## **Rectilinear Cooling Channel Status**



Science & Technology Facilities Council ISIS Neutron and Muon Source

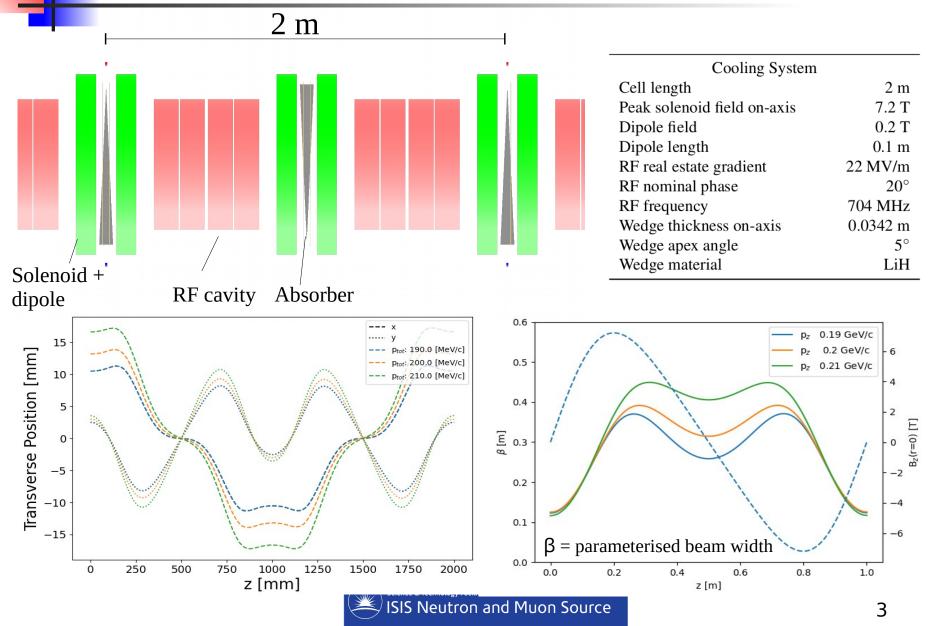
#### C. T. Rogers ISIS Rutherford Appleton Laboratory



- Acceptance is a crucial part of the cooling optimisation
  - Acceptance of solenoid lattices is not well understood (by me)
  - i.e. no "easy" formula for the acceptance
- Looking at acceptance scalings
  - Scaling with momentum
  - Scaling with beta
- Just looking at solenoids
  - No dipoles
  - No RF
  - No wedges
  - Assume the other stuff is a (small) perturbation

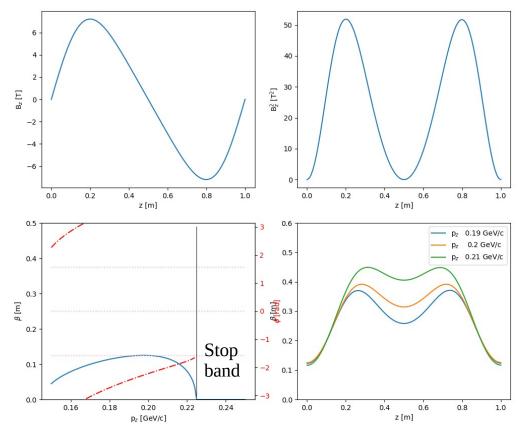


## Preliminary Cooling Cell Concept



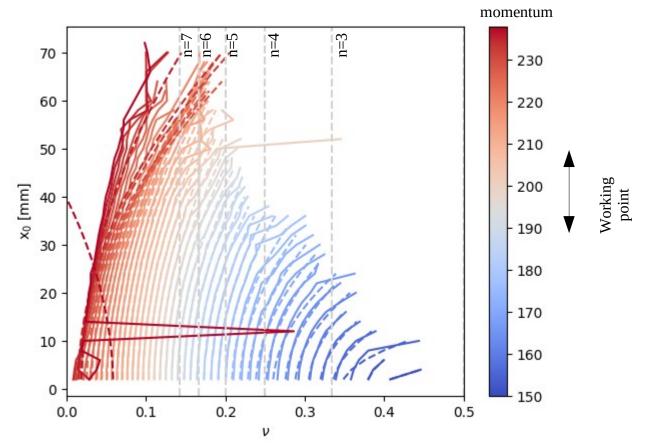
 $\int B^2(z) dz = 24.66 \text{ T}^2 \text{ m}$ 

**Optics** 



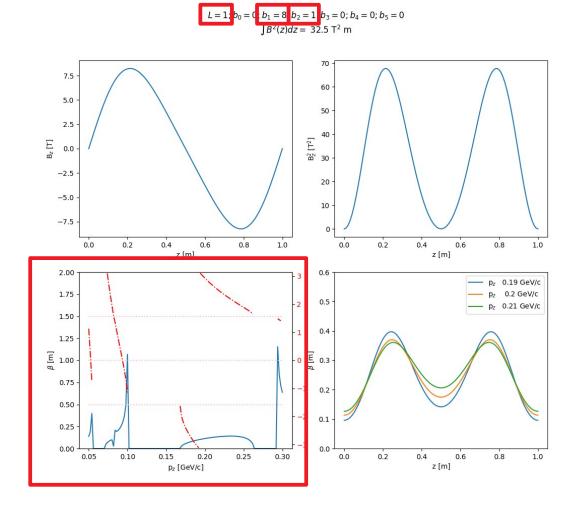
Note optics dependence on momentum

#### Detuning – vs momentum



- Tune dependence on amplitude
  - Particle initial coordinates are (x,px,y,py) = (x0, 0, 0, 0)
  - Momentum scan, indicated by colour

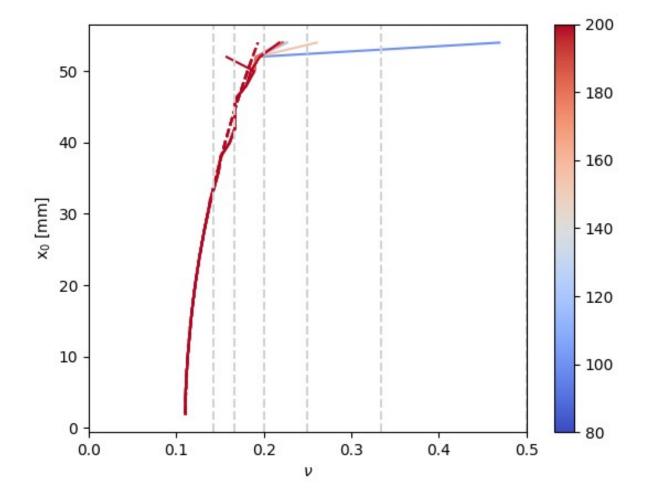
## Momentum scaling (movie 1)





### Momentum scaling

Scales perfectly



### Acceptance

• Normalised Amplitude ~  $x^2$  0 0  $A_{\perp}^2 = \frac{1}{\beta_{\perp}} \left( x^2 + y^2 \right) + \beta_{\perp} \left( \frac{\mathcal{P}_x}{\mathcal{P}_z} + \frac{\alpha_{\perp}}{\beta_{\perp}} x + \frac{\mathcal{L}}{\beta_{\perp}} y \right)^2 + \beta_{\perp} \left( \frac{\mathcal{P}_y}{\mathcal{P}_z} + \frac{\alpha_{\perp}}{\beta_{\perp}} y - \frac{\mathcal{L}}{\beta_{\perp}} x \right)^2,$ 

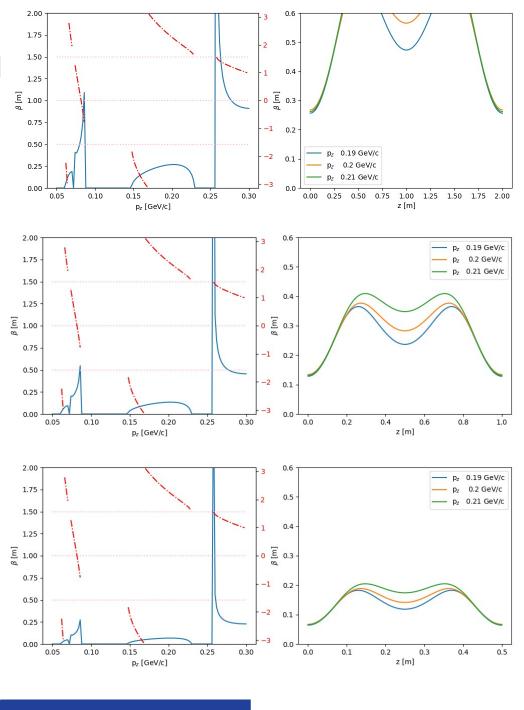
Transverse beta - constant

- Acceptance is constant with momentum
- Probably obvious from equations of motion
  - $d\underline{p}/dz = q d\underline{x}/dz \times \underline{B}$



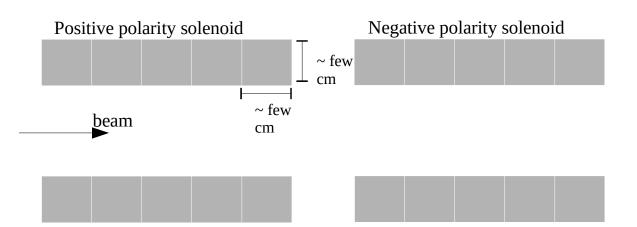
## **Beta Scaling**

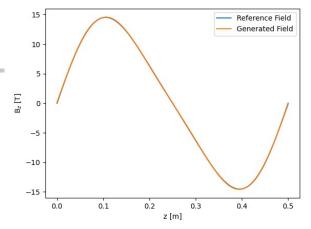
- What about if we scale  $\beta_1$ ?
  - Set B and 1/L

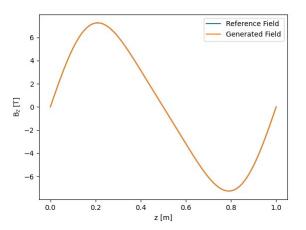


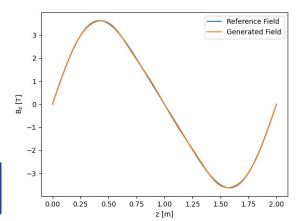
# Beta Scaling

Use "pixel" model to generate fields in G4BL





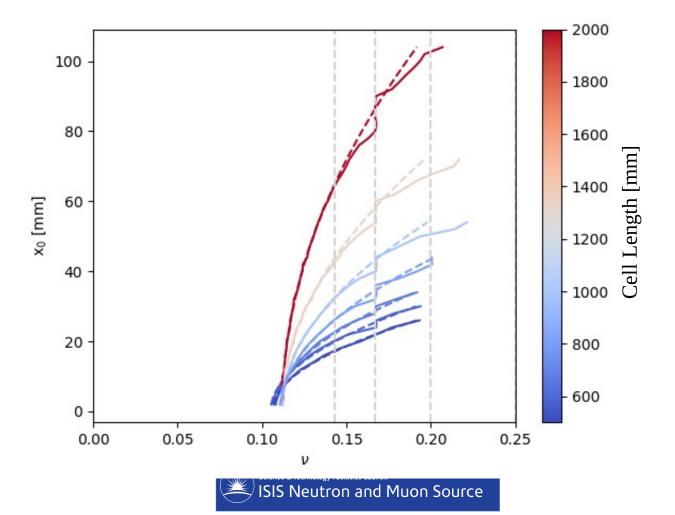






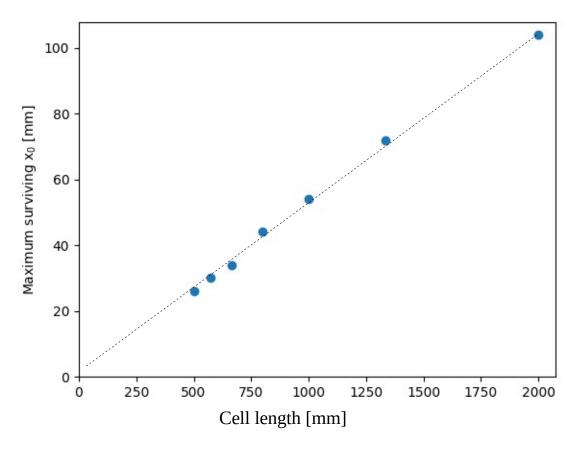
#### Tune dependence

Tune dependence



## Acceptance

- Acceptance
  - Line is for guidance only I haven't properly fitted
  - "cell length" is proportional to  $1/B_z$  and  $\beta_\perp$







- Should be able to phrase the acceptances in terms of theory
- Should use amplitude, not "x<sub>0</sub>"
- Compare with cooling formulae; look at where is the optimum



## ToDo (2)

Mu						Timeline													
				In general deliverables should come in the form of a document.		2023				2024				2025			2026		
OF	jective	Level	WRS	Activity/Deliverables	Responsible	01			04	<b>11</b> C							01.0		, 3 Q4
		Level		· · · · · · · · · · · · · · · · · · ·	Responsible		42	45	04	210	42 G	13 U	4 4	1 92	45	Q4		12 04	5 624
	2	1	2	Rectilinear Cooling															
		2	2.1	Beam physics design		_				_									
		3	2.1.1	Optics design, including tapering, understanding dynamic aperture					.										
		3	2.1.2	Tapering and matching between sections; further optimisation of the lattices		L													
		3	2.1.3	Alignment and tolerances															
		3	2.1.4	Collimation systems and radiation protection															
		3	2.1.5	Radiation load on SC magnets and other equipment															
		3	2.1.6	Liaison with RF and magnets															
		2	2.2	Beam loading															
		3	2.2.1	Effect of beam loading for each cell															
		3	2.2.2	Investigate mitigation, together with RF team															
2		2	2.3	Estimate significance of space charge															
		2	2.4	Beam instrumentation		_													
		3	2.4.1	Preliminary ideas for beam instrumentation - time, energy, beam profile															
		3	2.4.2	Physics design															
		2	2.5	Absorber design															
		3	2.5.1	Estimate magnitude of heat deposition															
		3	2.5.2	Absorber design															
		2	2.6	Engineering integration															
		3	2.6.1	Integration of magnets and RF															
		3	2.6.2	Alignment system															
		3	2.6.3	Integrated thermal design															
		3	2.6.4	Vacuum systems															

