

What lies beyond the Standard Model?

Supersymmetry

New motivations
From LHC Run 1

- Stabilize electroweak vacuum
- Successful prediction for Higgs mass
 - Should be < 130 GeV in simple models
- Successful predictions for couplings
 - Should be within few % of SM values
- **Naturalness, GUTs** string, ..., **dark matter**

Early Russian & Ukrainian Papers

LIE GROUPS WITH COMMUTING AND ANTICOMMUTING PARAMETERS

F. A. BEREZIN AND G. I. KAC

UDC 519.46

Abstract. In this paper we study analogs of Lie algebras and formal Lie groups of groups differ from usual Lie groups, roughly speaking, in that they admit anticommuting parameters. The analogs of Lie algebras differ from usual Lie algebras by proper tator. In the definition of these objects an essential role is played by the gradient ial they become Lie groups and algebras in the usual sense. To these generalize over classical theorems on the connection between Lie groups and algebras and tation theory.

EXTENSION OF THE ALGEBRA OF POINCARÉ GROUP GENERATORS AND VIOLATION OF P INVARIANCE

Yu.A. Gol'fand and E.P. Likhtman
Physics Institute, USSR Academy of Sciences
Submitted 10 March 1971
ZhETF Pis. Red. 13, No. 8, 452 - 455 (20 April 1971)

POSSIBLE UNIVERSAL NEUTRINO INTERACTION

D.V. Volkov and V.P. Akulov
Physico-technical Institute, Ukrainian Academy of Sciences
Submitted 13 October 1972
ZhETF Pis. Red. 16, No. 11, 621 - 624 (5 December 1972)

PHYSICS LETTERS

3 September 1973

IS THE NEUTRINO A GOLDSTONE PARTICLE?

D.V. VOLKOV and V.P. AKULOV

Physico-Technical Institute, Academy of Sciences of the Ukrainian SSR, Kharkov 108, USSR

Received 5 March 1973

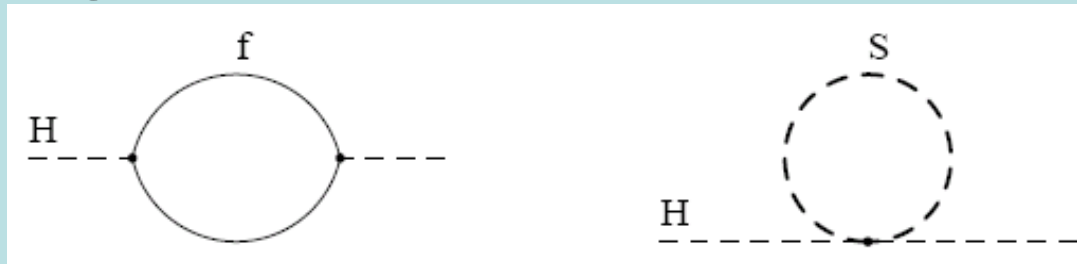
GAUGE FIELDS FOR SYMMETRY GROUP WITH SPINOR PARAMETERS

D. V. Volkov and V. A. Soroka

The inclusion of gauge fields for a symmetry group containing anticommuting parameters is considered. The Higgs effect is discussed for Goldstone fields with spin 1/2.

Loop Corrections to Higgs Mass²

- Consider generic fermion and boson loops:



- Each is quadratically divergent: $\int^\Lambda d^4k/k^2$

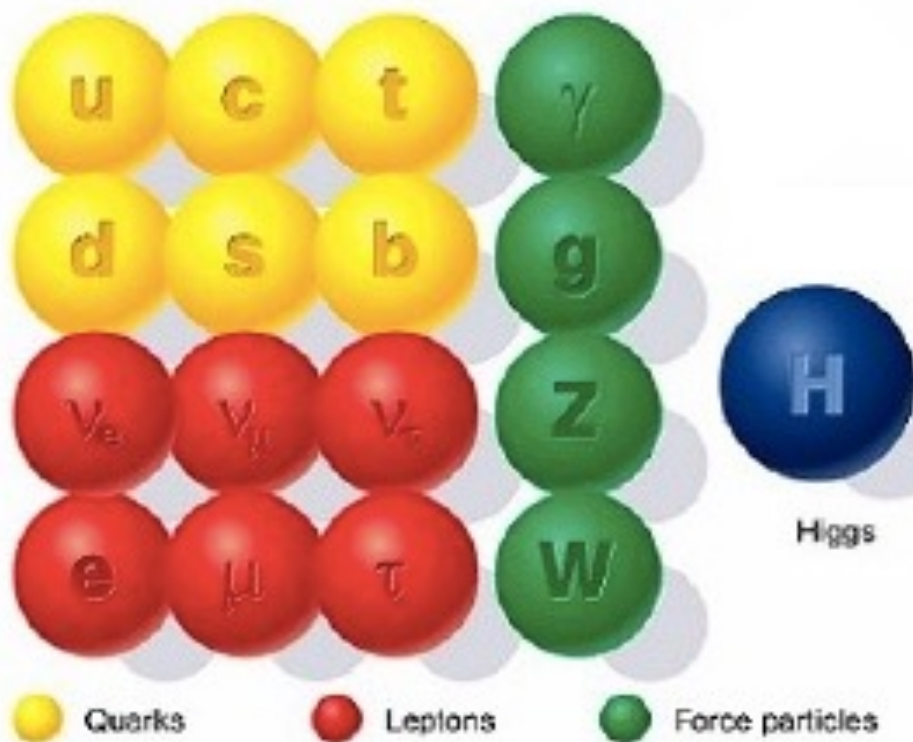
$$\Delta m_H^2 = -\frac{y_f^2}{16\pi^2} [2\Lambda^2 + 6m_f^2 \ln(\Lambda/m_f) + \dots]$$

$$\Delta m_H^2 = \frac{\lambda_S}{16\pi^2} [\Lambda^2 - 2m_S^2 \ln(\Lambda/m_S) + \dots]$$

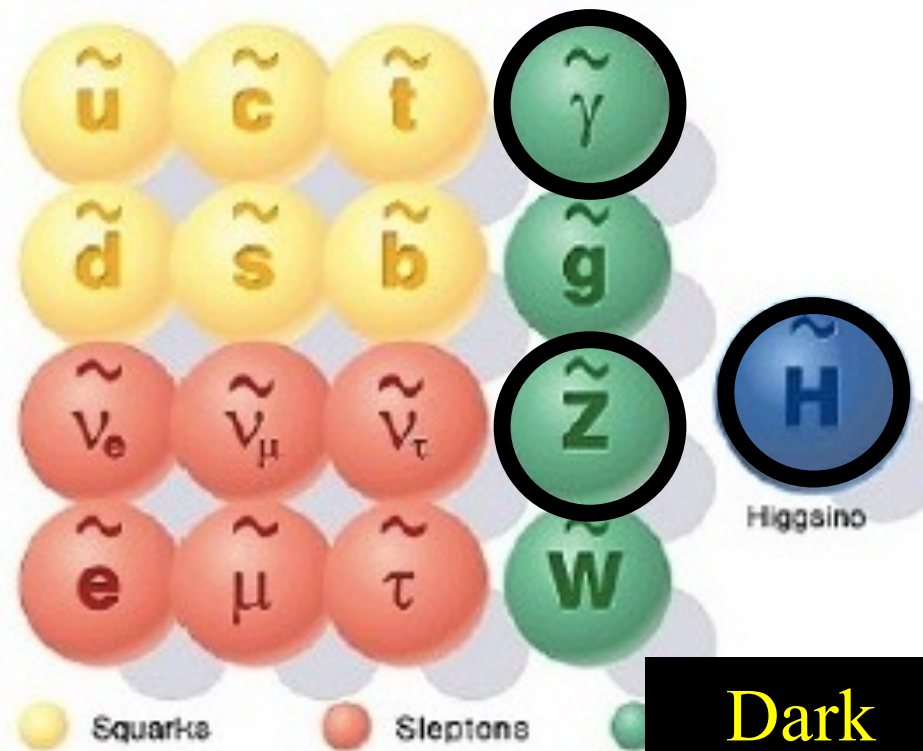
- Leading divergence cancelled if

$$\lambda_S = y_f^2 \times 2 \quad \text{Supersymmetry!}$$

Minimal Supersymmetric Extension of the Standard Model



Standard particles



SUSY particles

Minimal Supersymmetric Extension of the Standard Model (MSSM)

- Double up the known particles:

$$\begin{pmatrix} \frac{1}{2} \\ 0 \end{pmatrix} \text{ e.g., } \begin{pmatrix} \ell \text{ (lepton)} \\ \tilde{\ell} \text{ (slepton)} \end{pmatrix} \text{ or } \begin{pmatrix} q \text{ (quark)} \\ \tilde{q} \text{ (squark)} \end{pmatrix}$$
$$\begin{pmatrix} 1 \\ \frac{1}{2} \end{pmatrix} \text{ e.g., } \begin{pmatrix} \gamma \text{ (photon)} \\ \tilde{\gamma} \text{ (photino)} \end{pmatrix} \text{ or } \begin{pmatrix} g \text{ (gluon)} \\ \tilde{g} \text{ (gluino)} \end{pmatrix}$$

- Two Higgs doublets
 - 5 physical Higgs bosons:
 - 3 neutral, 2 charged
- Lightest neutral supersymmetric Higgs looks like the single Higgs in the Standard Model

Higgs Bosons in Supersymmetry

- Need 2 complex Higgs doublets
(cancel anomalies, form of SUSY couplings)
- $8 - 3 = 5$ physical Higgs bosons
Scalars h, H ; pseudoscalar A ; charged H^\pm
- Lightest Higgs $< M_Z$ at tree level:

$$M_{H,h}^2 = \frac{1}{2} \left[M_A^2 + M_Z^2 \pm \sqrt{(M_A^2 + M_Z^2)^2 - 4M_Z^2 M_A^2 \cos^2 2\beta} \right]$$

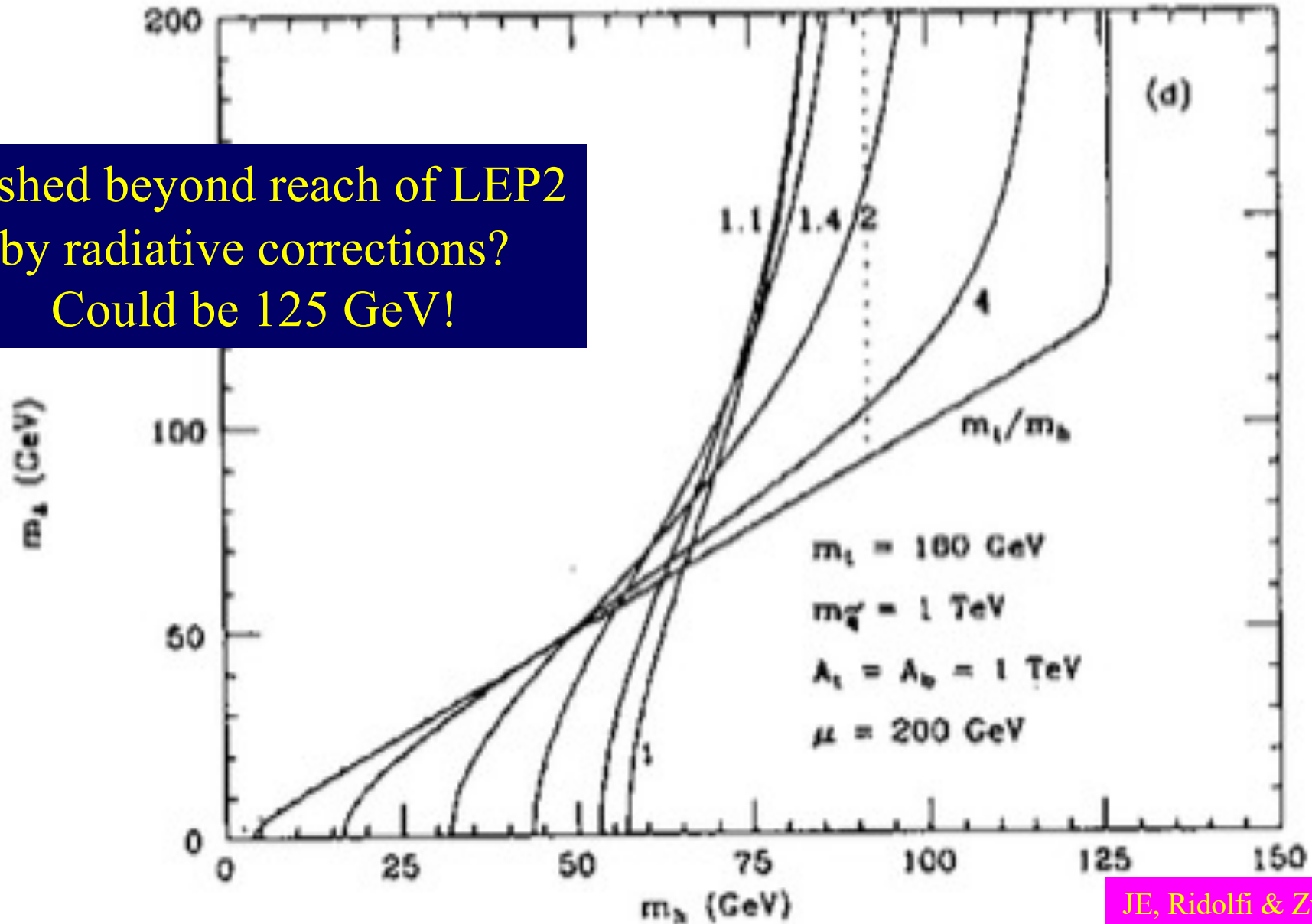
- Important radiative corrections to mass:

$$G_\mu m_t^4 \ln \left(\frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \right) \Delta M_H|_{\text{TH}} \sim 1.5 \text{ GeV}$$

1990/1

Higgs Mass in Supersymmetry

Pushed beyond reach of LEP2
by radiative corrections?
Could be 125 GeV!



Higgs properties in the pMSSM

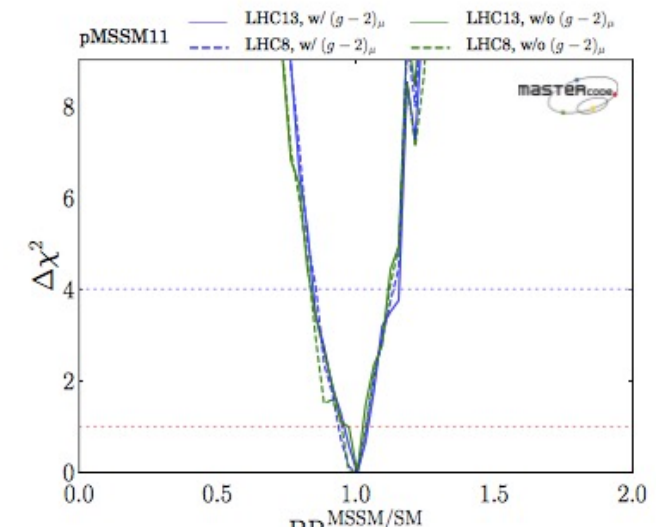
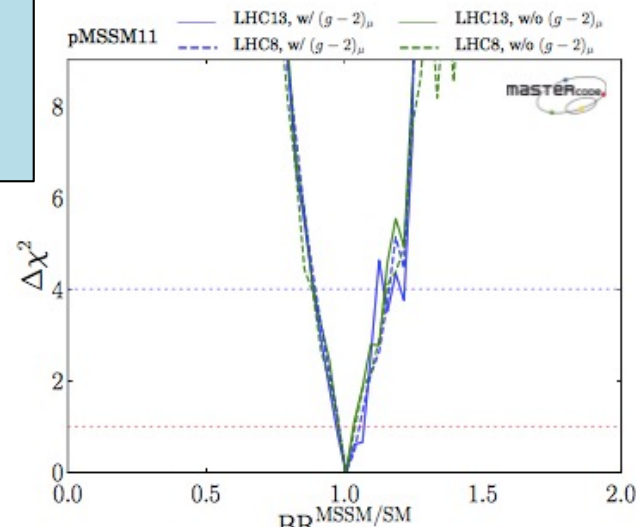
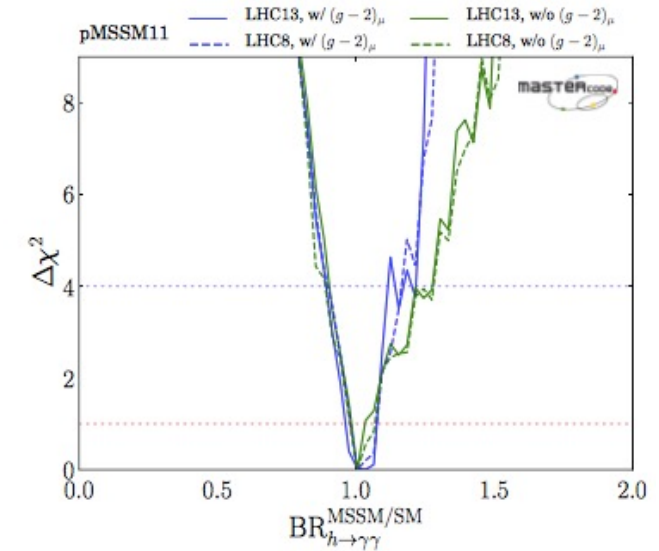
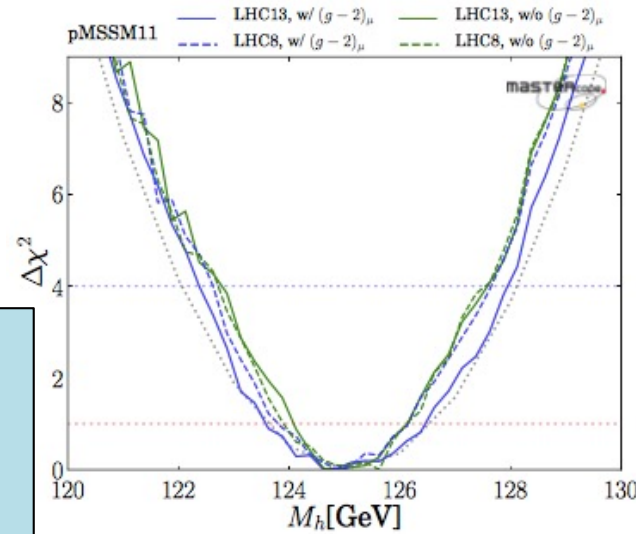


Fit with $g_{\mu-2}$

Fit without $g_{\mu-2}$

- No issue with measured Higgs mass
- Central values of decay BRs similar to SM
- Substantial deviations possible
- Opportunity for LHC!

Bagnaschi, Sakurai, JE et al,
arXiv:1710.11091

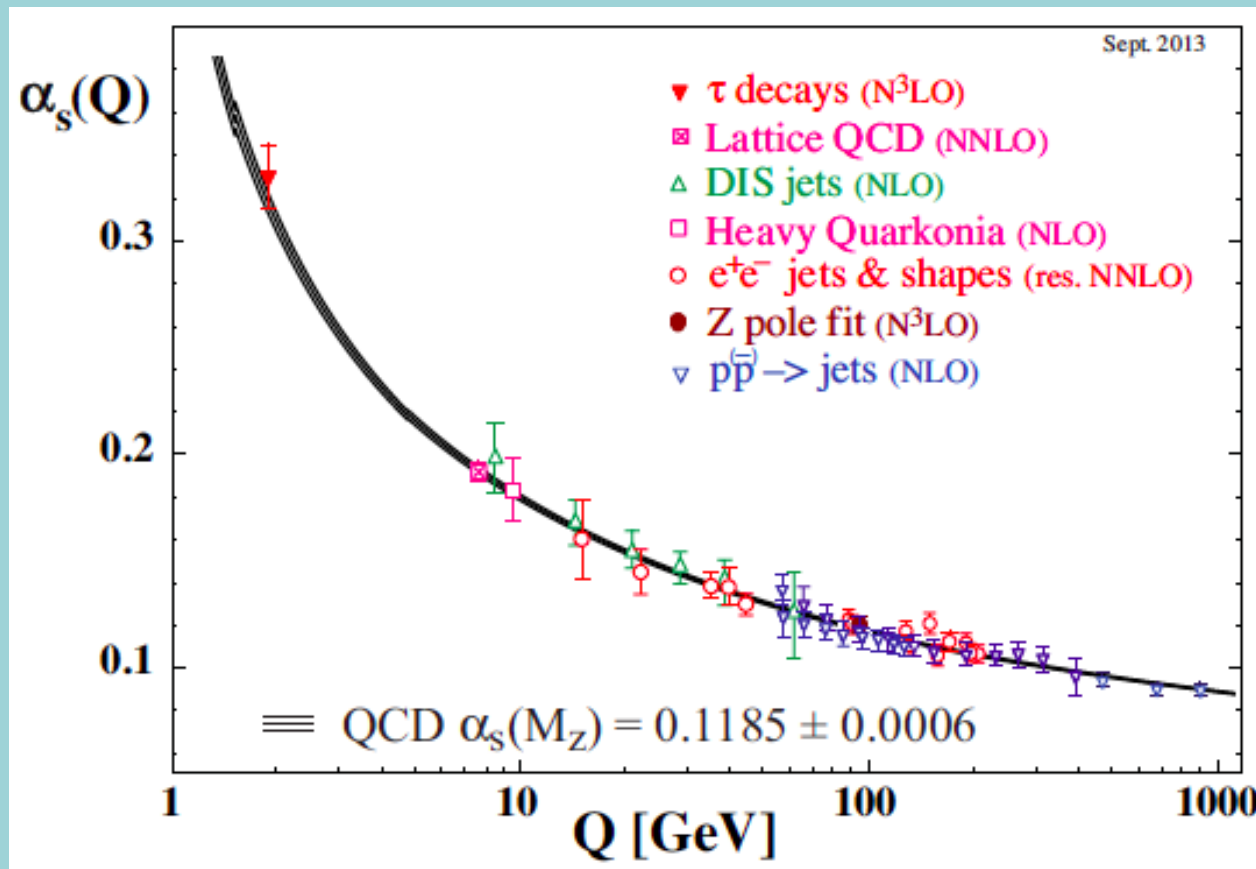


Towards Grand Unification

- The three Standard Model gauge couplings are different: $g_3 \gg g_2, g_1$
- Ratio $\sin^2 \theta_W \equiv \frac{g_1^2}{g_1^2 + g_2^2}$ is free parameter in Standard Model
- All couplings vary energy scale, calculable using renormalisation group
- Best known is decrease of $\alpha_s \equiv \frac{g_3^2}{4\pi}$, “asymptotic freedom”
- Offers prospect of unifying couplings at high energy, as in simple group structure, and predicting $\sin^2 \theta_W$

Strong Coupling “Constant”

- ... is not constant: weaker at higher energies



- **Asymptotic freedom**

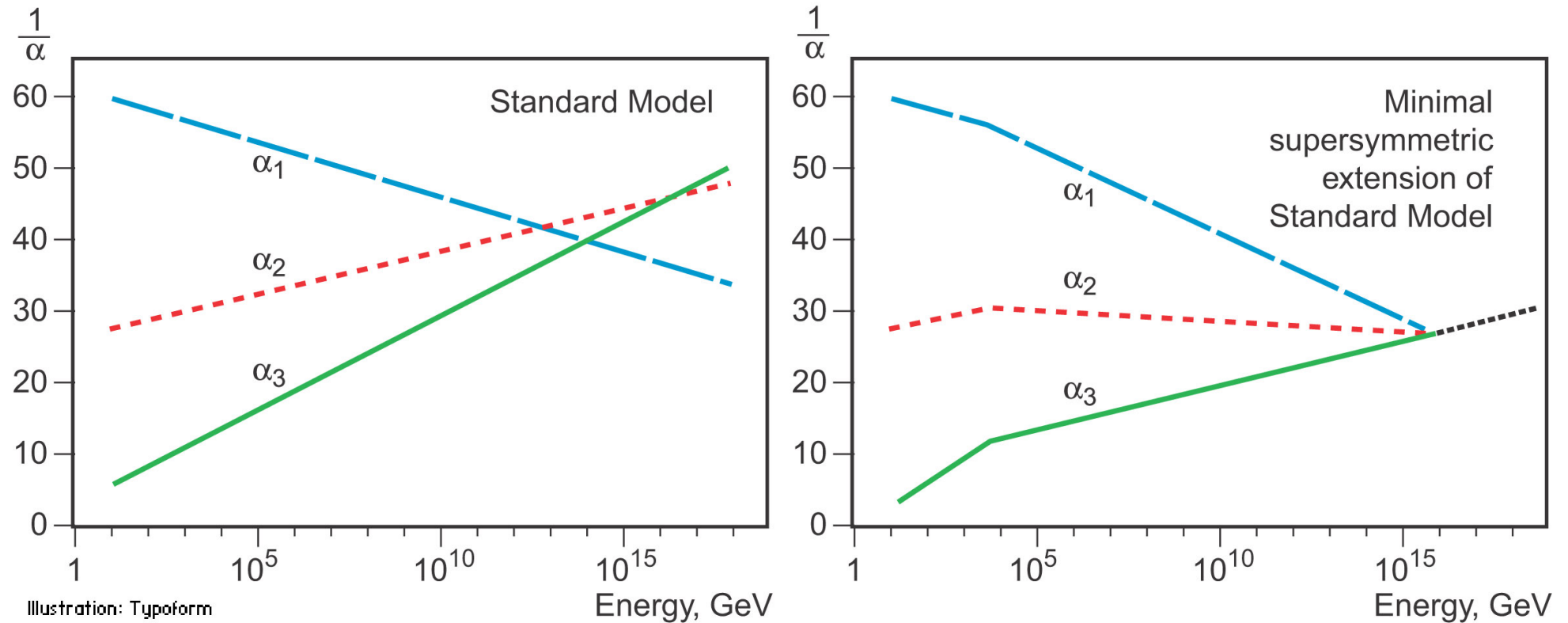
Grand Unification

- At one-loop order without/**with** supersymmetry:

$$b_i = \begin{pmatrix} 0 \\ -\frac{22}{3} \\ -11 \end{pmatrix} + N_g \begin{pmatrix} \frac{4}{3} \\ \frac{4}{3} \\ \frac{4}{3} \end{pmatrix} + N_H \begin{pmatrix} \frac{1}{10} \\ \frac{1}{6} \\ 0 \end{pmatrix} \quad b_i = \begin{pmatrix} 0 \\ -6 \\ -9 \end{pmatrix} + N_g \begin{pmatrix} 2 \\ 2 \\ 2 \end{pmatrix} + N_H \begin{pmatrix} \frac{3}{10} \\ \frac{1}{2} \\ 0 \end{pmatrix}$$

$$b_{ij} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & -\frac{136}{3} & 0 \\ 0 & 0 & -102 \end{pmatrix} + N_g \begin{pmatrix} \frac{19}{15} & \frac{3}{5} & \frac{44}{15} \\ \frac{1}{5} & \frac{49}{3} & 4 \\ \frac{4}{30} & \frac{3}{2} & \frac{76}{3} \end{pmatrix} + N_H \begin{pmatrix} \frac{9}{50} & \frac{9}{10} & 0 \\ \frac{3}{10} & \frac{13}{6} & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad b_{ij} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & -24 & 0 \\ 0 & 0 & -54 \end{pmatrix} + N_g \begin{pmatrix} \frac{38}{15} & \frac{6}{5} & \frac{88}{15} \\ \frac{2}{5} & 14 & 8 \\ \frac{11}{5} & 3 & \frac{68}{3} \end{pmatrix} + N_H \begin{pmatrix} \frac{9}{50} & \frac{9}{10} & 0 \\ \frac{3}{10} & \frac{7}{2} & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Grand Unification of Couplings



Almost works with just Standard Model particles
Better with supersymmetric particles

Simplest Grand Unified Theory

- Electromagnetic charge embedded in simple group: charge quantized

$$\sum_{q,\ell} Q_i = 3Q_u + 3Q_d + Q_e = 0$$

- Minimal model: SU(5)
- Fermions of a single generation accommodated

$$\bar{\mathbf{5}} : (\psi_i)_L = \begin{pmatrix} \bar{d}_1 \\ \bar{d}_2 \\ \bar{d}_3 \\ e^- \\ -\nu_e \end{pmatrix}_L \quad \mathbf{10} : (\chi^{ij})_L = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & \bar{u}_3 & -\bar{u}_2 & u_1 & d_1 \\ -\bar{u}_3 & 0 & \bar{u}_1 & u_2 & d_2 \\ u_2 & -\bar{u}_1 & 0 & u_3 & d_3 \\ -u_1 & -u_2 & -u_3 & 0 & e^+ \\ -d_1 & -d_2 & -d_3 & -e^+ & 0 \end{pmatrix}_L$$

- “Explain” “random” quantum numbers
- **Renormalization prediction $\sin^2 \theta_W \simeq 0.23$**

Electroweak Mixing Angle

- Related to ratio of SU(2), U(1) couplings:

$$\sin^2 \theta(m_Z) = \frac{g'^2}{g_2^2 + g'^2} = \frac{3}{5} \frac{g_1^2(m_Z)}{g_2^2(m_Z) + \frac{3}{5}g_1^2(m_Z)}$$

- At one loop:

$$\sin^2 \theta(m_Z) = \frac{1}{1 + 8x} \left[3x + \frac{\alpha_{em}(m_Z)}{\alpha_3(m_Z)} \right] = \frac{1}{5} \left(\frac{b_2 - b_3}{b_1 - b_2} \right)$$

- One-loop coefficients w' out/**with** supersymmetry:

$\frac{4}{3}N_G - 11 \leftarrow$	$b_3 \rightarrow 2N_G - 9 = -3$
$\frac{1}{6}N_H + \frac{4}{3}N_G - \frac{22}{3} \leftarrow$	$b_2 \rightarrow \frac{1}{2}N_H + 2N_G - 6 = +1$
$\frac{1}{10}N_H + \frac{4}{3}N_G \leftarrow$	$b_1 \rightarrow \frac{3}{10}N_H + 2N_G = \frac{33}{5}$
$\frac{23}{218} = 0.1055 \leftarrow$	$x \rightarrow \frac{1}{7}$

- Data:

$$x = \frac{1}{6.92 \pm 0.07}$$

LEP Data Consistent with Supersymmetric Grand Unification

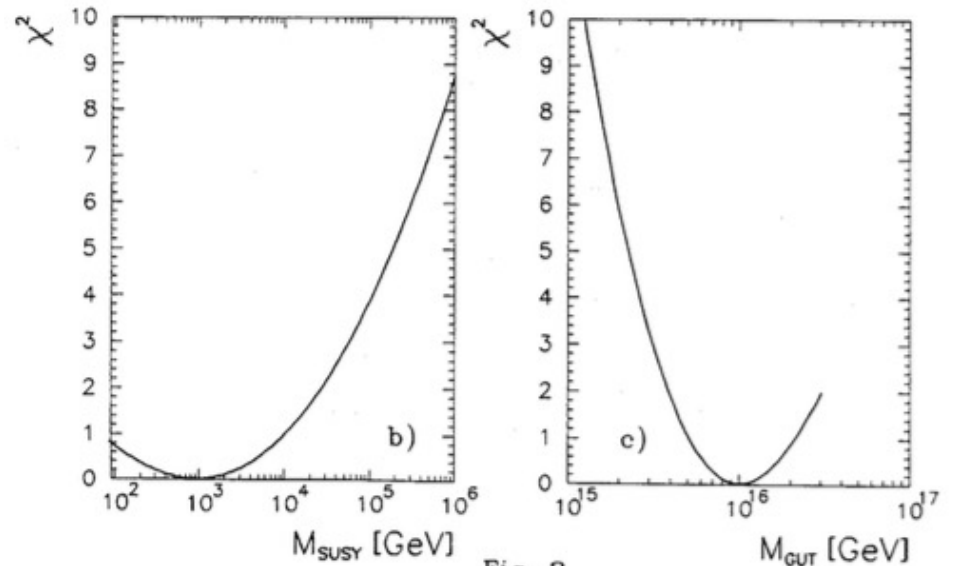
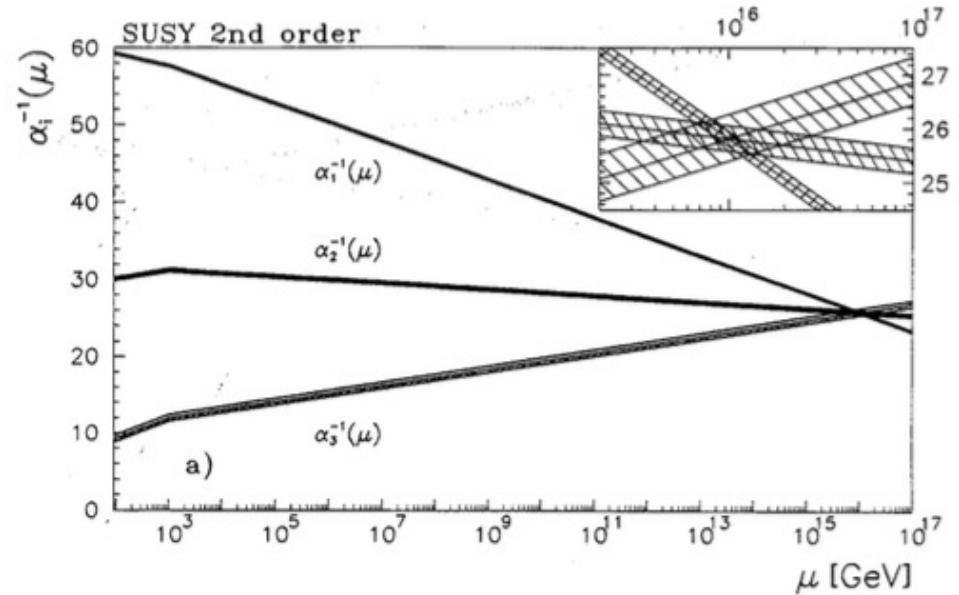
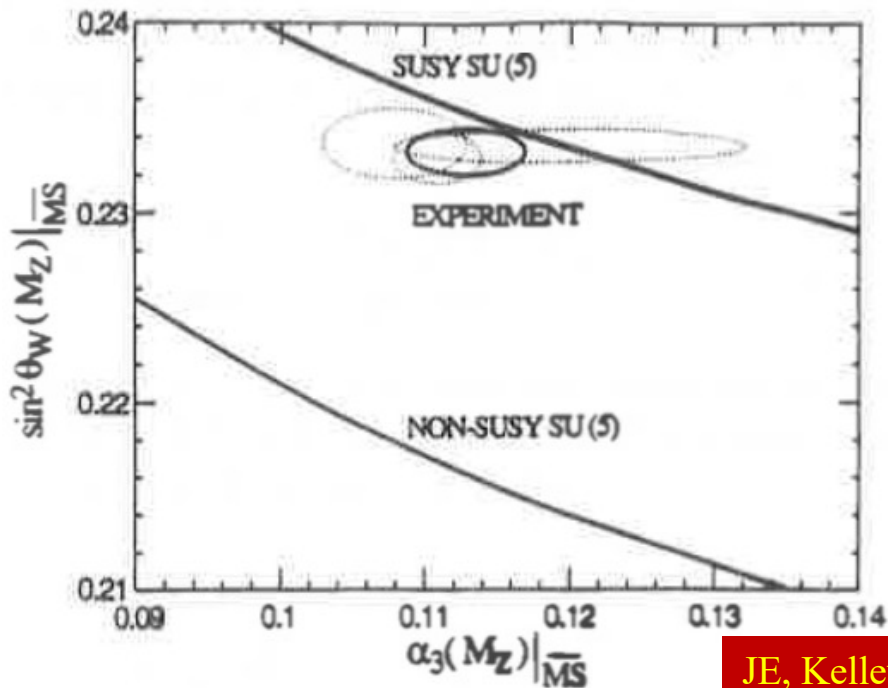


Fig. 2

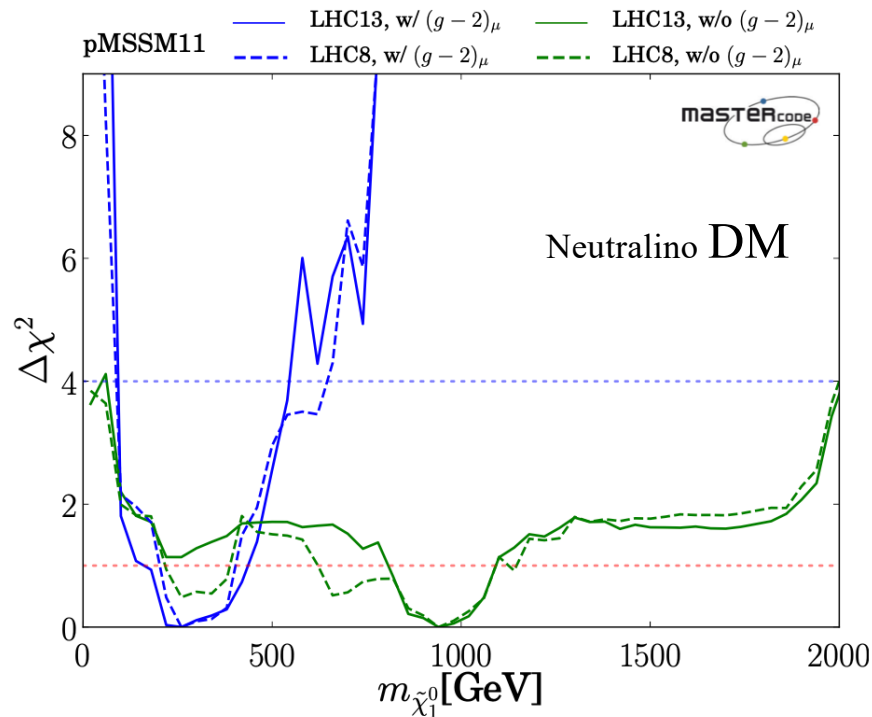
Amaldi, de Boer & Furstenau

Supersymmetry Breaking

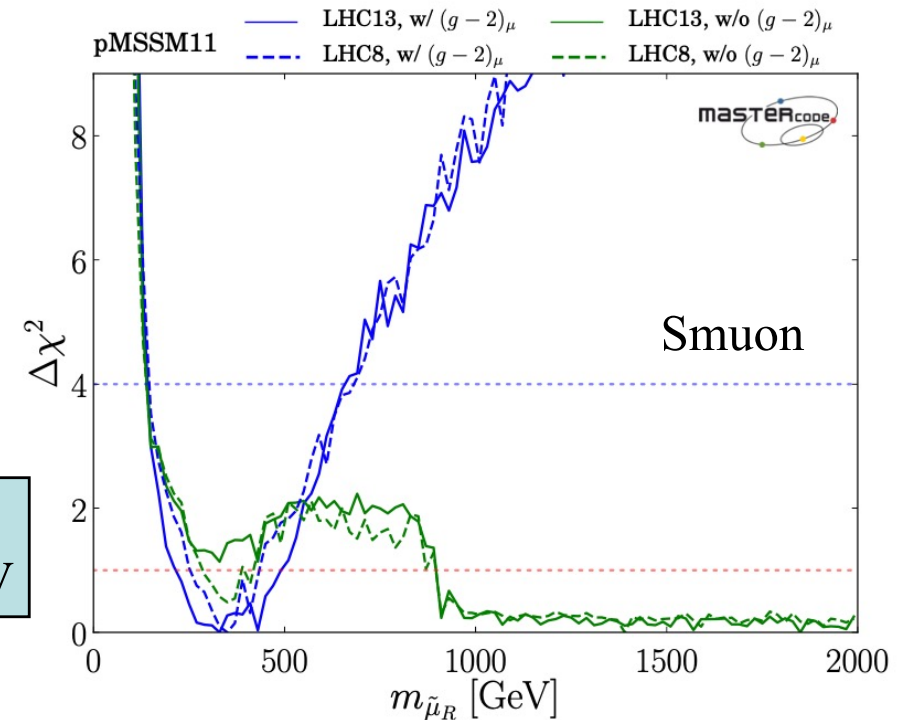
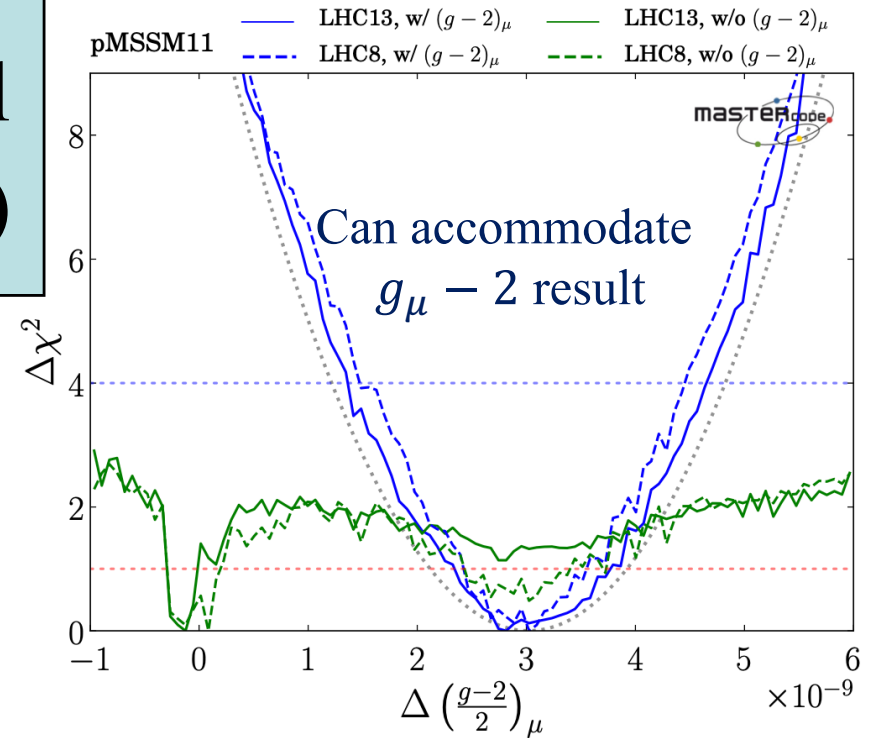
- Supersymmetry must be broken, many models, no clear guidance from theory
- Assume universality at GUT scale? (CMSSM)
 - Renormalisation effects increase \tilde{q} masses relative to $\tilde{\ell}$, \tilde{g} mass relative to W^\pm
 - Lighter stop squark may have $m_{\tilde{t}_1} < m_{\tilde{q}}$
 - Renormalization can drive $m_H^2 < 0$, enabling spontaneous gauge symmetry breaking
- Alternatively: treat particle masses as free parameters (pMSSM)

$g_\mu - 2$ in Phenomenological Supersymmetry (pMSSM11)

No relation between squark/gluino masses and slepton/neutralino masses



No problem accommodating BNL/FNAL result
Neutralino DM, smuon masses $\sim 300/400$ GeV



Mass Renormalizations

- **Assuming universality at the GUT scale**
- Gaugino masses:
 - $M_a = (\alpha_a / \alpha_{\text{GUT}}) m_{1/2}$, e.g., $\rightarrow M_2 / M_3 = \alpha_2 / \alpha_3$
- Squark and slepton masses:
 - Squark mass²: $m_0^2 + 6 m_{1/2}^2$
 - Left-handed slepton mass²: $m_0^2 + 0.5 m_{1/2}^2$
 - Right-handed slepton mass²: $m_0^2 + 0.15 m_{1/2}^2$
- Minimal flavour violation (MFV):
 - Flavour mixing of squarks and sleptons induced by CKM, neutrino mixing

Renormalization of Susy Breaking Parameters

- After cancellation of quadratic divergences:
renormalized logarithmically:

gaugino masses: $d M_a/dt \sim \beta_a M_a$

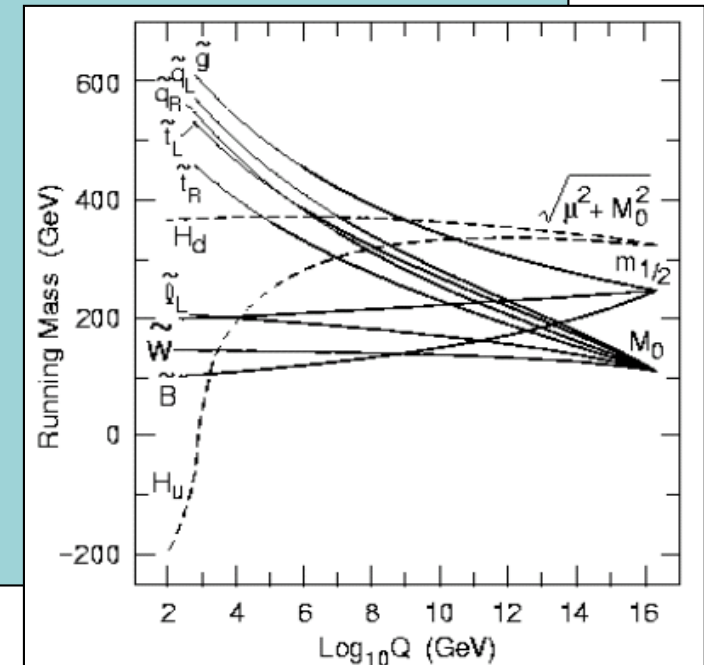
scalar masses²: $\frac{\partial m_{0_i}^2}{\partial t} = \frac{1}{16\pi^2} [\lambda^2(m_0^2 + A_\lambda^2) - g_a^2 M_a^2]$

- Assuming universal input parameters (CMSSM)
- Solutions at low energy scales Q:

$$M_a(Q) = (\alpha_a / \alpha_{\text{GUT}}) m_{1/2}$$

$$m_{0_i}^2 = m_0^2 + C_i m_{1/2}^2$$

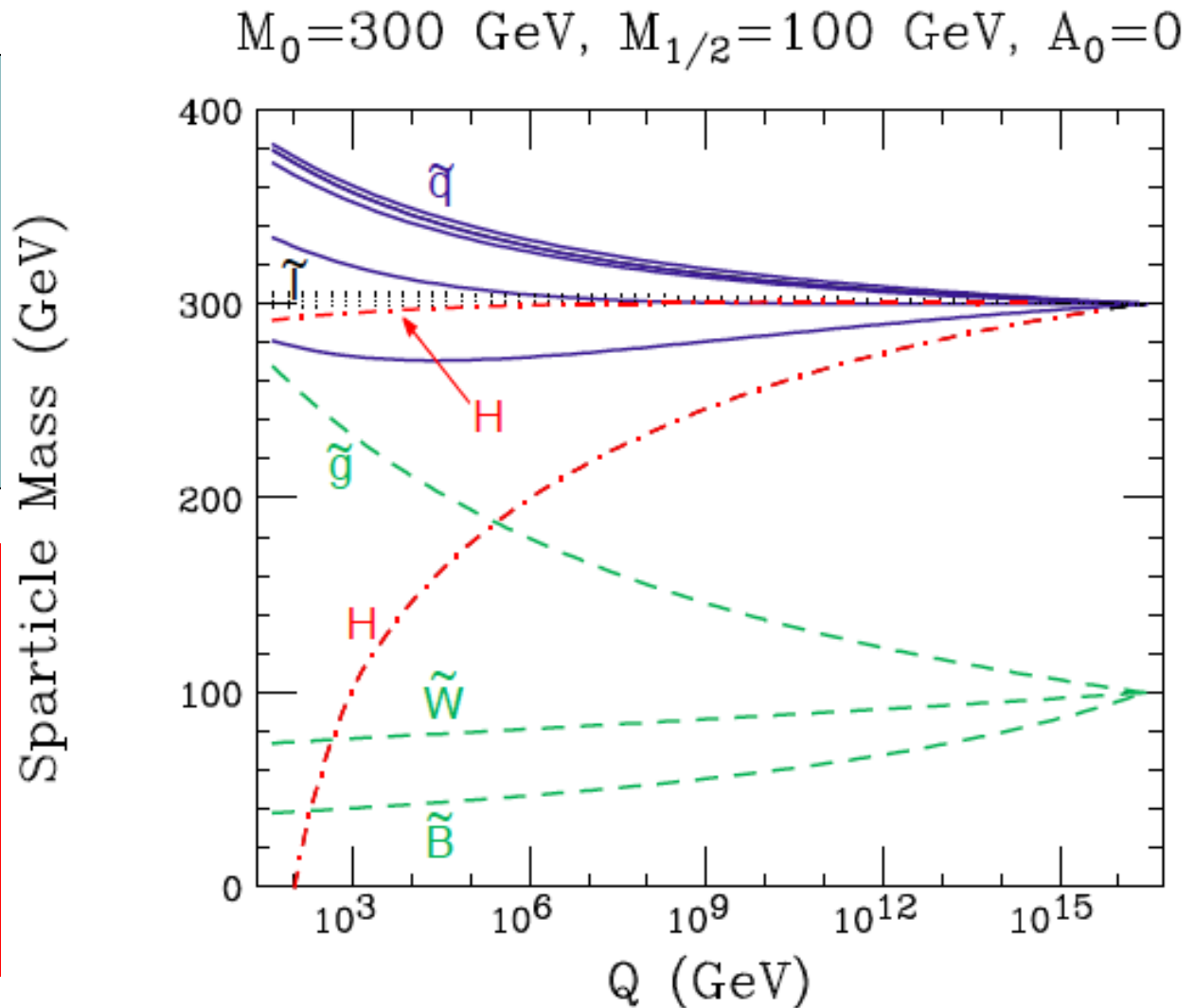
- Gluino heavier than photino, wino
- Squarks heavier than sleptons



Electroweak Symmetry Breaking

Could be driven by radiative corrections due to top quark

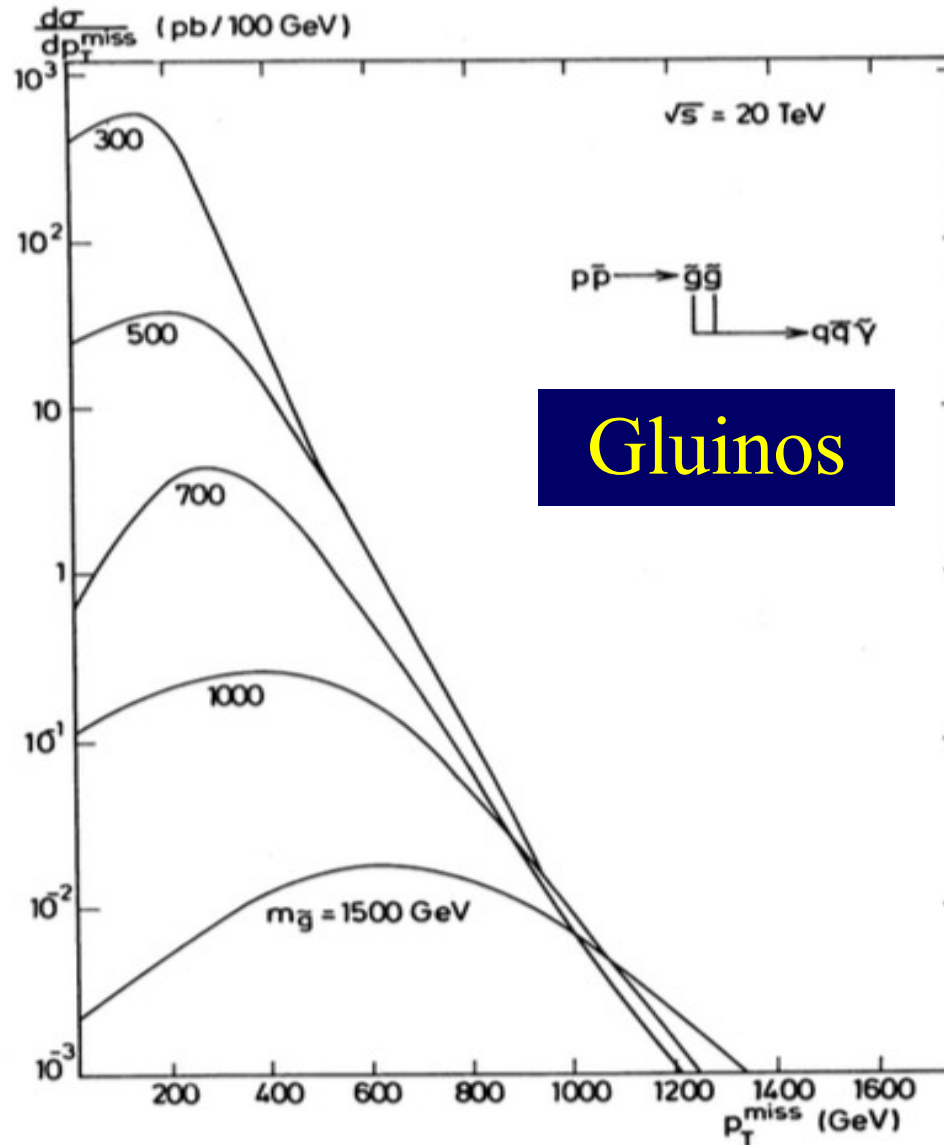
A bonus:
supersymmetry
may explain
why $\mu^2 < 0$



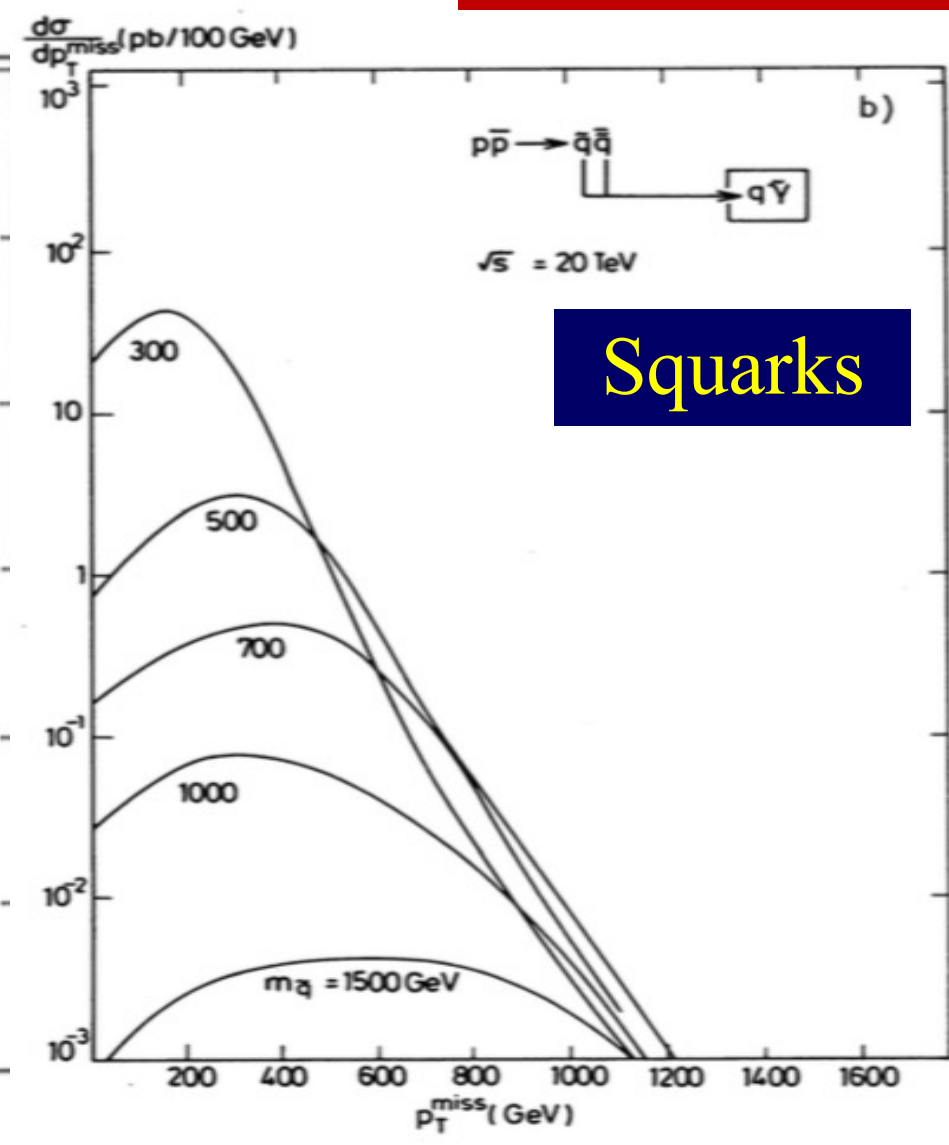
1984

A Preview of Supersymmetry @ LHC

JE, Gelmini & Kowalski, 1984



Gluinos

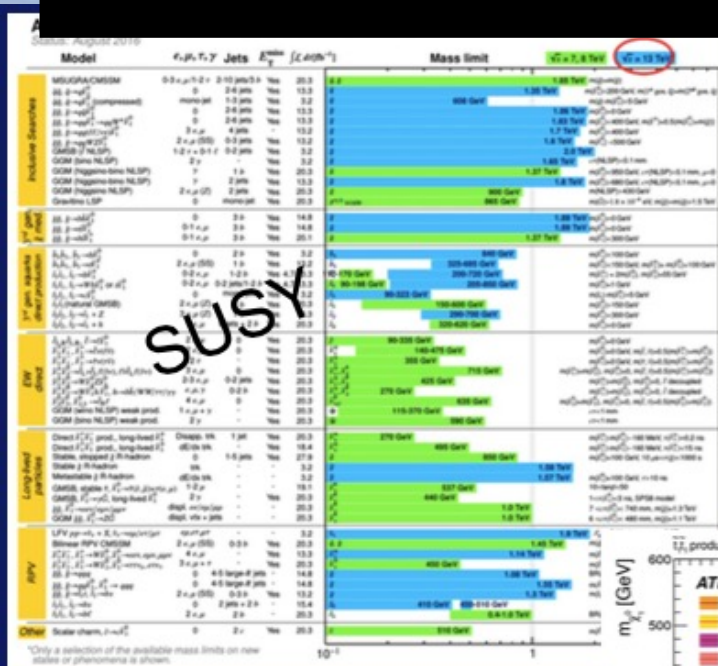


Squarks

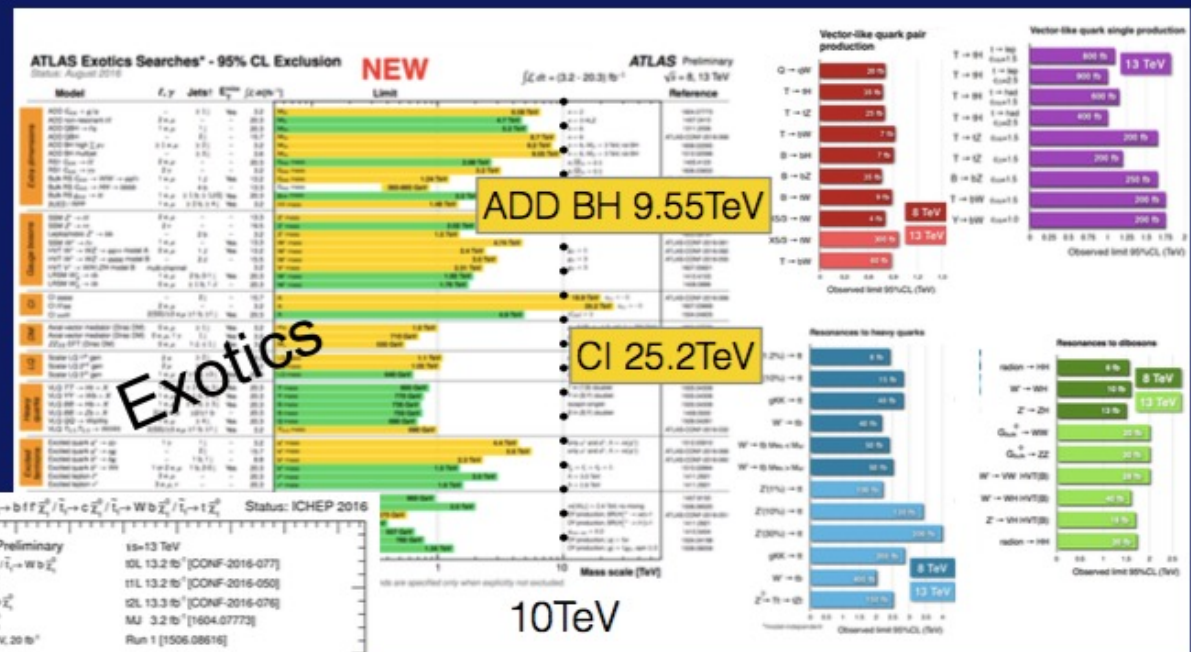
Nothing (yet) at the LHC

No supersymmetry

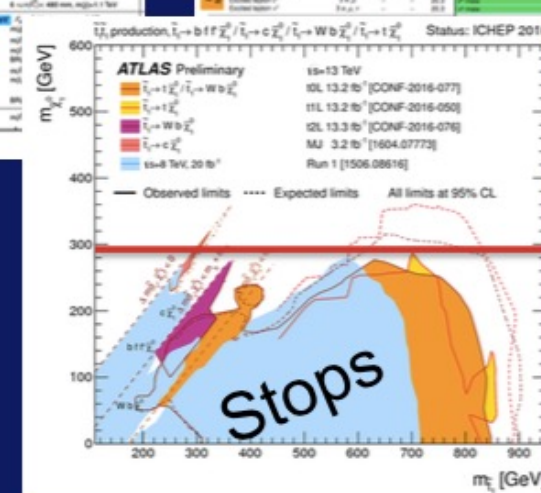
Nothing else, either



SUSY



Exotics



More of same?
Unexplored nooks?
Novel signatures?

Lightest Supersymmetric Particle

- Stable in many models because of conservation of R parity:

$$R = (-1)^{2S - L + 3B}$$

**where S = spin, L = lepton #, B =
baryon #**

- Particles have $R = +1$, sparticles $R = -1$:

Sparticles produced in pairs

Heavier sparticles \rightarrow lighter sparticles

- **Lightest supersymmetric particle (LSP) stable**

Lightest Sparticle as Dark Matter?

- No strong or electromagnetic interactions

Otherwise would bind to matter

Detectable as anomalous heavy nucleus

- Possible weakly-interacting candidates

Sneutrino

(Excluded by LEP, direct searches)

Lightest neutralino χ (partner of Z, H, γ)

Gravitino

(nightmare for detection)

The Dark Matter Hypothesis

- Proposed by Fritz Zwicky, based on observations of the Coma galaxy cluster
- The galaxies move too quickly
- The observations require a stronger gravitational field than provided by the visible matter
- **Dark matter?**



The Rotation Curves of Galaxies

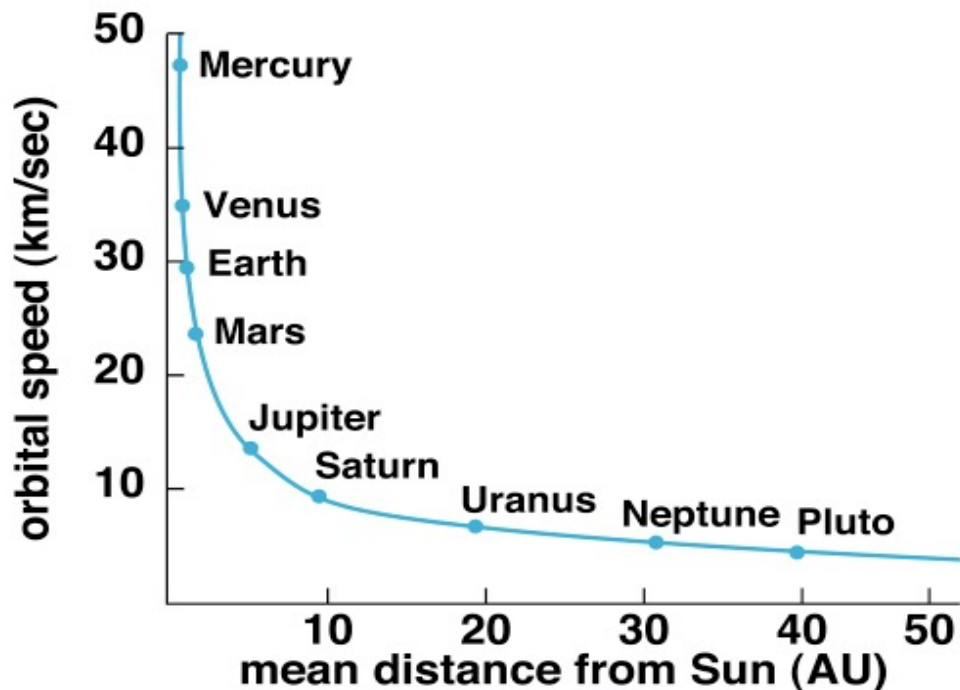
- Measured by Vera Rubin
- The stars also orbit ‘too quickly’
- Her observations also required a stronger gravitational field than provided by the visible matter
- **Further strong evidence for dark matter**
- Also:
 - Structure formation, cosmic background radiation, ...



Scanned at the American
Institute of Physics

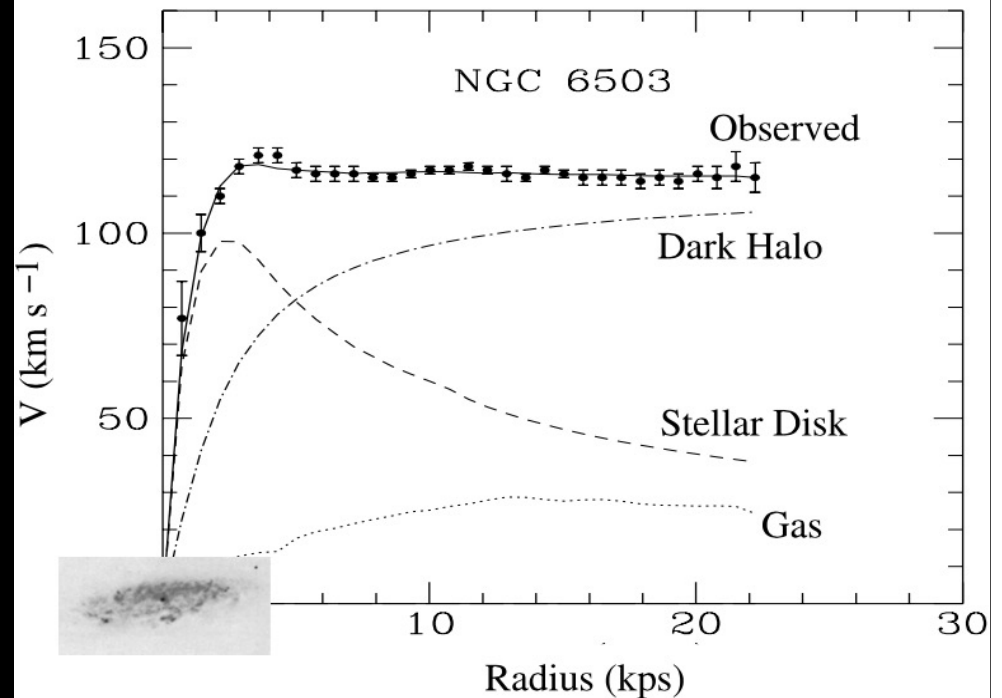
Galactic Rotation Curves

• In the Solar System



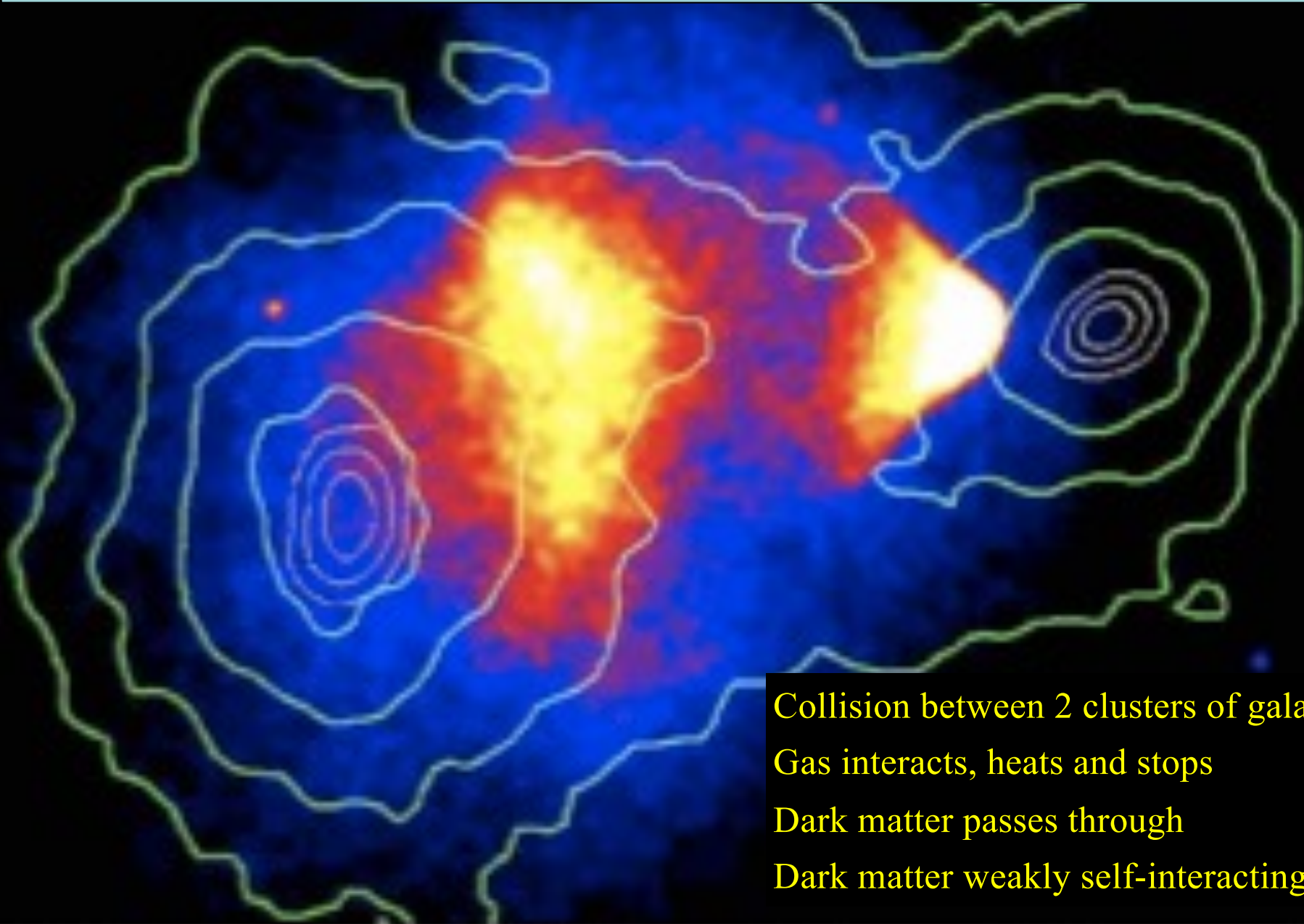
- The velocities decrease with distance from Sun
- Mass lumped at centre

• In galaxies



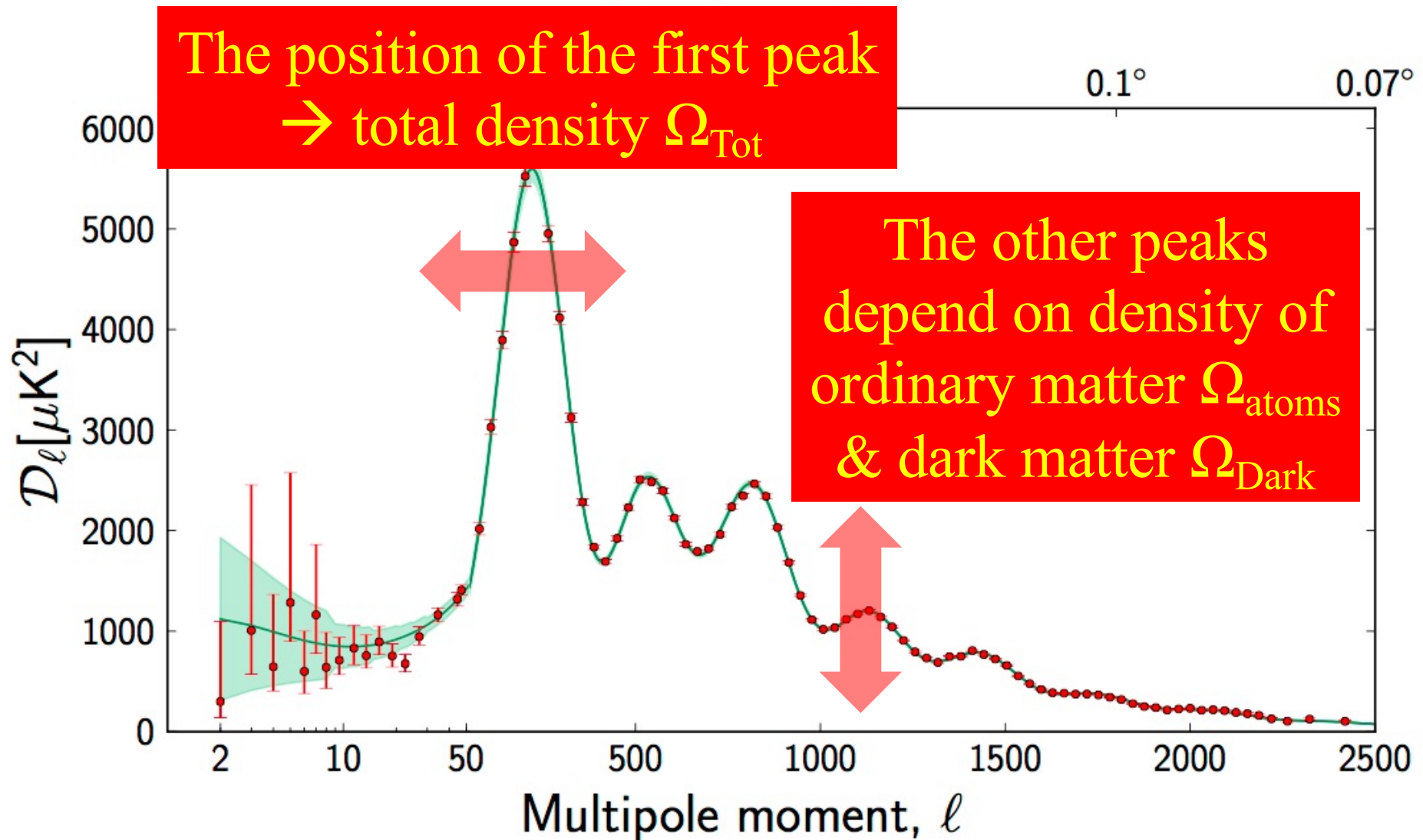
- The velocities do not decrease with distance
- Dark matter spread out

Biggest Collider in the Universe?



Collision between 2 clusters of galaxies:
Gas interacts, heats and stops
Dark matter passes through
Dark matter weakly self-interacting

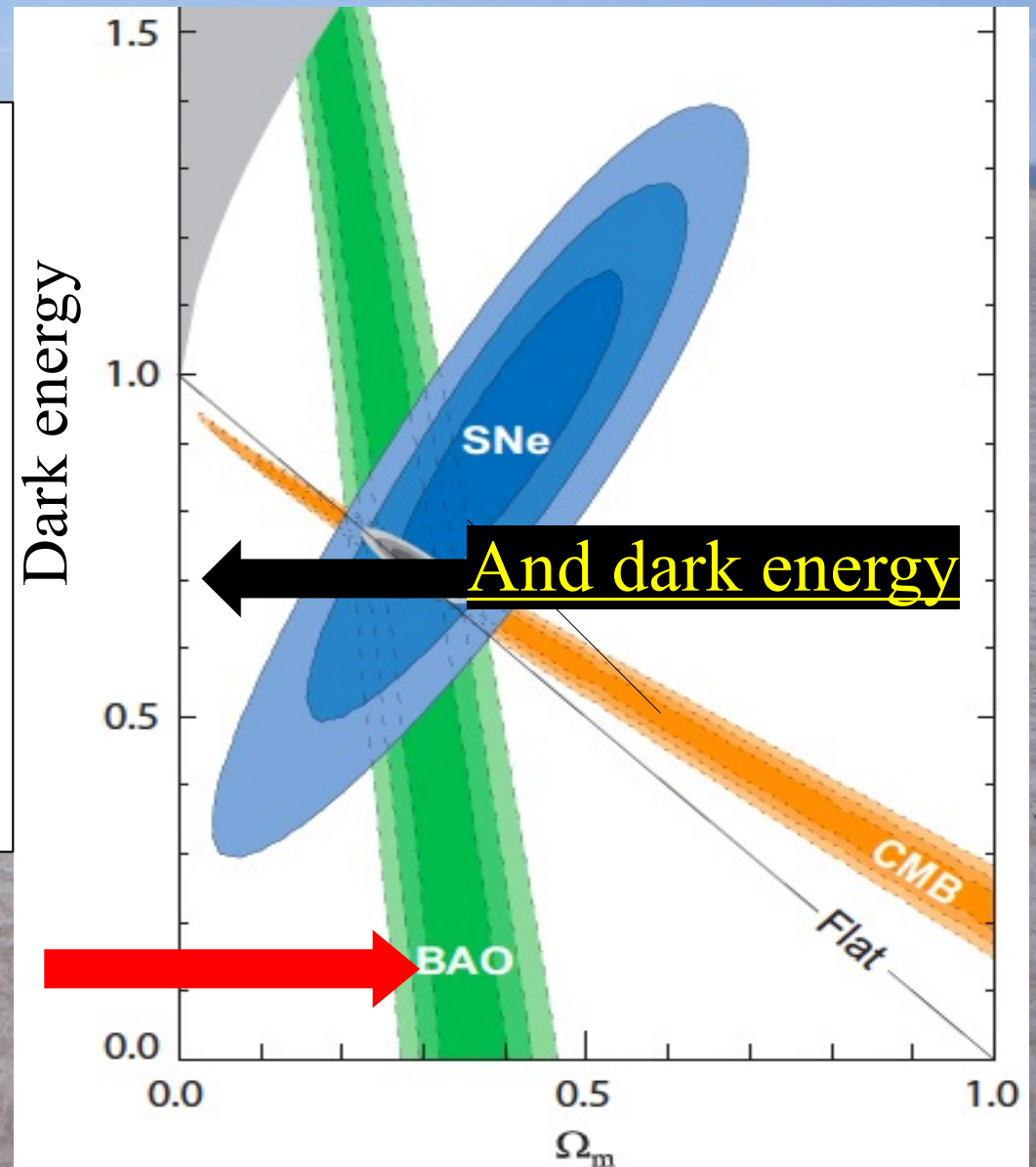
The Spectrum of Fluctuations in the Cosmic Microwave Background



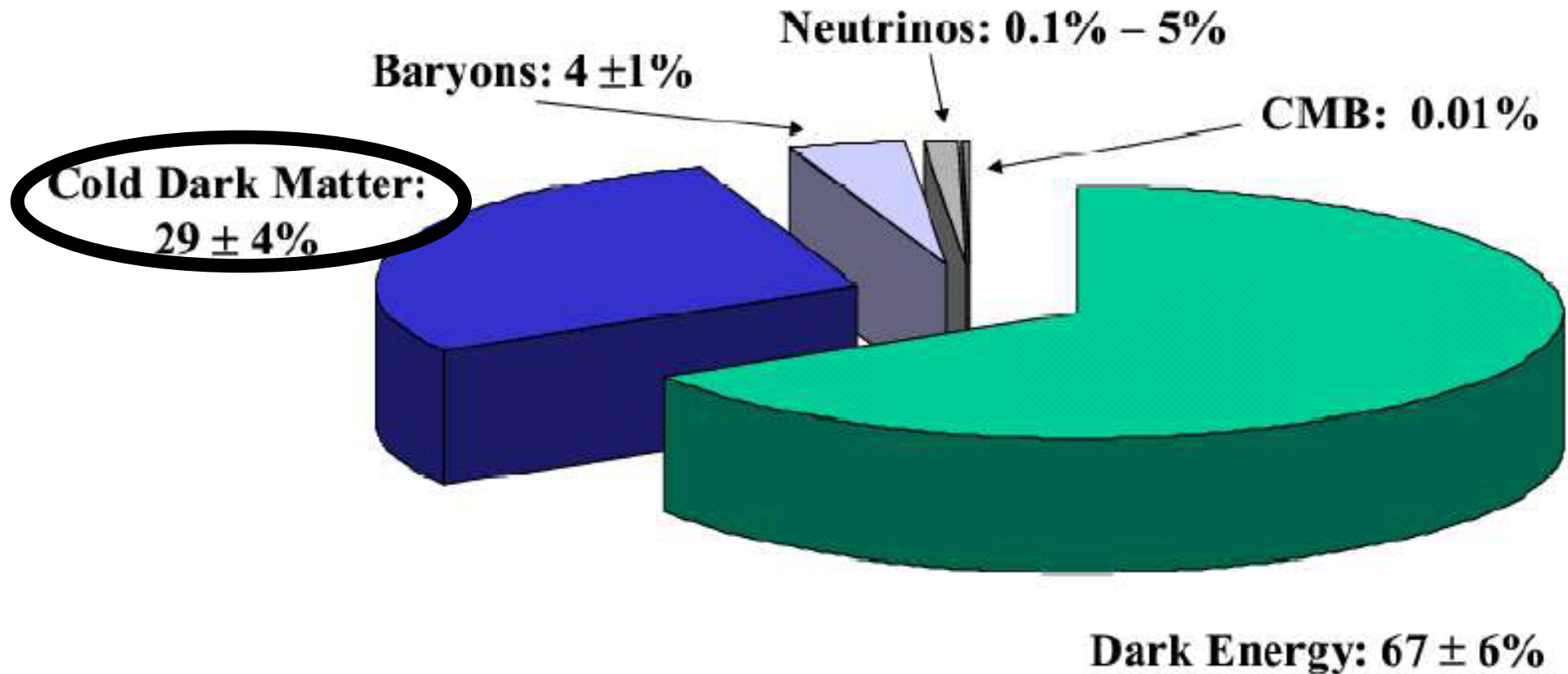
The Content of the Universe

- According to
 - Microwave background
 - Supernovae
 - Structures (galaxies, clusters, ...) in the Universe

There is dark matter



Strange Recipe for a Universe

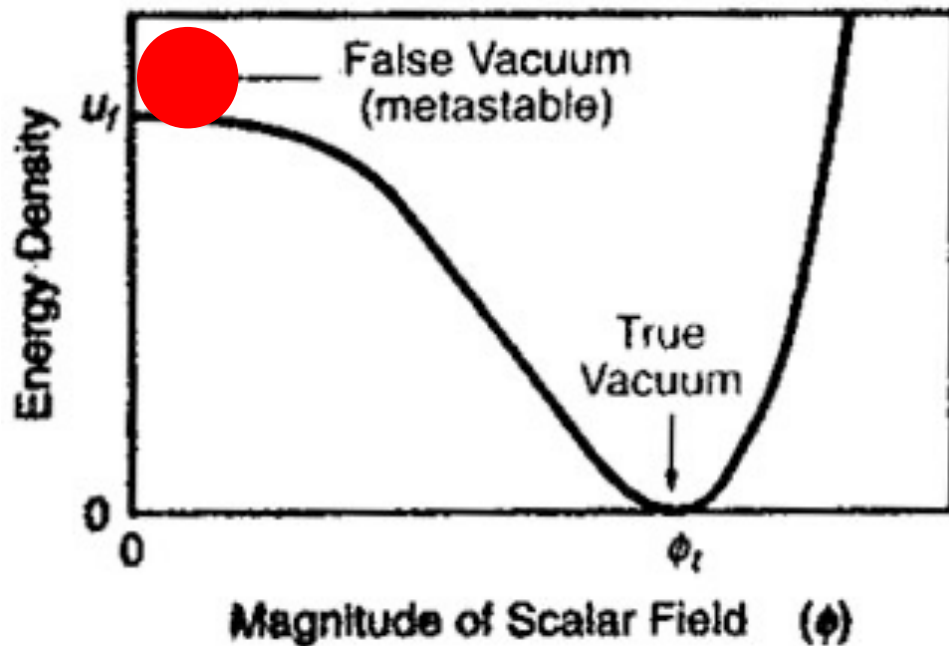


The 'Standard Model' of the Universe indicated by astrophysics and cosmology

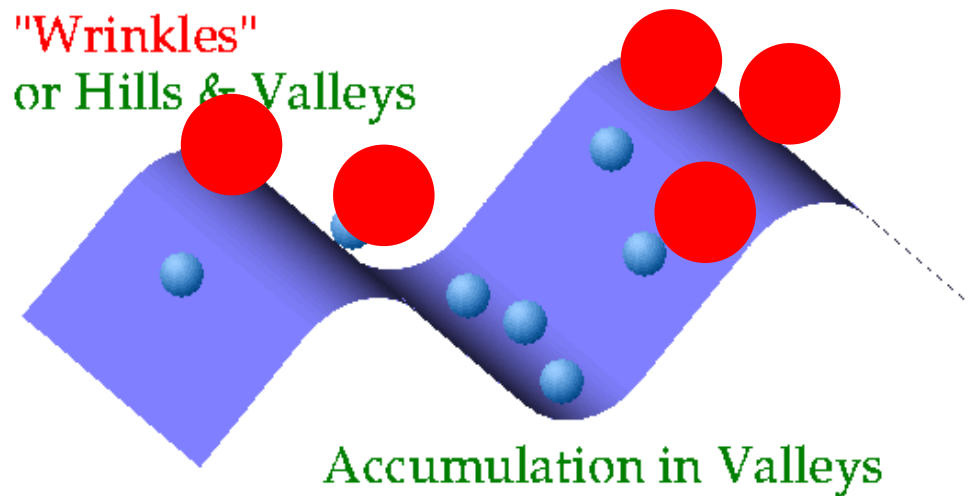
The Origin of Structures in the Universe

Small primordial
quantum fluctuations:
 $\sim 1/10^5$

Gravitational instability:
dark matter falls into the
gravitational potential wells,
visible matter follows



"Wrinkles"
or Hills & Valleys

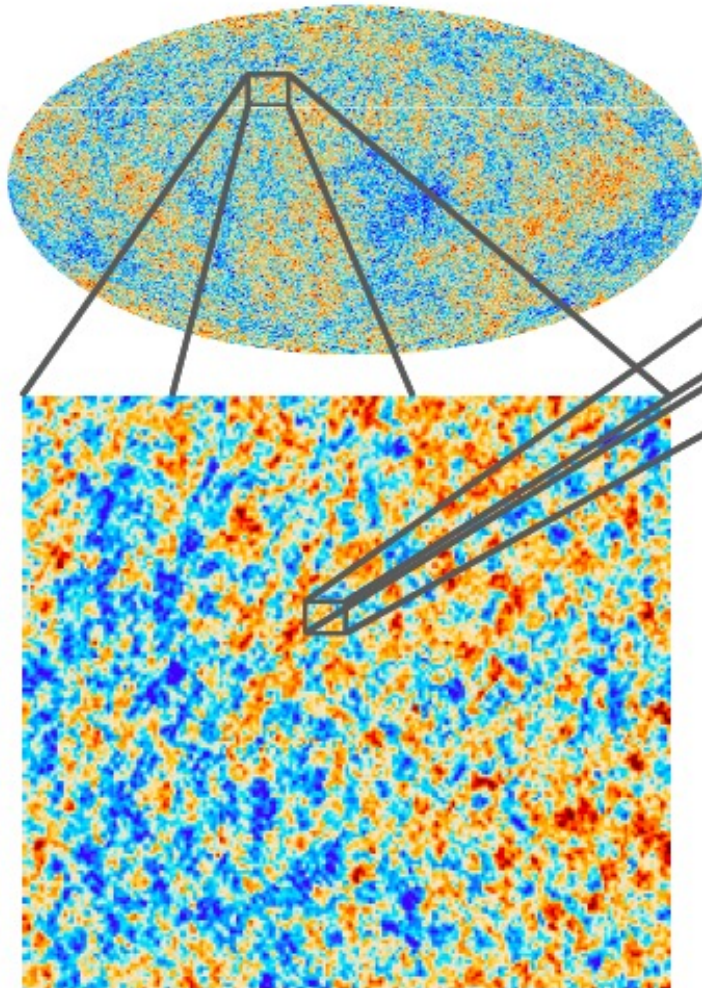


Become density fluctuations

Become structures in Universe

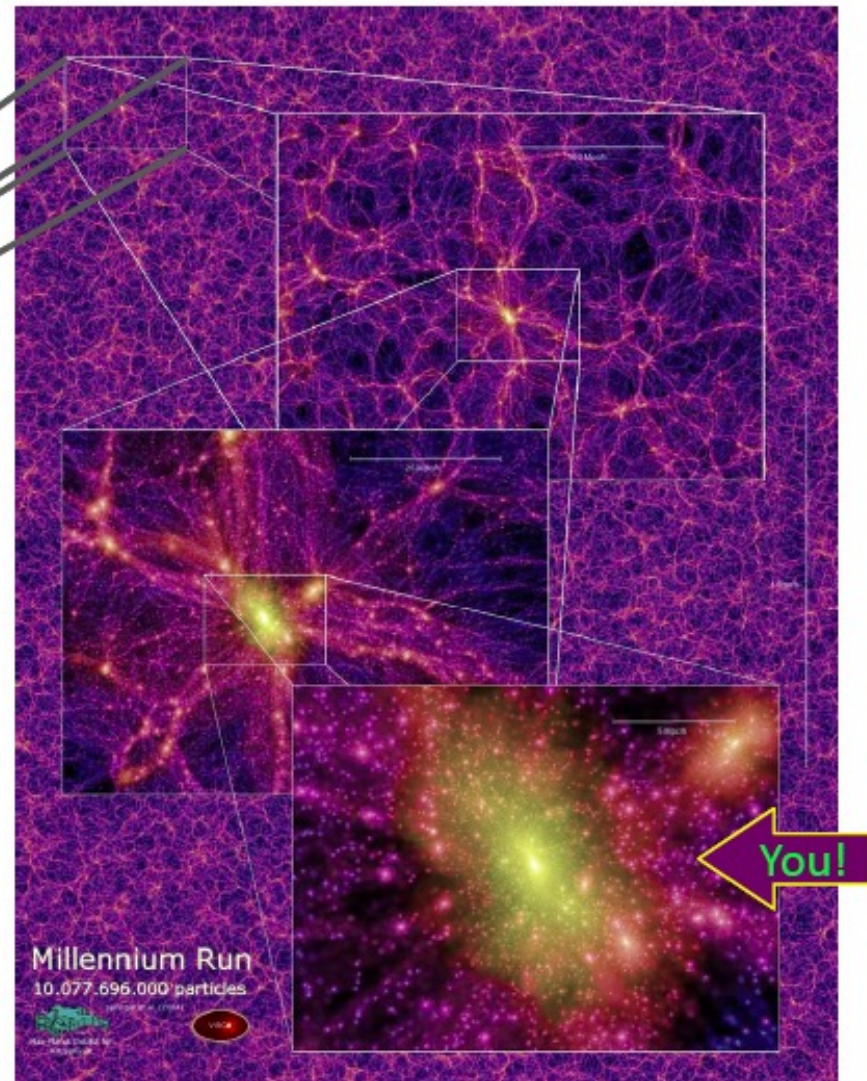
Dark Matter Generated Structures

Planck



Primordial quantum perturbations as seen in the Cosmic Microwave Background

Dark matter distribution today (simulated)



A Successful Theory of the Formation of Structures in the Universe

Dark matter:

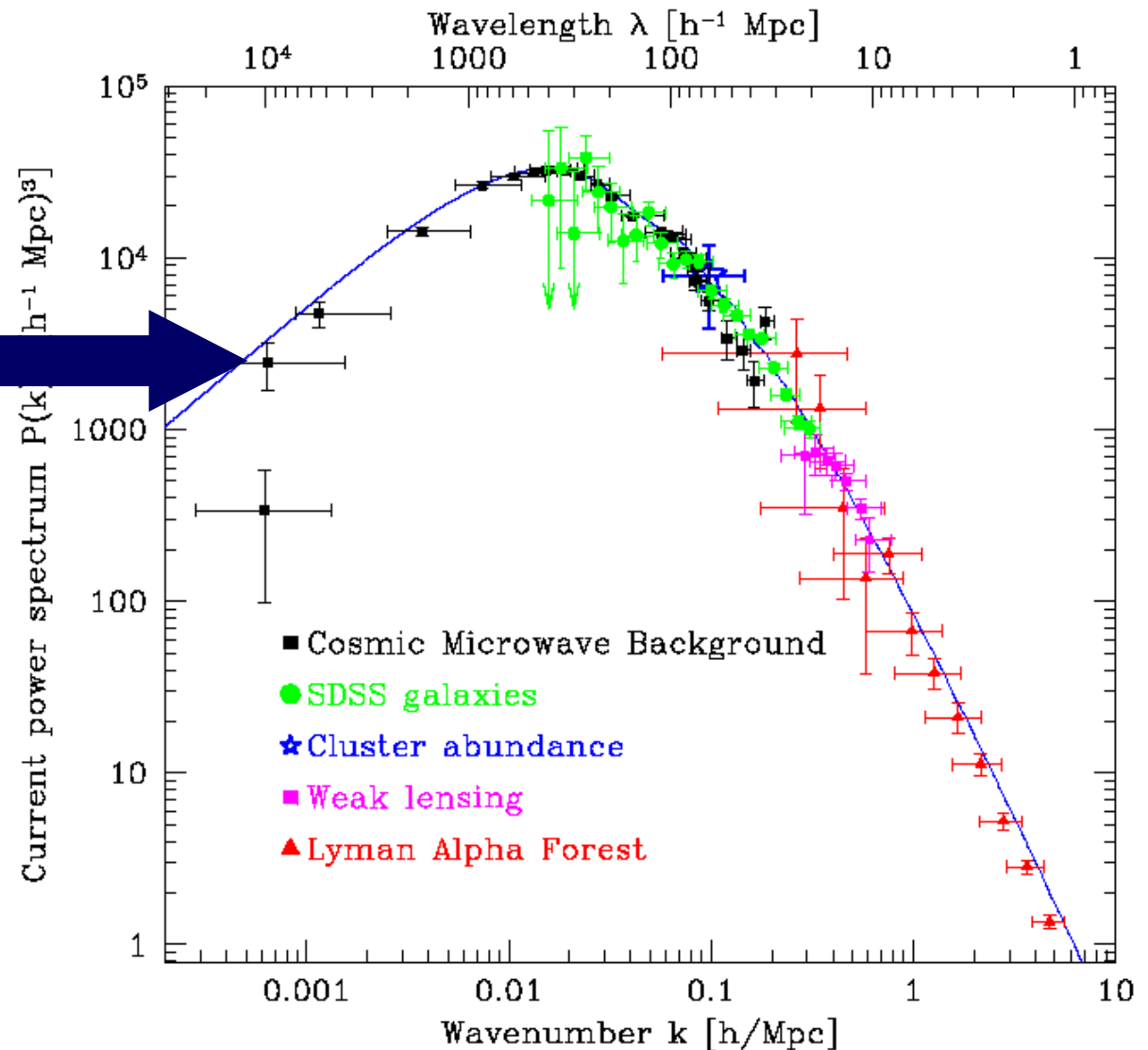
$$\Omega_{\text{CDM}} \sim 0.25,$$

Visible matter:

$$\Omega_b \sim 0.05,$$

Dark energy:

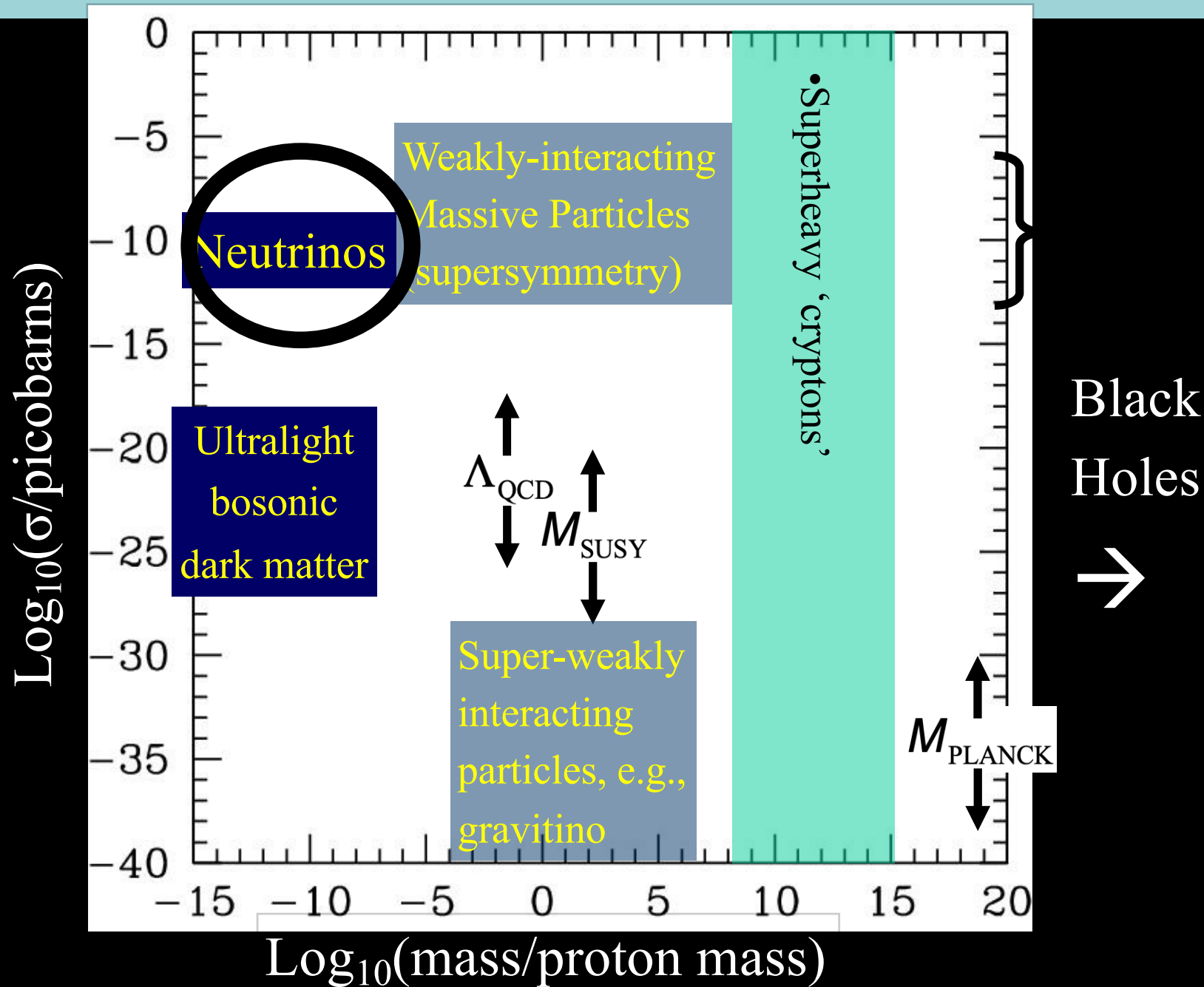
$$\Omega_\Lambda \sim 0.7$$



Properties of Dark Matter

- Should not have (much) electric charge
 - Otherwise we would have seen it
- Should interact weakly with ordinary matter
 - Otherwise we would have detected it, either directly or astrophysically
- Should not be too light
 - Needed for forming and holding together structures in the Universe: galaxies, clusters, ...

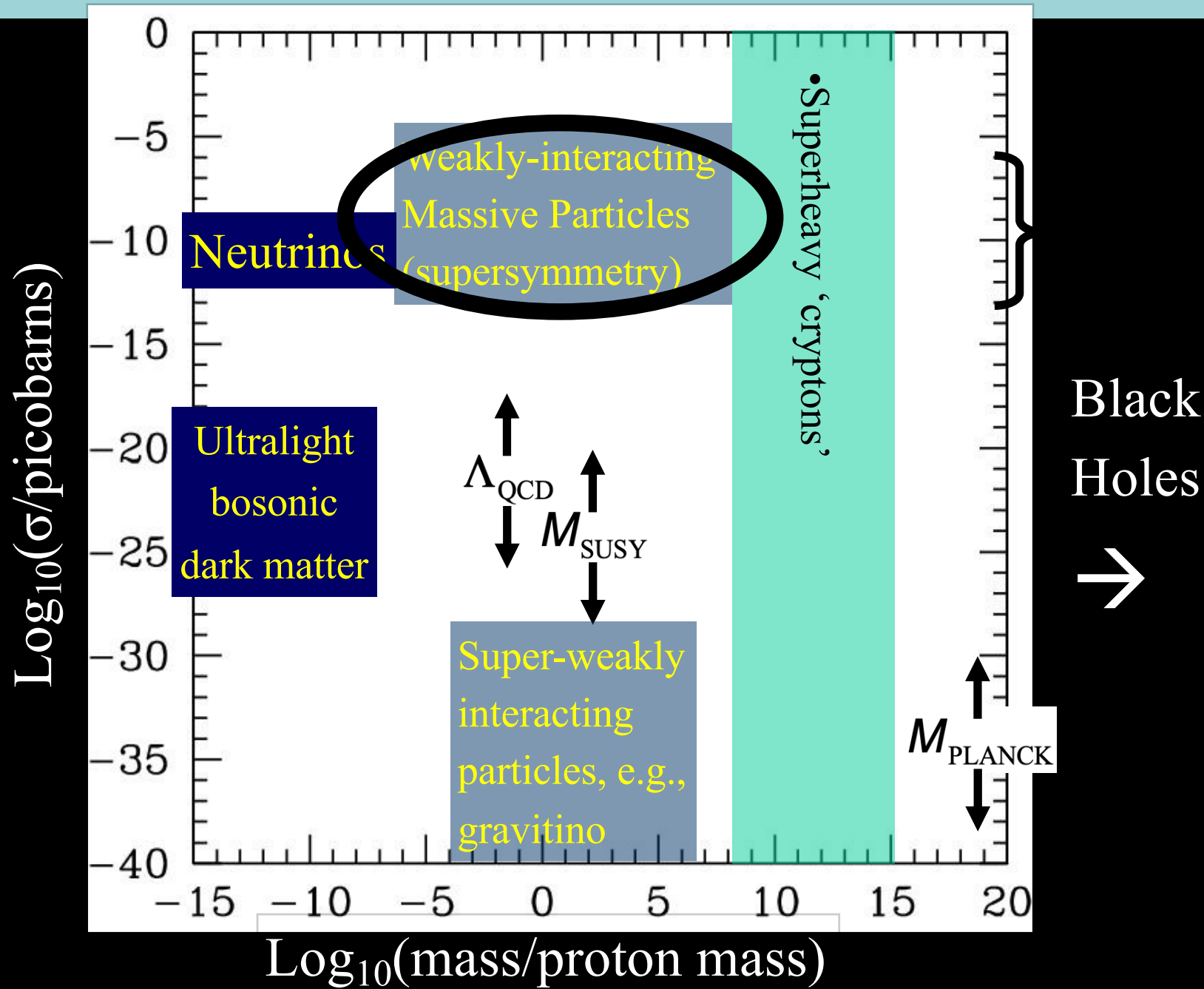
Particle Dark Matter Candidates



Neutrinos

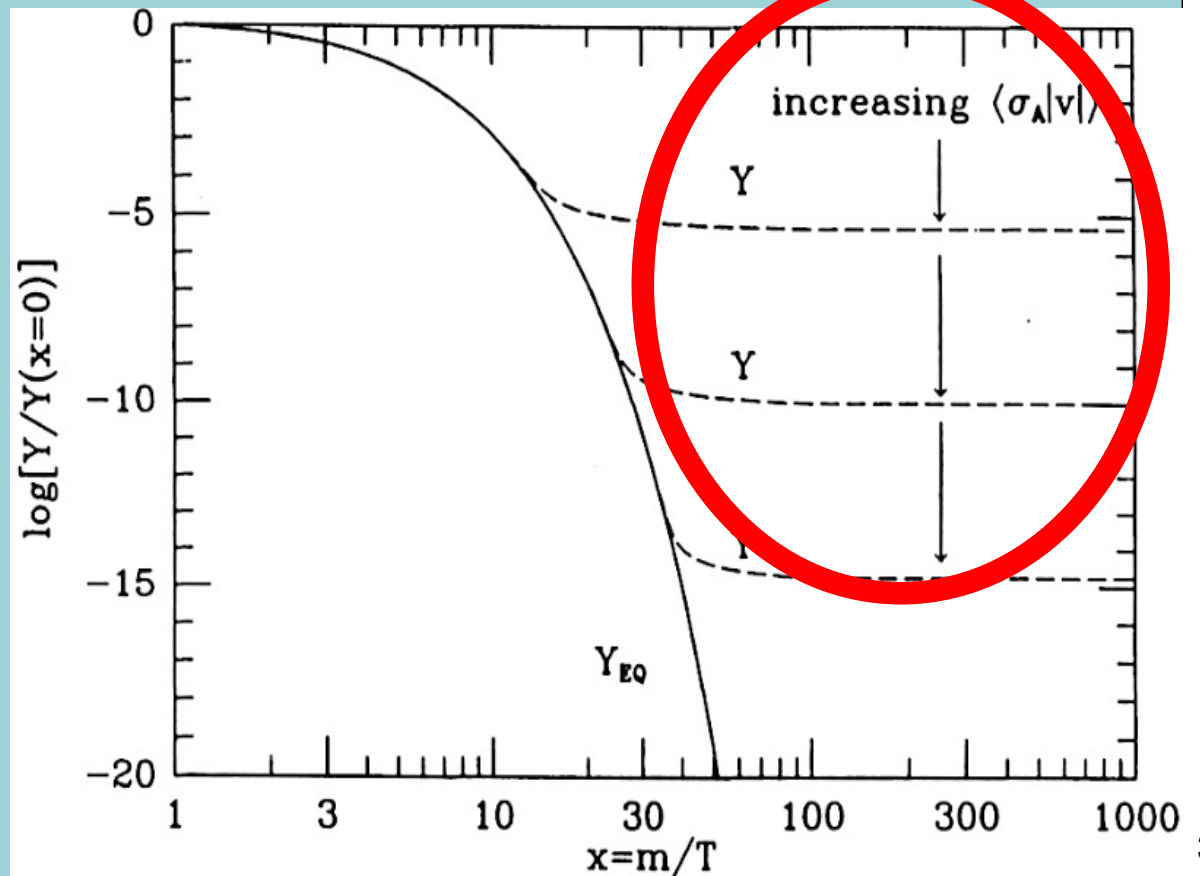
- They exist! 😊
- They have weak interactions 😊
- They have masses 😊
 - As indicated by neutrino oscillations
- But their masses are very small 😞
 - $< 1 \text{ eV}$ (= 1/1000,000,000 of proton mass)
- Not able to grow all structures in Universe 😞
 - (run away from small structures)
- Maybe some other neutrinos beyond the Standard Model?

Particle Dark Matter Candidates

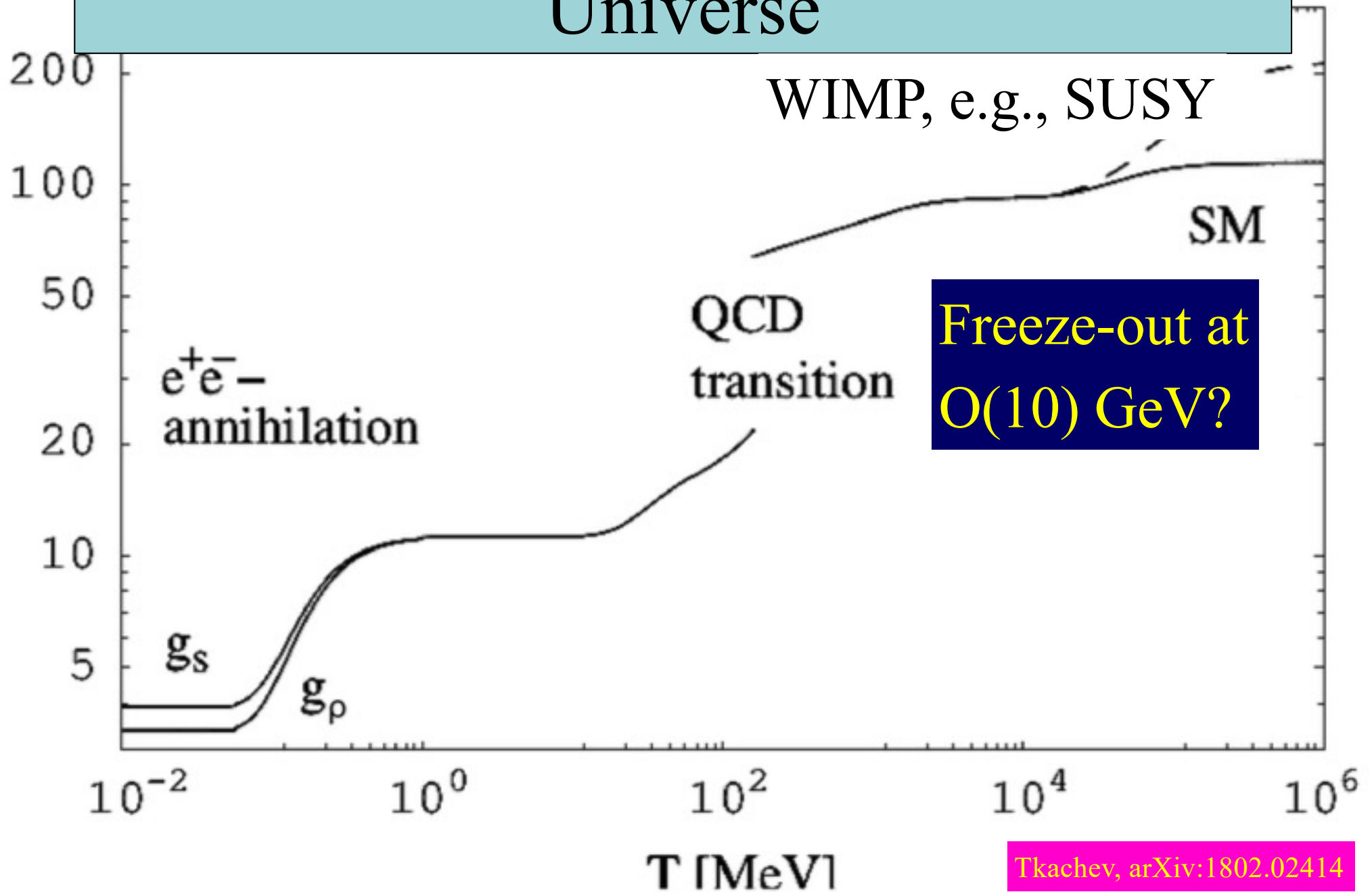


Weakly-Interacting Massive Particles (WIMPs)

- Expected to have been numerous in the primordial Universe when it was a fraction of a second old, full of a primordial hot soup
- Would have cooled down as Universe expanded
- Interactions would have weakened
- WIMPs decoupled from visible matter
- “Freeze-out”
- Larger $\sigma \rightarrow$ lower Y



'Standard' Thermal History of Early Universe



The WIMP 'Miracle'

- The TeV scale from cosmology:
- Generic density from freeze-out:

$$\text{TeV} \simeq \sqrt{M_{\text{Pl}} \times 2.7 \text{ K}}$$

$$\Omega_{\text{X}} h_0^2 \simeq \frac{1}{10^3 \langle \sigma v \rangle} \frac{1}{M_{\text{Pl}} \times 2.7 \text{ K}} \simeq \frac{1}{10^3 \langle \sigma v \rangle} \frac{1}{\text{TeV}^2}$$

- Generic annihilation cross-section:

$$\sigma v \simeq \frac{c \alpha^2}{m^2}$$

$$m \simeq \sqrt{M_{\text{Pl}} \times 2.7 \text{ K}} \cdot 16 \alpha \sqrt{C} \sqrt{\frac{\Omega_{\text{X}} h_0^2}{0.25}}$$

- Generic relic mass:

$$\simeq \text{TeV} \cdot 16 \alpha \sqrt{C} \sqrt{\frac{\Omega_{\text{X}} h_0^2}{0.25}}$$

- Putting the numbers in:

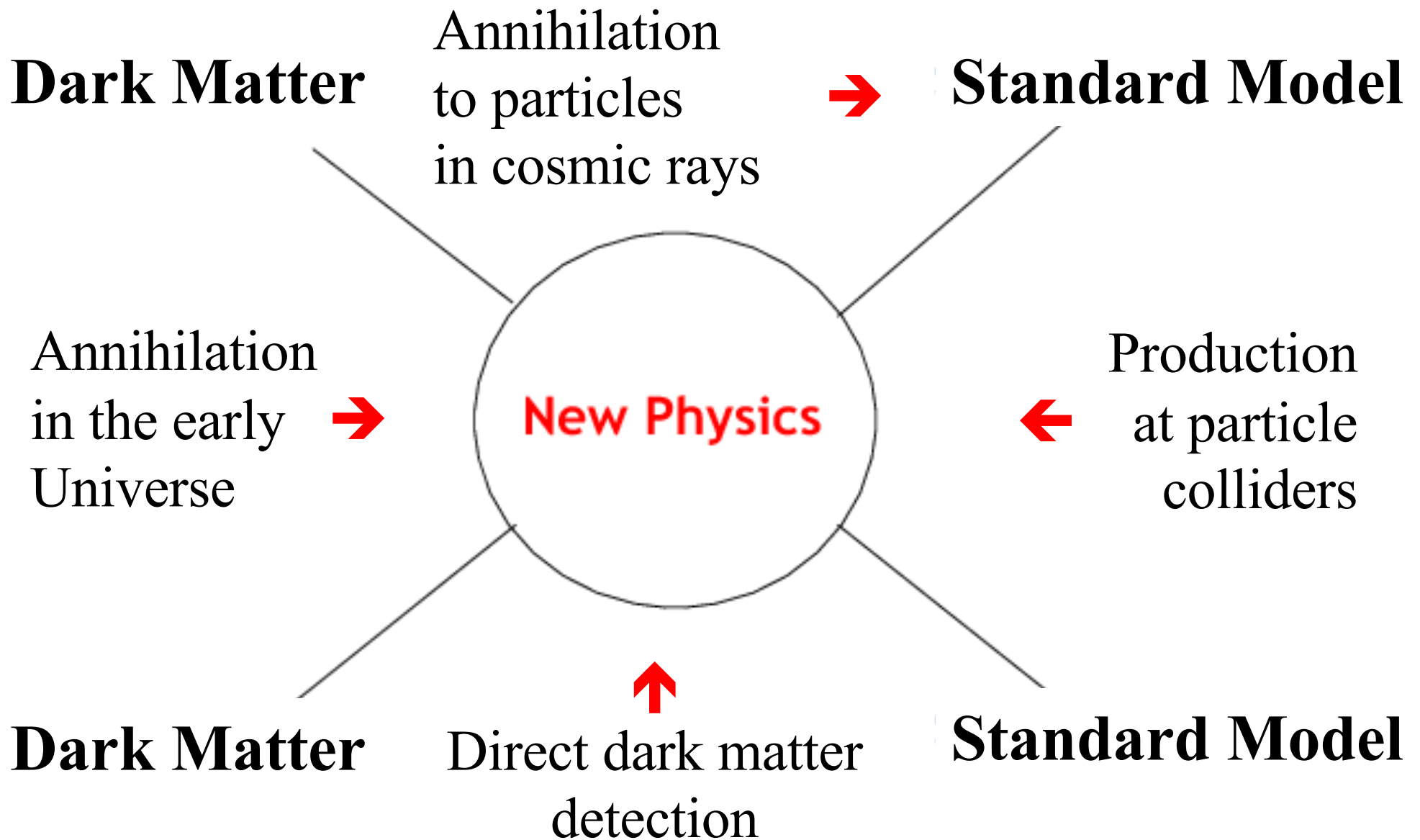
$$m \lesssim \frac{1}{2} \sqrt{10C} \text{ TeV} \lesssim 5 \text{ TeV}$$

WIMP Candidates

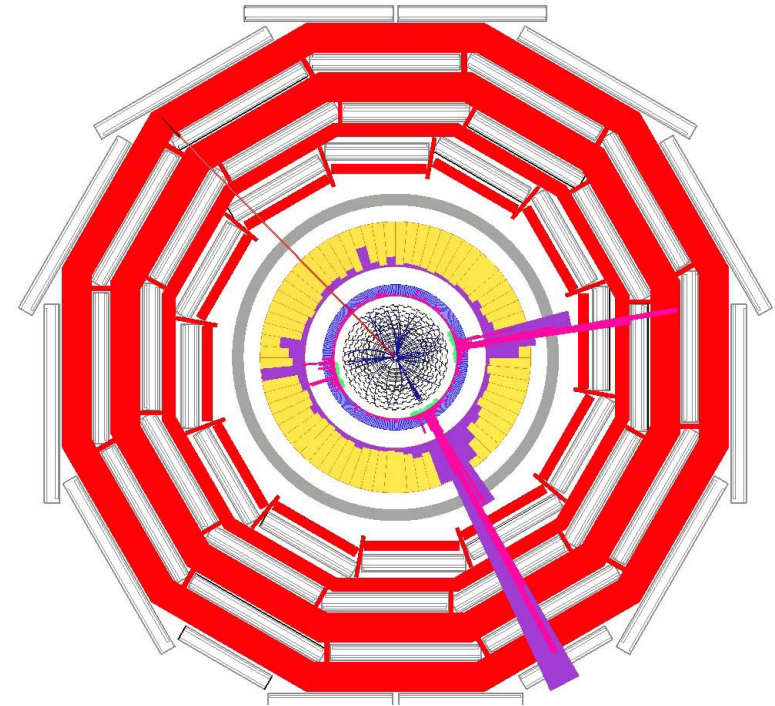
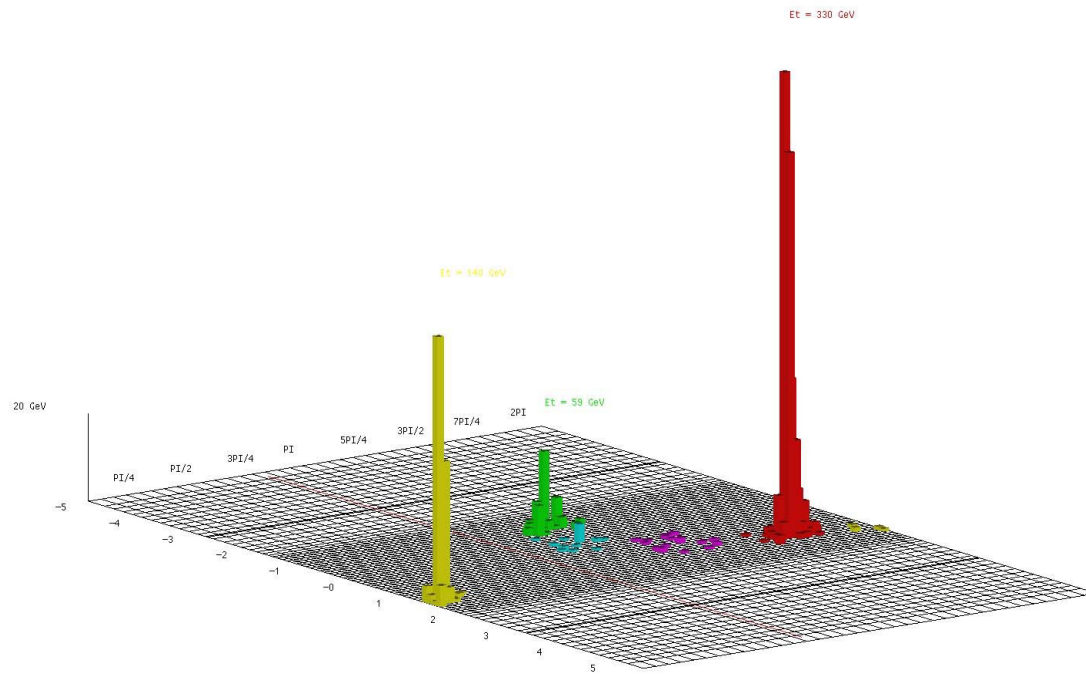
- Could have right density if weigh 100 to 1000 GeV (accessible to LHC experiments?)
- Present in many extensions of Standard Model
- Particularly in attempts to understand strength of weak interactions, mass of Higgs boson
- Examples:
 - Extra dimensions of space
 - **Supersymmetry**



Searches for Dark Matter



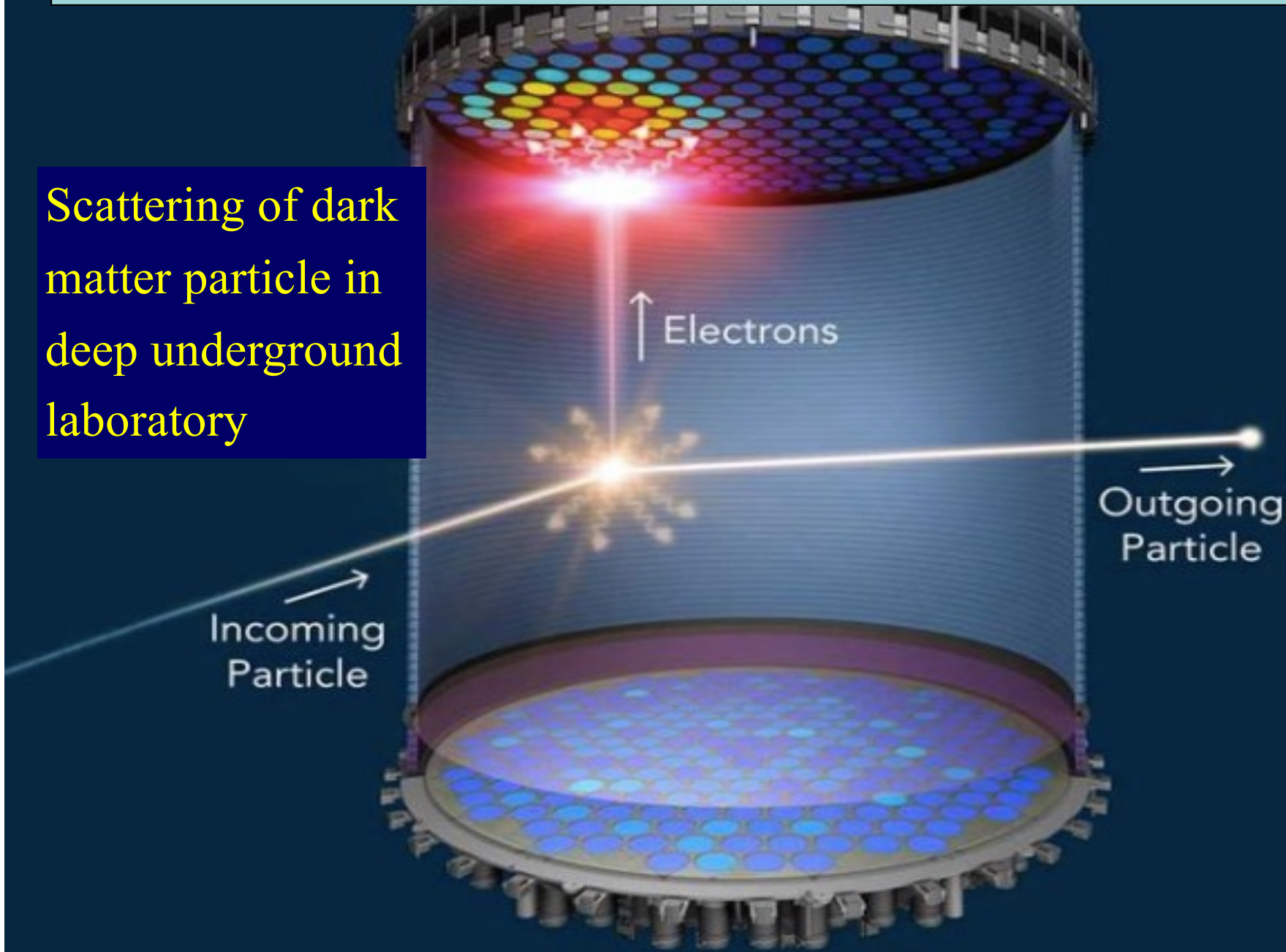
Classic Dark Matter Signature



Missing transverse energy
carried away by dark matter particles

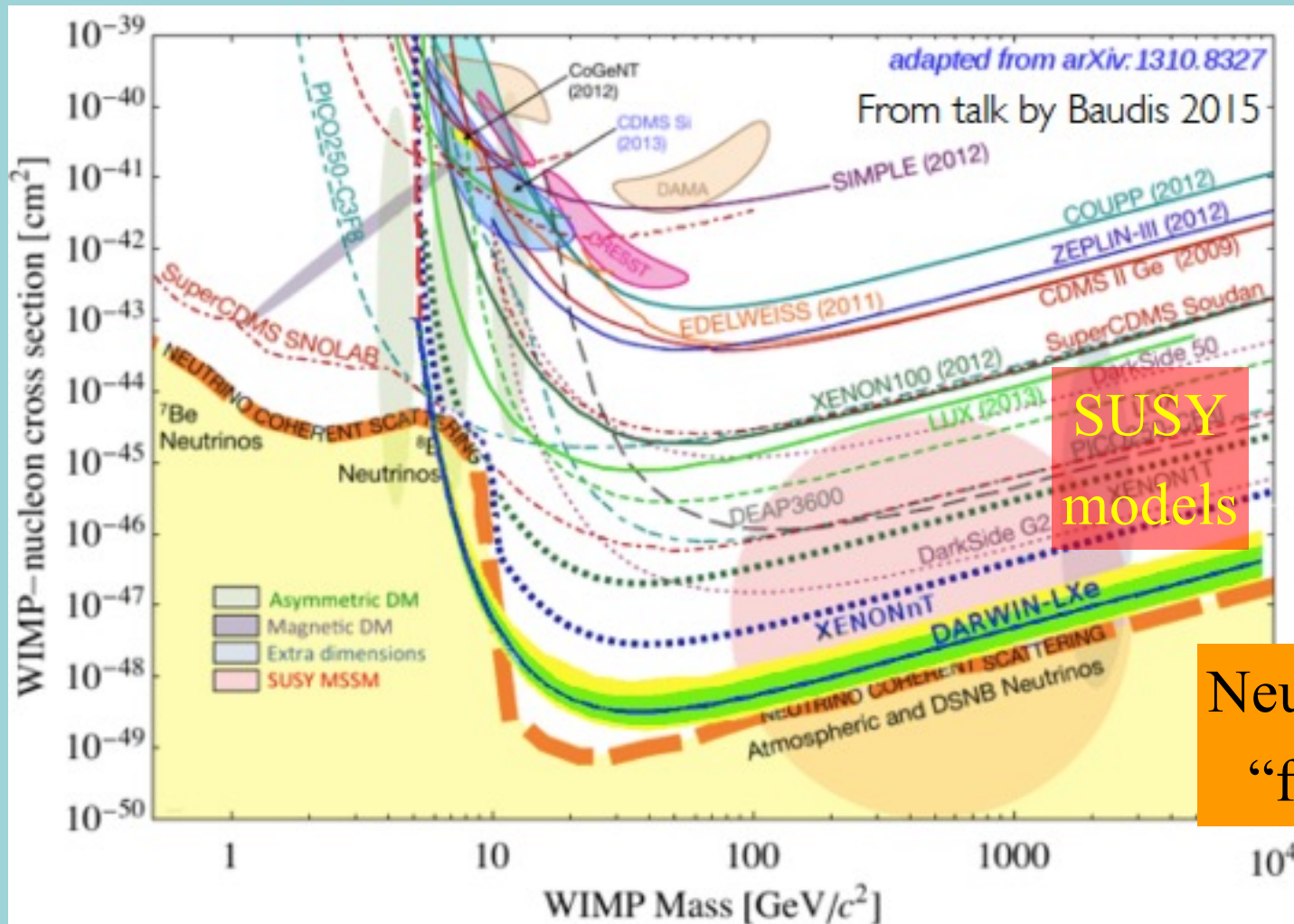
Direct Dark Matter Detection

Scattering of dark matter particle in deep underground laboratory



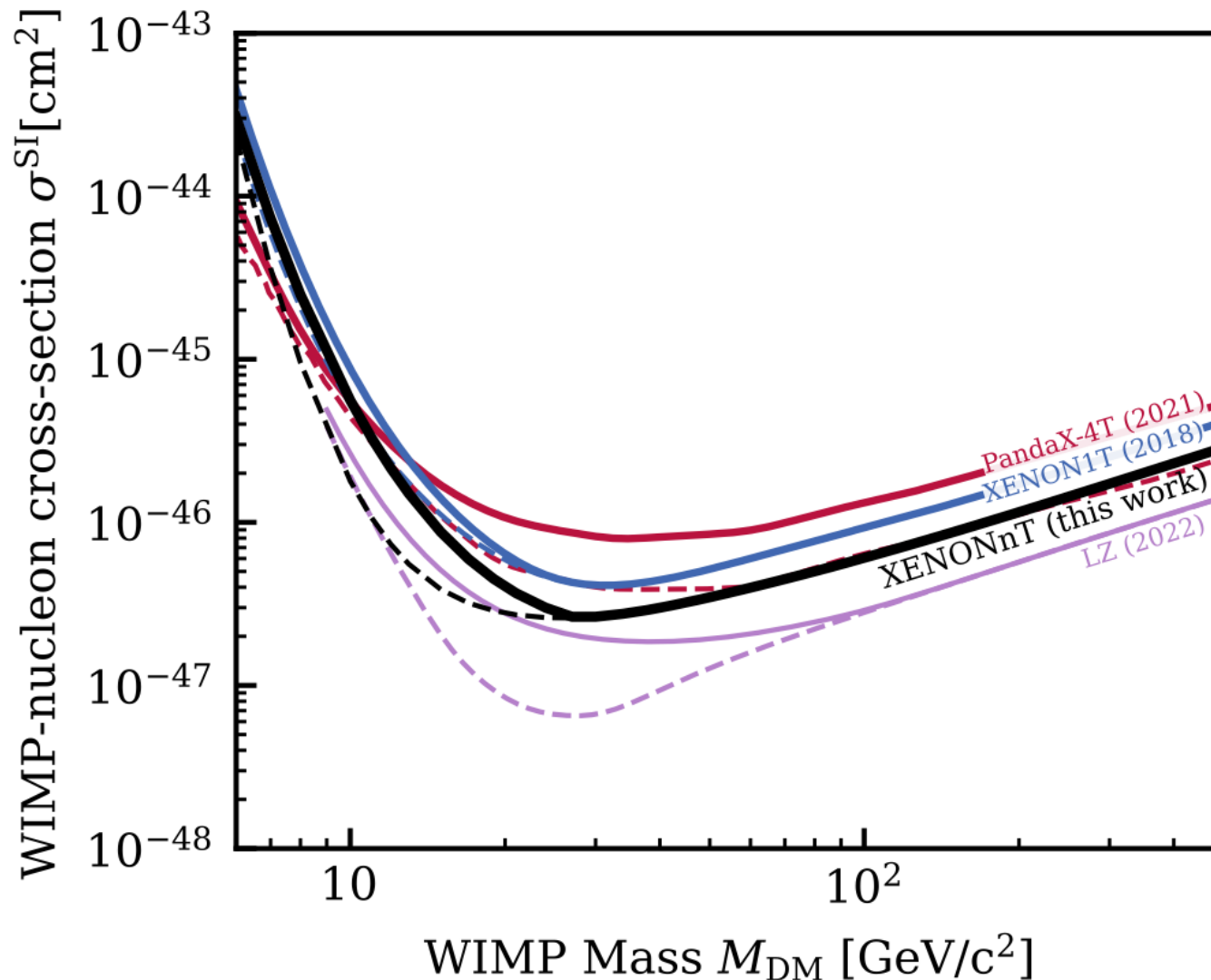
Direct Dark Matter Searches

- Compilation of present and future sensitivities



Direct Dark Matter Searches

- Latest experimental results





We still believe in supersymmetry

You must be joking