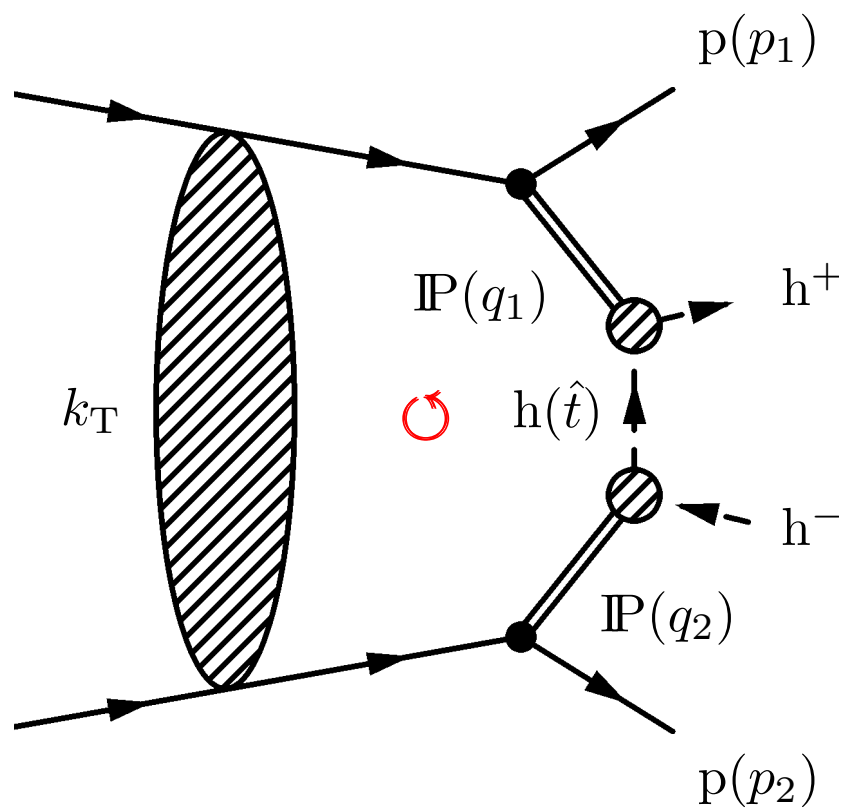


# Central exclusive production (nonresonant processes)



**Ferenc Siklér**

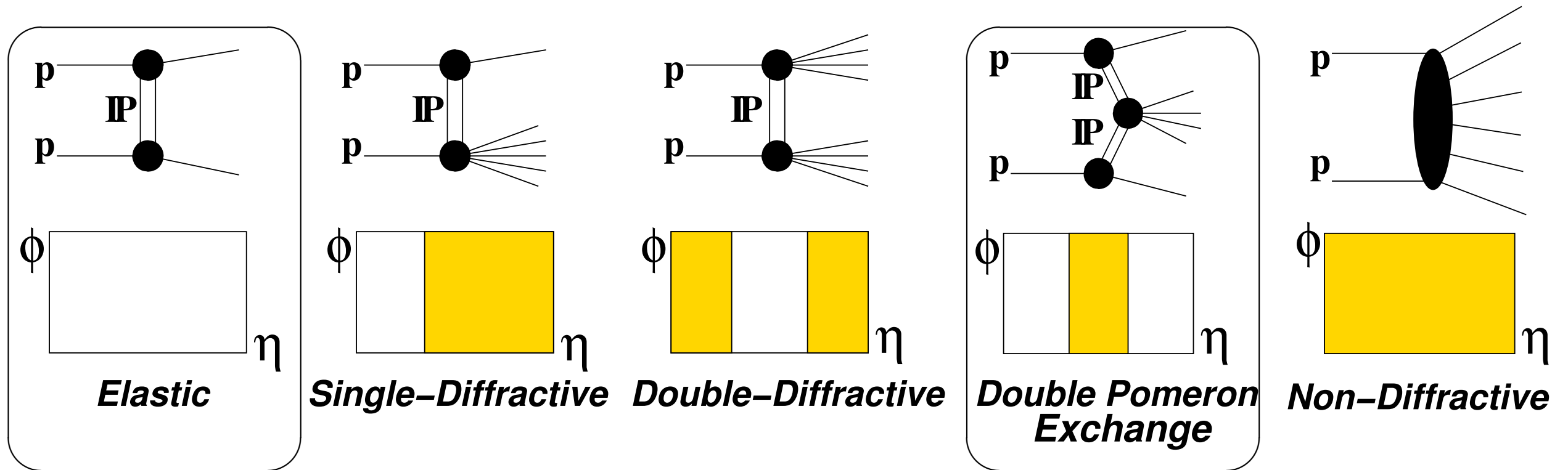
Wigner Research Centre for Physics, Budapest  
for the CMS and TOTEM Collaborations



*Low-x 2023, Leros, Greece*

September 4, 2023

# Proton-proton collisions



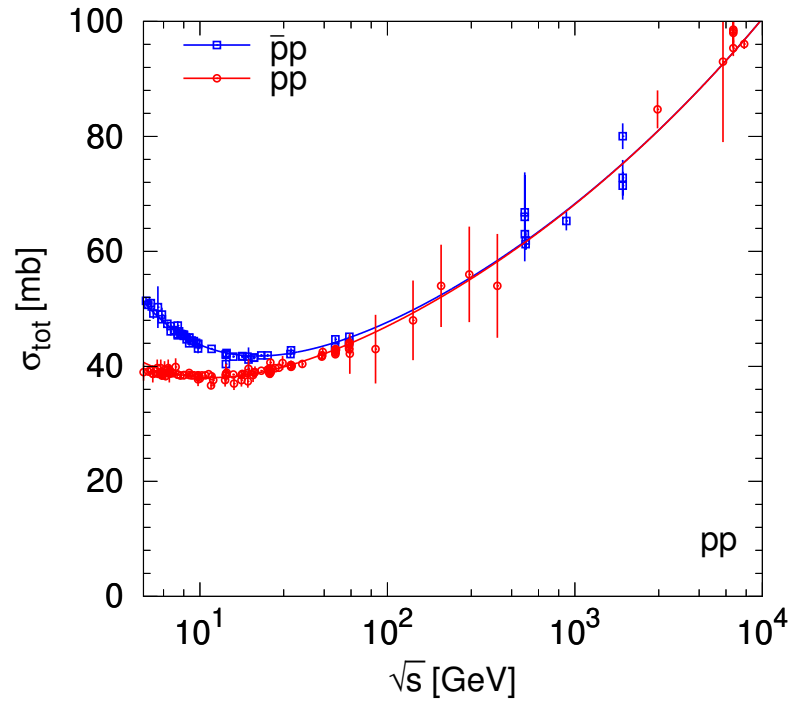
- Types

- elastic: no additional particles
- diffractive: one or both protons are excited and dissociate
- what is the exchanged particle? actually, is it a particle?

New result: detailed study of double pomeron exchange (nonresonant processes)

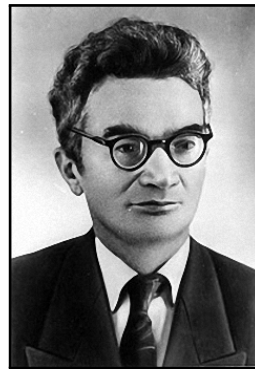
Physics Analysis Summary at: <https://cds.cern.ch/record/2867988>

# Pomeron ( $\mathbb{P}$ )



## • Problems

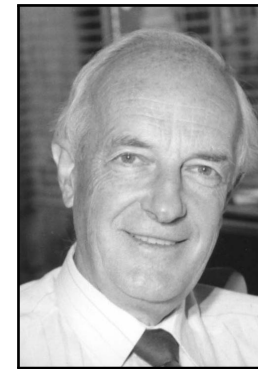
- the  $pp$  and  $\bar{p}p$  cross sections are similar
- they keep rising; exchange?
- force carrier must have zero charges
- gluon ladder? nonperturbative



Isaak Pomeranchuk



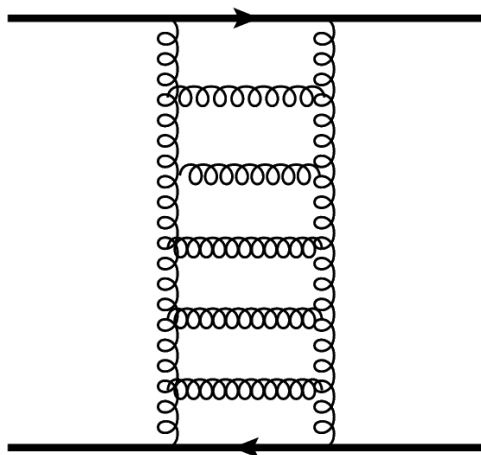
Vladimir Gribov



Sandy Donnachie



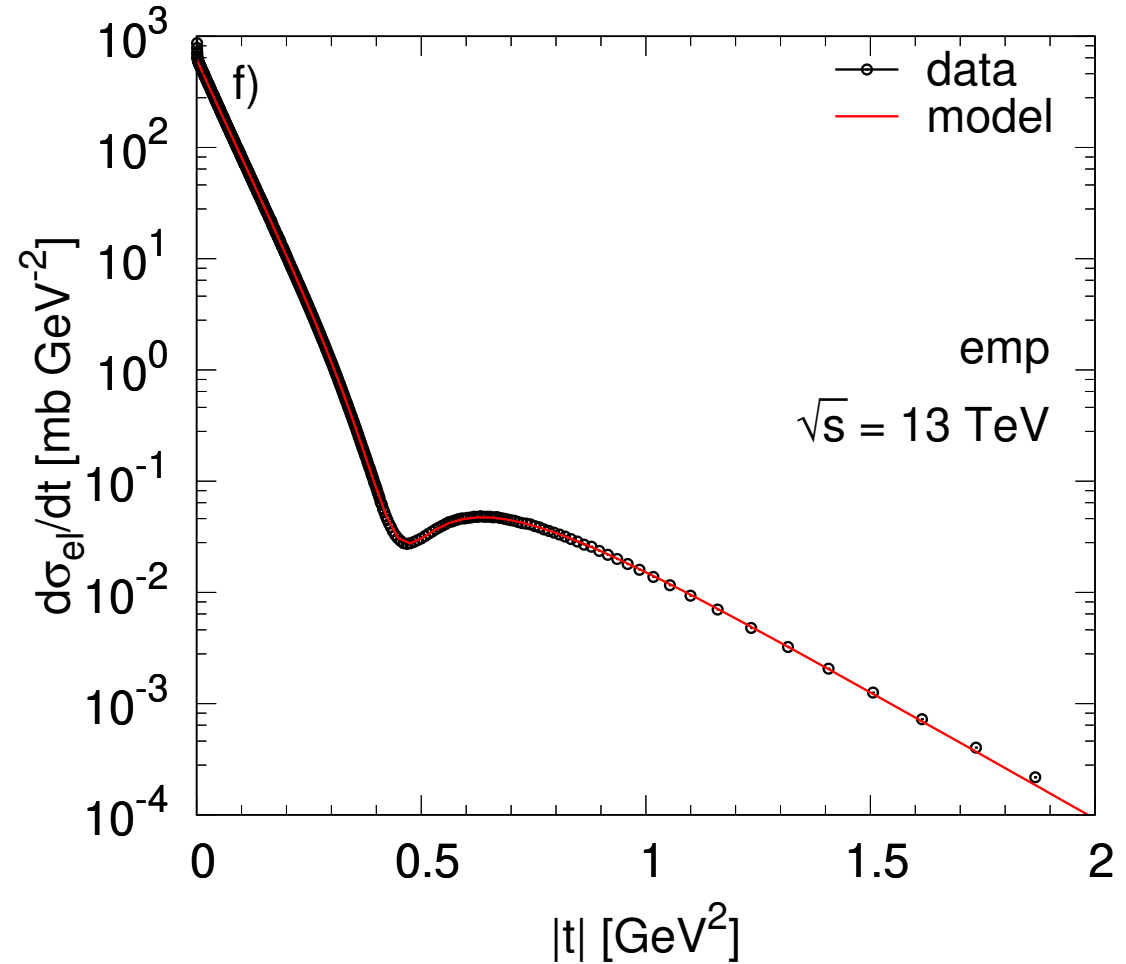
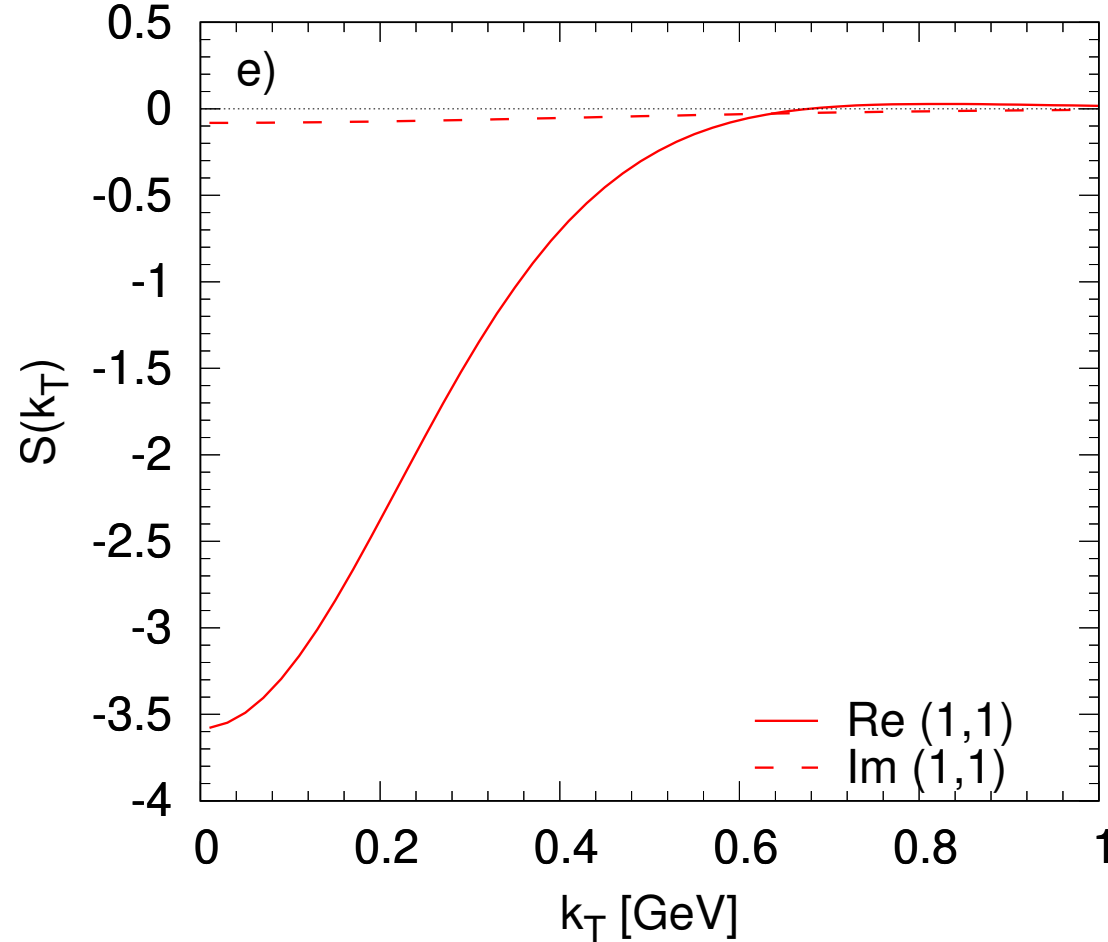
Peter Landshoff



$$\sigma_{\text{tot}}(s) = C_{\mathbb{P}}(s/s_0)^{\alpha_{\mathbb{P}}(0)-1} + (C_f \pm C_\rho)(s/s_0)^{\alpha_{\mathbb{R}}(0)-1}$$

- pomeron trajectory with intercept  $\alpha_{\mathbb{P}}(0)$

# Theory – elastic differential cross section

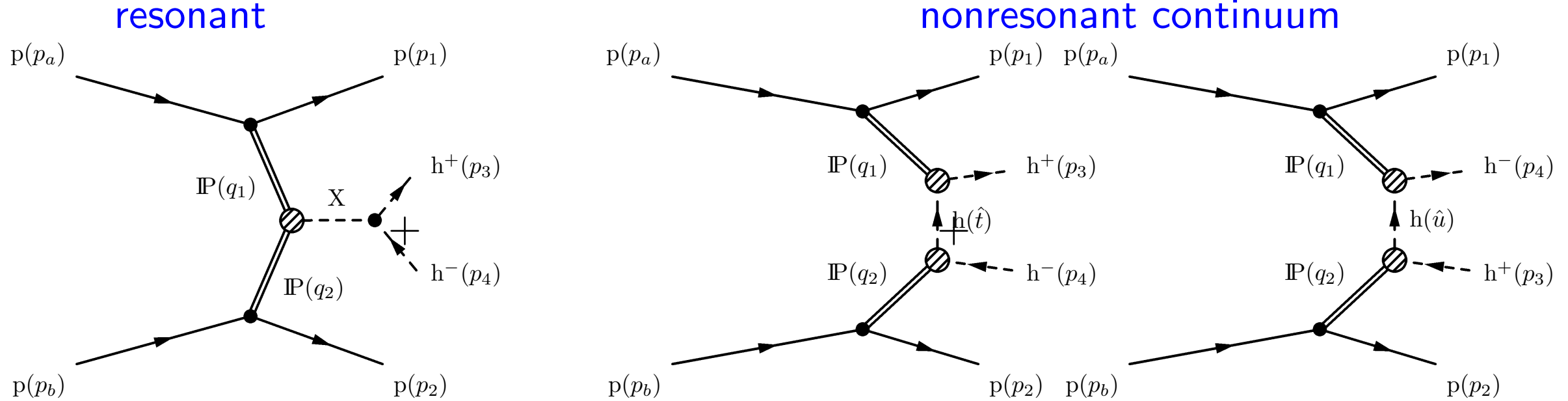


TOTEM Coll., EPJC **79** (2019) 785 and 861  
Fagundes et al, PRD **88** (2013) 094019

Get it from  $S(k_T) = T_{el}(k_T)/(2\pi)^2$  where  $T_{el}(t) = i \left[ G(t)\sqrt{A}e^{Bt/2} + e^{i\phi}\sqrt{C}e^{Dt/2} \right]$

Empirical parametrisation of TOTEM data (Phillips-Barger model)

# Theory – resonances vs background



- Nonresonant continuum

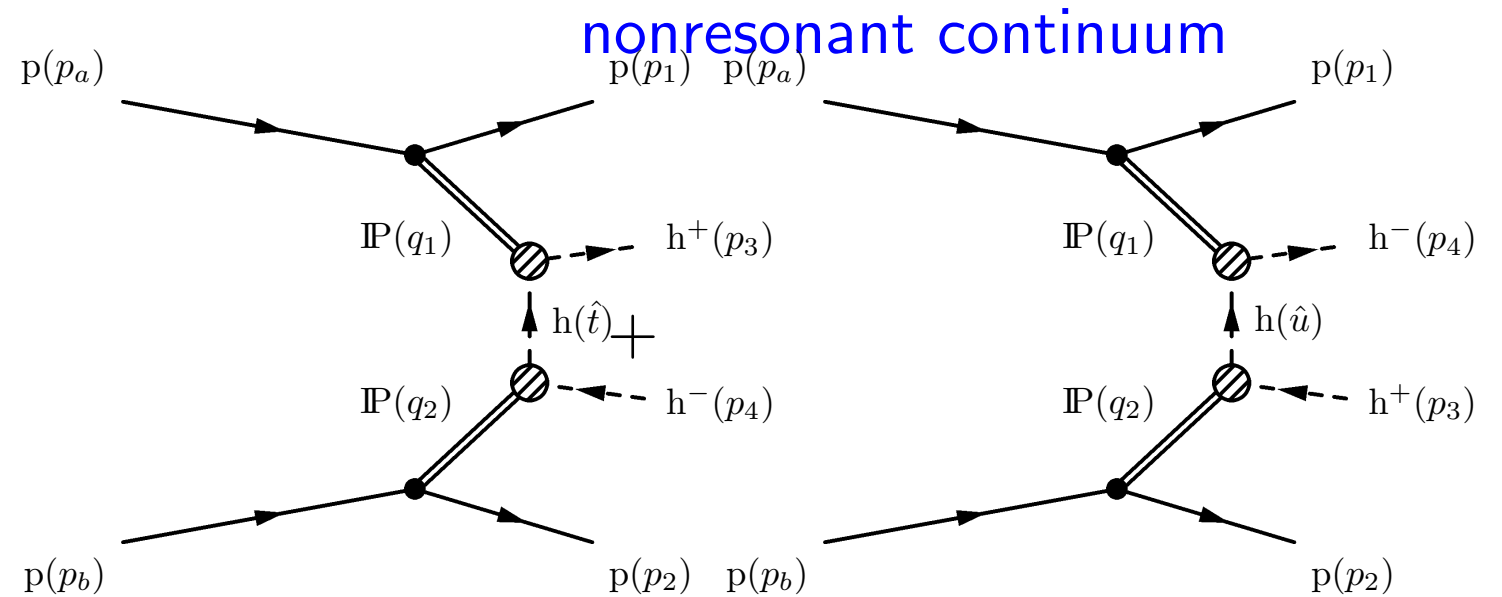
The matrix element for the nonresonant continuum process is

$$\mathcal{M} = M_{13}(t_1, s_{13}) \frac{F_m^2(\hat{t})}{\hat{t} - m^2} M_{24}(t_2, s_{24}) + M_{14}(t_1, s_{14}) \frac{F_m^2(\hat{u})}{\hat{u} - m^2} M_{23}(t_2, s_{23})$$

where  $M_{ik}$  denotes the “interaction” between a scattered proton and a created hadron,  $s_{ik} = (p_i + p_k)^2$ ,  $\hat{t} = (p_3 - q_1)^2 = (p_4 - q_2)^2$  and  $\hat{u} = (p_4 - q_1)^2 = (p_3 - q_2)^2$ .

The pomeron-meson form factor  $F_m(\hat{t})$  and the usual **propagator**  $1/(\hat{t} - m^2)$

# Theory – double pomeron exchange



- Nonresonant continuum

At high hadron-proton energies ( $> 20$  GeV) the **pomeron exchange dominates**

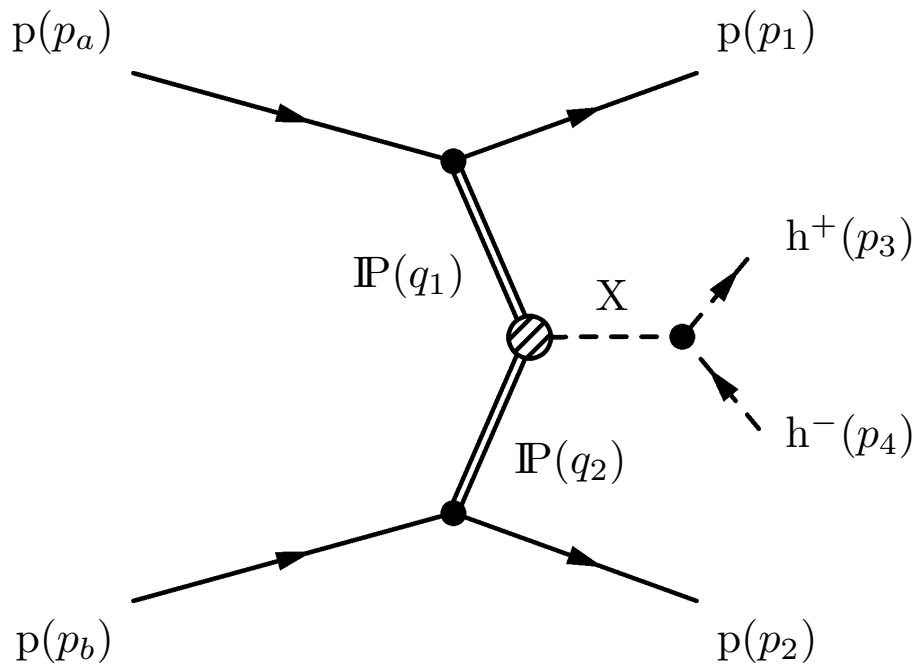
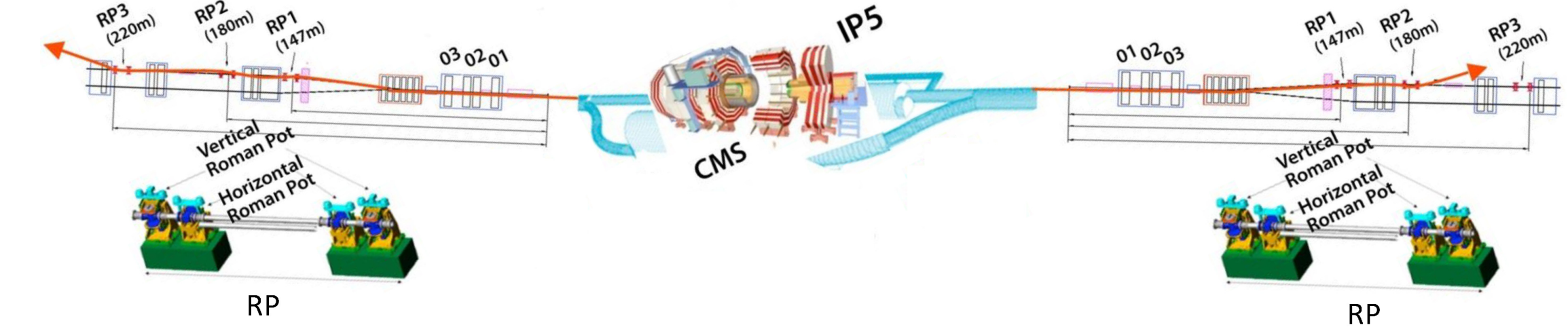
$$M_{ik}(t_i, s_{ik}) = i s_{ik} C_{\mathbb{P}} \left( \frac{s_{ik}}{s_0} \right)^{\alpha_{\mathbb{P}}(t_i) - 1} \exp \left( \frac{B_{\mathbb{P}}}{2} t_i \right)$$

Taking into account the reggeon exchange as well

$$\dots + [(a_f + i) s_{ik} C_f \pm (a_\rho - i) s_{ik} C_\rho] \cdot \left( \frac{s_{ik}}{s_0} \right)^{\alpha_{\mathbb{R}}(t_i) - 1} \exp \left( \frac{B_{\mathbb{R}}}{2} t_i \right)$$

The weight of an event (or the cross section) is proportional to  $|\mathcal{M}|^2/s^2$

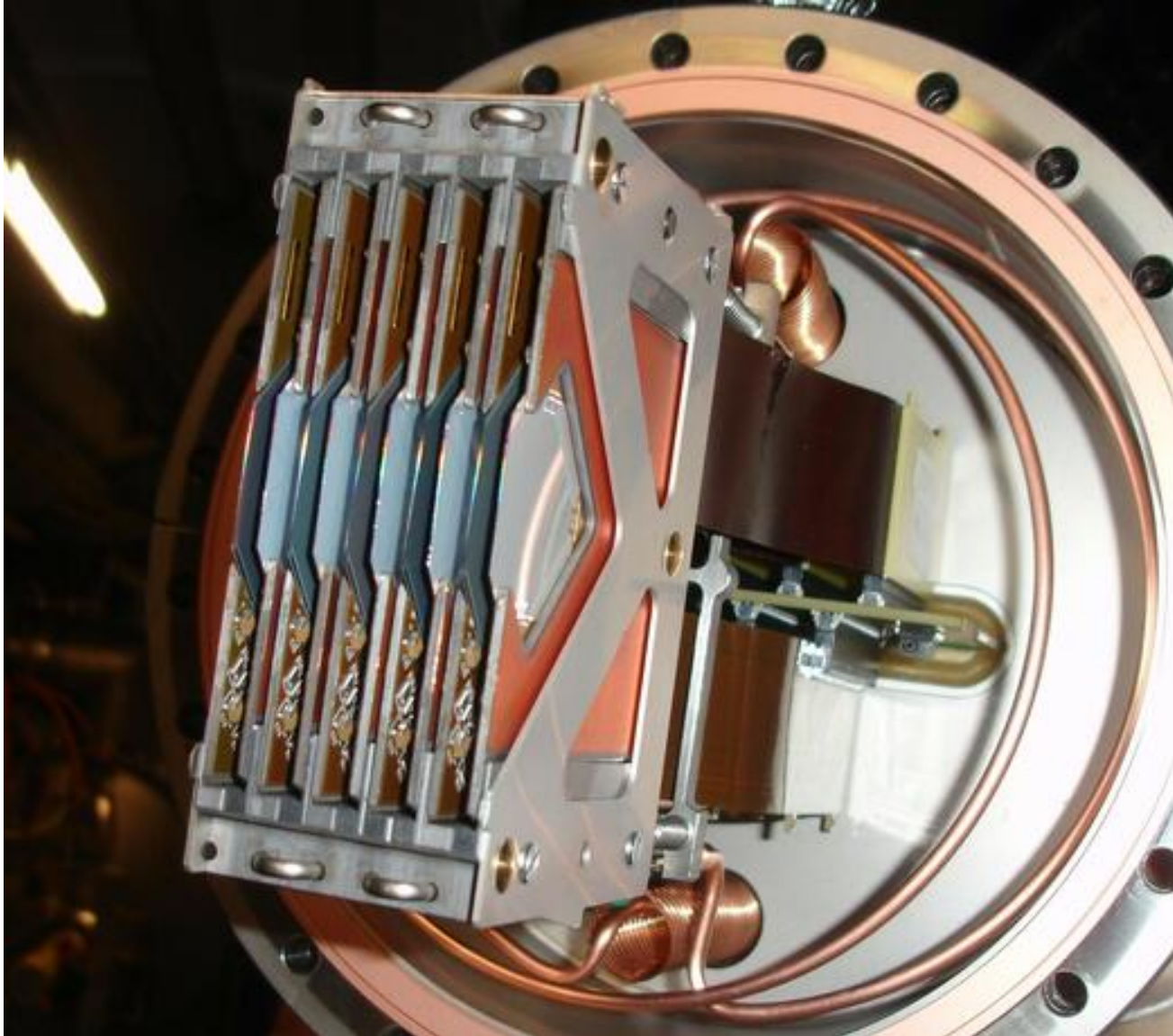
# Central exclusive production – data



- CMS+TOTEM dataset ( $\beta^* = 90$  m, 2018)
  - about 80 M events with **two scattered protons** and only **two reconstructed central tracks**
  - part of those is double pomeron exchange (DPE), where a central system (X) was created
  - decayed to particle-antiparticle pair  $h^+h^-$ , mostly  $\pi^+\pi^-$  or  $K^+K^-$ , but some  $p\bar{p}$
  - invariants:  $p_{1,T}, p_{2,T}, \phi; m_{h^+h^-}$

IP IP collider  $\rightarrow$  gluon-rich initial state

# Scattered protons – roman pots

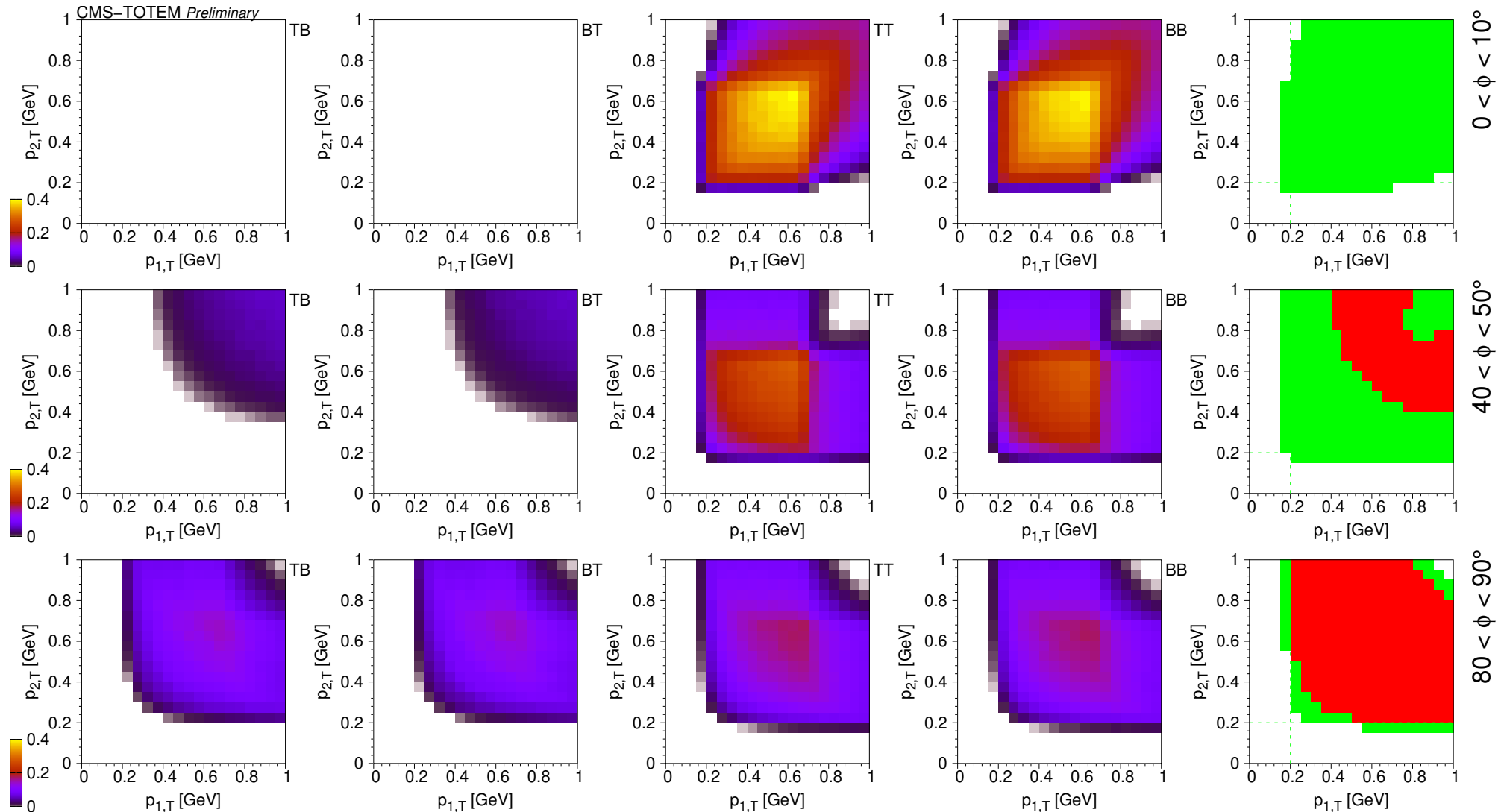


- Details
  - two arms (in sectors 45 and 56)
  - near and far stations (at  $\approx 213$  and 220 m)
  - top and bottom pots
  - within a pot:
    - 5 planes in 'u' and
    - 5 planes in 'v' directions
  - each plane has:  $4 \times 128$  strips
- Two pots per arm
  - two measurements
  - location and momentum at IP

Novel tracklet fits, relative alignment of planes, strip-level efficiencies

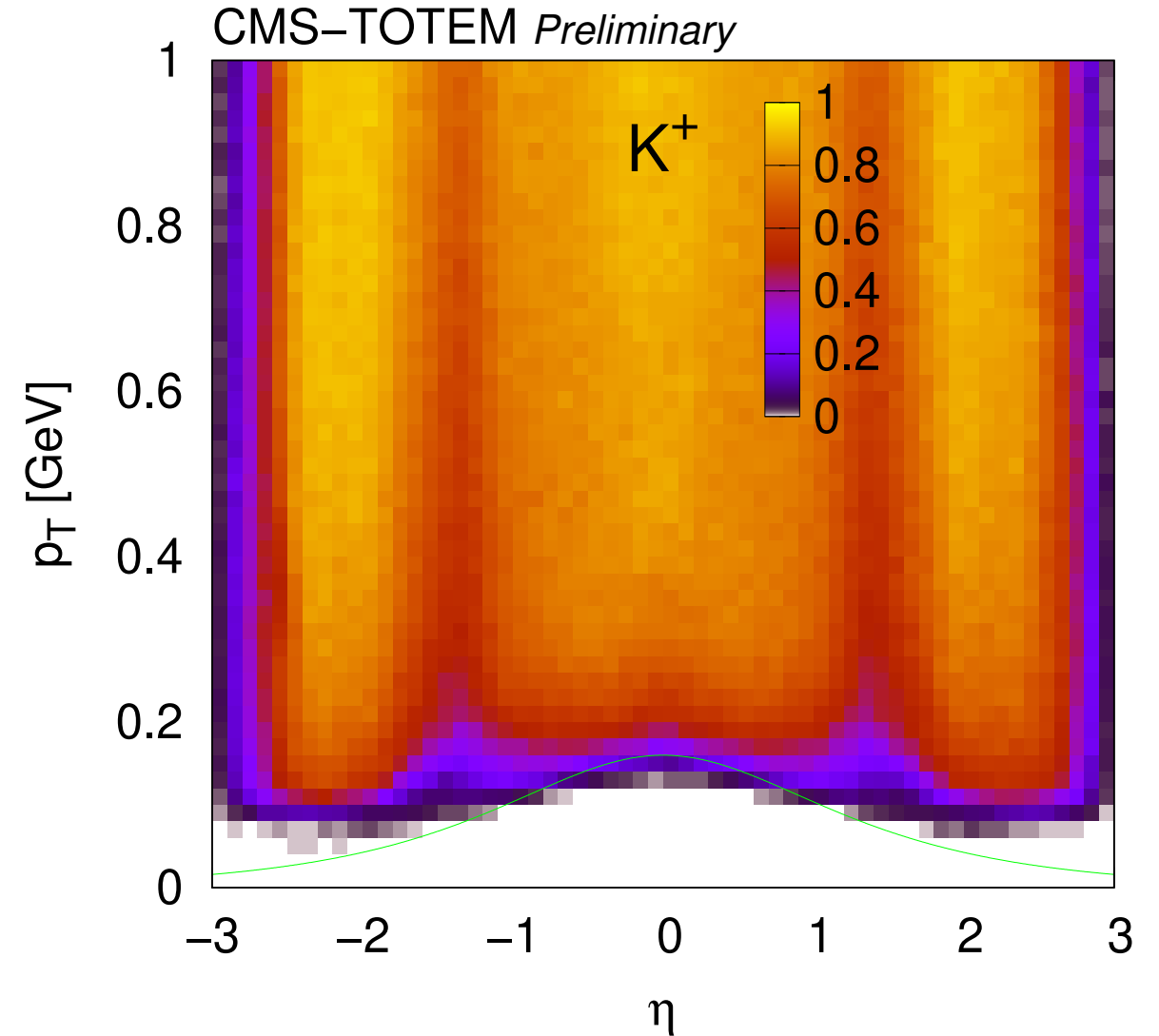
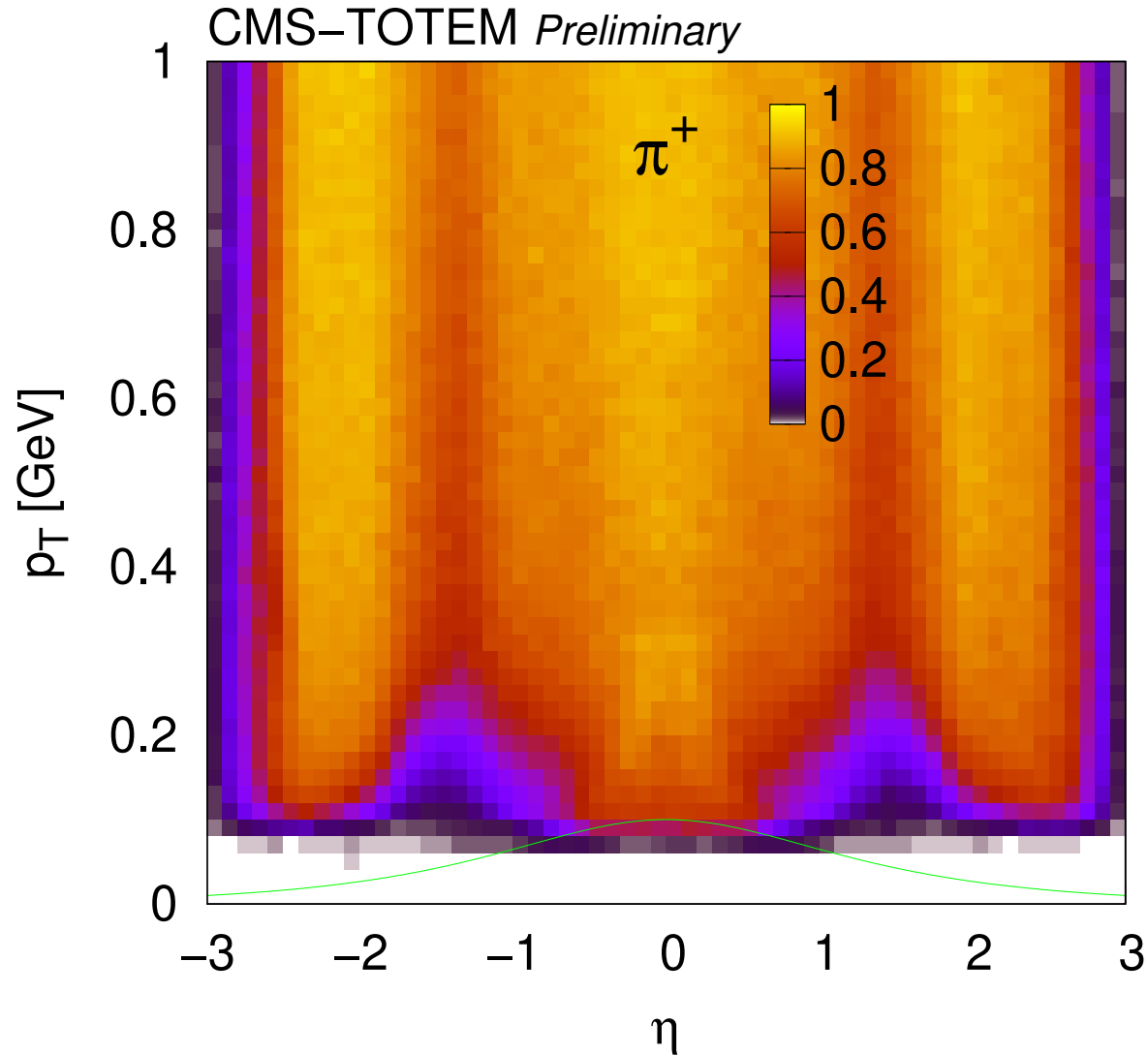


# Roman pots – proton-pair acceptance and coverage vs $\phi$



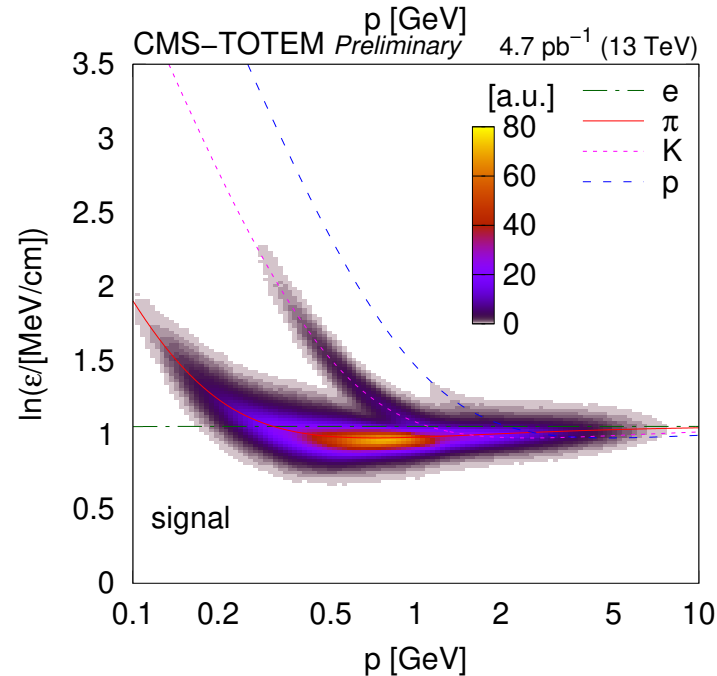
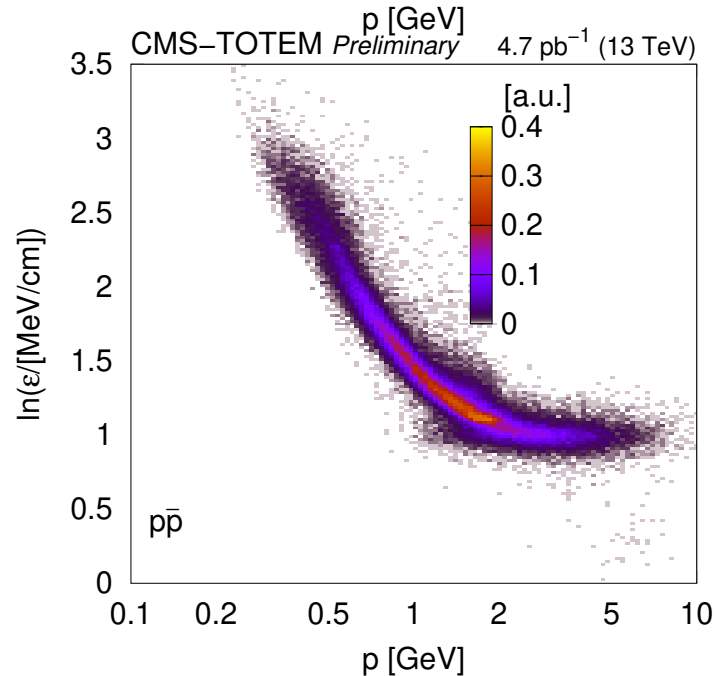
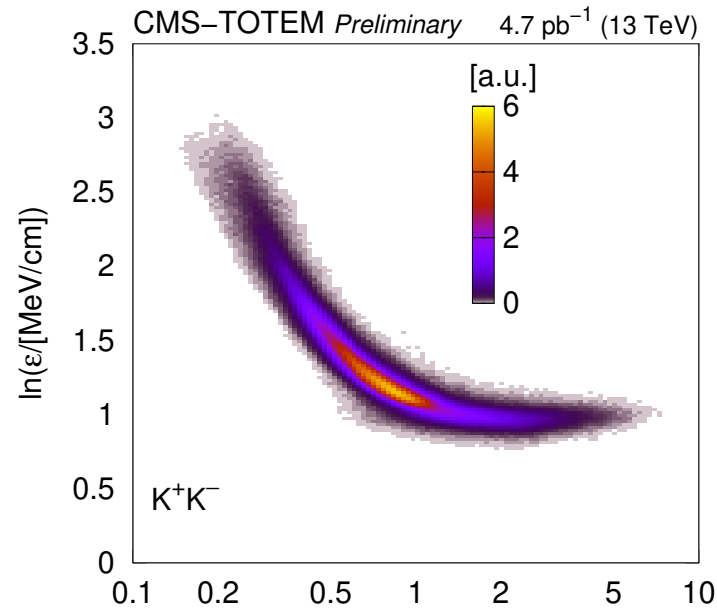
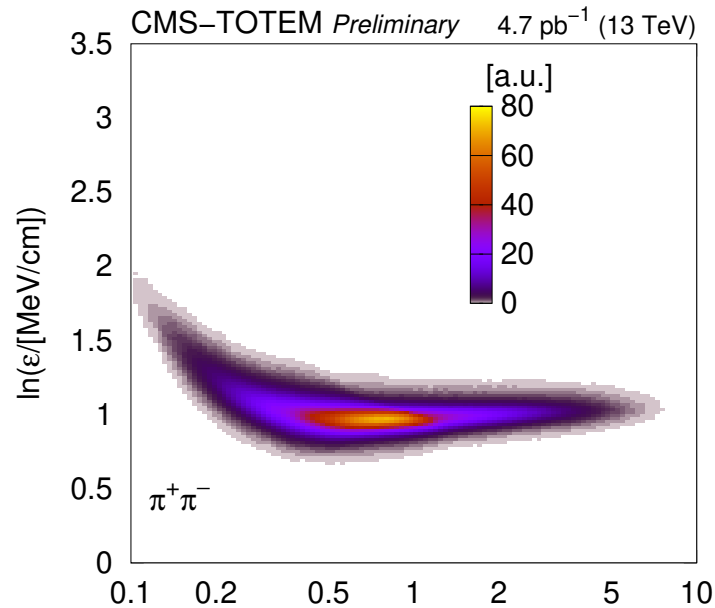
Calculated detection efficiencies for the pair of scattered protons  
as a function of their transverse momenta ( $p_{1,T}, p_{2,T}$ )

# Central hadrons – tracking and HLT efficiencies



At least 5 pixel clusters and at least 3 layers in barrel pixel, or at least one pixel track  
Inefficiencies, valleys to be corrected

# Central hadrons – particle identification through dE/dx



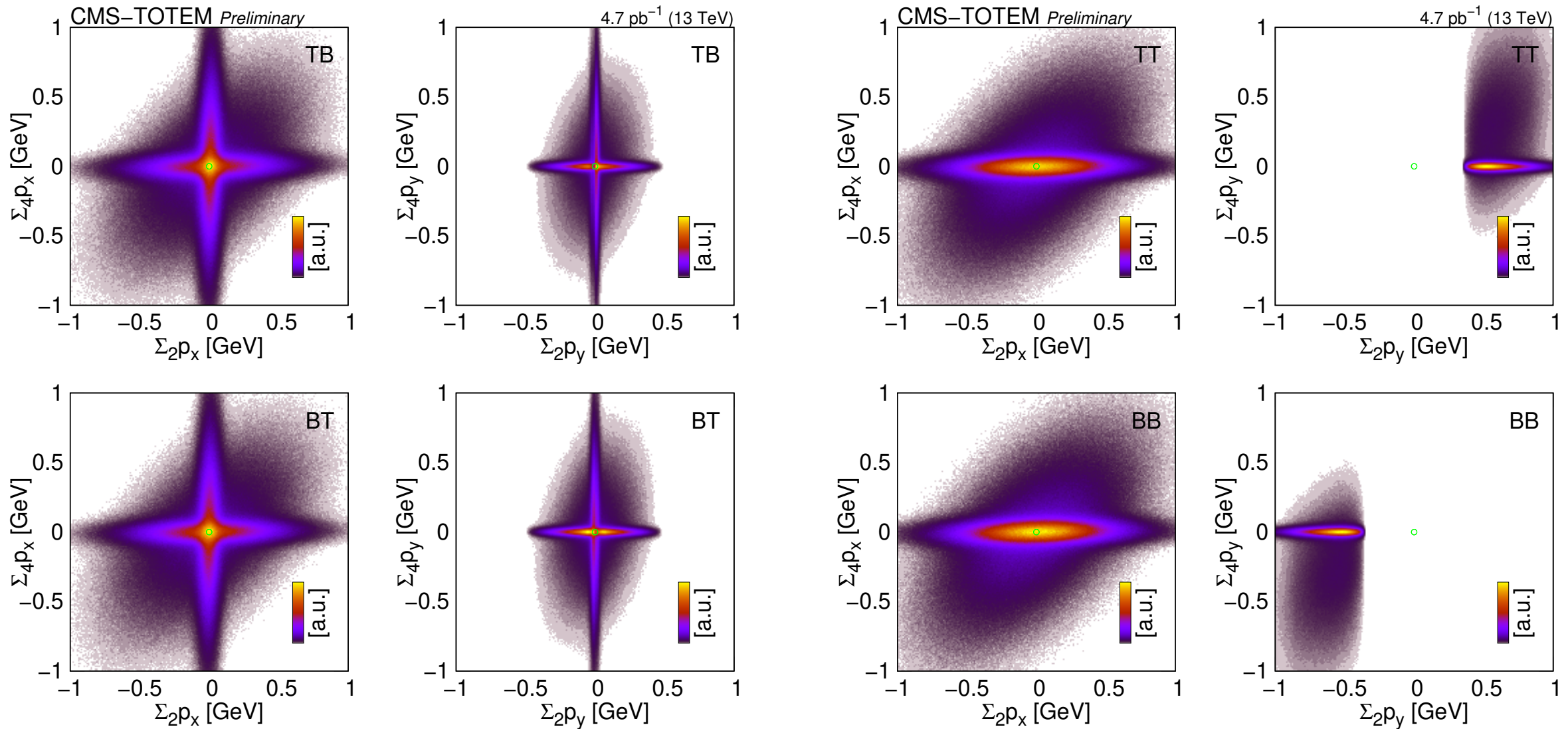
- Particle pair

- identified as type  $h^+h^-$  if  $P_{1,h}P_{2,h} > 10 \cdot P_{1,i}P_{2,i}$  for all  $i \neq h$

- Proof of exclusivity

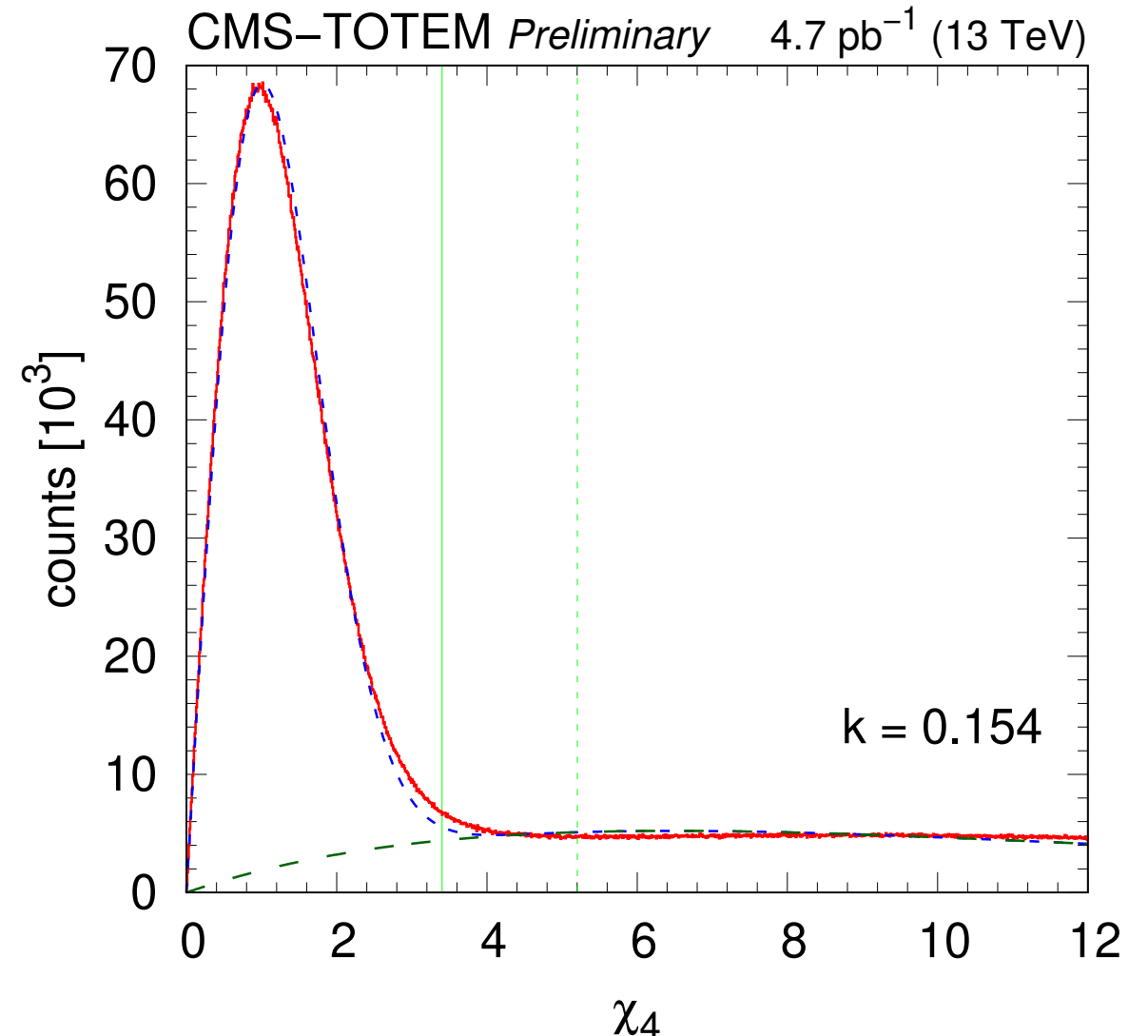
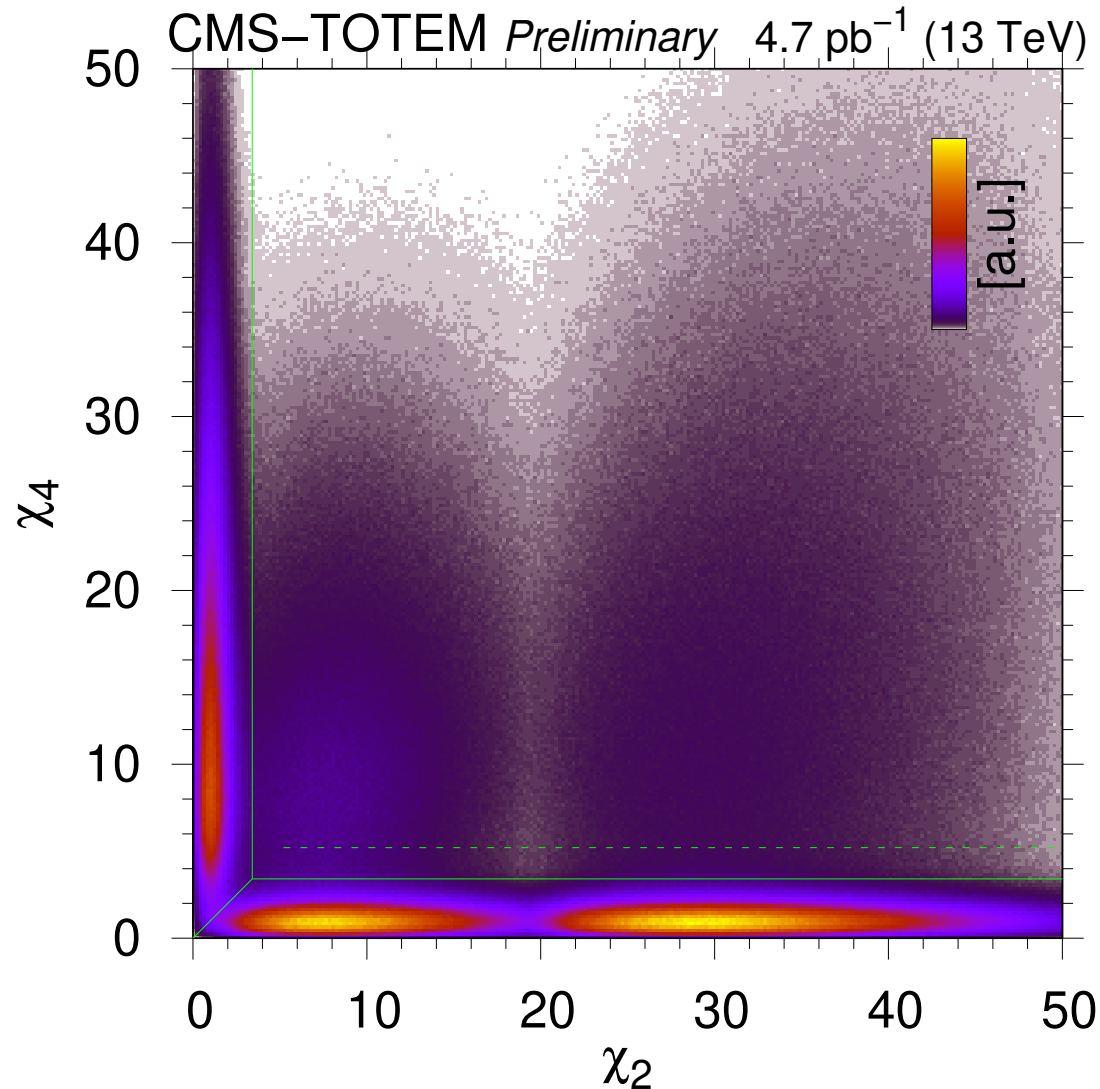
- $\pi^+\pi^-$ ,  $K^+K^-$ , and  $p\bar{p}$  pairs
- conservation laws at work: charge, strangeness, baryon number

# Event classification – true exclusive or pileup?



Based on ( $\Sigma_4 p_x$  vs  $\Sigma_2 p_x$ ,  $\Sigma_4 p_y$  vs  $\Sigma_2 p_y$ )

# Event classification – $\chi_4$ – signal and sideband

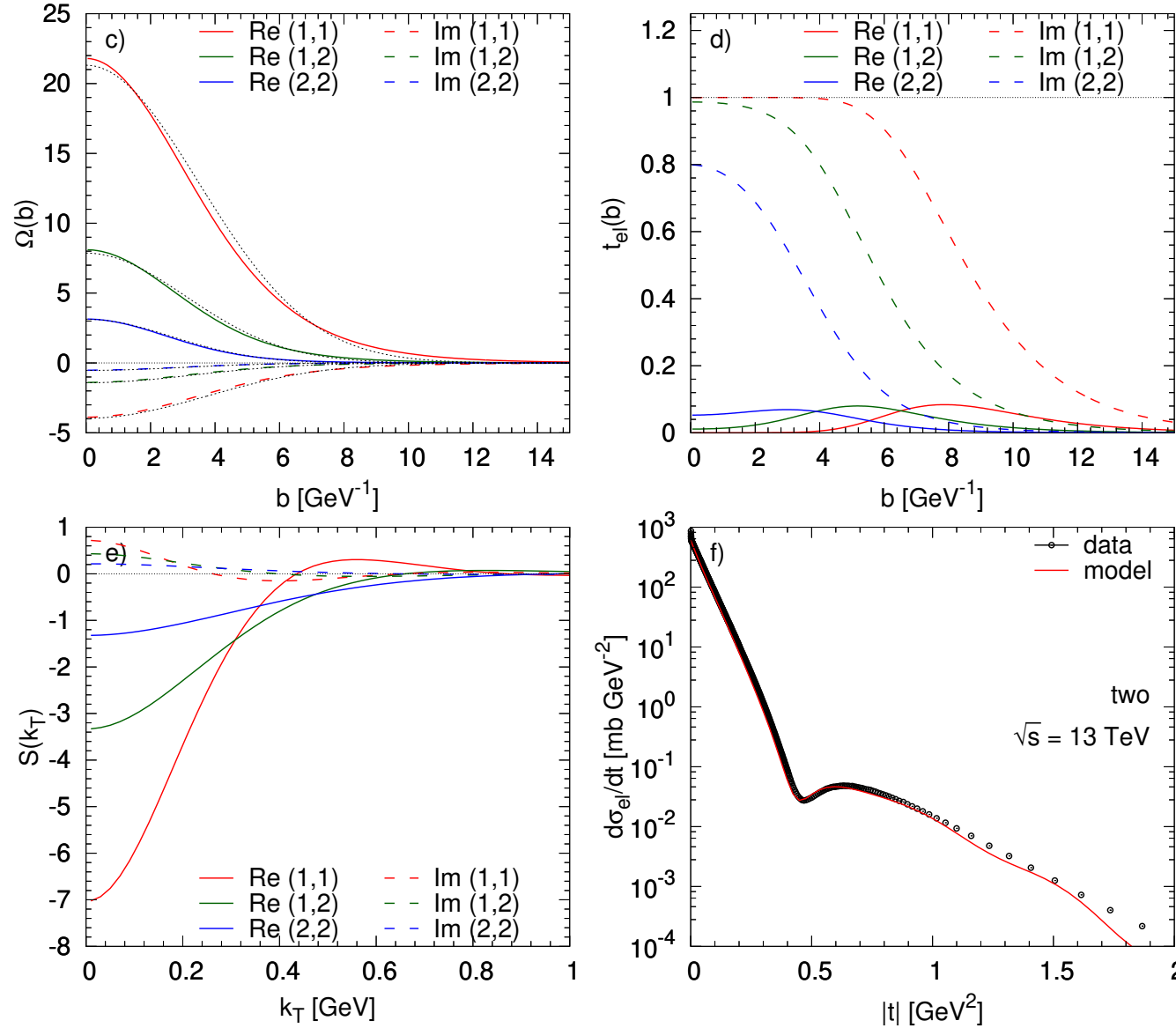


Mahalanobis distance  $\chi(\mathbf{s}) = (\mathbf{s}^T \mathbf{V}^{-1} \mathbf{s})^{1/2}$

$A \chi \exp(-\chi^2/2) + B \chi \exp(-k\chi)$

Components: signal ( $\chi$ -distribution with fixed parameters) and background

# Theory – elastic screening – two-channel



Khoze, Martin, Ryskin, EPJC **73** (2013) 2503  
TOTEM Coll., EPJC **79** (2019) 785 and 861

– linear combination of **diffractive eigenstates**

$$|p\rangle = \sum_i a_i |\phi_i\rangle$$

– eigenstate-IP couplings  $\gamma_i$

– amplitude between  $i$  and  $j$

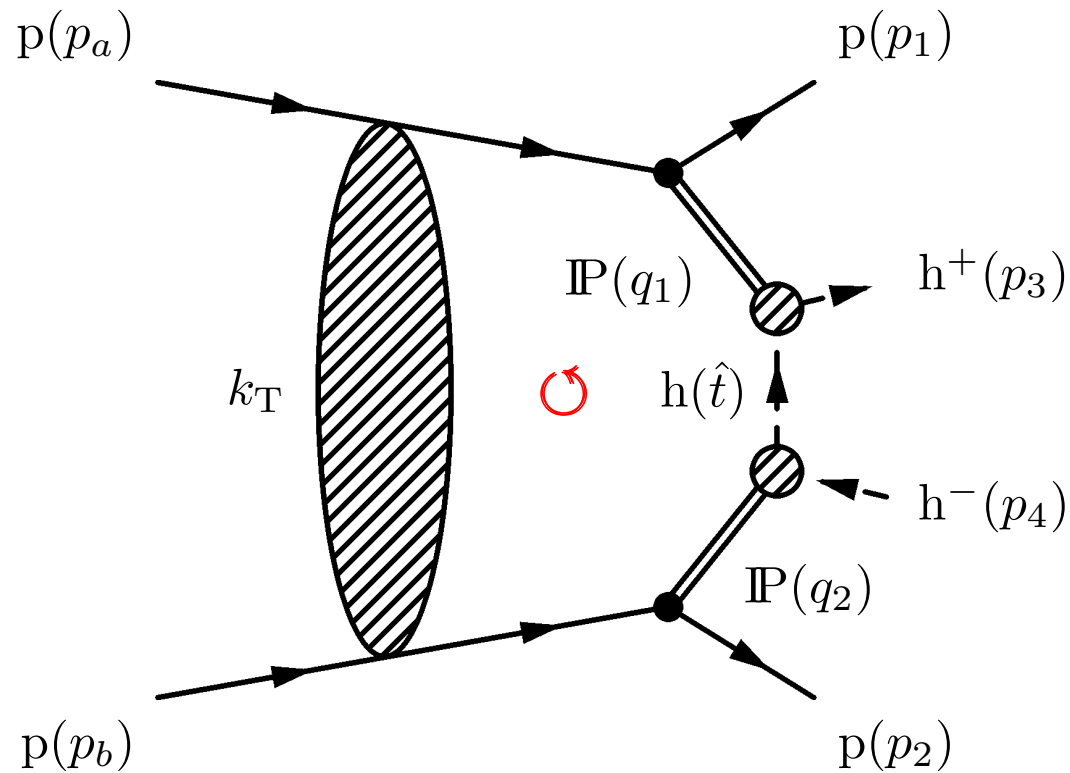
$$\Omega_{ij}(k_T) = \eta \sigma_0 \gamma_i F_i(t) \gamma_j F_j(t) (s/s_0)^{\alpha_{IP}(t)-1}$$

– elastic amplitude through

$$t_{el,ij}(b) = i (1 - e^{-\Omega_{ij}(b)/2})$$

$$T_{el}(k_T) = \sum_{i,j} |a_i|^2 |a_j|^2 \cdot 2\pi \int t_{el,ij}(b) J_0(k_T b) b db$$

# Theory – nonresonant continuum – interference!



- Full treatment

- incoming (outgoing) protons may scatter as well, additional complication
- **screening effects**  $S$ , related to “rapidity gap survival”
- several options for  $S$ 
  - \* from measured  $d\sigma_{el}/dt$ , **empirical** parametrisation (Fagundes et al)
  - \* from a theoretical calculation, **one- or two-channel** (eigenstates) (Khoze, Martin, Ryskin)
  - \* (Lebiedowicz, Nachtmann, Szczurek)

- Calculate

Sum of bare ( $\mathcal{M}_0$ ) and screened amplitudes at  $(\mathbf{p}_1, \mathbf{p}_2)$  of the scattered protons

$$\mathcal{M}(\mathbf{p}_1, \mathbf{p}_2) = \mathcal{M}_0(\mathbf{p}_1, \mathbf{p}_2) + \int d^2\mathbf{k}_T T_{el}(k_T) \mathcal{M}_0(\mathbf{p}_1 - \mathbf{k}_T, \mathbf{p}_2 + \mathbf{k}_T)$$

Involves a loop integral over the momentum  $k_T$  exchanged

# Models – DIME, working points

Parameter	DIME-1	DIME-2	DIME-3	DIME-4	Remark
$\sigma_P$ [mb]	23	33	60	50	pomeron strength
$\alpha_P$	1.13	1.115	1.093	1.11	pomeron intercept, $= 1 + \Delta$
$\alpha'_P$ [GeV <sup>-2</sup> ]	0.08	0.11	0.075	0.06	pomeron slope
$\gamma_i$	$1 \pm 0.55$	$1 \pm 0.4$	$1 \pm 0.42$	$1 \pm 0.47$	dimensionless coupling to eigenstate $i$
$2  a_i ^2$	$1 \pm 0.08$	$1 \pm 0.5$	$1 \pm 0.52$	$1 \pm 0.5$	$a_i$ is the amplitude of eigenstate $i$
$b_1$ [GeV <sup>-2</sup> ]	8.5	8	5.3	7.2	} pomeron coupling to eigenstates
$b_2$ [GeV <sup>-2</sup> ]	4.5	6	3.8	4.2	
$c_1$ [GeV <sup>2</sup> ]	0.18	0.18	0.35	0.53	
$c_2$ [GeV <sup>2</sup> ]	0.58	0.58	0.18	0.24	
$d_1$	0.45	0.63	0.55	0.6	
$d_2$	0.45	0.47	0.48	0.48	

Harland-Lang, Khoze, Ryskin, EPJC **74** (2014) 2848

- Proton-pomeron(eigenstate) coupling

- One-channel model:  $F_p(t) = \exp(B_{\mathbb{P}}/2 \cdot t)$

- Two-channel model:

$$F_i(t) = \exp \left[ -(b_i(c_i - t))^{d_i} + (b_i c_i)^{d_i} \right]$$

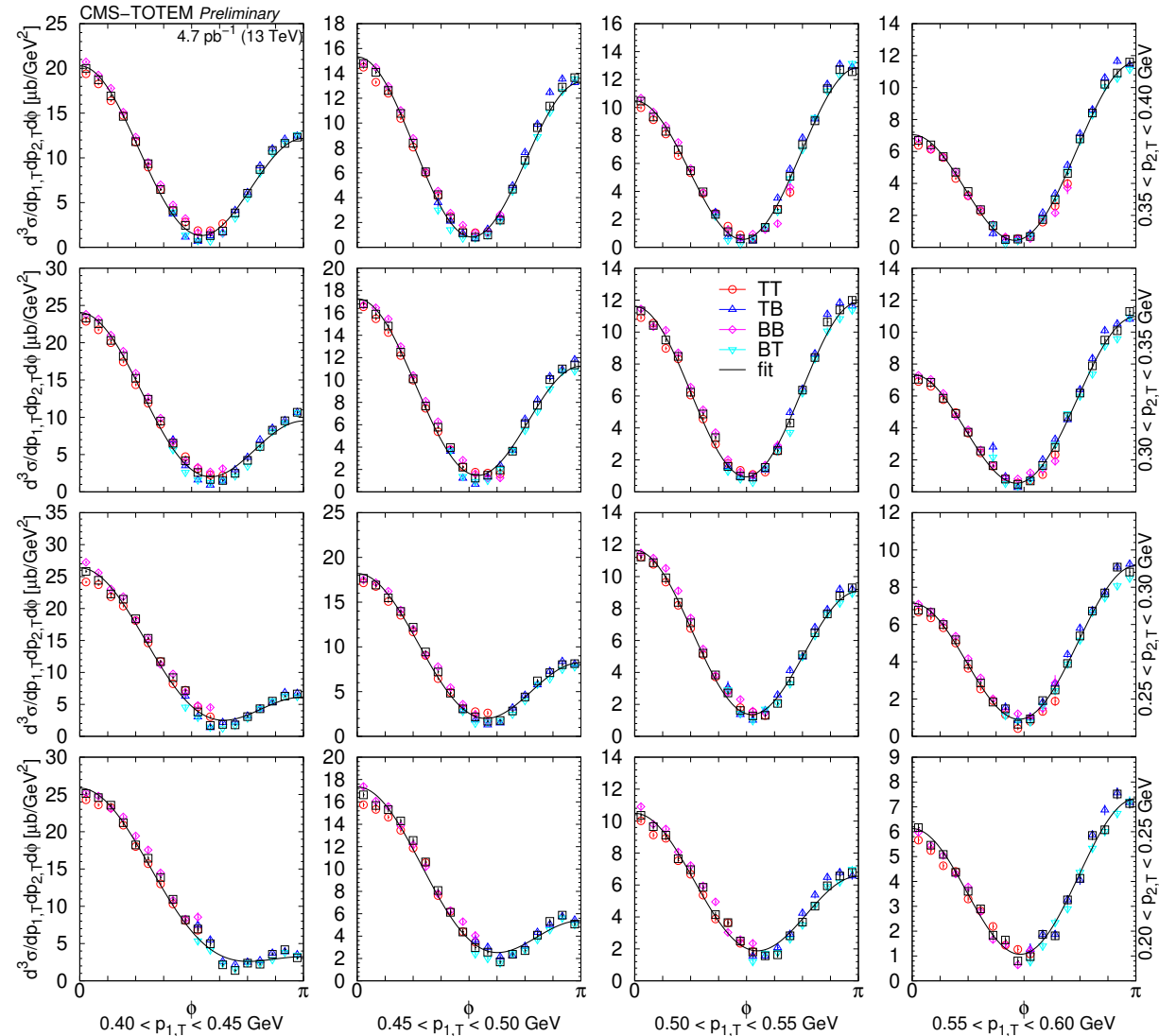
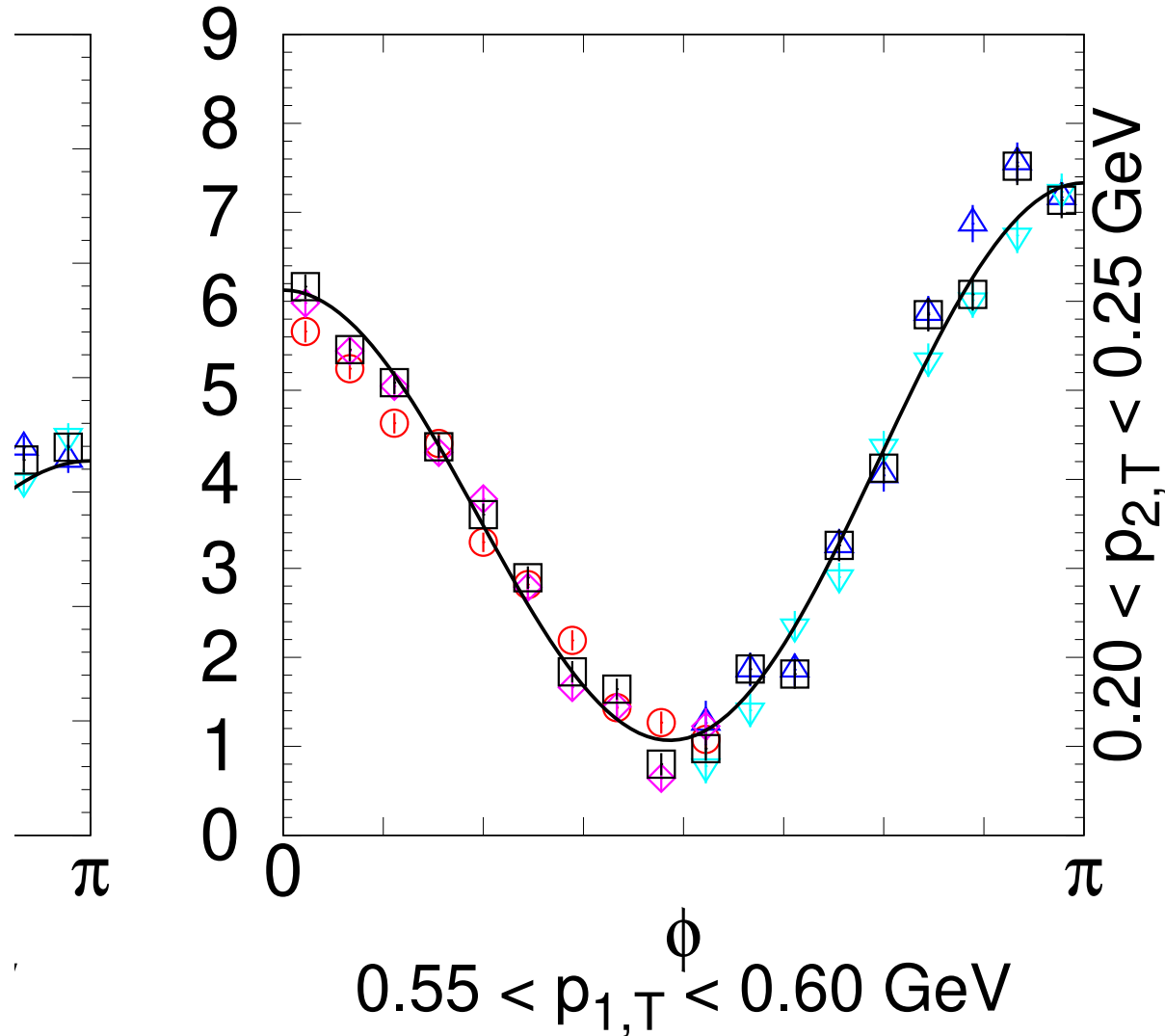
- Pomeron-meson coupling

$$F_m(\hat{t}) = \begin{cases} \exp(b_{\text{exp}}(\hat{t} - m^2)), \\ \exp(b_{\text{ore}}[a_{\text{ore}} - \sqrt{a_{\text{ore}}^2 - (\hat{t} - m^2)}]), \\ 1/(1 - b_{\text{pow}}(\hat{t} - m^2)) \end{cases}$$

Now using a new generator with proper physics content, from scratch

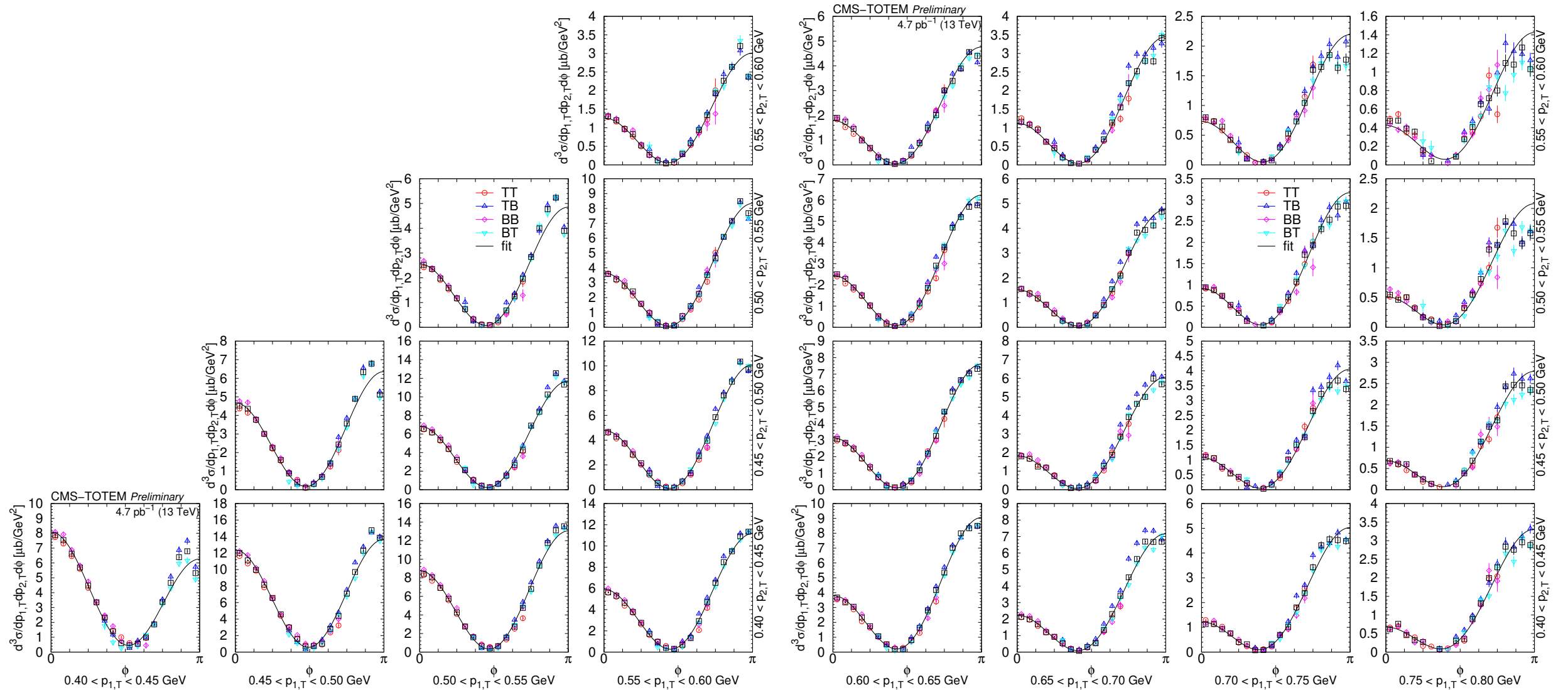


# Measurements – nonresonant $d^3\sigma/dp_{1,T}dp_{2,T}d\phi$



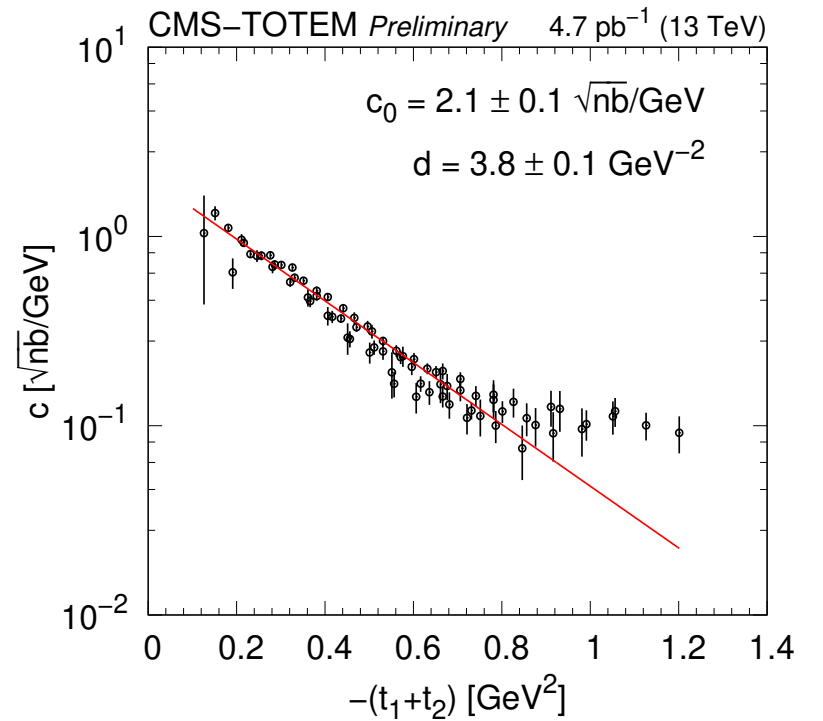
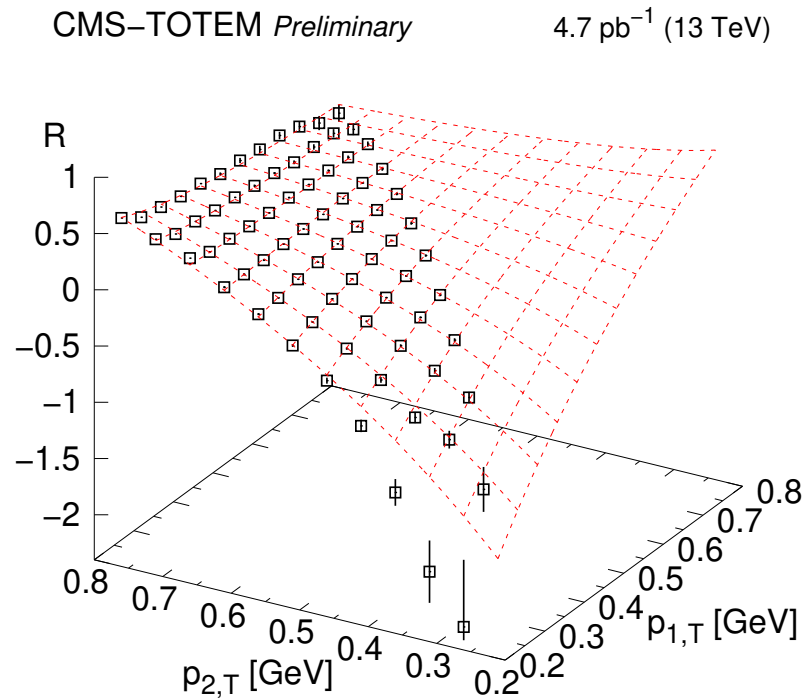
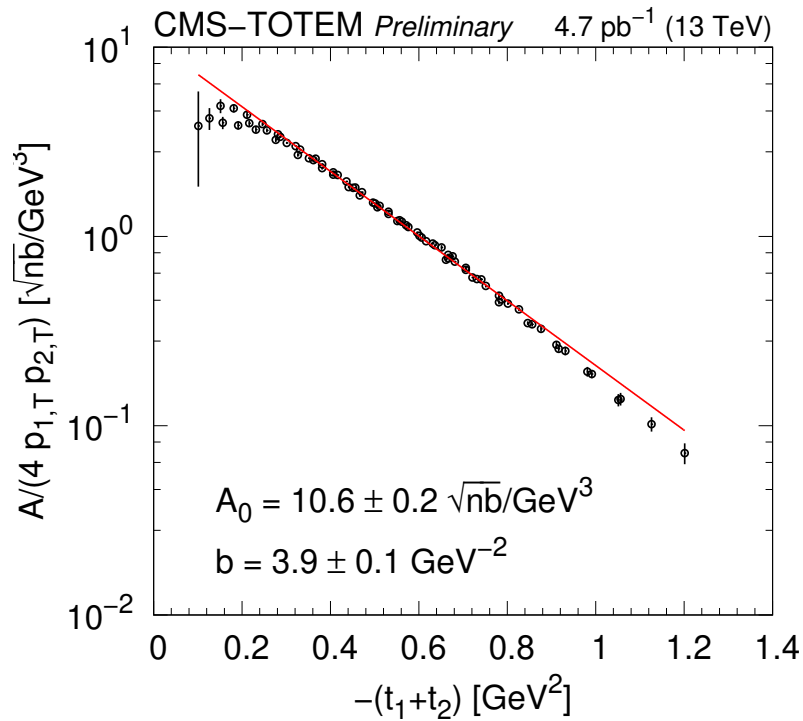
As a function of  $\phi$  in  $(p_{1,T}, p_{2,T})$  bins, in units of  $[\mu\text{b}/\text{GeV}^2]$ , if  $0.35 < m_{\pi\pi} < 0.65 \text{ GeV}$

# Measurements – nonresonant $d^3\sigma/dp_{1,T}dp_{2,T}d\phi$



Curves of a phenomenology-motivated fits with the form  $[A(R - \cos \phi)]^2 + c^2$  are plotted (Close, Kirk, Schuler)

# Parameter dependencies – $A$ , $R$ , $c$



Scaling described by theory-motivated functional forms

$$A(t_1, t_2) = 4\sqrt{t_1 t_2} \cdot A_0 e^{b(t_1+t_2)} \quad R(t_1, t_2) \approx \frac{1.2(\sqrt{-t_1} + \sqrt{-t_2}) - 1.6\sqrt{t_1 t_2} - 0.8}{\sqrt{t_1 t_2} + 0.1},$$

$$c(t_1, t_2) = c_0 e^{d(t_1+t_2)}$$

Model tuning with PROFESSOR (version 2.3.3)  $\Rightarrow$

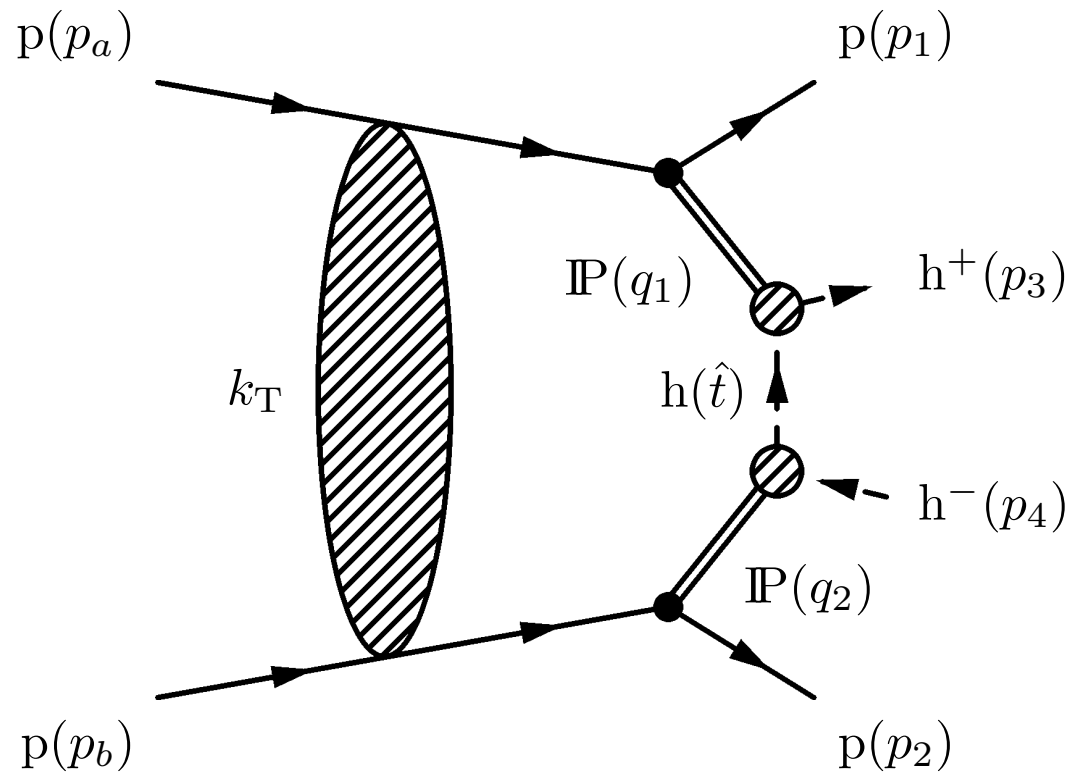
# Systematics

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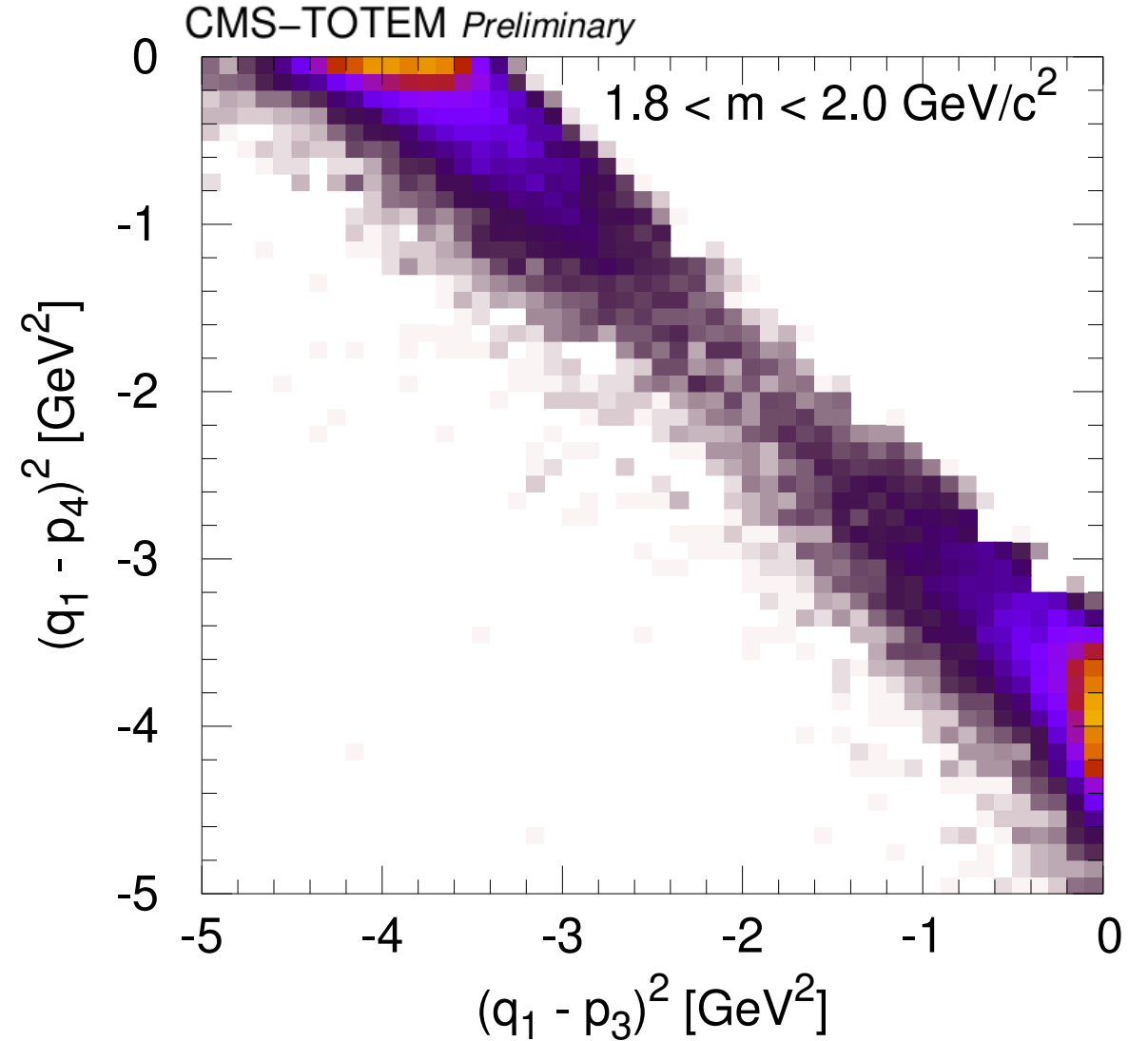
Source	Value	Remark
Pileup correction	1.0%	through visible cross section ( $\sigma_{\text{vis}}$ )
Lumisections with reduced RP availability	0.5%	
Integrated luminosity ( $L_{\text{int}}$ )	2.5%	
HLT efficiency	small	neglected
Total normalisation-type	2.7%	
Roman pot efficiency	$\approx 3.0\%$	to be taken twice
Background removal	$< 0.5\%$	neglected
Lost events during background removal	$-0.16\%$	neglected
Lost events due to looper cut	$< 0.5\%$	neglected
Single particle tracking efficiency	1.4%	to be taken twice
Particle identification efficiency	$< 1\%$	neglected
Total efficiency-type	4.7%	
Total systematics	5.4%	

Several sources, reasonable systematics  $\sim 5\%$

# Virtual hadron – proof

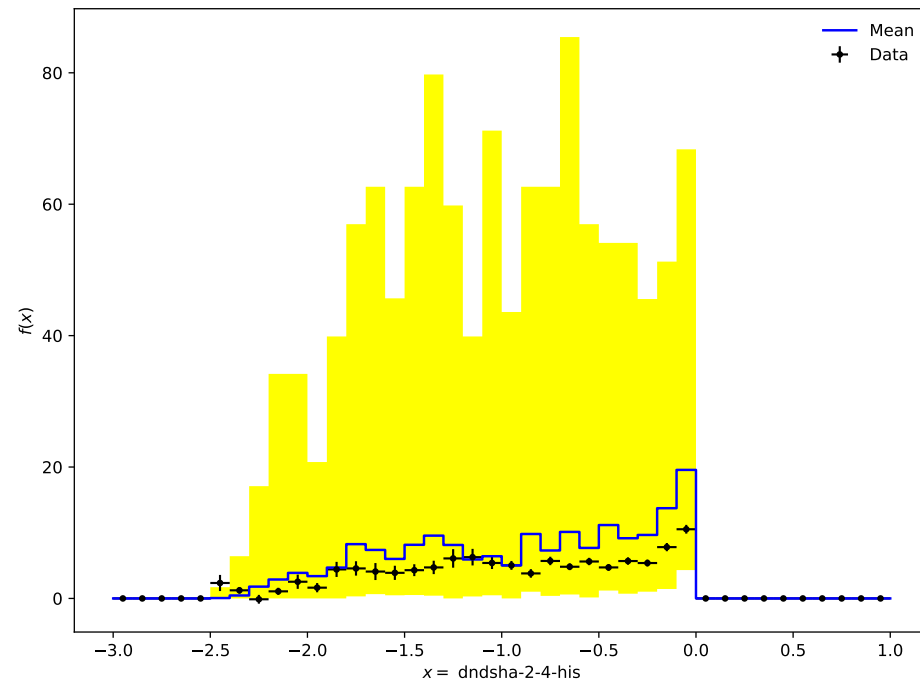
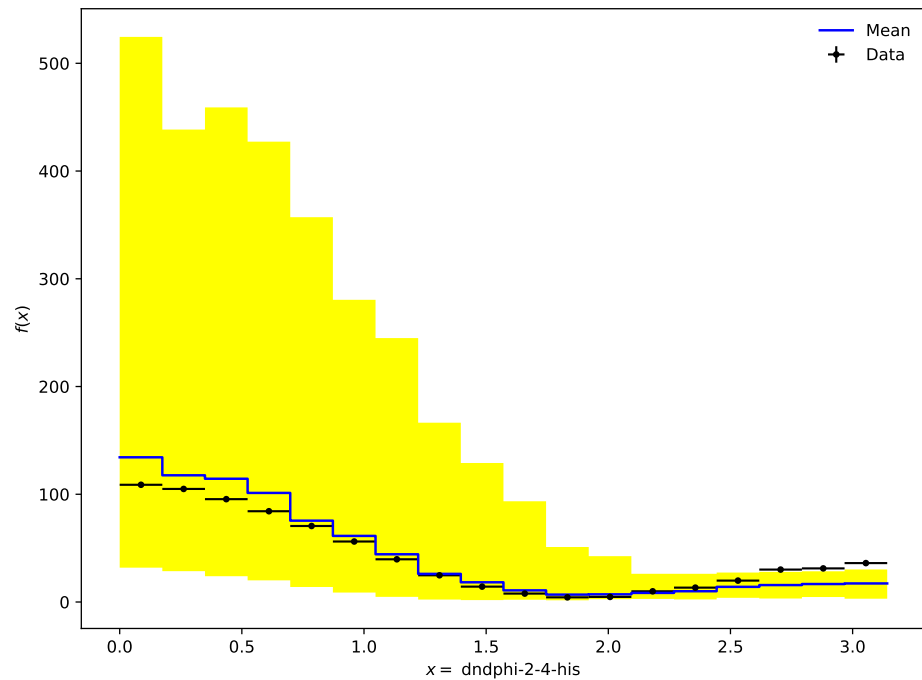


Propagator of virtual hadron:  
 $1/(\hat{t} - m^2)$



The squared four-momentum differences between  $\mathbb{P}$  and the hadrons  $h^\pm$

# Tuning with PROFESSOR (version 2.3.3)



- The tool, the tuning

- parametrises the per-bin generator response to variations, numerical optimisation
- reduces the exponentially expensive brute-force tuning to a scaling closer to a power-law
- the parameter space is up to 12 dimensional; the envelopes well cover the data points
- 400 generator runs are performed, each with 500 thousand generated events each

Tuned separately for different parametrisations of the  $\mathbb{P}$ -meson form factor

# Model tuning – result

Parameter	Exponential	Orear-type	Power-law	DIME 1 / 2
empirical model				
$a_{\text{ore}} [\text{GeV}]$	—	$0.735 \pm 0.015$	—	
$b_{\text{exp/ore/pow}} [\text{GeV}^{-2} \text{ or } -1]$	$1.084 \pm 0.004$	$1.782 \pm 0.014$	$1.356 \pm 0.001$	
$B_{\text{IP}} [\text{GeV}^{-2}]$	$3.757 \pm 0.033$	$3.934 \pm 0.027$	$4.159 \pm 0.019$	
$\chi^2/\text{dof}$	9470/5796	10059/5795	11409/5796	
one-channel model				
$\sigma_0 [\text{mb}]$	$34.99 \pm 0.79$	$27.98 \pm 0.40$	$26.87 \pm 0.30$	
$\alpha_P - 1$	$0.129 \pm 0.002$	$0.127 \pm 0.001$	$0.134 \pm 0.001$	
$\alpha'_P [\text{GeV}^{-2}]$	$0.084 \pm 0.005$	$0.034 \pm 0.002$	$0.037 \pm 0.002$	
$a_{\text{ore}} [\text{GeV}]$	—	$0.578 \pm 0.022$	—	
$b_{\text{exp/ore/pow}} [\text{GeV}^{-2} \text{ or } -1]$	$0.820 \pm 0.011$	$1.385 \pm 0.015$	$1.222 \pm 0.004$	
$B_{\text{IP}} [\text{GeV}^{-2}]$	$2.745 \pm 0.046$	$4.271 \pm 0.021$	$4.072 \pm 0.017$	
$\chi^2/\text{dof}$	7356/5793	7448/5792	8339/5793	
two-channel model				
$\sigma_0 [\text{mb}]$	$20.97 \pm 0.48$	$22.89 \pm 0.17$	$23.02 \pm 0.23$	23 / 33
$\alpha_P - 1$	$0.136 \pm 0.001$	$0.129 \pm 0.001$	$0.131 \pm 0.001$	0.13 / 0.115
$\alpha'_P [\text{GeV}^{-2}]$	$0.078 \pm 0.001$	$0.075 \pm 0.001$	$0.071 \pm 0.001$	0.08 / 0.11
$a_{\text{ore}} [\text{GeV}]$	—	$0.718 \pm 0.012$	—	
$b_{\text{exp/ore/pow}} [\text{GeV}^{-2} \text{ or } -1]$	$0.917 \pm 0.007$	$1.517 \pm 0.008$	$0.931 \pm 0.002$	0.45
$\Delta a ^2$	$0.070 \pm 0.026$	$-0.058 \pm 0.009$	$0.042 \pm 0.011$	-0.04 / -0.25
$\Delta\gamma$	$0.052 \pm 0.042$	$0.131 \pm 0.018$	$0.273 \pm 0.023$	0.55 / 0.4
$b_1 [\text{GeV}^2]$	$8.438 \pm 0.108$	$8.951 \pm 0.041$	$8.877 \pm 0.040$	8.5 / 8.0
$c_1 [\text{GeV}^2]$	$0.298 \pm 0.012$	$0.278 \pm 0.004$	$0.266 \pm 0.006$	0.18 / 0.18
$d_1$	$0.472 \pm 0.007$	$0.465 \pm 0.002$	$0.465 \pm 0.003$	0.45 / 0.63
$b_2 [\text{GeV}^2]$	$4.982 \pm 0.133$	$4.222 \pm 0.052$	$4.780 \pm 0.060$	4.5 / 6.0
$c_2 [\text{GeV}^2]$	$0.542 \pm 0.015$	$0.522 \pm 0.006$	$0.615 \pm 0.006$	0.58 / 0.58
$d_2$	$0.453 \pm 0.009$	$0.452 \pm 0.003$	$0.431 \pm 0.004$	0.45 / 0.47
$\chi^2/\text{dof}$	5741/5786	6415/5785	7879/5786	

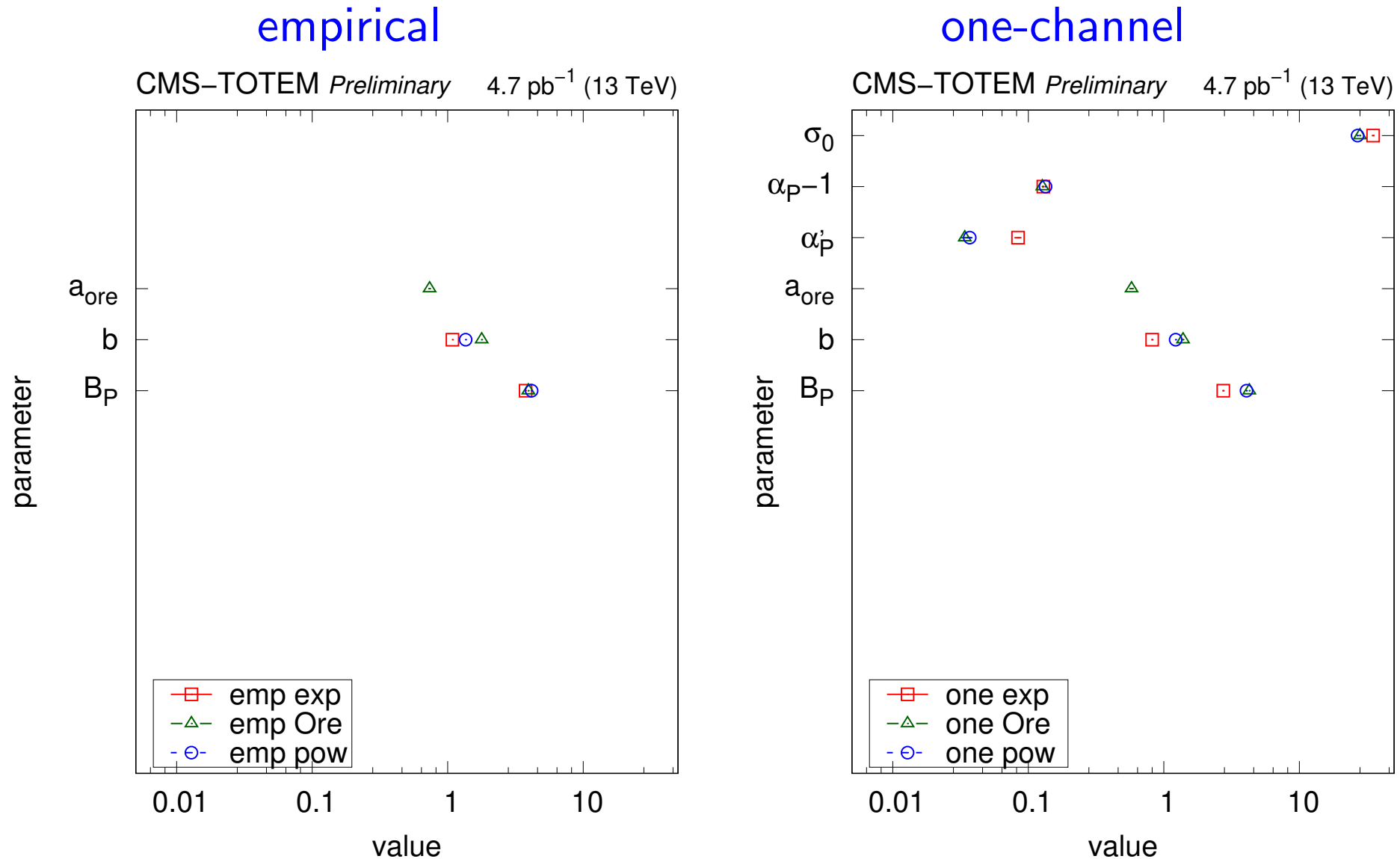
## • Models

- empirical  
(measured elastic diff cross section)
- one-channel  
(proton in ground state)
- two-channel  
(two diff eigenstates of the proton)

## • Form factors

- pomeron-meson  
(exponential, Orear-type, power-law)
- proton-pomeron

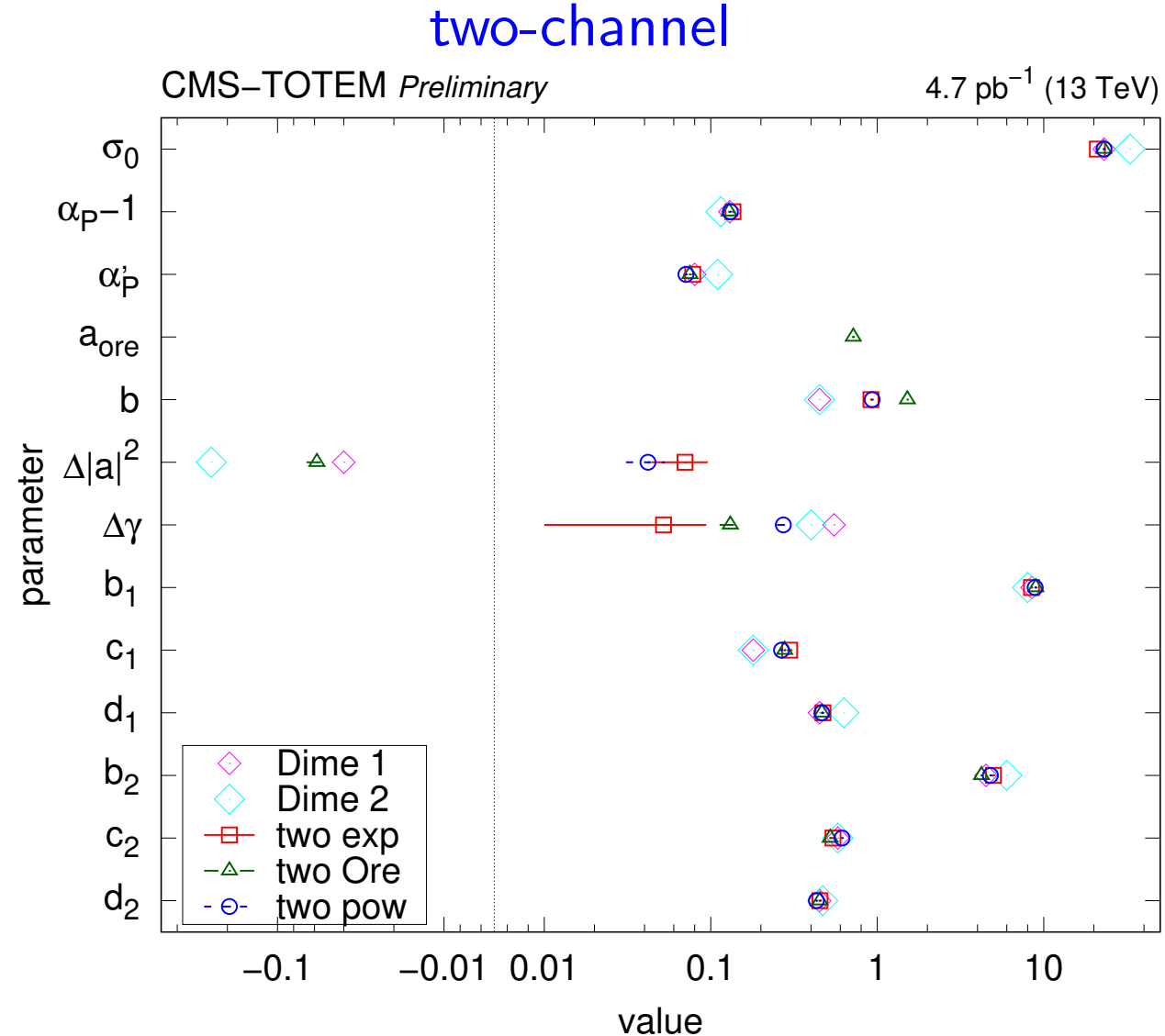
# Model tuning – result



Best fit with two-channel exponential, others are also close



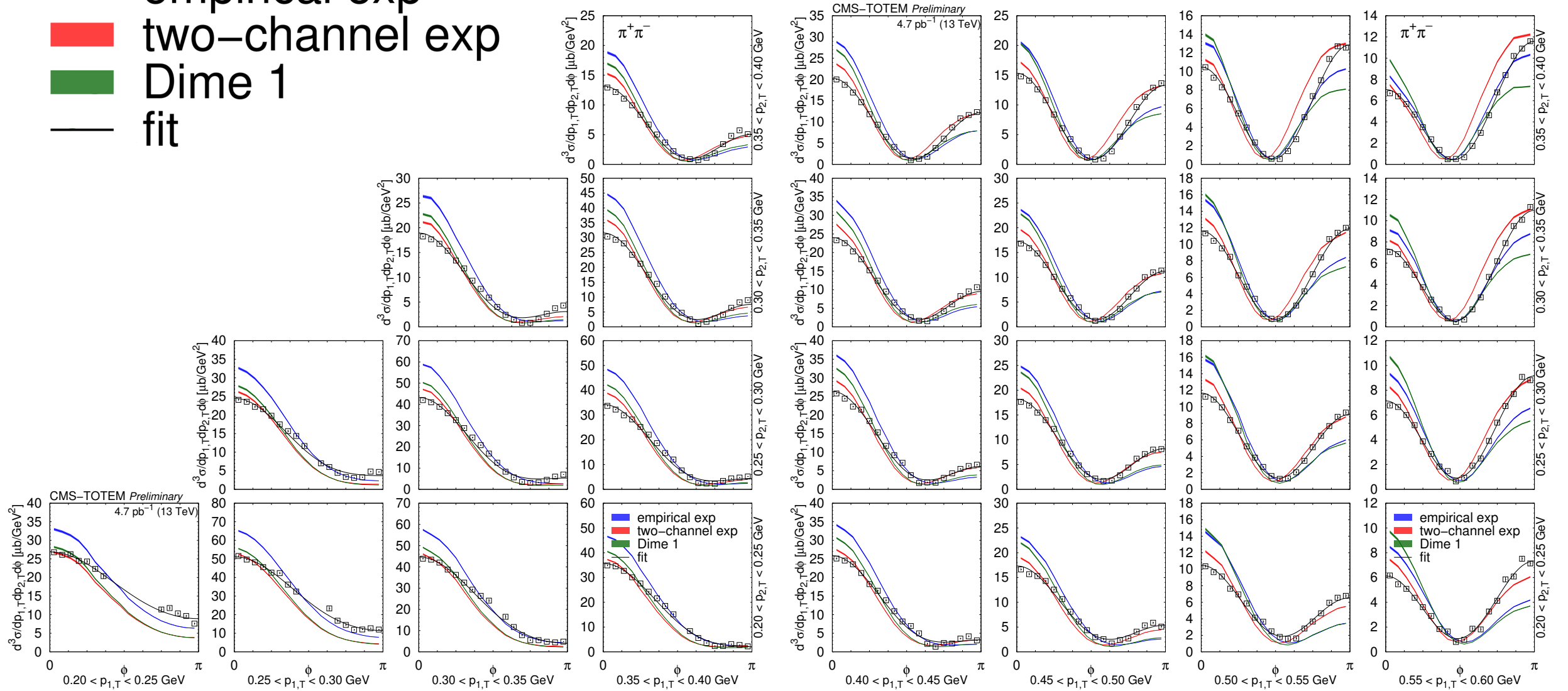
# Model tuning – result



Remarkable agreement with DIME (“soft model 1”), although with unexpected eigenstate weights ( $a_1 \approx a_2$ ) and eigenstate-pomeron coupling ( $\gamma_1 \approx \gamma_2$ )!

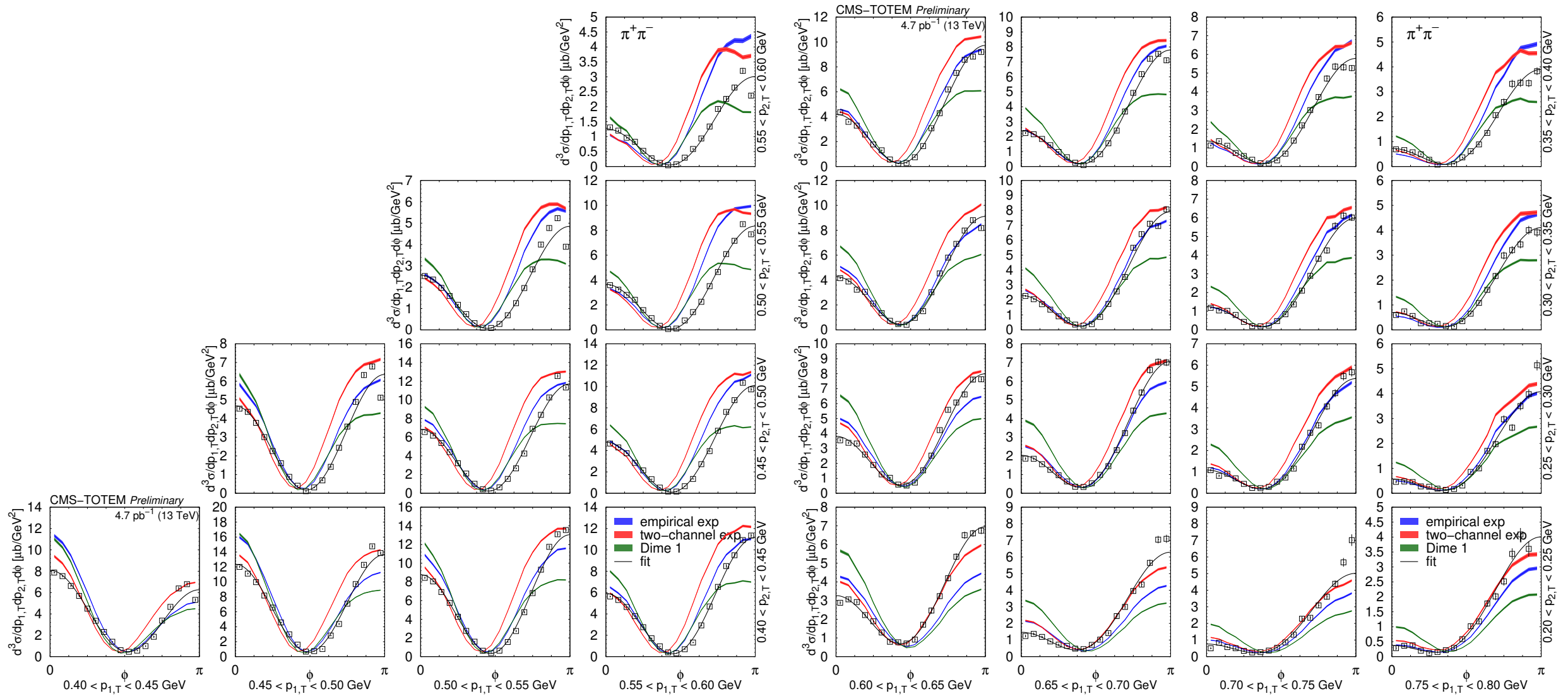
# $d\sigma/d\phi - \pi^+\pi^-$

- █ empirical exp
- █ two-channel exp
- █ Dime 1
- fit



Good quality

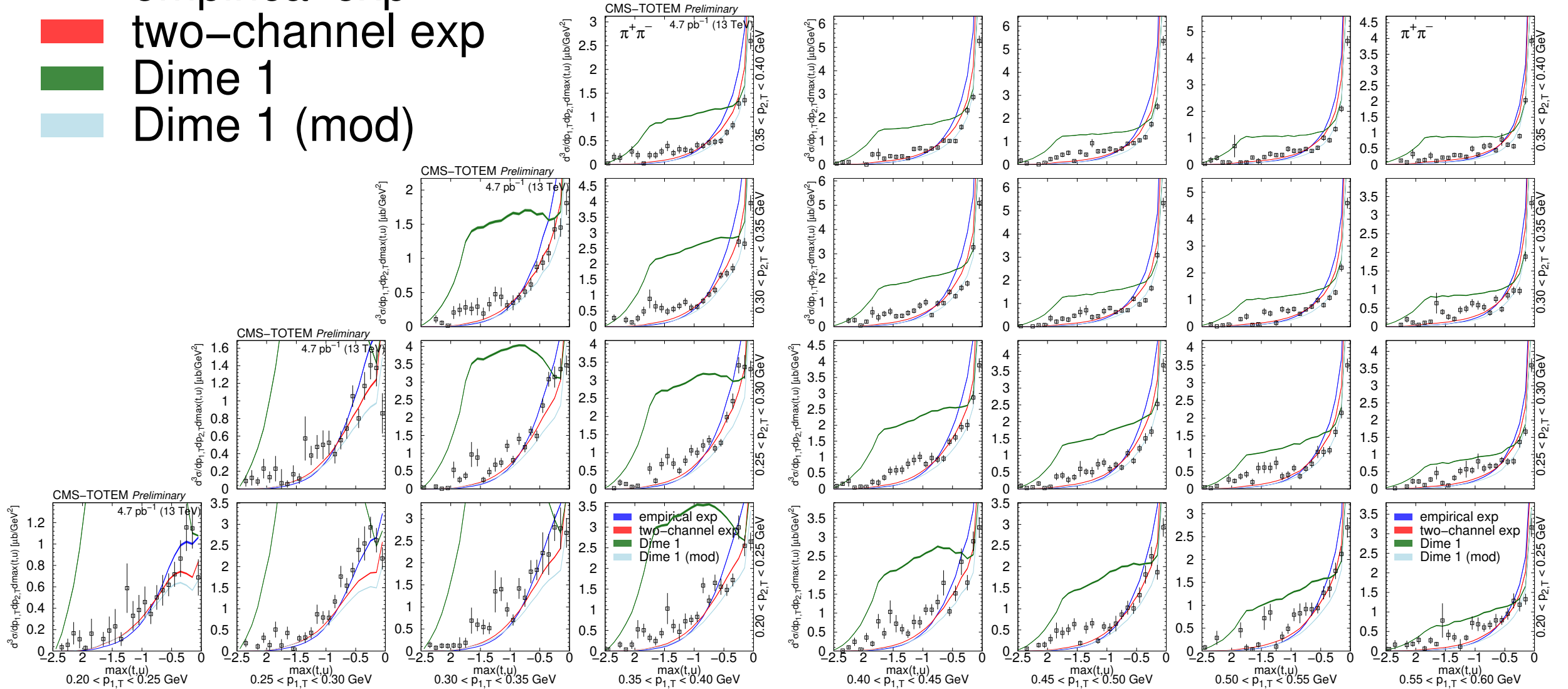
# $d\sigma/d\phi - \pi^+\pi^-$



Maybe a ground-state proton is enough? But then what about  $d\sigma/dt$

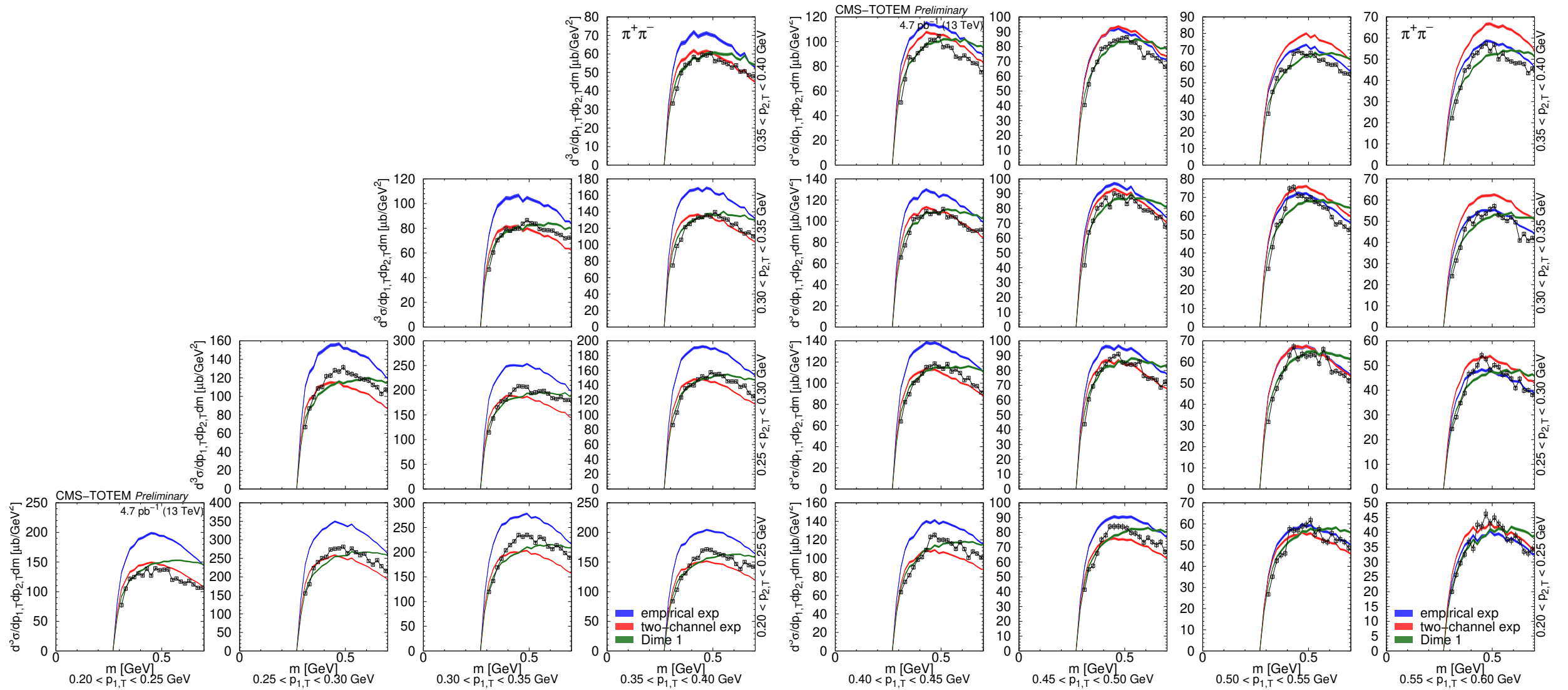
# $d\sigma/d\max(\hat{t}, \hat{u}) - \pi^+\pi^-$

- empirical exp
- two-channel exp
- Dime 1
- Dime 1 (mod)



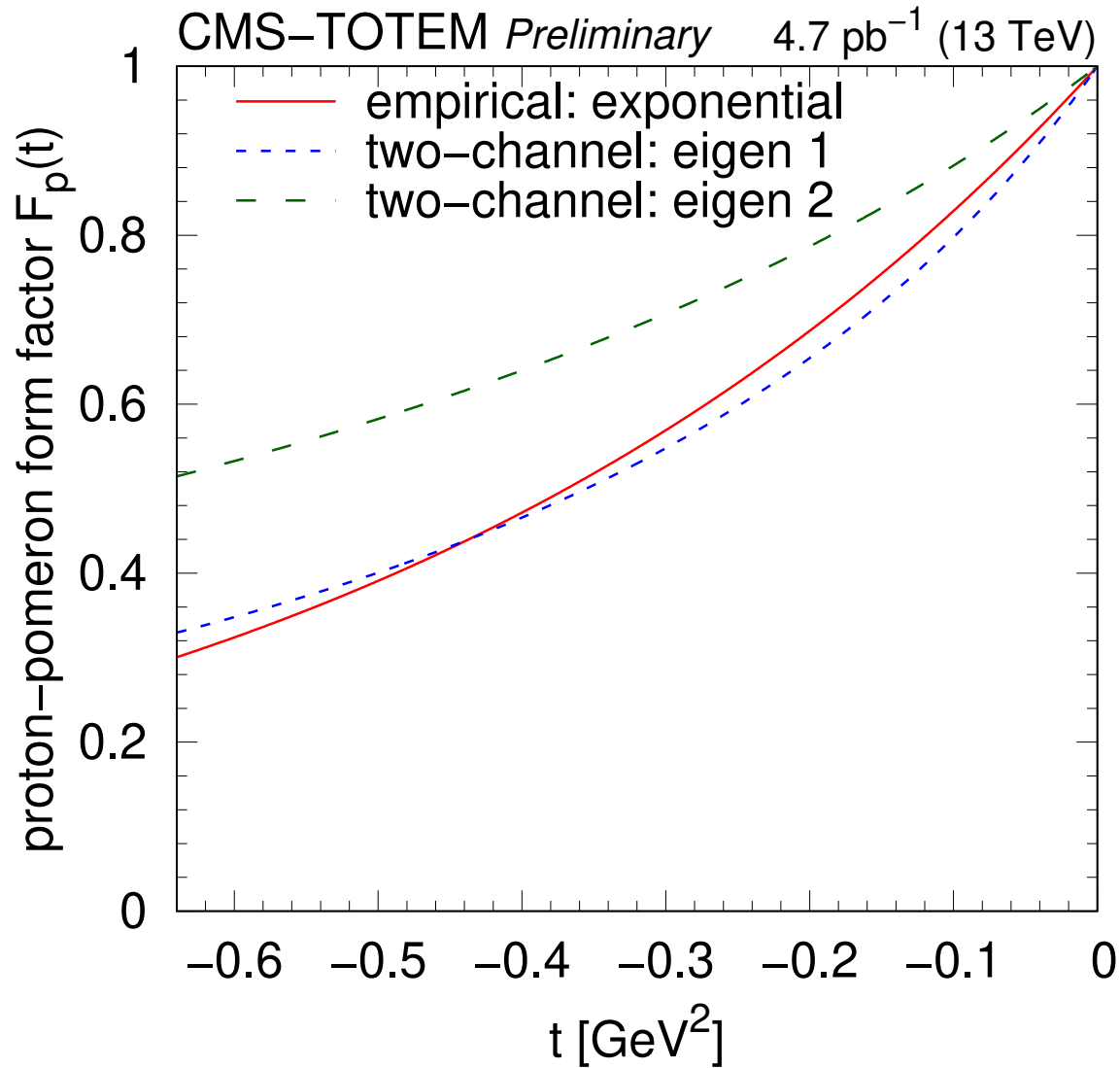
Virtual hadrons – important to fix the value of  $b_{\text{exp}}$  ( $0.45 \rightarrow 0.9 \text{ GeV}^{-2}$ )

# $d\sigma/dm - \pi^+\pi^-$

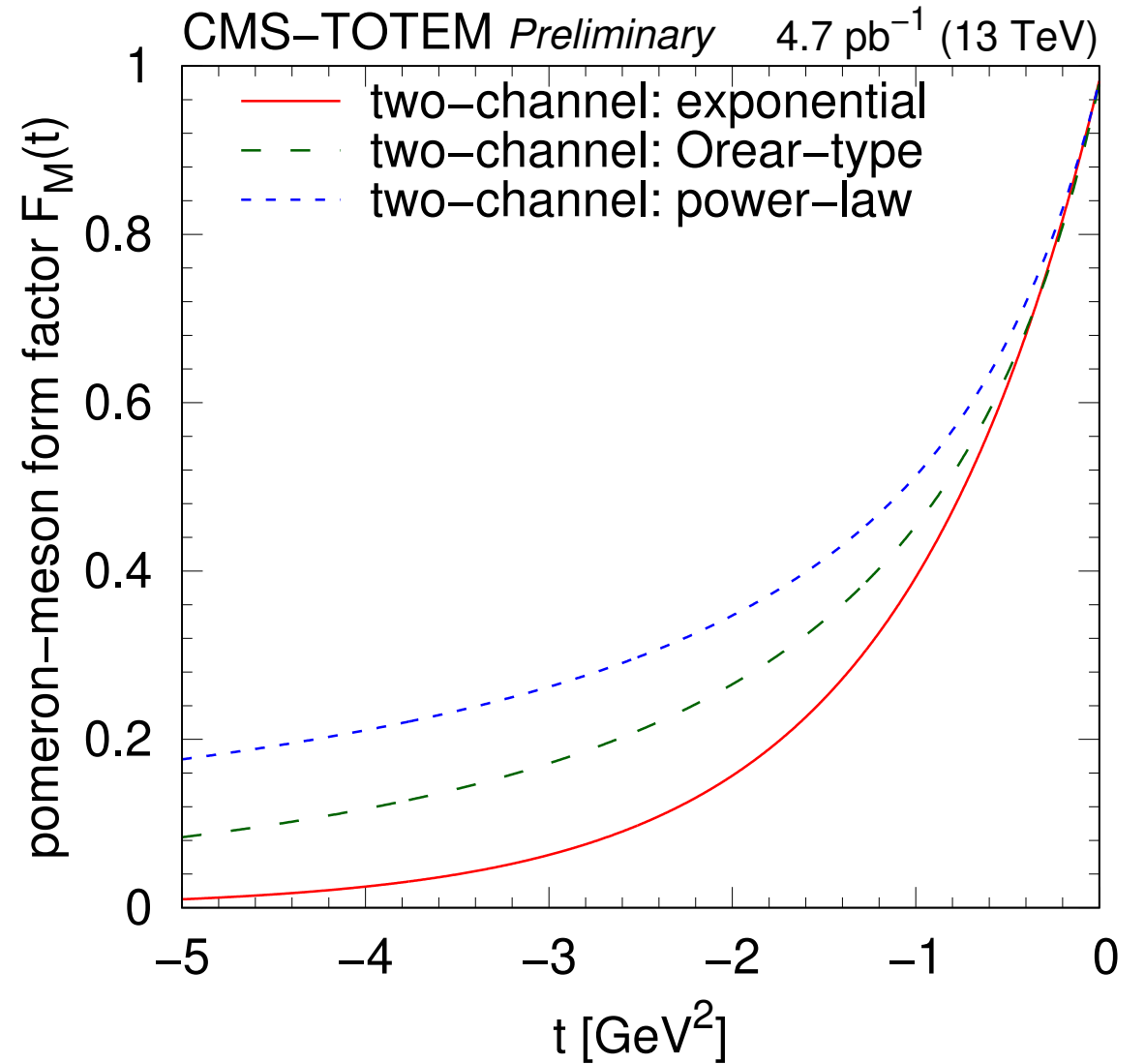


Invariant mass spectra of the central two-hadron system

# Form factors – $t$ -dependence

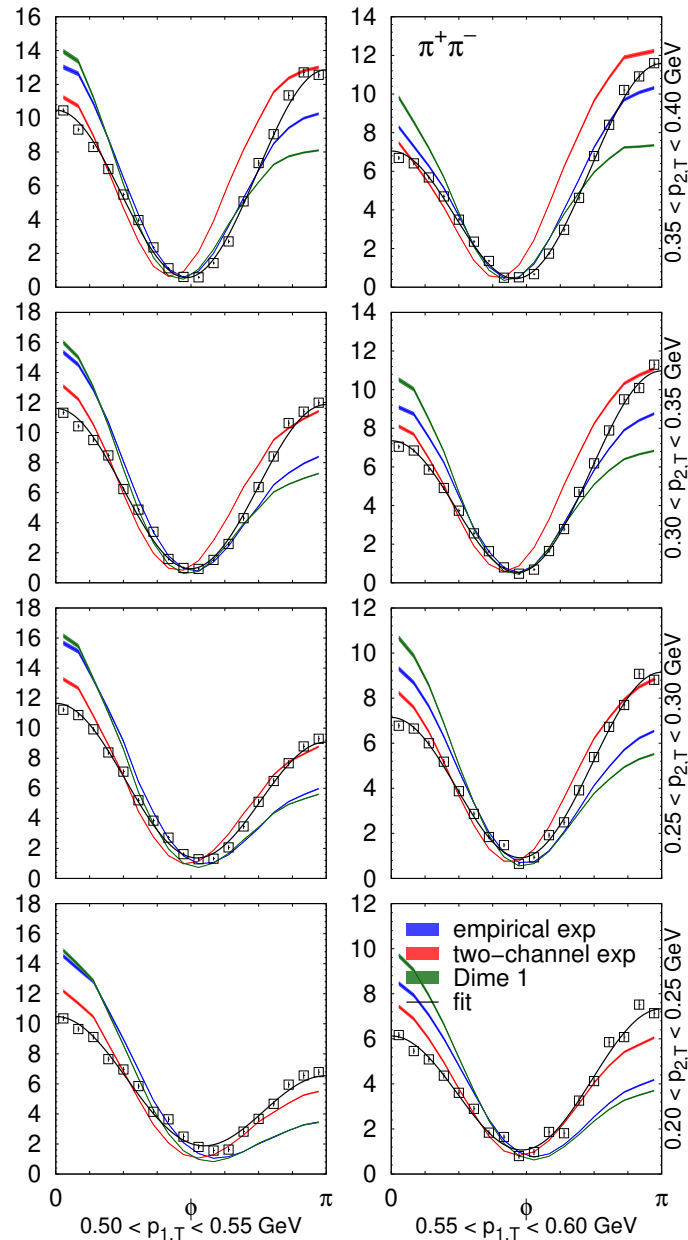


proton-pomeron



pomeron-meson

# Summary and conclusions



## • Analysis

- double pomeron exchange, charged hadron pairs, 13 TeV
- now the  $\pi^+\pi^-$  final state, resonance-free region
- differential cross sections in bins of  $(p_{1,T}, p_{2,T})$
- azimuthal angle  $\phi$  between the surviving protons

## • Results

- rich structure of nonperturbative interactions
- **parabolic minimum in the distribution of  $\phi$**  (first)
- **interference** of the bare and the rescattered amplitudes
- **model tuning: pomeron-related quantities** (first)
- good quality fits, **choices of form factors** tested

Physics Analysis Summary at: <https://cds.cern.ch/record/2867988>  
 More to come ( $\pi^+\pi^-$  and  $K^+K^-$  resonances!)