

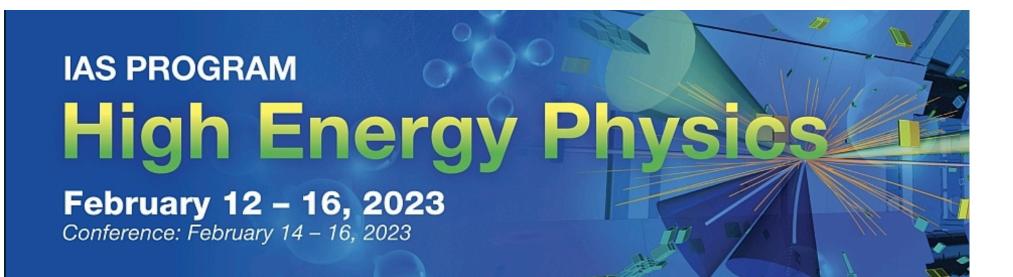






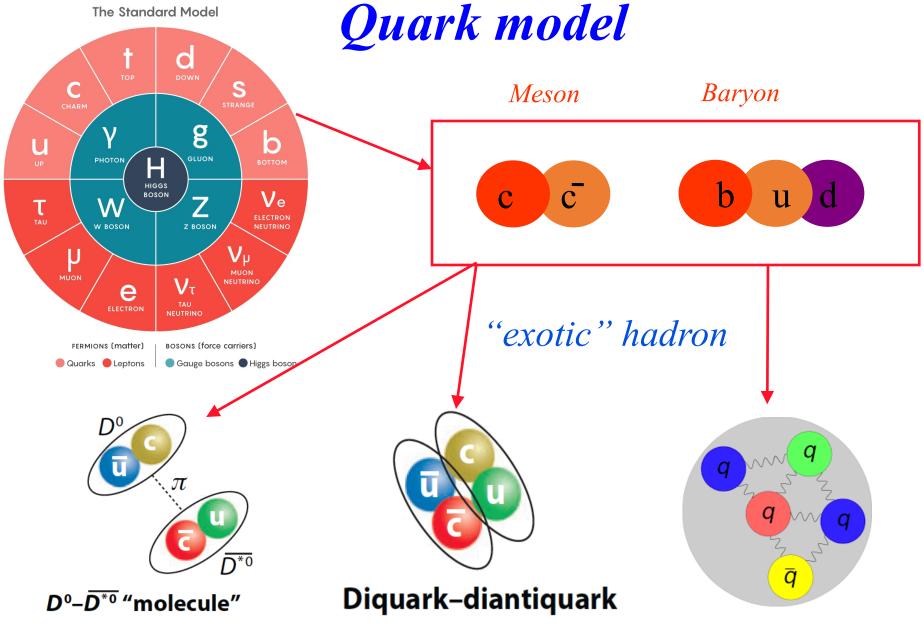
# J/ψJ/ψ Mass Spectrum at LHC & CEPC Kai Yi

## **Nanjing Normal University & Tsinghua University**



# Outline

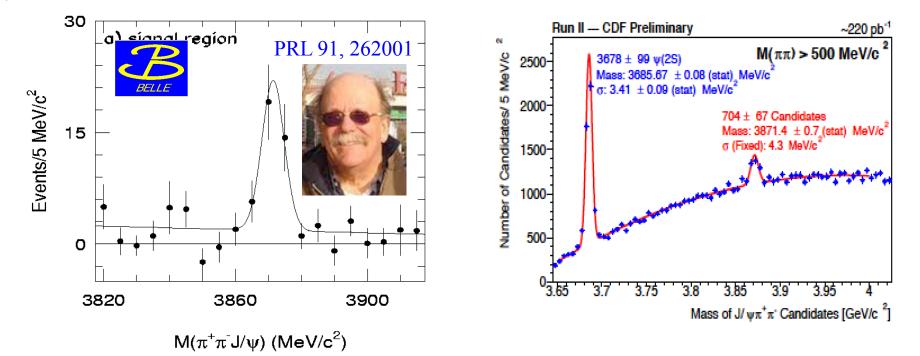
- About exotic hadron
- CMS contribution to heavy exotic hadron
- New Domain of Exotics: All-Heavy Tetra-quarks
- Discussion and future (CEPC)
- Summary



*Two possible extensions of meson to tetra-quark states* 

Possible penta-quark state

X(3872) (Belle)--2003



2017 Laureates

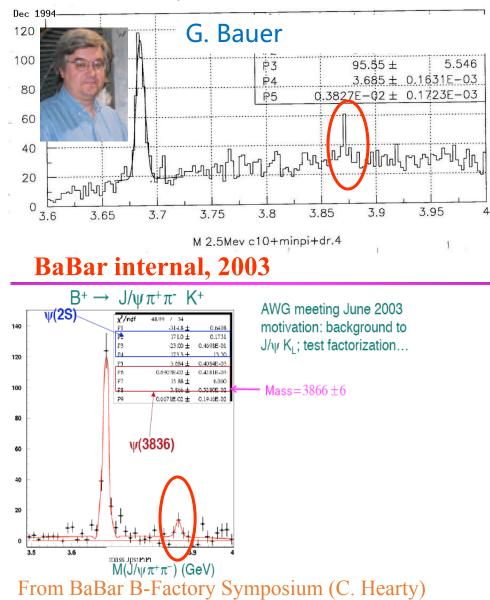


"...The X(3872) was discovered by Dr. Sookyung Choi and Dr. Stephen Olsen with their colleagues in the Belle experiment among the final states of the decay of B mesons. The X(3872) was confirmed by seven other experimental groups thereafter and is the first example of a new type of XYZ meson and the most well-established state among them. ..."

#### 2017 Korean Ho-Am Science Prize

### *Hints before the discovery of X(3872)* $\rightarrow$ *J*/ $\psi \pi^+ \pi$

**CDF internal**, 1994

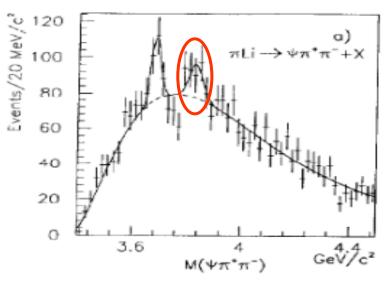


http://www-conf.slac.stanford.edu/b-factory-symposium/talks.asp

E705, PRD 50, 4258 (1994)

E705 saw  $\psi$ (3836) (2<sup>--)</sup>in 1994, 3.836±0.013 GeV

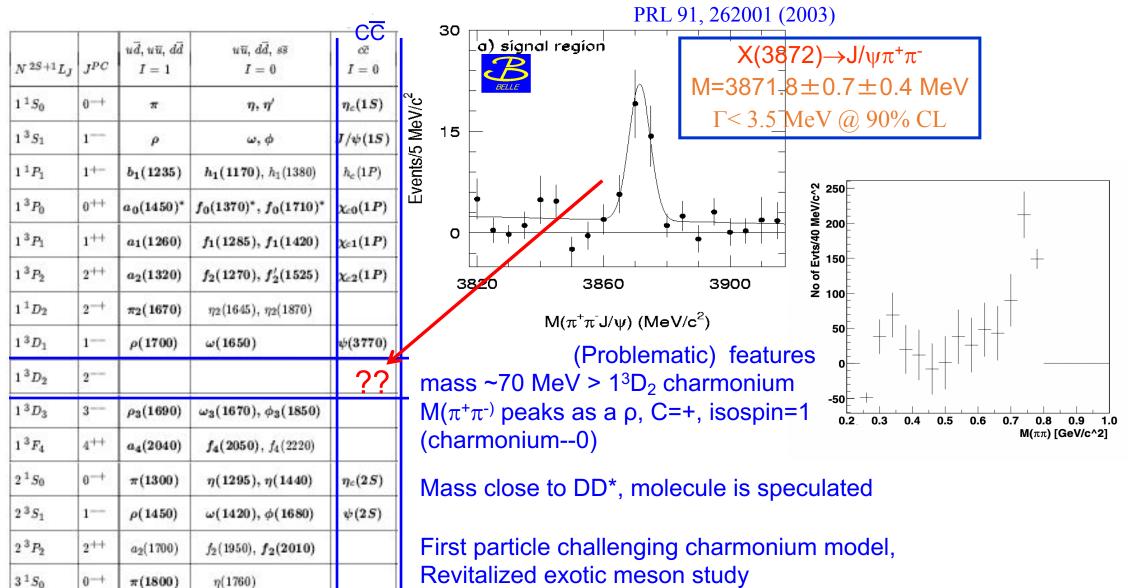
PRL 115 011803, PRL 111 032001



**CDF saw a hint in 1994**, unpublished BaBar saw a hint in 2003, unpublished

Both CDF and Babar spotted hints of X(3872) before its discovery!

## History: X(3872)—2003 (a slide from 2003)



*Heavy*—a factor to make us easier to identify "exotic"

## **Back to 2015**

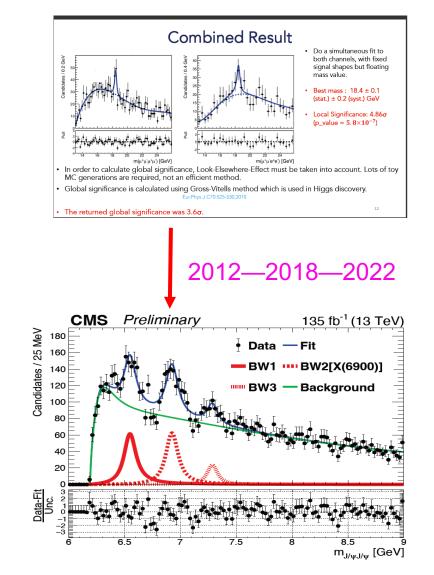
### Finally some progress in 2022

## **Prospects of New Physics Search below Z Mass in Multiple Lepton Final State**

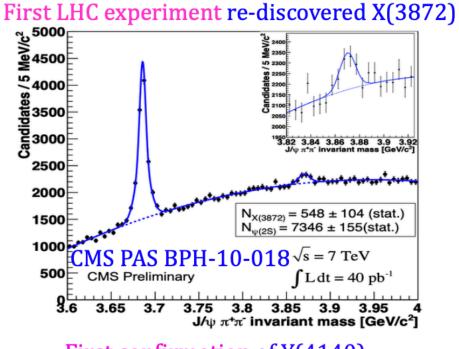
Kai Yi (University of Iowa) for the working group

Involved US Institutions: Iowa, Fermilab, Tennessee, Notre Dame, ...

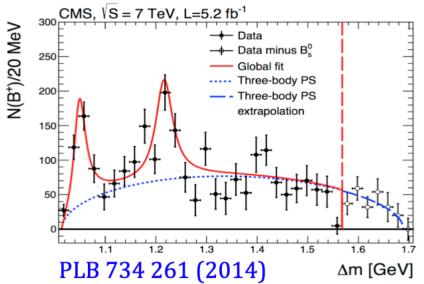
USCMS Annual Meeting, May 28, 2015, Cornell

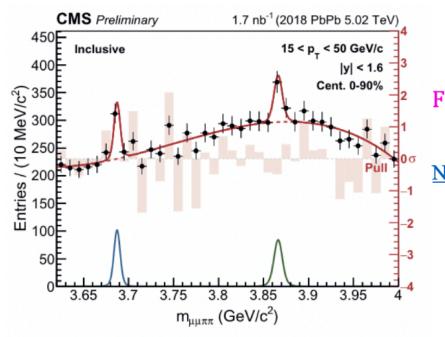


## **Selected CMS contributions to heavy exotic states**



### First confirmation of Y(4140)





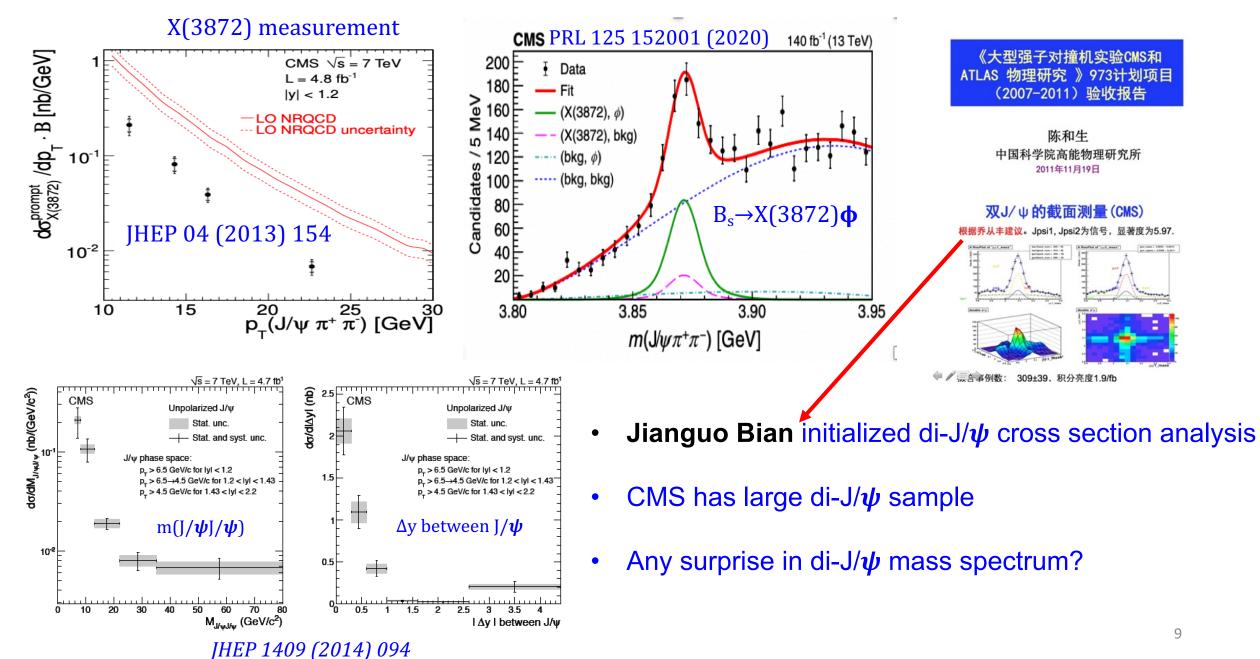
First X(3872) signal in PbPb

Nucl. Phys. Vol 1005 (2021)121781

CMS played the following leading roles

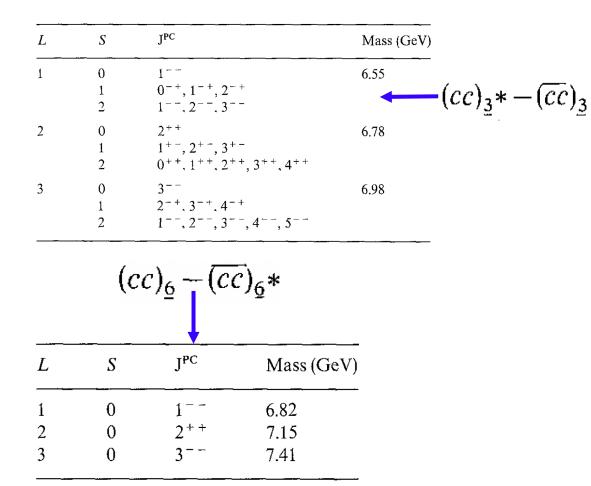
- First LHC experiment to see X(3872)
- First LHC experiment to see exotic hadron
- First LHC experiment to see X(3872) in PbPb data

## **Other selected CMS contributions to heavy exotic states**

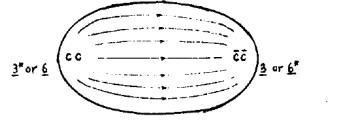


## **New Domain of Exotics: All-Heavy Tetra-quarks**

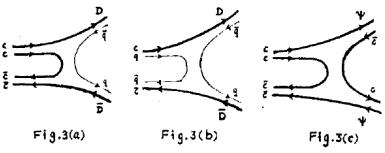
- First mention of 4c states at 6.2 GeV (1975): Prog. of Theo. Phys. Vol. 54, No. 2 (Just one year after the discovery of  $J/\psi$ )
- First calculation of 4c states (1981): Z. Phys. C 7 (1981) 317



### Linked by color electric flux in a bag







Possible P-wave to S-wave decays

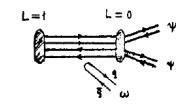
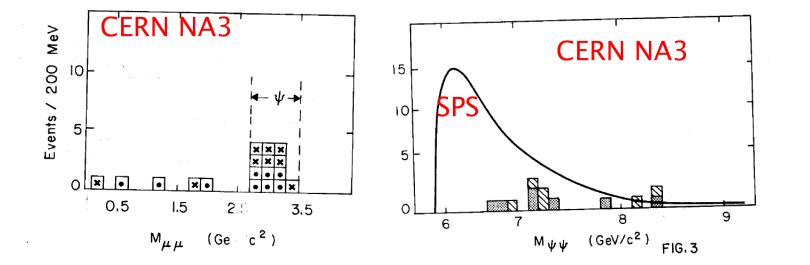


Fig.4

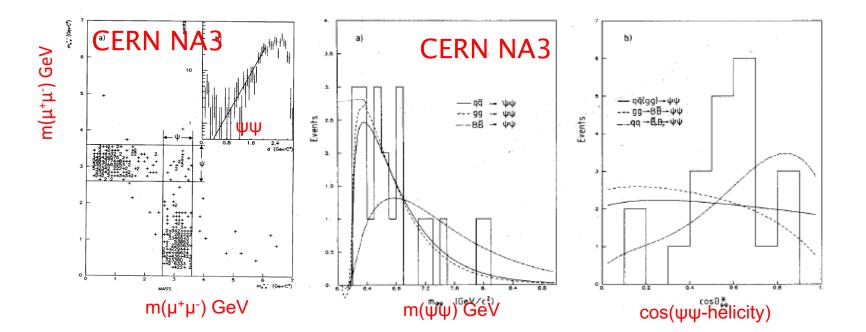
• A different exotic system comparing to exotic with light quarks

## $J/\psi J/\psi$ events—first evidence



### PLB114 (1982) 457

Was interoperated as 2<sup>++</sup> 4-quark state



#### PLB158 (1985) 85

11

11

## *Possible explanations of J/\psi-J/\psi states*

### 2<sup>++</sup> four-quark states, PRD29 (1984) 426

TABLE I. Parameters used in Eq. (8) to calculate the cross sections for vector-meson pair production. (+) and (-) denote two degenerate  $2^{++} Q^2 \overline{Q}^2$  states. Except in the case of JJ, we take  $4\pi/f_{I}^2=0.03$ , due to the fact that the  $2^{++} Q^2 \overline{Q}^2$  are expected to lie not far above the threshold.  $\alpha_s$  is determined from Eq. (11).

			Mj		
$V_1V_2$	$a_{V_1V_2}^i/a$	$b^{j}_{\alpha\beta} / \alpha_s \frac{a}{\sqrt{8}} \delta_{\alpha\beta}$	(GeV)	as	$m_1$
$J\phi^{(+)}$	-1/√6	$\frac{-1}{\sqrt{3}}\frac{4\pi}{f_{\perp}f_{\pm}}$	4.40	0.2	
$J\phi^{(-)}$	$1/\sqrt{12}$	$\left(\frac{2}{3}\right)^{1/2} \frac{4\pi}{f_L f_{\Phi}}$	4.40	0.2	
$J\omega^{(-)}$	1/12	$\left \frac{2}{3}\right ^{1/2} \frac{4\pi}{f_{\perp}f_{\omega}}$	4.05	0.2	
$\Upsilon J^{(+)}$	1/√6	$\frac{-1}{\sqrt{3}}\frac{4\pi}{f_{\rm X}f_{\rm I}}$	13.5	0.167	-
$\Upsilon J^{(-)}$	1/√12	$\left[\frac{2}{3}\right]^{1/2}\frac{4\pi}{f_{\rm X}f_{\rm Z}}$	13.5	0.167	
$B_c^* \overline{B}_c^{*(+)}$	$-1/\sqrt{6}$	$\frac{-1}{\sqrt{3}}\frac{4\pi}{f_{\rm T}f_{\rm I}}$	13.5	0.167	6.60
$B_c^* \overline{B}_c^{*(-)}$	1/√12	$\left[\frac{2}{3}\right]^{1/2}\frac{4\pi}{f_{\rm X}f_{\rm Z}}$	13.5	0.167	

There were other attempts

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## **New Domain of Exotics: All-Heavy Tetra-quarks**

(CC	cc) Phys. Rev. D	86, 034004 (2012)	
$0^{++'}$ :	$M=5.966{\rm GeV},$	$M-M_{\rm th}=-228.{\rm MeV},$	Below double J/ψ threshold
$1^{+-'}$ :	$M=6.051{\rm GeV},$	$M - M_{\rm th} = -142.  { m MeV},$	Search via J/ψμ⁺μ⁻, J/ψ <sup>*</sup>
$2^{++}:$	$M=6.223{\rm GeV},$	$M - M_{\rm th} = 29.5 {\rm MeV}.$	Above double J/ψ threshold
(bbo	cc)		Search via J/ψJ/ψ
$0^{++}a$ :	$M = 12.359 \mathrm{GeV},$	$M-M_{ m th}=-191.{ m MeV}$	
$0^{++}b$ :	$M=12.471{\rm GeV},$	$M - M_{\rm th} = -78.7 \mathrm{MeV},$	Below double B <sub>c</sub> threshold
$1^{+-}a:$	$M=12.424{\rm GeV},$	$M-M_{\rm th}=-126.{\rm MeV}$	J/ψY(1S) threshold
$1^{+-}b$ :	$M=12.488{\rm GeV},$	$M - M_{\rm th} = -62.5 \mathrm{MeV},$	?
$1^{++}:$	$M=12.485{\rm GeV},$	$M-M_{\rm th}=-64.9{\rm MeV},$	
$2^{++}:$	$M=12.566{\rm GeV},$	$M-M_{\rm th}=16.1{\rm MeV}.$	
(bbl	ob)		Above double B <sub>c</sub> threshold
$0^{++'}$ :	$M=18.754{\rm GeV},$	$M - M_{\rm th} = -544.  { m MeV},$	$J/\psi Y(1S)$ threshold
$1^{+-'}$ :	$M=18.808{\rm GeV},$	$M - M_{\rm th} = -490.  { m MeV},$	Search via the above two channels
$2^{++}$ :	$M=18.916{\rm GeV},$	$M - M_{\rm th} = -382. \mathrm{MeV}.$	Below double Y(1S) threshold
			Search via Y(1S)µ⁺µ⁻

Many recent theoretical studies on  $(c\overline{c}c\overline{c})$ ,  $(b\overline{b}b\overline{b})$ ,  $(b\overline{b}c\overline{c})$ : controversial on existence of bound states below  $\eta_b\eta_b$  threshold; consistent on existence of resonant states above  $\eta_b\eta_b$  threshold.

## Re-cap, mini summary of previous presentations

### • Feb 21, 2013 exotic state kick-off meeting—first proposed:

https://indico.cern.ch/getFile.py/access?contribId=4&resId=0&materialId=slides&confId=237108

### • March 13, 2013, B WG meeting—Showed VV mass distributions:

https://indico.cern.ch/getFile.py/access?contribId=3&resId=2&materialId=slides&confId=238055 https://indico.cern.ch/getFile.py/access?contribId=3&resId=0&materialId=slides&confId=238055

### • March 27, 2013, B WG meeting—2D fit result for $J/\psi J/\psi$ :

https://indico.cern.ch/getFile.py/access?contribId=2&resId=0&materialId=slides&confId=238057

### • April 3, 2013, B WG meeting—Follow-up on 2D fit:

https://indico.cern.ch/getFile.py/access?contribId=2&resId=0&materialId=slides&confId=238058

#### •July 24, 2013, B WG meeting—Tried µµee channel:

https://indico.cern.ch/getFile.py/access?contribId=2&resId=0&materiaIId=slides&confId=238058

#### • March 21, 2013, CMS Statistics Committee—Consulate search windows & LEE:

https://indico.cern.ch/getFile.py/access?contribId=0&resId=0&materialId=slides&confId=242367

& minute: https://twiki.cern.ch/twiki/bin/view/CMS/SCM20130321 proposed near threshold search windows [GeV]:

- J/ψ+J/ψ--[6.2, 9.0], J/ψ+Υ(1S)--[12.5, 14.5], Υ(1S)+Υ(1S)--[18.9,21.0]
- SC suggests to define two regions: near threshold region; beyond the near threshold region

January 17, 2014, X->VV meeting—Revealed some VV mass distributions: https://indico.cern.ch/event/297970/

....

### October 8, 2019, B PAG meeting—Re-start of J/ψJ/ψ analysis using Run II data

...

# $CMS J/\psi J/\psi$

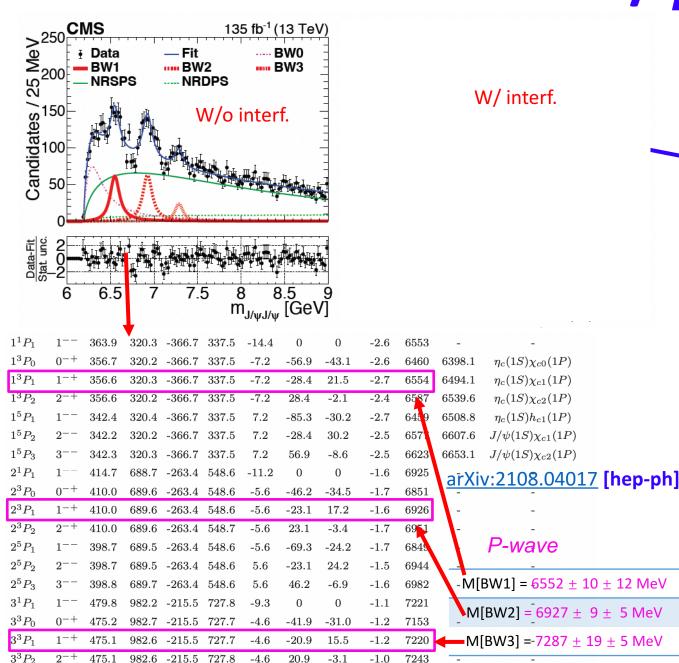
Table 1. Predictions of the masses (MeV) of S-wave fully heavy  $T_{4Q}(nS)$  tetraquarks. Only 0<sup>++</sup> and 2<sup>++</sup> are considered for  $T_{bc\bar{b}\bar{c}}$ . The uncertainty is from the coupling constant  $\alpha_s = 0.35 \pm 0.05$ .

#### Nucl. Phys. B 966 (2021) 115393

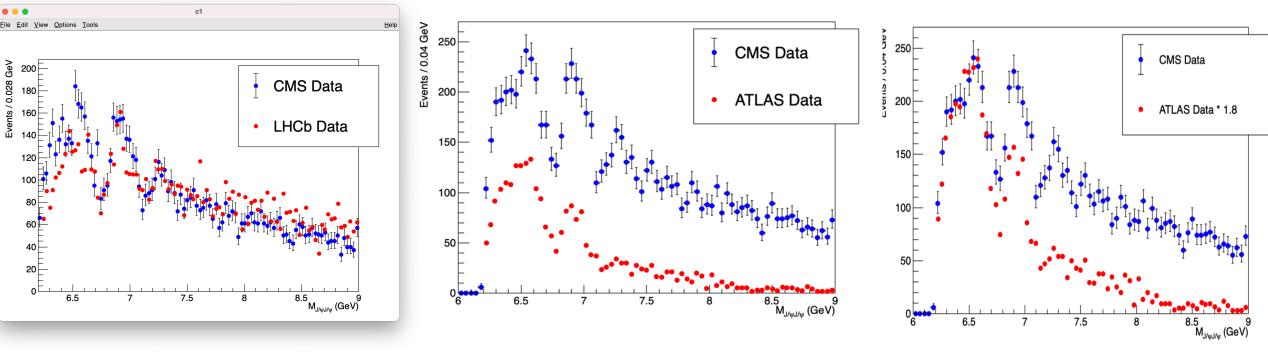
T <sub>4Q</sub> ( <i>nS</i> ) states	$J^{P}$	Mass(n=1)	Mass(n=2)	Mass(n=3)	Mass(n=4)
$T_{ccar{c}ar{c}ar{c}}$	0++	$6055\substack{+69\\-74}$	$6555^{+36}_{-37}$	$6883^{+27}_{-27}$	$7154^{+22}_{-22}$
	2++	$6090\substack{+62\\-66}$	$6566^{+34}_{-35}$	$6890\substack{+27\\-26}$	$7160^{+21}_{-22}$
$T_{ccar{c}ar{c}ar{c}}^\prime$	0++	$5984_{-67}^{+64}$	$6468 \scriptstyle \begin{array}{c} 35\\ 35\\ 35\\ \end{array}$	$6795^{+26}_{-26}$	$566^{+21}_{-22}$
$T_{bc\bar{b}\bar{c}}$	0++	$12387^{+109}_{-120}$	$12911^{+18}_{-31}$	$13200^{+35}_{-36}$	$13429\substack{+29\\-30}$
	2++	$12401\substack{+117\\-106}$	$12914\substack{+49\\-49}$	$13202^{+35}_{-36}$	$13430^{+29}_{-29}$
$T_{bcar{b}ar{c}}'$	0++	$12300\substack{+106\\-117}$	$12816\substack{+48 \\ -50}$	$13.04\substack{+35\\-35}$	$13333^{+29}_{-29}$
$T_{bbar{b}ar{b}}$	0++	$18475\substack{+151 \\ -169}$	$19073^{+59}_{-63}$	$19353\substack{+42\\-42}$	$19566\substack{+33\\-35}$
	2++	$18483\substack{+149 \\ -168}$	$19075\substack{+59\\-62}$	$19355^{+41}_{-43}$	$19567^{+33}_{-35}$
$T'_{bb\bar{b}\bar{b}}$	0++	$18383\substack{+149 \\ -167}$	$18976\substack{+59\\-62}$	$19356\substack{+43\\-42}$	$19468\substack{+34\\-34}$

S-wave

- Radial excited p-wave states like  $J/\psi$  series?
- Or Radial excited S-wave states?
- Important next step: measure J<sup>PC</sup>
- Interf. effect also indicate same J<sup>PC</sup>
- Natural question: what about YY final state?



# $J/\psi J/\psi$ comparison with LHCb & ATLAS



- CMS vs LHCb comparisons:
  - 135/9 **≈** 15X (int. lum.)
  - $(5/3)^4 \approx 8X$  (muon acceptance)
  - Higher muon p<sub>T</sub> ( >3.5 or 2.0 GeV vs >0.6 GeV)
  - Similar number of final events
  - 2X yield @CMS for X(6900)

- CMS vs ATLAS comparisons:
  - ATLAS is 1/3 –1/2 of CMS data (trigger?)
  - ATLAS used dR cut—remove high mass events
  - ATLAS has slightly worse resolution

## CMS has some advantage

# **Exotic zoo**

X(7300)

X(6900)

X(6600)

**J**<sup>PC</sup>=?<sup>+</sup>

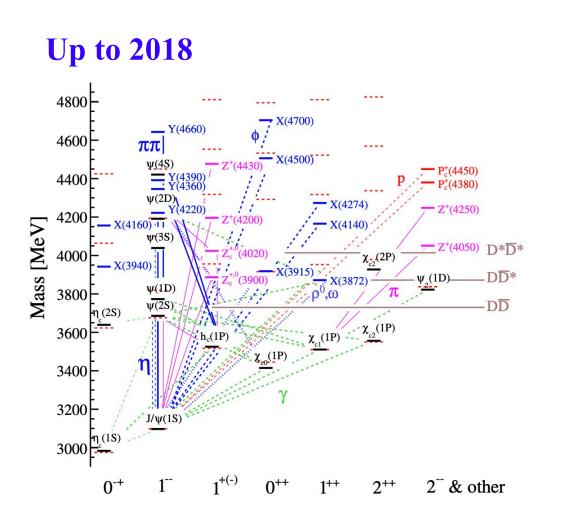


Many theoretical studies on  $(c\overline{c}c\overline{c})$ ,  $(b\overline{b}b\overline{b})$ ,  $(b\overline{b}c\overline{c})$ :

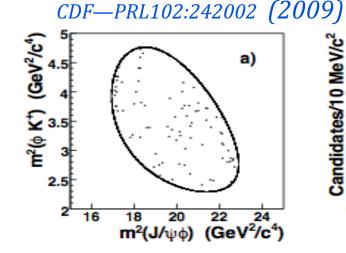
controversial on bound states below  $\eta_b \eta_b$  threshold

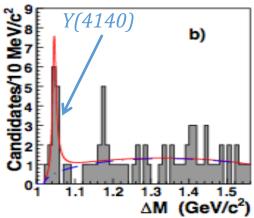
consistent on resonant states above  $\eta_{\rm b}\eta_{\rm b}$  threshold

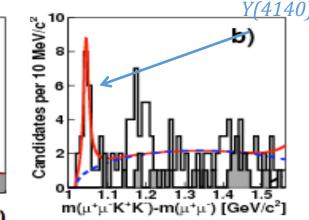
Expect similar structures in b sector



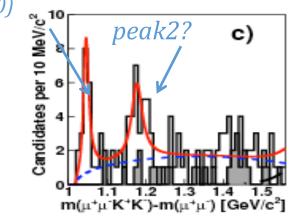
## What are they?



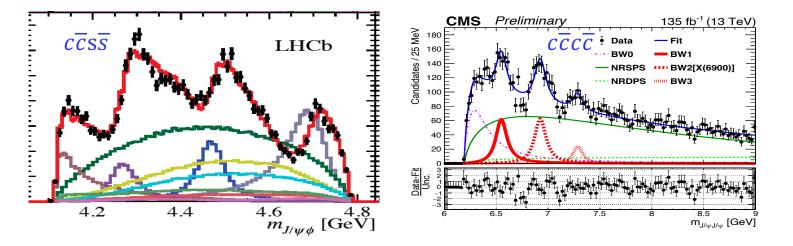


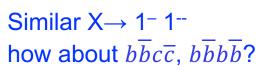


Mod.Phys.Lett. A32 (2017) no.26, 1750139



#### PRL 127, 082001 (2001)

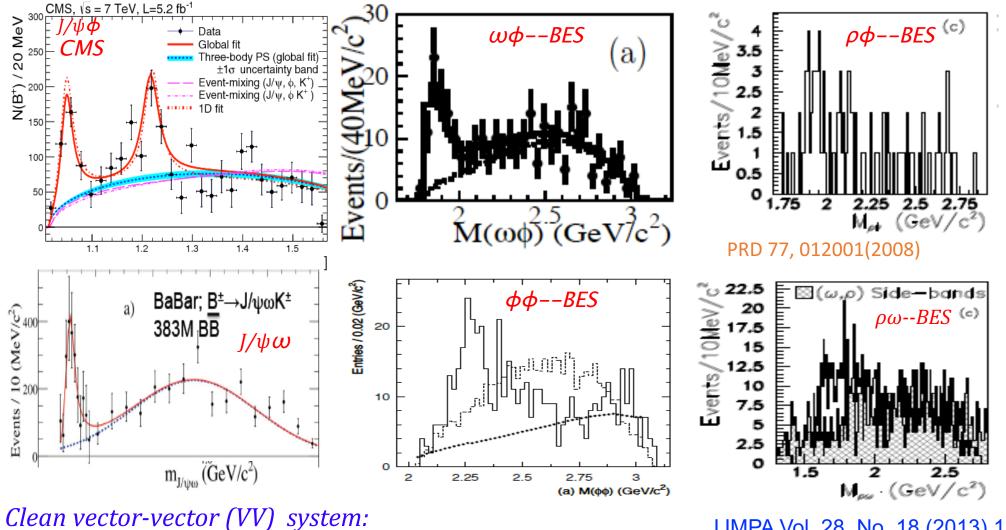




Belle II can contribute to  $c\overline{c}s\overline{s}$ 

"It will also be interesting to search for vector–vector structures composed entirely of c and b quarks near threshold because they may offer simpler systems to model theoretically." IJMPA Vol. 28, No. 18 (2013) 1330020

## **Motivation--Near Threshold puzzle**

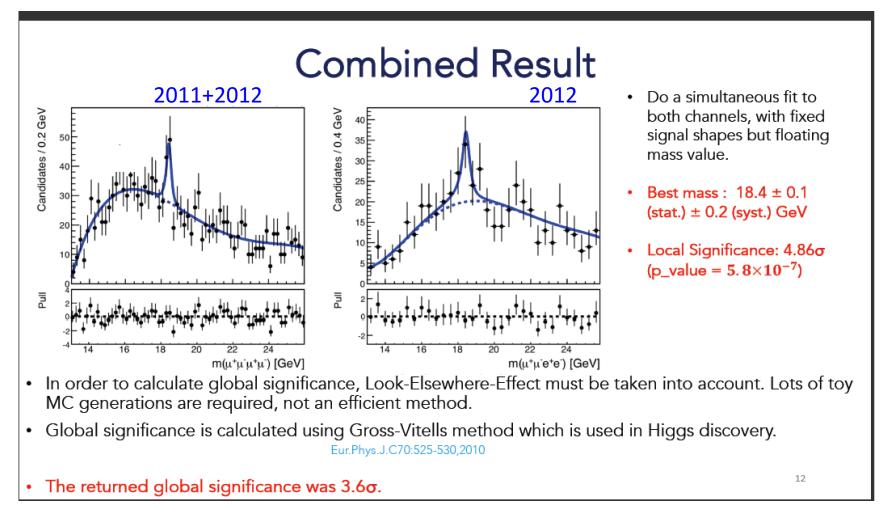


IJMPA Vol. 28, No. 18 (2013) 1330020

--excesses when both V has no isospin

--not clear when one V has isospin extend to other VV system, where V is composed of heavy quark such as  $J/\psi J/\psi$  and YY?

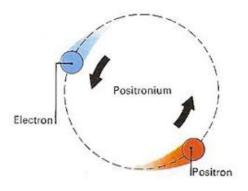
# Anything below $\eta_b \eta_b$ or Y(1s)Y(1S) threshold?



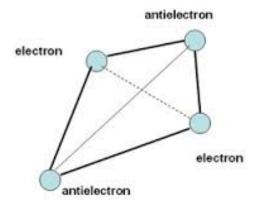
<u>Taken from: http://meetings.aps.org/Meeting/APR18/Session/U09.6</u> This can be studied in LHC experiments, and future circular/linear e<sup>+</sup>e<sup>-</sup> colliders If true, can be a breakthrough in QCD , or even something more exciting

# Something analogue to positronium molecule

### Positronium (1951)



### positronium molecule (2007)

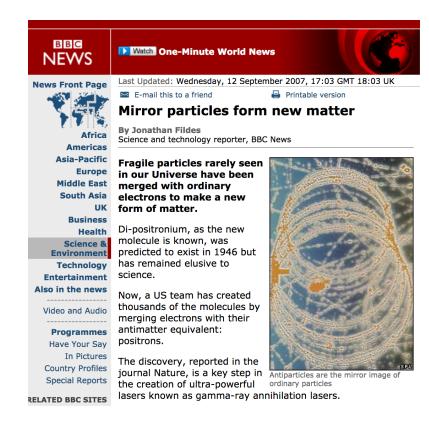


### Nature letter



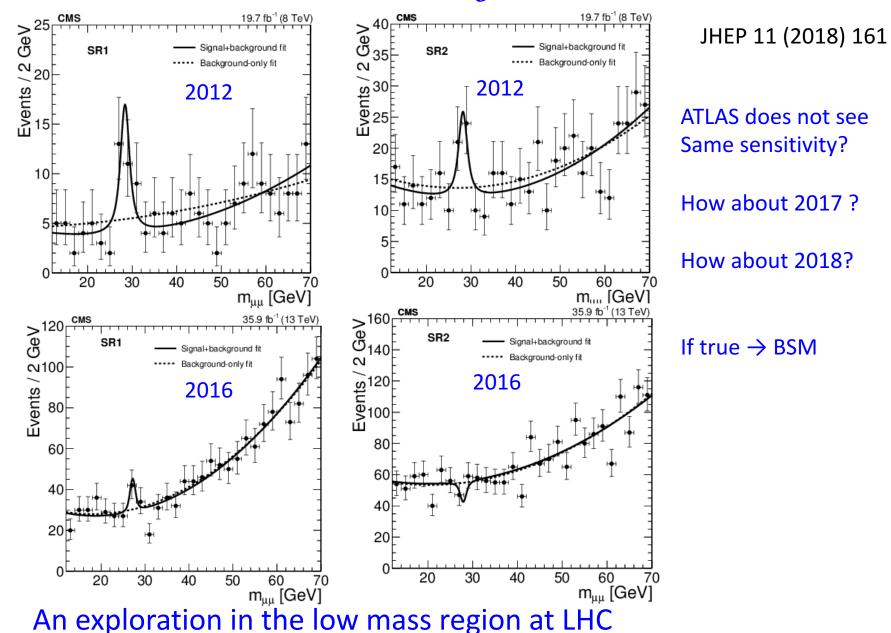
#### The production of molecular positronium

D. B. Cassidy<sup>1</sup> & A. P. Mills Jr<sup>1</sup>



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## **Dimuon result from CMS**



Same sensitivity? How about 2017? How about 2018?

If true  $\rightarrow$  BSM

## never fully explored (GeVs-Z mass) Multiple-lepton final states

### http://arxiv.org/abs/hep-ph/0312114

Experiment	$E_{cm}$ [GeV]
* ADONE-MEA	2.23
BEPC-BES	2.0 - 4.8
BEPC-BES	2.6 - 5.0
* SPEAR-SMAG <sup>†</sup>	2.4 - 5.0
* SPEAR-SMAG+LGW	3.598 - 3.886
SPEAR-Crystal Ball	3.670 - 4.496
SPEAR-Crystal Ball	5.0 - 7.4
SLAC-MARK-II	3.670 - 3.872
DORIS-DASP	3.6025 - 5.1950
DORIS-II-LENA	7.440 - 9.415
* DORIS-II-ARGUS	9.360
DORIS-II-Crystal Ball	9.39 - 9.46
* DORIS-II-DHHM	9.45 - 10.04
DORIS-II-DASP	9.51
VEPP-4-MD1	7.30 - 10.29
CESR-CUSB	10.43 - 11.09
CESR-CLEO	10.49
CESR-CLEO <sup>††</sup>	10.60 - 11.20
CESR-CLEO II	10.52
DORIS/PETRA-PLUTO	3.6 - 30.8
* PETRA-TASSO	12.0 - 41.4
* PETRA-TASSO	12.00 - 31.25
* PETRA-TASSO	14.03 - 43.70
PETRA-TASSO	41.45 - 44.20
PETRA-JADE	12.00 - 46.47
PETRA-MARK-J	12.00 - 46.47
* PETRA-MARK-J	31.57
* PETRA-MARK-J	34.85
PETRA-CELLO	14.0 - 46.6
PEP-MAC	29.0
* PEP-MARK-II	29.0
* TRISTAN-AMY	50.0 - 61.4
* TRISTAN-TOPAZ	50.0 - 61.4
* TRISTAN-TOPAZ	57.77
* TRISTAN-TOPAZ	57.37 - 59.84
* TRISTAN-VENUS	50.0 - 52.0
* TRISTAN-VENUS	63.6 - 64.0

A) Not enough energy (associated production)

### B) Not enough data

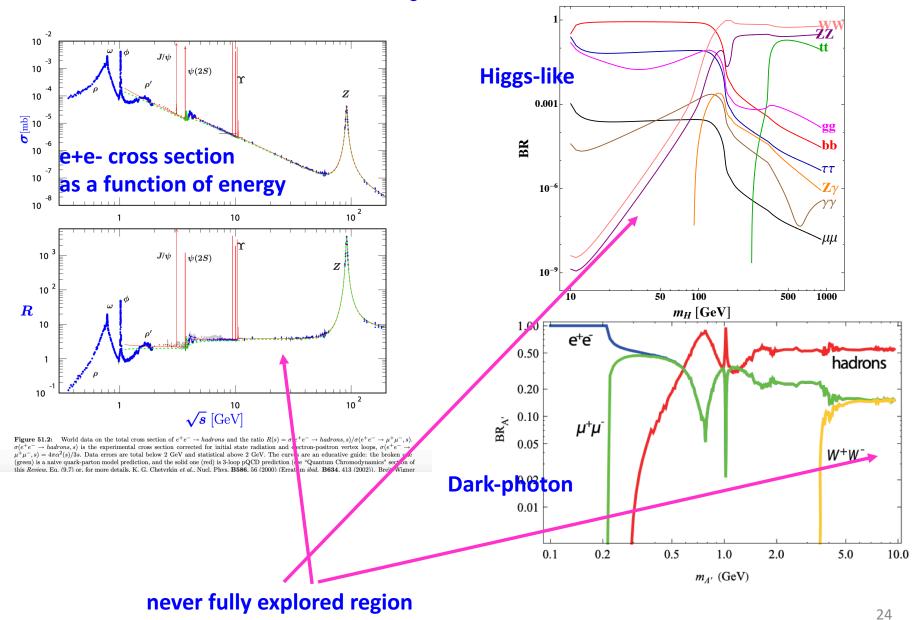
C) Opportunity comes with LHC Enough energy and luminosity

 D) Rich physics motivation + curiosity, BSM—new scalar, Higgs-like,...
 QCD—new dynamics, 4b states,...
 anything else unexpected?

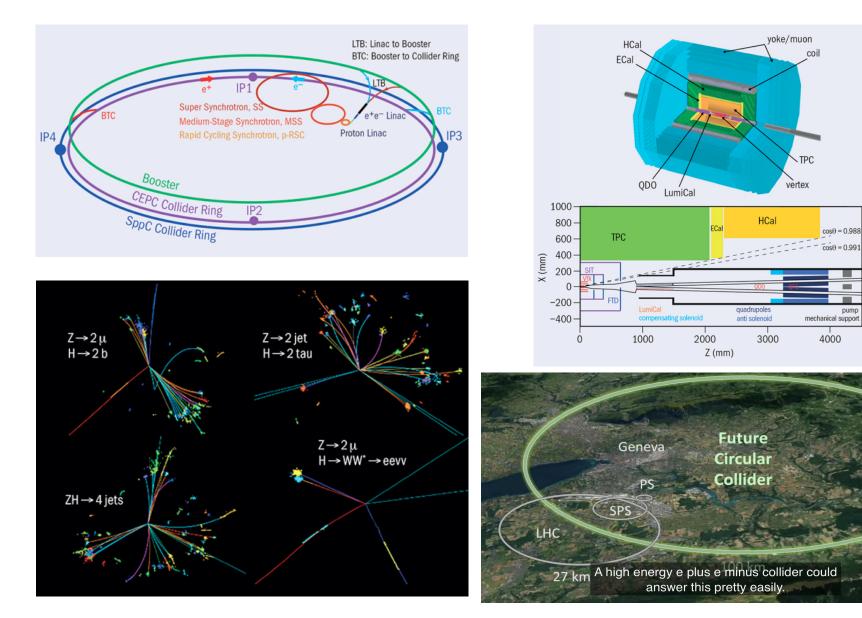
m<sub>z</sub>=90 GeV

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## **Motivation—Beyond Standard Model**



# **CEPC/FCC**



# **CEPC/FCC**

### LHC

•

• Double  $J/\psi$ : observation of multiple peaks (4c)

directly produced by pp

CEPC/FCC

- Associated with Z/gamma
- Produced by two photon process

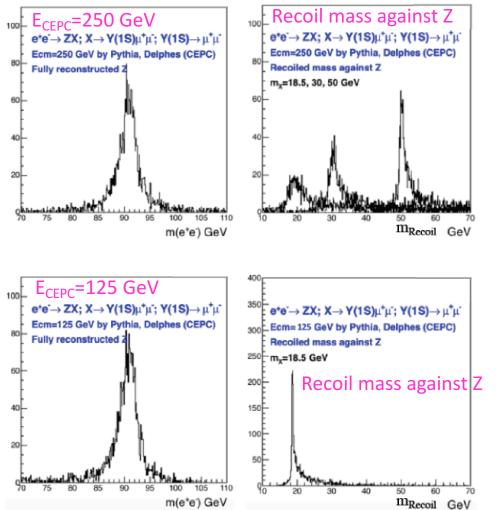
Double Upsilon: hints at 18 GeV

cannot be directly produced by ee (1--)

• Have been looking for theorists to collaborate on various productions

### IJMA, vol.33, 1850224

## **Recoil masses at CEPC**



### IJMA, vol.33, 1850224

Simulated using Delphes CEPC detector with different collision energy values.

An unique approach at CEPC  $e^+e^-$  collider

It is sensitive to all final states

It is useful to measure BFs

Fig. 2. The fully reconstructed Z mass and its recoiled mass against Z particle at the CEPC with different collision energy by assuming X particle mass as 18.5, 30 and 50 GeV produced in the process of  $e^+e^- \rightarrow ZX$ ;  $X \rightarrow Y(1S)\mu^+\mu^-$ ;  $Y(1S) \rightarrow \mu^+\mu^-$ . These events are simulated by Delphes with CEPC configuration.

## Other $\tau^{+}\tau$ final state at CEPC

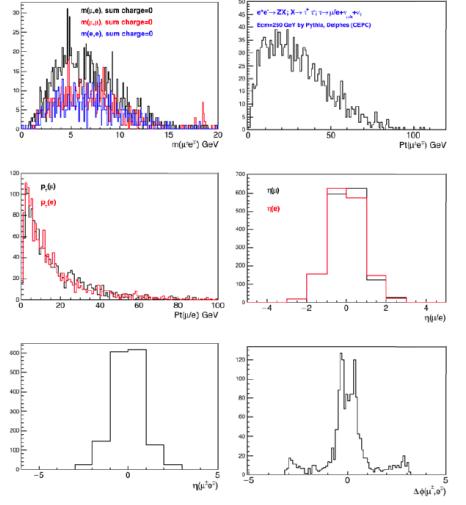


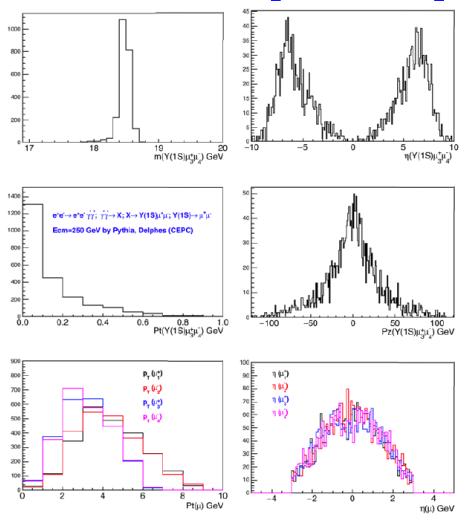
Fig. 7. The features of the  $\mu^{\pm}e^{\mp}$   $(\tau^{\pm}\tau^{\mp})$  system in the  $e^+e^- \rightarrow ZX$ ;  $X \rightarrow \tau^{\pm}\tau^{\mp}$ ;  $\tau^{\pm} \rightarrow \ell^{\pm} + \text{anything-else}$ ,  $\tau^{\mp} \rightarrow \ell^{\mp} + \text{anything-else}$ , where  $\ell = \mu$ , e process at the CEPC: (top left) the  $\mu^{\pm}e^{\mp}/\mu^{\pm}\mu^{\mp}/e^{\pm}e^{\mp}$  mass distributions; (top right) the  $p_T$  distributions of  $\mu^{\pm}e^{\mp}$ ; (middle left) the  $p_T$  distribution of muon and electron; (middle right) the  $\eta$  distribution of muon and electron; (bottom left) the  $\eta$  distribution of  $\mu^{\pm}e^{\mp}$ ; (bottom right) the  $\Delta\phi$  distribution between muon and electron. These events are simulated by Delphes with CEPC configuration.

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Simulated using Delphes CEPC detector

Another approach for  $\tau^+\tau^-$  final state through opposite u e channel at CEPC e<sup>+</sup>e<sup>-</sup> collider

## Two photon process at CEPC



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Simulated using Delphes CEPC detector

Another unique approach to study multiple lepton final state at CEPC e<sup>+</sup>e<sup>-</sup> collider

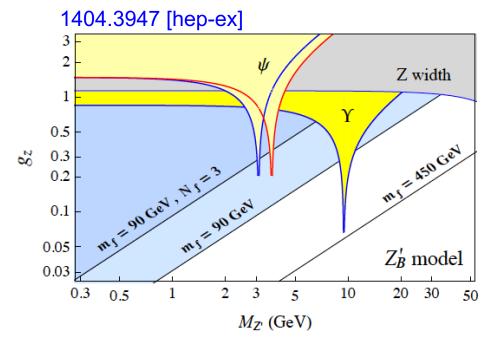
Fig. 8. The features of the four-muon system in the  $e^+e^- \rightarrow e^+e^-X$ ;  $X \rightarrow Y(1S)\mu^+\mu^-$ ;  $Y(1S) \rightarrow \mu^+\mu^-$  process at the CEPC: (top left) the invariant mass of the four muons; (top right) the  $\eta$  distribution of the four muons; (middle left)  $p_T$  of the four muons; (middle right)  $p_Z$  of the four muons; (bottom left)  $p_T$  of each muon; (bottom right)  $\eta$  of each muon. These events are simulated by Delphes with CEPC configuration.

# **Summary**

- CMS found a potential family of structures X(6600) X(6900), X(7200)
  - Confirms the existence of X(6900) observed by LHCb
  - which are candidates for all-charm tetra-quarks!
- More data/knowledge needed to understand nature of near threshold region
- All-heavy quark exotic structures offer system easier to understand
- A new window to understand strong interaction
- May extend for BSM in multiple lepton final state
- CEPC/FCC offers new opportunities to study heavy exotic hadrons, even BSM

Backup

# **BSM—light Z', light Higgs**



For  $g_z < 1.0$  case, Light Z' mass region between upsilon and 50 GeV is not constrained at all.

Main decay channel is jj, but difficult to search at hadron colliders.

This mass region is not explored before, can we explore now?

FIG. 1. Limits in the gauge coupling versus mass plane for  $Z'_B$ . Values of  $g_z$  above the straight lines are excluded by the anomaly cancellation conditions in conjunction with collider searches for new fermions, for  $N_f = 1$  or 3,  $m_f > 90$ GeV, and for  $N_f = 1$ ,  $m_f > 450$  GeV. The top regions are excluded by quarkonium and hadronic Z decays.

How?

How about possible light Higgs?

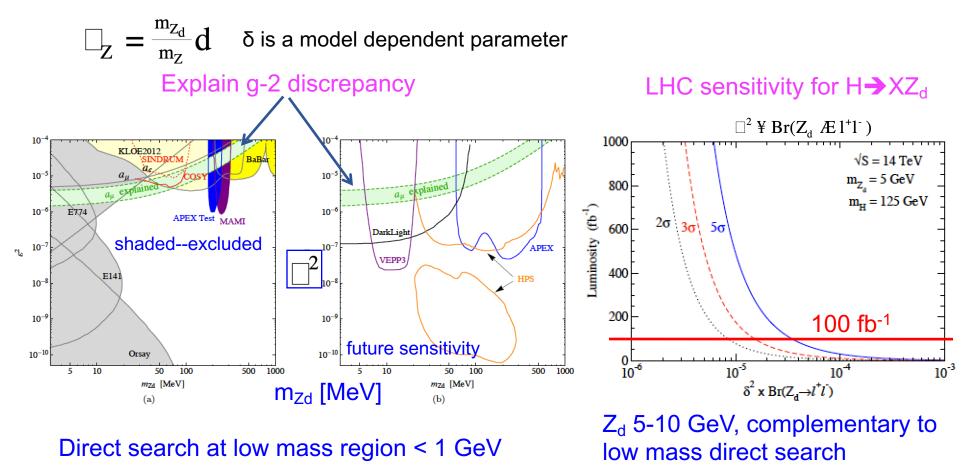
### g<sub>z</sub>—gauge coupling

## **BSM—dark sector**

• Physics Beyond Standard Model, i.e., a new particle Z<sub>d</sub> Phys. Rev. D 88, 015022 (2013)

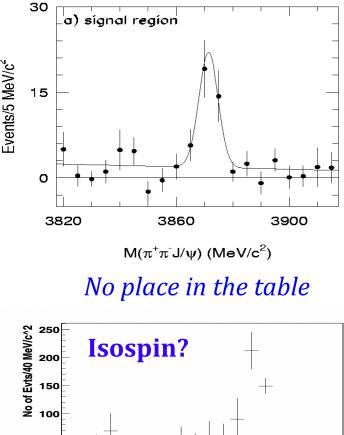
- ---Associated with dark sector including dark matter, no direct coupling to SM particles
- ---Coupled to Higgs via mass-mixing, or new heavy fermion loops

---Higgs  $\rightarrow$  XZ<sub>d</sub>, X=Z, Z<sub>d</sub>, or  $\gamma$ , four-lepton final state, u<sup>+</sup>u<sup>-</sup>u<sup>+</sup>u<sup>-</sup>, e<sup>+</sup>e<sup>-</sup>u<sup>+</sup>u<sup>-</sup>



## **Charmonium States**

	Quantum numbers		Name	Mass (MeV/c <sup>2</sup> )	width(MeV)		
<u>Notation</u> :	Ν	L	JPC	$N^{2S+1}L_J$			
<sup>2S+1</sup> [L] <sub>J</sub>	1	0	0-+	$1^{1}S_{0}$	η <sub>c</sub> (1S)	$2980.4 \pm 1.2$	$26.7 \pm 3$
L=S,P,D (0,1,2) (No cand. <i>with</i>	1	0	1	$1^{3}S_{1}$	J/ψ	$3096.916 \pm 0.01$ 1	$93.2 \pm 0.02$ × 10 <sup>-3</sup>
L>=3)	1	1	$0^{++}$	$1^{3}P_{0}$	χ <sub>c0</sub> (1P)	$3414.75 \pm 0.31$	$10.2 \pm 0.7$
$\mathbf{J} = \mathbf{L} + \mathbf{S}$	1	1	1++	$1^{3}P_{1}$	χ <sub>c1</sub> (1P)	$3510.66 \pm 0.07$	$0.89 \pm 0.05$
S(qq) = 0 or 1	-1	1	2++	$1^{3}P_{2}$	$\chi_{c2}(1P)$	$3556.20 \pm 0.09$	$2.03 \pm 0.12$
Parity: $P = (-1)^{L+1}$	1	1	1+-	$1^{1}P_{1}$	h <sub>c</sub> (1P)	$3525.93 \pm 0.27$	<1
Charge conjugation	1	2	1	$1^{3}D_{1}$	ψ(3770)	$3772.92 \pm 0.35$	$27.3 \pm 1.0$
eigen <i>vales:</i> C=(-1) <sup>L+S</sup>	2	0	0-+	$2^{1}S_{0}$	η <sub>c</sub> (2S)	$3637 \pm 4$	14±7
N: Radial	2	0	1	$2^{3}S_{1}$	ψ(2S)	$3686.09 \pm 0.04$	$317 \pm 9 \times 10^{-3}$
Quantum	2	1	2++	$2^{3}P_{2}$	$\chi_{c2}(2P)$	$3929 \pm 5$	29±10
Numbers	3	0	1	$3^{3}S_{1}$	ψ(4040)	$4039 \pm 1$	$80 \pm 10$
	2	2	1	$2^{3}D_{1}$	ψ(4160)	4153±3	$103 \pm 8$
	4	0	1	$4^{3}S_{1}$	ψ(4415)	$4421 \pm 4$	$62 \pm 20$



 $\frac{1}{9} \frac{1}{200} \frac{1}{9} \frac{1}{9} \frac{1}{150} \frac{1}{9} \frac{1}{9} \frac{1}{150} \frac{1}{9} \frac{1}{9} \frac{1}{150} \frac{1}{9} \frac{1$ 

*Heavy*—a factor to make us easier to identify "exotic"