

# Study of the Higgs boson CP property in LHC and CEPC

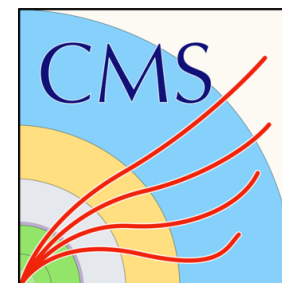
— *An Experimentalist Overview*

IAS Program on High Energy Physics, HKUST, 12-16, Feb, 2023

Bo Liu  
IHEP, CAS

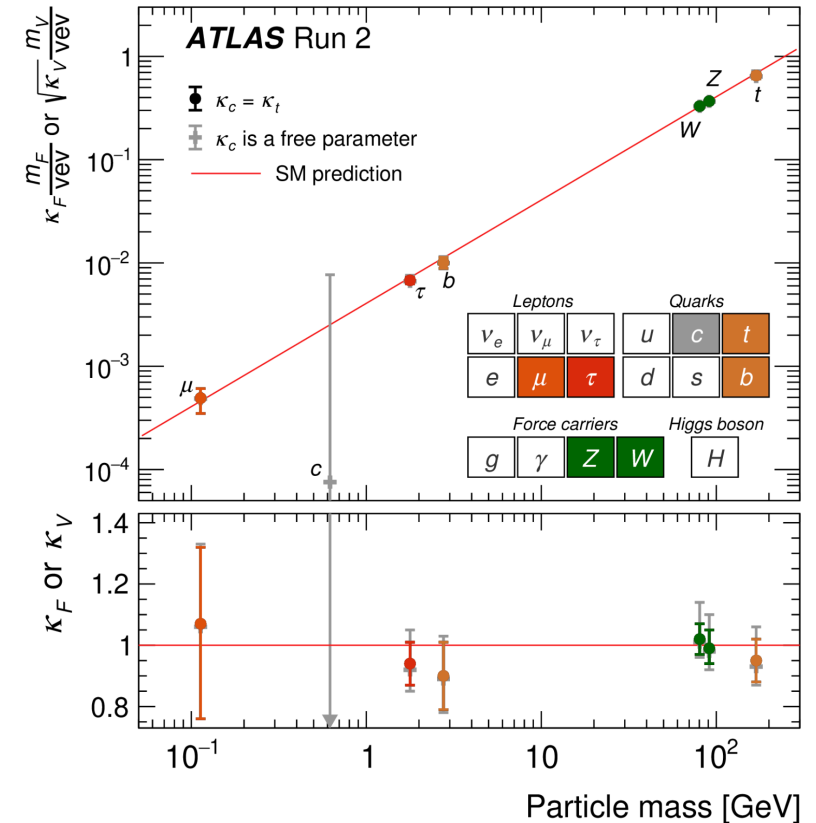
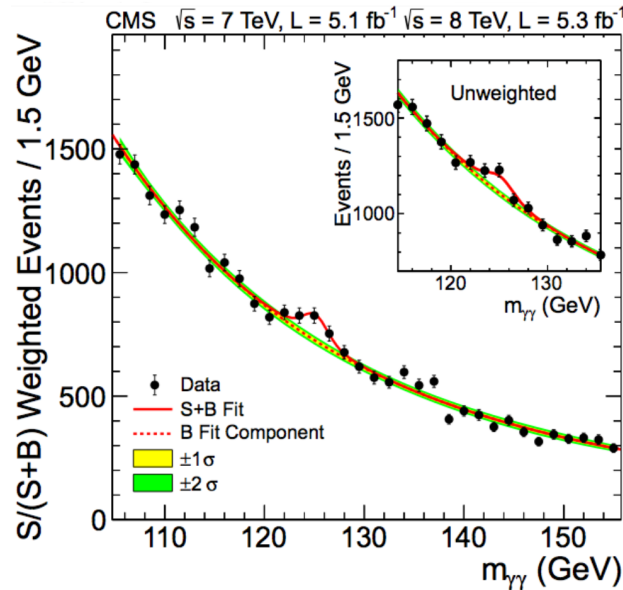
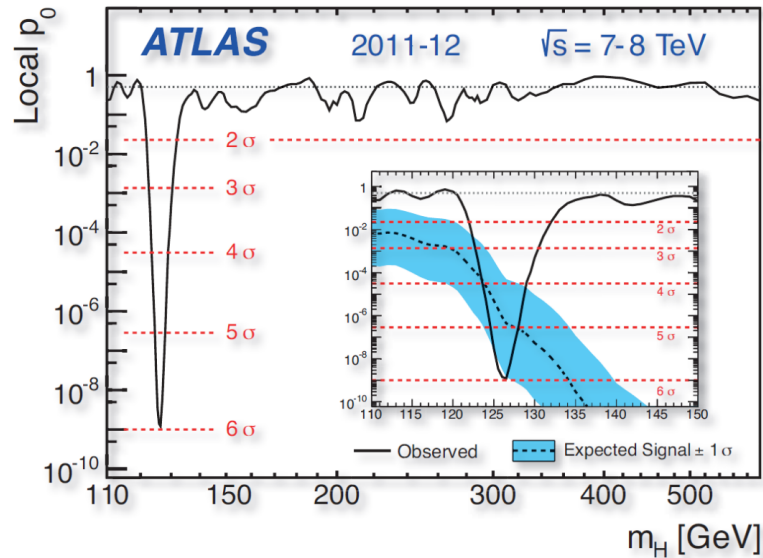
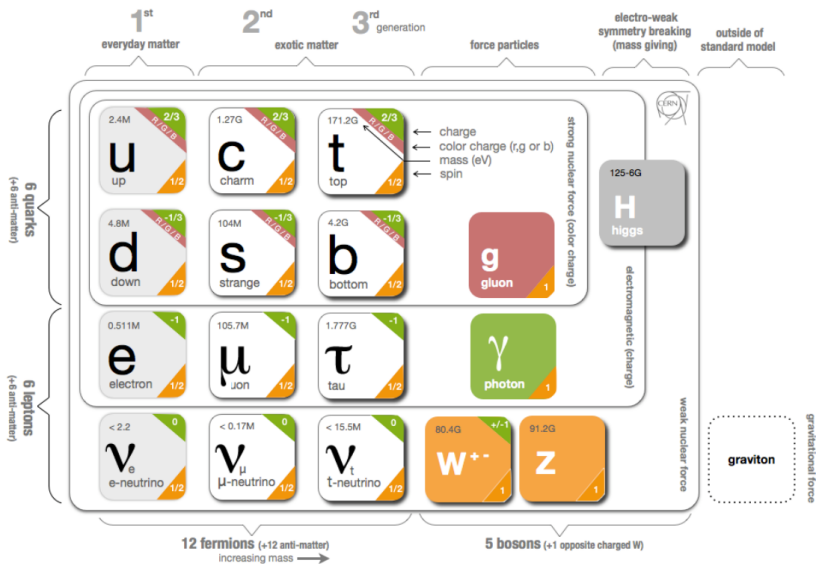


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*Institute of High Energy Physics*  
*Chinese Academy of Sciences*



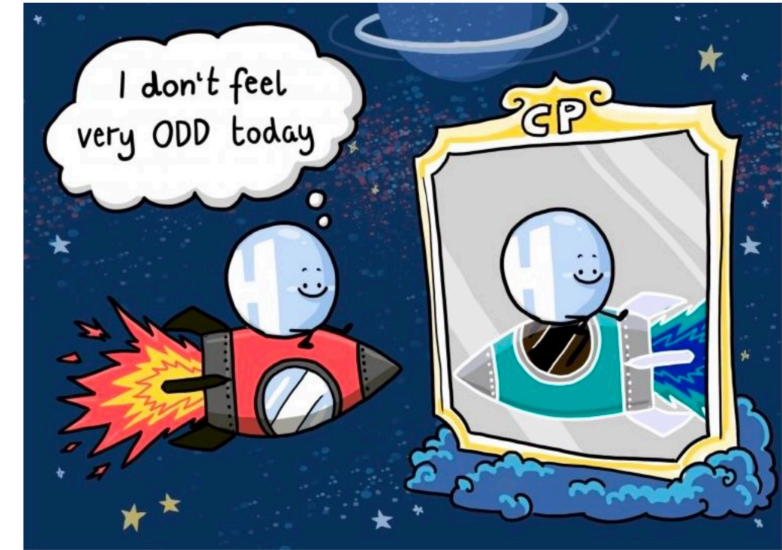
# The Discovery of the Higgs boson

- The SM is a successful model of the particle physics
- The Higgs boson play the unique role in the SM of giving mass to other particles via EW SSB
- Was discovered by ATLAS and CMS in 2012 in bosonic channels



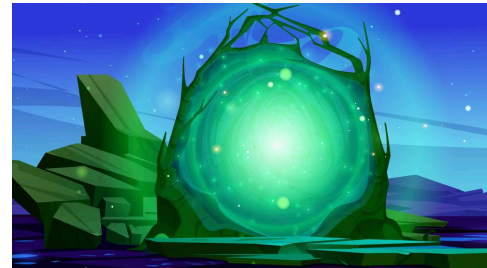
# CP property of the Higgs boson

- Determining the CP structure is important in the High Energy Physics
- Key component for Sakharov condition to explain matter-antimatter asymmetry
  - ✓ Baryon number violation
  - ✓ C and CP violation
  - ✓ Interactions out of thermal equilibrium
- Need to find new source of CPV beside the CP phase in CKM which is not enough for matter-antimatter asymmetry

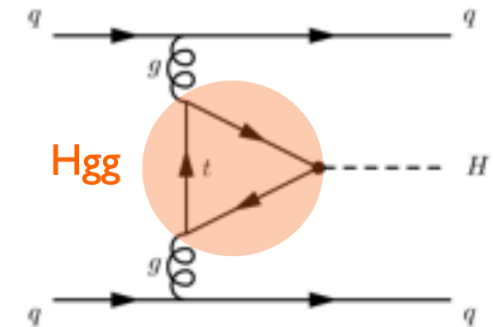
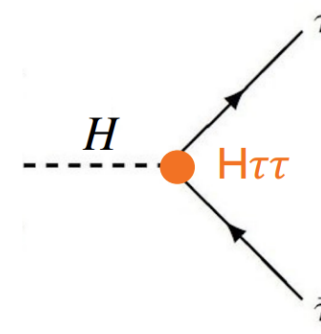
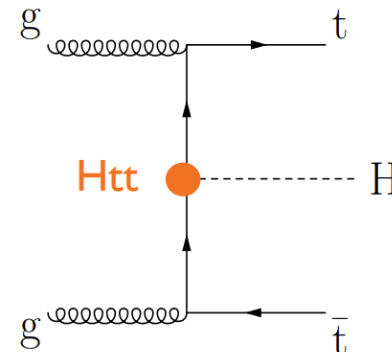
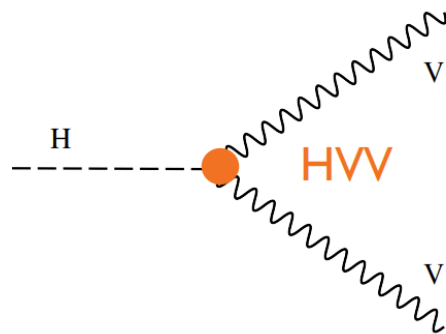
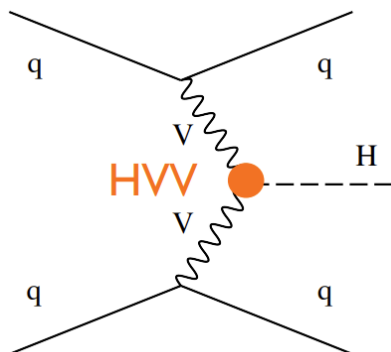


(image: DESY/designdoppel)



## The Higgs boson could be a good portal





- In the SM, the Higgs boson is CP-even
- No strong constraint to exclude CP-odd contribution
  - ✓ Those new CP-odd component could be new scalars or new interactions



# Recent ATLAS and CMS results

	 <b>ATLAS</b>	<b>CMS</b> 
$H \rightarrow ZZ^* \rightarrow \ell\ell\ell\ell$	<a href="#">Eur. Phys. J. C 80 (2020) 957</a> [139 fb <sup>-1</sup> , measured cross-section reinterpretation]	<a href="#">Phys. Rev. D 104 (2021) 052004</a> [137 fb <sup>-1</sup> , anomalous coupling using MELA discriminator] <a href="#">arXiv:2202.06923</a> [Offshell measurement]
$H \rightarrow WW^* \rightarrow \ell\nu\ell\nu$	<a href="#">Eur. Phys. J. C 82 (2022) 622</a> [36.1 fb <sup>-1</sup> ]	<a href="#">arXiv:2208.02686</a> [138 fb <sup>-1</sup> , multi-lepton]
$H \rightarrow \tau\tau$	<a href="#">arXiv:2212.05833</a> [139 fb <sup>-1</sup> , Hff coupling] <a href="#">Phys. Lett. B 805 (2020) 135426</a> [36.1 fb <sup>-1</sup> , VBF]	<a href="#">arXiv:2205.05120</a> [138 fb <sup>-1</sup> , MELA discriminator] <a href="#">JHEP 06 (2022) 012</a> [138 fb <sup>-1</sup> , Hff coupling]
$H \rightarrow \gamma\gamma$	<a href="#">arXiv:2208.02338</a> [139 fb <sup>-1</sup> , VBF] <a href="#">Phys. Rev. Lett. 125 (2020) 061802</a> [139 fb <sup>-1</sup> , ttH] <a href="#">JHEP 08 (2022) 027</a> [139 fb <sup>-1</sup> , measured cross section reinterpretation]	<a href="#">Phys. Rev. Lett. 125 (2020) 061801</a> [137 fb <sup>-1</sup> , ttH]
$H \rightarrow bb$	<a href="#">ATLAS-CONF-2022-016</a> [139 fb <sup>-1</sup> , ttH/tH]	

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Strong connection between experimentalists and theorists for Higgs boson CP studies

# Constrain CP-odd with differential measurements

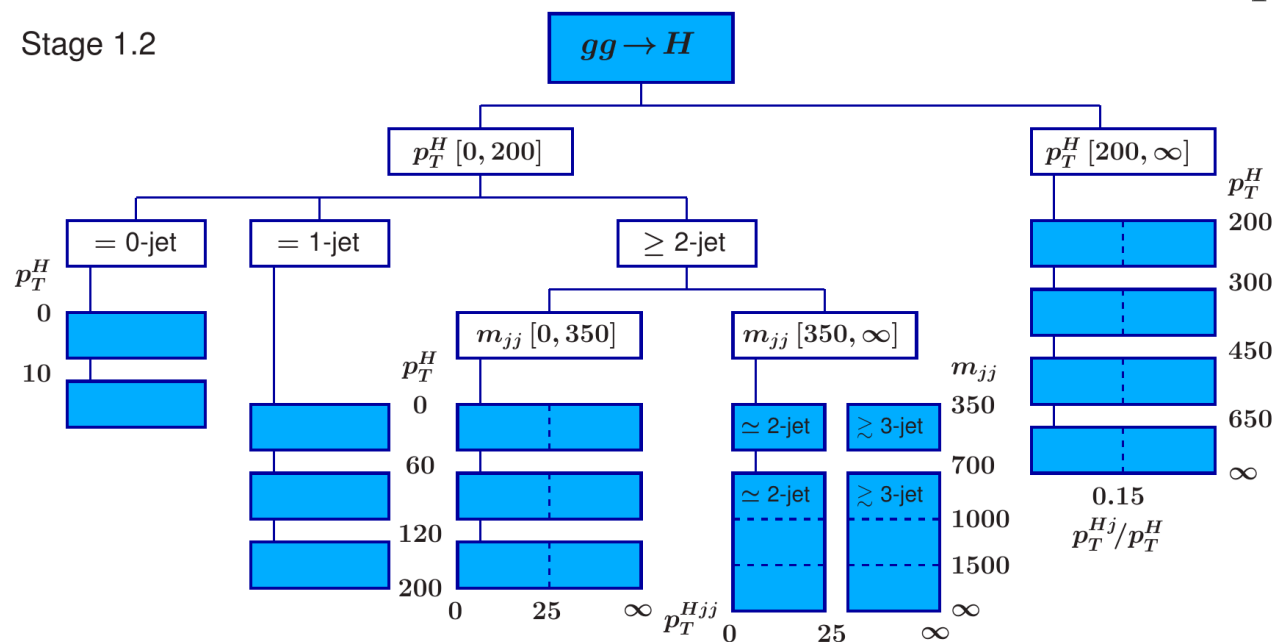


- Differential/STXS cross-section measurements could be interpreted in terms of CP-odd contributions
- SMEFT approach used for both  $H \rightarrow \gamma\gamma$  and  $H \rightarrow ZZ$  results

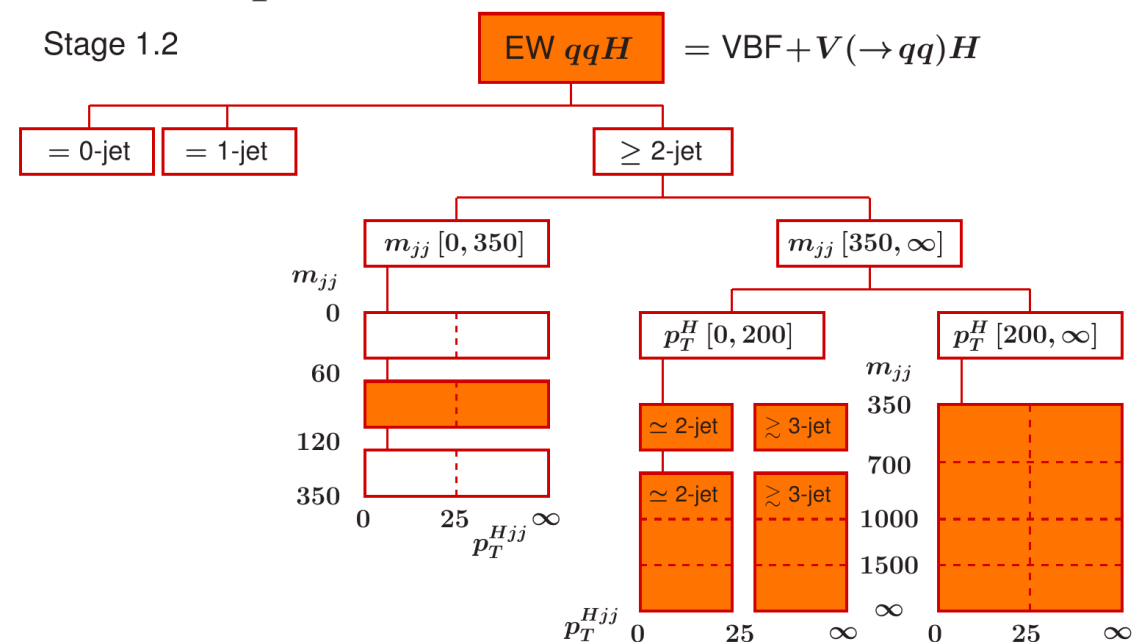
$$\mathcal{L}_{\text{eff}}^{\text{SMEFT}} \supset c_{HG} O'_g + c_{HW} O'_{HW} + c_{HB} O'_{HB} + c_{HWB} O'_{HWB} \\ + c_{H\tilde{G}} \tilde{O}'_g + c_{H\tilde{W}} \tilde{O}'_{HW} + c_{H\tilde{B}} \tilde{O}'_{HB} + c_{H\tilde{W}B} \tilde{O}'_{HWB}$$

## Simplified Template Cross Section scheme

Stage 1.2



Stage 1.2

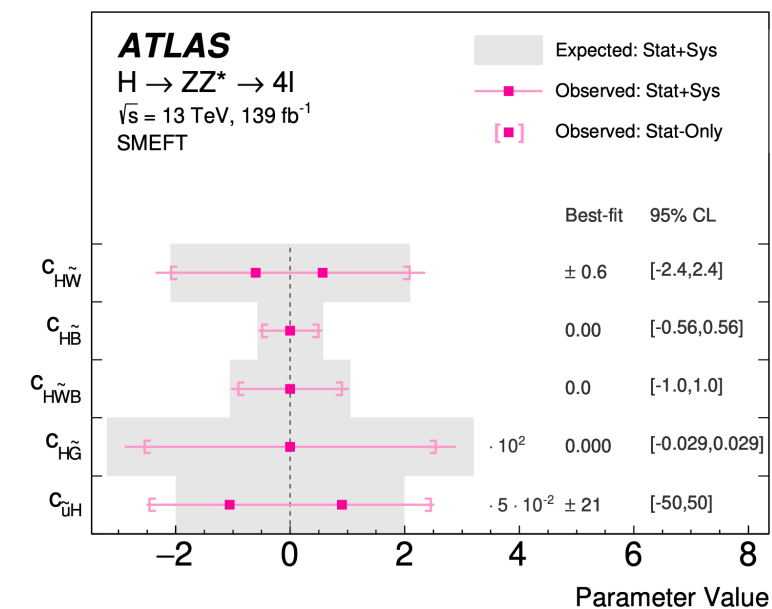
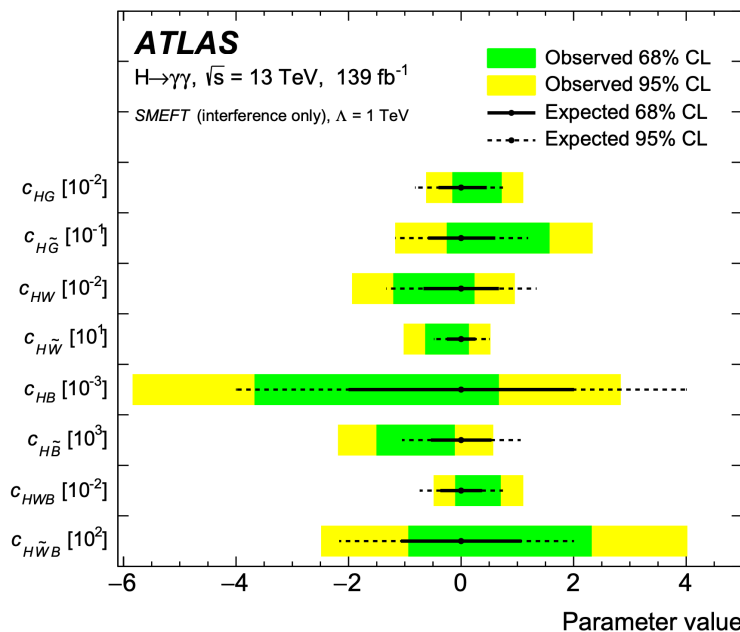
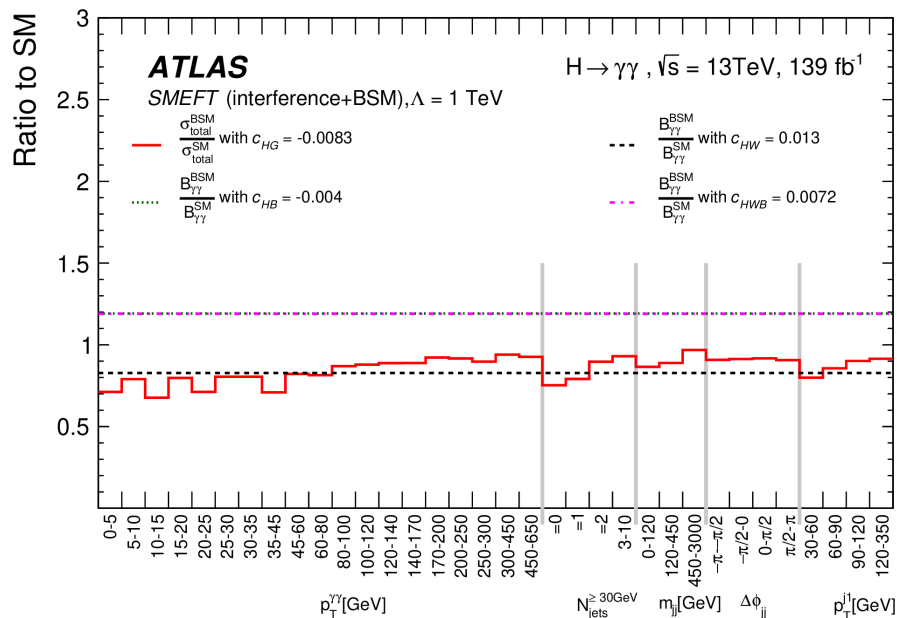
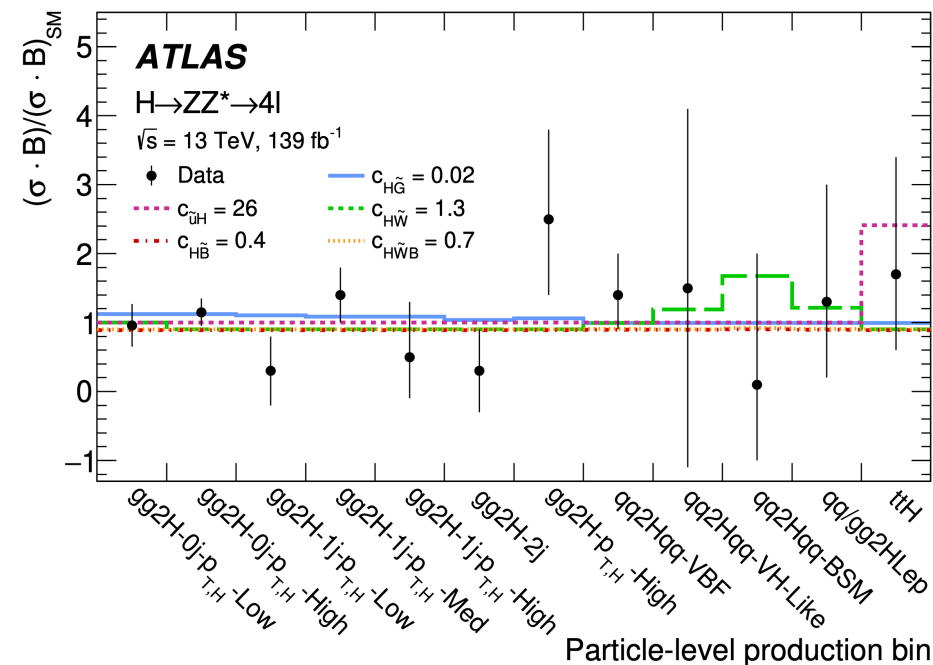


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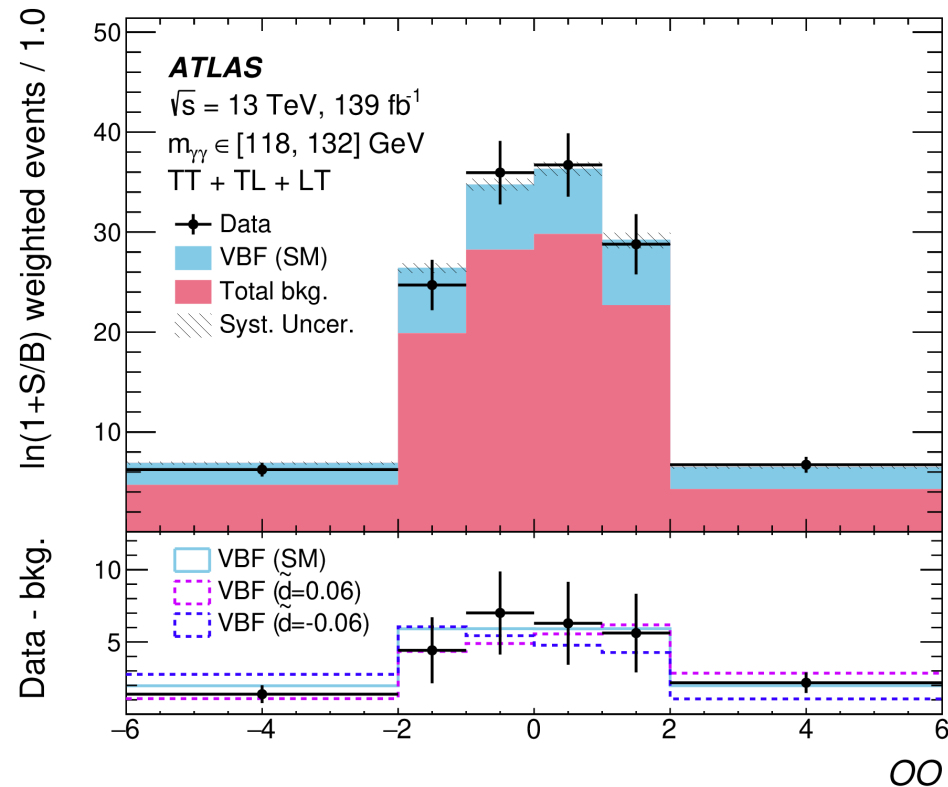
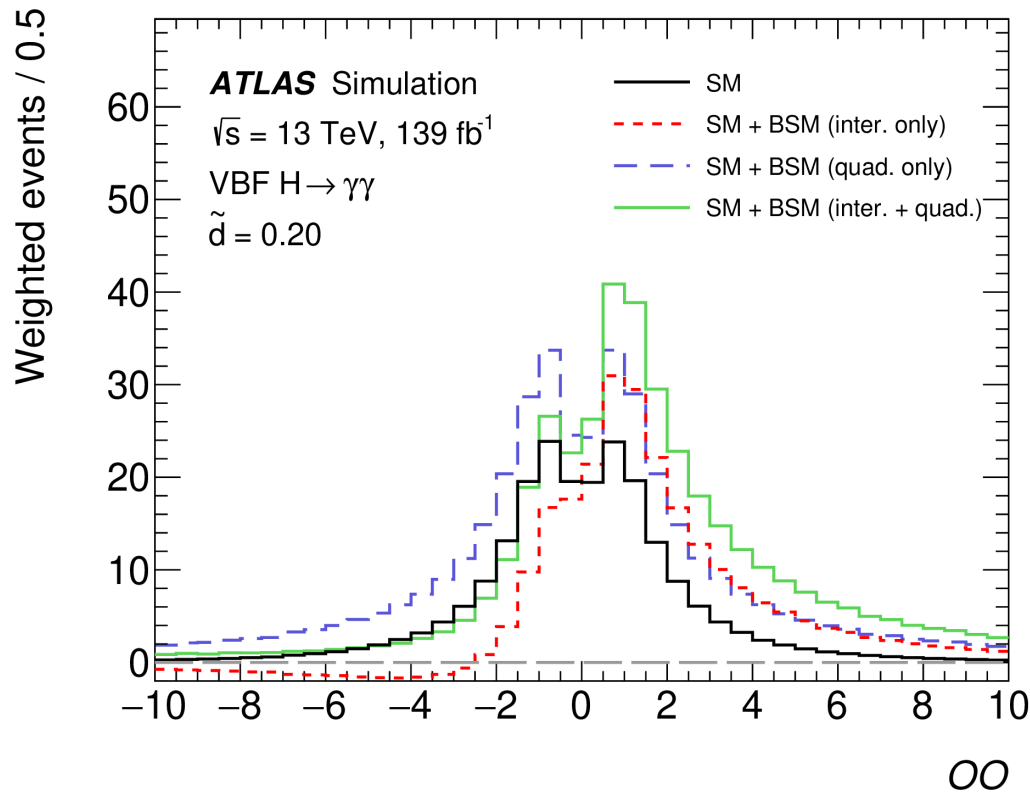
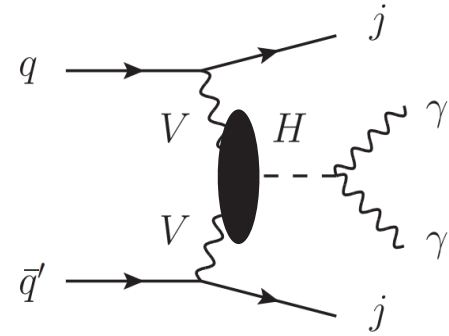
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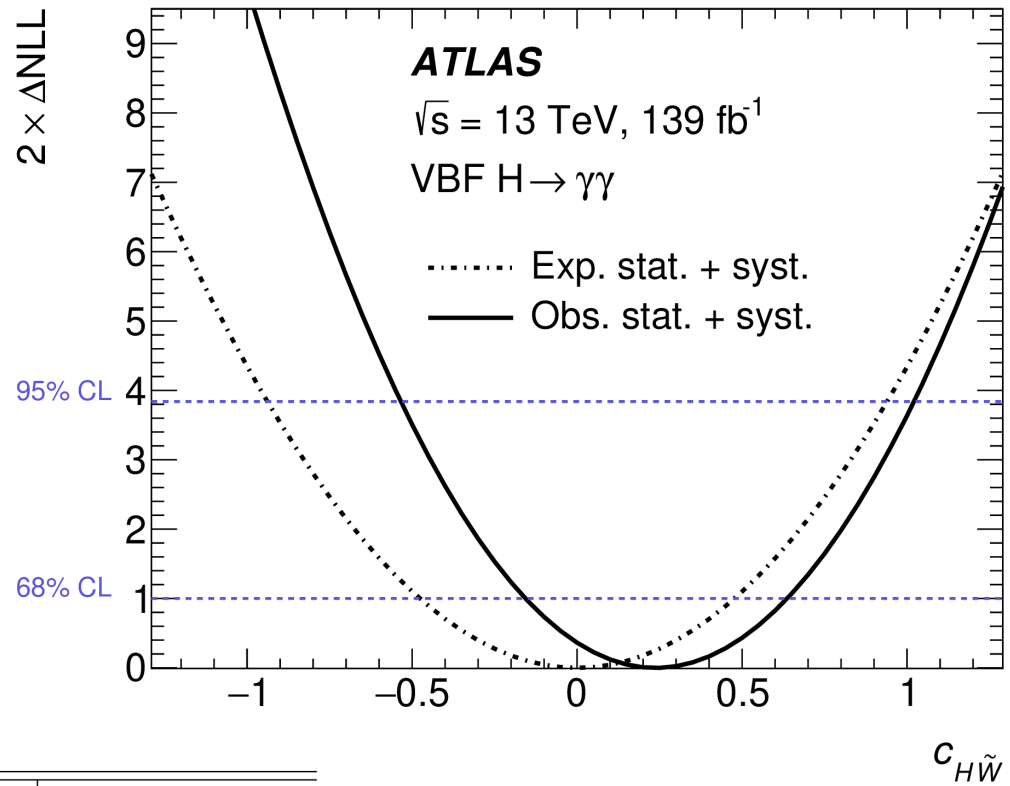
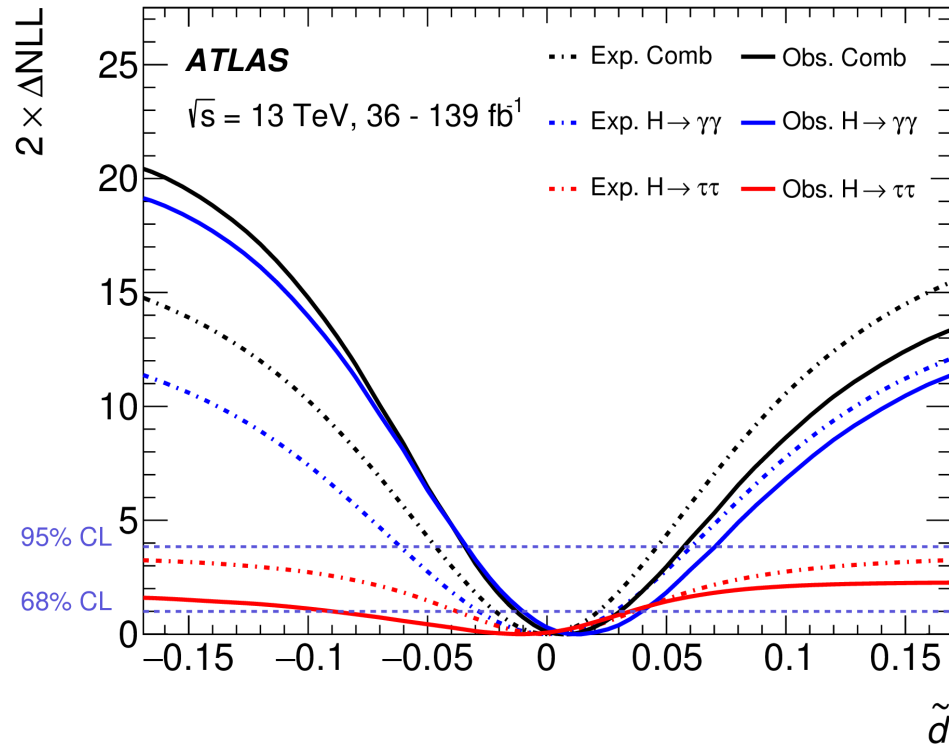


- Explore HVV CP property
- Interpreted results with two EFT bases
  - ✓ **HISZ basis** and **SMEFT Warsaw basis**
- Implement the Optimal Observable method
  - Better than  $\Delta\phi_{jj}$
  - Independent on Higgs Boson decay

$$OO = \frac{2\text{Re}(\mathcal{M}_{SM}^* \mathcal{M}_{CP\text{-odd}})}{|\mathcal{M}_{SM}|^2}$$







	68% (exp.)	95% (exp.)	68% (obs.)	95% (obs.)
$\tilde{d}$ (inter. only)	[-0.027, 0.027]	[-0.055, 0.055]	[-0.011, 0.036]	[-0.032, 0.059]
$\tilde{d}$ (inter.+quad.)	[-0.028, 0.028]	[-0.061, 0.060]	[-0.010, 0.040]	[-0.034, 0.071]
$\tilde{d}$ from $H \rightarrow \tau\tau$	[-0.038, 0.036]	—	[-0.090, 0.035]	—
Combined $\tilde{d}$	[-0.022, 0.021]	[-0.046, 0.045]	[-0.012, 0.030]	[-0.034, 0.057]
$c_{H\tilde{W}}$ (inter. only)	[-0.48, 0.48]	[-0.94, 0.94]	[-0.16, 0.64]	[-0.53, 1.02]
$c_{H\tilde{W}}$ (inter.+quad.)	[-0.48, 0.48]	[-0.95, 0.95]	[-0.15, 0.67]	[-0.55, 1.07]

✓ Compared to  $H \rightarrow ZZ$  and  $H \rightarrow \gamma\gamma$  from cross section interpretation, this analysis has about **2 ~ 5 time better limits**

- EFT from the Higgs Characterization model
- Explore CP structure in Higgs-gluon interaction with events produced in ggH+2jets

$$\mathcal{L}_0^{\text{loop}} = -\frac{g_{Hgg}}{4} \left( \kappa_{gg} \cos(\alpha) G_{\mu\nu}^a G^{a,\mu\nu} + \kappa_{gg} \sin(\alpha) G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \right) H$$

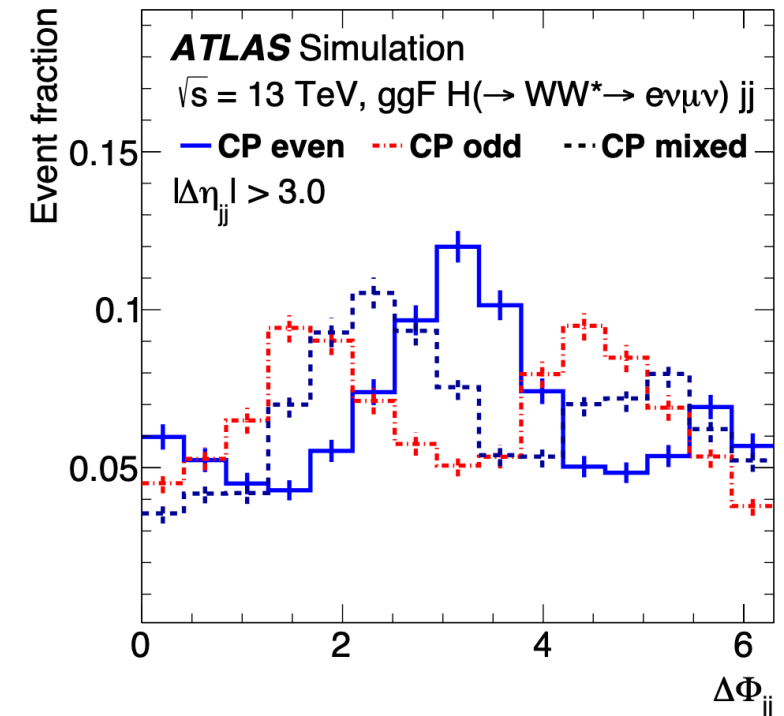
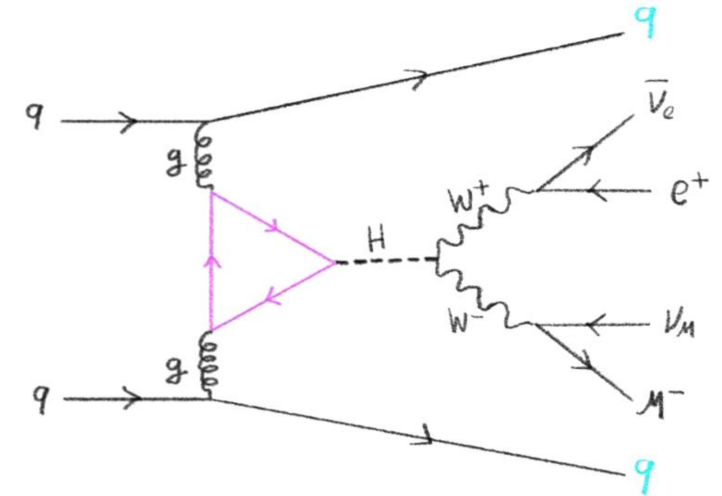
CP-even component

CP-even component

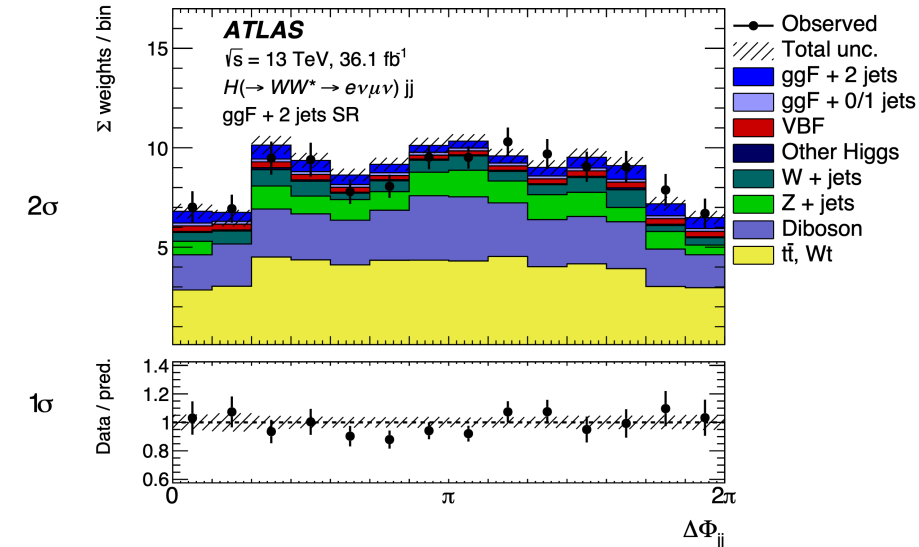
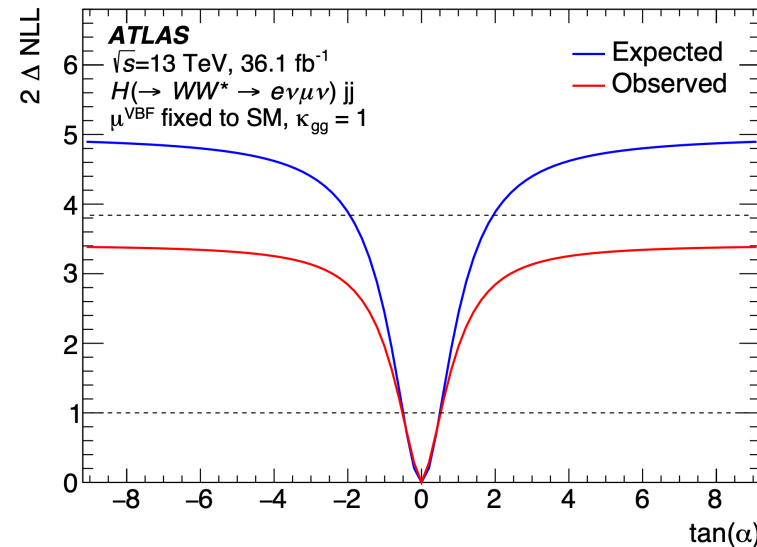
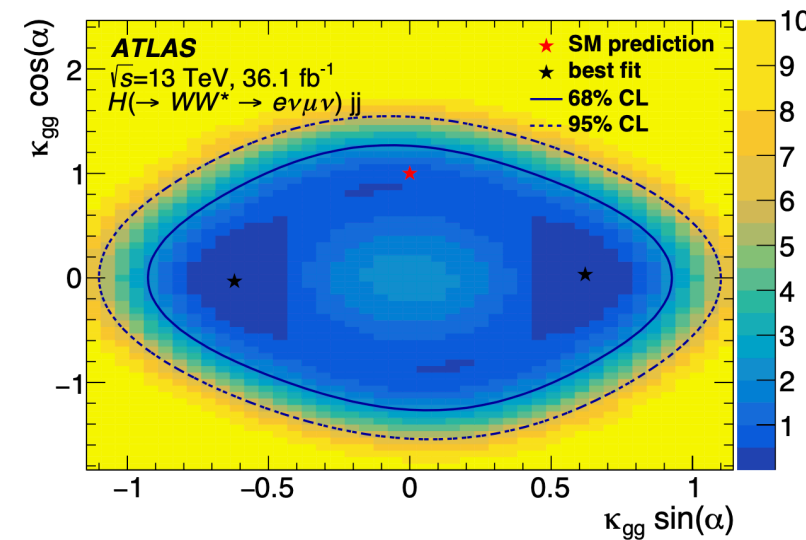
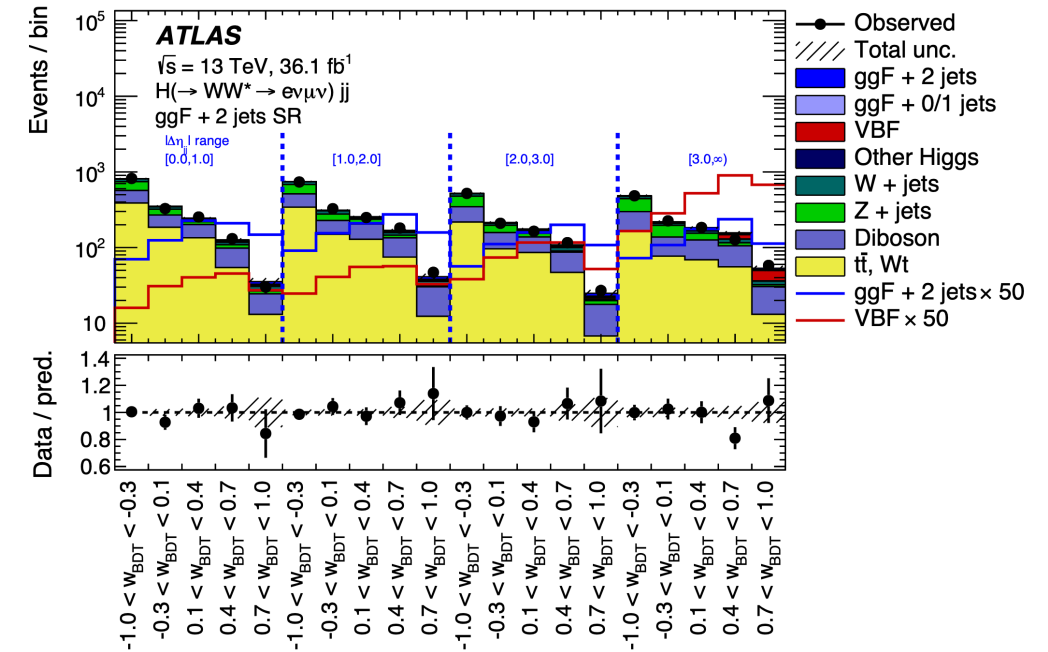
$\Delta\phi_{jj}$  is used as the CP sensitive discriminant

Scenario	Parameters
CP-even (SM)	$\kappa_{gg} = 1, \cos(\alpha) = 1$
CP-odd	$\kappa_{gg} = 1, \cos(\alpha) = 0$
CP-mixed	$\kappa_{gg} = 1, \cos(\alpha) = \frac{1}{\sqrt{2}}$

- Selected 2 opposite sign, different flavor leptons selected with  $\geq 2$  jets
- Additional kinematic selection
- BDT training to further separate signal with Top, WW and  $Z \rightarrow \tau\tau$  events
- Low BDT regions for background modeling



- Results obtained with a fit to  $\Delta\phi_{jj}$  distribution in total 12 event regions (3 BDT  $\times$  4  $|\Delta\phi_{jj}|$  bins)
  - Low BDT regions used for bkg constraints
- Shape+norm fit to provide best fit on  $\tan(\alpha)$ 
  - $\tan(\alpha) = 0.0 \pm 0.4(\text{stats.}) \pm 0.3(\text{syst.})$



# $H \rightarrow ZZ \rightarrow \ell\ell\ell\ell$



Multiple production modes involved

Explore generic HVV and Hff couplings

$$A(Hff) = -\frac{m_f}{v} \bar{\psi}_f (\kappa_f + i\tilde{\kappa}_f \gamma_5) \psi_f$$

tree-level CP-even

SM-like

anomalous couplings

CP-odd

anomalous coupling

$$A(HV_1V_2) \sim \left[ a_1^{VV} + \frac{\kappa_1^{VV} q_1^2 + \kappa_2^{VV} q_2^2}{(\Lambda_1^{VV})^2} \right] m_{V_1}^2 \epsilon_{V_1}^* \epsilon_{V_2}^* + a_2^{VV} f_{\mu\nu}^{*(1)} f^{*(2)\mu\nu} + a_3^{VV} f_{\mu\nu}^{*(1)} \tilde{f}^{*(2)\mu\nu}$$

$$f_{CP}^{Hff} = \frac{|\tilde{\kappa}_f|^2}{|\kappa_f|^2 + |\tilde{\kappa}_f|^2} \text{sign} \left( \frac{\tilde{\kappa}_f}{\kappa_f} \right)$$

$$f_{a_3}^{ggH} = \frac{|a_3^{gg}|^2}{|a_2^{gg}|^2 + |a_3^{gg}|^2} \text{sign} \left( \frac{a_3^{gg}}{a_2^{gg}} \right)$$

$$f_{a_i}^{VV} = \frac{|a_i^{VV}|^2 \alpha_{ii}^{(2e2\mu)}}{\sum_j |a_j^{VV}|^2 \alpha_{jj}^{(2e2\mu)}} \text{sign} \left( \frac{a_i^{VV}}{a_1^{VV}} \right)$$

Similar strategy is also performed in  $H \rightarrow \tau\tau$  channel

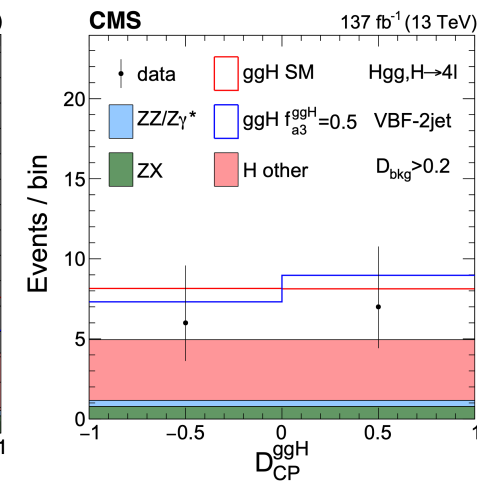
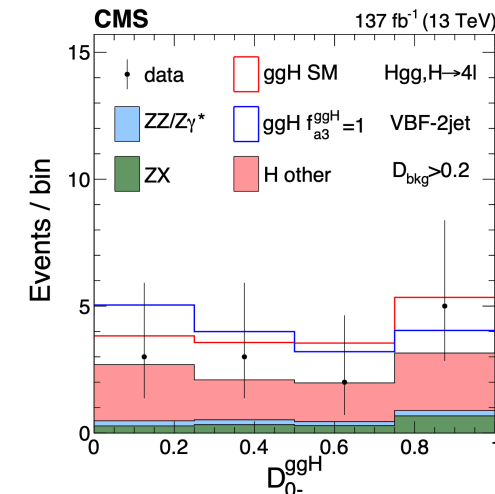
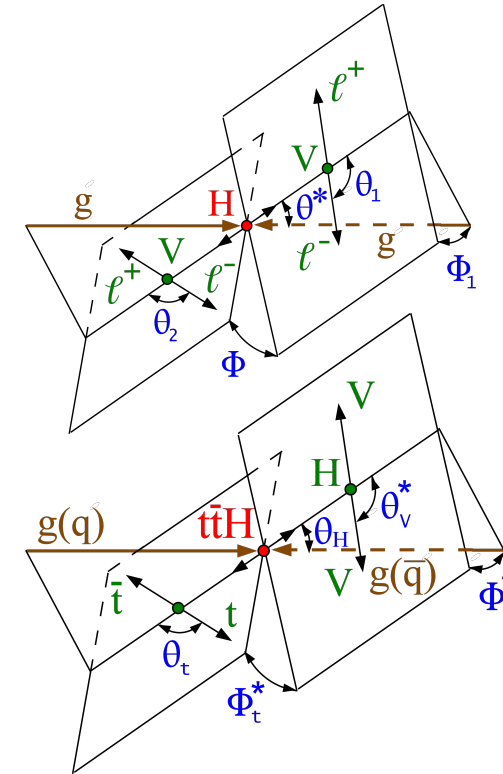
[arXiv:2205.05120](https://arxiv.org/abs/2205.05120)

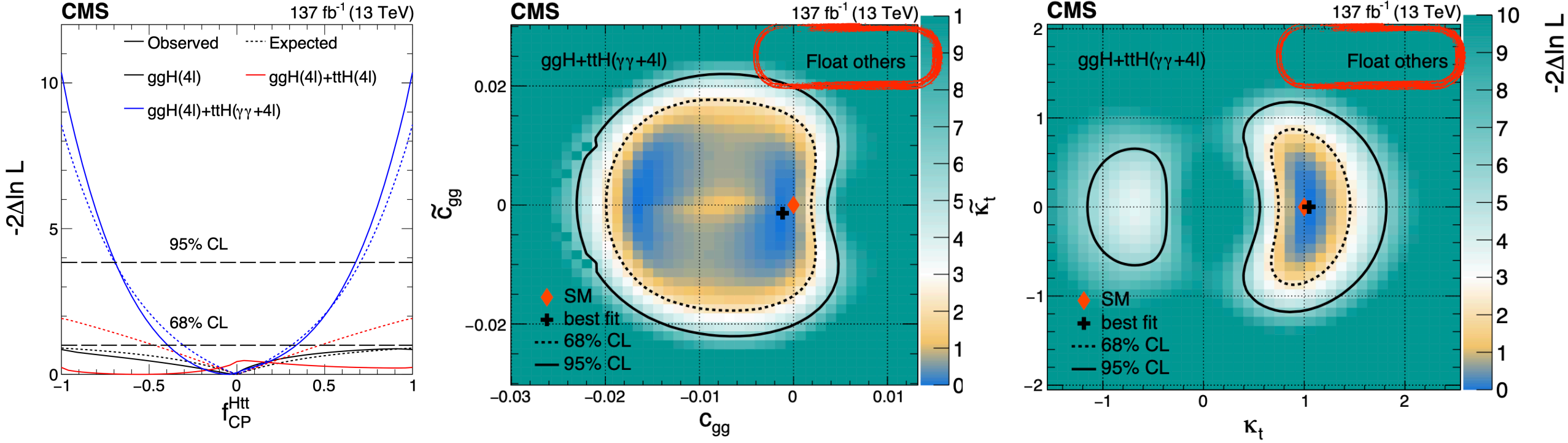
Enhance Higgs signal purity and build CP sensitive observable with MELA technique by exploring the angular distributions etc, improve separation with BDT.

$$\mathcal{D}_{\text{alt}}(\Omega) = \frac{\mathcal{P}_{\text{sig}}(\Omega)}{\mathcal{P}_{\text{sig}}(\Omega) + \mathcal{P}_{\text{alt}}(\Omega)}$$

$$\mathcal{D}_{\text{int}}(\Omega) = \frac{\mathcal{P}_{\text{int}}(\Omega)}{2 \sqrt{\mathcal{P}_{\text{sig}}(\Omega) \mathcal{P}_{\text{alt}}(\Omega)}}$$

Explore CP-odd component





Channels

Coupling

Observed

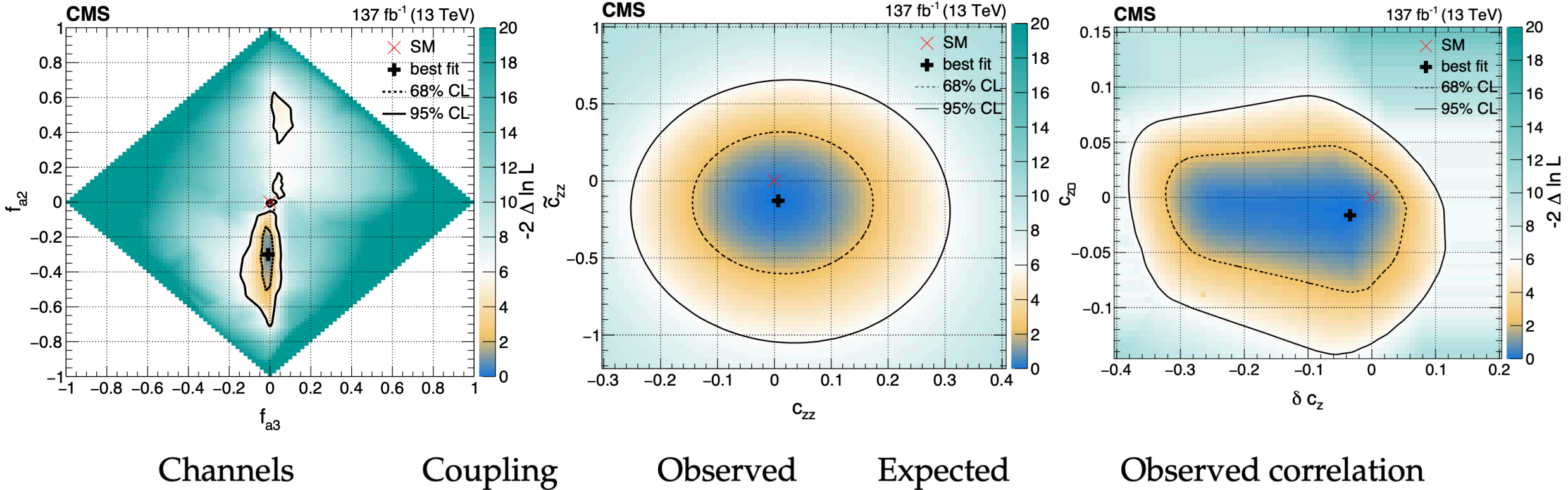
Expected

Observed correlation

## Constraints on $Hff/Hgg$ coupling in SMEFT Higgs basis

	$c_{gg}$	$\tilde{c}_{gg}$	$\kappa_t$	$\tilde{\kappa}_t$
$c_{gg}$	$-0.0012^{+0.0022}_{-0.0174}$	$0.0000^{+0.0019}_{-0.0196}$	1	$-0.050$
$\tilde{c}_{gg}$	$-0.0017^{+0.0160}_{-0.0130}$	$0.0000^{+0.0138}_{-0.0138}$	1	$+0.046$
$\kappa_t$	$1.05^{+0.25}_{-0.20}$	$1.00^{+0.34}_{-0.26}$	1	$+0.168$
$\tilde{\kappa}_t$	$-0.01^{+0.69}_{-0.67}$	$0.00^{+0.71}_{-0.71}$		1

tH & ttH & ggH



## Constraints on HVV coupling in SMEFT Higgs basis

	$\delta c_Z$	$c_{ZZ}$	$c_{Z\Box}$	$\tilde{c}_{ZZ}$
VBF & VH & $H \rightarrow 4l$	$-0.03^{+0.06}_{-0.25}$	$0.00^{+0.07}_{-0.27}$	1	$+0.241$
	$0.01^{+0.11}_{-0.10}$	$0.00^{+0.22}_{-0.16}$	1	$-0.060$
	$-0.02^{+0.04}_{-0.04}$	$0.00^{+0.06}_{-0.09}$	1	$-0.884$
	$-0.11^{+0.30}_{-0.31}$	$0.00^{+0.63}_{-0.63}$	1	$+0.058$
				$+0.020$
				1

# H → ττ coupling structure

The CP-mixing is parametrized to be sensitive to the angular of two tau planes from the Higgs Boson in the Higgs Boson center-of-mass frame

$$\frac{d\Gamma}{d\phi_{CP}}(H \rightarrow \tau^+\tau^-) \sim 1 - b(E^+)b(E^-) \frac{\pi^2}{16} \cos(\phi_{CP} - 2\alpha^{H\tau\tau})$$

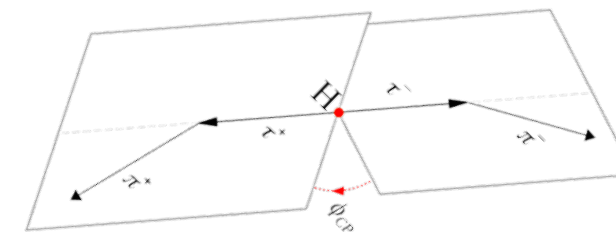
CP-mixing

$$\mathcal{L}_Y = -\frac{m_\tau}{v} H(\kappa_\tau \bar{\tau}\tau + \tilde{\kappa}_\tau \bar{\tau}i\gamma_5\tau)$$

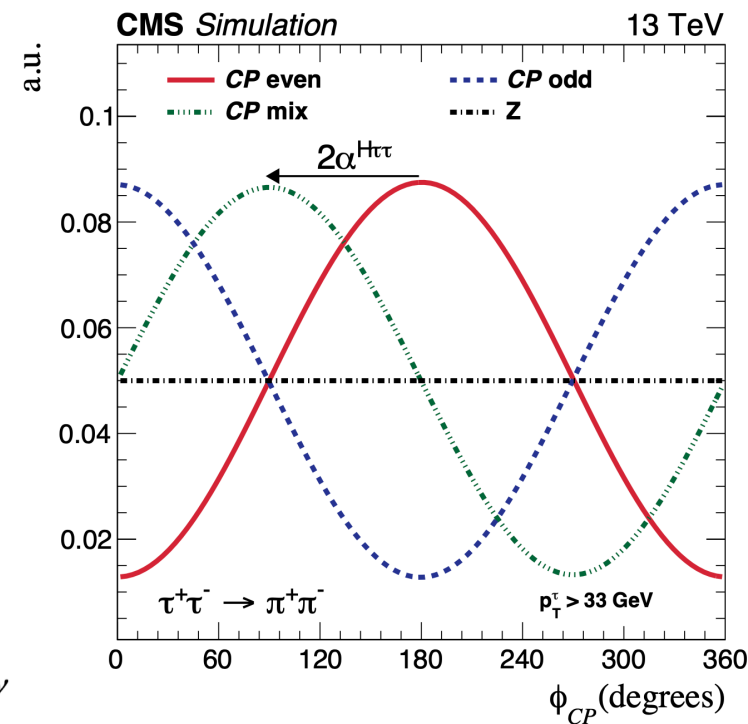
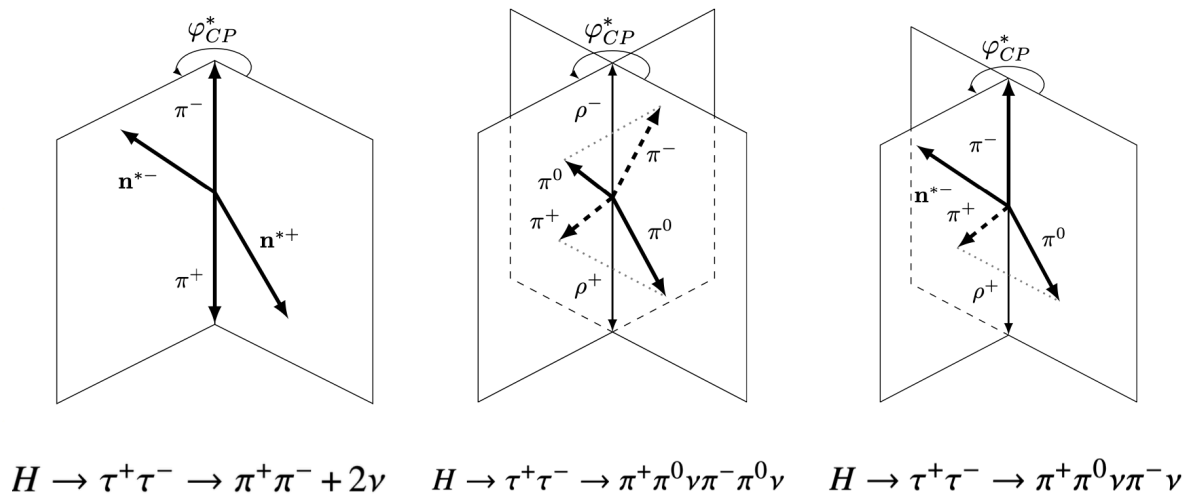
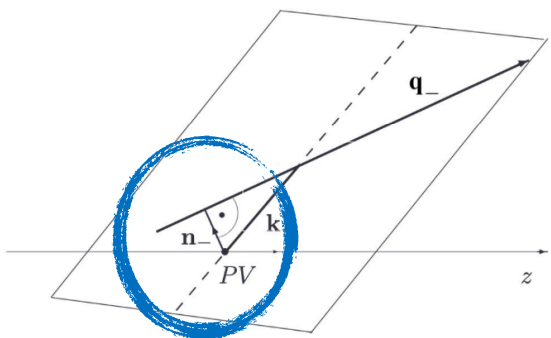
$$\tan(\alpha^{H\tau\tau}) = \frac{\tilde{\kappa}_\tau}{\kappa_\tau}$$

Depending on tau decays: several method developed to reconstructive  $\phi_{CP}$

Notation	Decay mode	Branching fraction	
$\ell$	$\ell^\pm \bar{\nu}\nu$	35.2%	<b>Impact parameter method</b>
1p0n	$h^\pm \nu (\pi^\pm \nu)$	11.5% (10.8%)	
1p1n	$h^\pm \pi^0 \nu (\pi^\pm \pi^0 \nu)$	25.9% (25.5%)	<b>Neutral pion method (+IP method)</b>
1pXn	$h^\pm \geq 2\pi^0 \nu (\pi^\pm 2\pi^0 \nu)$	10.8% (9.3%)	
3p0n	$3h^\pm \nu (3\pi^\pm \nu)$	9.8% (9.0%)	



## Impact parameter



# H → ττ coupling structure



JHEP 06 (2022) 012



arXiv:2212.05833

Current data prefer CP-even case

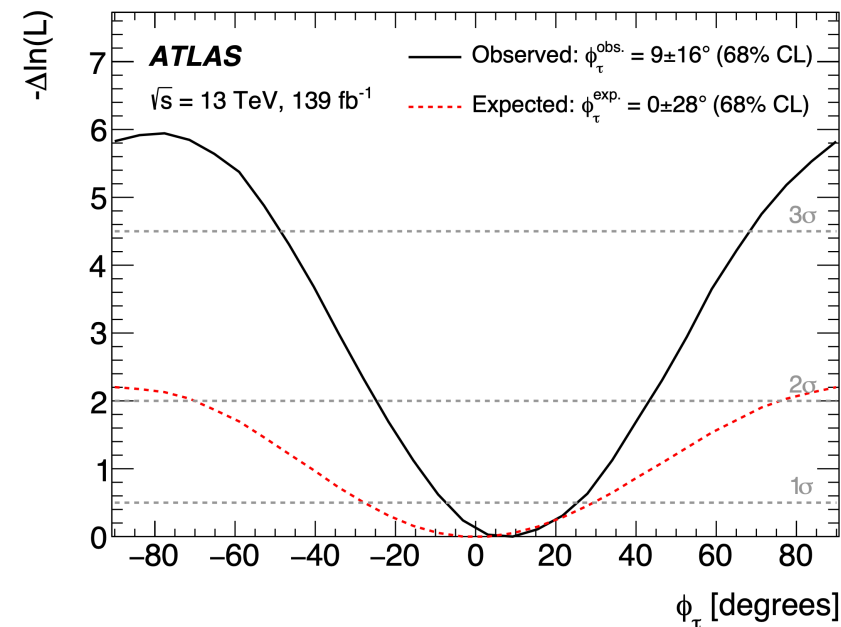
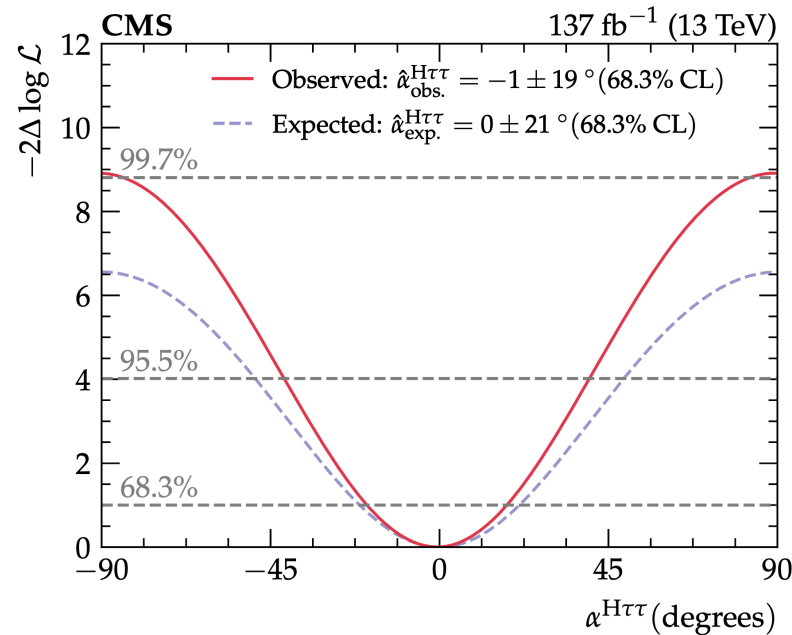
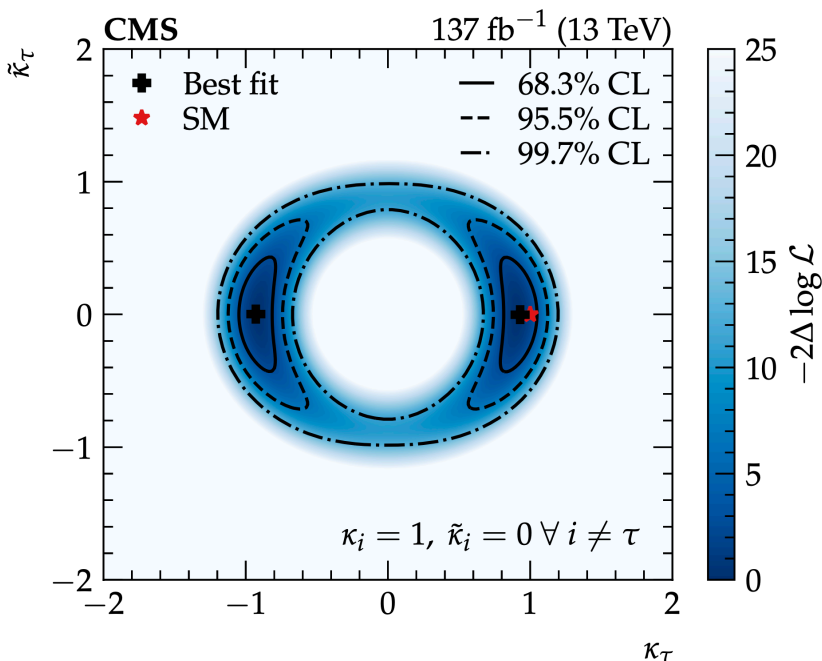
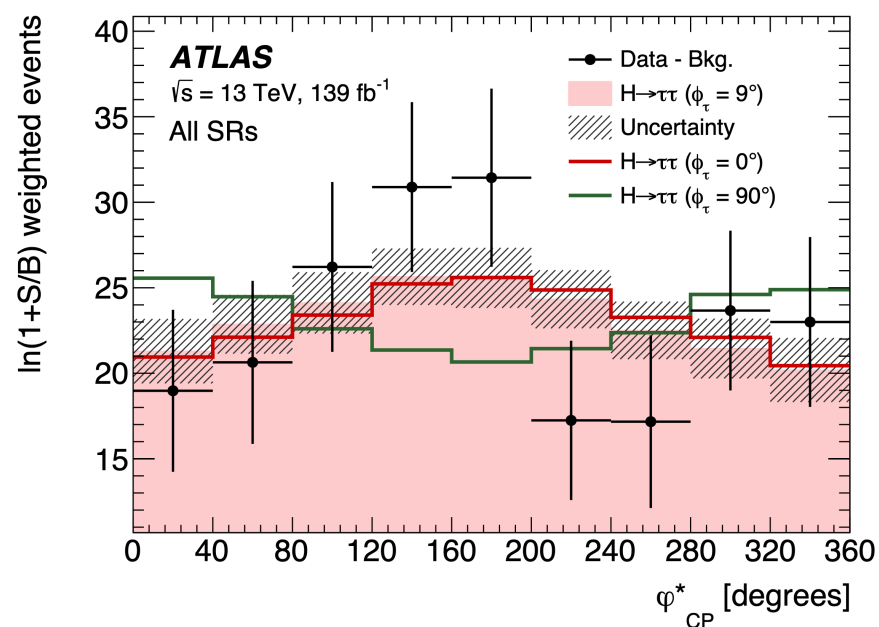
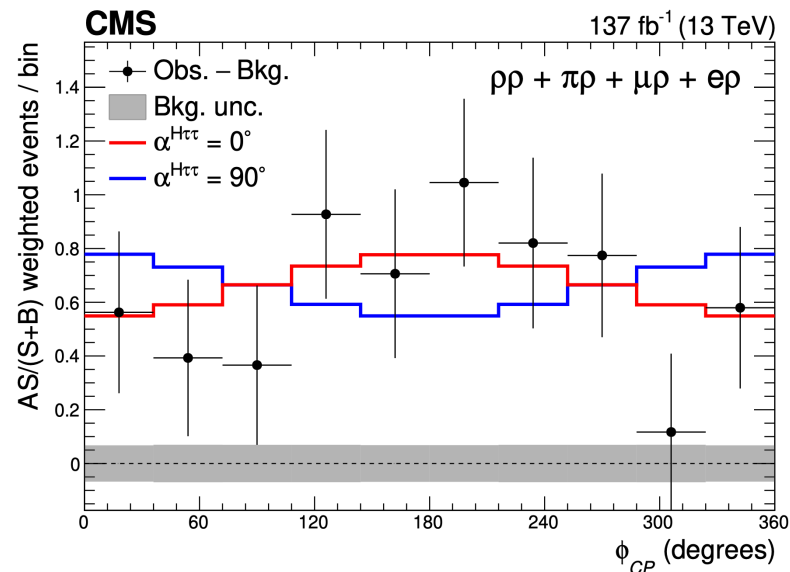
$$\alpha^{H\tau\tau} = -1 \pm 19 \text{ deg. } (\pm 21 \text{ deg.})$$

Pure CP-odd excluded @ 3σ

Similar strategy analysis done by ATLAS

$$\phi_\tau = 9 \pm 16 \text{ deg. } (\pm 28 \text{ deg.})$$

Pure CP-odd excluded @ 3.4σ

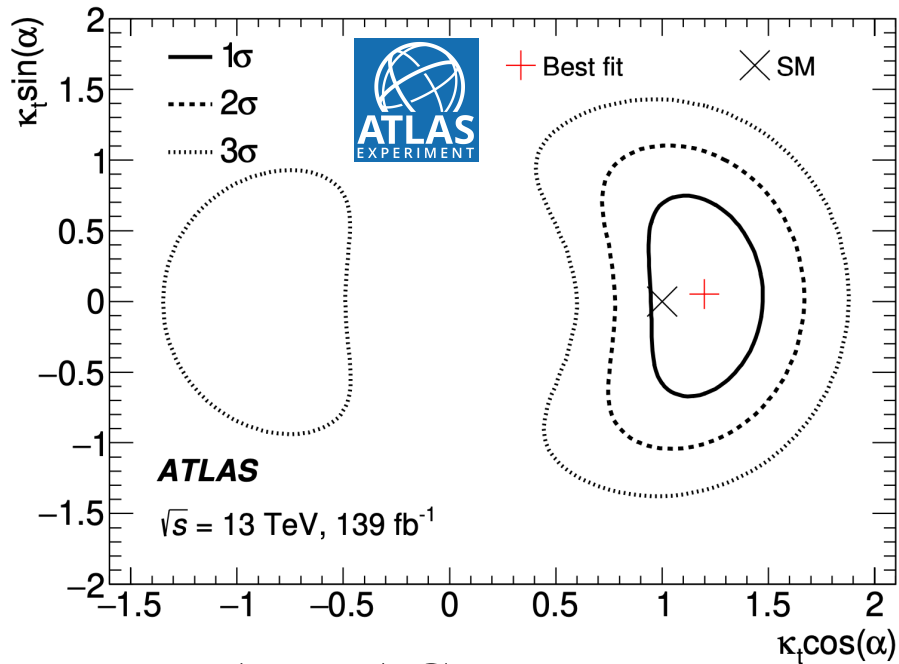
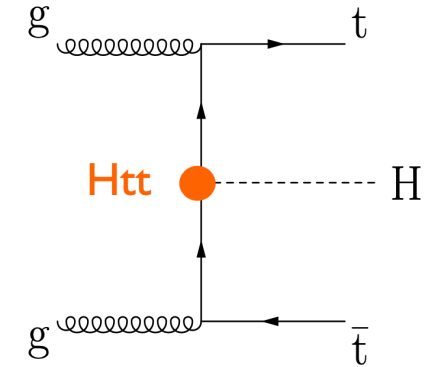




$$\mathcal{L}_t = -\frac{m_t}{v} (\underbrace{\kappa_t \bar{t}t}_{\text{CP-even}} + i \underbrace{\tilde{\kappa}_t \bar{t}\gamma_5 t}_{\text{CP-odd}}) H$$

$$\kappa_t = k_t \cos \alpha$$

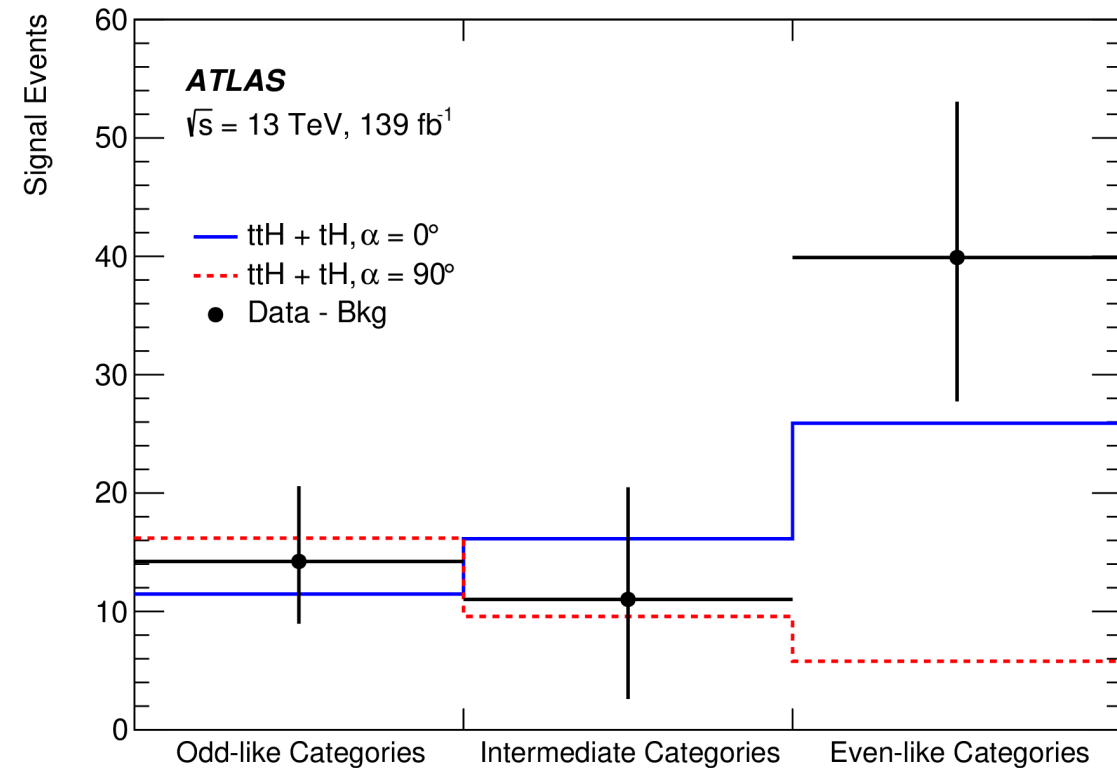
$$\tilde{\kappa}_t = k_t \sin \alpha$$



ATLAS  $H \rightarrow \gamma\gamma$

Mixing angle  $|\alpha| < 43^\circ$  @95% CL

Pure CP-odd excluded @3.9 $\sigma$

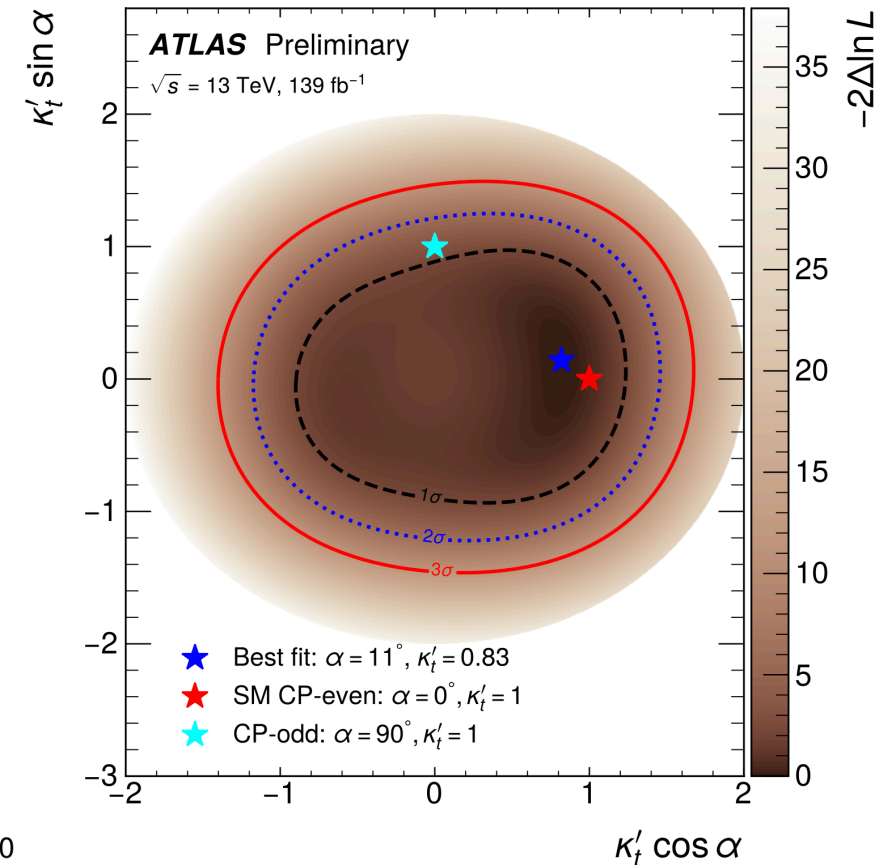
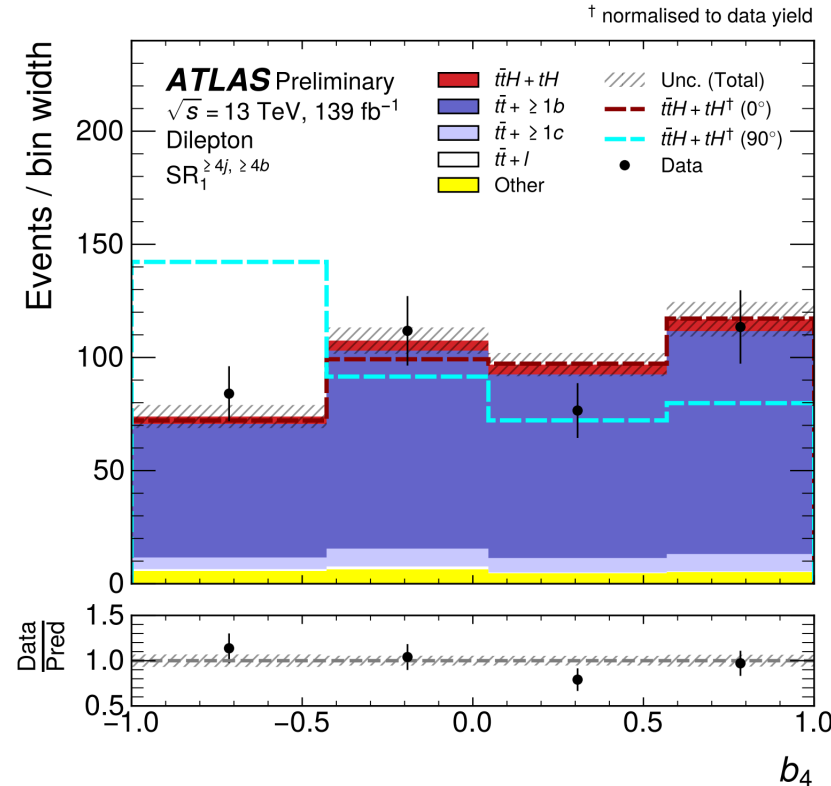
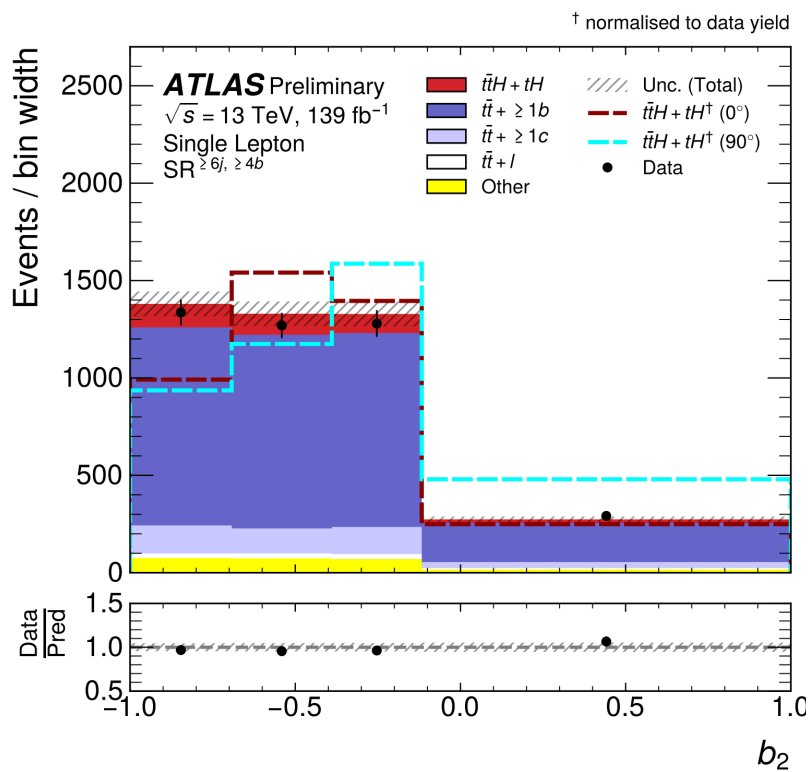


Two CP sensitive variables defined with top quark kinematic information in  $1\ell+jets$  and  $2\ell$  channel

$$b_2 = \frac{(\vec{p}_1 \times \hat{n}) \cdot (\vec{p}_2 \times \hat{n})}{|\vec{p}_1||\vec{p}_2|}, \text{ and } b_4 = \frac{p_1^z p_2^z}{|\vec{p}_1||\vec{p}_2|}$$

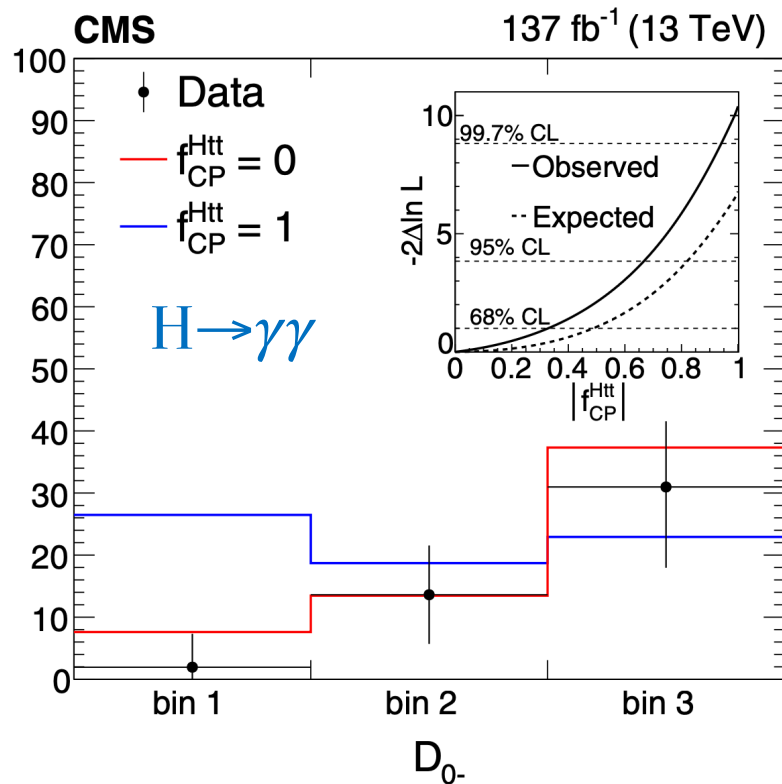
ATLAS  $H \rightarrow bb$

$\vec{p}_{1,2}$  are top momenta,  $\hat{n}$  is the unit vector for z-axis

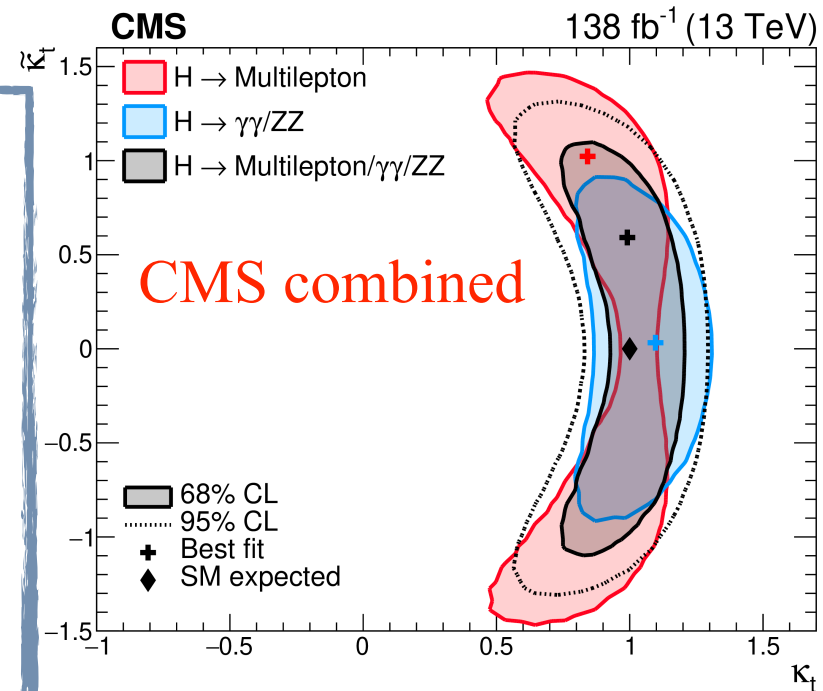
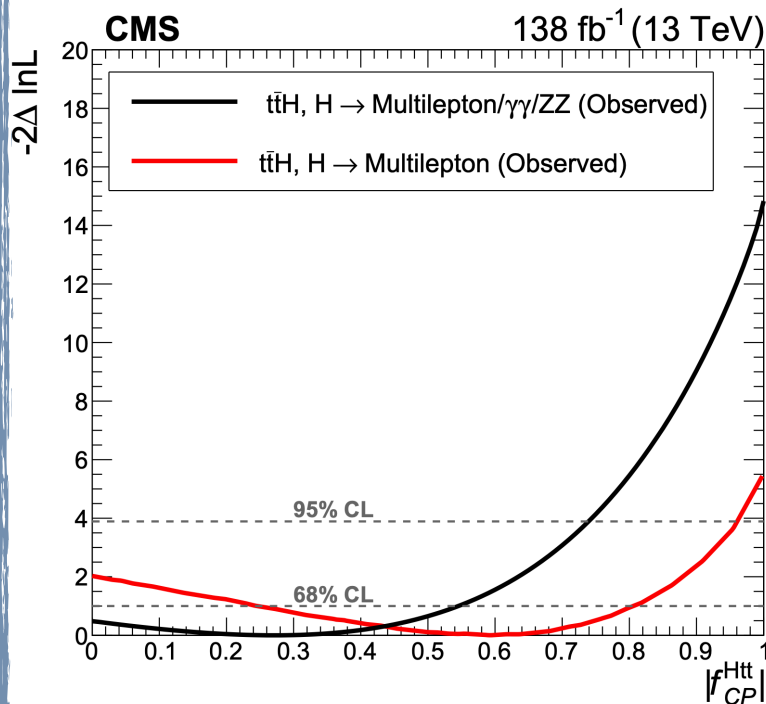


$$\mathcal{L}_t = -\frac{m_t}{v} \left( \underbrace{\kappa_t \bar{t}t}_{\text{CP-even}} + i \underbrace{\tilde{\kappa}_t \bar{t} \gamma_5 t}_{\text{CP-odd}} \right) H \quad f_{CP}^{Htt} = \frac{\tilde{\kappa}_t^2}{\tilde{\kappa}_t^2 + \kappa_t^2}$$

MELA-based CP sensitive observable to extract CP-odd information



Complicated final state, ML-based observable for CP measurement



Pure CP-odd excluded @3.7 $\sigma$

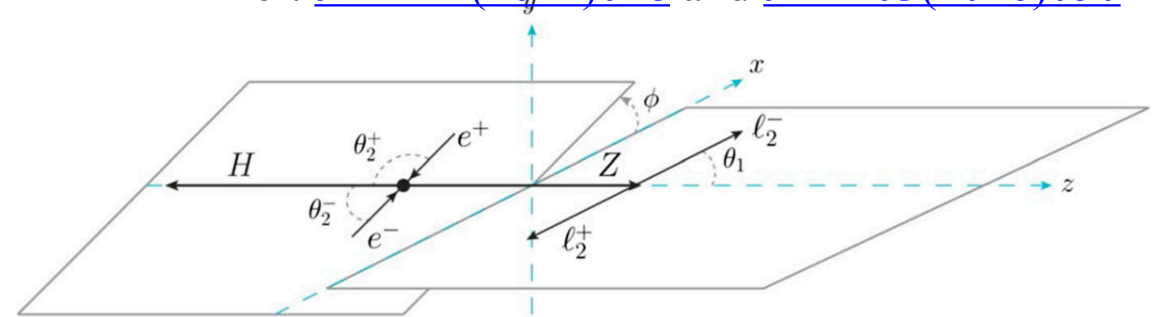
$H \rightarrow \gamma\gamma$  only exclude @3.2 $\sigma$

## Effective Lagrangian in Higgs basis

$$\begin{aligned} \mathcal{L}_{\text{eff}} \supset & c_{ZZ}^{(1)} H Z_\mu Z^\mu + c_{ZZ}^{(2)} H Z_{\mu\nu} Z^{\mu\nu} + c_{Z\tilde{Z}} H Z_{\mu\nu} \tilde{Z}^{\mu\nu} \\ & + c_{AZ} H Z_{\mu\nu} A^{\mu\nu} + c_{A\tilde{Z}} H Z_{\mu\nu} \tilde{A}^{\mu\nu} \\ & + H Z_\mu \bar{\ell} \gamma^\mu (c_V + c_{A\gamma 5}) \ell + Z_\mu \bar{\ell} \gamma^\mu (g_V - g_{A\gamma 5}) \ell \\ & - g_{\text{em}} Q_\ell A_\mu \bar{\ell} \gamma^\mu \ell, \end{aligned}$$

Theoretical framework follows

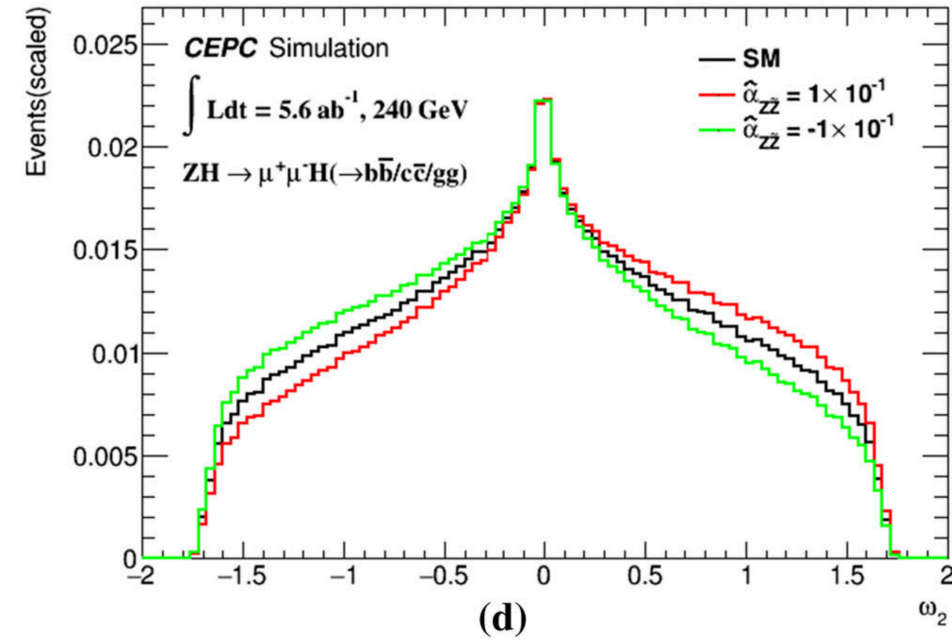
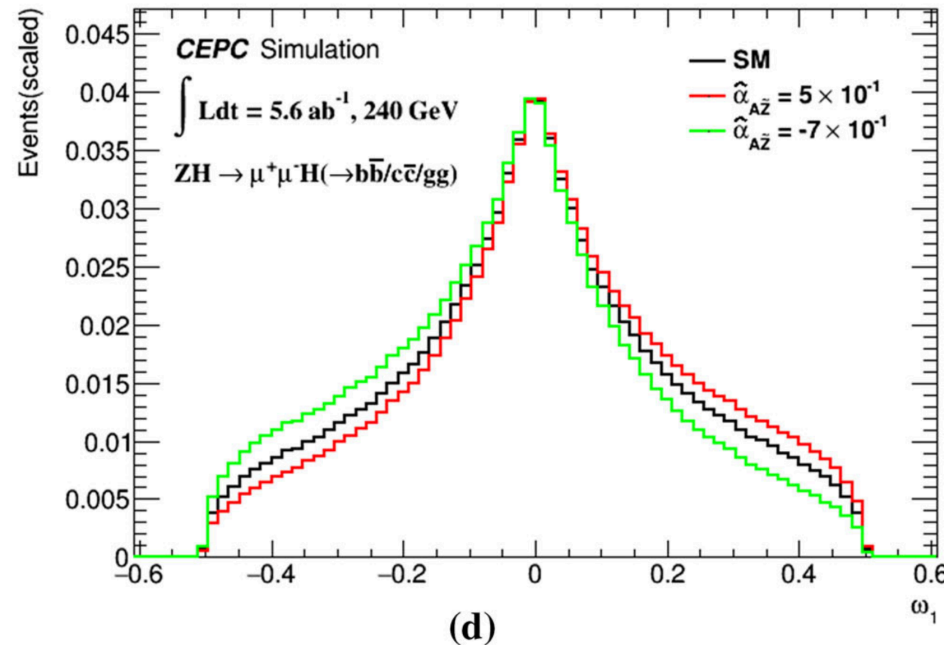
Ref. [JHEP11\(2014\)028](#) and [JHEP03\(2016\)050](#)

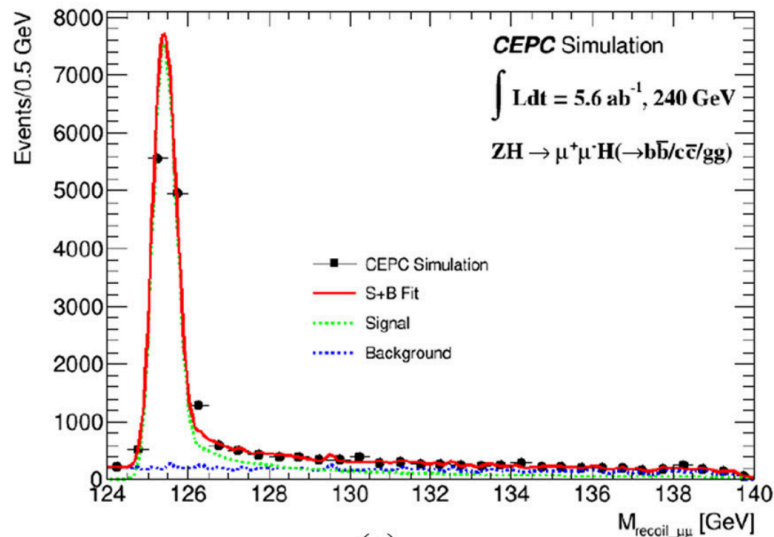


CP-sensitive variables defined from angular distributions as discriminators

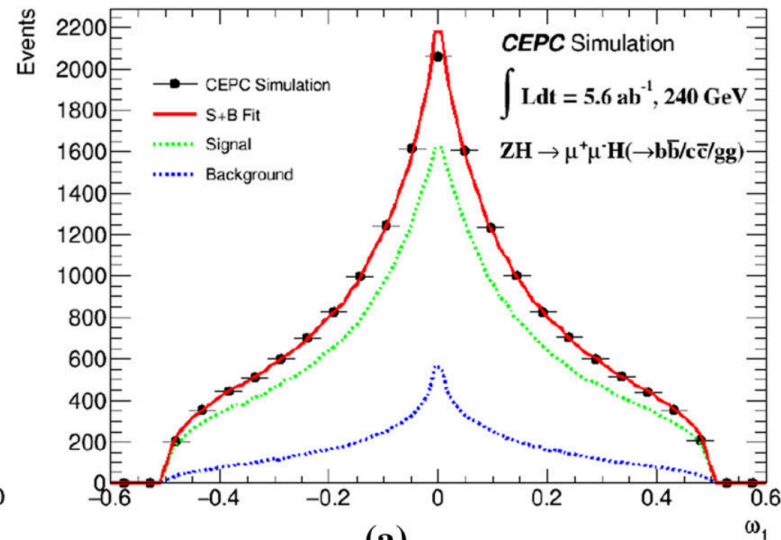
$$\omega_1 = \frac{J_{\text{odd}1}(\theta_1, \theta_2, \phi)}{J_{\text{even}}(\theta_1, \theta_2, \phi)}$$

$$\omega_2 = \frac{J_{\text{odd}2}(\theta_1, \theta_2, \phi)}{J_{\text{even}}(\theta_1, \theta_2, \phi)}$$

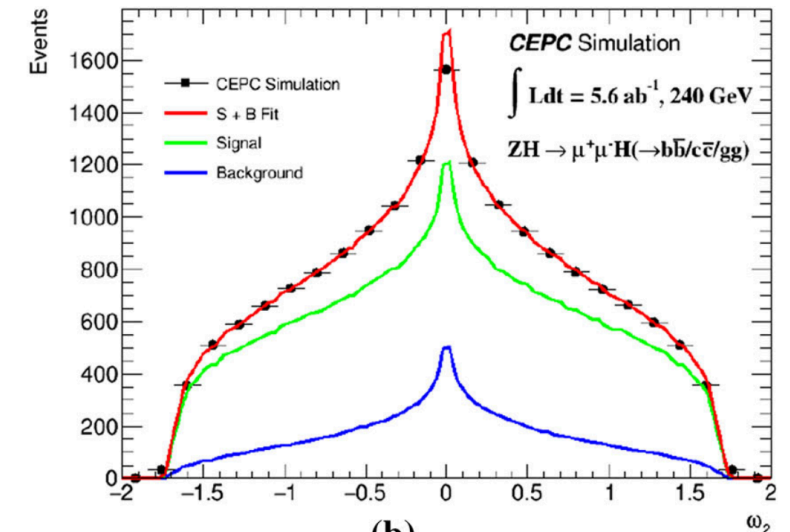




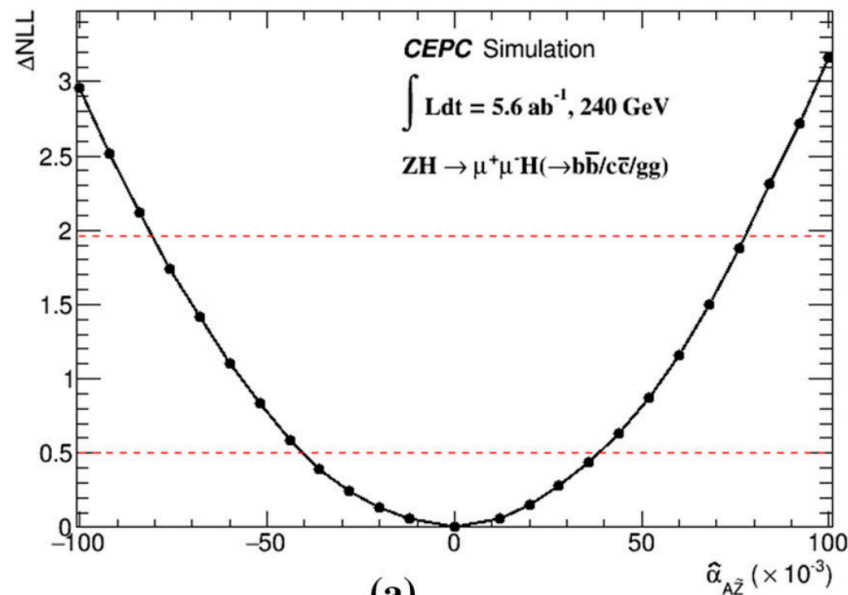
(c)



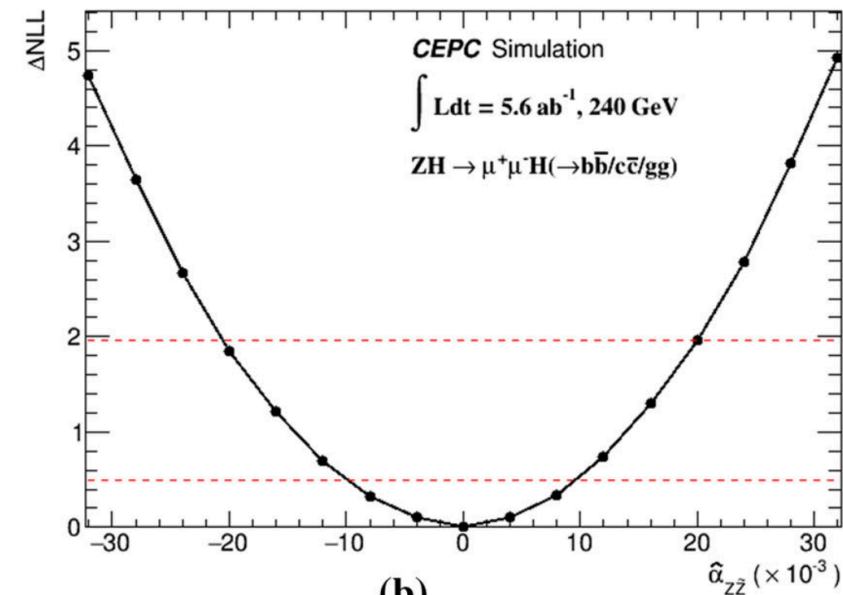
(a)



(b)



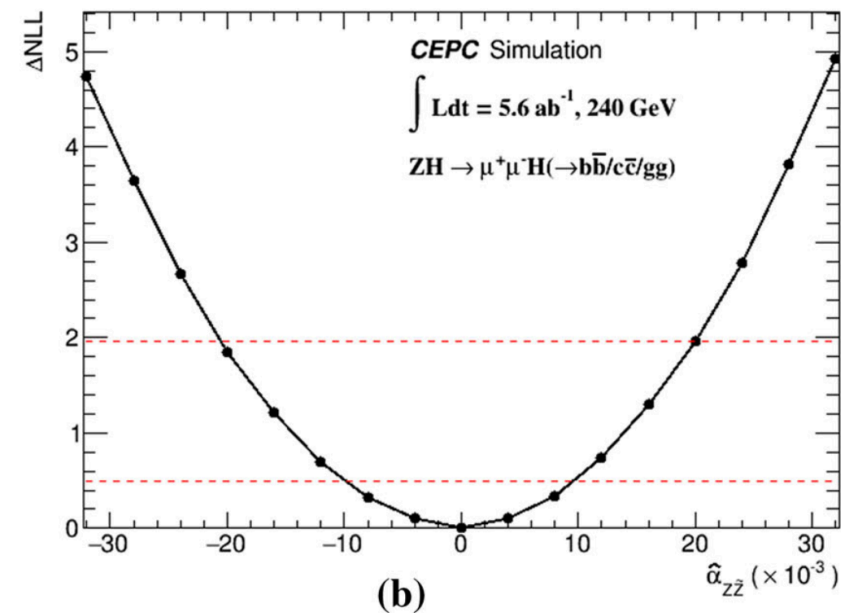
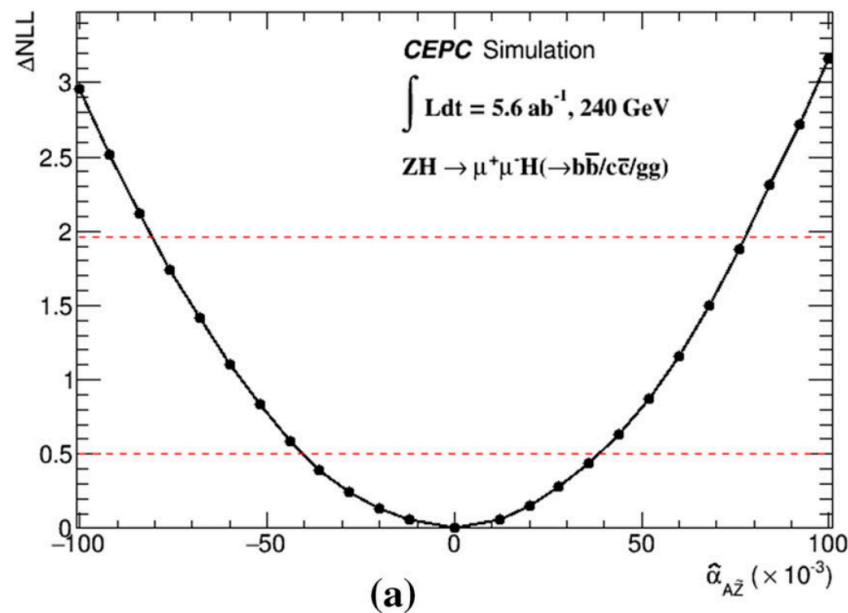
(a)



(b)

# Higgs CP measurement in CEPC

	HL-LHC	CLIC	CEPC	
Collider	$pp$	$e^+e^-$	$e^+e^-$	$e^+e^-$
$E$ (GeV)	14,000	3000	240	240
$\mathcal{L}$ ( $\text{fb}^{-1}$ )	3000	5000	5600	20,000
$\tilde{c}_{Z\gamma}$ ( $1\sigma$ )	$[-0.22, 0.22]$	$[-0.18, 0.18]$	$[-0.30, 0.27]$	$[-0.16, 0.14]$
$\tilde{c}_{ZZ}$ ( $1\sigma$ )	$[-0.33, 0.33]$	$[-0.12, 0.12]$	$[-0.06, 0.06]$	$[-0.03, 0.03]$

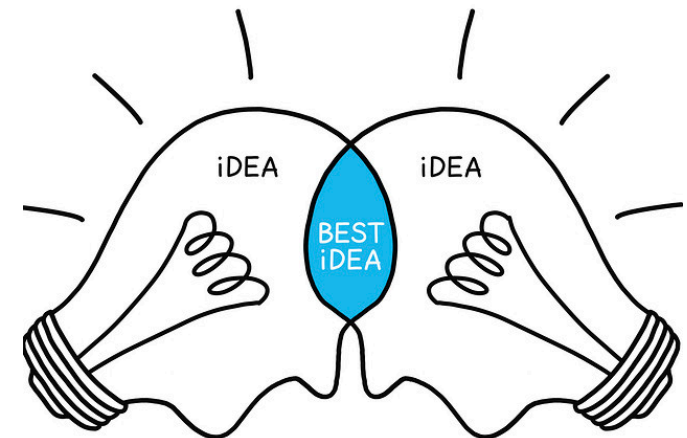


# Summary

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- Studies of the Higgs boson CP property is crucial for particle physics recent days
- Extensive analyses done by the ATLAS and CMS experiments to build a complete view of the Higgs CP properties and search for potential anomalies would resulting the “odd” CP phenomena
- Recent results show that data agrees with the SM predictions → still limited by the low statistics
  - ✓ Huge improvement expected from HL-LHC upgrade
  - ✓ Strong constraints from Future Higgs factory
- Purely CP-odd coupling has been excluded → still room for CP-mixing

*Collaboration between experimentalist and theorist would be very much appreciated*



感谢聆听  
Thanks for listening



# Backup

## Higgs CP

- With all final state particles reconstructed, we can perform a Matrix Element based analysis of the underlying Higgs CP mixing angle  $\Phi$ . The Higgs decay amplitude can be expressed as

$$\begin{aligned} |\mathcal{M}|^2 &\propto A + B \cos(2\phi) + C \sin(2\phi), \\ &\propto I_1 \cos^2(\phi) + I_2 \sin(\phi) \cos(\phi) + I_3 \sin^2(\phi) \end{aligned}$$

- Two observables can be reconstructed per event for the CP test
  - ❖ Optimal Observable (M. Davier et. al, Phys. Lett. B306,1993, 411):  $OO = I_2/I_1$
  - ❖ ME angle  $\Delta\Phi_{ME}$ , defined as

$$\begin{aligned} |\mathcal{M}|^2 &\propto A + \sqrt{B^2 + C^2} \cos(\Delta\phi_{ME} - 2\phi) \\ \cos(\Delta\phi_{ME}) &= \frac{B}{\sqrt{B^2 + C^2}}, \quad \sin(\Delta\phi_{ME}) = \frac{C}{\sqrt{B^2 + C^2}} \end{aligned}$$

At low mixing angle values, the two perform similarly, while in high values of  $\Phi$ ,  $\Delta\Phi_{ME}$  is better

## CP test in $H \rightarrow \tau\tau$ decay

- CP-odd Yukawa coupling can enter the Lagrangian at dim-4, thus sensitive at tree-level rather than with the dim-6 operators in HVV

$$-g_\tau (\cos\phi \bar{\tau}\tau + \sin\phi \bar{\tau}i\gamma_5\tau)h \quad \Phi \text{ is the mixing angle. } \Phi=0 \text{ (}\Phi=\pi/2\text{) means SM (CP odd)}$$

- CP of  $H\tau\tau$  coupling can be distinguished by the transverse tau spin correlations

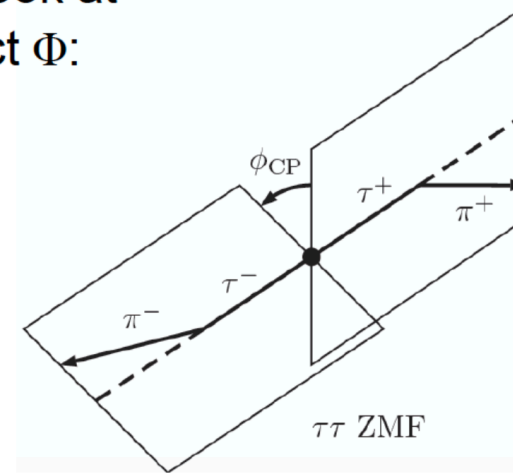
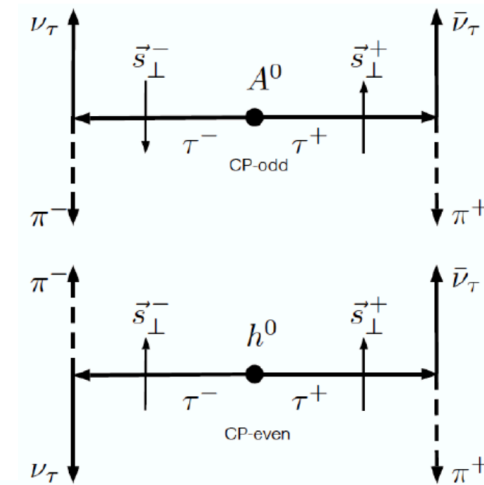
$$\Gamma(H, A \rightarrow \tau^-\tau^+) \sim 1 - s_z^{\tau^-} s_z^{\tau^+} \pm s_T^{\tau^-} s_T^{\tau^+}$$

Sensitive to CP (H vs A)

- For example, with the  $\tau \rightarrow \pi\nu$  decay, one can look at the angle between tau decay planes to extract  $\Phi$ :

$$\frac{d\Gamma(h \rightarrow \tau\tau \rightarrow \pi^+\pi^- + 2\nu)}{d\phi_{\text{CP}}} \propto 1 - \frac{\pi^2}{16} \cos(\phi_{\text{CP}} - 2\phi)$$

- It is experimentally challenging because the neutrinos are not reconstructed

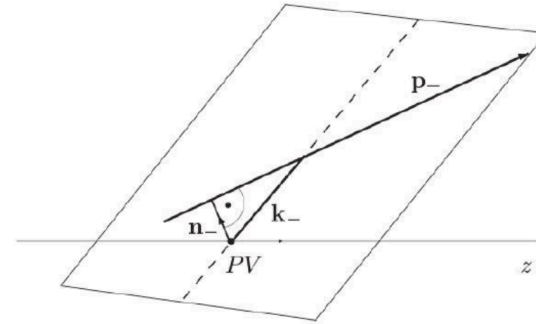


## CP test in $H \rightarrow \tau\tau$ decay

- There are two methods to extract CP from  $H \rightarrow \tau\tau$  decay:

### Impact Parameter (IP) method:

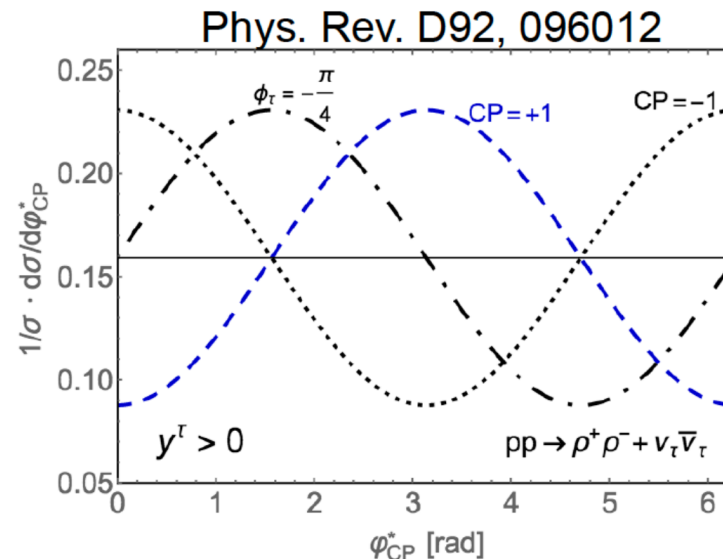
- Approximately reconstruct the tau decay plane from its leading track and IP
- Best for the  $\tau \rightarrow \pi\nu$  decay. The analyzing power is compromised for other tau decays



### Using the $\tau \rightarrow \rho\nu \rightarrow \pi^\pm \pi^0 \nu$ decay:

- The tau decay plane can be approximately reconstructed by the track and neutral pion
- However, the relative energy of  $\pi^\pm, \pi^0$  need to be classified in order to maximize the analyzing power

- In order to use the two methods, the **tau decay modes (substructure)** need to be well differentiated (next few slides)



A few extra references:

EPJC 74 (2014) 3164, Phys. Rev. D88 076009,

Phys. Lett. B579 (2004) 157, Phys. Lett. B543 (2002) 227

# Higgs CP in $H \rightarrow \tau\tau$ : $\phi_{CP}$ distribution

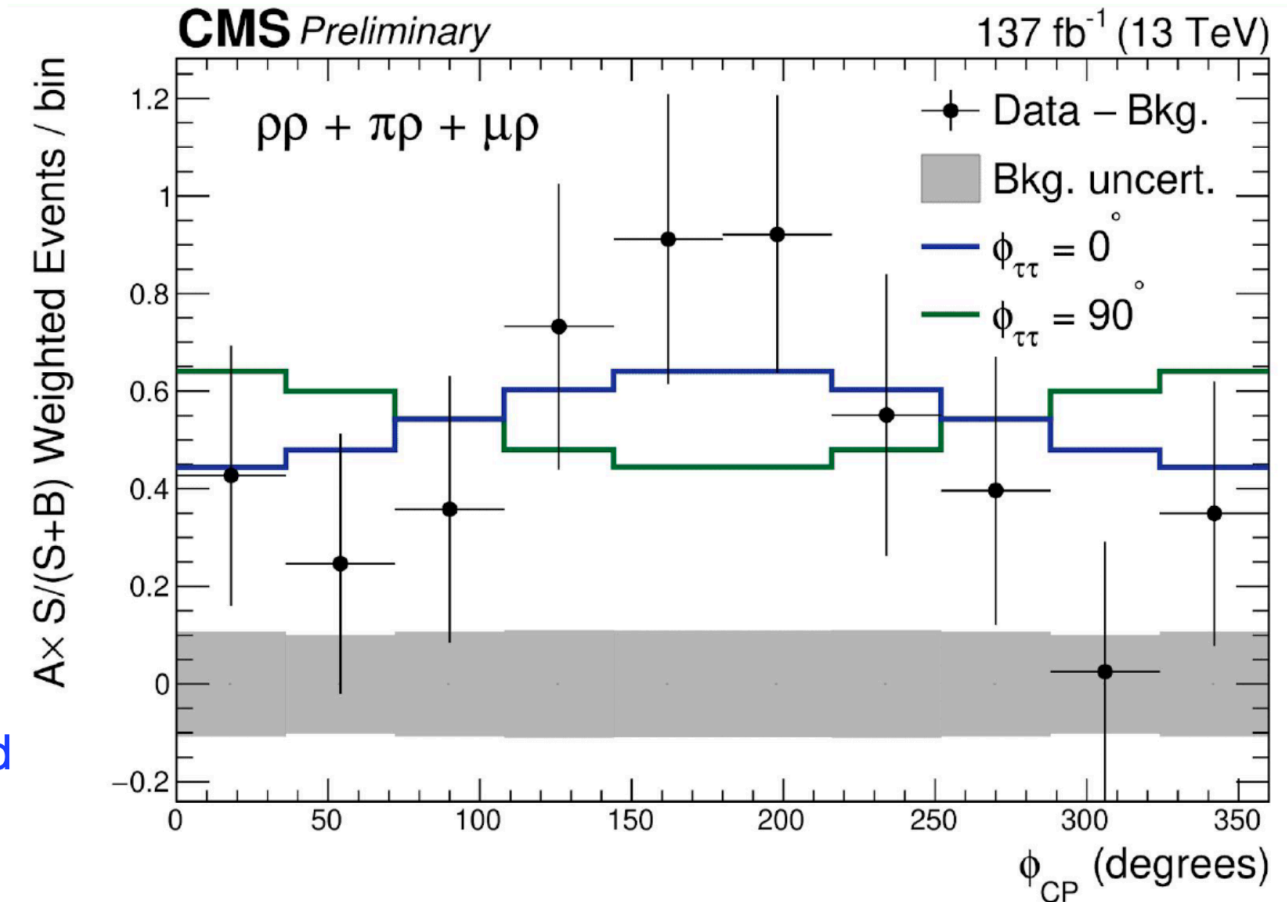
The results from the most sensitive channels are weighted and combined into a plot of  $\phi_{CP}$

Each BDT/NN score window is weighted by  $A \cdot S / (S+B)$ , being A the “average asymmetry”:

$$A = \frac{1}{N_{bins}} \sum \frac{|CP^{even} - CP^{odd}|}{|CP^{even} + CP^{odd}|}$$

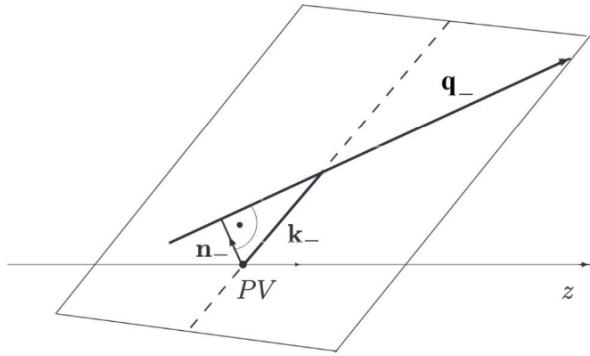
Background is subtracted from data.  
(Grey band: unc. on subtracted bkg.)

$H \rightarrow \tau\tau$  decays consistent with SM.  
CP-even case preferred over CP-odd case with  $3.2\sigma$  ( $2.3\sigma$  expected).



# Higgs CP in $H \rightarrow \tau\tau$ : $\phi_{CP}$ reconstruction

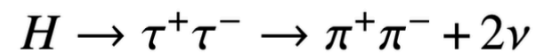
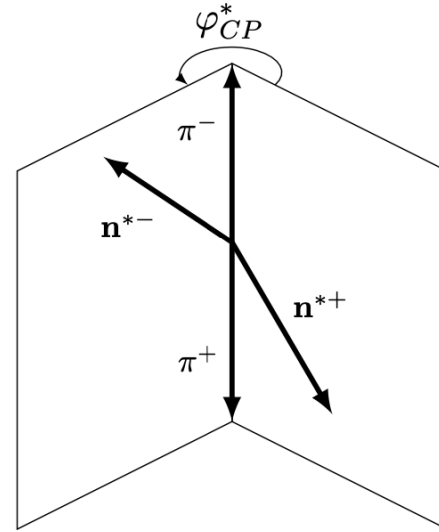
## $H \rightarrow \tau\tau$ decay CP



Impact parameter

directional distance of closest approach of charged particle's track to reconstructed PV of the event

4-vectors boosted to the rest frame of visible di- $\tau$  Zero Momentum Frame (e.g. two decay charged particles)

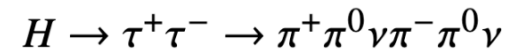
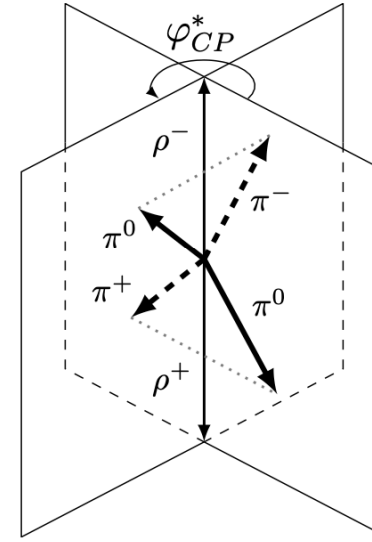


impact parameter

$$\varphi^* = \arccos(\hat{\mathbf{n}}_{\perp}^{*+} \cdot \hat{\mathbf{n}}_{\perp}^{*-})$$

$$O_{CP}^* = \hat{\mathbf{q}}^{*-} \cdot (\hat{\mathbf{n}}_{\perp}^{*+} \times \hat{\mathbf{n}}_{\perp}^{*-})$$

$$\varphi_{CP}^* = \begin{cases} \varphi^* & \text{if } O_{CP}^* \geq 0 \\ 360^\circ - \varphi^* & \text{if } O_{CP}^* < 0 \end{cases}$$

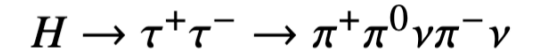
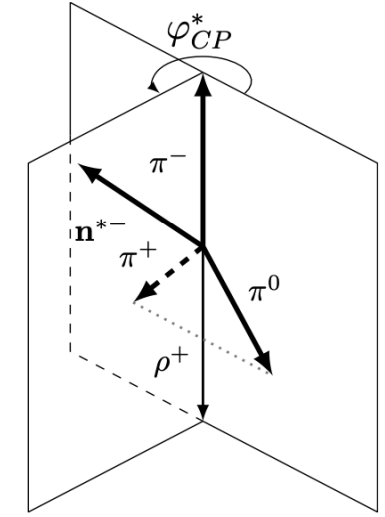


$\rho$  decay plane

$$\varphi^* = \arccos(\hat{\mathbf{q}}_{\perp}^{*0+} \cdot \hat{\mathbf{q}}_{\perp}^{*0-})$$

$$O_{CP}^* = \hat{\mathbf{q}}^{*-} \cdot (\hat{\mathbf{q}}_{\perp}^{*0+} \times \hat{\mathbf{q}}_{\perp}^{*0-})$$

$$\varphi^{*'} = \begin{cases} \varphi^* & \text{if } O_{CP}^* \geq 0 \\ 360^\circ - \varphi^* & \text{if } O_{CP}^* < 0 \end{cases} \quad \varphi_{CP}^{*'} = \begin{cases} \varphi^{*'} & \text{if } y_+^\rho y_-^\rho \geq 0 \\ \varphi^{*'} + 180^\circ & \text{if } y_+^\rho y_-^\rho < 0 \end{cases} \quad y_{\pm}^\rho = \frac{E_{\pi^\pm} - E_{\pi^0}}{E_{\pi^\pm} + E_{\pi^0}}$$



impact parameter +  
 $\rho$  decay plane

# CP parametrization for HVV and Hgg couplings

## ATLAS parametrisation

- Lagrangian in Higgs characterisation framework

$$\mathcal{L}_{eff} = H \left\{ c_\alpha \kappa_{SM} \left[ \frac{1}{2} \frac{2m_V^2}{v} Z_\mu Z^\mu + g_{HWW} W_\mu W^\mu \right] - \frac{1}{4} \frac{1}{\Lambda} s_\alpha \kappa_{AZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} - \frac{1}{2} \frac{1}{\Lambda} s_\alpha \kappa_{AWW} W_{\mu\nu}^+ \tilde{W}^{-\mu\nu} \right\}$$

$$\mathcal{L}_0^{\text{loop}} = -\frac{1}{4} \left( \kappa_{Hgg} g_{Hgg} G_{\mu\nu}^a G^{a,\mu\nu} + \kappa_{Agg} g_{Hgg} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \right) H,$$

- $k_{AVV}/k_{HVV}$  or similar extracted from the fit
- Other parametrisation in VBF  $H \rightarrow \tau\tau$  which has CP-odd contribution parametrised by  $\tilde{d}$

$$\tilde{d} = \frac{1}{4} \frac{v}{\Lambda} \frac{k_{AVV}}{k_{SM}} \tan \alpha$$

## CMS parametrisation

Scattering amplitude:

$$A(\text{HVV}) = \frac{1}{v} \left[ a_1^{\text{VV}} + \frac{\kappa_1^{\text{VV}} q_{V1}^2 + \kappa_2^{\text{VV}} q_{V2}^2}{(\Lambda_1^{\text{VV}})^2} + \frac{\kappa_3^{\text{VV}} (q_{V1} + q_{V2})^2}{(\Lambda_Q^{\text{VV}})^2} \right] m_{V1}^2 \epsilon_{V1}^* \epsilon_{V2}^* + \frac{1}{v} a_2^{\text{VV}} f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + \frac{1}{v} a_3^{\text{VV}} f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu},$$

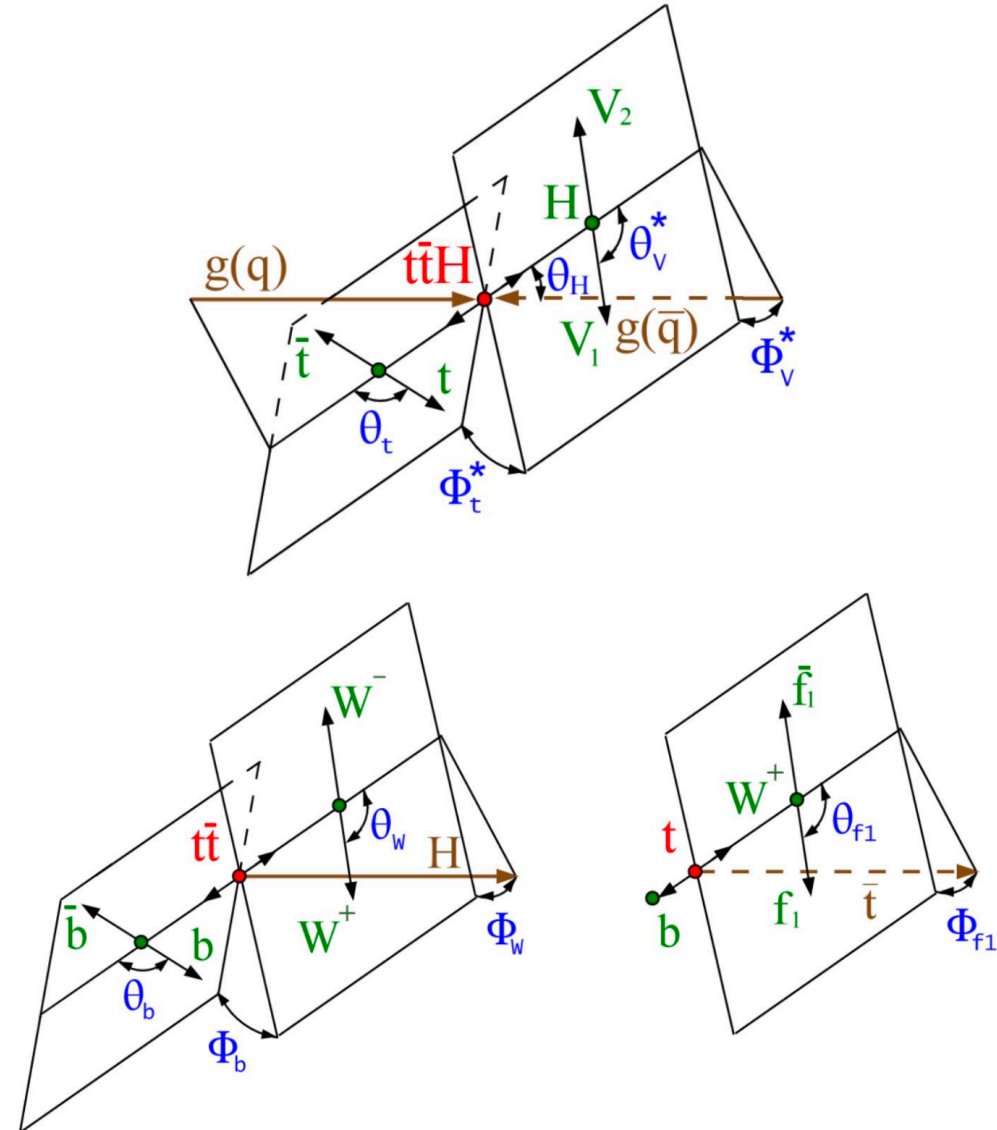
$f_{a3}$  parameter extracted from the fit (ratio of cross sections)

$$f_{a3}^{\text{ggH}} = \frac{|a_3^{\text{gg}}|^2}{|a_2^{\text{gg}}|^2 + |a_3^{\text{gg}}|^2} \text{sign} \left( \frac{a_3^{\text{gg}}}{a_2^{\text{gg}}} \right).$$

# ttH CP couplings

- (i)  $m_{t\bar{t}H}$ : invariant mass of the  $t\bar{t}H$  system;
- (ii)  $\theta_H$ : angle between the  $H$  boson direction and the incoming partons in the  $t\bar{t}H$  frame;
- (iii)  $\theta_V^*$ : angle of the  $H \rightarrow VV(f\bar{f})$  decay with respect to the opposite  $t\bar{t}$  direction in the  $H$  frame;
- (iv)  $\Phi_V^*$ : angle between the production plane, defined by incoming partons and  $H$ , and  $H \rightarrow VV(f\bar{f})$  decay plane;
- (v)  $\theta_t$ : angle between the top-quark direction and the opposite Higgs direction in the  $t\bar{t}$  frame;
- (vi)  $\Phi_t^*$ : angle between the decay planes of the  $t\bar{t}$  system and  $H \rightarrow VV(f\bar{f})$  in the  $t\bar{t}H$  frame;
- (vii)  $m_{t\bar{t}}$ : invariant mass of the  $t\bar{t}$  system;
- (viii)  $\theta_W$ : angle between  $W^+$  and opposite of the  $b\bar{b}$  system in the  $W^+W^-$  frame;
- (ix)  $\Phi_W$ : angle between the production  $(b\bar{b})(W^+W^-)H$  plane and the plane of the  $W^+W^-$  system in the  $t\bar{t}$  frame;
- (x)  $\theta_b$ : angle between the  $b$  quark and opposite of the  $W^+W^-$  system in the  $b\bar{b}$  frame;
- (xi)  $\Phi_b$ : angle between the planes of the  $b\bar{b}$  and  $W^+W^-$  systems in the  $t\bar{t}$  frame;
- (xii)  $m_{Wb1}$  or  $m_{Wb2}$ : invariant mass of the  $W^+b$  or  $W^-b$  system;
- (xiii)  $\theta_{f1}$  or  $\theta_{f2}$ : angles between fermion direction and opposite of the  $b$  or  $\bar{b}$  quark in the  $W^+$  or  $W^-$  frame;
- (xiv)  $\Phi_{f1}$  or  $\Phi_{f2}$ : angle between the  $W^+$  or  $W^-$  decay plane and the  $\bar{t}W^+b$  or  $tW^-b$  plane in the  $t$  or  $\bar{t}$ -quark frame;
- (xv)  $m_{f1\bar{f}1}$  or  $m_{f2\bar{f}2}$ : invariant mass of the  $f_1\bar{f}_1$  or  $f_2\bar{f}_2$  system.

Pheno paper PRD94,055023 (2016)





# ttH CP couplings

Pheno paper PRD94,055023 (2016)

$$f_{CP} = \frac{|\tilde{\kappa}_f|^2}{|\kappa_f|^2 + |\tilde{\kappa}_f|^2}, \quad \phi_{CP} = \arg(\tilde{\kappa}_f/\kappa_f),$$

$$= \sin^2\alpha \quad = 0 \text{ or } \pi.$$

$$\mathcal{P}_{\text{sig}}(\vec{x}_i; f_{CP}, \phi_{CP}) = (1 - f_{CP})\mathcal{P}_{0+}(\vec{x}_i) + f_{CP}\mathcal{P}_{0-}(\vec{x}_i)$$

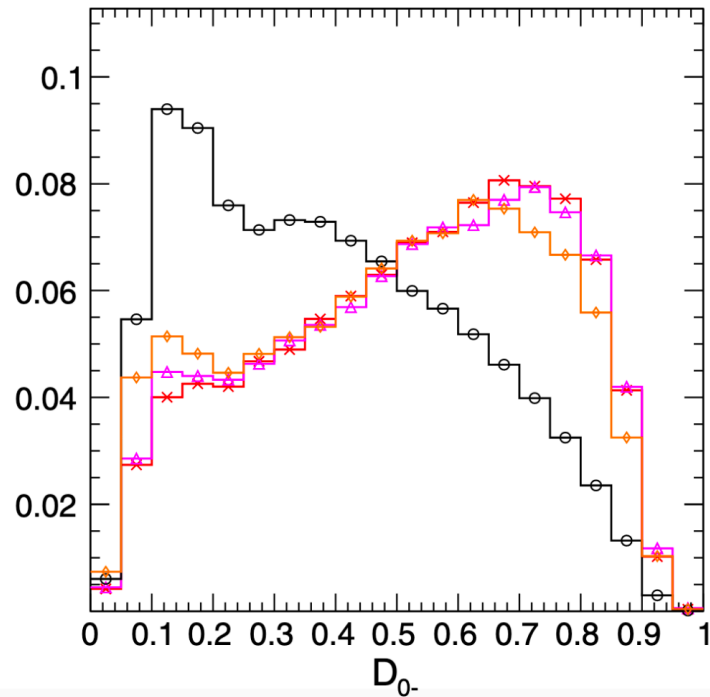
$$+ \sqrt{f_{CP}(1 - f_{CP})}(\mathcal{P}_{\text{int}}(\vec{x}_i) \cos \phi_{CP}$$

$$+ \mathcal{P}_{\text{int}}^\perp(\vec{x}_i) \sin \phi_{CP}), \quad (\ell$$

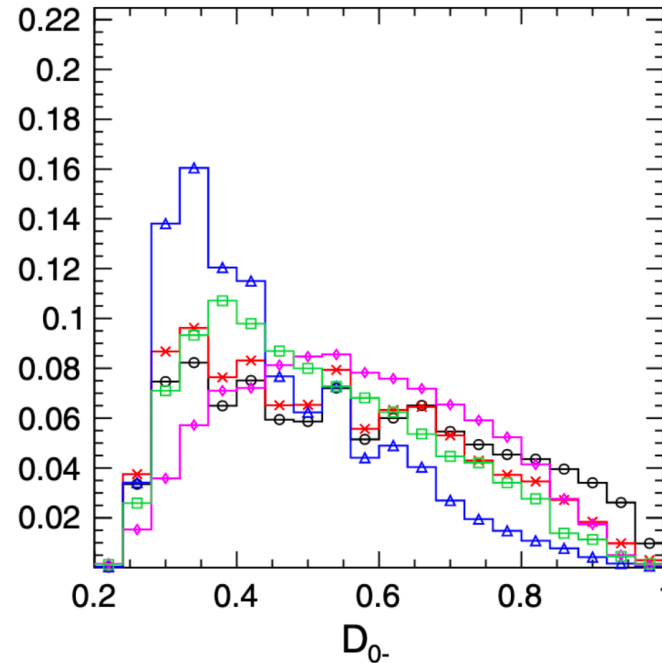
$$\mathcal{D}_{0-} = \frac{\mathcal{P}_{0+}(\vec{\Omega})}{\mathcal{P}_{0+}(\vec{\Omega}) + \mathcal{P}_{0-}(\vec{\Omega})}$$

$$\mathcal{D}_{CP} = \frac{\mathcal{P}_{\text{int}}(\vec{\Omega})}{\mathcal{P}_{0+}(\vec{\Omega}) + \mathcal{P}_{0-}(\vec{\Omega})}$$

$$\mathcal{D}_{CP}^\perp = \frac{\mathcal{P}_{\text{int}}^\perp(\vec{\Omega})}{\mathcal{P}_{0+}(\vec{\Omega}) + \mathcal{P}_{0-}(\vec{\Omega})}$$



Hff-induced ttH CP-odd (red, magenta)  
 Hff-induced ttH CP-even (black)  
 $tt\gamma\gamma$  background (orange)

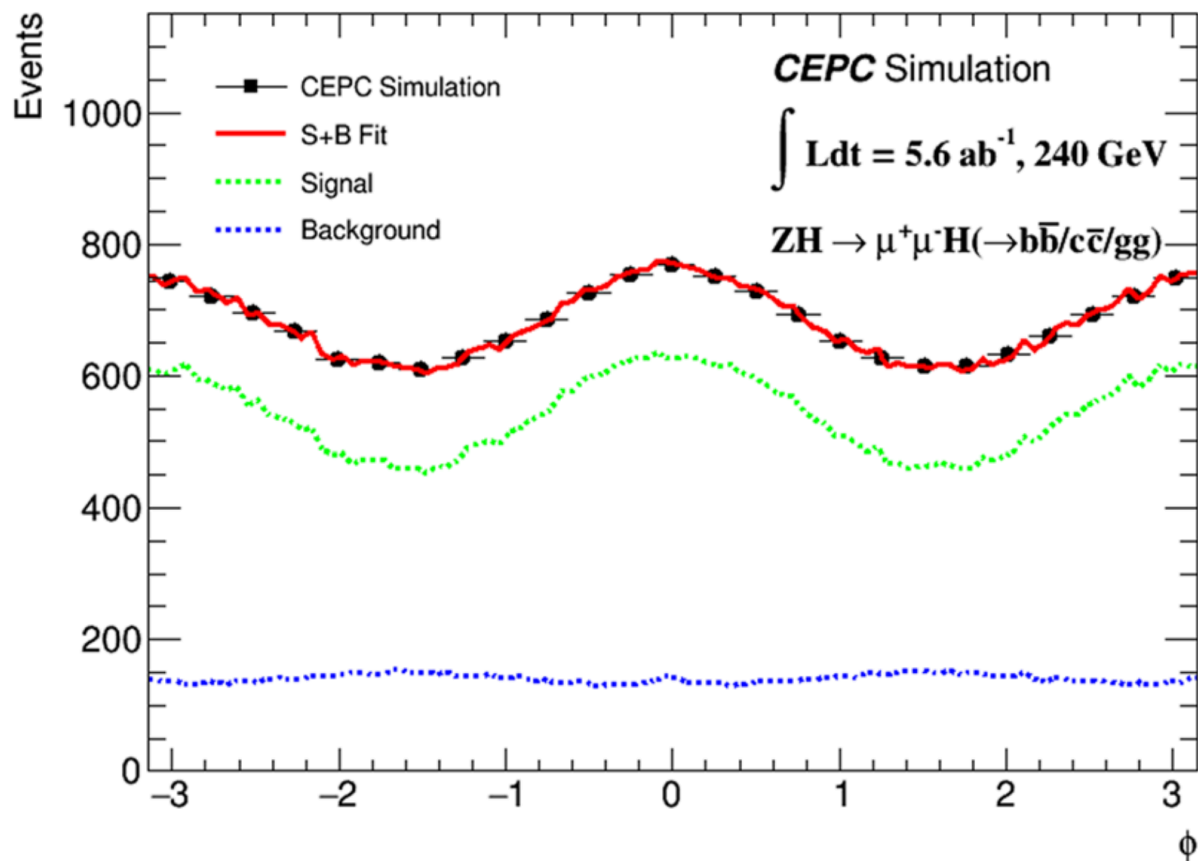


Hff-induced tH CP-odd (red)  
 Hff-induced tH CP-even (blue)  
 HVV-induced tH considered background (black)

**Only  $D_{0-}$  discriminant is used in CMS analysis (using a BDT instead of using MEM)**

**$D_{CP}$  requires flavor of tt decay particles, not possible in full hadronic and semi-leptonic, dropped in this analysis**

## Fit on $\phi$



**Table 2** Summary of  $1\sigma$  and  $2\sigma$  bounds on  $\hat{\alpha}_{A\tilde{Z}}$  and  $\hat{\alpha}_{Z\tilde{Z}}$  from various analyses by fitting to  $\phi$  and fitting to  $\omega$  through  $\mu^+\mu^-H$  process which is shown in Sects. 5.1 and 5.2.

	$\hat{\alpha}_{A\tilde{Z}} (\times 10^{-2})$	$\hat{\alpha}_{Z\tilde{Z}} (\times 10^{-2})$
$\omega$ -fitting		
68% CL( $1\sigma$ )	[-4.16, 3.88]	[-1.06, 1.00]
95% CL( $2\sigma$ )	[-8.10, 7.82]	[-2.06, 2.01]
$\phi$ -fitting		
68% CL( $1\sigma$ )	[-4.42, 4.21]	[-1.35, 1.24]
95% CL( $2\sigma$ )	[-8.66, 8.45]	[-2.62, 2.51]