

# Light mesons from light heavy neutrinos at colliders

NuFact 23, Seoul National University

Richard Ruiz<sup>1</sup>

Institute of Nuclear Physics – Polish Academy of Science (IFJ PAN)

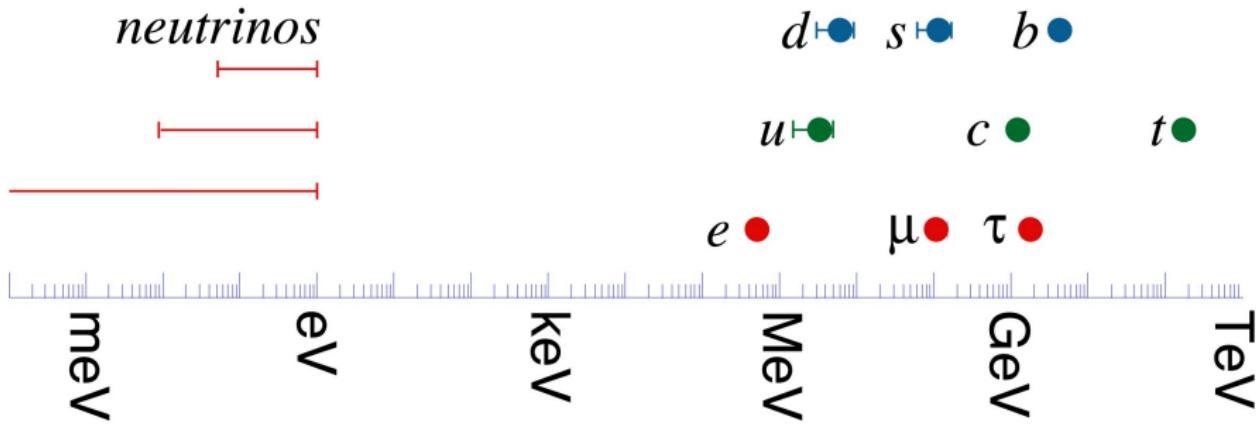
22 August 2023



<sup>1</sup> [w/ Jeon<sup>†</sup>, Fernandez-Martinez, et al (*in progress*)]

**Thank you for the invitation!**

**Problem:** according to the SM,  $m_\nu = 0$ . (Not enough ingredients but data obviously disagree!)

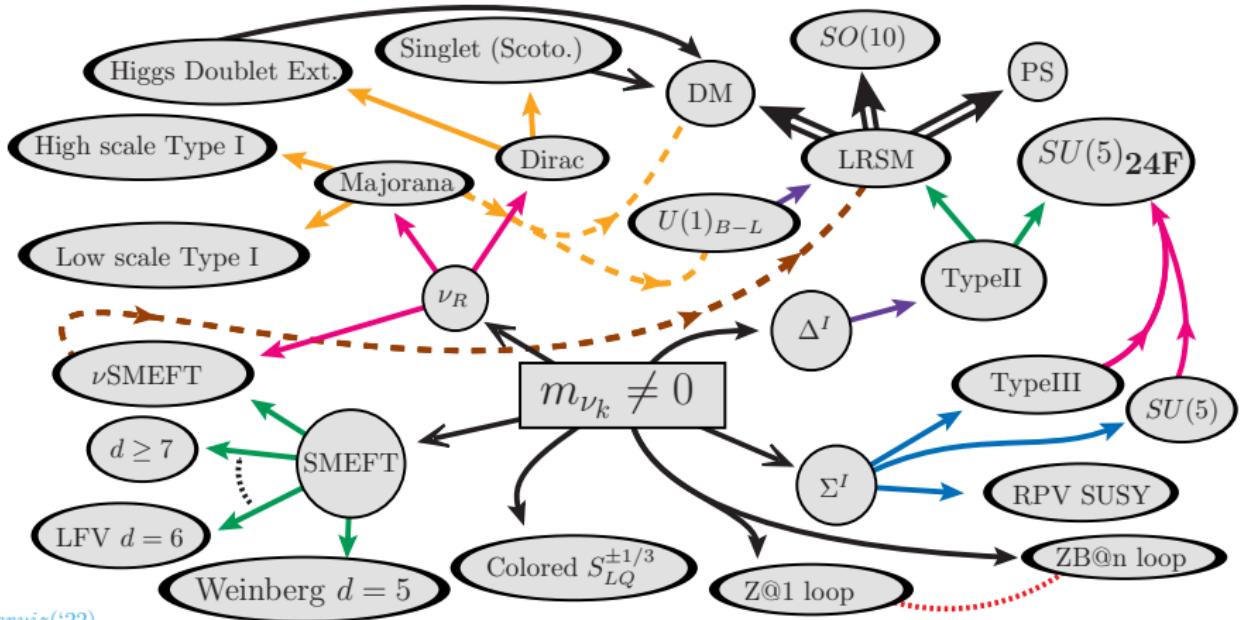


**Discovery of neutrino masses**  $\implies$  **several open questions:**

- $\nu$  have mass. **What is generating  $m_\nu$ ?**
- $\nu$  masses are *tiny*. **What sets the scale of  $m_\nu$ ?**
- $m_\nu$  are nearly degenerate. **What sets the pattern of  $m_\nu$ ?**
- $\nu$  carry no QCD/QED charge. **Are  $\nu, \bar{\nu}$  the same (Majorana)?**

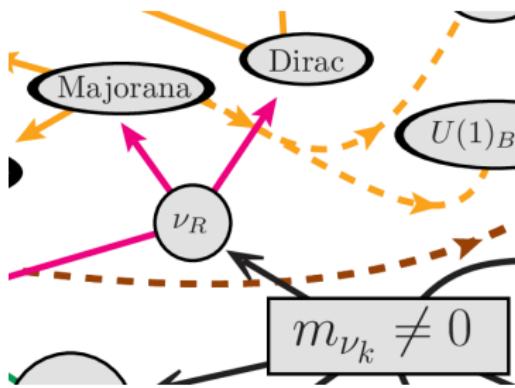
# These core ideas can be realized in *many* ways!

Minkowski ('77); Yanagida ('79); Glashow & Levy ('80); Gell-Mann et al., ('80); Mohapatra & Senjanović ('82); + *many* others



rruiz('22)

## right-handed neutrinos at the LHC<sup>2</sup>



<sup>2</sup>For reviews at colliders, see Cai, Han, Li, RR [1711.02180] and Pascoli, RR, Weiland [1812.08750]

## adding $\nu_R$ to the SM

To generate Dirac masses for  $\nu$  like other SM fermions, we need  $\nu_R$

$$\begin{aligned}\mathcal{L}_{\nu \text{ Yuk.}} &= -y_{\nu} \bar{\ell} \tilde{\Phi} \nu_R + H.c. = -y_{\nu} (\bar{\nu}_L \quad \bar{\ell}_L) \begin{pmatrix} \langle \Phi \rangle + h \\ 0 \end{pmatrix} \nu_R + H.c. \\ &= \underbrace{-y_{\nu} \langle \Phi \rangle}_{=m_D} \bar{\nu}_L \nu_R + H.c. + \dots\end{aligned}$$

$\nu_R$  do not exist in the SM, so pretend that they do and  $\nu_R = \nu_R^c$ :

$$\Rightarrow \mathcal{L}_{\text{mass}} = \frac{-1}{2} \underbrace{\begin{pmatrix} \bar{\nu}_L & \bar{\nu}_R^c \end{pmatrix}}_{\text{chiral state}} \underbrace{\begin{pmatrix} 0 & m_D \\ m_D & \mu \not{D} \end{pmatrix}}_{\text{mass matrix (chiral basis)}} \begin{pmatrix} \nu_L \\ \nu_R^c \end{pmatrix}$$

# adding $\nu_R$ to the SM

To generate Dirac masses for  $\nu$  like other SM fermions, we need  $\nu_R$

$$\begin{aligned}\mathcal{L}_{\nu \text{ Yuk.}} &= -y_{\nu} \bar{\ell} \tilde{\Phi} \nu_R + H.c. = -y_{\nu} (\bar{\nu}_L \quad \bar{\ell}_L) \begin{pmatrix} \langle \Phi \rangle + h \\ 0 \end{pmatrix} \nu_R + H.c. \\ &= \underbrace{-y_{\nu} \langle \Phi \rangle}_{=m_D} \bar{\nu}_L \nu_R + H.c. + \dots\end{aligned}$$

$\nu_R$  do not exist in the SM, so pretend that they do and  $\nu_R = \nu_R^c$ :

$$\Rightarrow \mathcal{L}_{\text{mass}} = \frac{-1}{2} \underbrace{\begin{pmatrix} \bar{\nu}_L & \bar{\nu}_R^c \end{pmatrix}}_{\text{chiral state}} \underbrace{\begin{pmatrix} 0 & m_D \\ m_D & \mu \not{e} \end{pmatrix}}_{\text{mass matrix (chiral basis)}} \begin{pmatrix} \nu_L \\ \nu_R^c \end{pmatrix}$$

After diagonalizing the mass matrix, identify  $\nu_L$  (chiral eigenstate) in the SM as a linear combination of mass eigenstates:

$$\underbrace{|\nu_L\rangle}_{\text{chiral state}} = \cos \theta \underbrace{|\nu\rangle}_{\text{light mass state}} + \sin \theta \underbrace{|N\rangle}_{\text{heavy mass state (this is a prediction!)}}$$

# For the experts (1 slide)

Generically parameterize active-sterile neutrino mixing via

Atre, et al [0901.3589]

$$\underbrace{\nu_{\ell L}}_{\text{flavor basis}} \approx \sum_{m=1}^3 \underbrace{U_{\ell m} \nu_m + V_{\ell m'=4} N_{m'=4}}_{\text{mass basis}} \quad (\text{neglect heavier } N_{m'})$$

The SM  $W$  coupling to **leptons** in the **flavor basis** is

$$\mathcal{L}_{\text{Int.}} = -\frac{g_W}{\sqrt{2}} W_\mu^- \sum_{\ell=e}^\tau [\bar{\ell} \gamma^\mu P_L \nu_\ell] + \text{H.c.}, \quad \text{where } P_L = \frac{1}{2}(1 - \gamma^5)$$

$\implies$   $W$  coupling to  $N$  in the **mass basis** is

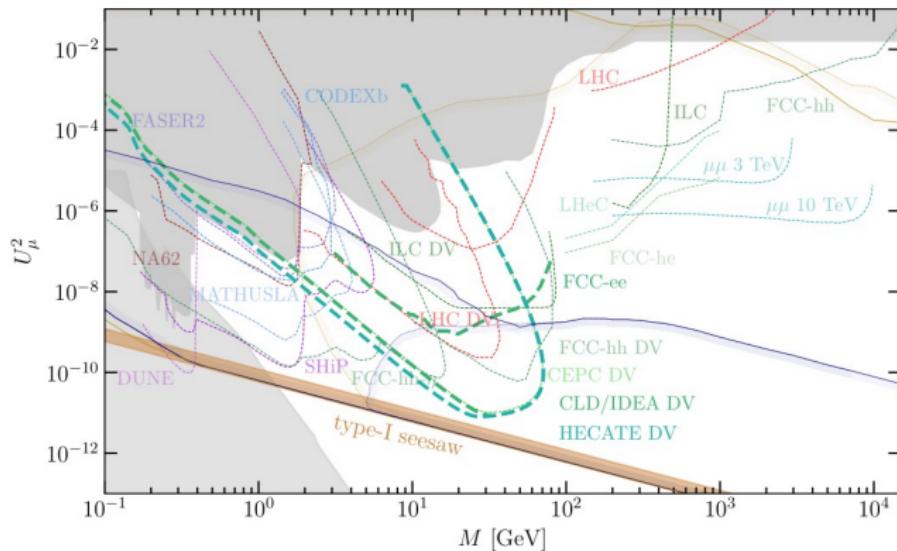
$$\mathcal{L}_{\text{Int.}} = -\frac{g_W}{\sqrt{2}} W_\mu^- \sum_{\ell=e}^\tau \left[ \bar{\ell} \gamma^\mu P_L \left( \sum_{m=1}^3 U_{\ell m} \nu_m + V_{\ell N} N \right) \right] + \text{H.c.}$$

$\implies N$  is **accessible through  $W/Z/h$  bosons**

# Outlook for low-mass heavy neutrinos ( $N$ )

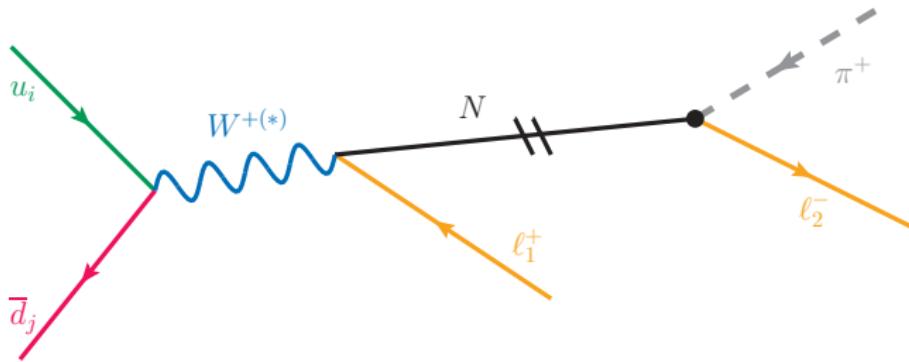
**Community Message:** Current + next-gen. facilities can probe *simplest* ( $m_{\nu_1} = 0$ ) leptogenesis scenario w/  $\nu_R$

Abdullahi, et al [2203.08039]; w/ Alimena, et al [2203.05502]



**Note:** LHC picture evolving with new strategies and channels

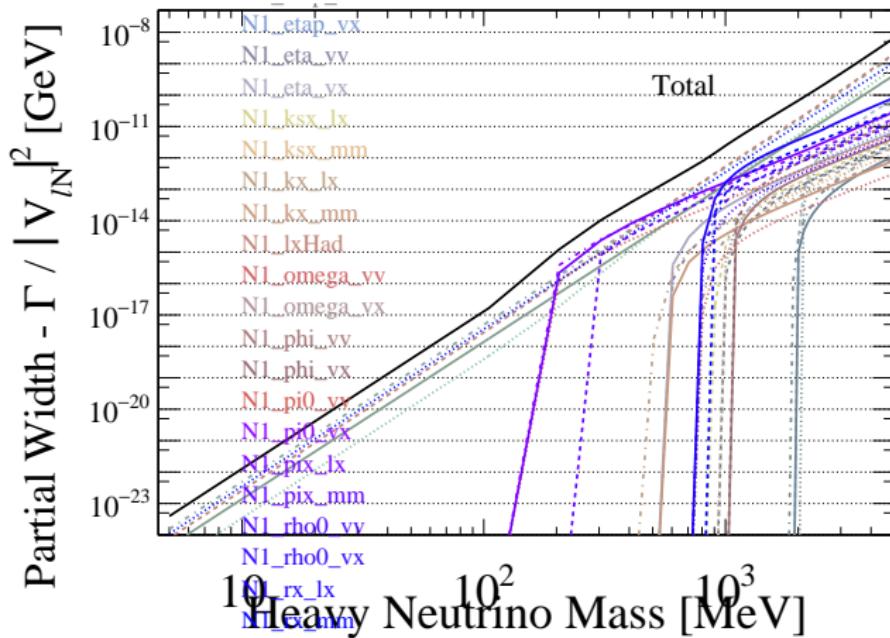
**what about low, low-mass  $N$ ?**



# Decays of sub-GeV $N$

For  $m_N \lesssim 2$  GeV,  $N \rightarrow \ell^\pm + n\text{Had}$ . decays disappear (no phase space)

– however, single-meson modes remain:  $N \rightarrow \ell^\pm M^\mp$  or  $\nu M^0$



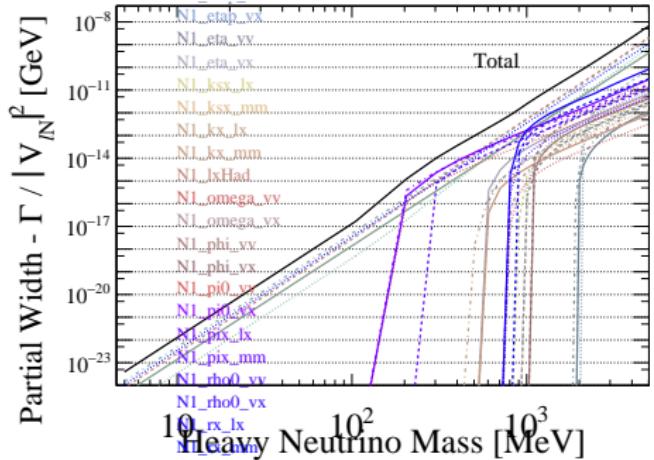
This plot is interesting →

$N \rightarrow \ell^\pm M^\mp$  and  $N \rightarrow \nu M^0$  decay rates were computed with

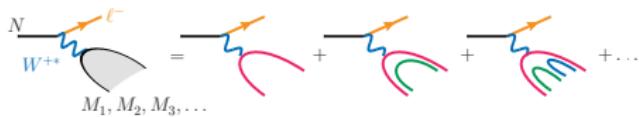
`HeavyN_Meson+MadGraph5_aMC@NLO`

`mg5amc` is a flagship event generator for collider experiments:

- up to NLO in QCD for (B)SM
- up to NLO in EW for SM
- BSM possible if Feynman rules are known (`FeynRules` “UFO” plugin)



[w/ Jeon<sup>†</sup>, Fernandez-Martinez, Kulkarni, et al (in progress)]



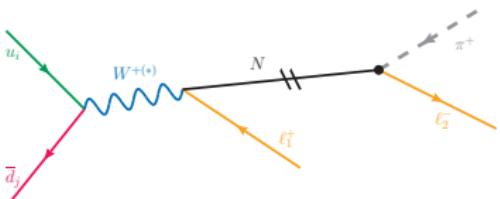
New: `HeavyN_Meson` UFO combines two things:

- HeavyN UFO: Feynman rules for Type I Seesaw
- Low-energy EFT for  $N$ - $M$ - $\ell$ / $\nu$

Degrard, RR, et al 1602.06957

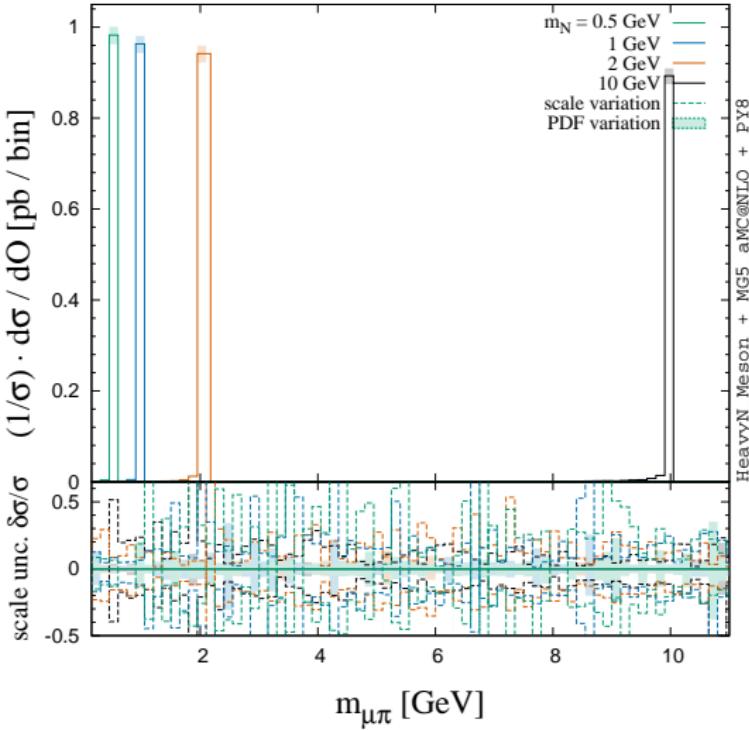
Coloma, Fernandez-Martinez, et al 2007.03701

# Light mesons from light $N$ at the LHC



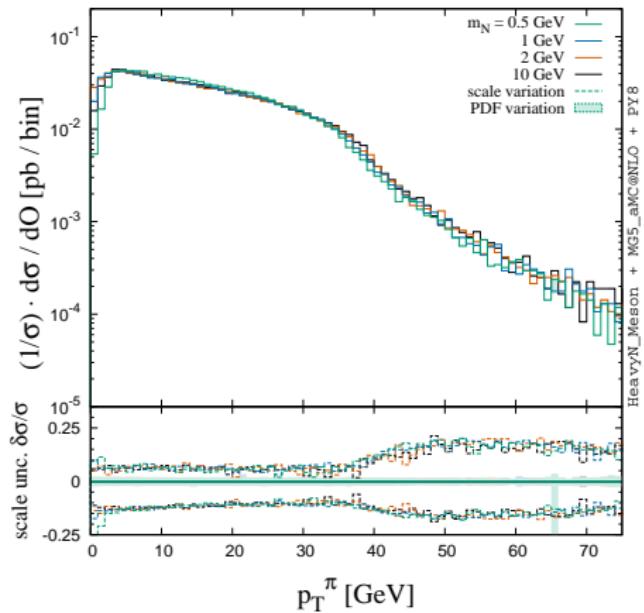
## Proof-of-concept:

1.  $pp \rightarrow W^{(*)} \rightarrow Ne^\pm$  at NLO in QCD at  $\sqrt{s} = 13$  TeV LHC
2.  $N \rightarrow \mu^\pm \pi^\mp$  decay with full spin correlation
3. full parton shower (PY8)
4. basic reconstruction

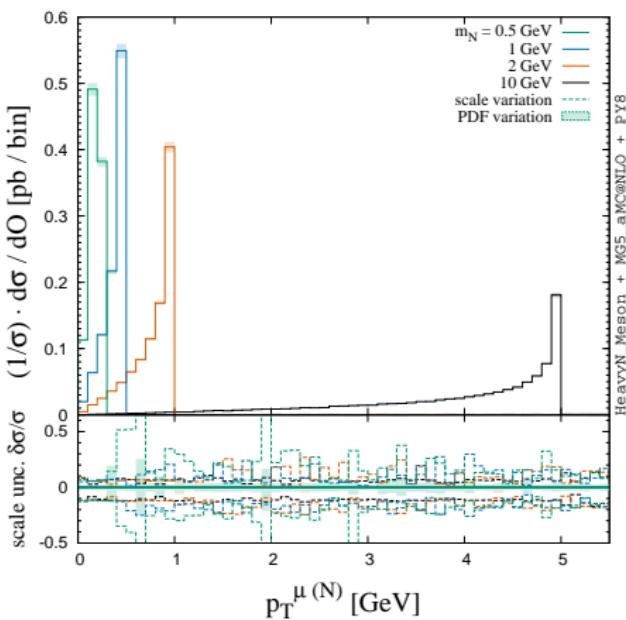


# Light mesons from light $N$ at the LHC

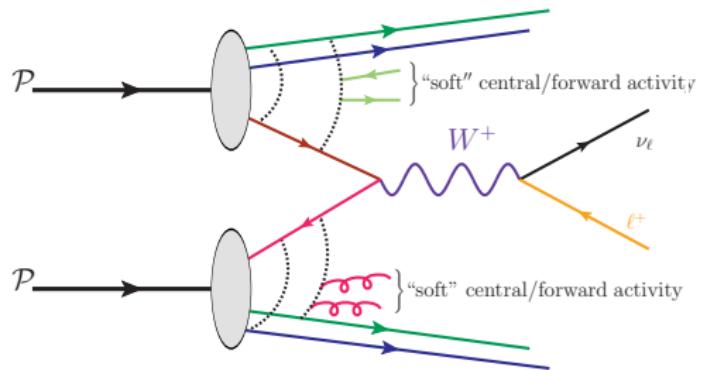
lab frame



$N$ 's frame



## challenges of a low-mass analysis



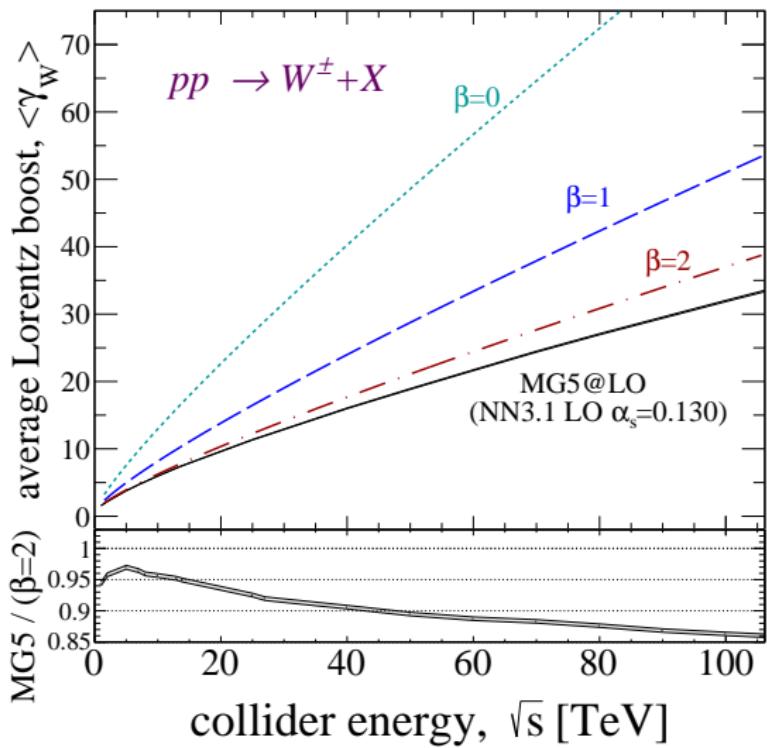
**Challenge:** at  $\sqrt{s} = 13/14$  TeV, lots of GeV-scale mesons

**interesting resolution** can be realized by approximating PDF:  $f_{i/p}(\xi) \approx \frac{\text{const.} \times (1-\xi)^\beta}{x^{1+\delta}}$

for  $\beta = 2$ ,  $\langle \gamma_W^{(\text{lab})} \rangle = \frac{-1 - 9\tau_0 + 9\tau_0^2 + \tau_0^3 - 6\tau_0(1+\tau_0)\log(\tau_0)}{3\sqrt{\tau_0}[3 - 3\tau_0^2 + (1 + 4\tau_0 + \tau_0^2)\log(\tau_0)]}$ , where  $\tau_0 = M_W^2/s$

**first take away:** varying  $\beta$  shows importance of  $\xi = 1$  and large  $y$  (rapidity) regions

**Plotted:** avg. Lorentz boost of  $W$   
 $(\langle \gamma_W^{(\text{lab})} \rangle = \langle E_W^{(\text{lab})} \rangle / M_W)$



**Plotted:** avg. Lorentz boost of  $N$   
 $(\langle \gamma_N^{(\text{lab})} \rangle = \langle E_N^{(\text{lab})} \rangle / m_N)$

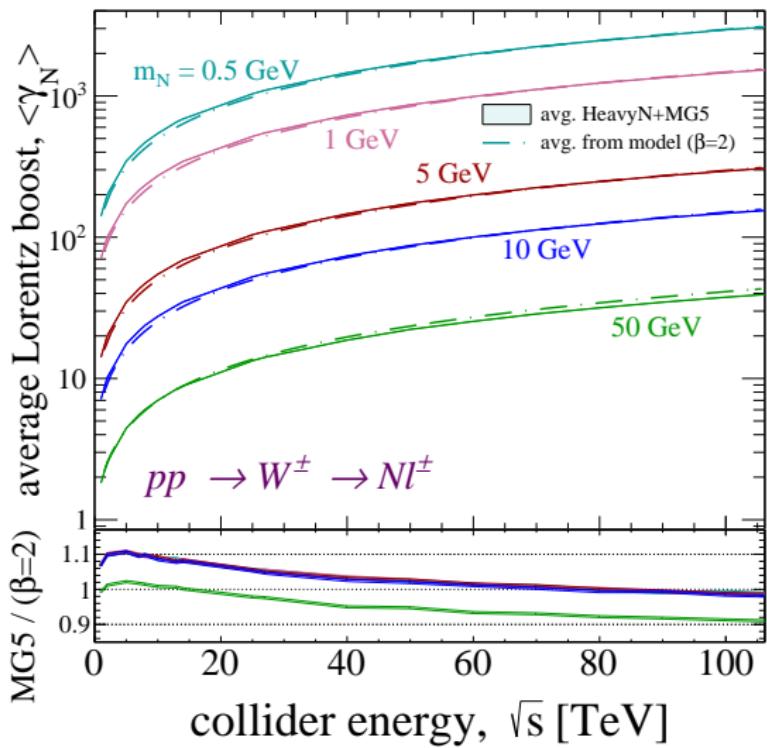
**Challenge:** at  $\sqrt{s} = 13/14$  TeV, lots of GeV-scale mesons

**interesting resolution** can be realized by approximating  $\langle \gamma_N^{(\text{lab})} \rangle = \langle \gamma_W^{(\text{lab})} \rangle|_{\beta=2} \times E_N^{(W)}$

where

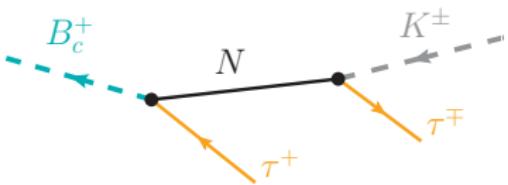
$$E_N^{(W)} = \frac{M_W}{2} \left( 1 + \frac{m_N^2}{M_W^2} - \frac{m_l^2}{M_W^2} \right)$$

**second take away:** ultra light  $N$  (and decay products) are still very energetic!



## $\mathcal{B}$ factories

For  $m_N \ll M_W$ ,  $N$  can appear in  $B_c^+ \rightarrow \tau^+\tau^\mp K^\pm$  decays (or similar)

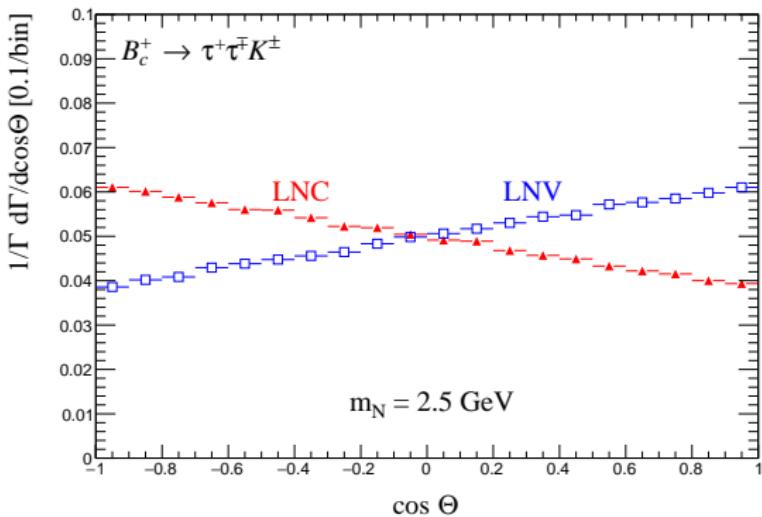


**PRELIMINARY:** polar angle of  $K^\pm$  w.r.t.  
 $N$ 's propagation direction

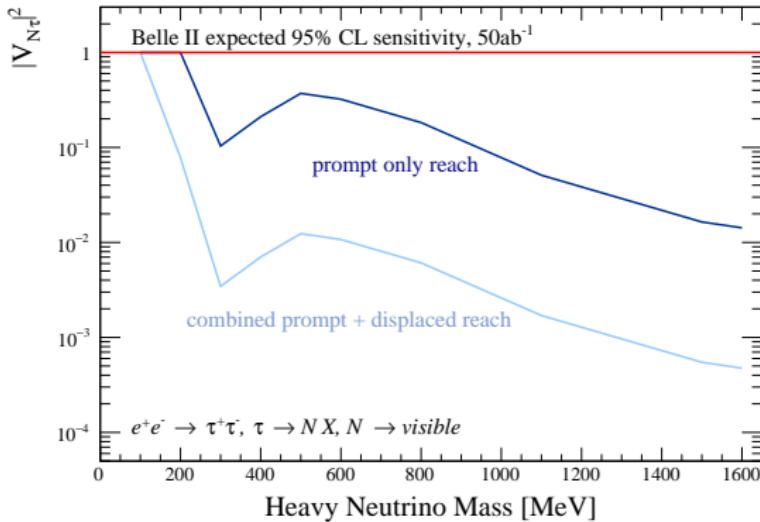
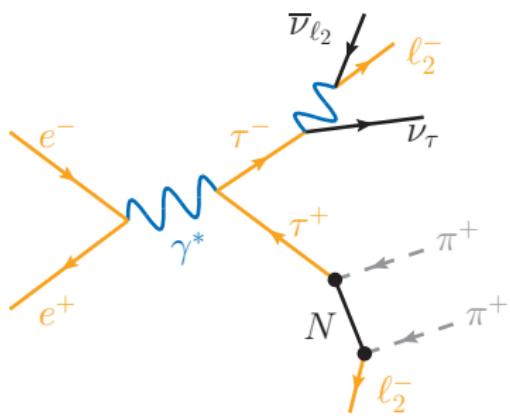
**Take away:** angular distributions encode differences between  
LN<sup>V</sup> ( $\tau^+\tau^+K^-$ ) and  
LFC ( $\tau^+\tau^-K^+$ )

Han, Lewis, RR, et al [1211.6447]

☺ reconstructed from evts  
using HeavyNMeson+MG5 →



For  $m_N \ll M_W$ ,  $N$  can appear in decays of  $\tau^\pm$



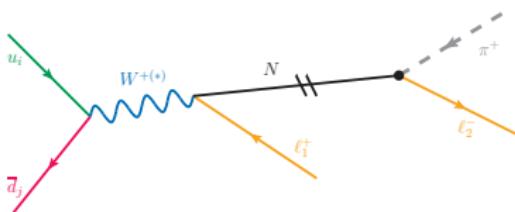
LHC is not the only collider looking for  $N$

- **PRELIMINARY: Belle 2's sensitivity to LNV and LFV from  $\tau^\pm$  decays show promise, but numbers need finalizing**

# Summary and conclusion

ν have mass and discovering their origin motivates searches at colliders!

for reviews, see Cai, Han, Li, RR [1711.02180] and Pascoli, RR, Weiland [1812.08750]



- the existence of (sub-)GeV sterile  $N$  is a well-motivated solution  
(but not only solution!)
- new software (HeavyN\_Meson) developed to facilitate state-of-the-art simulations for  $N \rightarrow M\ell/\nu$ ,  $M \rightarrow N\ell/\nu$ , and  $\tau \rightarrow NM$  at colliders
- Preliminary results are encouraging; final results out soon!

**Thank you!**

**backup**

# Approximating $\langle \gamma_W^{(\text{lab})} \rangle$

The starting point is the **Collinear Factorization Thm**

Collins, Soper, Sterman ('85, '88, '89); Collins, Foundations of pQCD (2011)

$$d\sigma^{\text{LO}}(pp \rightarrow W + X) = \sum_{a,b} f_a \otimes f_b \otimes d\hat{\sigma}^{\text{LO}}(ab \rightarrow W) + \mathcal{O}\left(\frac{\Lambda_{\text{NP}}^p}{Q^{p+2}}\right)$$

part./nucl. boundary

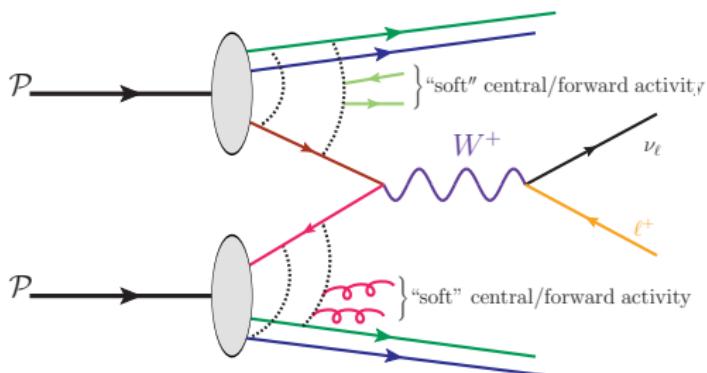
The average of a kinematic observable  $\mathcal{O}$  can be obtained from the matrix element:

$$\langle \mathcal{O} \rangle = \frac{1}{\sigma} \times \int d\sigma \times \mathcal{O}$$

$$\implies \langle E_W \rangle = \frac{1}{\sigma} \times \int d\sigma \times E_W$$

$$\implies \langle E_W \rangle|_{\text{events}} \approx \frac{1}{\sigma} \times \sum_i wgt_i \times E_W$$

Assuming  $f_{i/p}(\xi) \approx \frac{\text{const.} \times (1-\xi)^\beta}{x^{1+\delta}}$ , with  $\beta = 0, 1, 2, \dots$ , gives a closed form for  $\sigma(pp \rightarrow W + X)!$



## HeavyN : The Standard Model + Heavy Neutrinos at NLO in QCD

### Contact Author

Richard Ruiz

- Institute of Nuclear Physics Polish Academy of Science (IFJ PAN)
- richard.physics AT gmail.com

In collaboration with:

D. Alva and T. Han [ 1 ]; C. Degrande, O. Mattelear, and J. Turner [ 2 ]; S. Pascoli and C. Weiland [ 3, 4 ]; and V. Cirigliano, W. Dekens, J. de Vries, K. Fuyuto, E. Mere

### Usage resources

- For detailed instructions and examples on using the HeavyN UFO libraries, see C. Degrande, et al, [arXiv:1602.06957](#) and S. Pascoli, et al, [arXiv:1812.08750](#).
- **\*New\*** For heavy neutrinos in vSMEFT, see V. Cirigliano, et al, [arXiv:2105.11462](#).
- See **Validation** section below for additional information

### Citation requests

- For studies of heavy Majorana neutrinos, please consider citing [ 6 ] for the Lagrangian and [ 1, 2 ] for the Majorana FR/UFO files.
- For studies of heavy Dirac neutrinos, please also consider citing [ 4 ].
- **\*New\*** For studies of heavy neutrinos in vSMEFT, please consider citing [ 5 ].

## Model Description

### Majorana N

This effective/simplified model extends the Standard Model (SM) field content by introducing three right-handed (RH) neutrinos, which are singlets under the SM gauge symmetries. After electroweak symmetry breaking, the Lagrangian with three heavy Majorana neutrinos  $N_i$  (for  $i=1,2,3$ ) is given by [ 6 ]

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_N + \mathcal{L}_{N \text{ Int.}} \quad (1)$$

The first term is the Standard Model Lagrangian. In the mass basis, i.e., after mixing with active neutrinos, the heavy Majorana neutrinos' kinetic and mass terms are

$$\mathcal{L}_N = \frac{1}{2} \overline{N_k} i \not{\partial} N_k - \frac{1}{2} m_{N_k} \overline{N_k} N_k, \quad k = 1, \dots, 3, \quad (1)$$

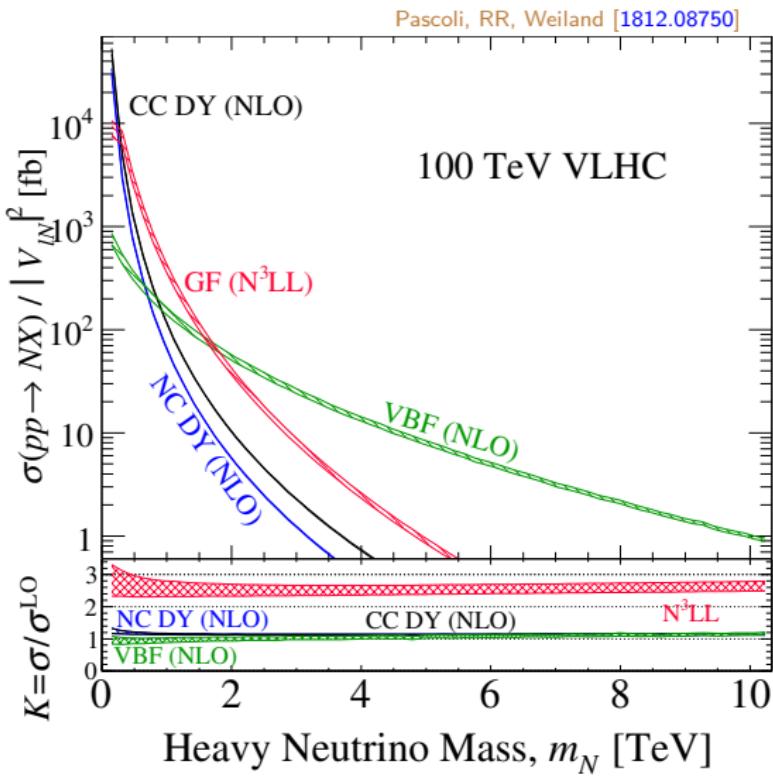


# FeynRules to MadGraph5aMC@NLO

Given a *Universal FeynRules Object* (UFO) file, run `mg5amc` out of the box

```
$ ./bin/mg5_aMC
> import model SM_HeavyN_NLO
> define p = g u c d s b u~ c~
d~ s~ b~ a
> define ell = mu+ mu-
> generate p p > n2 ell [QCD]
> output PP_Nmu_NLO
> launch PP_Nmu_NLO
> order=NLO
> fixed_order=ON
> set LHC 100
> set vmu2 1.0
> set mn2 scan:range(5,1001,25)
> set wn2 auto
```

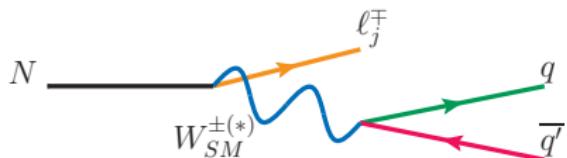
$\mathcal{O}(10)$  lines to get each curve →



# mg5amc+MadSpin+Parton Shower

If the **narrow width approximation** is justified ( $\Gamma_N/m_N \ll 1$ ), efficient generation of  $e^+e^- \rightarrow Z \rightarrow \nu N \rightarrow \nu \ell^\pm q\bar{q}'$  possible with MadSpin:

Spin-correlation fully treated, RR [2008.01092]



In `madspin_card.dat`, write:

```
set spinmode onshell  
  
define q = u c d s u~ c~ d~ s~  
  
define ee = e+ e-  
  
decay n1 > ee q q  
  
launch
```

Parton showering with PY8 or HERWIG straightforward

**Fun Fact:** possible to steer entire process with a script →

```
rruiz@mac-1R0-359:~/Scripts/MG5aMC$ more runEffLRSMnlo_pp_Ne_NLO_update.txt  
launch EffLRSMnlo_pp_wr_Ne_NLO  
order=NLO  
shower=PY8  
madspin=ON  
done  
set mwr 4000  
set mn1 100  
compute_widths wr+  
compute_widths n1  
set no_parton_cut  
set nevents 100k  
set LHC 13  
set shower_card nsplit_jobs 100  
set shower_card ue_enabled true  
  
launch EffLRSMnlo_pp_wr_Ne_NLO  
order=L0  
shower=ON
```