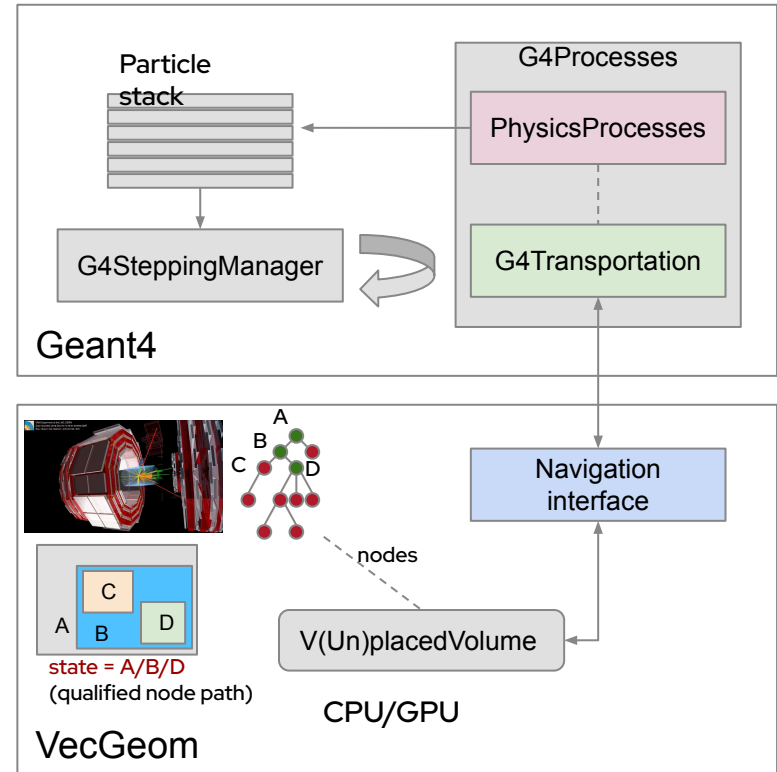


VecGeom surface modelling

andrei.gheata@cern.ch

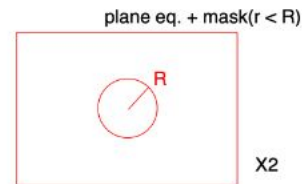
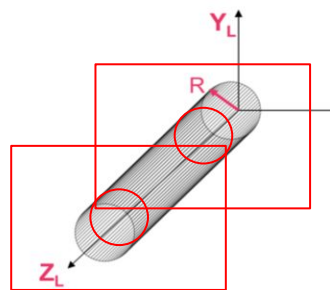
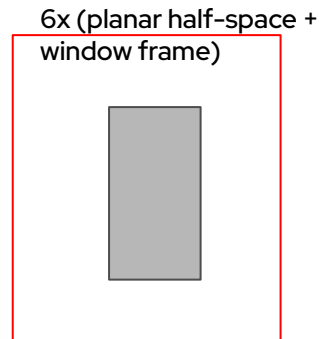
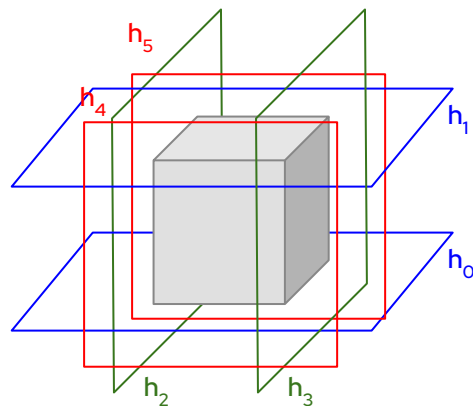
VecGeom: navigation back-end for Geant4

- ▶ Collaborative effort to develop most efficient navigation algorithms on top of Geant geometry description
 - Independent of the transport simulation toolkit
 - Supporting GPU (CUDA) as back-end
- ▶ State of the art geometry navigation backend for Geant4
 - **Hierarchic CSG (Boolean combinations) solid modeling based on containment**
 - Actively maintained and developed
 - **Main bottleneck for GPU sim workflows (see Ben's talk)**



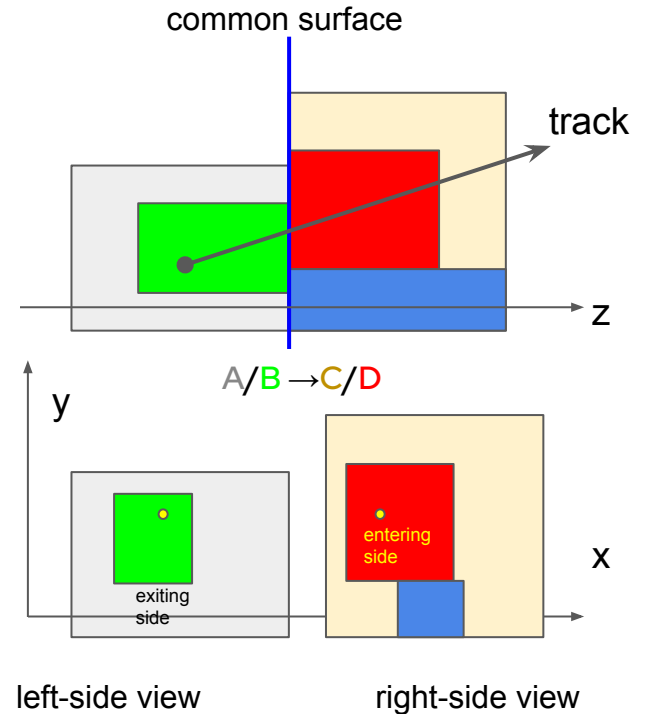
Bounded surface modeling - a different approach for the GPU

- ▶ 3D bodies represented as Boolean operation of half-spaces*
 - First and second order, infinite
 - Just intersections for convex primitives
 - ▷ e.g. box = $h_0 \& h_1 \& h_2 \& h_3 \& h_4 \& h_5$
- ▶ Storing in addition the solid imprint (frame) on each surface: **FramedSurface**
 - **Frame information is redundant**
 - ▷ helps taking navigation decisions more efficiently (hitting a framed surface means hitting the real solid)

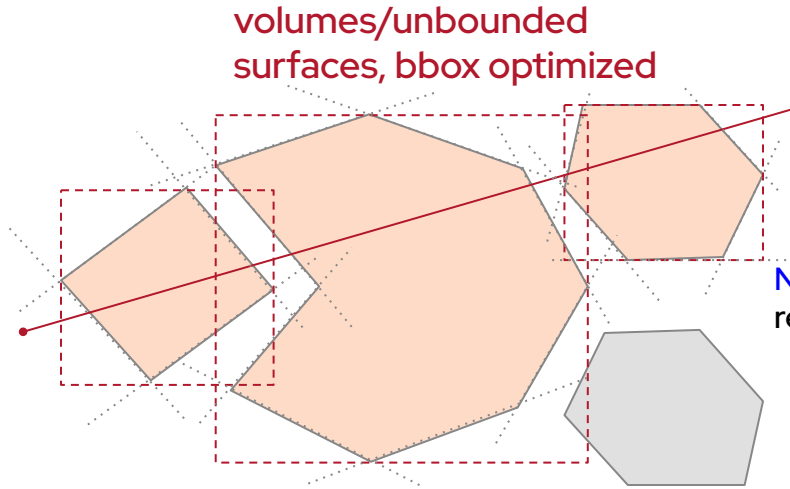


CommonSurface - the navigation primitive

- ▶ In Geant volumes can share common surfaces
 - Define "**CommonSurface**" as boundary between volumes
- ▶ A common surface is made of two sides, each having hierarchic **FramedSurfaces**
 - Checking frame masking conditions for the track crossing point on each side is equivalent to relocating to the next volume
 - Much cheaper than current volume relocation, non-recursive algorithm



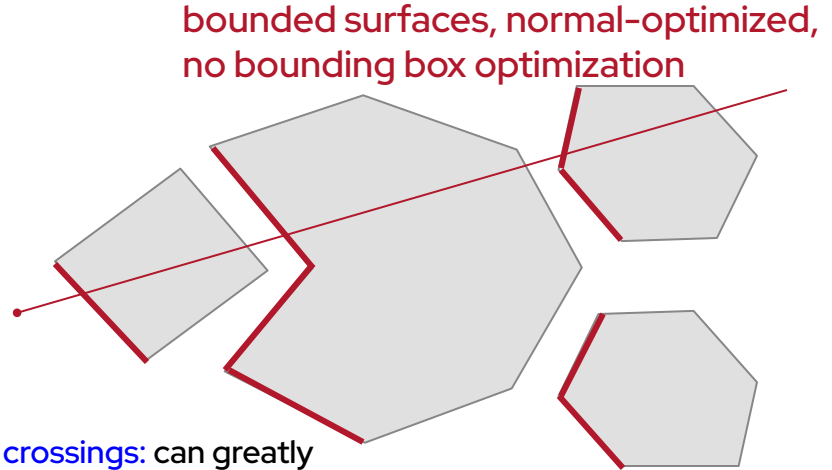
Why use frames ?



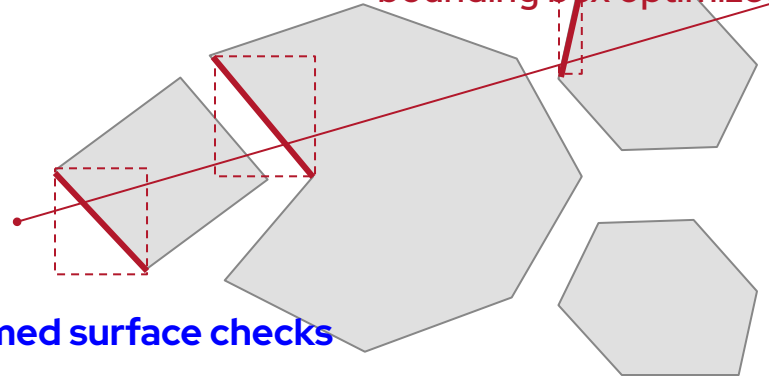
3 solid / 18 unbounded surface checks

High potential for work reduction compared to solid or unbounded models

No virtual crossings: can greatly reduce candidates to be checked




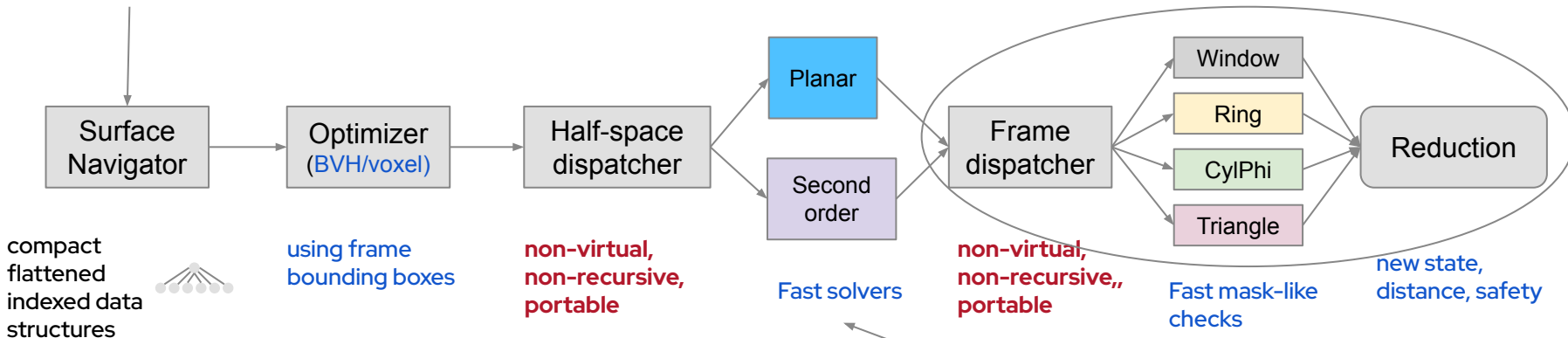
bounded surfaces, bounding box optimized




3 framed surface checks

Implementing a GPU-friendly computation pipeline

volume hierarchy 
state = /Lvl_0/Lvl_1/...



 better balanced input per particle due to **flattening** and **mixing** surfaces from different volumes

 faster divergent sections with **fewer** branches

Conversion of solids to framed surfaces

- ▶ Any solid surface can be constructed from predefined unplaced/frame types

- Conversion done behind the hood, implementation completely transparent

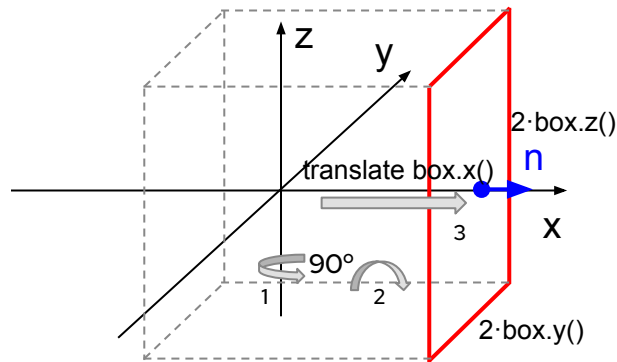
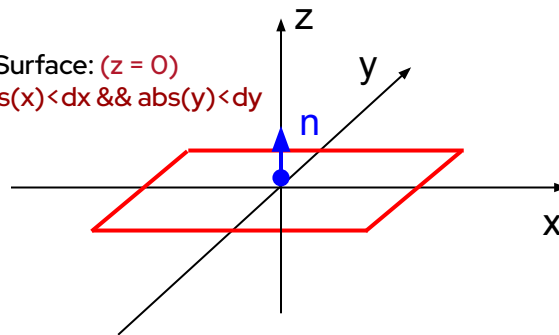
- ▶ Only box, tube, trapezoid for now

- The full supported set TBD

```
CreateLocalSurface(  
    CreateUnplacedSurface(kPlanar),  
    CreateFrame(kWindow, WindowMask_t{box.y(), box.z()}),  
    CreateLocalTransformation({box.x(), 0, 0, 90, 90, 0}));
```

see full box implementation [here](#)

UnplacedSurface: $(z = 0)$
Frame: $\text{abs}(x) < dx \ \&\& \ \text{abs}(y) < dy$



Making a box from framed surfaces

The complex cases: Boolean solids

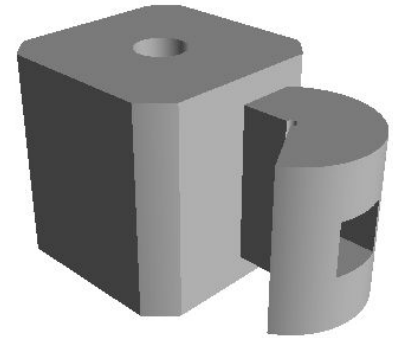
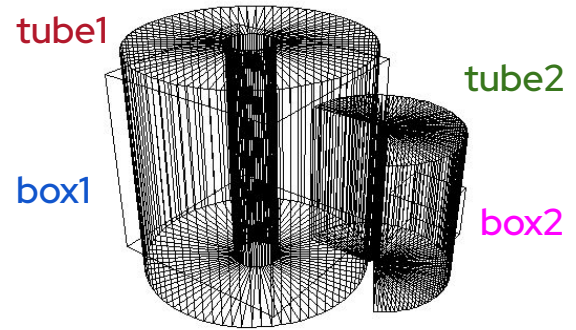
- ▶ Composite solids support intersection (&), union (|) and subtraction (&!) of arbitrary number of components
- ▶ Building logic expressions in terms of surface id's, using De Morgan's rules

```
(( 6 & 7 & 8 & 9 ) & ( 10 & 11 & 12 & 13 & 14 & 15 )) |  
( ( 16 & 17 & 18 & 19 & ( 20 | 21 ) ) & ( !22 | !23 | !24 | !25 | !26 | !27 ) )
```

- ▶ Expression simplification using Boolean algebra rules, keeping left operand the simplest to evaluate for short-circuiting

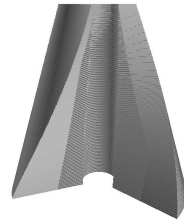
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( 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 & 15 ) | ( 16 & 17 & 18 & 19 & ( 20 | 21 ) & ( !22 | !23 | !24 |  
!25 | !26 | !27 ) )
```

More implementation details in the backup



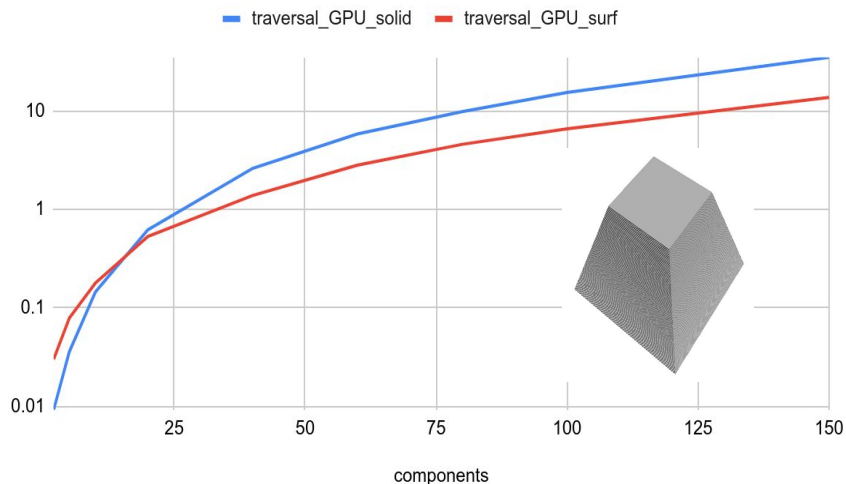
```
(tube1 & box1) | (tube2 & ! box2)
```


Scaling for the Boolean implementation



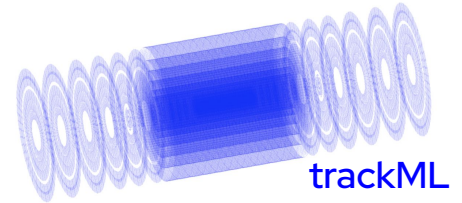
- ▶ Current implementation validated for correctness against the VecGeom solid model
 - Tested union of up to 150 layers of disks subtracting a box, more exhausts CUDA stack space for the solid approach
- ▶ Un-optimized version so far, but scaling looks good
 - 2x slower for 5 components, 2x faster for 50 components on GPU
 - Finding & tagging the real surfaces of a Boolean composite can help a lot

Traversal time for box tower



Ray-tracing example traversing all volume boundaries until exiting the setup

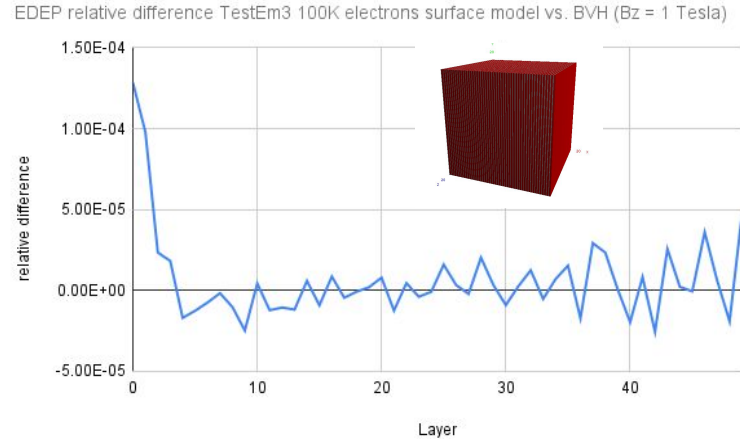
Preliminary performance



- ▶ Unit tests available for correctness checking against VecGeom solid model
 - Tube, trapezoid
 - TestEm3 - a simple layered calorimeter made of box slabs
- ▶ Ray-tracing benchmark, working with generic GDML input (supported solids only), validated/benchmarked against non-optimized solid navigator
 - Sampling points and directions in the bounding box of the setup
 - Computing location path and safe distance for each point
 - Propagation + relocation between boundaries until exiting the setup
- ▶ Results (compared to volume looping navigation) for trackML setup
 - Safety computation: ~2x slower on CPU, ~2x faster on GPU
 - Propagation + relocation: ~2x faster on CPU, ~6x faster on GPU
 - Memory: ~1 kByte per "touchable" volume

TestEm3 integration in AdePT

- ▶ Navigation interfaces of AdePT integrated in the *SurfNavigator* namespace
- ▶ Sampling calorimeter block of Pb + LAr box layers in constant Bz field (or no field)
- ▶ 10 GeV electrons shot towards the calorimeter along X axis
- ▶ Validated to 0.1 per mil level against existing solid navigators (BVH-optimized and simple loop)



	BVH	Loop	surf
no field	152s	162s	156s
Bz=1T	194s	-	184s

Next priority items

- ▶ Geant 3D solid coverage
 - Currently only few solids supported, we need to write converters for an extended set
- ▶ Support for logical scenes of surfaces
 - Pay the price of extra frame transformations for releasing the memory pressure
- ▶ Navigation optimization
 - Adapting existing BVH support to framed surfaces

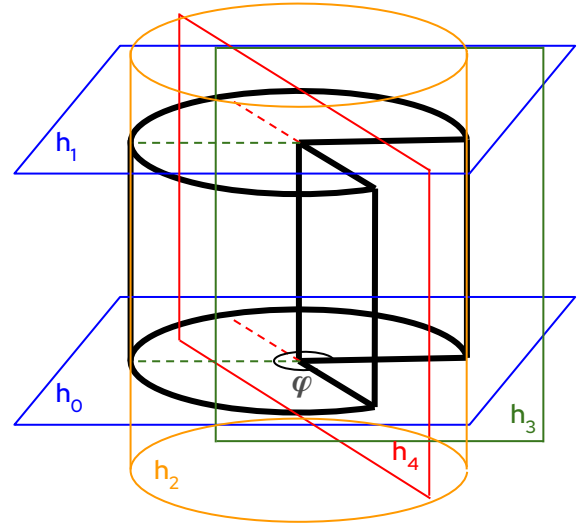
Outlook

- ▶ VecGeom went for a surface model approach enriched by solid frame information to be GPU-efficient
 - Even if redundant, the hope is that this allows better work balancing on GPU, avoiding reductions per volume
 - Allows addressing natively isotropic safe distance computation, essential for performance
- ▶ Currently implemented all the features required by particle transport, for a subset of solids
 - Integrated with AdePT, already usable with very simple setups
- ▶ Extensions and optimizations are essential to judge performance for realistic setups
 - We target the bottlenecks currently observed in AdePT advanced examples

Backup

Boolean evaluation for more complex solids

- ▶ Cut tube: **tube & wedge**
 - **tube** = $h_0 \& h_1 \& h_2$
 - **wedge** = $(\varphi < \pi) ? h_3 \& h_4 : h_3 \mid h_4$
- ▶ **Inside**: Evaluation of the Boolean expression (half-space information only)
 - $\text{Inside}(h_0 \& h_1 \& h_2 \& (h_3 \mid h_4))$
- ▶ **Distance/Safety**: Ignore Boolean expression for primitives (real surfaces)
 - ToIn/ToOut inferred from the start state (surfaces crossed from the wrong side ignored)
 - $\text{Distance}(h_i) < \text{dmin} \ \&\& \ \text{frame.crossed}$
 - Safety reduction takes into account convexity
- ▶ **Boolean solids**: complete evaluation of Boolean expression needed
 - The Boolean expression can generate virtual framed surfaces



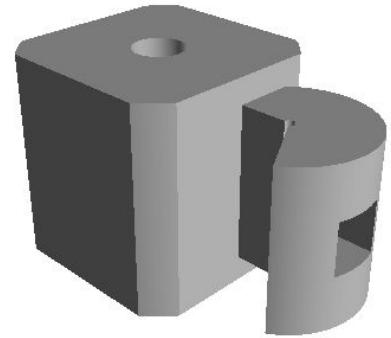
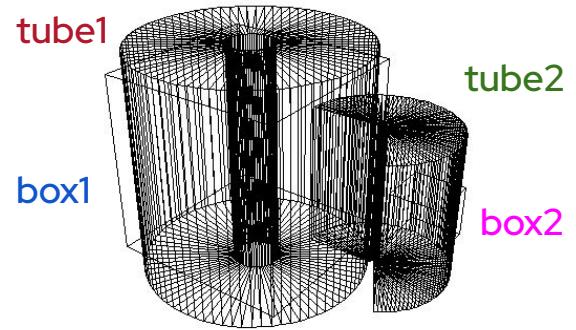
Logic expressions

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- ▶ The logic expressions with solids are expanded in terms of surface id's, using De Morgan's rules

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!25 | !26 | !27 ) )
```



```
(tube1 & box1) | (tube2 & ! box2)
```


Logic evaluation for distance queries

▶ Common approach for Distance and Safety queries

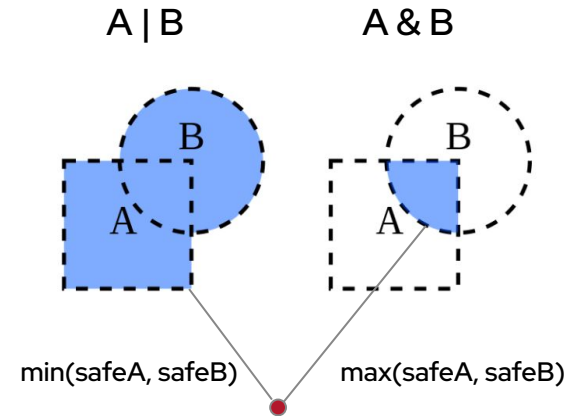
- Mix in the search all surfaces visible from the current state (Boolean and regular)
- Negated surfaces have flipped associated half-space
- Apply a `std::min` reduction on the distance to the surface half-space, excluding “far-away” candidates

▶ Distance computation

- Validate crossing point against the frame information
- If this hits a Boolean surface, exclude virtual solutions by checking the logic expression

▶ Safety computation

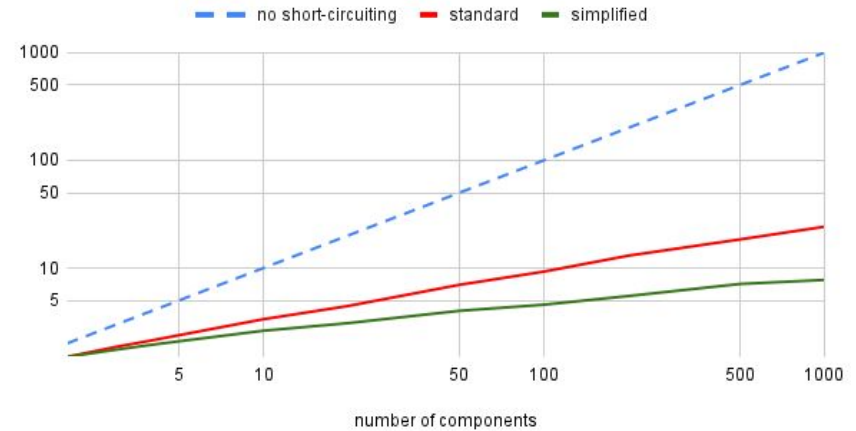
- Use frame information to correct the safe distance
- Use a stack-based infix logic evaluation using min/max as reduction (correct only if surfaces are ‘real’)



Logic evaluation

- ▶ Boolean operations can be short-circuited
 - true | any = true, false & any = false
- ▶ Infix stackless parsing for Inside evaluation
 - Inserting jumps exiting the current scope

Average surface check counts needed for "Inside" evaluation



Randomly generated Boolean expression

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
(a	&	b)		(c	&	!	d)				
(a	&	5	b)		15	(c	&	14	!	d)	

