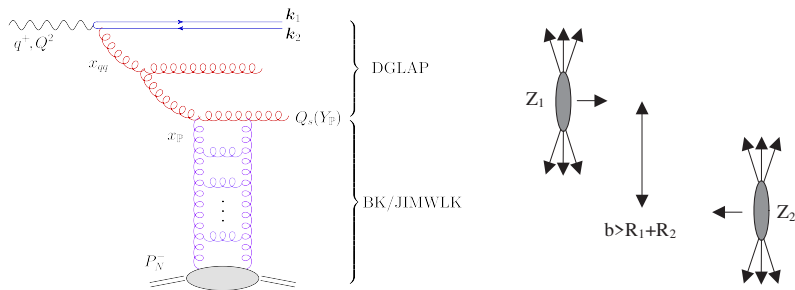


# Probing gluon saturation via diffractive jets in photon-nucleus interactions

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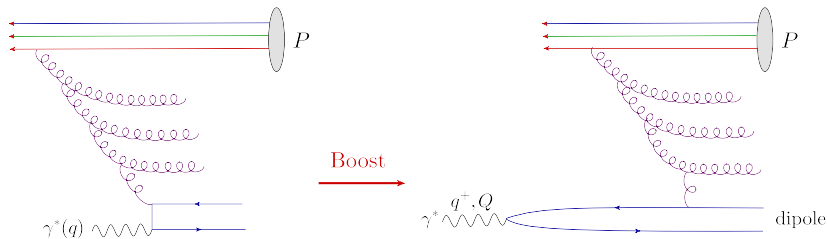
with A.H. Mueller, D.N. Triantafyllopoulos, and S.-Y. Wei  
 arXiv:2112.06353 (PRL) & 2207.06268 & 2304.12401



- Diffractive dijet production in photon-nucleus interactions at high energy:  
a golden channel to study saturation
  - electron-nucleus DIS at the future EIC (LHeC ?)
  - nucleus-nucleus UPCs at the LHC
- Why diffraction ?
  - elastic scattering  $\Rightarrow$  controlled by strong scattering (“black disk limit”)
  - particularly sensitive to high parton densities/gluon saturation
- Diffractive jets: a unique example of a hard process ( $P_{\perp} \gg Q_s \sim 1$  GeV) which is controlled by the physics of saturation
  - hard processes are easy to measure
  - a priori, well described by the collinear factorisation
  - saturation hidden in the diffractive PDFs (“non-perturbative”)
- The CGC allows one to compute diffractive dijets from first principles
  - collinear (actually, TMD) factorisation emerges from the CGC

# Dipole picture for DIS at high energy

- Small Bjorken  $x_{\text{Bj}} = \frac{Q^2}{2q^+P} \ll 1$ : convenient to work in the **dipole frame**
  - Lorentz boost to a frame where the dipole is energetic: **large  $q^+$**

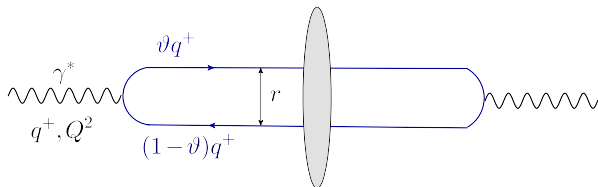


$$x_{\text{Bj}} = \frac{Q^2}{2P^-q^+} \ll 1 \iff \Delta x^+ \simeq \frac{2q^+}{Q^2} \gg \frac{1}{P^-}$$

- the virtual photon fluctuates into a  $q\bar{q}$  pair long before the scattering
- the  $q\bar{q}$  color dipole acts as a probe of the gluon distribution
- the dipole transverse size  $r$  is preserved by the scattering

# Dipole factorisation for inclusive DIS

- Photon wavefunction ( $\gamma^* \rightarrow q\bar{q}$ ) times dipole scattering (known to NLO)



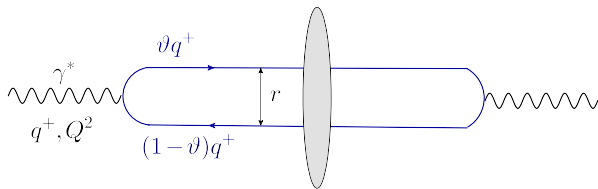
$$\sigma_{\gamma^* A}(Q^2, x) = \int d^2r \int_0^1 d\vartheta |\Psi_{\gamma^* \rightarrow q\bar{q}}(r, z; Q^2)|^2 \underbrace{\sigma_{\text{dipole}}(r, A, x)}_{2\pi R_A^2 T_A(r, x)}$$

- Dipole amplitude  $T_A(r, x)$ : solution to BK/JIMWLK equations (to NLO)

$$T_A(r, x) \simeq \begin{cases} r^2 Q_s^2(A, x) & \text{for } rQ_s \ll 1 \text{ (color transparency)} \\ 1 & \text{for } rQ_s \gtrsim 1 \text{ (black disk/saturation)} \end{cases}$$

- Saturation momentum:  $Q_s^2(A, x) \sim A^{1/3}/x^{\lambda_s}$  with  $\lambda_s \sim 0.3$

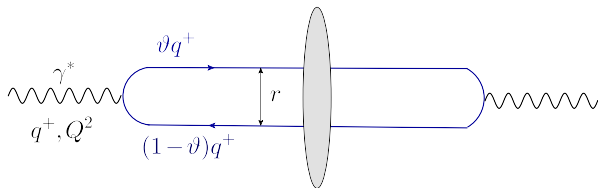
# Inclusive DIS in the dipole picture



$$\sigma_{\gamma^* A}(Q^2, x) = \int d^2 r \int_0^1 d\vartheta |\Psi_{\gamma^* \rightarrow q\bar{q}}(r, z; Q^2)|^2 \underbrace{\sigma_{\text{dipole}}(r, A, x)}_{2\pi R_A^2 T_A(r, x)}$$

- Dipole size limited by virtuality:  $r^2 \lesssim 1/\bar{Q}^2$  with  $\bar{Q}^2 \equiv \vartheta(1-\vartheta)Q^2$
- To probe saturation, one needs  $r \gtrsim 1/Q_s$ , hence  $\bar{Q}^2 \lesssim Q_s^2$
- A priori, two interesting situations:
  - symmetric jets  $\vartheta \sim 1/2$ , but semi-hard photon:  $Q^2 \sim Q_s^2$
  - hard photon  $Q^2 \gg Q_s^2$ , but asymmetric jets (“aligned”):  $\vartheta(1-\vartheta) \ll 1$

# Inclusive DIS in the dipole picture

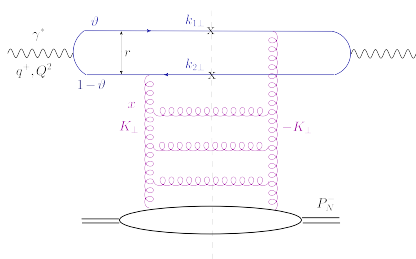
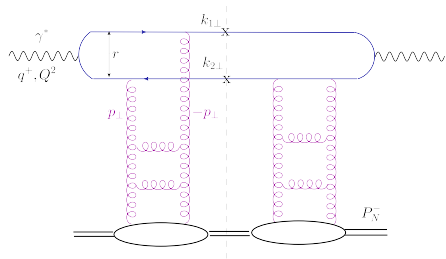


$$\sigma_{\gamma^*A}(Q^2, x) = \int d^2r \int_0^1 d\vartheta |\Psi_{\gamma^* \rightarrow q\bar{q}}(r, z; Q^2)|^2 \underbrace{\sigma_{\text{dipole}}(r, A, x)}_{2\pi R_A^2 T_A(r, x)}$$

- Excellent fits to *ep* data ( $F_2$ ,  $F_L$ ,  $F_{2c}$ ) at HERA:  $x \leq 10^{-2}$ ,  $Q^2 \leq 50 \text{ GeV}^2$
- However, inclusive DIS probes (quasi)symmetric  $q\bar{q}$  configurations  
 $\Rightarrow$  gluon saturation probed only for low  $Q^2 \sim Q_s^2 \lesssim 1 \text{ GeV}^2$ 
  - limited region in phase-space, non-perturbative contamination ☹️
- Can one measure saturation directly at high  $Q^2$  ?

- Elastic scattering/diffraction is **more sensitive to strong scattering**

$$\sigma_{el} \propto |T|^2 \longleftrightarrow \sigma_{tot} \propto 2\text{Im}T$$

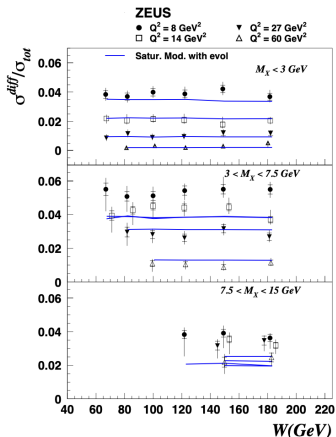


- Colourless exchange: 2-gluon ladder, (BFKL) Pomeron, rapidity gap  $Y_{\mathbb{P}}$
- $F_{2D}$  controlled by the **black disk limit** ( $T \sim 1$ ) even when  $Q^2 \gg Q_s^2$ 
  - asymmetric  $q\bar{q}$  pairs,  $\vartheta(1 - \vartheta) \ll 1$ , with large size  $r \sim 1/Q_s$
  - would be non-perturbative,  $r \sim 1/\Lambda$ , in absence of saturation

# One vs two Pomerons... at HERA

- Naively (2-gluon exchange):  $\sigma_{\text{diff}}$  rises with  $\frac{1}{x}$  or with  $A$  like two Pomerons

$$T^2 \simeq \left( r^2 Q_s^2(A, x) \right)^2 \propto \frac{A^{2/3}}{x^{2\lambda_s}} \quad \text{vs.} \quad T \simeq r^2 Q_s^2(A, x) \propto \frac{A^{1/3}}{x^{\lambda_s}}$$



- But it doesn't! Diffraction is controlled by  $T \sim 1$ , or  $r \sim 1/Q_s$
- Almost the same scaling as  $\sigma_{\text{tot}}$ :

$$\frac{\sigma_{\text{el}}}{\sigma_{\text{tot}}} \sim \frac{1}{\ln(Q^2/Q_s^2)}$$

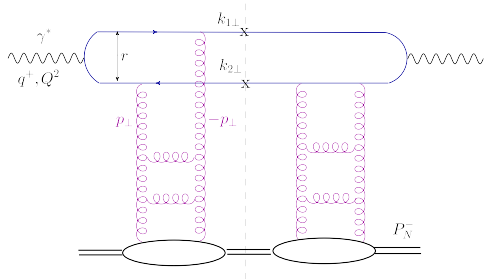
- Weak  $x$ -dependence confirmed by HERA (*Bartels, Golec-Biernat, Kowalski, 2002*)
- Would be interesting to also check the  $A$ -dependence at the EIC

Figure 9: The ratio of  $\sigma_{\text{diff}}/\sigma_{\text{tot}}$  versus the  $\gamma^*p$  energy  $W$ . The data is from ZEUS and the solid



# Exclusive dijets is higher twist

- What would be a **jet measurement** analogous to  $F_{2D}$  ?
- Elastic scattering can also produce **exclusive dijets**:
  - a  $q\bar{q}$  pair which is hard:  $k_{1\perp} \simeq k_{2\perp} \equiv P_{\perp} \gg Q_s$  & symmetric:  $\vartheta \sim 1/2$
- ... but these are rare events (“higher twist”), **insensitive to saturation**:
  - $\sigma_{\text{el}} \sim |T_{q\bar{q}}(r, Y_{\mathbb{P}})|^2$  with  $r \sim 1/P_{\perp}$
  - $P_{\perp} \gg Q_s(Y_{\mathbb{P}})$ : small dipole  $\implies$  weak scattering



- **rapidity gap**  $Y_{\mathbb{P}} = \ln \frac{1}{x_{\mathbb{P}}}$

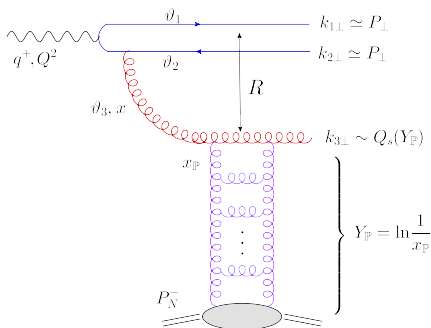
$$\frac{d\sigma_{\text{el}}^{\gamma A \rightarrow q\bar{q}A}}{d\vartheta_1 d\vartheta_2 d^2\mathbf{P}} \propto \frac{1}{P_{\perp}^6}$$

$$Q_s^2 \equiv Q_s^2(A, Y_{\mathbb{P}}) \sim A^{1/3} e^{0.3Y_{\mathbb{P}}}$$

# Diffractive 2+1 jets

(E.I., A.H. Mueller, D.N. Triantafyllopoulos, *Phys.Rev.Lett.* 128 (2022) 20)

- Can one have diffractive dijets **at leading twist** ? ( $\sim 1/P_{\perp}^4$ )
- Yes ... provided one allows for **strong scattering** !
- 2+1 jets: 2 hard ( $P_{\perp} \gg Q_s$ ) and 1 semi-hard ( $k_{3\perp} \sim Q_s$ )

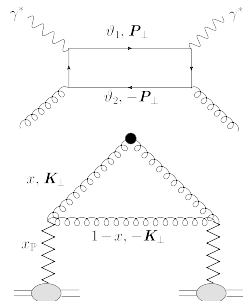
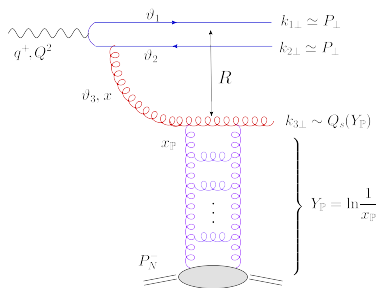


$$R \sim \frac{1}{Q_s} \gg r \sim \frac{1}{P_{\perp}}$$

- Effective **gluon-gluon** dipole
  - Strong scattering:  $T_{gg}(R, Y_{\mathbb{P}}) \sim 1$
  - **Semi-inclusive** dijet production
  - $\mathcal{O}(\alpha_s)$ , but leading-twist
- 3rd jet controls the hard dijet imbalance:  $K_{\perp} \equiv |\mathbf{k}_1 + \mathbf{k}_2| = k_{3\perp} \ll P_{\perp}$

# TMD factorisation for diffractive 2+1 jets

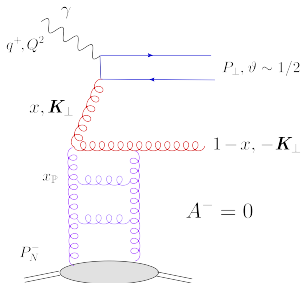
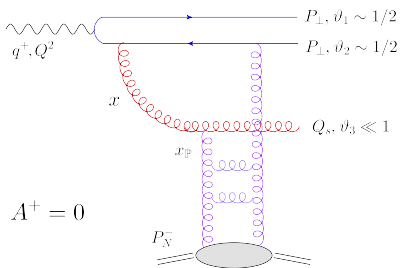
- The third jet is relatively **soft**:  $k_3^+ = \vartheta_3 q^+$  with  $\vartheta_3 \sim \frac{Q^2}{Q_s^2} \ll 1$ 
  - gluon formation time must be small enough to scatter:  $\frac{k_3^+}{k_{3\perp}^2} \lesssim \frac{q^+}{Q^2}$
- It can alternatively be seen as a part of the **Pomeron wavefunction**
  - boost back to target infinite momentum frame & change gauge



- $x$ : energy fraction of the exchanged gluon **with respect to the Pomeron**

# TMD factorisation for diffractive 2+1 jets (2)

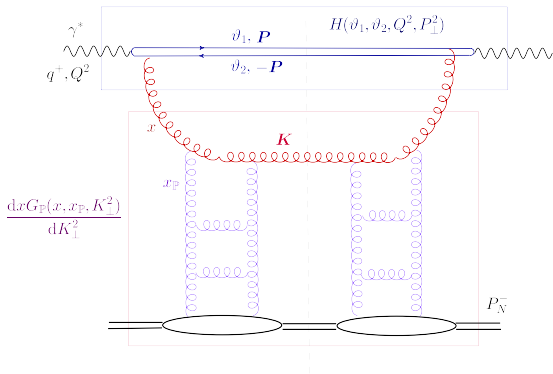
- The strong ordering in **both**  $k_{\perp}$  and  $k^+$  is essential for factorisation
- The **dipole picture** holds in the **projectile** light cone gauge  $A^+ = 0$ 
  - right moving partons couple to the  $A^-$  component of the target field



- The **TMD picture** holds in the **target** light cone gauge  $A^- = 0$ 
  - only the soft gluon couples to the target field:  $v^i A^i$  with  $v^i = k^i/k^+$

# TMD factorisation for diffractive 2+1 jets (3)

$$\frac{d\sigma_{2+1}^{\gamma^* A \rightarrow q\bar{q}gA}}{d\vartheta_1 d\vartheta_2 d^2\mathbf{P} d^2\mathbf{K} dY_{\mathbb{P}}} = H_{T,L}(\vartheta_1, \vartheta_2, Q^2, P_{\perp}^2) \frac{dx G_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}}$$

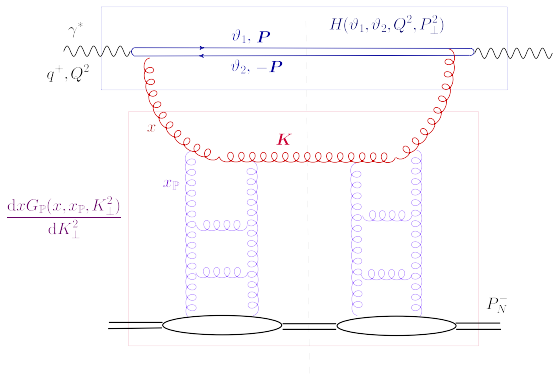


- **The hard factor:**  $\gamma^* \rightarrow q\bar{q}$  decay & the gluon emission

$$H_T = \alpha_{\text{em}} \alpha_s \left( \sum e_f^2 \right) \vartheta_1 \vartheta_2 (\vartheta_1^2 + \vartheta_2^2) \frac{1}{P_{\perp}^4} \quad \text{when } Q^2 \ll P_{\perp}^2$$

# TMD factorisation for diffractive 2+1 jets (3)

$$\frac{d\sigma_{2+1}^{\gamma^* A \rightarrow q\bar{q}gA}}{d\vartheta_1 d\vartheta_2 d^2\mathbf{P} d^2\mathbf{K} dY_{\mathbb{P}}} = H_{T,L}(\vartheta_1, \vartheta_2, Q^2, P_{\perp}^2) \frac{dx G_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}}$$



- The unintegrated gluon distribution of the Pomeron: a **diffractive TMD**
- Implicit in early studies of inclusive diffraction  
(*Hebecker, Golec-Biernat, Wüsthoff, Hautmann, Soper ... 97-01*)

$$\frac{dx G_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2 K} = \frac{S_{\perp}(N_c^2 - 1)}{4\pi^3} \underbrace{\Phi_g(x, x_{\mathbb{P}}, K_{\perp}^2)}_{\text{occupation number}}$$

- Explicitly computed in terms of the gluon-gluon dipole amplitude  $T_{gg}(R, Y_{\mathbb{P}})$

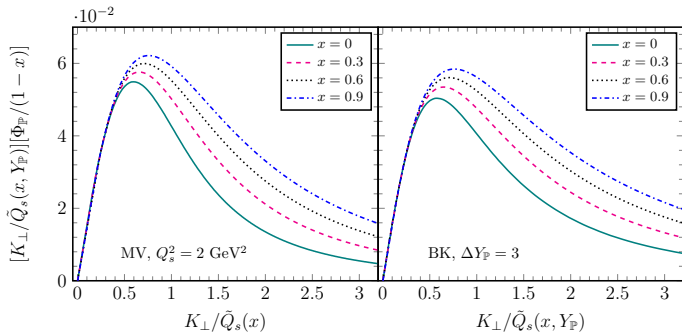
$$\Phi_g(x, x_{\mathbb{P}}, K_{\perp}^2) \simeq (1-x) \begin{cases} 1, & K_{\perp} \lesssim \tilde{Q}_s(x) \\ \frac{\tilde{Q}_s^4(x)}{K_{\perp}^4}, & K_{\perp} \gg \tilde{Q}_s(x) \end{cases}$$

- Valid for small  $x_{\mathbb{P}} \lesssim 10^{-2}$  but any  $x \leq 1$ 
  - effective saturation momentum:  $\tilde{Q}_s^2(x, Y_{\mathbb{P}}) = (1-x)Q_s^2(Y_{\mathbb{P}})$
- Very fast decrease  $\sim 1/K_{\perp}^4$  at large gluon momenta  $K_{\perp} \gg \tilde{Q}_s(x)$
- The bulk of the distribution lies at **saturation**:  $K_{\perp} \lesssim \tilde{Q}_s(x)$

# Numerical results

(E.I., A.H. Mueller, D.N. Triantafyllopoulos, S.-Y. Wei, arXiv:2207.06268)

- Left: McLerran-Venugopalan model. Right: adding high-energy evolution
- Pronounced peak at  $K_{\perp} \simeq \tilde{Q}_s$ : **diffraction is controlled by saturation**



- **BK evolution of  $T_{gg}(R, Y_P)$** : evolution of  $\Phi_P(x, x_P, K_{\perp})$  in  $x_P$  and  $K_{\perp}$ 
  - increasing  $Q_s^2(Y_P)$ , but the shape remains the same (geometric scaling)



# The gluon diffractive PDF

- By integrating the gluon momentum  $K_{\perp}$ : the usual **collinear factorisation**

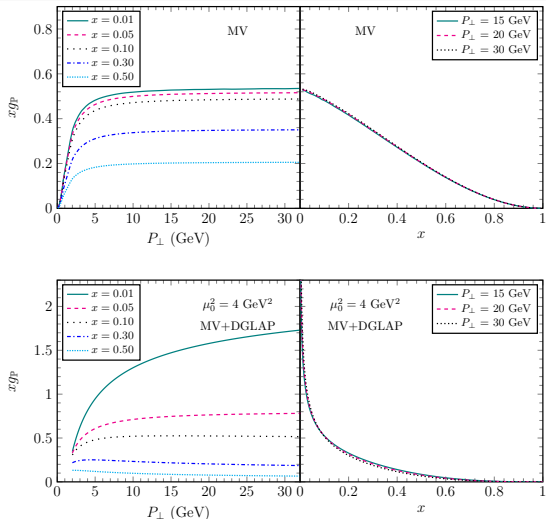
$$\frac{d\sigma_{2+1}^{\gamma A \rightarrow q\bar{q}gA}}{d\vartheta_1 d\vartheta_2 d^2\mathbf{P} dY_{\mathbb{P}}} = H(\vartheta_1, \vartheta_2, Q^2, P_{\perp}^2) xG_{\mathbb{P}}(x, x_{\mathbb{P}}, P_{\perp}^2)$$

- ... but with an **explicit result** for the gluon diffractive PDF:

$$xG_{\mathbb{P}}(x, x_{\mathbb{P}}, P_{\perp}^2) \equiv \int^{P_{\perp}} d^2\mathbf{K} \frac{dxG_{\mathbb{P}}(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}} \propto (1-x)^2 Q_s^2(A, Y_{\mathbb{P}})$$

- The integral is rapidly converging and effectively **cut off at**  $K_{\perp} \sim \tilde{Q}_s(x)$
- The  $(1-x)^2$  vanishing at the end point is a hallmark of saturation
- **DGLAP evolution** with increasing  $P_{\perp}^2$
- **Initial condition** for DGLAP determined by **saturation** (MV+BK)

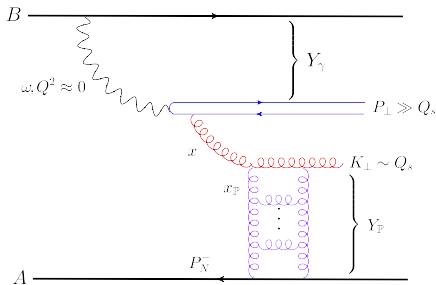
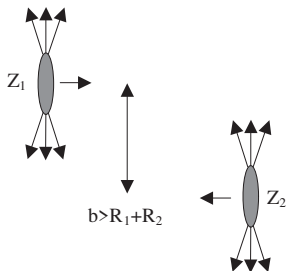
# The gluon diffractive PDF: numerical results



- **DGLAP:** increase for very small  $x \leq 0.01$ , slight decrease for  $x > 0.05$
- When  $x \rightarrow 1$ , the distribution vanishes even faster

# 2+1 diffractive dijets in $AA$ UPCs

- Large impact parameter  $b > R_A + R_B \implies$  photon-mediated interactions
  - one nucleus acts as a photon emitter, the other one as a hadronic target
- Quasi-real photon: virtuality  $Q^2 = (\omega/\gamma)^2$  with  $\gamma =$  Lorentz factor

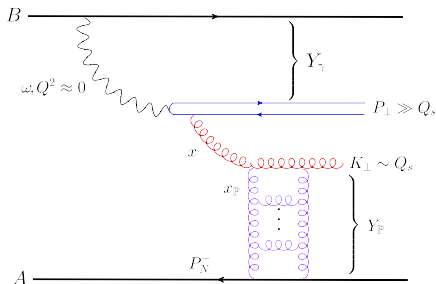
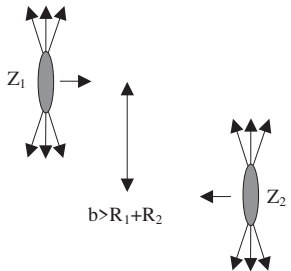


$$\frac{d\sigma_{2+1}^{AB \rightarrow q\bar{q}gAB}}{d\eta_1 d\eta_2 d^2\mathbf{P} d^2\mathbf{K} dY_{\mathbb{P}}} = \omega \frac{dN_B}{d\omega} H(\eta_1, \eta_2, P_{\perp}^2) \frac{dx G_{\mathbb{P}}^A(x, x_{\mathbb{P}}, K_{\perp}^2)}{d^2\mathbf{K}} + (A \leftrightarrow B)$$

- Energy flux  $\times$  Hard factor  $\times$  Gluon diffractive TMD

# 2+1 diffractive dijets in $AA$ UPCs

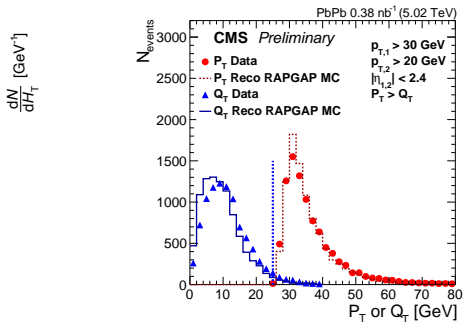
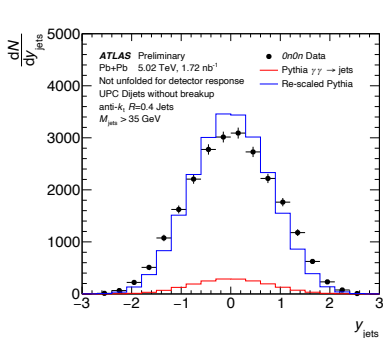
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- **Coherent diffraction:** target nucleus does not break
  - rapidity gaps on both sides: photon gap + diffractive gap
  - how to distinguish the photon emitter from the nuclear target ?

# Diffractive jets in Pb+Pb UPCs at the LHC

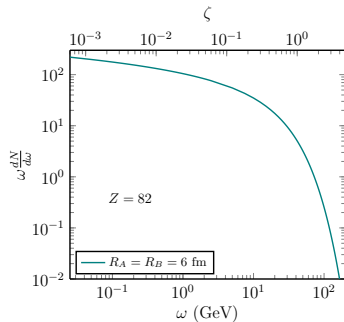
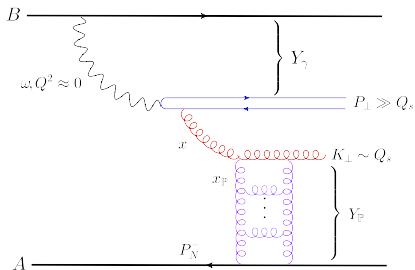
- Recent measurements: *ATLAS-CONF-2022-021* and *CMS arXiv:2205.00045*



- Several thousands of candidate-events for **coherent diffraction**
  - no just  $\gamma\gamma$  scattering: cross-section would be 10 times smaller
- Most likely: 2+1 jets ... but not that easy to experimentally check
  - the experimental set-up is not ideal for observing the 3rd jet

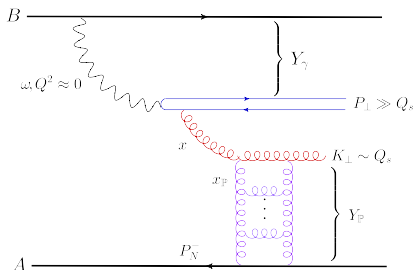
# Energy cutoff

- Energy is **not that high**:
  - LHC:  $\sqrt{s_{NN}} = 2E_N = 5 \text{ TeV}$ , yet  $\sqrt{s_{\gamma N}} = \sqrt{4\omega_{\max}E_N} \simeq 650 \text{ GeV}$
  - upper energy cutoff:  $b \sim \frac{1}{Q} > 2R_A \Rightarrow \omega < \frac{\gamma}{2R_A} \equiv \omega_{\max} \simeq 40 \text{ GeV}$
  - exponential suppression for  $\omega > \omega_{\max}$



# $x_{\mathbb{P}}$ is not that small

- Limited energy and relatively hard dijets  $P_{\perp} \geq 15 \text{ GeV}$ 
  - relatively large  $x_{\mathbb{P}}$ :  $x_{\mathbb{P}} \gtrsim 5 \times 10^{-3}$
  - one cannot probe the high energy evolution of the Pomeron



$$\eta_1 \simeq \eta_2 \equiv y$$

$$x_{\mathbb{P}, \min} = \frac{P_{\perp}}{E_N} e^{-y}$$

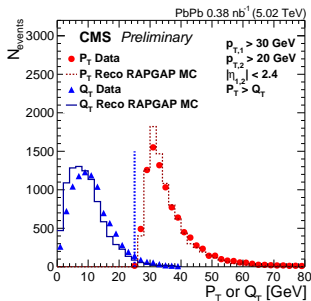
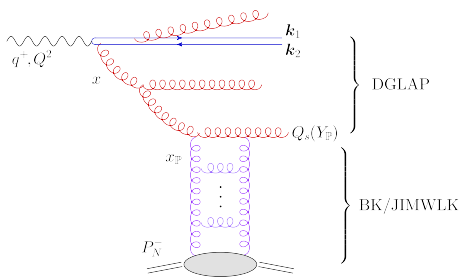
$$\omega = P_{\perp} e^y$$

$$P_{\perp} \sim \omega_{\max} \Rightarrow y \lesssim 1$$

- Not the ideal “small- $x_{\mathbb{P}}$ ” set-up! Similar in that sense to the EIC
- Decreasing  $P_{\perp}$  would greatly help !

# The 3rd jet is not easy to observe

- $K_{\perp} \sim Q_s \sim 1 \div 2 \text{ GeV}$ : not really a jet! could be measured as a hadron
- Large  $P_{\perp} \Rightarrow$  large phase-space for DGLAP evolution
  - additional gluons with transverse momenta  $Q_s \ll k_{\perp} \ll P_{\perp}$

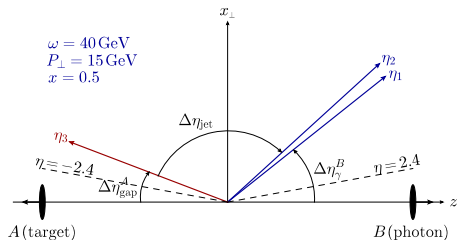


- Large dijet imbalance  $Q_T = |\mathbf{k}_1 + \mathbf{k}_2| \sim 10 \text{ GeV} \gg Q_s$  (seen at the LHC)
  - consistent with final state radiation (*Hatta et al, 2010.10774*)
  - insensitive to the 3rd jet



# How to measure the 3rd jet ?

- Observing the 3rd jet would be **extremely useful**
  - it propagates towards the nuclear target: lift the  $A$  vs.  $B$  ambiguity
  - measure the diffractive rapidity gap and thus infer  $x_{\mathbb{P}}$
- E.g.: assume the photon to be a **right mover**: it was emitted by nucleus  $B$

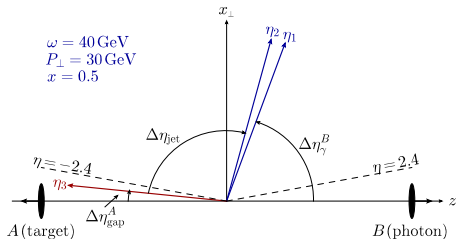


$$\Delta\eta_{\text{jet}} \gtrsim \ln \frac{2P_{\perp}}{Q_s} \simeq 2 \div 3$$

- large  $\omega = 40 \text{ GeV}$ ,  $P_{\perp} = 15 \text{ GeV}$
- $\eta_{1,2} \simeq 1$ ,  $\Delta\eta_{\text{jet}} = 2.7$ ,  $x_{\mathbb{P}} \simeq 0.004$
- Rapidity separation  $\Delta\eta_{\text{jet}}$ : a **direct measure of the saturation momentum  $Q_s$**
- The 3rd “jet” could have been seen as a hadron by CMS:  $|\eta_3| < |\eta_{\text{max}}| = 2.4$

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- E.g.: assume the photon to be a **right mover**: it was emitted by nucleus  $B$

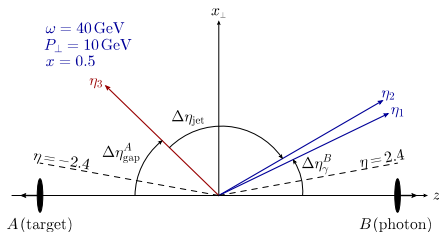


$$\Delta\eta_{\text{jet}} \gtrsim \ln \frac{2P_{\perp}}{Q_s} \simeq 2 \div 3$$

- large  $\omega = 40 \text{ GeV}$ , larger  $P_{\perp} = 30 \text{ GeV}$
- $\eta_{1,2} \simeq 0.3$ ,  $\Delta\eta_{\text{jet}} = 3.4$ ,  $x_{\mathbb{P}} \simeq 0.02$
- Rapidity separation  $\Delta\eta_{\text{jet}}$ : a **direct measure of the saturation momentum  $Q_s$**
- Yet, CMS measured  $P_{\perp} = 30 \text{ GeV}$ ... so they missed it! ([arXiv:2205.00045](https://arxiv.org/abs/2205.00045))

# How to measure the 3rd jet ?

- Observing the 3rd jet would be **extremely useful**
  - it propagates towards the nuclear target: lift the  $A$  vs.  $B$  ambiguity
  - measure the diffractive rapidity gap and thus infer  $x_{\mathbb{P}}$
- E.g.: assume the photon to be a **right mover**: it was emitted by nucleus  $B$



$$\Delta\eta_{\text{jet}} \gtrsim \ln \frac{2P_{\perp}}{Q_s} \simeq 2 \div 3$$

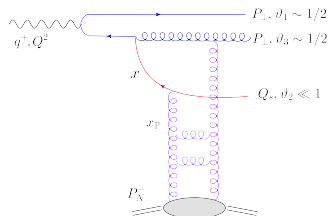
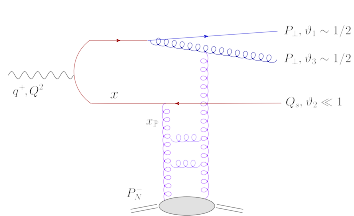
- large  $\omega = 40 \text{ GeV}$ , lower  $P_{\perp} = 10 \text{ GeV}$
- $\eta_{1,2} \simeq 1.4$ ,  $\Delta\eta_{\text{jet}} = 2.3$ ,  $x_{\mathbb{P}} \simeq 0.002$
- Rapidity separation  $\Delta\eta_{\text{jet}}$ : a direct measure of the saturation momentum  $Q_s$
- The situation would **greatly improve** by decreasing  $P_{\perp}$  (ALICE ?)

# Conclusions

- Diffraction in  $\gamma A$  (EIC, UPC): the best laboratory to study **gluon saturation**
- For sufficiently small  $x_{\mathbb{P}} \lesssim 10^{-2}$  and/or large  $A \sim 200$ , **diffractive TMDs and PDFs can be computed from first principles**
- Due to saturation, diffractive dijets are dominated by **(2+1)-jet events**
- Experimentally observing the semi-hard, 3rd, jet appears to be tough, but it would be **highly beneficial**
  - distinguish the photon emitter from the target nucleus
  - confirm the overall physical picture and its predictions
- Measure dijets (or dihadrons) with lower  **$P_{\perp} \leq 10$  GeV**
- Use hadronic detectors at **larger rapidities**

# 2+1 jets with a hard gluon

- The third (semi-hard) jet can also be a **quark**: same-order



- TMD factorisation: **quark unintegrated distribution of the Pomeron**

