

RELATING ELASTOINERTIAL TURBULENCE TO THE PHENOMENOLOGY OF POLYMER DRAG REDUCTION

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ABSTRACT

A small amount of flexible polymer additives may cause drastic reduction in turbulent friction drag. The rich dynamics of polymer-turbulence interplay behind the drag reduction (DR) phenomenon is reflected in the transitions in turbulent phenomenology between several distinct stages as the fluid becomes more elastic (higher Weissenberg number Wi)¹.

Starting from the Newtonian limit, there is initially no DR (NDR) until Wi reaches its onset level Wi_{onset} . As Wi further increases, the flow enters the low-extent DR (LDR) stage, where DR effects are contained in the turbulent buffer layer only². Transition to the high-extent DR (HDR) stage is manifested by several distinct markers in flow statistics, especially those in the log-law layer². There are still ongoing debates about conflicting observations in the HDR stage¹. Finally, at sufficiently high Wi , the level of DR converges to the maximum DR (MDR) limit, whose full mechanism remains unexplained.

Recent discovery of the so-called elastoinertial turbulence (EIT), a distinct type of high- Wi flow instability where polymer elasticity feeds into, rather than suppressing, turbulent fluctuations, sparked much interest among researchers. We focus on building the connection between EIT and the phenomenology of DR, especially the multistage transitions in turbulent dynamics as described above. Several interesting findings arose during our investigation. First, although EIT has been widely associated with MDR, we found that MDR cannot be described by the simple convergence to a single EIT state³. Second, EIT shows up a lot earlier than MDR does. Its rise to dominance marks a previously unknown transition, which would explain the seemingly contradictory observations in HDR⁴. Third, opposite to the prevailing view, transition to EIT is triggered by a new linear instability⁵, which is also a sharp contrast to the laminar-turbulent transition in Newtonian fluids.

On the numerical side, EIT dynamics cannot be captured with spectral methods because its sharp stress shockfronts would be smeared by the artificial diffusion term required for numerical stability. This has cast doubt over the general reliability of spectral methods in viscoelastic fluid simulation. We show that although artificial diffusion is detrimental to EIT structures, it has minimal impact on the traditional inertia-driven turbulence (IDT), provided that the numerical diffusivity is chosen at a proper magnitude^{4,6}. Therefore, artificial diffusion can not only still be used in IDT, it also provides a way for us to separate the two types of turbulent dynamics by selectively removing EIT.

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