Introduction to MAD-X

N. Fuster Martínez, IFIC (CSIC-UV) Material based on Guido Sterbini, Öznur Mete and Bruce Yee courses 16th of January 2023

GOAL

The goal of this introduction to MAD-X lecture and workshop is to **complement** with "hands-on" numerical exercises the **lectures on Transverse Beam Dynamics** using the beam optics code **MAD-X**. We will focus on **magnet lattice design** and as a consequence you will be exposed to the **transverse beam dynamics concepts** from a new perspective.

DISCLAIMER

□ This material is intended to be a very brief introduction to MAD-X: a large part of the code capabilities are not discussed in detail or are not discussed at all!

□ If you want to deepen into the subject you can find a lot of material in:

✓ The official MAD-X web site: <u>http://mad.web.cern.ch/mad/</u>



MAD-X workshop overview

50 minutes lecture (now!)

First "hands-on" session (3h) (today in the afternoon).
 Tutorial 1: My first accelerator, a FODO cell.
 Tutorial 2: My first matching.
 BREAK (30 minutes)
 Tutorial 3: Building a circular machine.

Second "hands-on" session (3h) (tomorrow in the afternoon).

✓ Tutorial 4: Natural chromaticity.

Tutorial 5: Chromaticity correction and non-linearities.
 BREAK (30 minutes)

✓ Tutorial 6: Building a transfer line.

Tutors: Nuria Fuster-Martínez, Guido Sterbini, Axel Poyet, Davide Gamba.



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L_{cell}

Outline

□ Introduction. *Description of basic concepts*.

□ MAD-X language. Syntax, variables.

□ MAD-X commands. *Magnets, sequence and beam definition*.

Advanced MAD-X commands. *Twiss, matching and tracking.*

Example case. A FODO cell.

□ How to run MAD-X. Interactive mode, batch mode and python interface.

Introduction

General purpose of a beam optics code.

□ What is MAD-X?

Do we use MAD-X for everything? No!

U Why MAD-X?

How does it work?

□ Source code: the basic components.

General purpose of a beam optics code

Define the **lattice** of circular or linear accelerators.

- □ Compute **optics** parameters and **beam properties** along a given lattice.
- Design a lattice for getting the desired properties (matching).
- Simulate accelerator imperfections and design correction schemes.

□ Simulate **beam dynamics**: study single-particle motion.





Interaction Point 5

What is MAD-X?

MAD-X (Methodical accelerator Design).

A general purpose beam optics software.



□ Distributed for free by CERN and used since more than 25 years for machine design and simulations (PS, SPS, LHC, linacs...).

□ MAD-X is written in C/C++/fortran77/Fortran90 (source code is available under the CERN copyright).

Do we use MAD-X for everything? No!

We use MAD-X to:

Perform basic layout design and optimization.

Perform basic single-particle tracking and sensitivity analysis of beam lines, synchrotrons, storage rings....

We don't use MAD-X for:

□ Multi-particle and multi-bunch simulations.

- Simulations requiring non static Machine, i.e., beam changes its own environment (space charge, instabilities, beam-beam effects).
 - \checkmark Often the programs used for these kind of studies use inputs from MAD-X.





□ Multipurpose from early to final stages of design studies.

Why MAD-X?

□ **Multiplatform** (Linux, OSX, WINDOWS).

□ Source is **free** and very **flexible** and possible to extend.

Developed for complicated applications, powerful and rather complete.

□ Mainly designed for large projects (LEP, LHC, CLIC, ILC...) with $\ge 10^4$ elements.



Point 4

Radio frequency acceleration syster Point 5

CMS



Point 6 Beam dump

> UJ 68 UD 68

> > UP 68

RR 73

Point 7

Cleanina

Existing work

Point 8

LHC-B

How does it work?



□ What is the source code? Via text.

✓ It can be used in an **interactive way** (input from command line) or in **batch** (input from a file).

□ MAD-X has its own scripting language, which is used to interface with the software.

- ✓ Strong resemblance to "C" language (but NO need for declaration and NOT case sensitive).
- ✓ Many features of programming language (loops, if, macros...).

Source code: the basic components

Description of the machine

✓ Accelerator elements, physical attributes and location....

What is the machine in question?

Description of the beam

✓ Type of particle, energy...

What will be running in the machine?

Actions

✓ Optics calculation, matching, tracking....

What do you want to study about the machine?







Courtesy of W. Hillert

MAD-X language

Language features.

Conventions.

Optic variables.

Language features

□ All the sentence end with **semicolon ";"**.

□ Arithmetic expressions, including basic functions (exp, log, sin...), built-in random number generators and predefined constants (c, e, π , m_e , m_p ...).

Assignments:

- ✓ Regular (=). **a=b**, if **b** changes **a** does not.
- ✓ Deferred (:=). **a:=b**, if **b** changes **a** is updated too.

□ Variables can be used in **expressions**:

- ✓ NBEND = 40;
- ✓ ANGLE=2*PI/NBEND;

Comments:

 \checkmark Start with two slashes (//) or an exclamation mark (!) for single lines.

 \checkmark Are enclosed by (/*) and (*/) for multiple lines.

Deferred expressions Important for the variables you may need to change along the code (e.g. matching parameters...)!

Conventions

Units: all parameters are in terms of **SI** units, except the **energy**, expressed in **GeV**.

□ Horizontal plane is assumed to be the **bending plane**.

Elements are placed along the reference orbit moving along s.

- \checkmark x = y = 0 in a curvilinear system.
- ✓ The reference orbit is the path of a charge particle having the central momentum of the accelerator though idealised and perfectly aligned magnets.



Optics variables

Coordinates in MAD-X	Description
х, у	Horizontal and vertical positions in [m] referred to the reference orbit.
рх, ру	Horizontal and vertical canonical momenta of the closed orbit $p_{\rm x}$ and $p_{\rm y}$ divided by the reference momentum.
S	Arc length s along the reference orbit in [m].
deltap	Momentum deviation from the design momentum deltap= $\Delta p/p_0$. This quantity is used to normalize the elements strength.

Optical functions in MAD-X	Description
betx, bety	Horizontal and vertical beta functions in units of [m].
alfx, alfy	Horizontal and vertical alpha functions.
mux, muy	Horizontal and vertical phase advances [2 π].
dx, dy	Dispersion function in [m].

MAD-X commands

Generic pattern for MAD-X commands.

□ Definition of lattice elements. ✓ The strength of the magnets.

The lattice sequence.

Basic MAD-X commands.

Generic pattern for MAD-X commands



Definition of lattice elements

Each machine element or group of elements must be defined by a command.



label<mark>: keyword, properties;</mark>

□ MAD-X keywords are used to define the type of element.

Elements can be: magnets, markers, RF cavities, collimators...

Examples:

- ✓ Dipole magnet:
- ✓ Quadrupole magnet:
- ✓ Sextupole magnet:
- ✓ Marker:

MBL: SBEND, L=10.0; MQ: QUADRUPOLE, L=3.3; MSF: SEXTUPOLE, L=1.0; MARKER1: MARKER;











The strength of the magnets

□ The name of the parameter that defines the **normalised magnetic strength** depends on the element:

✓ For a dipole magnet (horizontal bending) is: *angle* [rad]

MBL: SBEND, <u>ANGLE=0.05</u>, L=10.0;

✓ For a quadrupole magnet is :
$$k_1 = \frac{1}{B\rho} \frac{\partial B_y}{\partial x} [m^{-2}] \left(=\frac{1}{lf}\right)$$

MQ: QUADRUPOLE, K1=0.00156, L=3.3;

✓ For a sextupole magnet is:
$$k_2 = \frac{1}{B\rho} \frac{\partial^2 B_y}{\partial x^2} [m^{-3}]$$

ksf= 0.00015; <mark>MSF: SEXTUPOLE, K2=ksf, L=1.0;</mark>

✓ Octupoles, multiple magnet "thin" element...









The lattice sequence

- □ A lattice sequence is an ordered collection of machine elements defining the accelerator to be studied.
- □ The position of each element in the sequence can be defined with respect to the CENTRE, EXIT or ENTRY of the element, the start of the sequence or the position of another element.

Example:

#Element definition MQ: QUADRUPOLE, L=3.3, K1=0.005; # Sequence definition mycell: SEQUENCE, REFER=ENTRY, L=10; q1: MQ, at s=0; marker1: marker, at s=2.5; ENDSEQUENCE;



Basic MAD-X commands

Beam definition:

BEAM, PARTICLE=particle_type (proton, electron...), ENERGY=value ;

A sequence has to be activated in order to be usable for other operations with the USE command:

USE, SEQUENCE=name_sequence;

□ Call an external file:

CALL, FILE=name_file.madx;

□ Print a value in the terminal:

VALUE variable_name;

 \Box Production of graphical output (e.g. β -function)*:

PLOT, HAXIS=s, VAXIS=betx,bety, COLOUR=100, FILE="test";

* Note that the data has to be generated first using the advances commands such as TWISS or TRACK.

Advances MAD-X commands

TWISS*. Optics calculations.

□ MATCHING*. Optics optimization.

TRACKING*. Beam dynamics studies.

*These commands require a **beam** and an **active sequence**.



□ The TWISS command will compute the **linear lattice function** (optical functions and the CO) around the machine and optionally the chromatic functions.

□ It is a matrix code where first and second order matrices are used to get the optics.

For a periodic solution

TWISS, SEQUENCE=sequence_label, exit(by default), FILE="test.txt", table=TWISS (by default);

For an initial condition (IC) solution **TWISS, SEQUENCE=sequence_label, betx=1, alfx=0, bety=1, alfy=0;**

More attributes: DELTAP, CHROM...

After a successful TWISS run, MAD-X creates a table of summary parameters named 'SUMM' which includes tunes, chromaticity, etc. as well as a 'TWISS' table and ASCII file if requested with most of the computed parameters.

TWISS output

SUMM table.

- ✓ Length of the cell
- ✓ Tunes: q1, q2
- ✓ Chromaticity: dq1, dq2

✓ ...

Access the data: a=table(SUMM,dq1);

TWISS table. *a=table(TWISS,q1,betx);* ASCII file.

- \checkmark With most of the parameters computed by MAD-X.
- ✓ SELECT, flag=TWISS, column=name, keyword, s, betx, alfx, mux, bety, alfy, muy;

NAME	KEYWORD	S	BETX	ALFX	MUX	BETY	ALFY	MUY
%s	%s	%le	%le	%le	%le	%le	%le	%le
"MYCELL\$START"	"MARKER"	0	105.6855764	-2.259230089	0	21.7840267	0.4573523215	0
"Q1"	"QUADRUPOLE"	1	105.9701387	1.978472039	0.001493921339	21.7840267	-0.4573523215	0.00735746345
"DRIFT_0"	"DRIFT"	6	87.34479015	1.74659768	0.009769065687	27.74523085	-0.7348885096	0.03995368946
"B1"	"SBEND"	11	69.17896128	1.856667625	0.01997132749	36.48179689	-1.012424698	0.06507035749
"DRIFT_1"	"DRIFT"	16	52.21942634	1.535239362	0.0332266184	47.9937248	-1.289960886	0.08413368703
"B2"	"SBEND"	21	37.43543691	1.397224472	0.05118922695	62.2810146	-1.567497074	0.09870931652
"DRIFT_2"	"DRIFT"	35	13.77011836	0.2931554251	0.1569385083	117.0503512	-2.3445984	0.124924296
"Q2"	"QUADRUPOLE"	36	13.80615426	-0.3296705349	0.1685688634	117.0503512	2.3445984	0.126274979
"DRIFT_3"	"DRIFT"	41	19.11044739	-0.7311880903	0.2183687567	94.99204817	2.067062212	0.1338245632
"B3"	"SBEND"	46	27.82671663	-0.9977190119	0.2530083111	75.70910699	1.789526024	0.1432136723
"DRIFT_4"	"DRIFT"	51	39.59664721	-1.356267103	0.2770733231	59.20152769	1.511989836	0.1551111302
"B4"	"SBEND"	56	53.74757777	-1.450626954	0.294285777	45.46931027	1.234453648	0.1704728215
"DRIFT_5"	"DRIFT"	70	105.6855764	-2.259230089	0.3240223299	21.7840267	0.4573523215	0.2438418116
"MYCELL\$END"	"MARKER"	70	105.6855764	-2.259230089	0.3240223299	21.7840267	0.4573523215	0.2438418116

			++ table: summ
gammatr	alfa	orbit5	length
2.97009686	0.1133597226	—0	70
dxmax	betxmax	dq1	q1
18.28374049	105.9701387	-0.2894713472	0.3240223299
q2	xcorms	xcomax	dxrms
0.2438418116	Ø	Ø	14.1747586
dyrms	dymax	betymax	dq2
Ø	Ø	117.0503512	-0.2895087383
synch_1	deltap	ycorms	ycomax
0	Ø	0	Ø
synch_5	synch_4	synch_3	synch_2
Ø	0	0	0
	nflips	synch_8	synch_6
	0	0	Ø

TWISS plot

 \Box Production of graphical output of the main optical functions (e.g. β -function):

PLOT, HAXIS=s, VAXIS=betx,bety, COLOUR=100, FILE="test";



Global matching

□ It is possible to modify the optical parameters of a lattice using the MATCHING module.

□ Adjusting the magnetic strengths to get the desired **global properties.**

 ✓ Examples for global parameters: Q1 and Q2 (horizontal and vertical tunes) and dQ1 and dQ2 (horizontal and vertical chromaticity).

Example

ENDMATCH:

MATCH, SEQUENCE=sequence_name;

GLOBAL, Q1=26.58; H-tune GLOBAL, Q2=26.62; V-tune

VARY, NAME=kqf, STEP=0.00001; VARY, NAME=kqd, STEP=0.00001;

LMDIF, CALLS=50, TOLERANCES=1e-6;

What we want! What we change!

Methods for the minimization. LMDIF accepts two attributes: CALLS, maximum number of calls to the penalty function; TOLERANCES, the desired tolerance for the minimum. http://mad.web.cern.ch/mad/rele ases/5.02.08/madxuguide.pdf

Other types of matching

Local matching and **performance matching**:

✓ Local optical functions (insertions, local optics changes).

✓ Any user defined variable.

Example:

MATCH, SEQUENCE=sequence_name;

CONSTRAIN, range=#s/#e, BETX=50; CONSTRAIN, range=#s/#e, ALFX=-2;

VARY, NAME=kqf, STEP=0.00001; VARY, NAME=kqd, STEP=0.00001;

LMDIF, CALLS=50, TOLERANCES=1e-6;

ENDMATCH;







The TRACK module allows us to perform single particle tracking for given initial conditions.
 It is based on building transfer maps by solving the Hamiltonian equations of each element.

Example

SELECT, FLAG=makethin, SLICE=1; MAKETHIN, SEQUENCE=seq_name;

TRACK, dump, file="name", DELTAP=0.01;

Convert the thick lattice to a thin lens one!

Off-momentum!

Number of turns!

START, x=1e-3, px=0, y=1e-3, py=0; START, x=1e-2, px=0, y=1e-3, py=0;

run, turns=100;

Particles initial conditions!

Output: '*TRACK'* table, file.txt



PLOT, file="track1",table=track, haxis=x, vaxis=px, colour=100;

Example case

What is the machine in question?



What will be running in the machine?

What do you want to study about the machine?

	<pre>! ************************************</pre>
	<pre>! ************************************</pre>
MAD-X .	<pre>plot, haxis=s, vaxis=betx,bety,dx,colour=100,file=MyfirstF0D0;</pre>

How to run MAD-X

□ Interactive mode.

Batch mode.

D Python interface.

How to run MAD-X: interactive mode

□ You download the last release from the repository and follow the instruction in: <u>http://madx.web.cern.ch/madx/</u>

□ In Windows, run the executable.

□ In Linux (OXS), execute ./madx in the containing directory.





How to run MAD-X: batch mode

myfile.madx

□ After writing your script in a separate file *myfile.madx*, you can call it in Windows after opening MAD-X:

madx

X: ==> call, file=myfile.madx;

□ In Linux, you can also type in the terminal:

./madx myfile.madx

```
Definition of parameters
l_cell=100;
quadrupoleLenght=5;
f=200:
myK:=1/f/guadrupoleLenght;// m^-2
****
Definition of magnets
QF: guadrupole, L=guadrupoleLenght, K1:=myK;
QD: quadrupole, L=quadrupoleLenght, K1:=-myK;
Definition of sequence
myCell:sequence, refer=entry, L=L CELL;
quadrupole1: QF, at=0;
marker1: marker, at=25;
quadrupole2: QD, at=50;
endsequence;
Definition of beam
*****
beam, particle=proton, energy=2;
Use of the sequence
use, sequence=myCell;
! TWISS
title, 'My first twiss';
twiss, file=MyfirstFOD0.madx;
plot, haxis=s, vaxis=betx,bety,dx,colour=100, title="test",file=MyfirstFODO;
```

How to run MAD-X: python interface I

During the workshop we will use MAD-X trough a python jupyter interface based on the python scripting language.



Why?

□ MAD-X has no graphical interface and for detailed processing of MAD-X results, other programming languages are often used.

Python is widely used in the physics community and provides powerful numerical and plotting libraries.

□ Jupyter is web application that allows to create and share live code.

How to run MAD-X: python interface II



*It is a binding to <u>MAD-X</u> for giving full control and access to a MAD-X interpreter in python. <u>http://hibtc.github.io/cpymad/getting-started</u>

mad@cern.ch, http://cern.ch/mad date: 2021.05.03 date: 2021.12.20 16:04:22

How to run MAD-X: python interface III



How to run MAD-X: python interface IV

□ We provided you with the instructions to **set-up the working environment**:

https://fusterma.github.io/JUAS2023/

JUAS2023

I hope you have been successful installing and testing the environment!

MAD-X workshop JUAS2023

N. Fuster-Martínez, D. Gamba, A. Poyet, G. Sterbini

For the MAD-X workshop at JUAS 2023 we will be using the MAD-X accelerator design software, together with Python as scripting language and Jupyter as interface for the analysis.

In order to be ready for the workshop please follow the instructions before coming to JUAS to prepare yourself and your laptop for the course.

For the workshop we will ask you to download the last version of the MAD-X Workshop JUAS2023 repository. In this repository you will find one folder for each tutorial with the corresponding jupyter-notebook and MAD-X input files to be completed during the workshop as well as the corresponding solutions. The tutorials statements can be found here.

Once the environment is set-up you can download the last version of the "MAD-X Workshop JUAS2023 repository", and open a JupyterLab interface and start working on the tutorials!

How to run MAD-X: python interface V

□ If you had problems with the environment set-up:

✓ You can work using the SWAN CERN service using the CERN computing account.

SWAN CERN service:

- ✓ <u>https://swan.cern.ch</u>
- ✓ Log-in with your credentials
- ✓ Create a new project, "JUAS 2023"
- ✓ Load the folders and files in the "MAD-X Workshop JUAS2023 repository" into the new project.
- ✓ Open the first tutorial jupyternotebook "Tutorial1.ipynb".

a	Projects	Share	CERNBox		>_	. 🎦 ? 🚥 🖨
SWAN > My Projects > JUAS2023 > Tutorial1						
Tutorial1 🗠						
NAME -				SIZE	STATUS	MODIFIED
😂 Tutorial1.ipynb				122 kB		31 minutes ago
Tutorial1_solutions.ipynb				374 kB		22 minutes ago
G FODO.png				40.7 kB		33 minutes ago
myfirstfodo.txt				60.1 kB		24 minutes ago
Tutorial1.madx				1.22 kB		34 minutes ago
Tutorial1_solution.madx				825 B		33 minutes ago
Tutorial1_solution_adding_markers.madx				1.72 kB		33 minutes ago
i withmarkers.txt				65.4 kB		24 minutes ago

Thank you very much for your attention!

Questions?

Let's finish with a quick quiz!



