



McGill

Based on work with [Wei Xue](#) and [Jim Cline](#)

arXiv:1001.5399

arXiv:1009.5383

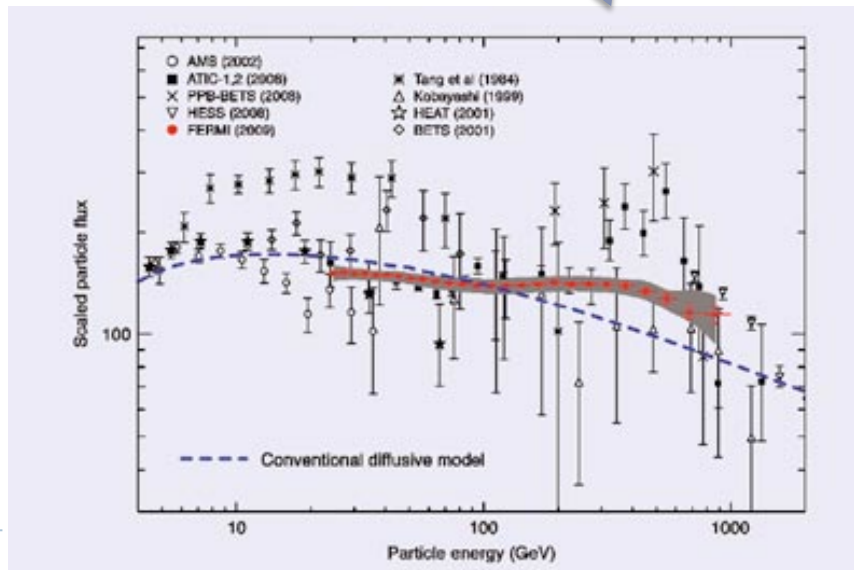
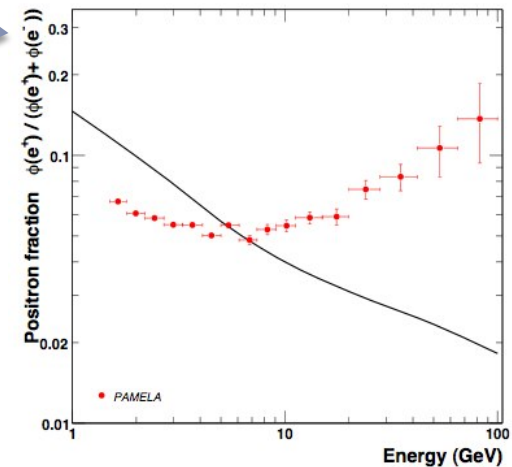
Cosmic Ray Anomalies, Gamma Ray Constraints and Subhalos in Models of Dark Matter Annihilation

Aaron C. Vincent

McGill University

Motivation

- ▶ Cosmic ray “anomalies”:
 - ▶ PAMELA positron fraction
 - ▶ ATIC Fermi electron + positron data

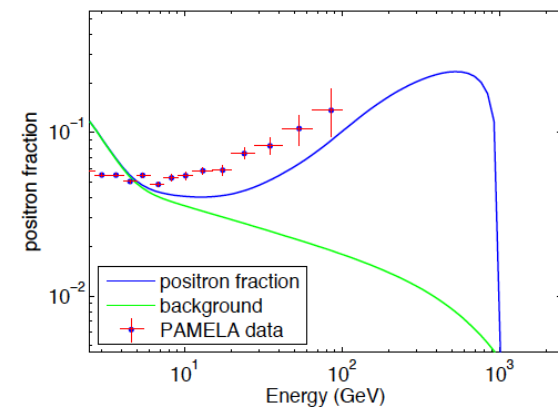
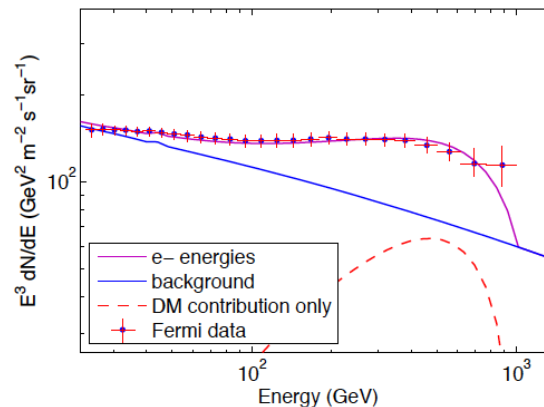
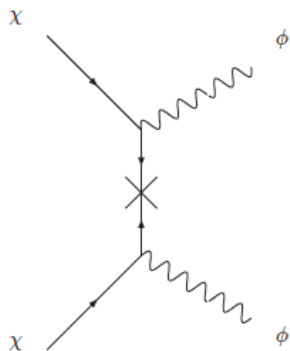


Dark matter annihilation

- ▶ These phenomena have no known astrophysical origin (could be pulsars?)
- ▶ Most promising scenario: a $M = 1 \text{ TeV}$ WIMP, annihilating to electrons and positrons via some intermediate gauge boson ϕ lighter than $2m_{\text{proton}}$ (Investigated by many authors). Requires some boost factor BF:

$$\langle \sigma v \rangle = \text{BF} \times 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

- ▶ Two issues:
 - ▶ This assumes a smooth central halo. What about **substructure**?
 - ▶ Where there are high energy electrons, there are **gamma rays**. These are particularly troublesome in the GC. Can we lower their flux?



Why substructure is interesting

- ▶ Numerical simulations of DM universally predict a large number of local overdensities within the main dark matter halo, extending far beyond the baryonic component of the galaxy.
- ▶ These subhalos can augment dark matter **annihilation into leptons** in two ways:
 - ▶ I. Larger local density
 - ▶ II. Small velocities mean large boosts in Sommerfeld-enhanced models.
- ▶ Other studies: subhalos as a source of gamma rays (to constrain models), but not necessarily as sources for the PAMELA and Fermi leptons themselves.



GALPROP and Via Lactea II

- ▶ The [diffusion eq. for e+e-](#) was solved numerically using the public [GALPROP](#) (Strong & Moskalenko, some mods from I. Cholis & ourselves)

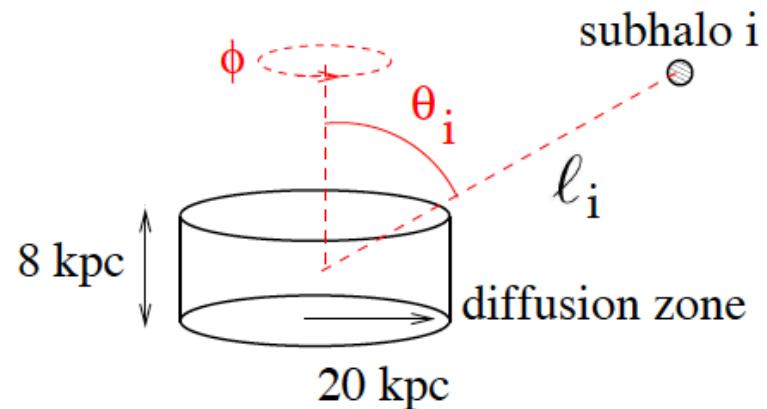
- ▶ **Source Terms**

- ▶ **Main Halo:**
$$\rho_{\text{Ein}}(r) = \rho_s \exp \left\{ -\frac{2}{\alpha} \left[\left(\frac{r}{r_s} \right)^\alpha - 1 \right] \right\}$$

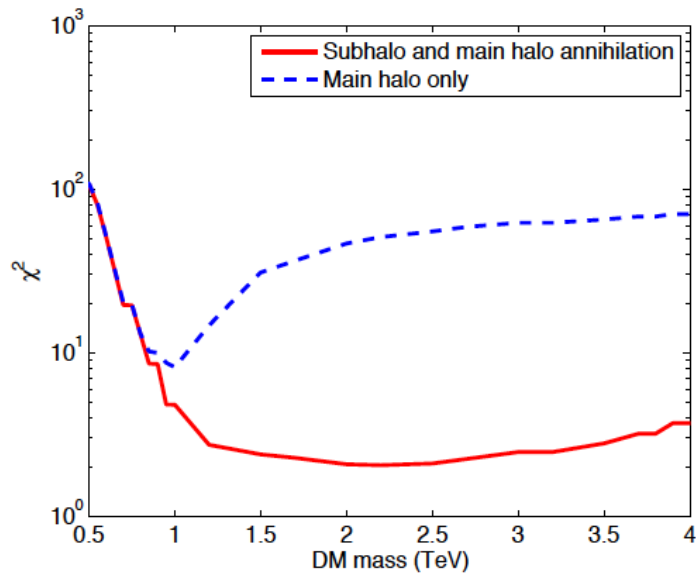
- ▶ **Subhalos:** Used results from the [Via Lactea II](#) N-body simulation (about 20 000 “typical subhalos”)

- ▶ **By adding a contribution from the large amount of substructure, can we get a better fit to the data while reducing the gamma ray constraints from the galactic center?**

- ▶ Yes we can!



Numerical results 1: Adding subhalos means a better fit to the data



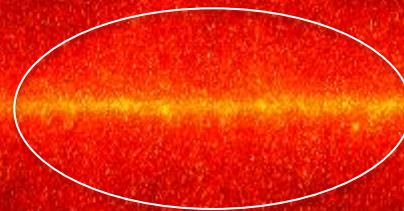
Better fit to PAMELA and Fermi with 2.2 TeV WIMP when subhalos are included
Larger mass is because of larger propagation distance – energy loss to Inverse Compton scattering with CMB, IR and Starlight

(4e final state. Going to a larger gauge boson mass allows mu and pi production, but results are ostensibly the same)



Gamma Rays

- ▶ Best DM annihilation models predict much larger gamma ray fluxes near the galactic center (GC) from Final-state radiation (Bremsstrahlung) and Inverse Compton Scattering (ICS)
- ▶ Fermi Large Area Telescope measured gamma rays from the entire sky in the exact range we're interested in (10-300 GeV)



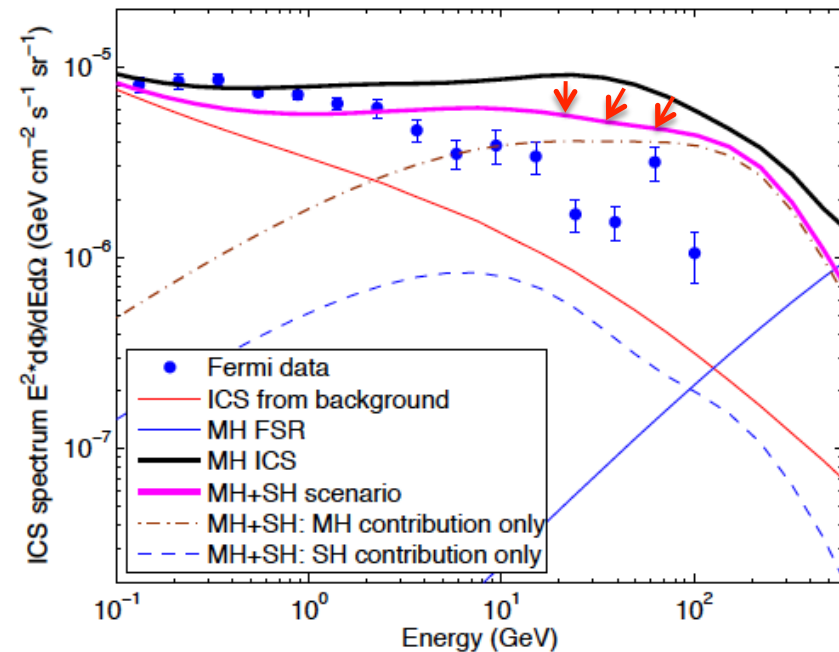
Most constraints come from inverse compton scattering (ICS) here

- ▶ We used the first year of Fermi LAT diffuse gamma ray (Aug 8 2008 to Aug 25 2009) data available from NASA to constrain the allowable DM annihilation
- ▶ Error estimates are from Porter et al. 2009

Numerical Results II: Gamma rays

- ▶ Unfortunately adding subhalos and still explaining PAMELA and Fermi only slightly reduces the gamma ray constraints.
- ▶ Issue: DM is still in the galactic center, annihilating.

- ▶ The DM **profile** (Einasto vs Isothermal, Burkert) and the **final state** (4e, 4 mu, pi, e) have some impact on this, but **not enough**



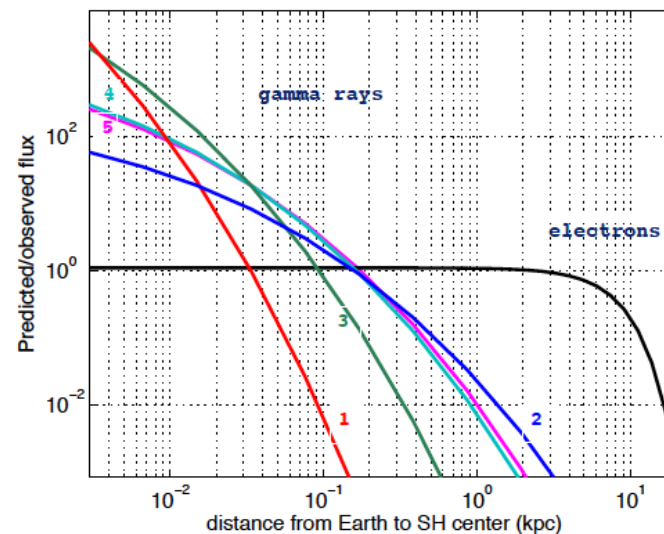
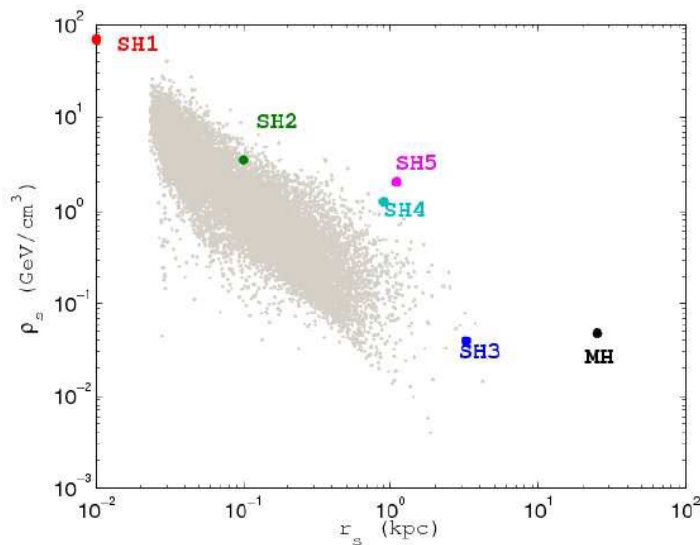
Gamma rays cont.

- ▶ We obtained constraints for the MH boost factor in the case of an Einasto DM profile, annihilation to **4e**:
 - ▶ $\text{BF} < 25$ (35) at 1σ (2σ) for $M = 1.0$ TeV
 - ▶ $\text{BF} < 42$ (52) at 1σ (2σ) for $M = 2.2$ TeV
- ▶ Increasing intermediate gauge boson mass to allow decay to **muons & pions**:
 - ▶ $\text{BF} < 23$ (28) at 1σ (2σ) for $M = 1.2$ TeV
- ▶ ...and choosing a flatter **isothermal** DM profile:
 - ▶ $\text{BF} < 62$ (72) at 1σ (2σ) for $M = 1.2$ TeV
- ▶ All well short of the required boost factors to explain PAMELA and Fermi electron excesses.



What about **local** substructure?

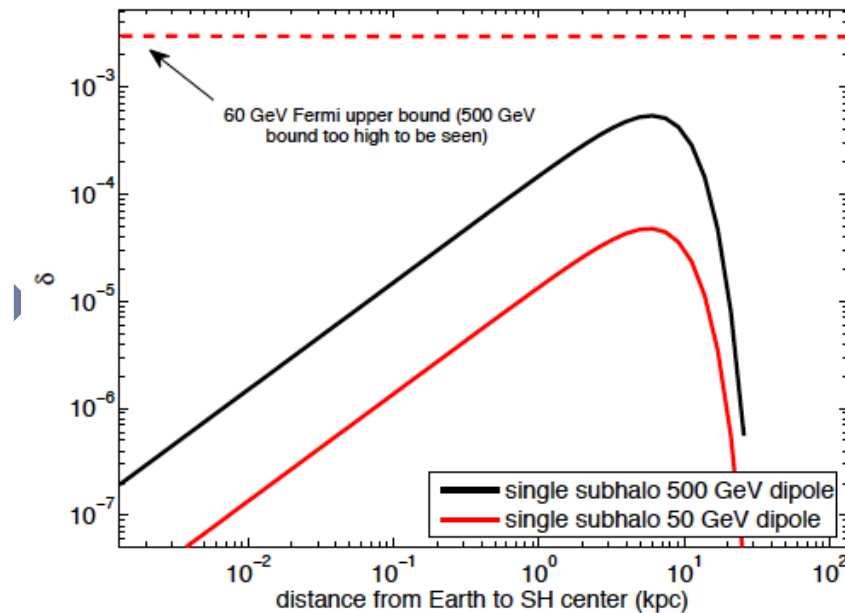
- ▶ We picked a few subhalos from the **Via Lactea II** population, and put them between us and the GC (lowest GR constraints)
- ▶ If we're **within ~ 3 kpc** of the subhalo center, but farther away than **$3 \sim 20$ pc**, the PAMELA and Fermi excesses could come from such a subhalo



Possible constraints on this scenario

- ▶ Fermi dipole anisotropy of $e^+ + e^-$

$$\delta = \frac{3D(E)}{c} \frac{|\vec{\nabla} n_e|}{n_e},$$



Bounds from dwarf spheroidals are not very constraining.

- ▶ Bounds from CMB => ok

Particle Physics Realization

- ▶ Consider a DM particle χ with a U(1) coupling to a dark gauge boson of mass μ
- ▶ This gives rise to an attractive Yukawa interaction (aka **Sommerfeld Enhancement**) which grows with decreasing relative velocity. Can approximately write:

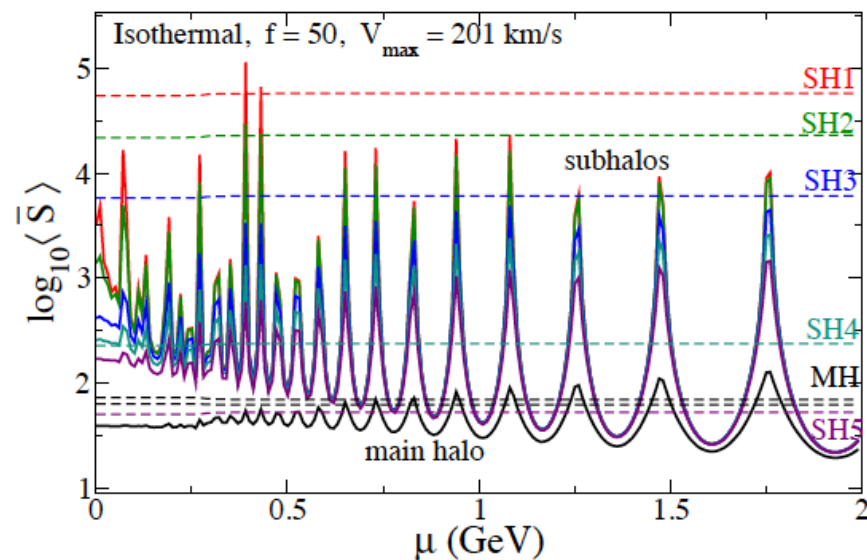
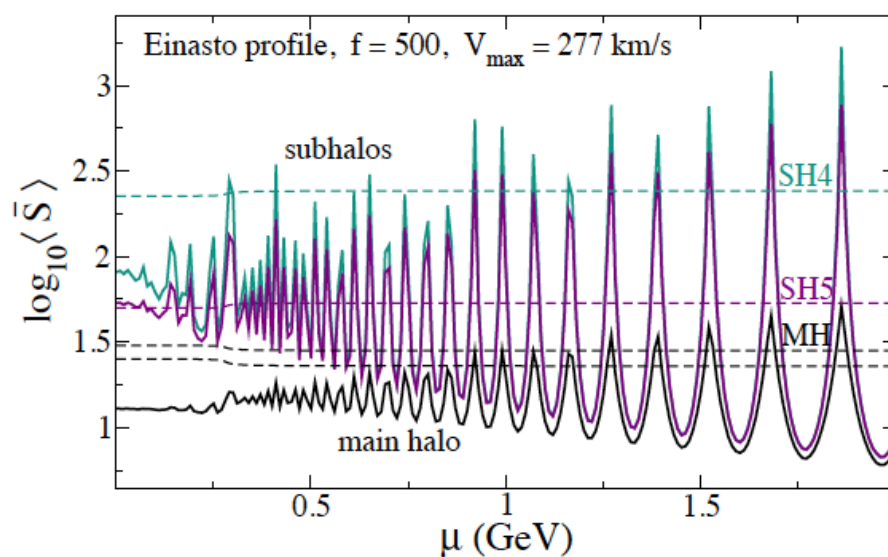
$$S = \frac{\pi}{\epsilon_v} \frac{\sinh X}{\cosh X - \cos \sqrt{\frac{2\pi}{\bar{\epsilon}_\phi} - X^2}}$$
$$\begin{aligned}\epsilon_v &= v/(\alpha_g c) \\ \epsilon_\phi &= \mu/(\alpha_g M) \\ X &= \epsilon_v/\bar{\epsilon}_\phi\end{aligned}$$

- ▶ Using realistic velocity distributions and correct α_g this typically predicts **too much** enhancement! Gamma ray constraints are immediately saturated.
-



Particle physics, cont'

- ▶ Solution: only a fraction $1/f$ contributes to the enhanced annihilation with $f \sim 50-500$
- ▶ In this way, relic density is correct, gamma ray constraints are respected, and PAMELA and Fermi anomalies can be addressed:



Conclusion

- ▶ **Substructure** is an interesting place to look for constraints on annihilating DM models
- ▶ We can't solve the gamma ray problem with a heavier WIMP annihilating in faraway subhalos, but a **close subhalo** may be the key
- ▶ Caveat: need **large, dense subhalos**: these should be rare around our location in the Milky Way.
- ▶ A realistic U(1) model typically produces **too much Sommerfeld enhancement**. This can be solved if only **part** of the DM can annihilate to the Standard Model through this channel.



II. Subhalos: how CRs get from there to here

▶ Diffusion equation:

$$\frac{d}{dt}\psi_{e^\pm}(\mathbf{x}, \mathbf{p}, t) = Q_{e^\pm}(\mathbf{x}, E) + \nabla \cdot (D(E)\nabla\psi_{e^\pm}(\mathbf{x}, \mathbf{p}, t)) + \frac{\partial}{\partial E} [b(\mathbf{x}, E)\psi_{e^\pm}(\mathbf{x}, \mathbf{p}, t)]$$

- ▶ **Source** term (particle physics of the DM model)

$$Q_{e^\pm} = \frac{1}{2} \left(\frac{\rho(\mathbf{x})}{M} \right)^2 \langle \sigma v \rangle \frac{dN_{e^\pm}}{dE} = \frac{n_{DM}^2}{2} BF \langle \sigma v \rangle_0 \frac{dN_{e^\pm}}{dE}.$$

- ▶ **Diffusion** coefficient – species do more or less of a random walk. Parameters set by measured B/C, Sub-Fe/Fe

$$D(E) = D_0 \left(\frac{E}{4 \text{ GeV}} \right)^\delta$$

Energy-loss term: Inverse Compton Scattering (ICS), and B field

$$b(x, E) = -\frac{dE_e}{dt} = \frac{32\pi\alpha_{em}}{3m_e^4} E_e^2 \left[u_B + \sum_{i=1}^3 u_{\gamma i} \cdot R_i(E_e) \right]$$



-
- ▶ We used both an unconstrained, freely varying the normalization of the background (consistent with some other authors), as well as a set of diffusion parameters from Simet & Hooper (much better approach), who fit GALPROP predictions to **B/C & sub-Fe/Fe abundances**

$$D_{0xx} = 6.04 \times 10^{28} \text{ cm}^2 \text{ s}^{-1} \text{ (0.19 kpc}^2\text{/Myr)}$$

$$L_{\text{eff}} = 5.0 \text{ kpc}$$

$$\delta = 0.41$$

$$V_A = 31 \text{ km s}^{-1}$$

$$\rho_{\odot} = 0.37 \text{ GeV cm}^{-3} \quad (\text{VL2, Catena \& Ullio 2009, ...})$$



IV. Gamma Rays

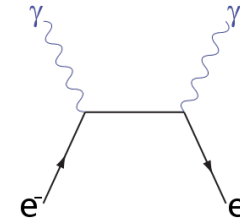
- ▶ Where there are electrons there is **Bremsstrahlung (final state radiation)** ...

$$\frac{d\Phi_{\text{main}}}{dE_\gamma d\Omega} = \frac{1}{2} \frac{\langle \sigma v \rangle}{4\pi} r_\odot \frac{\rho_\odot^2}{m_\chi^2} \frac{dN}{dE_\gamma} \bar{J}_{\text{main}} \quad , \quad \bar{J}_{\text{main}} = \frac{1}{\Delta\Omega} \int_{\Delta\Omega} d\Omega \int_{\text{l.o.s.}} \frac{ds}{r_\odot} \left(\frac{\rho_{\text{main}}[r(s, \psi)]}{\rho_\odot} \right)^2$$

particle
astro

...and **Inverse Compton Scattering**

$$\frac{d\Phi_{\gamma'}}{dE_{\gamma'} d\Omega} = \frac{1}{2} \hbar^2 c^3 \alpha_{EM}^2 \int_{\text{l.o.s.}} ds \int \int \frac{dn_e}{dE_e} \frac{du_\gamma}{dE_\gamma} \frac{dE_\gamma}{E_\gamma^2} \frac{dE_e}{E_e^2} f_{IC}$$



Electrons and positrons scatter off radiation from **CMB**, **IR** from dust and **starlight**, producing high-energy gamma rays in the **10-200 GeV** range.

- ▶ Both of these integrals can be performed numerically along the line of sight for our particular DM model and **known radiation distribution**, and compared to experimental **data**.

