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CERN RF Group RF Amplifiers and Couplers

CAS course on "RF for Accelerators", 18 June - 01 July 2023, Berlin Germany

**RF for Accelerators** 

# RF power generation









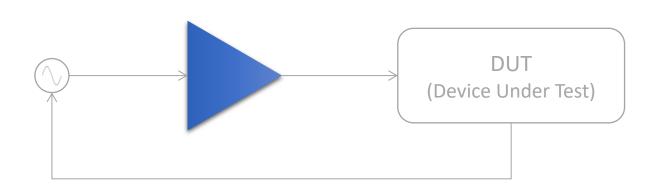
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#### RF Power - preamble



#### 

Very important for all projects

Rule of thumbs, HPRF acquisition costs From 5 € / W (MW amplifiers) to 10 € / W (kW amplifiers)

### RF Power - preamble

Class of operation	Α	В	С
Advantage	Linear	Almost linear	Non linear
DC to RF efficiency	30 %	78.5 %	90 %
Wall plug efficiency	20 %	40 %	50 %
Cost per 10 year [k€] 100 kW RF CW < 800 MHz 5000 hours/year	3750	1870	1500

W	$\rightarrow$	kW	$\rightarrow$	MW
€	$\rightarrow$	k€	$\rightarrow$	M€

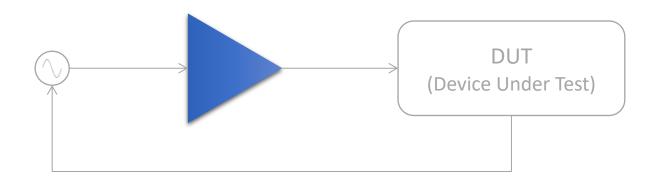
#### Very important for all projects

Rule of thumbs, HPRF operational costs  $\frac{0.20 \notin / kWh}{Wall \ plug \ efficiency}$ 

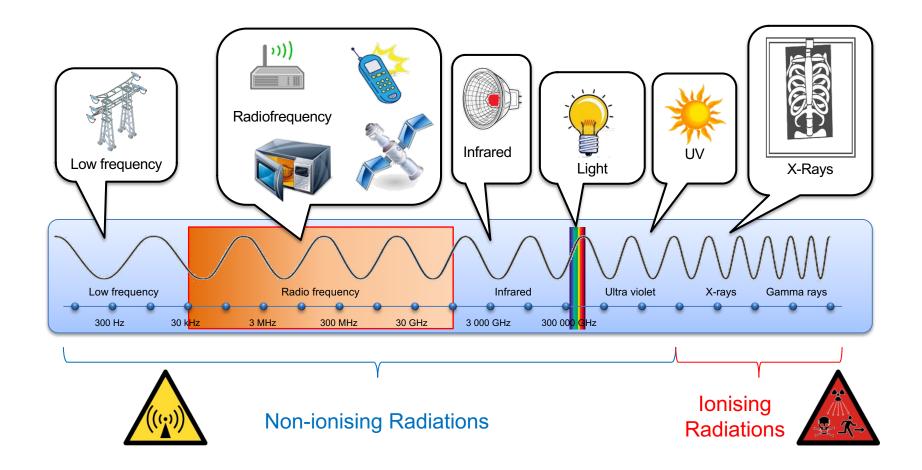
## Outlook

**RF** power basics Vacuum Tubes Vacuum Cathodes Triodes Tetrodes Klystrons **IOTs** Transistors LDMOS Combining Efficiency Conclusion

#### **RF** Power basics



### Electromagnetic waves



# Wavelength, frequency

$$\lambda = \frac{c}{f \sqrt{\varepsilon}} \quad \leftrightarrow \quad f = \frac{c}{\lambda \sqrt{\varepsilon}}$$

$$\lambda$$
 = Wavelength

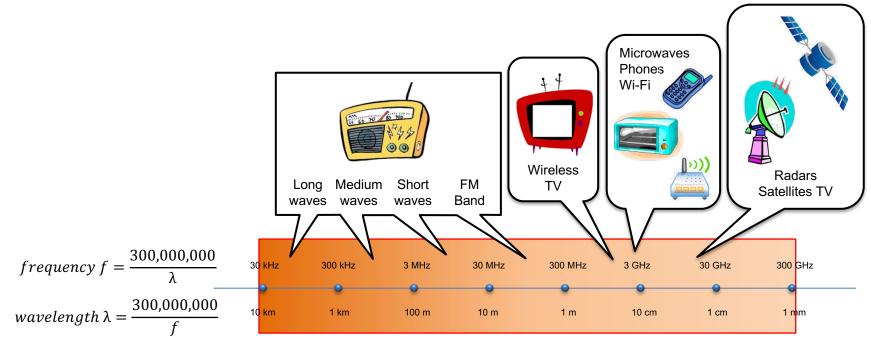
$$\lambda$$
 = wavelength in meters (m)

- c = velocity of light (m/s) (~ 300,000,000 m/s)
- f = frequency in hertz (Hz)
- $\varepsilon_{e}$  = dielectric constant of the propagation medium (~ 1.0 in air at 20 °C)

Depends on the medium we are talking about

 $\varepsilon air = 1$   $\varepsilon vacuum = 1$   $\varepsilon 'plastic' = 3-5$  $\varepsilon 'ceramic' = ~9$ 

### Radiofrequency waves



With  $\varepsilon = \sim 1.0$  (dielectric constant of air at 20 °C)

# Decibel (dB)

 $dBm = 10 \, Log_{10} \left( P_{mW} \right)$ 

$$dB = 10 \, Log_{10} \left(\frac{P_1}{P_2}\right)$$

$$dB = 20 \ Log_{10} \ (V_1/V_2)$$
  

$$dBV = 20 \ Log_{10} \ (V_{Vrms})$$
  

$$dB\mu V = 20 \ Log_{10} \ (V_{\mu Vrms})$$
  

$$dBc = 10 \ Log_{10} \ (P_{carrier}/P_{signal})$$

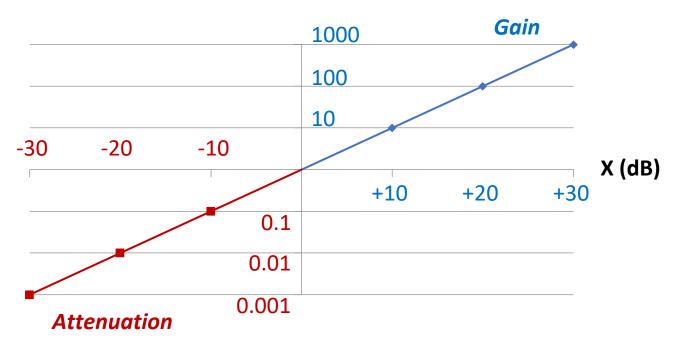
#### dBm, W

$$x_{dBm} = 10 Log_{10} (PmW) \quad \leftrightarrow \quad P_{mW} = 10^{(x_{dBm}/10)}$$

0	dBm	=	1	mW
30	dBm	=	1	W
60	dBm	=	1	kW
90	dBm	=	1	MW

#### dB, Power ratio

 $x_{dB} = 10 Log_{10} (P/P_{ref}) \quad \leftrightarrow \quad P/P_{ref} = 10^{(x_{dB}/10)}$ 

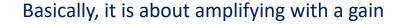


 $P/P_{ref}$ 

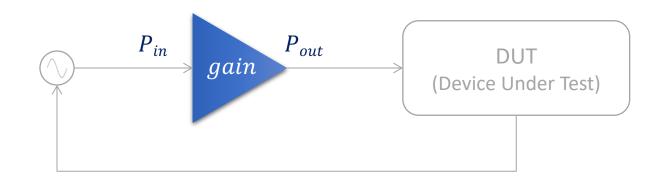
#### dB, Power ratio

x (dB)	P/P <sub>ref</sub>	
+ 0.1	1.023	+ 2.5%
+ 0.5	1.122	+ 12%
+ 1	1.259	+ 25%
+ 3	1.995	2
- 0.1	0.977	- 2.5%
- 0.5	0.891	- 11%
- 1	0.794	- 20%
- 3	0.501	0.5

#### **RF** Power Amplifier



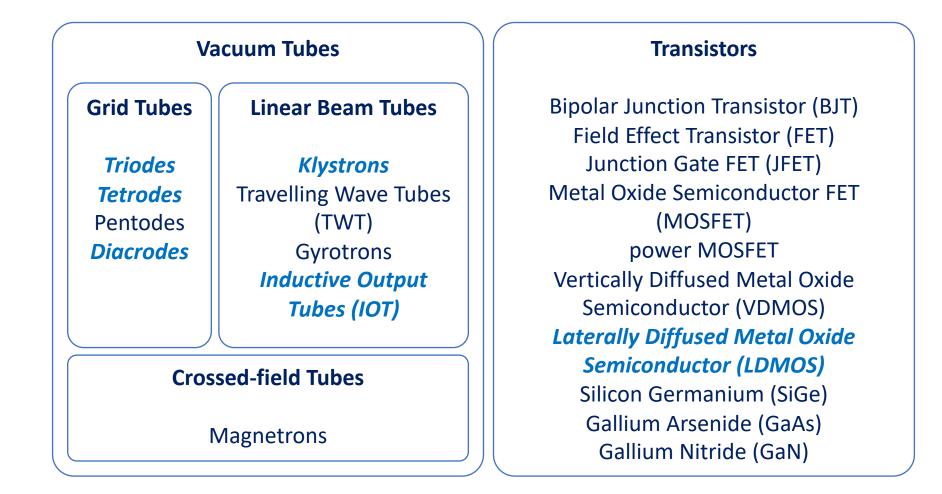
 $P_{out} = gain . Pin$ 



The ideal power amplifier Large bandwidth amplifying all frequencies equally No saturation Infinite power Zero delay No added noise Unconditionally stable Resistant to reverse power Radiation hard Efficient to transform AC input into RF output

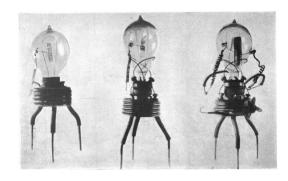
Unfortunately, such a device does not exist (yet?)

### RF power source classification



### Grid tubes

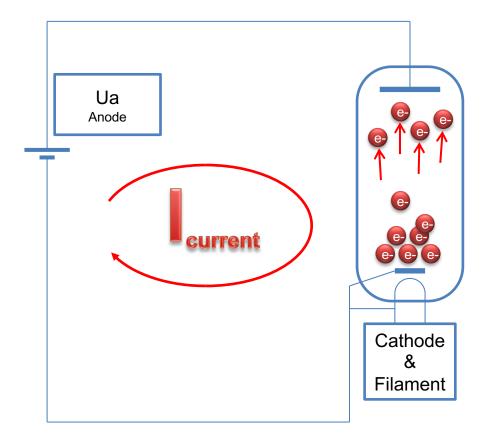
- 1904 Diode, John Ambrose Fleming
- 1906 Audion (first triode), Lee de Forest
- 1912 Triode as amplifier, Fritz Lowenstein
- 1913 Triode 'higher vacuum', Harold Arnold
- 1915 First transcontinental telephone line, Bell
- 1916 *Tetrode*, Walter Schottky
- 1926 Pentode, Bernardus Tellegen
- 1994 Diacrode, Thales Electron Devices



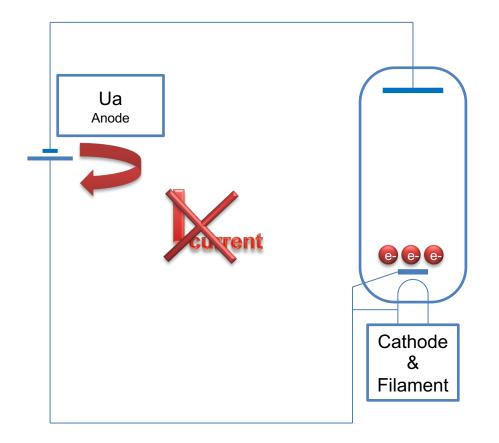
The first diode prototype Fleming Diode, 1904



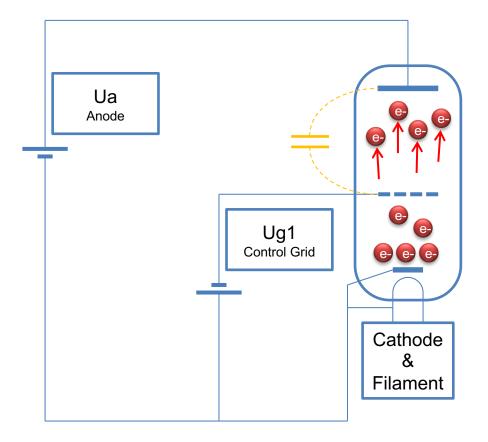
Thales TH 628 diacrode, 1998



#### Vacuum tube Heater + Cathode Heated cathode Coated metal, carbides, borides,... thermionic emission **Electron cloud** Anode Diode



#### Vacuum tube Heater + Cathode Heated cathode Coated metal, carbides, borides,... thermionic emission **Electron cloud** Anode Diode



#### Triode

Modulating the grid voltage proportionally modulates the anode current

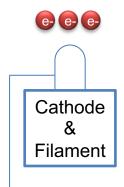
Transconductance

Voltage at the grid

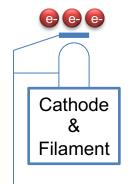
Current at the anode

#### Limitations

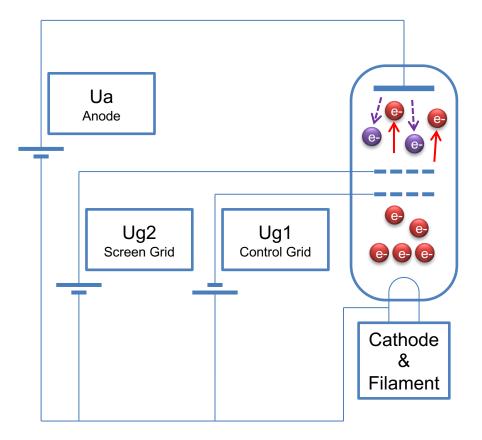
Parasitic capacitor Anode/g1 Tendency to oscillate



Direct heating cathode, Thoriated Tungsten



#### Indirect heating cathode, Oxide



#### Tetrode

Screen grid Positive (lower anode) Decouple anode and g1 Higher gain Limitations Secondary electron Anode treated to reduce secondary emission

#### Tetrode RS 2004 CERN SPS amplifier

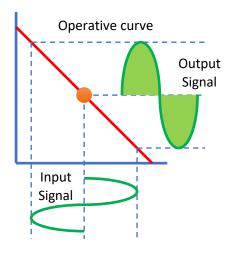


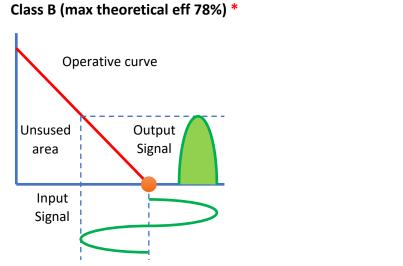
CERN SPS, RS 2004 Tetrode, Trolley (single amplifier), and transmitter (combination of amplifiers) Two transmitters of eight tubes delivering 2 x 1 MW @ 200 MHz, into operation since 1976

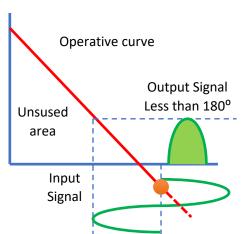
### Amplifier class

\* Class B and Class C need resonant circuitry for output sine therefore narrow band amplifiers

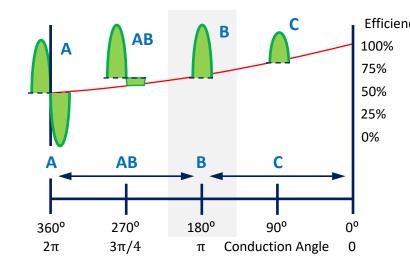








Class C (max theoretical eff > 78%) \*



псу	Amplifier Class	Description
_	Class-A	High linearity required, low power amplifiers
	Class-B	Regularly used in dual push-pull configuration, so as to restore full sine anode current and cancel even harmonics
_	Class-C	High efficiency Efficiency depends on conduction angle More the efficiency, less the gain

## Theoretical Class B efficiency

DC power is Pdc = Vdc Idc

Assuming the tube is linear whilst it is conducting, the dc anode current is found by Fourier analysis of the current waveform and is Idc =  $Ipk/\pi$  (resonant circuit output)

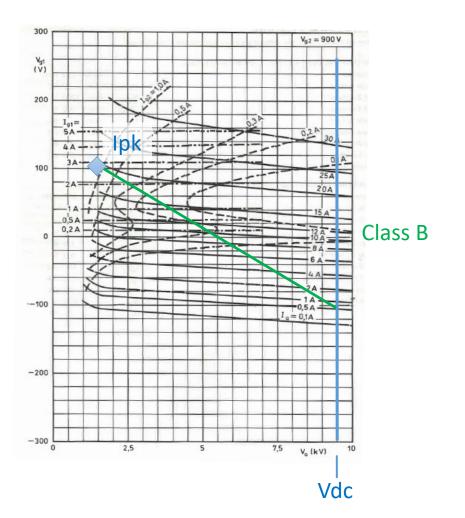
Irf = Ipk/2 = Idc  $\pi/2$ , and ideal class B, Vrf = Vdc

So, RF power is  $Prf = \frac{1}{2} Vrf Irf$ 

Prf =  $\frac{1}{2}$  Vdc Idc  $\pi/2 = \pi/4$  Vdc Idc

Theoretical efficiency  $\eta = Prf/Pdc = \frac{1}{4} Vdc Ipk / Vdc Idc$ 

η = 78.5 %



# Class B efficiency in practice

Two reasons for not achieving this impressive number

- 1. tube is not fully linear whilst it is conducting
- 2. Anode voltage must be higher than G2 voltage, VG2 being ~ 10% Vdc

This leads into

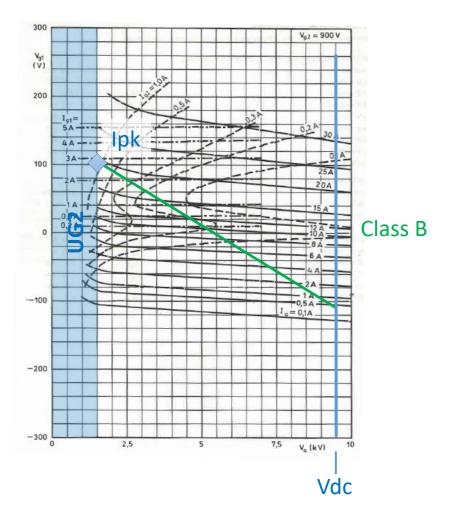
Pdc = Vdc Idc = Vdc 1.05 lpk/ $\pi$ 

 $Prf = \frac{1}{2} Vrf Irf = \frac{1}{4} 0.9 Vdc Ipk$ 

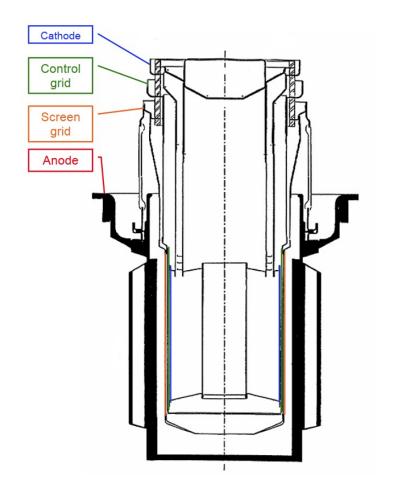
Theoretical efficiency in practice

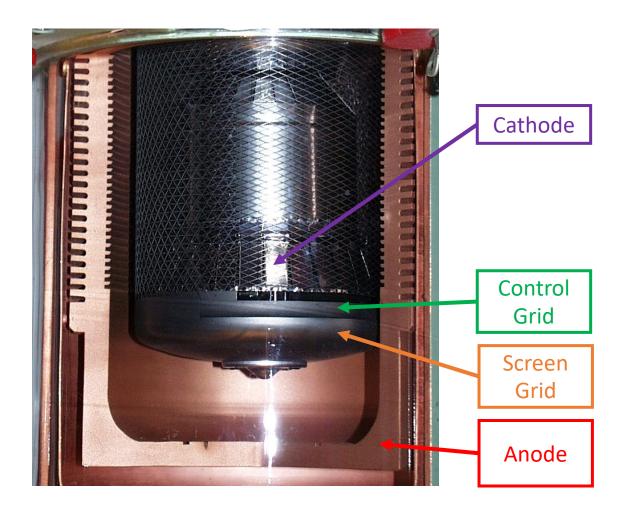
 $\eta = Prf/Pdc = \frac{1}{4} 0.9 Vdc Ipk / 1.05 Vdc Ipk/\pi$ 

η = 67 %



#### Construction





#### **Construction** limitations

The main limitations faced by grid-base devices are the following

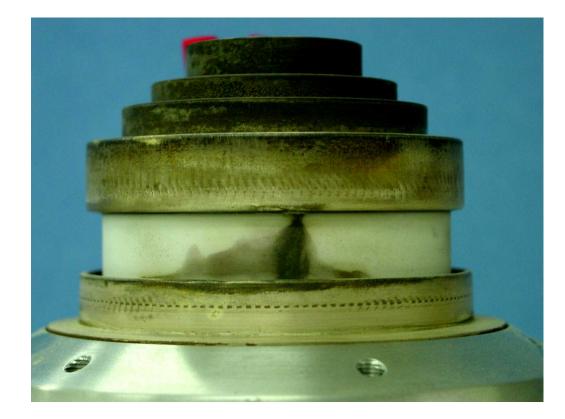
**Physical size**, ideally RF voltages between electrodes should be uniform, but this condition cannot be achieved unless the major electrode dimensions are significantly smaller than 1/4 wavelength at the operating frequency, this is achievable at lower frequencies than 400 MHz, but at higher frequencies, this becomes a difficulty

**Electron transit time**, electrode spacing, principally between the grid and the cathode must be scaled inversely with frequency to avoid excessive loading of the drive source, reduction in power gain, back heating of the cathode and reduced conversion efficiency

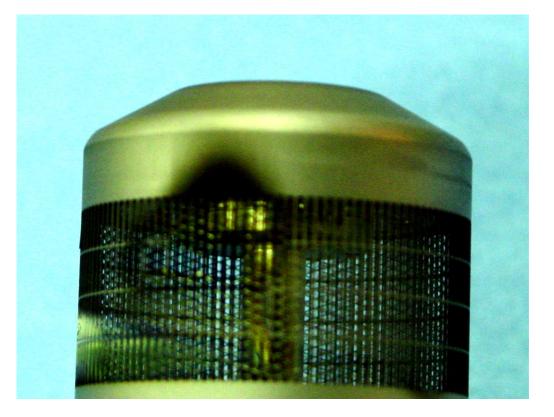
**Voltage breakdown**, high power tubes operate at high voltages that presents significant problems placing restrictions on the operating voltages that may be applied to the individual elements

**Circulating currents**, important RF currents may develop as a result of inherent inter electrode capacitances and inductances of the device, causing significant heating of the grid, the connections and the vacuum seals

**Heat dissipation**, as the element must be kept small with respect to the required power, power dissipation is accordingly consequently limited



External arcing between Anode and G2



Internal arcing on G2



#### Overheating due to lack of air cooling



#### Ceramic crack due to internal metallization of the ceramic, perhaps due to over filament



The cathodes we are interested in here emit electrons in the vacuum envelop

Almost all tubes use thermoelectronic cathodes

A metal is heated to a very high temperature

The kinetic energy of the electrons is such that some leave the metal spontaneously and are emitted into the vacuum

They do not go far away because electronic neutrality keeps them in the immediate vicinity of the cathode

However, all that needs to be done is to apply an electric field to form a beam from this 'space charge'



$$J_c = A \cdot S \cdot T^2 \cdot e^{-\frac{W_0}{kT}}$$

- $\begin{array}{ll} J_c & \_Maximum \ Cathode \ current \ density \\ A & = Constant \end{array}$
- S = Surface
- $W_0 = output Work function$  (kinetic energy to provide to an electron to extract it from the metal)
- = operating Temperature T
- = Boltzmann constant (1.38 10<sup>-23</sup>) K

Lower the output Work function  $W_0$ , greater the current

Greater the cathode temperature *T*, strictly linked to filament voltage, less the cathode lifetime

As a rule of thumb, - 5 % Filament Voltage  $\rightarrow$  + 25 % lifetime

Type of Cathode	Output Work function $W_0$	Operating Temperature T	<b>Current density</b> $J_c$	Application
Pure Tungsten	4.6 eV	2 200 °C	0.3 A/cm <sup>2</sup>	Old generation of radio tubes. (not used anymore)
Oxide Cathode	1 eV	800 °C	0.3 A/cm <sup>2</sup> Up to 40 A/cm <sup>2</sup> up to 2 μs	Triodes and old klystrons
Thorium Tungsten	2.6 eV	1 700 °C	1 to 3 A/cm <sup>2</sup>	Triodes and Tetrodes Magnetrons for microwave oven
Impregnated Cathodes (type S: W-Ba; type M and MM: W-Ba-Os)	1.8 eV	1 000 °C	1 to 10 A/cm <sup>2</sup>	Klystrons and IOTs



Thorium Tungsten is the one used in our high power tubes (could also be Barium or Osmium)

1.5 % of Thorium oxide is added to the Tungsten

Thorium Tungsten is carburized with an hydrocarbon gas, as a result, a layer of Tungsten carbide is formed

All along the lifetime of the cathode, the Thorium evaporates ageing the cathode

At the end of the tube life, the tungsten carbide layer disappears and emission level drops

Too high cathode temperature Accelerate decarburization process Tends to deform cathode shape

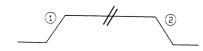
Too low cathode temperature

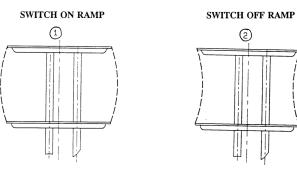
Reduce thermal electrons flow

Slow down the process of thorium diffusion to the surface

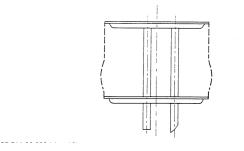
As a rule of thumb, - 5 % Filament Voltage  $\rightarrow$  + 25 % lifetime

#### HEATING SEQUENCE





#### AFTER SEVERAL ON/OFF CYCLES



Heater voltage, always with gradual application and gradual shutdown

The ramp allows cathode assembly, cathode and its support, to absorb differences caused by thermal expansion

Tube lifetime depends on the duration of the ramp, and on the on/off cycling frequency as well

It is advised to keep heater voltage to nominal, during short transmitter interruptions

One cycle per day must be considered as a maximum

### Grids



Control grid (G1) controls the electrons flow from the cathode

Screen grid (G2) accelerates the electrons flow and absorb the secondary electrons coming back from the anode

They are almost the same size, only a fraction of mm separate them

Traditional Grids materials are

Molybdenum

Tantalum

Tungsten

Various coating materials are used to reduce secondary emission, among them Zirconium, Platinum..., involving various processes

Thermal emission

Grids become electrons sources due to the high emissivity of the normal grid materials (Mo [Molybdenum], Ta [Tantalum] and W [Tungsten])

Secondary emission is directly related to

grid material

surface regularity

velocity of impinging electrons

Mechanical rigidity

Ordinary grids are made by using spot welding techniques, which can cause grid deformation in hard operating conditions

#### Grids



#### Pyrobloc<sup>®</sup> grids by Thales

Pyrolytic graphite is a form of crystal carbon produced by cracking an hydrocarbon gas under high temperature The useful properties of Pyrobloc® grids high temperature stability, no thermal expansion high toughness against thermal shock, no grid deformation low thermal emission, since actually close to black body material lower secondary emission than traditional grids electric conductivity as high as coated metallic grids excellent mechanical stability, even better under high temperature

### Anode



#### Anode collects the flow of electrons

Anode is made of massive oxygen-free copper

The design depends on aimed power dissipation, and on anode cooling system

Anode acts as electrons collector vacuum enclosure heat sink

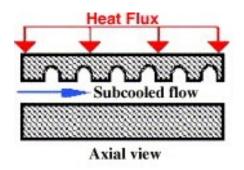
Secondary emission of electrons take place in the collector and special treatment are applied to reduce them

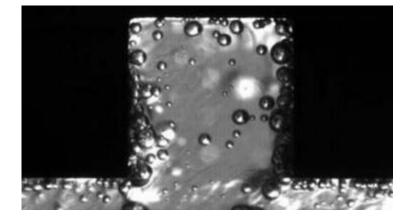
# Anode cooling



#### Anode cooling efficiency

Forced air cooling 100 W/cm<sup>2</sup>



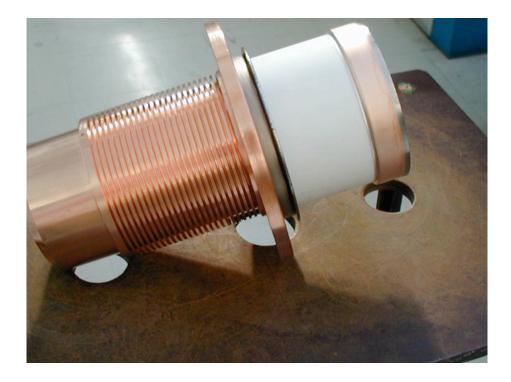


Water cooling vapotron supervapotron Hypervapotron

350 W/cm<sup>2</sup> 500 W/cm<sup>2</sup> 2000 W/cm<sup>2</sup>

# Tube assembly





Ceramics are used to join the grids and the anode in order to provide the vacuum leak tightness inside the tube, and to provide the needed insulation material between them

Kovar rings are brazed to the ceramics, as their thermal property are as close as possible to the ceramic for a metal

Final welding are performed to assemble the various elements

# Tube assembly

Every raw materials, parts and subassemblies are assessed along the manufacturing process

After final assembly and before pumping, cold measurements, such as capacitances and voltage insulation, are performed on each tube

During the tube being under vacuum pumping, it is baked out at 450°C for 10 hours, a second step, that can last several days, is to activate the cathode by heating it at a much higher temperature than in normal operation

Vacuum is monitored at each step of the process and must remain within 10<sup>-7</sup> to 10<sup>-8</sup> mbar Insufficient vacuum would cause arcing, early cathode decarburization, metallization of isolators

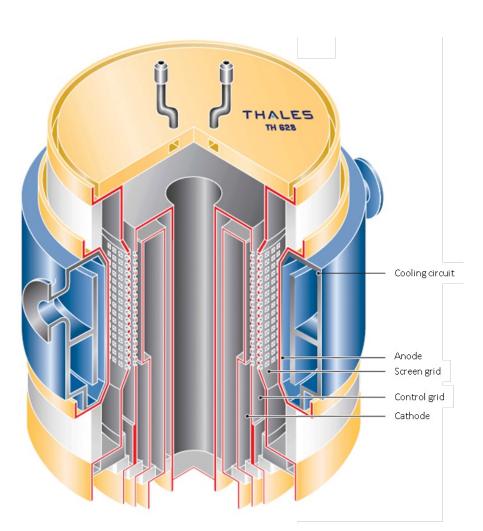
A final tests is performed with all the tubes on specific test benches simulating their working conditions



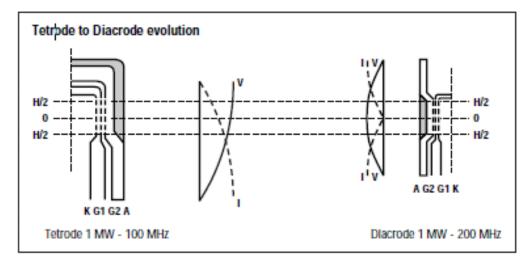
# **Operation & Possible failures**

Factors of influence	Damage in the tube	Limiting factors	
Cathode temperature	Cathode deformation Cathode decarburization	Filament voltage too high Dissipated power on the grids RF losses due to harmonics	
Cathode cycling	Cathode deformation	More than one on/off cycle per day Mains failure	
Overvoltage and overcurrent	Grids damaged due to flashes between KG1 or G1G2	Bad tuning Accidental circuit mismatch Defective protective devices Defective damping circuits	
Overheating	Outgassing or even melting of the anode or of the base of the tube	Bad cooling Bad tuning Accidental circuit mismatch	
Vacuum	Drop of emission	Bad contacts Corrosion Overheating	
Handling	Broken cathode or grids		

# Diacrode

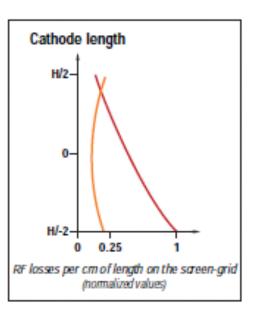


The basic Diacrode design limits electrical losses and electrodes heating by minimizing the reactive currents in the cathode and grids meshes. This means that compared with conventional tetrodes, Diacrodes can either double the output power at a given operating frequency or double the frequency for a given power output. Diacrodes provide the same gain and efficiency as conventional tetrodes - but at frequencies which are out of reach for tetrodes at an equivalent output power



The main difference is in the position of the active zones of the tubes in the resonant coaxial circuits, resulting in improved reactive current distributing in the tube's electrodes

> Example of calculated RF losses on the screen grid for the same cathode length at an output power of 1.4 MW cw @ 120 MHz — Diacrode — Tetrode



### Diacrode

Los Alamos already successfully operate several Diacrodes since 2015



Within the Test Infrastructure and Accelerator Research Area (TIARA) program, CERN and Los Alamos tested a Diacorde for the Ionisation Cooling Test Facility at the Rutherford Appleton Laboratory

Novel pulsed RF power amplifier design, Milestone MS28 <u>https://cds.cern.ch/record/1510945/files/TIARA-REP-WP7-</u>2013-002.pdf

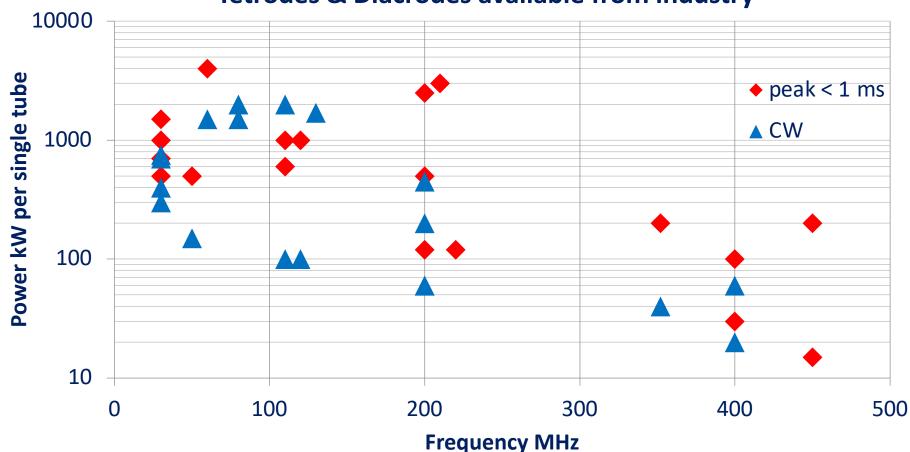
### Design report of a 3 MW power amplifier, Deliverable 7.4 <u>https://cds.cern.ch/record/1647574/files/TIARA-REP-WP7-</u>2014-005.pdf



Pulse duration [μs]	Repetition rate [pps]	Anode Voltage [kV]	Anode current [A]	Grid2 voltage [kV]	Pout [MW]	η <sub>rf/dc</sub> [%]
1000	120	26.1	108	1.5	2.0	69.5
300	30	29.4	153	1.6	3.0	65.3

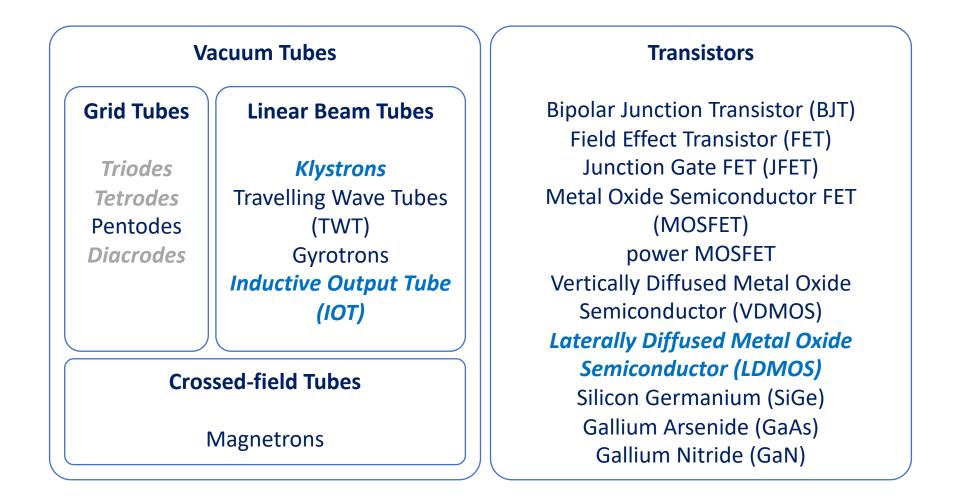
John Lyles, Los Alamos National Laboratory, Design, test and implementation of new 201.25 MHz RF power amplifier for LANSCE Linac\* LA-UR-12-20983

# Frequency & Power range of tetrodes



**Tetrodes & Diacrodes available from industry** 

### RF power source classification



### Linear beam tubes

- 1937 Klystron, Russell & Sigurd Variant
- 1938 IOT, Andrew V. Haeff
- 1939 Reflex klystron, Robert Sutton
- 1940 Few commercial IOT
- 1945 Helix Travelling Wave Tube (TWT), Kompfner
- 1948 Multi MW klystron
- 1959 Gyrotron, Twiss & Schneider
- 1963 Multi Beam Klystron, Zusmanovsky and Korolyov
- 1980 High efficiency IOT
- 2022 High Efficiency Klystron

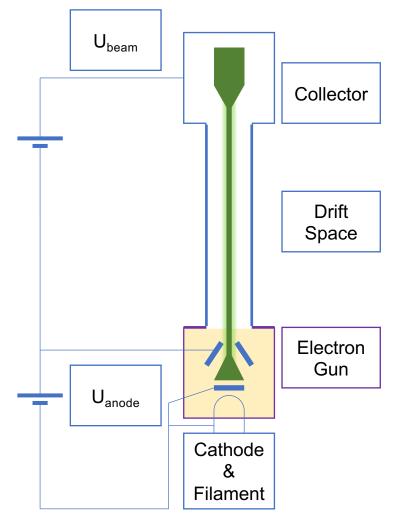


Russell & Sigurd Varian klystron, 1937

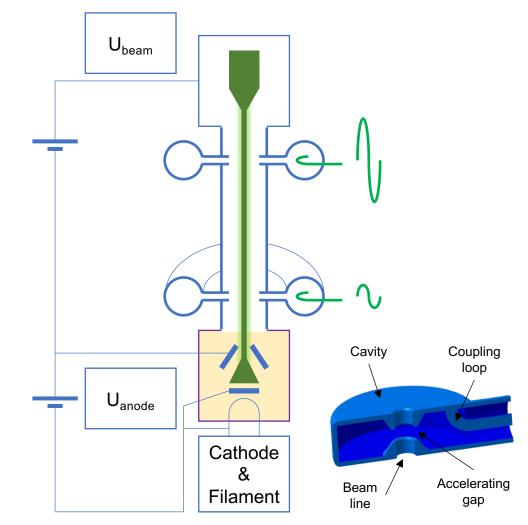


#### Thales TH 1802, 2002

CAS course on "RF for Accelerators" 18 June - 01 July 2023, Berlin Germany



**Klystrons velocity** modulation converts the kinetic energy into radio frequency power Vacuum tube **Electron** gun Thermionic cathode Anode **Electron beam** Drift space Collector e- constant speed until the collector



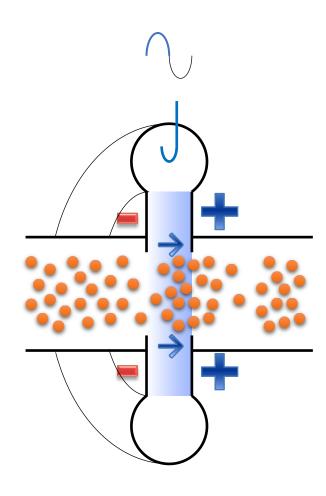
### **Cavity resonators**

RF input cavity (Buncher) modulates e- velocity Some are accelerated Some are neutral Some are decelerated Bunching the e-

### RF output cavity (Catcher) Resonating at the same frequency as the input cavity At the place with the numerous number of e-

Kinetic energy converted into voltage and extracted

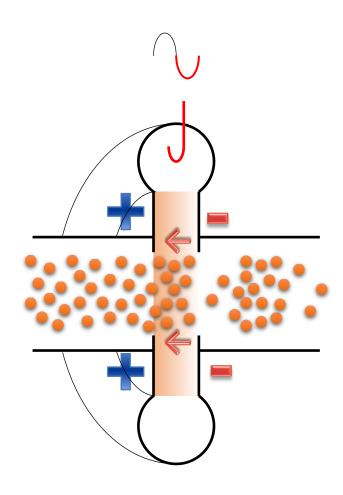
CAS course on "RF for Accelerators" 18 June - 01 July 2023, Berlin Germany



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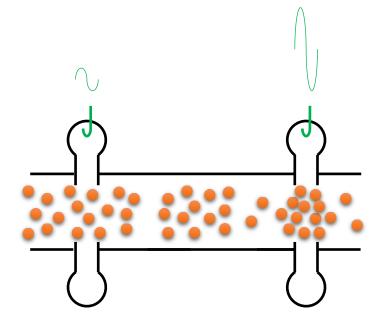
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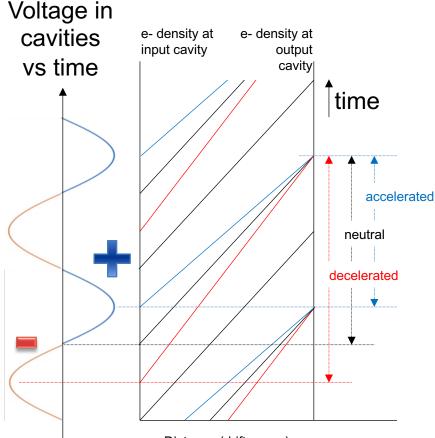
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**Cavity resonators** 

RF input cavity (Buncher) modulates e- velocity Some are accelerated Some are neutral Some are decelerated Bunching the e-

RF output cavity (Catcher) Resonating at the same frequency as the input cavity At the place with the numerous number of e-Kinetic energy converted into voltage and extracted



Distance (drift space)

#### Bunching of e- beam in a klystron

CAS course on "RF for Accelerators Germany

#### RF Power generation, eric.montesinos@cern.ch, CERN RF Amplifiers & Couplers

Cavity resonators

**RF** input cavity (Buncher)

modulates e-velocity

Some are accelerated

Some are decelerated

RF output cavity (Catcher)

Resonating at the same frequency as the input

numerous number of e-

Kinetic energy converted

into voltage and extracted

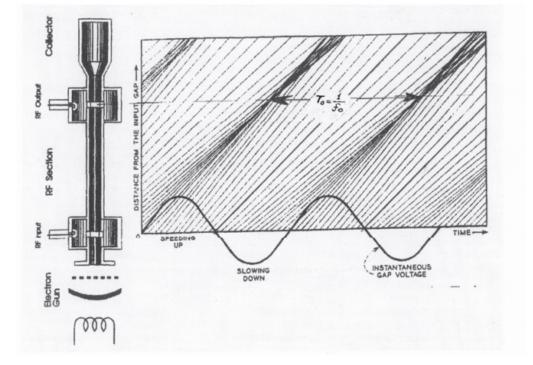
At the place with the

Some are neutral

Bunching the e-

cavity

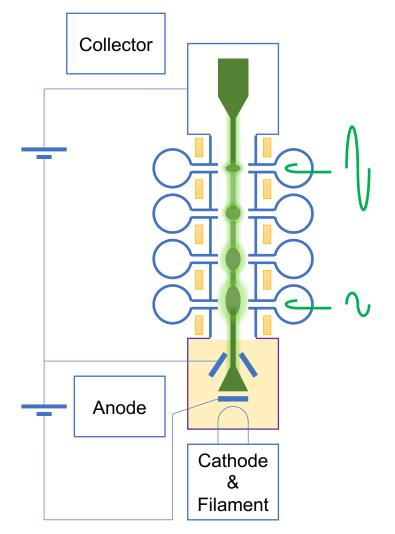
52



#### The Applegate diagram

The velocity modulation principle, which made klystrons possible, was explained by Russell Variant as follows, in a book written by his wife, Dorothy: 'Just picture a steady steam of cars from San Francisco to Palo Alto, if the cars left San Francisco at equal increments and at the same velocity, then even in Palo Alto they would be evenly spaced and you would call this a direct flow of cars. But suppose somehow the speed of some cars, as they left San Francisco, was increased a bit and others retarted. Then, with time, the fast cars would tend to catch up with the slow ones and they would bunch into groups. Thus, if the velocity of the cars was sufficiently different or the time long enough, the steady stream of cars would be broken and, under ideal conditions, would arrive in Palo Alto in clearly defined groups. In the same way an electron tube can built in which the control of the e-beam is produced by the principle of bunching, rather than the direct control of a grid in a triode...'

This is illustrated by the 'Applegate' diagram, showing electrons from an electron gun traversing a gap in a first cavity, and having their velocity modulated by the voltage across that gap. As a result, they arrive in bunches at the second, or output cavity. Bunches form around the electrons crossing the first gap when the sinusoidal voltage there crosses from negative to positive (from decelerating to accelerating). Bunches arrive at the second cavity with a period TO, which corresponds to the period of the sinusoidal power input to the first cavity. The bunching action shown in the Applegate diagram is entirely ballistic, or kinematic, i.e. the charge of the electrons does not come into play as their trajectories come very close and actually cross. In an average klystron, space charge will modify these trajectories and the interaction between cavities and beam will be better described by 'space-charge wave theory', which treats space charge as an elastic medium and describes electron motion in term of wave.



# Additional bunching cavities

- Resonate with the prebunched electrons beam
- Generate an additional accelerating/decelerating field
- Better bunching Gain 10 dB per cavity
- Focusing magnets To maintain the e- beam as expected and where expected

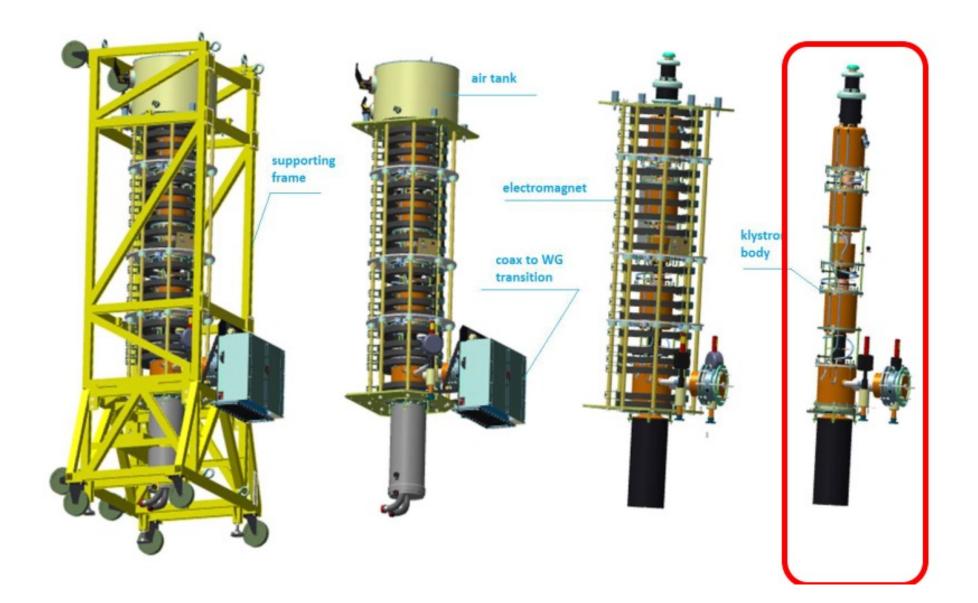
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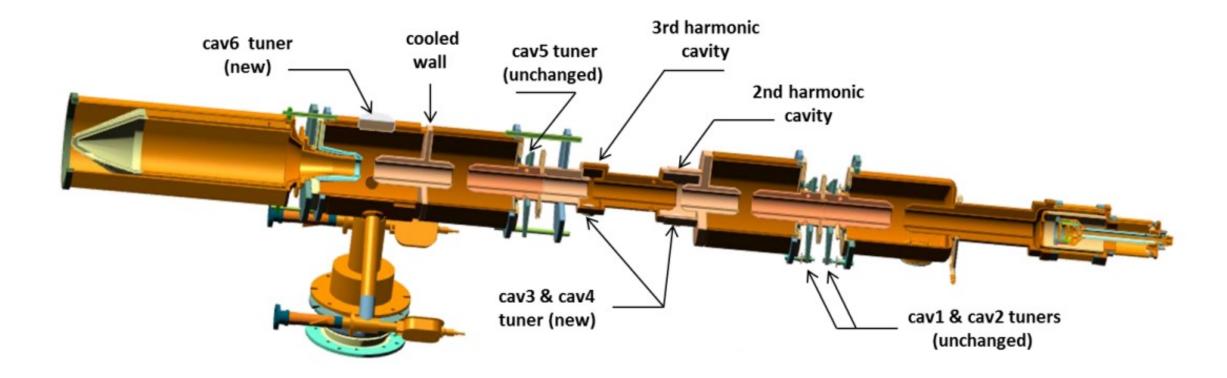


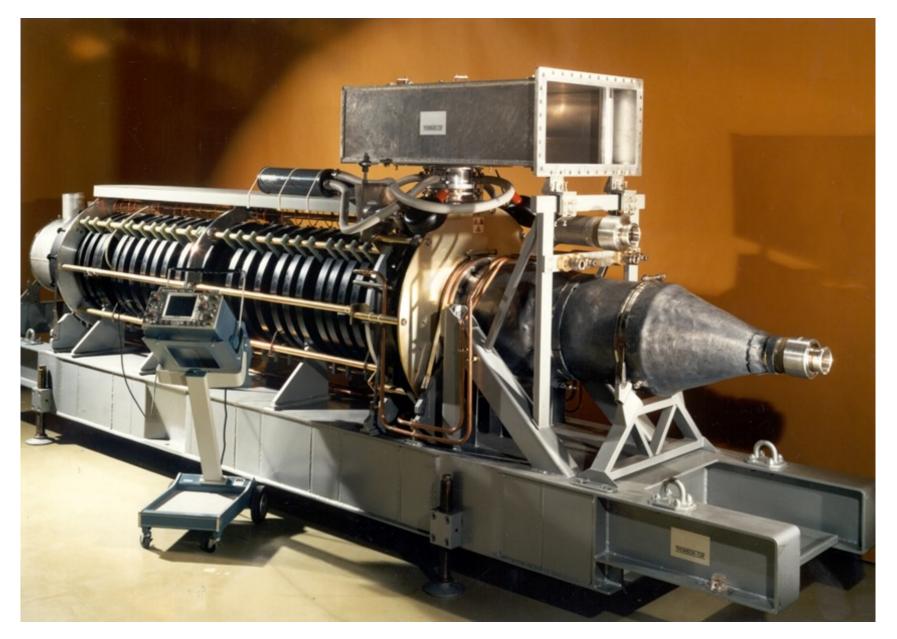


#### CERN LHC, TH 2167 klystron and in UX45 cavern 16 klystrons delivering 330 kW @ 400 MHz, into operation since 2008

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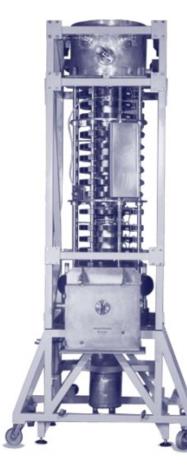




### LHC TH2167 high efficiency project

Commonly with CERN, be the first team to develop, manufacture and operate a high efficiency (CSM based) klystrons set in reliable conditions

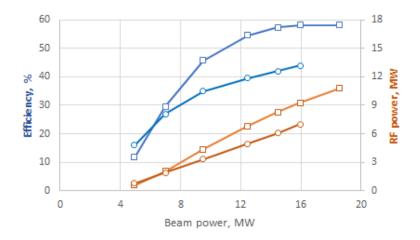
Integrating the major improvements held over the last four years on klystron modeling within HEIKA, compatible with industrial manufacturing margin



# High Efficiency Klystron



	E37113 at factory	E37117 design
Voltage, kV	154	154
Current, A	93	94
Frequency, GHz	11.994	11.994
Peak power, MW	6.2	8.16
Sat. gain, dB	49	58
Efficiency, %	42	57/ FCI
Life time, hours	30 000	30 000
Solenoidal magnetic field, T	0.35	0.4
RF circuit length, m	0.127	0.127

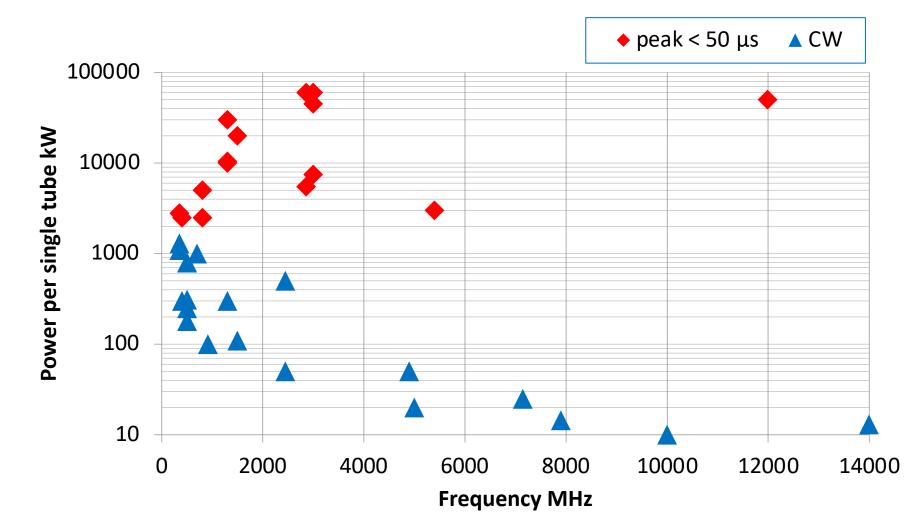


High Efficiency solution allowed to increase peak RF power available for the high gradient X-band test facility at CERN by 35% within original environment (re-used modulator and solenoid)

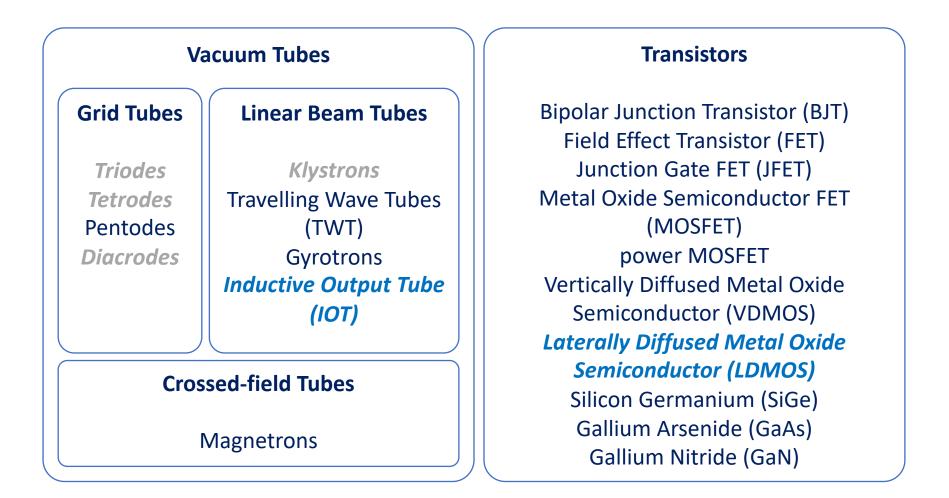
Tube is now commercially available, prototype successfully tested in December 2022

Technology(ies) developed at CERN allow to improve significantly efficiency/RF power of any existing commercial klystron (based on retrofit approach if necessary)

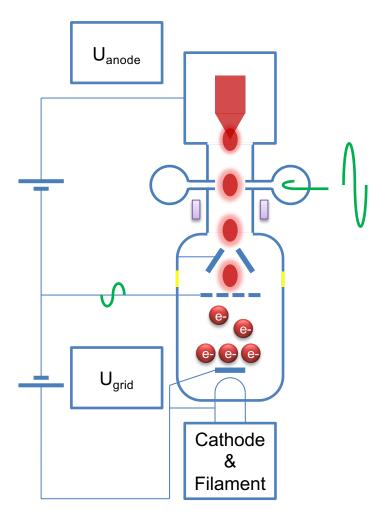
### Klystrons available from industry



### RF power source classification



# Essentials of IOT



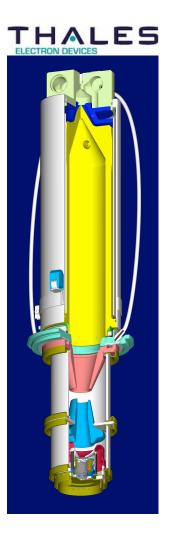
### IOT density modulation

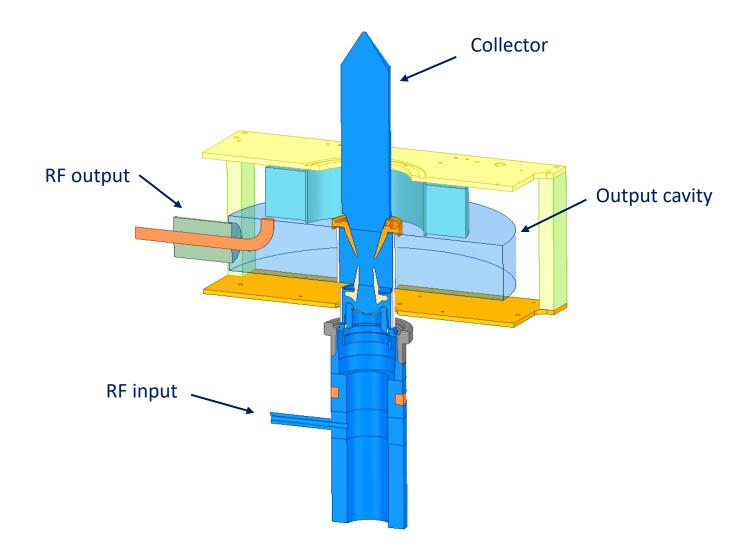
converts the kinetic energy into radio frequency power

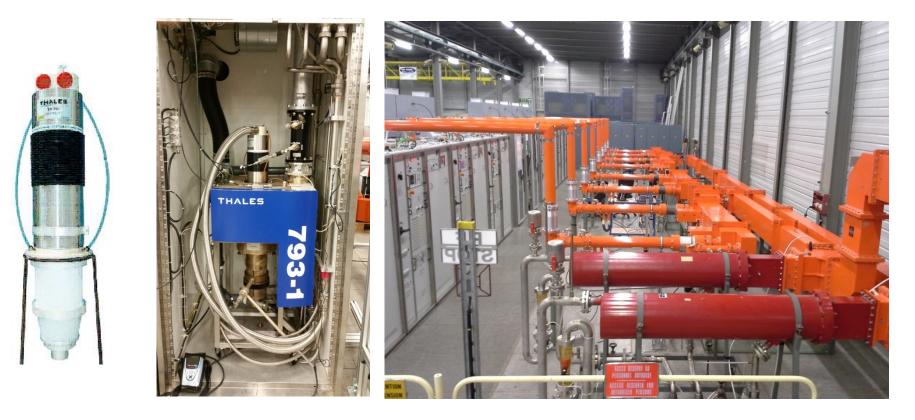
### Vacuum tube

Triode input Thermionic cathode Grid modulates e- emission Klystron output Anode accelerates e- buckets Short drift tube & magnets

### Catcher cavity







CERN SPS, TH 795 IOT, Trolley (single amplifier), and transmitter (combination of amplifiers) Two transmitters of four tubes delivering 2 x 240 kW @ 801 MHz, into operation since 2014



# R&D program, MB-IOT



EUROPEAN SPALLATION SOURCE



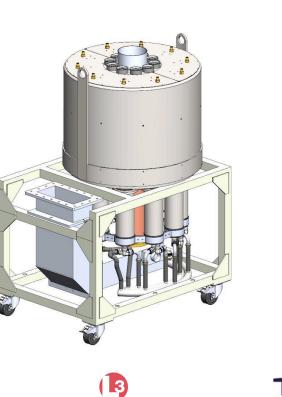
In order to provide an alternative to klystrons, ESS launched a R&D program for Multi Beam IOT

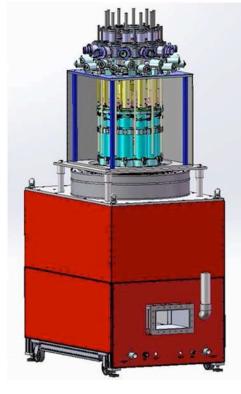
Two prototypes will be delivered in 2016

The goal was to reach 1.3 MW @ 704 MHz pulsing up to 3.5 ms - 14 Hz

Each tubes were composed of 10 guns, combined into a single output cavity

Both tubes successfully achieved the required performances

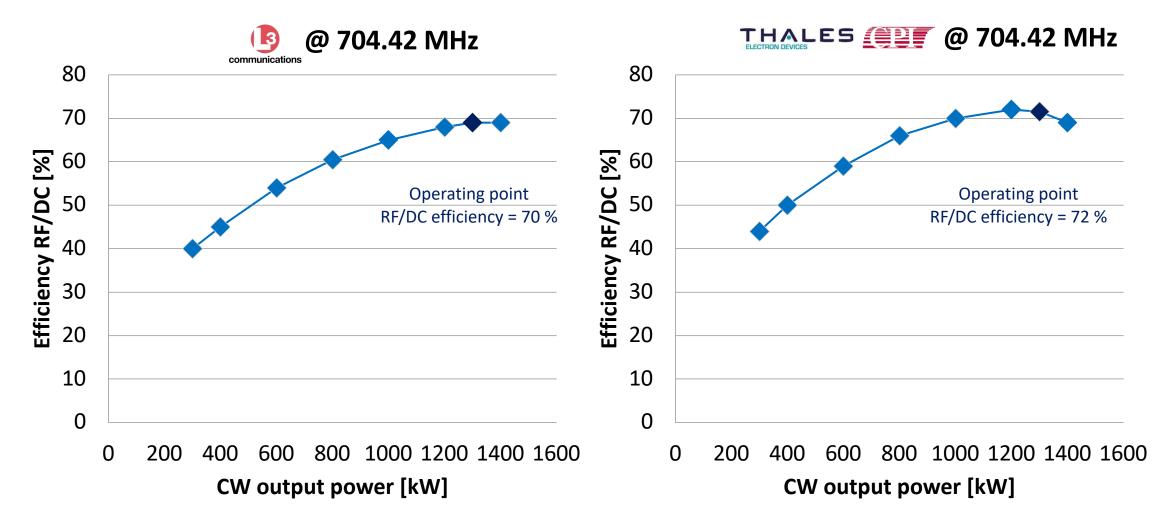




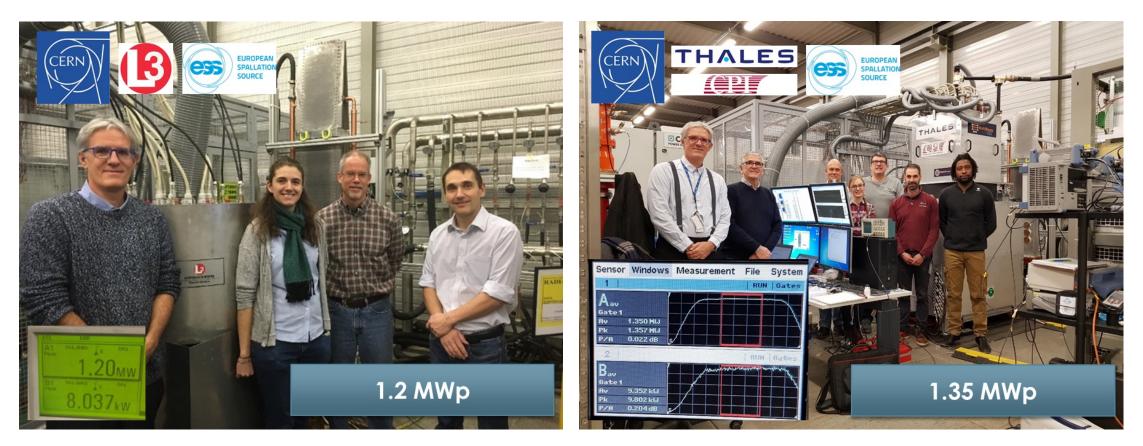




### R&D program, MB-IOT







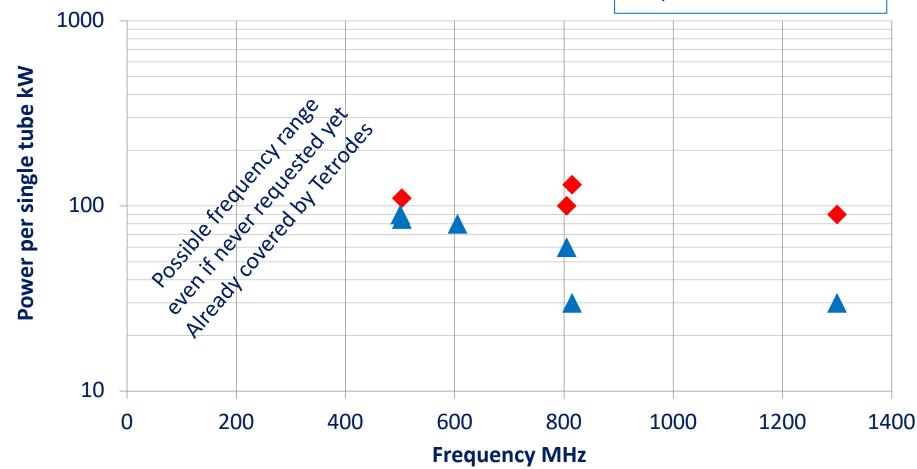
#### L3 MB-IOT, 750 MHz, 5 % duty cycle

#### Thales-CPI MB-IOT, 750 MHz, 5 % duty cycle

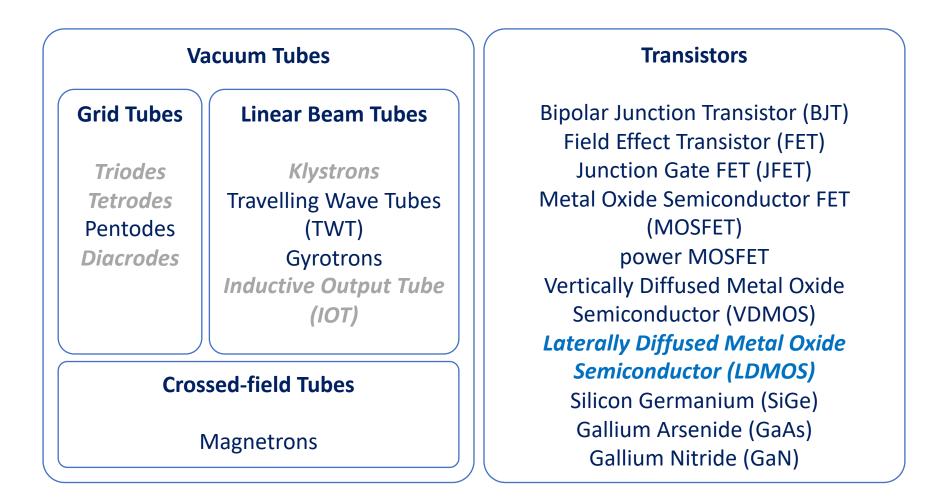
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### IOT available from industry

♦ peak < 10 ms ▲ CW</p>



### RF power source classification



# Transistor for RF power

- 1925 theory, Julius Edgar Lilienfeld
- 1947 Germanium US first transistor, John Bardeen, Walter Brattain, William Shockley
- 1948 Germanium European first transistor, Herbert Mataré and Heinrich Welker
- 1953 first high-frequency transistor, Philco
- 1954 Silicon transistor, Morris Tanenbaum
- 1960 MOS, Kahng and Atalla
- 1966 Gallium arsenide (GaAs)
- 1980 VDMOS
- 1989 Silicon-Germanium (SiGe)
- 1997 Silicon carbide (SiC)
- 2004 Carbon graphene

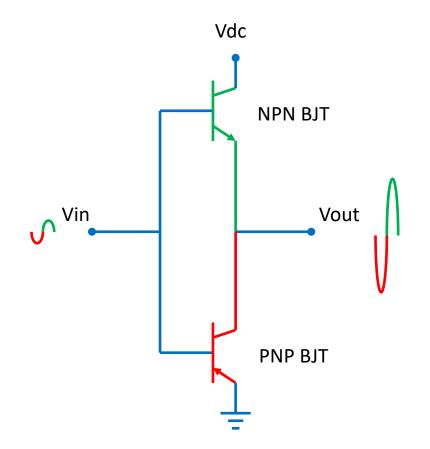


First transistor invented at BELL labs in 1947



XXI century LDMOS

# Essentials of RF transistor

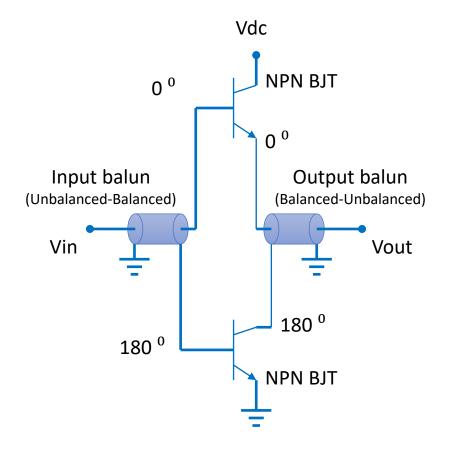


In a push-pull circuit the RF signal is applied to two devices One of the devices is active on the positive voltage swing and off during the negative voltage swing The other device works in the opposite manner so that the two devices conduct half the time

The full RF signal is then amplified

Two different type of devices

# Essentials of RF transistor



Another push-pull configuration is to use a balun (balancedunbalanced)

it acts as a power splitter, equally dividing the input power between the two transistors

the balun keeps one port in phase and inverts the second port in phase

Since the signals are out of phase only one device is on at a time

### This configuration is easier to manufacture since only one type of device is required

# Essentials of RF transistor

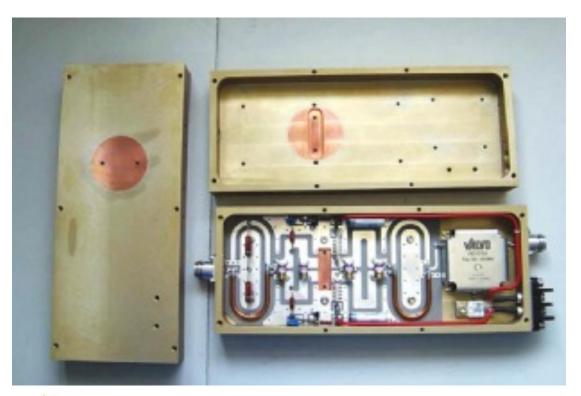


 elementary amplifier module
 VDMOS-D1029UK05 operated at 330 W at 352 MHz under 30 Vdc with a gain of 11 dB
 Each module is with a Valvo 500 W circulator to protect the transistors from excess of reflected power

# Essential of transistors

An important aspect of high-power transistors is the heat transfer to the cooling system

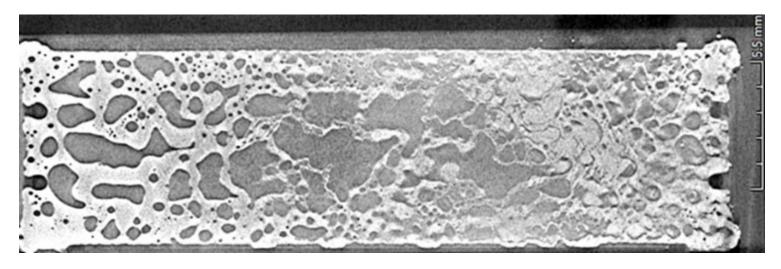
An upgrade of the SOLEIL system was the insertion of a copper slug through the aluminium case of the amplifier modules, at the transistor location, significantly improving the heat transfer, computer simulations shown a 15°C temperature drop

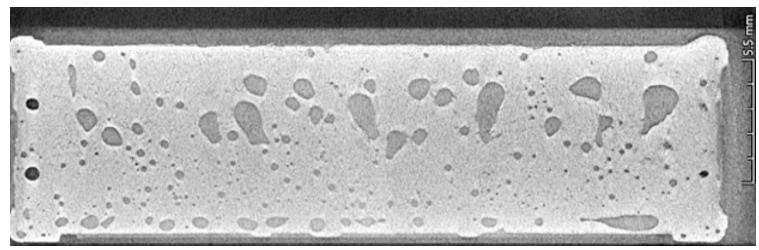


amplifier module with copper slug through the aluminium case

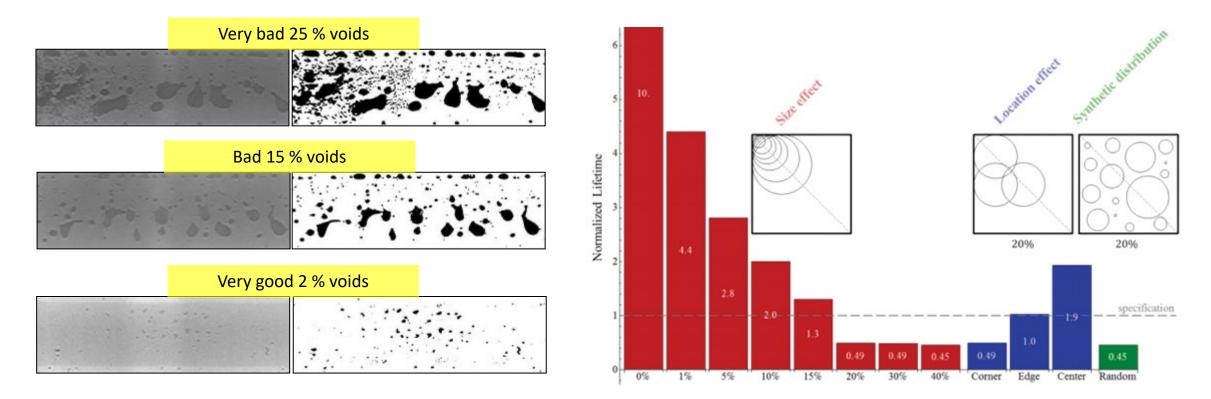
# VOIDS

Thermal effect are closely linked to the way the transistors are brazed to their cold plate



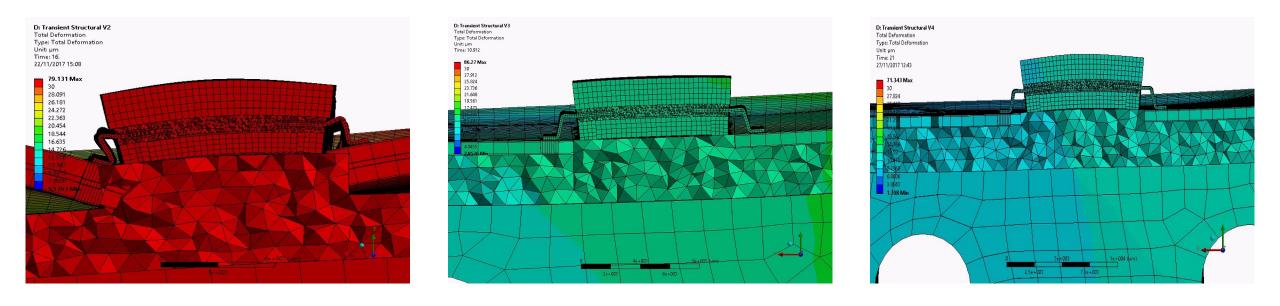


# Voids



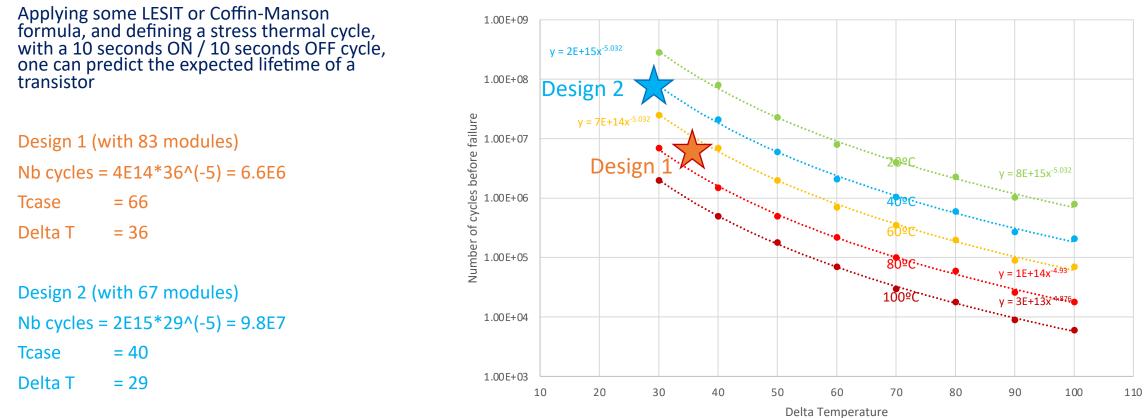
One must develop a very specific way to proceed with the brazing, under vacuum, with a special deposition of the brazing pate, and a specific thermal ramp up and ramp down in order to minimize the number and the shape of voids

# Thermal stress on PCB & transistors



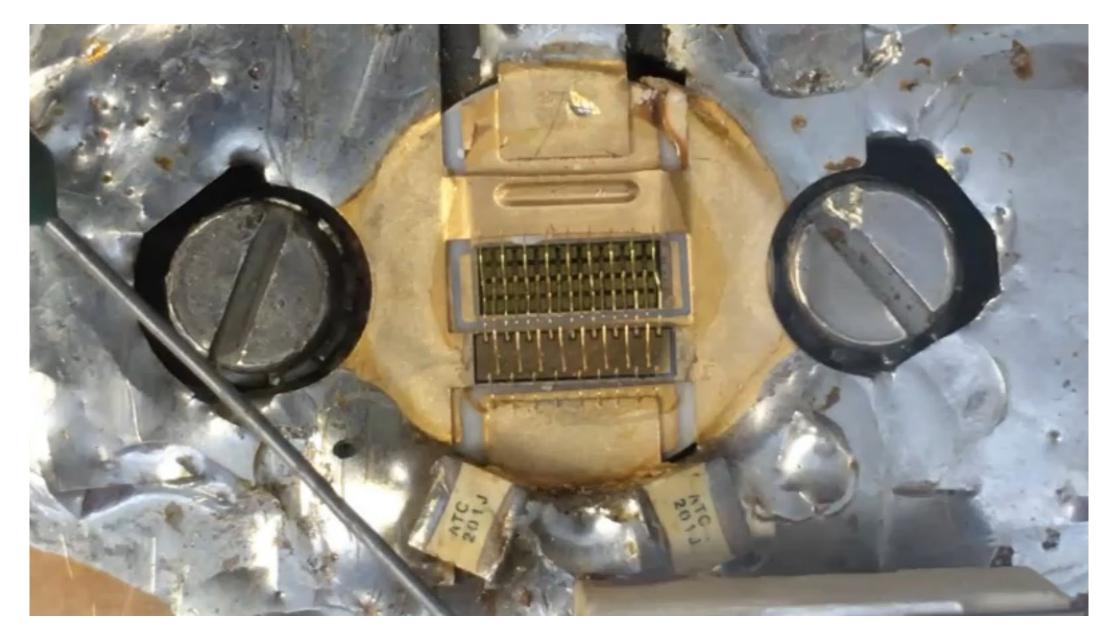
Regarding the cycling of your machine, thermal stress can damage your transistor to PCB link Careful simulations are mandatory to define the best design

# Lifetime thermal improvement



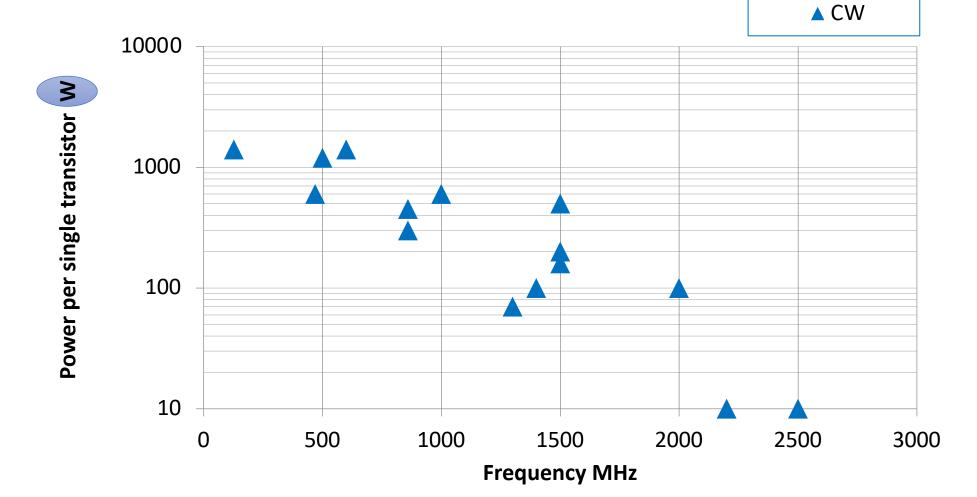
#### LESIT

#### Improvement factor =8.2E7/7.5E6 = **15**



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## Transistors available from industry



# Transistor power ratings

Device	Distance	Power
Phone	20 km	2 W
Microcell	2 km	10 W
Macrocell	20 km	50 W

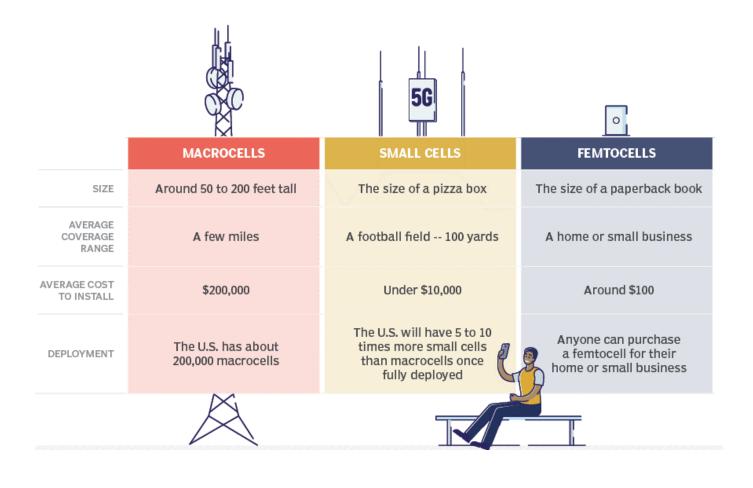
#### Voltage limits

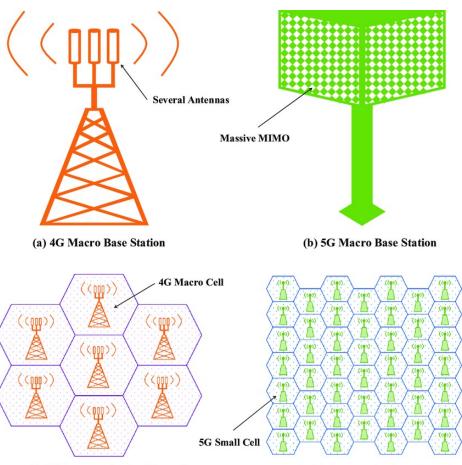
	2002	Since 2006
900 MHz	41 V/m	
1800 MHz	58 V/m	3 V/m
2100 MHz	61 V/m	



The tendency is to increase the number of smaller cells in order to keep the phone battery autonomy, increase the data bandwidth, and reduce the exposition of population to too high electromagnetic fields

# Macro cells vs Small cells vs femtocells

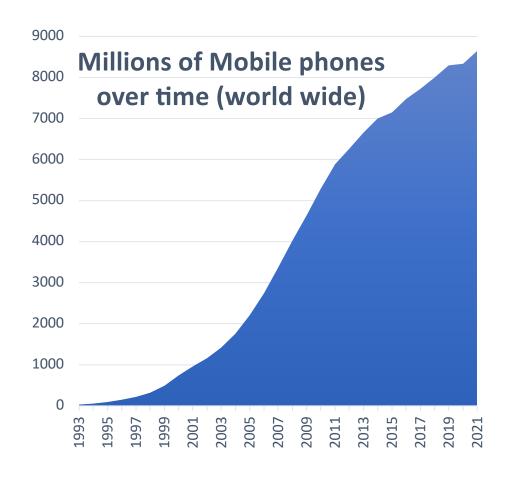


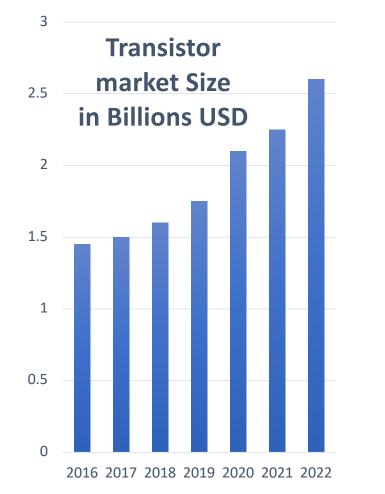


(c) 4G Communication Network

(d) 5G Communication Network

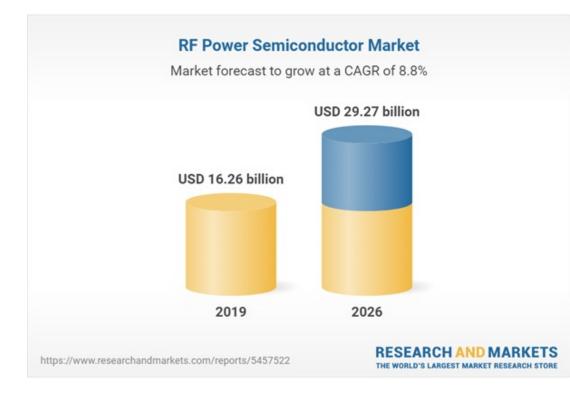
# A few numbers to situate RF transistors in accelerators



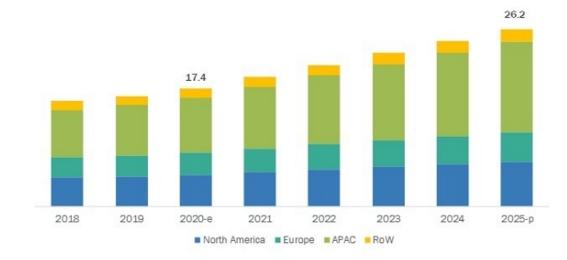


Some of the Key Players Ampleon **Analog Devices BONN Elecktronik** Broadcom Pte. Cree **General Dynamics** Infineon Integra MACOM Maxim Integrated Mitsubishi NoleTec NXP Semiconductors Qorvo Qualcomm **Skyworks Solutions STMicroelectronics Tagore Technology Thales Alenia Space** Toshiba

# A few numbers to situate RF transistors in accelerators



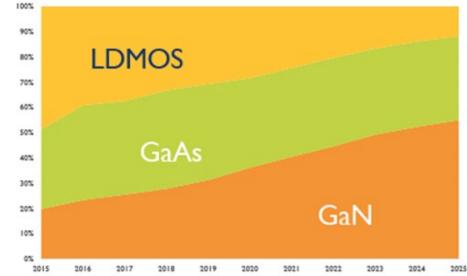
RF SEMICONDUCTOR MARKET, BY REGION (USD BILLION)



# A few numbers to situate RF transistors in accelerators

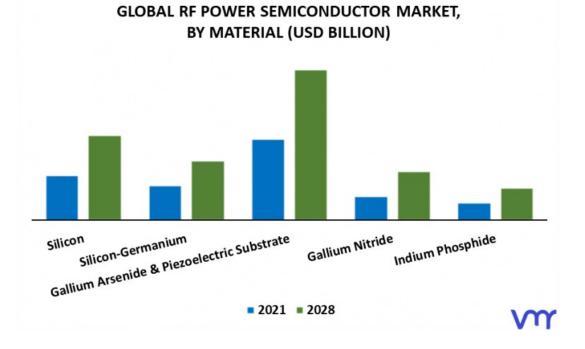
#### RF power device market, in value Breakdown by technology

Only considering RF power semiconductors above 3W, excluding such applications as mobile PAs (Source: RF power market and technologies 2017: GaN, GaAs and LDMOS, July 2017, Yole Développement)



#### Source: RF Power Semiconductor Market Trends From Yole Développement

Patrick Hindle - Editor, Microwave Journal July 11, 2017



100%

# A few numbers to situate RF transistors in accelerators HL-LHC (400 MHz) due in ~ 5 years

1000 W -SOT467B SOT467C SOT502A SOT502B SOT502E SOT502F (9.7 x 5.8 x max. 4.7 (mm)) (20.3 x 5.8 x max. 4.7 (mm)) (34.0 x 9.8 x max. 4.7 (mm)) (20.6 x 9.8 x max. 4.7 (mm)) (20.6 x 9.8 x max. 4.7 (mm)) (34.0 x 9.8 x max. 4.7 (mm)) 100 W -Silicon GaN/SiC LDMOS SOT1121E SOT539A SOT539AN SOT539B SOT539BN SOT1121A Power (41.2 x 10.2 x max. 4.7 (mm)) (41.2 x 10.2 x max. 4.7 (mm)) (32.3 x 10.2 x max. 4.7 (mm)) (32.3 x 10.2 x max. 4.7 (mm)) (34.0 x 9.8 x max. 4.7 (mm)) (20.6 x 9.8 x max. 4.7 (mm) 10 W GaN/Si SOT1135A SOT1135B SOT1214A SOT1227A SOT1227B SOT1228A (20.3 x 9.8 x max, 4.7 (mm)) (9.8 x 9.8 x max, 4.7 (mm)) (34.0 x 9.8 x max, 4.7 (mm)) (14.0 x 4.1 x max, 3.7 (mm)) (5.1 x 4.1 x max, 3.7 (mm)) (29.0 x 5.8 x max, 5.2 (mm) 1 W GaAs SOT1228B SiGe (17.3 x 5.8 x max. 5.2 (mm)) 1 GHz 10 GHz 100 GHz

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Frequency

FCC (400 MHz to 800 MHz) due in ~ 15 years

# Transistor power ratings – *personal view* of future perspective (CWRF 2016, updated 2022)

Transistor supplier main business will not be higher power per transistor

Conclusion: below a GHz, 1 kW per transistor (LDMOS) seems (to me) a very good goal

8.5 Billions Smartphones in 2021

90 Millions Femtocell stations 2016

7 Millions Macrocell stations 2017

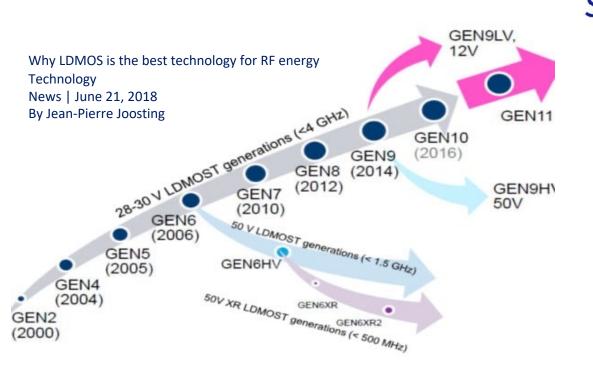
NXP Semiconductors revenue in 2020 was \$8'600 Millions

#### Assumption (with a lot of simplifications)

Machine	# RF stations	Power	# 1 kW LDMOS
FCC	1'000	1 MW	1'000'000
Cost of a	LDMOS	~ \$100	
Total cost	of FCC	~ \$100 N	Aillion
Over mini	mum 5 years		
of constru	iction	∼ \$20 N	1illion per year

#### RF for accelerators could be 20 / 8600 = 0.2 % of main suppliers revenue

# Drain voltage





SYNCHROTRON. elementary 600 W 300 Vdc / 30 Vdc converter board

Evolution of the transistors market is quick

This is still a volatile market (as tubes have been a century ago)

Drain voltage is increasing with the development of transistors, and the Drain supply used with a generation of device could not suit the next generation (moving from 12V to 24 V to 30 V to 36 V to 48 V to 50 V to 60 V to 80 V to 100 V)

Changing the transistor will not be the only challenge, either it will be under used as keeping the previous power supply, or power supply voltage will have to be upgraded

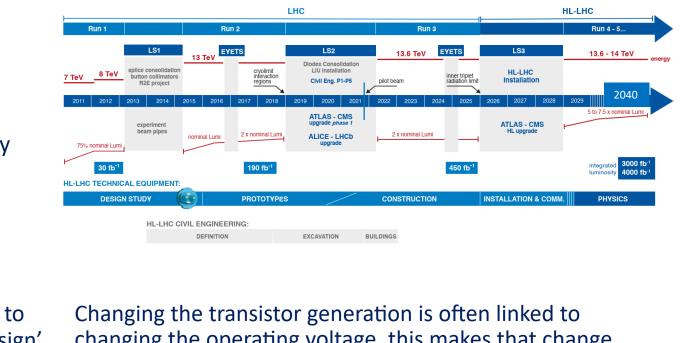
# Obsolescence

When we started SPS SSPA in 2017, the chosen transistor was the 'best for new design' quoted by the transistor supplier

Beginning 2022, we received a 'Last Buy Order' email...

(the same with other labs, within 3-5 years, 'best to use' transistors turn to be 'do not use for new design', and to 'obsolete' item...)

The difficulty with Accelerators is that when we buy a new amplifier, it has to last 20-25 years



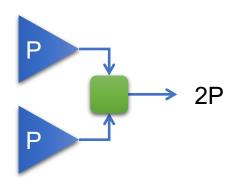
changing the operating voltage, this makes that change out of budget

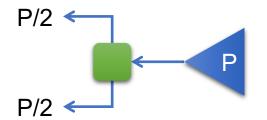
The amplifier architecture should then be designed such that the amplifier will last the 20 years without major upgrade

LHC / HL-LHC Plan

# **Combiners & Splitters**

RF power combiners and RF power splitters are the same items





Resistive power splitters & Combiners Cheap and easy to build Use of resistor to maintain the impedance Power limitation and losses induces by the resistors  $(\rightarrow \text{ not used in high power})$ 

Hybrid power splitters & Combiners Use RF lines Low levels of loss Limitation by the size of the lines

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# Combination

3 dB combiner is very common for RF power combination at these frequencies since the 70's

If one correctly adjusts the phases and the amplitudes, equations show that

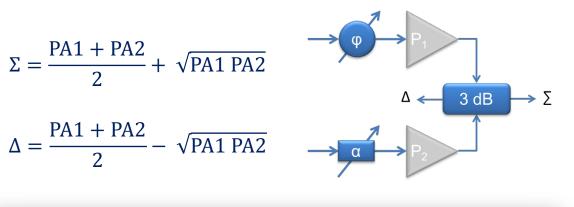
With PA1 = PA2 = PA3 = PA4 = P then

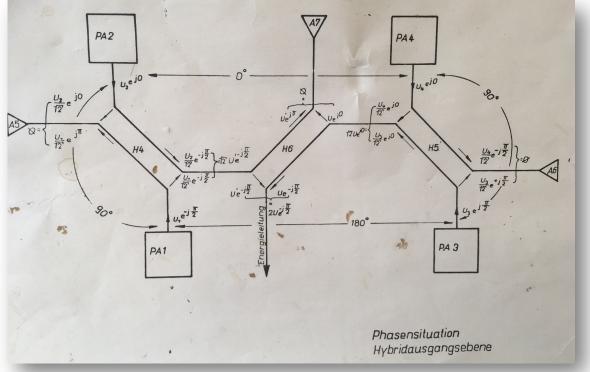
**Pout = 4 P** 

Load A5 = A6 = A7 = 0

In case **one** amplifier is **stopped** (PA1 for example), then

Pout = (9/16) 4P = **2,25 P** Load A5 = 0,5 P Load A7 = 0,25 P

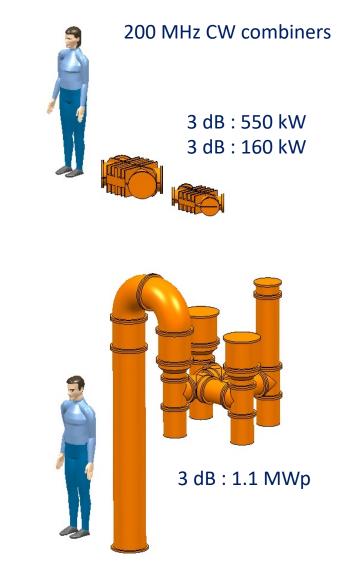




# Combination



#### CERN SPS 16:1 combiner @ 200 MHz



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# **Combiners & Splitters**

#### Low loss T-Junction

 $Z_{c} \sqrt{N}$   $\lambda/4 \qquad Z_{c}$   $Z_{c} \qquad \lambda/4 \qquad Z_{c}$   $\lambda/4 \qquad Z_{c}$ 

With  $Z_{\lambda/4} = Zc \sqrt{N}$ We have a N-ways splitter





CRISP (Sept 2010)

Jörn Jacob (ESRF) asked for support to the development of cavity combiners receiving funding from the EU as work package WP7 in the framework of the FP7/ESFRI/CRISP program

CERN immediately supported it

CRISP, 2<sup>nd</sup> yearly meeting, PSI 18-19 March 2013

ESRF cavity combiner

144:1 Cavity combiner for CERN-LIU-SPS

In addition, please refer to two excellent papers from ESRF at IPAC

MOPC005-IPAC11, 352.2 MHZ – 150 kW Solid State Amplifiers at the ESRF

WEPFI004-IPAC13, Commissioning of first 352.2 MHz - 150 kW Solid state amplifiers at the ESRF and status of R&D



CLUSTER OF RESEARCH INFRASTRUCTURES FOR SYNERGIES IN PHYSICS



#### HIGH POWER SOLID STATE RF AMPLIFIERS USING CAVITY COMBINERS

Jörn Jacob & Michel Langlois, ESRF



The radius of a cylindrical resonator is set so that the E010 mode frequency is 200 MHz

A fine tuning is provided by a piston located at the bottom of the resonator

The electrical field is vertical and maximum at the resonator symmetry axis

The magnetic field is circular and maximum close to the resonator wall

These field patterns are perfectly suited for coupling many inputs loops protruding through the cavity wall and coupling out the power with a capacitive plate

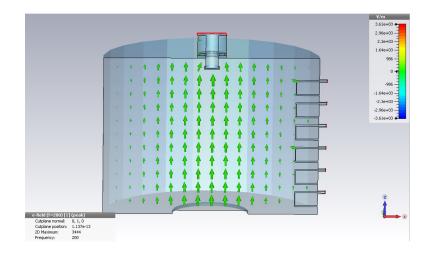
All input signals must have the same amplitude and phase

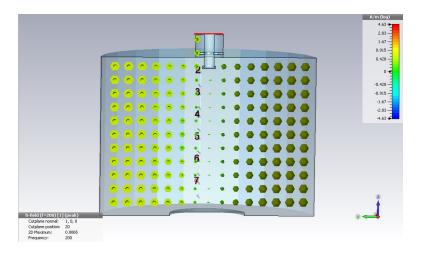
Attention should be paid to several issues

There is a possibility of resonance on another mode for the same frequency, the best suspect being H111, it can be controlled with the height of the resonator

At high power, the electric field in the vicinity of the output coupling may be high and cause breakdowns

- There may be crosstalk between adjacent loops
- Input and output coupling must be determined so that  $\beta$ out=n\* $\beta$ in, n being the number of inputs
- Behaviour of the combiner for harmonics



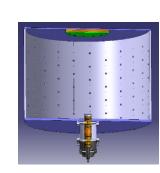


Feb 2013, within the CRISP programme, we received a report from ESRF, describing how to build our LIU-SPS 200 MHz 144:1 cavity combiner

We completed the calculations and build a first prototype

We also completed the coupling loop design, the tuning design, and the output coupling element and we finally obtained at fantastic 144:1 cavity combiner with only 0,1 dB insertion loss, as calculated







# VHPCC (Very High Power Cavity Combiner)

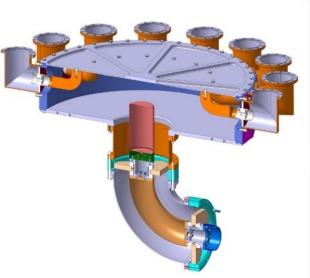
We also designed a VHPCC (Very High Power Cavity Combiner)

The goal was to have 16:1 combiner with inputs in the hundred of kW range and an output in the MW range

The 'cavity' has been machined from a single piece of metal

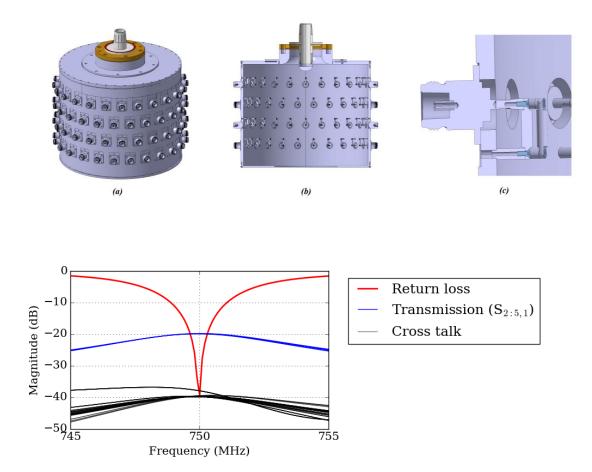
We tested it in reverse mode, as we had no hundred kW class amplifiers to test it in forward mode, and we checked that we had a perfect distribution between the test loads

With 1.26 MWp input, we obtained 78 kW +/- 1 kW and the losses were less than 10 kW









With our latest combiner, the body is comprised of four main pieces

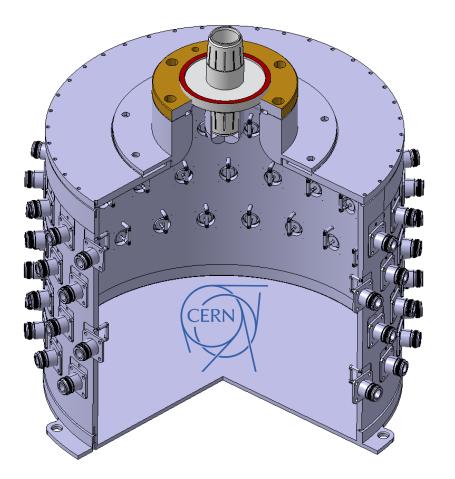
a tube

- a bottom plate
- a top plat
- an output probe housing

The tube has machined holes compatible with N-type solder cups, the bottom plate has an indentation for disc tuning and the output probe housing is compatible with a standard EIA 3-1/8" flange.

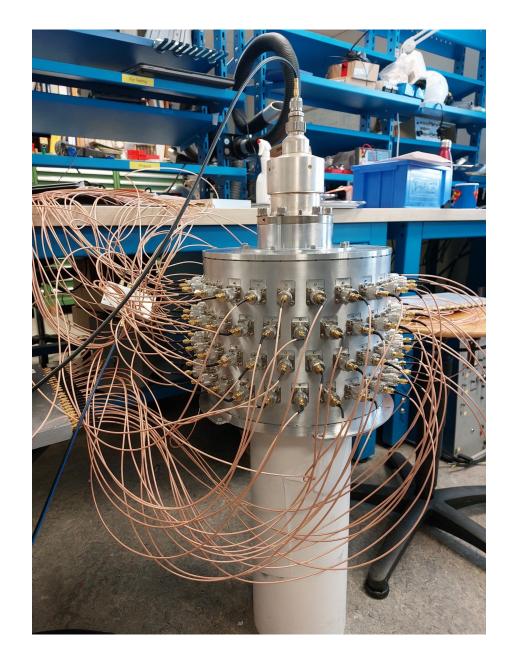
The return loss of the output port is  $\leq$  -20 dB between over a 1 MHz bandwidth

The transmission between the 96 individual inputs and output is -19.84  $\pm$  0.05 and the cross talk between the inputs is < -35 dB



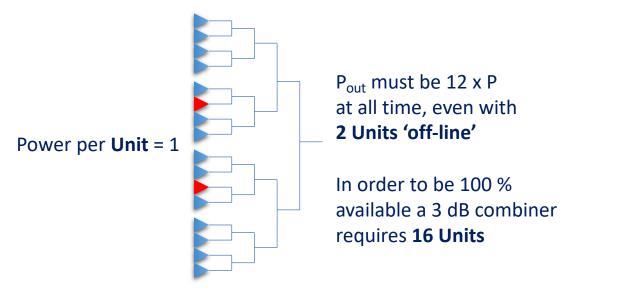
We measured it with only – 0.15 dB insertion losses

(even being made in aluminium)



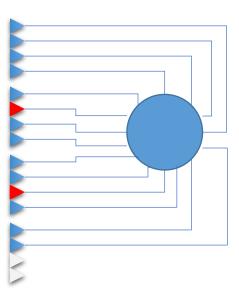
# Redundancy

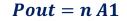
In order to ensure 100 % availability, given a *Redundancy*, the technology of the combining system will define the number of **Units** 



P<sub>out</sub> must be 12 x P at all time, even with **2 Units 'off-line'** 

In order to be 100 % available a cavity combiner only requires 14 Units



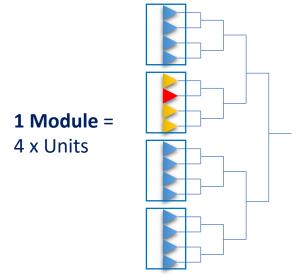


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 $Pout = \frac{A1 + A2}{2} + \sqrt{A1 \cdot A2}$ 

# Granularity

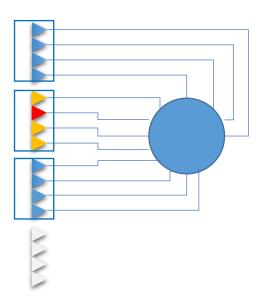
In order to ensure 100 % availability, given a *Granularity*, the technology of the combining system will define the number of **Modules** 



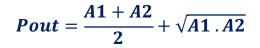
P<sub>out</sub> must be 8 x P at all time, even with **1 Unit 'off-line'** 

In order to be 100 % available a 3 dB combiner requires **16 Units**  P<sub>out</sub> must be 8 x P at all time, even with 1 **Unit 'off-line'** 

In order to be 100 % available a cavity combiner only requires 12 Units



Pout = nA1



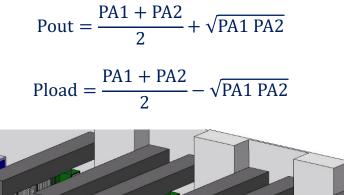
# Redundancy & Granularity

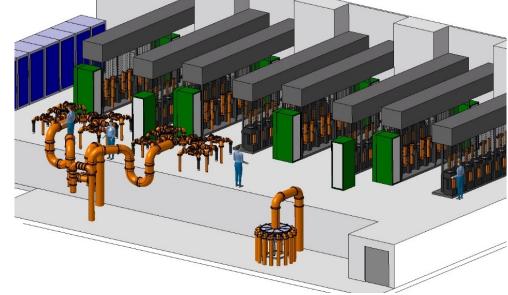
Cavity combiner is one of the best way to achieve power density with multiple sources

A fantastic intrinsic characteristic of a cavity combiner is that if you present a short circuit at a missing input, the output is the exact sum of all remaining inputs

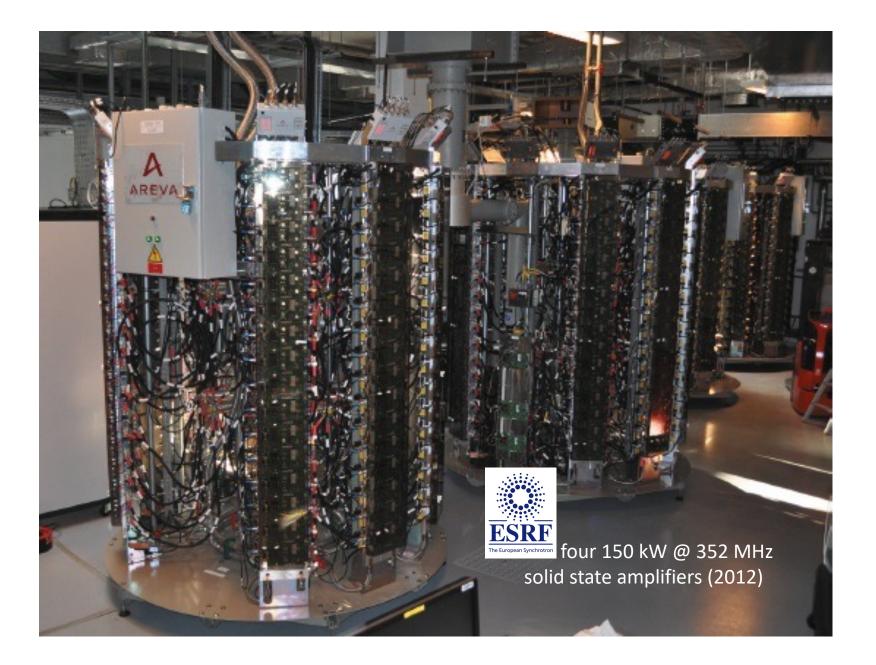
16:1 combiner with	3 dB combiner Pout	Cavity combiner Pout
0 missing input	16 P	16 P
1 missing input	14 P	15 P
4 missing inputs	9 P	12 P

3 dB Combiner (given the phases and amplitudes are correct)











## CERN 2 x 16 x 160 kWp @ 200 MHz tower solid state amplifiers (2022)

## Power density





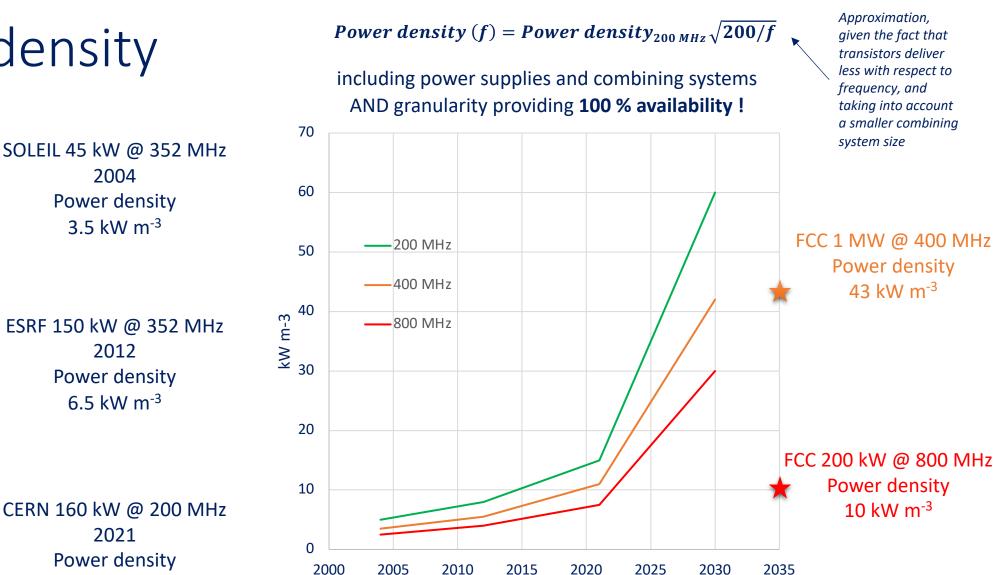
ESRF 150 kW @ 352 MHz 2012 Power density 6.5 kW m<sup>-3</sup>

2004

Power density 3.5 kW m<sup>-3</sup>



CERN 160 kW @ 200 MHz 2021 Power density 15 kW m<sup>-3</sup>

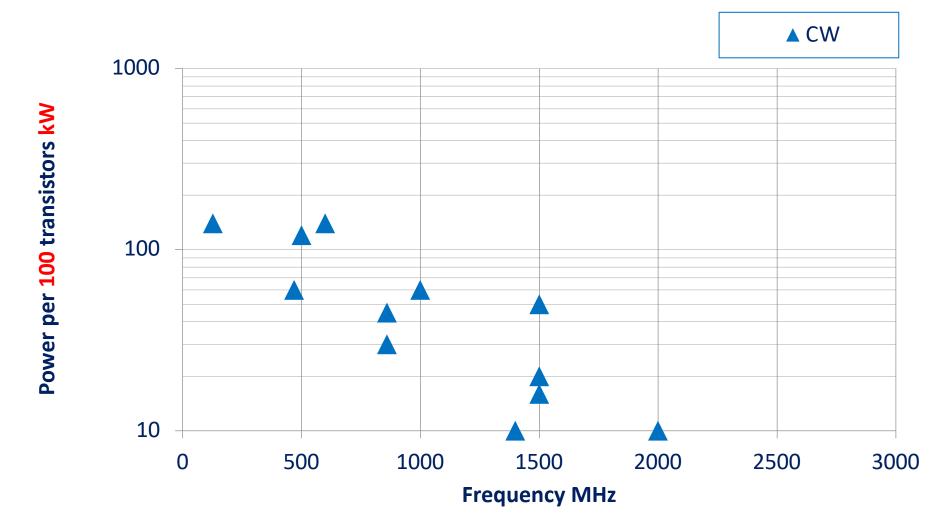


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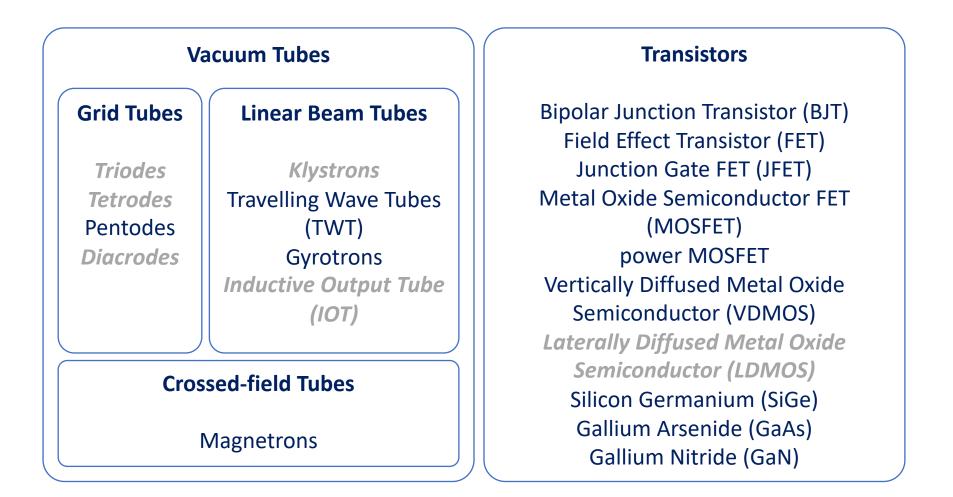
RF Power generation, eric.montesinos@cern.ch, CERN RF Amplifiers & Couplers

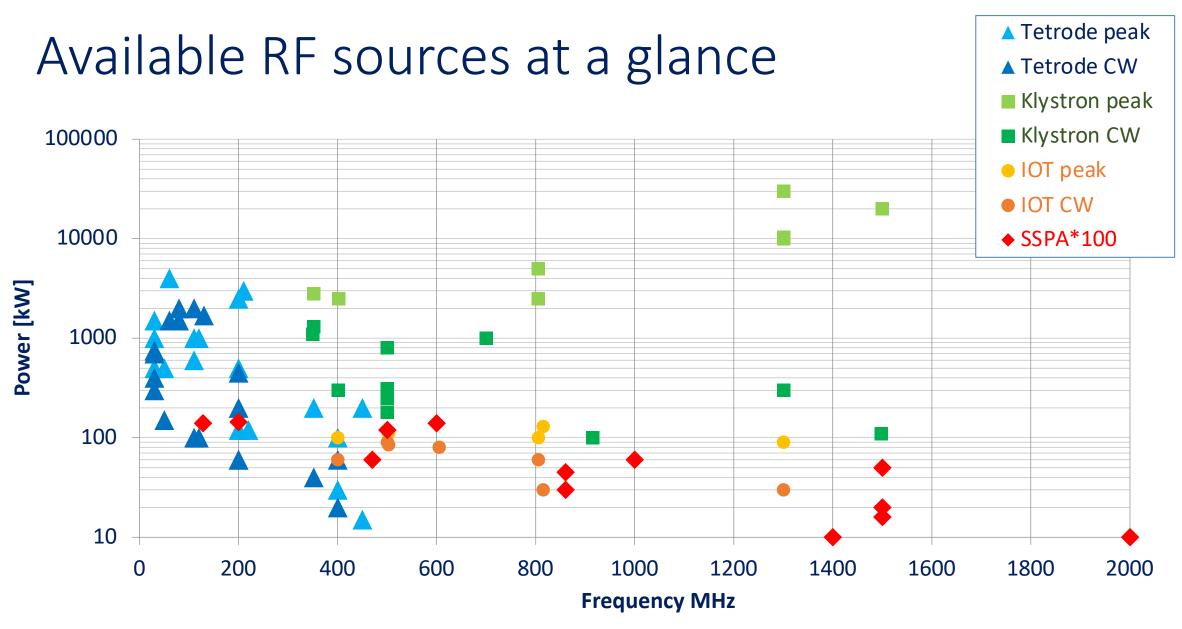
Year

### Transistors available from industry



## RF power source classification





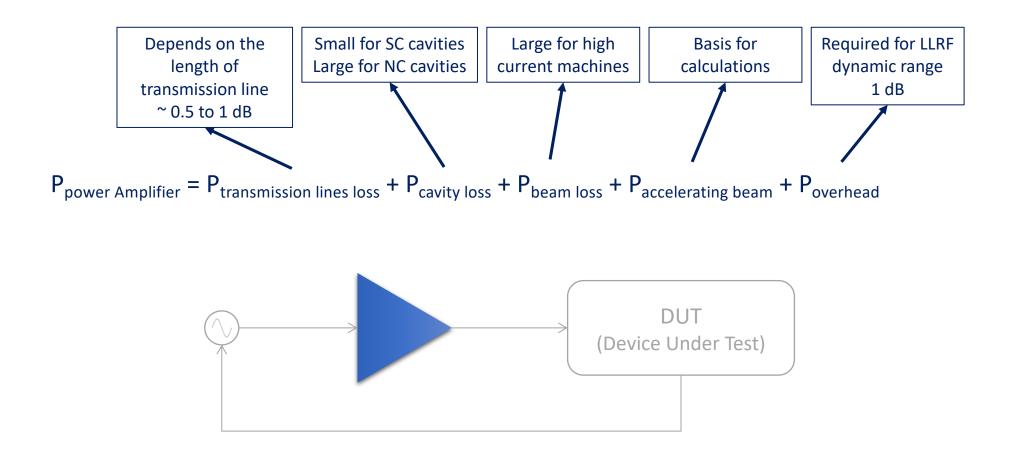
### Good Machine =

(when my boss does not hear about it)

### Efficiency \* Reliability \* <u>AVAILABILITY</u> \* Experienced team \* **k**

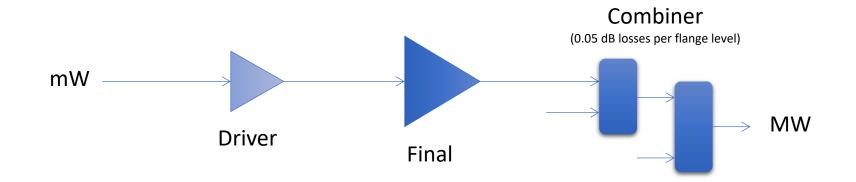
RF/DC efficiency Overall efficiency Including peripherals & building HVAC Oversize Acquisition cost Quantity of spares Obsolescence Overhead Preventive Maintenance Operation costs Manpower managementEverythingAge profileElseTrainingI missed

### **RF** Power Amplifier



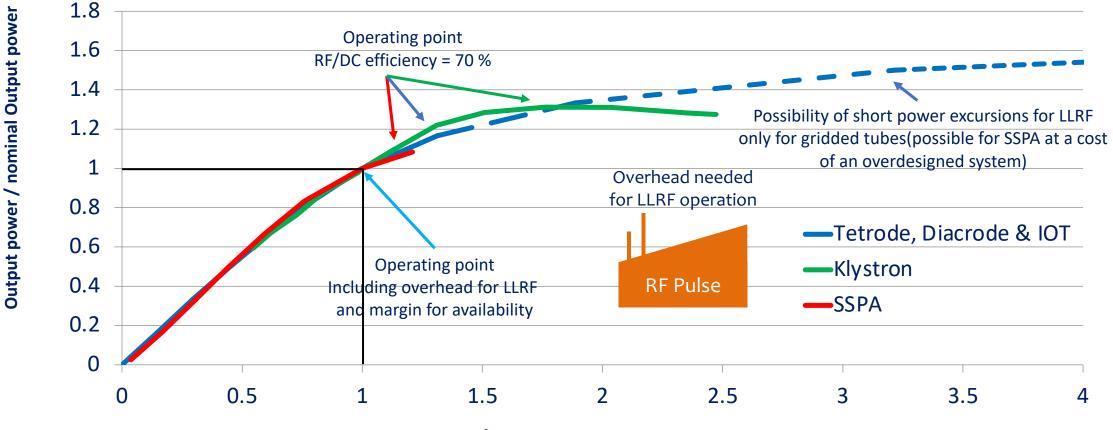
## High Power options

Final	Voltage	Driver	Gain	Power per unit	Combiner (for 1 MW)
Tetrode	15 kV	6.2 kW	13 dB	135 kW	8:1
Klystron	100 kV	10 W	50 dB	1 MW	-
IOT	40 kV	320 W	23 dB	65 kW	16:1
SSPA	50 V	5 W	23 dB	1100 W	1024:1



### Overhead and maximum power

### Grid tubes, Klystrons, SSPA



### Input power / nominal Input power

## Tetrodes, Diacrodes, IOT

Overhead needed for LLRF operation

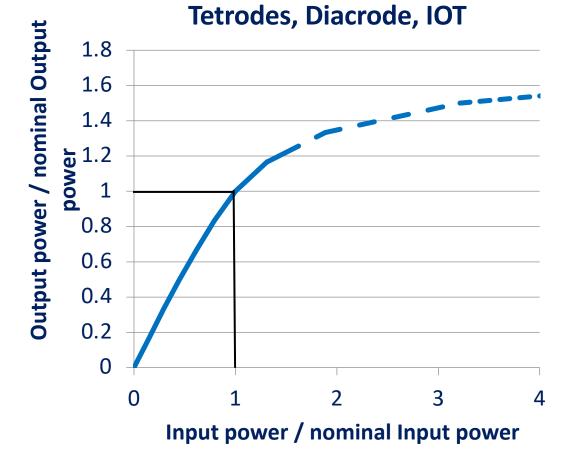


A great advantage of gridded tubes is that they allow overdrive without damage

Thanks to that, they can be operated very close to their nominal point

Tetrodes & Diacrodes are limited in frequency (max ~ 400 MHz), not IOT

Lower gain, some more stages, addition of limiting parameters



# Klystrons

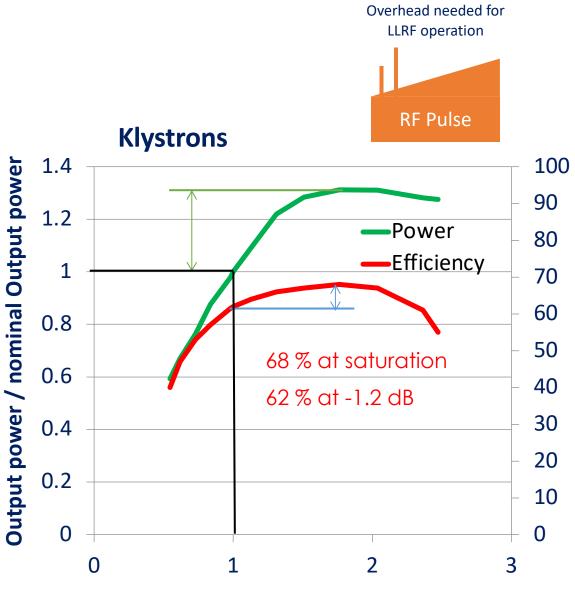
### Output power reduces if we go over saturation (nominal) point of operation

Need to operate lower than nominal point of operation

Loss of efficiency

Double cost (acquisition + operation)

Phase stability is given by construction from HV stability (very expensive)



### Input power / nominal Input power

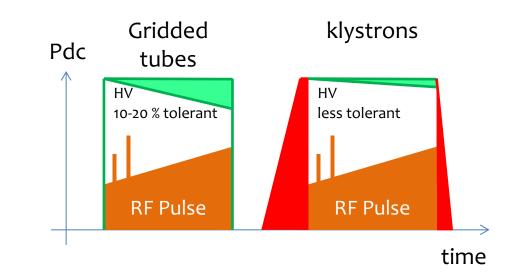
### **HVPS**

For gridded tubes HVPS is very simple

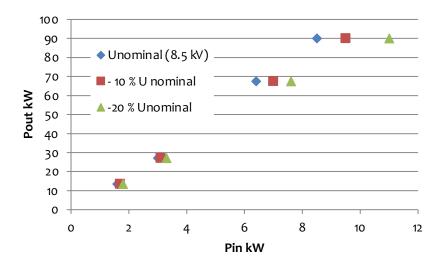
No RF -> idle current (can be zero in class B or class C)

Even if HV is drooping, the LLRF will impose output power, and tetrode remains able to deliver requested Power

Stability of the klystron is much more dependent on stability of the HVPS as any drop will result on different acceleration, and length of drift tube remains the same, it means a phase variation



### RS2004 tetrode



### SSPA



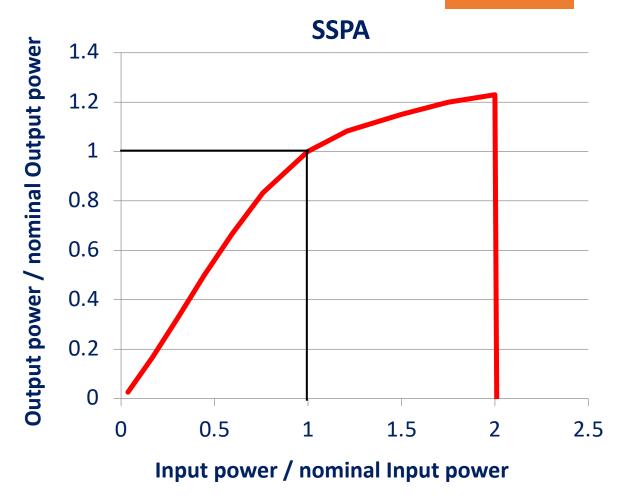
**RF** Pulse

Destruction in case of large overdrive (+ 3 dB) longer than  $\sim$  100  $\mu s$ 

Hard protection limit are needed, could be built in, but then it is complex to manage for LLRF, so we try to have a good LLRF protection system

Overhead must be perfectly and correctly defined

Overhead very costly (compare to gridded tubes)



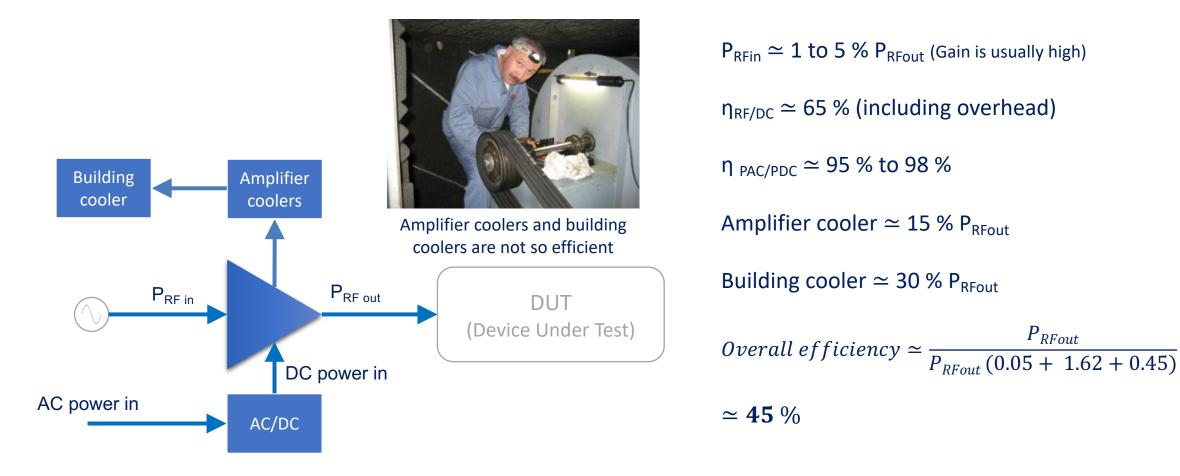
## A few values

RF source type Numbers for lower than 0.5 GHz range	Gain range	Maximum peak output Power per unit	Rise time	Pulse length range	Repetition rate range	Maximum output power CW	Efficiency at working point	High voltage needs
	[dB]	[kW]		[ms]	[Hz]	[kW]	[%]	[kV]
Tetrode	15	4000	ns			1500	70	10 – 25
Diacrode	15	3000	ns	Almost whatever requested (depends on HVPS design)		2000	70	20 – 30
ЮТ	20	130	ns			85	70	36 – 38
MB-IOT	20	1300	ns			150	70	50
Klystron	>50	3000	ns			1000	60	100
SSPA	20	0.1	ns			0.1	70	0.05

Reminder: Grid modulates RF, No RF means No current, direct impact onto efficiency

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# Overall Efficiency $\simeq \frac{P_{RFout}}{P_{ACin} + PR_{Fin} + Pc_{oolers}} \simeq 45\%$



## Availability

### Case of an injector

SPS is an injector for LHCRF is 4.5 MW for 30 % of the timeAC to RF efficiency is 42 %SPS electrical consumption is then 3 MVA

LHC is consuming 99 MVA for its magnets

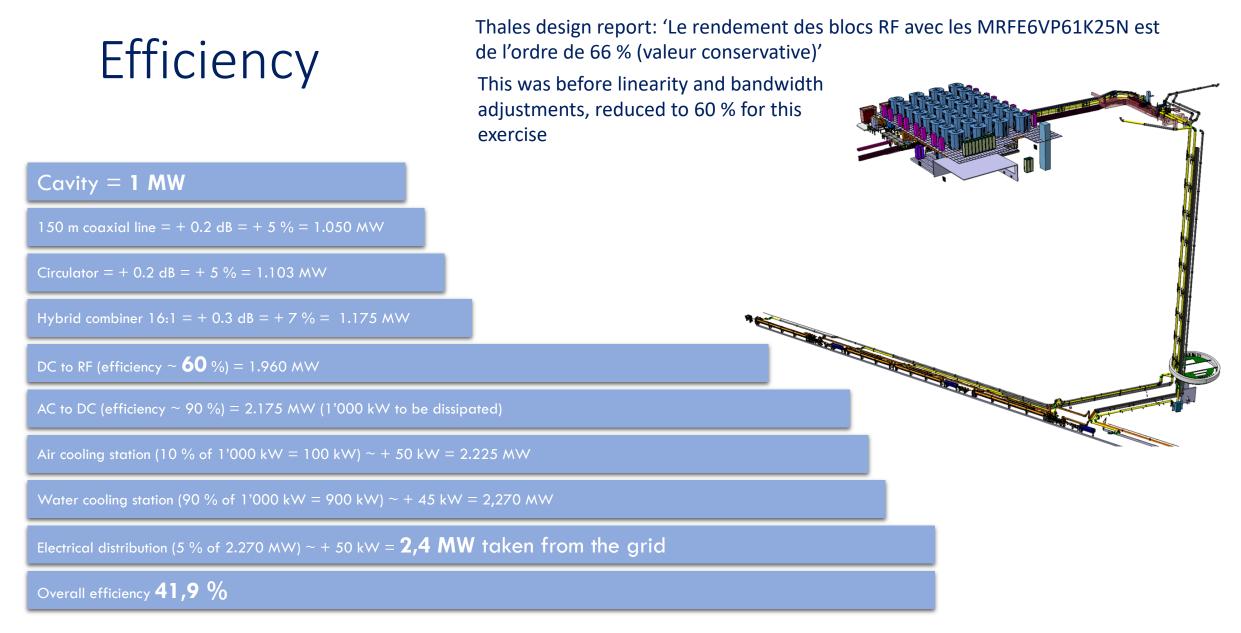
Main parameter for SPS is availability

### Case of a CW machine

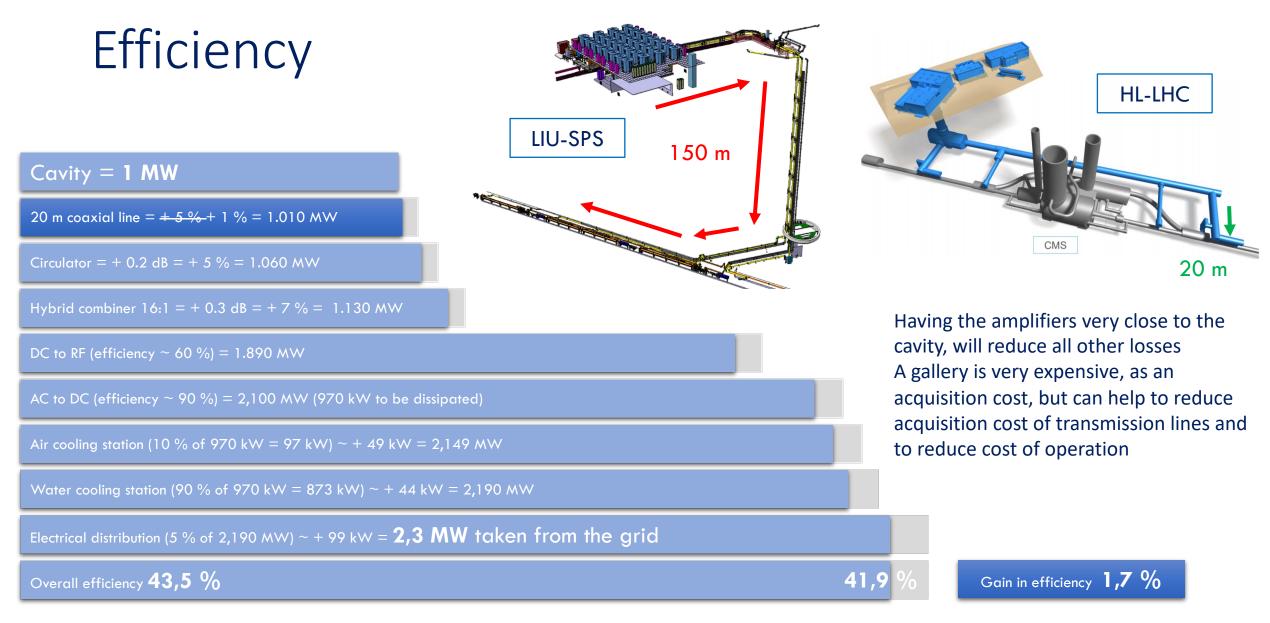
FCC will be 1000 RF power sources of 1 MW each RF will be CW

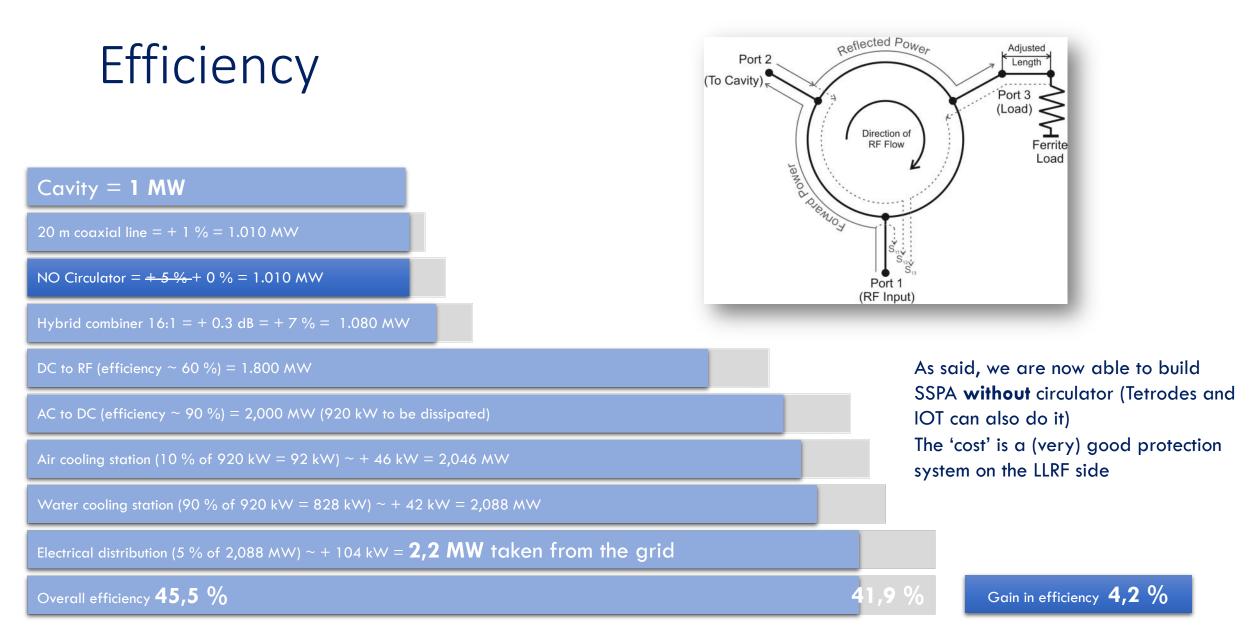
Availability will be thanks to redundancy in the number of cavities and RF power stations

AC to RF will be the main challenge for RF power generation regarding FCC and other big CW machines

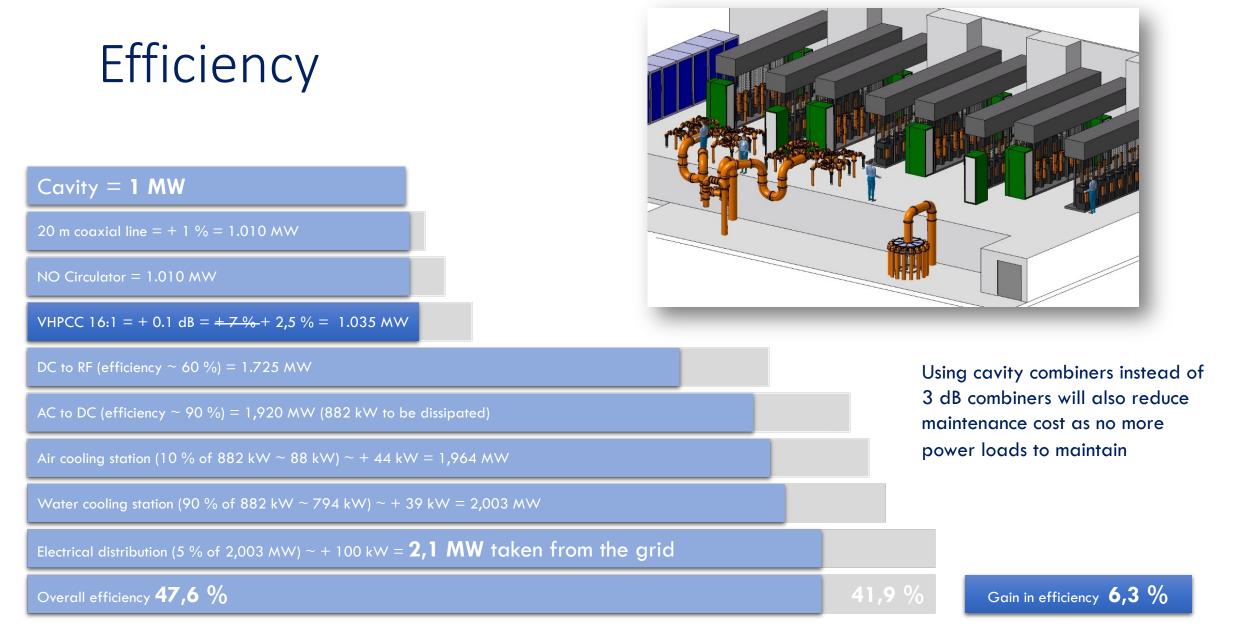


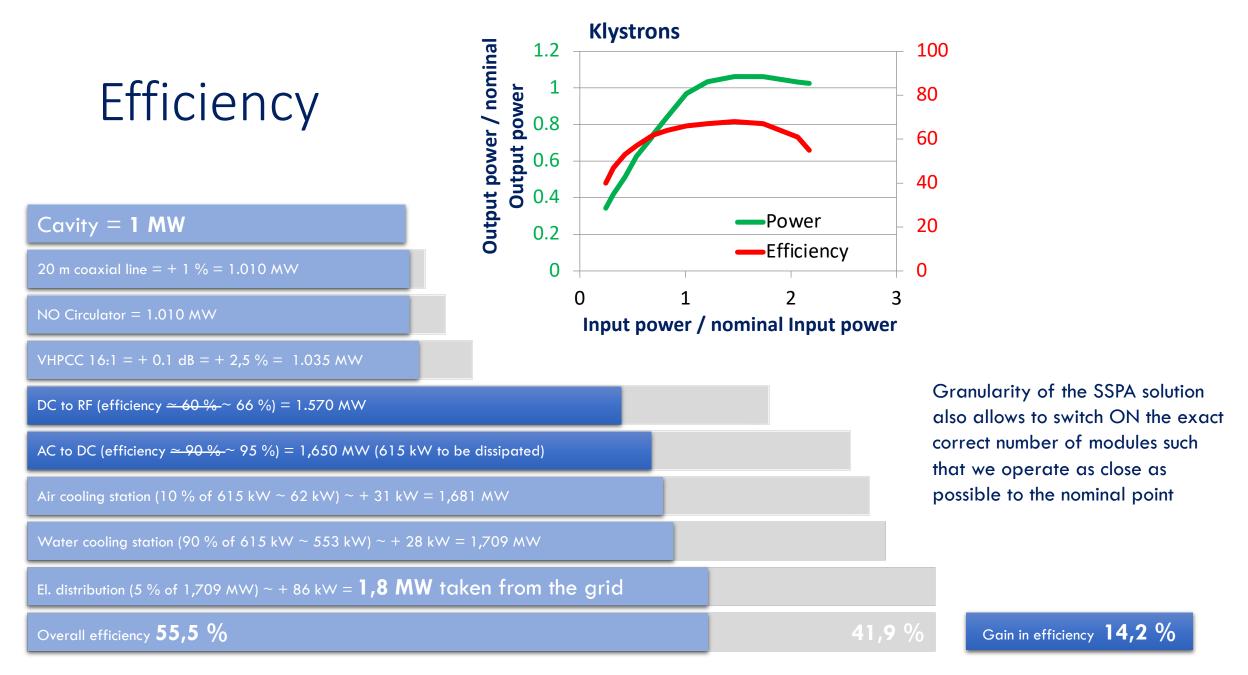
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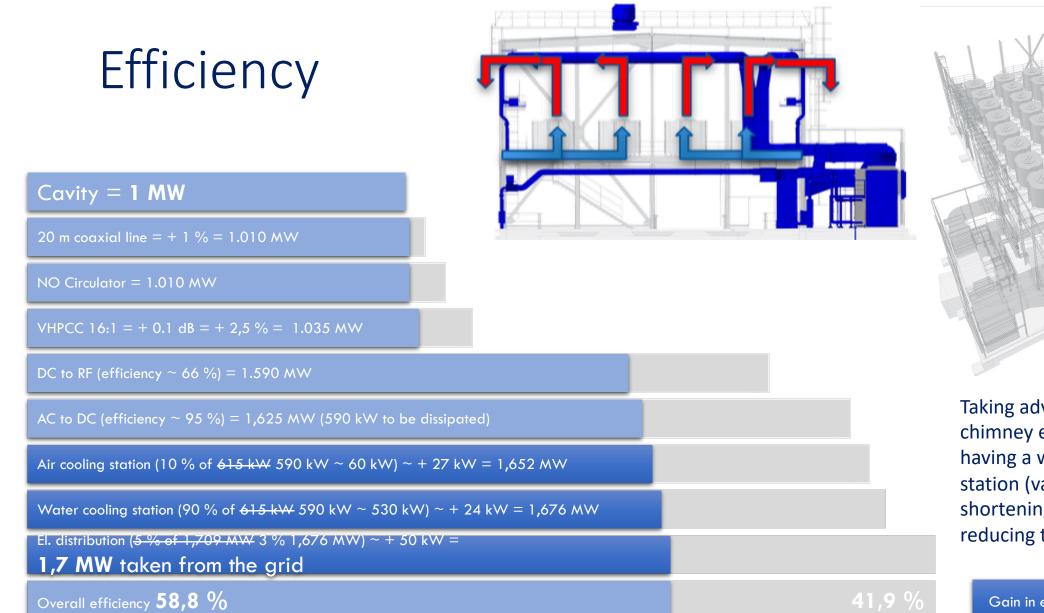




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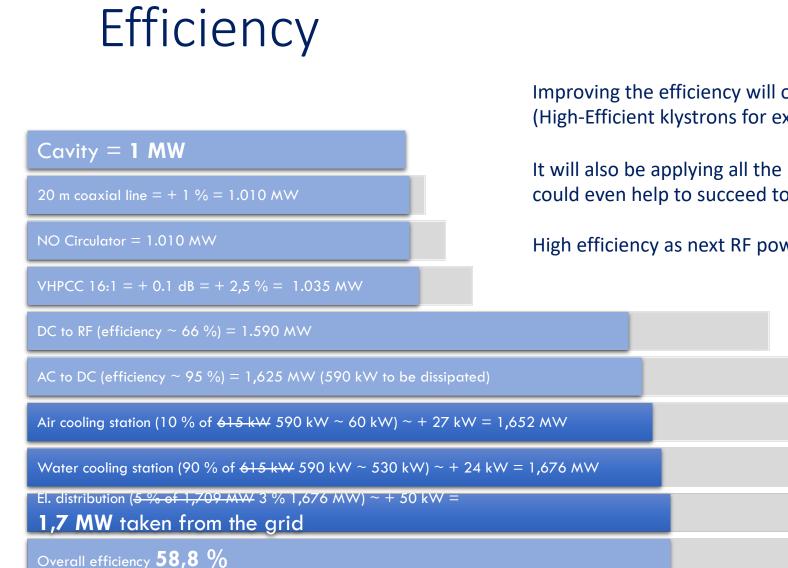




Taking advantage of the natural chimney effect of the tower, having a well-defined water station (variable speed), and shortening the LV cables will help reducing the remaining losses

5 m from HV to LV

Gain in efficiency 16,9 %



Improving the efficiency will of course be improving the DC to RF efficiency (High-Efficient klystrons for example)

It will also be applying all the principles listed, and some additional others that could even help to succeed to reach higher numbers (we are working it out)

High efficiency as next RF power generation is probably the next key challenge

## Conclusion 1/2

As Tube market perspectives are decreasing, the community is moving to SSPA However, keep in mind that Tetrodes, IOTs, MB-IOTs, Klystrons, HE-klystrons are still very interesting

SSPA is a very quickly evolving market, all of us must witness the market evolutions

Labs should focus R&D where industrials need us, with respect to our specific needs

# Conclusion 2/2

We plan to launch (or we even already launched) R&D on

**Combining systems**, this will reduce footprint and increase power density; plenty of ideas, cavity combiners, DNA waveguide progressive combiners, RF transmission combiners, Gysel combiners, multi layers waveguides combiners

Availability, including granularity, hot swappable modules, oversizing, embedded spares

Efficiency, next key parameter, must be grid AC to RF for fair comparison

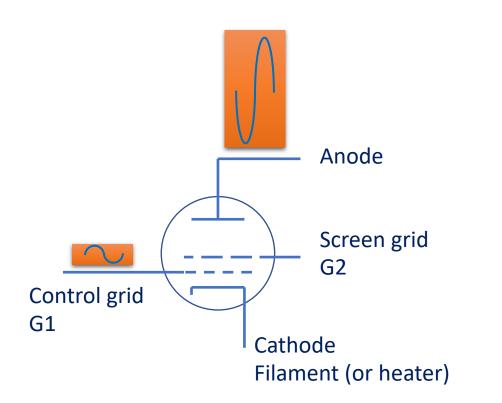
Low cost circulators, at small power level ~kW and high-power level ~MW

**Cost optimization**, asking the correct architecture

Mass production optimization, asking for the correct parameters

**Close follow-up** of new technologies available in large series production (SiC, GaN, High Voltage GaN, GaAs, 2D transistors...)

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### Thank you very much

They did not know it was impossible, so they did it (Mark Twain)

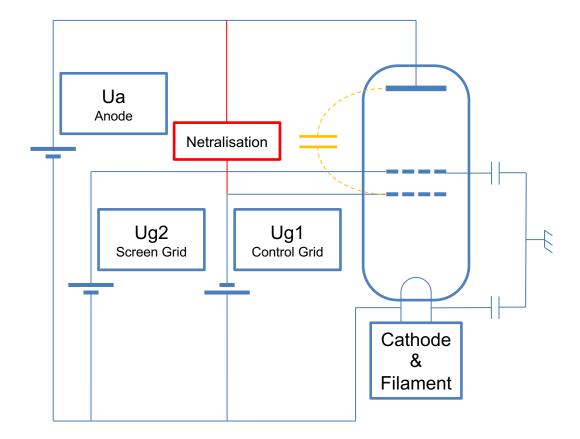
Simplicity is the ultimate sophistication (Leonardo da Vinci, 500 years ago)

### References

# Spare slides

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### How to use tetrodes



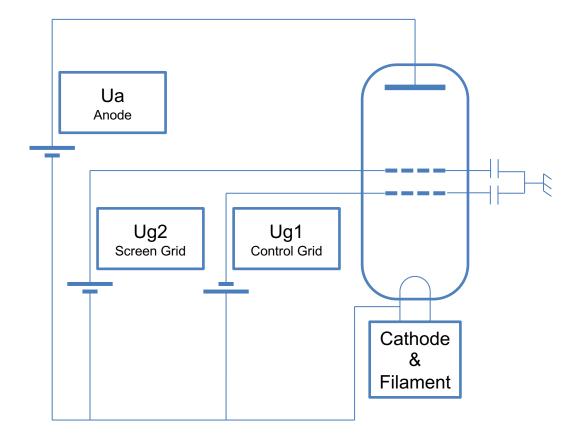
Cathode based or Grounded cathode Main advantage High gain Drawback neutralization circuit required

Typically used with tetrodes in MW amplifiers and audio amplifiers

#### Gain is only limited by RF losses

Neutralization circuit is to be adjusted to cancel G1-Anode capacitance

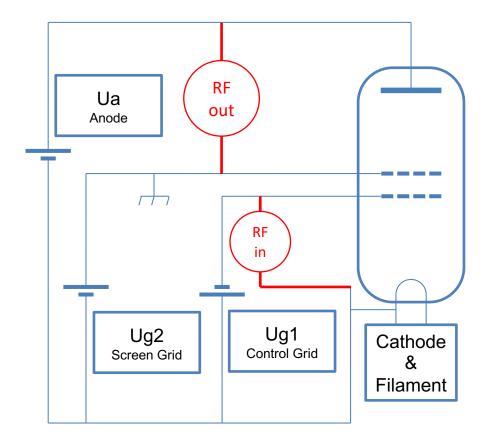
### How to use tetrodes



Common Grid or Grounded grids Main advantage Stability Drawback less amplification

Typically used with triodes amplifiers Grids held at ground isolate input from output

### How to use tetrodes



Grounded screen-grid

Main advantage reduced control grid power dissipation

Configuration used with the large MW range CERN SPS RF amplifiers

# Klystron tutorial SLAC

### The Klystron:

A Microwave Source of Surprising Range and Endurance

George Caryotakis

Stanford Linear Accelerator Center, Stanford University, Stanford CA 94309

The rf current produced by the bunched beam, moving from left to right, causes the output cavity (the "extended interaction" circuit to the right of the illustration above) to "ring" at its fundamental frequency. The current induced at the output circuit produces a voltage across it, which slows the beam down, converting its kinetic energy to rf energy in the cavity, and dispersing the bunches. Power is taken out by a waveguide (not shown). The electrons shown between bunches detract from good efficiency. More electrons can be directed toward the bunches by inductively tuned cavities placed before the output circuit (as the single TM01 resonator shown above), or by one or more 2nd harmonic cavities upstream. Space charge forces prevent tighter bunches from being formed. These forces increase with **beam perveance**, which is defined as:



Hence, the lower the perveance, the tighter the bunching and the conversion efficiency.

## Klystron tutorial SLAC

A *gap resistance Rg* must be chosen to optimize the gap voltage for good conversion efficiency. Its value depends on the coupling coefficient M between beam and circuit, and on the ratio of rf to dc current, I1/I0. M and I1/Io are usually determined by simulation. An empirical formula for the gap resistance Rg is:

$$Rg = \frac{V0}{I0} \frac{1}{M^2 \frac{I_1}{I_0}}$$

The required gap resistance and the cavity R/Q determine how tightly the output cavity is to be coupled to the output waveguide (or how low the Qe can be). R/Q is proportional to the ratio of the square of the gap voltage to the energy stored in the cavity.

$$Q_e = \frac{R_g}{\frac{R}{Q}}$$

A low Qe implies better circuit efficiency and wider bandwidth for the klystron. Good design calls for a high coupling coefficient and R/Q, either of which results in a low Qe. Low-perveance klystrons have good efficiency, but because of a higher Rg, have narrower bandwidth and lower **output circuit efficiency**.

$$\eta = \frac{Q_0}{Q_0 + Qe}$$

In pulsed, high-peak power klystrons, it is essential to minimize the surface gradients at the output circuit to avoid *rf breakdown*. A single cavity is often unsuitable and "extended" circuits must be employed. Their function is to develop the required interaction voltage over a longer distance to reduce surface gradients.