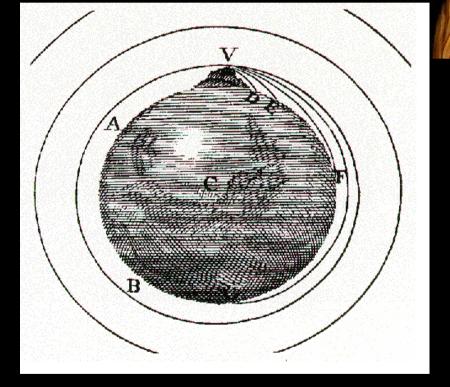
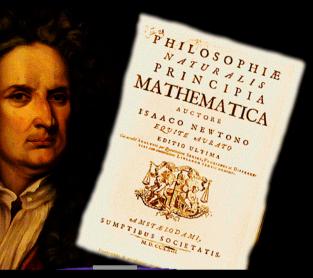
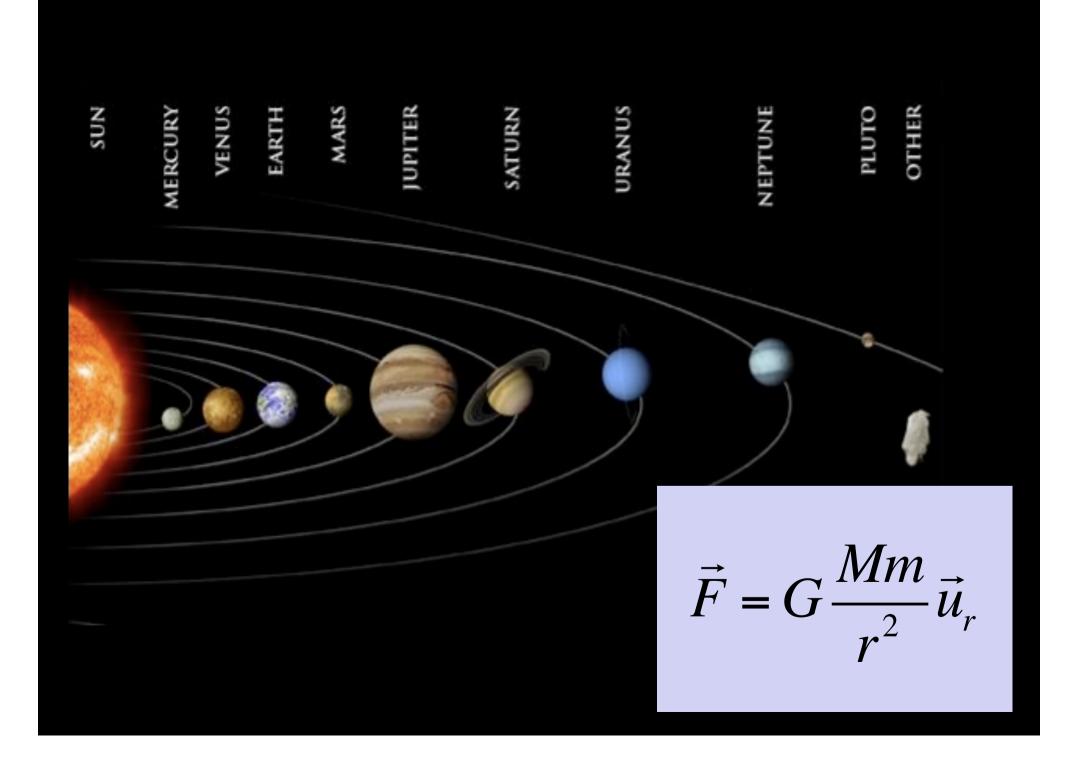
# Gravitational wave astronomy

Eugenio Coccia IFAE - Institute of High Energy Physics, Barcelona Gran Sasso Science Institute and INFN

# Newton







1) 
$$F = m_i a$$
  $F = G \frac{M m_g}{r^2}$ 

Experimental result:  $\frac{m_i}{m_g} = const = 1$ 

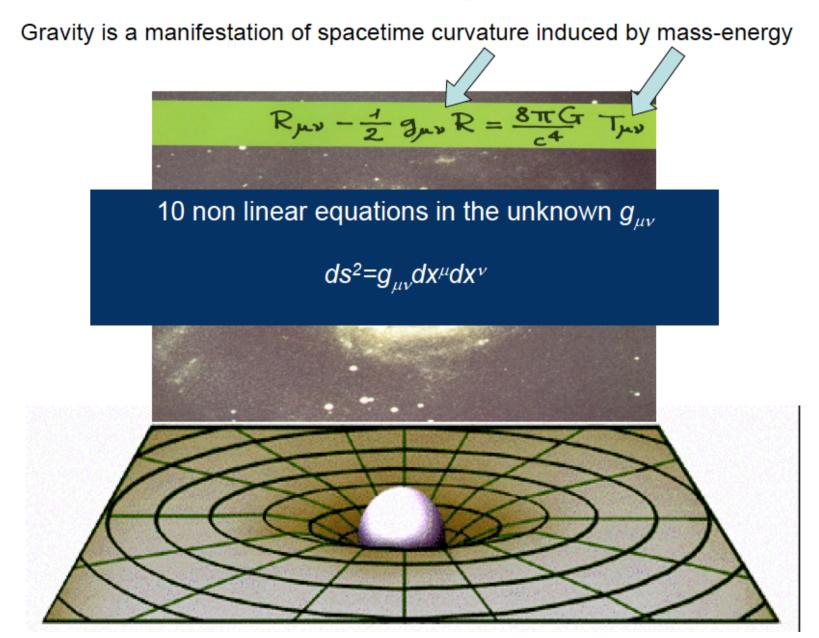
a coincidence?

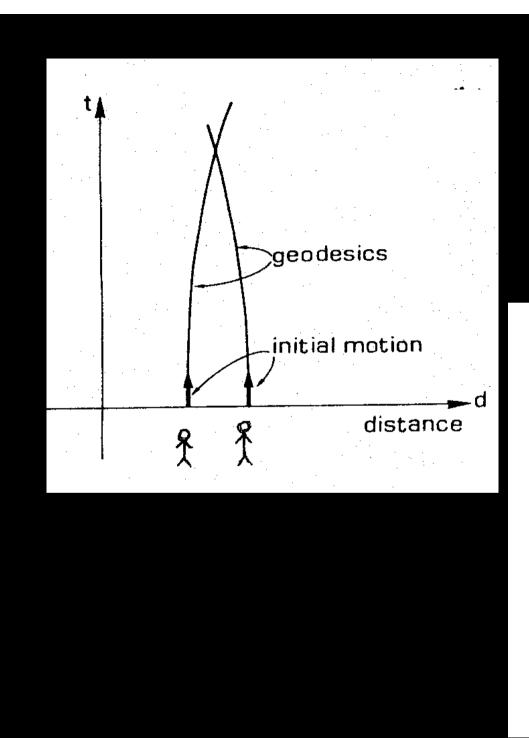
2) Newtonian gravity propagates with infinite speed!

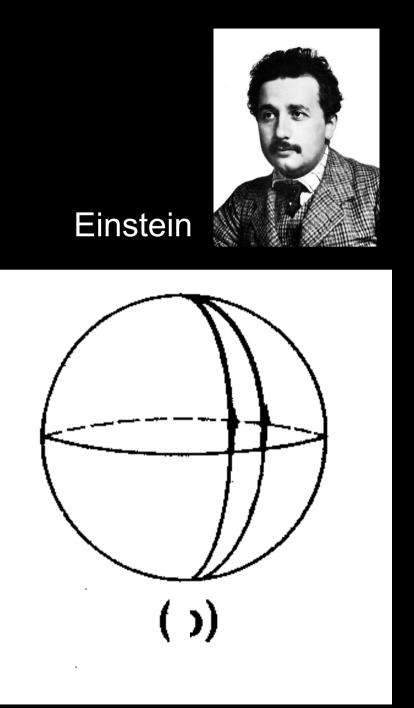


## Einstein

## General Relativity (1915)

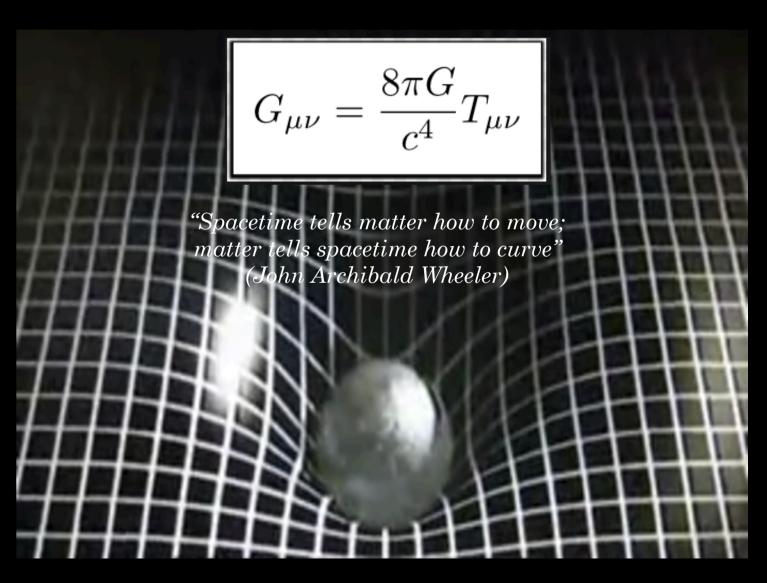


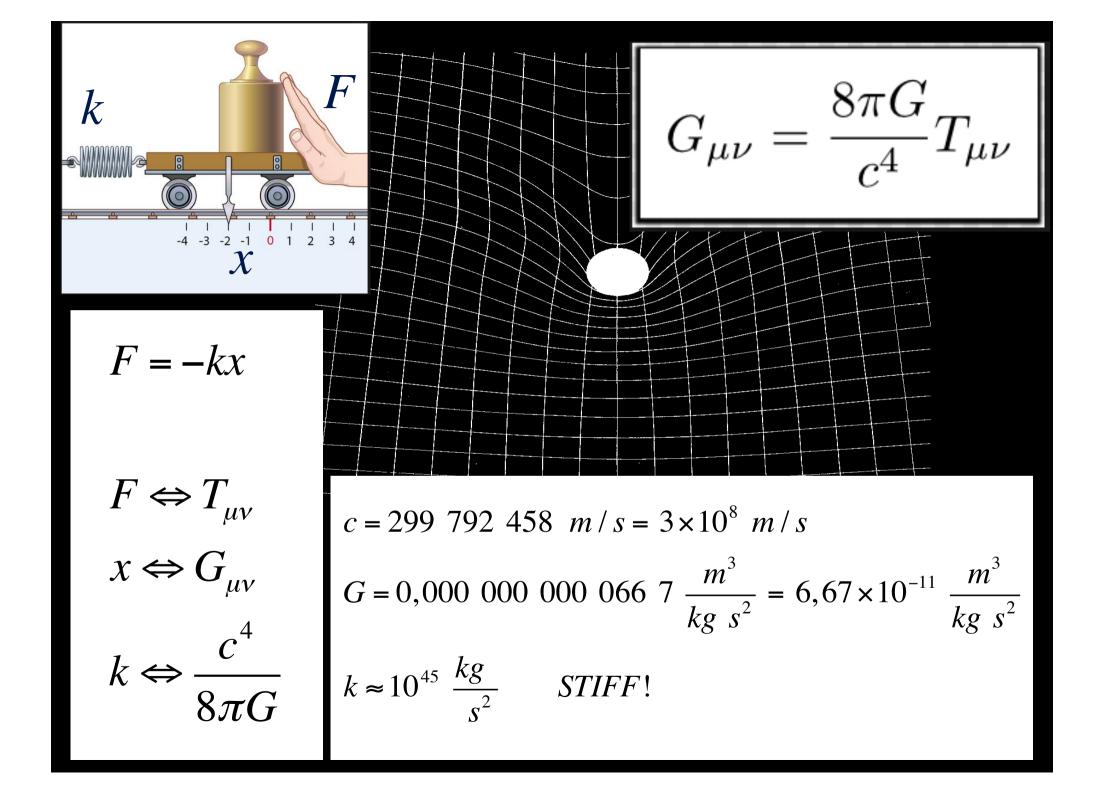




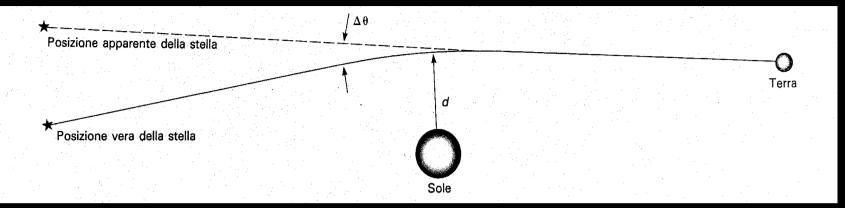
# Einstein's Theory of Gravitation

Gravity is a manifestation of spacetime curvature induced by mass-energy





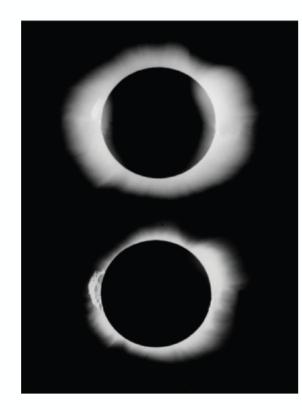
## Light deflection





Eddington

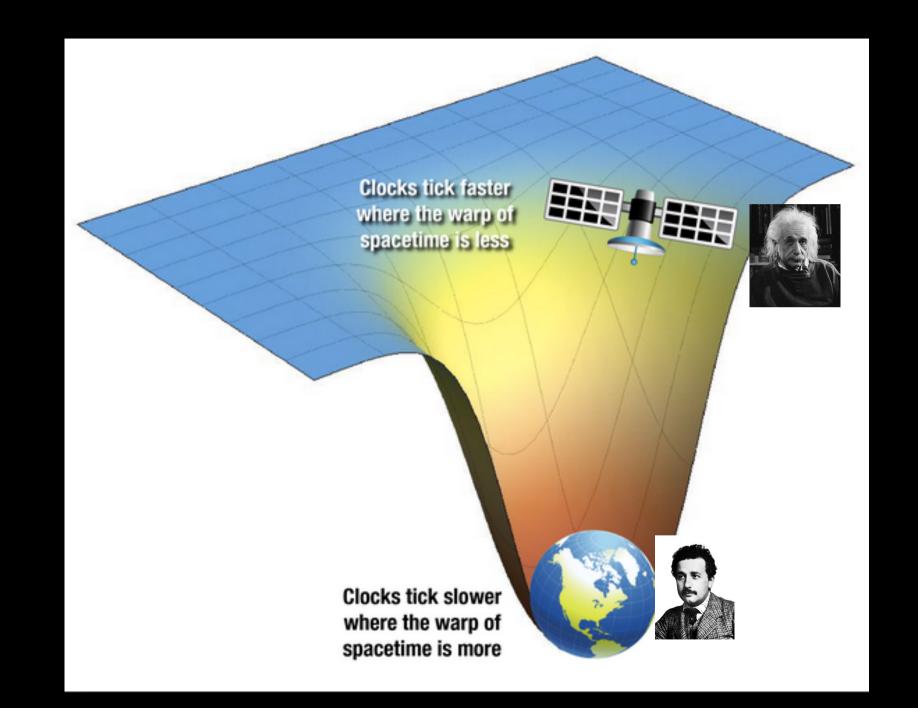




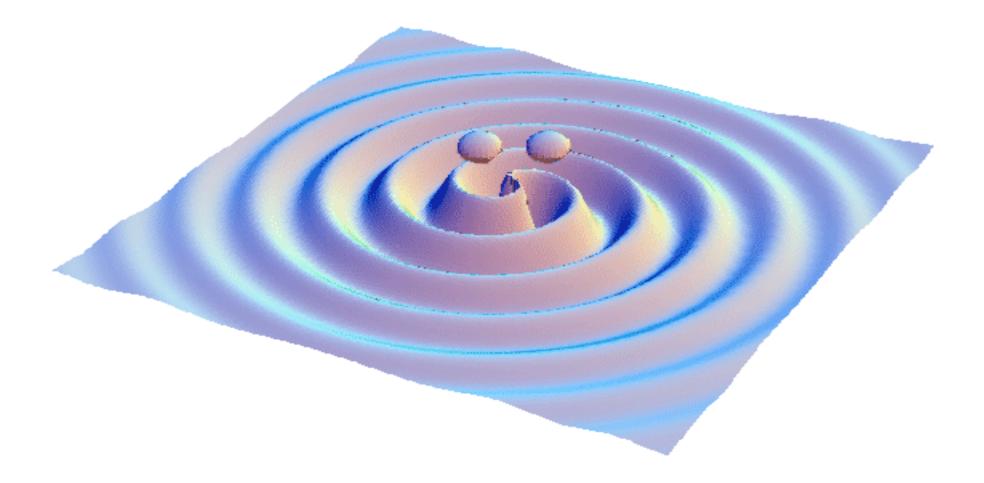


## Harvard

# Redshift Pound and Rebka 1959



# **Gravitational Waves**



## 1916

#### Über Gravitationswellen.

#### Von A. EINSTEIN.

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist sehon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden<sup>4</sup>. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.

Wie damals beschränke ich mich auch hier auf den Fall, daß las betrachtete zeiträumliche Kontinuum sich von einem »galileischen» nur sehr wenig unterscheidet. Um für alle Indizes

$$g_{\mu\nu} = -\delta_{\mu\nu} + \gamma_{\mu\nu} \tag{1}$$

setzen zu können, wählen wir, wie es in der speziellen Relativitätstheorie üblich ist, die Zeitvariable  $x_i$ rein imaginär, indem wir

$$x_4 = it$$

setzen, wobei t die "Lichtzeit" bedeutet. In (1) ist  $\delta_{\mu\nu} = 1$  bzw.  $\delta_{\mu\nu} = 0$ , je nachdem  $\mu = \nu$  oder  $\mu \neq \nu$  ist. Die  $\gamma_{\mu\nu}$  sind gegen 1 kleine Größen, welche die Abweichung des Kontinuums vom feldfreien darstellen; sie bilden einen Tensor vom zweiten Range gegenüber LORENTZ-Transformationen.

#### § 1. Lösung der Näherungsgleichungen des Gravitationsfeldes durch retardierte Potentiale.

Wir gehen aus von den für ein beliebiges Koordinatensystem gültigen<sup>2</sup> Feldgleichungen

$$-\sum_{\alpha} \frac{\partial}{\partial x_{\alpha}} { uv \atop \alpha} + \sum_{\alpha} \frac{\partial}{\partial x_{\nu}} { u\alpha \atop \alpha} + \sum_{\alpha,\beta} { \mu\alpha \atop \beta} { v\beta \atop \beta} { v\beta \atop \beta} - \sum_{\alpha,\beta} { uv \atop \alpha} { \alpha\beta \atop \beta} { \alpha\beta \atop \beta} = - \times \left( T_{uv} - \frac{1}{2} g_{uv} T \right) \cdot$$

$$(2)$$

<sup>1</sup> Diese Sitzungsber. 1916, S. 688ff.

 $^2$  Von der Einführung des \*<br/>2-Gliedes- (vgl. diese Sitzungsber. 1917. S. 142) ist dabei Abstand genommen.

Sitzungsberichte 1918.

(1)

La prima pagina di un lavoro di Albert Einstein del 1918 in cui per la prima volta vengono dedotte le equazioni della propagazione ondosa del campo gravitazionale.

#### Weak field approximation

$$g_{\mu\nu} = g^o_{\mu\nu} + h_{\mu\nu}$$
$$|h_{\mu\nu}| <<1$$

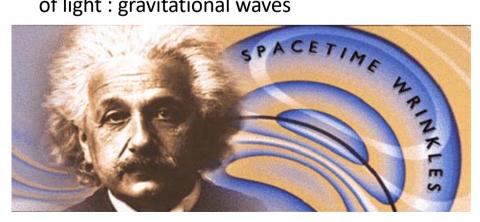
The Einstein equation in vacuum becomes

$$(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2})h_{\mu\nu} = 0$$

Having solutions

$$h_{\mu\nu}(t-x/c)$$

Spacetime perturbations, propagating in vacuum like waves, at the speed of light : gravitational waves



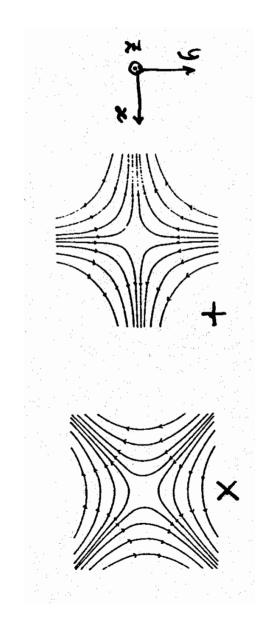
## Gravitational waves are strain in space propagating with the speed of light

## **Main features**

- 2 transversal polarization states
- Associated with massless, spin 2 particles (gravitons)
- Emitted by time-varying quadrupole mass moment no dipole radiation because of conservation laws

$$-\frac{dE}{dt} = \frac{2G}{3e^3} \left( \dot{\vec{d}} \right)^2 + \frac{G}{45c^5} \left( \ddot{Q} \right)^2 + \dots$$
$$\dot{d} = \sum_i m_i \dot{x}_i \Rightarrow \ddot{d} = 0 \qquad Q_{ij} = \int \rho x_i x_j d^3 x$$

$$h_{ij}(t) = \frac{2G}{rc^4} \ddot{Q}_{ij}(t - r/c)$$



### No laboratory equivalent of Hertz experiments for production of GWs

Luminosity due to a mass M and size R oscillating at frequency  $\omega \sim v/R$ :

$$L = \frac{2G}{5c^5} \left\langle \ddot{Q}^2 \right\rangle \approx \frac{GM^2 v^6}{R^2 c^5} \qquad Q \approx MR^2 \sin\omega t$$

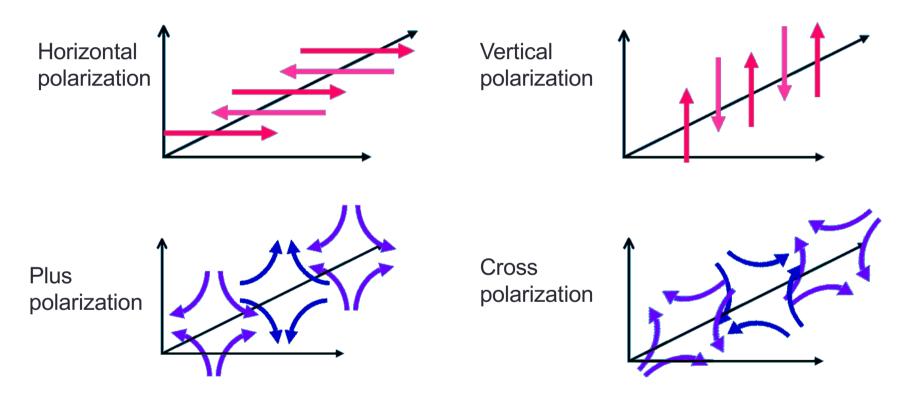
M=1000 tons, steel rotor, f = 4 Hz  $\implies$  L = 10<sup>-30</sup> W Einstein: "... a pratically vanishing value..."

Collapse to neutron star 1.4  $M_o \implies L = 10^{52} \text{ W}$ 

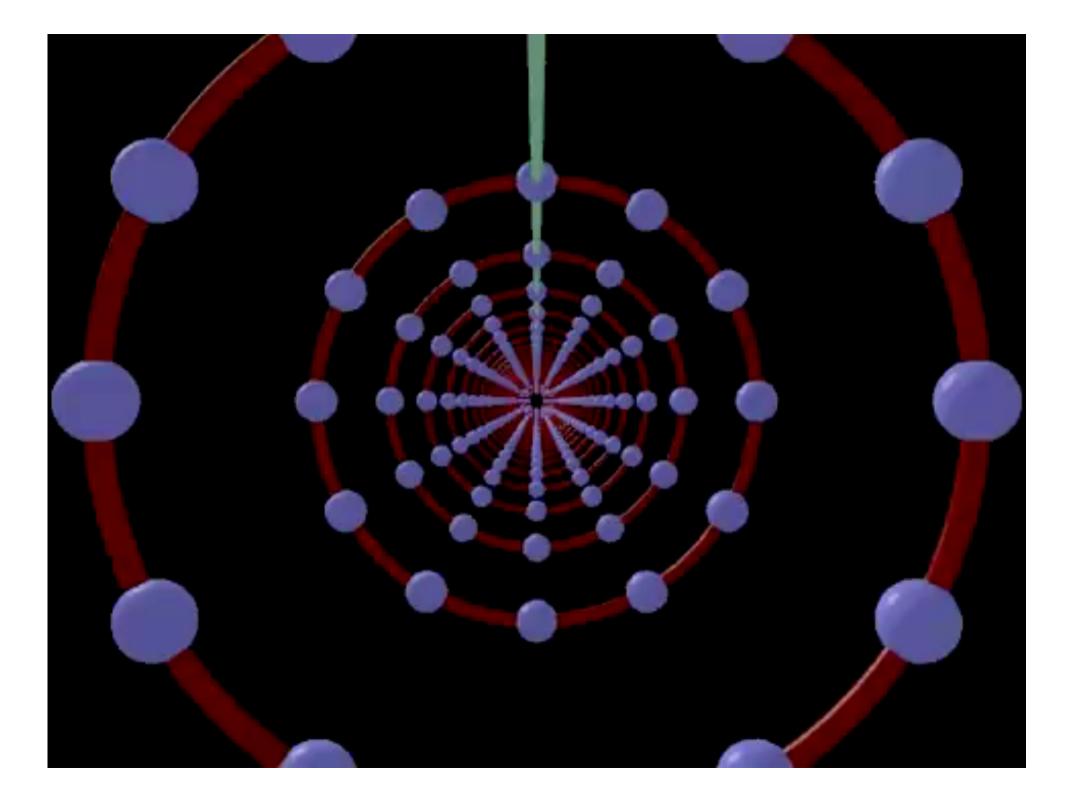
 $h \sim W^{1/2}d^{-1}$ ; source in the Galaxy  $h \sim 10^{-18}$ , in VIRGO cluster  $h \sim 10^{-21}$ Fairbank: "...a challenge for contemporary experimental physics.."

# **Gravitational Waves**

## Comparison with electromagnetic waves



The so-called "electromagnetic theory of light" has not helped us hitherto . . it seems to me that it is rather a backward step . . . the one thing about it that seems intelligible to me, I do not think is admissible . . That there should be an electric displacement perpendicular to the line of propagation? Lord Kelvin



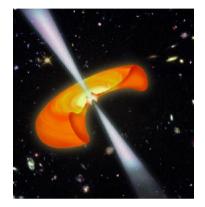
# **GW OBJECTIVES**

**FIRST DETECTION** test Einstein prediction

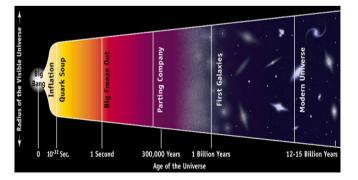
$$\mathbf{G} = \frac{8\pi G}{c^4} \mathbf{T}$$

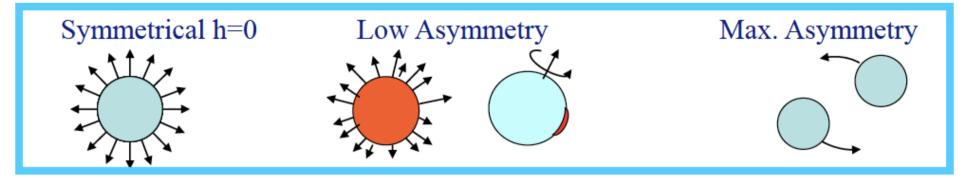
## **ASTRONOMY & ASTROPHYSICS**

look beyond the visible, understand Black Holes, Neutron Stars and supernovae understand GRB



**COSMOLOGY** the Planck time: look as back in time as theorist can conceive

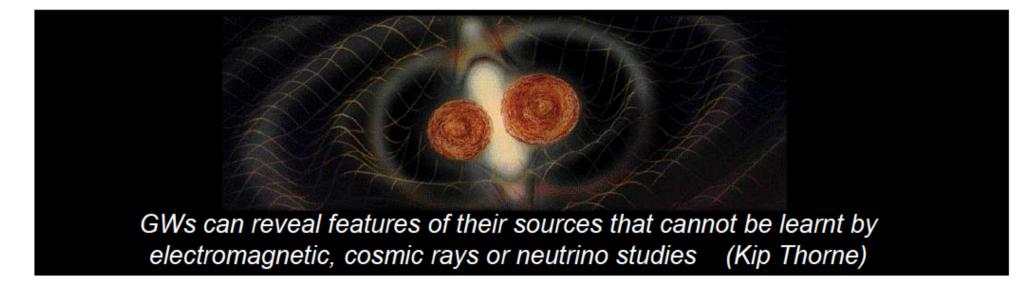


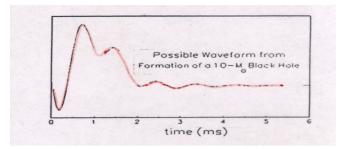


Observing gravitational radiation gives unique information complementary to those derived by em observations

- em radiation is the result of an incoherent combination of the radiation emitted by electrons, atoms and molecules ←→ gravitational radiation is the result of a coherent mass acceleration.

- em radiation interacts strongly with matter, and is absorbed significantly while travelling toward the detector ←→ gravitational radiation propagates "freely" and can bring us info from the innermost region of a star





Pulsar Waveform

### SUPERNOVAE.

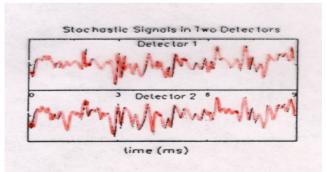
If the collapse core is non-symmetrical, the event can give off considerable radiation in a millisecond timescale.

### SPINNING NEUTRON STARS.

Pulsars are rapidly spinning neutron stars. If they have an irregular shape, they give off a signal at constant frequency (prec./Dpl.)

## Chirp Waveform from Two 10-M Block Holes 0.00 0.02 0.04 0.06 0.08 0.10 time (s)

time (s)



### COALESCING BINARIES.

Two compact objects (NS or BH) spiraling together from a binary orbit give a chirp signal, whose shape identifies the masses and the distance

### STOCHASTIC BACKGROUND.

Random background, relic of the early universe and depending on unknown particle physics. It will look like noise in any one detector, but two detectors will be correlated.

#### Information

Inner detailed dynamics of supernova See NS and BH being formed Nuclear physics at high density

#### Information

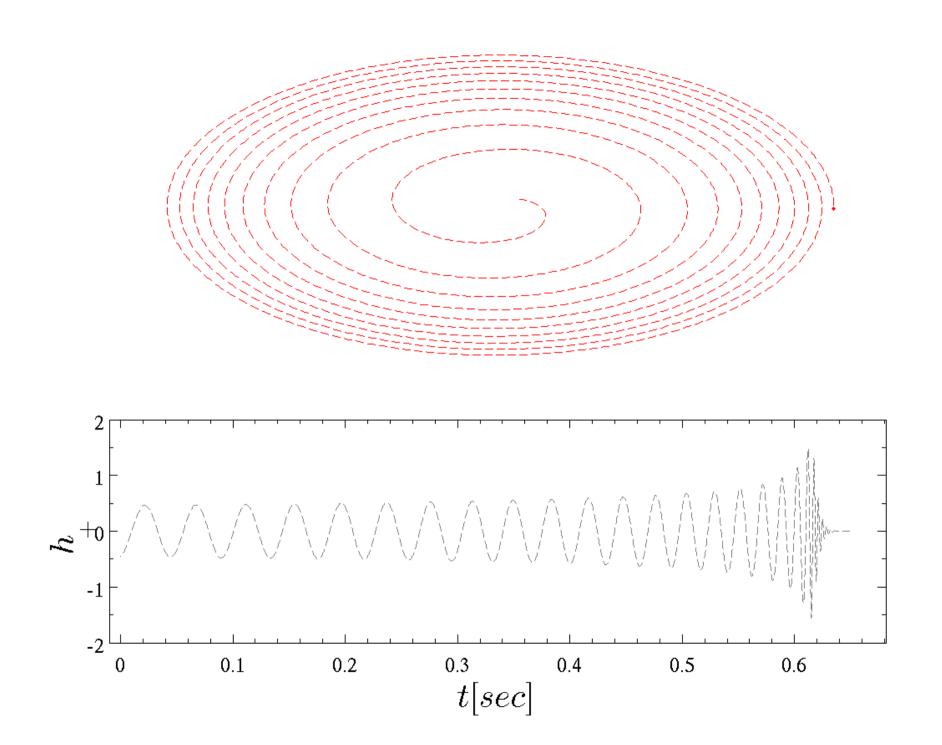
Neutron star locations near the Earth Neutron star Physics Pulsar evolution

#### Information

Masses of the objects BH identification Distance to the system Hubble constant Test of strong-field general relativity

#### Information

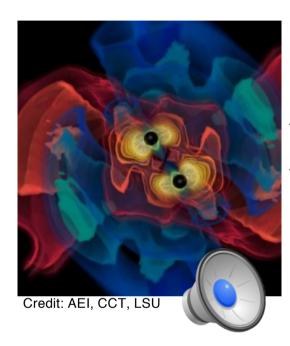
Confirmation of Big Bang, and inflation Unique probe to the Planck epoch Existence of cosmic strings





# Astrophysical sources of gravitational waves

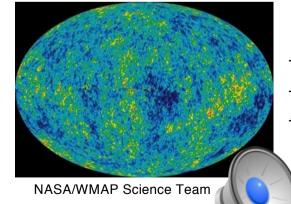




<u>Compact</u> <u>Binaries</u>

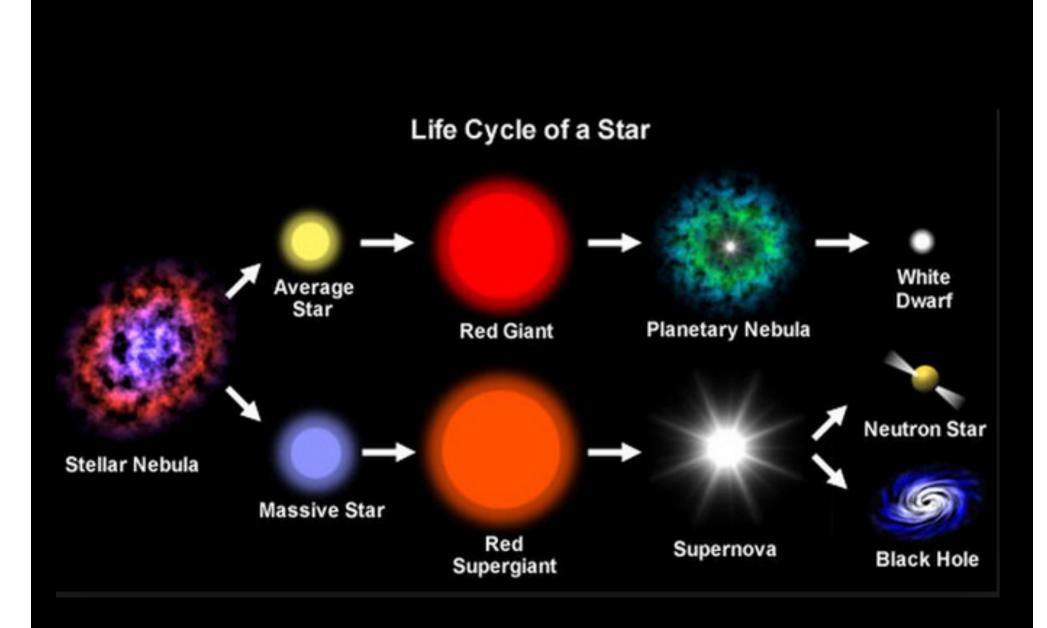
Credit: Chandra X-ray Observatory

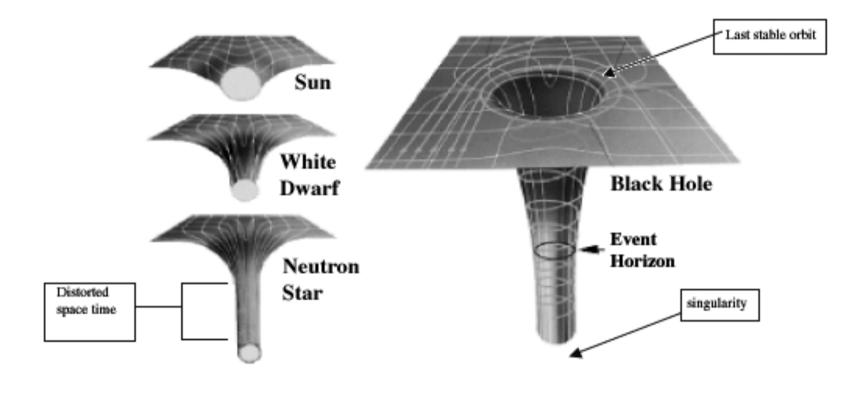
<u>Supernovae</u>

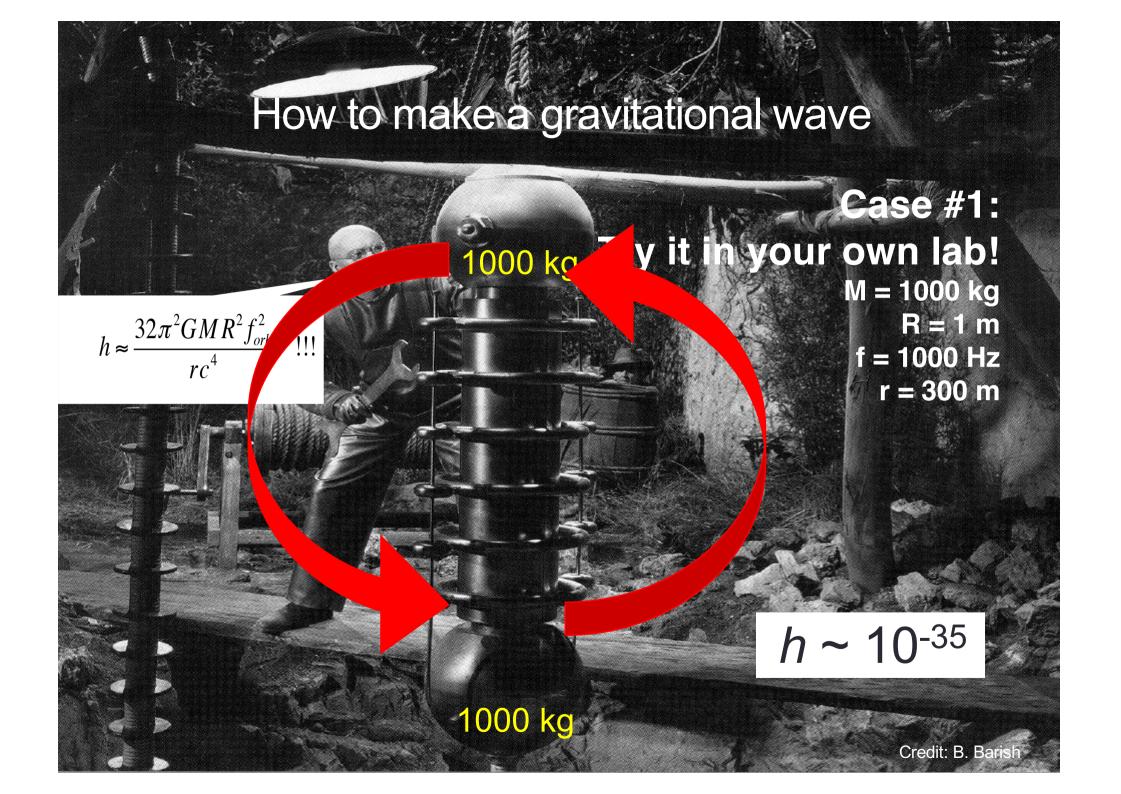


<u>Cosmic</u> <u>Gravitational-wave</u> <u>Background</u> Spinning neutron stars

Casey Reed, Penn State







$$A = \frac{\varkappa}{24\pi} \sum_{\alpha\beta} \left( \frac{\partial^3 J_{\alpha\beta}}{\partial t^3} \right)^2$$
(21)

Würde man die Zeit in Sekunden, die Energie in Erg messen, so würde zu diesem Ausdruck der Zahlenfaktor  $\frac{1}{c^4}$  hinzutreten. Berücksichtigt man außerdem, daß  $z = 1.87 \cdot 10^{-27}$ , so sieht man, daß A in allen nur denkbaren Fällen einen praktisch verschwindenden Wert haben muß.

> ".....in any case one can think of A will have a practically vanishing value."

# How to make a gravitational wave that might be detectable

Consider 1.4 solar mass binary neutron star pair

M = 1.4 M<sub>☉</sub> R = 20 km f = 400 Hz r = 5 10<sup>23</sup> m (15Mpc)

 $h \approx \frac{4\pi^2 GMR^2 f_{orb}^2}{c^4 r}$ 

 $h \sim 10^{-21}$ 

 $h = \frac{\Delta L}{L} = \frac{10^{-18}m}{10^3 m} = 10^{-21}$ 

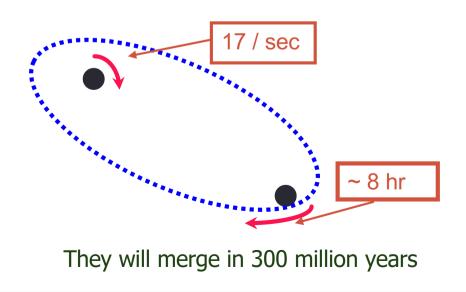




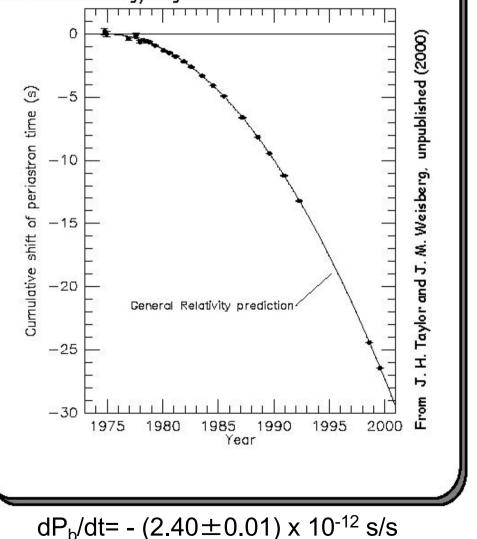




Joseph Taylor Russell Hulse



Comparison between observations of the binary pulsar PSR1913+16, and the prediction of general relativity based on loss of orbital energy via gravitational waves



## • GWs are detectable in principle

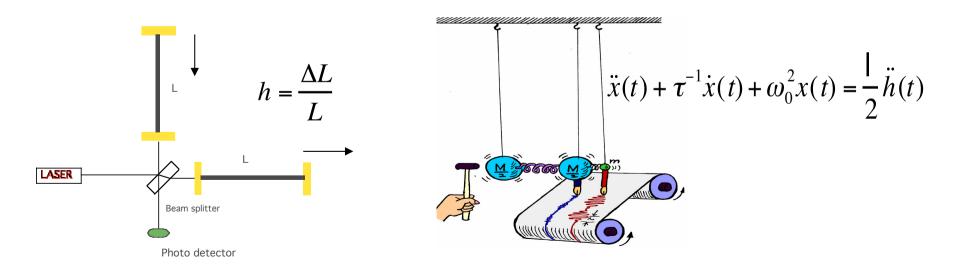
The equation for geodetic deviation is the basis for all experimental attempts to detect GWs:

$$\frac{d^2 \delta l^{j}}{dt^2} = -R_{joko} l^k = \frac{1}{2} \frac{\partial^2 h_{jk}}{\partial t^2} l^k$$

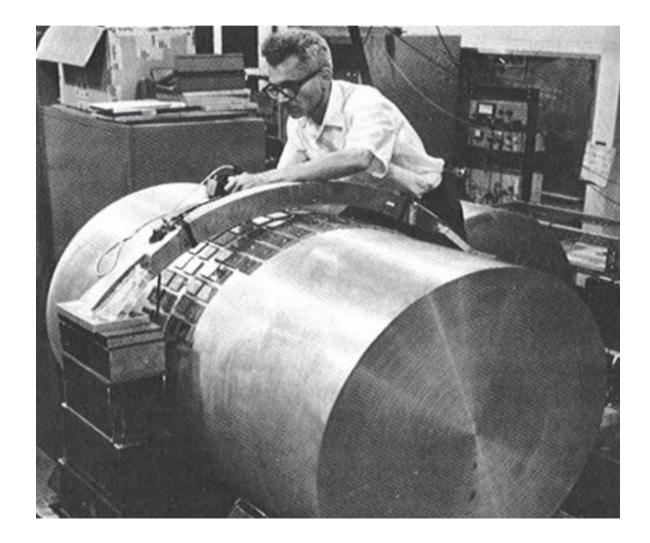
• GWs change ( $\delta$ I) the distance (I) between freely-moving particles in empty space.

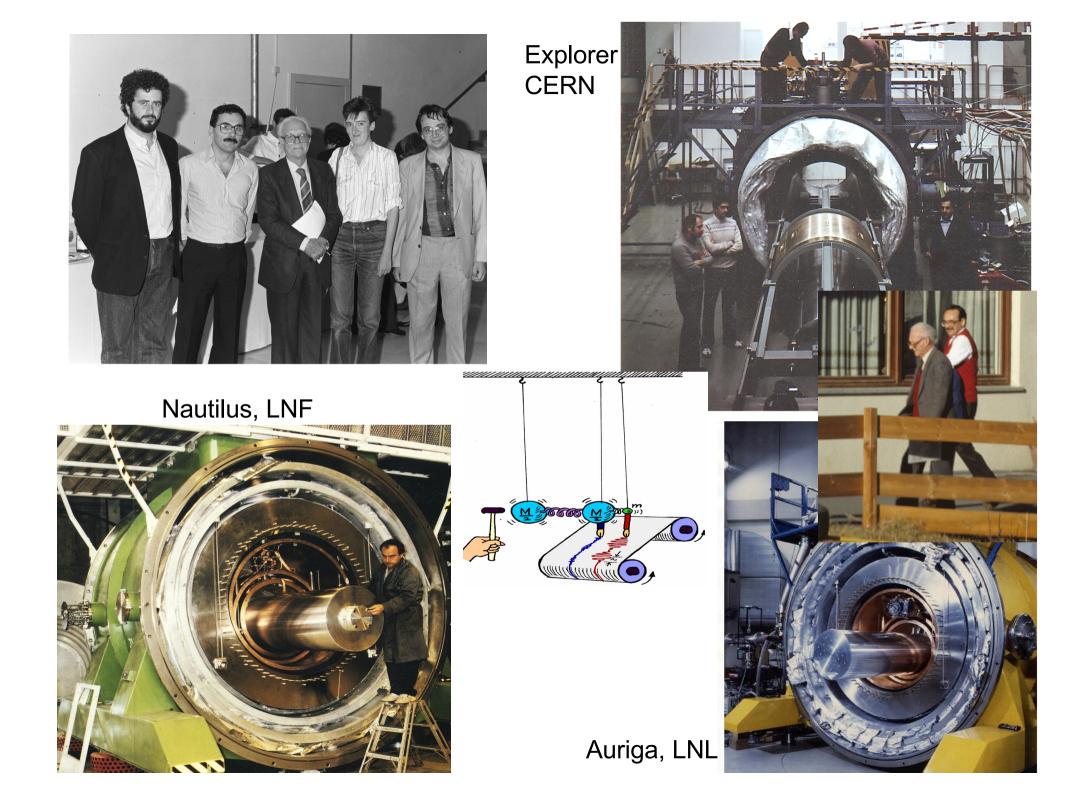
They change the proper time taken by light to pass to and fro fixed points in space

In a system of particles linked by non gravitational (ex.: elastic) forces, GWs perform work and deposit energy in the system



# Weber's bar





## Some perspective: 50 years of attempts at detection:



60': Joe Weber

pioneering work

Since the pioneering work of Joseph Weber in the '60, the search for Gravitational Waves has never stopped, with an increasing effort of manpower and ingenuity:



90': Cryogenic Bars

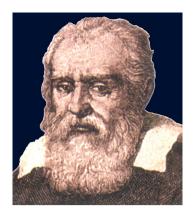




2000' - : Large Interferometers

1997: GWIC was formed

# 2nd lecture



Experimental gravitational physicists are heirs to several great traditions:

- High precision mechanical experiments (Cavendish, Eotvos, Dicke..) detection of weak forces applied on mechanical test bodies
- High precision optical measurements (Michelson, laser developers...)
- Operation of ultraprecise e-m measurement systems (microwave pioneers of World War II)
- Low temperature physics (K. Onnes) superfluids and superconductors technology

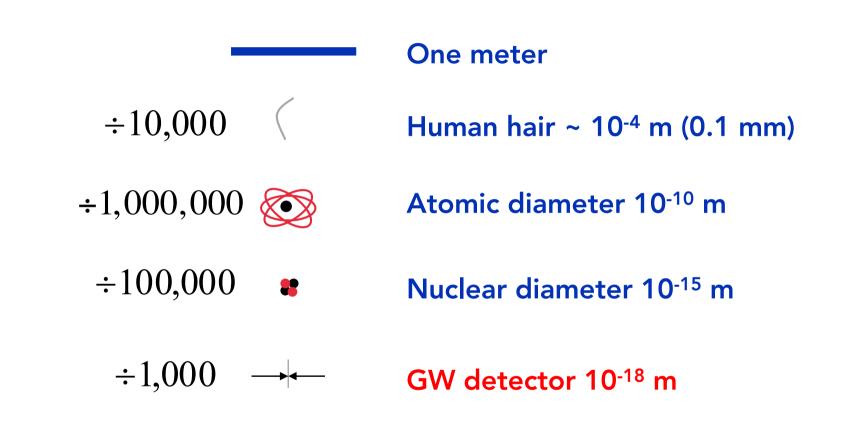


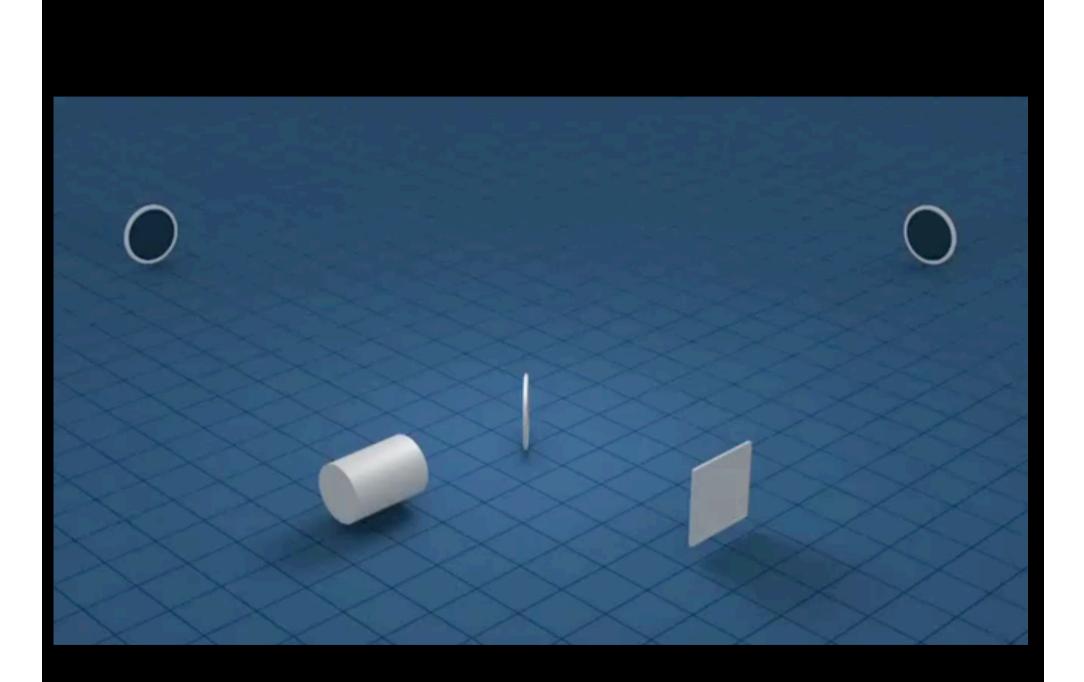




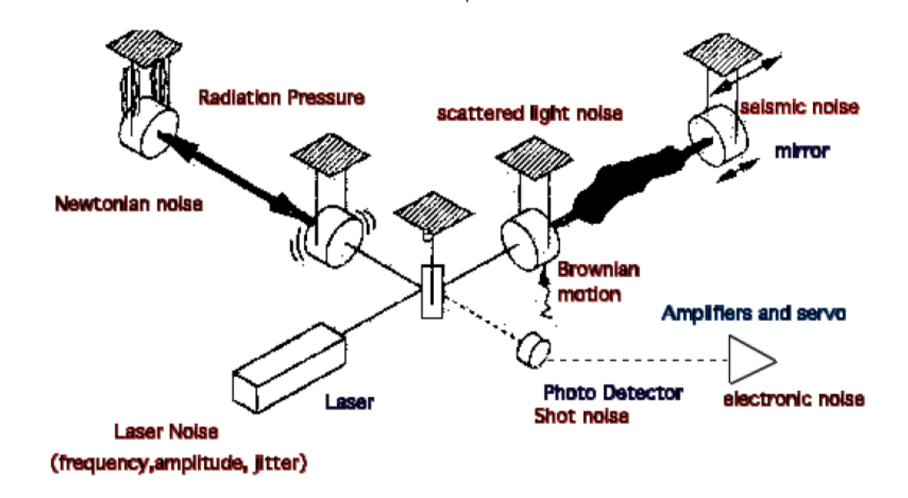


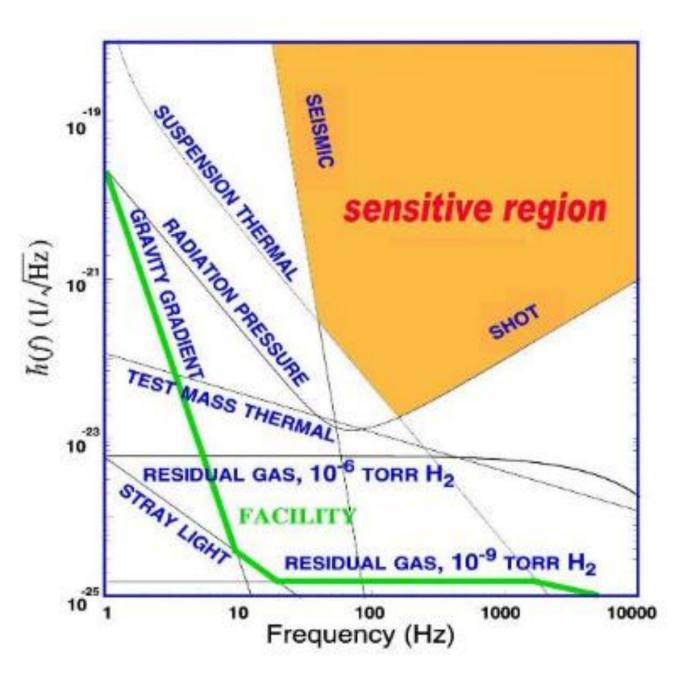
# How Small 10<sup>-18</sup> meter is?



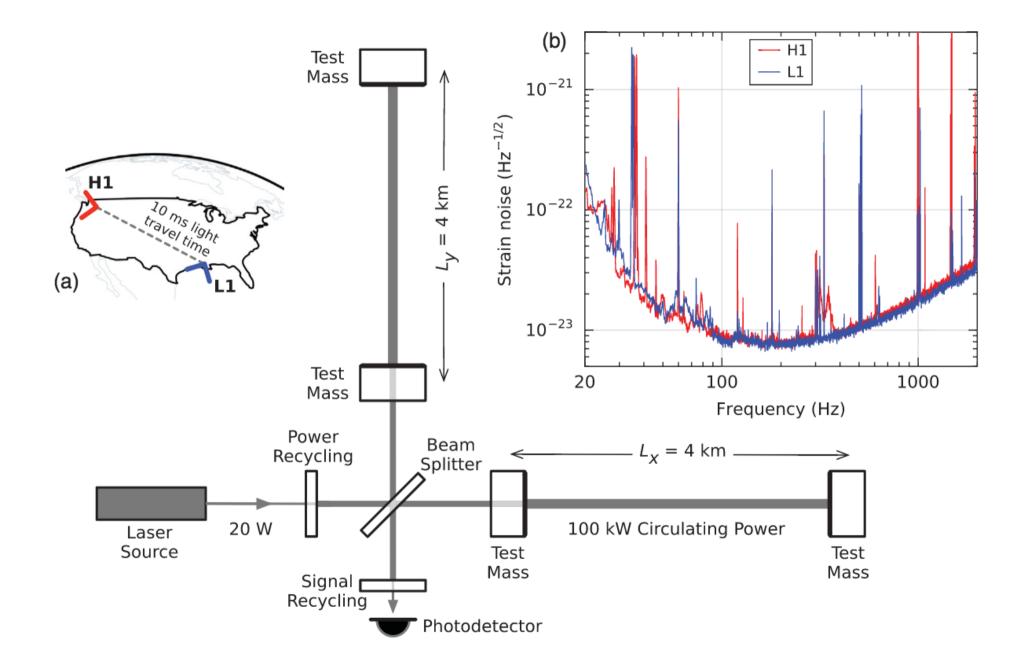


## Main noise sources in interferometric GW detectors





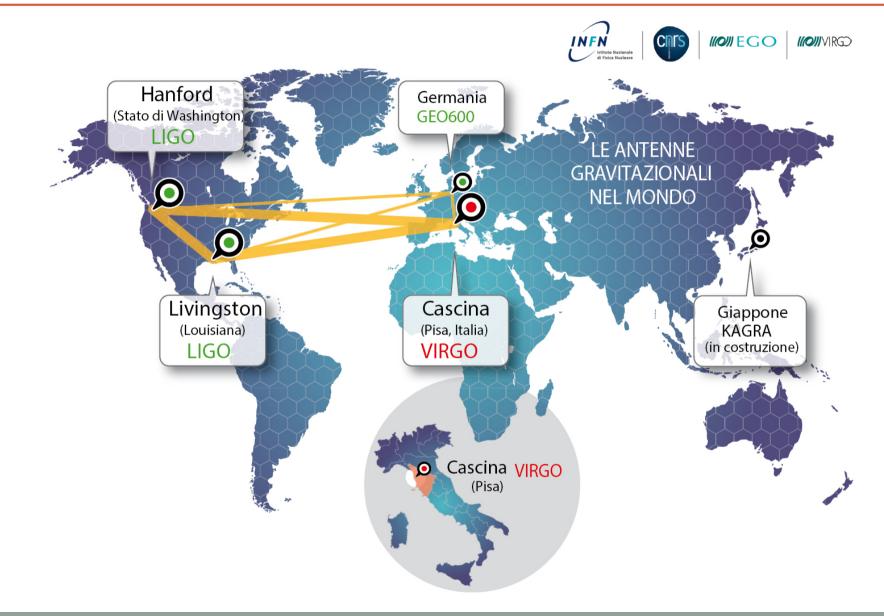
E. Coccia - 2016



## **Global Network of Detectors**

vanced Virgo





## LIGO Scientific Collaboration



www.ligo.org

900+ members, 80+ institutions, 16 countries



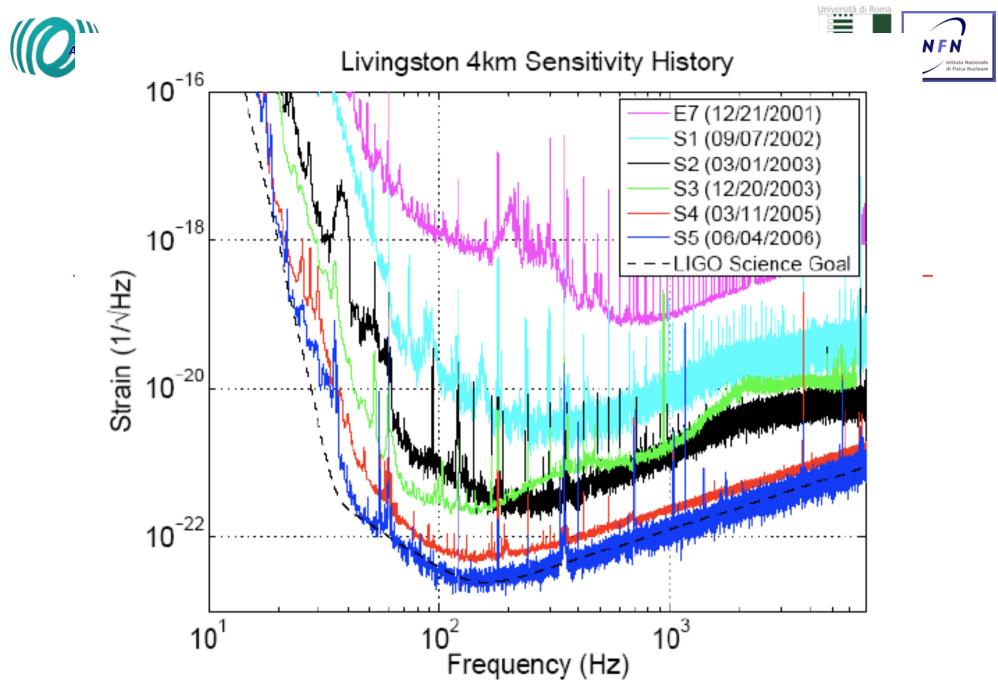
## Virgo Collaboration

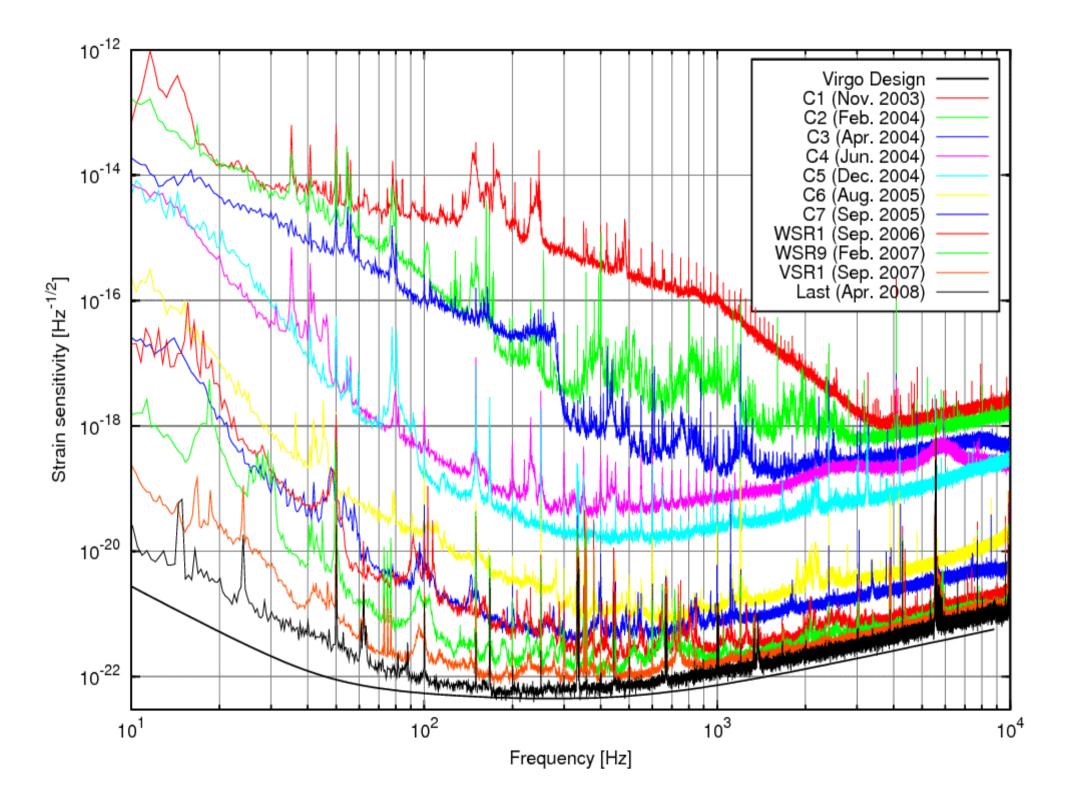


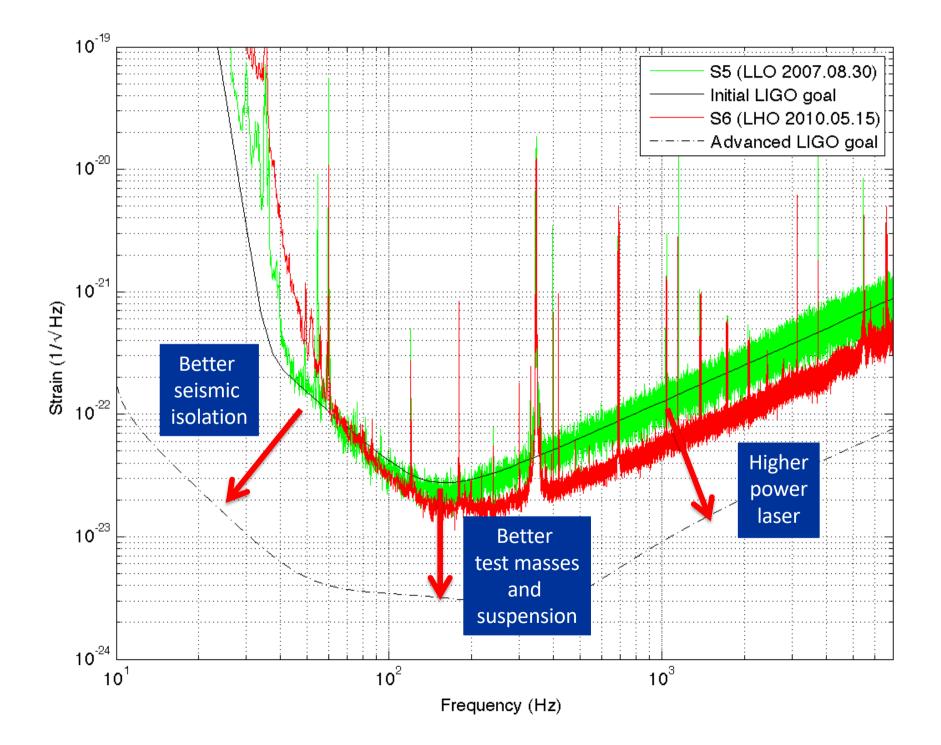
- 5 European countries, 19 labs, ~250 members
- Scientists from Italy and France (former founders of Virgo), The Netherlands, Poland and Hungary

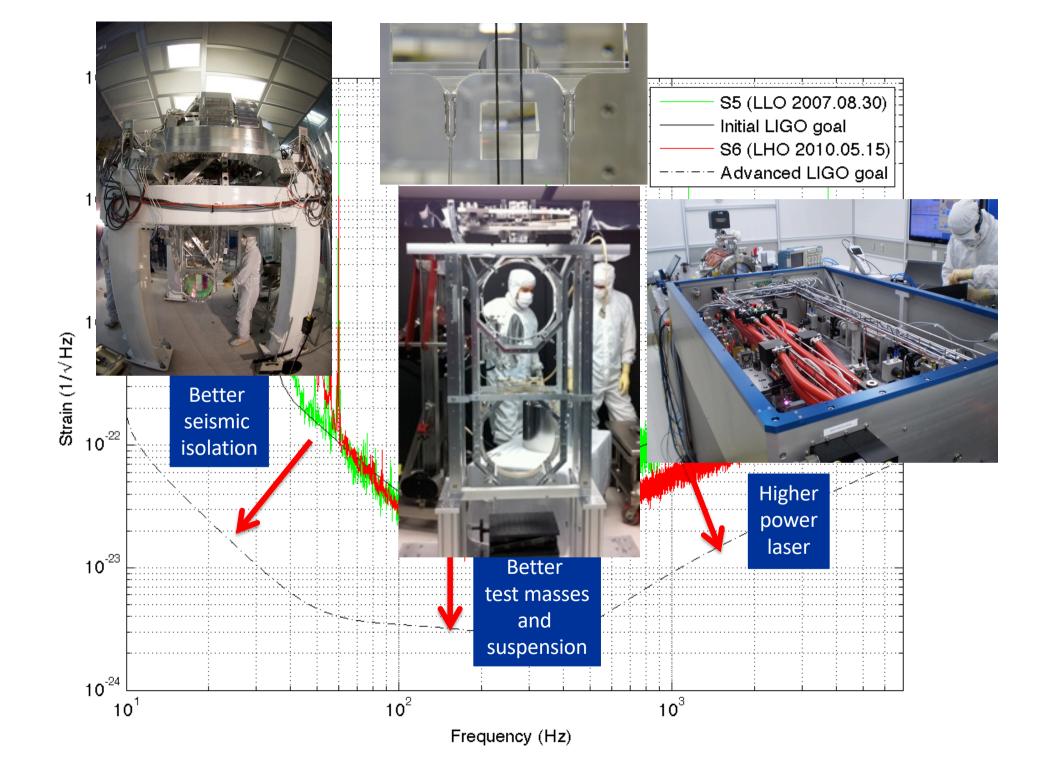


APC Paris ARTEMIS Nice EGO Cascina INFN Firenze-Urbino INFN Genova INFN Napoli **INFN** Perugia INFN Pisa INFN Roma La Sapienza INFN Roma Tor Vergata INFN Trento-Padova LAL Orsay - ESPCI Paris LAPP Annecy LKB Paris LMA Lyon NIKHEF Amsterdam POLGRAW(Poland) RADBOUD Uni. Nijmegen **RMKI Budapest** Gran Sasso Science Institute







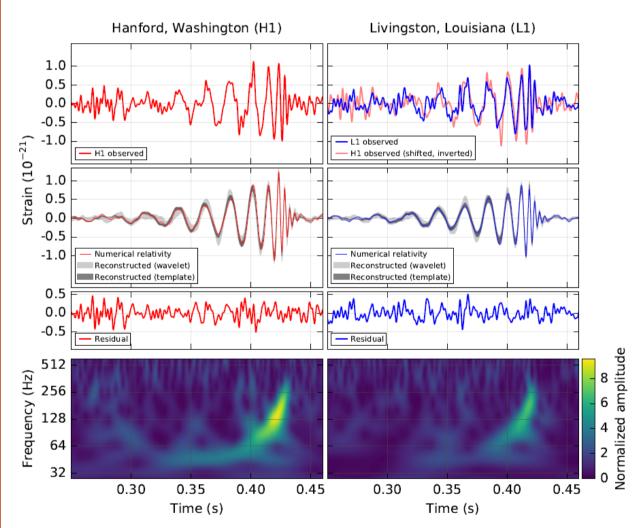






- Top row left Hanford
- Top row right Livingston
- Time difference ~ 6.9 ms with Livingston first
- Second row calculated GW strain using Numerical Relativity Waveforms for quoted parameters compared to reconstructed waveforms (Shaded)
- Third Row –residuals
- Bottom row time frequency plot showing frequency increases with time (chirp)

September 14<sup>th</sup>, 2015 at 09:50:45 UTC



# GW150914: Estimated Strain Amplitude

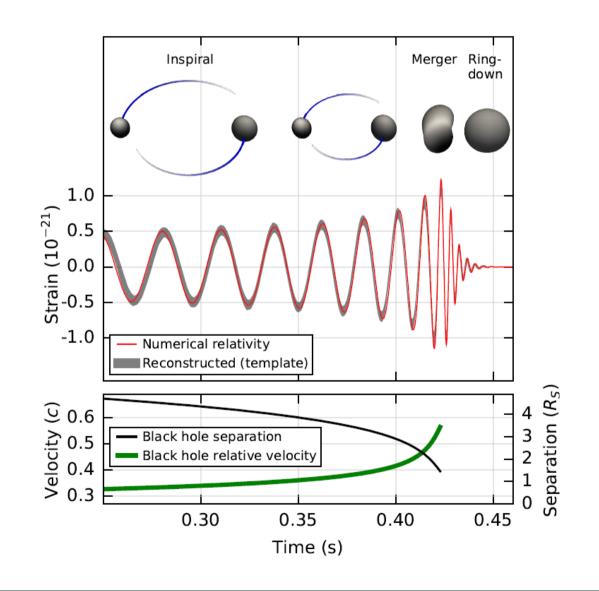


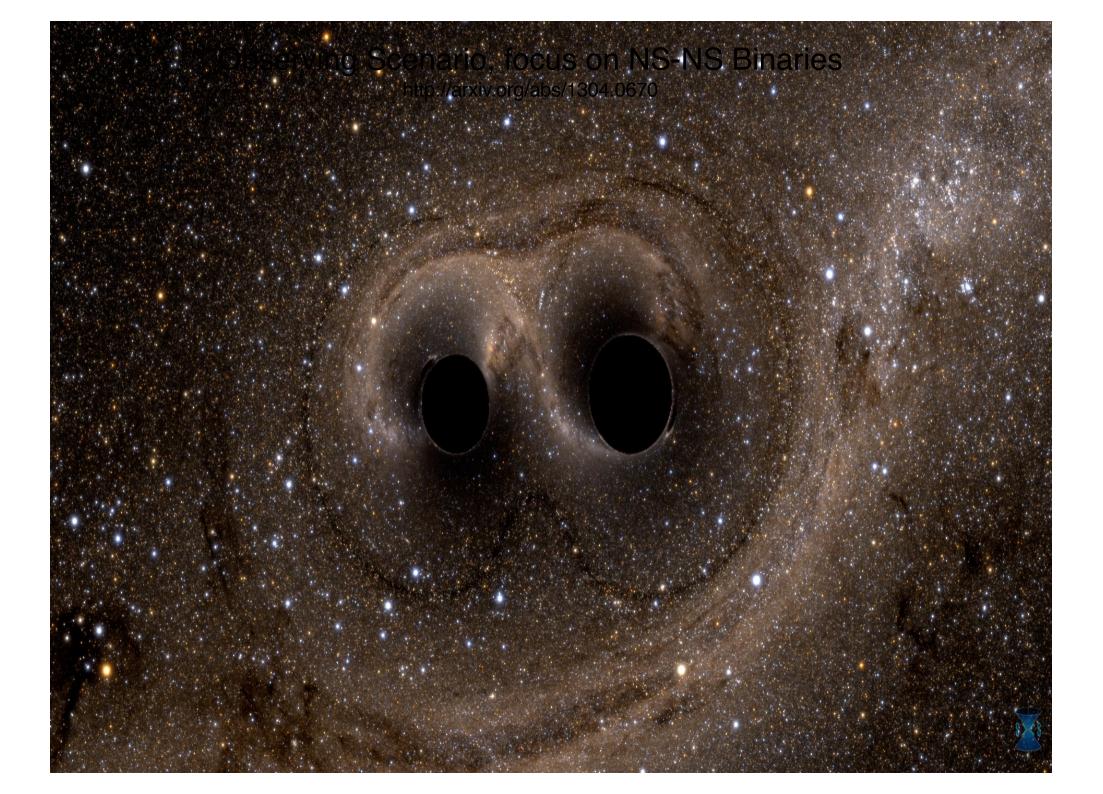
$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left[ \frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^{3/5}$$

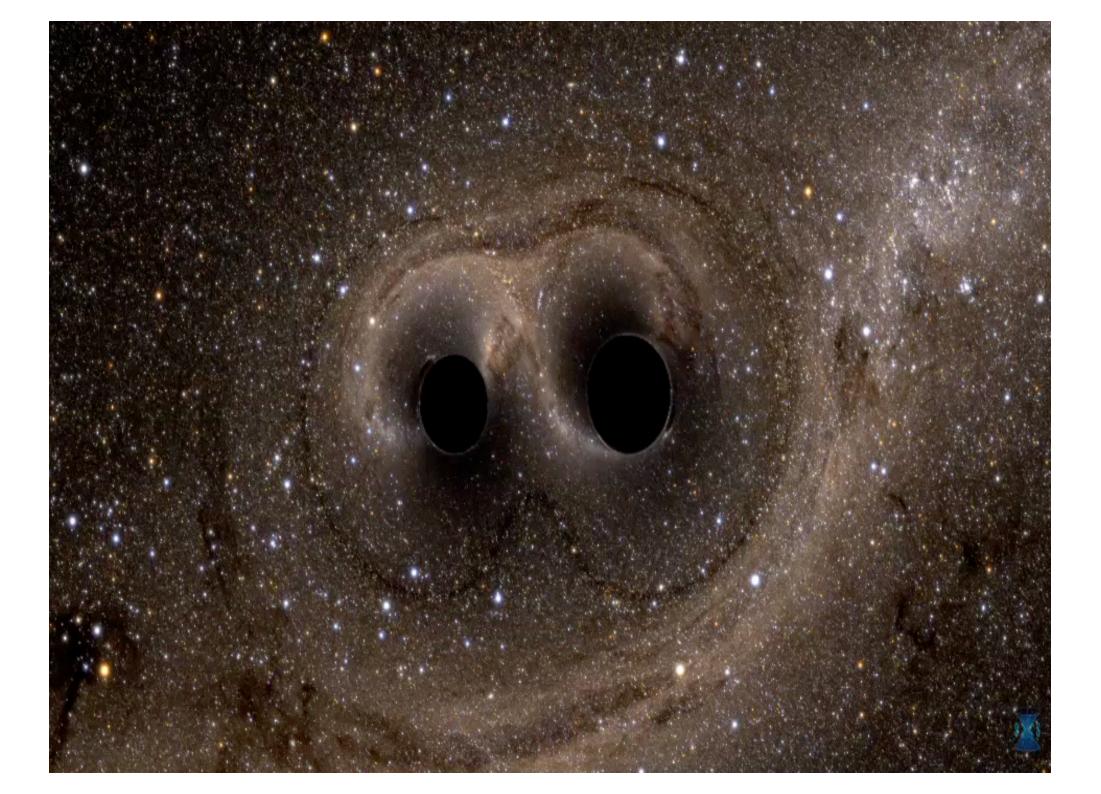
- Numerical relativity models of black hole horizons during coalescence
- Effective black hole separation in units of Schwarzschild radius  $(R_s=2GM_{tot}/c^2=210km);$ and effective relative velocities given by post-Newtonian parameter v/c =  $(GM_{tot}\pi f_{GW}/c^3)^{1/3}$

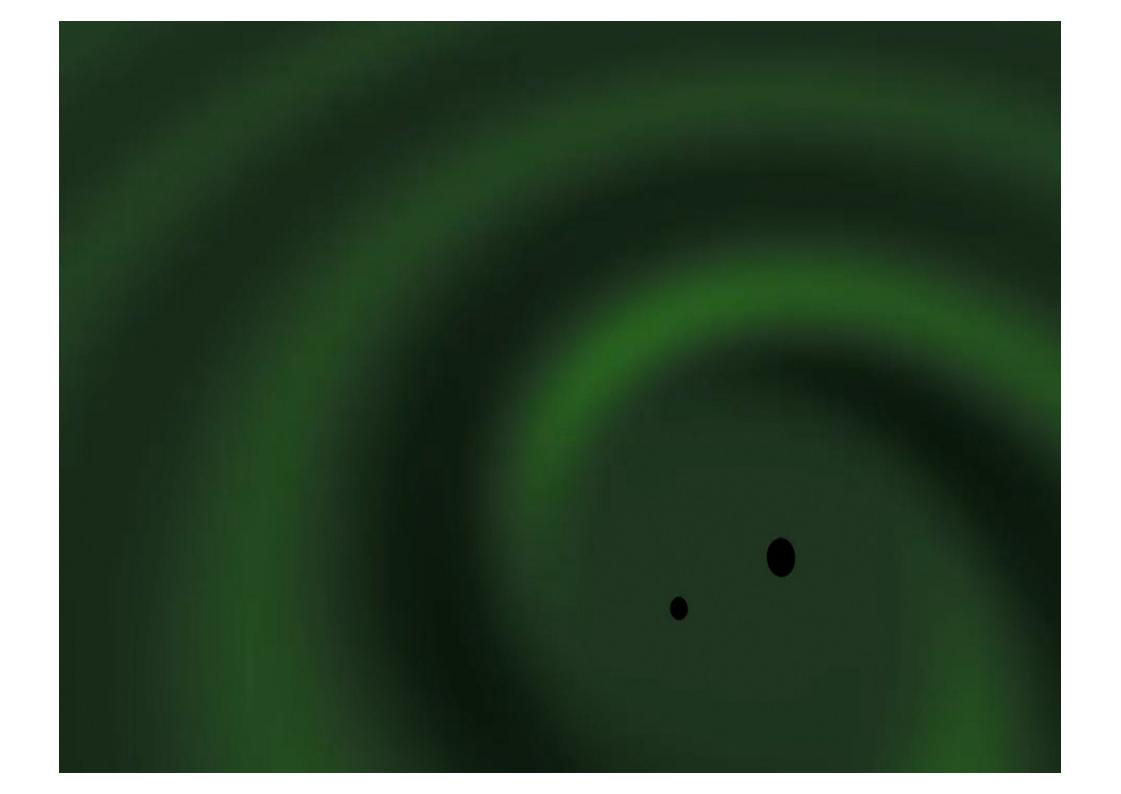
Binary Black Hole System

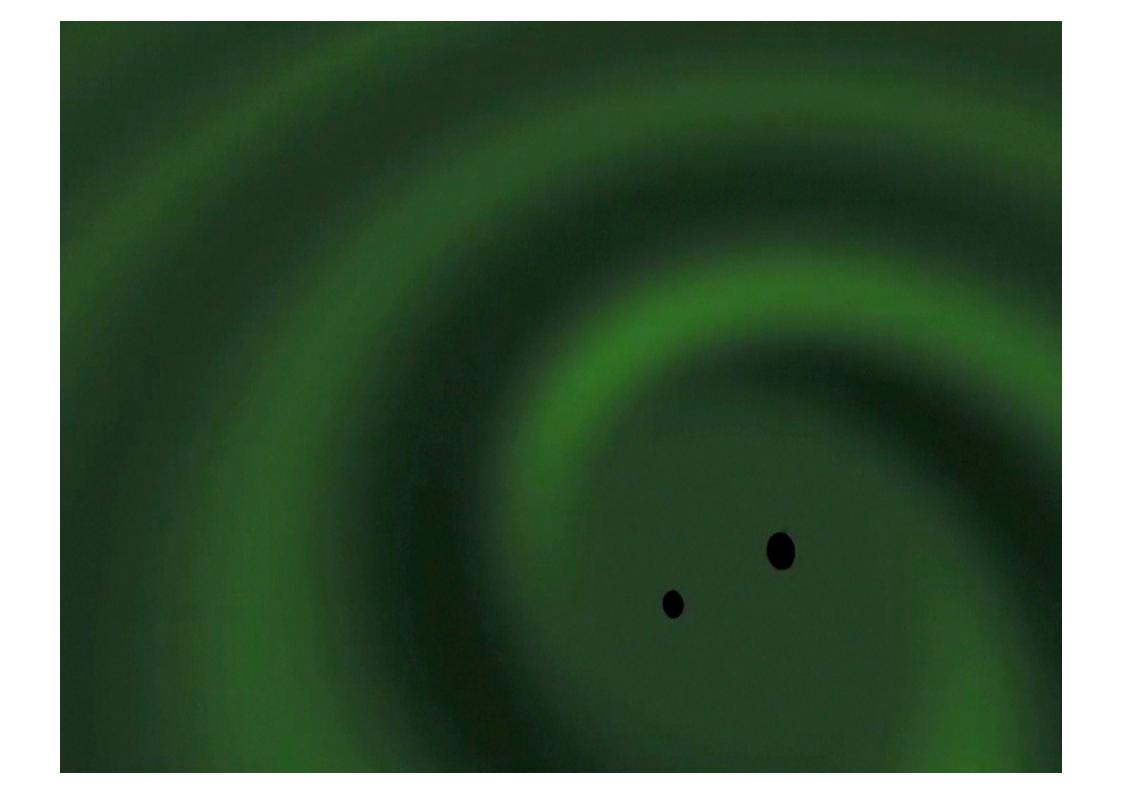
- M1 = 36 +5/-4 M<sub>sol</sub>
- M2 = 29 +/- 4 M<sub>sol</sub>
- Final Mass = 62 +/- 4  $M_{sol}$
- distance=410 +160/-180 MPc (redshift z = 0.09)

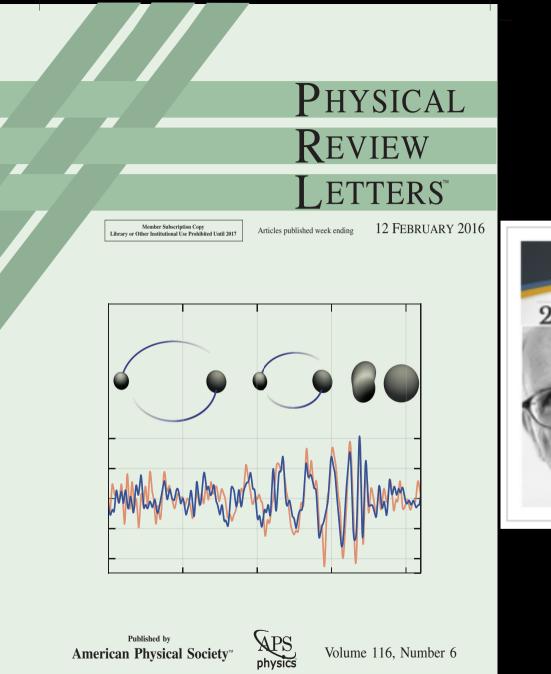


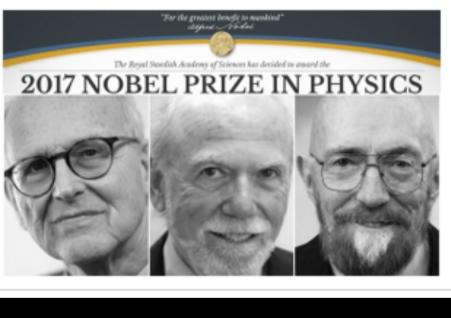












## Bounding graviton mass

• If gravitation is propagated by a massive field, then the velocity of GWs (gravitons) will depend upon their frequency as

$$\frac{v_g}{c} = 1 - \left(\frac{c}{f\lambda_g}\right)^2$$

 $\lambda_{g} = h/m_{g}c$  is the graviton Compton wavelenght.

- In the case of inspiralling compact binaries, GWs emitted at low frequency early in the inspiral will travel slightly slower than those emitted at high frequency later, resulting in an offset in the relative arrival times at a detector → the phase evolution of the observed inspiral gravitational waveform is modified.
- Matched filtering of the waveforms can bound such frequency-dependent variations in propagation speed → bound the graviton mass

#### Compton Wave-length of the Graviton

C. M. Will, Phys. Rev. D 57, 2061 (1998).

We assume a modified dispersion relation for gravitational waves

$$(v_{g}/c)^{2} = 1 - \{hc/(\lambda_{g}E)\}^{2}$$

 In the massive graviton theory an extra phase term is added to the CBC evolution (formally a 1PN order term)

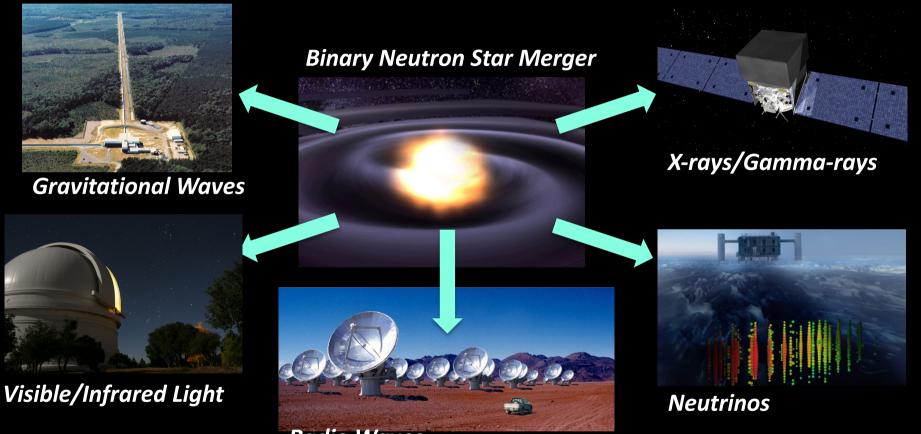
$$\phi_{MG}(f) = -(\pi D c) / [\lambda_g^2 (1+z) f]$$

 Our constrain on the 1PN terms permit to derive a down limit for the Compton wavelength of the graviton

$$\lambda_g = 2 \pi \hbar / (m_g c) > 10^{13} \text{ km}$$

- It corresponds to a limit  $m_g < 1.2 \times 10^{-22} \text{ eV/c}^2$ .
  - limit better than that set by Solar System observations
  - thousand time better of the binary pulsar bounds
  - worse than bounds from dynamics of galaxy clusters and weak lensing observations (model- dependent bounds)

## Multi-Messenger Astronomy: Gravitational Wave + Photons + Neutrinos



Radio Waves

A goal of LIGO and Virgo interferometers is the first direct detection of gravitational waves from ENERGETIC ASTROPHYSICAL events:

Mergers of NeutronStars and/or BlackHoles SHORT GRB
Kilonovas

> Core Collapse of Massive Stars

Cosmic String Cusps

Main motivations for joint GW/EM observations:

- Increase the GW detection confidence;
- Get a precise (arcsecond) localization, identify host galaxy;

➡ Supernovae

LONG GRB

**EM burst** 

- Provide insight into the progenitor physics;
- In the long term start a joint GW/EM cosmology.





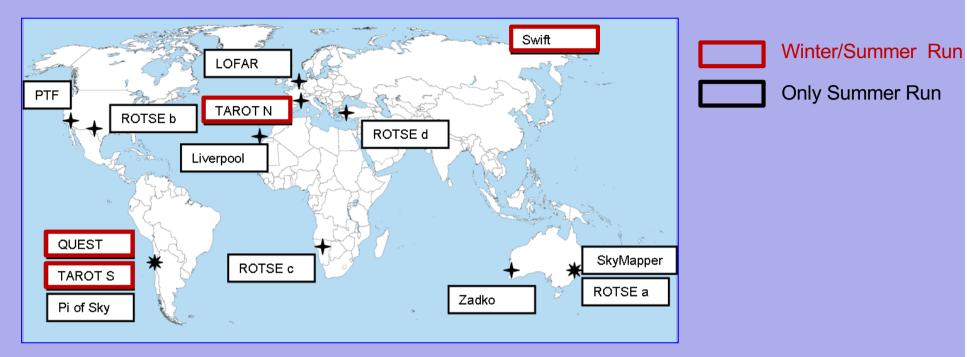








#### Ground-based and space EM facilities observing the sky at Optical, X-ray and Radio wavelengths involved in the follow-up program



#### **Optical Telescopes**

**TAROT SOUTH/NORTH** 1.86° X 1.86° FOV Zadko 25 X 25 arcmin FOV ROTSE

1.85 ° X 1.85° FOV **QUEST** 

9.4 square degree FOV

#### **SkyMapper** 5.6 square degree FOV **Pi of the Sky** 20° X 20° FOV **Palomar Transient Factory** 7.8 square degree FOV

Liverpool telescope 4.6 X 4.6 arcmin FOV



Swift Satellite 0.4° X 0.4° FOV

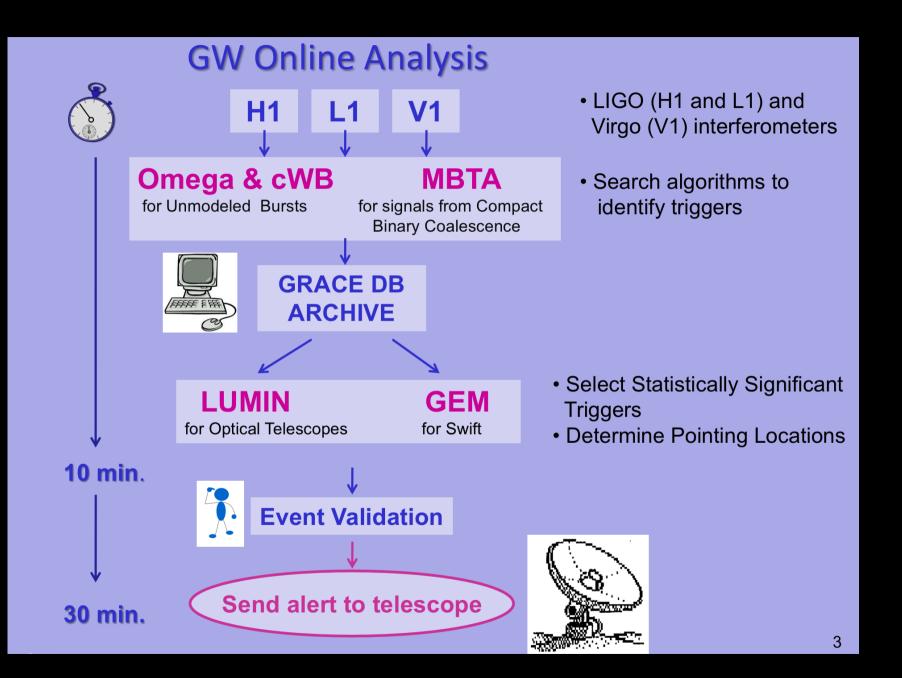


X-ray and UV/Optical Telescope

#### **Radio Interferometer**

LOFAR 10 – 250 MHz





## 17 August 2017

## GW 170817

Scientists to discuss new developments in gravitational-wave astronomy

Scientists representing LIGO, Virgo, and some 70 observatories will reveal new details and discoveries made in the ongoing search for gravitational waves.

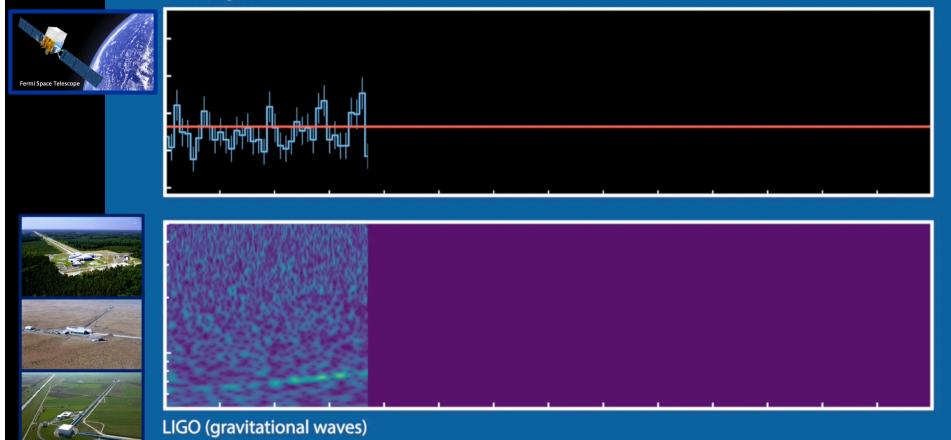
**WHAT:** Journalists are invited to join the National Science Foundation as it brings together scientists from the LIGO and Virgo collaborations, as well as representatives for some 70 observatories, on Monday, October 16, at 10:00 a.m. EDT at the National Press Club in Washington, D.C.

The gathering will begin with an overview of new findings from LIGO, Virgo, and partners that span the globe, followed by details from telescopes that work with the LIGO and Virgo Collaboration to study extreme events in the cosmos.

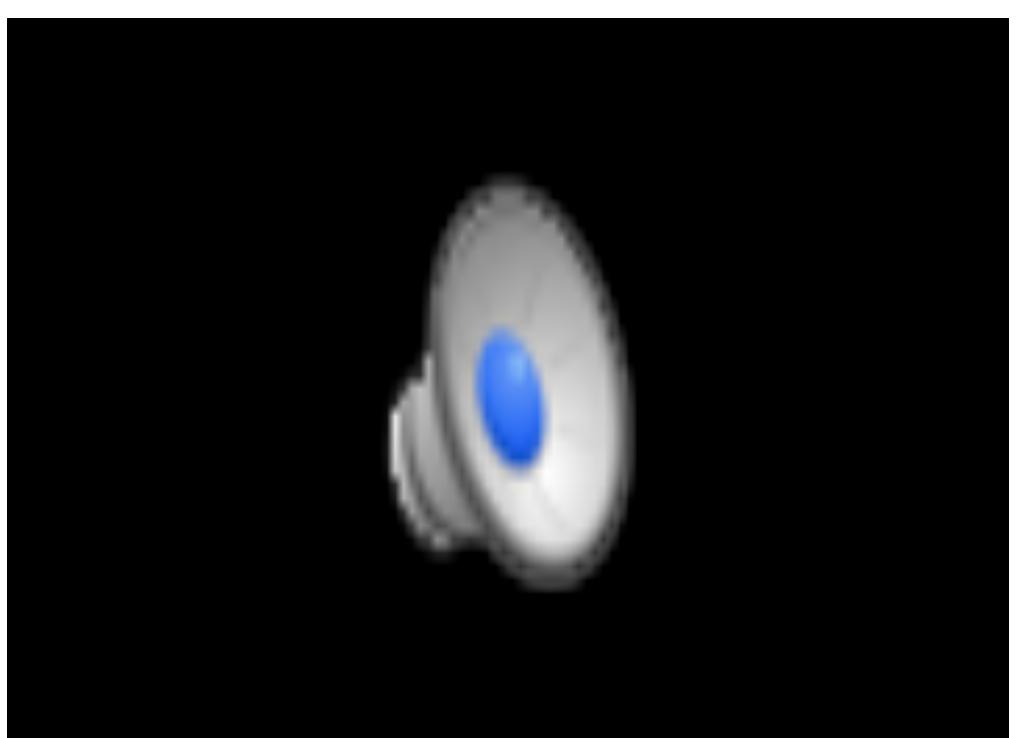
#### Marica Branchesi

Virgo Collaboration Astrophysicist Gran Sasso Science Institute/INFN

#### Fermi (light)



Credit: NASA's Goddard Space Flight Center/CI Lab



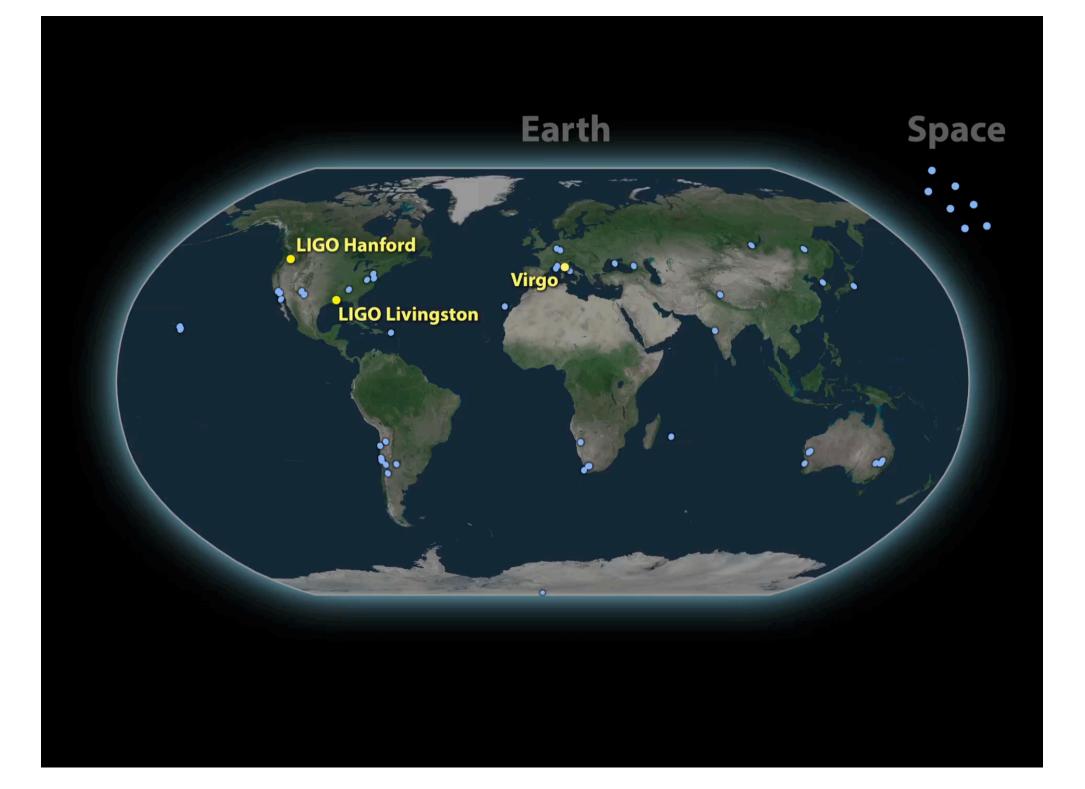
1 H		P	Per	i0(	dic	Ta	abl	e	of	th	9						2 He
3 Li	4 Be									5 B	6 C	7 N	8 O	9 F	10 Ne		
11 Na	12 Mg		121		3111							13 Al	14 Sí	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 TI	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra																
			57	58	59	60	61	62	63	64	65	66	67	68	69	70	71
			La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Но	Er	Tm	Yb	Lu
			89 Ac	90 Th	91 Pa	92 U											

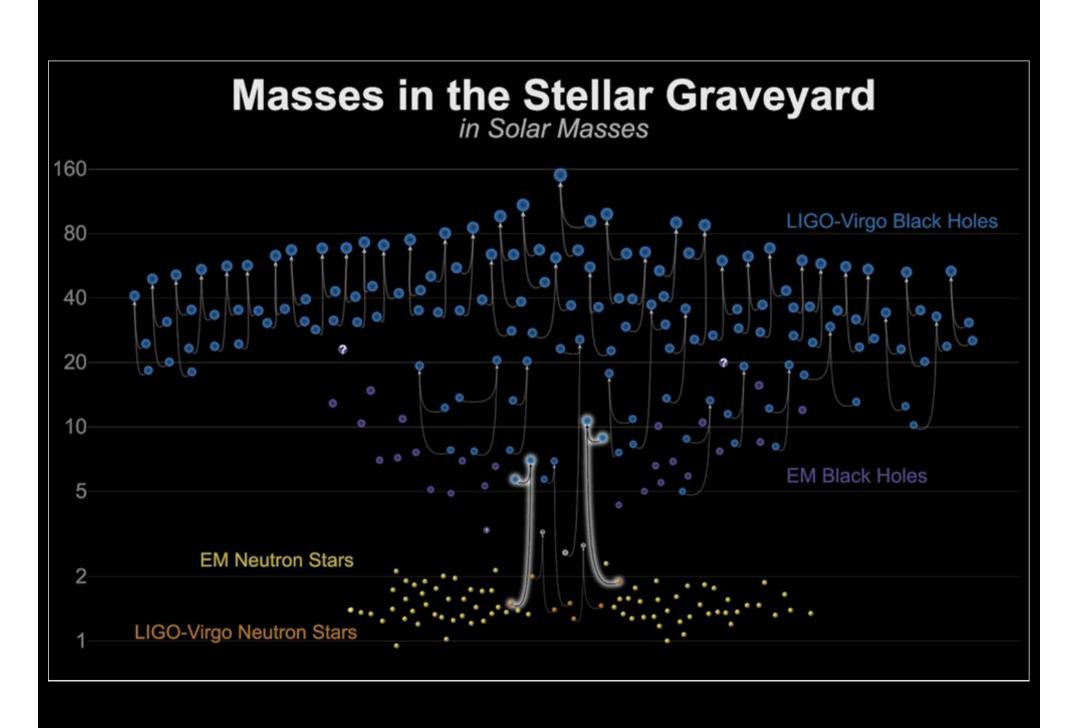
Yellow: Formed by Merging Neutron Stars

Credit:Jennifer Johnson/

### RIPPLES OF GRAVITY, FLASHES OF LIGHT:

WORLD'S OBSERVATORIES WITNESS A COSMIC CATACLYSM





## FIND OUT MORE:

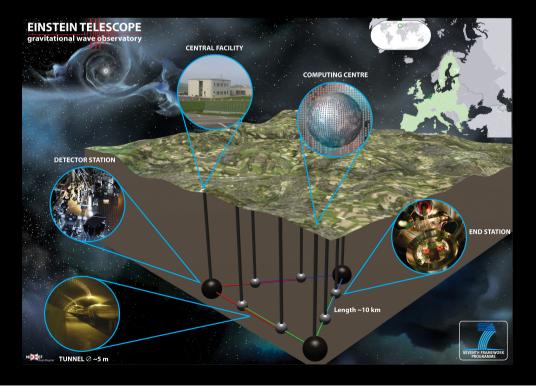
Visit our websites:

www.ligo.org, www.virgo-gw.eu, gwcenter.icrr.u-tokyo.ac.jp/en/

#### 8 Recommendations to GWIC to guide the development of the field

#### 8.5 Toward a third-generation global network

"Background— The scientific focus of a third-generation global network will be gravitational wave astronomy and astrophysics as well as cutting edge aspects of basic physics. Third-generation underground facilities are aimed at having excellent sensitivity from ~1 Hz to ~10<sup>4</sup> Hz. As such, they will greatly expand the new frontier of gravitational wave astronomy and astrophysics.

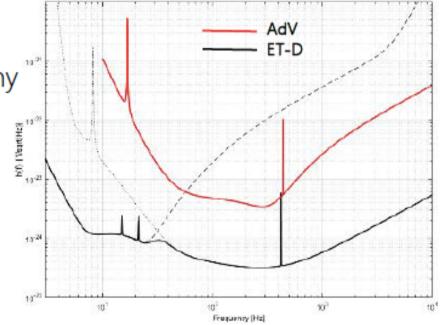


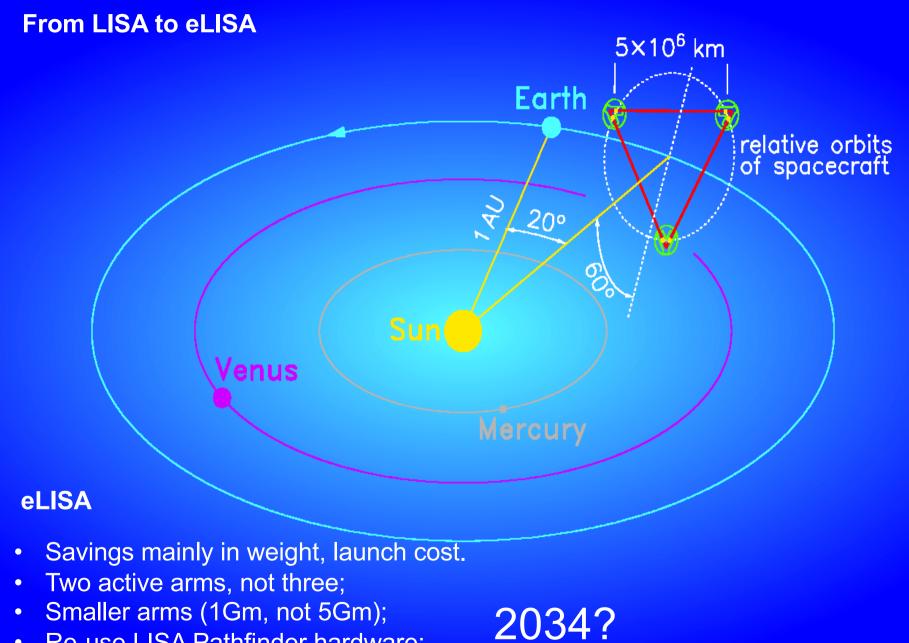
In Europe, a three year-long design study for a thirdgeneration gravitational wave facility, the Einstein Telescope (ET), has recently begun with funding from the European Union.



# EINSTEIN TELESCOPE

- ✓Design study of ET funded by the European Commission under FP7
  - interest primarily focused on the Infrastructure rather than on the detector and its technologies
  - The infrastructure should no limit the sensitivity of the future hosted detectors
    - Size
    - Environmental noises (seismic and NN)
  - ET absorbed and developed many concepts in GW detectors:
    - Underground and cryo-compatible facility, pioneered in Japan by CLIO and KAGRA
    - Triangular geometry, concept used in LISA
    - Xylophone configuration

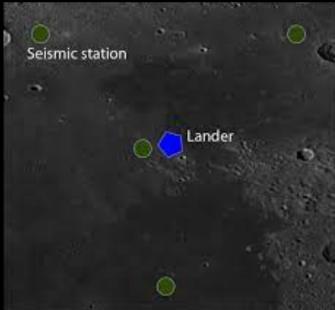




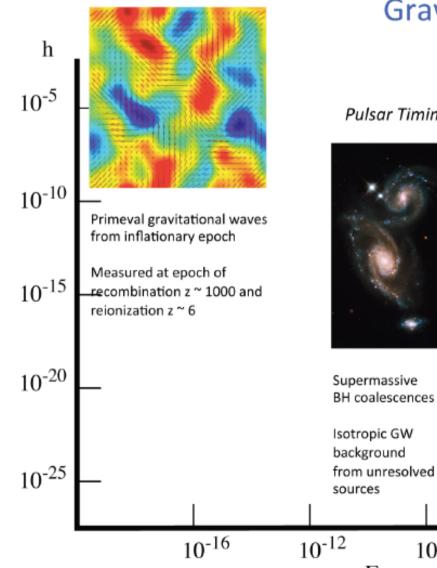
Re-use LISA Pathfinder hardware; •

#### Lunar Gravitational-wave Antenna The Astrophysical Journal,910:1(22pp), 2021 March 20





#### Cosmic Microwave Background Polarization B Modes



#### **Gravitational Wave Spectrum**

# Supermassive

10<sup>-8</sup>

Frequency Hz

Pulsar Timing

Small mass/BH infalls

Massive BH coalescences

White dwarf binaries in our galaxy

Space-based Interferometers



10<sup>-4</sup>

Compact binary coalescences: neutron stars and black holes

Asymmetric pulsar rotations

Ground-based Interferometers

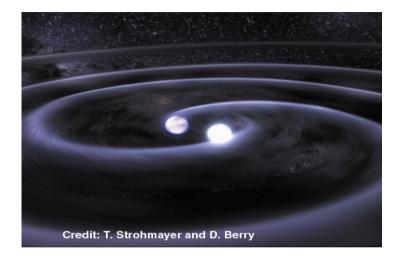


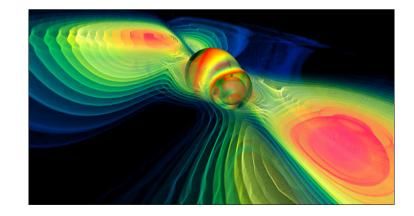
 $10^{4}$ 

 $10^{0}$ 

## THE GLOBAL PLAN

- Advanced Detectors (LIGO, VIRGO) will initiate gravitational wave astronomy through the detection of the most luminous sources - compact binary mergers.
- Third Generation Detectors (ET and Cosmic Explorer) will expand detection horizons and provide new tools for extending knowledge of fundamental physics, cosmology and relativistic astrophysics.
- Observation of low frequency gravitational wave with eLISA will probe the role of super-massive black holes in galaxy formation and evolution





# Every newly opened astronomical window has found unexpected results

Window	Opened	1 <sup>st</sup> Surprise	Year
Optical	1609 Galilei	Jupiter's moons	1610
Cosmic Rays	1912	Muon	1930s
Radio	1930s	Giant Radio Galaxies CMB Pulsars	1950s 1964 1967
X - ray	1948	Sco X-1 X-ray binaries	1962 1969 Uhuru
g - ray	1961	GRBs	Late 1960s+ Vela
GW	2015	Massive BH-BH mergers	2016

Thank you for your attention