

Prediction for impact parameter and transverse sphericity in heavy-ion collisions at the LHC

Workshop on Application of AI and ML

10th Nov 2022



Neelkamal Mallick

Department of Physics, IIT Indore

neelkamal.mallick@cern.ch

Based on:

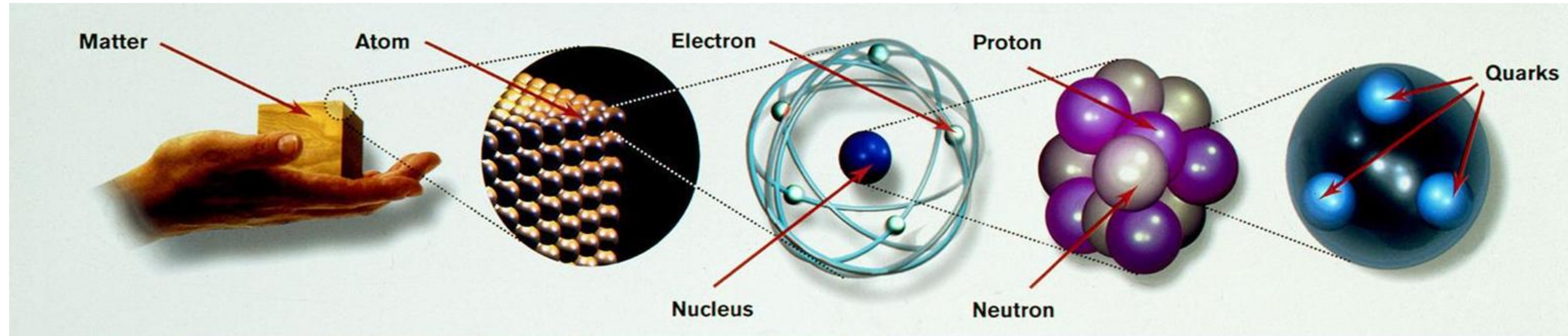
N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

Outline

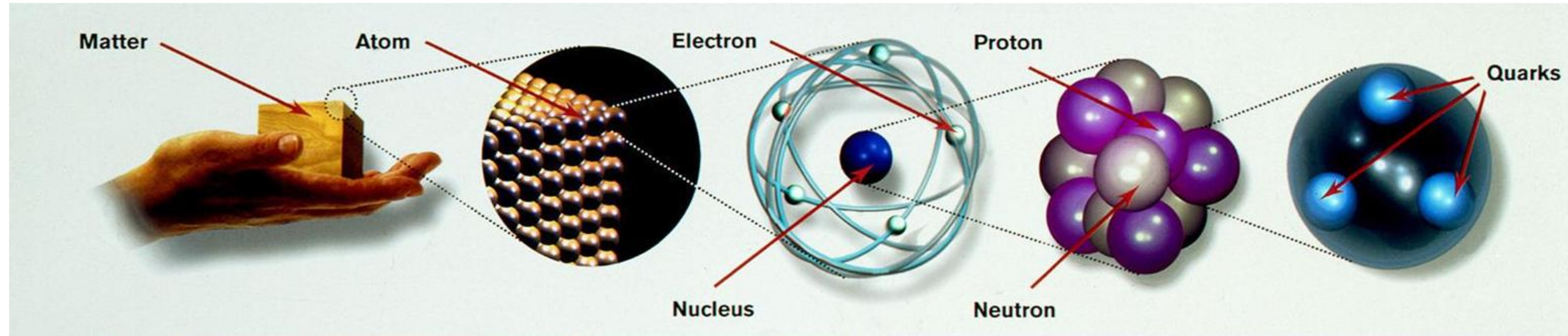
- Quark-gluon plasma
- Heavy-ion collisions
- Machine learning in HEP
- Inversion problem
- Decision Trees
- Results
- Summary

Quark-gluon plasma

Quark-gluon plasma

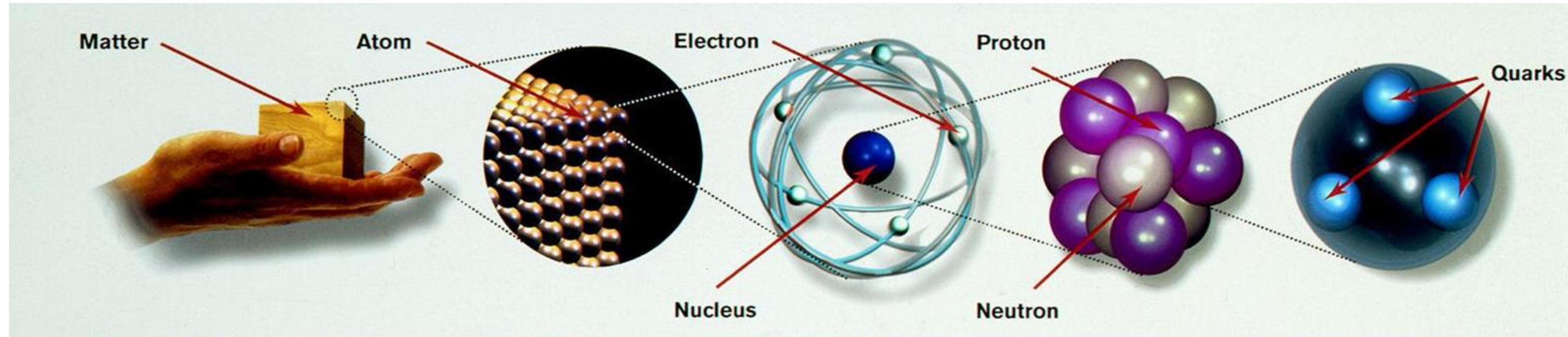


Quark-gluon plasma

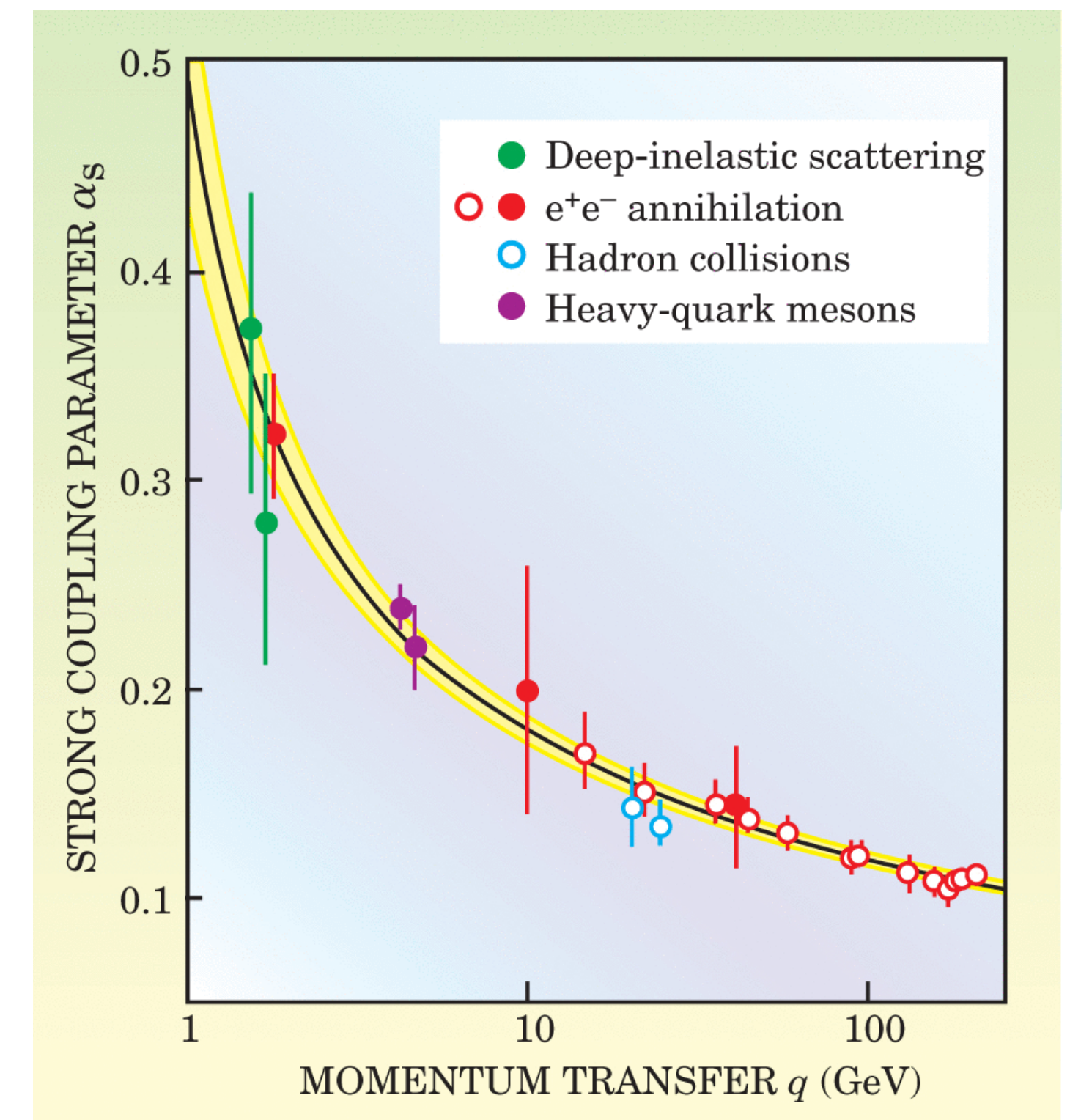


- Quarks: the fundamental bits of matter
- Gluons: carrier of strong force
- Theory of strong force: Quantum Chromodynamics (QCD)
- Color confinement: quarks and gluons can not be isolated
- Asymptotic freedom: weaker interaction at higher energy
- Heavy-ions: Pb, Au, Xe nucleus
- Quark-gluon plasma: Thermalised hot and dense state of deconfined partons

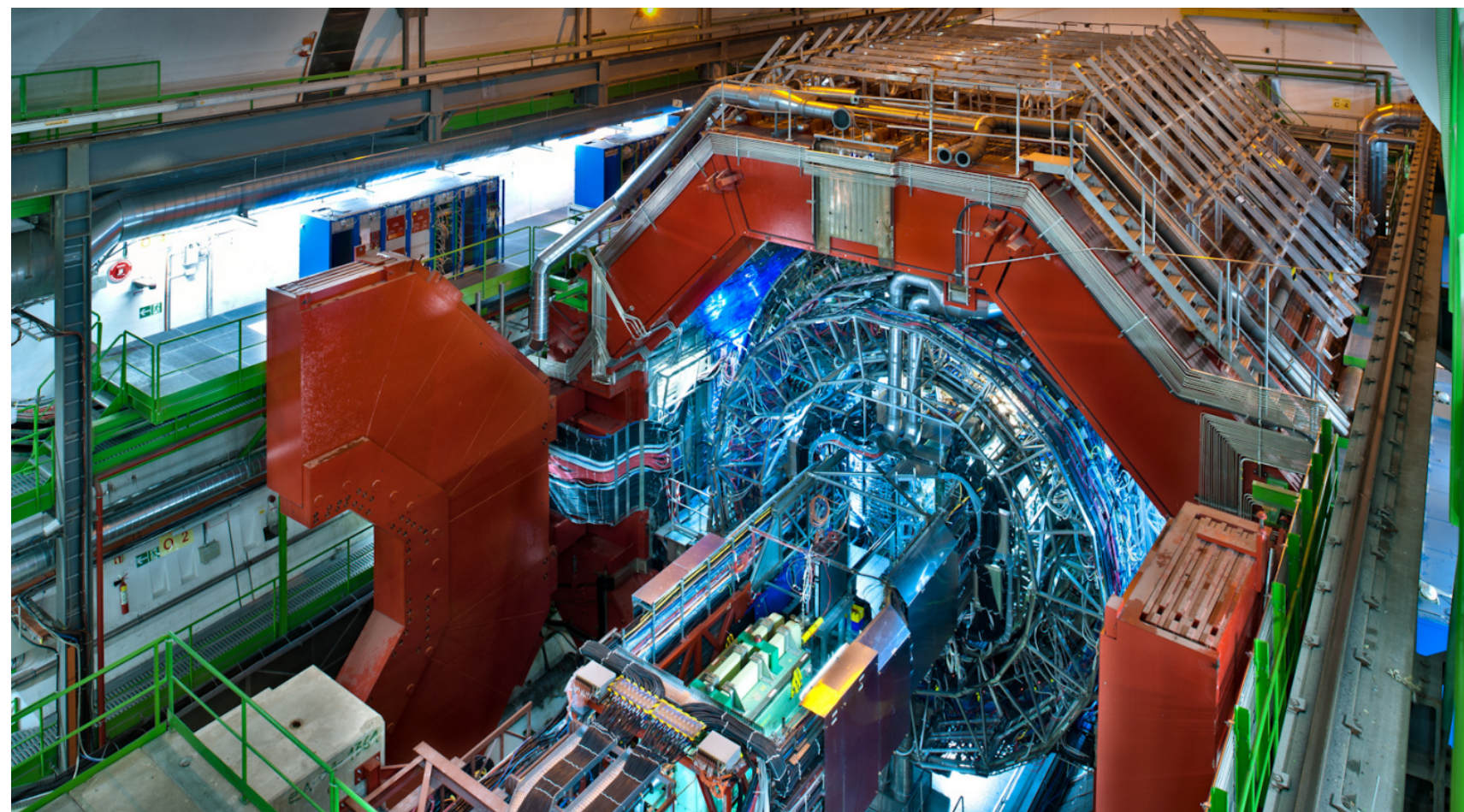
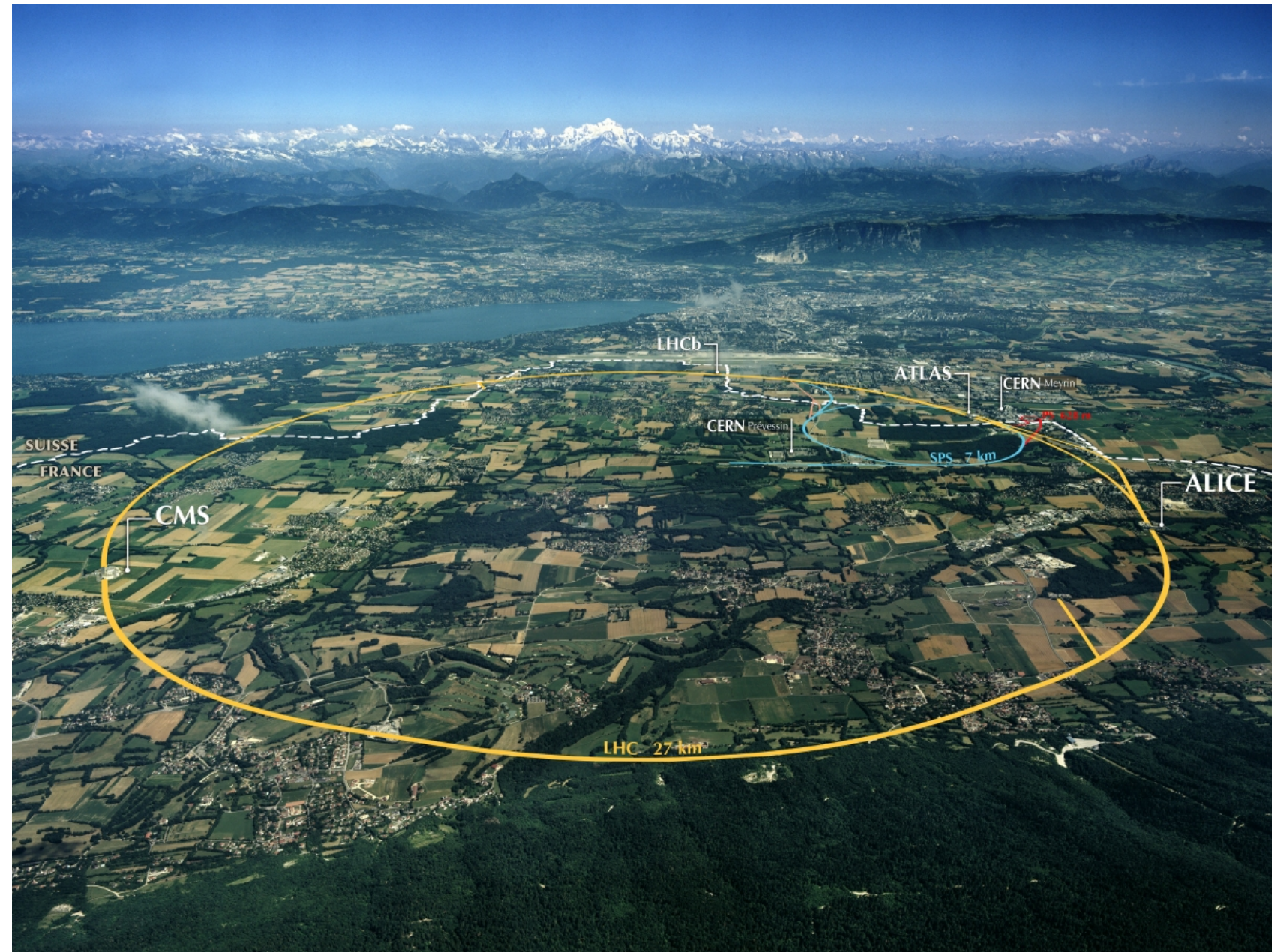
Quark-gluon plasma



- Quarks: the fundamental bits of matter
- Gluons: carrier of strong force
- Theory of strong force: Quantum Chromodynamics (QCD)
- Color confinement: quarks and gluons can not be isolated
- Asymptotic freedom: weaker interaction at higher energy
- Heavy-ions: Pb, Au, Xe nucleus
- Quark-gluon plasma: Thermalised hot and dense state of deconfined partons



Heavy-ion collisions

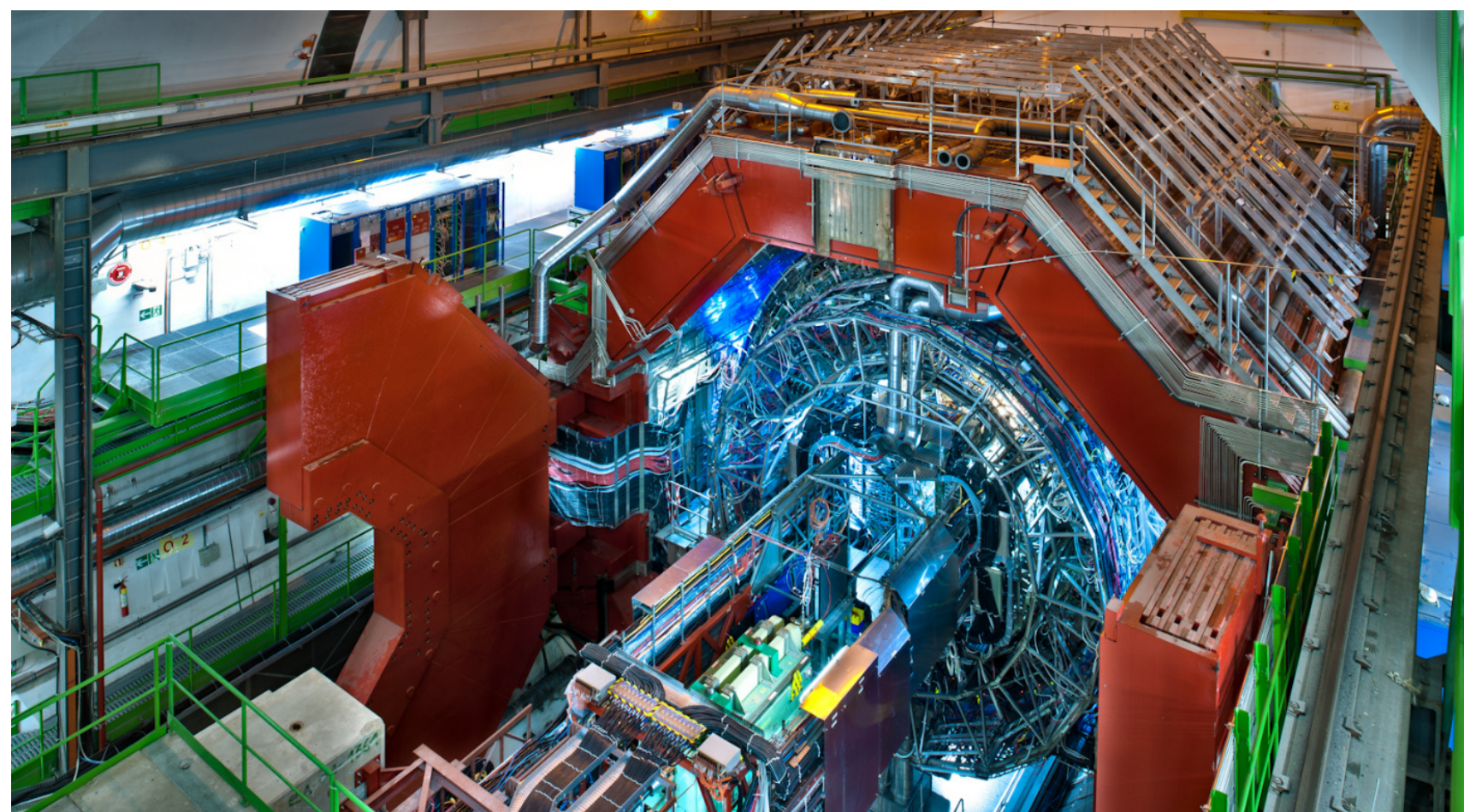
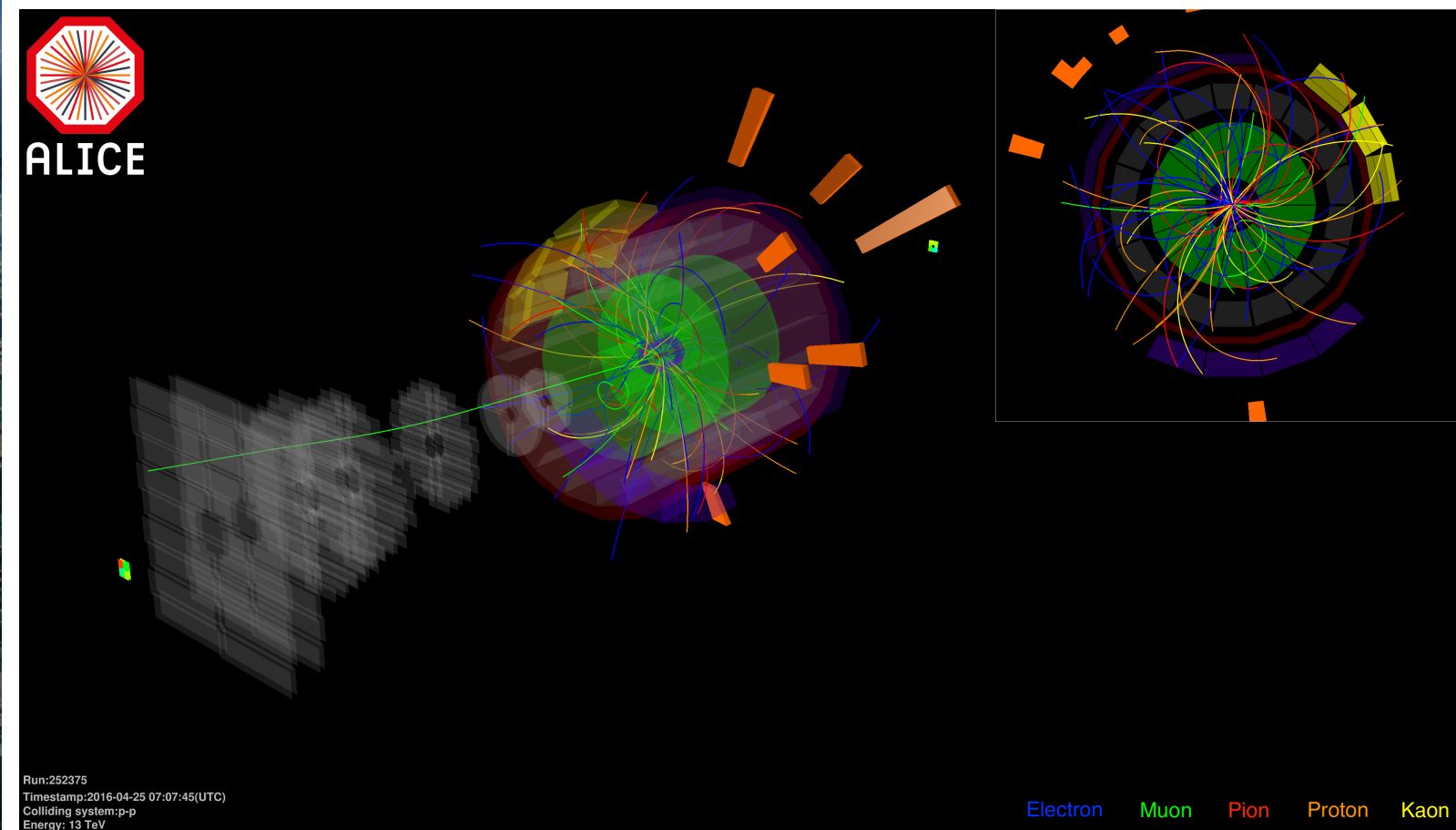


ALICE Detector, LHC, CERN

Heavy-ion collisions



proton-proton collisions, $\sqrt{s} = 13 \text{ TeV}$

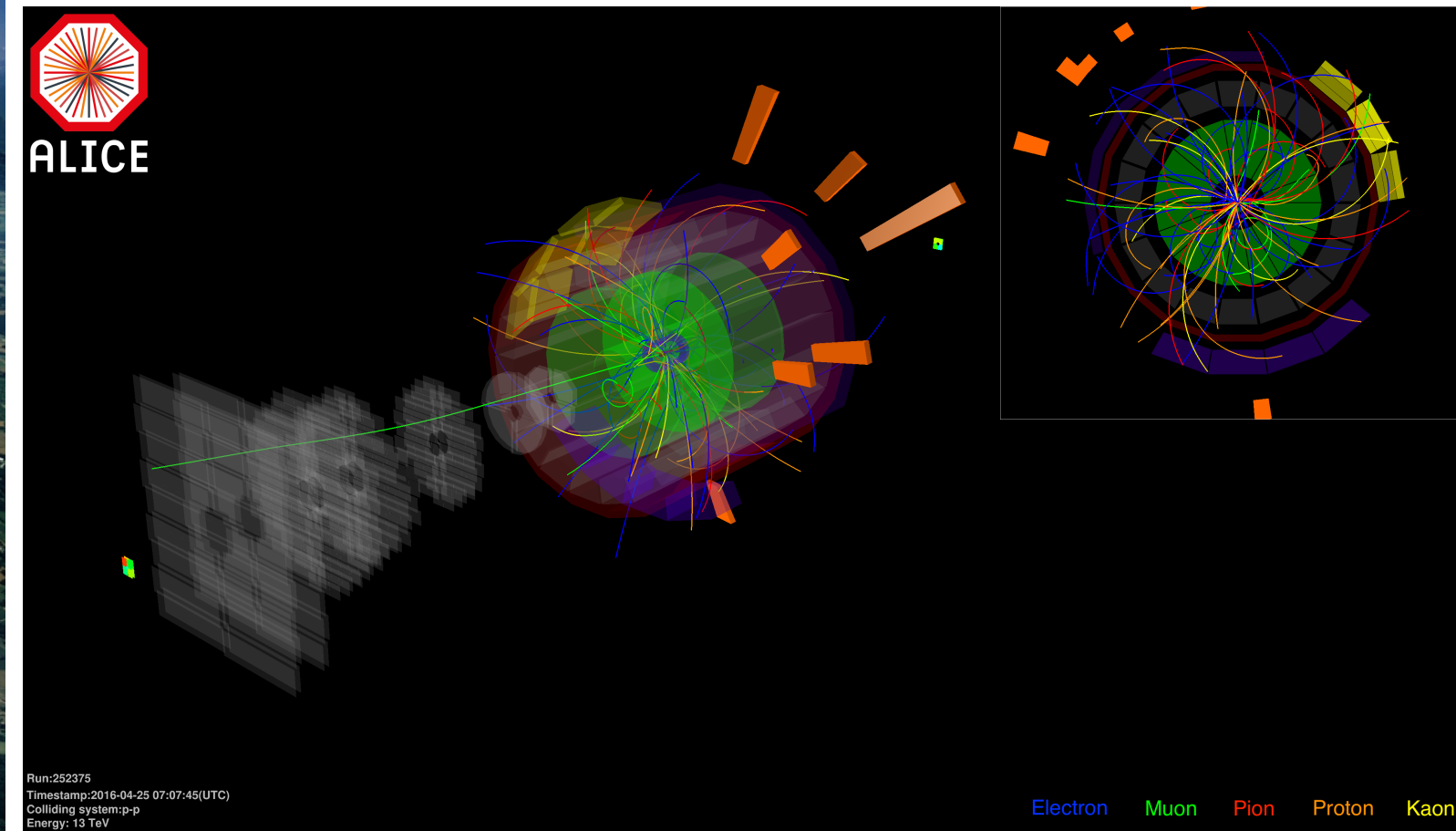


ALICE Detector, LHC, CERN

Heavy-ion collisions

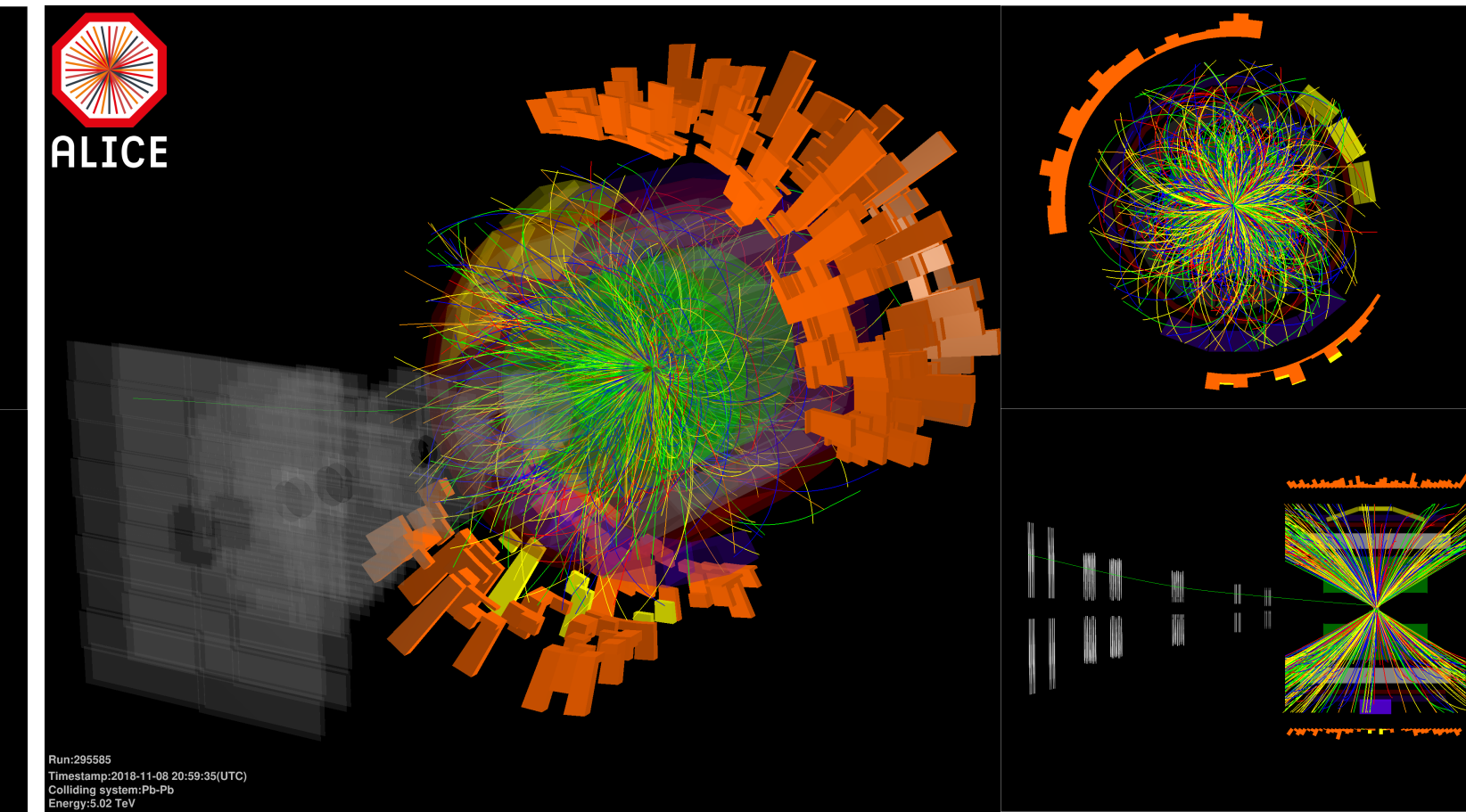


proton-proton collisions, $\sqrt{s} = 13 \text{ TeV}$

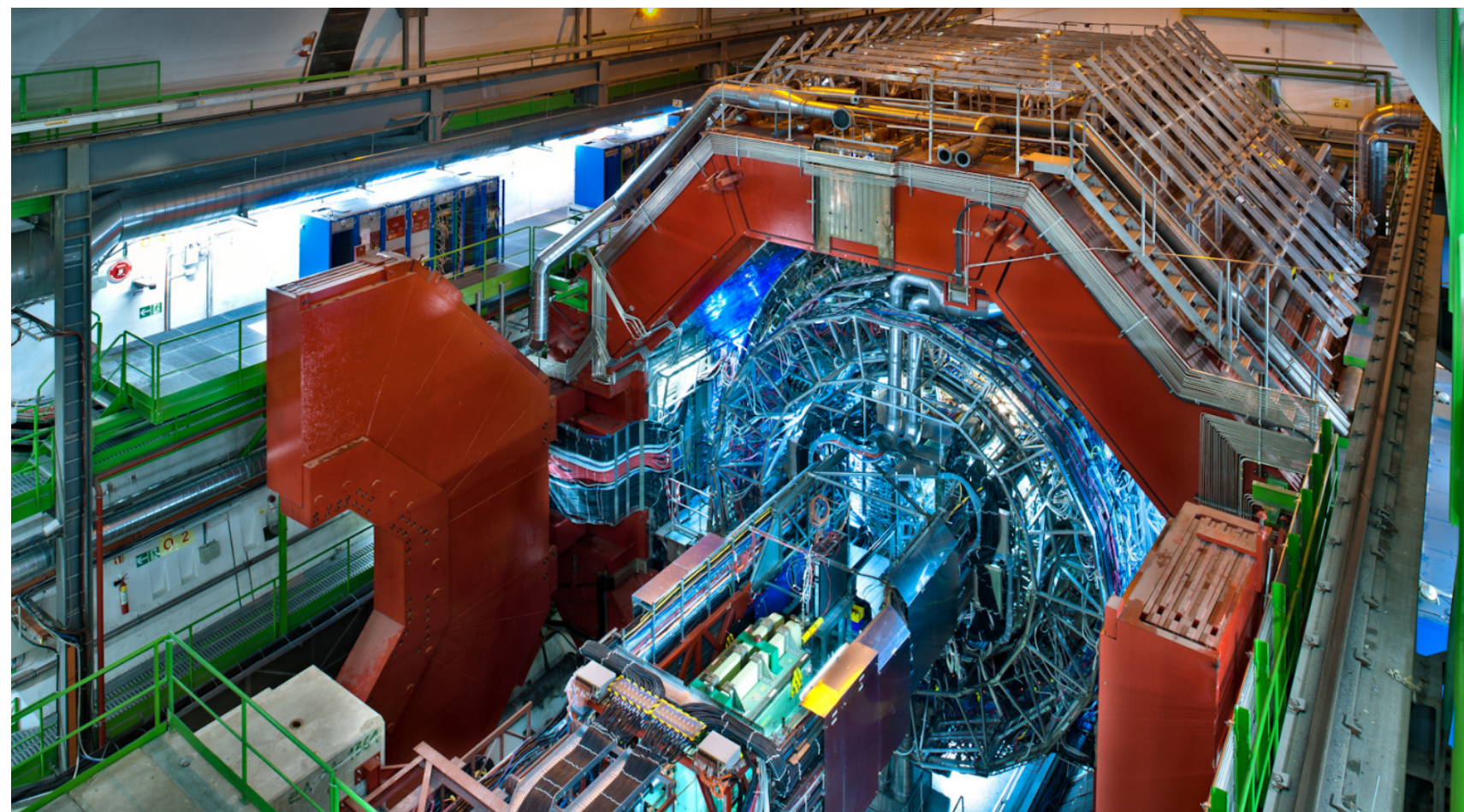


<https://cds.cern.ch/record/2149032>

Pb-Pb collisions, $\sqrt{s_{NN}} = 5.02 \text{ TeV}$



<https://cds.cern.ch/record/2108293>

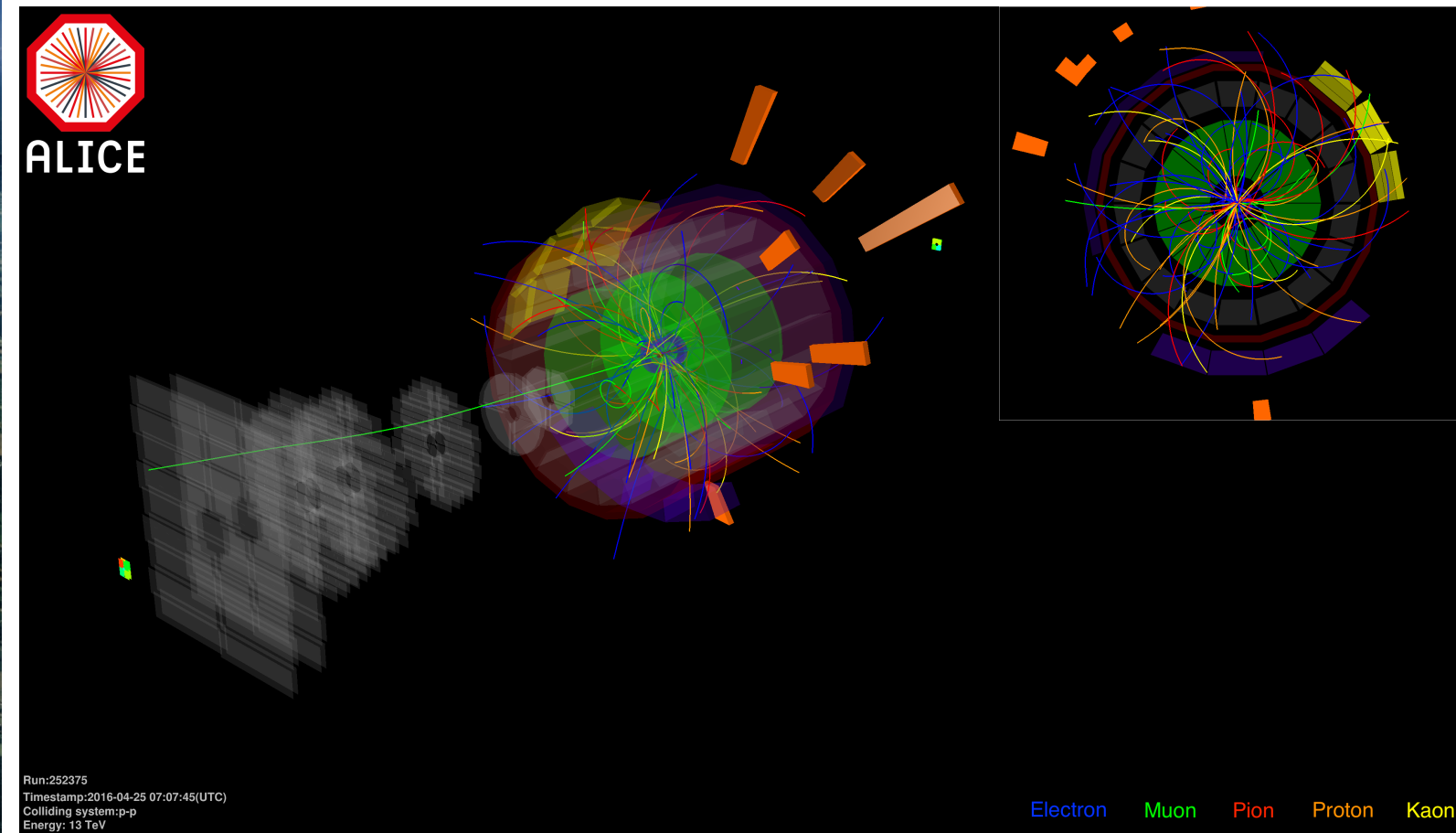


ALICE Detector, LHC, CERN

Heavy-ion collisions

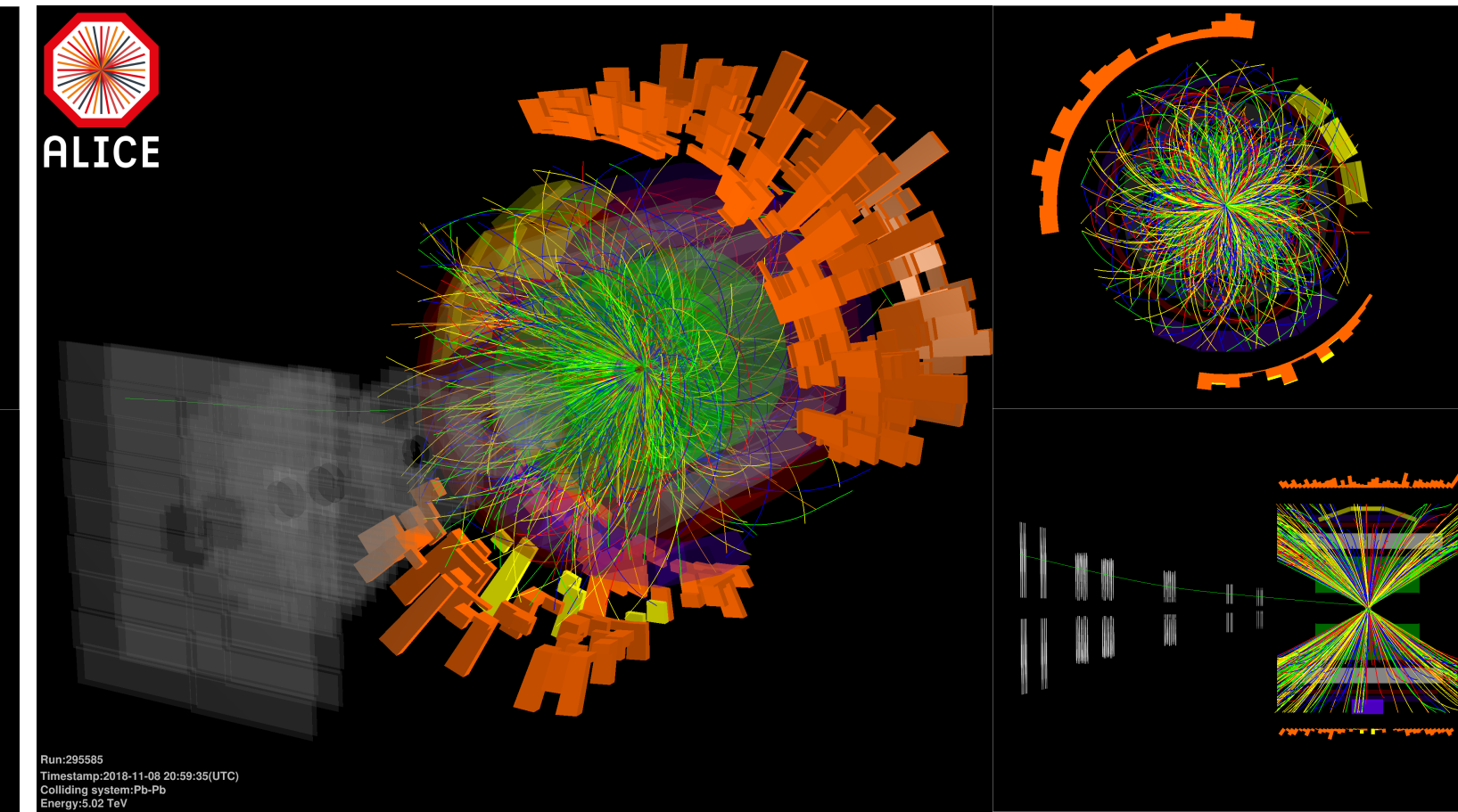


proton-proton collisions, $\sqrt{s} = 13 \text{ TeV}$

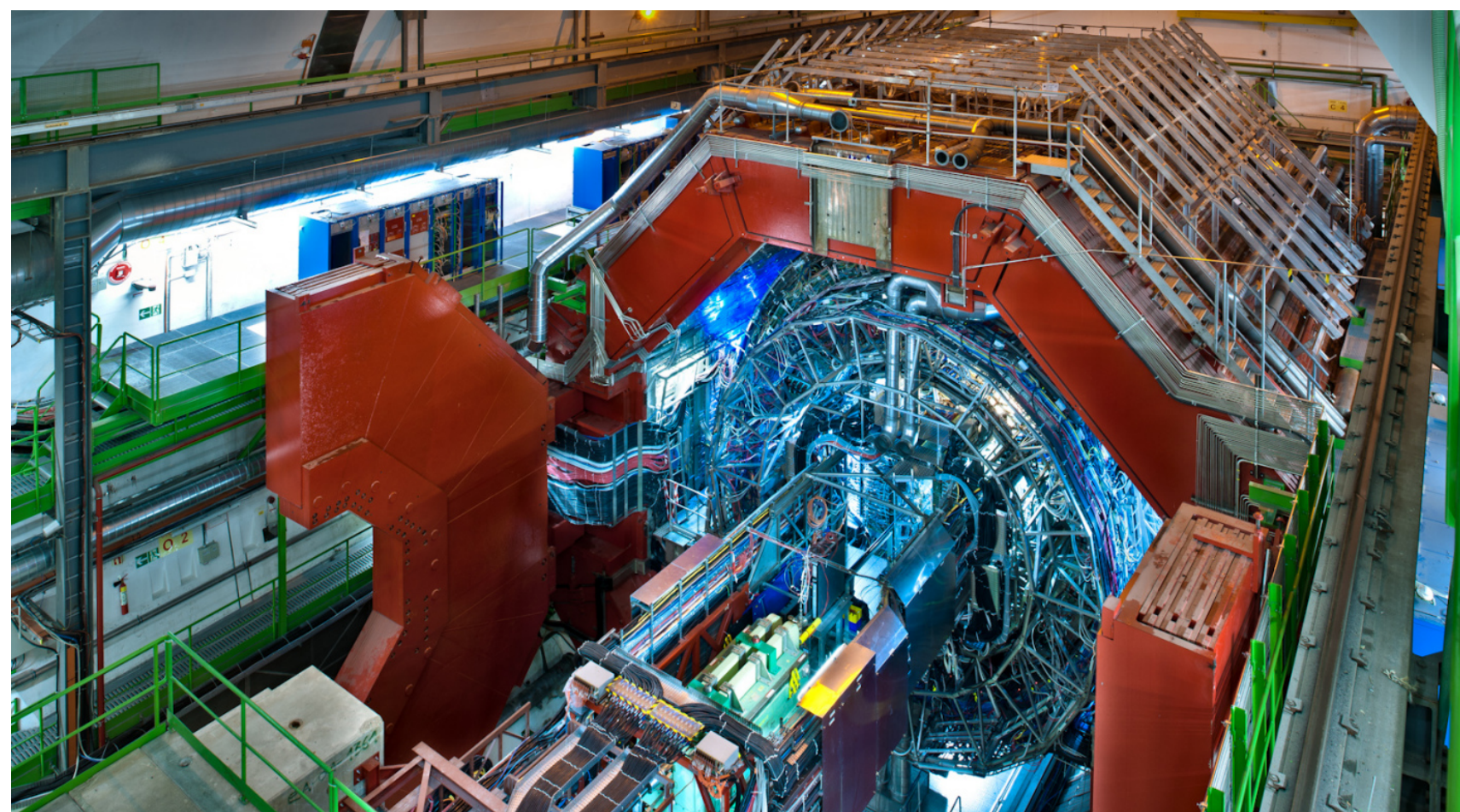


<https://cds.cern.ch/record/2149032>

Pb-Pb collisions, $\sqrt{s_{NN}} = 5.02 \text{ TeV}$

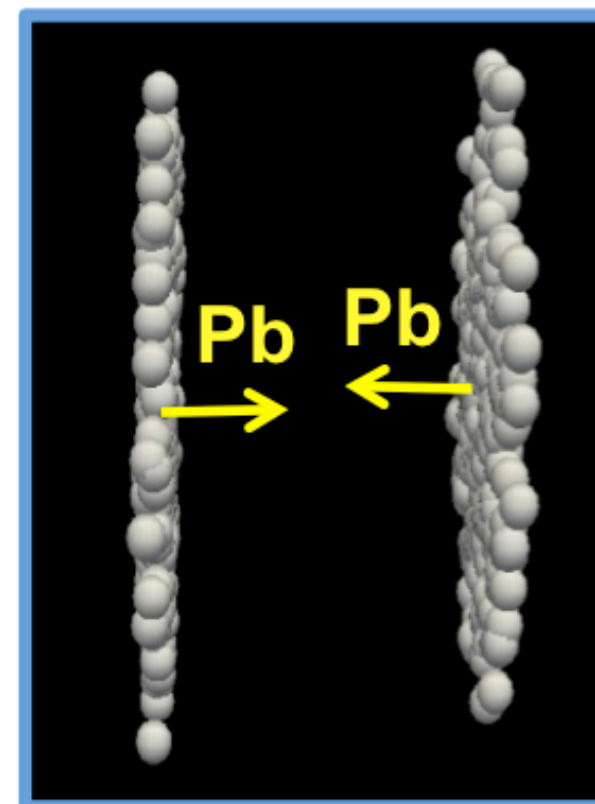


<https://cds.cern.ch/record/2108293>

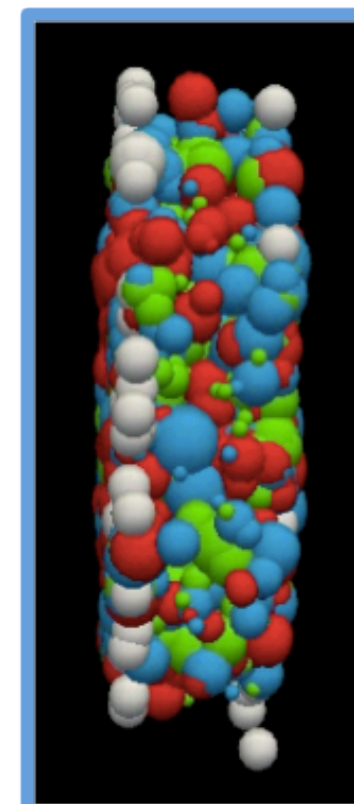


ALICE Detector, LHC, CERN

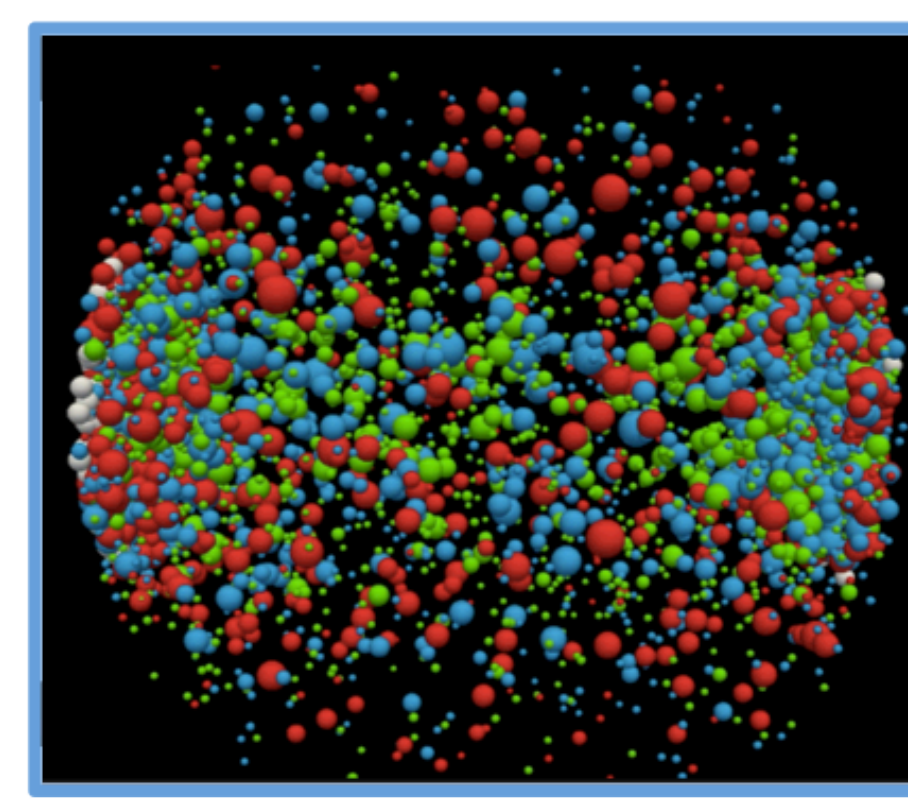
Pre-reaction



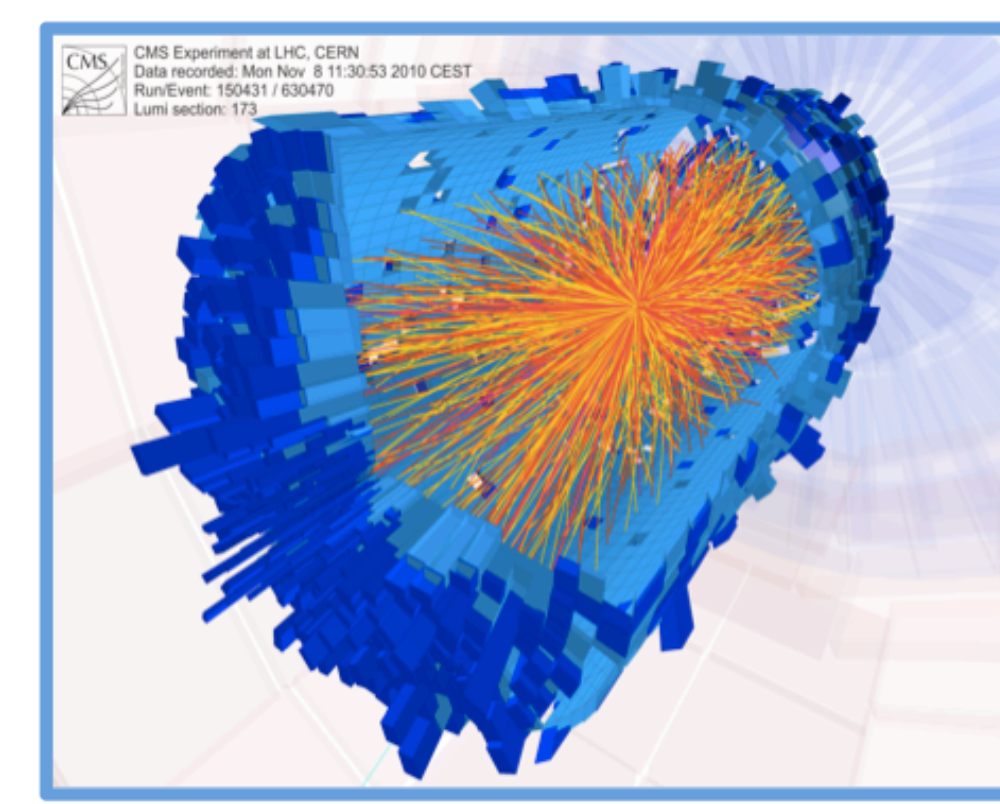
QGP



Hadronization



Detection



Machine learning in HEP

<https://iml-wg.github.io/HEPML-LivingReview/>

Machine learning in HEP

- Particle Identification
- Track reconstruction
- Triggering
- Fast Simulation
- Data Quality Monitoring
- Unfolding Techniques
- Signal and background classification
- Jet identification and tagging
- Beyond standard model physics
- **Heavy-ion physics and QGP phenomenology**

Machine learning in HEP

- Particle Identification
- Track reconstruction
- Triggering
- Fast Simulation
- Data Quality Monitoring
- Unfolding Techniques
- Signal and background classification
- Jet identification and tagging
- Beyond standard model physics
- **Heavy-ion physics and QGP phenomenology**



<https://root.cern/>

<https://root.cern/manual/tmva/>

[Scikit-learn: Machine Learning in Python](#), Pedregosa et al., JMLR 12, pp. 2825-2830, 2011

<https://keras.io/>

<https://www.tensorflow.org/>



*TensorFlow, the TensorFlow logo and any related marks are trademarks of Google Inc.



<https://iml-wg.github.io/HEPML-LivingReview/>

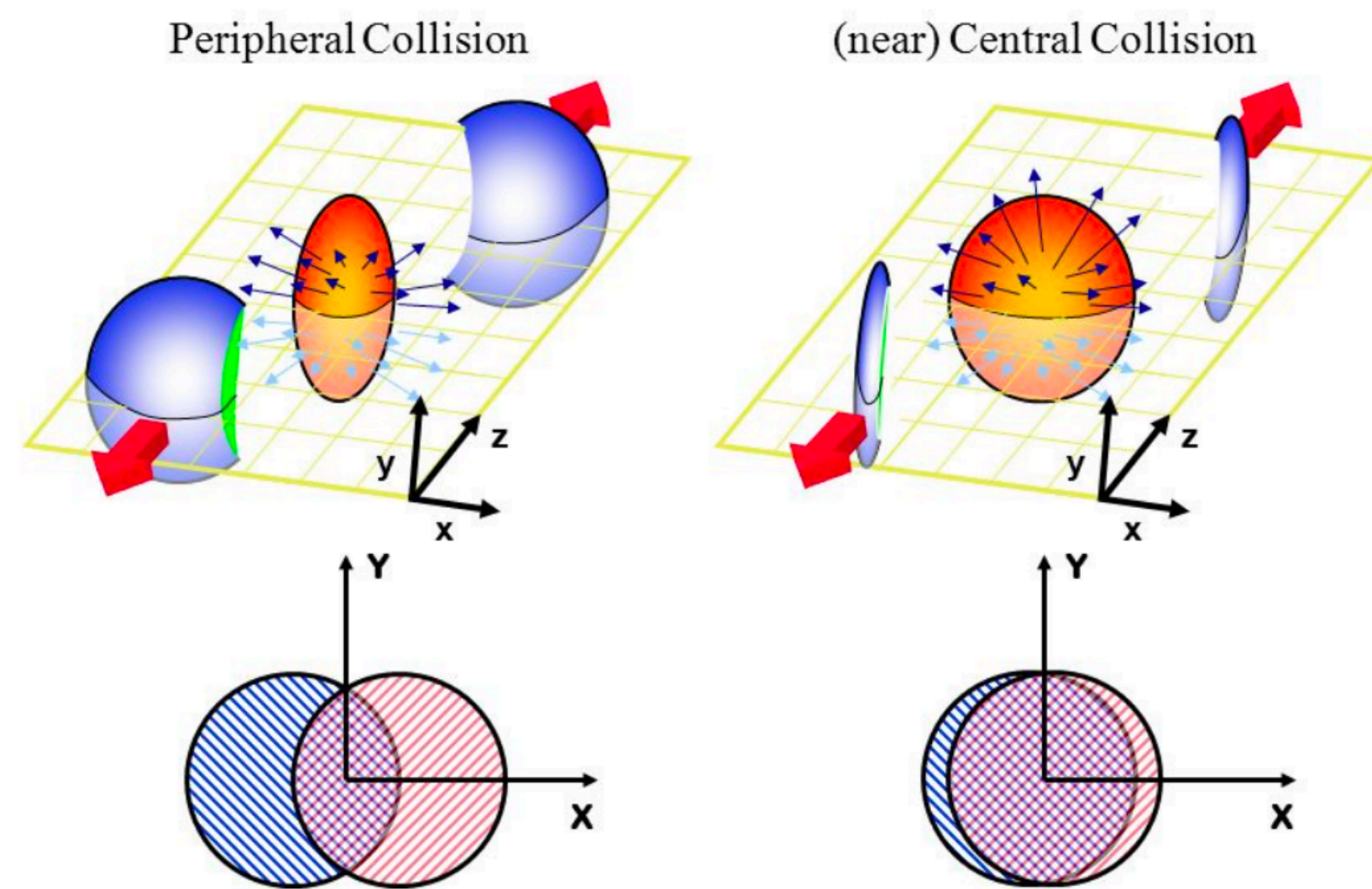
Impact parameter (b)

Impact parameter (b)

- Transverse distance between the centres of colliding nuclei
- Initial geometry affects the final state particle production
- Order of a few fermi (10^{-15} m)

Impact parameter (b)

- Transverse distance between the centres of colliding nuclei
- Initial geometry affects the final state particle production
- Order of a few fermi (10^{-15} m)

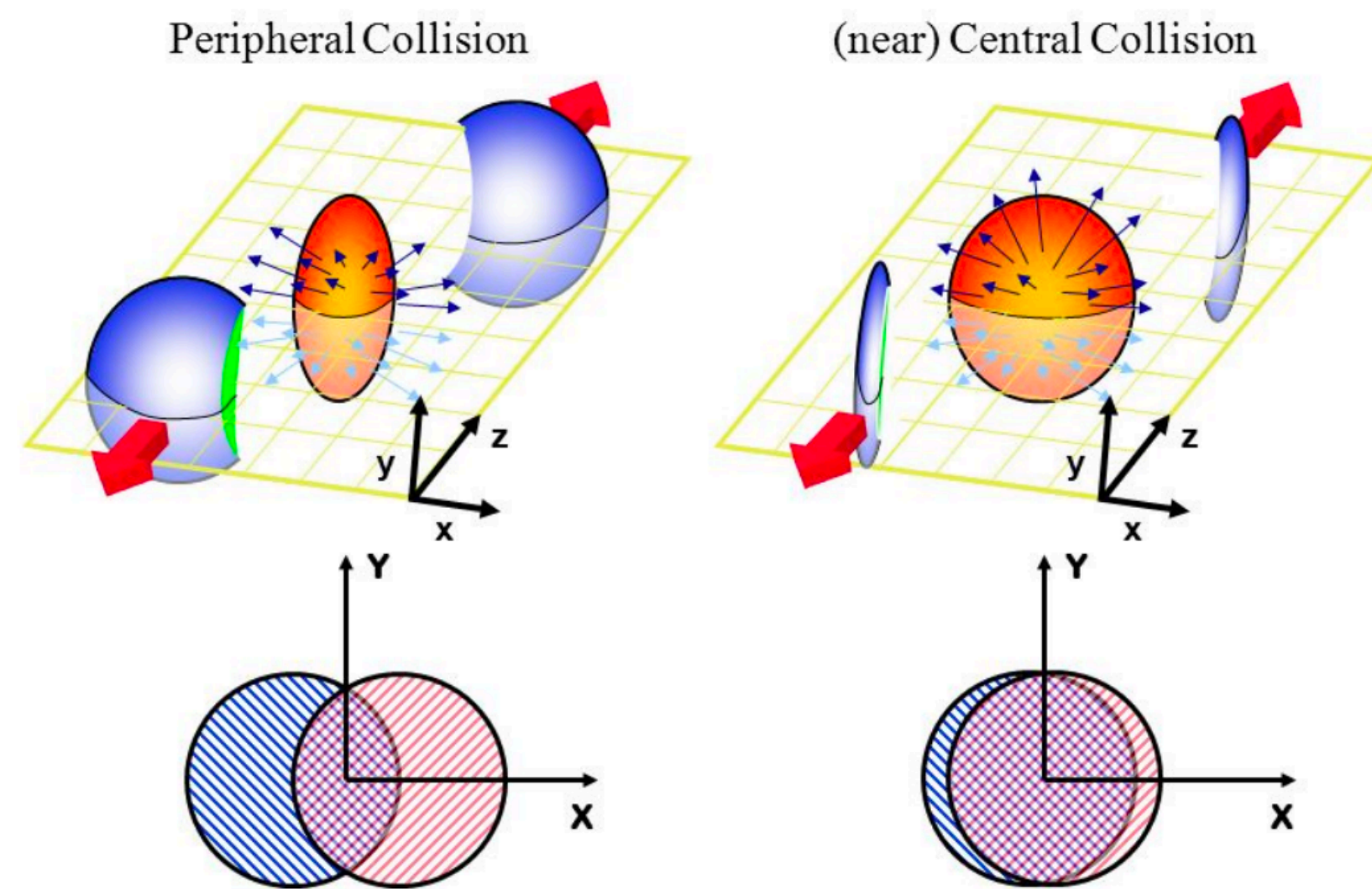


$$0 \leq b \leq 2R$$

Impact parameter (b)

Transverse Spherocity (S_0)

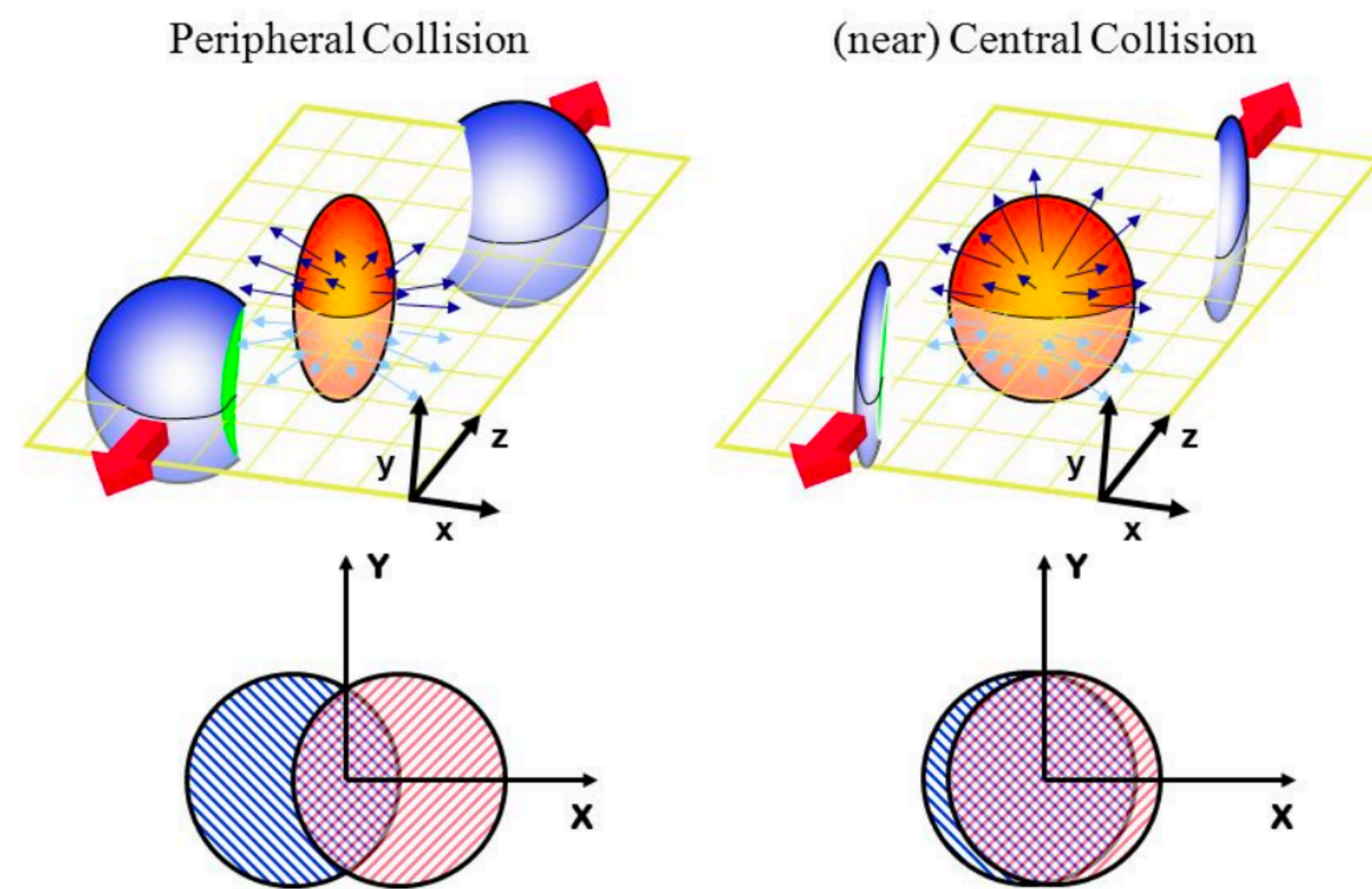
- Transverse distance between the centres of colliding nuclei
- Initial geometry affects the final state particle production
- Order of a few fermi (10^{-15} m)



$$0 \leq b \leq 2R$$

Impact parameter (b)

- Transverse distance between the centres of colliding nuclei
- Initial geometry affects the final state particle production
- Order of a few fermi (10^{-15} m)



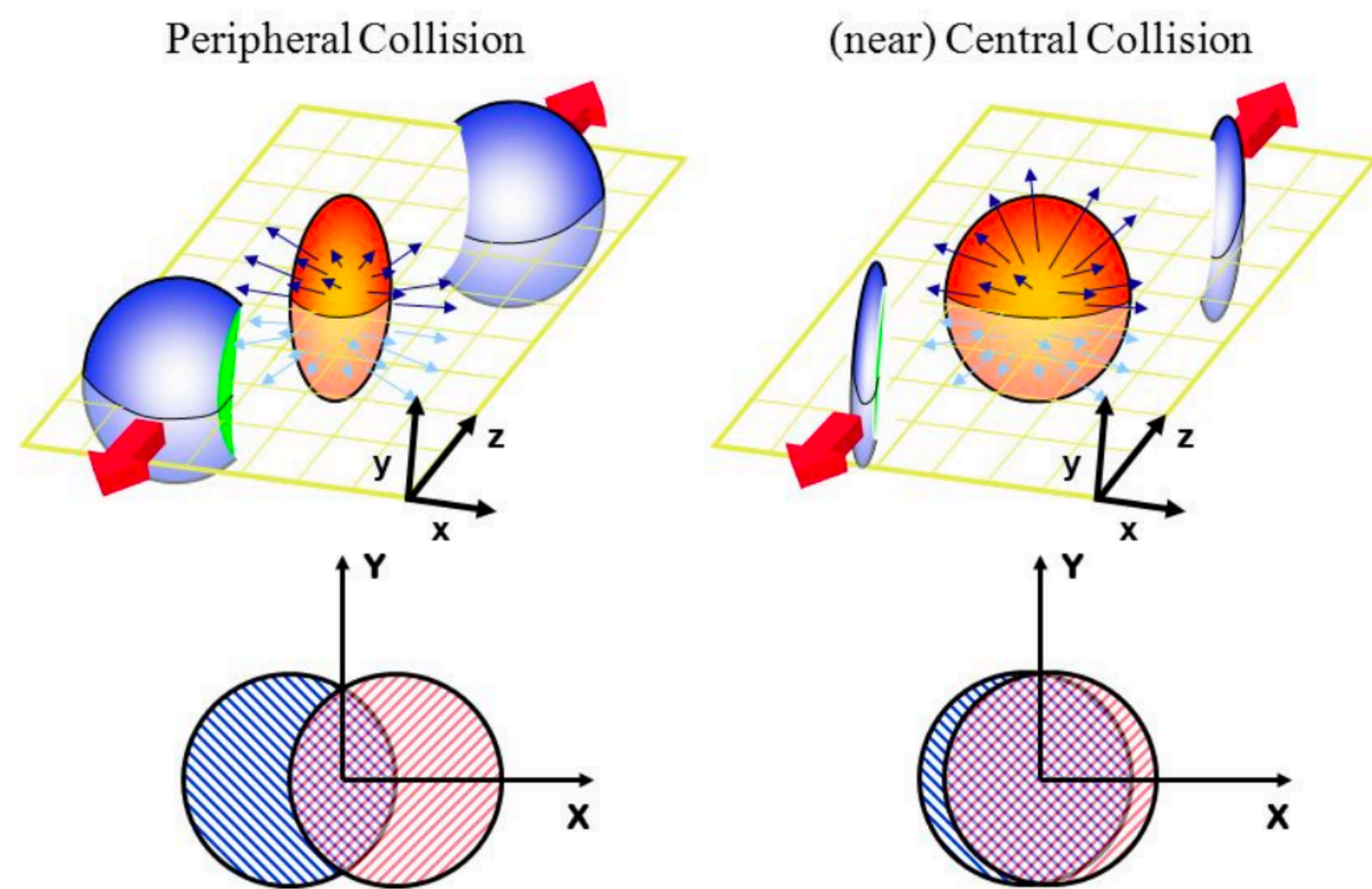
$$0 \leq b \leq 2R$$

Transverse Spherocity (S_0)

- In pp collisions,
 1. **Jetty**: Back-to-back structure, indication of hard-QCD
 2. **Isotropic**: soft-QCD process
- Dominance of isotropic events in high multiplicity pp collisions

Impact parameter (b)

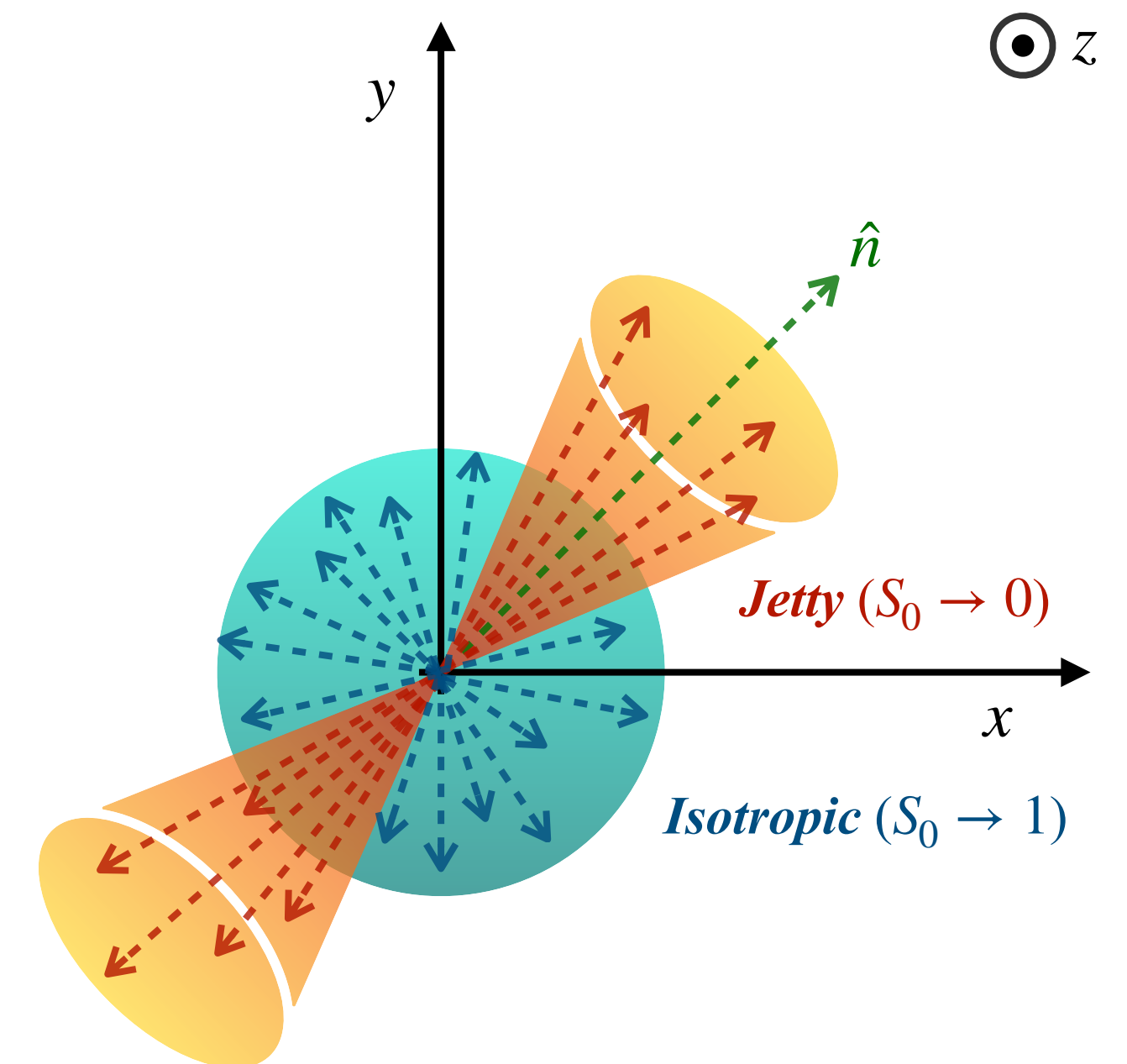
- Transverse distance between the centres of colliding nuclei
- Initial geometry affects the final state particle production
- Order of a few fermi (10^{-15} m)



$$0 \leq b \leq 2R$$

Transverse Spherocity (S_0)

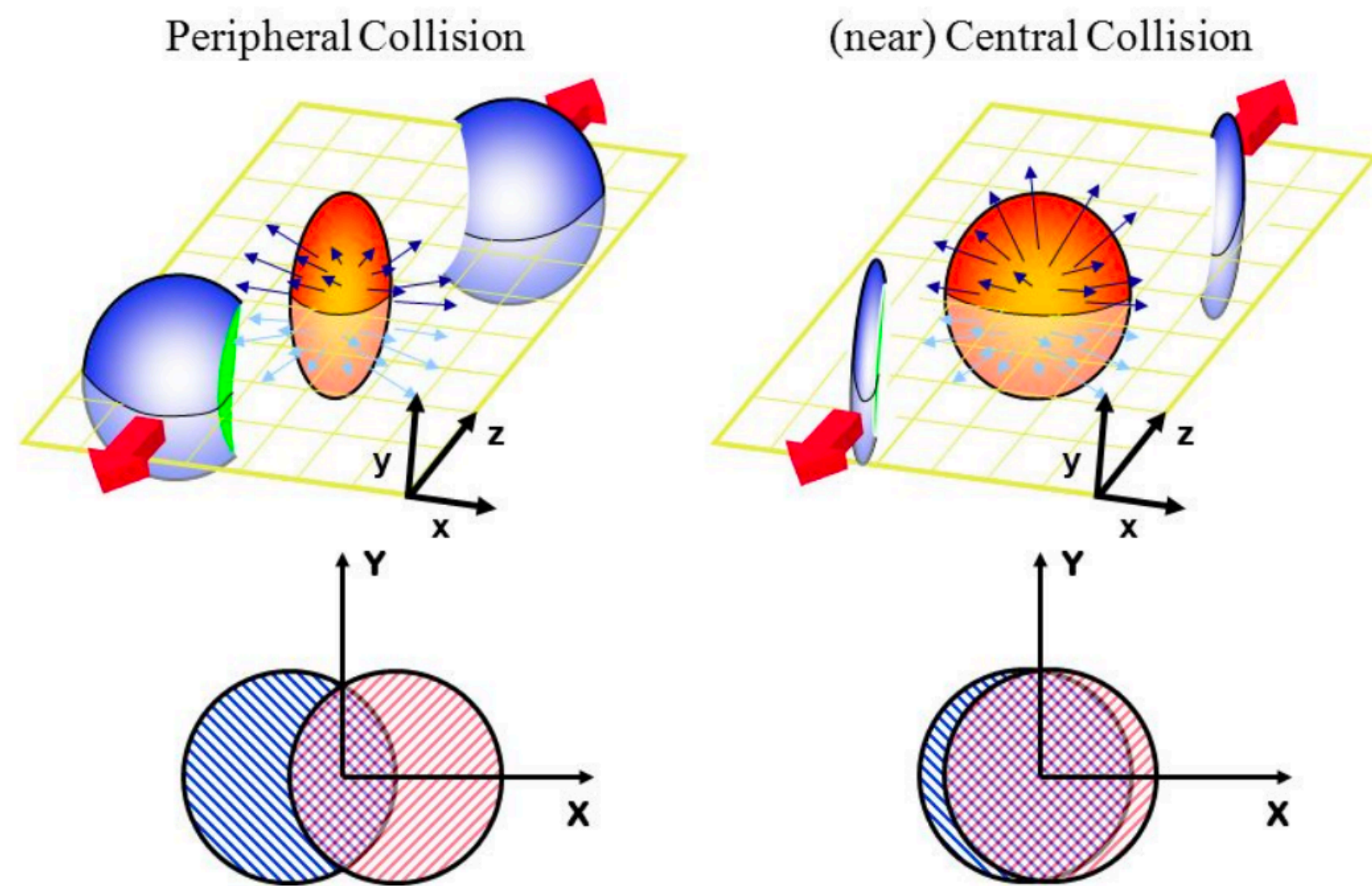
- In pp collisions,
 1. **Jetty**: Back-to-back structure, indication of hard-QCD
 2. **Isotropic**: soft-QCD process
- Dominance of isotropic events in high multiplicity pp collisions



Schematic picture showing possible **jetty** and **isotropic** event formations in the transverse plane

Impact parameter (b)

- Transverse distance between the centres of colliding nuclei
- Initial geometry affects the final state particle production
- Order of a few fermi (10^{-15} m)



$$0 \leq b \leq 2R$$

Transverse Spherocity (S_0)

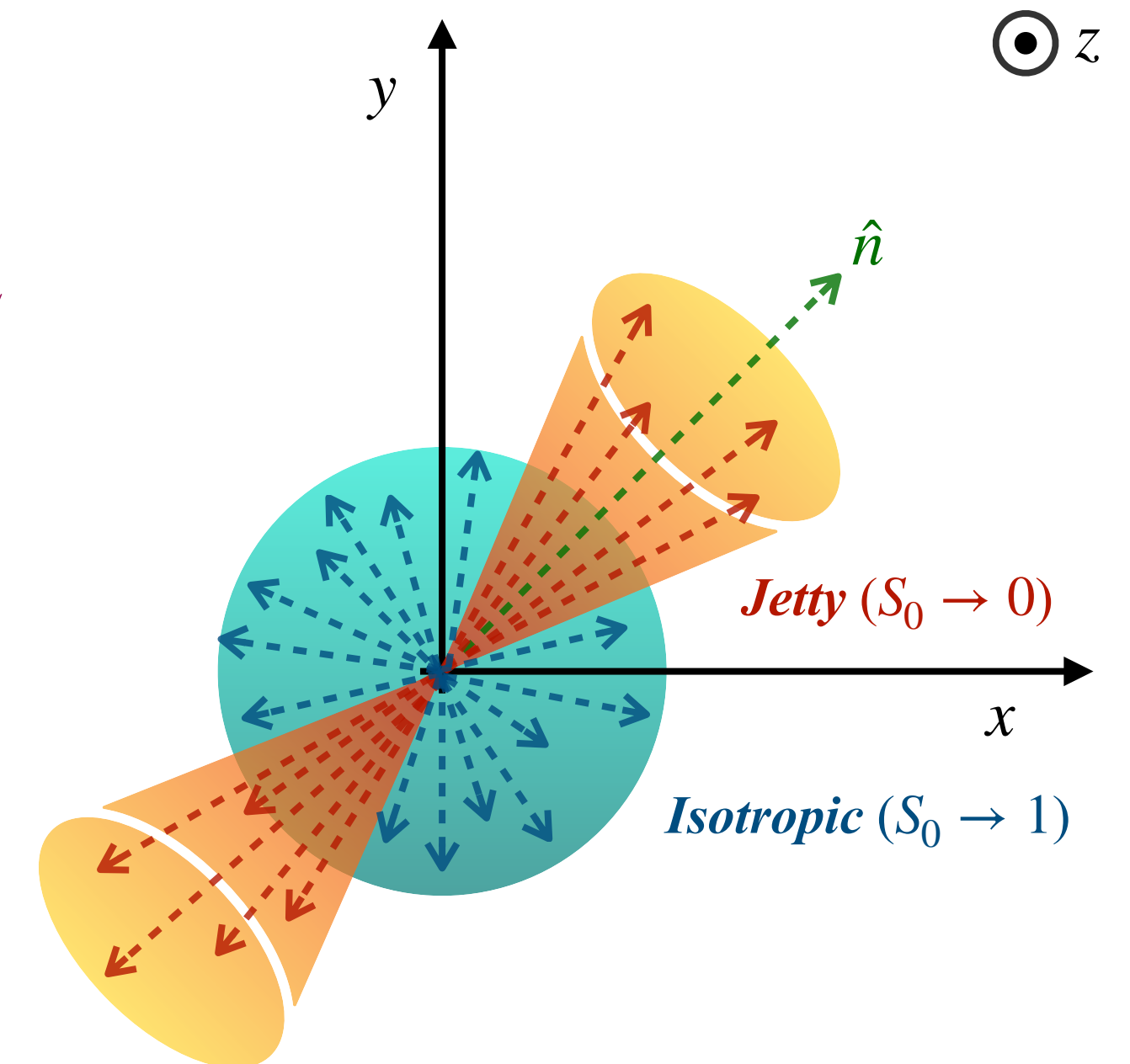
- In pp collisions,
 1. **Jetty**: Back-to-back structure, indication of hard-QCD
 2. **Isotropic**: soft-QCD process
- Dominance of isotropic events in high multiplicity pp collisions

$$S_0 = \frac{\pi^2}{4} \times \min_{\hat{n} = (n_x, n_y, 0)} \left(\frac{\sum_i |\vec{p}_{T_i} \times \hat{n}|}{\sum_i p_{T_i}} \right)^2$$

$$p_T = \sqrt{p_x^2 + p_y^2}$$

A. Khuntia et al., J. Phys. G48, 035102 (2021)

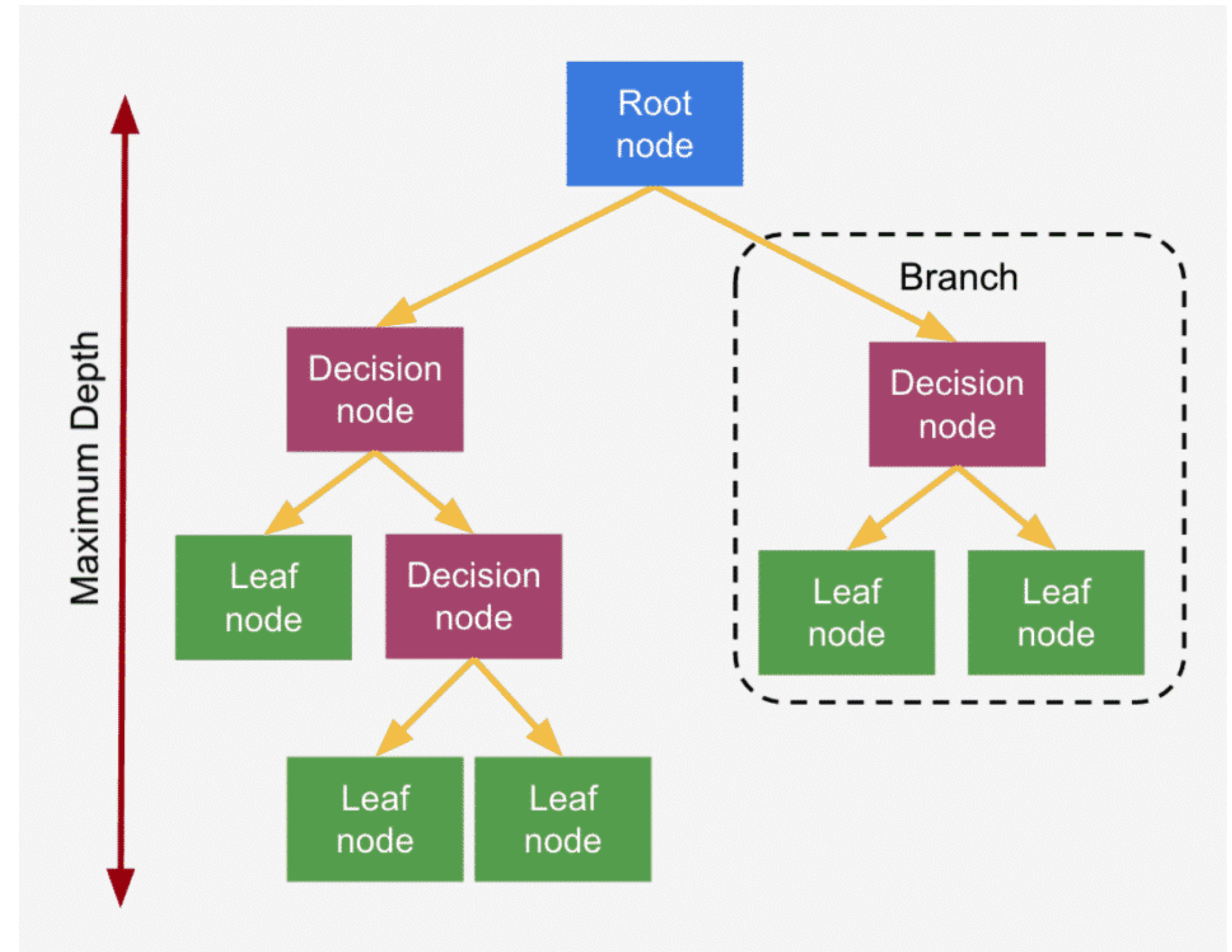
S. Prasad, N. Mallick, D. Behera, R. Sahoo, and S. Tripathy, Sci.Rep. 12, 3917 (2022)



Schematic picture showing possible **jetty** and **isotropic** event formations in the transverse plane

Boosted Decision Trees

- Trees are structures that takes recursive decisions
- Built in a top-down approach
- Root node: The starting point
 - Internal nodes: further decision points
 - Leaf nodes: End points (target class or values)
- Criteria of splitting:
 - Classification: Minimise the node impurity
 - Regression: Minimise the MSE, MAE
- Splitting continues till a preset (max_depth)
- Boosting: Building an additive forward staged model by combining the outcomes of all previous ones
- Boosting compensates the shortcomings
- Shortcomings are identified as the gradient



Input observables and correlation

- Pearsons correlation coefficient:

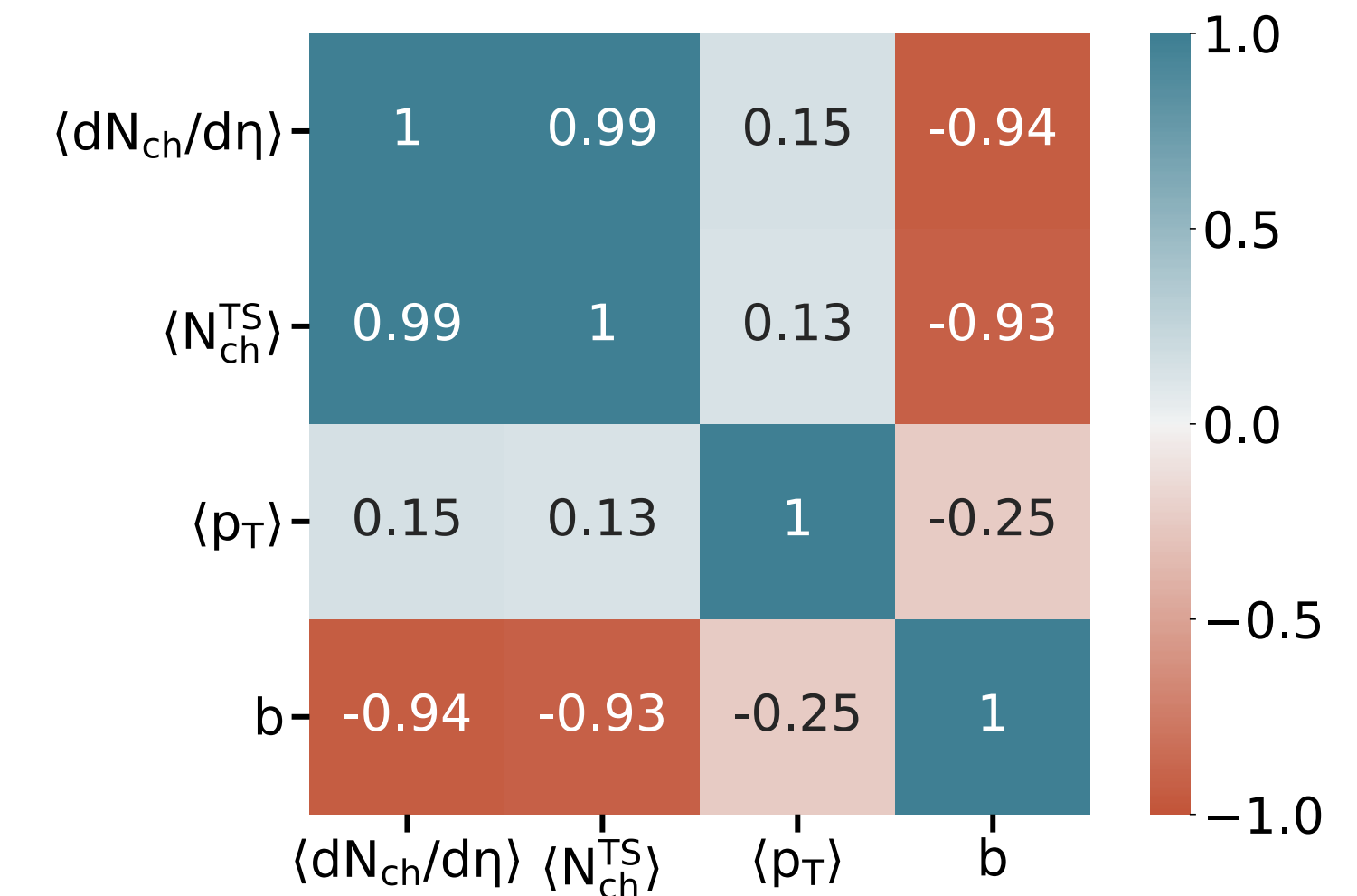
$$\rho = \frac{\text{cov}(x, y)}{\sigma_x \sigma_y}$$

Input variables: $\langle dN_{ch}/d\eta \rangle$, $\langle N_{ch}^{TS} \rangle$ and $\langle p_T \rangle$

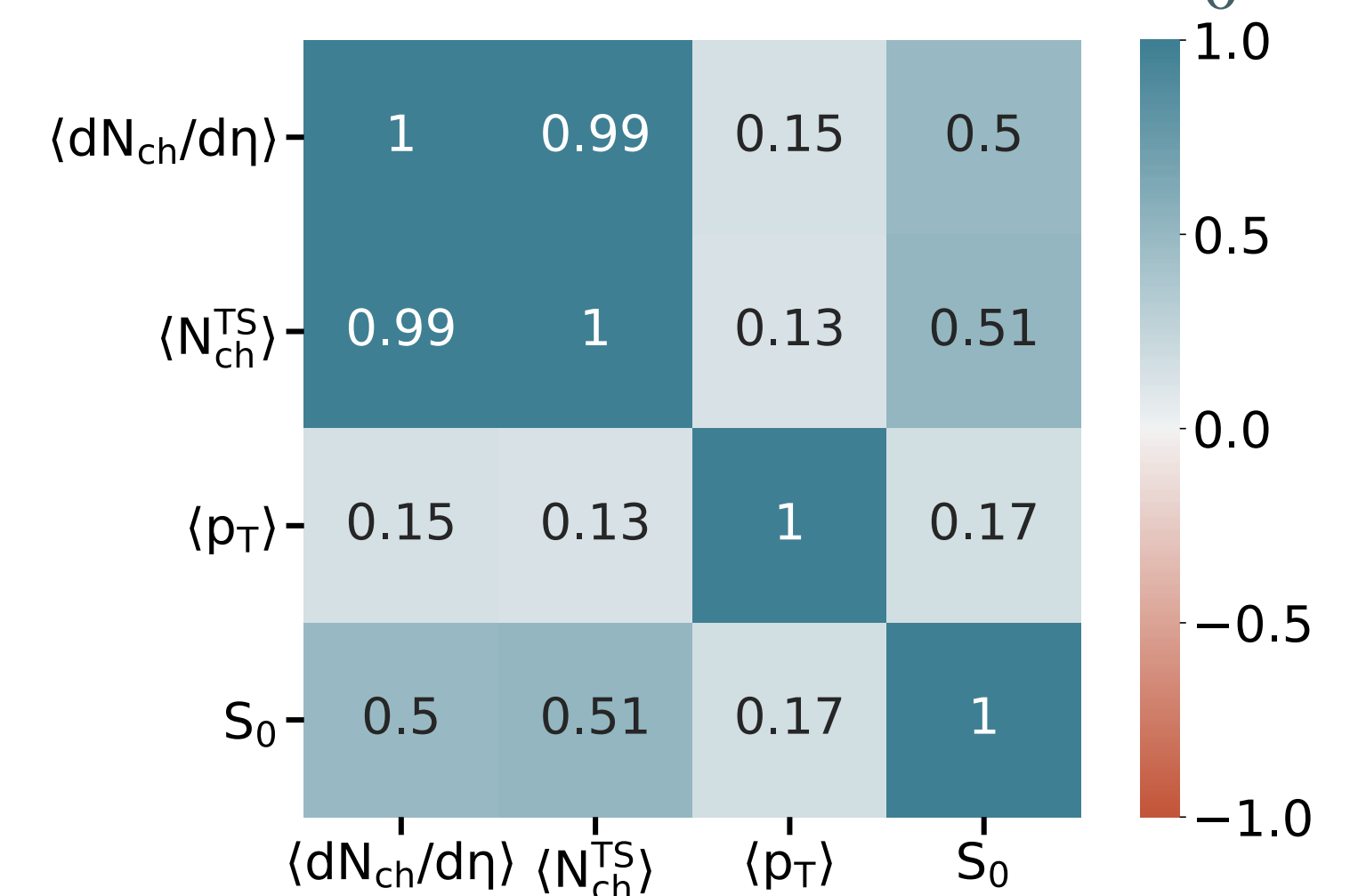
Output variable: b and S_0

- Good correlation is seen among chosen input and output variables
- The algorithm tries to understand the correlation and exploit the features to arrive on a conclusion (a number)

Impact parameter (b)



Transverse Sphericity (S_0)



Parameters and training

- Loss Function: Least Square Loss
- Small learning rate = 0.1
- Number of trees = 100
- Training Size: 60,000 events (min. bias)

$$\text{Least Square loss : } l(y_i, F(\mathbf{x}_i)) = \frac{1}{2}(y_i - F(\mathbf{x}_i))^2$$

$$\Delta S_0 = \frac{1}{N_{\text{events}}} \sum_{n=1}^{N_{\text{events}}} |S_{0_n}^{\text{true}} - S_{0_n}^{\text{pred.}}|$$

Size of training data	2K	10K	20K	40K	50K	60K
Δb [fm] (Impact parameter)	0.71	0.62	0.58	0.53	0.52	0.52
ΔS_0 (Sphericity)	0.079	0.068	0.062	0.058	0.056	0.055

N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#).

J. H. Friedman, *Ann. Stat.* 29, 1189 (2001).

L. Breiman, J. H. Friedman, R. A. Olshen, and C. J. Stone, *Classification and Regression Trees* (Wadsworth & Brooks/ Cole Advanced Books & Software, Monterey, CA, 1984), p. 358, <https://doi.org/10.1002/cyto.990080516>.

Parameters and training

- Loss Function: Least Square Loss
- Small learning rate = 0.1
- Number of trees = 100
- Training Size: 60,000 events (min. bias)

$$\text{Least Square loss : } l(y_i, F(\mathbf{x}_i)) = \frac{1}{2}(y_i - F(\mathbf{x}_i))^2$$

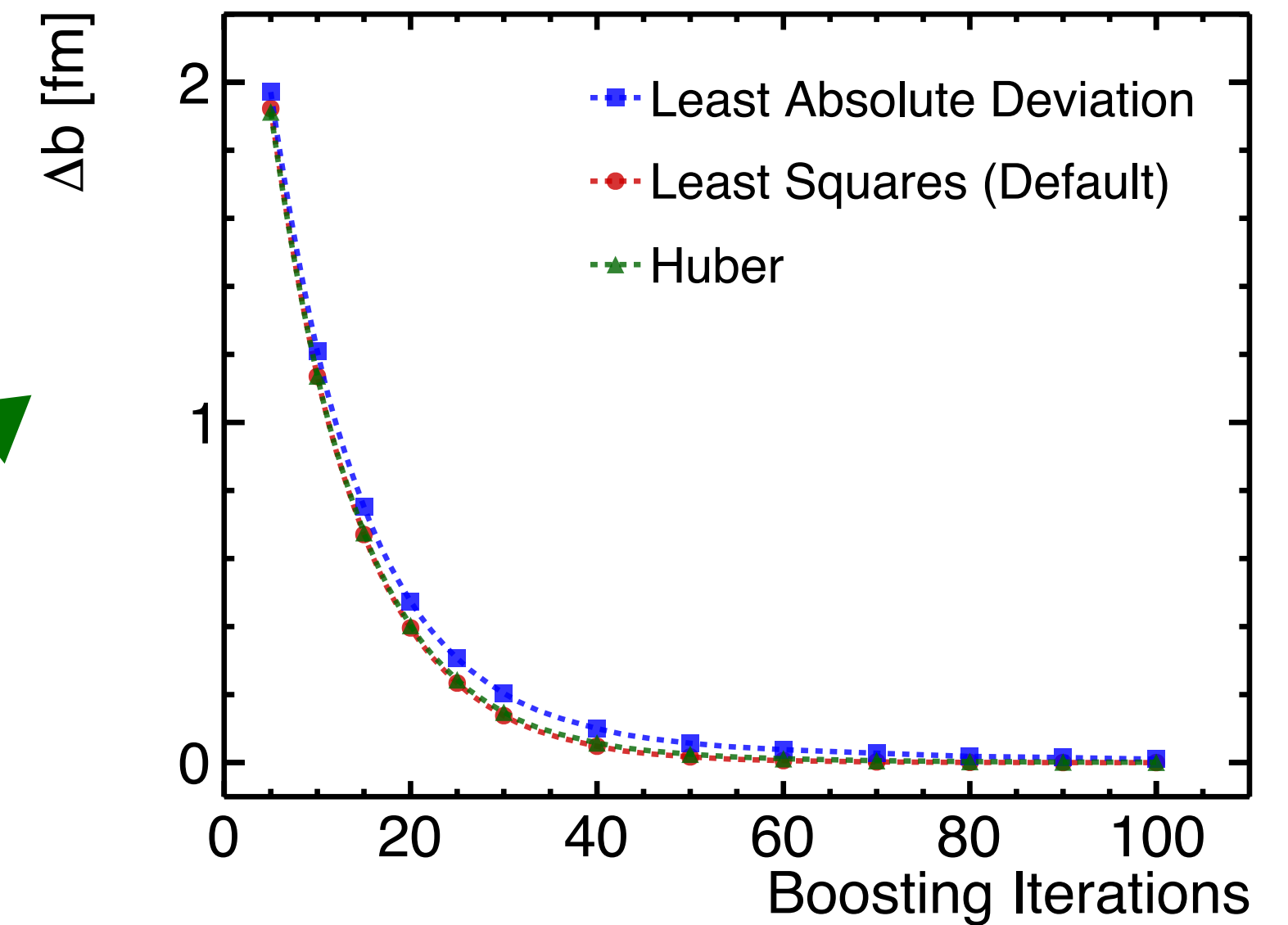
$$\Delta S_0 = \frac{1}{N_{\text{events}}} \sum_{n=1}^{N_{\text{events}}} |S_{0_n}^{\text{true}} - S_{0_n}^{\text{pred.}}|$$

Size of training data	2K	10K	20K	40K	50K	60K
Δb [fm] (Impact parameter)	0.71	0.62	0.58	0.53	0.52	0.52
ΔS_0 (Sphericity)	0.079	0.068	0.062	0.058	0.056	0.055

N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, *Phys. Rev. D*103, 094031 (2021).

J. H. Friedman, *Ann. Stat.* 29, 1189 (2001).

L. Breiman, J. H. Friedman, R. A. Olshen, and C. J. Stone, *Classification and Regression Trees* (Wadsworth & Brooks/ Cole Advanced Books & Software, Monterey, CA, 1984), p. 358, <https://doi.org/10.1002/cyto.990080516>.



Parameters and training

- Loss Function: Least Square Loss
- Small learning rate = 0.1
- Number of trees = 100
- Training Size: 60,000 events (min. bias)

$$\text{Least Square loss : } l(y_i, F(\mathbf{x}_i)) = \frac{1}{2}(y_i - F(\mathbf{x}_i))^2$$

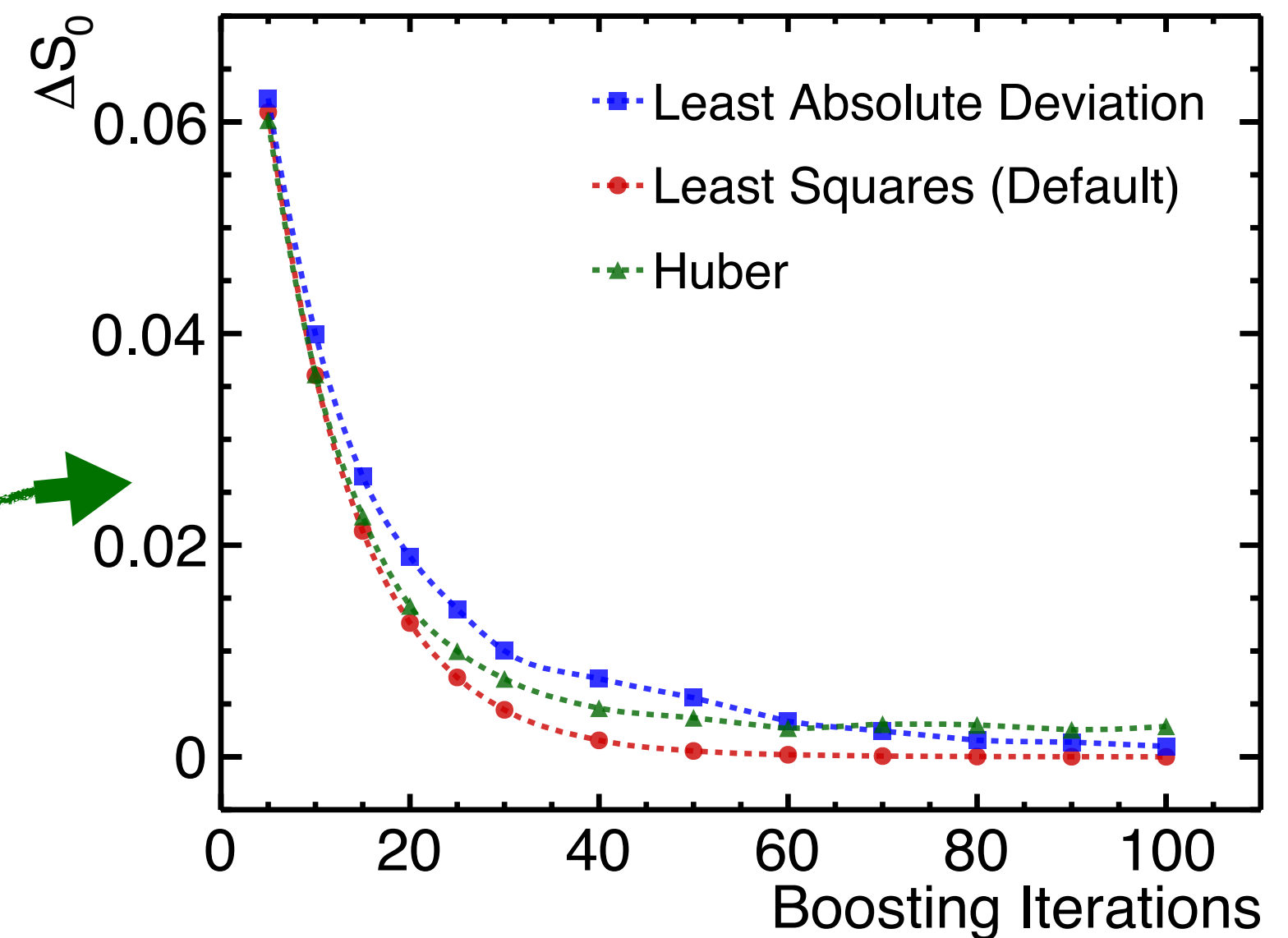
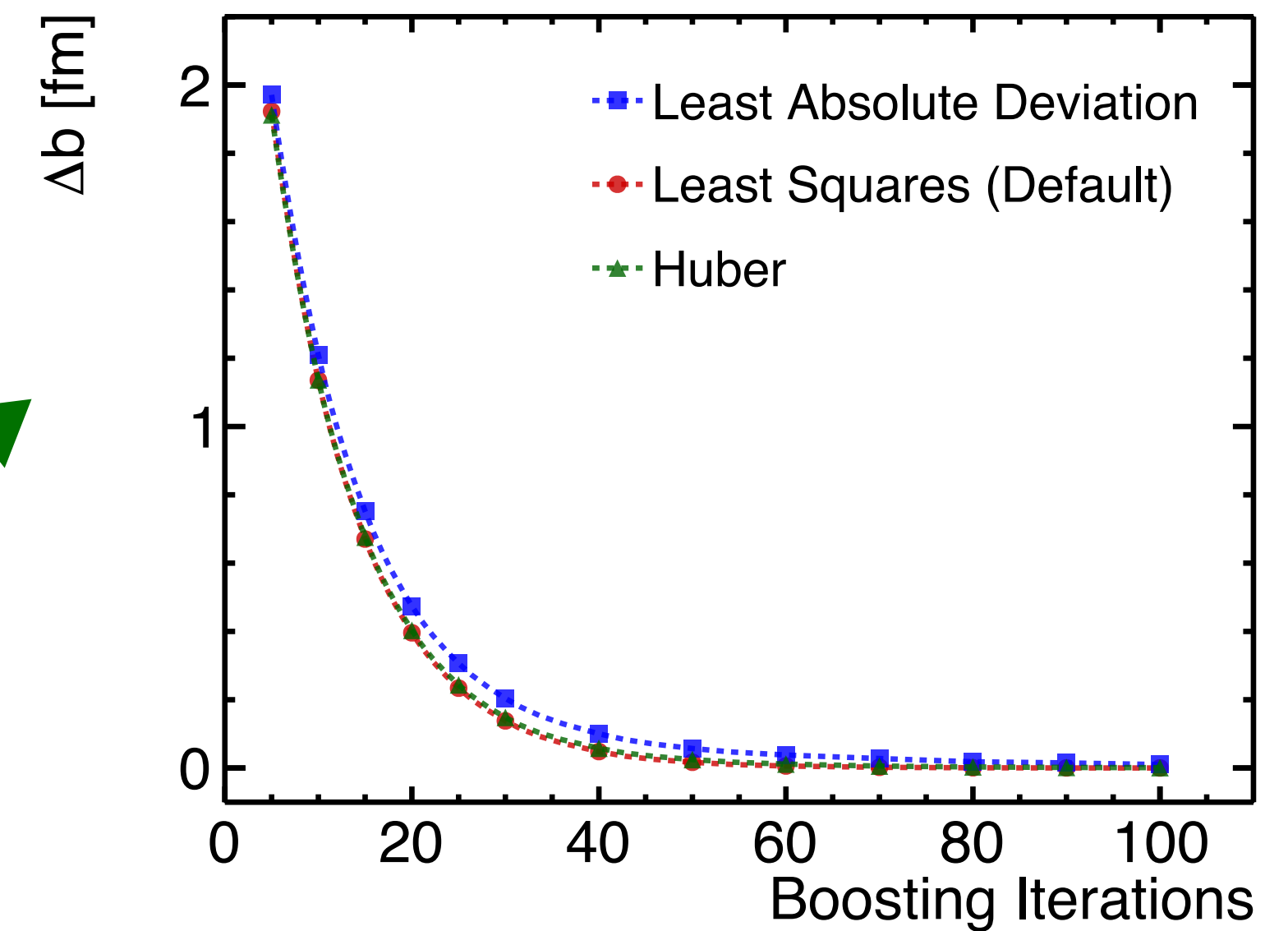
$$\Delta S_0 = \frac{1}{N_{\text{events}}} \sum_{n=1}^{N_{\text{events}}} |S_{0_n}^{\text{true}} - S_{0_n}^{\text{pred.}}|$$

Size of training data	2K	10K	20K	40K	50K	60K
Δb [fm] (Impact parameter)	0.71	0.62	0.58	0.53	0.52	0.52
ΔS_0 (Sphericity)	0.079	0.068	0.062	0.058	0.056	0.055

N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, *Phys. Rev. D*103, 094031 (2021).

J. H. Friedman, *Ann. Stat.* 29, 1189 (2001).

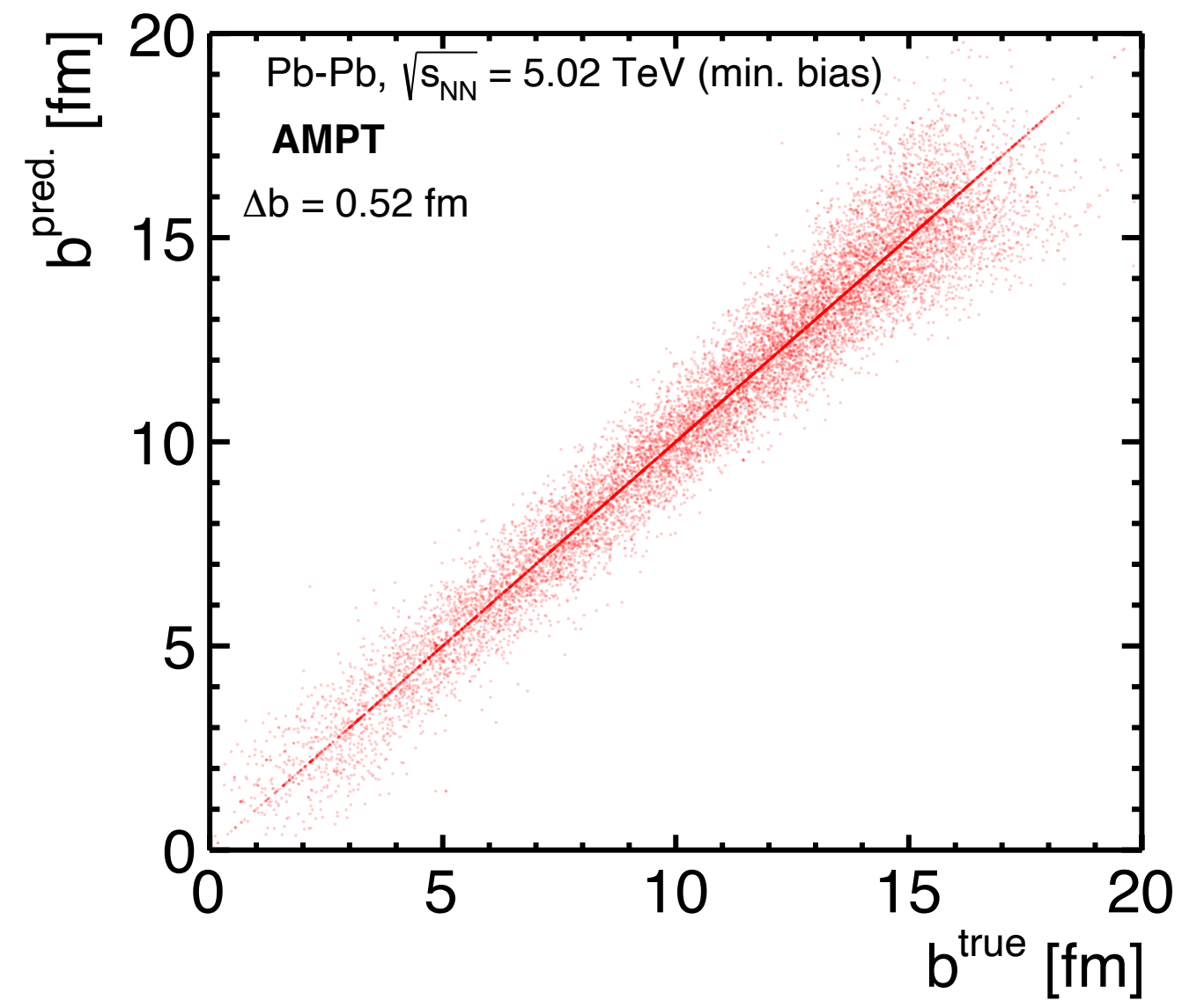
L. Breiman, J. H. Friedman, R. A. Olshen, and C. J. Stone, *Classification and Regression Trees* (Wadsworth & Brooks/ Cole Advanced Books & Software, Monterey, CA, 1984), p. 358, <https://doi.org/10.1002/cyto.990080516>.



Results

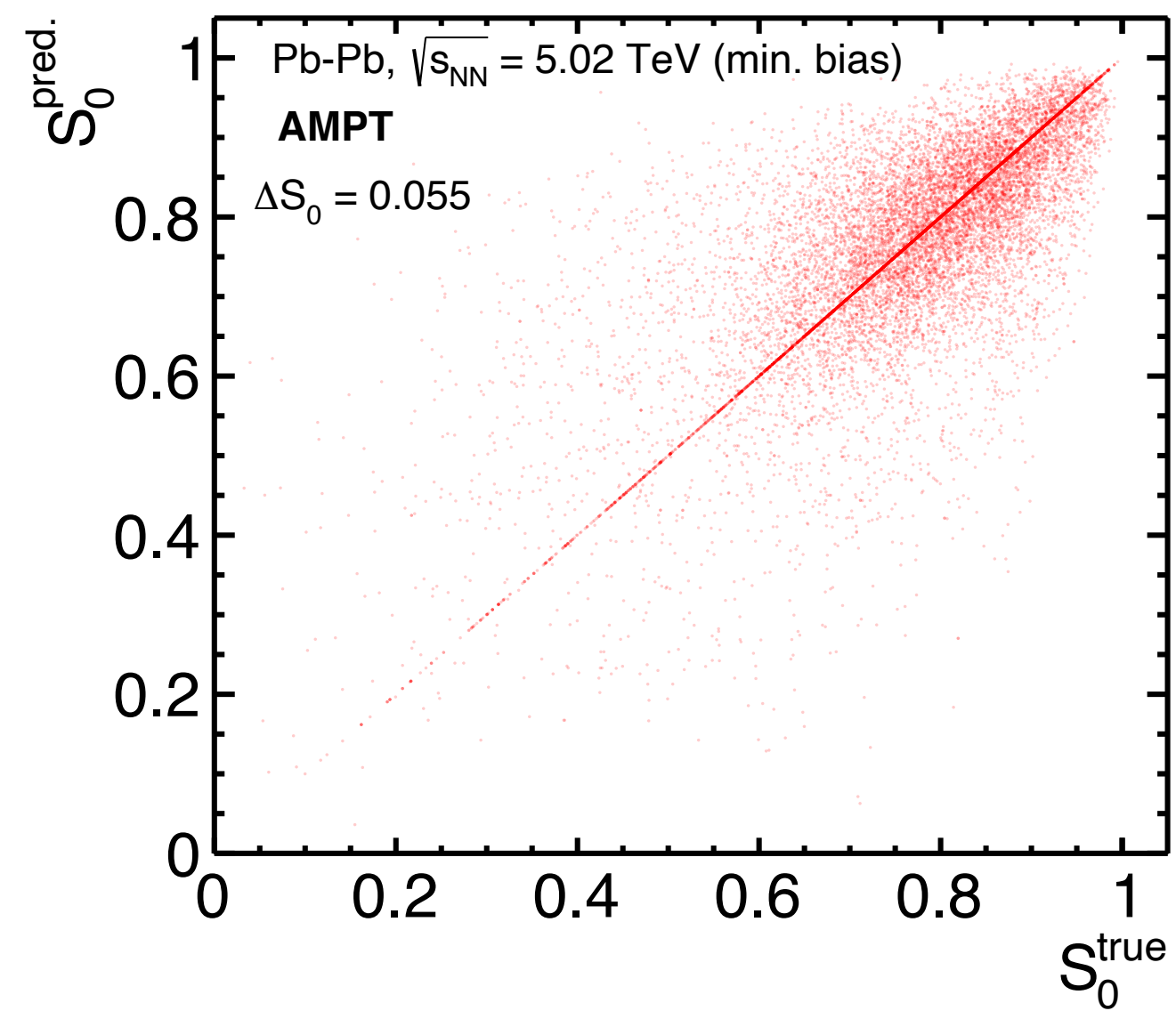
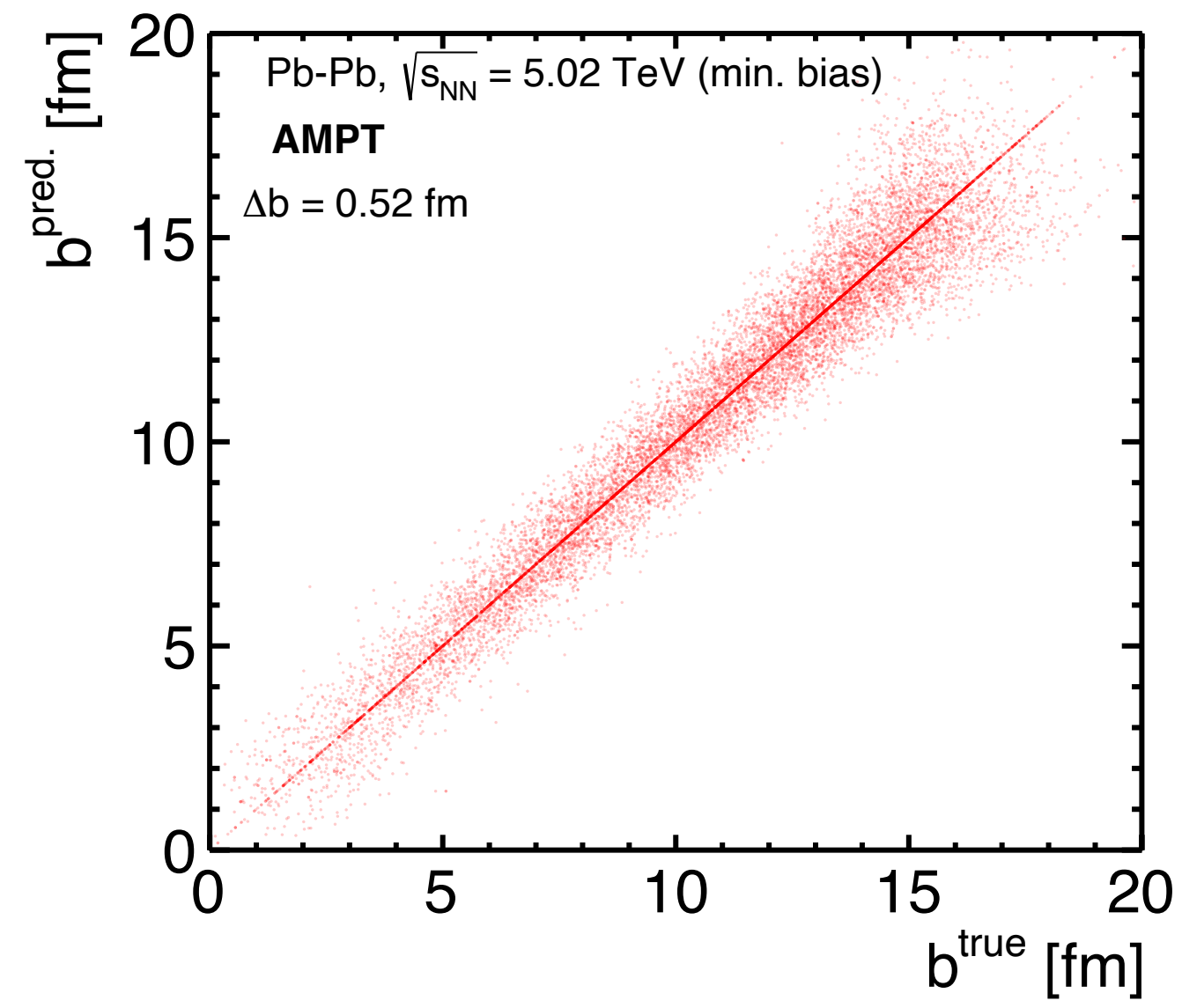
N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

Results



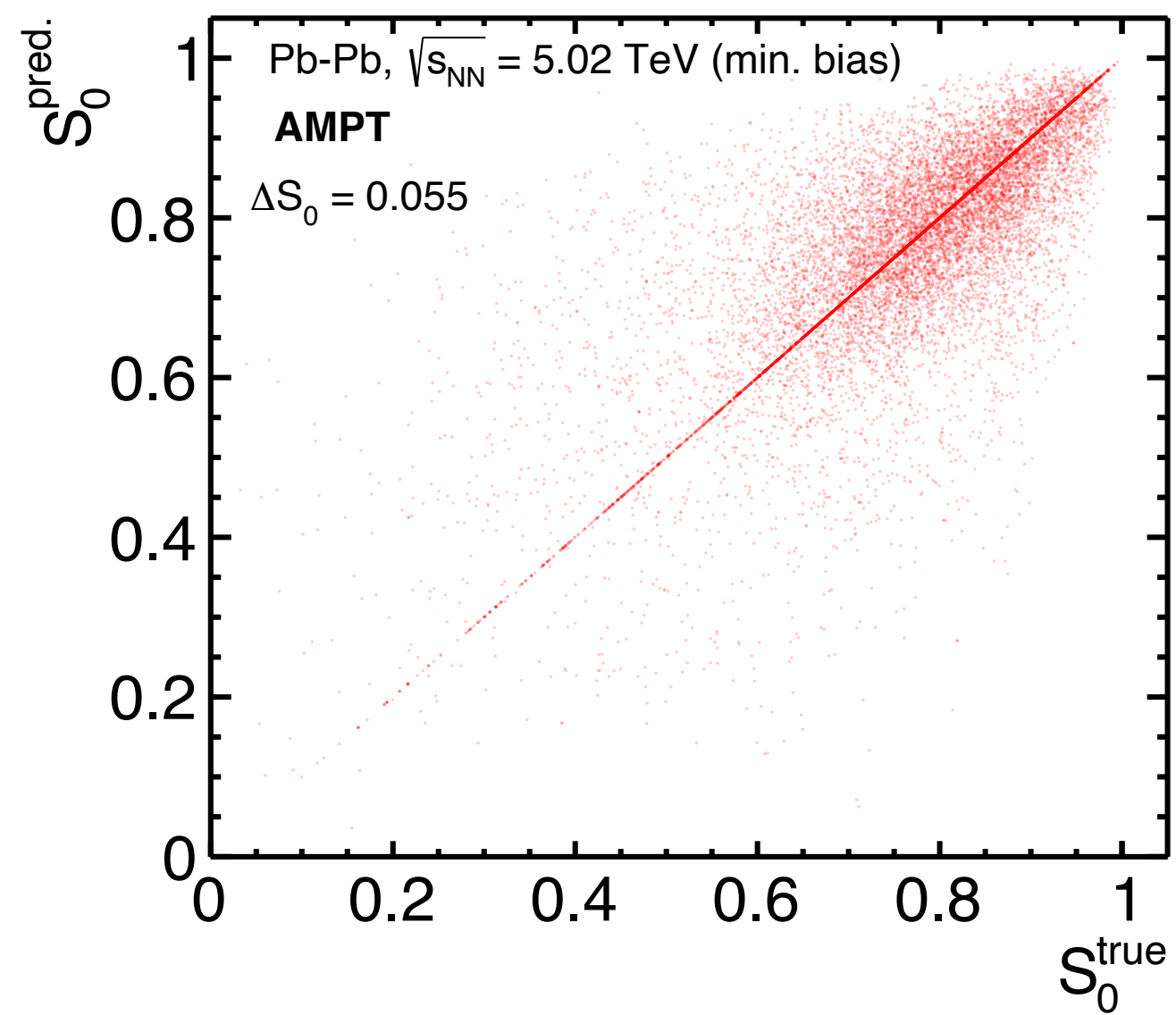
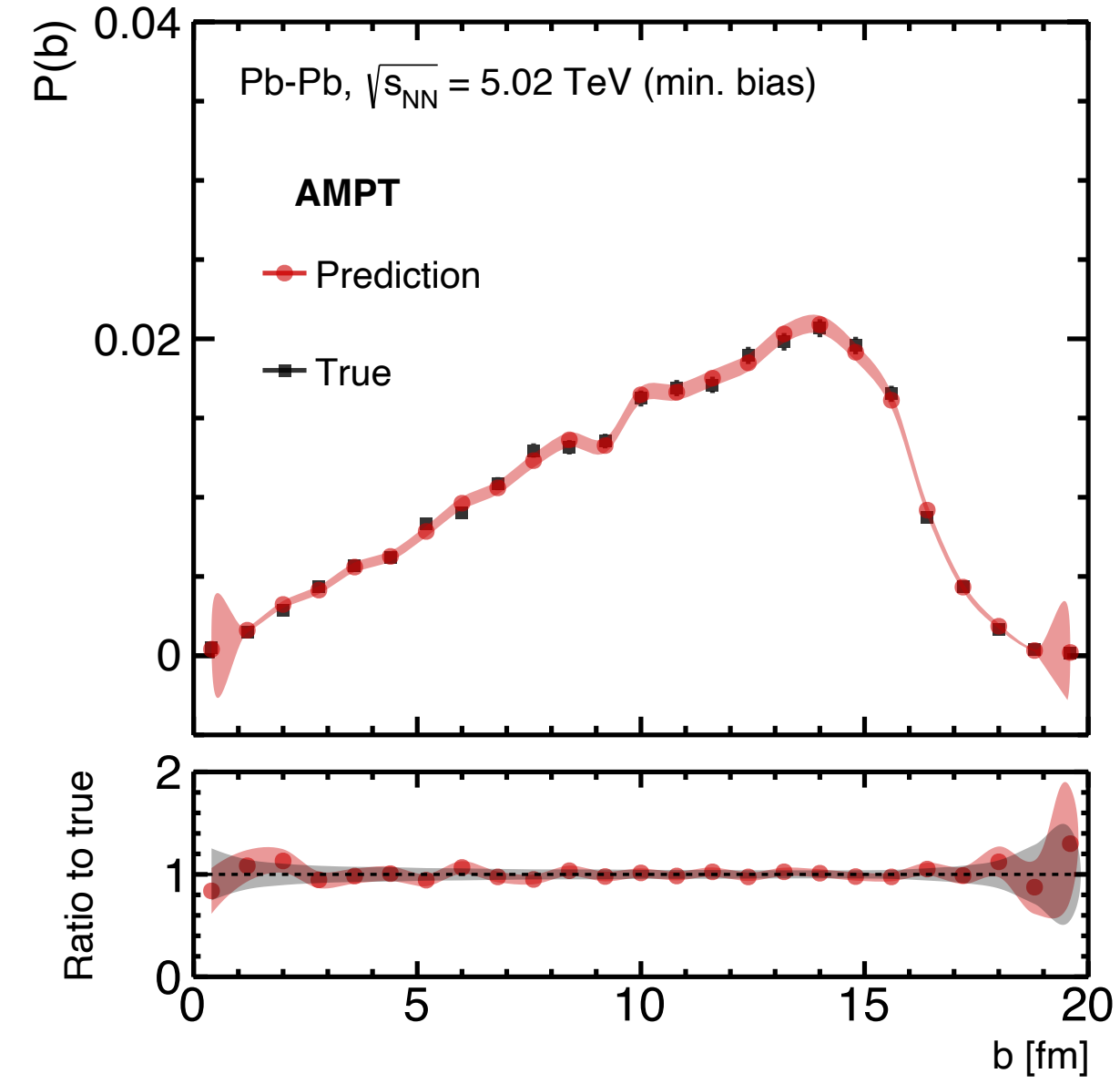
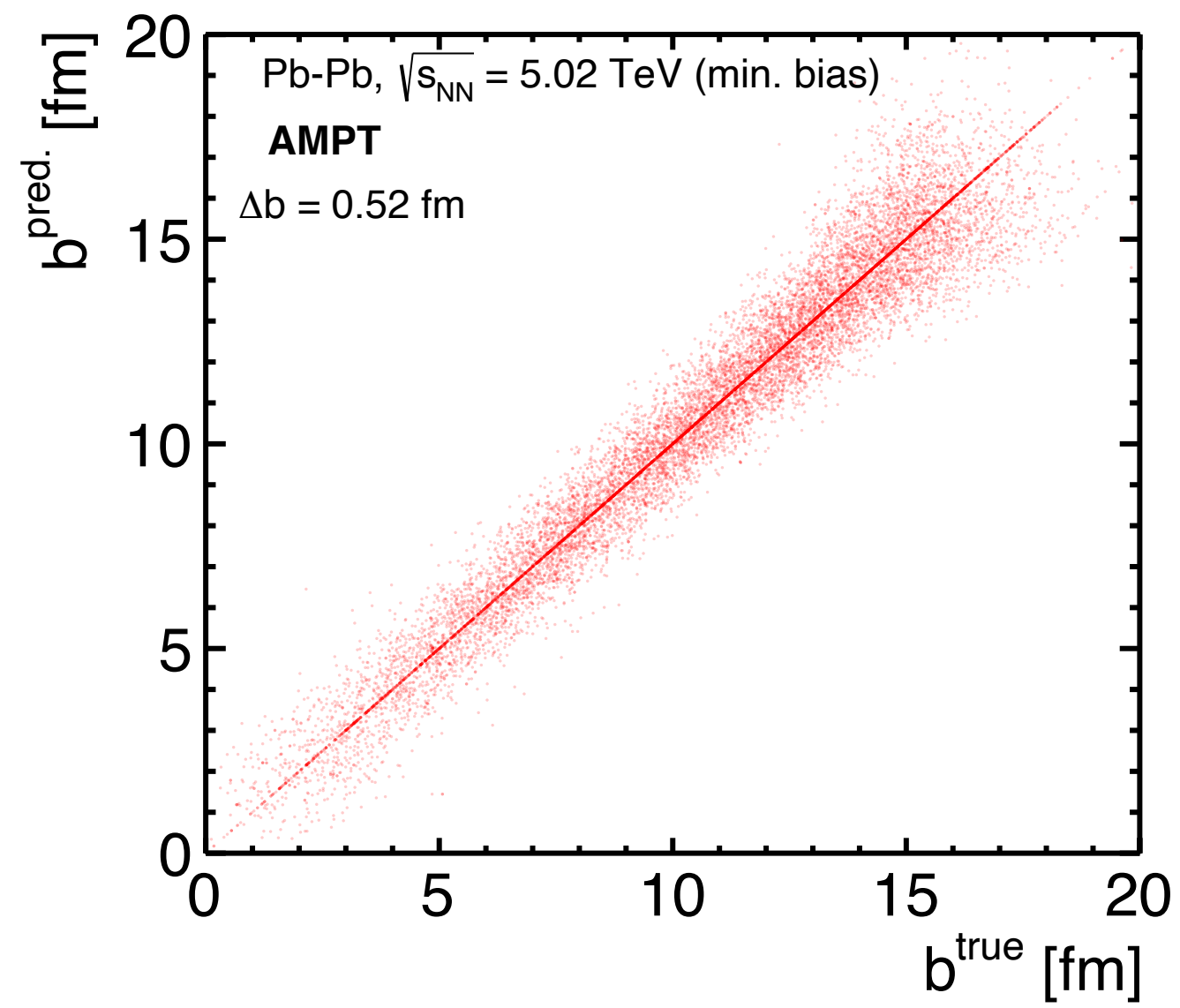
N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

Results



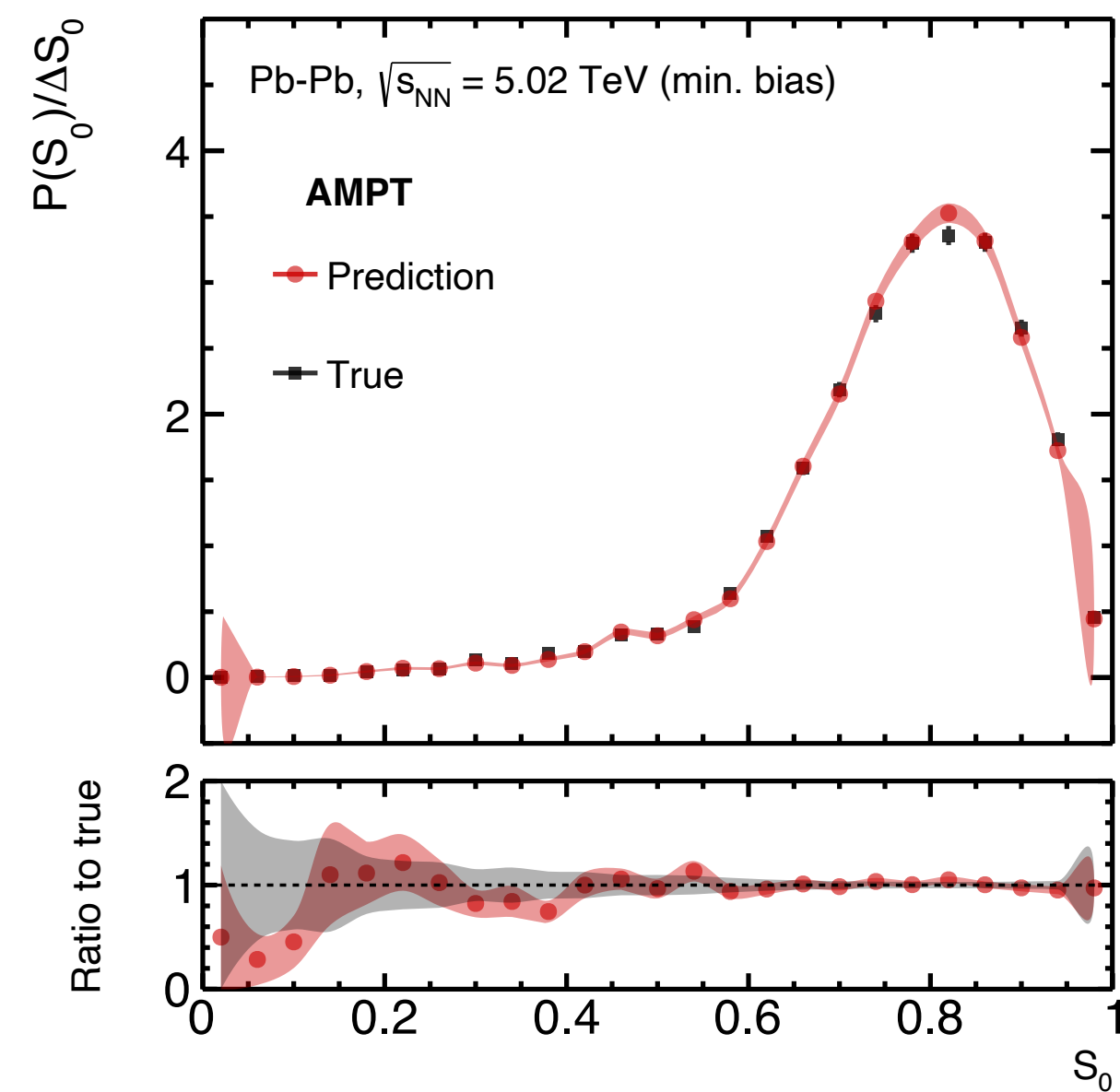
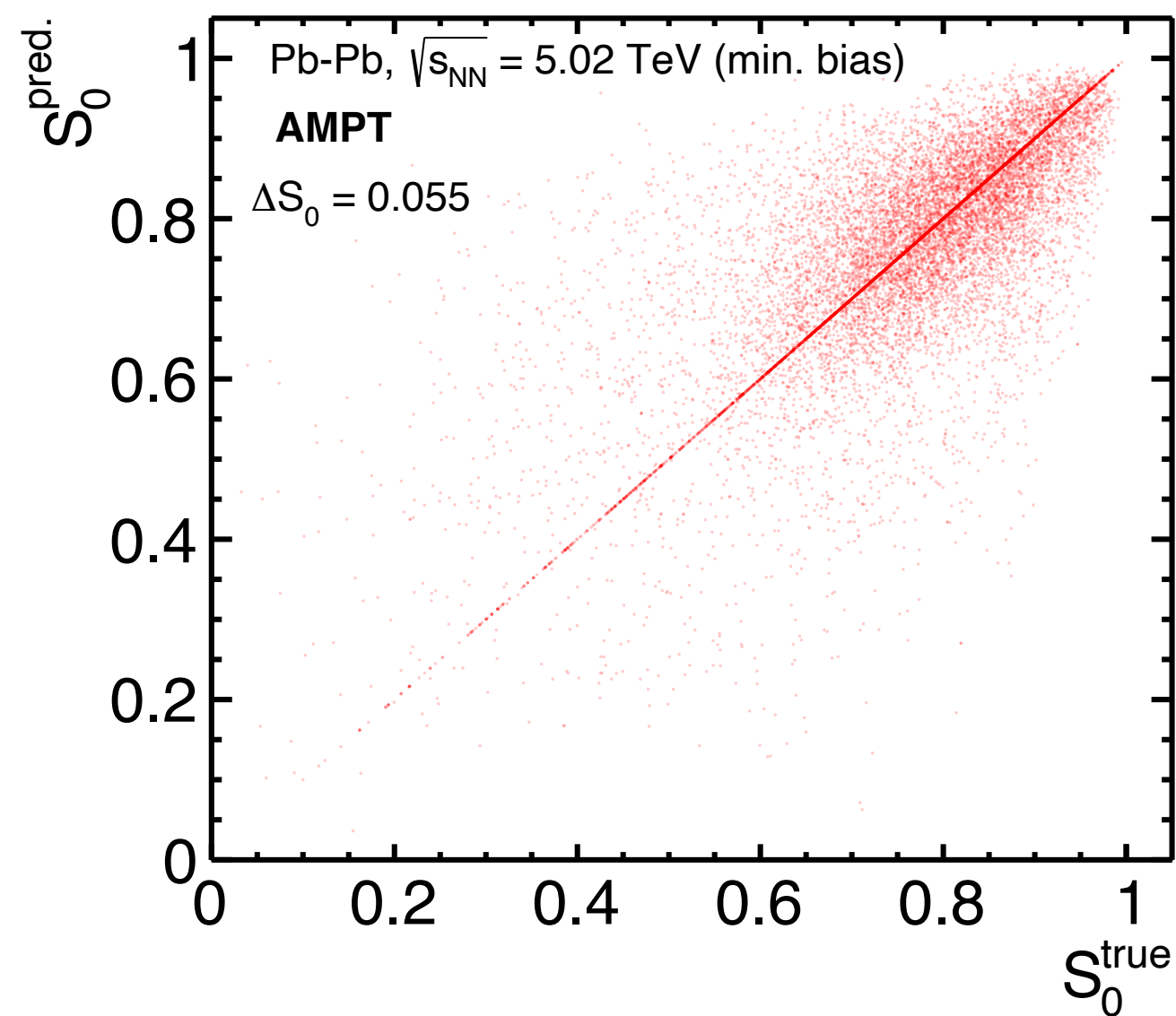
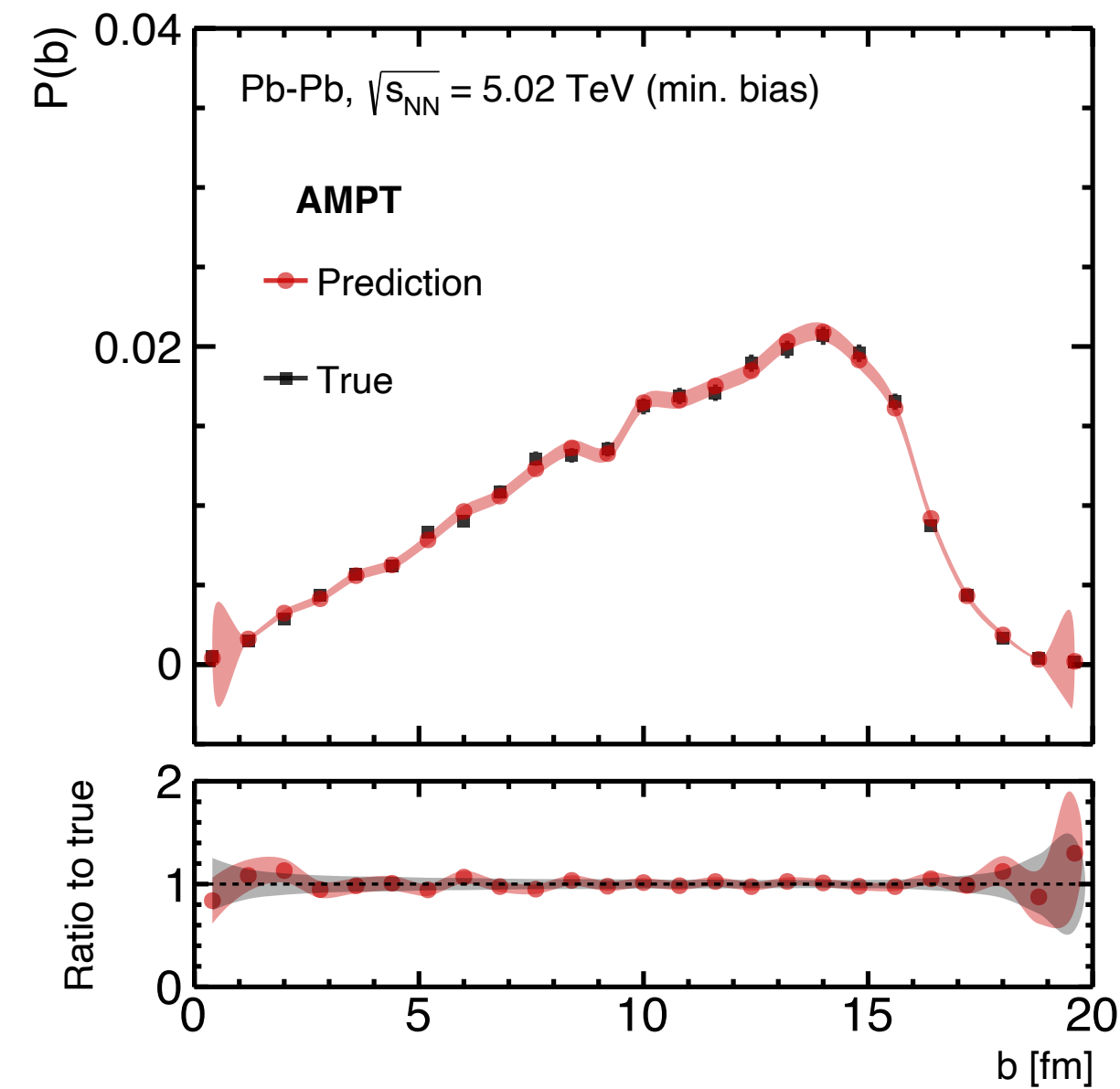
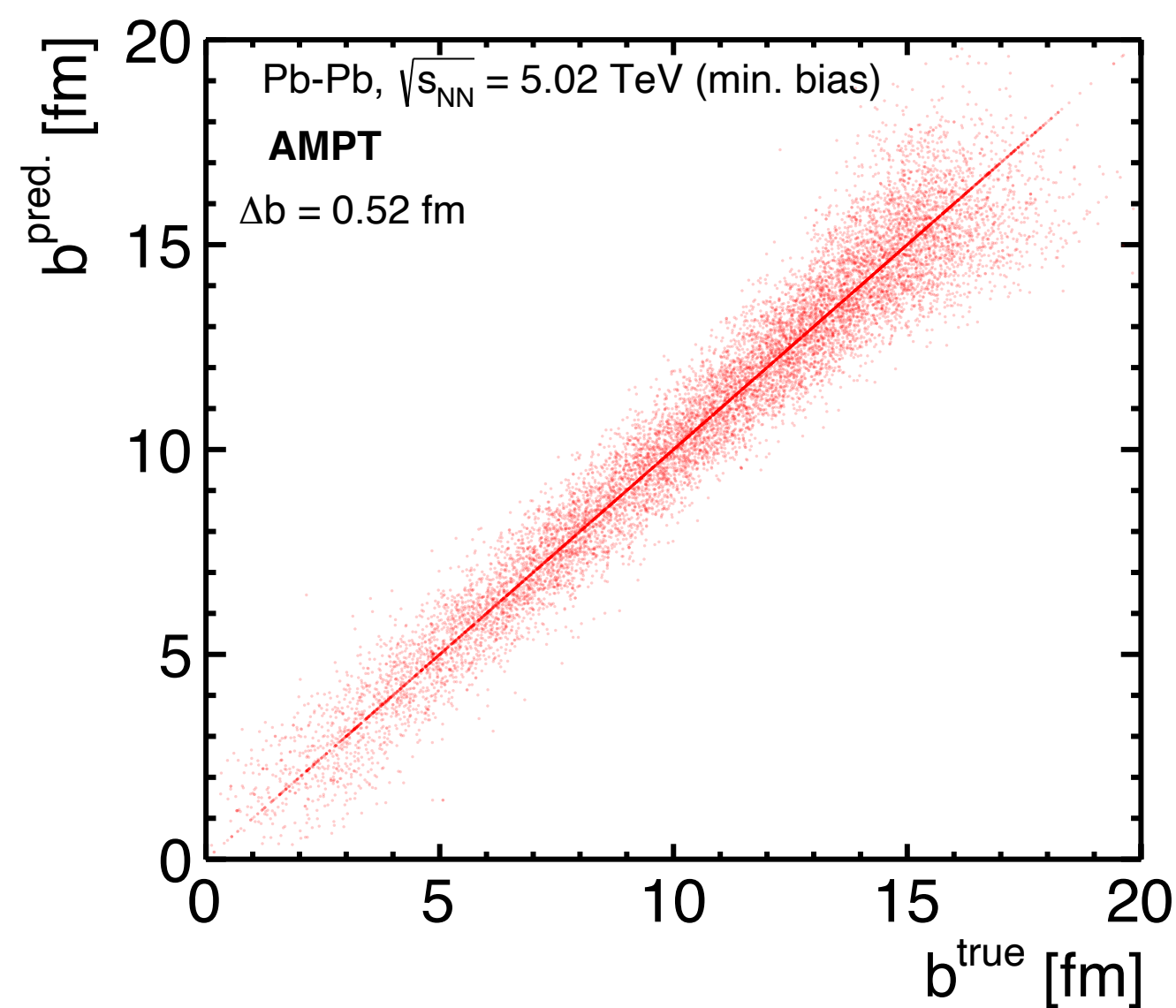
N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

Results



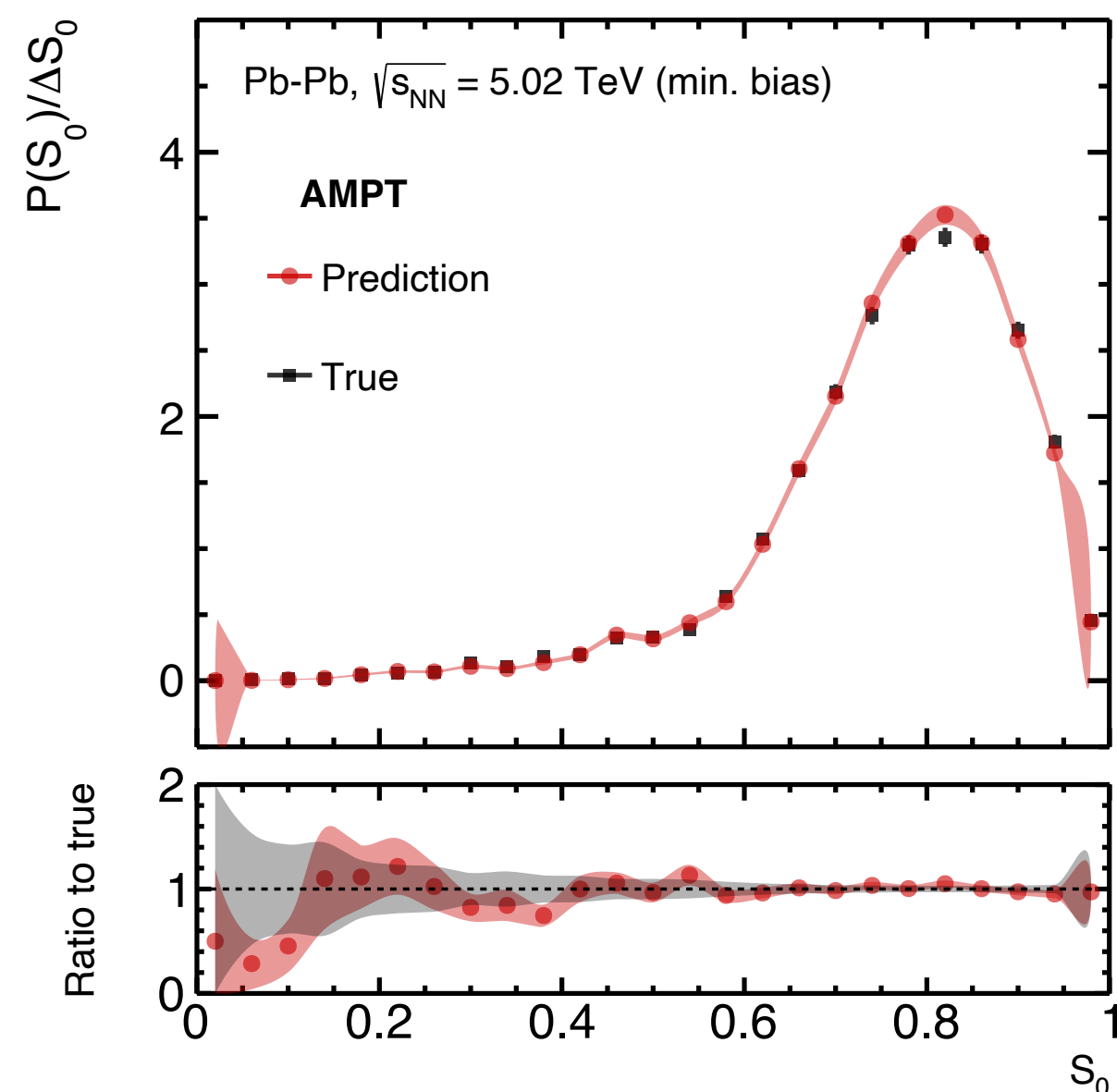
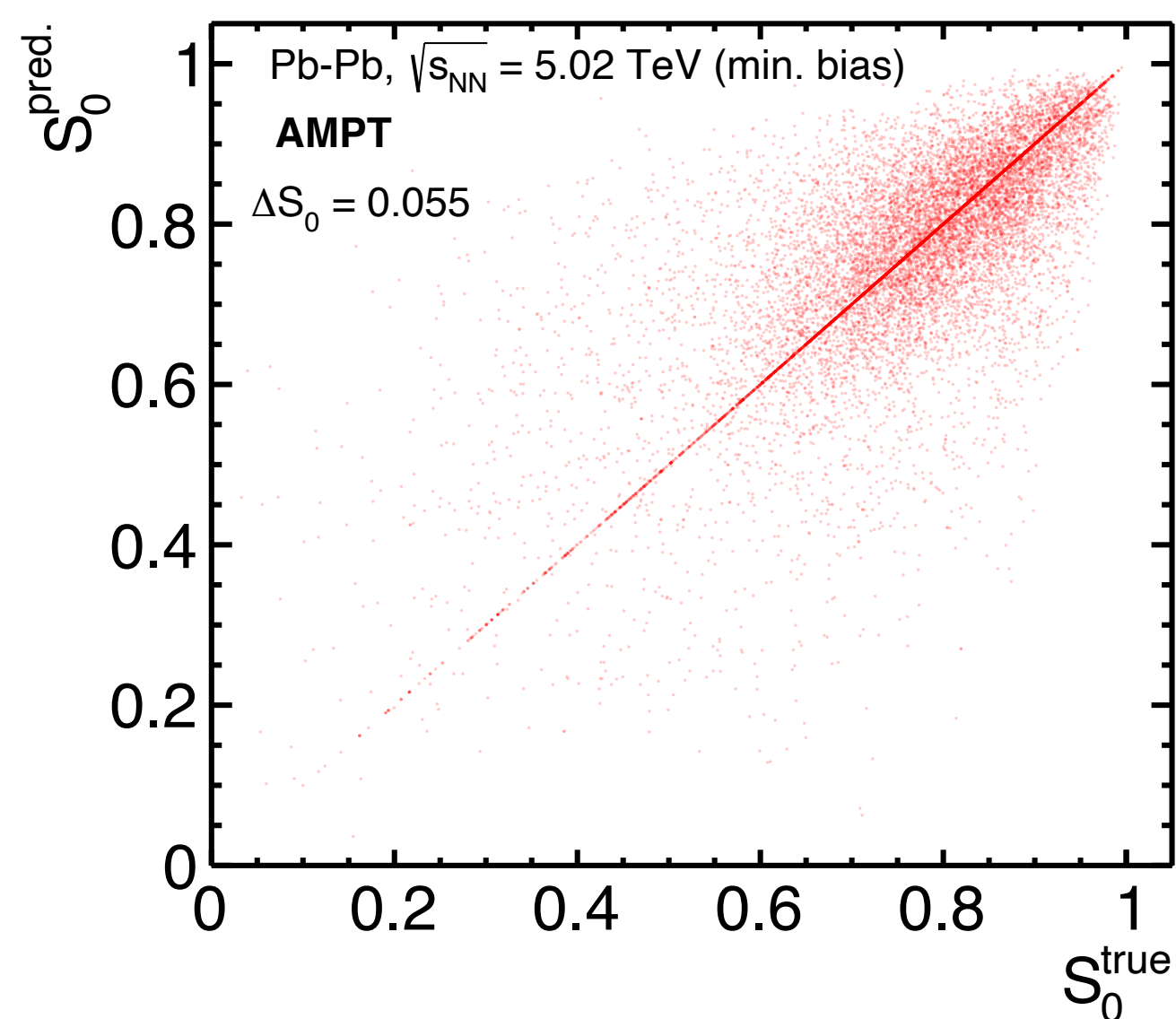
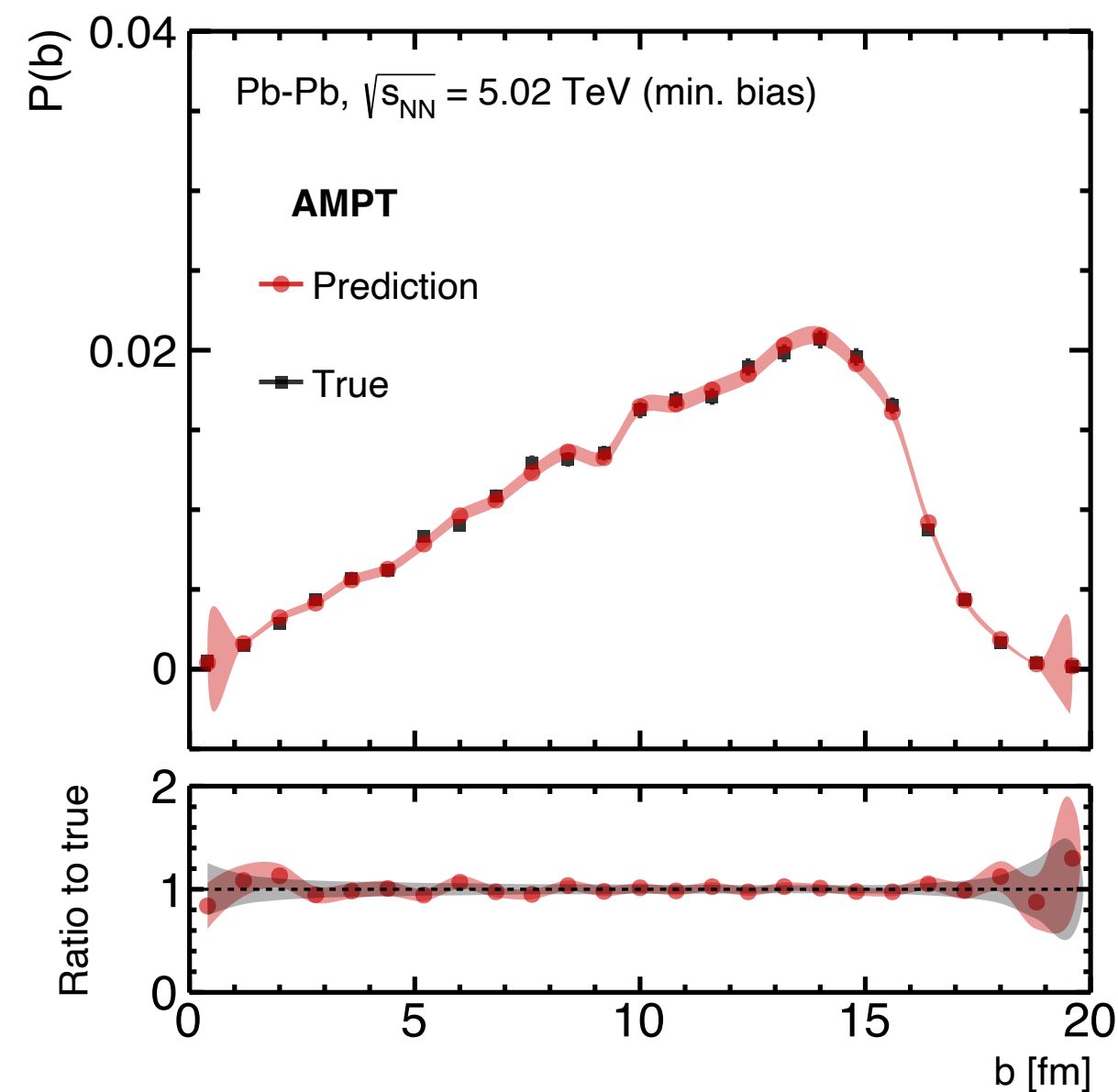
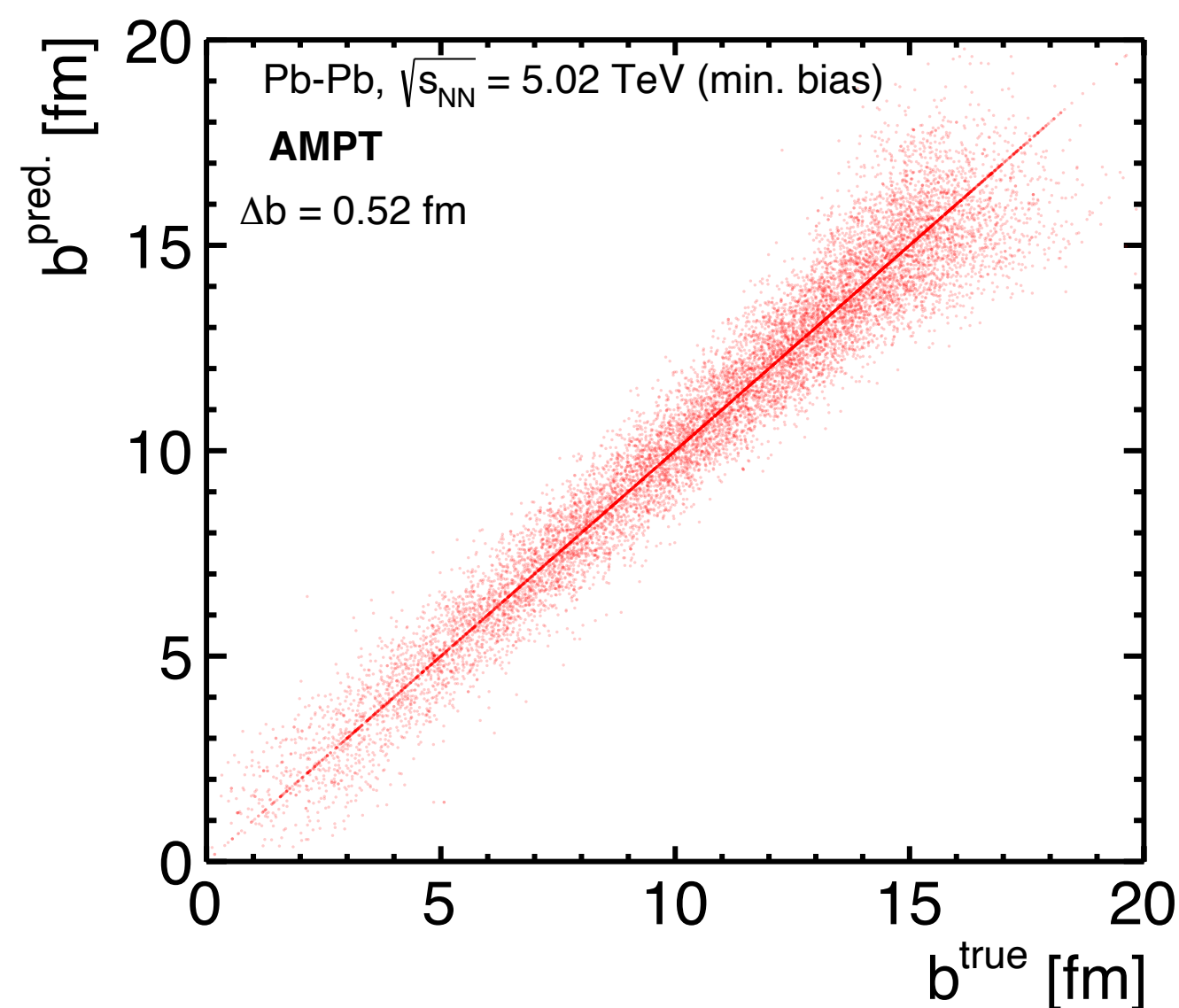
N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

Results



N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

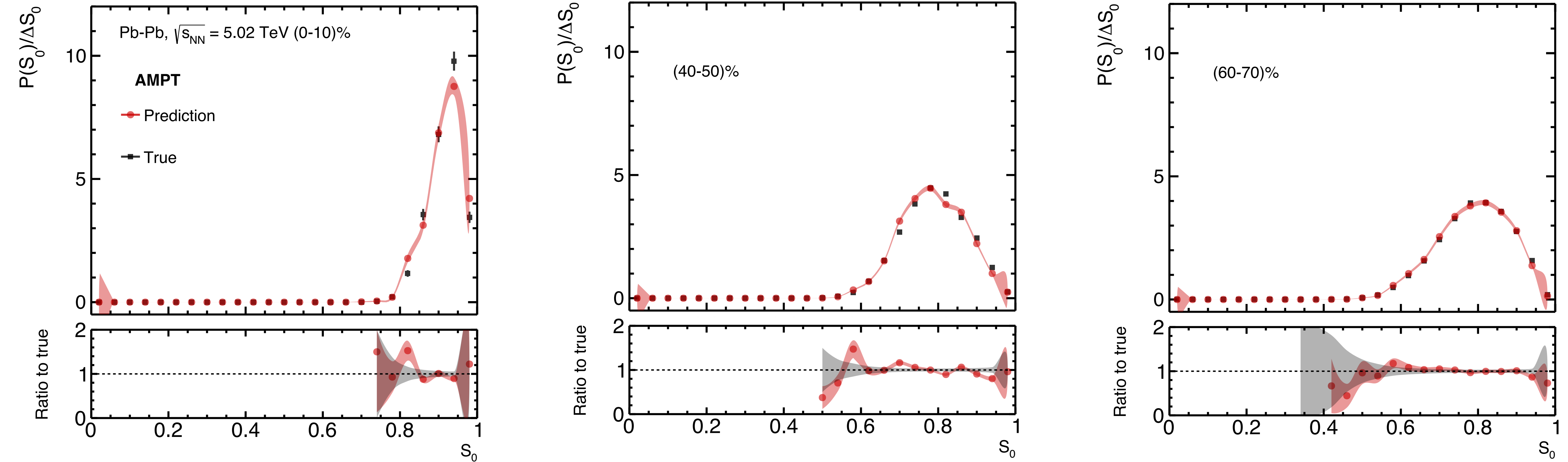
Results



- The ML model trained with 5.02 TeV minimum bias simulated data
- Most of the points populate $y = x$
- The predictions for both impact parameter and spherocity distributions are in good agreement with the simulated data

N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

Results



- Centrality-wise spherocity distributions
- Training is done using minimum bias simulated data
- **BDT preserves the centrality (or multiplicity) dependence**

N. Mallick, S. Tripathy, A. N. Mishra, S. Deb, and R. Sahoo, [Phys. Rev. D103, 094031 \(2021\)](#)

Summary

Summary

- Report the first implementation of ML tools for the estimation of impact parameter and transverse sphericity in heavy-ion collisions at the LHC
- BDT preserves the centrality and energy dependence of particle production
- Final state particle information is used
- Training is resource hungry → application is faster and economic
- A learning process → Scope for improvements

Summary

- Report the first implementation of ML tools for the estimation of impact parameter and transverse sphericity in heavy-ion collisions at the LHC
- BDT preserves the centrality and energy dependence of particle production
- Final state particle information is used
- Training is resource hungry → application is faster and economic
- A learning process → Scope for improvements

Thank you!