

# Quantum Stereodynamics at cold energies.

P. G. Jambrina, J. Casas

 **IBER 2023**

XVII Iberian Joint Meeting on Atomic and  
Molecular Physics



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CAMPUS DE EXCELENCIA INTERNACIONAL



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Damm,  
Segmentation  
Fault !!

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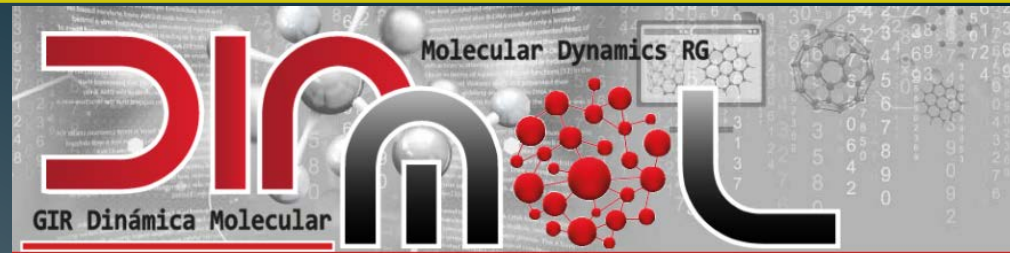
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**800 AÑOS  
UNIVERSIDAD  
D SALAMANCA**

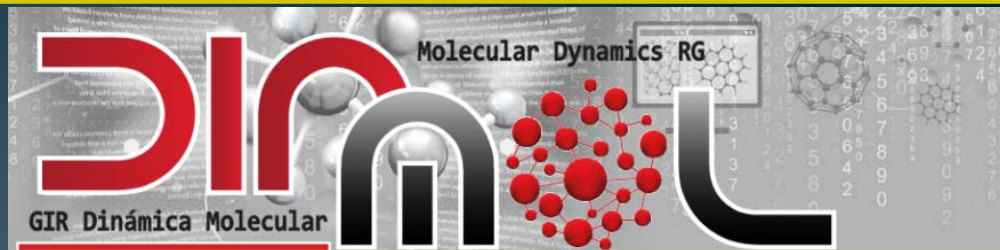
# Credits



- **Hua Guo** (New Mexico)
- **Naduvath Balakrishnan** (Nevada)
- **James Croft** (Dood-Walls Centre, New Zealand)
- **F. Javier Aoiz** (Universidad Complutense de Madrid)



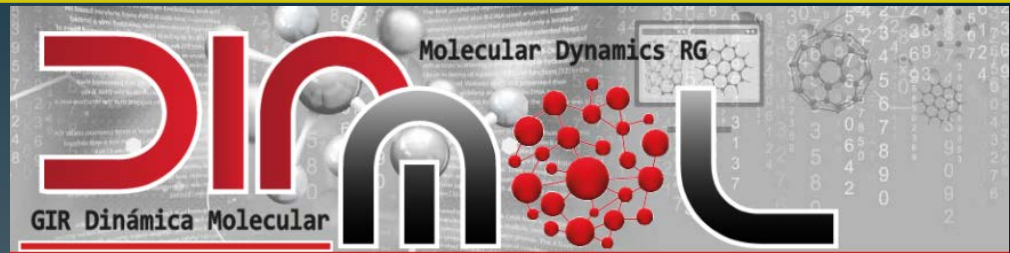
# Outline:



- Inelastic Collisions at Cold energies
- Stereodynamics. SARP Experiments
- Results:  $D_2 + D_2$
- Results:  $He + D_2$
- Conclusions

Aim: Reproduce Experimental Measurements

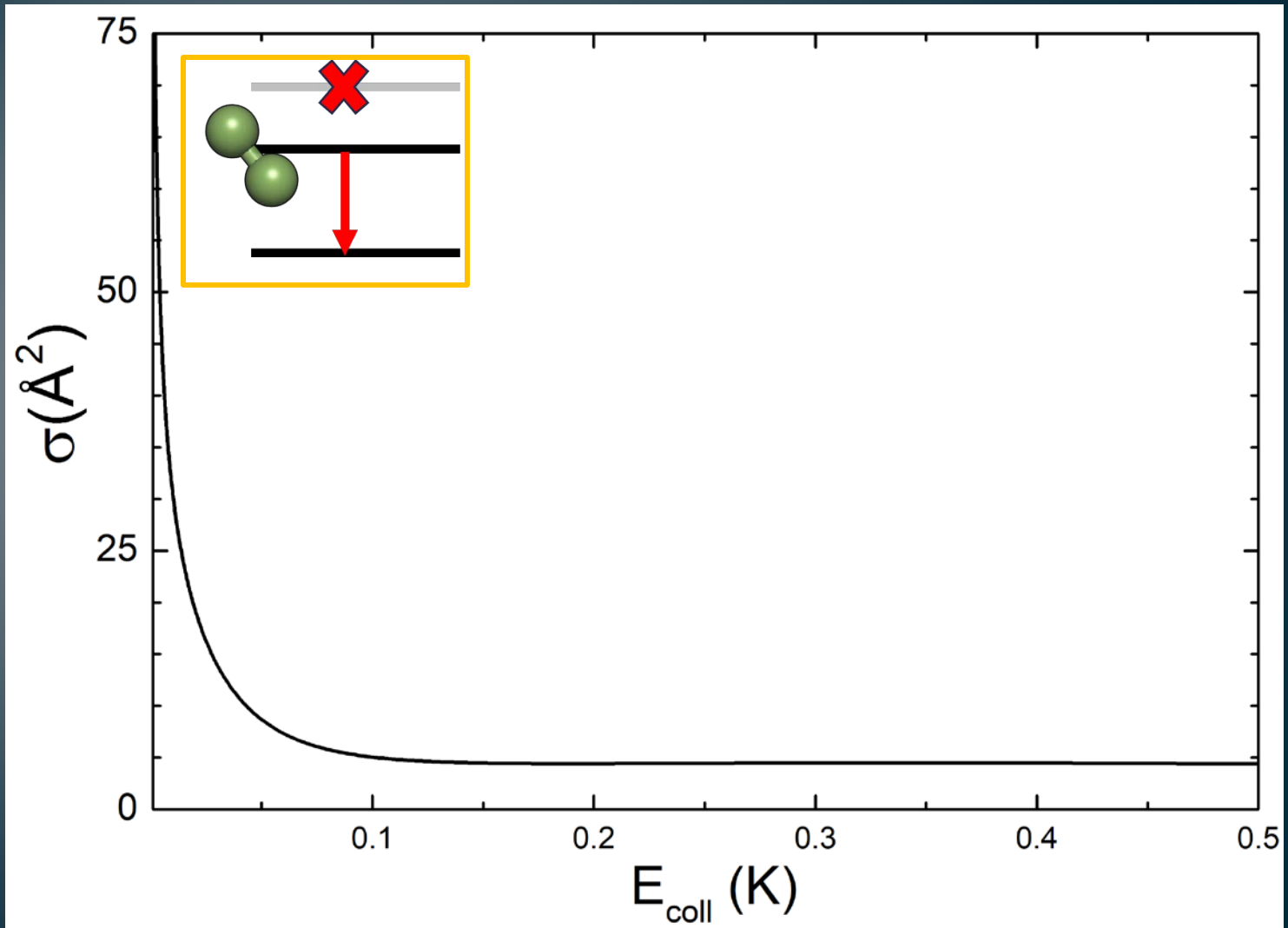
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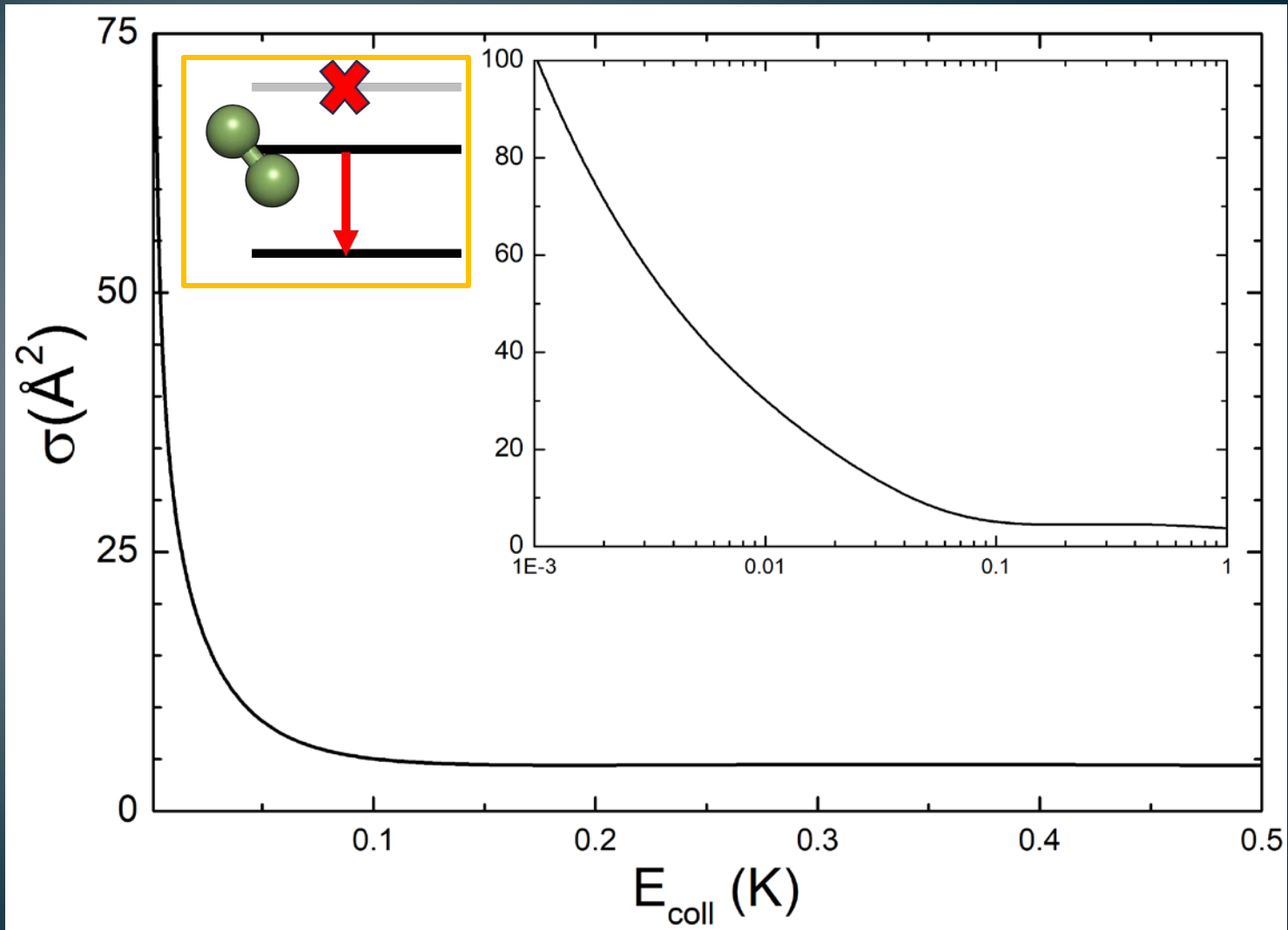
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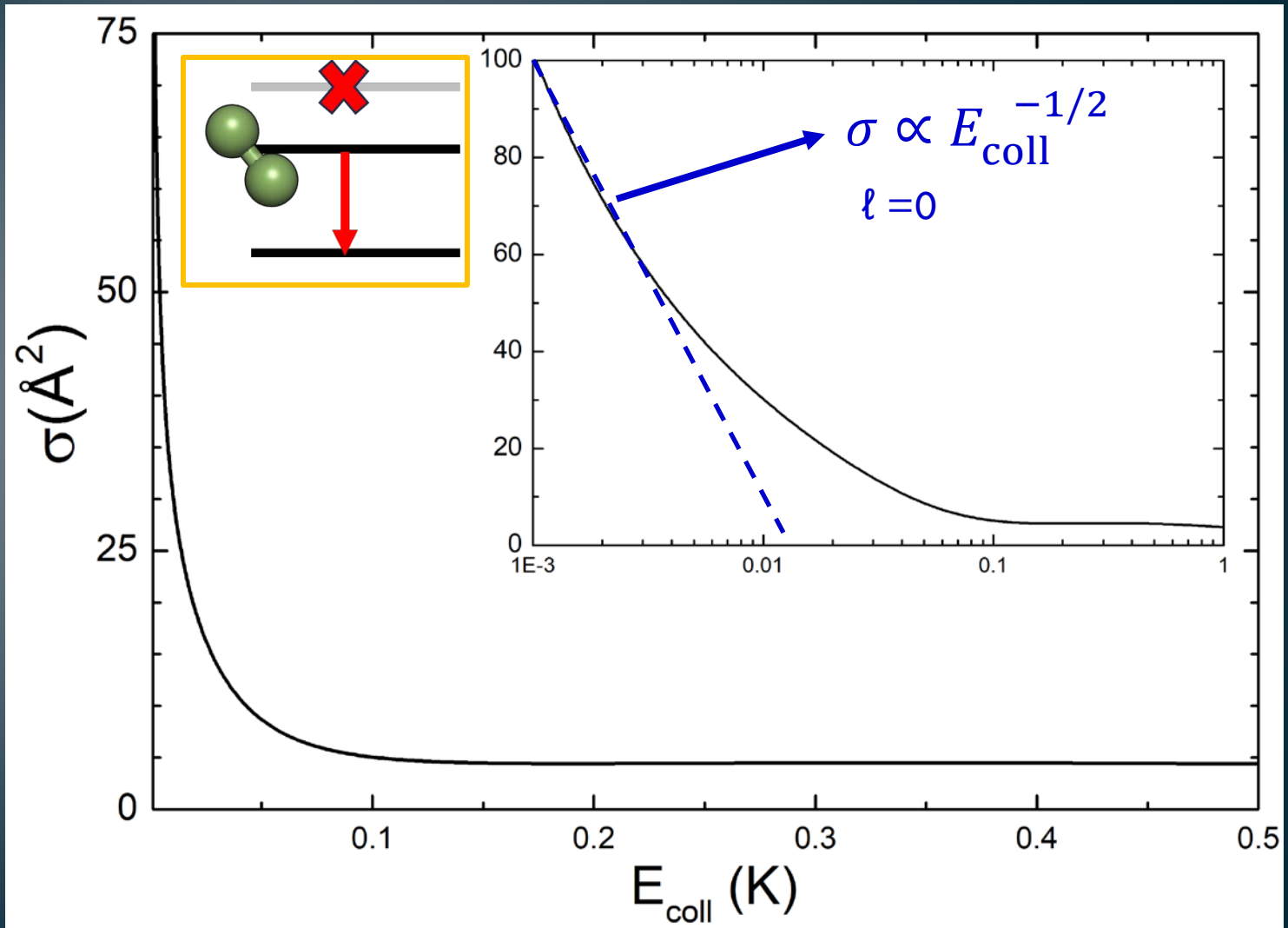
# Inelastic Collisions at low energies



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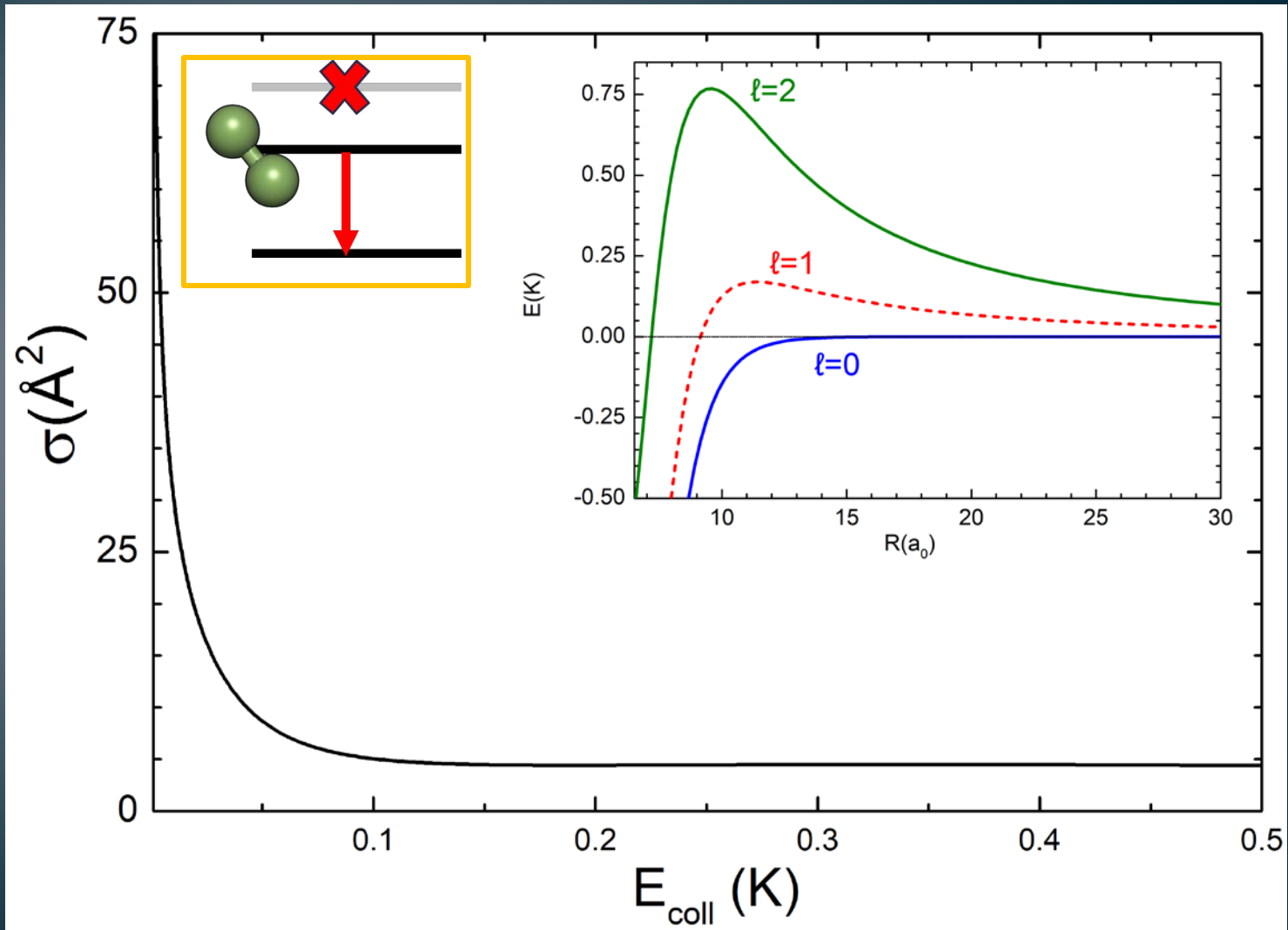


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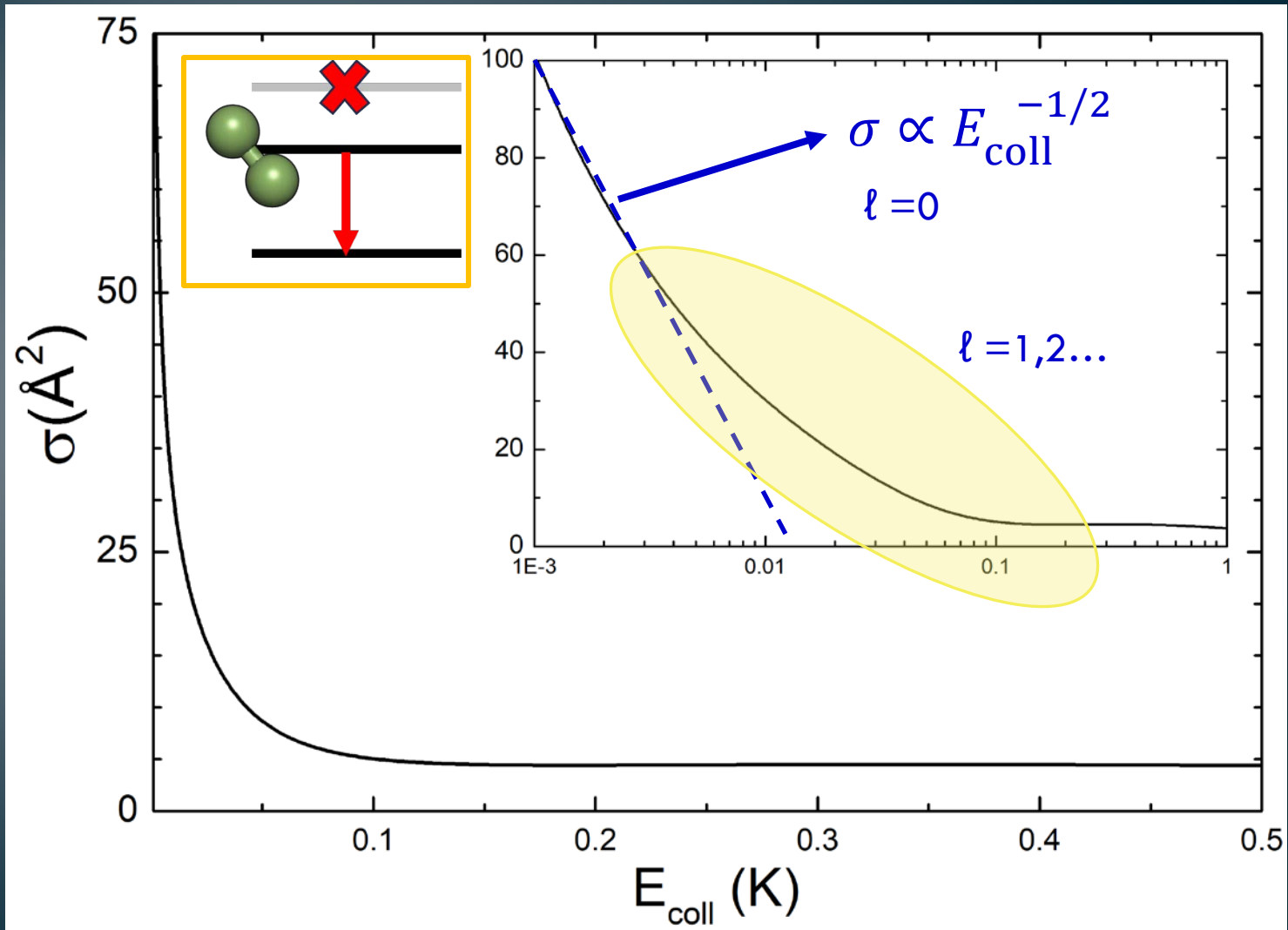




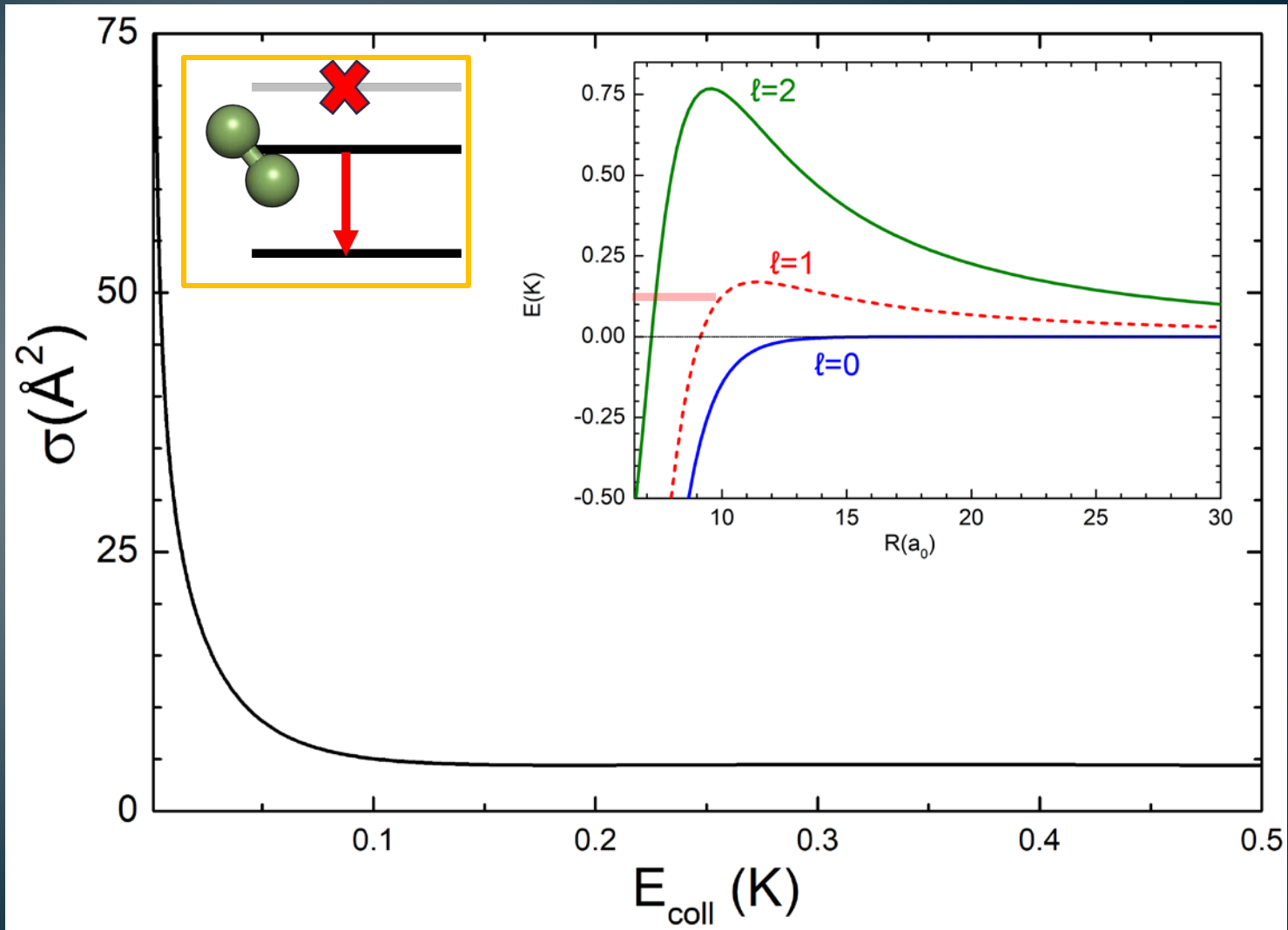
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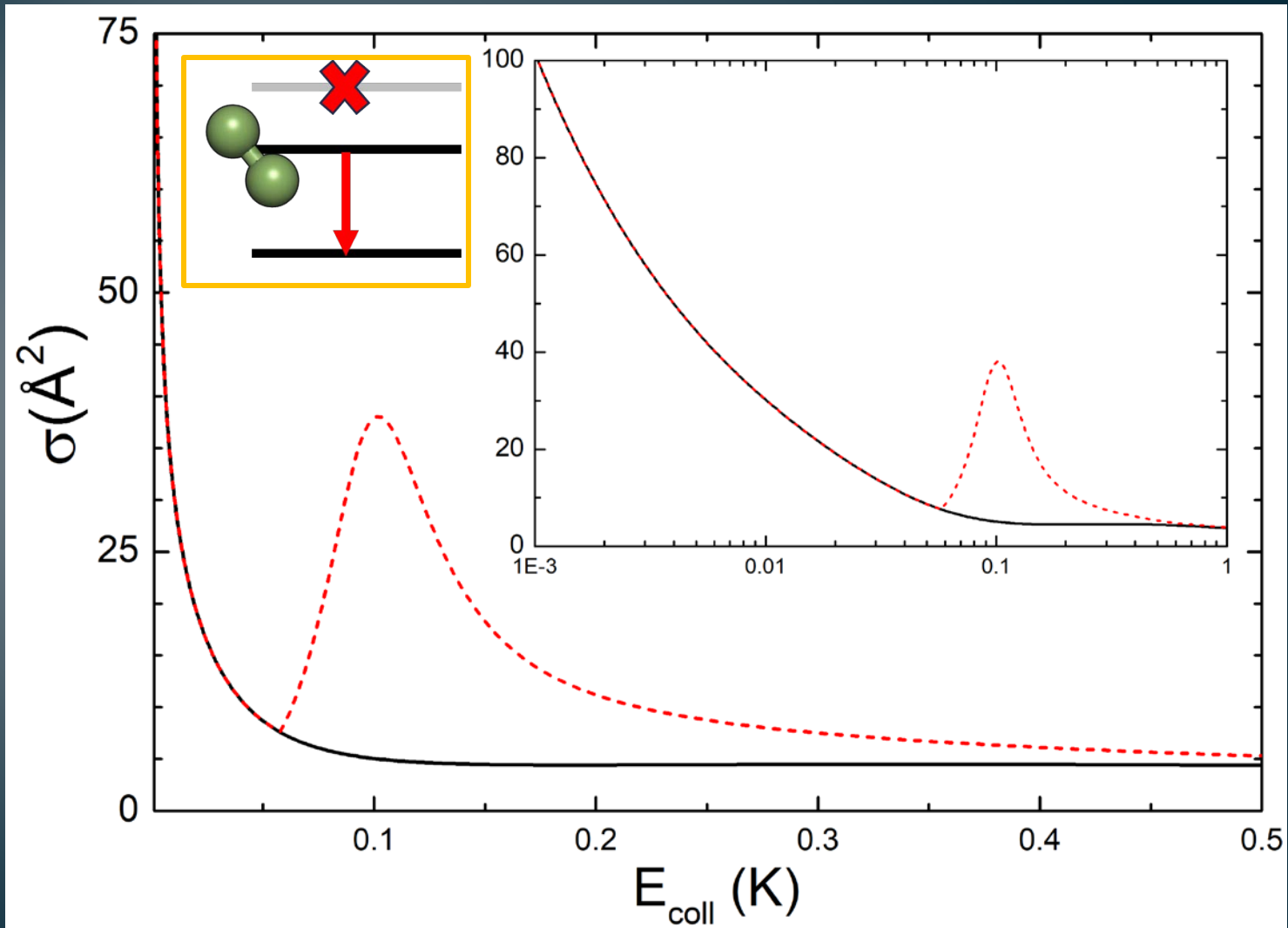
# Inelastic Collisions at low energies



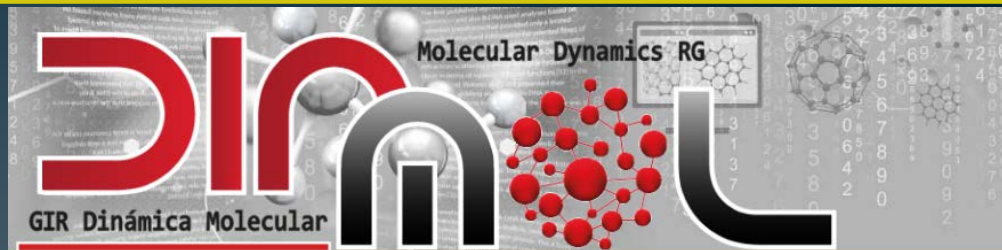
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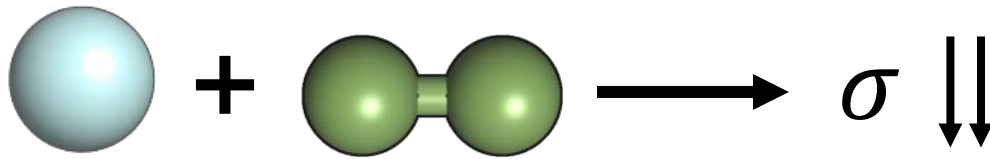
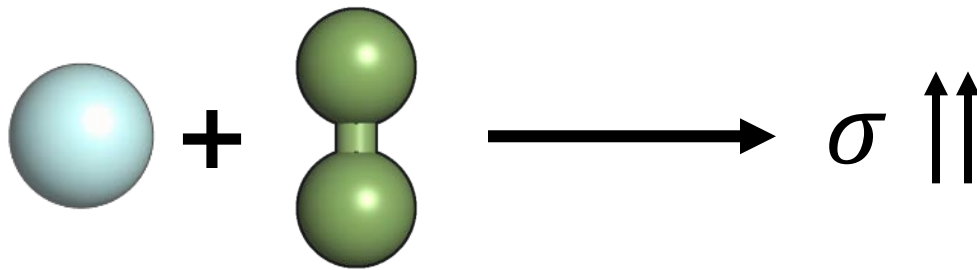
**Aim: Reproduce Experimental Measurements**

# What we would like to learn

- Can we talk about **collision mechanisms**?
- How could we define it? ( Even quantify it?, measure it? )
- **HANDICAP**: No trajectories (Quantum Scattering)

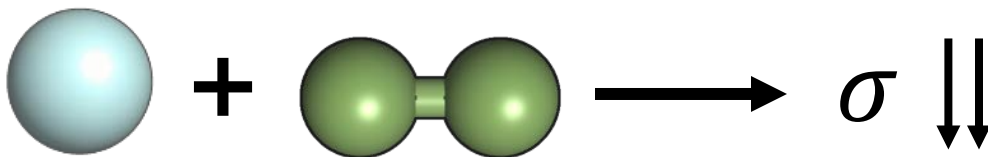
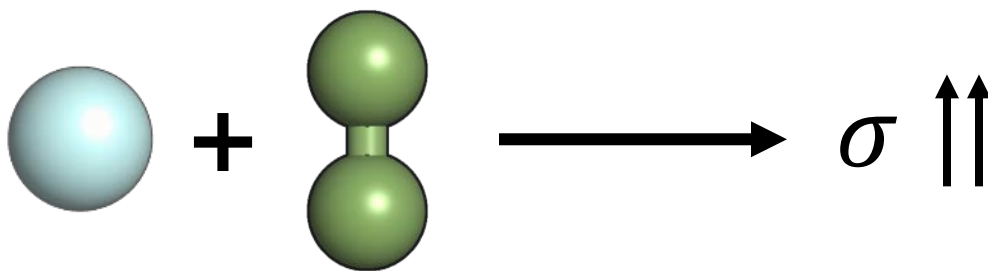
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# What we would like to learn

- How the collision **outcome** depends on the relative orientation/**alignment of the reactants**? What happens in the presence of quantum effects?



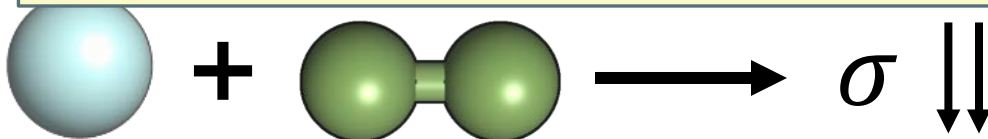


# What we would like to learn

- How the collision **outcome** depends on the relative orientation/**alignment of the reactants**? What happens in the presence of quantum effects?



It is experimentally possible to prepare aligned and/or oriented reactants



# SARP Experiment

## Quantum-Controlled Collisions of H<sub>2</sub> Molecules

Nandini Mukherjee\*

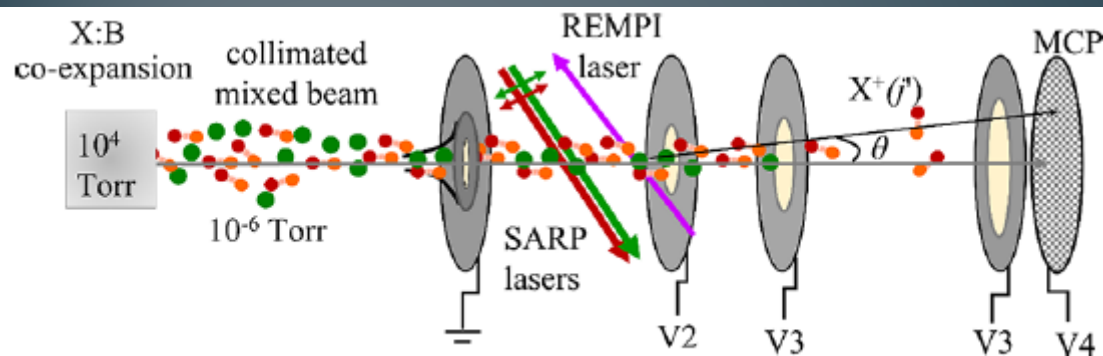


Cite This: <https://doi.org/10.1021/acs.jpca.2c06808>



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co-expansion beam experiments for which using Optical Raman Pumping is possible to prepare a pure  $|v, j, m=0\rangle$  state.  $m$ , determined regard to a laboratory frame (space-fixed).

Figure 3. Schematic of a cold scattering experiment within a co-expanded mixed supersonic beam containing the colliding partners (X and B). Polarized SARP laser beams (red and green) prepare the target molecule X (H<sub>2</sub>, HD, or D<sub>2</sub>) in a given rovibrational  $m$  eigenstate ( $v, j, m$ ), where  $m$  refers to the projection of the rotational angular momentum  $j$  along the molecular beam direction. The colliding partner B (He, Ne, H<sub>2</sub>, D<sub>2</sub>, or HD) is left unprepared. The collision product is ionized state-selectively using REMPI with tunable vacuum ultraviolet pulses and detected on a multichannel plate (MCP) following a passage through the time-of-flight mass spectrometer, which is attached to the

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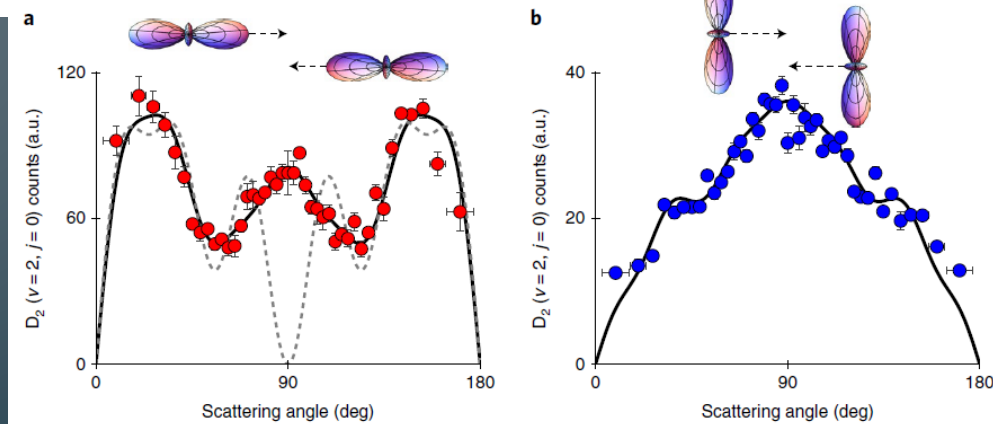
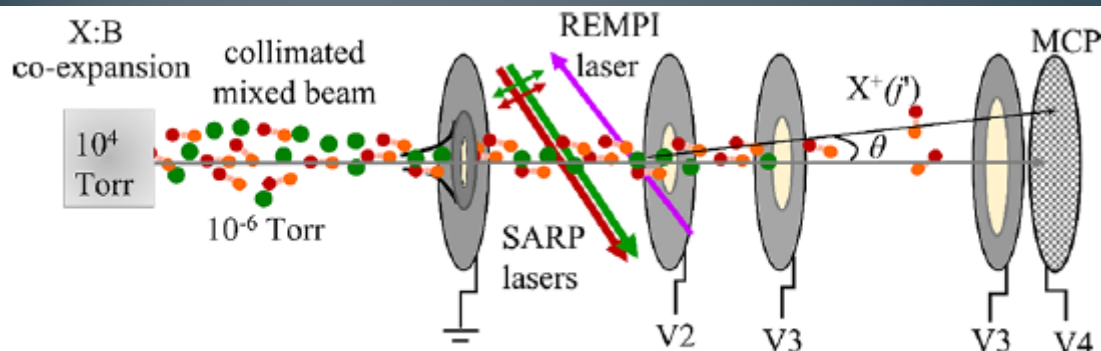


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Zhou et al., *Nature Chemistry*, 14, 658–663 (2022)

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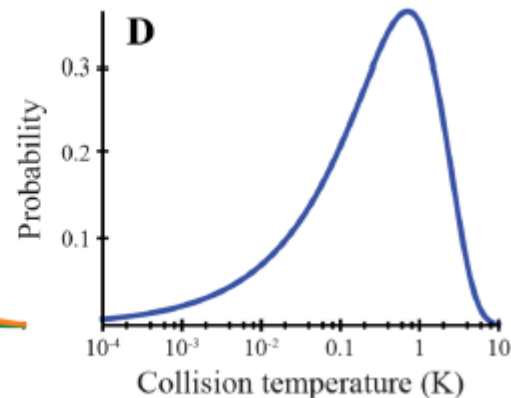
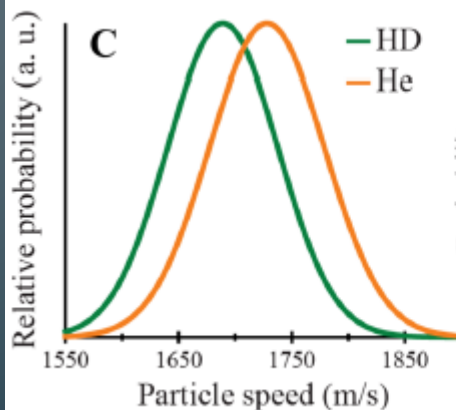
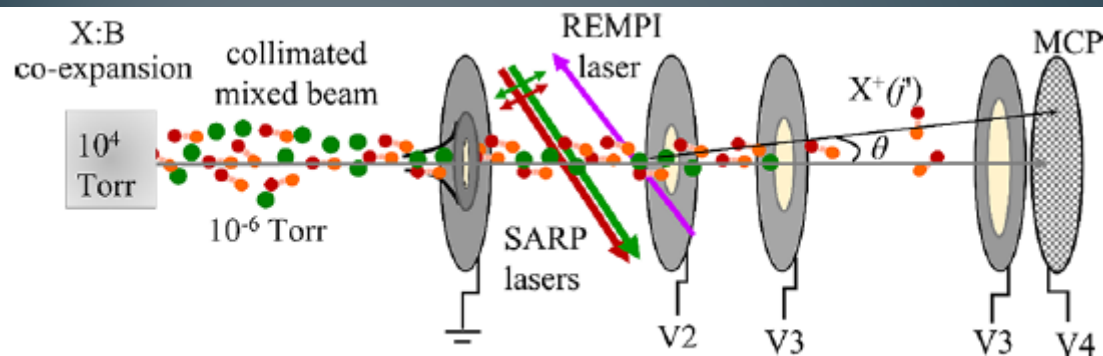


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# SARP Experiment

RESEARCH

CHEMICAL PHYSICS

## Quantum control of molecular collisions at 1 kelvin

William E. Perreault, Nandini Mukherjee,\* Richard N. Zare\*

nature  
chemistry

ART

<https://doi.org/10.1038/s41557-022-0028-5>

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## Quantum Controlled Cold Scattering Challenges Theory

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RESEARCH

QUANTUM MECHANICS

## Quantum mechanical double slit for molecular scattering

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Very stringent test for  
calculations

# SARP Experiment. 4 e<sup>-</sup> systems



# SARP Experiment. $4 e^-$ systems



- **Conclusions:**

- For both systems they infer the presence of an intense  $\ell=2$  resonance
- For  $D_2 + D_2$  only collisions between aligned-aligned molecules are relevant



# SARP Experiment. 4 e<sup>-</sup> systems



- Inelastic collisions
- 6D PES (probably rigid rotor also works)
- No open-shell fragments
- Very accurate PES



- Inelastic collisions
- 3D PES (probably rigid rotor also works)
- No open-shell fragments
- Very accurate PES

# SARP Experiment. 4 e<sup>-</sup> systems



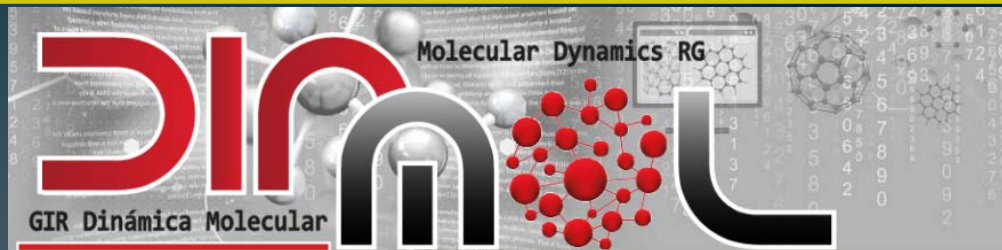
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- Inelastic collisions
- 3D PES (probably rigid rotor also works)
- No open-shell fragments
- Very accurate PES

- But cold energies require very high accuracy
- And we need the machinery to make calculations for non-isotropic reactants

# Outline:

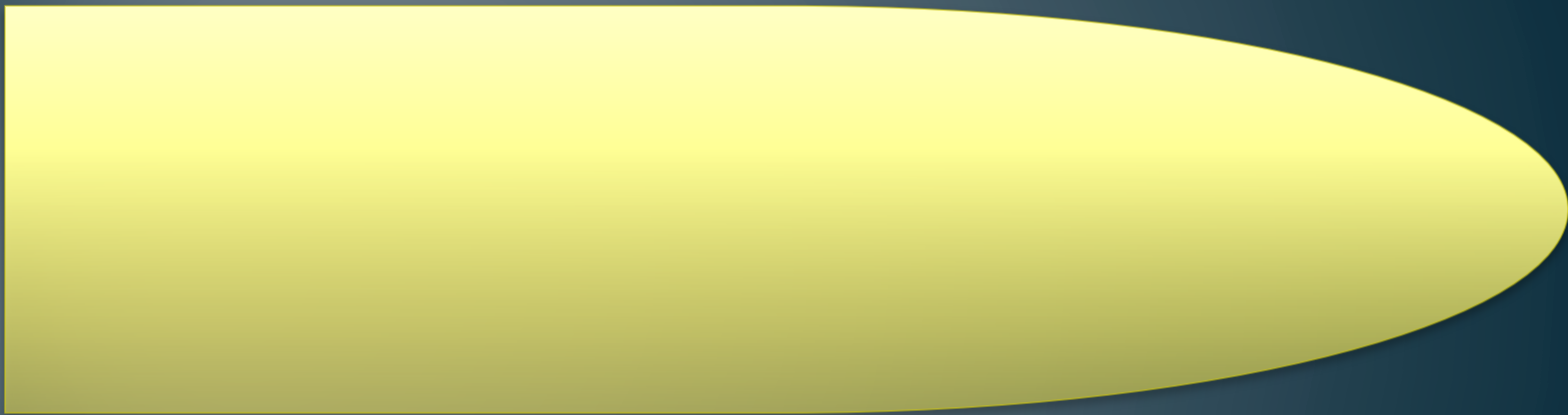


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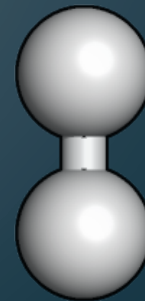
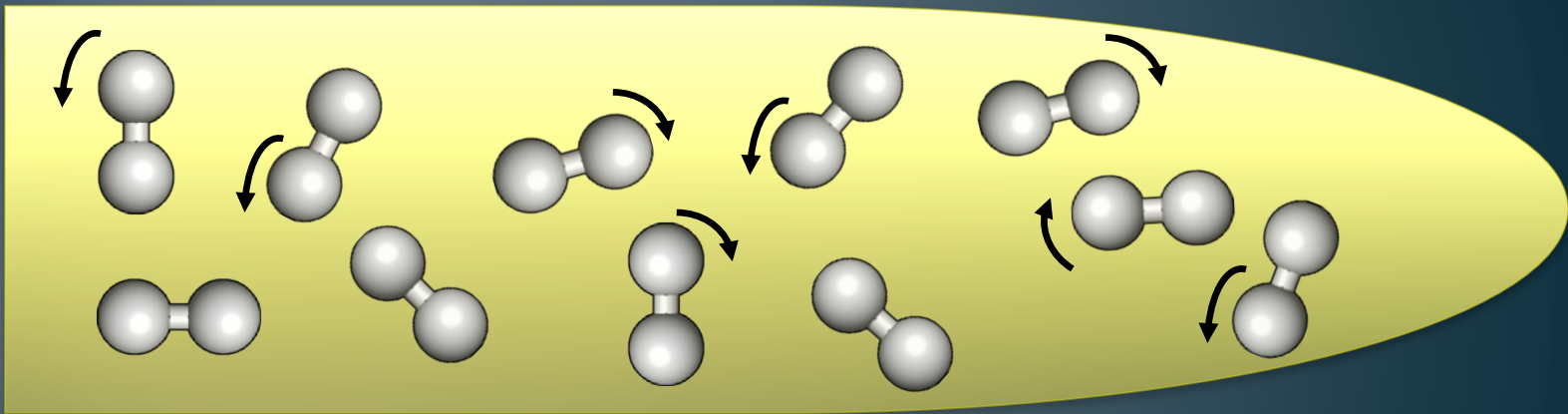
# $D_2 + D_2$ collisions

propagation axis of the molecular beam



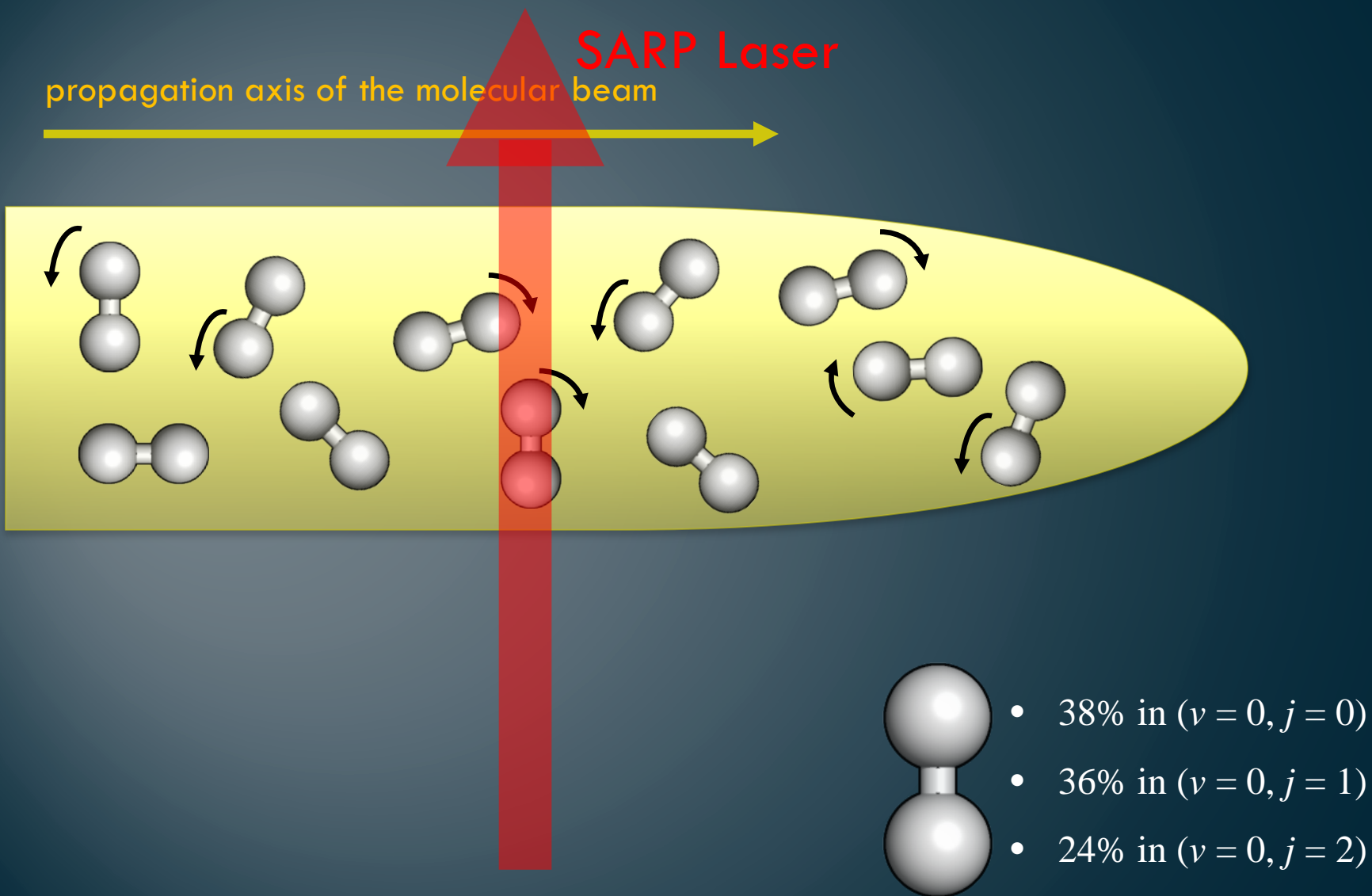
# $D_2 + D_2$ collisions

propagation axis of the molecular beam



- 38% in  $(v = 0, j = 0)$
- 36% in  $(v = 0, j = 1)$
- 24% in  $(v = 0, j = 2)$

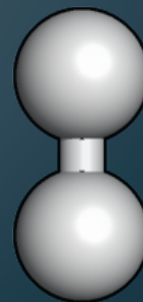
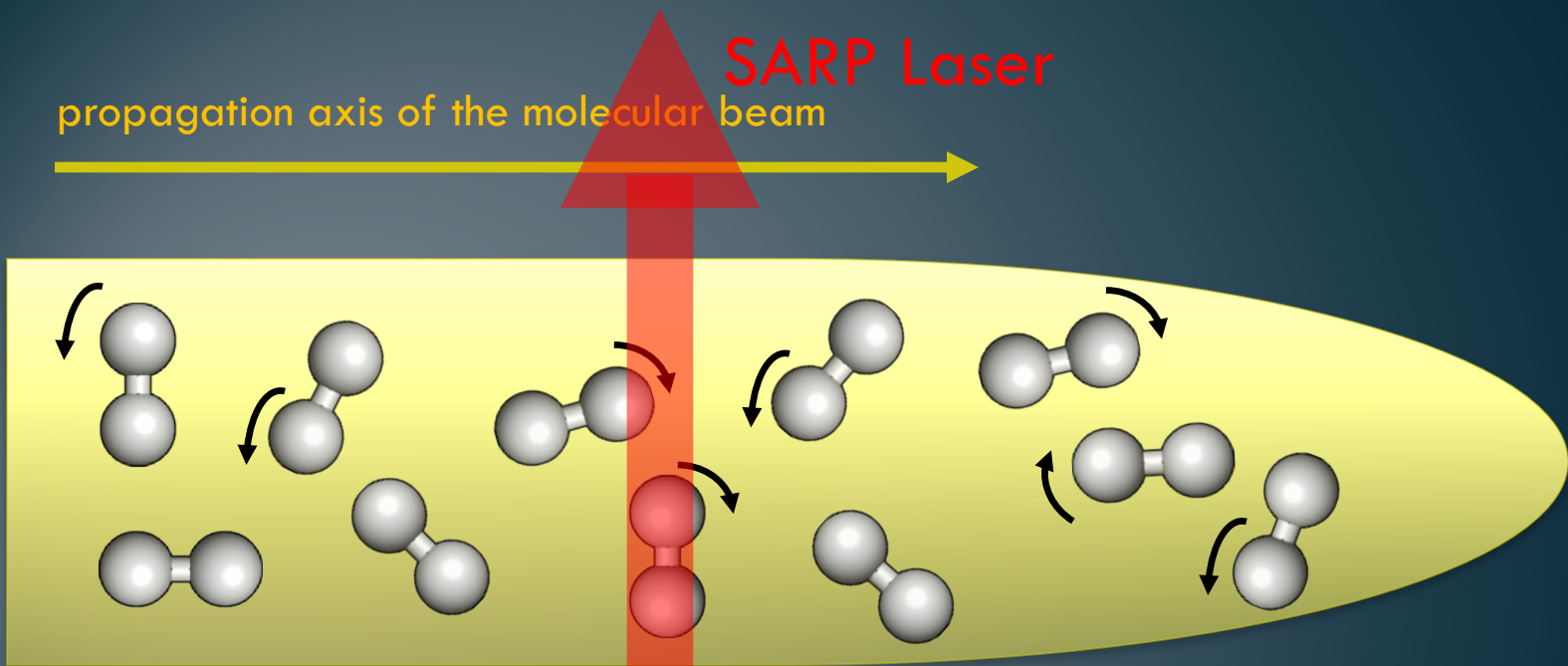
# $D_2 + D_2$ collisions



# D<sub>2</sub> + D<sub>2</sub> collisions

SARP Laser

propagation axis of the molecular beam



• 38% in ~~(v = 0, j = 0)~~

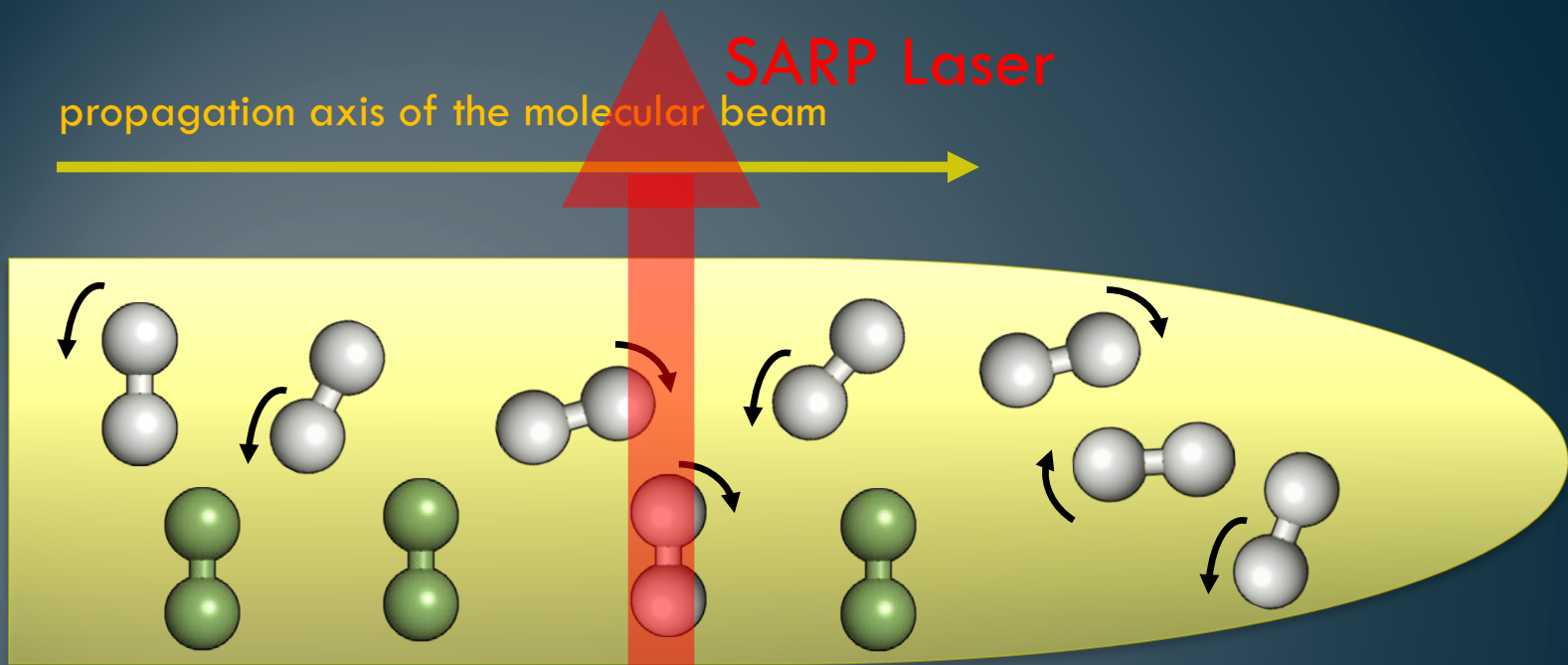
• 36% in (v = 0, j = 1)

• 24% in (v = 0, j = 2)

# $D_2 + D_2$ collisions

SARP Laser

propagation axis of the molecular beam



Aligned



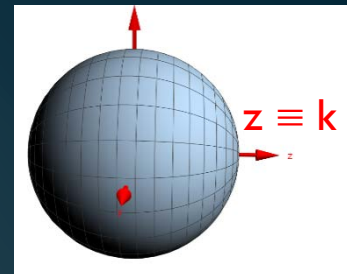
• 38% in  $(v=2, j=2)$

• 36% in  $(v=0, j=1)$

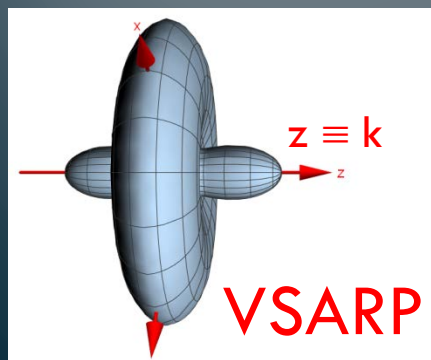
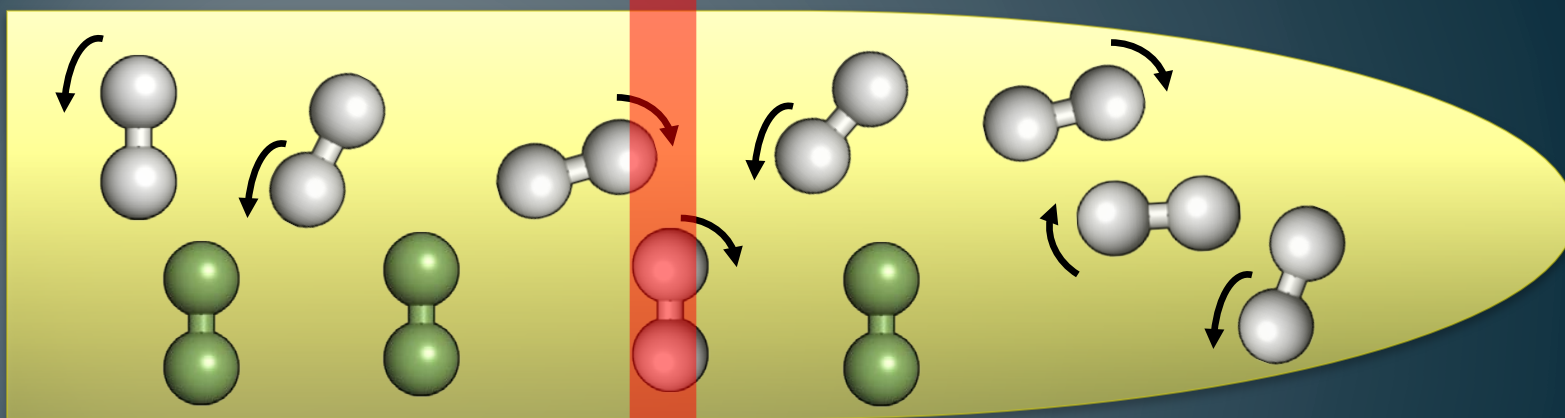
• 24% in  $(v=0, j=2)$



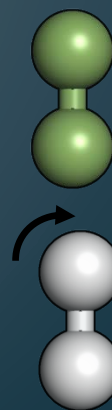
# D<sub>2</sub> + D<sub>2</sub> collisions



SARP Laser  
propagation axis of the molecular beam



Aligned

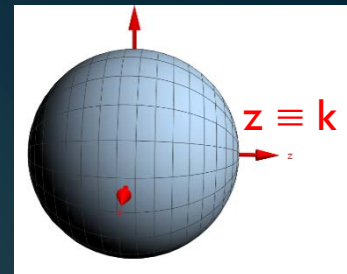


• 38% in ( $v = 2, j = 2$ )

• 36% in ( $v = 0, j = 1$ )

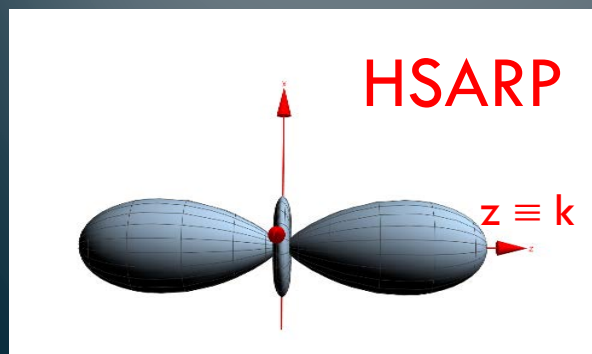
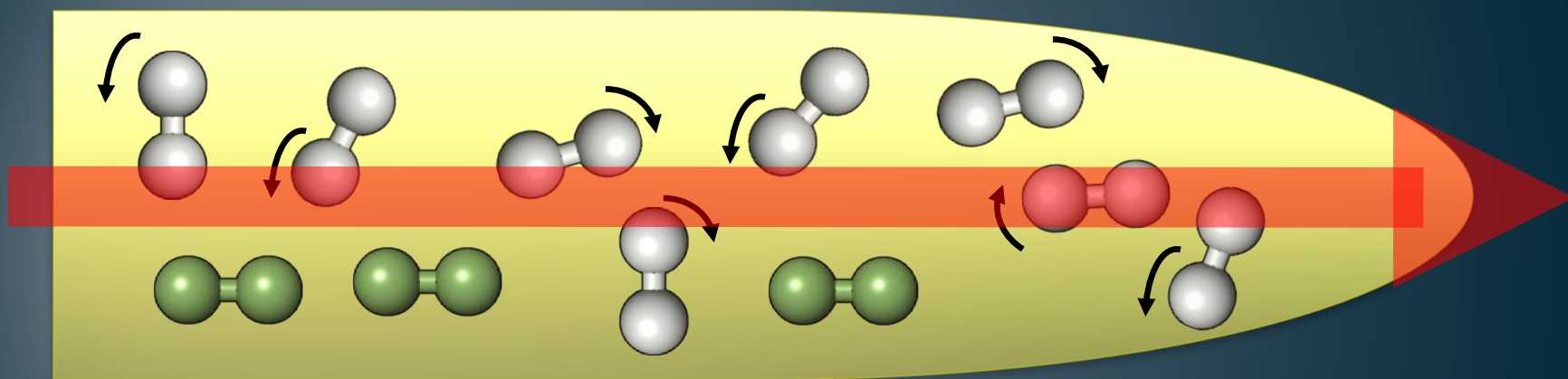
• 24% in ( $v = 0, j = 2$ )

# D<sub>2</sub> + D<sub>2</sub> collisions



SARP Laser

propagation axis of the molecular beam



Aligned

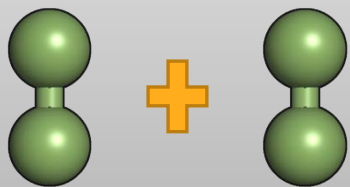


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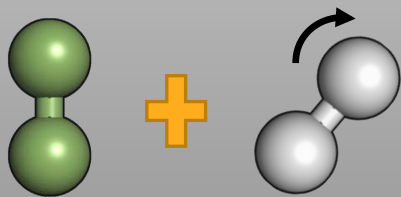
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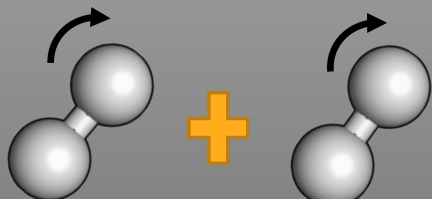
# $D_2 + D_2$ collisions



$(v = 2, j = 2) + (v = 2, j = 2)$

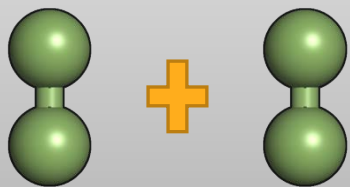


$(v = 2, j = 2) + (v = 0, j = 1, 2)$



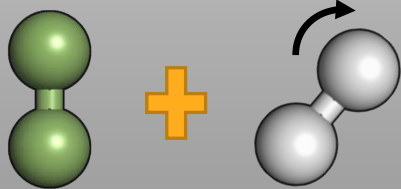
$(v = 0, j = 1, 2) + (v = 0, j = 1, 2)$

# $D_2 + D_2$ collisions



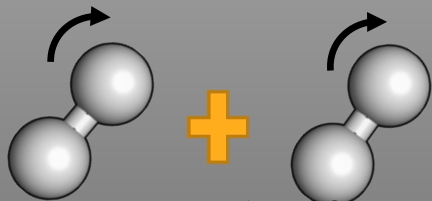
+

$(v = 2, j = 2)$   $(v = 2, j = 2)$



+

$(v = 2, j = 2)$   $(v = 0, j = 1, 2)$



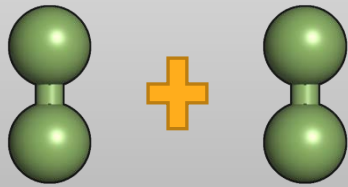
+

$(v = 0, j = 1, 2)$   $(v = 0, j = 1, 2)$

Detect  $(v=2, j=0)$

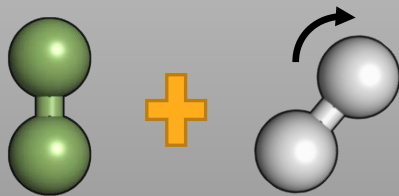


# $D_2 + D_2$ collisions



$(v = 2, j = 2)$   $(v = 2, j = 2)$

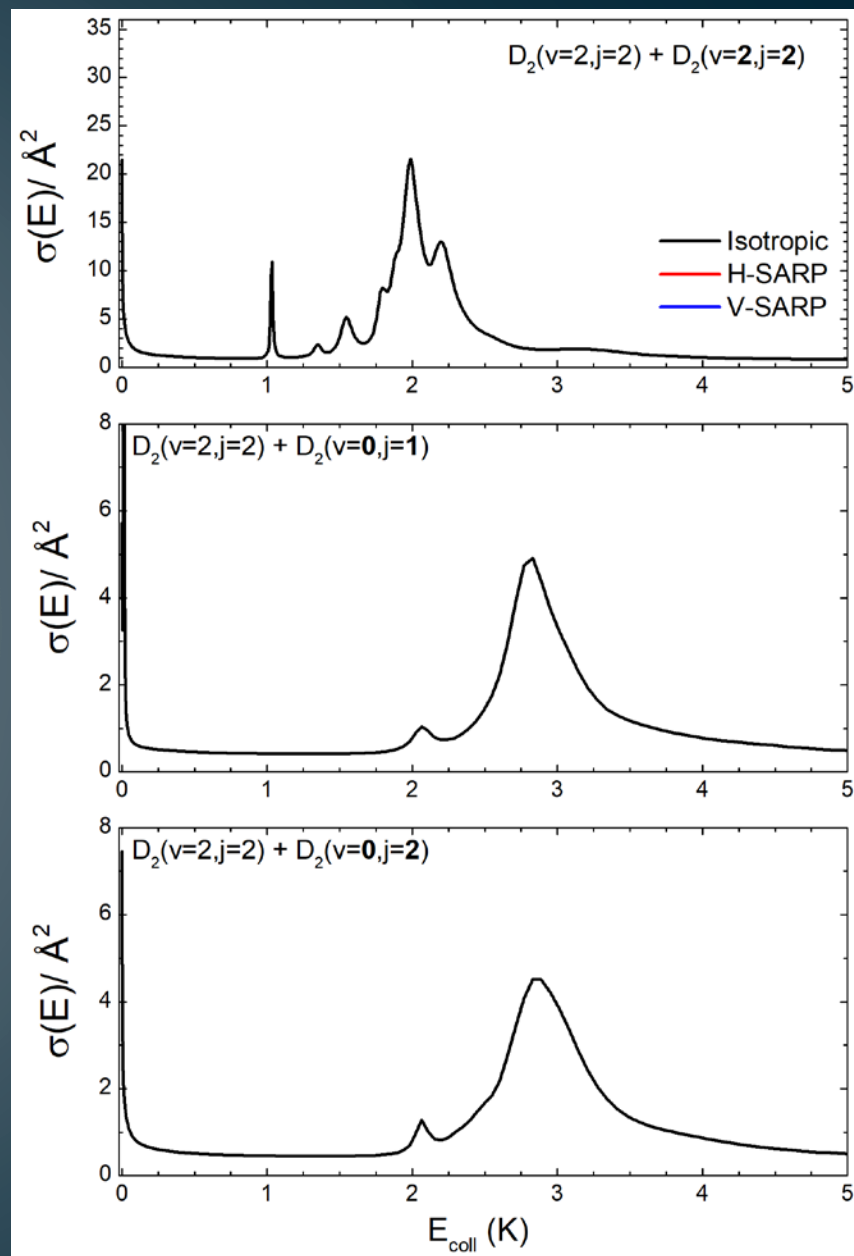
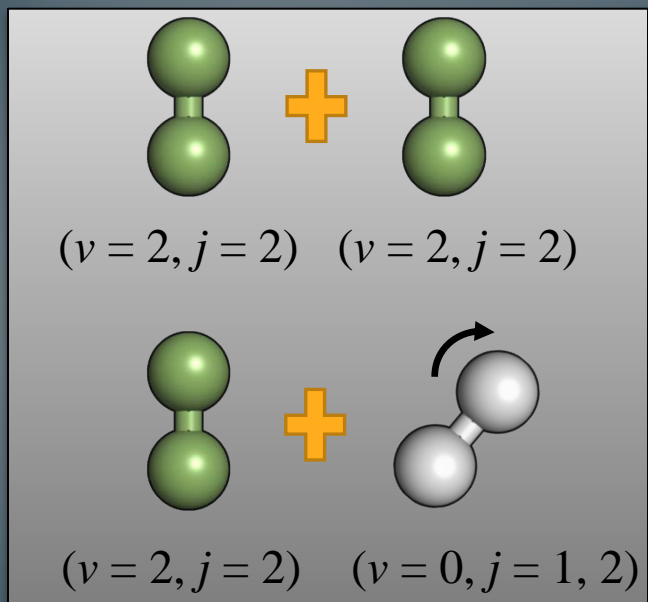
4-vector correlations ( $k-i_1-i_2-k'$ )



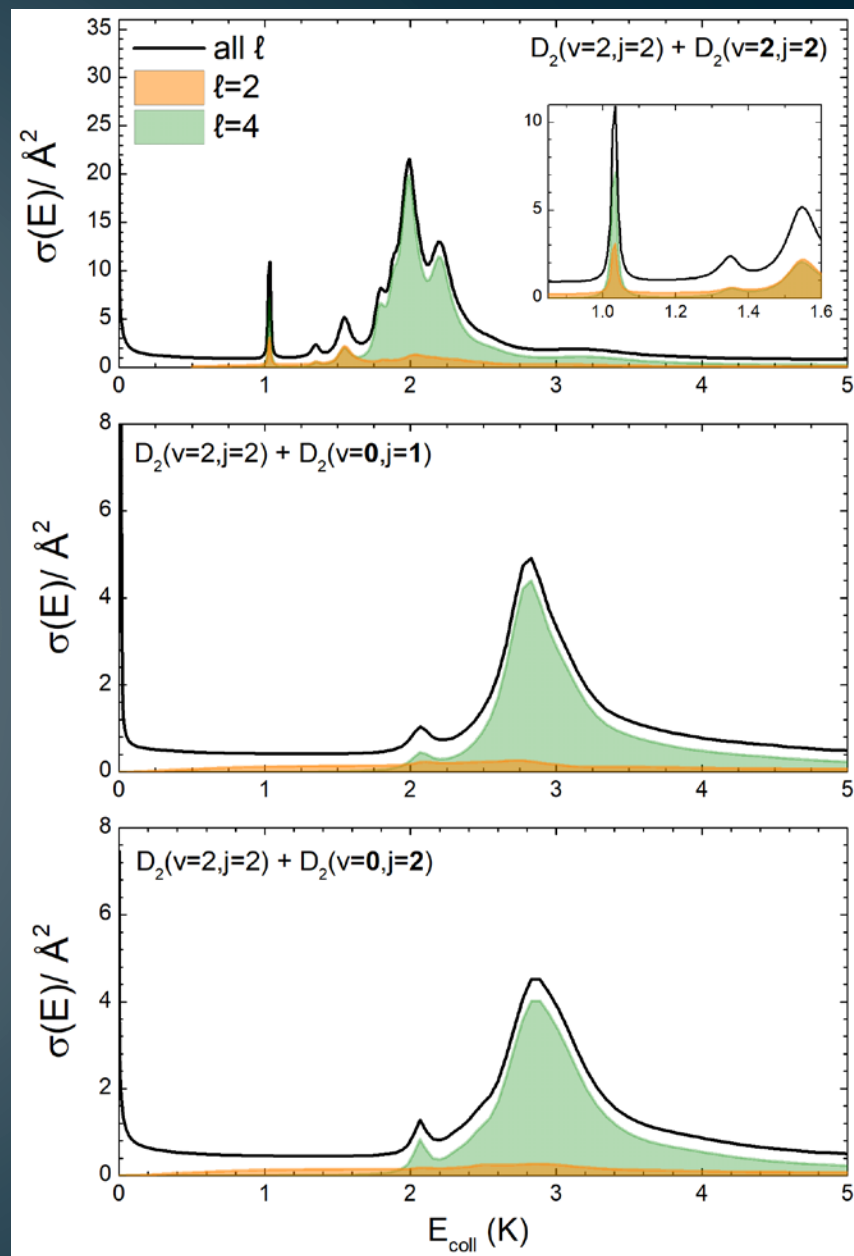
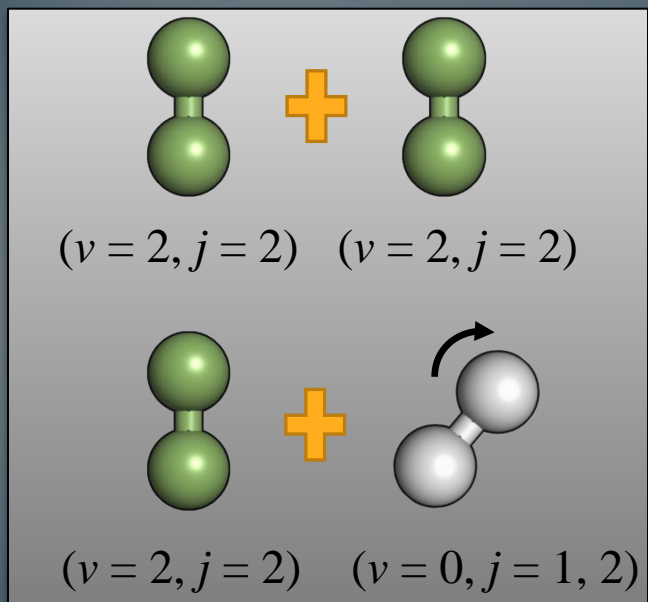
$(v = 2, j = 2)$   $(v = 0, j = 1, 2)$

3-vector correlations ( $k-i_1-k'$ )

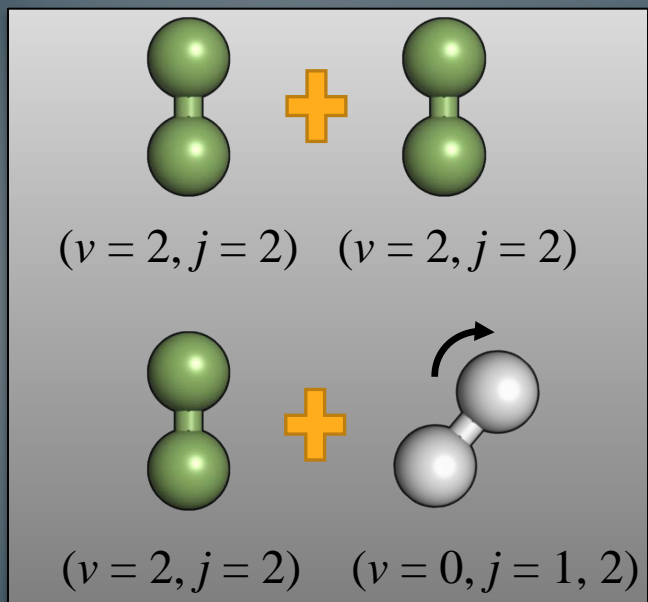
# D<sub>2</sub> + D<sub>2</sub> collisions



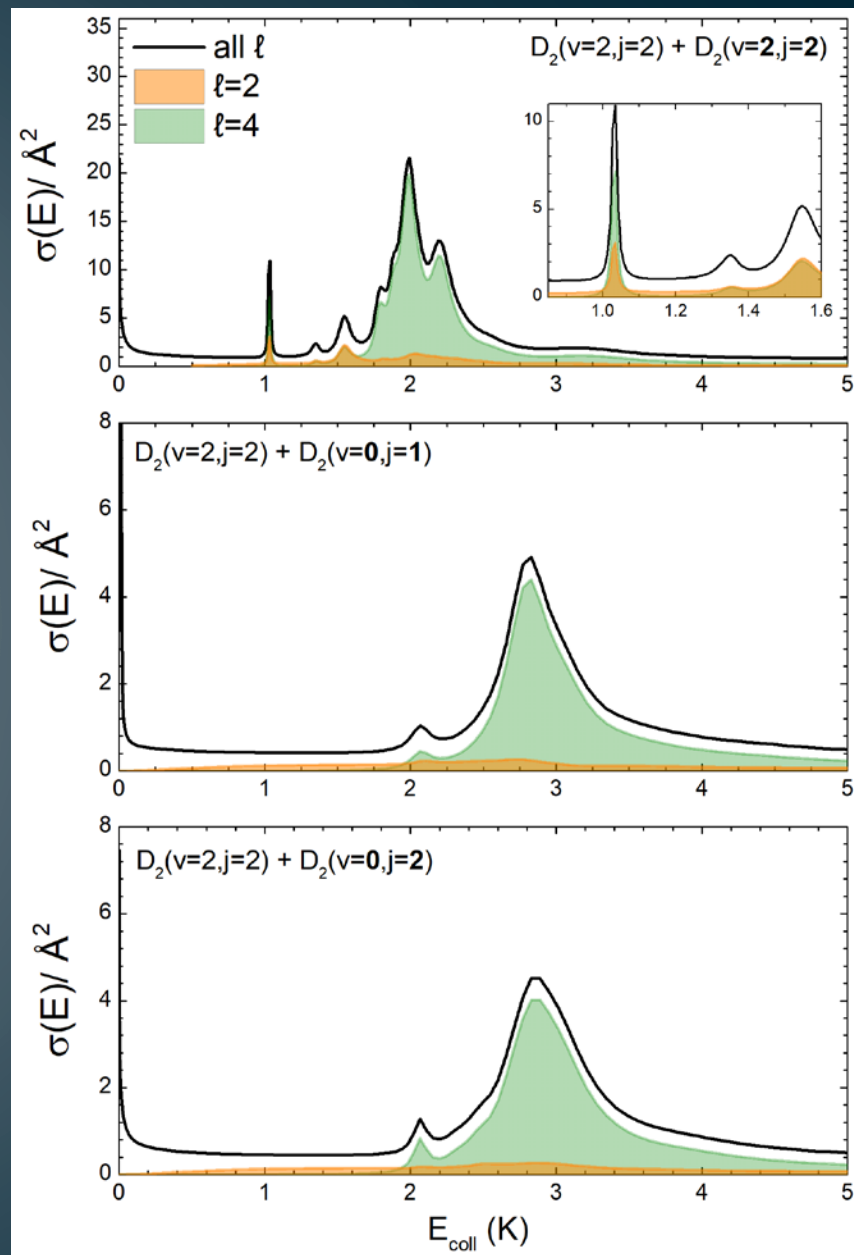
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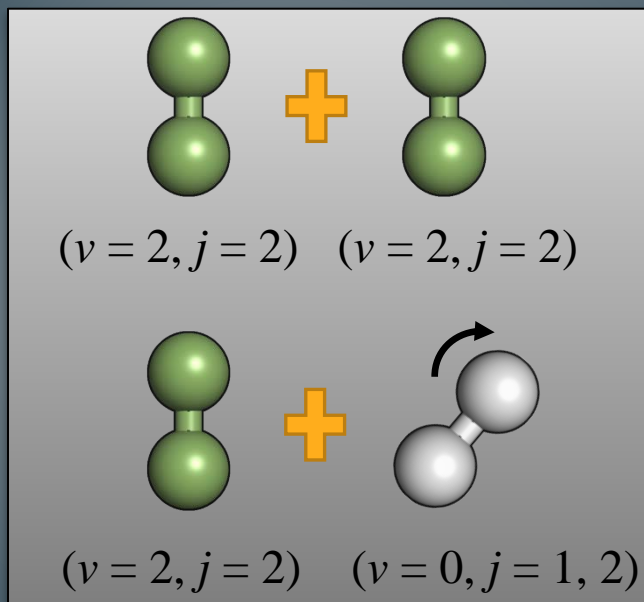


$\ell=2$

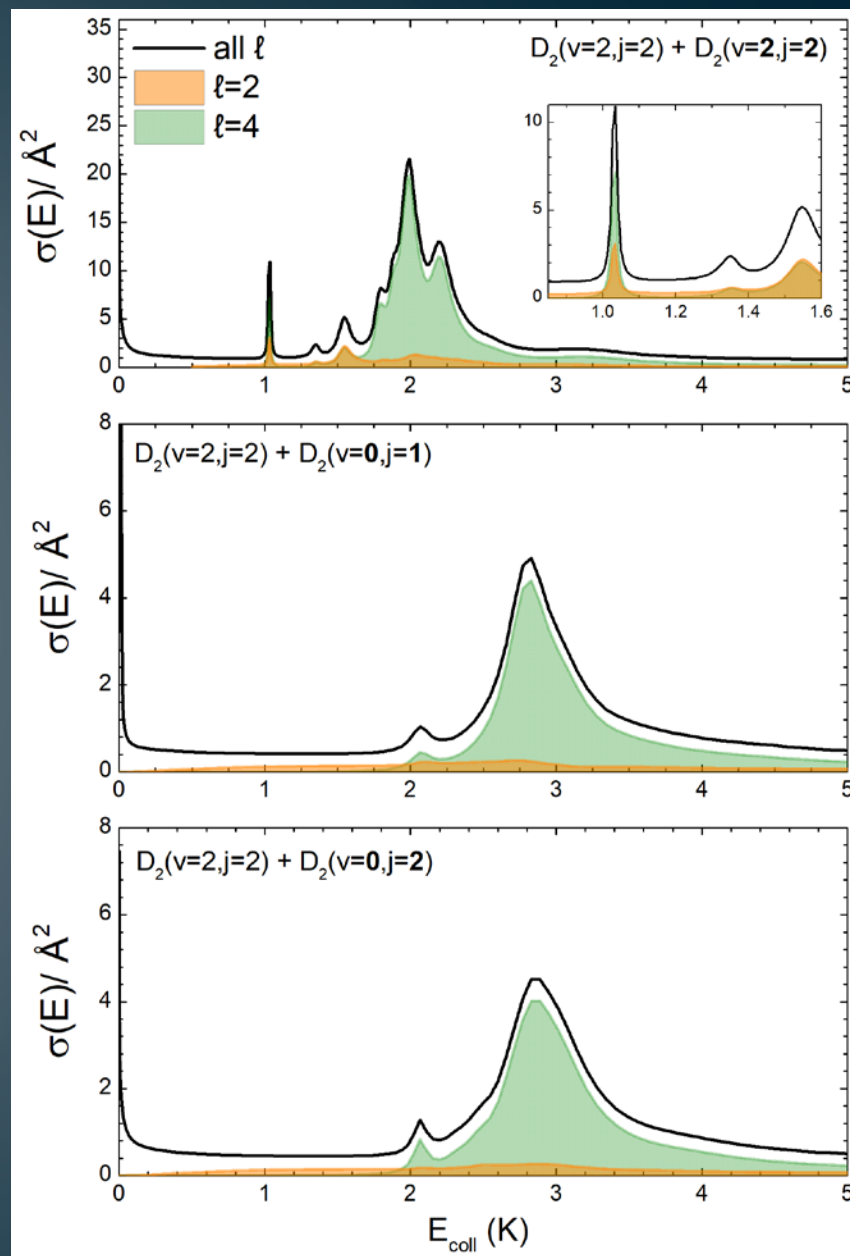




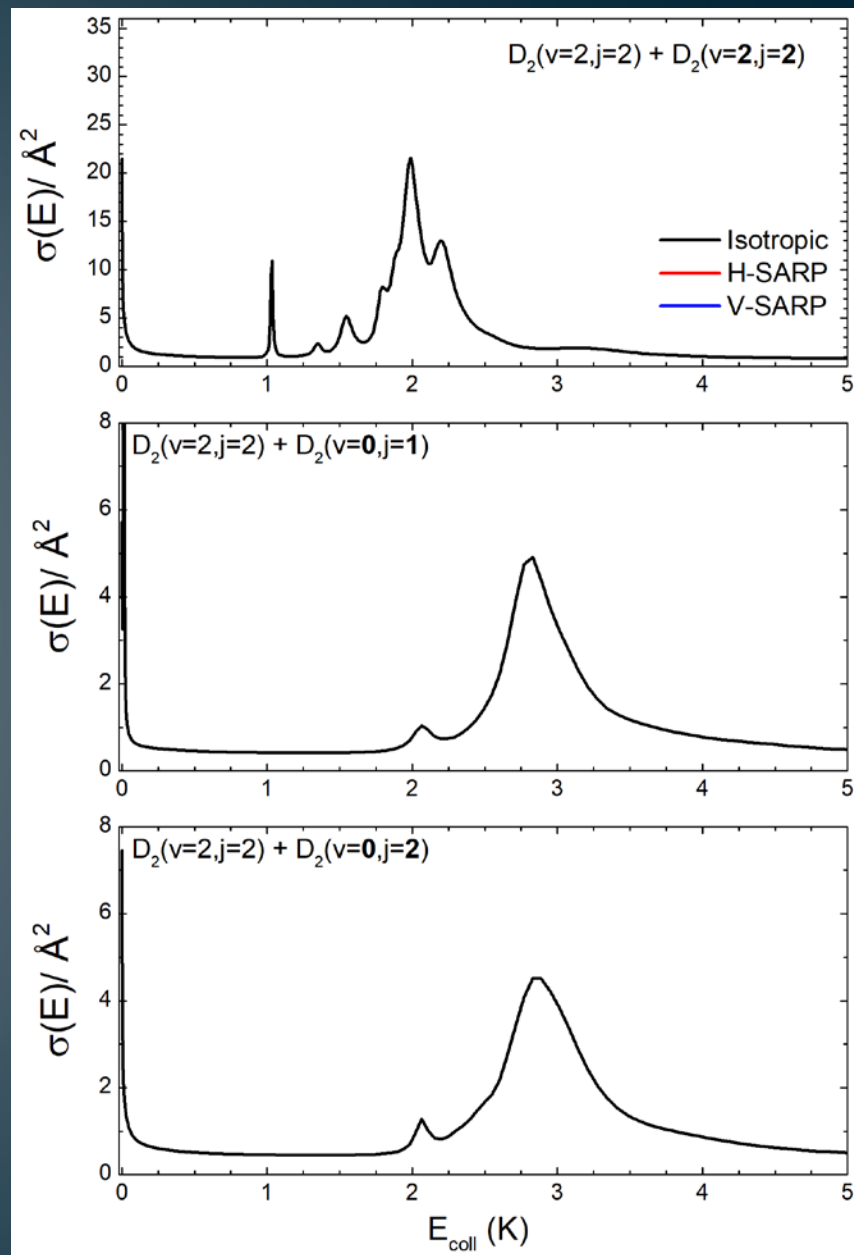
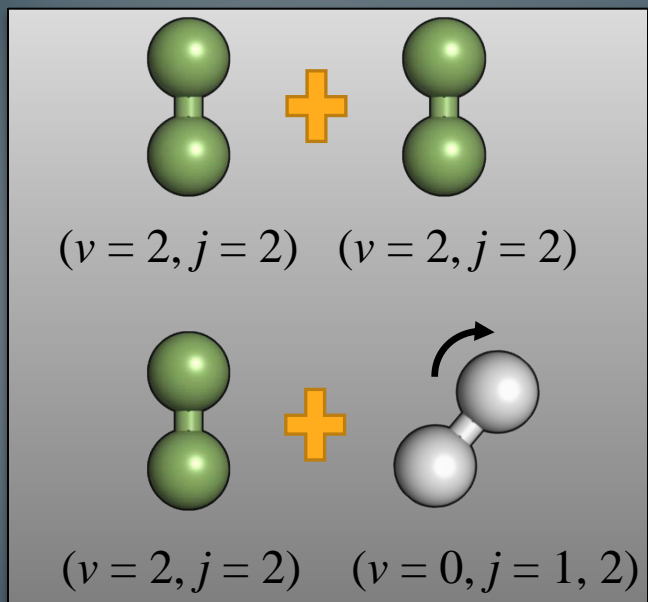
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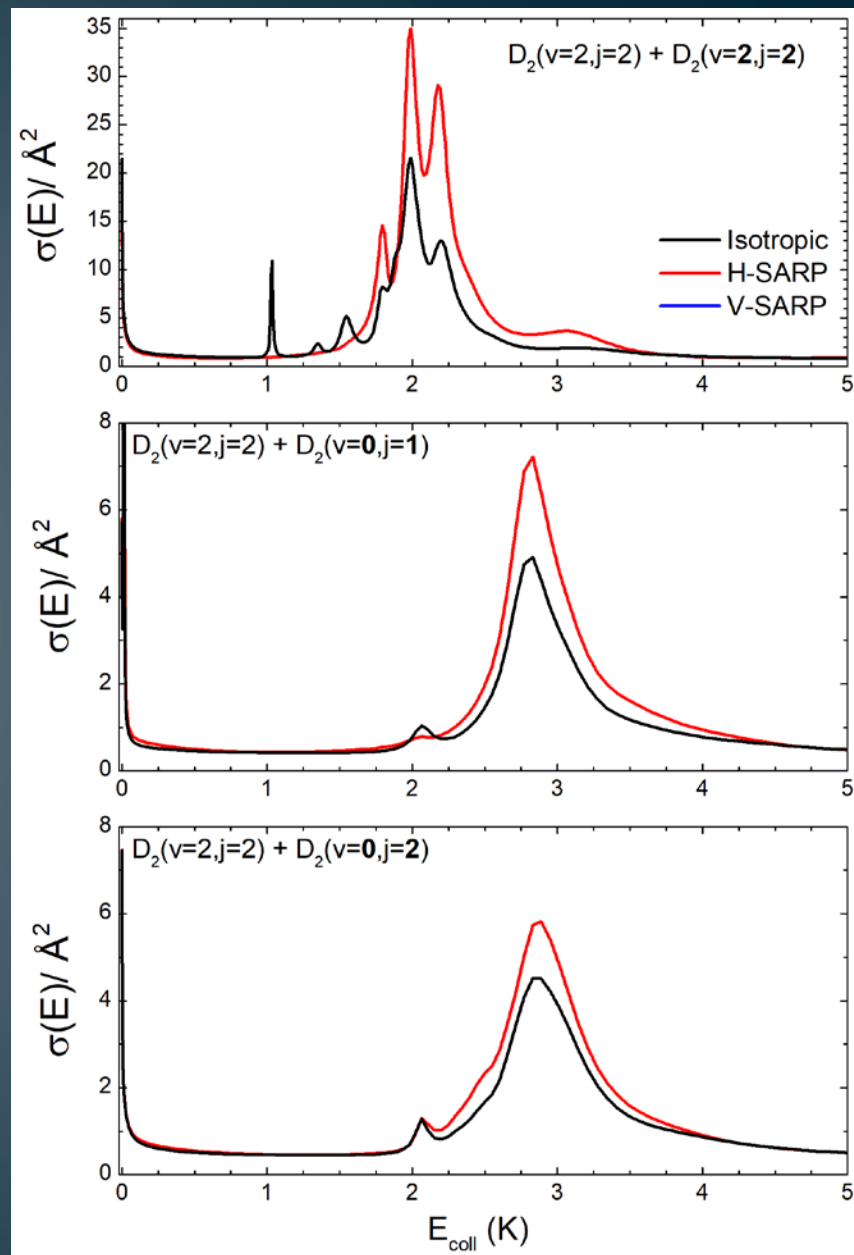
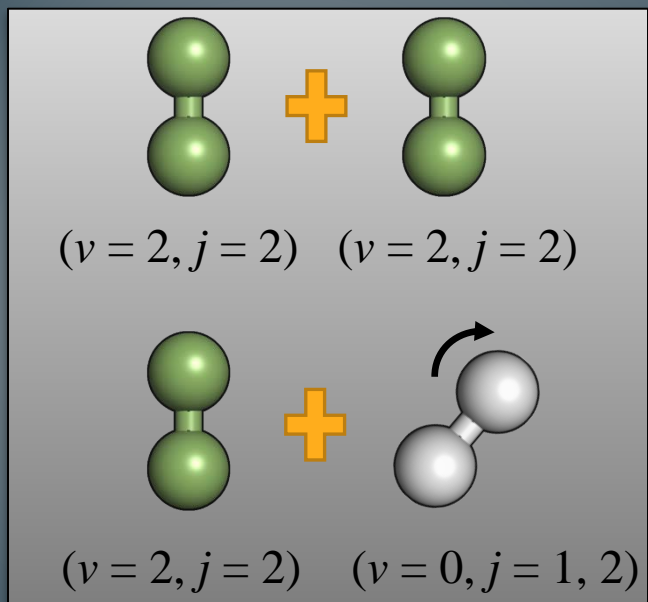
~~$\ell=2$~~     $\ell=4$



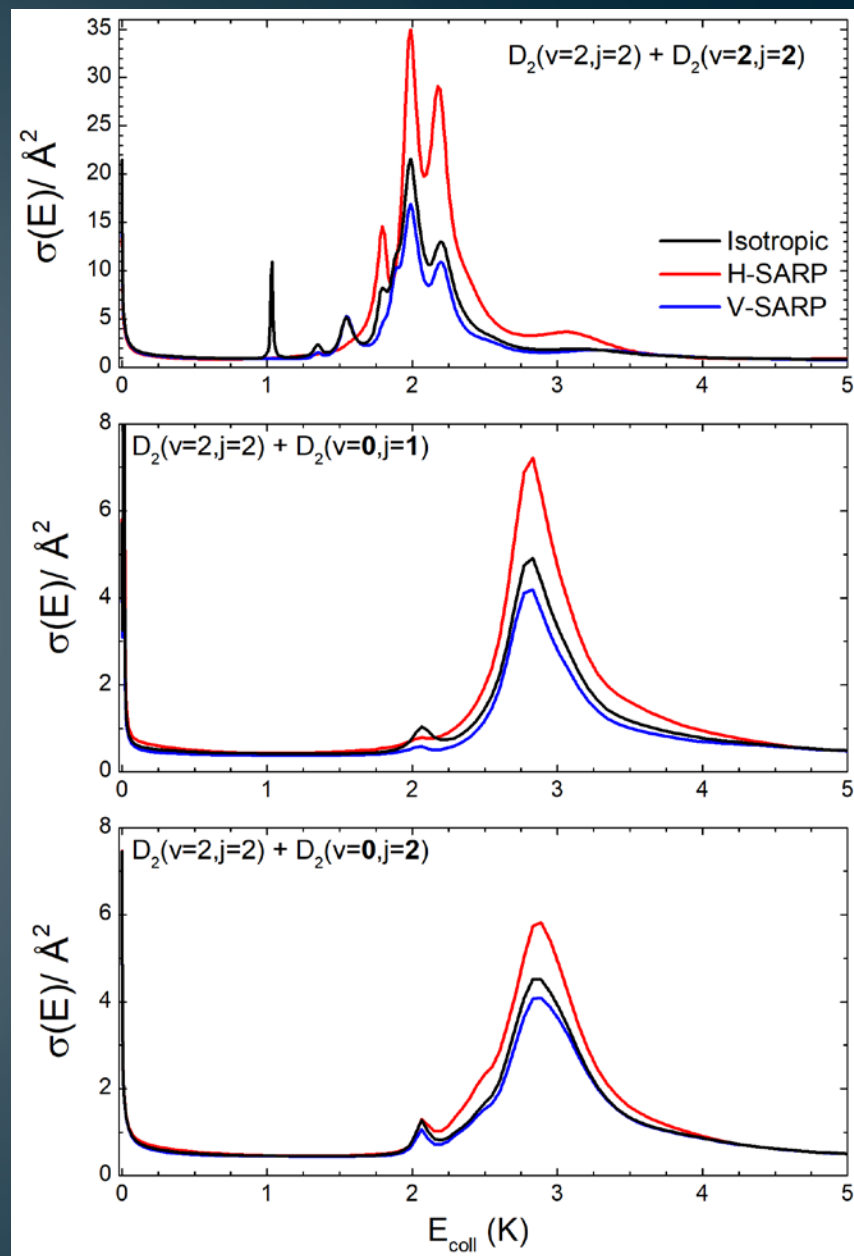
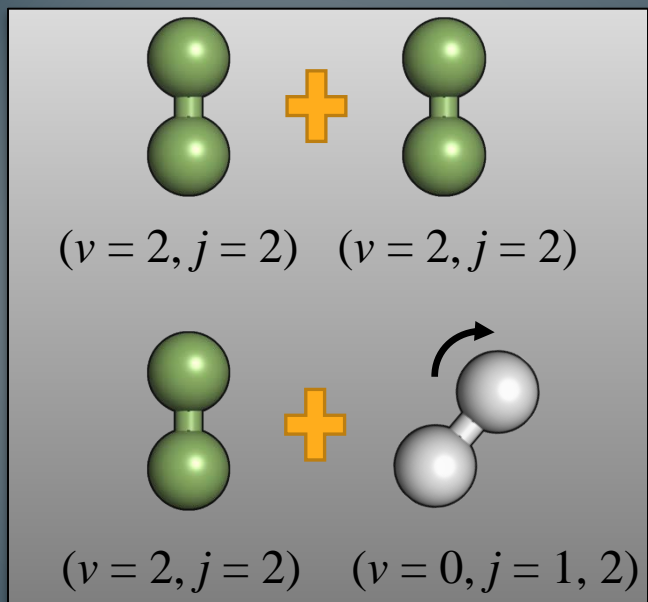
# D<sub>2</sub> + D<sub>2</sub> collisions



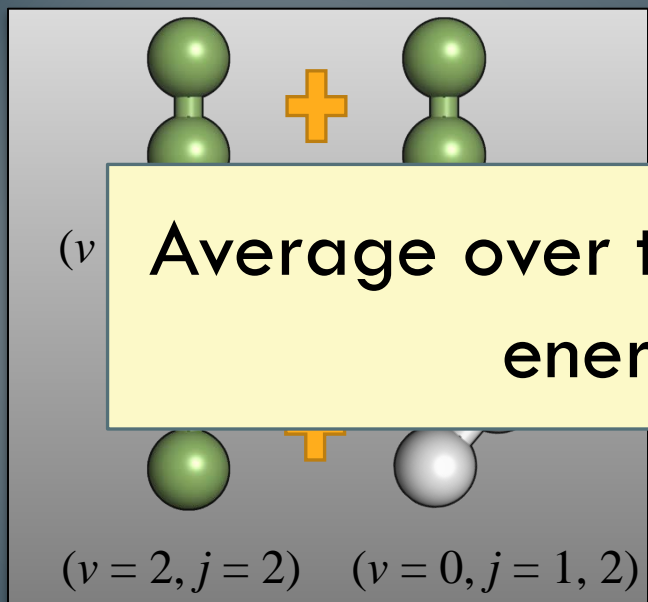
# D<sub>2</sub> + D<sub>2</sub> collisions



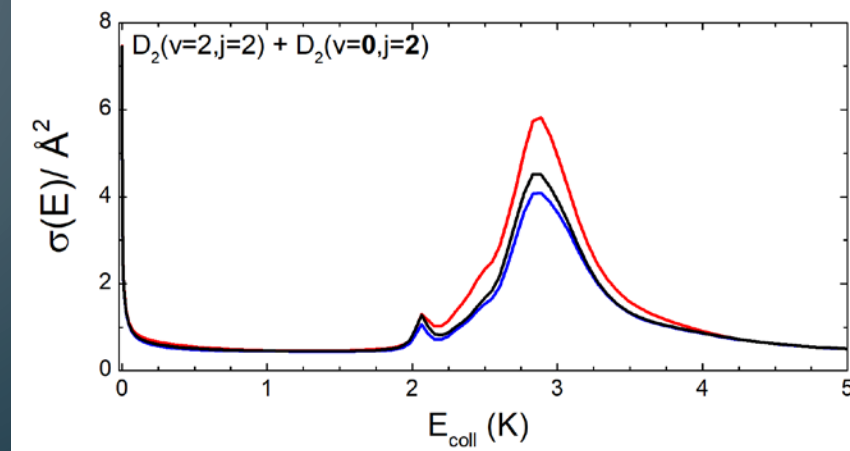
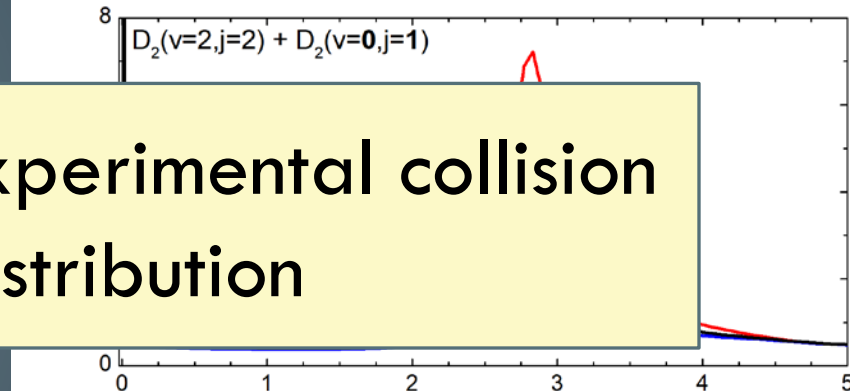
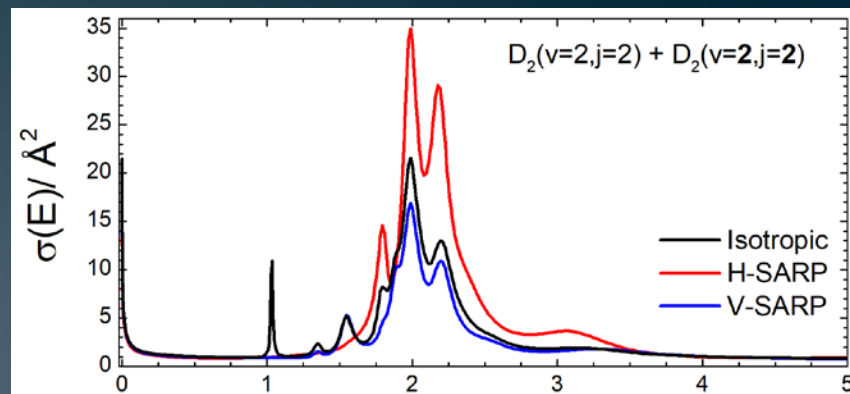
# D<sub>2</sub> + D<sub>2</sub> collisions



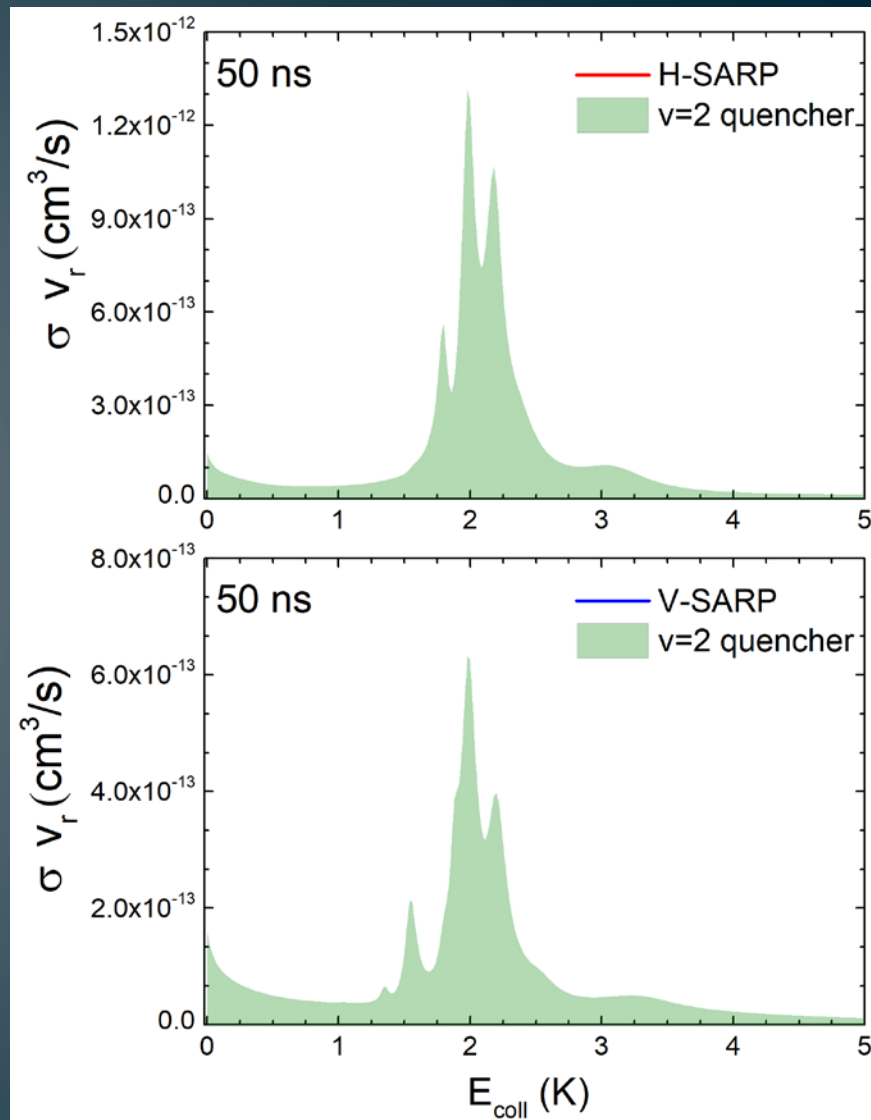
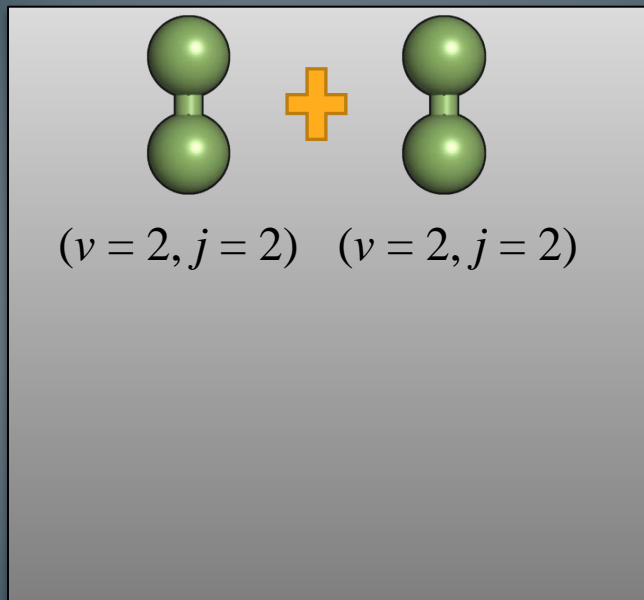
# D<sub>2</sub> + D<sub>2</sub> collisions



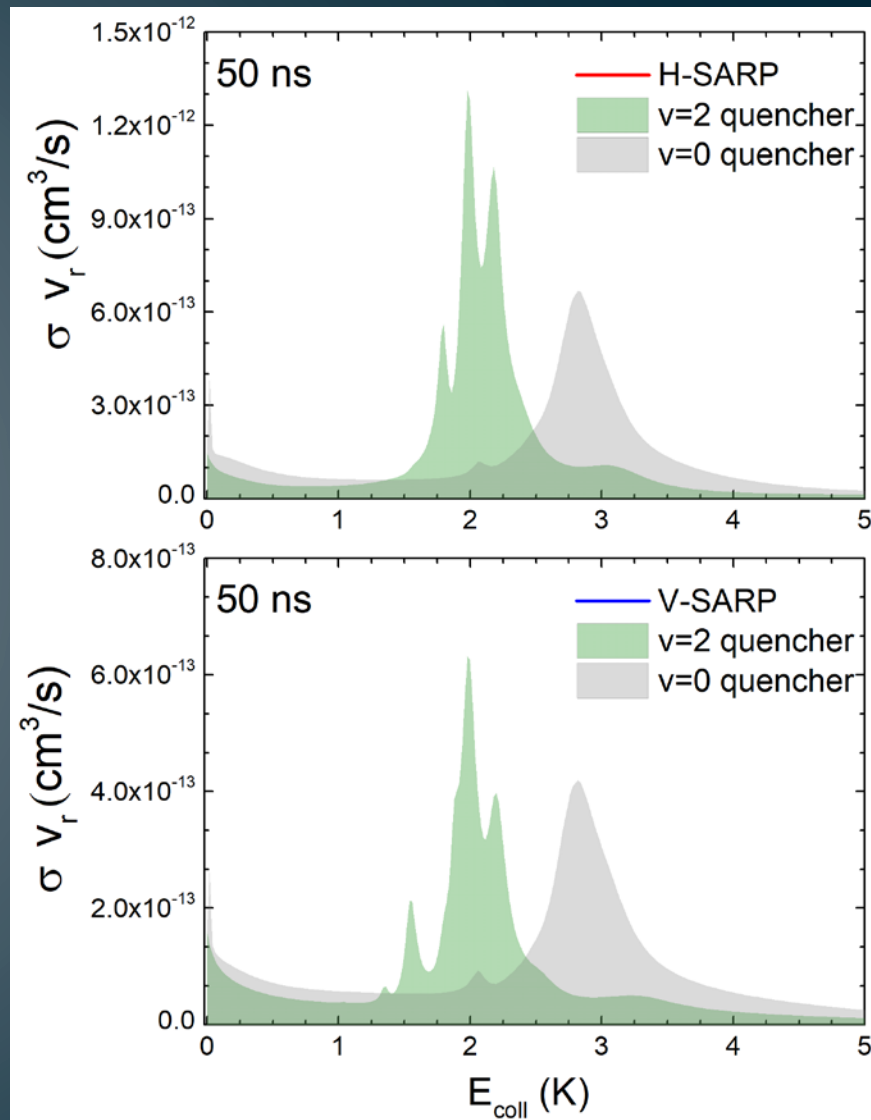
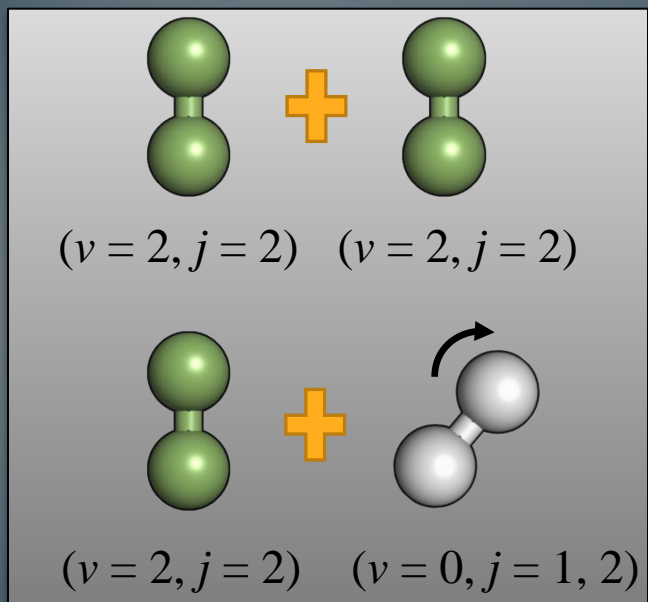
Average over the Experimental collision energy distribution



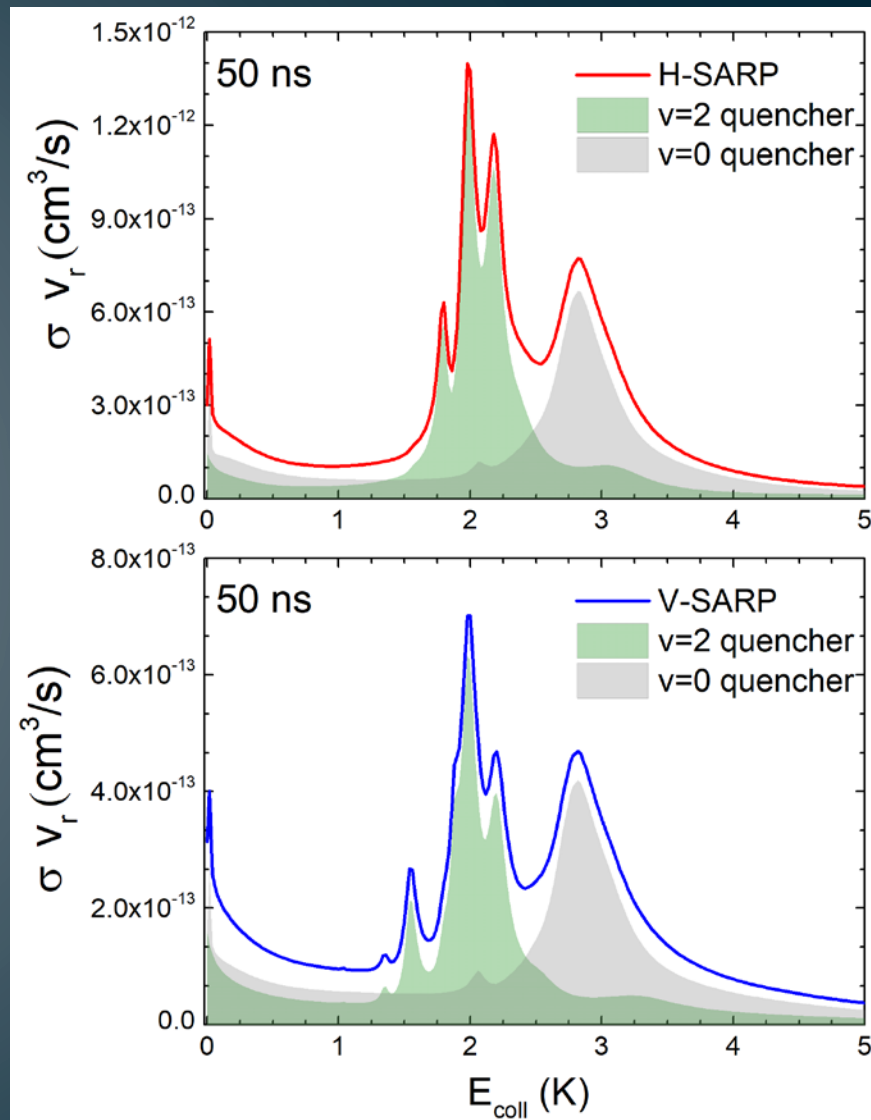
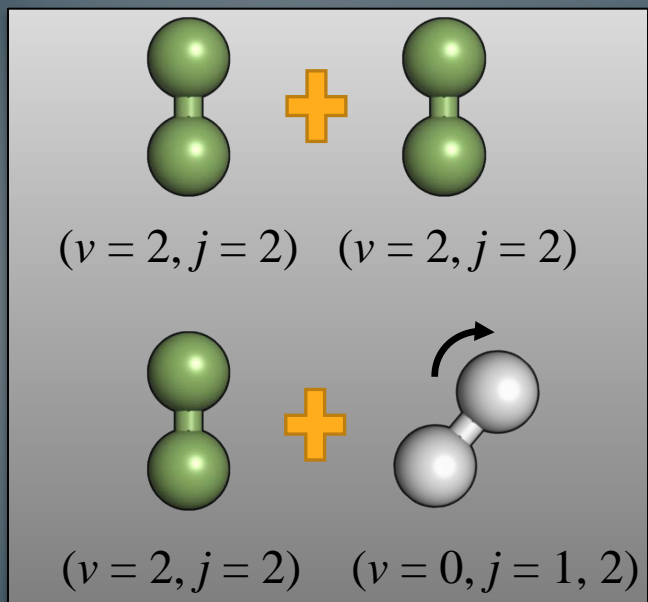
# $D_2 + D_2$ collisions



# D<sub>2</sub> + D<sub>2</sub> collisions

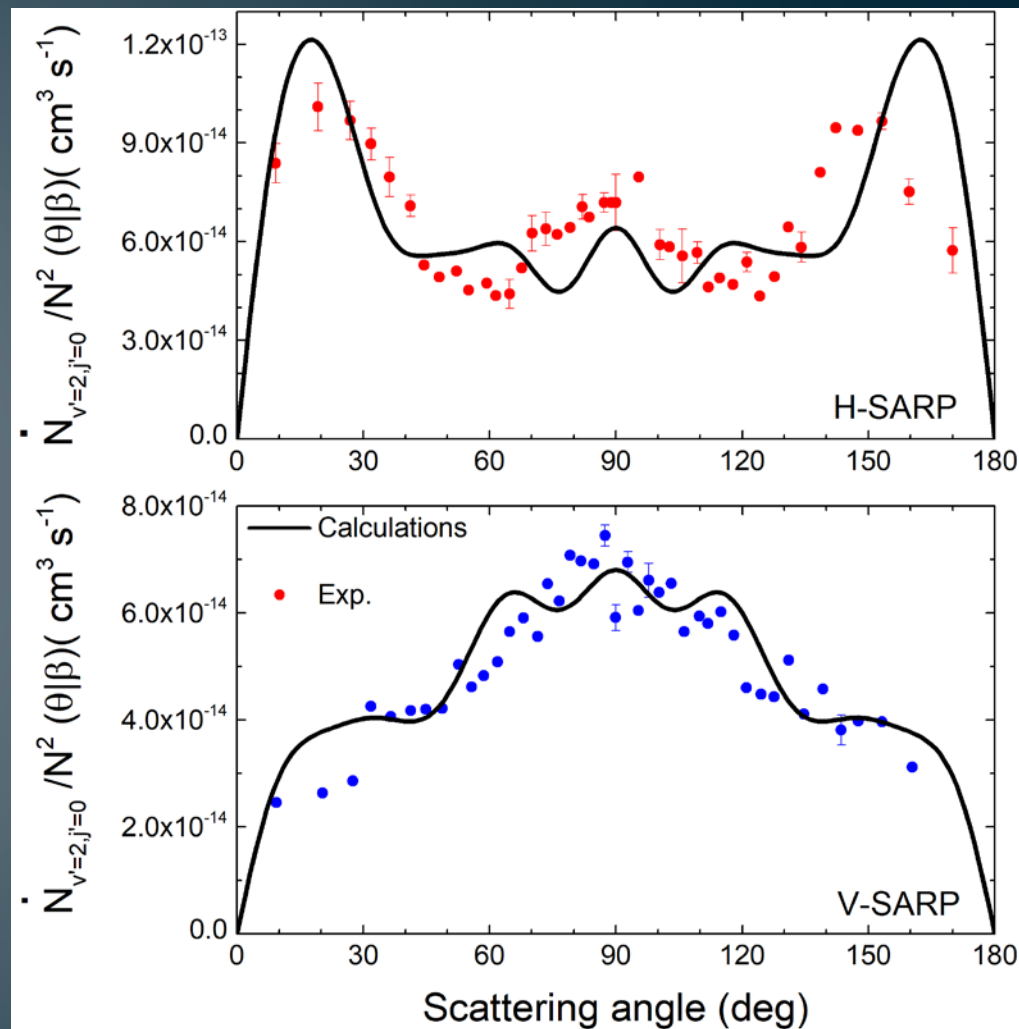
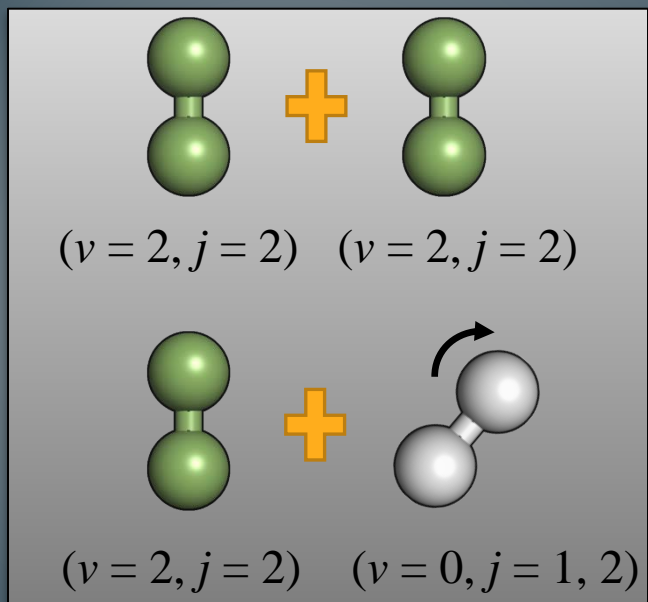


# D<sub>2</sub> + D<sub>2</sub> collisions





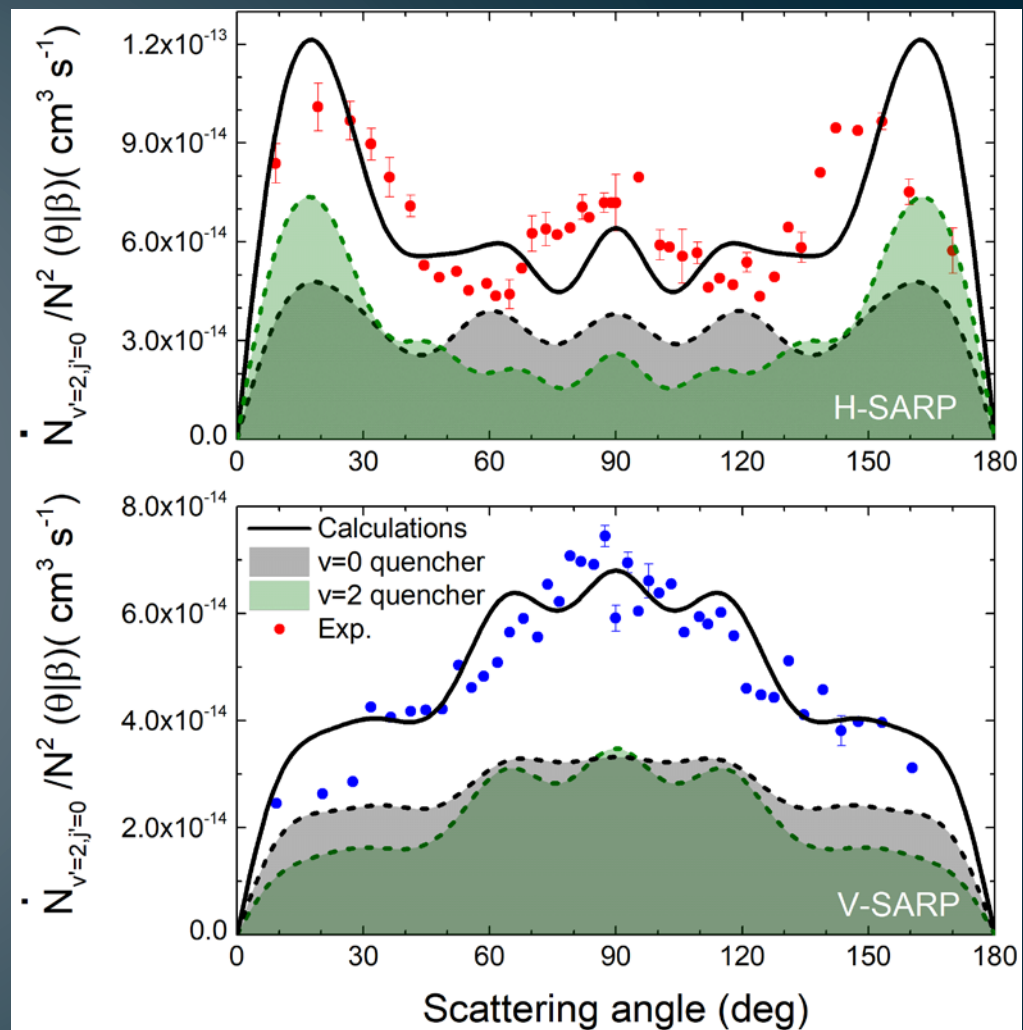
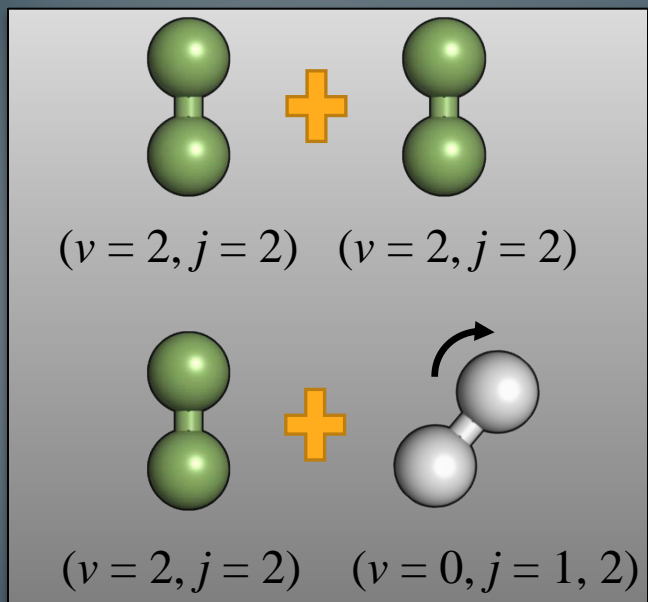
# D<sub>2</sub> + D<sub>2</sub> collisions



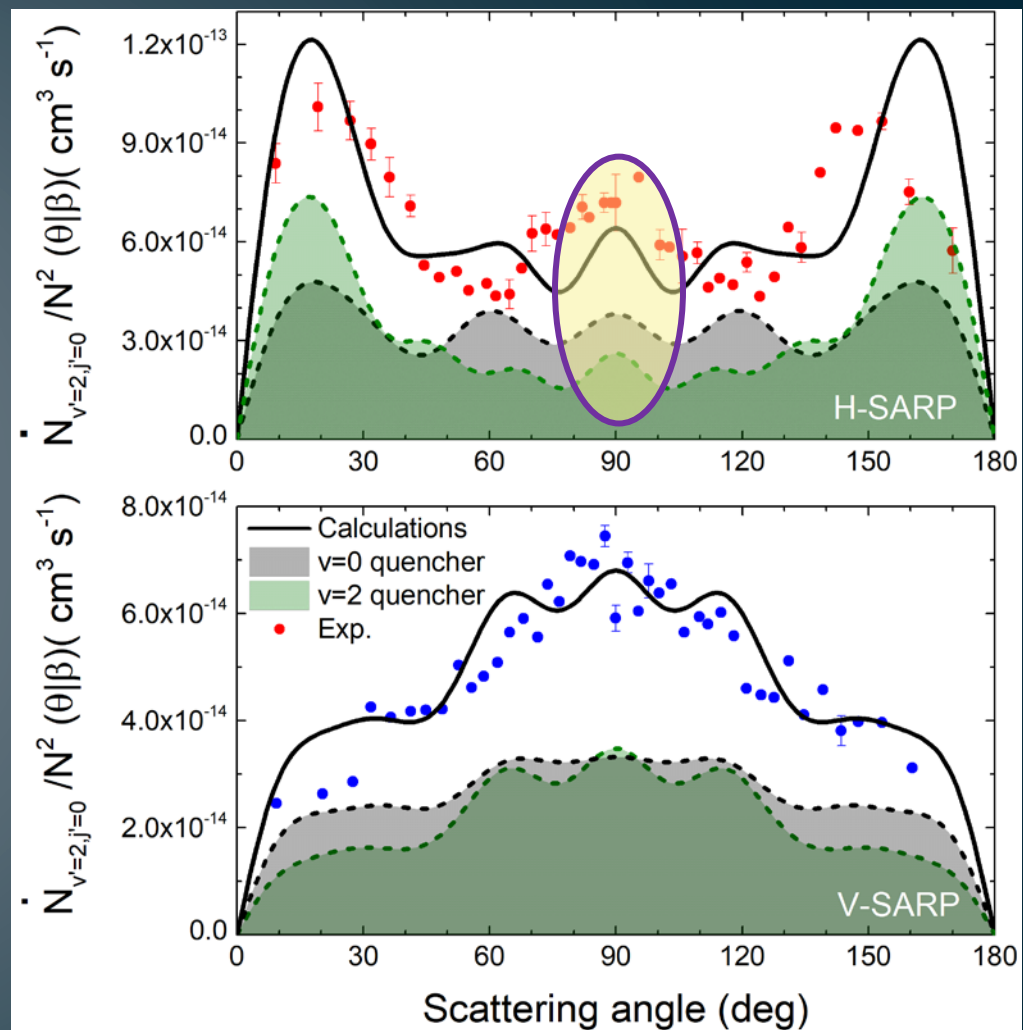
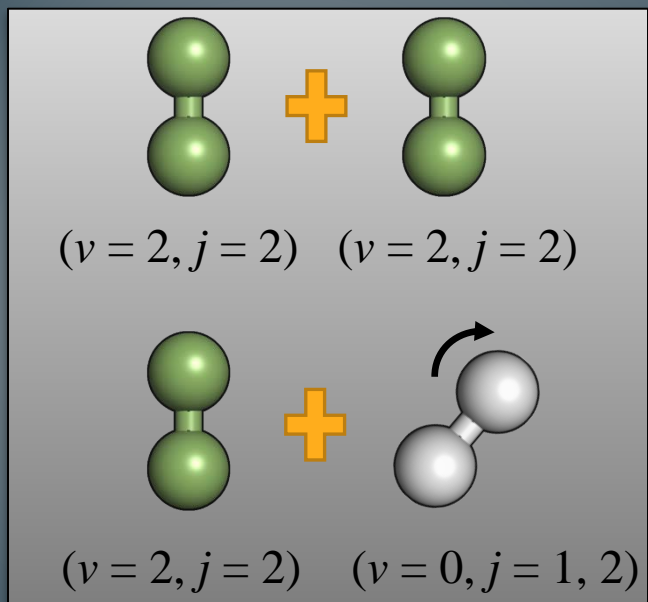
**Experiments:** Zhou, Perreault, Mukherjee, Zare, Nat. Chem. **14**, 658 (2022).

Jambrina, Croft, Zuo, Guo, Balakrishnan, Aoiz Phys. Rev. Lett., **130**, 033002 (2023)

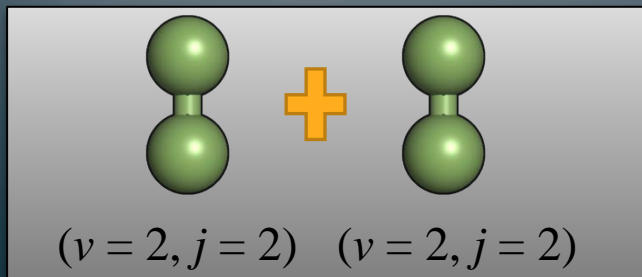
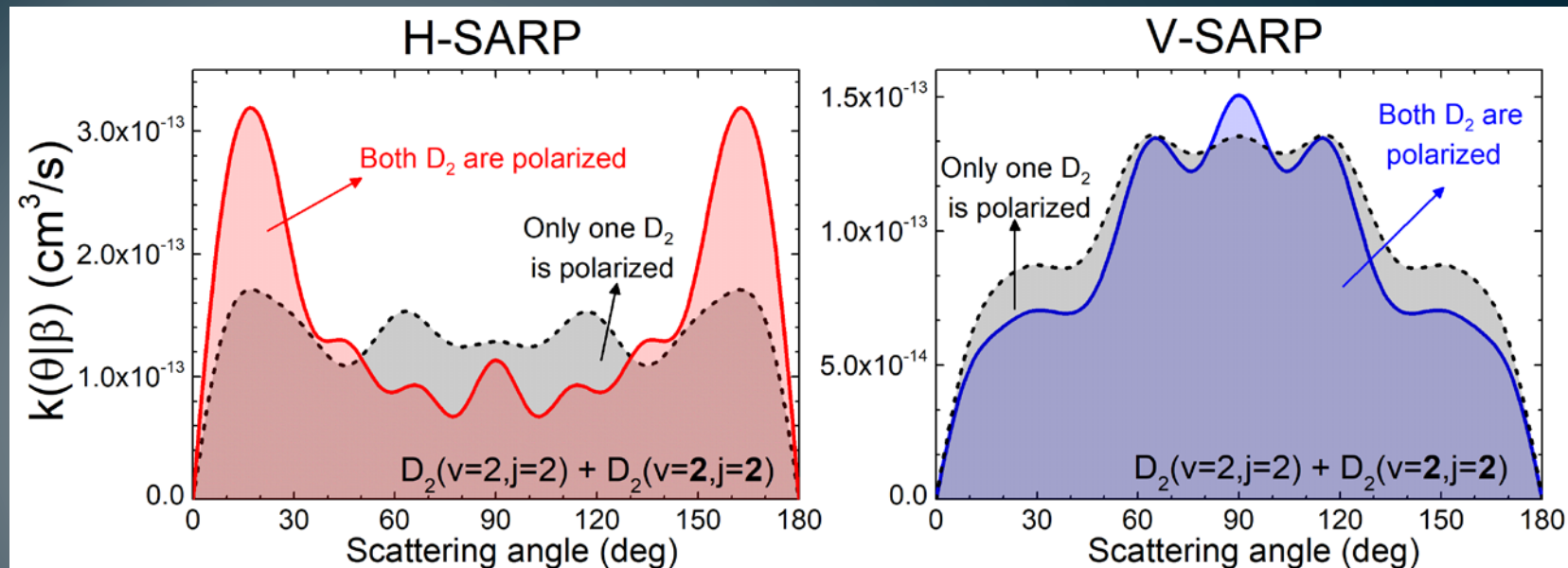
# D<sub>2</sub> + D<sub>2</sub> collisions



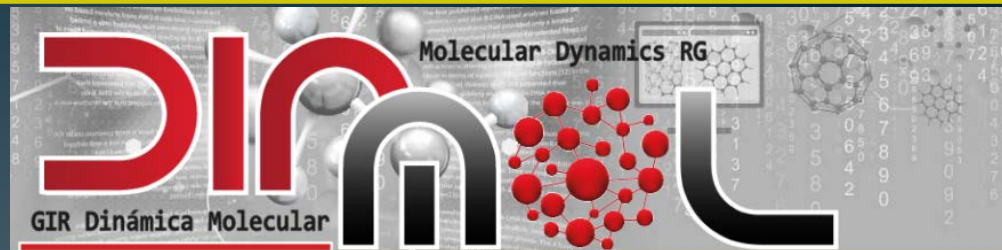
# D<sub>2</sub> + D<sub>2</sub> collisions



# $D_2 + D_2$ collisions



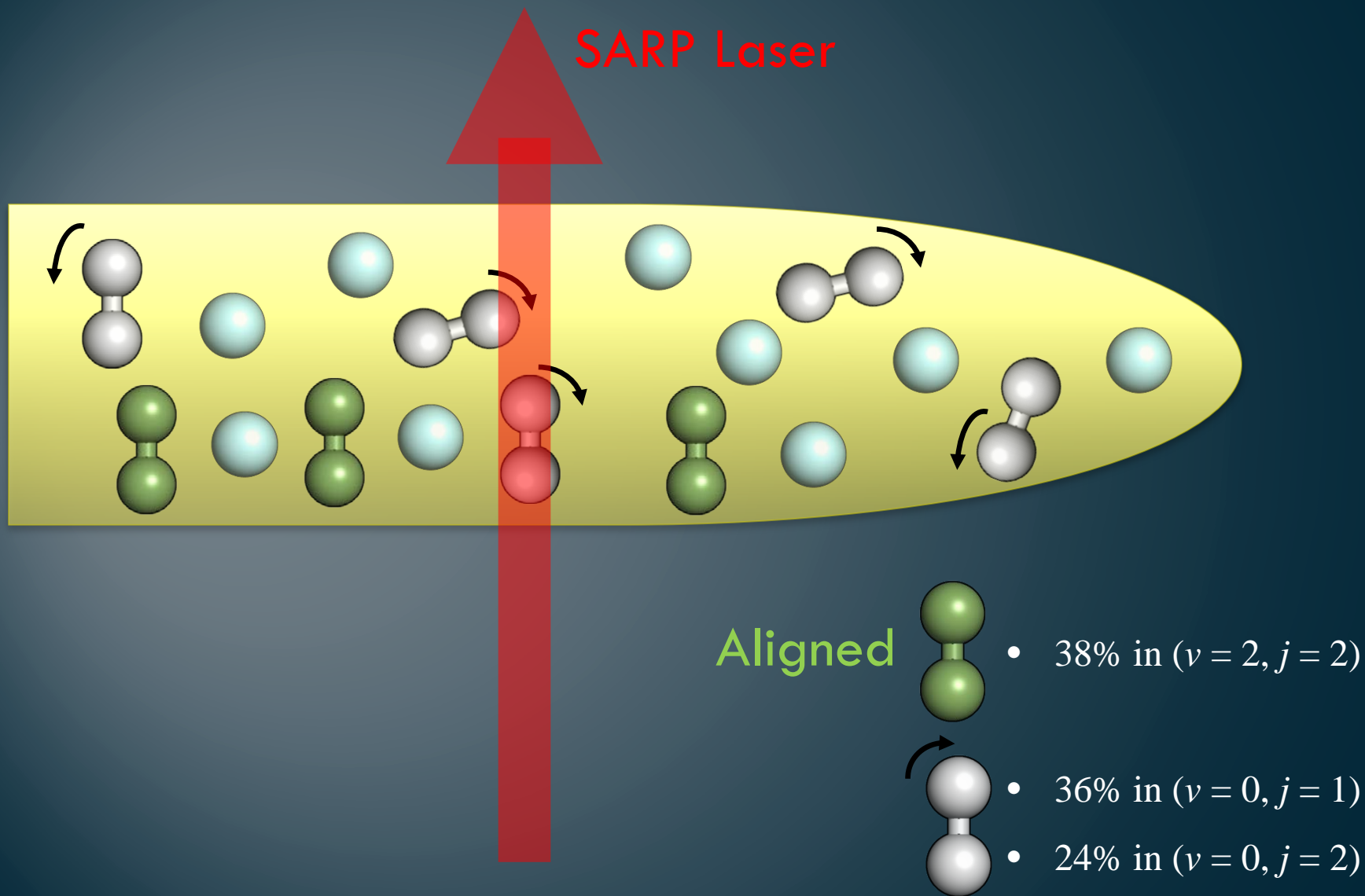
# Outline:



- Inelastic Collisions at Cold energies
- Stereodynamics. SARP Experiments
- Results:  $D_2 + D_2$
- Results:  $He + D_2$
- Conclusions

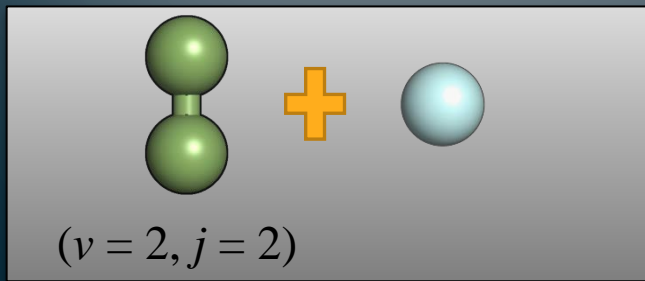
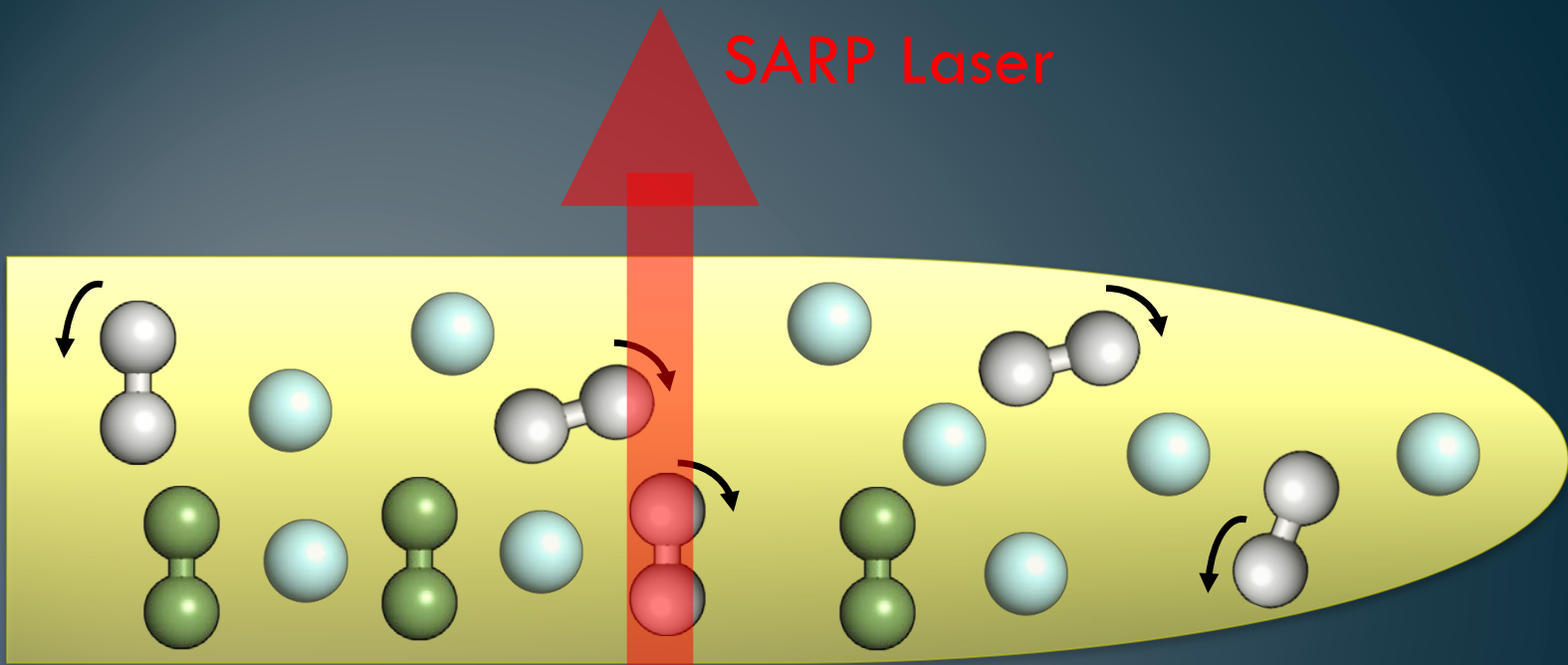
**Aim: Reproduce Experimental Measurements**

# He + D<sub>2</sub> ( $v=2, j=2$ ) collisions



# He + D<sub>2</sub> ( $v=2, j=2$ ) collisions

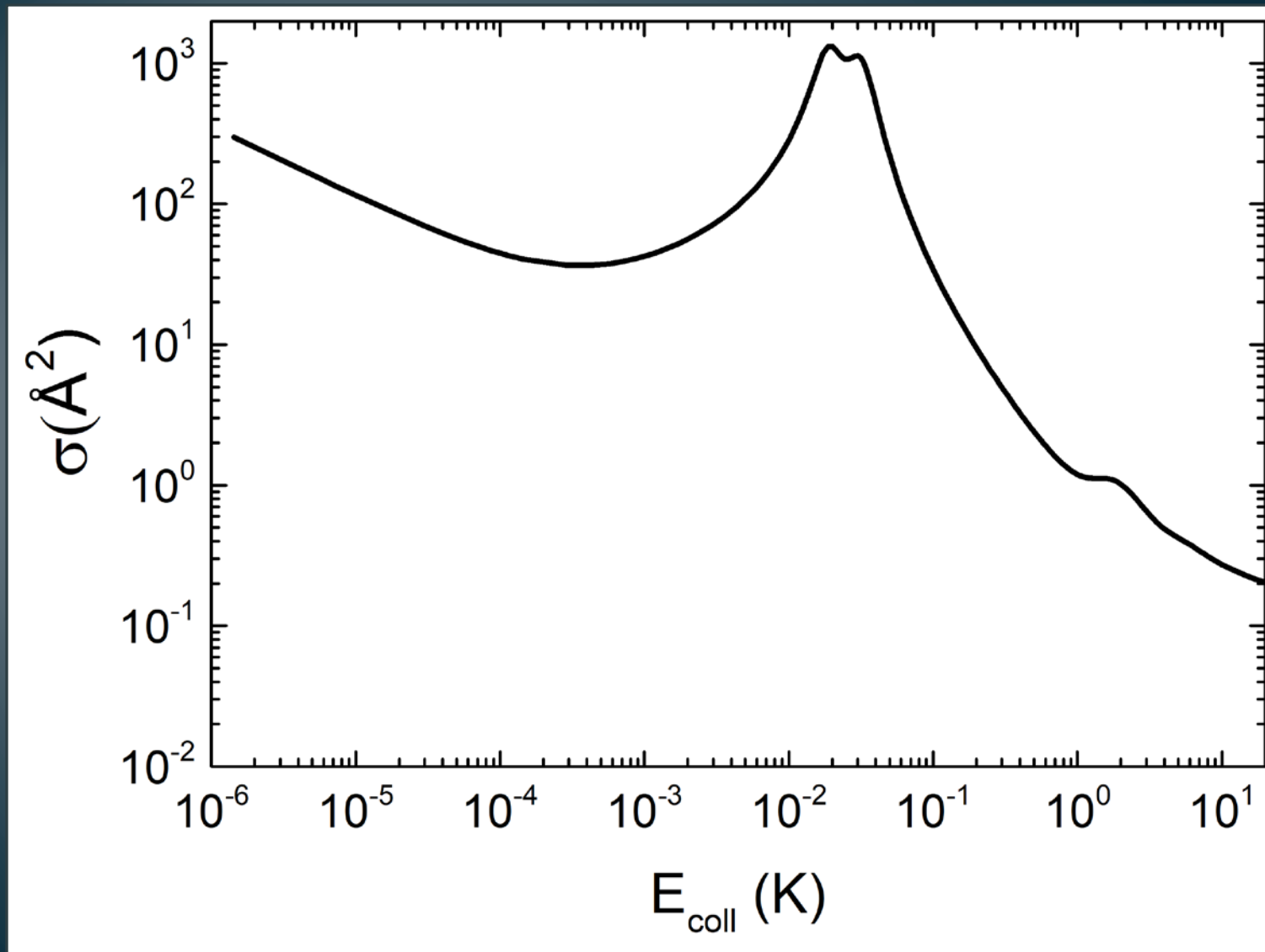
SARP Laser



Aligned

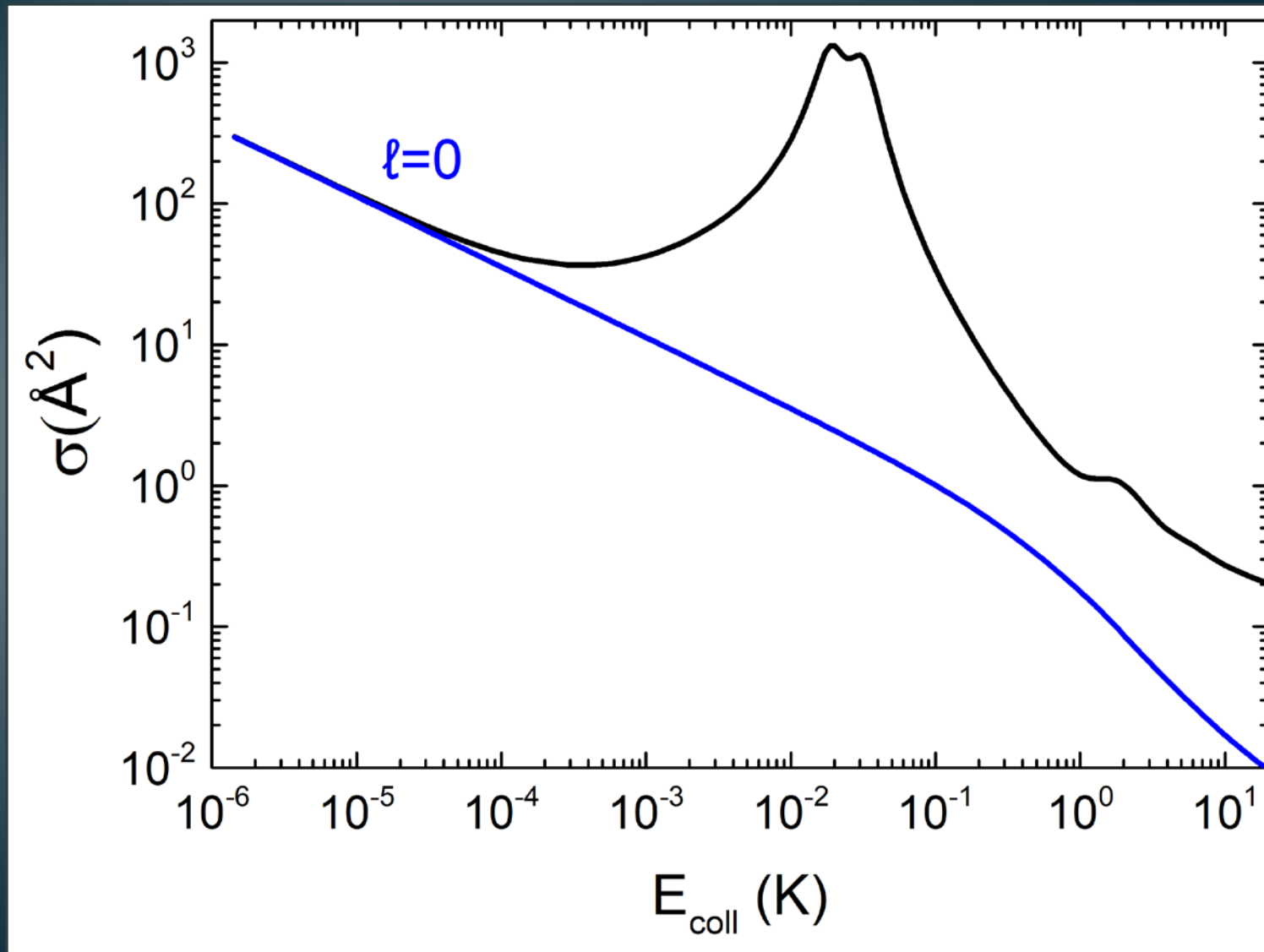
- 38% in ( $v=2, j=2$ )
- 36% in ( $v=0, j=1$ )
- 24% in ( $v=0, j=2$ )

# He + D<sub>2</sub> (v=2, j=2) collisions

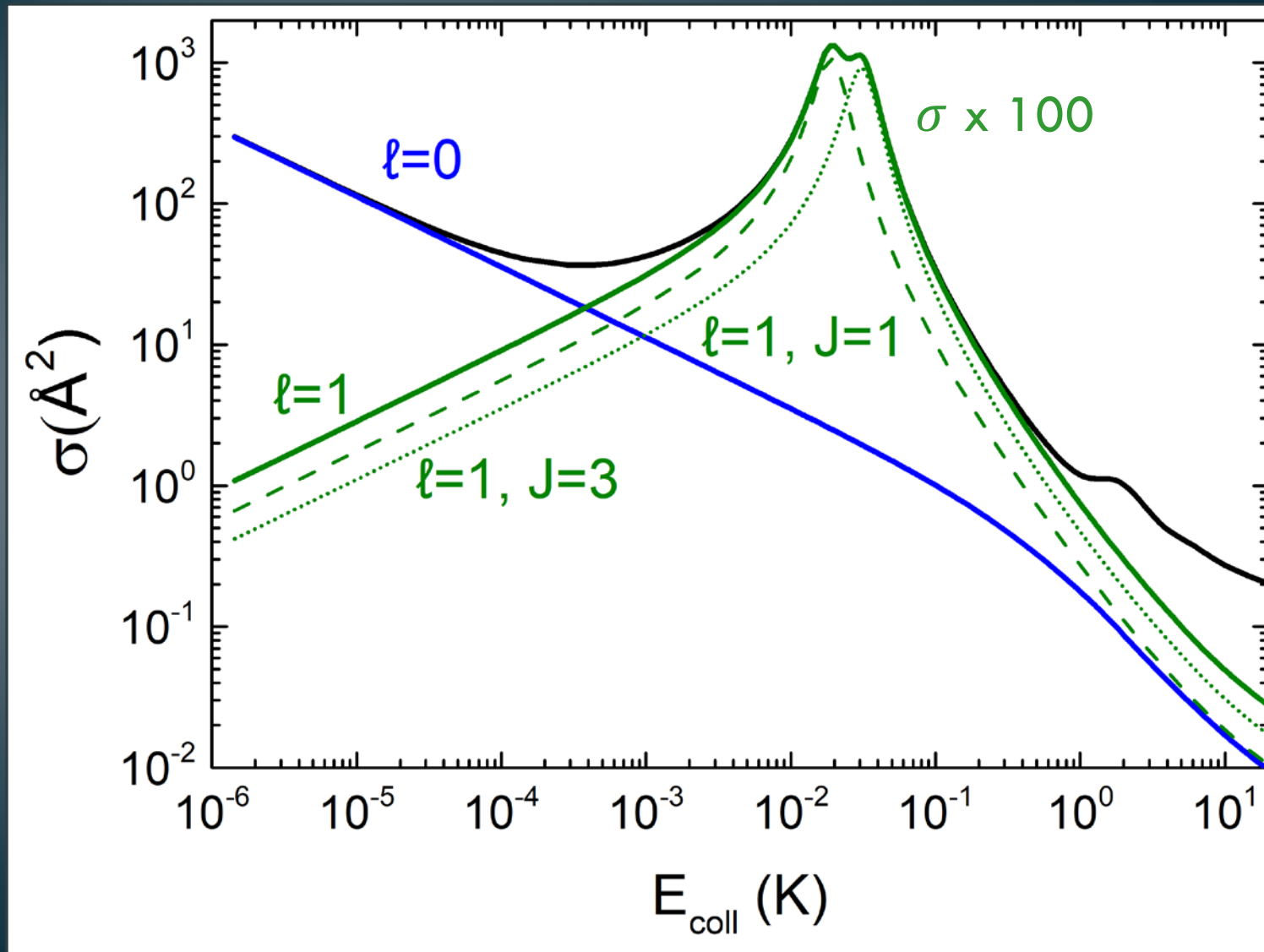




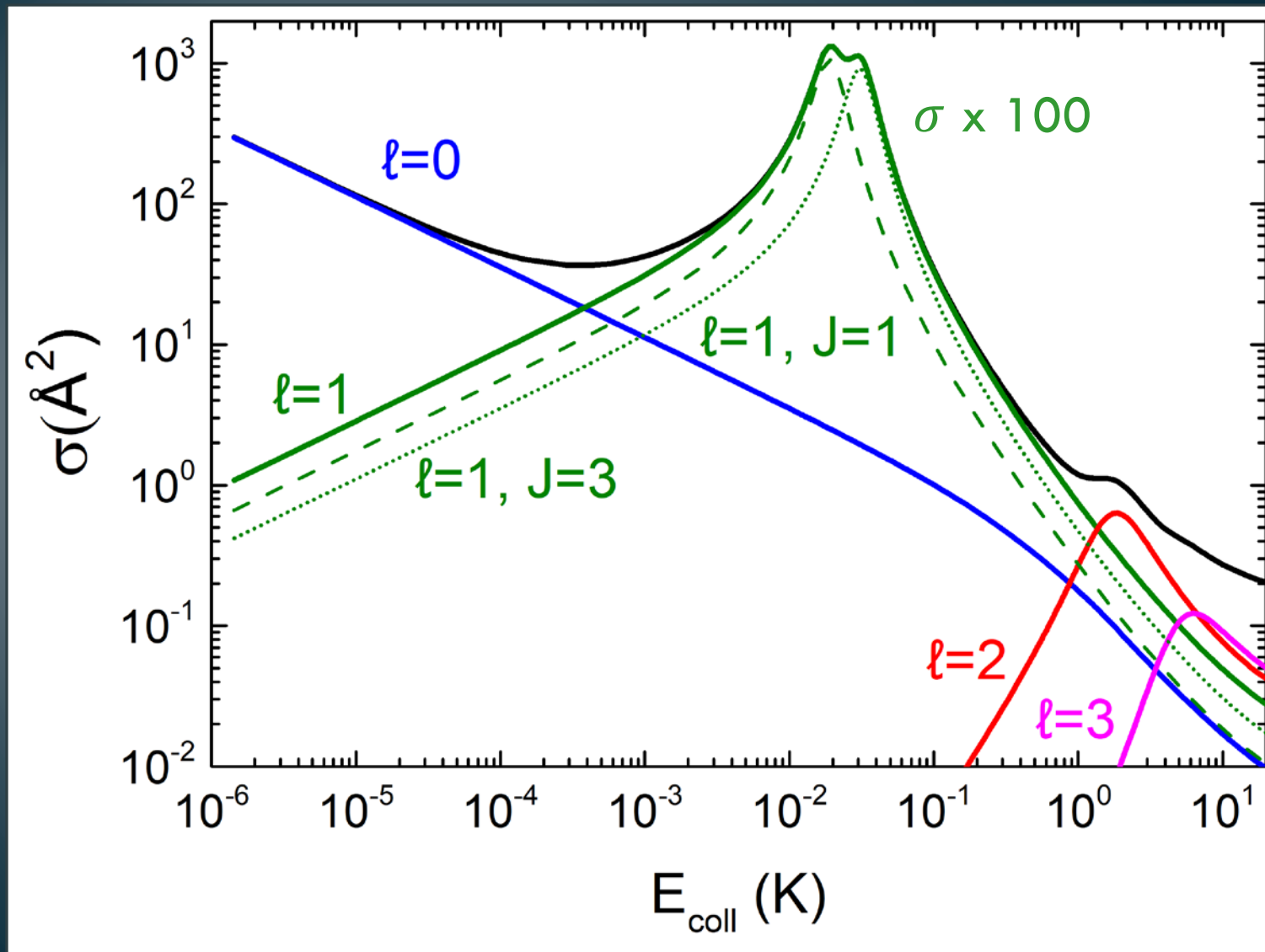
# He + D<sub>2</sub> (v=2, j=2) collisions



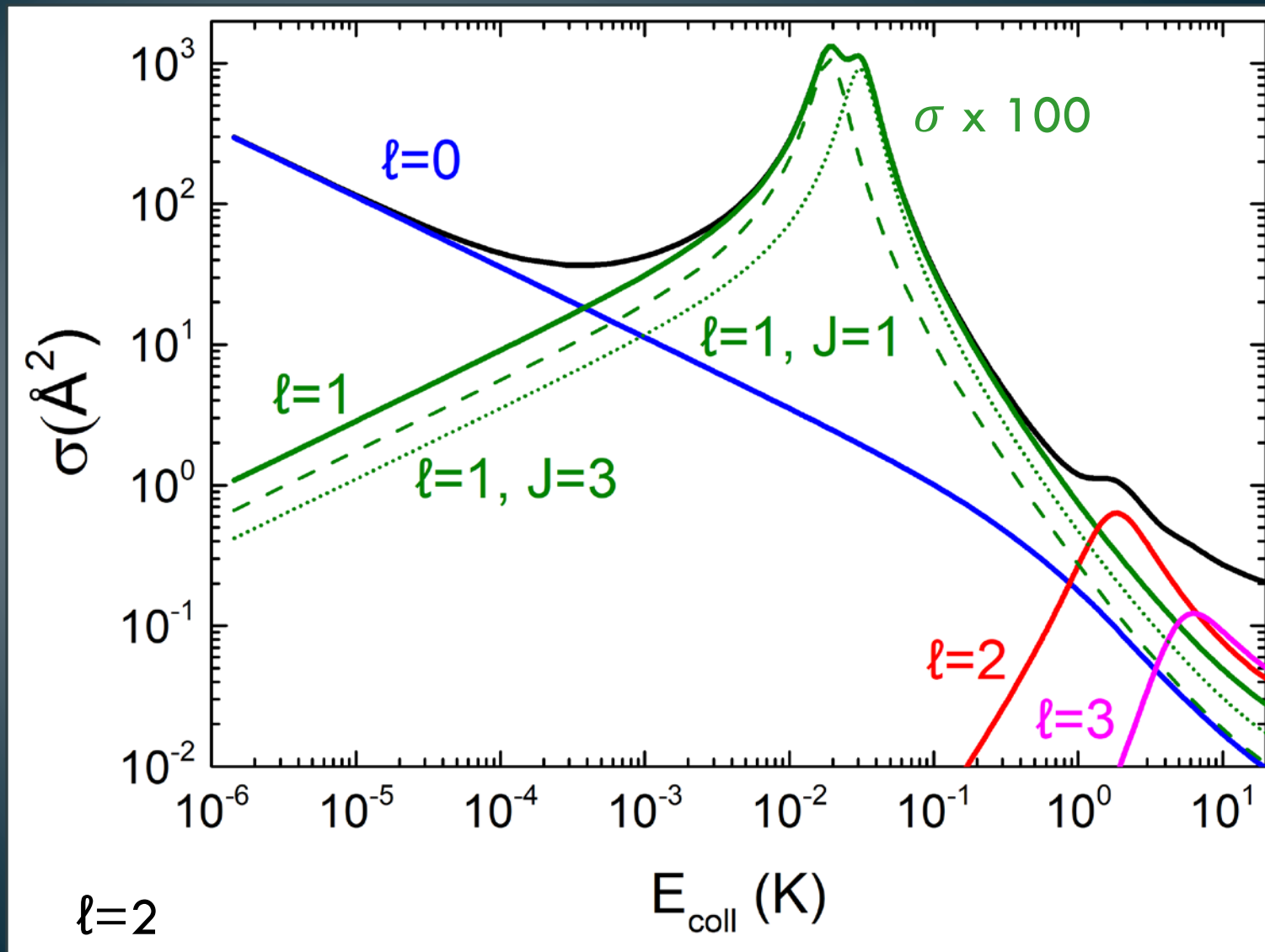
# He + D<sub>2</sub> (v=2, j=2) collisions



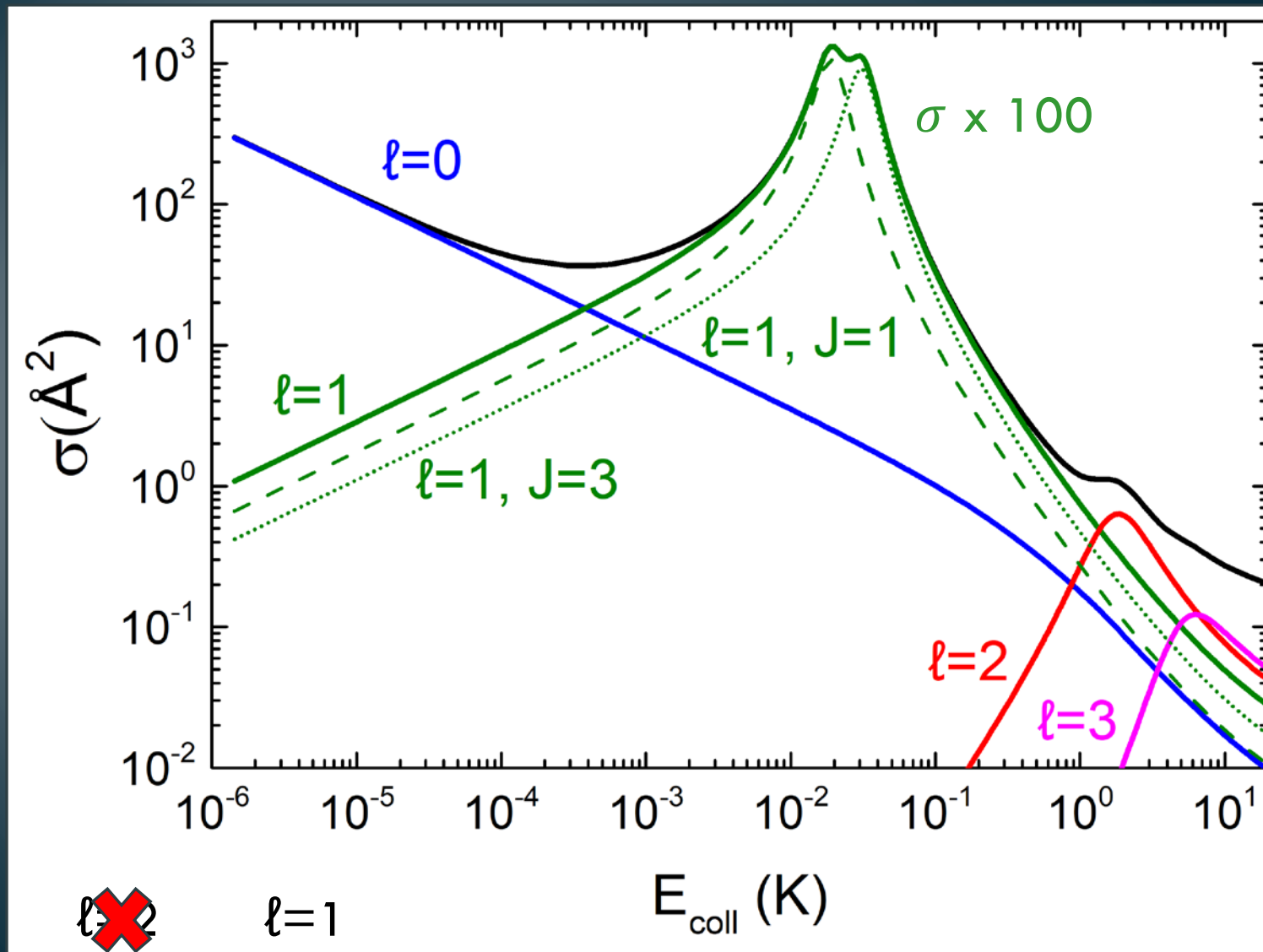
# He + D<sub>2</sub> (v=2, j=2) collisions



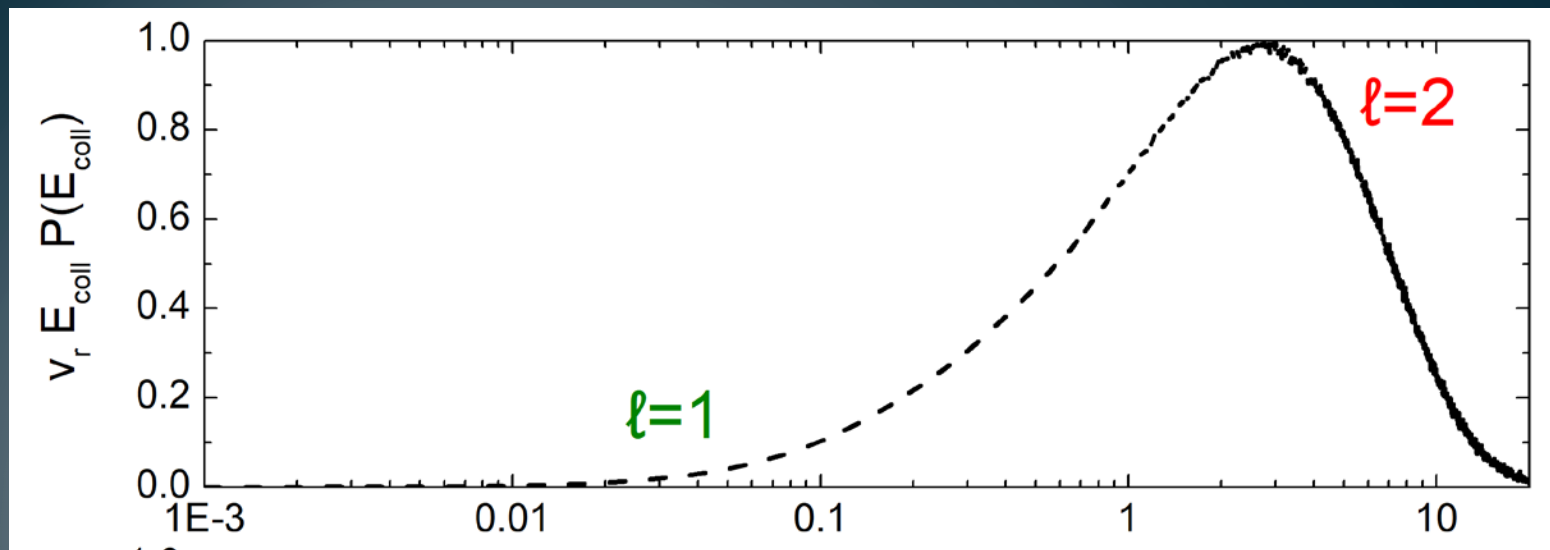
# He + D<sub>2</sub> (v=2, j=2) collisions



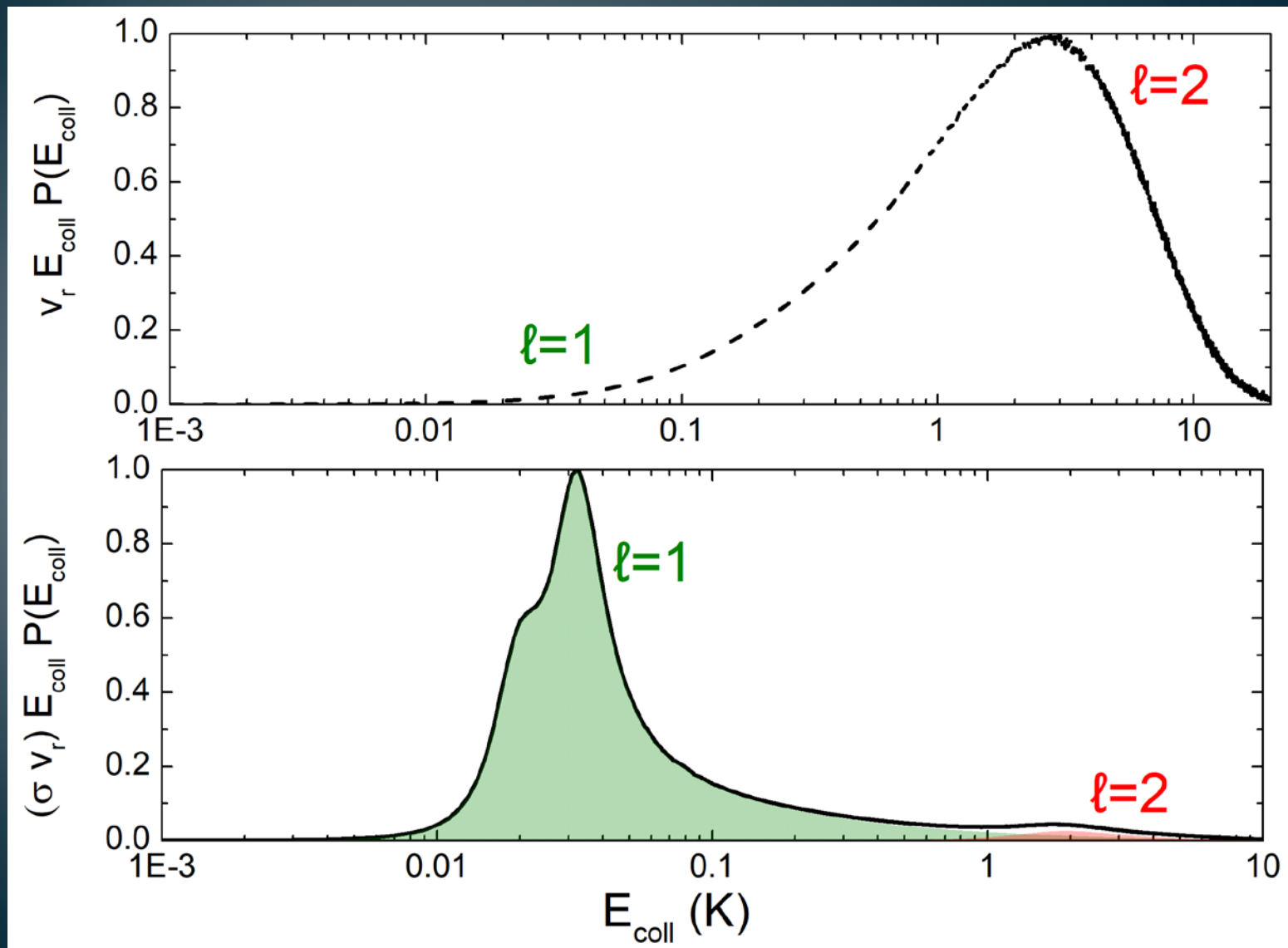
# He + D<sub>2</sub> (v=2, j=2) collisions



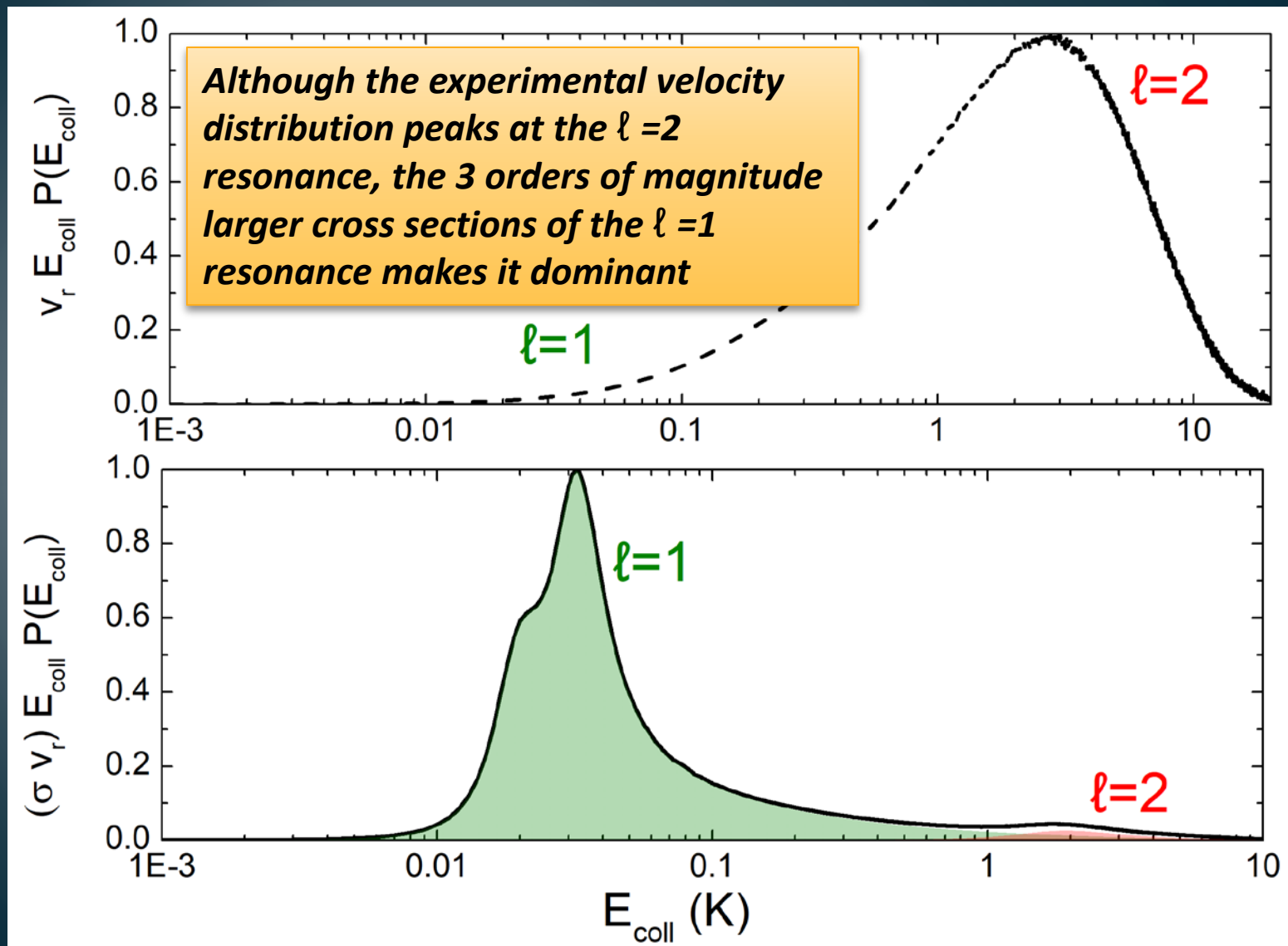
# He + D<sub>2</sub> (v=2, j=2) collisions



# He + D<sub>2</sub> (v=2, j=2) collisions

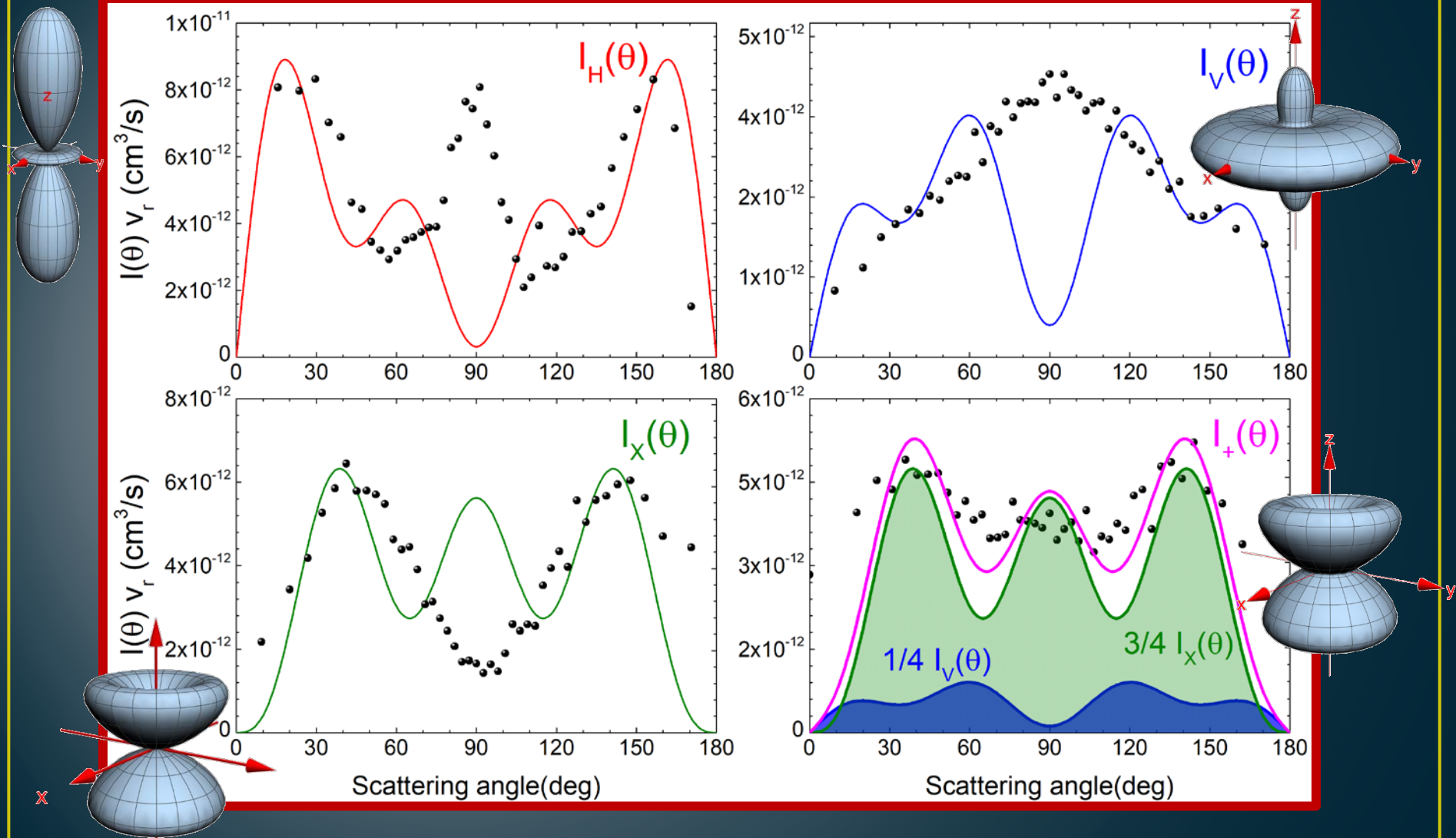


# He + D<sub>2</sub> (v=2, j=2) collisions



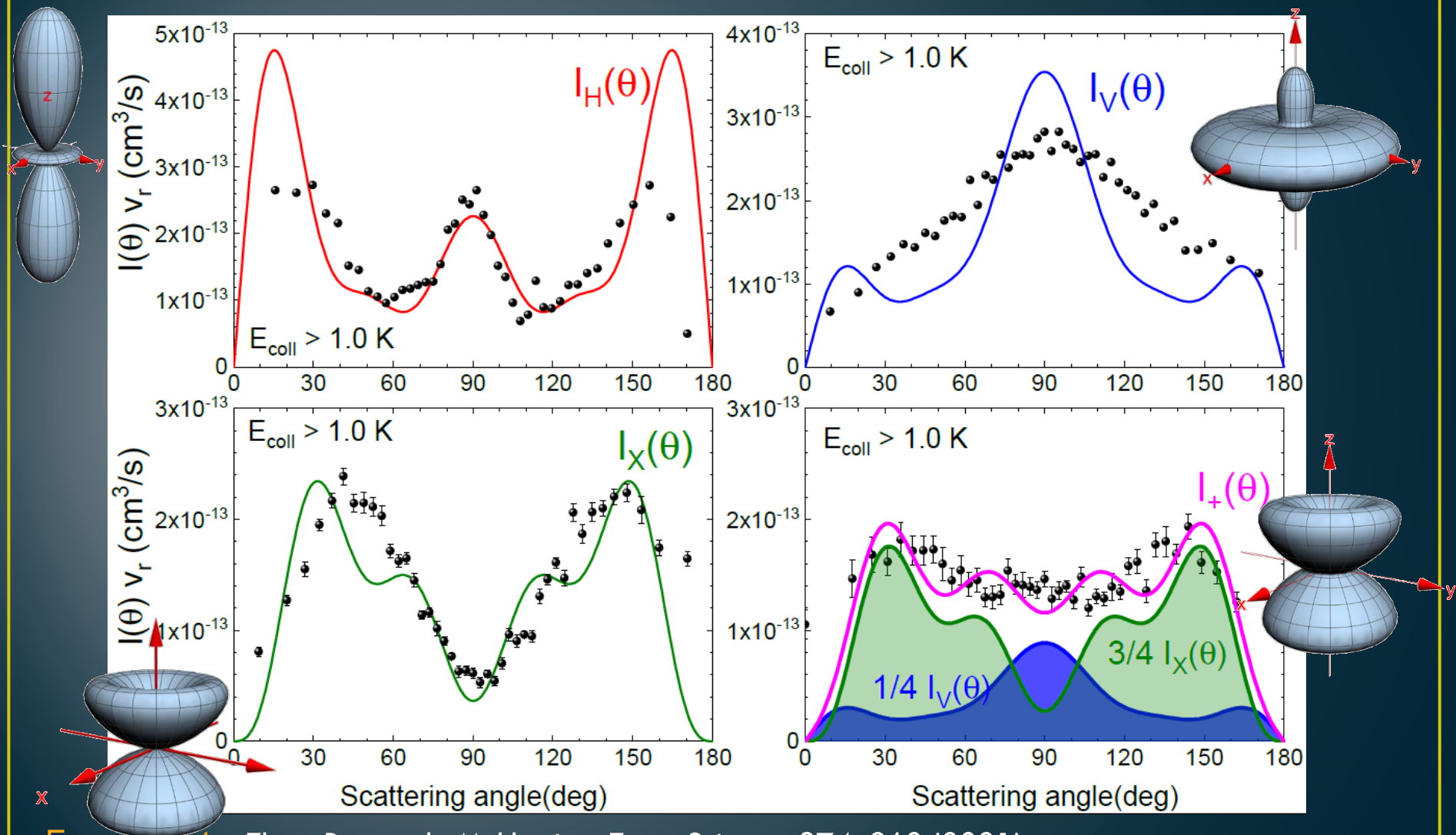


# He + D<sub>2</sub> (v=2, j=2) collisions



**Experiments:** Zhou, Perreault, Mukherjee, Zare. Science. 374. 960 (2021)  
Jambrina, Morita, Croft, Aoiz, Balakrishnan, JPC Lett. **13**, 4064 (2022)

# He + D<sub>2</sub> (v=2, j=2) collisions



Experiments: Zhou, Perreault, Mukherjee, Zare. Science. 374. 960 (2021)

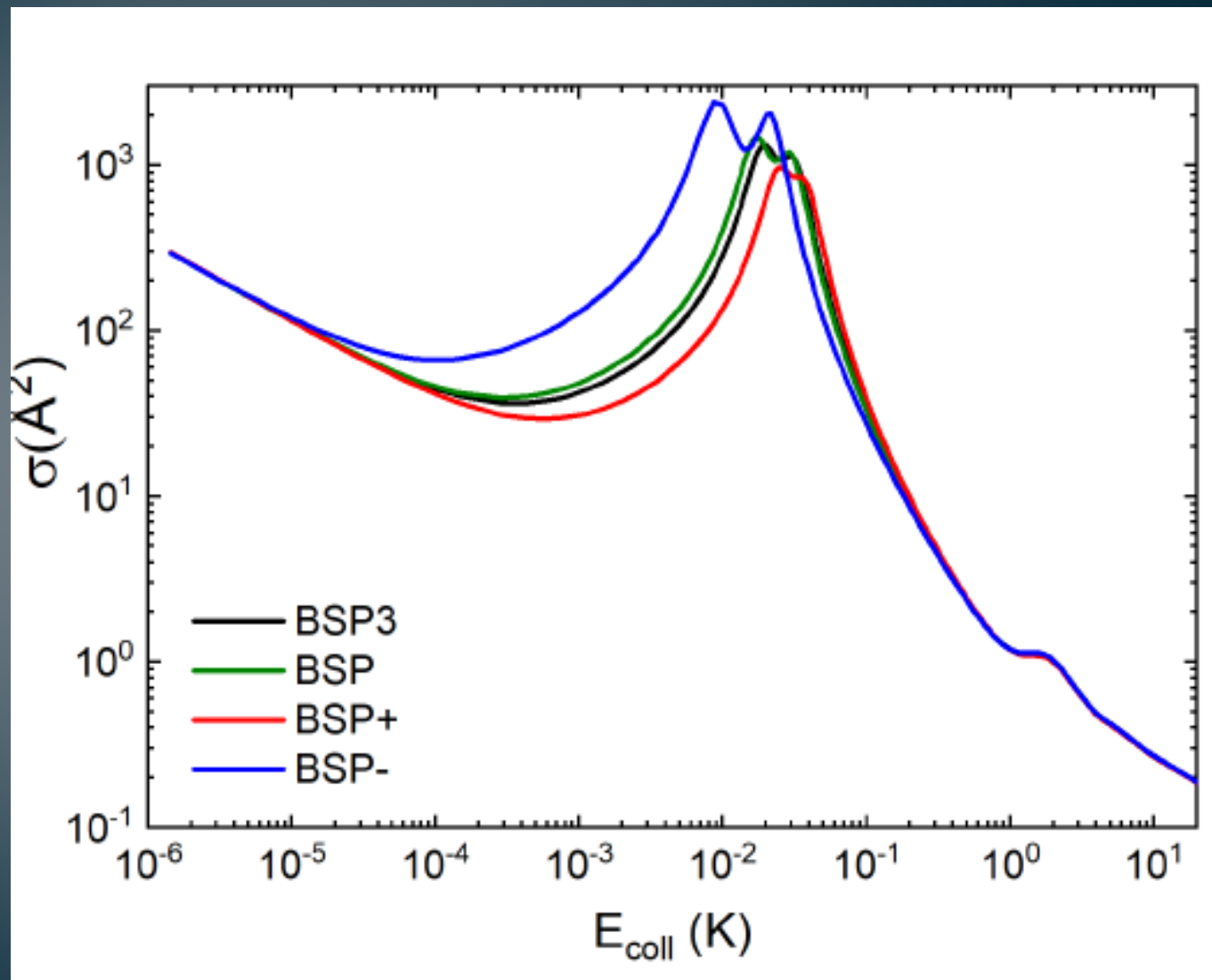
Jambrina, Morita, Croft, Aoiz, Balakrishnan, JPC Lett. 13, 4064 (2022)

# Possible sources of discrepancy

- Theory side

- Scattering Calculations are wrong
  - Tested with different codes (different people). Similar results
- What about the formalism?
  - It worked for other experiments.
- What about the PES?

# Problems with the PES ??



# Possible sources of discrepancy

- Theory side

- Scattering Calculations are wrong
  - Tested with different codes (different people). Similar results
- What about the formalism?
  - It worked for other experiments.
- What about the PES? Unlikely

- Experimental side

- Something related to the velocity distribution?

# Possible sources of discrepancy

- Theory side

- Scattering Calculations are wrong

- Tested with different codes (different people). Similar results

- WI

Perhaps we are not calculating what they are measuring

- I

- WI

- Experimental side

- Something related to the velocity distribution?

# CONCLUSIONS

- The shape of the DCS changes dramatically with the alignment of the intermolecular axis.
- Experimental results can be simulated from first principles for inelastic collisions.
- Contribution of theory is important for the interpretation of the experimental results.
- No agreement for He + D<sub>2</sub>. More calcs/expt are needed

# More information



VNiVERSiDAD  
D SALAMANCA

CAMPUS DE EXCELENCIA INTERNACIONAL



800 AÑOS  
VNiVERSiDAD  
D SALAMANCA

He + D<sub>2</sub> :

P. G. Jambrina et al. *J. Phys. Chem. Lett.* 2022, 13, 4064–4072

D<sub>2</sub> + D<sub>2</sub> :

P. G. Jambrina et al. *Phys. Rev. Lett.* 2023, 130, 033002



# Funding



PID2020-113147-GA-IOO



Fundación Salamanca City of Culture and Knowledge  
(programme for attracting scientific talent to Salamanca)



Muito Obrigado !!!



$$\begin{aligned}
F_{m'_A m'_B m_A m_B}(\theta) &= \frac{\sqrt{(1 + \delta_{v_A v_B} \delta_{j_A j_B})(1 + \delta_{v'_A v'_B} \delta_{j'_A j'_B})}}{2ik} \\
&\times \sum_J (2J + 1) d_{m'_A + m'_B, m_A + m_B}^J(\theta) \\
&\times S_{m'_A m'_B m_A m_B}^J(E), \tag{4}
\end{aligned}$$

$$d\sigma(\theta|\beta, \alpha) = \sum_{k_A=0}^{2j_A} \sum_{q_A} \sum_{k_B=0}^{2j_B} \sum_{q_B} (2k_A + 1)(2k_B + 1) \\ \times \left[ U_{q_A, q_B}^{(k_A, k_B)}(\theta) \right]^* a_{q_A}^{(k_A)} a_{q_B}^{(k_B)},$$

$$a_q^{(k)} = C_{kq}(\beta, \alpha) A_0^{(k)} = C_{kq}(\beta, \alpha) \langle j_A 0, k 0 | j_A 0 \rangle,$$

$$\begin{aligned}
U_{q_A, q_B}^{(k_A, k_B)}(\theta) &= \frac{1}{(2j_A + 1)(2j_B + 1)} \\
&\times \sum_{\substack{m'_A, m'_B \\ m_A, m_B}} F_{m'_A m'_B m_A m_B}(\theta) F_{m'_A m'_B (m_A + q_A) (m_B + q_B)}^*(\theta) \\
&\times \langle j_A m_A, k_A q_A | j_A (m_A + q_A) \rangle \\
&\times \langle j_B m_B, k_B q_B | j_B (m_B + q_B) \rangle. \tag{6}
\end{aligned}$$