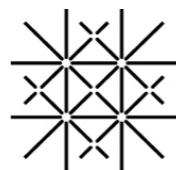


# Protection symmetries for TeV-scale leptoquarks

Admir Greljo

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BERN



University  
of Basel

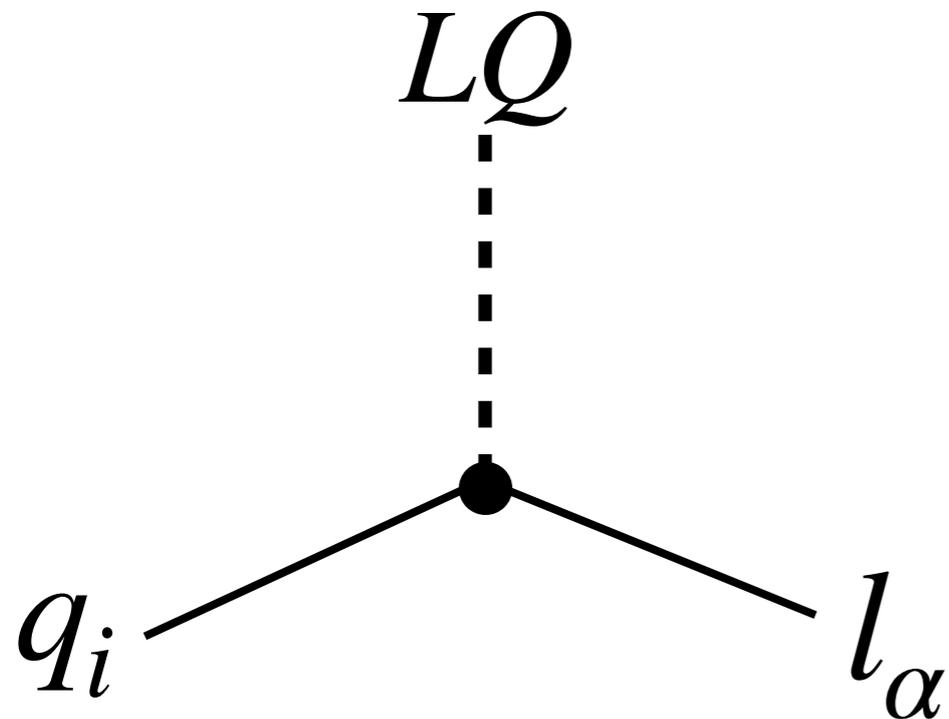
FNSNF

SWISS NATIONAL SCIENCE FOUNDATION

[Eccellenza, Project-186866](#)

# Leptoquarks at the TeV scale?

Doršner, Fajfer, AG, Kamenik, Košnik; [1603.04993](#) (Physics Reports Review)

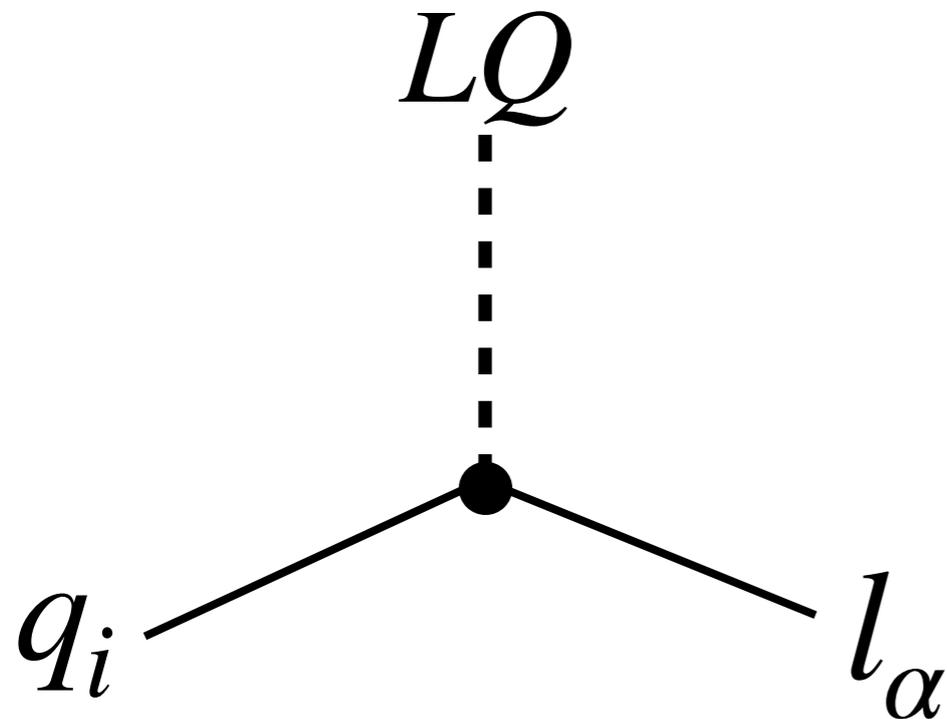


## Wanted:

- A LQ with a TeV-scale mass and (some)  $\mathcal{O}(1)$  couplings

# Leptoquarks at the TeV scale?

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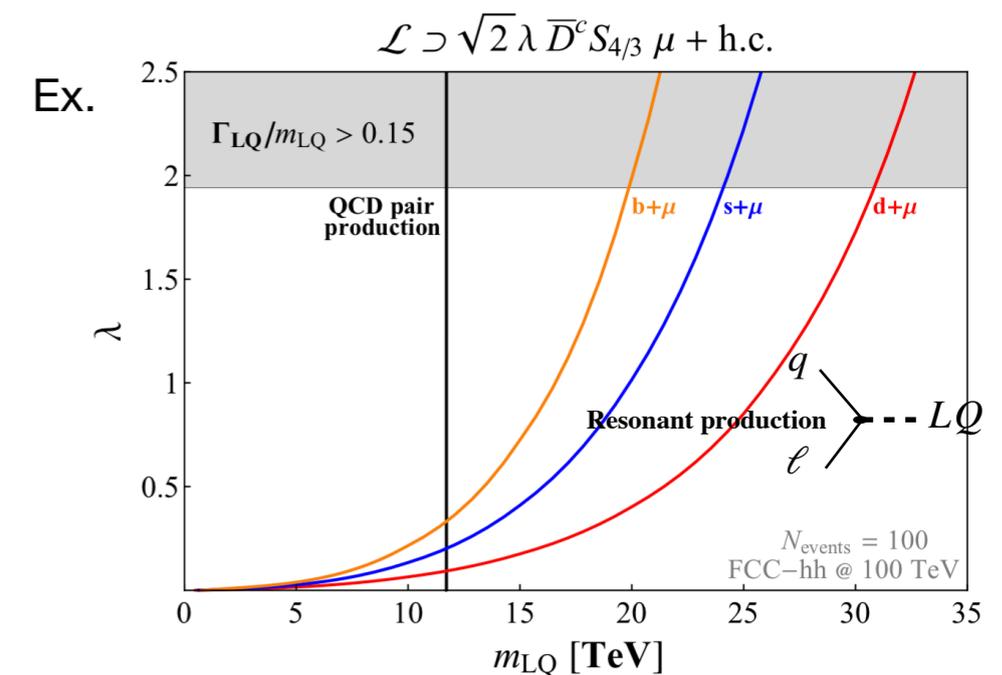
## Wanted:

- A LQ with a TeV-scale mass and (some)  $\mathcal{O}(1)$  couplings

## Why?

### Phenomenology

- Rich collider and flavor pheno?



Buonocore, AG, Krack, Nason, Selimovic, Tramontano, Zanderighi; [2209.02599](#)

### Theory

- Quark-lepton unification!

Pati-Salam, SU(5), SO(10) GUT predict LQs but generically not in this mass-coupling range. New model building directions...

# Outline

## PART I

### Theory

- A model building direction: Gauged flavour

## PART II

### Phenomenology

- Interpretation of  $b \rightarrow s\ell\ell$  anomalies after the recent LHCb update

# Accidental Symmetries in the SM

$$q_i, \ell_i, U_i, D_i, E_i \quad \text{flavour } i = 1, 2, 3$$

$$\mathcal{L}_{\text{SM}} \text{ sans Yukawa: } U(3)_q \times U(3)_\ell \times U(3)_U \times U(3)_D \times U(3)_E$$

$$-\mathcal{L}_{\text{Yuk}} = \bar{q} V^\dagger \hat{Y}_u \tilde{H} U + \bar{q} \hat{Y}_d H D + \bar{\ell} \hat{Y}_e H E$$

[ $U(3)^5$  transformation and a singular value decomposition theorem]



$$\mathcal{L}_{\text{SM}} : U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$$

- $B - L$  and  $L_i - L_j$  are exact
- $B + L$  is anomalous: non-perturbative dynamics implies a selection rule  $\Delta B = \Delta L = 0 \pmod{3}$

# TeV-scale BSM?

- A viable model at the TeV-scale should not (excessively) violate the accidental symmetries.
- Not a generic case!

## Example: Leptoquarks

$$\dim[\mathcal{O}] = 4$$

$$\mathcal{L}_4 = y_{ij} Q^i L^j S + z_{ij} Q^i Q^j S^\dagger$$

$B(S) = -\frac{1}{3}$                        $B(S) = \frac{2}{3}$

~~$U(1)_B$~~       Proton decay  $[z \cdot \gamma]$        $\tau_p \gtrsim 10^{34}$  years

~~$U(1)_e \times U(1)_\mu \times U(1)_\tau$~~        $\mu \rightarrow e \gamma$   $[i \neq j]$        $BR(\mu \rightarrow e \gamma) \lesssim 10^{-13}$

- Generic TeV-scale LQs are dead!

# Gauged $U(1)_X$ $e$ $\mu$ $\tau$ + leptoquarks

## The storyline

- Selection rules for a TeV-scale leptoquark
- Neutrino masses
- Proton stability
- Unification



# A $U(1)_X$ model

■ The initial model  $U(1)_{B-3L_\mu}$  AG, Stangl, Thomsen; [2103.13991](#)

■ The generalisation

$$X = 3m(B - L) - n(2L_\mu - L_e - L_\tau) , \quad \text{gcd}(m, n) = 1$$

Davighi, AG, Thomsen; [2202.05275](#)

# A $U(1)_X$ model

- The initial model  $U(1)_{B-3L_\mu}$  AG, Stangl, Thomsen; [2103.13991](#)

- The generalisation

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Davighi, AG, Thomsen; [2202.05275](#)

	Fields	$U(1)_X$
Quarks	$q_i, u_i, d_i$	$m$
Electrons and taus	$\ell_{1,3}, e_{1,3}, \nu_{1,3}$	$n - 3m$
Muons	$\ell_2, e_2, \nu_2$	$-2n - 3m$
Higgs	$H$	$0$
$(\bar{\mathbf{3}}, \mathbf{3}/\mathbf{1})_{1/3}$ — Leptoquarks	$S_3, S_1$	$2m + 2n$
Scalars (SM singlets)	$\phi_{e\tau}$	$6m - 2n$
	$\phi_\mu$	$6m + n$

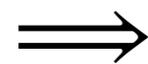
# Selection rules

Gauge symmetry selection rules:

✓  $q\mu S$

✗  $qqS^\dagger, qeS, q\tau S$

## “Muoquark”



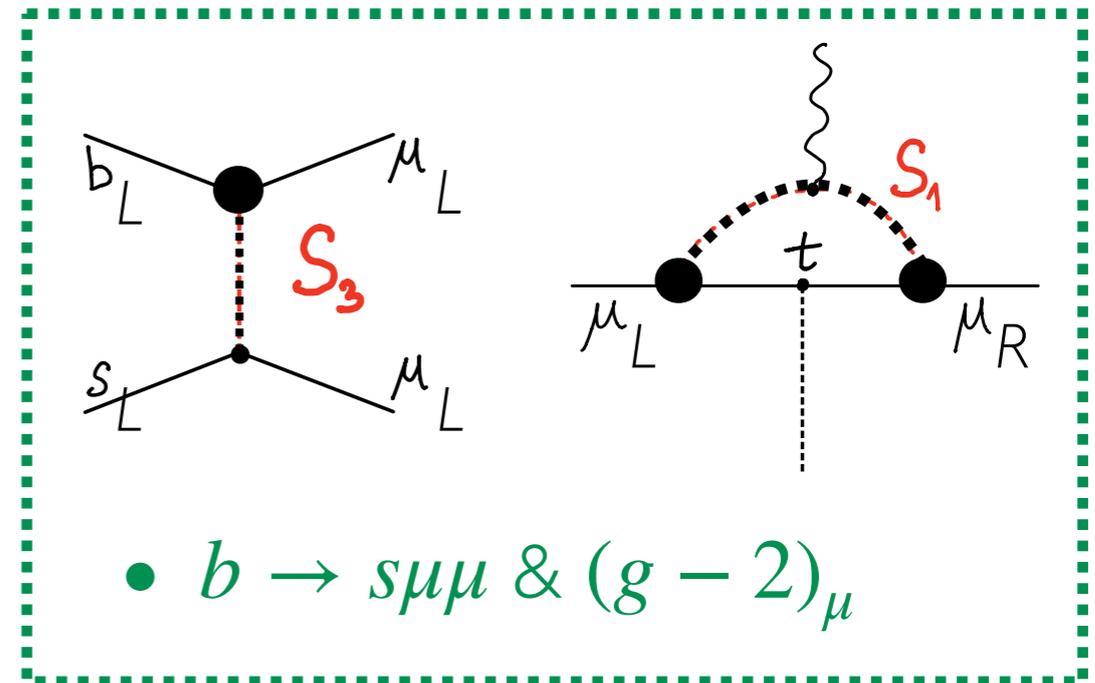
The accidental symmetry of  $\mathcal{L}_{LQ}$  is  $U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$  and the LQ charge is  $(-1/3, 0, -1, 0)$

# Selection rules

Gauge symmetry selection rules:

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✗  $qqS^\dagger, qeS, q\tau S$

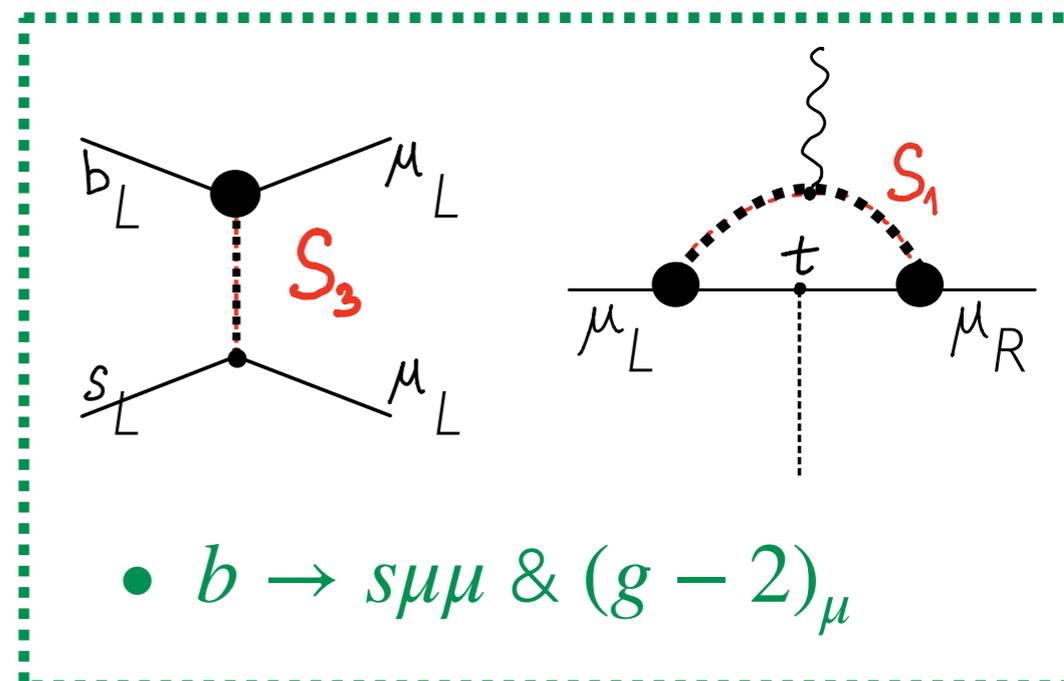


# Selection rules

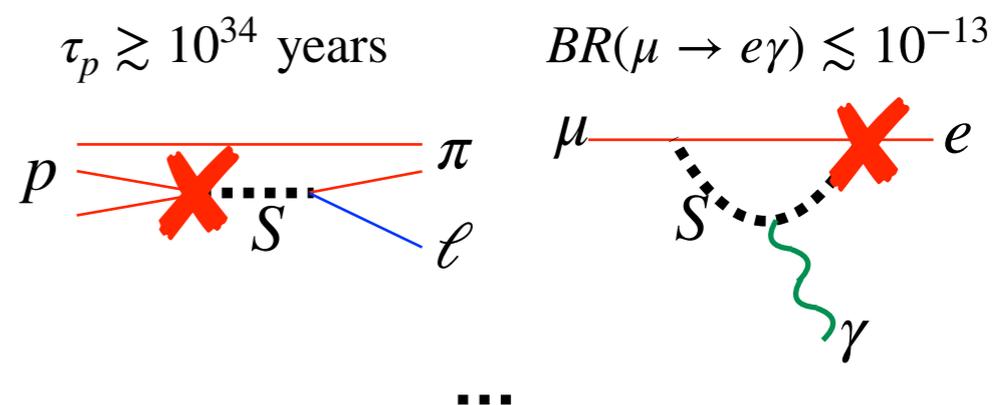
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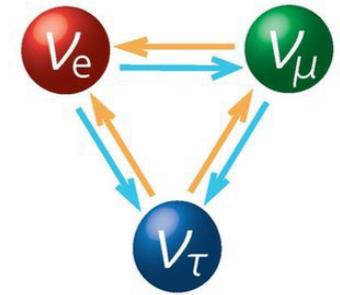


• No proton decay & cLFV



# Neutrino Masses

- The PMNS is full of  $\mathcal{O}(1)$  elements.
- The correct neutrino masses and mixings dictate the  $U(1)_X$  breaking.
- A dense Majorana mass matrix needs two SM-singlet scalar fields with charges  $6m - 2n$  and  $6m + n$  to get a VEV

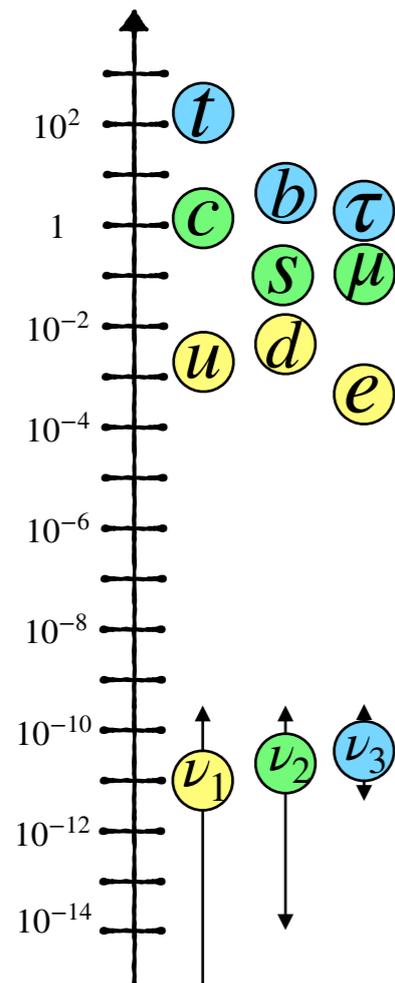


## Type-I seesaw mechanism

$$Y_\nu \sim \begin{pmatrix} \times & 0 & \times \\ 0 & \times & 0 \\ \times & 0 & \times \end{pmatrix} ; \quad \mathcal{L} \supset \bar{\nu}_R^{ic} \nu_R^j (\xi_{e\tau}^{ij} \phi_{e\tau} + \xi_{\mu}^{ij} \phi_\mu) \implies \frac{M_\nu}{v_X} \sim \begin{pmatrix} \times & \times & \times \\ \times & 0 & \times \\ \times & \times & \times \end{pmatrix}$$

- More general than two-zero minor structure type  $D_1^R$  [Asai; 1907.04042](#)
- This is enough to accommodate for:
  - Neutrino oscillations data,
  - The Planck limit on the sum of neutrino masses,
  - The absence of neutrinoless double beta decay.

# Neutrino Masses

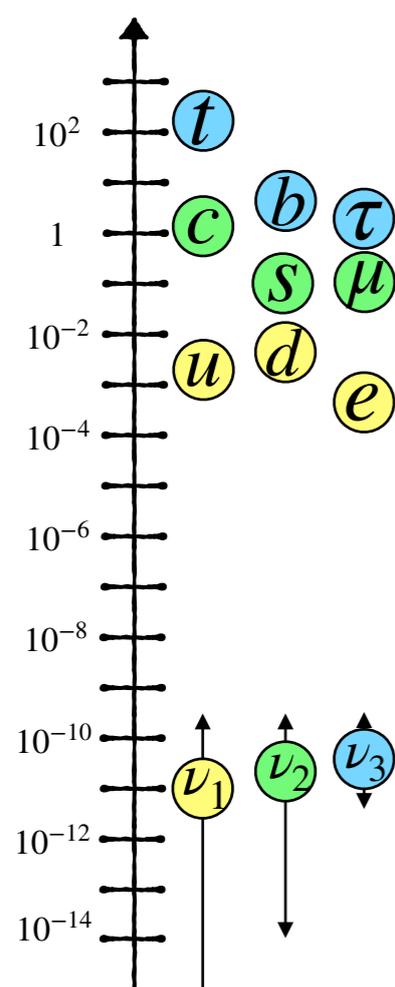


$U(1)_X$  breaking at the high scale?

The mass gap is explained if  $\langle \phi_{e\tau} \rangle, \langle \phi_{\mu} \rangle \gg \langle H \rangle$

Standard thermal leptogenesis at high scale

# Neutrino Masses



$U(1)_X$  breaking at the high scale?

The mass gap is explained if  $\langle \phi_{e\tau} \rangle, \langle \phi_\mu \rangle \gg \langle H \rangle$

Standard thermal leptogenesis at high scale

but

In the  $U(1)_X$  broken phase one can *naively* write renormalisable terms  $qqS^*$  and  $q_i \ell_j S$  that violate  $U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$

- What happens?
- Is there proton decay? cLFV?

# *The IR: discrete gauge subgroup*

$\phi_{e\tau}$	$6m - 2n$
$\phi_{\mu}$	$6m + n$

- Fixed by neutrinos

# The IR: discrete gauge subgroup

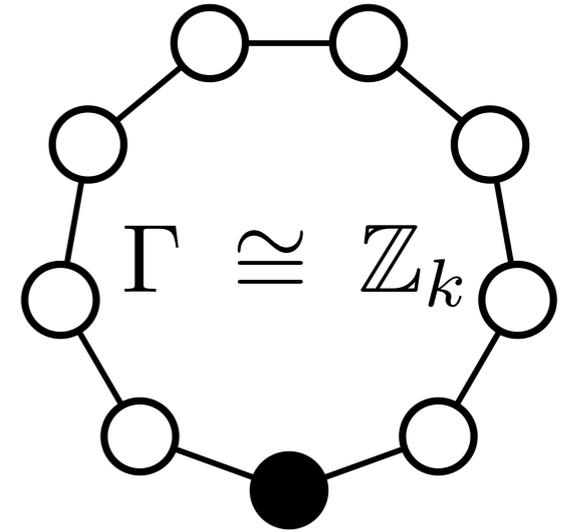
$\phi_{e\tau}$	$6m - 2n$
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- Fixed by neutrinos

$$k = \text{gcd}([\phi_{e\tau}]_X, [\phi_\mu]_X)$$

$$e^{i\frac{2\pi}{k}[\phi]_X}\phi = \phi$$

- The scalars  $\phi_{e\tau}$  and  $\phi_\mu$  are  $\Gamma$  singlets
- An unbroken discrete subgroup  $\Gamma \subset U(1)_X$  acting on matter in the IR



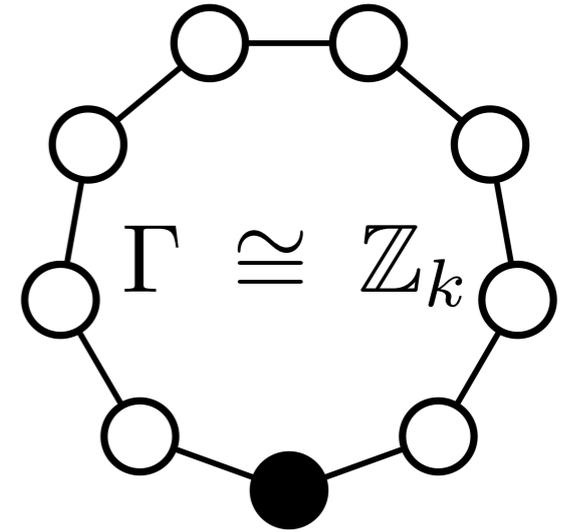
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- The diquark operators  $qqS^*$  are banned by  $\Gamma$  when:

$$(m, n) = (3a + r, 9b + 3r), \quad \text{for } r \in \{1, 2\},$$

$$(a, b) \in \mathbb{Z}^2, \quad \text{and } \text{gcd}(3a + r, b - a) = 1.$$

$$\Gamma \cong \begin{cases} \mathbb{Z}_9, & \text{for } b + r \in 2\mathbb{Z} + 1 \\ \mathbb{Z}_{18}, & \text{for } b + r \in 2\mathbb{Z} \end{cases}$$

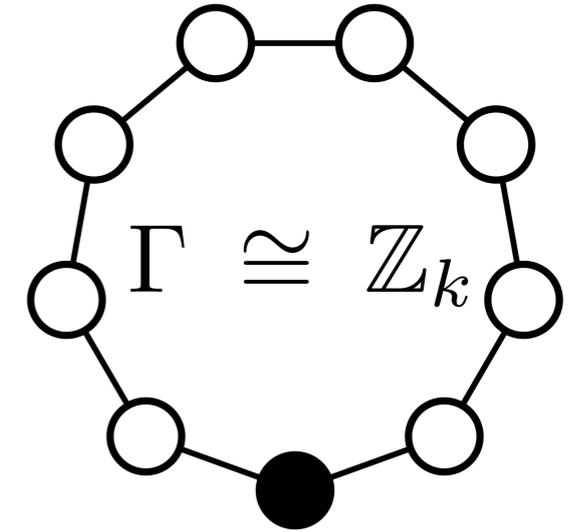
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- No proton decay!

- Both  $B - L$  and the lepton-flavoured factor required!  $X = 3m(B - L) - n(2L_\mu - L_e - L_\tau)$

# The IR: discrete gauge subgroup

$b + r \pmod{2}$	$\Gamma$	$\ell$	$q$	$S$	$qS\ell$	$qS^*q$
0	$\mathbb{Z}_{18}$	$9(b - a)$	$3a + r$	$6a + 8r$	0	$12r$
1	$\mathbb{Z}_9$	0	$3a + r$	$6a + 8r$	0	$3r$

Charges under the remnant discrete symmetry  $\Gamma$

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$b + r \pmod{2}$	$\Gamma$	$\ell$	$q$	$S$	$qS\ell$	$qS^*q$
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Charges under the remnant discrete symmetry  $\Gamma$

- The  $\Gamma$  protection goes beyond just banning the diquark operators. Integrate out  $S$ . Selection rule:

$$\Delta B = 0 \pmod{3}$$

**Exact proton stability to all orders in the SMEFT!**

~~$qqq\ell$~~  and so on

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**Exact proton stability to all orders in the SMEFT!**

~~$qqq\ell$~~  and so on

- Neutron—antineutron oscillations also forbidden
- $\Delta B = 3$  processes are allowed, in analogy to sphalerons.

## What about cLFV?

- $\Gamma$  is lepton flavour universal, otherwise no PMNS.
- cLFV through higher-dim. operators in the  $U(1)_X$ -invariant effective theory:

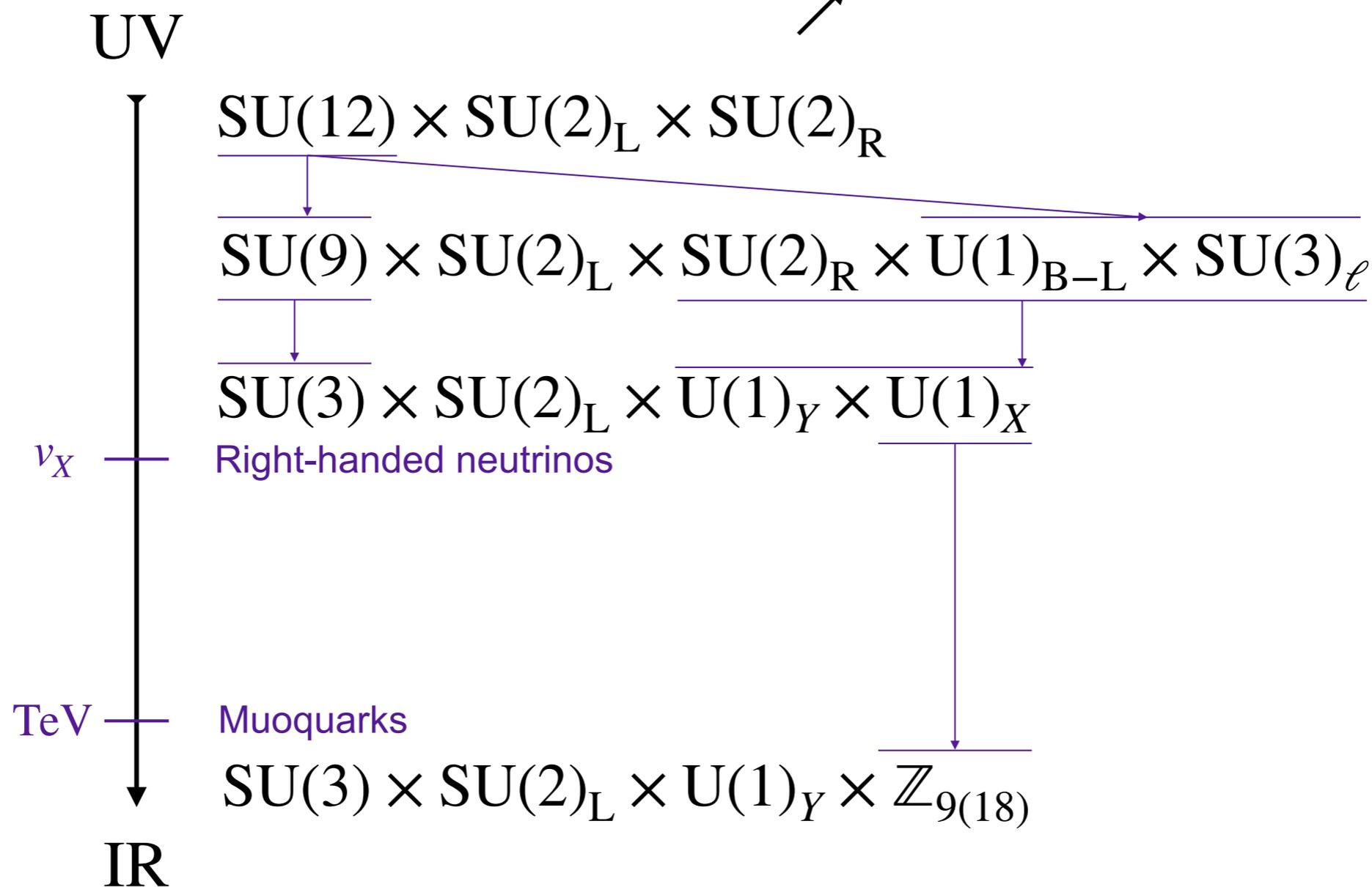
$$\frac{1}{\Lambda^2} \phi_{e\tau} \phi_{\mu}^* q \mathcal{S}_{1/3} \ell_{1,3} \qquad \frac{1}{\Lambda^2} \phi_{e\tau} \phi_{\mu}^* u \mathcal{S}_1 e_{1,3}$$

- A modest scale separation is sufficient to suppress cLFV processes to a level compatible with current bounds.

# Deeper into the UV: Unification

All 3 families of fermions fit into:

$$\Psi_L \sim (\mathbf{12}, \mathbf{2}, \mathbf{1}) \quad \Psi_R \sim (\mathbf{12}, \mathbf{1}, \mathbf{2})$$



Tentative gauge–flavour unification scenario.

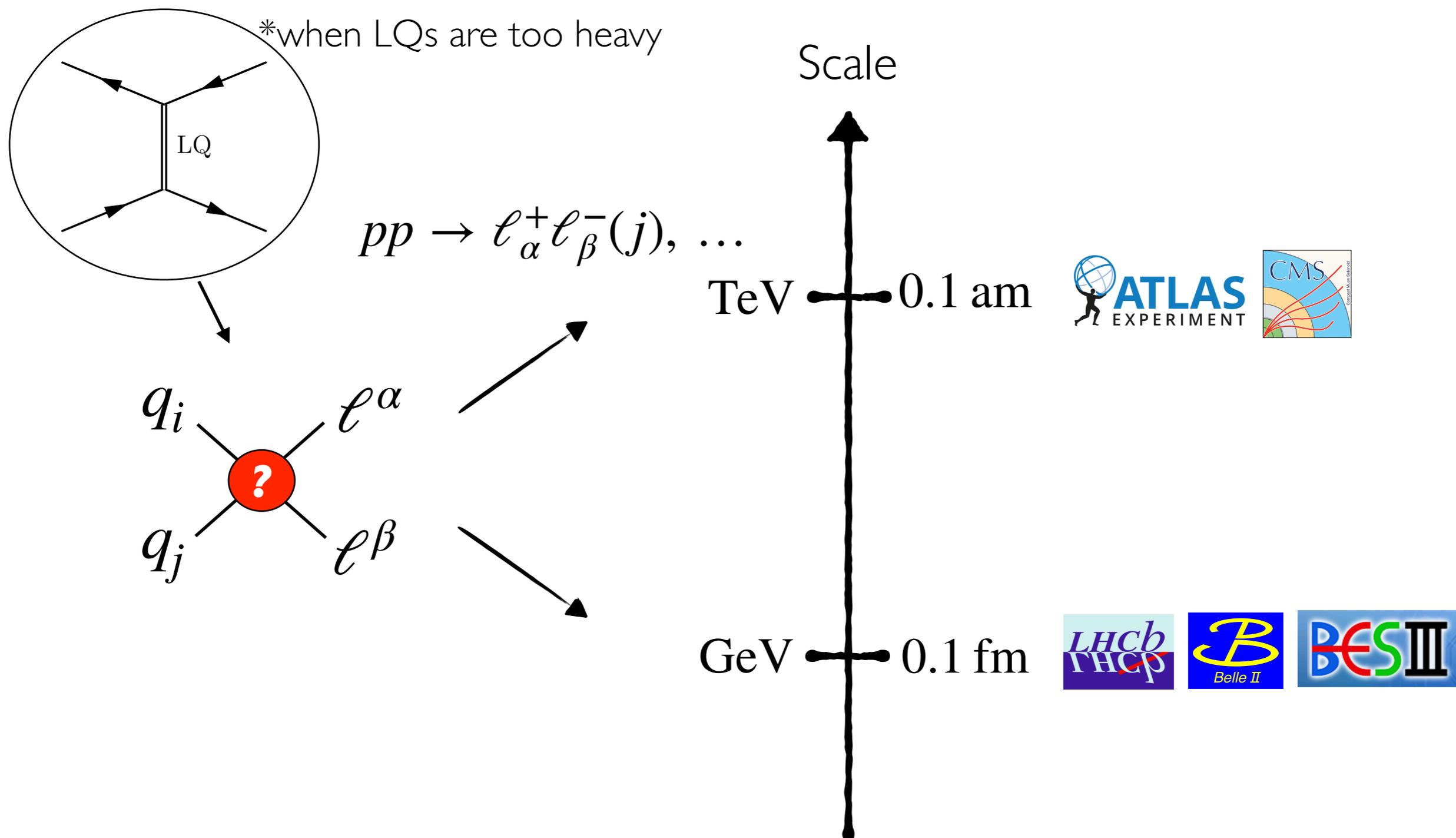
PART II

# Comments on $R_{K^{(*)}}$

The storyline

- Interpretation of  $b \rightarrow s\ell\ell$  anomalies after the recent LHCb update

# Drell-Yan versus $B$ -decays



Example:  $b \rightarrow s\mu\mu$  vs Drell-Yan  
 AG, Marzocca; [1704.09015](#)

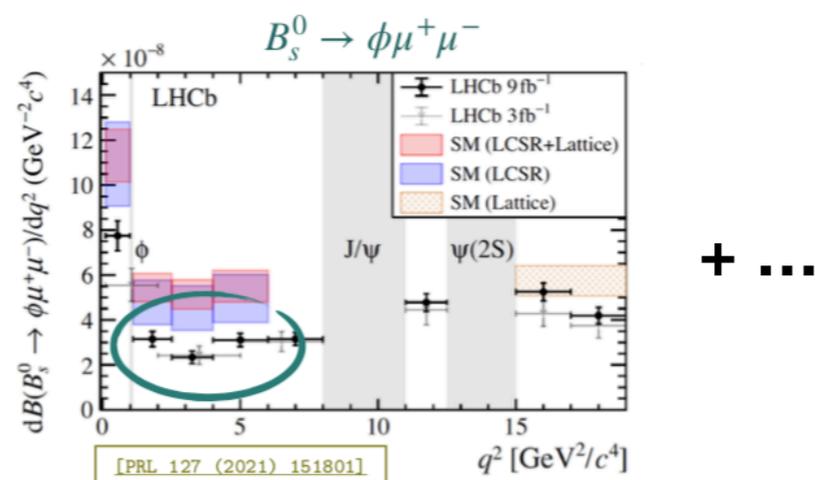
Systematic SMEFT study using flavio  
 AG, Salko, Smolkovic, Stangl; [2212.10497](#)

# The status of $b \rightarrow s\ell\ell$ anomalies

- Anomalies in  $b \rightarrow s\mu\mu$

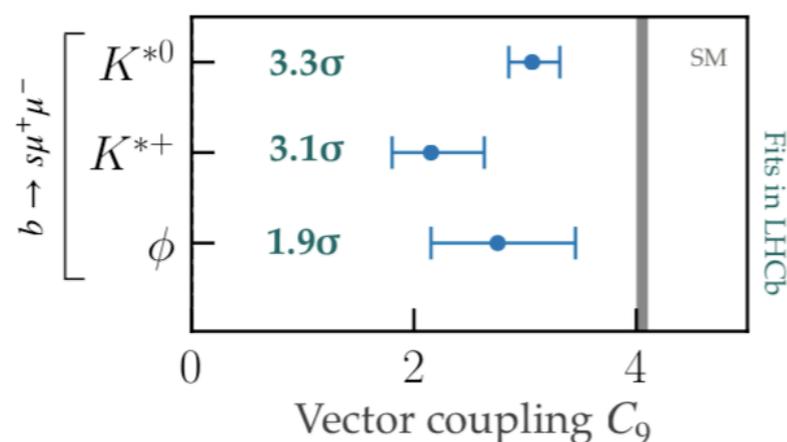
cf. Renato Quagliani, CERN seminar 20.12.2022.

$b \rightarrow s\mu^+\mu^-$  differential decay rates

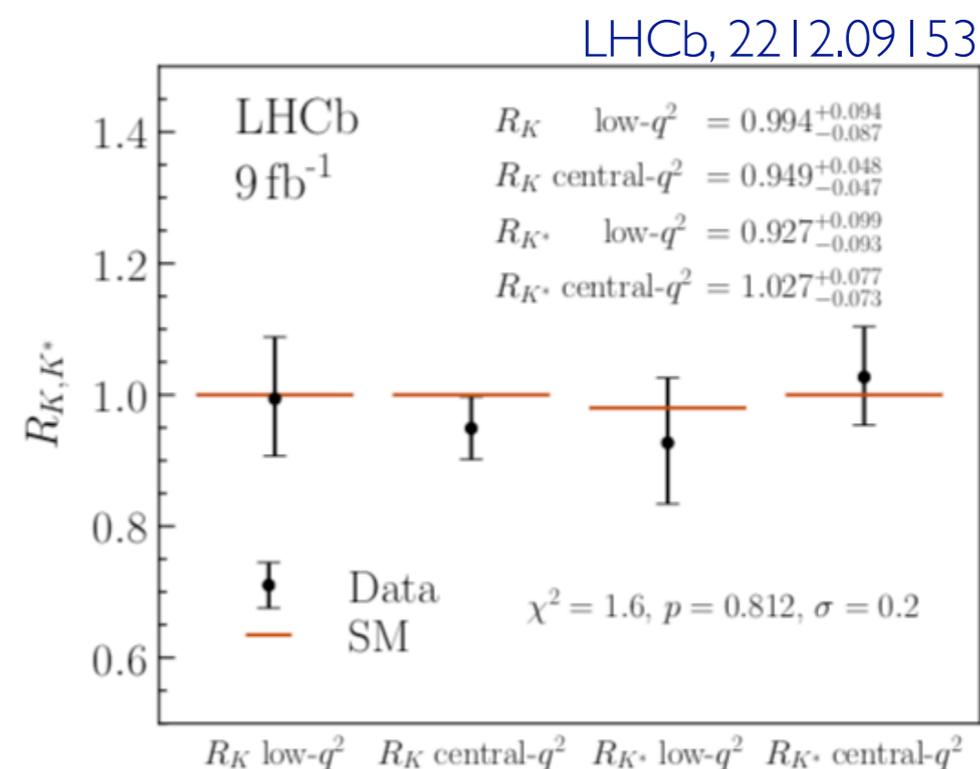


- But **L**epton **F**lavor **U**niversality ratios are SM-like

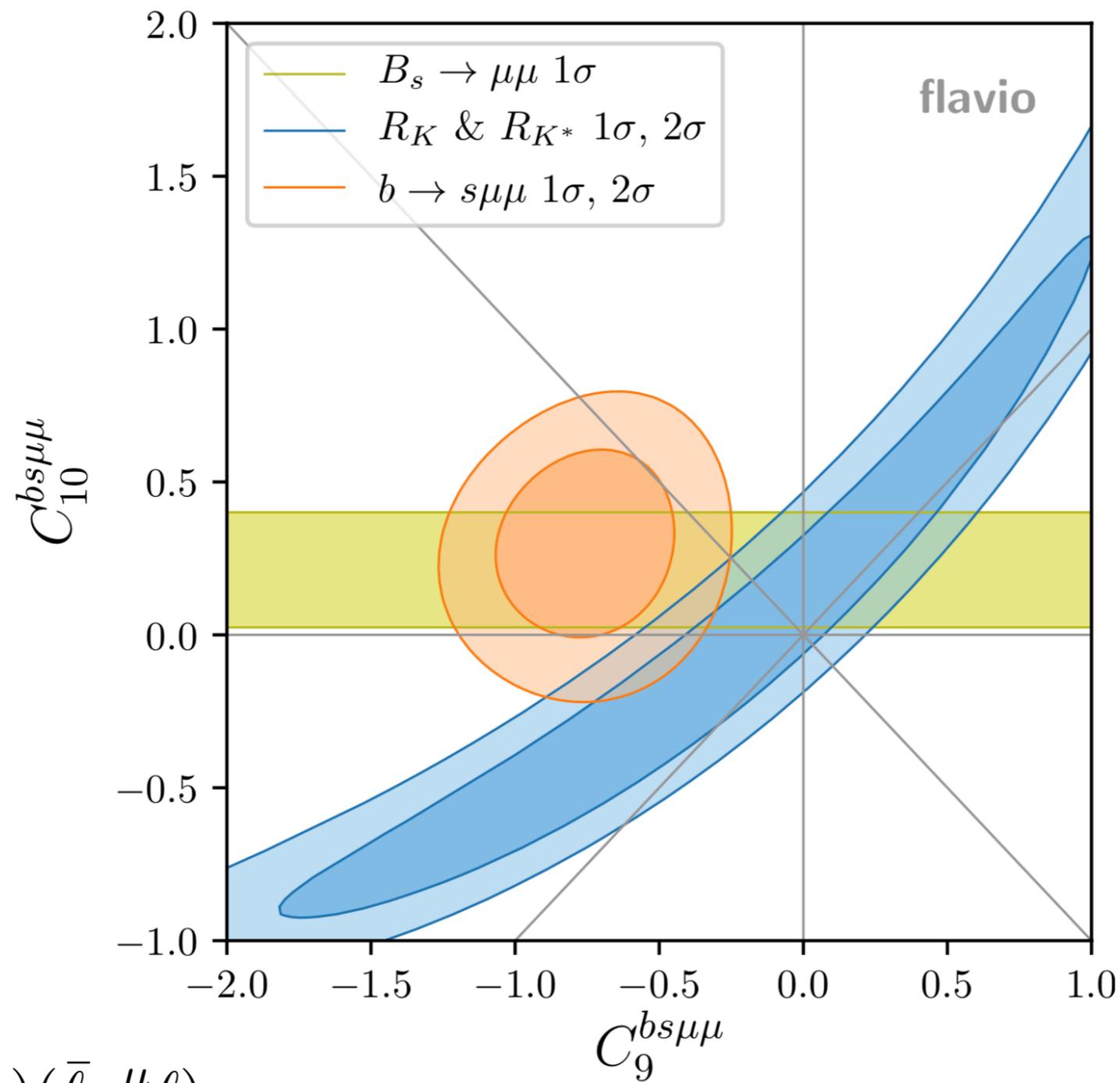
$b \rightarrow s\mu^+\mu^-$  angular analyses



- ♦ Intriguing coherent and consistent pattern
  - ▶ However, *charm-loops* can mimic shift in  $C_9$



# The EFT fit

AG, Salko, Smolkovic, Stangl; [2212.10497](#)

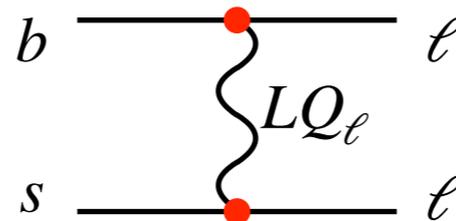
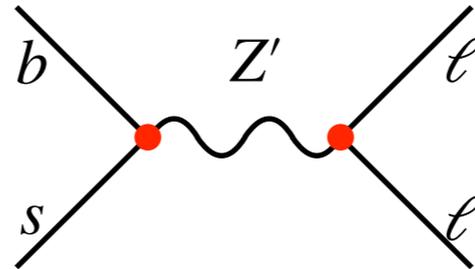
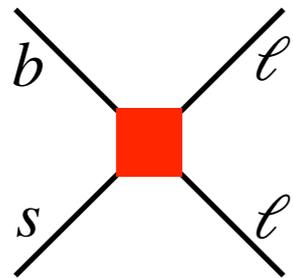
Tension!

$$O_9^{bqll} = (\bar{q}\gamma_\mu P_L b)(\bar{l}\gamma^\mu l),$$

$$O_{10}^{bqll} = (\bar{q}\gamma_\mu P_L b)(\bar{l}\gamma^\mu \gamma_5 l)$$

# LFU models for $b \rightarrow s\ell\ell$

## Tree-level models



- LFU  $Z'$

$$U(1)_{B-L}$$

$$U(1)_{3B_3-L}$$

...

- LFU  $LQ$

$$(\bar{\mathbf{3}}, \mathbf{3}, 1/3) \times 2 = LQ_e + LQ_\mu$$

$$U(1)_e \times U(1)_\mu \times Z_2^{\text{LFU}}$$

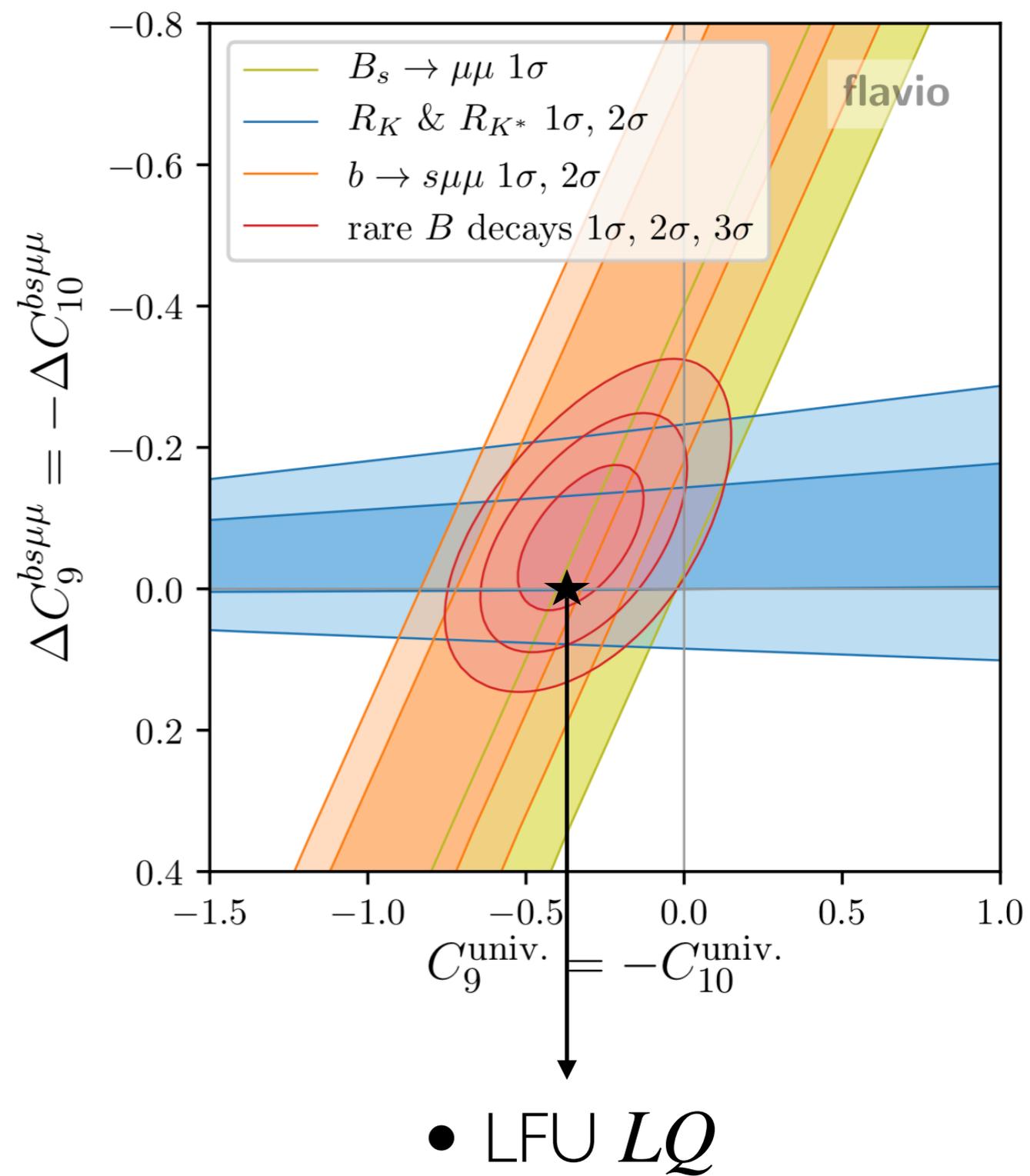
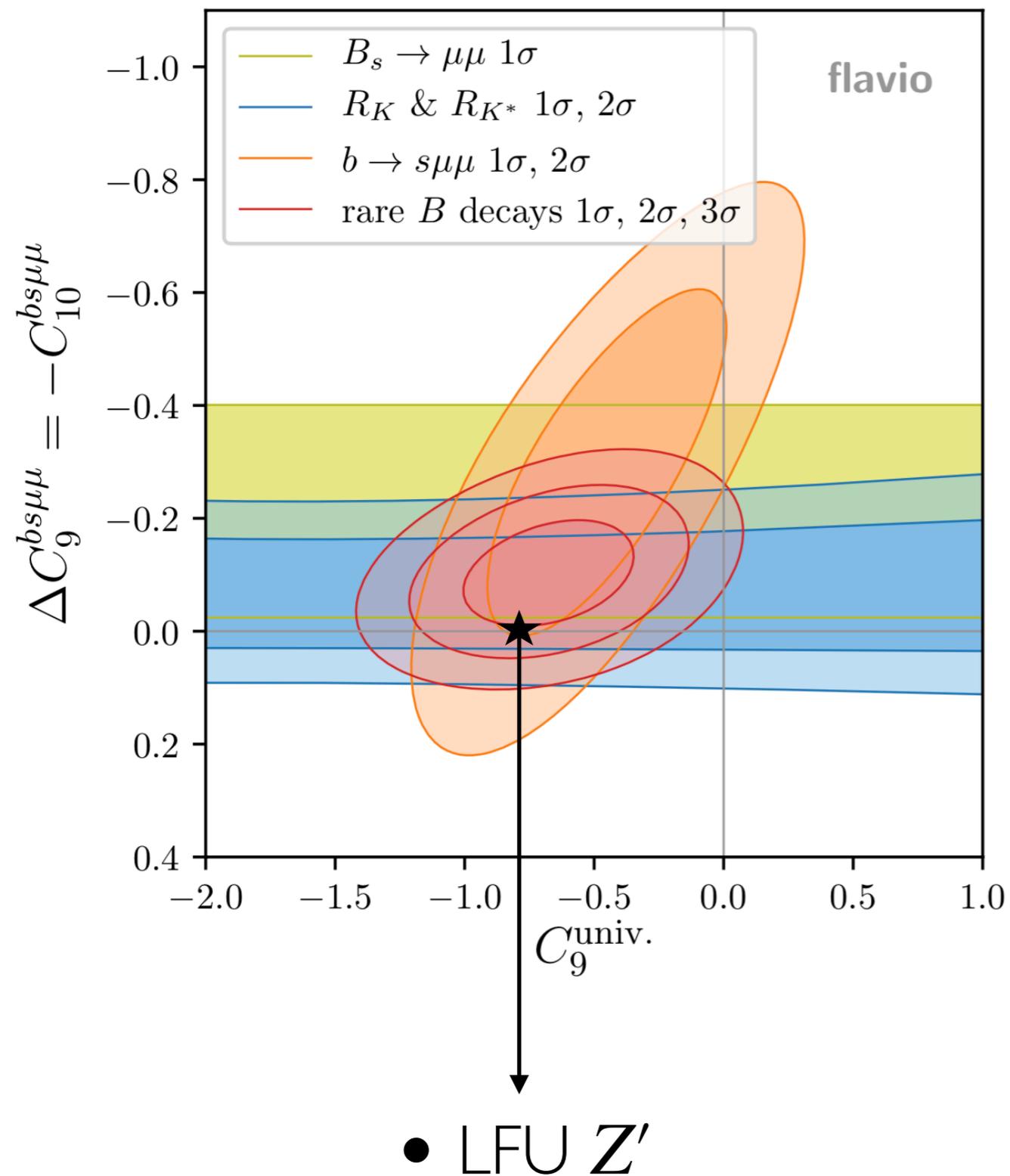


$$\begin{array}{ccc} LQ_e & \longleftrightarrow & LQ_\mu \\ e & \longleftrightarrow & \mu \end{array}$$

Mass/Coupling degeneracy  
Gauged flavour (Part I) ?

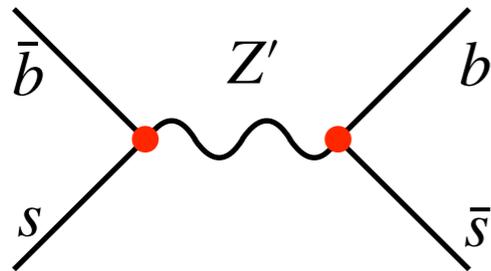
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AG. Salko, Smolkovic, Stangl: 2212.10497

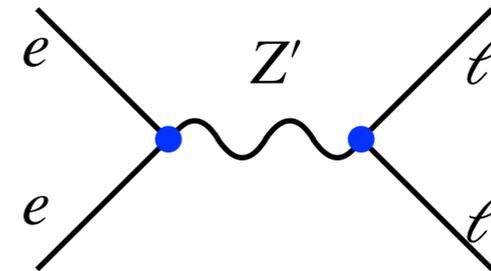


**LFU** models:  $Z'$ 

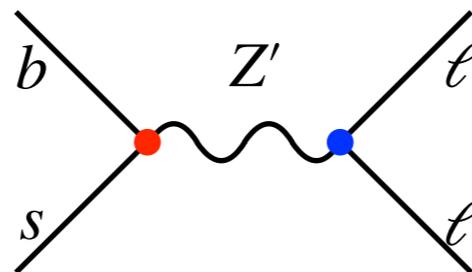
- The bounds from

**Meson mixing**

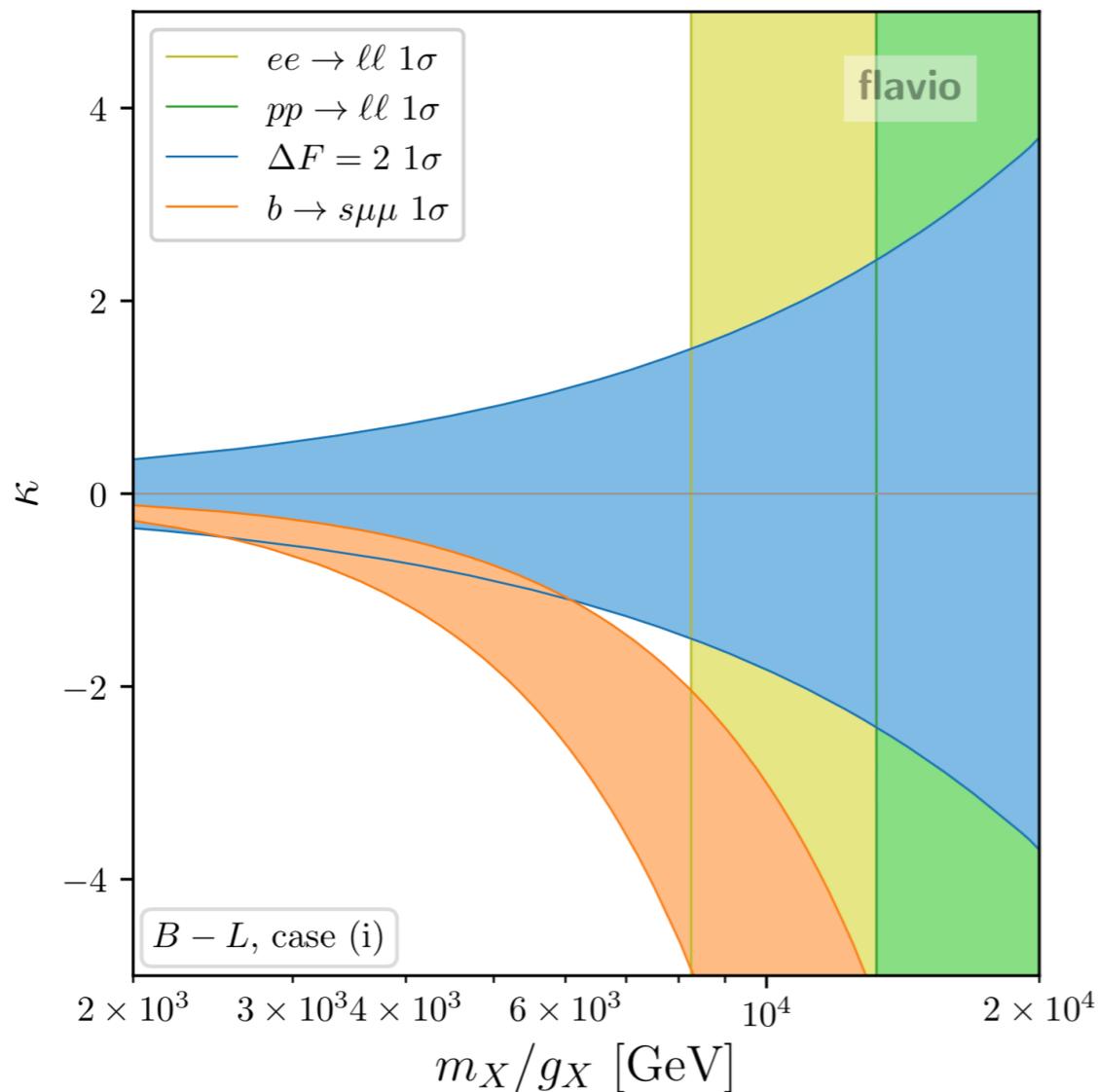
+

**LEP II**

are constraining

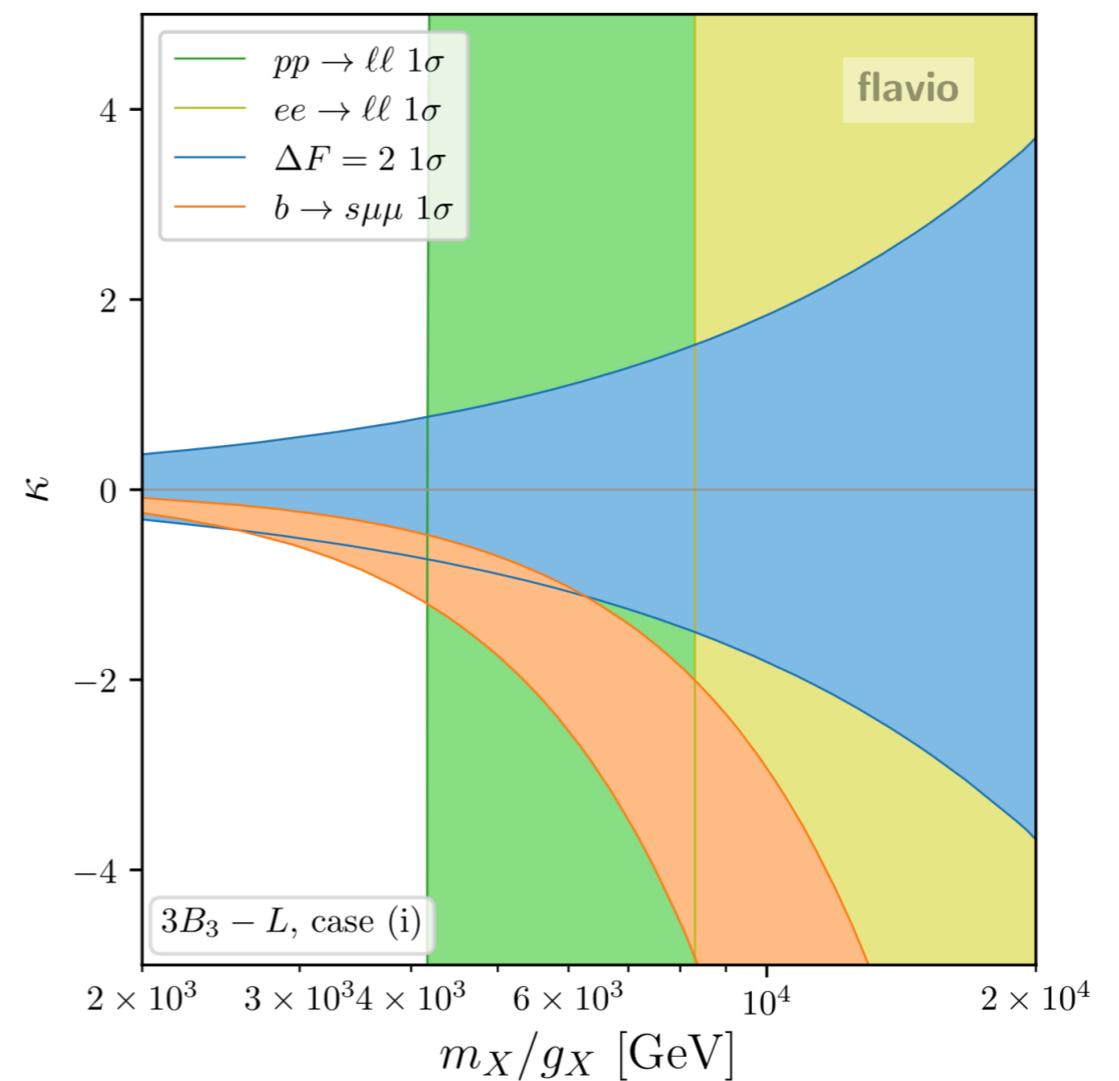


!

**LFU** models:  $Z'$  $B - L$ 

$$J_X^\mu = J_{B-L}^\mu + \frac{1}{3}\epsilon_{ij}\bar{q}_i\gamma^\mu q_j$$

$$\epsilon_{ij} = -\kappa |V_{ts}|(\delta_{i2}\delta_{j3} + \delta_{i3}\delta_{j2})$$

 $3B_3 - L$ 

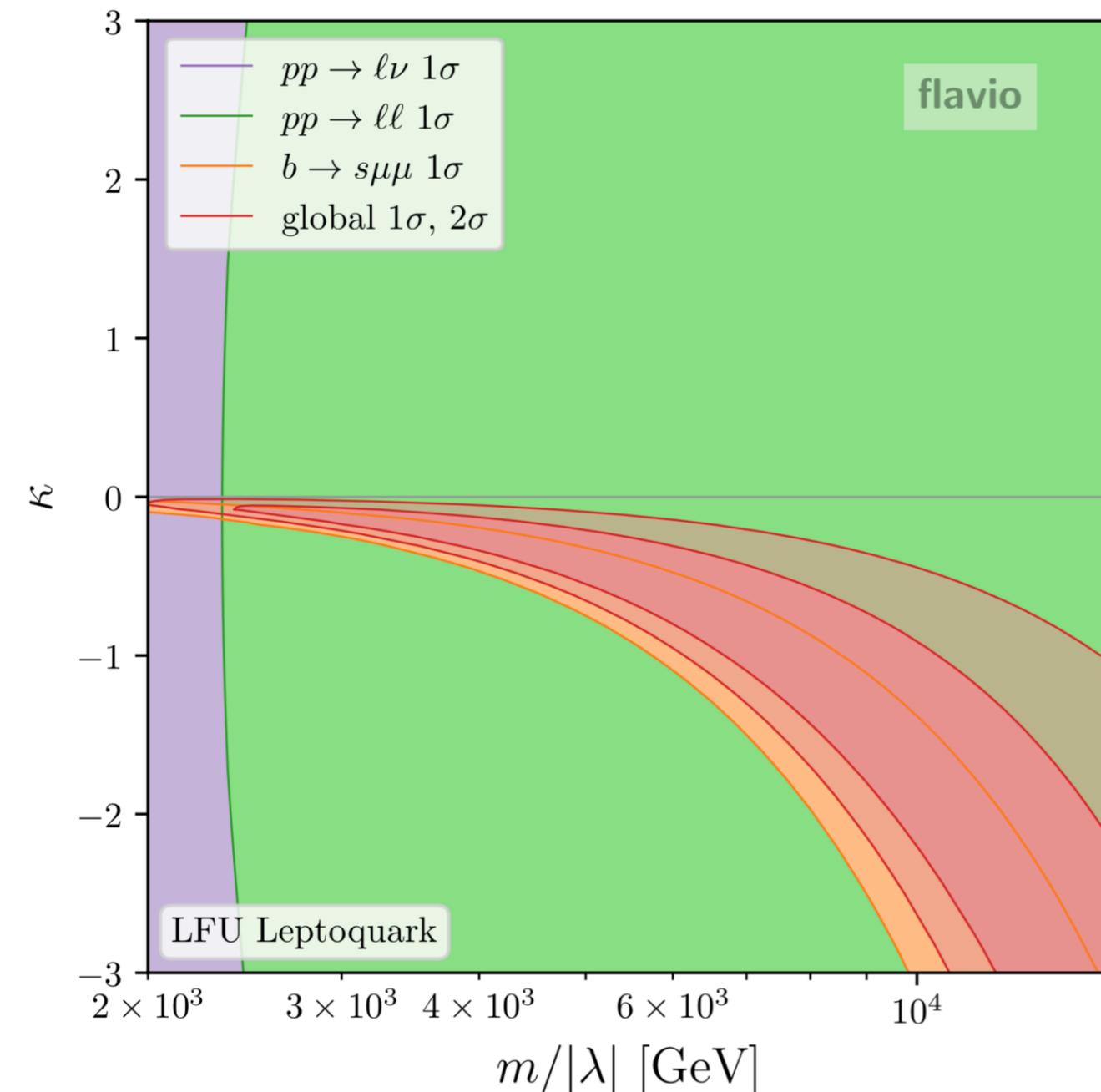
$$J_X^\mu = J_{3B_3-L}^\mu + \frac{1}{3}\epsilon_{ij}\bar{q}_i\gamma^\mu q_j$$

Tension!

# LFU leptoquark

$$\mathcal{L} \supset (D_\mu S^\alpha)^\dagger (D^\mu S^\alpha) - m^2 S^{\alpha\dagger} S^\alpha - (\lambda_i \bar{q}_i^c l_\alpha S^\alpha + \text{h.c.})$$

$$\lambda_i = \lambda (\kappa V_{td}, \kappa V_{ts}, 1)$$



- Tree-level  $2q2\ell$ ,
- Loop-suppressed  $4q$  and  $4\ell$



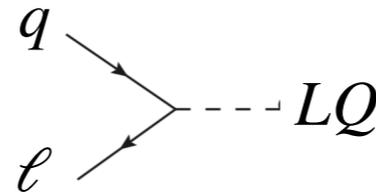
# Conclusions

- Gauged lepton flavour  $\implies$  Selection rules for TeV-scale Leptoquarks
- A mechanism to render the proton **exactly** stable to all orders in EFT:  
*Spontaneously broken lepton-flavoured gauged  $U(1)$  in the UV to generate neutrino masses, leaving a discrete symmetry in the IR*
- Complementarity between high-mass Drell-Yan tails and  **$B$**  decays
- Status of  $b \rightarrow s\ell\ell$  anomalies after the  $R_{K^{(*)}}$  update

***Backup***

# Rich pheno example: $pp \rightarrow LQ$

- Novel production mechanism:  
using lepton PDF inside the proton

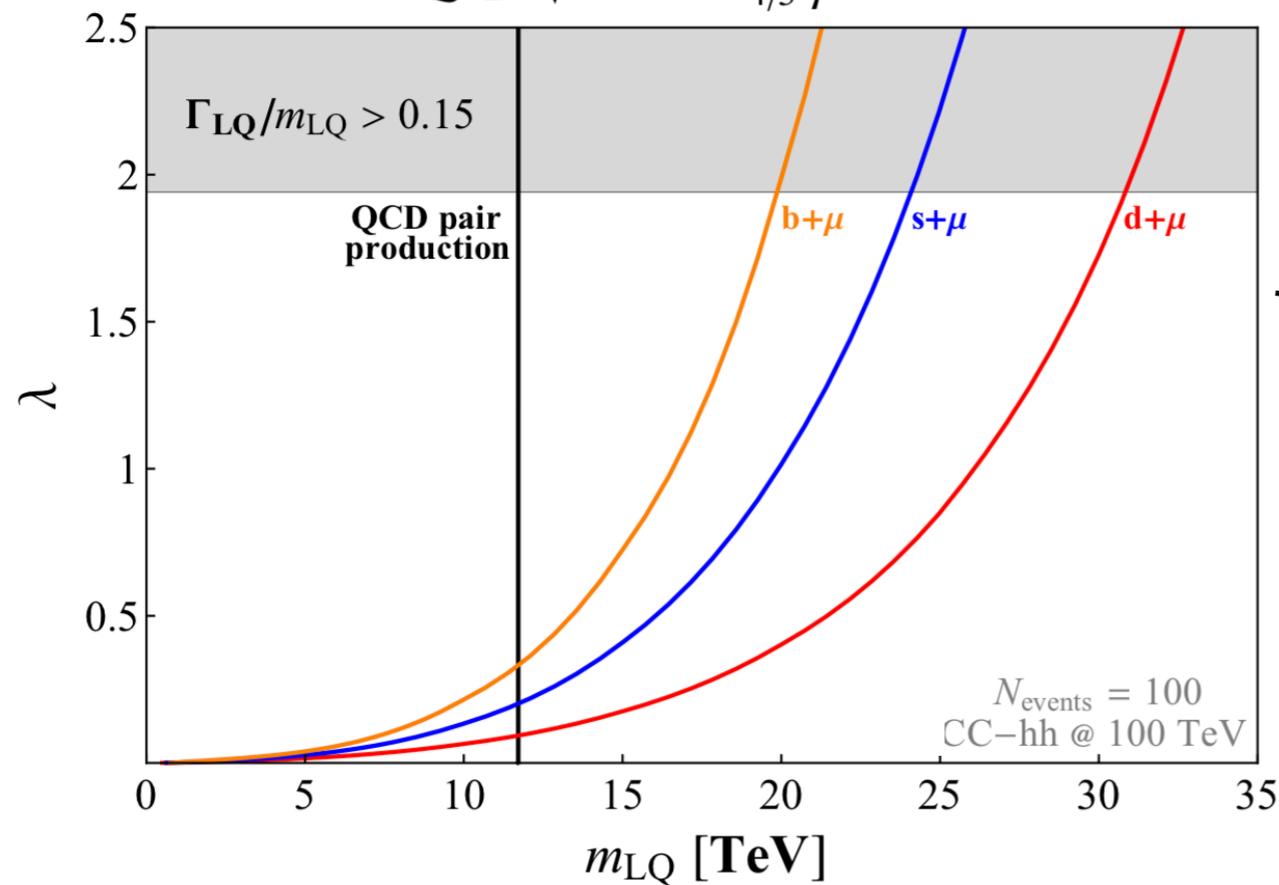


Buonocore, Haisch, Nason, Tramontano, Zanderighi; [2005.06475](#)  
AG, Selimovic; [2012.02092](#)  
Haisch, Polesello; [2012.11474](#)

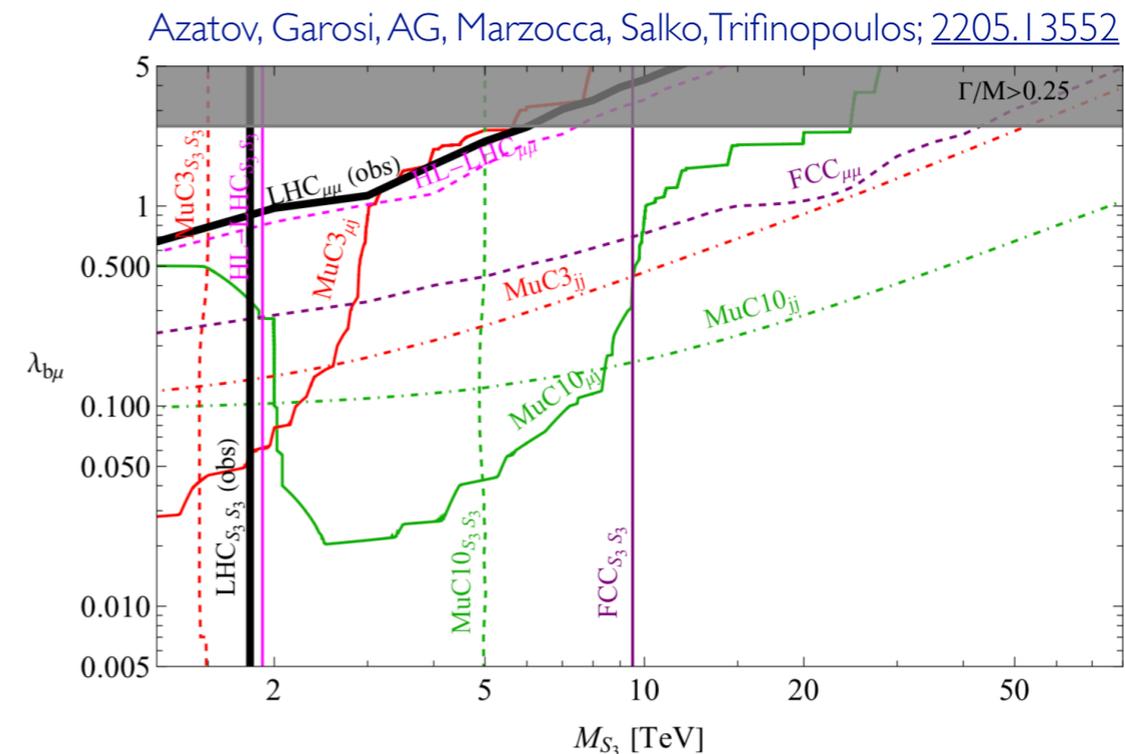
- NLO QCD + QED matched to parton shower:  
POWHEG + HERWIG implementation

Buonocore, AG, Krack, Nason, Selimovic, Tramontano, Zanderighi; [2209.02599](#)

$$\mathcal{L} \supset \sqrt{2} \lambda \bar{D}^c S_{4/3} \mu + \text{h.c.}$$



To be added



$$\lambda_{ql} \sim \mathcal{O}(1)$$

# The $U(1)_X$ atlas

- 18 chiral fermions

$$\begin{aligned} Q_i &\sim (\mathbf{3}, \mathbf{2}, \frac{1}{6}, X_{Q_i}), & U_i &\sim (\mathbf{3}, \mathbf{1}, \frac{2}{3}, X_{U_i}), & D_i &\sim (\mathbf{3}, \mathbf{1}, -\frac{1}{3}, X_{D_i}), \\ L_i &\sim (\mathbf{1}, \mathbf{2}, -\frac{1}{2}, X_{L_i}), & E_i &\sim (\mathbf{1}, \mathbf{1}, -1, X_{E_i}), & N_i &\sim (\mathbf{1}, \mathbf{1}, 0, X_{N_i}). \end{aligned}$$

- Six anomaly cancelation conditions:

$$\begin{aligned} \text{SU}(3)_C^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (2X_{Q_i} - X_{U_i} - X_{D_i}) = 0, \\ \text{SU}(2)_L^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (3X_{Q_i} + X_{L_i}) = 0, \\ \text{U}(1)_Y^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (X_{Q_i} + 3X_{L_i} - 8X_{U_i} - 2X_{D_i} - 6X_{E_i}) = 0, \\ \text{Gravity}^2 \times \text{U}(1)_X &: \sum_{i=1}^3 (6X_{Q_i} + 2X_{L_i} - 3X_{U_i} - 3X_{D_i} - X_{E_i} - X_{N_i}) = 0, \\ \text{U}(1)_Y \times \text{U}(1)_X^2 &: \sum_{i=1}^3 (X_{Q_i}^2 - X_{L_i}^2 - 2X_{U_i}^2 + X_{D_i}^2 + X_{E_i}^2) = 0, \\ \text{U}(1)_X^3 &: \sum_{i=1}^3 (6X_{Q_i}^3 + 2X_{L_i}^3 - 3X_{U_i}^3 - 3X_{D_i}^3 - X_{E_i}^3 - X_{N_i}^3) = 0. \end{aligned}$$

- Integer charges:  $-10 \leq X_{F_i} \leq 10$  [Allanach, Davighi, Melville; 1812.04602](#)

21'546'920 inequivalent solutions (up to flavour permutation, etc)

# Lepton-flavoured catalog

## Quark flavour universal class

- $Y_{u,d}$  are allowed  $\Rightarrow X_{Q_i} = X_{U_j} = X_{D_k}$  –  $10 \leq X_{F_i} \leq 10$   
 $(X_H = 0)$  [276 inequivalent solutions]
- Muoquark requirement  
 eg.  $S_3$  LQ:  $X_{L_2} \neq \{X_{L_{1,3}}, -3X_q\}$  [273 inequivalent solutions]
- Further classification:
  - $Y_e$  allowed  $\Rightarrow$  **vector category** :  $X_{L_i} = X_{E_i}$  [252 inequivalent solutions]
  - chiral category** : the rest. [21 inequivalent solutions]