

Neutrino Mass Models

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Disclaimer:

“Neutrino Mass Models” is a topic that spans a vast area of research.
This talk will only touch upon selected topics (reflecting my own bias) in
this field.

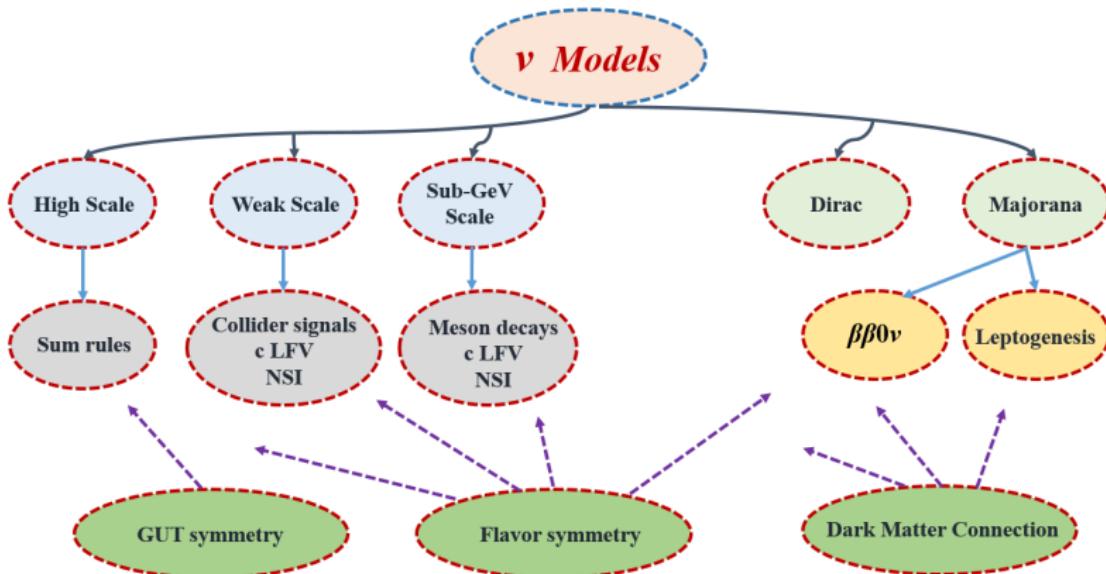
Current knowledge of 3-neutrino oscillations

NuFIT 5.1 (2021)

		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 2.6$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
without SK atmospheric data	$\sin^2 \theta_{12}$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^\circ$	$33.44^{+0.77}_{-0.74}$	$31.27 \rightarrow 35.86$	$33.45^{+0.77}_{-0.74}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.573^{+0.018}_{-0.023}$	$0.405 \rightarrow 0.620$	$0.578^{+0.017}_{-0.021}$	$0.410 \rightarrow 0.623$
	$\theta_{23}/^\circ$	$49.2^{+1.0}_{-1.3}$	$39.5 \rightarrow 52.0$	$49.5^{+1.0}_{-1.2}$	$39.8 \rightarrow 52.1$
	$\sin^2 \theta_{13}$	$0.02220^{+0.00068}_{-0.00062}$	$0.02034 \rightarrow 0.02430$	$0.02238^{+0.00064}_{-0.00062}$	$0.02053 \rightarrow 0.02434$
	$\theta_{13}/^\circ$	$8.57^{+0.13}_{-0.12}$	$8.20 \rightarrow 8.97$	$8.60^{+0.12}_{-0.12}$	$8.24 \rightarrow 8.98$
	$\delta_{\text{CP}}/^\circ$	194^{+52}_{-25}	$105 \rightarrow 405$	287^{+27}_{-32}	$192 \rightarrow 361$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.515^{+0.028}_{-0.028}$	$+2.431 \rightarrow +2.599$	$-2.498^{+0.028}_{-0.029}$	$-2.584 \rightarrow -2.413$

Esteban, Gonzalez-Garcia, Maltoni, Schwetz, Zhou (2020)

Roadmap for Neutrino Models



Effective Field Theory for neutrino masses

- Neutrino masses are zero in the Standard Model. Observed oscillations require new physics beyond Standard Model
- Neutrino masses and oscillations can be explained in terms of the celebrated Weinberg operator
- It is the leading operator in Standard Model EFT and arises at dimension-five, suppressed by one power of an inverse mass scale
- It violates lepton number by two units and generates neutrino masses:

$$\begin{aligned}\mathcal{O}_1 &= \frac{\kappa_{ab}}{2} (L_a^i L_b^j) H^k H^l \epsilon_{ik} \epsilon_{jl} \\ &= \frac{\kappa_{ab}}{2} (\nu_a H^0 - \ell_a H^+) (\nu_b H^0 - \ell_b H^+) \\ &\Rightarrow (M_\nu)_{ab} = (\kappa)_{ab} v^2\end{aligned}$$

- $\kappa^{-1} \sim (10^{14} \text{ GeV})$ can be inferred from data

Strong reasons to go beyond EFT

- ▶ EFT description cannot be the end goal, or else important phenomena would be missed
- ▶ What if neutrinos are Dirac particles? \mathcal{O}_1 is then the wrong description
- ▶ What if neutrino masses arose from $d = 7$ operators or $d = 9$ operators in a fundamental theory, and not through \mathcal{O}_1 ?
- ▶ Even when the scale of new physics is beyond reach of current experiments, opening the EFT operator can give new insights
- ▶ An example is baryon asymmetry generation via leptogenesis
- ▶ Requires opening up the Weinberg operator. Baryon asymmetry originates from the decays of N^c , the mediator of the operator \mathcal{O}_1

Origin of neutrino mass: Seesaw mechanism

- ▶ Adding right-handed neutrino N^c which transforms as singlet under $SU(2)_L$,

$$\mathcal{L} = f_\nu (L \cdot H) N^c + \frac{1}{2} M_R N^c N^c$$

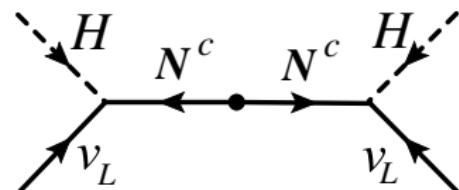
- ▶ Integrating out the N^c , $\Delta L = 2$ operator is induced:

$$\mathcal{L}_{\text{eff}} = -\frac{f_\nu^2}{2} \frac{(L \cdot H)(L \cdot H)}{M_R}$$

- ▶ Once H acquires VEV, neutrino mass is induced:

$$m_\nu \simeq f_\nu^2 \frac{v^2}{M_R}$$

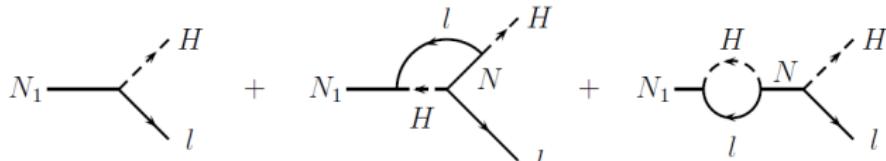
- ▶ For $f_\nu v \simeq 100$ GeV, $M_R \simeq 10^{14}$ GeV.



Minkowski (1977)
Yanagida (1979)
Gell-Mann, Ramond, Slansky (1980)
Mohapatra & Senjanovic (1980)

Baryogenesis via leptogenesis and type-I seesaw

- In the early history of the universe, a lepton asymmetry may be dynamically generated in the decay of N [Fukugita, Yanagida \(1986\)](#)
- N being a Majorana fermion can decay to $L + H$ as well as $\bar{L} + H^*$



- Three Sakharov conditions can be satisfied: B violation via electroweak sphaleron, C and CP violation in Yukawa couplings of N , and out of equilibrium condition via expanding universe
- Lepton asymmetry in decay of N_1 (with $M_1 \ll M_{2,3}$):

$$\varepsilon_1 \simeq \frac{3}{16\pi} \frac{1}{(f_\nu f_\nu^\dagger)_{11}} \sum_{i=2,3} \text{Im} [(f_\nu f_\nu^\dagger)_{i1}^2] \frac{M_1}{M_i}$$

- $\varepsilon \sim 10^{-6}$ can explain observed baryon asymmetry of the universe
- Indirect tests in Majorana nature of ν and in CP violation in oscillations

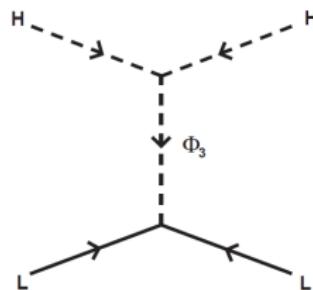
Seesaw mechanism (cont.)

Type II seesaw: $\Phi_3 \sim (1, 3, 1)$

Mohapatra & Senjanovic (1980)

Schechter & Valle (1980)

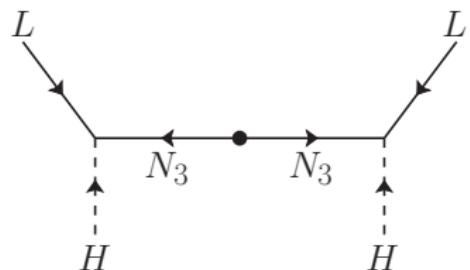
Lazarides, Shafi, & Wetterich (1981)



Type III seesaw: $N_3 \sim (1, 3, 0)$

Foot, Lew, He, & Joshi (1989)

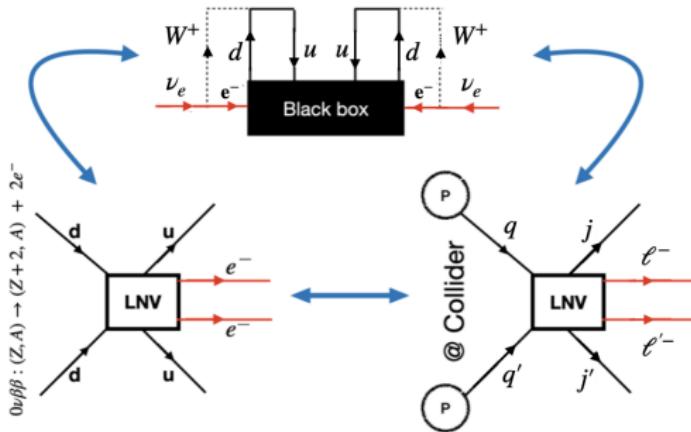
Ma (1998)



- ▶ Φ_3 and N_3 contain charged particles which can be looked for at LHC
- ▶ Eg: $\Phi^{++} \rightarrow \ell^+ \ell^+$, $\Phi^{++} \rightarrow W^+ W^+$ decays would establish lepton number violation

Lepton Number Violation at the LHC

- Classic way to establish Majorana nature of neutrino is to observe neutrinoless double beta decay (Schechter, Valle, 1981)
- $pp \rightarrow \ell^\pm \ell^\pm + \text{jets}$ process can also establish L violation by two units, and hence Majorana nature of neutrino (Keung, Senjanovic, 1983)
- This is realized in type-II seesaw model (Babu, Barman, Gonçalves, Ismail, 2022)



L-violation in type-II Seesaw at LHC

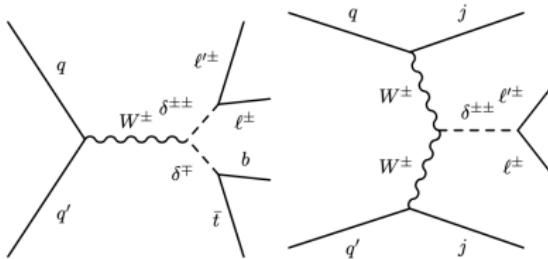
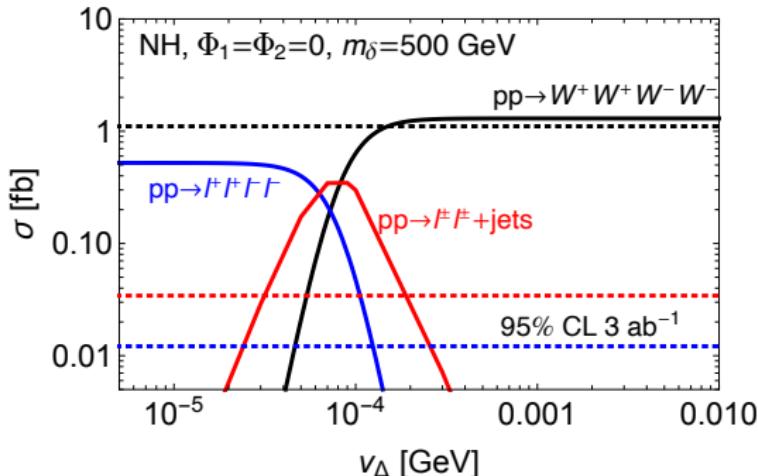


Figure: $pp \rightarrow \ell^\pm \ell'^\pm + \text{jets}$



(Babu, Barman, Gonçalves, Ismail, 2022)

Dirac Neutrino Models

- ▶ Neutrinos may be Dirac particles without lepton number violation
- ▶ Oscillation experiments cannot distinguish Dirac neutrinos from Majorana neutrinos
- ▶ Spin-flip transition rates (in stars, early universe) are suppressed by small neutrino mass:

$$\Gamma_{\text{spin-flip}} \approx \left(\frac{m_\nu}{E} \right)^2 \Gamma_{\text{weak}}$$

- ▶ If neutrinos are Dirac, it would be nice to understand the smallness of their mass
- ▶ Models exist which explain the smallness of Dirac m_ν
- ▶ “Dirac leptogenesis” can explain baryon asymmetry

Dick, Lindner, Ratz, Wright (2000)

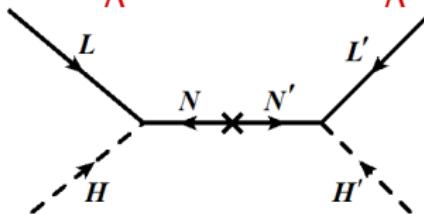
Dirac Seesaw Models

- Dirac seesaw can be achieved in Mirror Models
Lee, Yang (1956); Foot, Volkas (1995); Berezhiani, Mohapatra (1995),
Silagadze(1997)
- Mirror sector is a replica of Standard Model, with new particles transforming under mirror gauge symmetry:

$$L = \begin{pmatrix} \nu \\ e \end{pmatrix}_L ; \quad H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix} ; \quad L' = \begin{pmatrix} \nu' \\ e' \end{pmatrix}_L ; \quad H' = \begin{pmatrix} H'^+ \\ H'^0 \end{pmatrix}$$

- Effective dimension-5 operator induces small Dirac mass:

$$\frac{(LH)(L'H')}{\Lambda} \Rightarrow m_\nu = \frac{vv'}{\Lambda}$$



- $B - L$ may be gauged to suppress Planck-induced Weinberg operator $(LLHH)/M_{Pl}$ that would make neutrino pseudo-Dirac particle

Dirac Neutrinos from Left-Right Symmetry

- Fermion transformation:

$$Q_L (3, 2, 1, 1/3) = \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \quad Q_R (3, 1, 2, 1/3) = \begin{pmatrix} u_R \\ d_R \end{pmatrix},$$

$$\Psi_L (1, 2, 1, -1) = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad \Psi_R (1, 1, 2, -1) = \begin{pmatrix} \nu_R \\ e_R \end{pmatrix}.$$

- Vector-like fermions are introduced to realize “universal seesaw” for charged fermion masses: [Davidson, Wali \(1987\)](#)

$$P(3, 1, 1, 4/3), \quad N(3, 1, 1, -2/3), \quad E(1, 1, 1, -2).$$

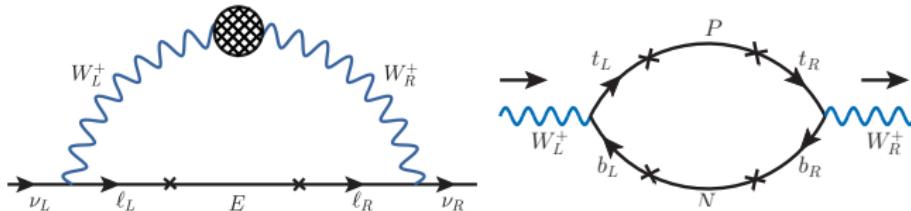
- Higgs sector is very simple:

$$\chi_L (1, 2, 1, 1) = \begin{pmatrix} \chi_L^+ \\ \chi_L^0 \end{pmatrix}, \quad \chi_R (1, 1, 2, 1) = \begin{pmatrix} \chi_R^+ \\ \chi_R^0 \end{pmatrix}$$

- $\langle \chi_R^0 \rangle = \kappa_R$ breaks $SU(2)_R \times U(1)_X$ down to $U(1)_Y$, and $\langle \chi_L^0 \rangle = \kappa_L$ breaks the electroweak symmetry with $\kappa_R \gg \kappa_L$

Two-loop Dirac Neutrino Masses

- ▶ Higgs sector is very simple: $\chi_L(1, 2, 1, 1/2) + \chi_R(1, 1, 2, 1/2)$
- ▶ $W_L^+ - W_R^+$ mixing is absent at tree-level in the model
- ▶ $W_L^+ - W_R^+$ mixing induced at loop level, which in turn generates Dirac neutrino mass at two loop Babu, He (1989)



- ▶ Flavor structure of two loop diagram needs to be studied to check consistency
- ▶ Oscillation date fits well within the model regardless of Parity breaking scale Babu, He, Su, Thapa (2022)

Neutrino Fit in Two-loop Dirac Mass Model

Oscillation parameters	3 σ range NuFit5.1	Model prediction			
		BP I (NH)	BP II (NH)	BP III (IH)	BP IV (IH)
$\Delta m_{21}^2 (10^{-5} \text{ eV}^2)$	6.82 - 8.04	7.42	7.32	7.35	7.30
$\Delta m_{23}^2 (10^{-3} \text{ eV}^2) (\text{IH})$	2.410 - 2.574	-	-	2.48	2.52
$\Delta m_{31}^2 (10^{-3} \text{ eV}^2) (\text{NH})$	2.43 - 2.593	2.49	2.46	-	-
$\sin^2 \theta_{12}$	0.269 - 0.343	0.324	0.315	0.303	0.321
$\sin^2 \theta_{23}$ (IH)	0.410 - 0.613	-	-	0.542	0.475
$\sin^2 \theta_{23}$ (NH)	0.408 - 0.603	0.491	0.452	-	-
$\sin^2 \theta_{13}$ (IH)	0.02055 - 0.02457	-	-	0.0230	0.0234
$\sin^2 \theta_{13}$ (NH)	0.02060 - 0.02435	0.0234	0.0223	-	-
δ_{CP} (IH)	192 - 361	-	-	271°	296°
δ_{CP} (NH)	105 - 405	199°	200°	-	-
$m_{\text{light}} (10^{-3} \text{ eV})$	0.66	0.17	0.078	4.95	
M_{E_1} / M_{W_R}	917	321.3	639	3595	
M_{E_2} / M_{W_R}	0.650	19.3	1.54	5.03	
M_{E_3} / M_{W_R}	0.019	1.26	0.054	2.94	

- ▶ Ten parameters to fit oscillation data
- ▶ Both normal ordering and inverted ordering allowed
- ▶ Dirac CP phase is unconstrained
- ▶ Left-right symmetry breaking scale is not constrained

Tests with N_{eff} in Cosmology

- Dirac neutrino models of this type will modify N_{eff} by about 0.14

$$\Delta N_{\text{eff}} \simeq 0.027 \left(\frac{106.75}{g_*(T_{\text{dec}})} \right)^{4/3} g_{\text{eff}}$$

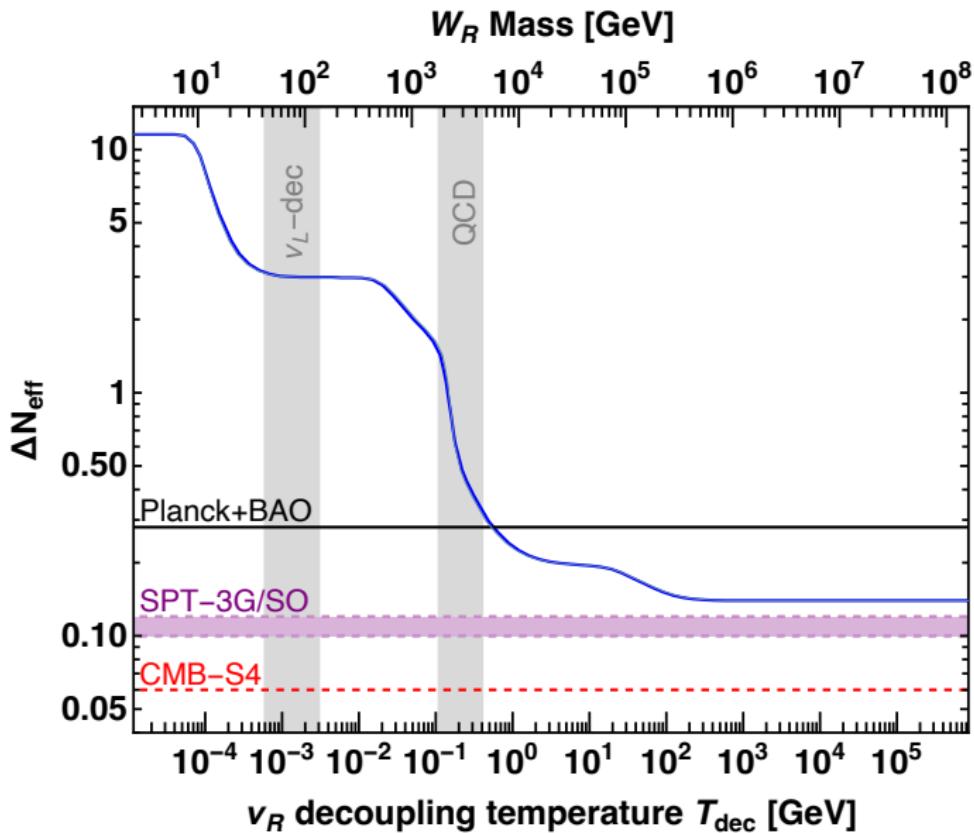
$$g_{\text{eff}} = (7/8) \times (2) \times (3) = 21/4$$

- Can be tested in CMB measurements: $N_{\text{eff}} = 2.99 \pm 0.17$ (Planck+BAO)

$$G_F^2 \left(\frac{M_{W_L}}{M_{W_R}} \right)^4 T_{\text{dec}}^5 \approx \sqrt{g^*(T_{\text{dec}})} \frac{T_{\text{dec}}^2}{M_{\text{Pl}}}$$

$$T_{\text{dec}} \simeq 400 \text{ MeV} \left(\frac{g_*(T_{\text{dec}})}{70} \right)^{1/6} \left(\frac{M_{W_R}}{5 \text{ TeV}} \right)^{4/3}$$

- Present data sets a lower limit of 7 TeV on W_R mass



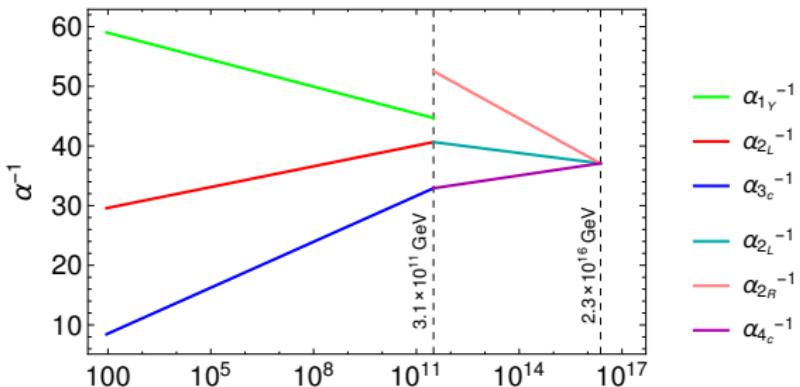
Unification of Forces & Matter in $SO(10)$

16 members of a family fit into a spinor of $SO(10)$

u_r : { - + + + - }	d_r : { - + + - + }	u_r^c : { + - - + + }	d_r^c : { + - - - - }
u_b : { + - + + - }	d_b : { + - + - + }	u_b^c : { - + - + + }	d_b^c : { - + - - - }
u_g : { + + - + - }	d_g : { + + - - + }	u_g^c : { - - + + + }	d_g^c : { - - + - - }
v : { - - - + - }	e : { - - - - + }	v^c : { + + + + + }	e^c : { + + + - - }

First 3 spins refer to color, last two are weak spins

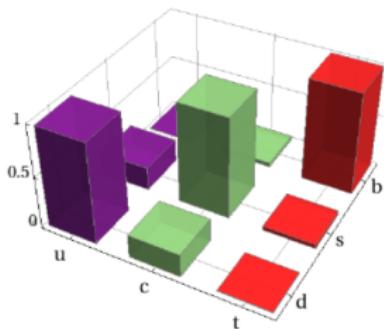
$$Y = \frac{1}{3}\Sigma(C) - \frac{1}{2}\Sigma(W)$$



Disparity in Quark & Lepton Mixings

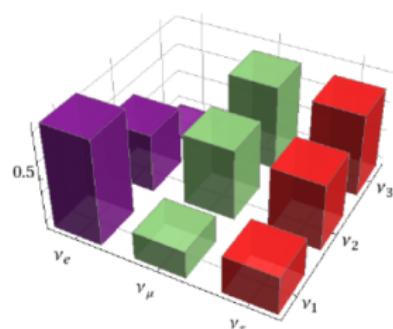
- Quark Mixings

$$V_{CKM} \sim \begin{bmatrix} 0.976 & 0.22 & 0.004 \\ -0.22 & 0.98 & 0.04 \\ 0.007 & -0.04 & 1 \end{bmatrix}$$



- Leptonic Mixings

$$U_{PMNS} \sim \begin{bmatrix} 0.85 & -0.54 & 0.16 \\ 0.33 & 0.62 & -0.72 \\ -0.40 & -0.59 & -0.70 \end{bmatrix}$$



Yukawa Sector of Minimal $SO(10)$

$$16 \times 16 = 10_s + 120_a + 126_s$$

- At least two Higgs fields needed for family mixing
- Symmetric 10_H and $\overline{126}$ is the minimal model

$$W_{SO(10)} = 16^T (Y_{10} 10_H + Y_{126} \overline{126}_H) 16 .$$

$$M_U = v_u^{10} Y_{10} + v_u^{126} Y_{126}$$

$$M_D = v_d^{10} Y_{10} + v_d^{126} Y_{126}$$

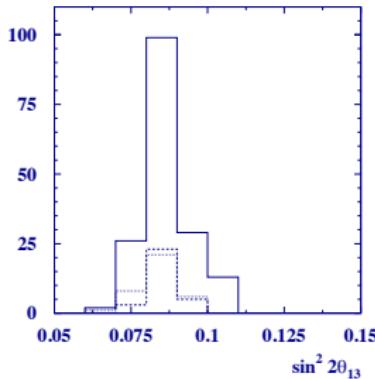
$$M_E = v_d^{10} Y_{10} - 3v_d^{126} Y_{126}$$

$$M_{\nu_D} = v_u^{10} Y_{10} - 3v_u^{126} Y_{126}$$

$$M_R = Y_{126} V_R$$

Minimal Yukawa sector of SO(10)

- ▶ 12 parameters plus 7 phases to fit 18 observed quantities
- ▶ This setup fits all obsevables quite well
- ▶ Large neutrino mixings coexist with small quark mixings
- ▶ θ_{13} prediction turned out to be correct



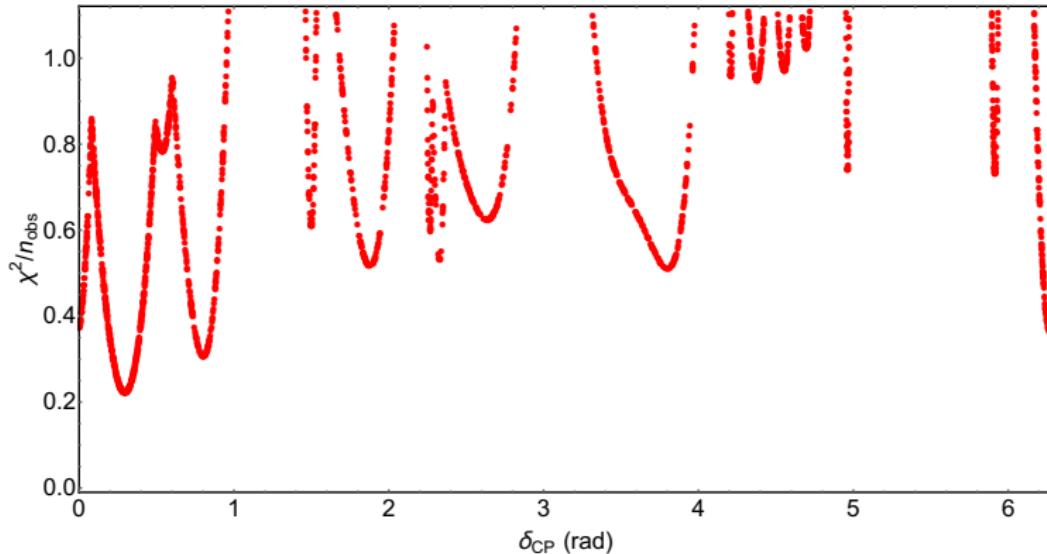
Babu, Mohapatra (1993); Bajc, Senjanovic, Vissani (2001); (2003); Fukuyama, Okada (2002); Goh, Mohapatra, Ng (2003); Bajc, Melfo, Senjanovic, Vissani (2004); Bertolini, Malinsky, Schwetz (2006); Babu, Macesanu (2005); Dutta, Mimura, Mohapatra (2007); Aulakh et al (2004); Bajc, Dorsner, Nemevsek (2009); Joshipura, Patel (2011); Dueck, Rodejohann (2013); Ohlsson, Penrow (2019); Babu, Bajc, Saad (2018); Babu, Saad (2021)

Best fit values for fermion masses and mixings

Observables (masses in GeV)	SUSY			non-SUSY		
	Input	Best Fit	Pull	Input	Best Fit	Pull
$m_u/10^{-3}$	0.502 ± 0.155	0.515	0.08	0.442 ± 0.149	0.462	0.13
m_c	0.245 ± 0.007	0.246	0.14	0.238 ± 0.007	0.239	0.18
m_t	90.28 ± 0.89	90.26	-0.02	74.51 ± 0.65	74.47	-0.05
$m_b/10^{-3}$	0.839 ± 0.17	0.400	-2.61	1.14 ± 0.22	0.542	-2.62
$m_s/10^{-3}$	16.62 ± 0.90	16.53	-0.09	21.58 ± 1.14	22.57	0.86
m_b	0.938 ± 0.009	0.933	-0.55	0.994 ± 0.009	0.995	0.19
$m_e/10^{-3}$	0.3440 ± 0.0034	0.344	0.08	0.4707 ± 0.0047	0.470	-0.03
$m_\mu/10^{-3}$	72.625 ± 0.726	72.58	-0.05	99.365 ± 0.993	99.12	-0.24
m_τ	1.2403 ± 0.0124	1.247	0.57	1.6892 ± 0.0168	1.688	-0.05
$ V_{us} /10^{-2}$	22.54 ± 0.07	22.54	0.02	22.54 ± 0.06	22.54	0.06
$ V_{cb} /10^{-2}$	3.93 ± 0.06	3.908	-0.42	4.856 ± 0.06	4.863	0.13
$ V_{ub} /10^{-2}$	0.341 ± 0.012	0.341	0.003	0.420 ± 0.013	0.421	0.10
δ_{CKM}^o	69.21 ± 3.09	69.32	0.03	69.15 ± 3.09	70.24	0.35
$\Delta m_{21}^2/10^{-5}(eV^2)$	8.982 ± 0.25	8.972	-0.04	12.65 ± 0.35	12.65	-0.01
$\Delta m_{31}^2/10^{-3}(eV^2)$	3.05 ± 0.04	3.056	0.02	4.307 ± 0.059	4.307	0.006
$\sin^2 \theta_{12}$	0.318 ± 0.016	0.314	-0.19	0.318 ± 0.016	0.316	-0.07
$\sin^2 \theta_{23}$	0.563 ± 0.019	0.563	0.031	0.563 ± 0.019	0.563	0.01
$\sin^2 \theta_{13}$	0.0221 ± 0.0006	0.0221	-0.003	0.0221 ± 0.0006	0.0220	-0.16
δ_{CP}^o	224.1 ± 33.3	240.1	0.48	224.1 ± 33.3	225.1	0.03
χ^2	-	-	7.98	-	-	7.96

Dirac CP phase

Multiple χ^2 minima make δ_{CP} prediction difficult



Babu, Bajc, Saad (2018)

Proton decay predictions

- ▶ Proton decay branching ratios determined by neutrino oscillation fits
- ▶ Mediated by superheavy gauge bosons
- ▶ Lifetime has large uncertainties, $\tau_p \approx (10^{32} - 10^{36})$ yrs.

Prediction of branching ratios

$$\Gamma(p \rightarrow \pi^0 e^+) \rightarrow 47\%$$

$$\Gamma(p \rightarrow \pi^0 \mu^+) \rightarrow 1\%$$

$$\Gamma(p \rightarrow \eta^0 e^+) \rightarrow 0.20\%$$

$$\Gamma(p \rightarrow \eta^0 \mu^+) \rightarrow 0.00\%$$

$$\Gamma(p \rightarrow K^0 e^+) \rightarrow 0.16\%$$

$$\Gamma(p \rightarrow K^0 \mu^+) \rightarrow 3.62\%$$

$$\Gamma(p \rightarrow \pi^+ \bar{\nu}) \rightarrow 48\%$$

$$\Gamma(p \rightarrow K^+ \bar{\nu}) \rightarrow 0.22\%$$

Nemesvek, Bajc, Dorsner (2009)

Babu, Khan (2015)

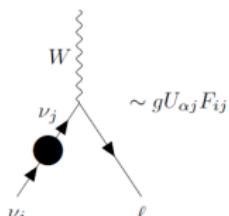
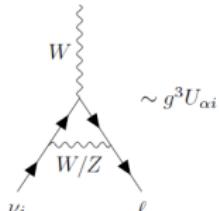
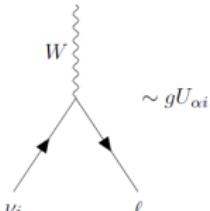
Energy-dependent oscillation parameters

- In presence of light new physics coupled to neutrinos, oscillation angles at production and detection may not coincide
- Quantum corrections can lead to observable signals in neutrino oscillations. Babu, Brdar, de Gouvea, Machado (2021); (2022)
- For neutrino produced in pion decay, $Q_p^2 = m_\pi^2$, but if detected via $\nu + n \rightarrow e^- + p$, $Q_d^2 \approx m_n E_\nu$. For two flavors,

$$P_{e\mu} = P_{\mu e} = \sin^2(\theta_p - \theta_d) + \sin 2\theta_p \sin 2\theta_d \sin^2 \left(\frac{\Delta m^2 L}{4E} + \frac{\beta}{2} \right)$$

$$\theta(Q_p^2) \equiv \theta_p, \quad \theta(Q_d^2) \equiv \theta_d, \quad \text{and} \quad \tilde{\beta}(Q_d^2) - \tilde{\beta}(Q_p^2) \equiv \beta$$

- $\theta_p \neq \theta_d$ if there are light states in the mass range Q_p and Q_d



Addressing MiniBoone Anomaly

- Active neutrinos assumed to mix with two sterile neutrinos:

$$M_\nu = \begin{pmatrix} x & x & x & \mu_e & 0 \\ x & x & x & \mu_\mu & 0 \\ x & x & x & \mu_\tau & 0 \\ \mu_e & \mu_\mu & \mu_\tau & 0 & M \\ 0 & 0 & 0 & M & 0 \end{pmatrix}$$

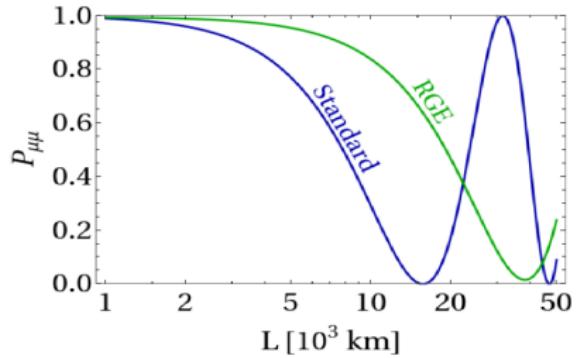
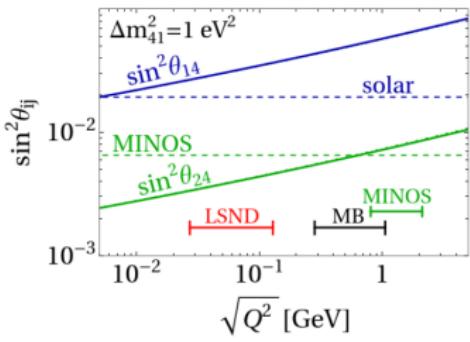
$$\tan \theta_{14} \simeq \frac{\mu_e}{M}, \quad \tan \theta_{24} \simeq \frac{\mu_\mu}{M}$$

- If N_i couple to a light gauge boson, M will decrease with energy, and thus θ_{14} and θ_{24} will decrease

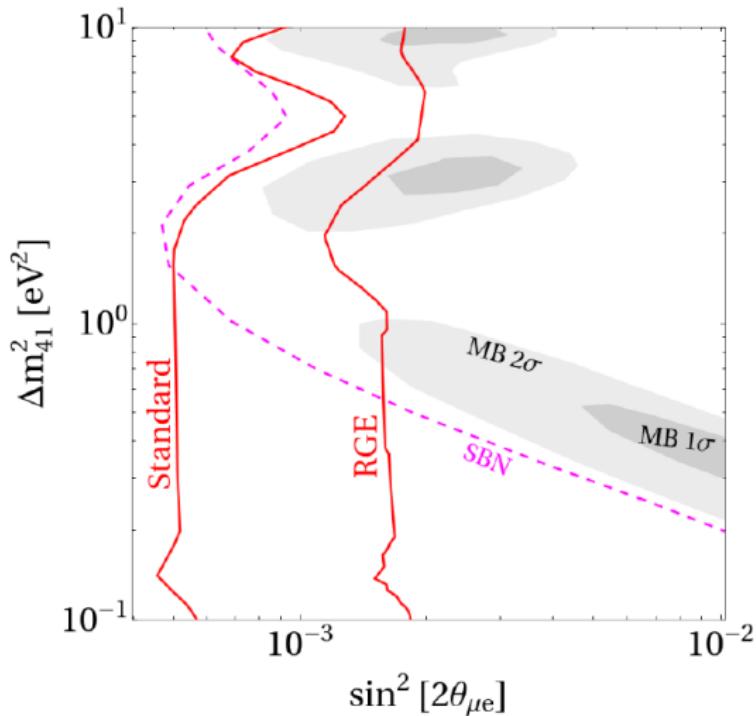
$$M(\mu) = M(\mu_0) \left(1 - \frac{5g'(\mu_0)^2}{24\pi^2} \ln\left(\frac{\mu}{\mu_0}\right) \right)^{9/4}$$

- Tension between appearance and disappearance experiments can be relaxed by this running effect

Addressing MiniBoone Anomaly: Results



MiniBoone Results



Babu, Brdar, de Gouvea, Machado (2022)

Radiative neutrino mass generation

- ▶ An alternative to seesaw is radiative neutrino mass generation, where neutrino mass is absent at tree level, but arises via quantum loop corrections
- ▶ The smallness of neutrino mass is explained by loop and chiral suppressions
- ▶ Loop diagrams may arise at 1-loop, 2-loop or 3-loop levels
- ▶ New physics scale typically near TeV and thus accessible to LHC
- ▶ Further tests in observable LFV processes and as nonstandard neutrino interaction (NSI) in oscillations

Effective $\Delta L = 2$ Operators

$$\begin{aligned}\mathcal{O}_1 &= L^i L^j H^k H^l \epsilon_{ik} \epsilon_{jl} \\ \mathcal{O}_2 &= L^i L^j L^k e^c H^l \epsilon_{ij} \epsilon_{kl} \\ \mathcal{O}_3 &= \{L^i L^j Q^k d^c H^l \epsilon_{ij} \epsilon_{kl}, \quad L^i L^j Q^k d^c H^l \epsilon_{ik} \epsilon_{jl}\} \\ \mathcal{O}_4 &= \{L^i L^j \bar{Q}_i \bar{u}^c H^k \epsilon_{jk}, \quad L^i L^j \bar{Q}_k \bar{u}^c H^k \epsilon_{ij}\} \\ \mathcal{O}_5 &= L^i L^j Q^k d^c H^l H^m \bar{H}_i \epsilon_{jl} \epsilon_{km} \\ \mathcal{O}_6 &= L^i L^j \bar{Q}_k \bar{u}^c H^l H^k \bar{H}_i \epsilon_{jl} \\ \mathcal{O}_7 &= L^i Q^j \bar{e}^c \bar{Q}_k H^k H^l H^m \epsilon_{il} \epsilon_{jm} \\ \mathcal{O}_8 &= L^i \bar{e}^c \bar{u}^c d^c H^j \epsilon_{ij} \\ \mathcal{O}_9 &= L^i L^j L^k e^c L^l e^c \epsilon_{ij} \epsilon_{kl} \\ \mathcal{O}'_1 &= L^i L^j H^k H^l \epsilon_{ik} \epsilon_{jl} H^{*m} H_m\end{aligned}$$

Babu & Leung (2001)

de Gouvea & Jenkins (2008)

Angel & Volkas (2012)

Cai, Herrero-Garcia, Schmidt, Vicente, Volkas (2017)

Lehman (2014) – all $d = 7$ operators

Li, Ren, Xiao, Yu, Zheng (2020); Liao, Ma (2020) – all $d = 9$ operators

Operator \mathcal{O}_2 and the Zee model

- ▶ Introduce a singly charged scalar and a second Higgs doublet to standard model:

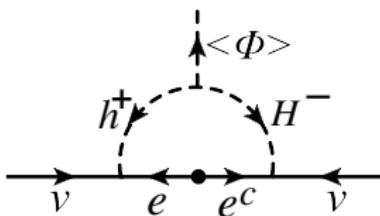
$$\mathcal{L} = f_{ij} L_i^a L_j^b h^+ \epsilon_{ab} + \mu H^a \Phi^b h^- \epsilon_{ab} + \text{h.c.}$$



$$\mathcal{O}_2 = L^i L^j L^k e^c H^l \epsilon_{ij} \epsilon_{kl}$$

Zee (1980)

- ▶ Neutrino mass arises at one-loop.



- ▶ A minimal version of this model in which only one Higgs doublet couples to a given fermion sector with a Z_2 symmetry yields: Wolfenstein (1980)

$$m_\nu = \begin{pmatrix} 0 & m_{e\mu} & m_{e\tau} \\ m_{e\mu} & 0 & m_{\mu\tau} \\ m_{e\tau} & m_{\mu\tau} & 0 \end{pmatrix}, \quad m_{ij} \simeq \frac{f_{ij}}{16\pi^2} \frac{(m_i^2 - m_j^2)}{\Lambda}$$

It requires $\theta_{12} \simeq \pi/4 \rightarrow$ ruled out by solar + KamLAND data.

Koide (2001); Frampton *et al.* (2002); He (2004)

Neutrino oscillations in the Zee model

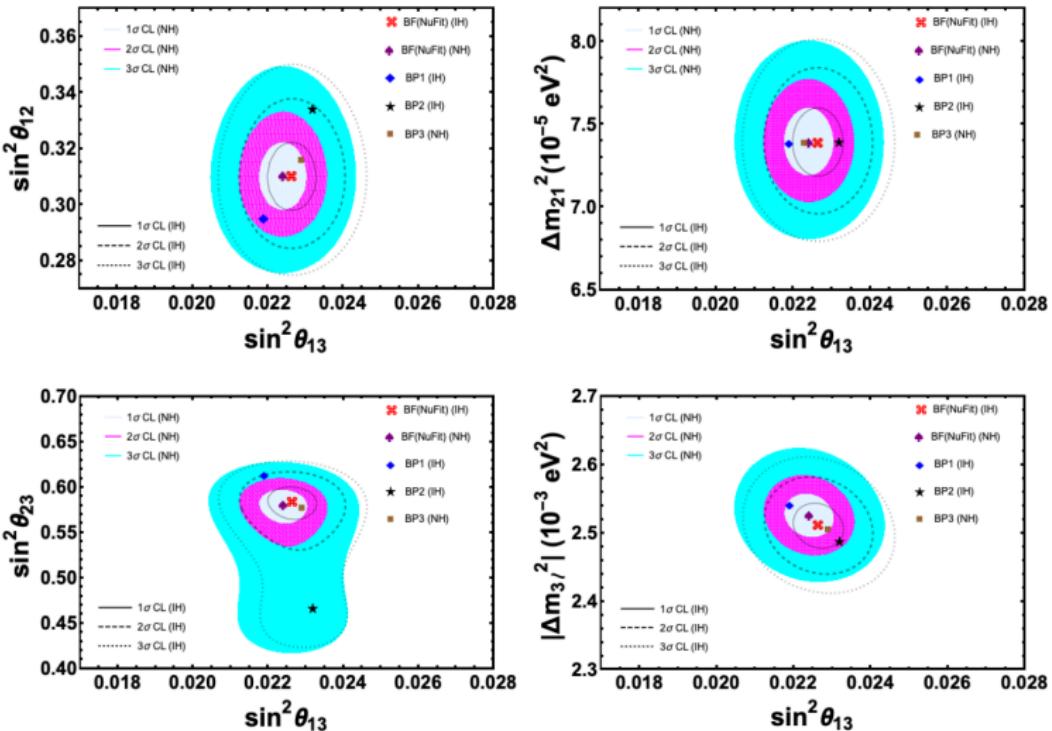
- Neutrino oscillation data can be fit to the Zee model consistently without the Z_2 symmetry
- Some benchmark points for Yukawa couplings of second doublet:

$$\text{BP I: } Y = \begin{pmatrix} Y_{ee} & 0 & Y_{e\tau} \\ 0 & Y_{\mu\mu} & Y_{\mu\tau} \\ 0 & Y_{\tau\mu} & Y_{\tau\tau} \end{pmatrix}$$

$$\text{BP II: } Y = \begin{pmatrix} 0 & Y_{e\mu} & Y_{e\tau} \\ Y_{\mu e} & 0 & Y_{\mu\tau} \\ 0 & Y_{\tau\mu} & Y_{\tau\tau} \end{pmatrix}$$

$$\text{BP III: } Y = \begin{pmatrix} Y_{ee} & 0 & Y_{e\tau} \\ 0 & Y_{\mu\mu} & Y_{\mu\tau} \\ Y_{\tau e} & 0 & Y_{\tau\tau} \end{pmatrix}$$

Neutrino fit in the Zee model



Babu, Dev, Jana, Thapa (2019)

Neutrino Non-Standard Interactions (NSI)

- Neutrino oscillation picture would change if there are non-standard interactions
- Modification of matter effects most important
- EFT for neutrino NSI:

$$\mathcal{L}_{\text{NSI}}^{\text{NC}} = -2\sqrt{2}G_F \sum_{f,X,\alpha,\beta} \varepsilon_{\alpha\beta}^{fx} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_X f) ,$$

$$\mathcal{L}_{\text{NSI}}^{\text{CC}} = -2\sqrt{2}G_F \sum_{f,f',X,\alpha,\beta} \varepsilon_{\alpha\beta}^{ff'X} (\bar{\nu}_\alpha \gamma^\mu P_L \ell_\beta) (\bar{f}' \gamma_\mu P_X f)$$

Wolfenstein (1978)

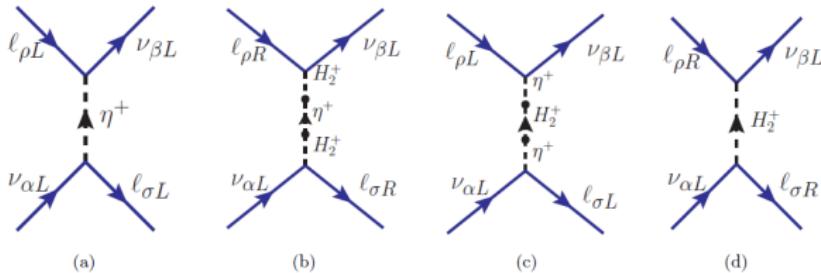
- Effective Hamiltonian for neutrino propagation in matter is now:

$$H = \frac{1}{2E} U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger + \sqrt{2} G_F N_e(x) \begin{pmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}$$

- $\varepsilon_{\alpha\beta}$ measure of NSI normalized to weak interaction strength

Neutrino NSI in the Zee model

- The two charged scalars of the Zee model mediate NSI



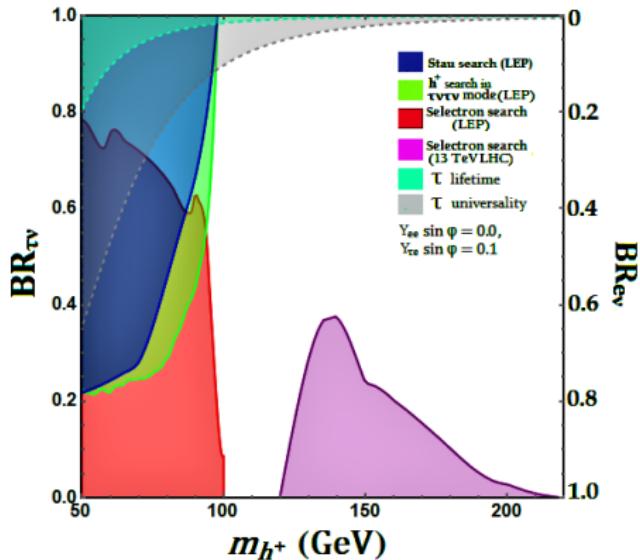
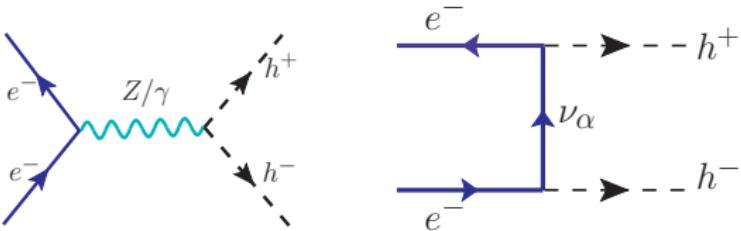
- The NSI parameters are given by:

$$\varepsilon_{\alpha\beta} = \frac{1}{4\sqrt{2}G_F} Y_{\alpha e} Y_{\beta e}^* \left(\frac{\sin^2 \varphi}{m_{h^+}^2} + \frac{\cos^2 \varphi}{m_{H^+}^2} \right)$$

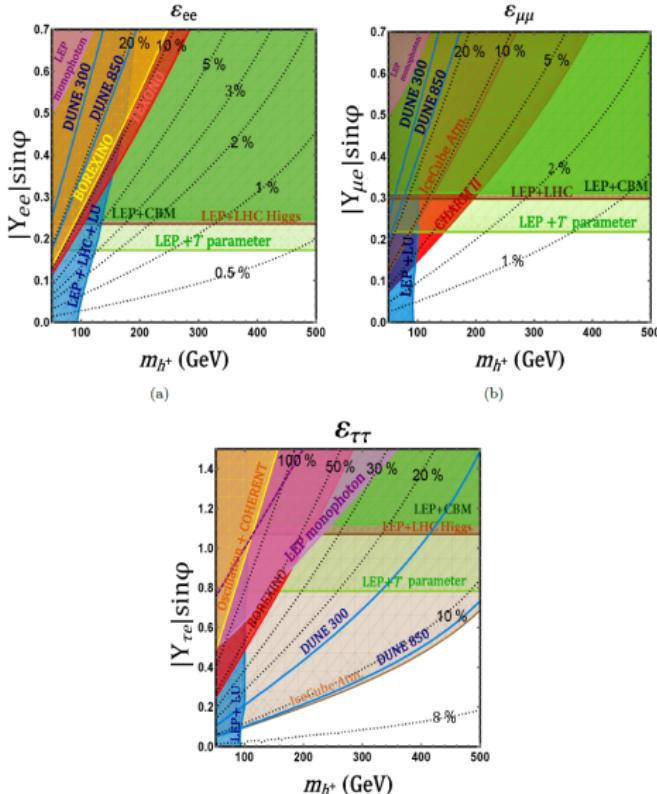
- Constrained by LHC and LEP direct limits; cLFV; precision electroweak tests; neutrino oscillation data; and theory

Babu, Dev, Jana, Thapa (2019)

LEP and LHC constraints on Charged Scalar

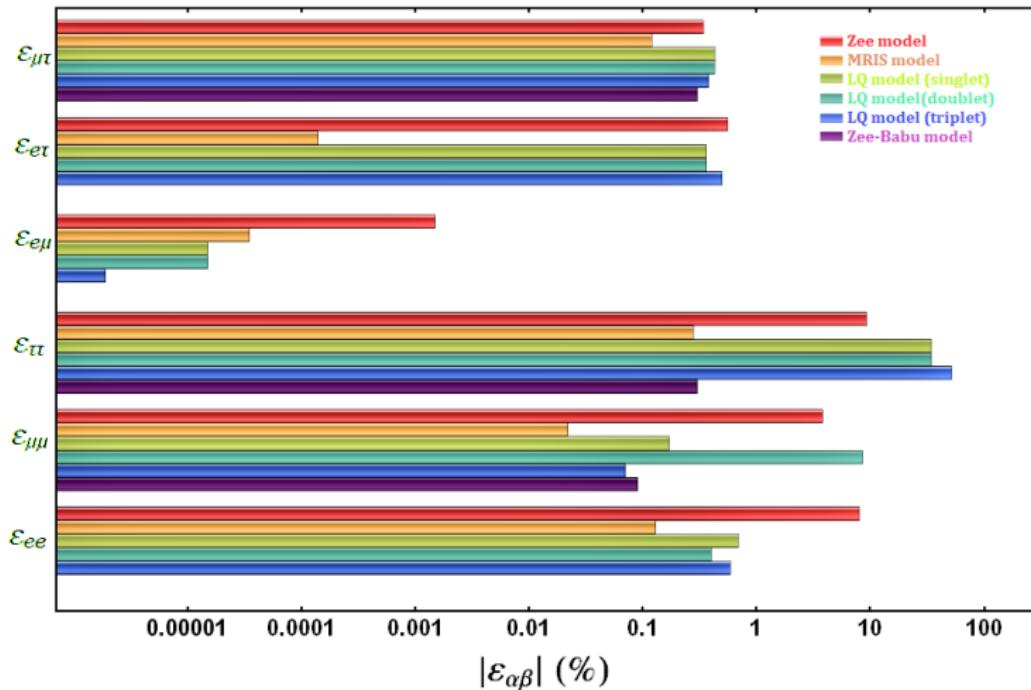


Diagonal NSI in Zee model



Babu, Dev, Jana, Thapa (2019)

Summary of NSI in radiative models



Babu, Dev, Jana, Thapa (2019)

Conclusions

- ▶ EFT description alone in neutrino sector is inadequate; we may miss important phenomena such as leptogenesis
- ▶ Grand Unification provides powerful tools to interconnect neutrino sector with quark sector
- ▶ Neutrino may very well be Dirac particles; interesting models of Dirac neutrino exist
- ▶ Lepton number violation by two units is accessible at the LHC, which would imply Majorana nature of neutrino
- ▶ Energy-dependent oscillation angles can arise in presence of light fields coupled to neutrinos
- ▶ Various $d = 7$ and $d = 9$ lepton number violating EFT operators can lead to interesting neutrino mass models