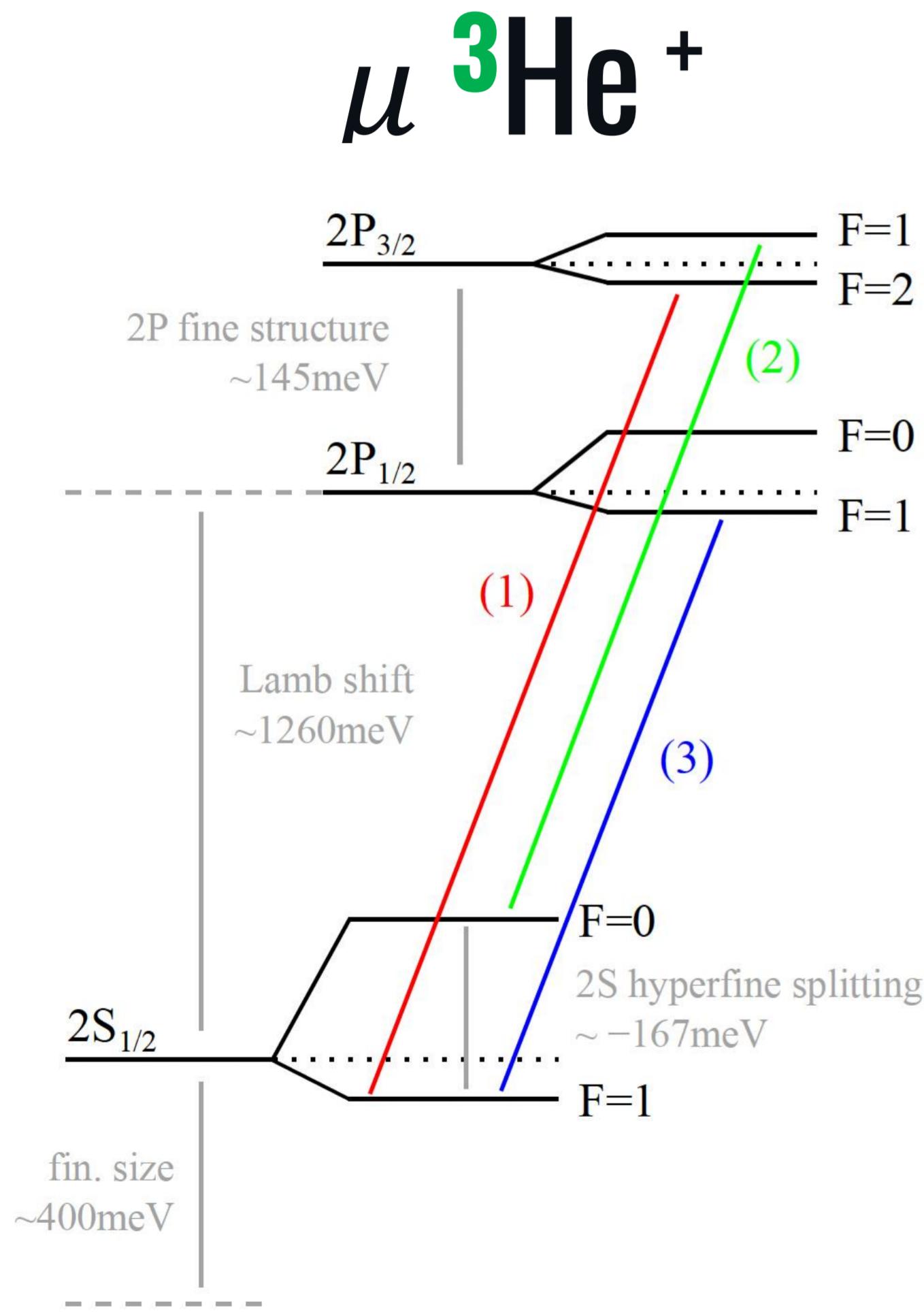
$$r_\alpha = 1.67824(13)_{\text{exp}} (82)_{\text{theo}} \text{ fm}$$

Krath, Nature, 589, 527, 2021



- Most precise measurement of the alpha particle radius
- 0.05% uncertainty
- Agreement with e-He scattering but 4.8x more accurate
- Benchmark few-nucleon theories
- Bounds nuclear flavour-violating interactions

# Helion radius extracted

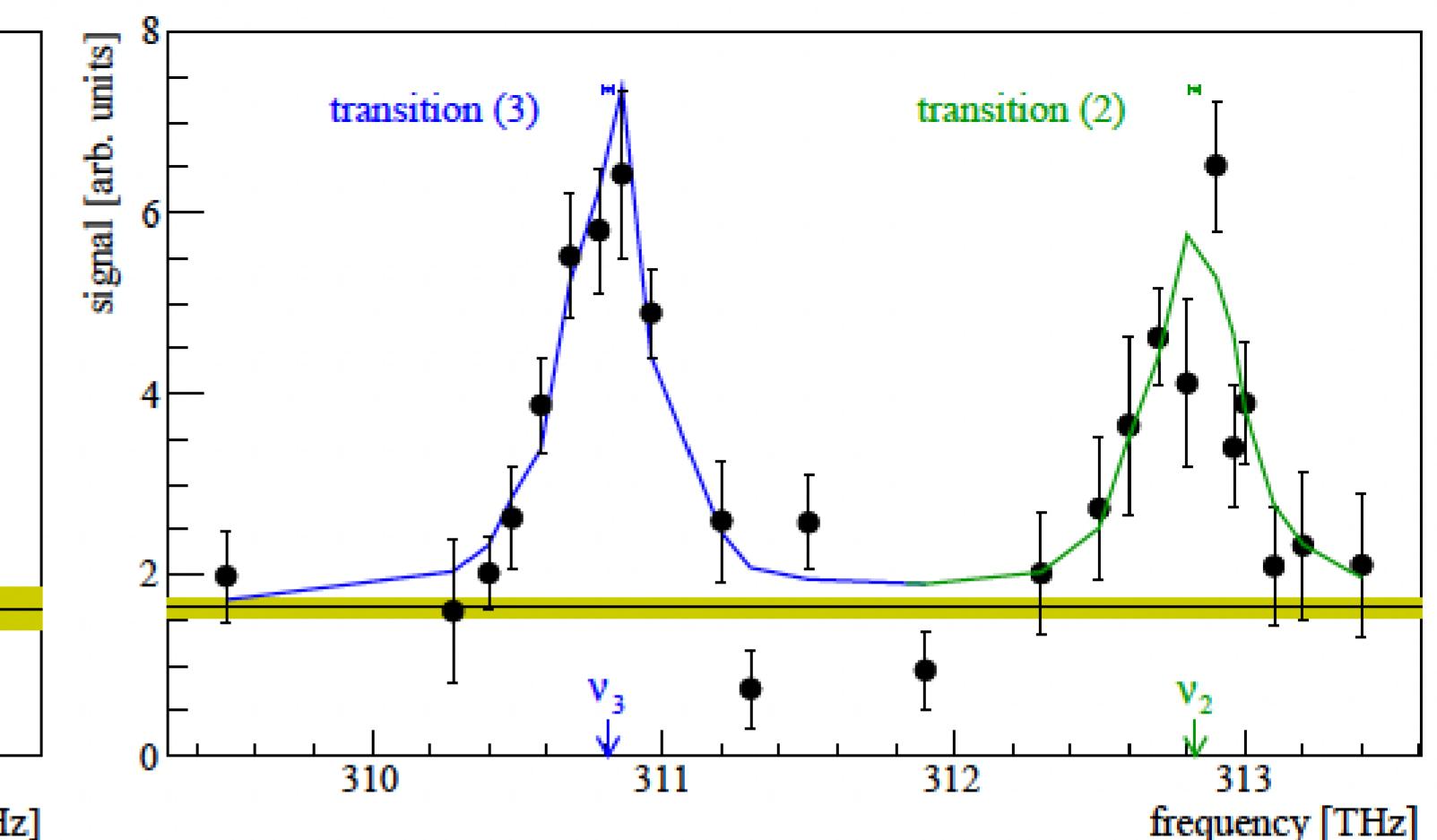
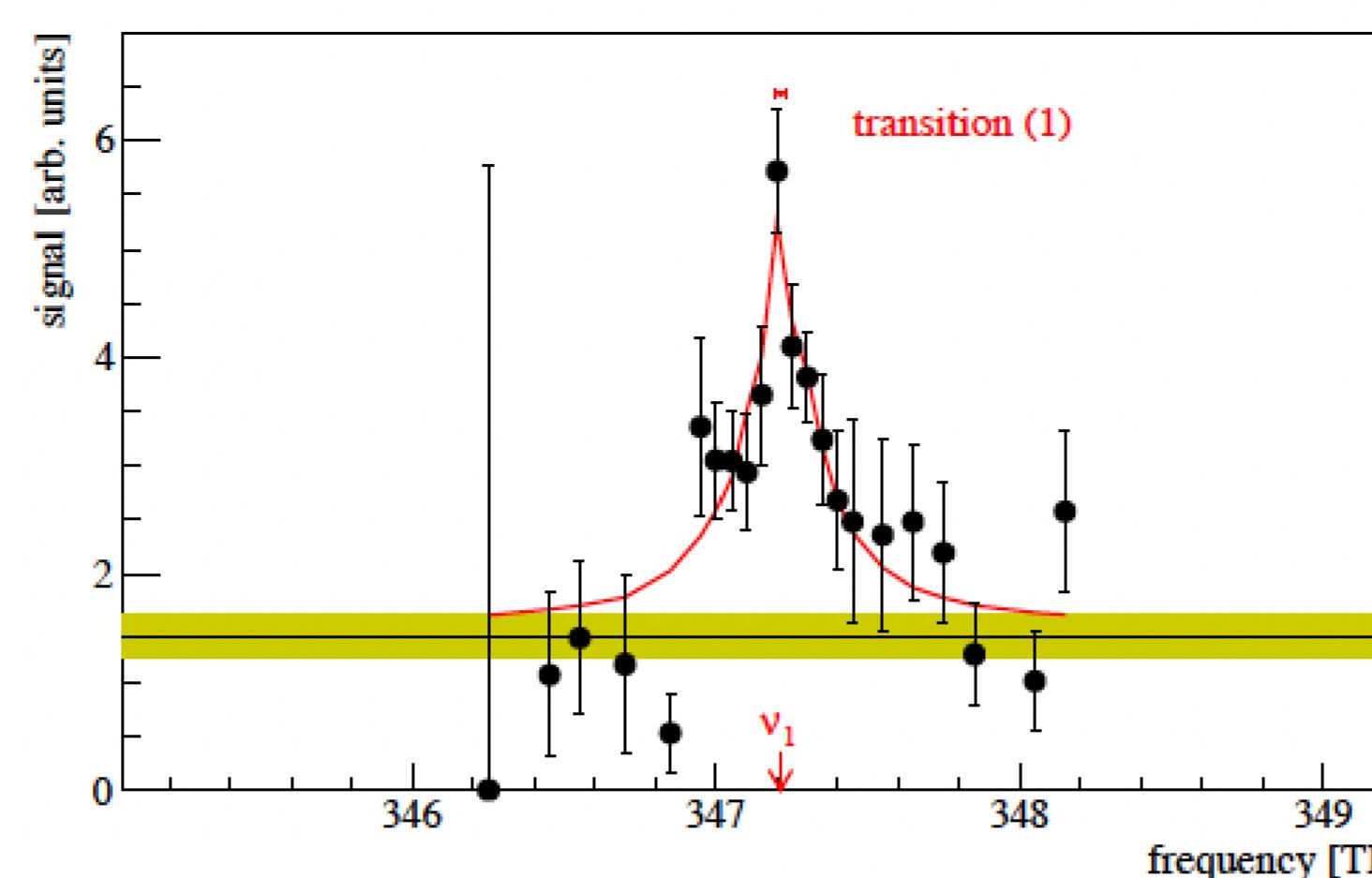
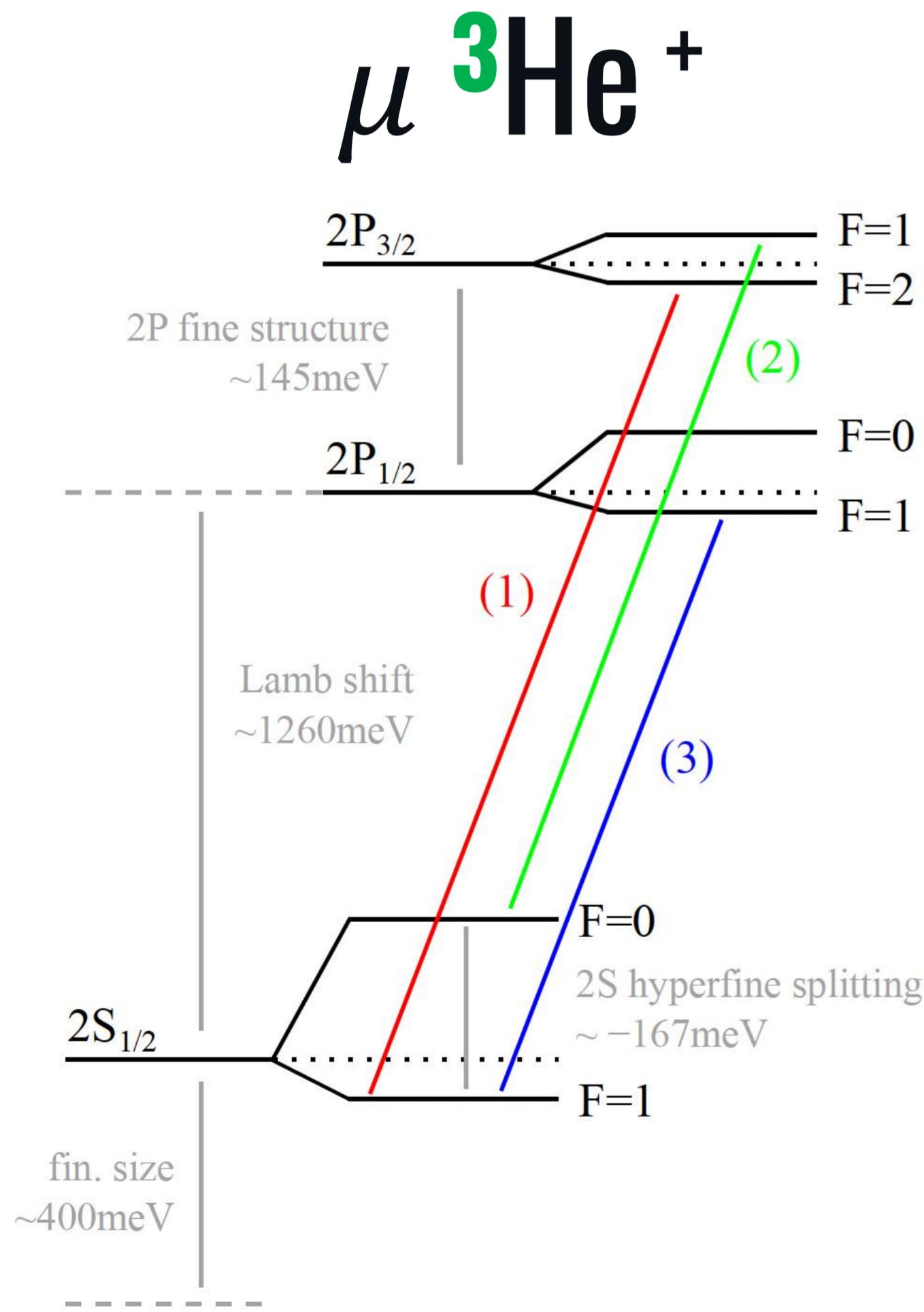


$$\nu_1 = \Delta E_{LS}^{KP} + \frac{1}{4}\beta_0 + \Delta E_{FS}^K - \frac{3}{8}HFS_{\{3/2\}}^K - \frac{3}{4}\Delta$$

$$\nu_2 = \Delta E_{LS}^{KP} - \frac{3}{4}\beta_0 + \Delta E_{FS}^K + \frac{5}{8}HFS_{\{3/2\}}^K - \frac{3}{4}\Delta$$

$$\nu_3 = \Delta E_{LS}^{KP} + \frac{1}{4}\beta_0 - \frac{1}{4}HFS_{\{1/2\}}^K - \frac{3}{4}\Delta$$

# Helion radius extracted

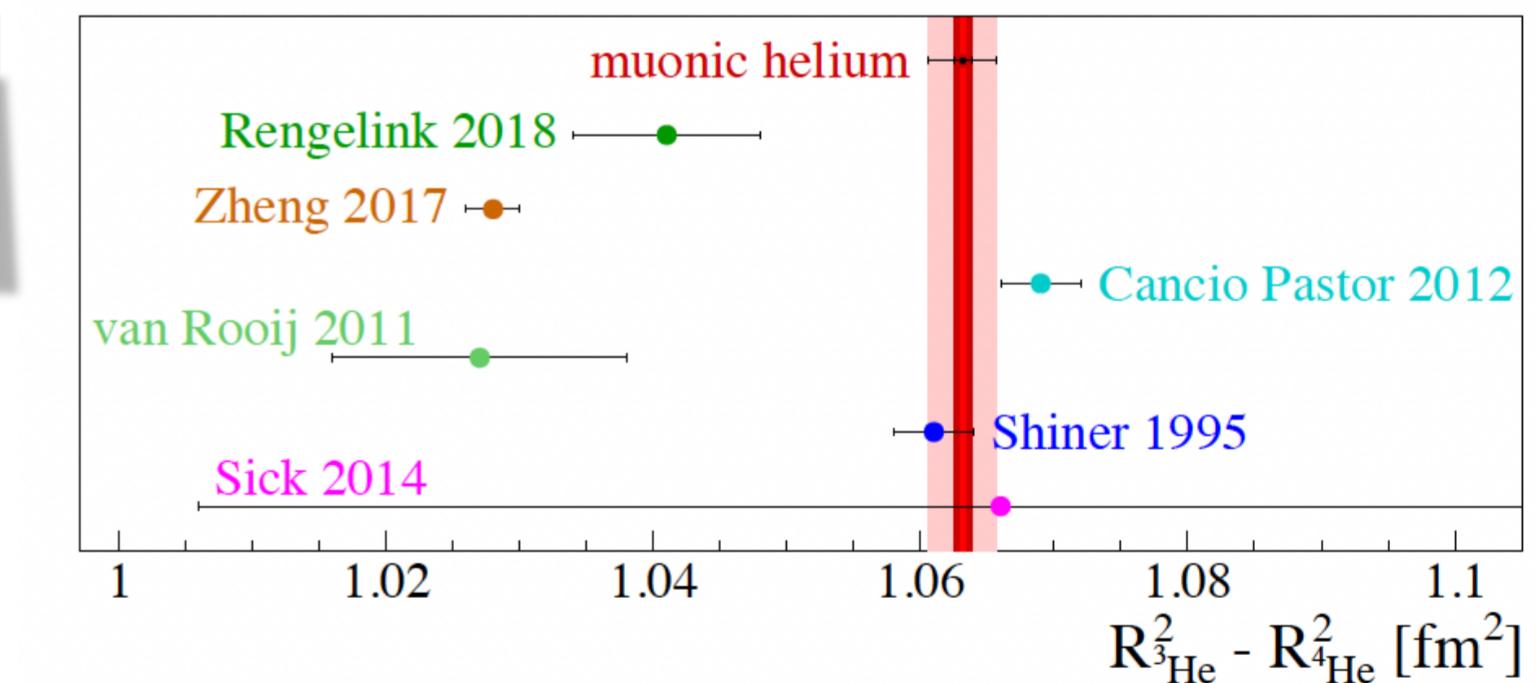
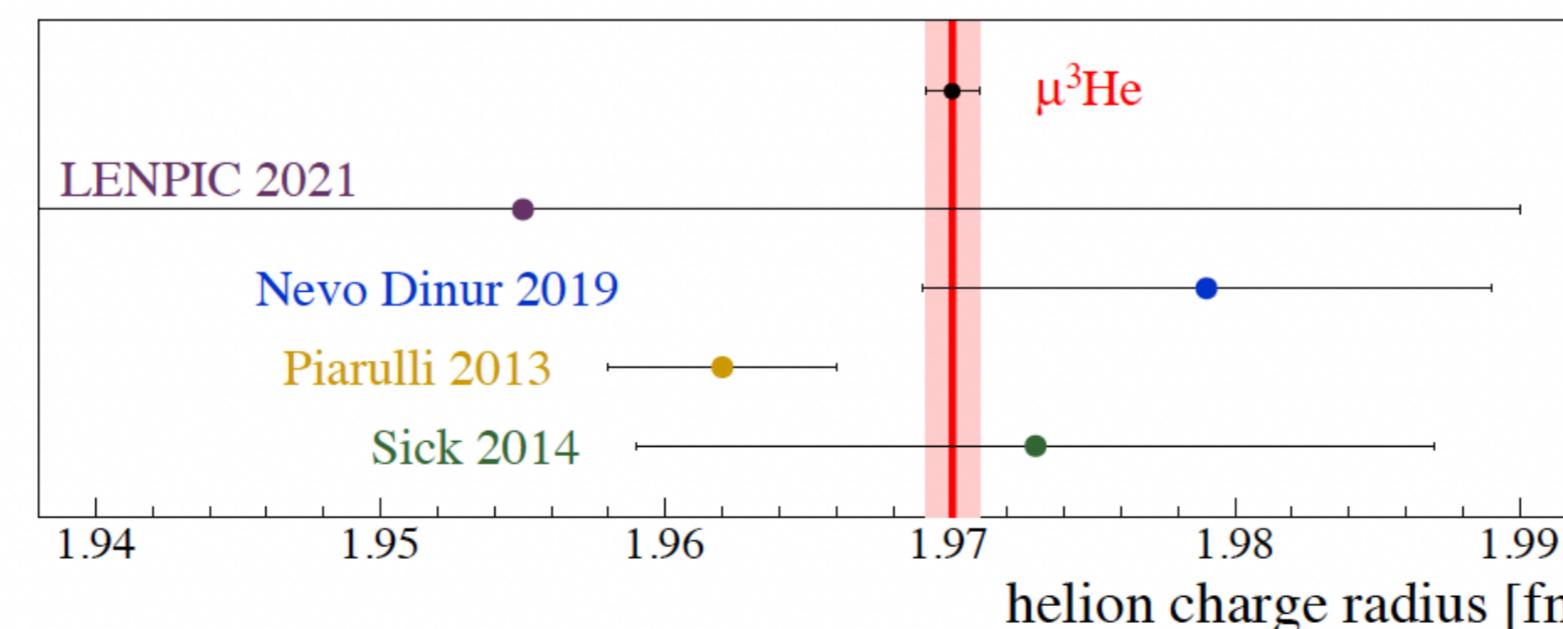


2s hyperfine

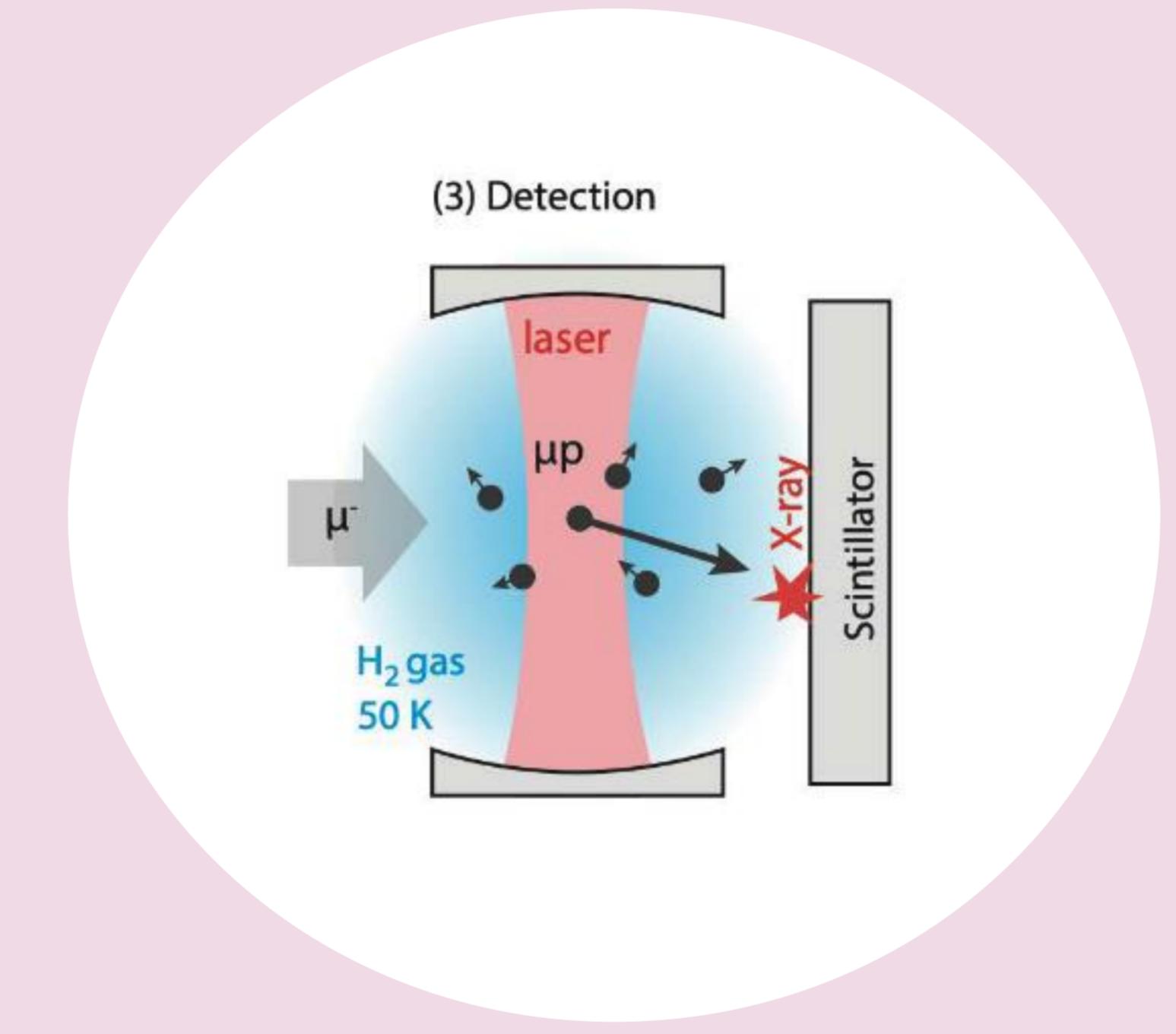
Isotopic shift

$$E_{\text{HFS}}^{\text{exp}} = -166.496(104)^{\text{exp}}(3)^{\text{theo}} \text{ meV}$$

helion radius



Schuhmann, Science, under review



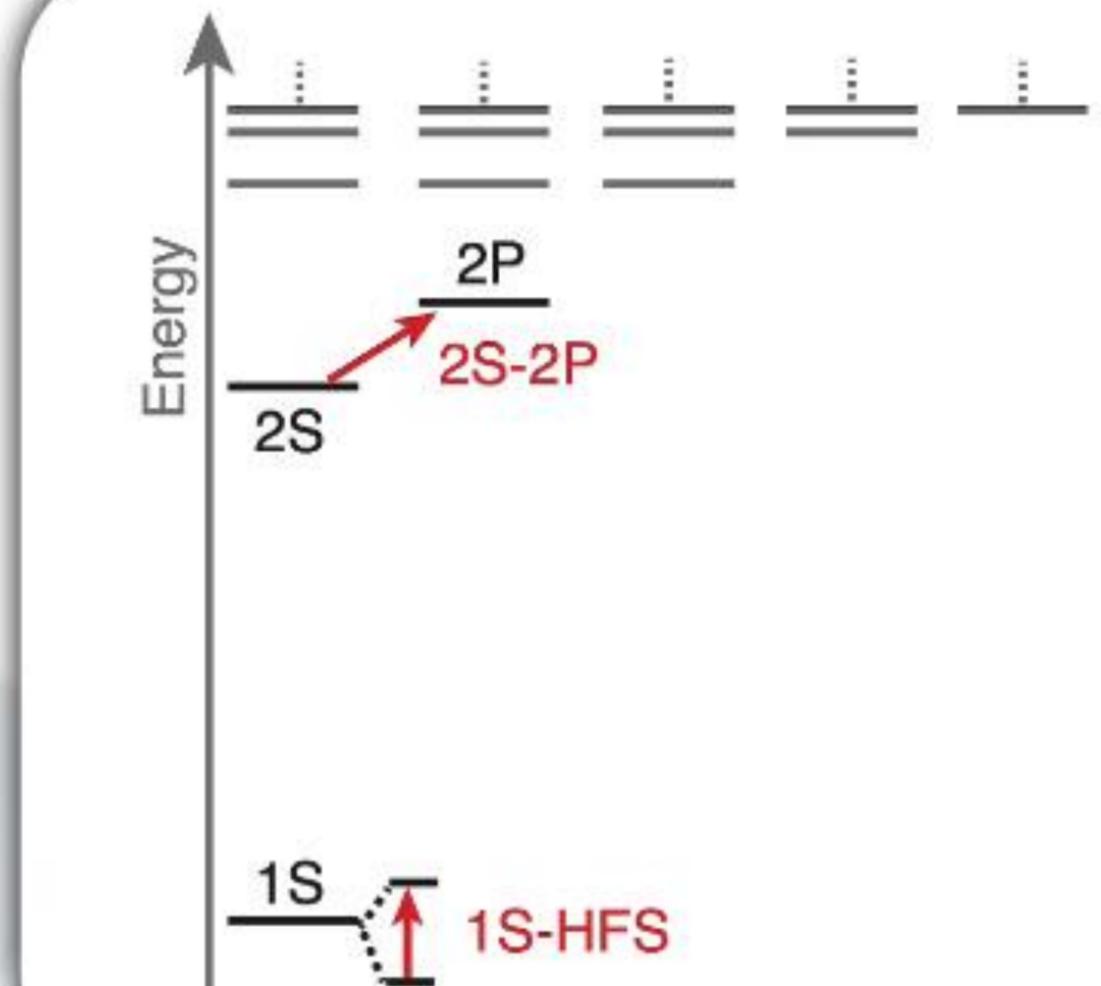
$\mu p$  hyperfine structure

# Hyperfine splitting of muonic hydrogen - HyperMu

HyperMu

Switzerland (PSI,  
ETHZ), France,  
Germany, Portugal,  
Taiwan, Poland

- From 2S-2P  
→ charge radii
- From HFS  
→ magnetic (Zemach) radii



- 2S-2P  $\mu p$
- 2S-2P  $\mu d$
- 2S-2P  $\mu^3\text{He}, \mu^4\text{He}$
- 1S-HFS  $\mu p$

# Hyperfine splitting of muonic hydrogen

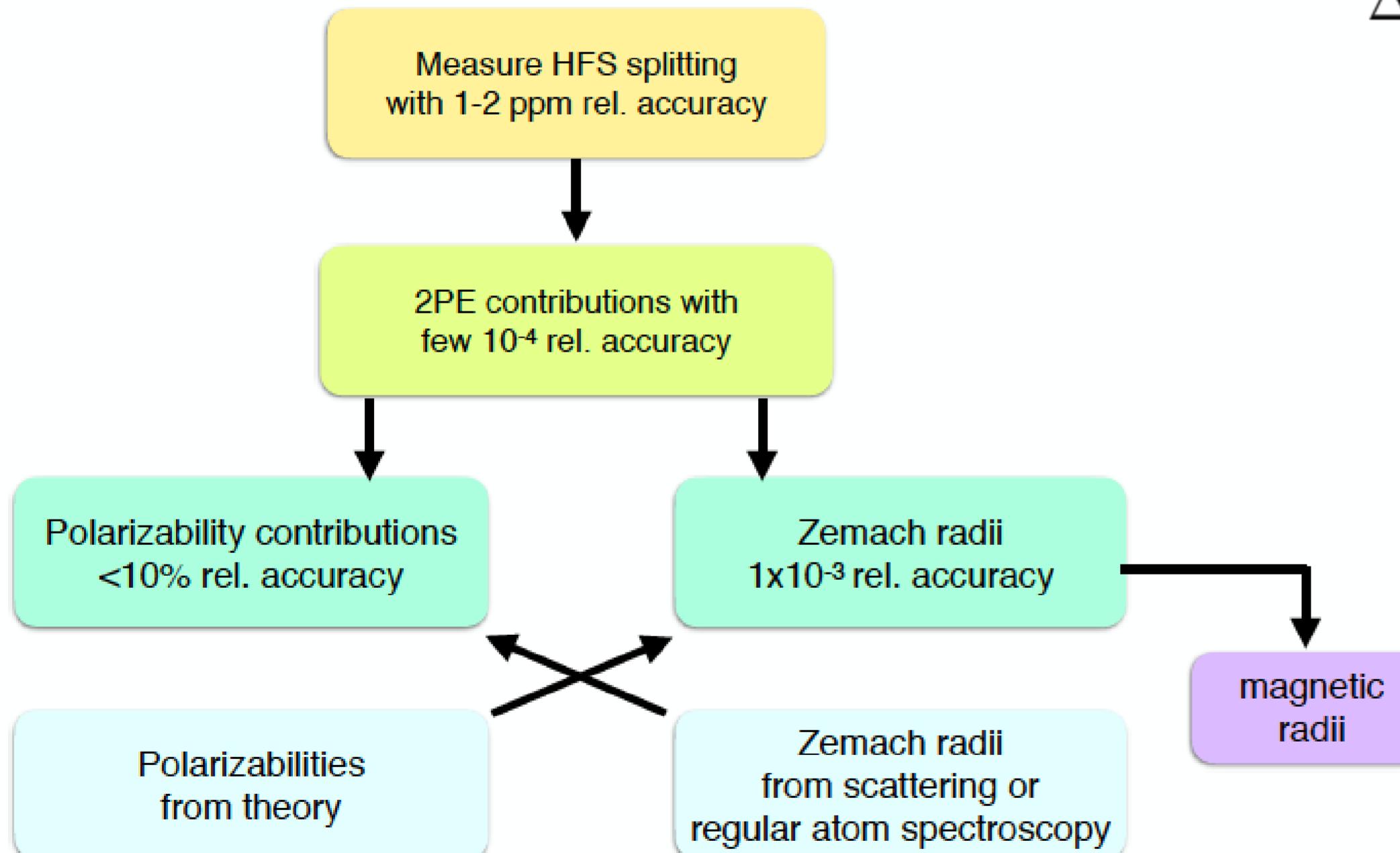
## Goal

Measure the 1S-HFS in  $\mu p$   
with 1-2 ppm accuracy

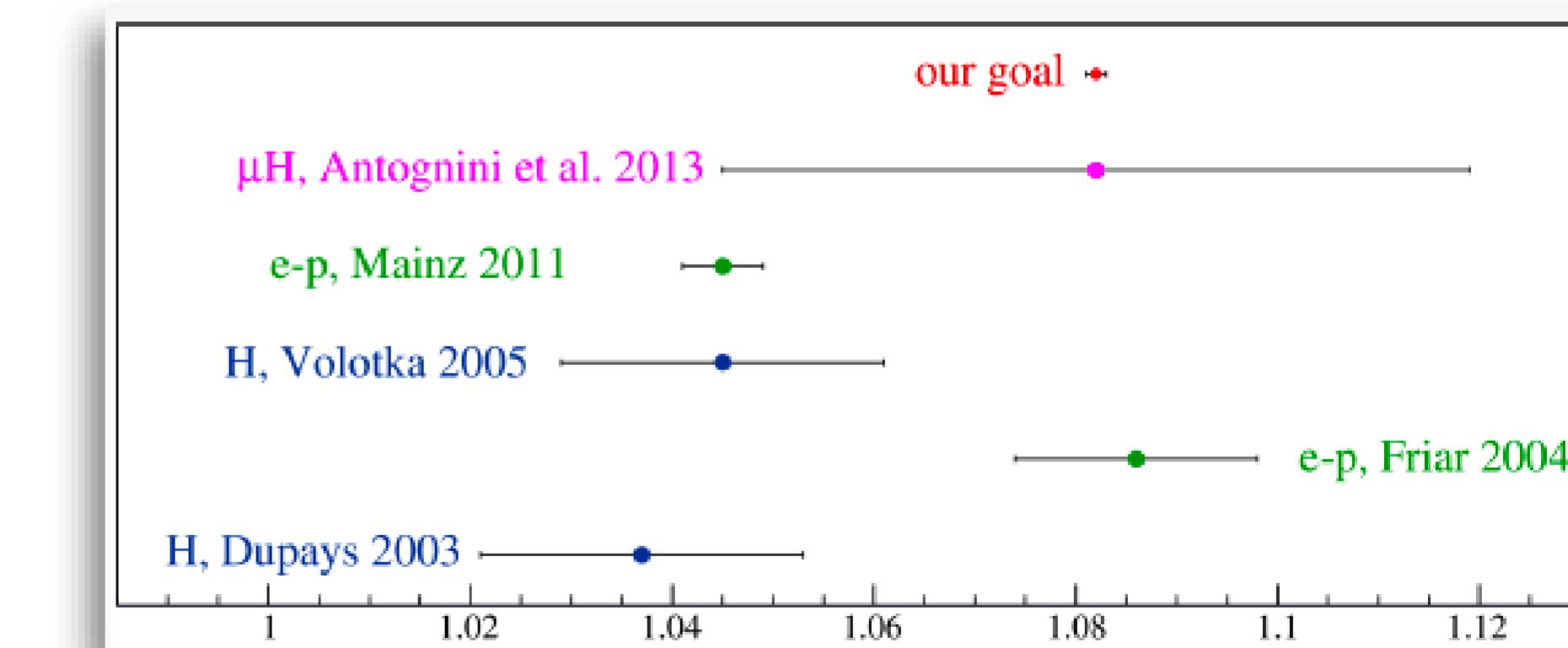
## Impact

- ▶ TPE contribution with  $3 \times 10^{-4}$  rel. accuracy
- ▶ Zemach radius and polarisability contributions

$$\Delta E_{\text{HFS}}^{\text{th}} = 182.819(10) - \underbrace{1.301 R_Z + 0.064(21)}_{\text{TPE}} + \dots \text{ meV}$$

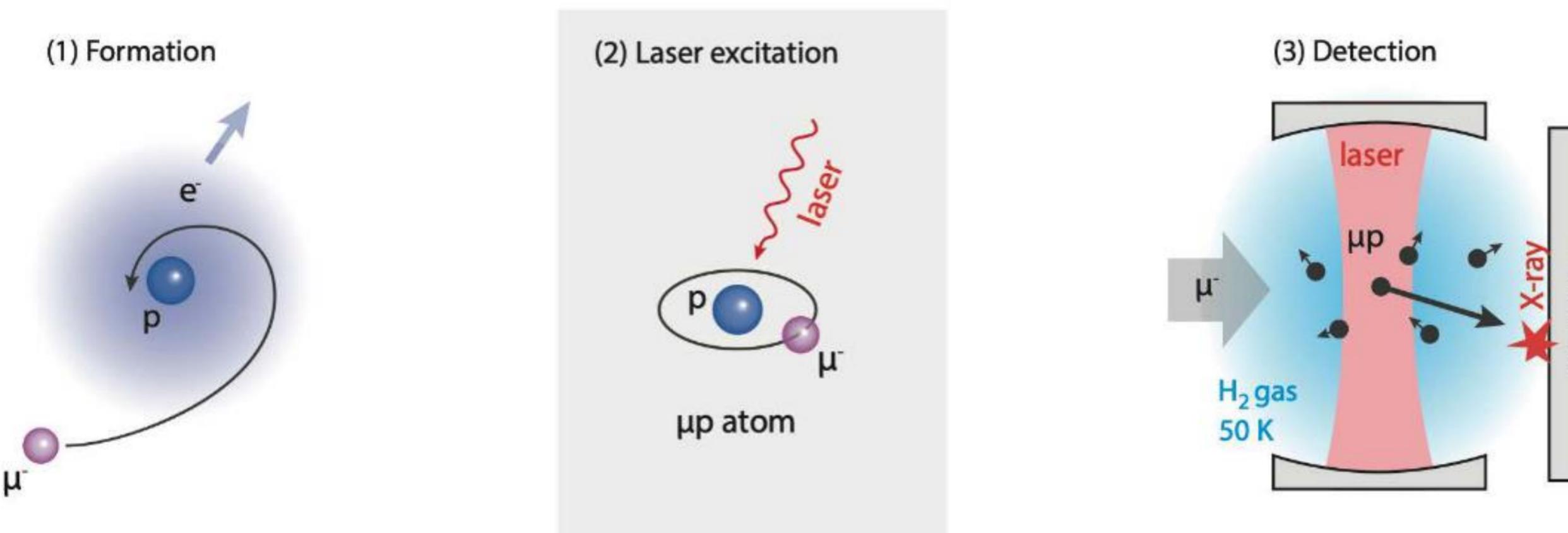


Test of fundamental nuclear theories:  
Quiral PT, dispersion theories, QCD, etc



Proton Zemach radius  $R_Z$  [fm]

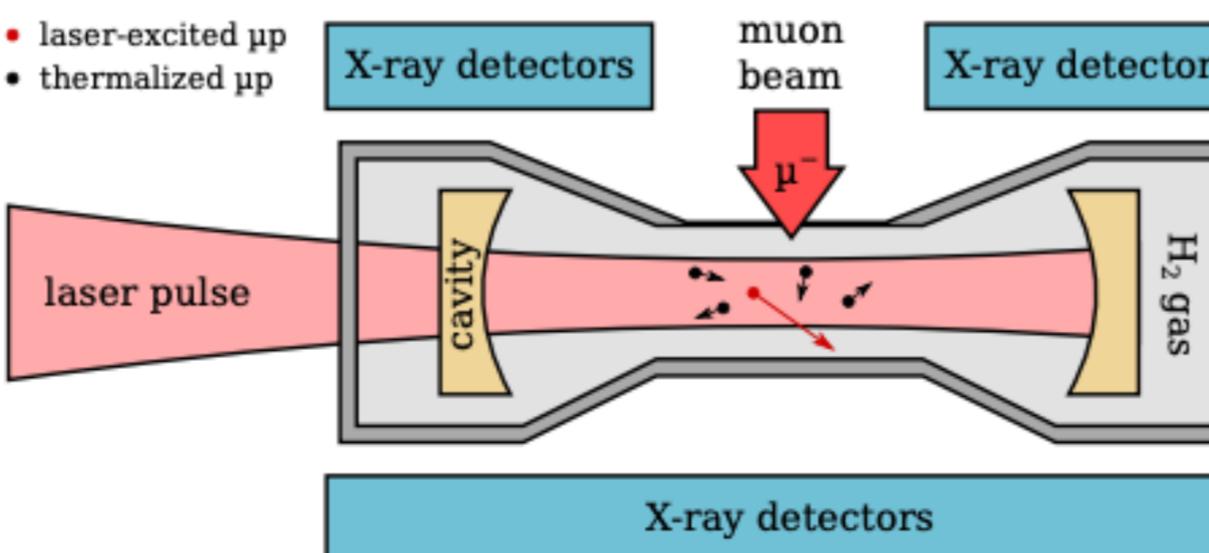
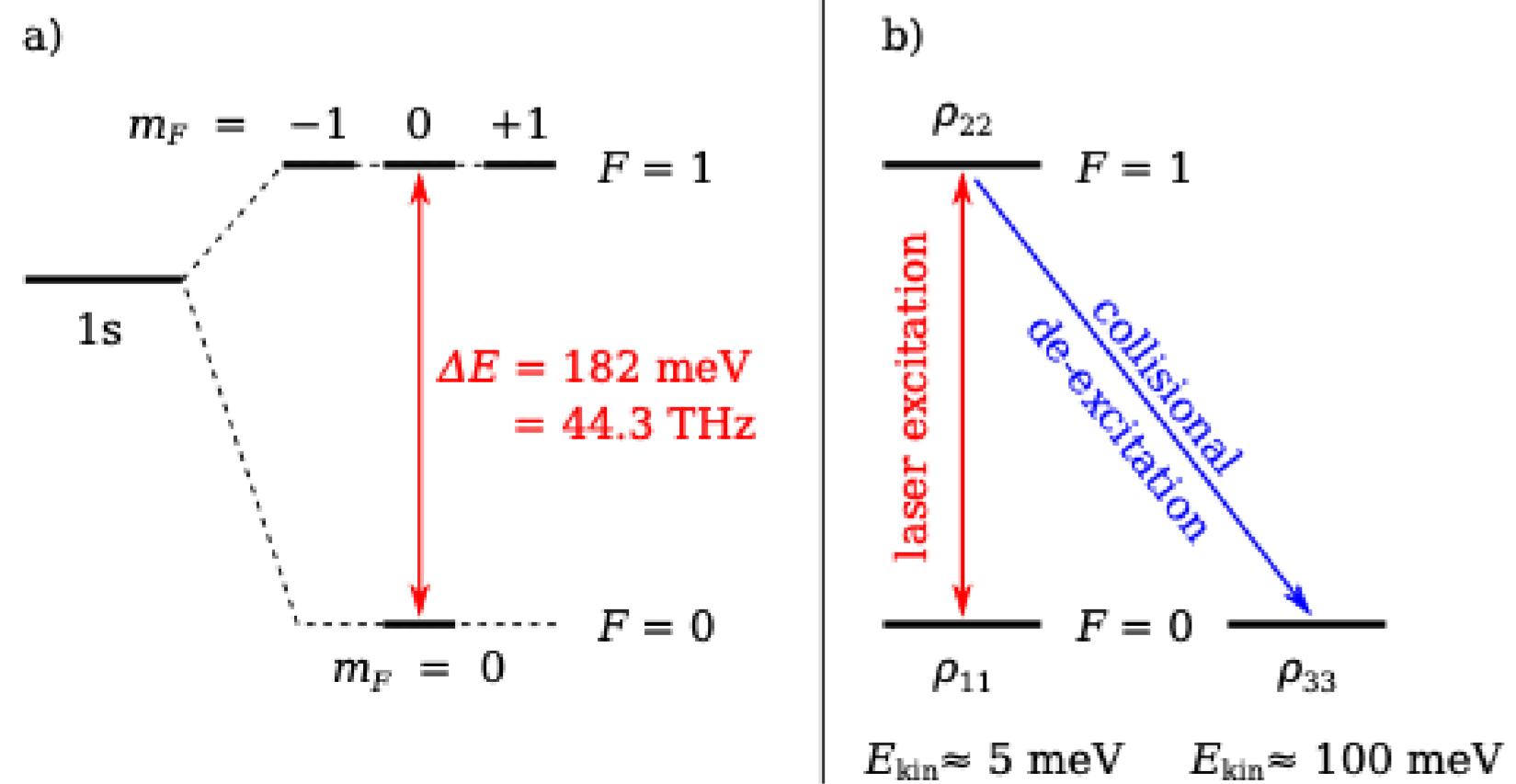
# Experiment HyperMu



## Challenges to overcome

Signal detection

Laser wavelength with power

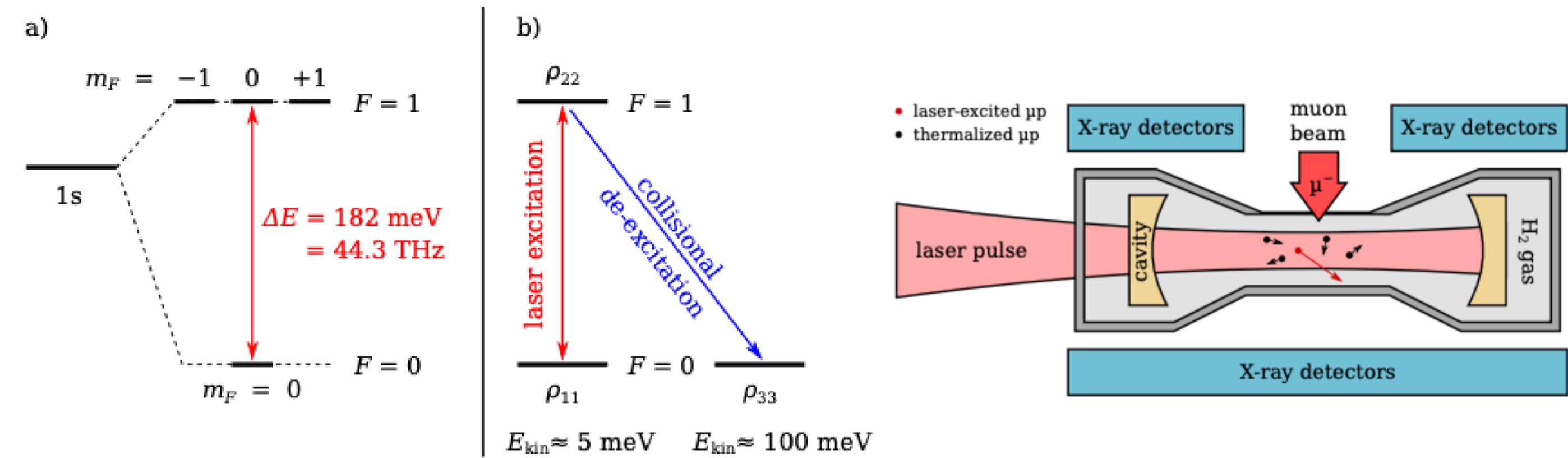
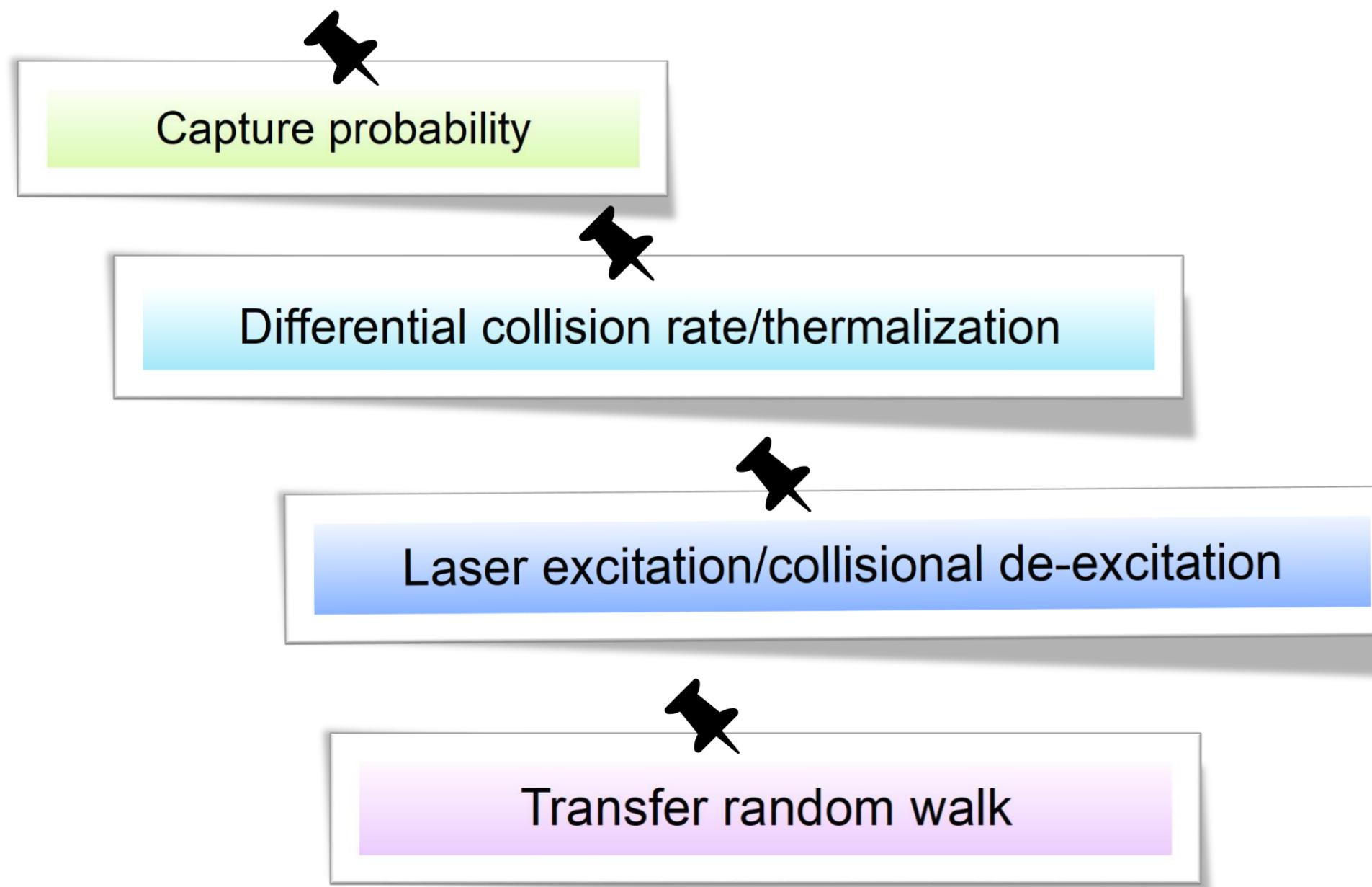


- ▶ Laser pulse:  $\mu p(F=0) + \gamma \rightarrow \mu p(F=1)$
- ▶ De-excitation:  $\mu p(F=1) + H_2 \rightarrow \mu p(F=0) + H_2 + E_{\text{kin}}$
- ▶ Diffusion: X-rays produce at target walls
- ▶ Resonance: Number of X-ray vs laser freq.

# Model of the experiment HyperMu

- laser requirements?
- gas conditions ?
- target geometry ?
- are correlated ?

## Monte-Carlo simulation checklist



## Laser excitation/deexcitation with Bloch equations

$$\begin{aligned}\frac{d\rho_{11}}{dt}(t) &= -\text{Im}(\Omega\rho_{12}e^{i\Delta t}) + \Gamma_{\text{sp}}\rho_{22}, \\ \frac{d\rho_{22}}{dt}(t) &= \text{Im}(\Omega\rho_{12}e^{i\Delta t}) - (\Gamma_i + \Gamma_{\text{sp}})\rho_{22}, \\ \frac{d\rho_{12}}{dt}(t) &= \frac{i\Omega^*}{2}(\rho_{11} - \rho_{22})e^{-i\Delta t} - \frac{\Gamma_c}{2}\rho_{12}, \\ \frac{d\rho_{33}}{dt}(t) &= \Gamma_i\rho_{22},\end{aligned}$$

## Laser excitation/collisional de-excitation

$$\begin{aligned}\frac{d\rho_{11}}{dt}(t) &= -\text{Im}(\Omega\rho_{12}e^{i\Delta t}) + \Gamma_{\text{sp}}\rho_{22}, \\ \frac{d\rho_{22}}{dt}(t) &= \text{Im}(\Omega\rho_{12}e^{i\Delta t}) - (\Gamma_i + \Gamma_{\text{sp}})\rho_{22}, \\ \frac{d\rho_{12}}{dt}(t) &= \frac{i\Omega^*}{2}(\rho_{11} - \rho_{22})e^{-i\Delta t} - \frac{\Gamma_c}{2}\rho_{12}, \\ \frac{d\rho_{33}}{dt}(t) &= \Gamma_i\rho_{22},\end{aligned}$$

- **Laser-atom strength**
- **molecular collisions**
- **Laser bandwidth**
- **Doppler broadening**

$$\begin{aligned}
 \frac{d\rho_{11}}{dt}(t) &= -\text{Im}(\Omega\rho_{12}e^{i\Delta t}) + \Gamma_{\text{sp}}\rho_{22}, \\
 \frac{d\rho_{22}}{dt}(t) &= \text{Im}(\Omega\rho_{12}e^{i\Delta t}) - (\Gamma_i + \Gamma_{\text{sp}})\rho_{22}, \\
 \frac{d\rho_{12}}{dt}(t) &= \frac{i\Omega^*}{2}(\rho_{11} - \rho_{22})e^{-i\Delta t} - \frac{\Gamma_c}{2}\rho_{12}, \\
 \frac{d\rho_{33}}{dt}(t) &= \Gamma_i\rho_{22},
 \end{aligned}$$

- **Laser-atom strength**
- **molecular collisions**
- **Laser bandwidth**
- **Doppler broadening**

## Laser-atom strength

$$\Omega = \sqrt{\frac{8\pi\alpha\mathcal{I}}{\hbar}}\mathcal{M}$$

Atom	Transition	$\mathcal{M}$ [m]	$\frac{\Omega}{\sqrt{\mathcal{I}}}$ [m/ $\sqrt{\text{Js}}$ ]
$\mu p$	$2s^{F=1} \rightarrow 2p_{3/2}^{F=2}$	$\sqrt{5}a_\mu = 6.367 \times 10^{-13}$	$2.65 \times 10^4$
$\mu^3\text{He}^+$	$2s^{F=1} \rightarrow 2p_{3/2}^{F=2}$	$\frac{\sqrt{5}}{2}a_\mu = 2.969 \times 10^{-13}$	$1.24 \times 10^4$
$\mu p$	$1s^{F=0} \rightarrow 1s^{F=1}$	$\frac{\hbar}{4m_\mu c} \left( g_\mu + \frac{m_\mu}{m_p} g_p \right)$ $= 1.228 \times 10^{-15}$	$5.12 \times 10^1$ <sup>a</sup>
$\mu^3\text{He}^+$	$1s^{F=1} \rightarrow 1s^{F=0}$	$\frac{\hbar}{4\sqrt{3}m_\mu c} \left( g_\mu + \frac{m_\mu}{m_{\text{He}}} g_{\text{He}} \right)$ $= 4.965 \times 10^{-16}$	$2.07 \times 10^1$

<sup>a</sup>  $1.77 \times 10^1$  m/ $\sqrt{\text{Js}}$  according to Ref. [37]

## Molecular collisions and laser bandwidth

$$\begin{aligned}\frac{d\rho_{11}}{dt}(t) &= -\text{Im}(\Omega\rho_{12}e^{i\Delta t}) + \Gamma_{\text{sp}}\rho_{22}, \\ \frac{d\rho_{22}}{dt}(t) &= \text{Im}(\Omega\rho_{12}e^{i\Delta t}) - (\Gamma_i + \Gamma_{\text{sp}})\rho_{22}, \\ \frac{d\rho_{12}}{dt}(t) &= \frac{i\Omega^*}{2}(\rho_{11} - \rho_{22})e^{-i\Delta t} - \frac{\Gamma_c}{2}\rho_{12}, \\ \frac{d\rho_{33}}{dt}(t) &= \Gamma_i\rho_{22},\end{aligned}$$

$$\Gamma_c = 2\pi\Delta_l + \Gamma_e^{F=0} + \Gamma_e^{F=1} + \Gamma_i + \Gamma_{\text{sp}}$$

$$\Gamma = \overline{v_r \sigma(v_r)} \rho_{\text{H}_2}$$

	p = 0.5 bar		T = 22 K		T = 30 K		T = 50 K	
	Stat.	Boltz.	Stat.	Boltz.	Stat.	Boltz.	Stat.	Boltz.
$\Gamma_e^{F=0}$	20	20	15	15	9	9		
$\Gamma_e^{F=1}$	52	29	41	24	28	18		
$\Gamma_i$	82	93	59	66	34	37		
	p = 1 bar		T = 22 K		T = 30 K		T = 50 K	
	Stat.	Boltz.	Stat.	Boltz.	Stat.	Boltz.	Stat.	Boltz.
$\Gamma_e^{F=0}$	40	39	30	30	19	19		
$\Gamma_e^{F=1}$	104	59	83	47	55	37		
$\Gamma_i$	164	187	118	133	68	74		
	p = 2 bar		T = 22 K		T = 30 K		T = 50 K	
	Stat.	Boltz.	Stat.	Boltz.	Stat.	Boltz.	Stat.	Boltz.
$\Gamma_e^{F=0}$	79	79	61	61	38	37		
$\Gamma_e^{F=1}$	208	118	165	94	110	74		
$\Gamma_i$	328	374	235	265	137	148		

- Laser-atom strength
- Molecular collisions
- Laser bandwidth
- Doppler broadening

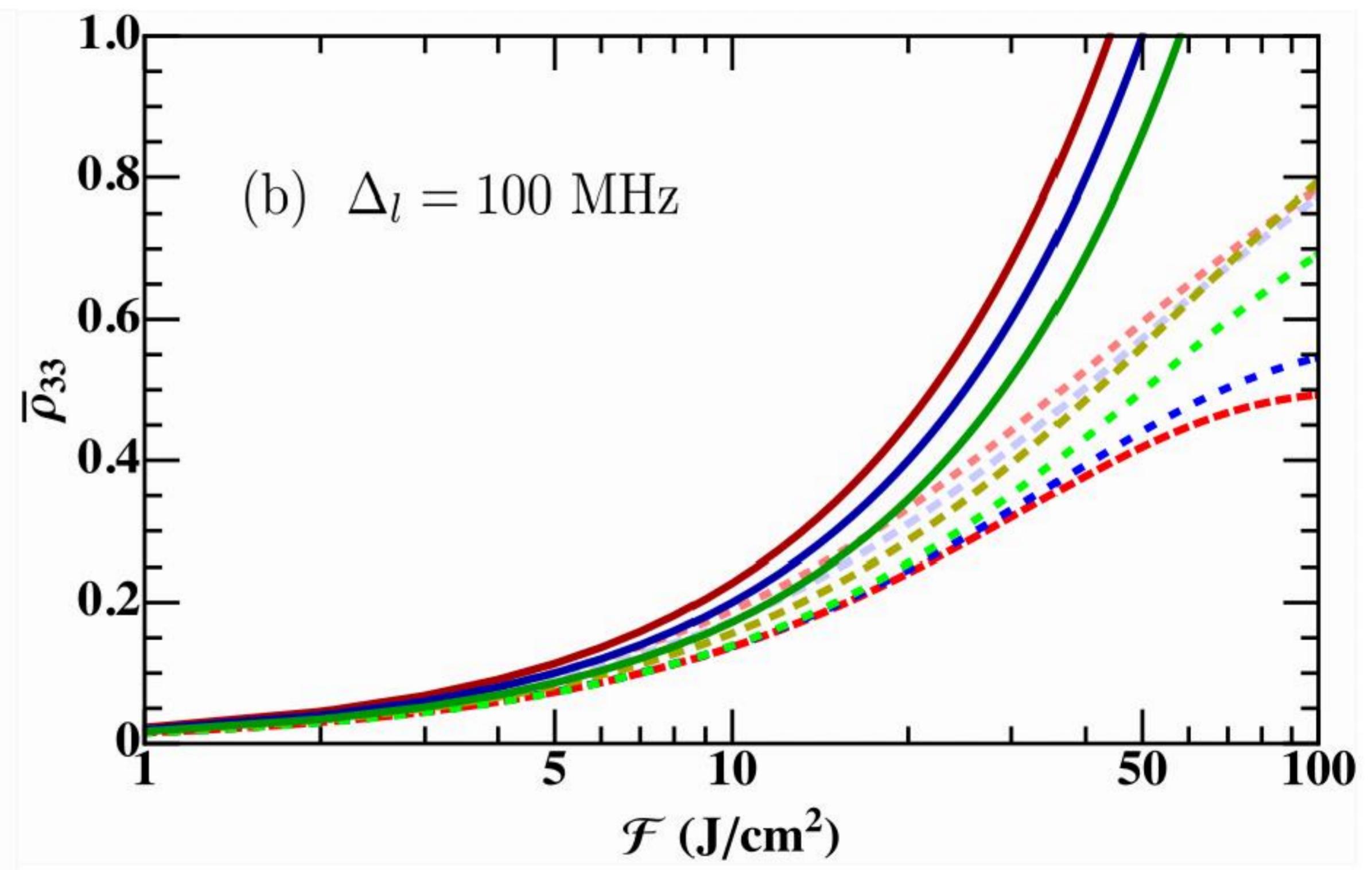
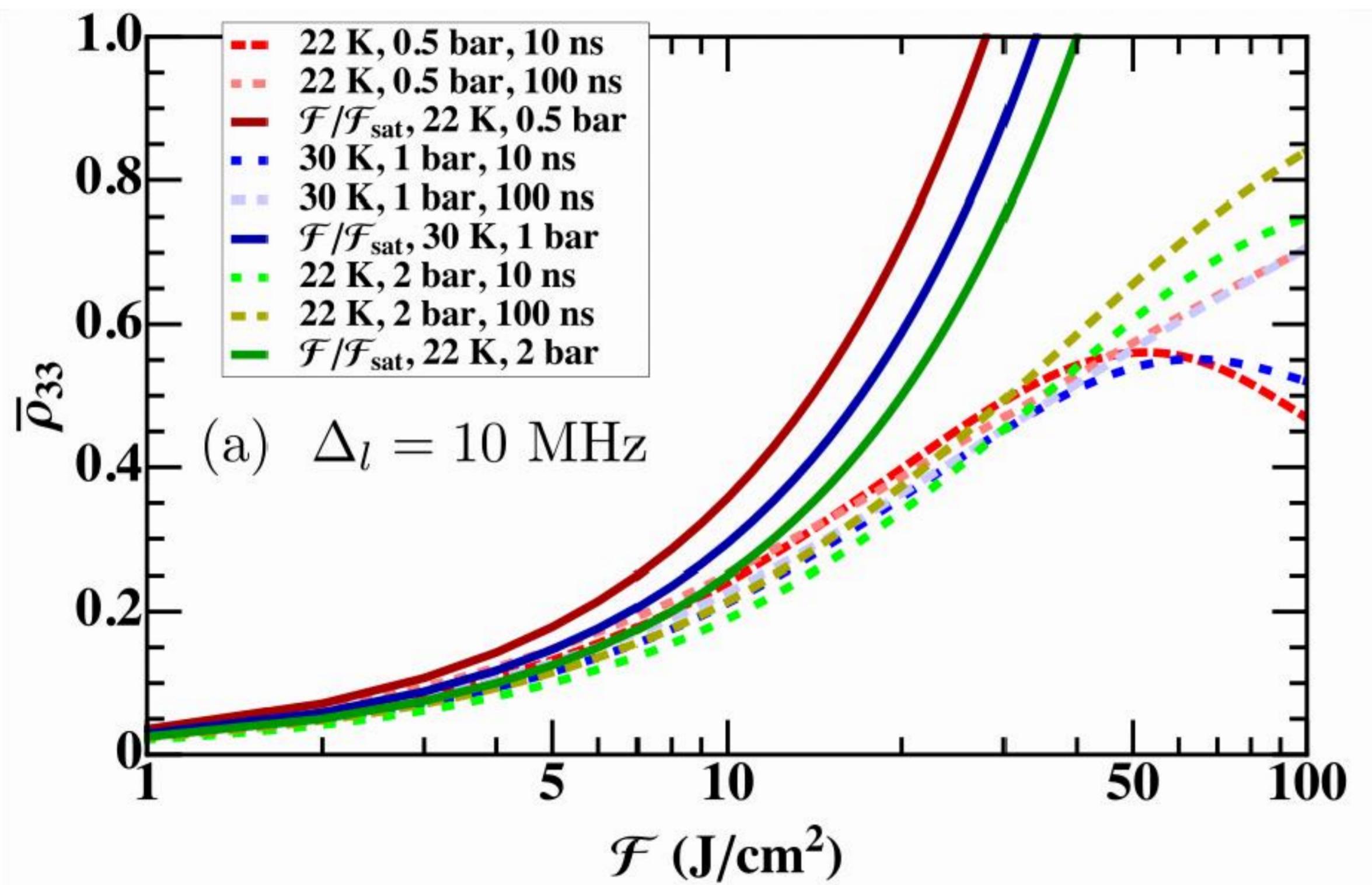
## Doppler broadening

$$\gamma_D = \omega_r \sqrt{\frac{kT}{(m_\mu + m_p)c^2}} \simeq 7.98 \times 10^7 \sqrt{T} \text{ [rad/s]}$$

Laser excitation and shape depend on gas temperature and pressure via collisional and Doppler

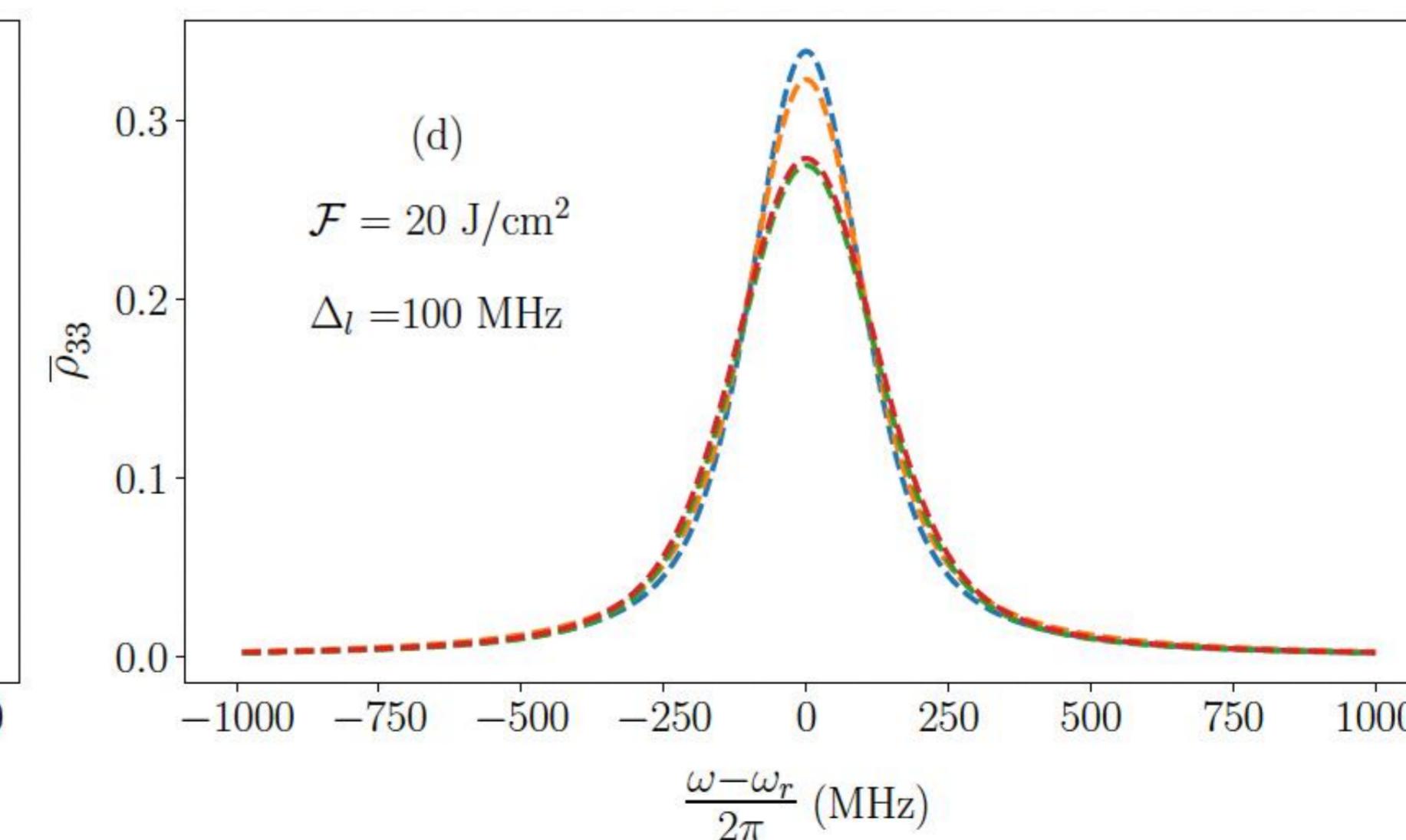
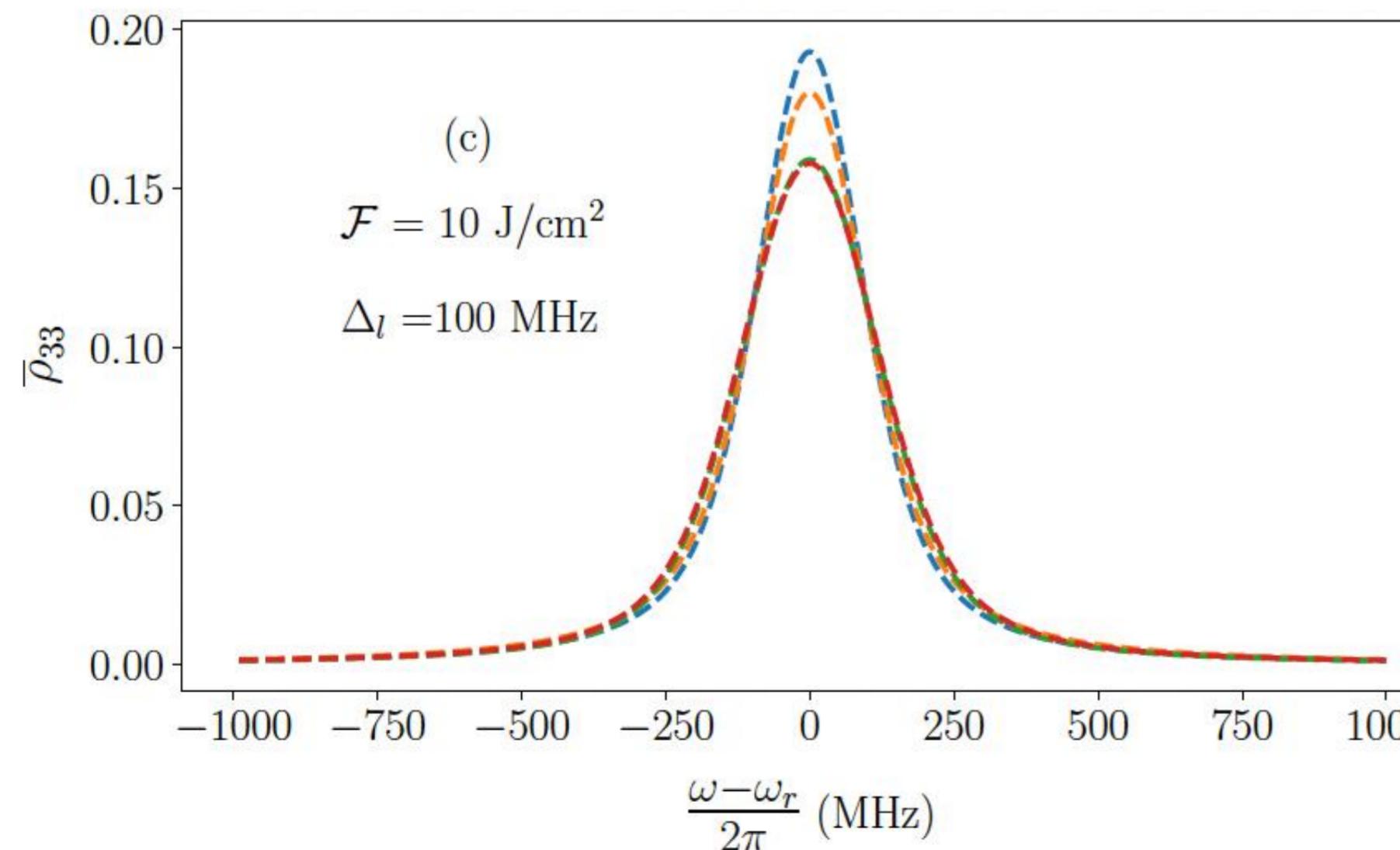
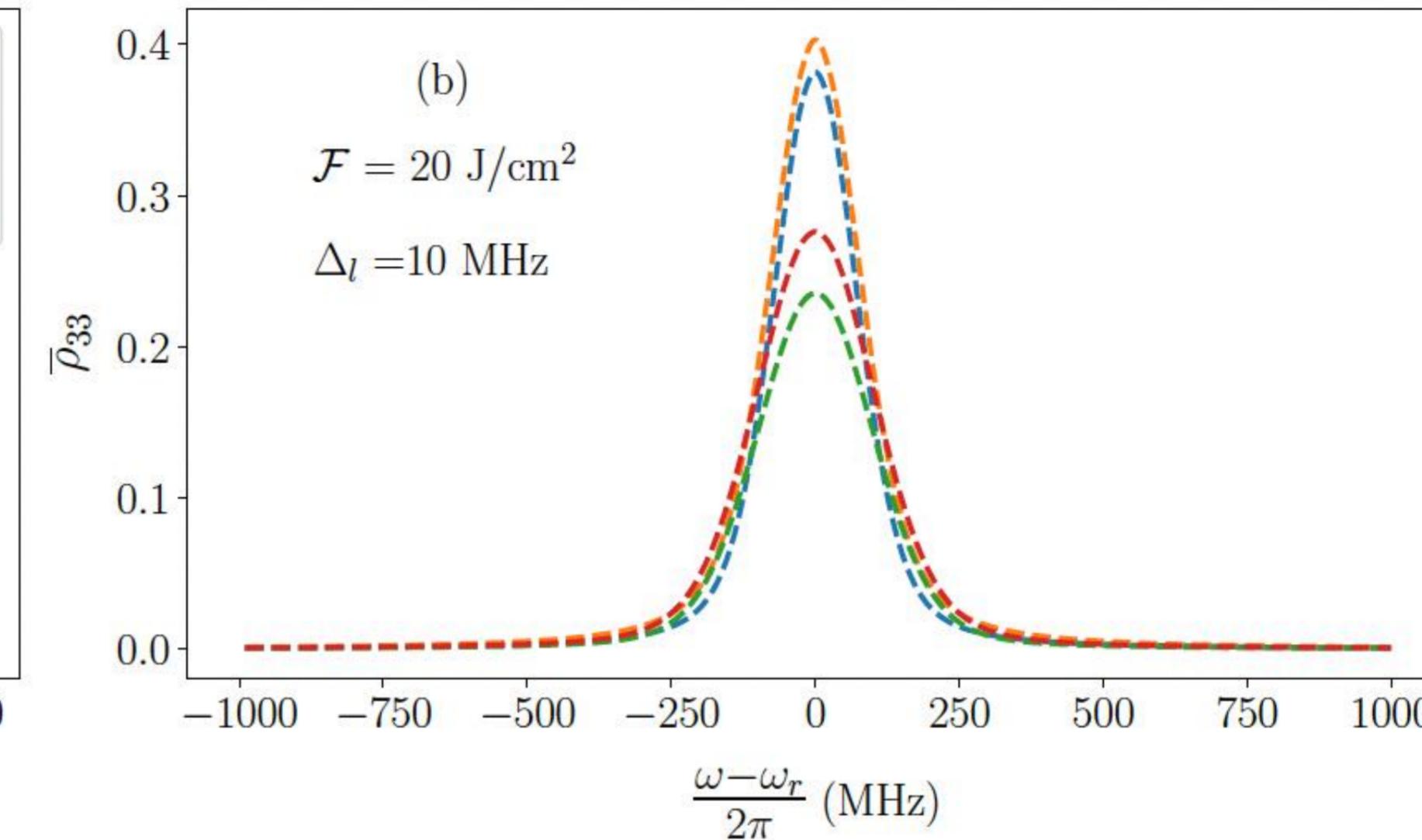
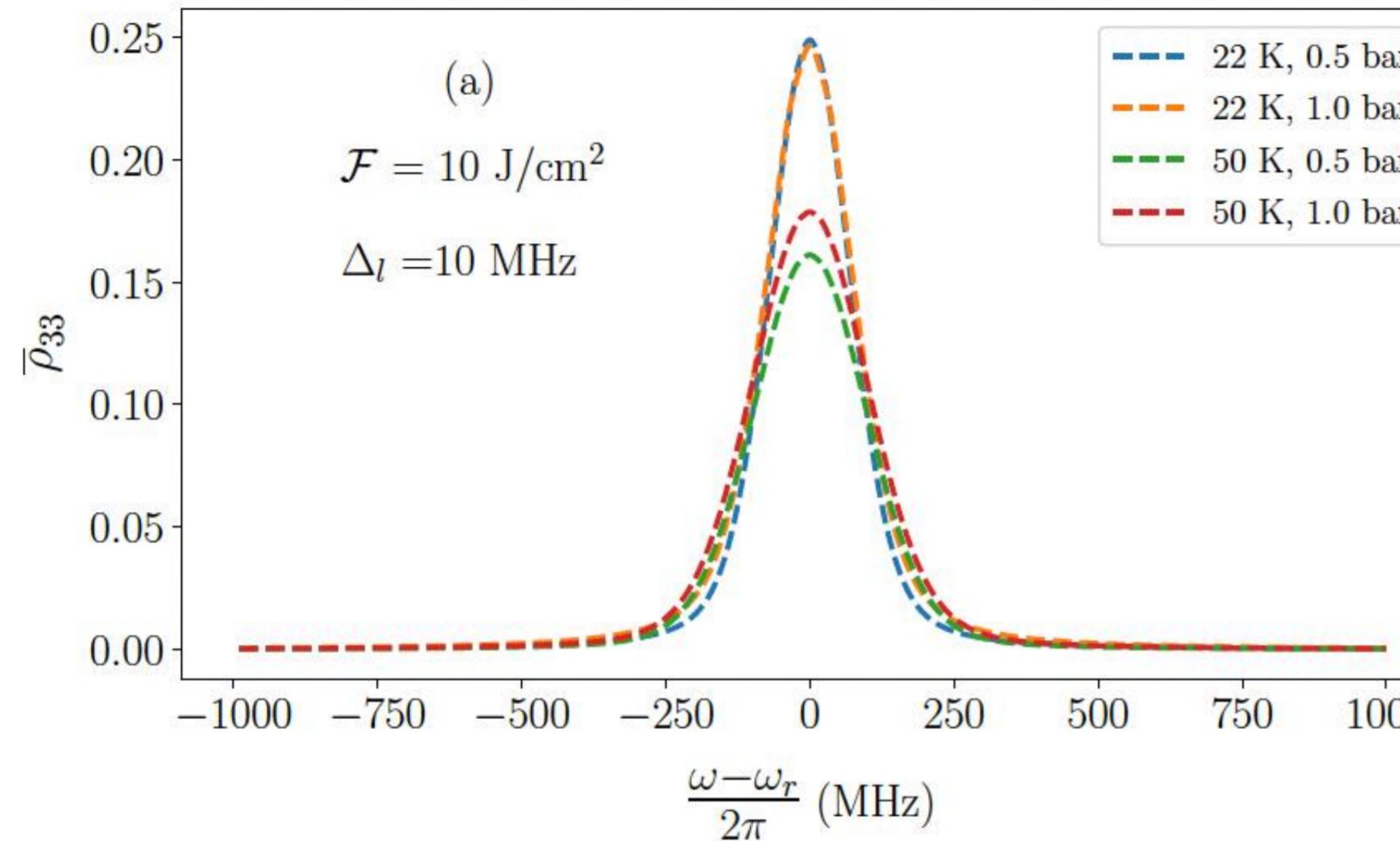
## Saturation fluences

Atom	Transition	$T$ [K]	$p$ [bar]	$\nu_r$ [THz]	$\Gamma_{\text{sp}}$ [MHz]	$\Gamma_c^{\Delta_l \rightarrow 10}$ [MHz]	$\Gamma_c^{\Delta_l \rightarrow 100}$ [MHz]	$\sigma_D$ [MHz]	$\mathcal{F}_{\text{sat}}^{\Gamma_c \rightarrow 0}$ [J/cm <sup>2</sup> ]	$\mathcal{F}_{\text{sat}}^{\Delta_l \rightarrow 10}$ [J/cm <sup>2</sup> ]	$\mathcal{F}_{\text{sat}}^{\Delta_l \rightarrow 100}$ [J/cm <sup>2</sup> ]
$\mu p$	$2s^{F=1} \rightarrow 2p_{3/2}^{F=2}$	300	0.001	49.9	$1.16 \times 10^5$		$1.16 \times 10^5$	$2.48 \times 10^2$			0.0165
$\mu^3\text{He}^+$	$2s^{F=1} \rightarrow 2p_{3/2}^{F=2}$	300	0.004	379	$2.00 \times 10^6$		$2.00 \times 10^6$	$1.13 \times 10^3$			1.304
$\mu p$	$1s^{F=0} \rightarrow 1s^{F=1}$			44.2	$1.23 \times 10^{-11}$						
		22	0.5			205	770	60	23	28	44
		22	1			348	913	60	23	32	49
		22	2			633	1198	60	23	40	58
		30	0.5			168	733	70	27	31	47
		30	1			273	838	70	27	34	50
		50	0.5			128	693	90	35	37	53
		50	1			192	757	90	35	39	55

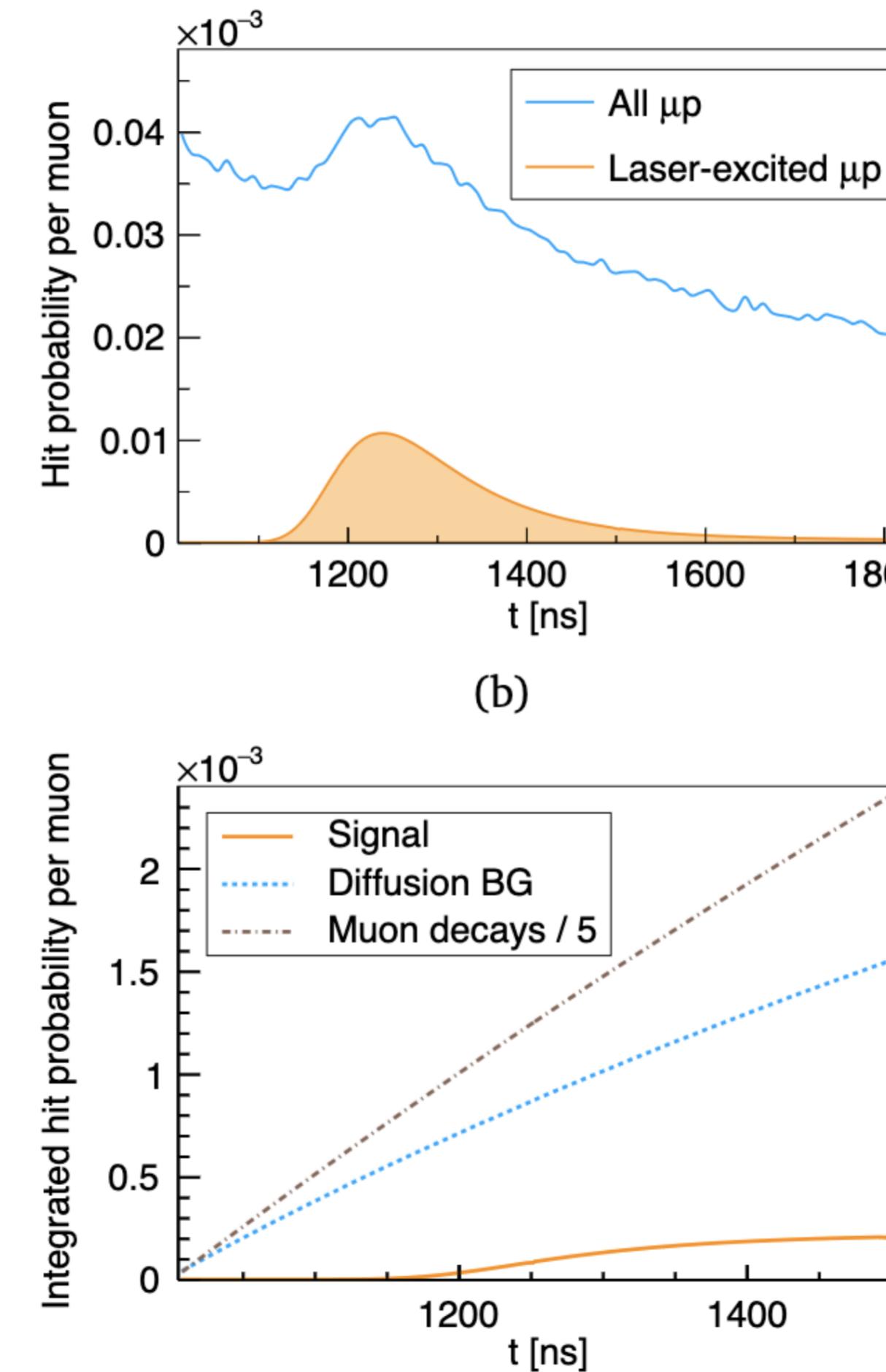
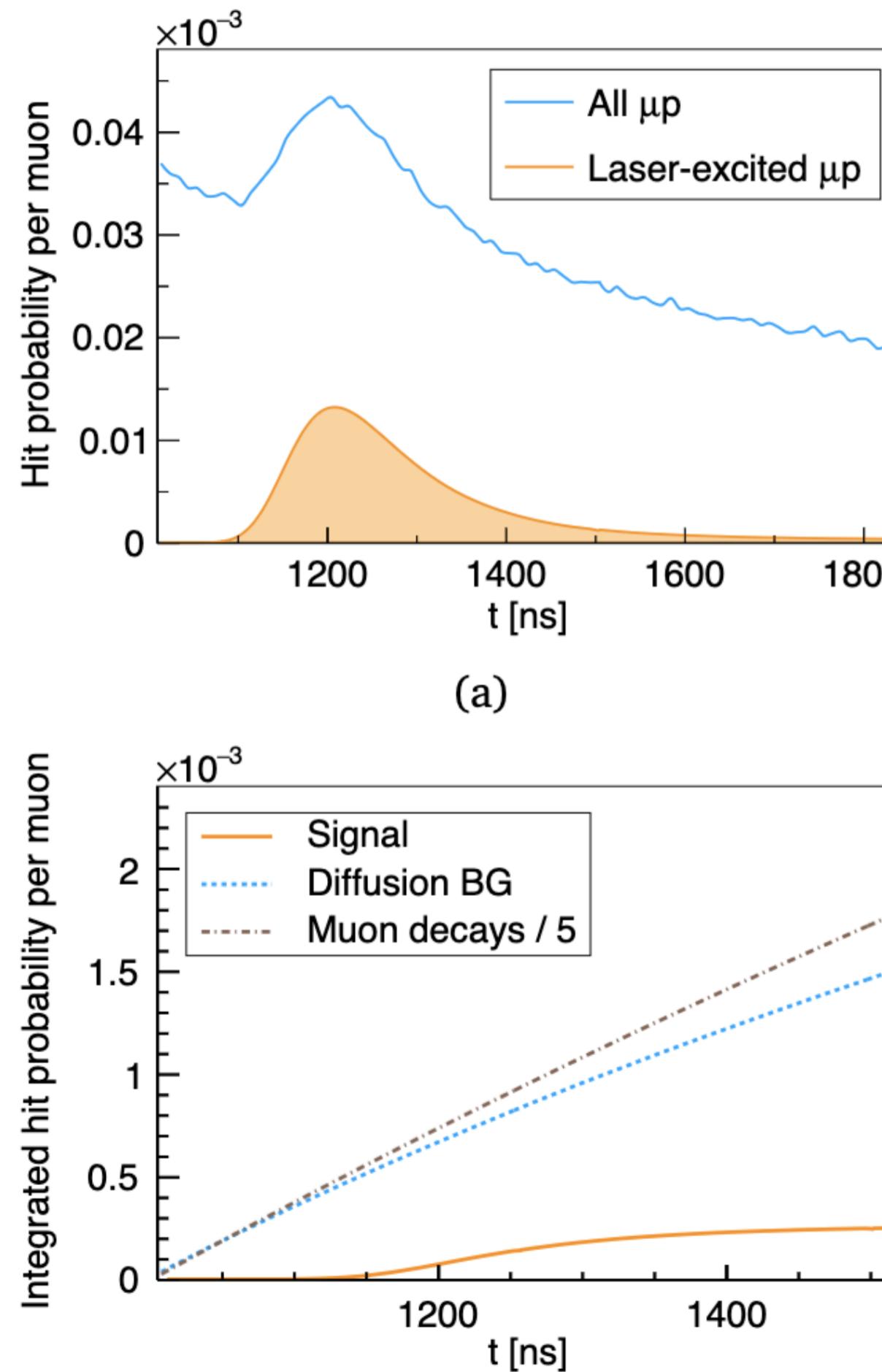


# Signal shape

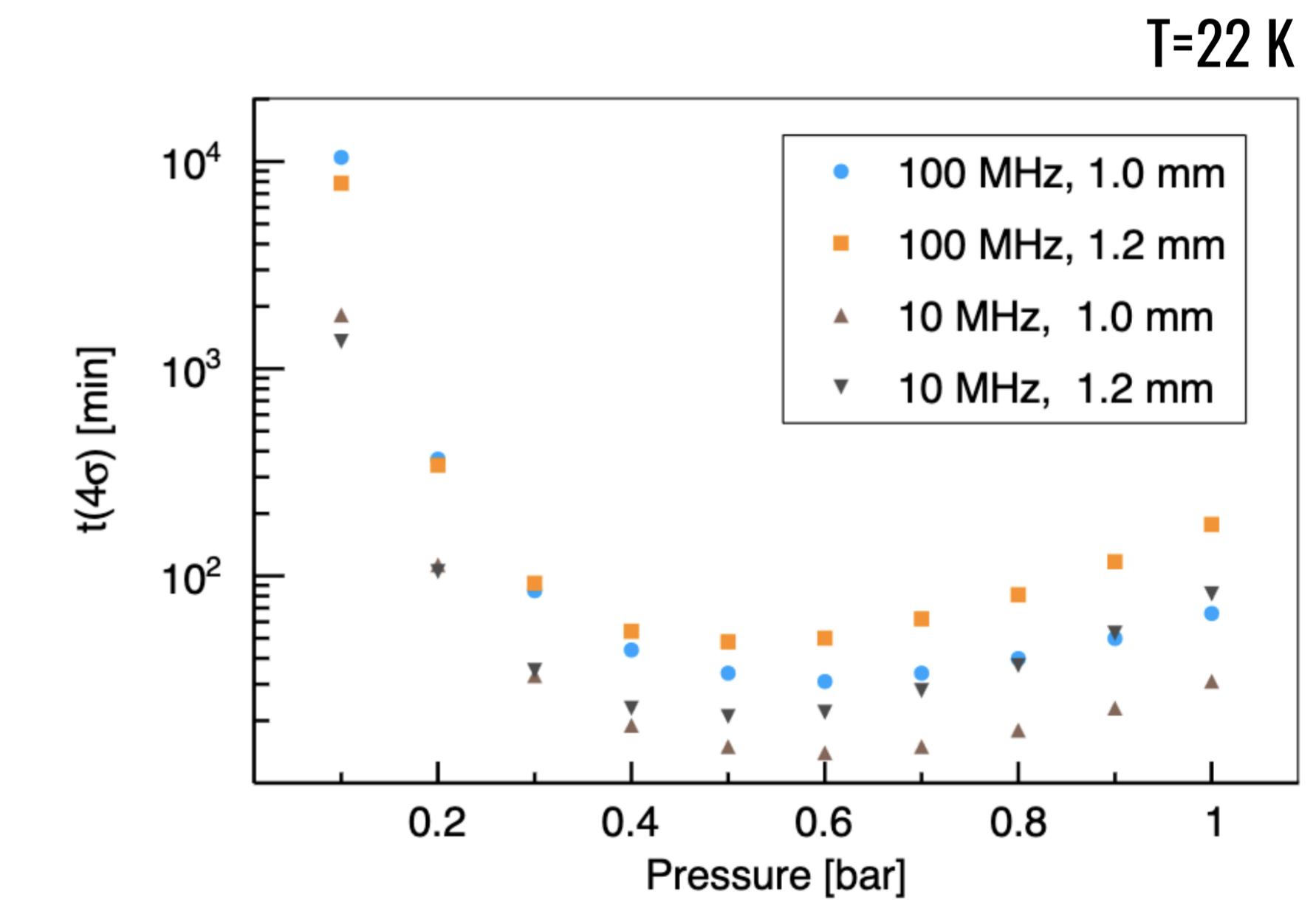
Laser excitation/collisional de-excitation



# Monte-Carlo results HyperMu



J. Nuber *et al*, SciPost Phys. Core 6 57 2023



# Concluding remarks



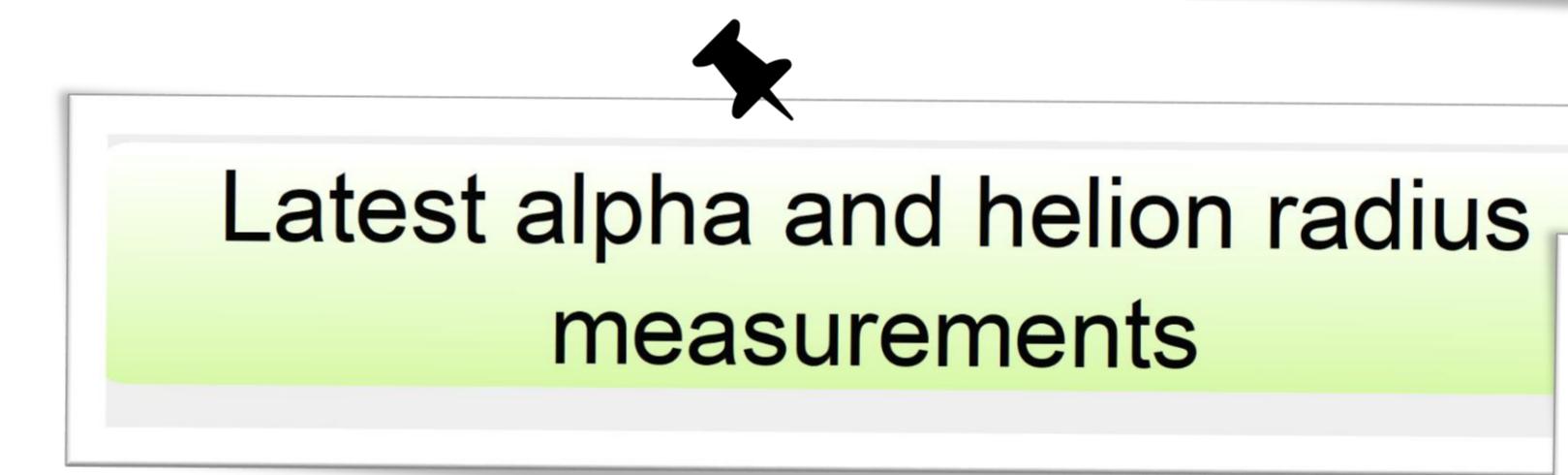
Past

$\mu\text{H}$  Lamb shift



Present

$\mu\text{He}$  Lamb shift

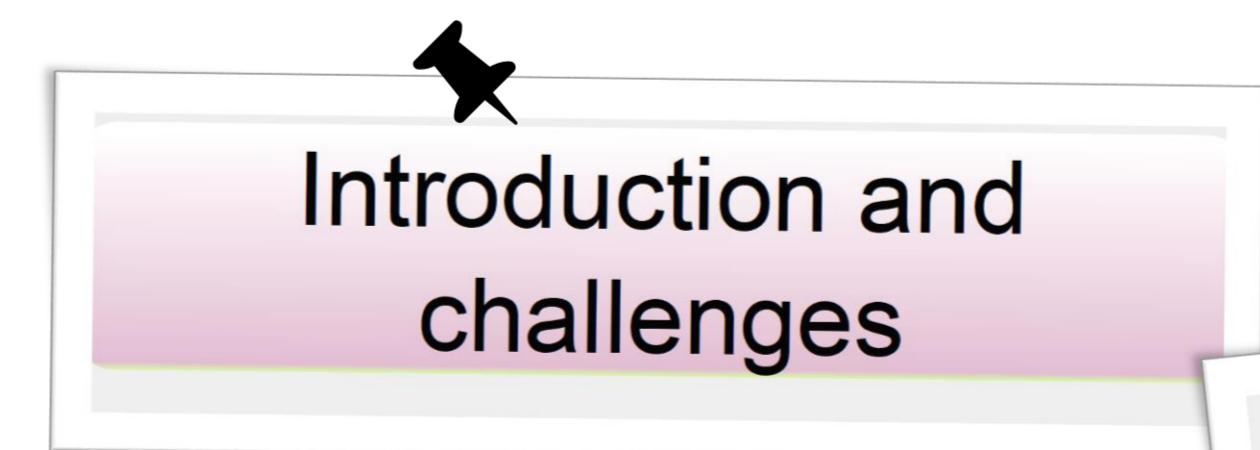


Agreement with most of previous exps.



Future

$\mu\text{H}$  hyperfine structure



Exp model gives 10-60 min for  $4\sigma$  detection

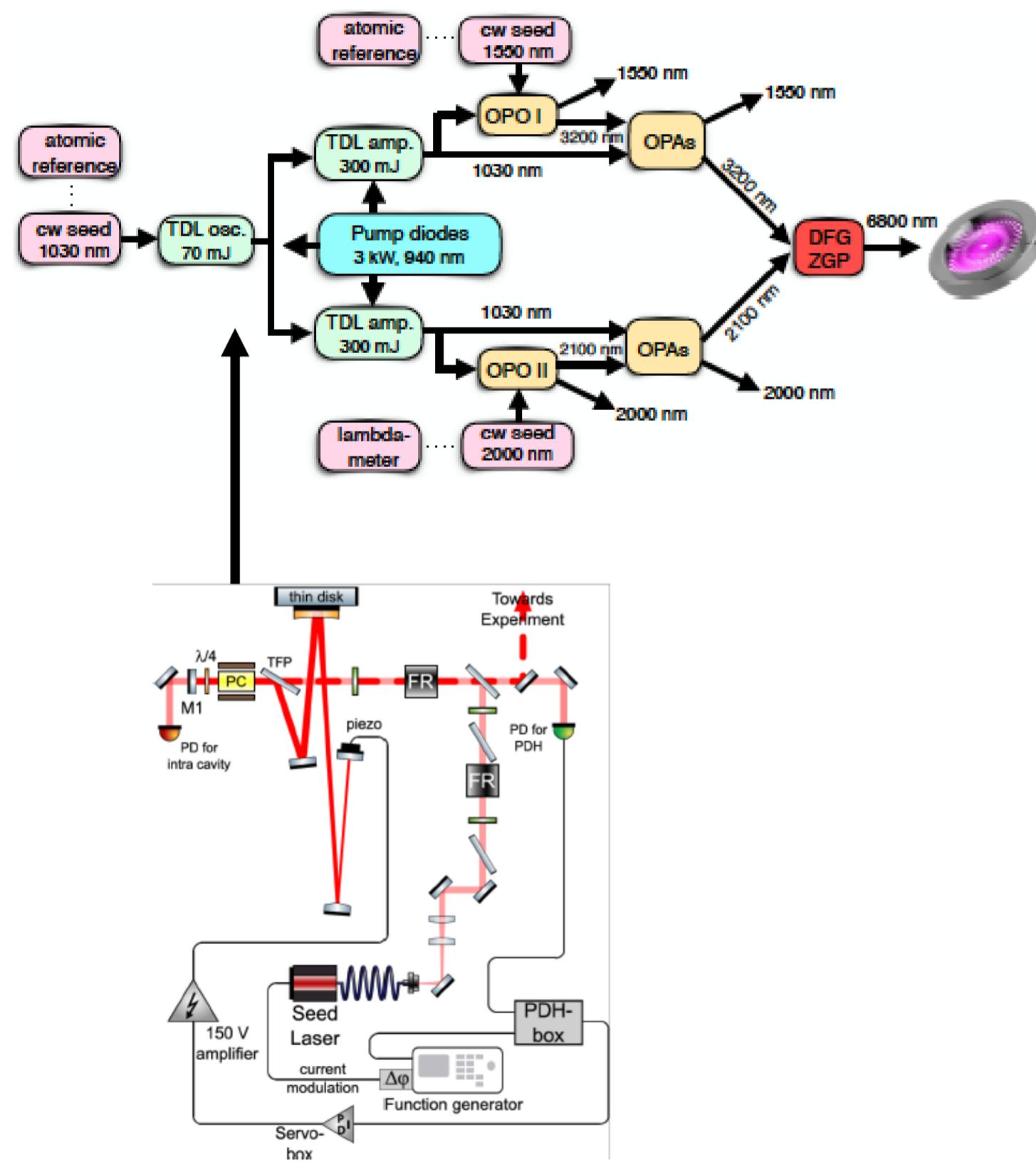
# Hyperfine splitting of muonic hydrogen

- Preparations and prospects for the measurement

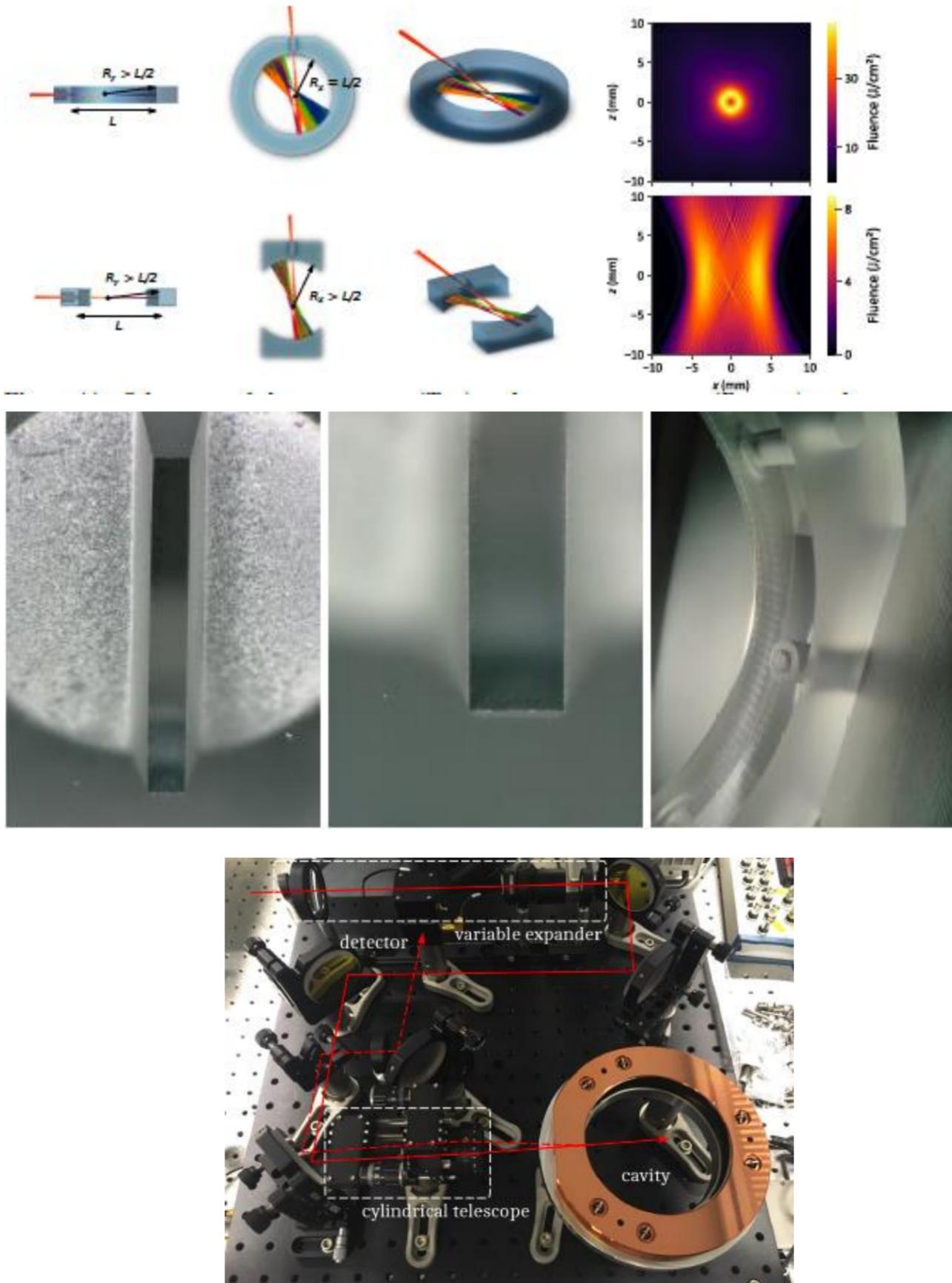


## Laser system development

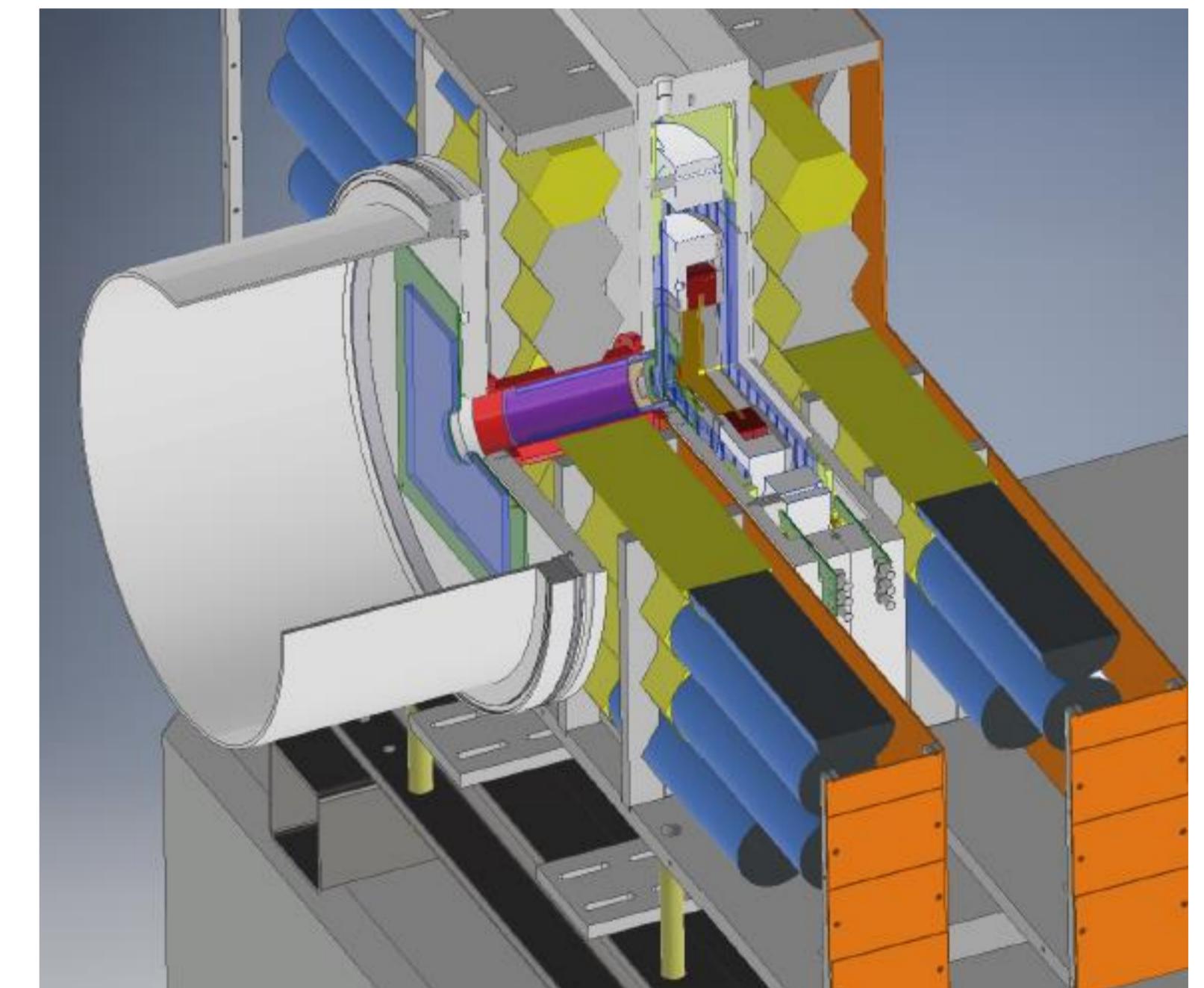
**Patent:** European Patent Office entitled *Powers scalable optical system for nonlinear frequency conversion*



## Target cavity



## Detector system



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**Thank you!**