EFT interpretation of $b ightarrow d\,\ell\ell$ decays

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Based on 2109.01675 & 2209.04457.

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Rare decays probing BSM physics

• FCNCs are loop and CKM suppressed in the SM.



BSM contributions could be of same size as the SM.

Bonus if ℓ are attached (rare decays):

- SM lepton couplings are flavour universal, LU can be tested.
- If $\ell \neq \ell'$ (zero in the SM), LFC can be tested as well.

Excellent place to search for BSM physics!

EFT approach to rare *B* decays

() Symmetries to build all O_i up to desired dimension (D = 6):

$$\mathcal{H}_{
m eff} \supset rac{4 \; G_{
m \textit{F}}}{\sqrt{2}} \; V_{tq}^{st} V_{tb} rac{lpha_{e}}{4\pi} \sum_{i} c_{i}^{(\prime)} \; O_{i}^{(\prime)} \; , \quad c_{i} = C_{i}^{
m SM(\prime)} + C_{i}^{(\prime)} \; ,$$

$$O_{7}^{(\prime)} = \frac{e}{16\pi^{2}} m_{b} \left(\bar{q}_{L(R)} \sigma_{\mu\nu} b_{R(L)}\right) F^{\mu\nu} ,$$

$$O_{8}^{(\prime)} = \frac{g_{s}}{16\pi^{2}} m_{b} \left(\bar{q}_{L(R)} \sigma_{\mu\nu} T^{a} b_{R(L)}\right) G_{a}^{\mu\nu} ,$$

$$O_{9(10)}^{(\prime)} = \left(\bar{q}_{L(R)} \gamma_{\mu} b_{L(R)}\right) \left(\bar{\ell} \gamma^{\mu} (\gamma_{5}) \ell\right) , \dots$$

- **②** Compute $C_i(\mu_{\rm EW})$ and RGEs to go down $\mu_{\rm low} \approx m_b$.
 - $C_7^{\rm SM}(m_b) pprox -0.3\,, \ C_8^{\rm SM}(m_b) pprox -0.15\,, \ C_9^{\rm SM}(m_b) pprox 4.1\,, \ C_{10}^{\rm SM}(m_b) pprox -4.2 \;.$

($O_i(\mu_{low})$) from non-perturbative techniques (Lattice, LCSR, ...)

Include resonances (or better avoid them).

An intriguing pattern in $b o s \, \ell \ell$ transitions

- Over the past decade a set of tensions with SM predictions has emerged in $b \rightarrow s \, \ell \ell$ transitions:
 - Branching ratios: are below the SM values.
 - **2** Angular obserbables: 4σ deviation from the SM in global fits.
 - **Output LU** ratios: $e \mu$ universality violation has been evidenced by LHCb in R_{κ} , strengthening the trend in measurements of R_{κ} -like ratios.
- Interestingly, 1 3 can be explained consistently together by NP contribution in a single operator:

$$C_9^{(bs)} \cdot O_9^{bs} \approx -1 \cdot (\bar{s}_L \gamma_\mu b_L) (\bar{\ell} \gamma^\mu \ell)$$

• While this strongly points to NP, further scrutiny is required before firm conclusions can be drawn.

Shedding some light on the flavor anomalies

• Differences between $b \rightarrow d \ell \ell \& b \rightarrow s \ell \ell$ in the SM:



(1) CKM matrix elements: V_{td} vs V_{ts} , (2) Light quark masses: m_d vs m_s

$$\begin{split} C_i^{(b \to d)} &\approx C_i^{(b \to s)} , (\text{CKMs factorized in } \mathcal{H}_{\text{eff}}) \\ C_i^{\prime(b \to d)} &\approx \left(\frac{m_d}{m_s}\right) C_i^{\prime(b \to s)} , (O_i^{\prime} \text{ chiral suppression}) \end{split}$$

• A violation would signal additional BSM sources of quark flavor violation (beyond (1) and (2)); an agreement would indicate similar effects as the current flavor anomalies (maybe NP?).

Global fit of $b \rightarrow d \,\ell \ell$ transitions

What observables do we use?

- Branching ratios of rare $b
 ightarrow d \ \mu^+ \mu^-$, γ decays:
 - **1** $B^+ \to \pi^+ \mu^+ \mu^-$ (3 binned), 1509.00414.
 - 2 $B_s^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-$ (full integrated), 1804.07167.
 - (3) $B^0 \to \mu^+ \mu^-$, 2108.09283.
 - $\ \, \bullet \ \, \bar{B} \to X_d \gamma, \ 1005.4087,1503.01789.$
- In total we use 6 observables, compared with $b \rightarrow s \, \ell \ell$ transitions:

$$rac{\# ext{ obs. exp. } (b
ightarrow d\,\ell\ell)}{\# ext{ obs. exp. } (b
ightarrow s\,\ell\ell)} \sim rac{1}{50} ext{ (ideally 1)}$$

$B^+ ightarrow \pi^+ \mu^+ \mu^-$

2209.04457



- Very good agreement (below 1 σ) except for [22, 25] GeV² with 1.6 σ .
- Low- q^2 bin [0.1, 2] GeV², suffers from ρ , ω and ϕ resonances.
- $q^2 \approx 9.5 \text{ GeV}^2 \& q^2 \approx 13.5 \text{ GeV}^2$ suffer from J/ψ and ψ resonances.
- Only include the theoretically clean bins: [2, 4], [4, 6], [15, 22] GeV².

 $B^0_c o ar{K}^{*0} \mu^+ \mu^-$



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$B^0 o \mu^+ \mu^-$ and scalar operators

• In the SM, only the operator O_{10} contributes which yields

$$\begin{split} \mathcal{B}(B^0 &\to \mu^+ \mu^-)_{\text{SM}} = (1.14 \pm 0.12) \cdot 10^{-10} \ , \\ \mathcal{B}(B^0 &\to \mu^+ \mu^-)_{\text{exp}} = (1.20 \pm 0.84) \cdot 10^{-10} \ , \end{split}$$

in agreement with the experimental value 2108.09283. • $\mathcal{B}(B^0 \to \mu^+ \mu^-)$ is sensitive to $O_{10}^{(\prime)}$, $O_S^{(\prime)}$, and $O_P^{(\prime)}$ operators.

$$\begin{split} \frac{\mathcal{B}(B^0 \to \mu^+ \mu^-)}{\mathcal{B}(B^0 \to \mu^+ \mu^-)_{\rm SM}} &= |\mathcal{P}|^2 + |\mathcal{S}|^2 \\ \mathcal{B}(B^0 \to \mu^+ \mu^-)_{\rm SM} &= |\mathcal{P}|^2 + |\mathcal{S}|^2 \\ \mathcal{S} &= \frac{m_B^2}{2 \, m_\mu} \sqrt{1 - \frac{4m_\mu^2}{m_B^2}} \left(\frac{1}{m_b + m_d}\right) \left(\frac{C_{P^-}}{C_{10}^{\rm SM}}\right) \,. \end{split}$$

• Using the current experimental information

$$\begin{split} -1.4 \lesssim C_{10^-} \lesssim 1.9 \quad \text{or} \quad 6.5 \lesssim C_{10^-} \lesssim 9.8 \\ - & 0.05 \lesssim C_{P^-} \lesssim 0.06 \quad \text{or} \quad 0.2 \lesssim C_{P^-} \lesssim 0.3 \\ & |C_{S^-}| \lesssim 0.1 \,, \end{split}$$

• $O_S^{(\prime)}$, and $O_P^{(\prime)}$ are more constrained than $O_{10}^{(\prime)}$ (due to m_B/m_μ) not considered in the global fits.

$ar{m{B}} o m{X}_{m{d}} \gamma$

• The SM prediction for the CP-averaged $\bar{B} \rightarrow X_d \gamma$ branching ratio

$$egin{aligned} \mathcal{B}(ar{B} o X_d \gamma)_{\mathsf{SM}} &= (17.7 \pm 1.7) \cdot 10^{-6} \ , \ \mathcal{B}(ar{B} o X_d \gamma)_{\mathsf{exp}} &= (14.1 \pm 5.7) \cdot 10^{-6} \ , \end{aligned}$$

in very good agreement.

•
$${\cal B}(ar B o X_d\gamma)$$
 is sensitive to $O_7^{(\prime)}$ and $O_8^{(\prime)}$ operators.

$\mathcal{B}(\bar{B} \to X_d \gamma) = \sum_{i=1}^{9} a_i^{(\bar{B}X_d)} w_i^{(\bar{B}X_d)}$	$a_1^{(\bar{B}X_d)}$	$a_2^{(\bar{B}X_d)}$	$a_3^{(\bar{B}X_d)}$
$i{=}1$	1.77	-3.72	-0.91
$w_i^{(\bar{B}X_d)} = \{1, C_7, C_8, C_7^2, C_8^2,\}$	$a_4^{(\bar{B}X_d)} = a_6^{(\bar{B}X_d)}$	$a_5^{(\bar{B}X_d)} = a_7^{(\bar{B}X_d)}$	$a_8^{(\bar{B}X_d)} = a_9^{(\bar{B}X_d)}$
$(C_7')^2, (C_8')^2, C_7 \cdot C_8, C_7' \cdot C_8'$	2.60	0.25	1.22

In units of 10^{-5}

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Fit approach



In practice: * MIGRAD from the Python package iminuit to conduct the numerical minimization.

* Confidence intervals are computed using MINOS algorithm from iminuit.

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One-dimensional fits

scenario	fit parameter	best fit	1σ	2σ	$\chi^2_{H_i,\rm min}$	Pull_{H_i}	$p\text{-value}\ (\%)$
H_1	C_7	0.01	[-0.11, 0.15]	[-0.23, 0.31]	3.87	0.10	56
H_2	C_8	0.31	[-0.31, 1.42]	[-0.82, 4.05]	3.66	0.47	59
H_3	C_9	-1.37	[-2.97, -0.47]	[-7.65, 0.26]	1.23	1.63	94
H_4	C_{10}	0.96	[0.31, 1.74]	[-0.27, 2.88]	1.55	1.53	90
H_5	C'_7	-0.03	[-0.22, 0.19]	[-0.39, 0.39]	3.86	0.12	56
H_6	C_8'	-0.03	[-1.15, 1.11]	[-1.89, 1.87]	3.88	0.02	56
H_7	C'_9	-0.21	[-0.91,0.47]	[-1.63, 1.15]	3.78	0.32	58
H_8	C_{10}^{\prime}	0.18	[-0.40, 0.75]	[-0.99, 1.32]	3.78	0.31	58
H_9	$C_9 = +C_{10}$	0.24	[-0.52, 1.04]	[-1.18, 1.79]	3.79	0.30	58
H_{10}	$C_9 = -C_{10}$	-0.54	[-0.90, -0.20]	[-1.29, 0.13]	1.32	1.60	93
H_{11}	$C'_9 = +C'_{10}$	0.05	[-0.72, 0.79]	[-1.43, 1.45]	3.88	0.06	56
H_{12}	$C_9^\prime = -C_{10}^\prime$	-0.12	[-0.45, 0.23]	[-0.78, 0.58]	3.76	0.34	58
H_{13}	$C_9 = -C'_9$	-1.74	[-3.26, -0.27]	[-4.04, 0.44]	2.08	1.34	83
H_{14}	$C_9 = +C_9'$	-0.55	[-1.29, -0.07]	[-4.13, 0.34]	2.53	1.16	77
H_{15}	$C_9 = -C_{10} = -C_9' = -C_{10}'$	-0.58	[-1.06, -0.20]	[-4.04, 0.12]	1.28	1.61	93
H_{16}	$C_9 = -C_{10} = +C_9' = -C_{10}'$	-0.24	[-0.46, -0.04]	[-0.70, 0.16]	2.47	1.19	78

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What do we learn from the one-dimensional fits?

- The most favored scenario is H_3 NP in C_9 (pull=1.63, p-value=94%), followed by H_4 with NP in C_{10} (pull=1.53, p-value=90%).
- Scenarios relating 2 WCs (H₉,...,H₁₄):
 - H_{10} with LH quarks and LH leptons, $C_9 = -C_{10}$, is preferred by data (pull=1.60, p-value=93%). For comparison, we explore benchmark H_9 , LH quarks and RH leptons $C_9 = C_{10}$, results are close to the SM.
 - 2 We work correlations in $C'_{9,10}$ and find p-values closer to the SM one.
 - [●] We consider $C_9 = \pm C'_9$, where we find similar results (pull≈1.3, p-value≈80%).

* Consistency with the SM, but data shows a clear preference to include NP via C_9 , similar as in global fits to $b \rightarrow s \mu^+ \mu^-$ data. * Future data is very welcome to confirm or refute this pattern!

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Let's further entertain with two-dimensional fits!

scen.	fit parameters	best fit	1σ	2σ	$\chi^2_{H_i, \min}$	Pull_{H_i}	p-v. (%)
H_{17}	(C_7, C_8)	(-0.22, 1.47)	([-0.46, 0.08], [-0.2, 3.73])	([-0.64, 0.36], [-1.36, 4.6])	3.14	0.40	53
H_{18}	(C_7, C_9)	(0.11, -1.55)	([-0.05, 0.34], [-3.05, -0.61])	([-0.18, 1.46], [-10.07, 0.18])	0.77	1.25	94
H_{19}	(C_7, C_{10})	(0.09, 1.1)	([-0.07, 0.28], [0.39, 2.04])	([-0.2, 0.55], [-0.23, 8.64])	1.25	1.10	86
H_{20}	(C_7, C_7)	(0.01, -0.03)	([-0.11, 0.16], [-0.23, 0.19])	([-0.23, 0.31], [-0.41, 0.4])	3.85	0.02	42
H_{21}	(C_7, C'_9)	(0.02, -0.23)	([-0.11, 0.16], [-0.92, 0.46])	([-0.23, 0.32], [-1.64, 1.16])	3.76	0.07	43
H_{22}	(C_7, C'_{10})	(0.02, 0.19)	([-0.11, 0.16], [-0.39, 0.77])	([-0.23, 0.32], [-0.99, 1.35])	3.76	0.07	43
H_{23}	(C_9, C_{10})	(-1.28, 8.34)	([-7.54, 0.71], [6.39, 9.31])	([-9.12, 1.85], [-1.38, 9.79])	1.12	1.14	89
H_{24}	(C'_{7}, C_{9})	(0.08, -1.43)	([-0.2, 0.35], [-2.97, -0.5])	([-0.53, 0.55], [-7.64, 0.26])	1.17	1.13	88
H_{25}	(C_9, C'_9)	(-2.22, 1.18)	([-6.55, -0.63], [-2.99, 2.89])	([-7.58, 0.23], [-3.92, 3.81])	0.87	1.22	92
H_{26}	(C_9, C'_{10})	(-1.83, -0.38)	([-6.58, -0.6], [-1.2, 0.32])	([-7.6, 0.25], [-1.8, 0.99])	0.95	1.20	91
H_{27}	(C'_{7}, C_{10})	(0.06, 1.01)	([-0.19, 0.33], [0.33, 1.92])	([-0.38, 0.55], [-0.27, 2.53])	1.50	1.03	82
H_{28}	(C'_{9}, C_{10})	(0.26, 1.09)	([-0.52, 1.03], [0.34, 2.12])	([-1.32, 1.81], [-0.28, 8.7])	1.44	1.05	83
H_{29}	(C_{10}, C'_{10})	(0.97, -0.04)	([0.3, 1.87], [-1.0, 0.72])	([-0.29, 2.45], [-4.52, 4.48])	1.54	1.01	81
H_{30}	(C'_{7}, C'_{9})	(0.03, -0.28)	([-0.23, 0.28], [-1.15, 0.62])	([-0.45, 0.49], [-2.01, 1.51])	3.77	0.07	43
H_{31}	$(C_{7}^{\prime},C_{10}^{\prime})$	(0.0, 0.18)	([-0.22, 0.23], [-0.45, 0.8])	([-0.4, 0.42], [-1.09, 1.41])	3.78	0.06	43
H_{32}	$(C_{9}^{\prime},C_{10}^{\prime})$	(-0.13, 0.11)	([-1.11, 0.77], [-0.68, 0.89])	([-2.06, 1.57], [-1.41, 1.64])	3.76	0.07	43
H_{33}	$(C_9 = -C'_9, C_{10} = +C'_{10})$	(-1.73, 0.44)	([-3.34, -0.19], [0.04, 0.95])	([-4.1, 0.51], [-0.34, 4.52])	0.88	1.22	92
H_{34}	$(C_9 = -C'_9, C_{10} = -C'_{10})$	(-1.73, 0.05)	([-3.69, 0.18], [-0.4, 0.94])	([-4.59, 1.04], [-0.79, 5.0])	2.07	0.83	72
H_{35}	$(C_9 = +C'_9, C_{10} = +C'_{10})$	(0.6, 2.18)	([0.26, 0.89], [-0.58, 4.77])	([-4.95, 1.19], [-0.92, 5.1])	2.27	0.76	68
H_{36}	$(C_9 = -C_{10}, C'_9 = +C'_{10})$	(-0.56, 0.37)	([-2.02, -0.2], [-1.39, 2.79])	([-1.36, 0.13], [-2.98, 4.04])	1.27	1.10	86
H_{37}	$(C_9 = -C_{10}, C'_9 = -C'_{10})$	(-0.61, 0.16)	([-1.07, -0.22], [-0.26, 0.64])	([-1.82, 0.14], [-0.65, 1.43])	1.19	1.13	88

* Similar pattern as 1D fits, if C_9 present, p-values are large, ~ 90%! * The most favored scenario is H_{18} (pull=1.25, p-value=94%) fitting simultaneously C_7 and C_9 .

2D contours of dipole coefficients



* Excellent complementarity between different observables!
* Improved limits on C₇^(*i*) compared to previous works. 1106.5499
* Data is consistent with the hypothesis of minimal quark flavor violation. 2109.01675 & 2209.04457

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2D contours of $C_{9,10}^{(\prime)}$



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Summary of 2D contours of $C_{9,10}^{(\prime)}$



- Complementarity between the observables is not currently as good as for dipole coefficients, leading to weaker limits on C_9 and C_{10} .
- The branching ratios of $B^+ \to \pi^+ \mu^+ \mu^-$ and $B^0_s \to \bar{K}^{0*} \mu^+ \mu^-$ cooperate to reduce the thickness of the annulus (red area) but do not lift the degeneracy between C_9 and C_{10} .
- The branching ratio of $B^0 \to \mu^+\mu^-$ can help due to its dependence on $C_{10}^{(\prime)}$, however, the present precision is insufficient.
- Note that due to the flat likelihood along the ring (red area) the bestfit point (magenta) is only shown for completeness but has little statistical preference over other points in this flat direction.
- All 2D contours make visible discrete ambiguities, for instance the two yellow bands in C_{10}, C_{10}' .
- To remove all these ambiguities additional complementary observables are necessary.
- Data is consistent with the hypothesis of minimal quark flavor violation.

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Conclusions & Outlook

* Model-independent analysis of rare radiative and semileptonic $|\Delta b| = |\Delta d| = 1$ process.

* Data consistent with the SM, but leave sizable room for NP.

* Same pattern of $b \rightarrow s \, \mu^+ \mu^-$ branching ratios suppressed with respect to the SM, although within larger uncertainties.

* Improving the fit is not just higher statistics, but also of adding observables sensitive to different combinations of WCs.

* Rare $b \rightarrow d \mu^+ \mu^-$ decays can be studied at LHCb, Belle II, and a possible future e^+e^- collider running at the Z.

Thank you!

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