

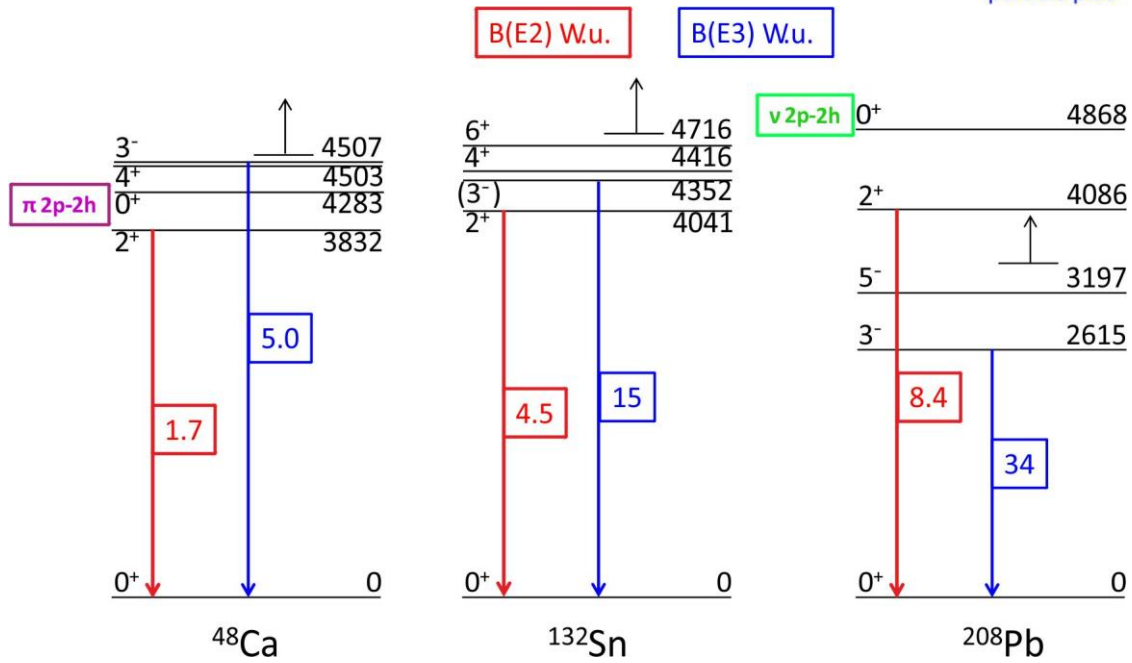
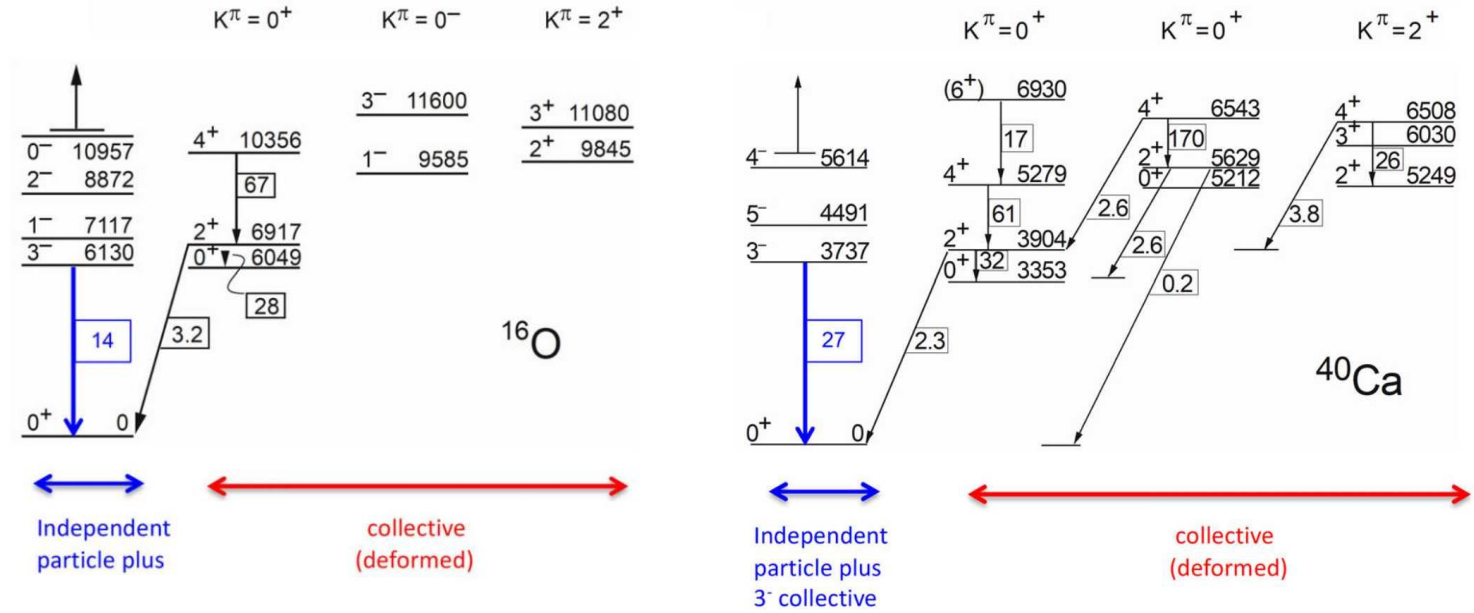
Transition probabilities of low-lying excited states in ^{210}Po and ^{210}Pb

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How magic are the doubly magic nuclei?

N=Z doubly magic nuclei (^{16}O and ^{40}Ca)
 → examples of *shape coexistence* at the level of first excited states

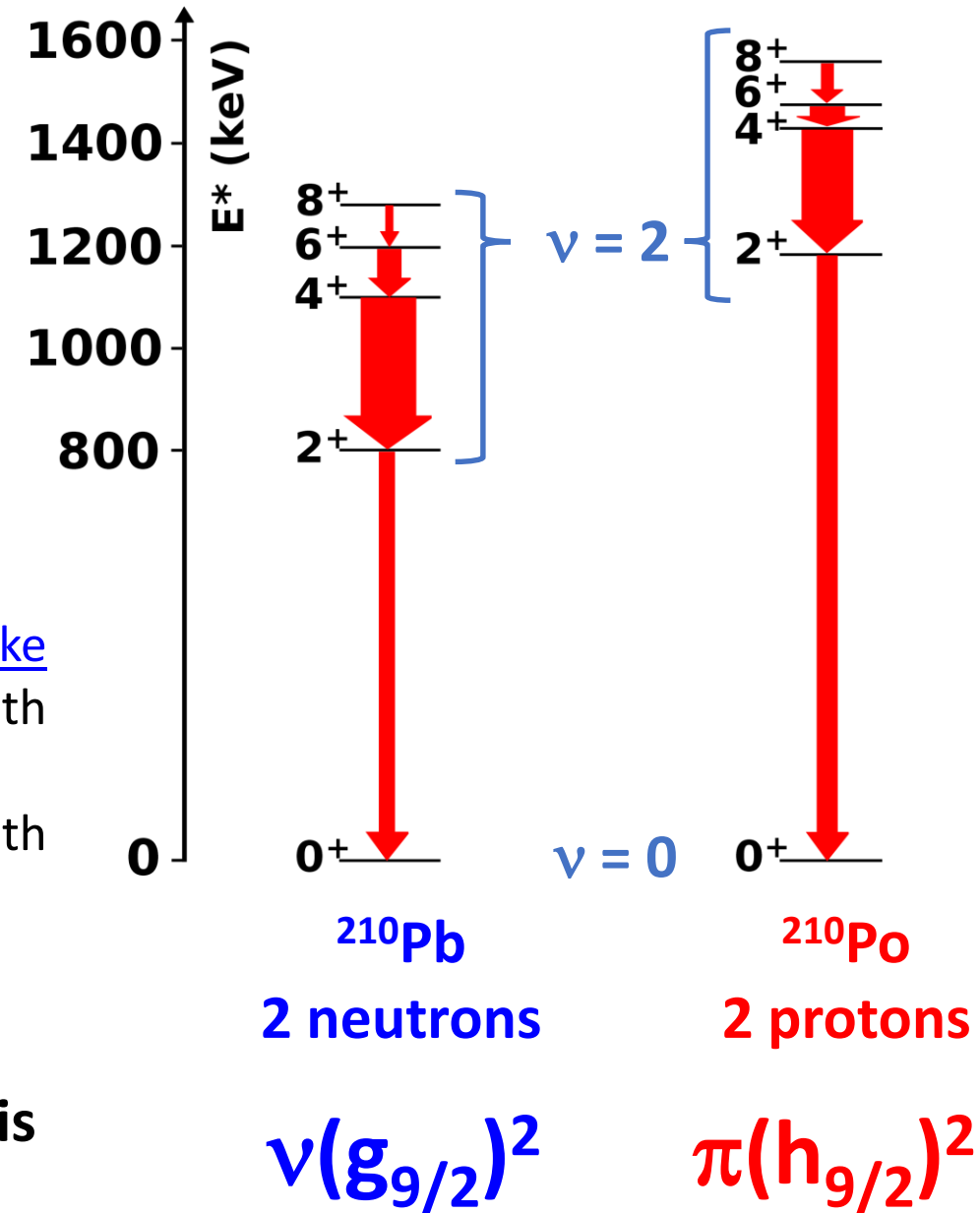


N > Z doubly magic nuclei (^{48}Ca , ^{132}Sn , ^{208}Pb)
 → *octupole correlations* at the (very) low excitation energies

Do we understand the structure of ^{208}Pb and its vicinity???

Properties of the 2-particle configurations above ^{208}Pb

	^{210}Po $\alpha=100\%$	^{211}Po $\alpha=100\%$	^{212}Po $\alpha=100\%$
	^{209}Bi Abundance=100.0%	^{210}Bi $\beta^- = 100\%$	^{211}Bi $\alpha \approx 100\%$
Z = 82	^{208}Pb Abundance=52.4%	^{209}Pb $\beta^- = 100\%$	^{210}Pb $\beta^- = 100\%$
	N = 126		



- The energies of the yrast 2^+ , 4^+ , 6^+ , and 8^+ states follow [seniority-like pattern of decreasing energy splitting](#) between adjacent states with increasing spin;
- The magnetic moments of the 6^+ and the 8^+ states are known in both nuclei:

$$g(8^+; ^{210}\text{Pb}) = -0.312(8)$$

$$g(6^+; ^{210}\text{Pb}) = -0.312(15)$$

$$g(8^+; ^{210}\text{Po}) = +0.891(6)$$

$$g(6^+; ^{210}\text{Po}) = +0.913(8)$$

In both nuclei the structure of the 2^+ , 4^+ , 6^+ , and 8^+ states is dominated by the seniority 2 configuration

Properties of the 2 – particle configurations above ^{208}Pb

Shell model calculations

Kuo-Herling interaction (E. K. Warburton and B. A. Brown, Phys. Rev. C 43, 602 (1991)).

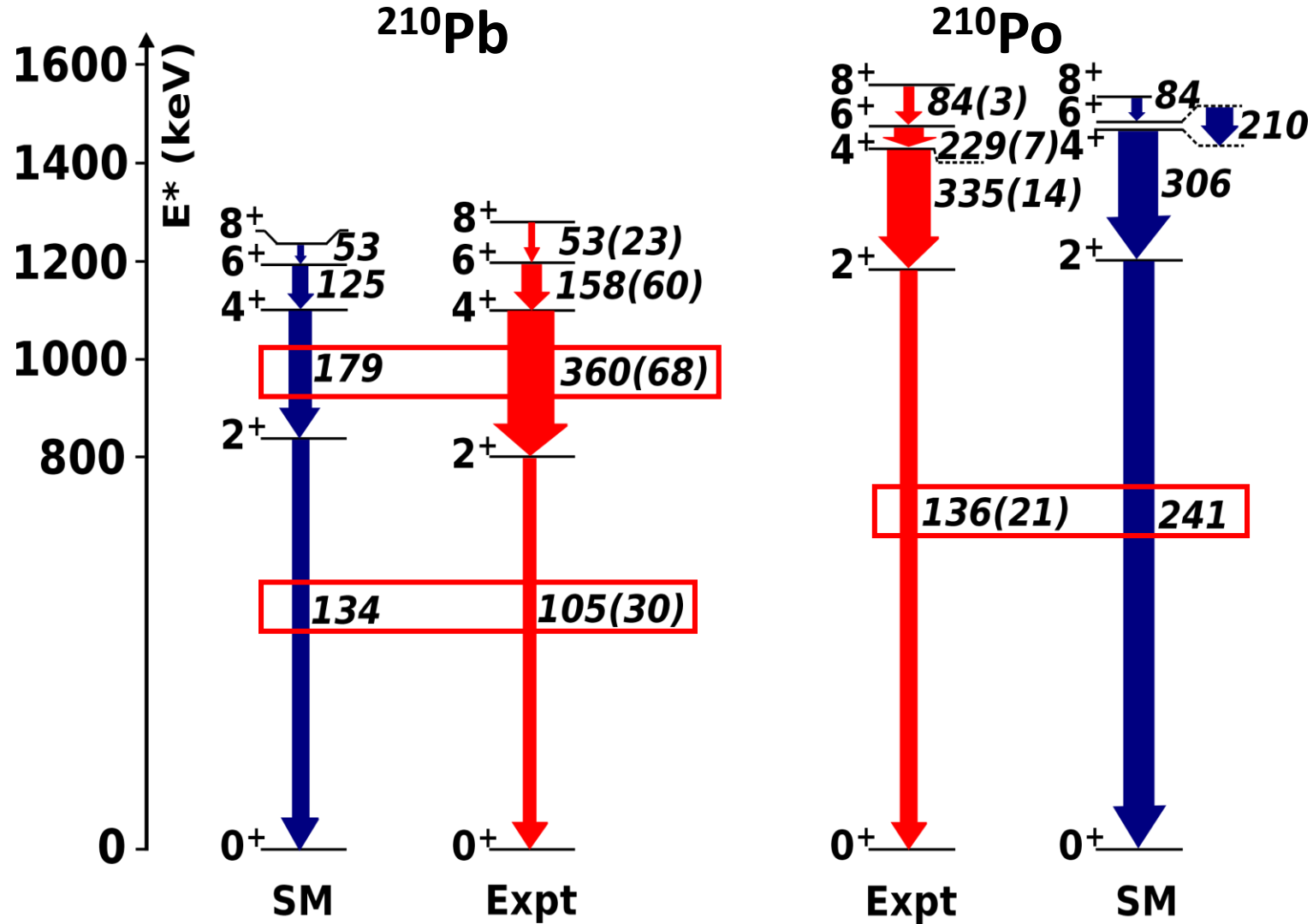
2 protons in $(2p_{1/2}, 2p_{3/2}, 1f_{5/2}, 1f_{7/2}, 0h_{9/2}, 0i_{13/2})$ and 2 neutrons in $(3s_{1/2}, 2d_{3/2}, 2d_{5/2}, 1g_{7/2}, 1g_{9/2}, 0h_{11/2}, 0j_{15/2})$

$(e_{\pi}, e_{\nu}) = (1.44e, 0.91e)$ fixed to the $B(E2; 8^+_1 \rightarrow 6^+_1)$ values in ^{210}Po and ^{210}Pb , respectively

Results:

- Almost perfect reproductions of the energies of the yrast states;
- Good agreement between the experimental and the calculated static moments;
- Good agreement between all experimental and theoretical $B(E2)$ but the $B(E2; 2^+_1 \rightarrow 0^+_1)$ values (and $B(E2; 4^+_1 \rightarrow 2^+_1)$ in ^{210}Pb)

The problem is present in all shell model calculations available in this mass region (CD Bonn potential, H208 interaction) but also appears in QPM calculations.



Properties of the 2 – particle configurations above ^{208}Pb ?

Two hypothesis:

- 1) There are some **deficiencies** in the shell model
- 2) The experimental results for the lifetimes of the 2^+_1 states of ^{210}Pb and ^{210}Po **contain systematic errors.**

PHYSICAL REVIEW C **67**, 054310 (2003)

Large-scale shell model calculations for the $N=126$ isotones Po–Pu

E. Caurier,¹ M. Rejmund,² and H. Grawe³

particle units (W.u.). The agreement for the two- and three-particle nuclei ^{210}Po and ^{211}At is noteworthy and corroborates the choice of the polarization charge. The deviation observed for the $2^+ \rightarrow 0^+$ transition in ^{210}Po can be ascribed both to a systematic uncertainty in the experimental data as deduced from (d, d') inelastic scattering [33], and to the neglect of ^{208}Pb ph excitations in the shell model, which enter most sensitively the $I^\pi = 2^+$ states [34] (see footnote in Table

M.S.M. Gerathy et al., Phys. Lett. **B823**, 136738 (2021).

... The discrepancy between theory and experiment for the 2^+ state in ^{210}Po (1.8(3)W.u. cf. 3.4W.u.) is well known and has been attributed to a lack of particle-hole excitations in the theoretical calculations [31,36,37]. However, **it should also be recognized that the data evaluators for the A=210 mass chain [38] note that the 2^+ lifetime measurement in ^{210}Po should be tested**, so excessive interpretation of this potential discrepancy is not warranted. ...

$$^{210}\text{Po}: B(E2; 2^+_1 \rightarrow 0^+_1)$$

C. Ellegaard *et al.*, Nucl. Phys. **A206**, 83 (1973)
(d, d') & (p, p') **42(9) e²fm⁴**

The same technique used for the $B(E2; 2^+_1 \rightarrow 0^+_1)$ of ^{210}Pb

D. Kocheva *et al.*, Eur. Phys. J. **A53**, 175 (2017)
DSAM in a transfer reaction 136(21) e²fm⁴

Shell model gives 241 e²fm⁴

Possible impact of the long-lived states feeding the level of interest - is it correctly accounted for?

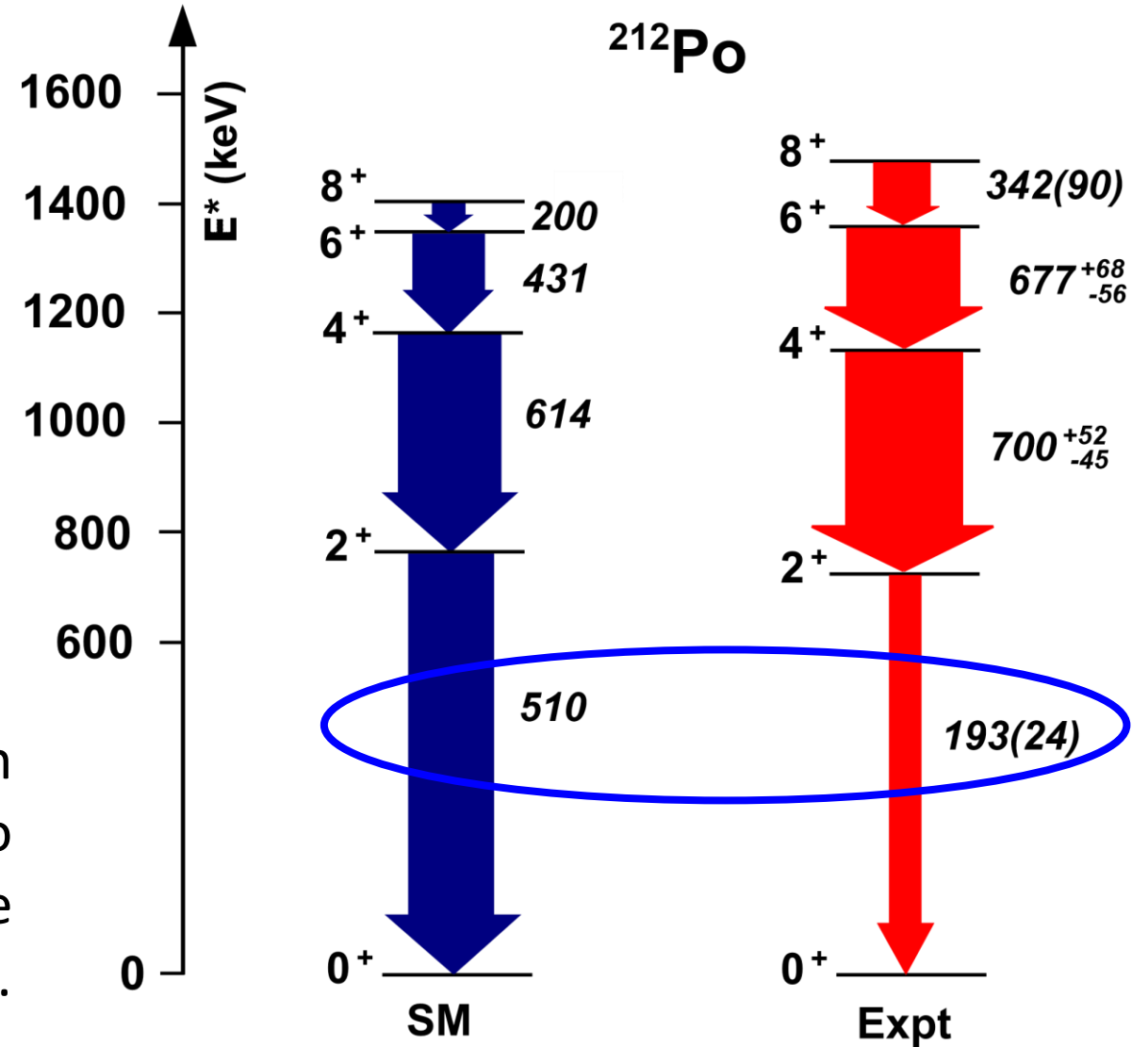
A. E. Stuchbery and J. L. Wood, Physics 4, 697 (2022).

Properties of the 2 – particle configurations above ^{208}Pb ?

It is necessary to remeasure/test/verify the $B(E2; 2^+_1 \rightarrow 0^+_1)$ values in ^{210}Po and ^{210}Pb and eventually the $B(E2; 4^+_1 \rightarrow 2^+_1)$ value in ^{210}Pb by using alternative experimental methods!

	^{210}Po $\alpha=100\%$	^{211}Po $\alpha=100\%$	^{212}Po $\alpha=100\%$
	^{209}Bi Abundance=100.0%	^{210}Bi $\beta^- = 100\%$	^{211}Bi $\alpha \approx 100\%$
Z = 82	^{208}Pb Abundance=52.4%	^{209}Pb $\beta^- = 100\%$	^{210}Pb $\beta^- = 100\%$
	N = 126		

To understand the structures of the “open shell” nuclei north-east of ^{208}Pb we have to understand completely the properties of the simplest 2-particle configurations above ^{208}Pb .



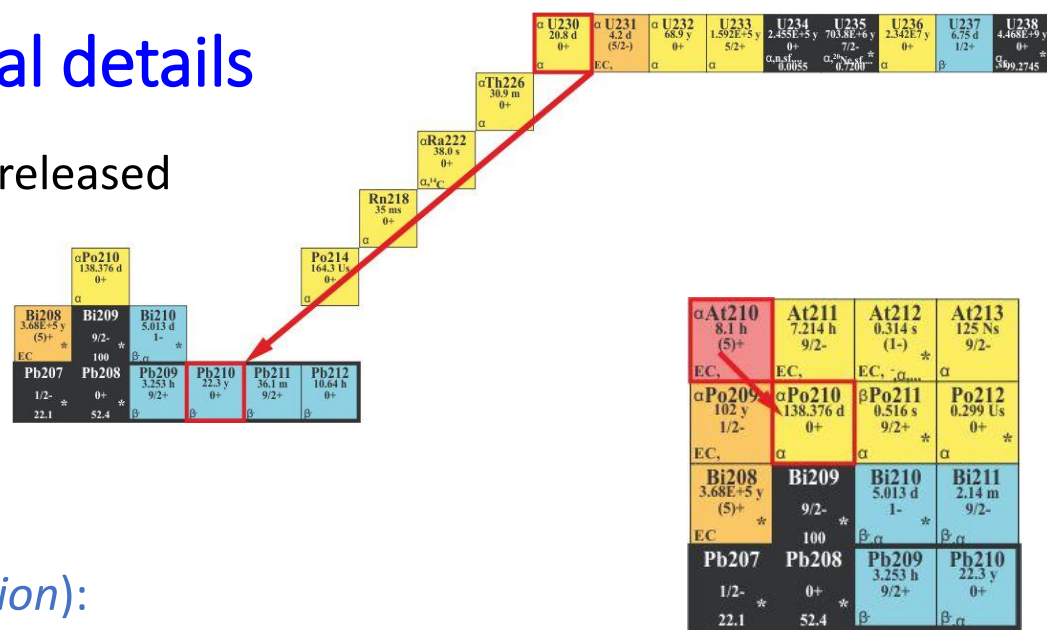
RIB production from ISOLDE and experimental details

- ^{210}Pb – produced in UC_x target as a **daughter of ^{230}U** (20.8 d) – not released during target irradiation

- (conservative) in-target production estimate $\sim 1 \times 10^7$ p/ μC

- ^{210}Po – considering only ^{210}At decay (8.3h) – **cold target irradiation**

- (conservative) in-target production estimate $\sim 1 \times 10^8$ p/ μC



RILIS Ionization efficiencies, **corrected** (*B. Marsh, private communication*):

- **~5 % for Po** (*estimated*, no mass marker available)
- **~25 % for Pb** (using the new ionization scheme)

Charge breeding and low-energy transport (*F. Wenander*) \rightarrow ~5%

Post-acceleration (*J.A. Rodriguez*) \rightarrow 75%

Beam intensity on Miniball target – **at least 2×10^5 pps** for 1 day of beam on target

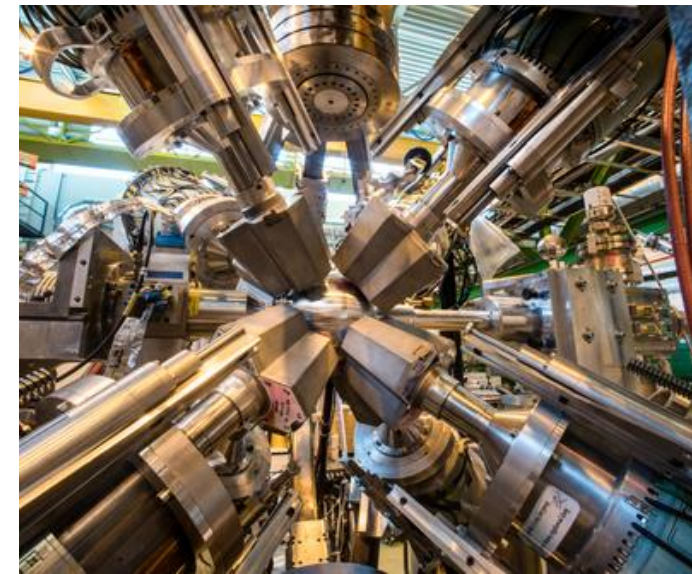
Considering all of the above efficiencies those intensities should be achievable after:

- 1 week irradiation of UC_x target (@ 1 μA) – in the ^{210}Pb case
- **1.5 days of a cold target irradiation** (@ 1 μA) – in the ^{210}Po case

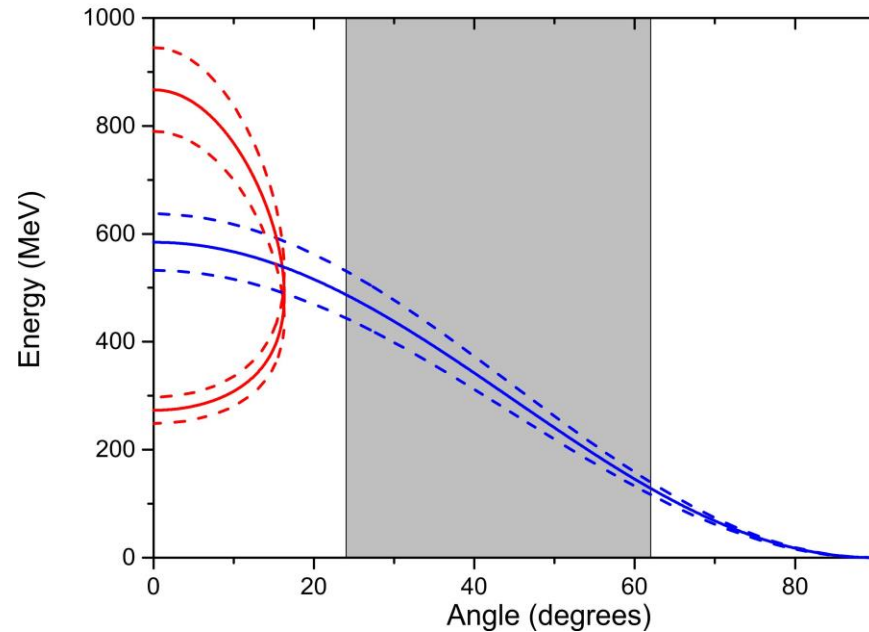
Coulomb excitation using Miniball @ 4.5 MeV/u



- **Heavy beam** ($^{210}\text{Po}/^{210}\text{Pb}$) @ 4.5 MeV/u
- **Light target** – ^{58}Ni of 2 mg/cm²



Kinematics →



- **912 γ 's per day** in the $2^+_1 \rightarrow 0^+_1$ in ^{210}Po (3% statistical uncertainty).
- **2352 γ 's per day** in the $2^+_1 \rightarrow 0^+_1$ in ^{210}Pb (2% statistical uncertainty).
 - **55 γ 's per day** in the $4^+_1 \rightarrow 2^+_1$ in ^{210}Pb (13% statistical uncertainty).

Beam-time request

Summary of requested shifts (modified):

- 3 shifts (1 day) with 2×10^5 pps ^{210}Po beam at 4.5 MeV/u on a ^{58}Ni target;
 - from a “cold irradiated” UC_x target
 - a total of 10^{10} ^{210}Po ions @ Miniball target
 - 3 shifts (1 day) with 2×10^5 pps ^{210}Pb beam at 4.5 MeV/u on a ^{58}Ni target
 - from (any) already used UC_x (RILIS) target
 - 2 x 1 shift for tuning/calibrations with beam (at lower beam intensity)
- A total of 8 shifts (*without protons*) requested

Yield estimates, Thierry Stora and Simon Stegemann

	In-target prod 210At [/muC]	Comment		Eff. Cascade [%]	Comment
FLUKA	1.00E+08	> taking pessimistic one	production	93.75%	build-up for irradiation time (4*Thalf)
ABRABLA	2.00E+08		release	100.00%	long-lived-> assume all is released
			ionization	40.00%	https://doi.org/10.1016/j.nimb.2008.05.142
			transport	5.00%	
			post-acc	80.00%	
			Post-acc yield 210Po [/muC]		
			1.50E+06		

	In-target prod 230U [/muC]	Comment		Eff. Cascade [%]	Comment
FLUKA	6.00E+08		production	21.54%	build-up for irradiation time (7d)
ABRABLA	8.00E+07	> taking pessimistic one	release	100.00%	long-lived-> assume all is released
			ionization	30.00%	RILIS improved scheme x10
			transport	5.00%	
			post-acc	80.00%	
			Post-acc yield 210Pb [/muC]		
			2.07E+05		