

# Top mass reconstruction in ATLAS

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On  
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JOHANNES GUTENBERG  
UNIVERSITÄT MAINZ

GEFÖRDERT VOM



Bundesministerium  
für Bildung  
und Forschung



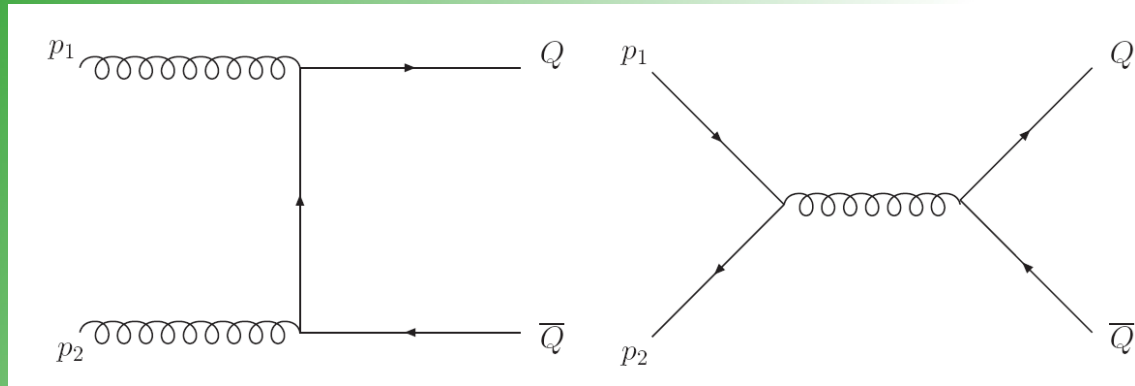
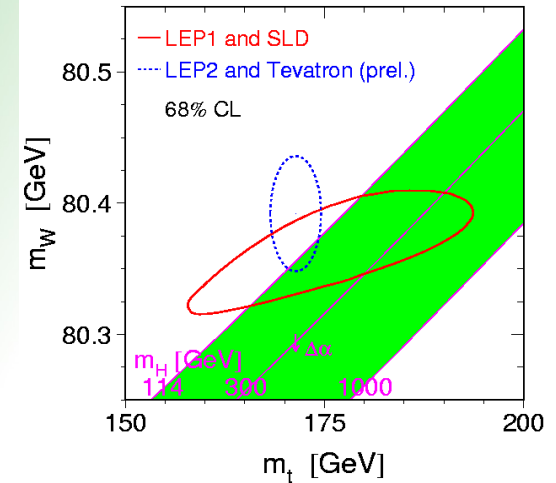
FSP 101

ATLAS



# Motivation

- Heaviest yet observed particle (decays as a free quark)
- Large electroweak radiative corrections
- Consistency of SM (new couplings?)
- Higgs mass limits



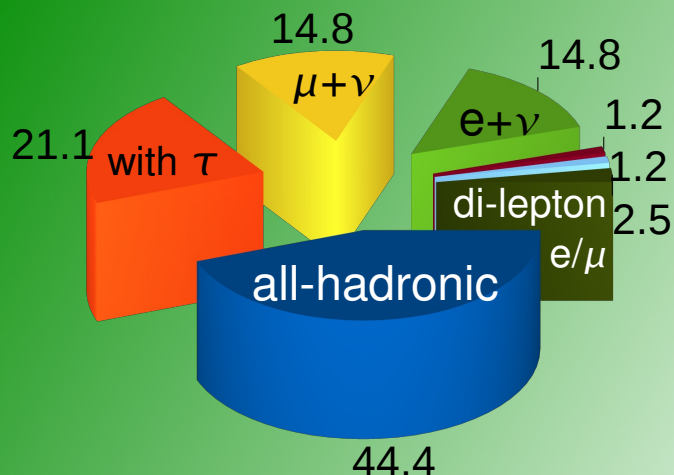
Production via  $q\bar{q}$  and  $gg$  (LO)



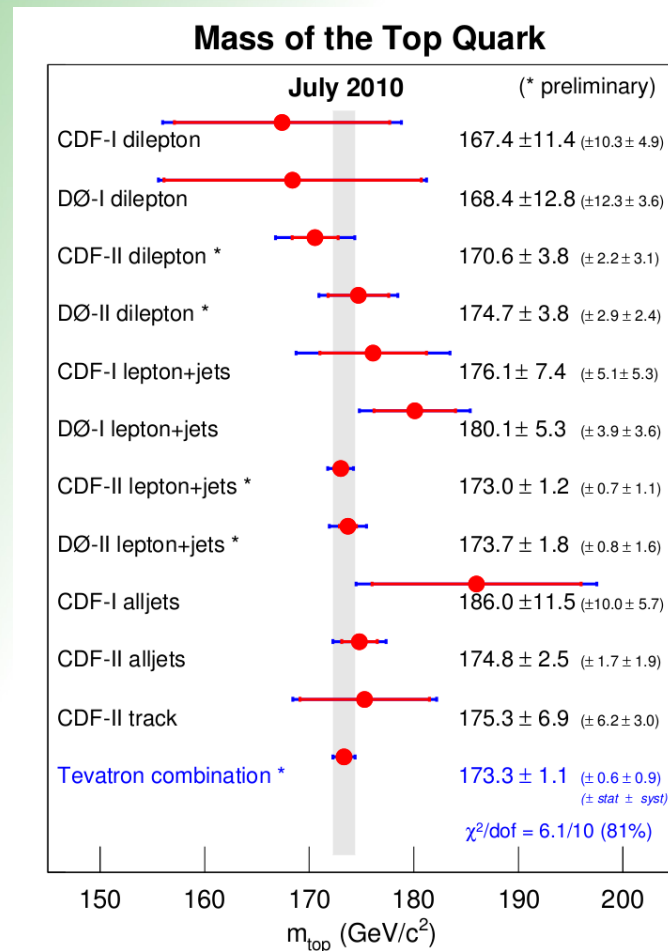
# Overview on top mass

- Almost 100%:  $t\bar{t}$  →  $b\bar{b}W$

W decays determine event signature:



- Most precise measurements so far:  
lepton ( $\mu/e$ ) + jets channel (30%)
- Largest systematic uncertainty: jet energy scale (JES)
- ATLAS presented 3 complementary measurements to differently assess the JES systematic (ATLAS-CONF-2011-033)





# ATLAS and LHC

- LHC in 2010:
  - Total delivered, integrated Luminosity:  $\sim 50 \text{ pb}^{-1}$
  - Highest instantaneous Luminosity:  $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
  - Max. #Filled bunches: 368 (stable beams)

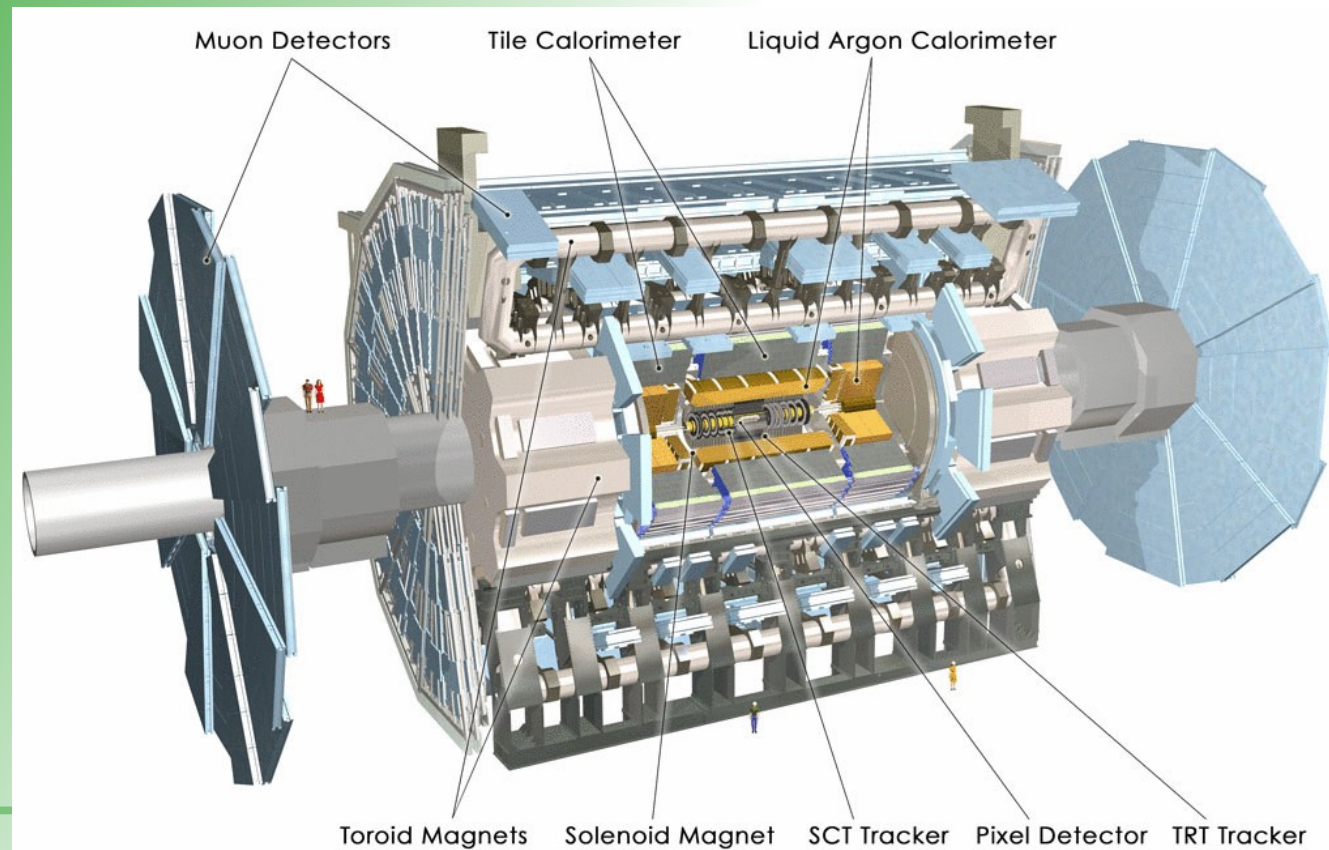
- ATLAS:

Max. #Colliding  
bunches: 348

$$L = 35.3 \pm 1.2 \text{ pb}^{-1}$$

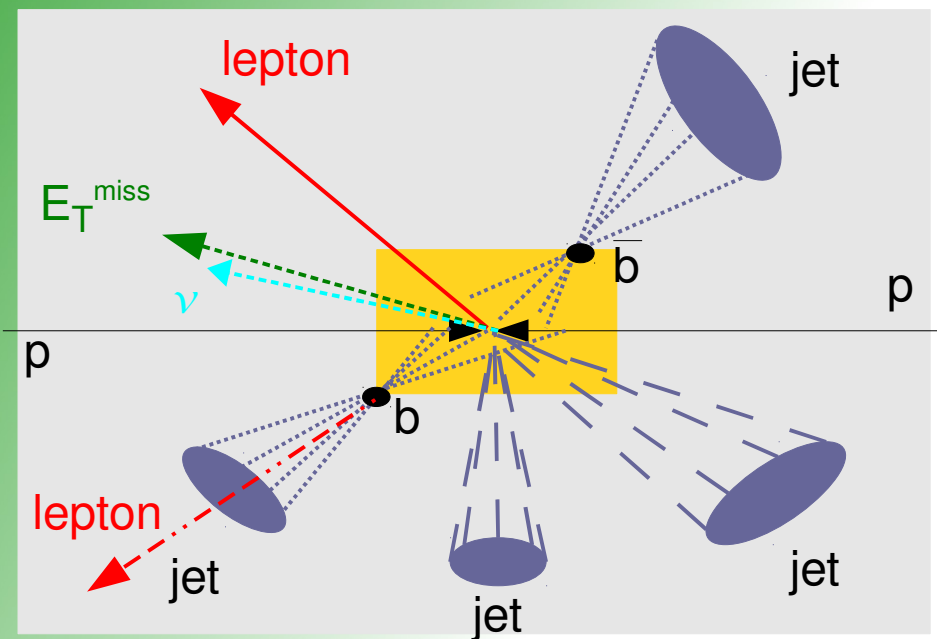
Max. #pileup events:  
 $\sim 4.7$

For details please refer to  
Peter Loch's talk





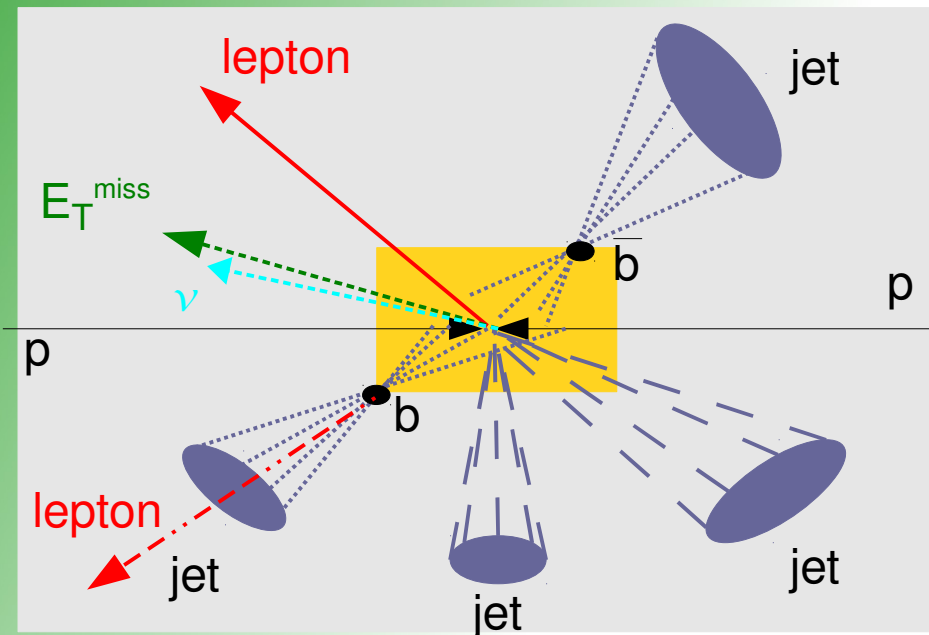
# Event topology and inputs





# Event topology and inputs

Trigger: lepton trigger  
(fully efficient at 20 GeV)

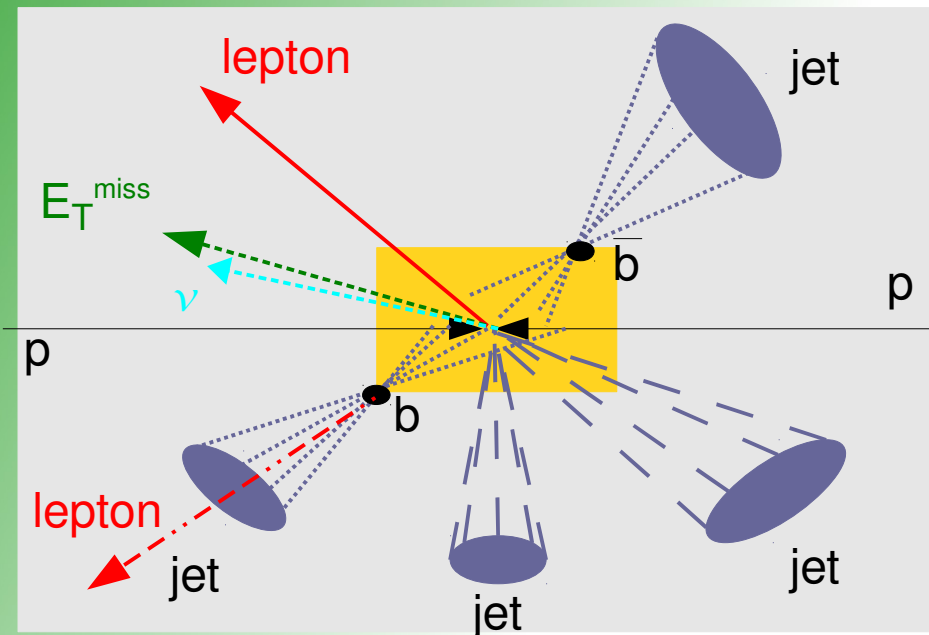




# Event topology and inputs

Trigger: lepton trigger  
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Primary vertex with at  
least 5 charged particles



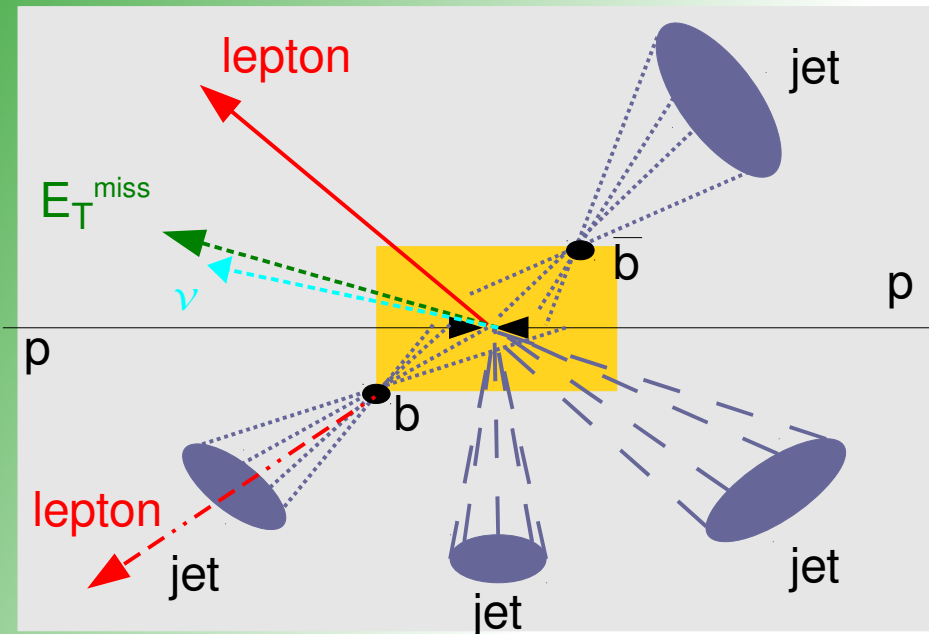
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**Electrons:** isolated,  
no high- $p_T$  and  
isolated muon,  
 $p_T > 20$  GeV  
 $|\eta| < 1.37$  or  
 $1.52 < |\eta| < 2.47$

**Muons:** isolated,  
no high- $p_T$  and isolated  
electron,  
 $p_T > 20$  GeV  
 $|\eta| < 2.5$   
 $dR(\mu, \text{jet}) > 0.4$





# Event topology and inputs

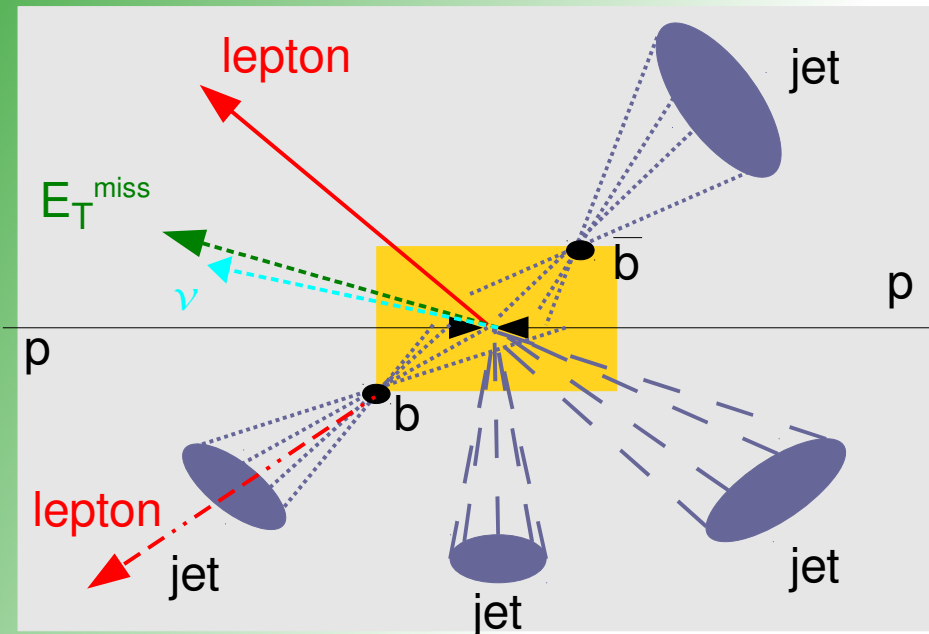
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**Jet-lepton removal:**  
Fake **jets** from electrons  
**Muons** from semi-lept.  
decay

**Electrons:** isolated,  
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 $p_T > 20$  GeV  
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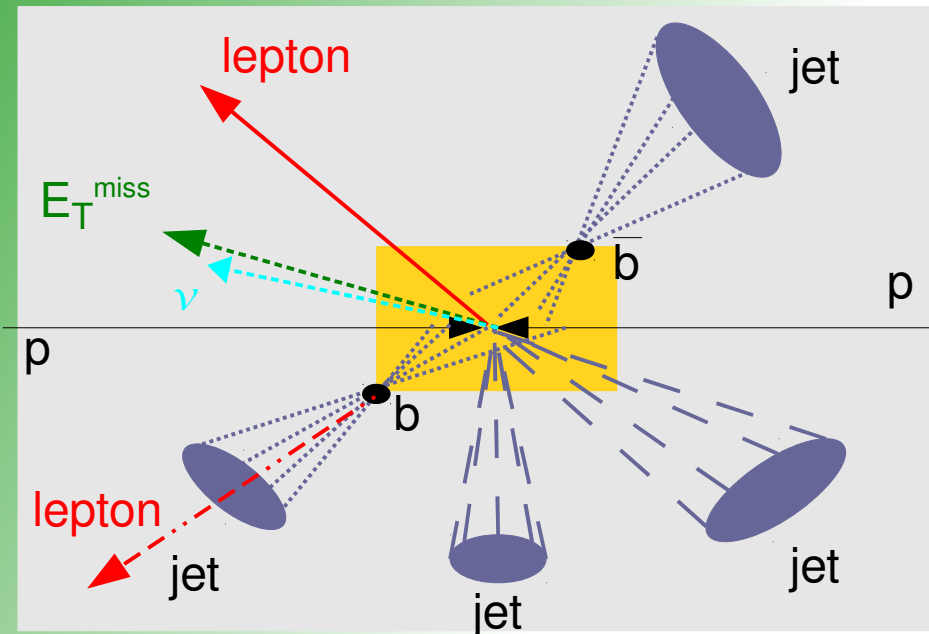
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$E_T^{\text{miss}}$ :  
calo cells+muons  
Object-specific calibration  
Electron (Muon) channel:  
 $E_T^{\text{miss}} > 35$  (20) GeV

**Electrons:** isolated,  
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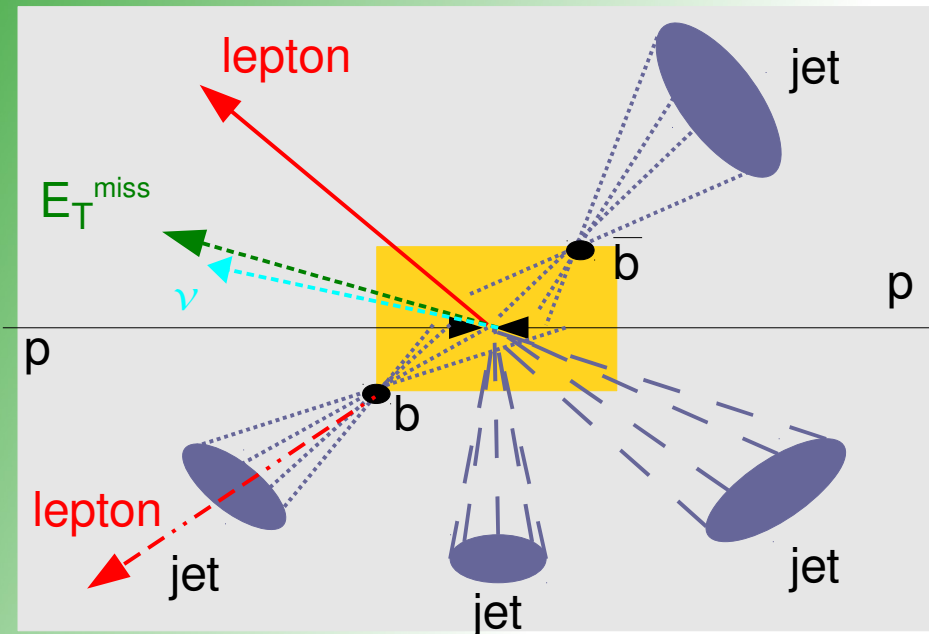
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 $E_T^{\text{miss}} > 35$  (20) GeV

**W transverse mass:**  
QCD bkg suppression  
electron-channel:  
 $m_W^T > 25$  GeV  
muon-channel:  
 $E_T^{\text{miss}} + m_W^T > 60$  GeV

**Electrons:** isolated,  
no high-pT and  
isolated muon,  
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Primary vertex with at  
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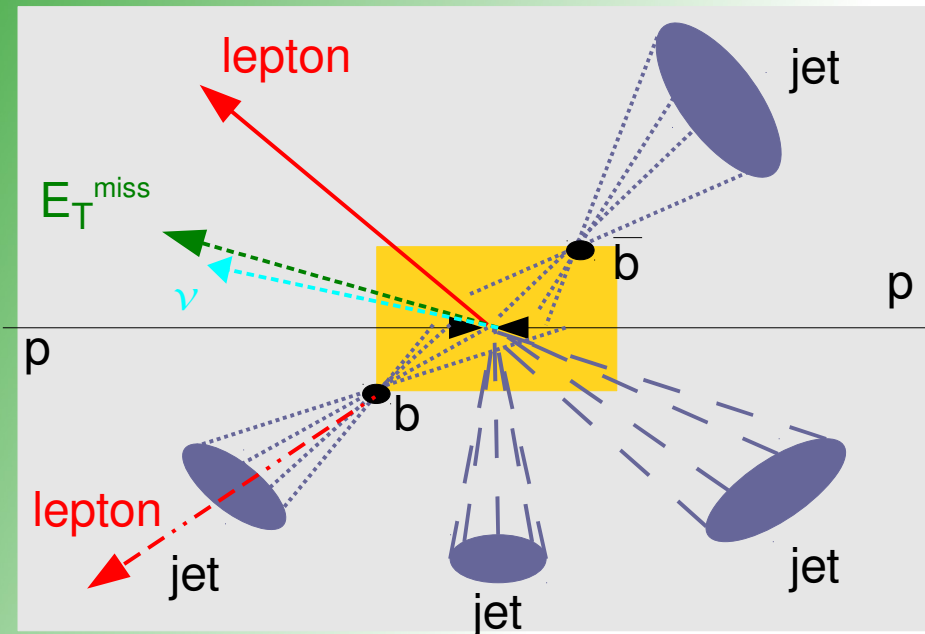
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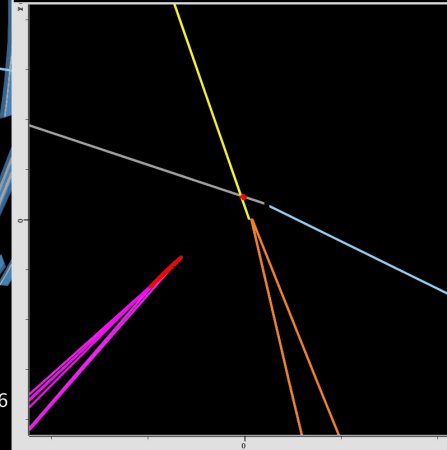
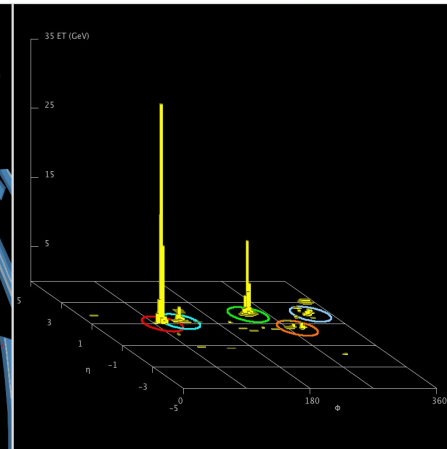
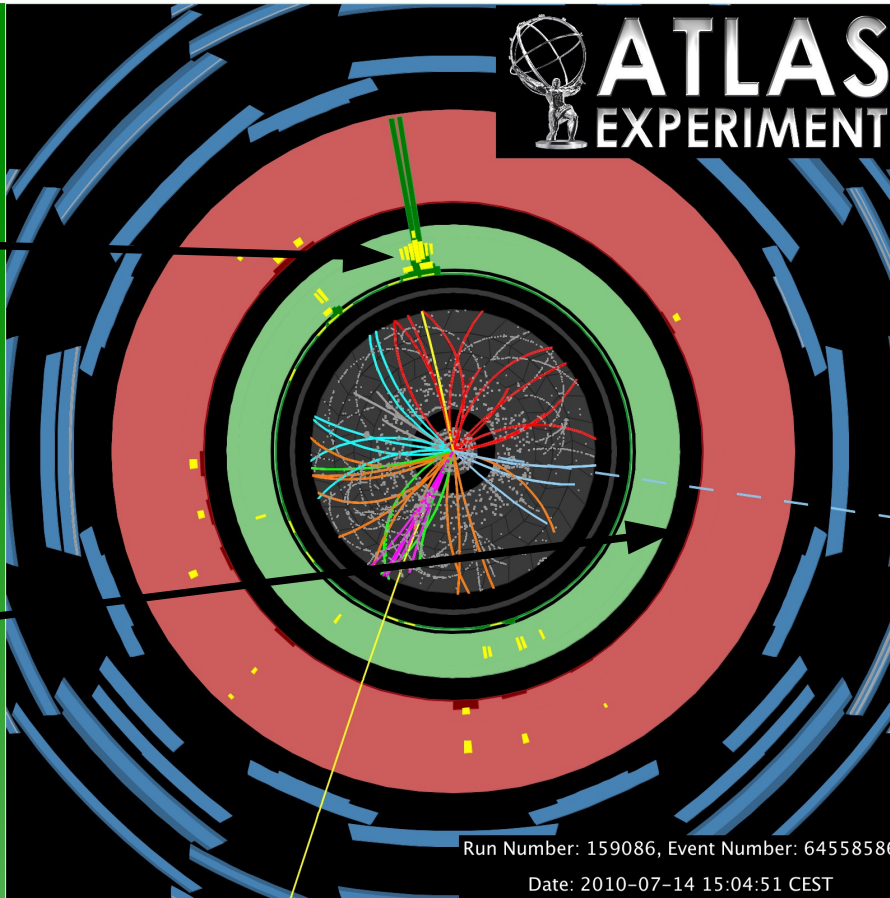


**Jets:** anti- $k_t$   $R=0.4$   
Had. scale calib.  $(p_T, \eta)$   
 $|\eta| < 2.5$ ,  $p_T > 25$  GeV  
 $\# \text{jets} \geq 4$   
At least 1 b-tagged jet  
No "bad" jets in event

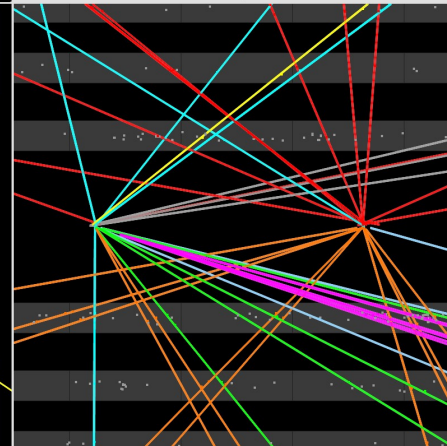
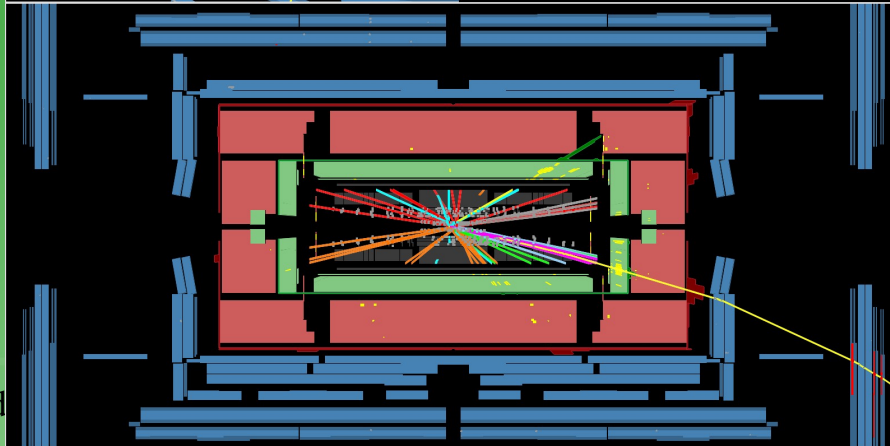
# Event display: electron plus jets

Electron

EtMiss



Secondary vertex of the b-tagged jet



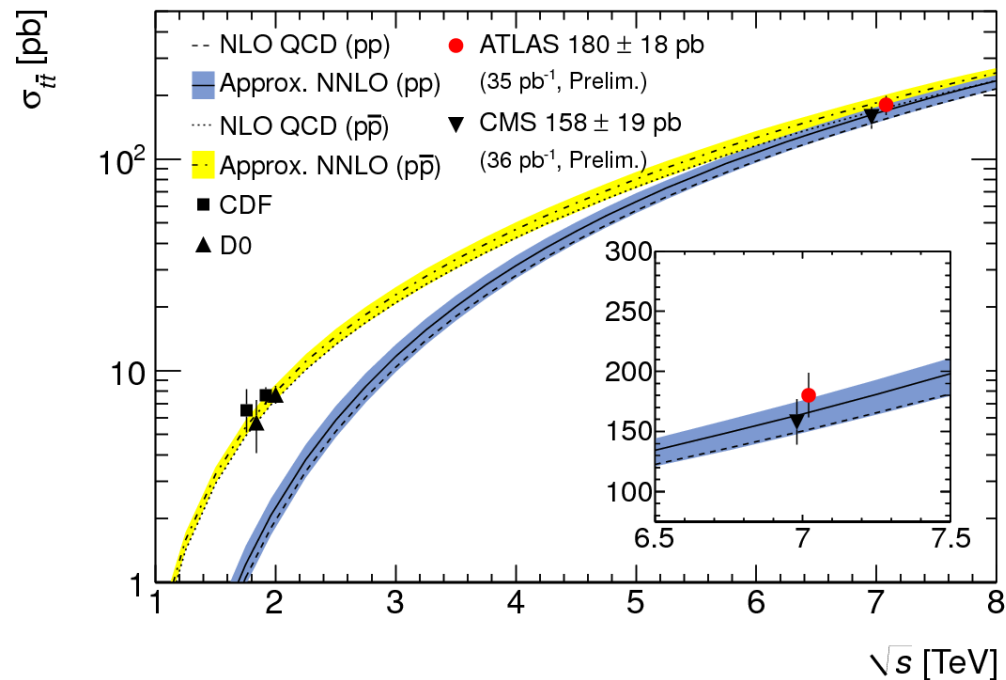
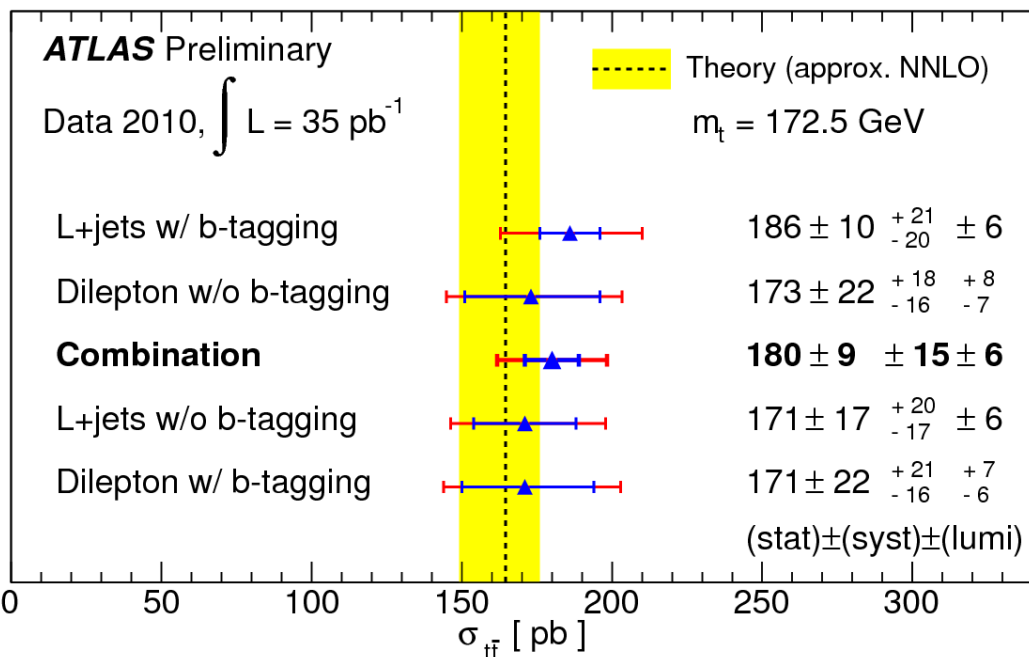
High pT vertex + Pileup vertex



# Top cross section

- With these inputs we can measure top pair production in good agreement with NNLO (with and without b-tagging)

Combination of Tevatron and LHC measurements strengthen our confidence in our understanding



➔ Measure the top-quark mass from these events



# Top mass measurements

- Short overview of template methods at ATLAS:

- BASE-LINE
- **1-D fit of  $R_{32} = \frac{m_{\text{top}}^{\text{reco}}}{m_{\text{W}}^{\text{reco}}}$  :**  
smallest expected uncertainty, stability against JES variations, based on the resolution on  $m_{\text{top}}$
  - 2-D fit of  $m_{\text{top}}^{\text{reco}}$  and Jet energy scale factor (JSF)
  - 1-D kinematic likelihood fitter: using all decay products

- Complementary methods: cross check, address systematics differently, improve knowledge
- As long not stated differently: presenting baseline method

# Top mass measurements

- Short overview of template methods at ATLAS:

BASE-LINE {

- 1-D fit of  $m_{top}^{reco}$  with smallest variation

yield is the smallest

Hadronic top reco:  
4-vector sum with highest  $p_T$   
W boson reco:  
mass window  
 $60 \text{ GeV} < m_W^{reco} < 100 \text{ GeV}$

Jet-triplet (had. top):  
> rejected if 2 jets are b-tagged  
> No b-tag: chose jets with smallest dR in top rest-frame

Smallest event yield from all methods

- 2-D fit of  $m_{top}^{reco}$  and Jet energy scale factor (JSF)
  - 1-D kinematical likelihood fitter to all decay products
- Complementary methods: cross check, address systematics differently, improve knowledge
  - As long not stated differently: presenting baseline method



# Background and Signal

- $t\bar{t}$  signal (MC@NLO) several  $\text{fb}^{-1}$
- Background (bkg): other decay channels, single-top (s-top), di-boson, W/Z+jets processes and QCD multijet
- Except QCD bkg all others estimated by MC (Herwig, Alpgen): low background
- QCD background estimated from data

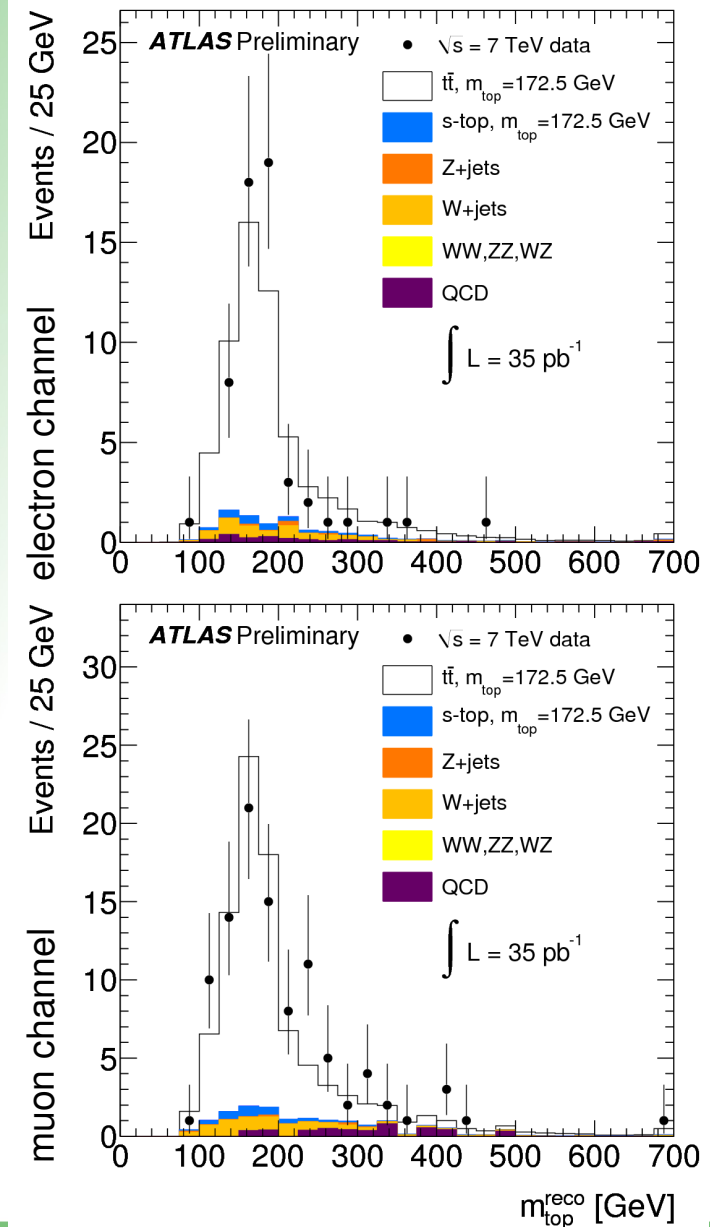
MC: electron (muon) channel

$S/B = 52.6/9.1$  ( $77.3/14.9$ ) = 5.8 (5.2)

Observed data events: 56 (99)

Data well described by sum of signal and background

(List of details in backup slides)



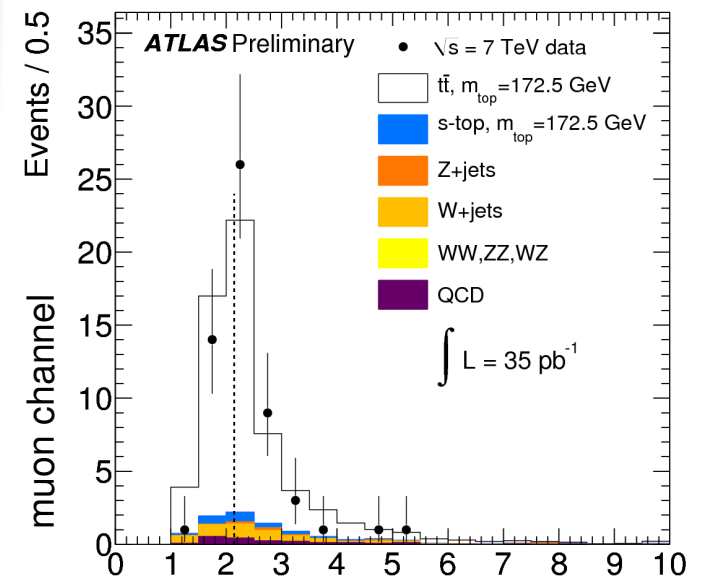
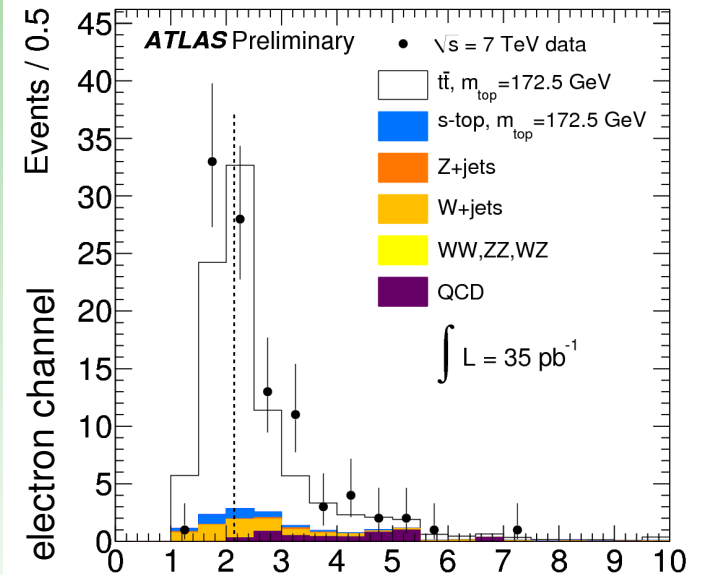
# 1-D $R_{32}$ baseline method

- Likelihood fit of the  $R_{32}$  templates to data: event-by-event ratio of had. top mass  $m_{\text{top}}^{\text{reco}}$  and corresponding W boson mass  $m_W^{\text{reco}}$
- Different  $m_{\text{top}}$  assumptions: 160, 170, 172.5, 180 and 190 GeV

Steps:

- Template parametrization (signal, bkg)
- Likelihood construction
- Pseudo-experiments

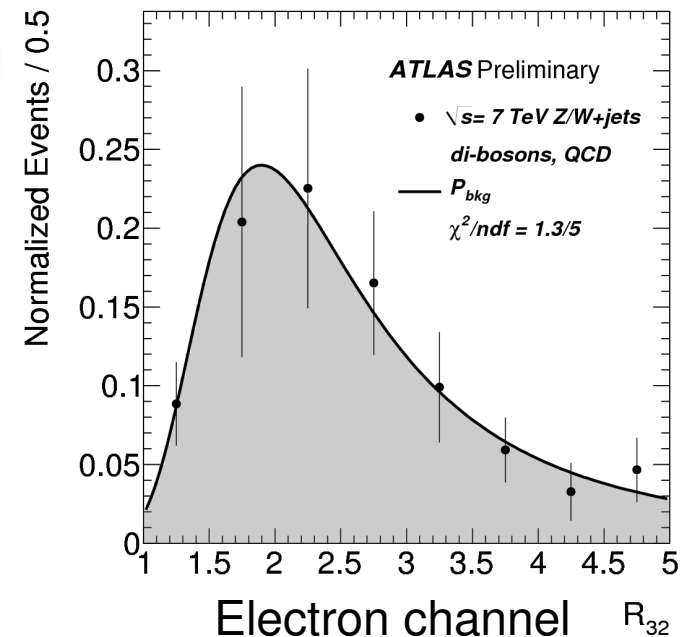
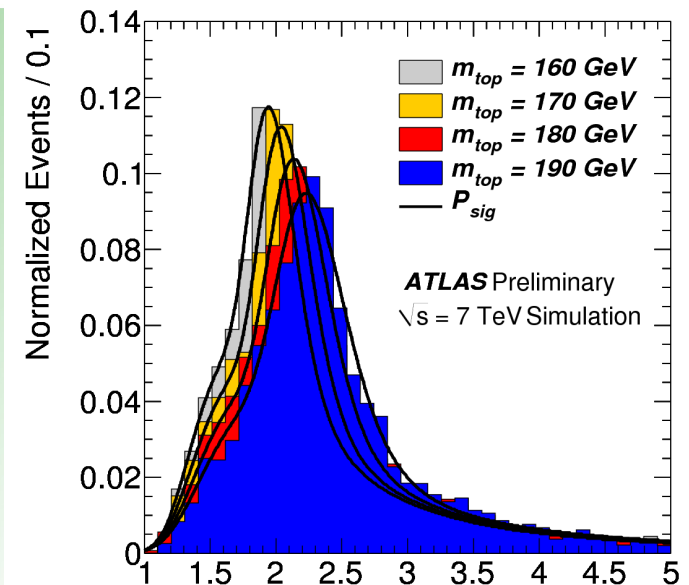
Data well described by sum of signal and background



$$R_{32} = m_{\text{top}}^{\text{reco}} / m_W^{\text{reco}}$$

# Template parametrizations

- Each channel has its own parametrization
- Signal  $P_{\text{sig}}(R_{32}; m_{\text{top}})$  :
  - > derived for all  $m_{\text{top}}$  dependent samples (include single-top events)
  - > description by the sum of a ratio of two Gaussians and a Landau function
  - > each parameter has a linear dependence on the top-quark mass
- Background  $P_{\text{bkg}}(R_{32}; m_{\text{top}})$  :
  - > each background sample is well represented by a Landau function
  - > individual contributions are summed into one parametrization (for all  $m_{\text{top}}$  samples)





# Likelihood fit

- Contains 3 parts: account for shape of  $R_{32}$  distribution ( $L_{\text{shape}}(R_{32}; m_{\text{top}})$ ), relative relation of signal and background ( $L_{n_s+n_b}$ ) in  $N$  observed events, constraint on background events ( $L_{\text{bkg}}$ )

$$L(R_{32}; m_{\text{top}}) = \prod \frac{n_s P_{\text{sig}}(R_{32}; m_{\text{top}})_i + n_b P_{\text{bkg}}(R_{32})_i}{n_s + n_b} \times \frac{e^{-(n_s+n_b)} (n_s+n_b)^N}{N!} \times \exp\left\{-\frac{(n_b - n_b^{\text{pred}})^2}{2 \sigma_{n_b^{\text{pred}}}^2}\right\}$$

Product over  
all events  $N$

- Pseudo-experiments: are used to validate the chosen fitting approach as well as to evaluate systematic uncertainty effects on the result
- Validation: 50 pseudo-experiments for each input top-quark mass, observed events Poisson fluctuated, with  $35 \text{ pb}^{-1}$  integrated luminosity, good linearity between input and output top-quark mass (pull distributions are consistent with the expectation)

# Systematic uncertainties

- Each quantity of systematic uncertainty is varied by  $\pm 1\sigma \rightarrow$  pseudo-experiments corresponding to integrated luminosity of  $5 \text{ fb}^{-1}$
- Quoted systematic: quadratic sum of all contributions

Detailed list of uncertainties  
in backup slides

**Method:**  
calibration

**Theory uncertainties:**  
ISR/FSR (2.6 GeV)  
Proton PDF

**MC uncertainties:**  
Hadronisation (1 GeV)  
Pileup simulation  
Signal MC

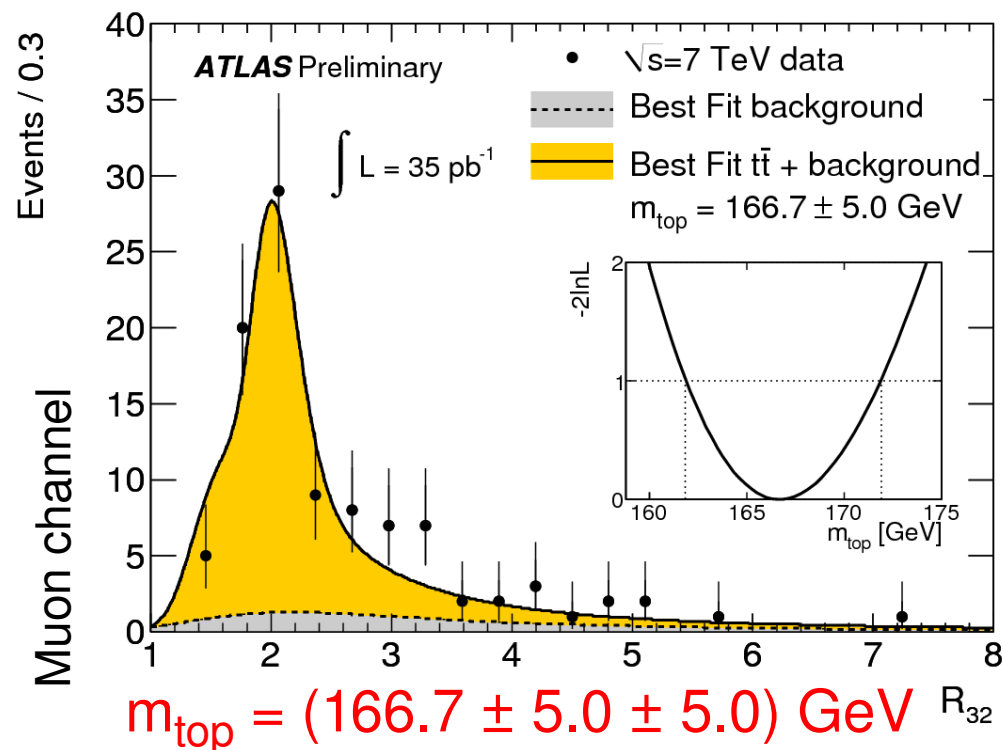
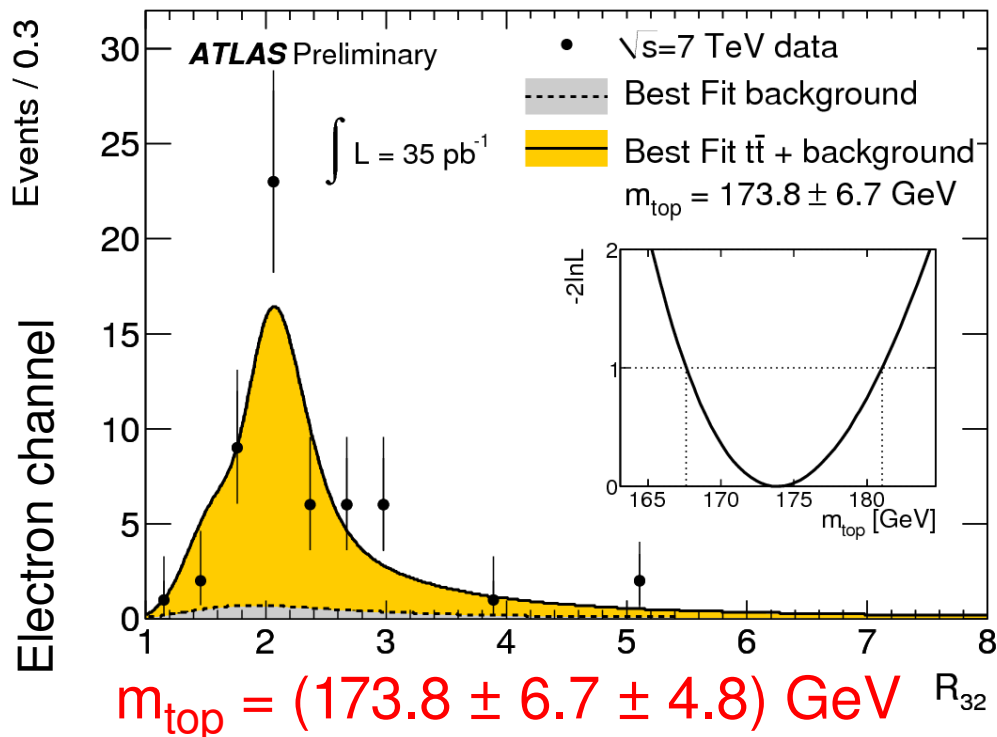
**Measurement:**  
JES (2.3 GeV)  
b-JES (2.5 GeV)  
B-tagging  
Jet energy resolution (1.1 GeV)  
Jet reco efficiency

**Background:**  
MC bkg estimates (1.7 GeV)  
QCD bkg estimates

**Total systematic uncertainty:**  
4.8 GeV (electron channel)  
5.0 GeV (muon channel)



# Results



- Good description of data
- Statistical uncertainty within expectations
- Both measurements are statistically consistent with each other and in agreement with the world average
- Combination:  $m_{\text{top}} = (169.3 \pm 4.0 \pm 4.9) \text{ GeV}$

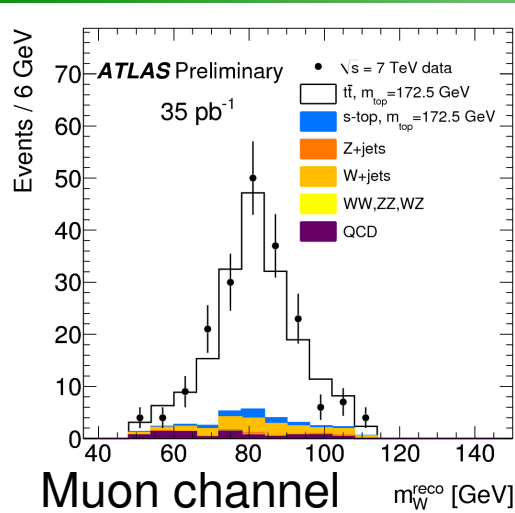
# Cross check: 2-D analysis

- Templates( $m_{\text{top}}(\text{input})$ ):  $m_{\text{top}}^{\text{reco}}$  and  $m_{\text{W}}^{\text{reco}}$  of the hadronic decaying top
- Global jet energy scale factor (JSF) determined mainly from  $m_{\text{W}}^{\text{reco}}$  distributions differences in data and MC
- Transfer JES uncertainty into additional statistical uncertainty
- Hadronic W boson decay candidate: fit the jet energies with the W mass constraint, minimal  $\chi^2$  determines the jet pair assigned to the W

W boson candidates:  
mass window  $\pm 3\sigma$   
Hadronic top jet-triplet:  
4-vector sum with  
highest  $p_{\text{T}}$

$$\chi^2 = \left[ \frac{E_{\text{jet1}}(1-\alpha_1)}{\sigma_{\text{jet1}}} \right]^2 + \left[ \frac{E_{\text{jet2}}(1-\alpha_2)}{\sigma_{\text{jet2}}} \right]^2 + \left[ \frac{M_{jj}(\alpha_1, \alpha_2) - m_{\text{W}}}{\Gamma_{\text{W}}} \right]^2 \longrightarrow \text{Determine } \alpha_i\text{'s (JSF)}$$

- Calculate hadronic top with the b-tagged jet in the event and the  $\alpha_i$ 's

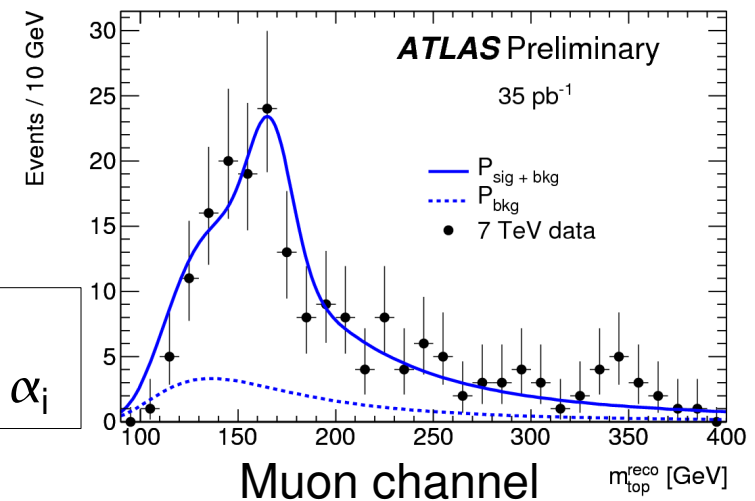


Template 1:  
W mass without the  $\alpha_i$

N events: 134 (120) in the  
electron (muon) channel

Template 2:  
Top mass with the  $\alpha_i$

PisaJet11





# 2-D analysis

- Pseudo-experiments verify unbiased reconstruction of  $m_{\text{top}}$  and JSF
- Same top mass samples as before (160-190 GeV) and JSF in the range (0.9-1.1)

$$m_{\text{top}} = (168.3 \pm 6.2 \pm 4.3) \text{ GeV (electron channel)}$$

$$m_{\text{top}} = (163.5 \pm 6.7 \pm 4.6) \text{ GeV (muon channel)}$$

$$m_{\text{top}} = (166.1 \pm 4.6 \pm 4.4) \text{ GeV (combined)}$$

- Fitted JSF:  $1.08^{+0.04(\text{stat})}_{-0.06(\text{stat})}$  ( $1.01^{+0.05(\text{stat})}_{-0.05(\text{stat})}$ ) in the electron (muon) channel
- Reduced JES systematic of **0.7 GeV** achieved but at a reduced statistical precision
- b-JES and ISR/FSR uncertainty same size as baseline method



# Cross check: kinematic fitter

- Template( $m_{\text{top}}(\text{input})$ ):  $m_{\text{top}}^{\text{reco}}$  obtained by a kinematic fit
- Method is using entire ttbar event
- Observed events: 157 (247) in the electron (muon channel)
- Likelihood contains (input 4j+l+EtMiss):

$$L = \text{Breit-Wigner}(W, \text{top}) \times \text{Transfer-Functions}(j, l, \nu) \times \text{Delta-Function}(b\text{-tag})$$

Constrains:

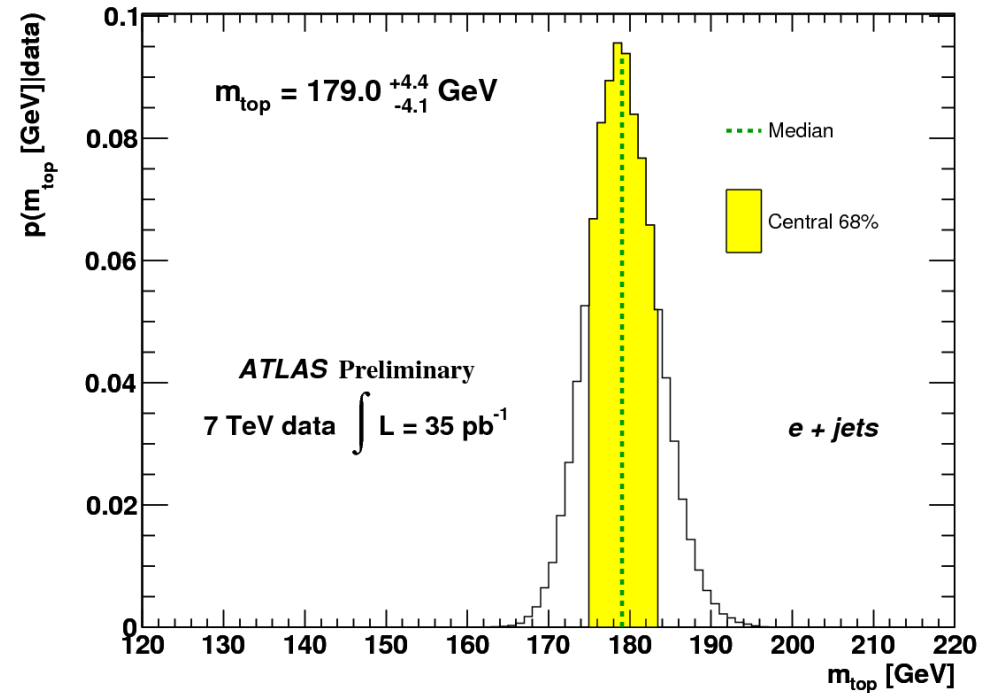
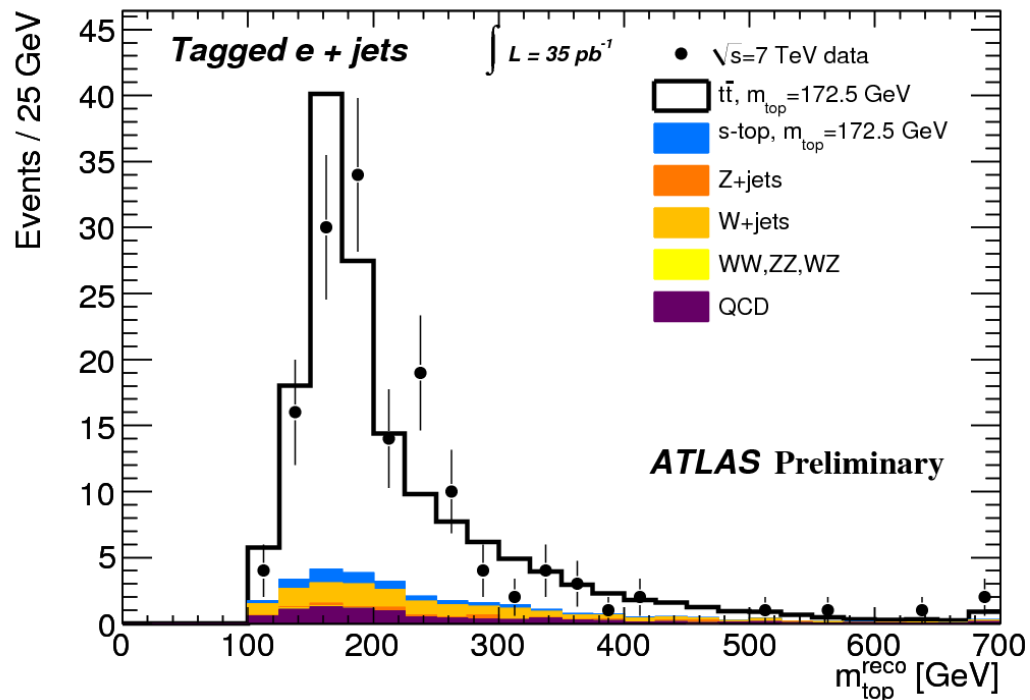
- > W boson mass (had. and lep.)
- > identity of had. and lep. top mass

resolution for jet energy, eta, phi,  
lepton energy,  $E_{\text{T}}^{\text{miss}}$  from signal MC

Reduce  
permutations

- Per event result estimator for  $m_{\text{top}}^{\text{reco}}$  which maximizes the likelihood
- Utilization of correlations and a high fitting efficiency (less combinatorial bkg) lead to a narrower  $m_{\text{top}}^{\text{reco}}$  distribution than the baseline method (but much more sensitive to JES variations)
- Pseudo-experiments show the linearity between output and input top mass

# Kinematical fitter



- Same top mass samples as before (160-190 GeV)
- data can be well described by signal and bkg description (no discrepancies between MC predictions and data)
- JES systematic: **6.6 GeV**, b-JES and ISR/FSR uncertainty same size as baseline method

$$m_{\text{top}}(e) = (179.0 \pm 4.3 \pm 7.5) \text{ GeV}$$

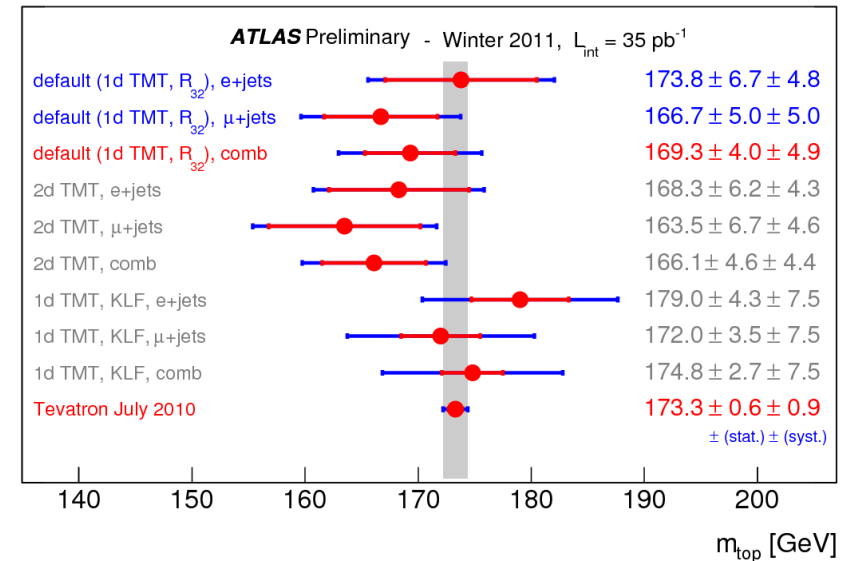
$$m_{\text{top}}(\mu) = (172.0 \pm 3.5 \pm 7.5) \text{ GeV}$$

**Combined:**

$$m_{\text{top}} = (174.8 \pm 2.7 \pm 7.5) \text{ GeV}$$

# Comparison of the measurements

- Results of all analyses (each channel) are consistent within uncertainties
- Muon channel: slightly smaller statistical uncertainties
- Systematic uncertainties are similar between channels
- With about  $1 \text{ fb}^{-1}$  the expected statistical uncertainty  $\sigma_{\text{stat}}$  (from current pseudo-experiments) will diminish to:  
 $0.7 \text{ GeV (1-D kin. fit)} < 1.3 \text{ GeV (1-D } R_{32} \text{ fit)} < 1.7 \text{ GeV (2-D fit)}$
- This order is reverted for the systematic uncertainties at our present level of understanding (especially of JES)
- With increasing luminosity the method that gives the best expected result will likely change





# Conclusions

- Baseline ATLAS measurement with integrated Luminosity of  $L = 35.3 \pm 1.2 \text{ pb}^{-1}$  by the event-by-event ratio of  $R_{32}$  is in agreement with the world average

$$m_{\text{top}} = (169.3 \pm 4.0 \pm 4.9) \text{ GeV}$$

- Three complementary top-quark mass measurements support the unbiasedness of the estimators used
- Stability of the results indicate a good description of data by our MC
- Main source of systematic uncertainty is the (b-)jet energy scale (latest jet energy scale uncertainty is decreased by a factor of 2)
- Achieving a more precise measurement involves working on reducing systematic uncertainties



# BACKUP

# Signal and background

Process	Channel	
	Electron	Muon
$t\bar{t}$ signal	$52.6 \pm 0.5$	$77.3 \pm 0.6$
Single top	$2.23 \pm 0.07$	$3.12 \pm 0.08$
W+jets	$3.9 \pm 0.3$	$6.6 \pm 0.4$
Z+jets	$0.71 \pm 0.05$	$0.63 \pm 0.04$
ZZ/WZ/WW	$0.07 \pm 0.01$	$0.11 \pm 0.01$
QCD multijet (data)	$2.1 \pm 2.1$	$4.5 \pm 4.5$
$m_{\text{top}}$ independent background	$6.9 \pm 2.1$	$11.8 \pm 4.5$
Total background	$9.1 \pm 2.2$	$14.9 \pm 4.5$
Signal + background	$61.7 \pm 2.2$	$92.2 \pm 4.5$
Data	56	99
S/B	5.8	5.2

Table 1: The observed numbers of events for the 1d- $R_{32}$  analysis in the data compared to the expected numbers of signal and background events for the data luminosity, in the electron and muon channels. The Monte Carlo estimates assume SM cross-sections. For all Monte Carlo estimates the uncertainties are statistical only, for the QCD multijet estimate obtained from ATLAS data also the systematic uncertainty is included, see text for details.

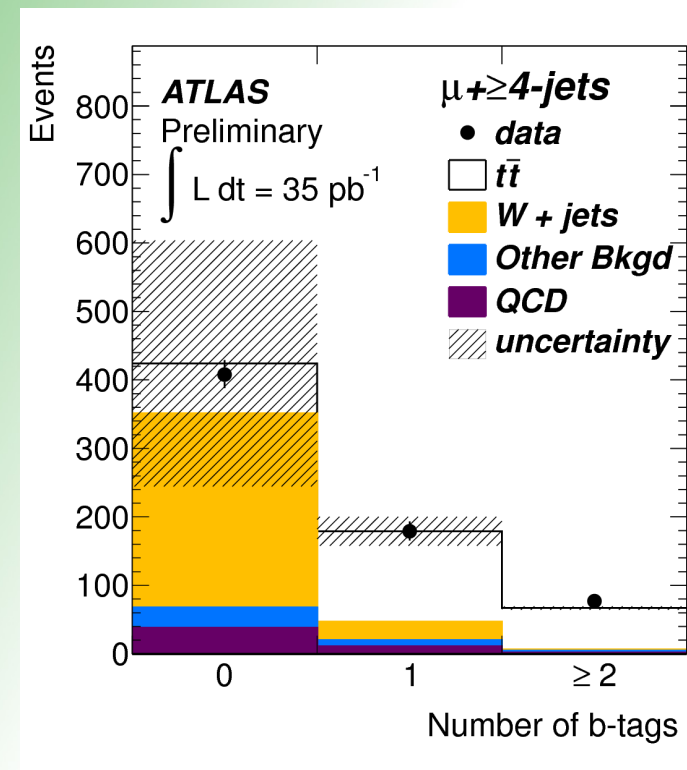
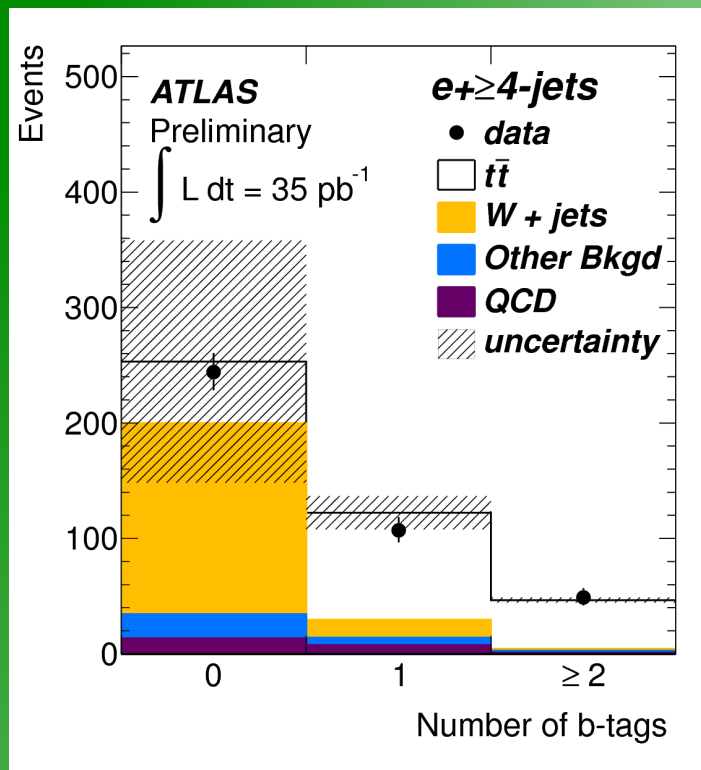
# Systematics

	Uncertainty [GeV]	
	Electron channel	Muon channel
Statistical uncertainty	6.7	5.0
Method calibration	0.7	0.5
Signal MC generator(PowHEG vs. MC@NLO)	0.7	0.6
Hadronization PowHEG (PYTHIA vs. HERWIG)	1.0	0.5
Pileup	0.6	0.8
ISR and FSR (signal only)	2.2	2.6
Proton PDF	0.6	0.5
W/Z+jets background normalization ( $\pm 100\%$ )	1.3	1.7
W/Z+jets background shape	0.6	1.0
QCD background normalization ( $\pm 100\%$ )	0.8	0.7
QCD background shape	0.6	0.5
Jet energy scale ( $\pm 1\sigma$ ) plus 5% for close by jets	2.3	1.9
<i>b</i> -jet energy scale ( $\pm 2.5\%$ )	2.5	2.5
<i>b</i> -tagging efficiency and mistag rate	0.6	0.5
Jet energy resolution	0.6	1.1
Jet reconstruction efficiency ( $\pm 2\%$ )	0.6	0.5
Total systematic uncertainty	4.8	5.0

Table 2: The contributions of various sources to the uncertainty for  $m_{\text{top}}$ . The quoted values correspond to the larger of the observed shift using the pseudo-experiment and the statistical precision of the estimates.

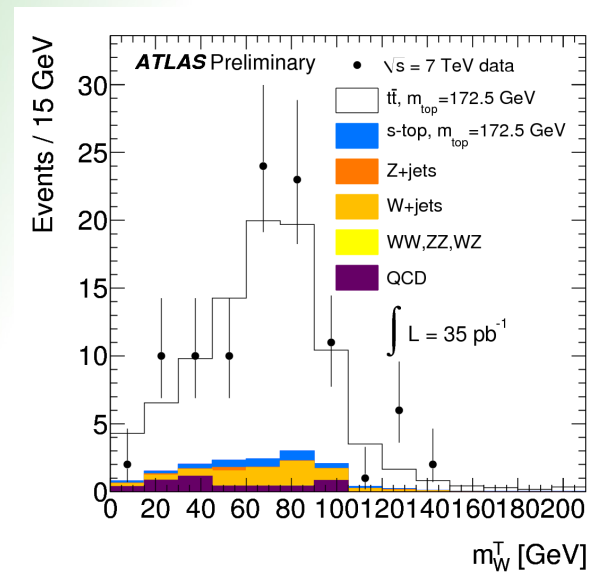
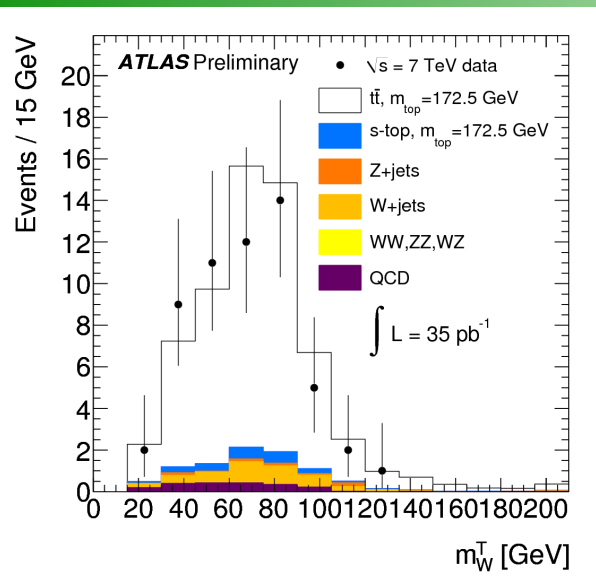
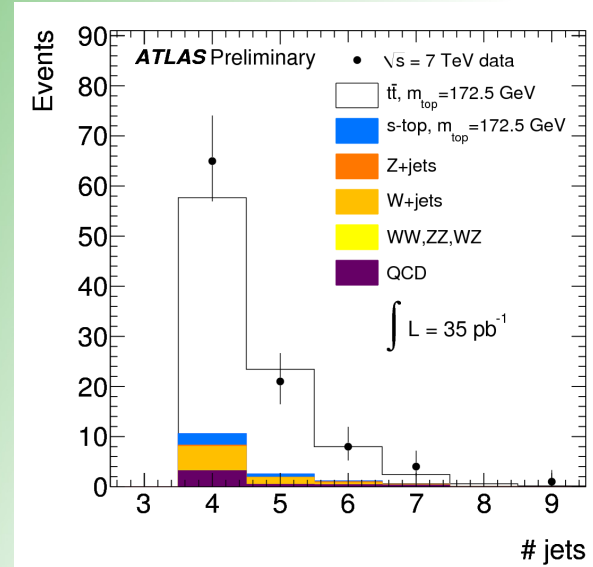
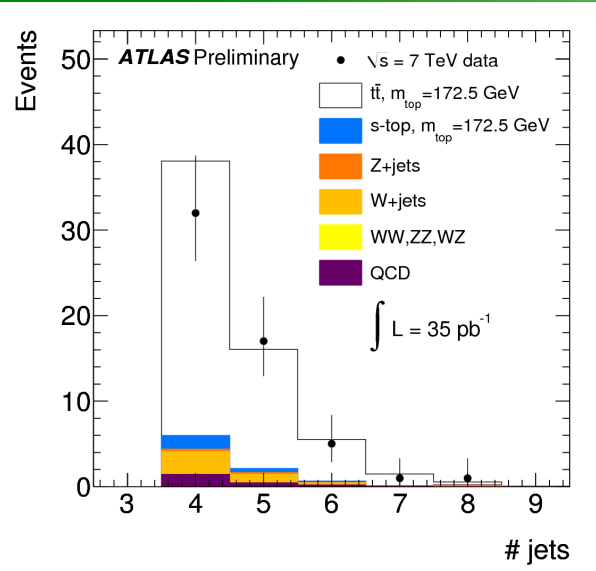
# Top cross section plots

- Number of b-tagged jets in electron (muon) channel

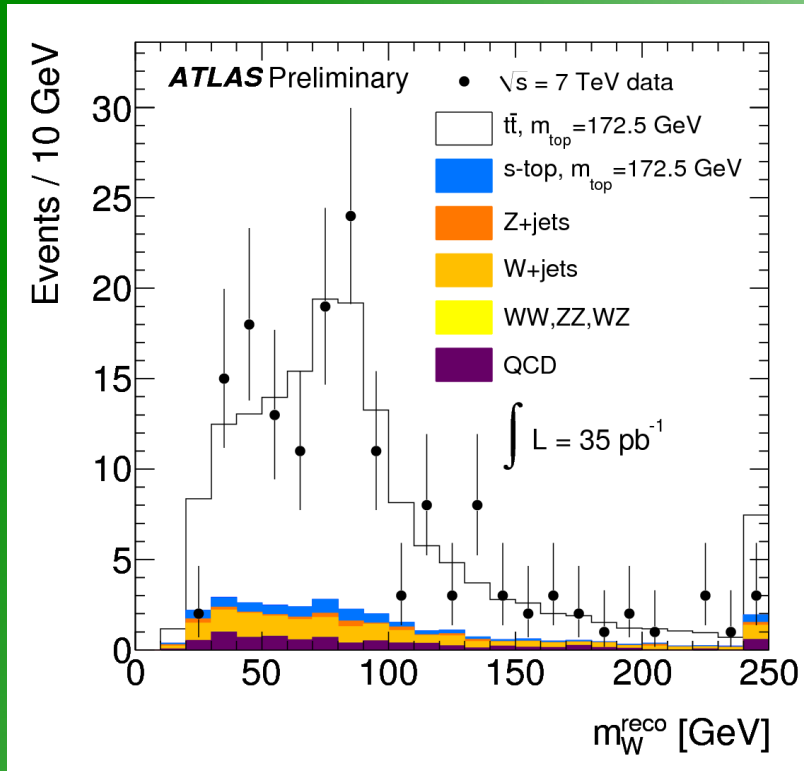




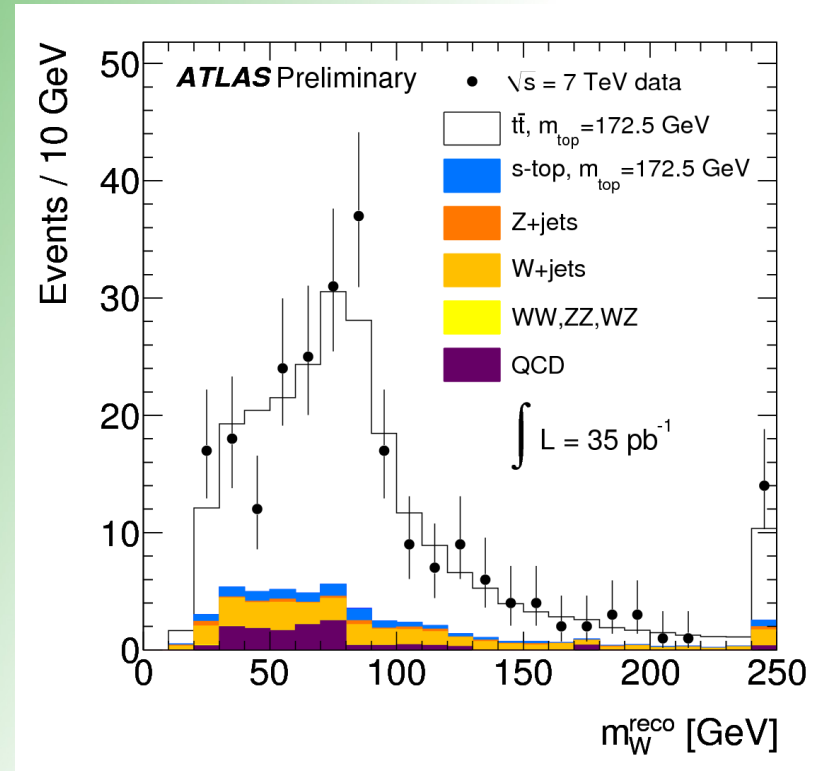
# Baseline method: properties



# Baseline method: W boson mass

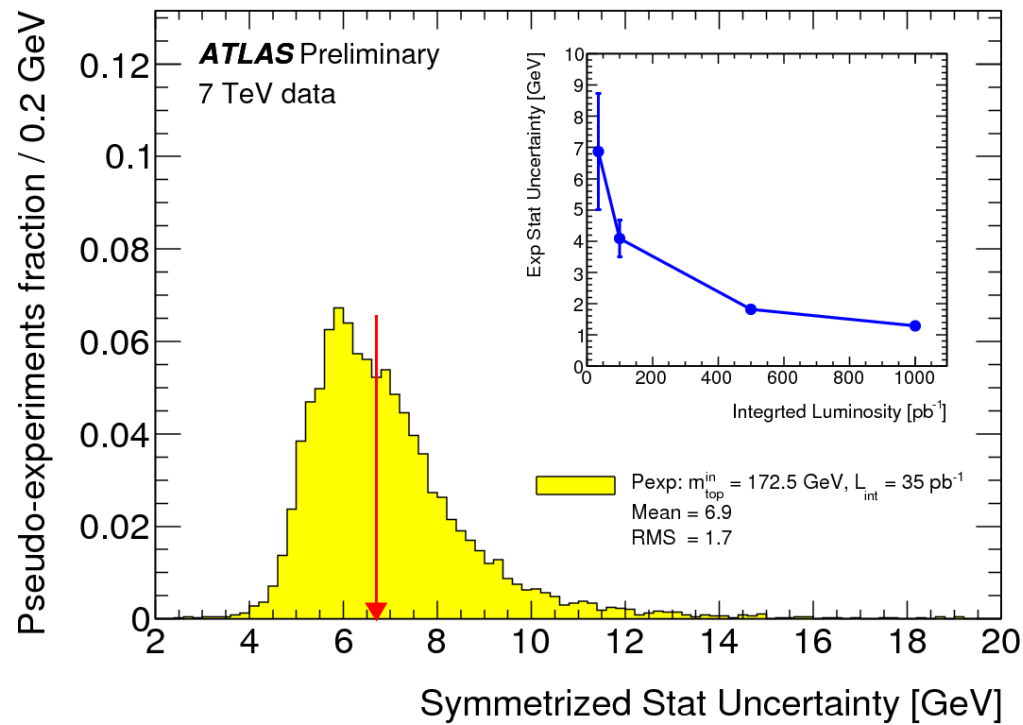


electron channel

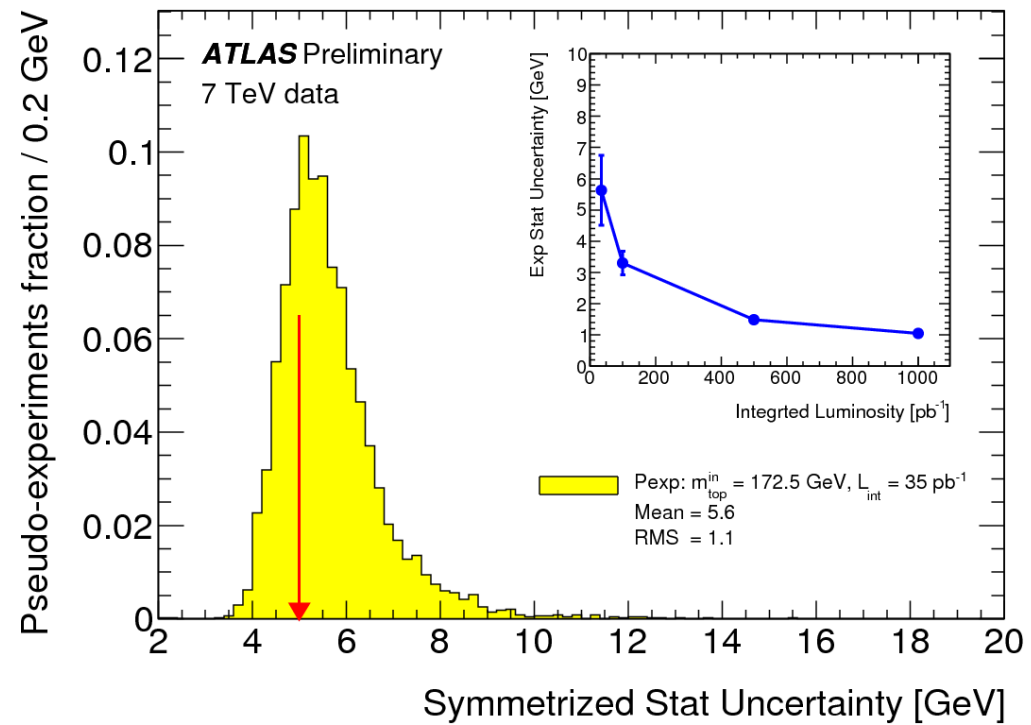


muon channel

# Baseline method: stat. uncertainty

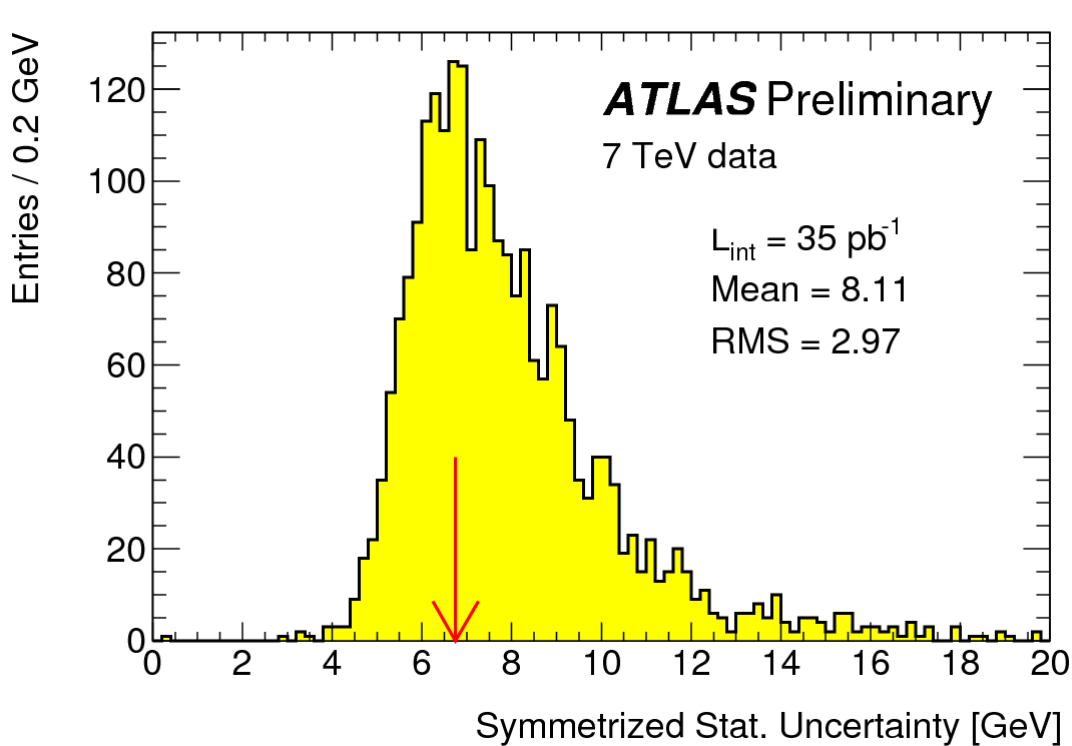


electron channel

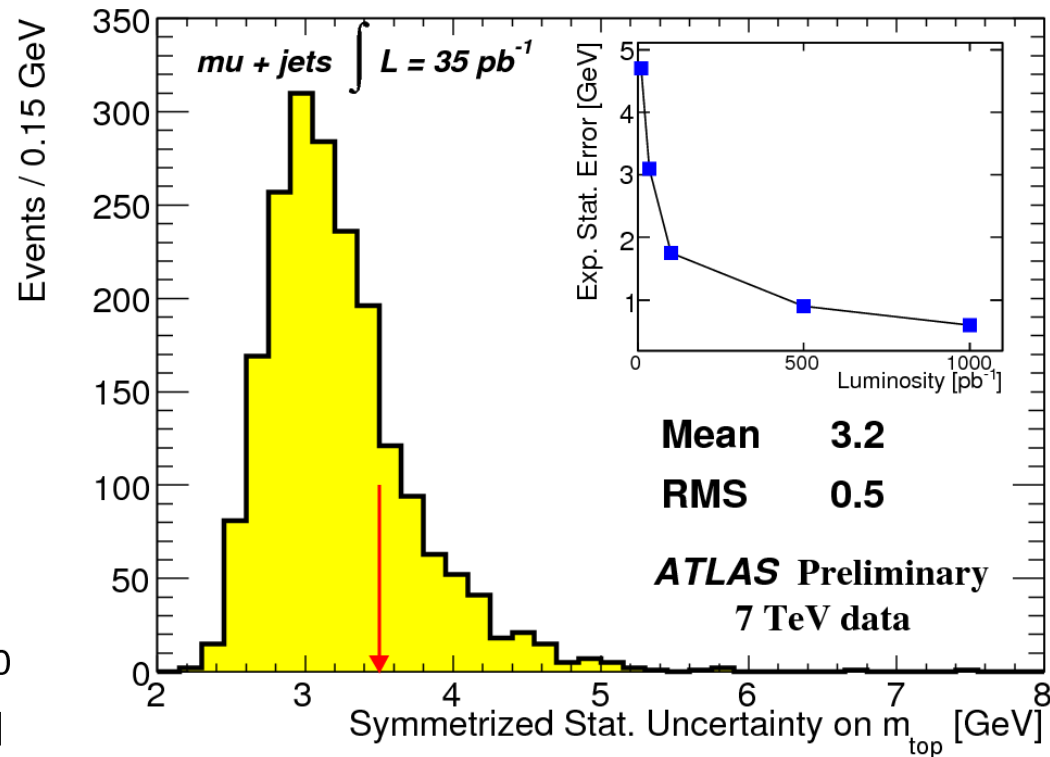


muon channel

# Statistical uncertainties



2-D analysis



1-D kinfit