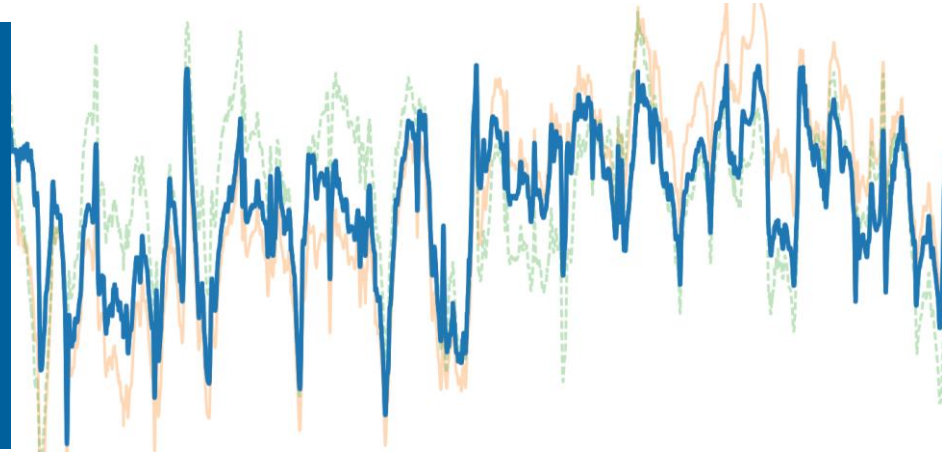
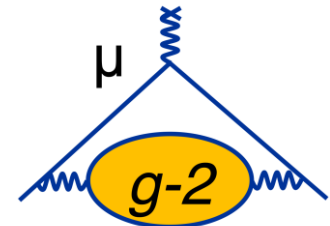


MEASUREMENT OF THE MAGNETIC FIELD IN THE FERMILAB MUON G-2 EXPERIMENT



SIMON CORRODI
Argonne National Laboratory

on behalf of the Muon g-2 collaboration
NuFact 2023, Seoul
August 25, 2023



RUN 1 (2018)



RUN 2/3 (2019/2020) and beyond



RUN 2/3 (2019/2020) and beyond

$$\omega_a = \omega_s - \omega_c$$

store polarized muons
in a **dipole B** field

extract the muon magnetic anomaly
215 ppb

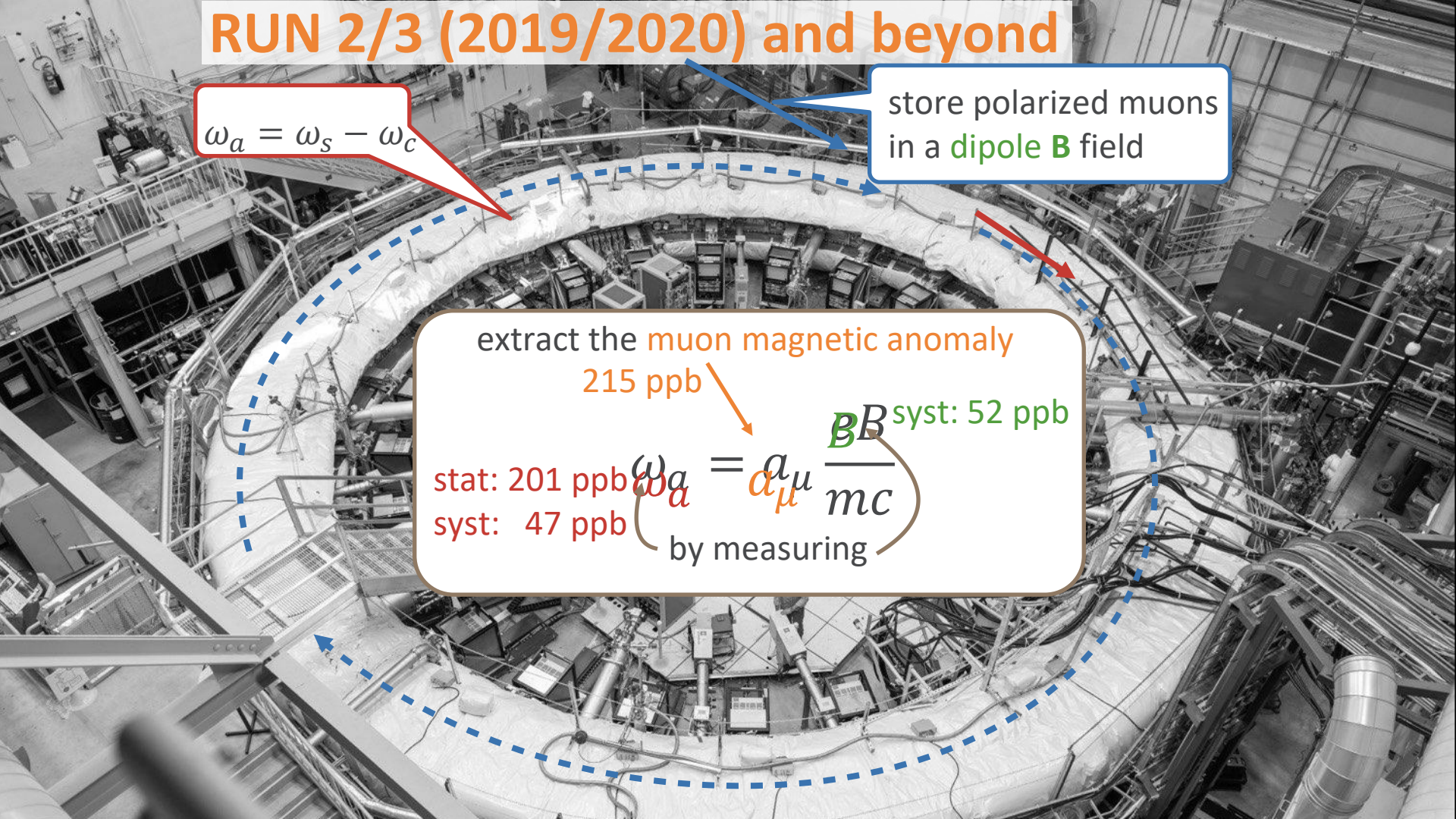
$\mathcal{B}\mathcal{B}$ syst: 52 ppb

stat: 201 ppb

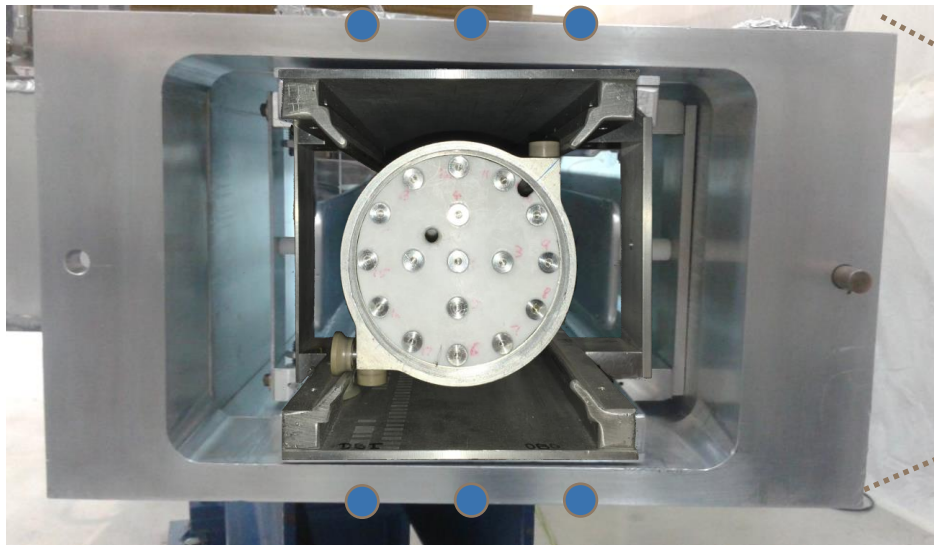
syst: 47 ppb

$$\omega_a = a_\mu \frac{\mathcal{B}\mathcal{B}}{mc}$$

by measuring

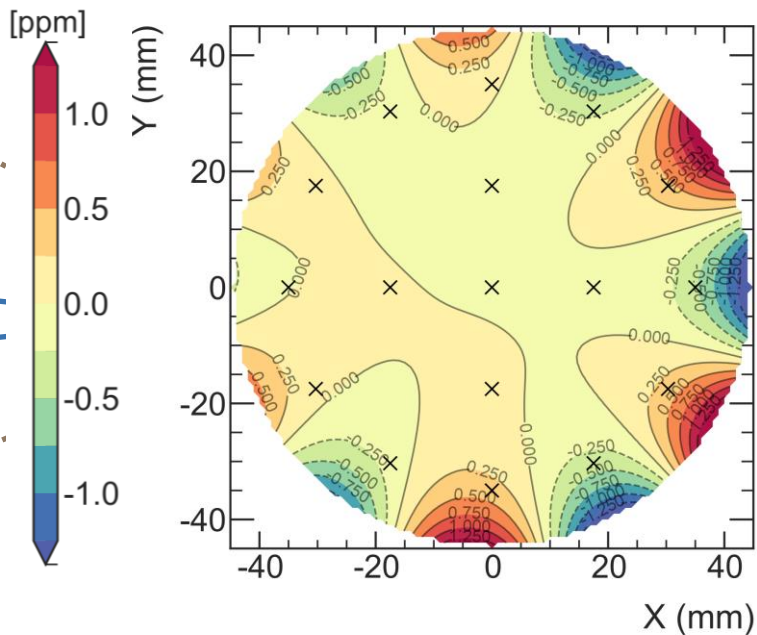


Filed Monitor: Fixed NMR Probes



Trolley: Field Mapper

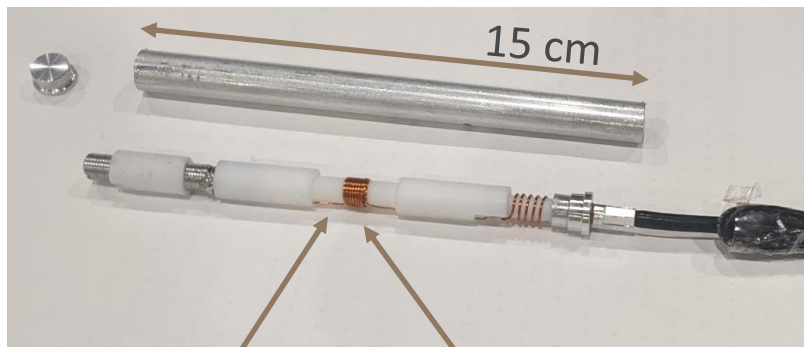
Designed for homogeneity (and stability)



azimuthally averaged B
field

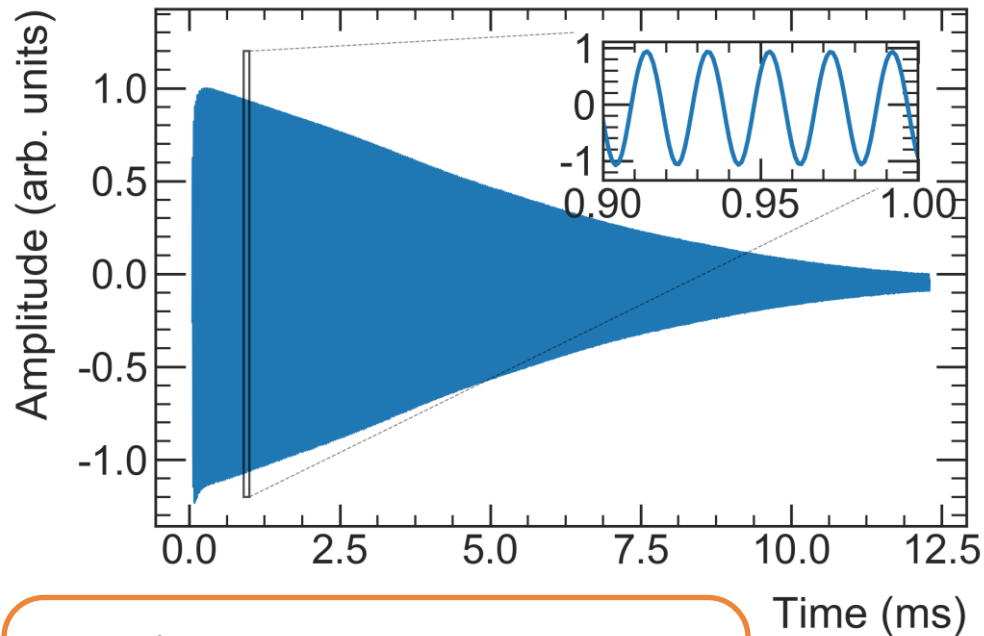
NUCLEAR MAGNETIC RESONANCE: “COMAGNETOMETER”

$$B = \gamma_p \omega_p$$



proton rich sample

coil:
spin-flip & pick-up

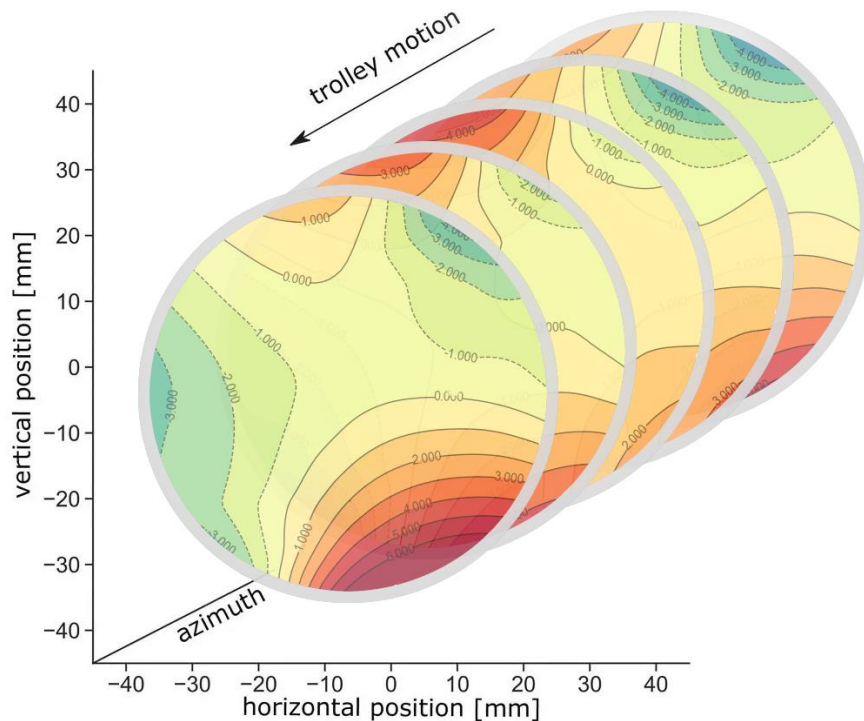
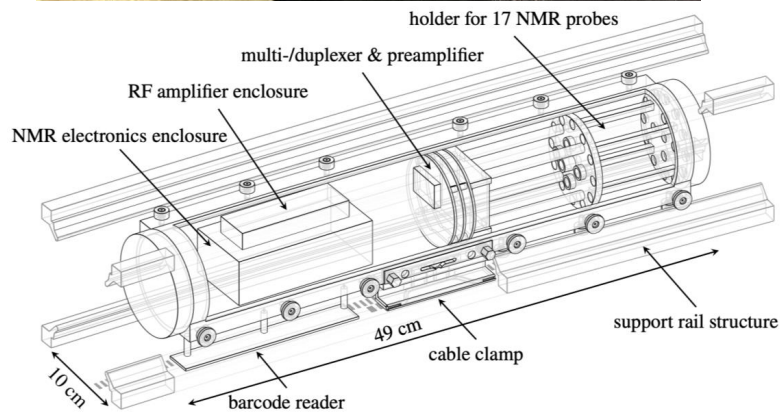


Run-2/3 improvement:

Evaluation of unc. in ω_p extraction
uncertainty: 16 - 19 ppb

MAPPING THE FIELD: THE TROLLEY

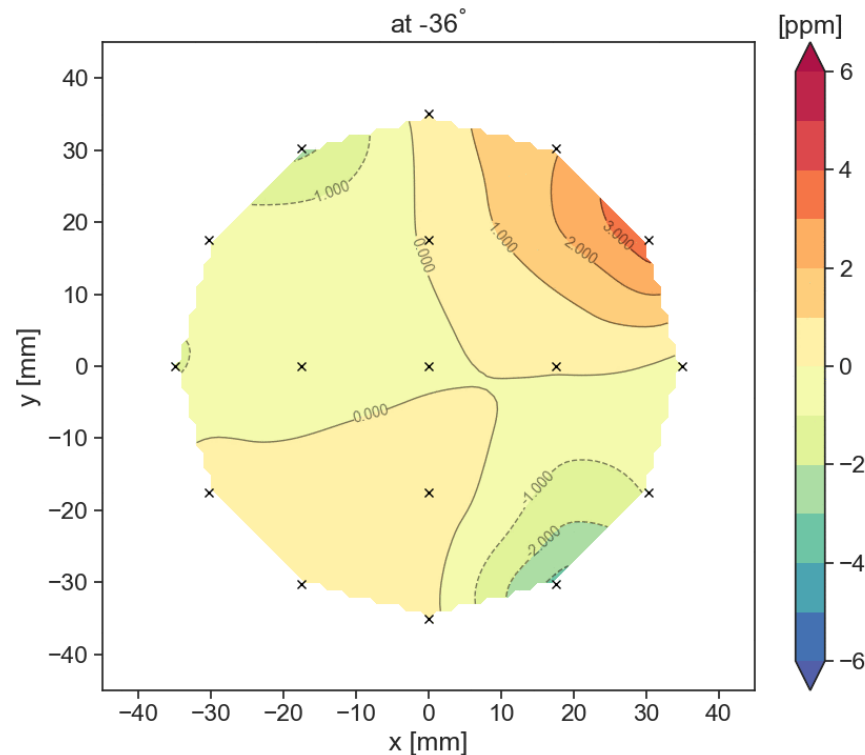
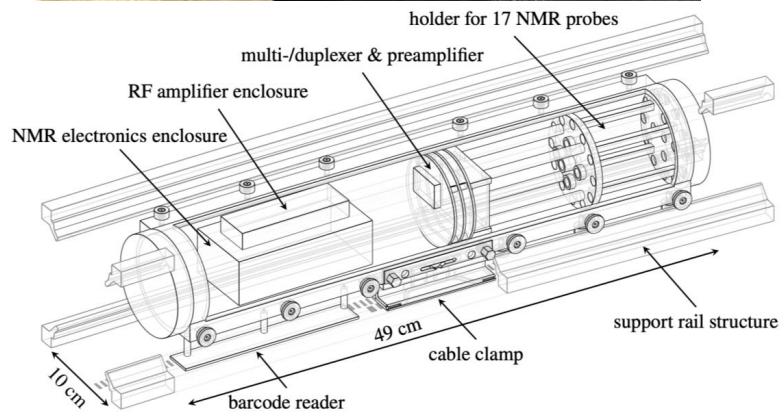
17 probes, moves around the ring (70min)



~9000 2D field maps around the ring

MAPPING THE FIELD: THE TROLLEY

17 probes, moves around the ring (70min)

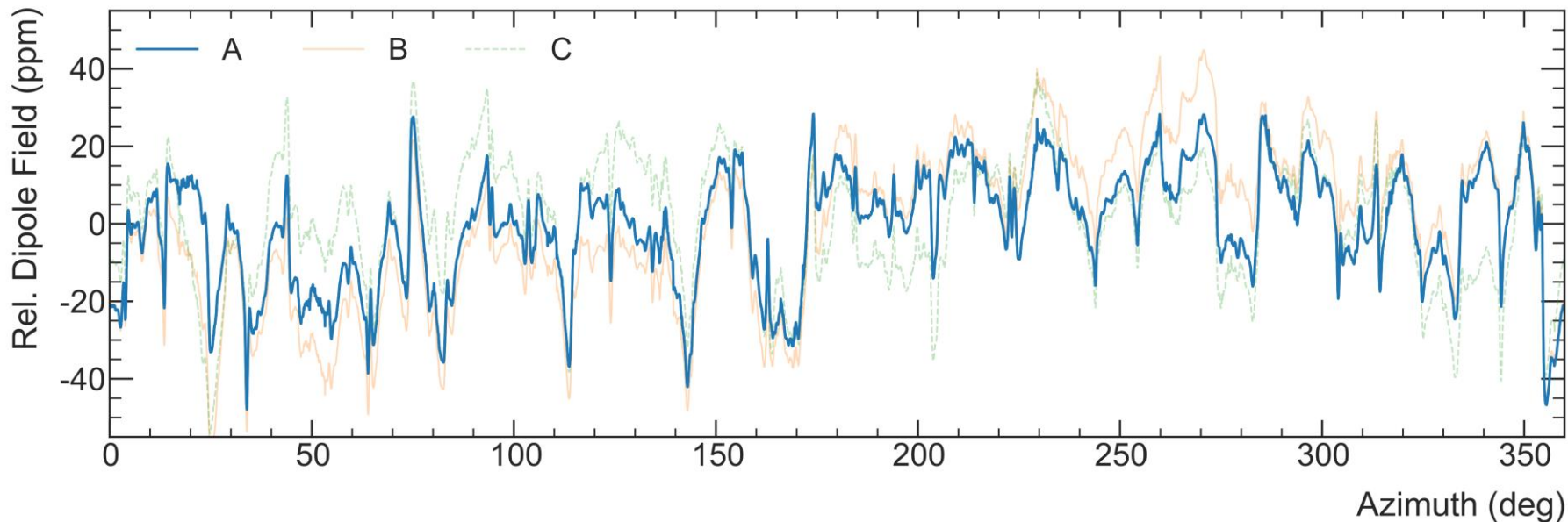


FIELD MAPS

12 parameter multipole expansion to describe the field in 2D slices

RMS around the ring <20 ppm

take field maps every 3-5 days



uncertainty from parametrization: 3 - 8 ppb

FIELD MAPS: CHALLENGES

Challenges/sources of uncertainties



(Non-uniform) motion
-> small eddy currents
uncertainty: 18 ppb

non perfect rail alignment
uncertainty: ~10 ppb

position determination
uncertainty: 4 ppb

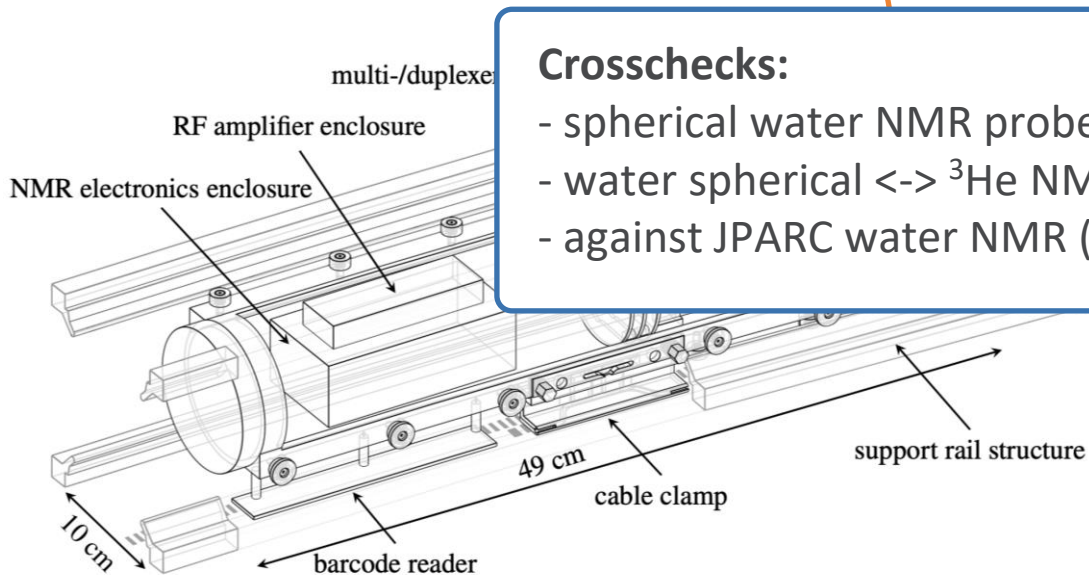
Run-2/3 improvement:
NMR probe temperature
dependence
uncertainty: 9-15 ppb

CALIBRATION

Calibrate to the Larmor frequency of shielded protons in a spherical sample: ω'_p

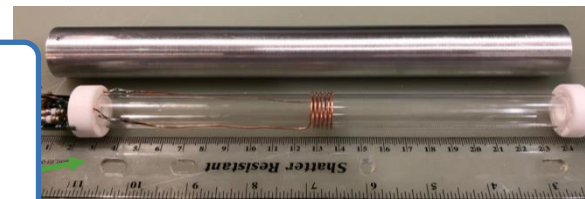
NMR probes are in the
“trolley’s magnetic environment”

water based calibration probe



Crosschecks:

- spherical water NMR probe (BNL)
- water spherical \leftrightarrow ^3He NMR
- against JPARC water NMR (CW)



in situ uncertainty: 17 ppb

- 2) correct for material effects
- 3) correct from cylinder \rightarrow sphere
uncertainty: 9 ppb

CALIBRATION

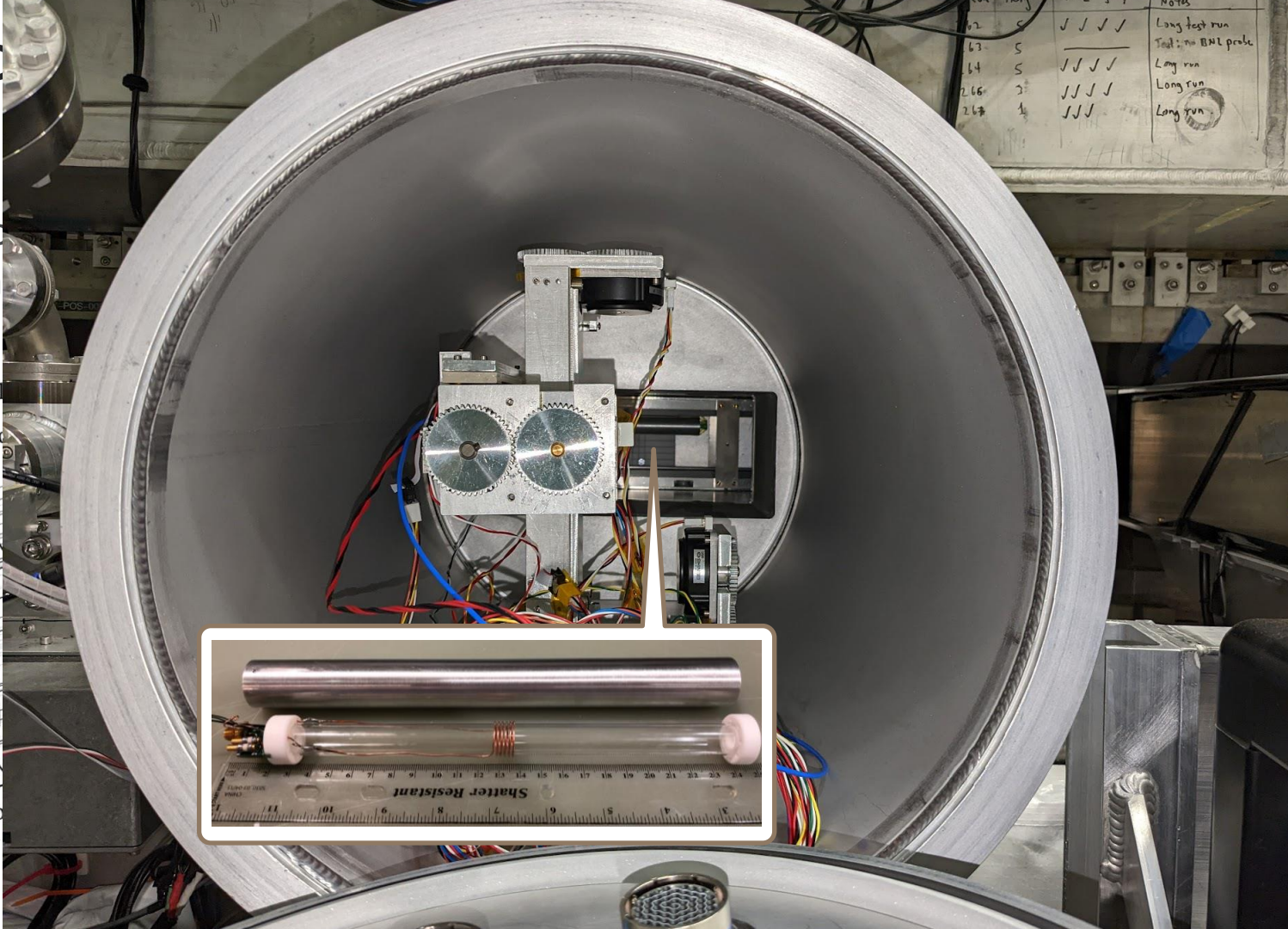
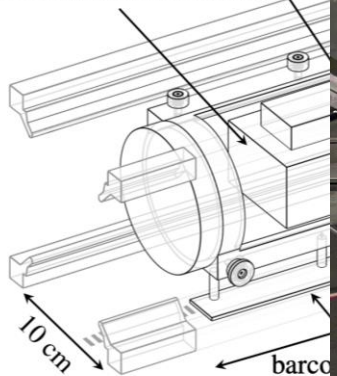
Calibrate to the

NMR p
“trolley’s m

mul

RF amplifier encl

NMR electronics enclosure



NOTES		
62	S	✓✓✓✓ Long test run
63	S	Test: no BNL probe
64	S	✓✓✓✓ Long run
246	3	✓✓✓✓ Long run
267	4	✓✓✓ Long run

CALIBRATION

Calibrate to the Larmor frequency of shielded protons in a spherical sample: ω'_p

$$a_\mu = \frac{\omega_a}{\omega'_p} \frac{\mu'_p}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}$$

ω'_p : 10.5 ppb uncertainty (hydrogen maser) Metrologia **13**, 179 (1977)
 bound state QED calc., exact
 $\frac{g_e}{2}$: 0.13 ppt uncertainty PDG, dominated by Phys. Rev. Lett. **130**, 071801 (2023)
 $\frac{m_\mu}{m_e}$: 22 ppb uncertainty (Muonium hyper fine split.) Phys. Rev. Lett. **82**, 711 (1999)

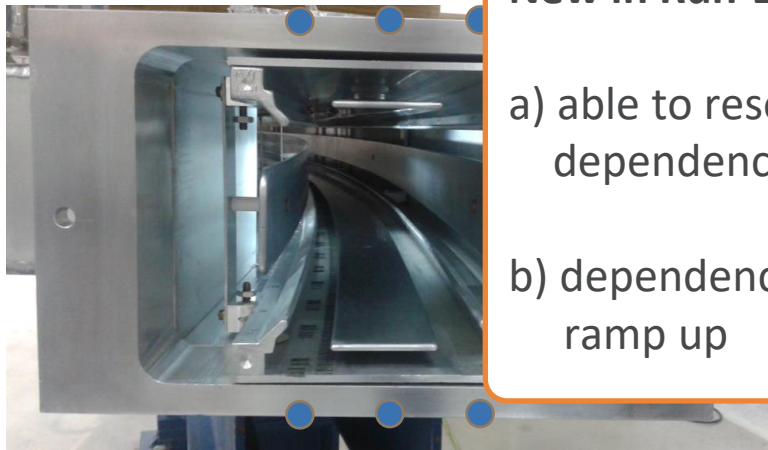
magnetic field seen by the muons

TRACKING THE FIELD OVER TIME

378 Fixed Probes

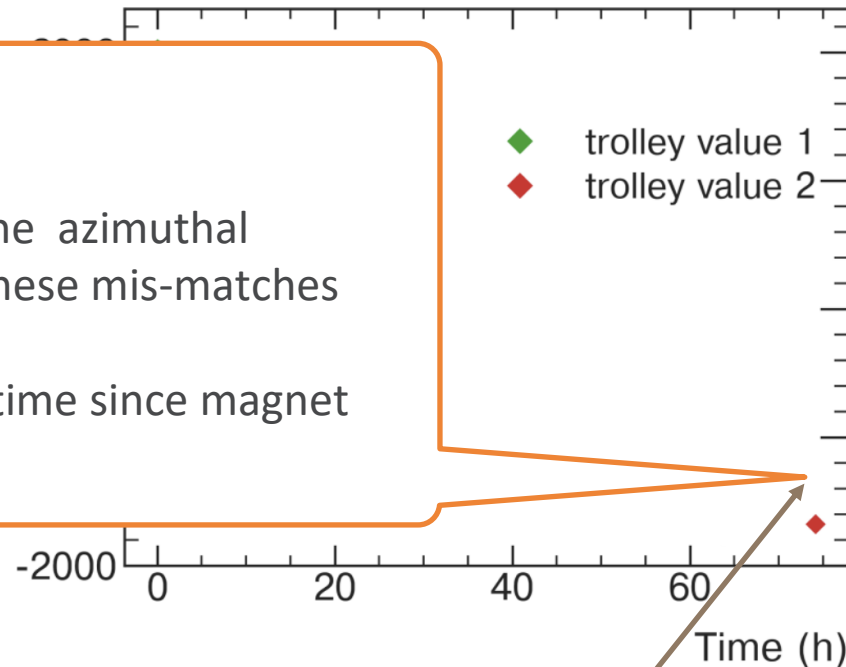
- Outside of the storage region
- 72 position, $\sim 5\text{deg}$ azimuth

the field at one azimuth



New in Run-2/3

- a) able to resolve the azimuthal dependence of these mis-matches
- b) dependence on time since magnet ramp up



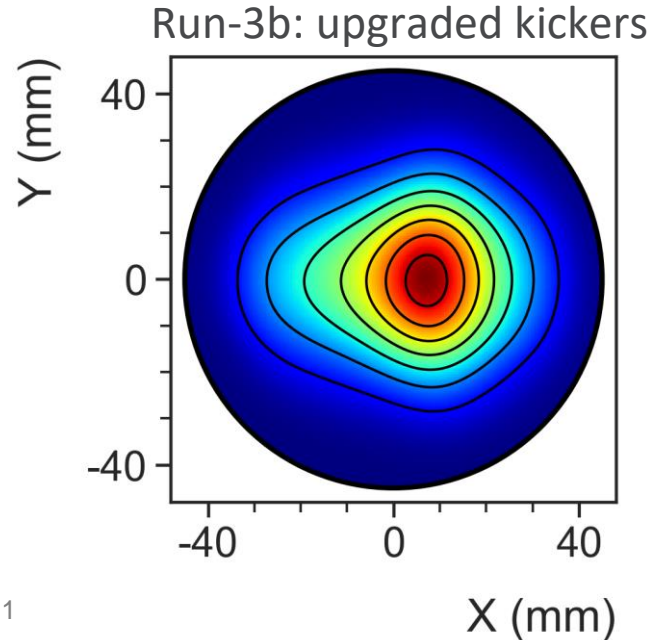
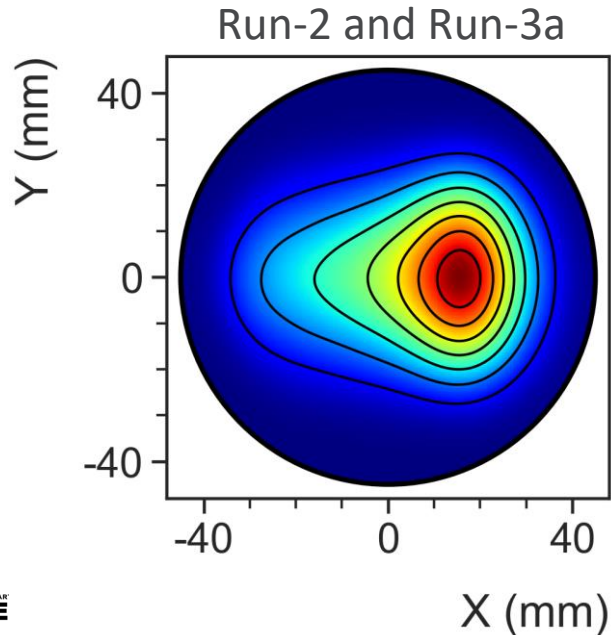
tracking uncertainty from these mis-matches
uncertainty: ~ 17 ppb

WEIGHTING THE FIELD BY THE MUON DISTRIBUTION

field maps $\omega'_p(x, y, \phi; t)$
tracked by the fixed probes

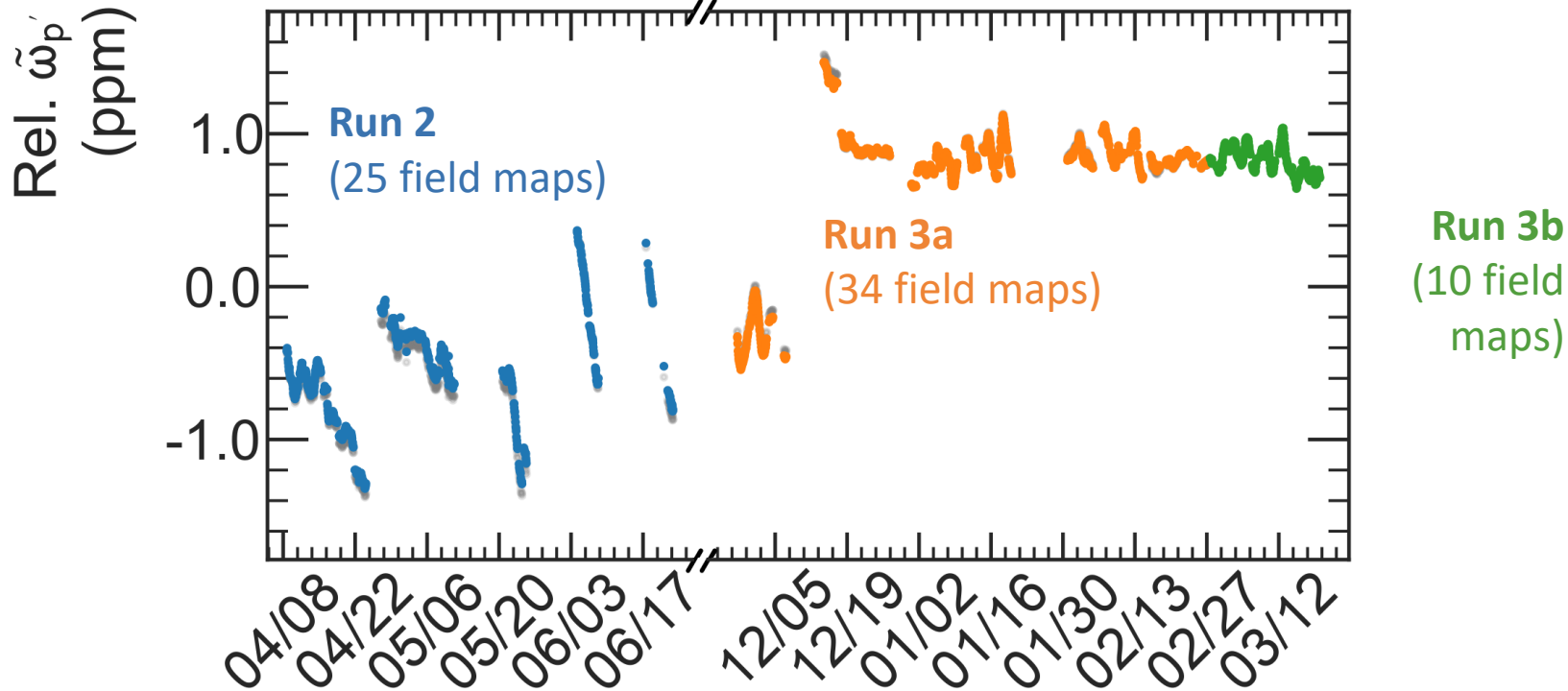
muon distribution $M(x, y, \phi; t)$
from trackers + simulation *uncertainty: 7 - 13 ppb*

$$\tilde{\omega}'_p(t) = \frac{\int \omega'_p(x, y, \phi; t) M(x, y, \phi; t) dV}{\int M(x, y, \phi; t) dV}$$

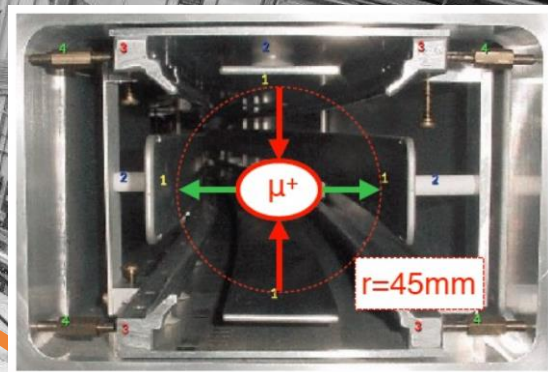
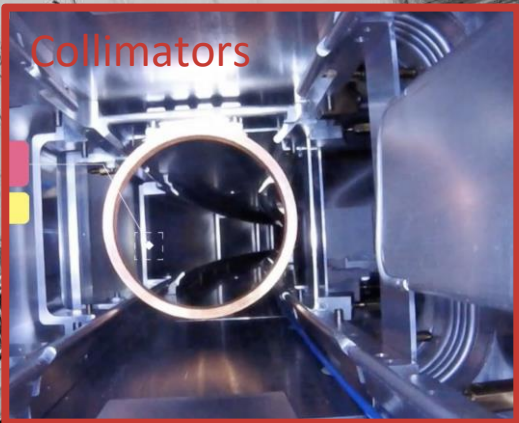


THE MAGNETIC FIELD OF RUN 2/3

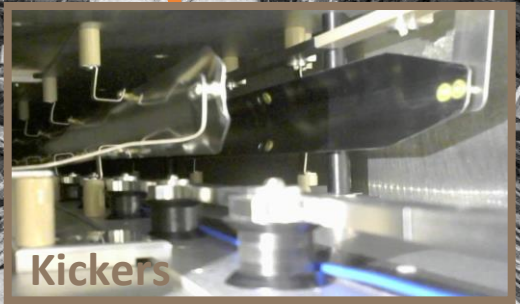
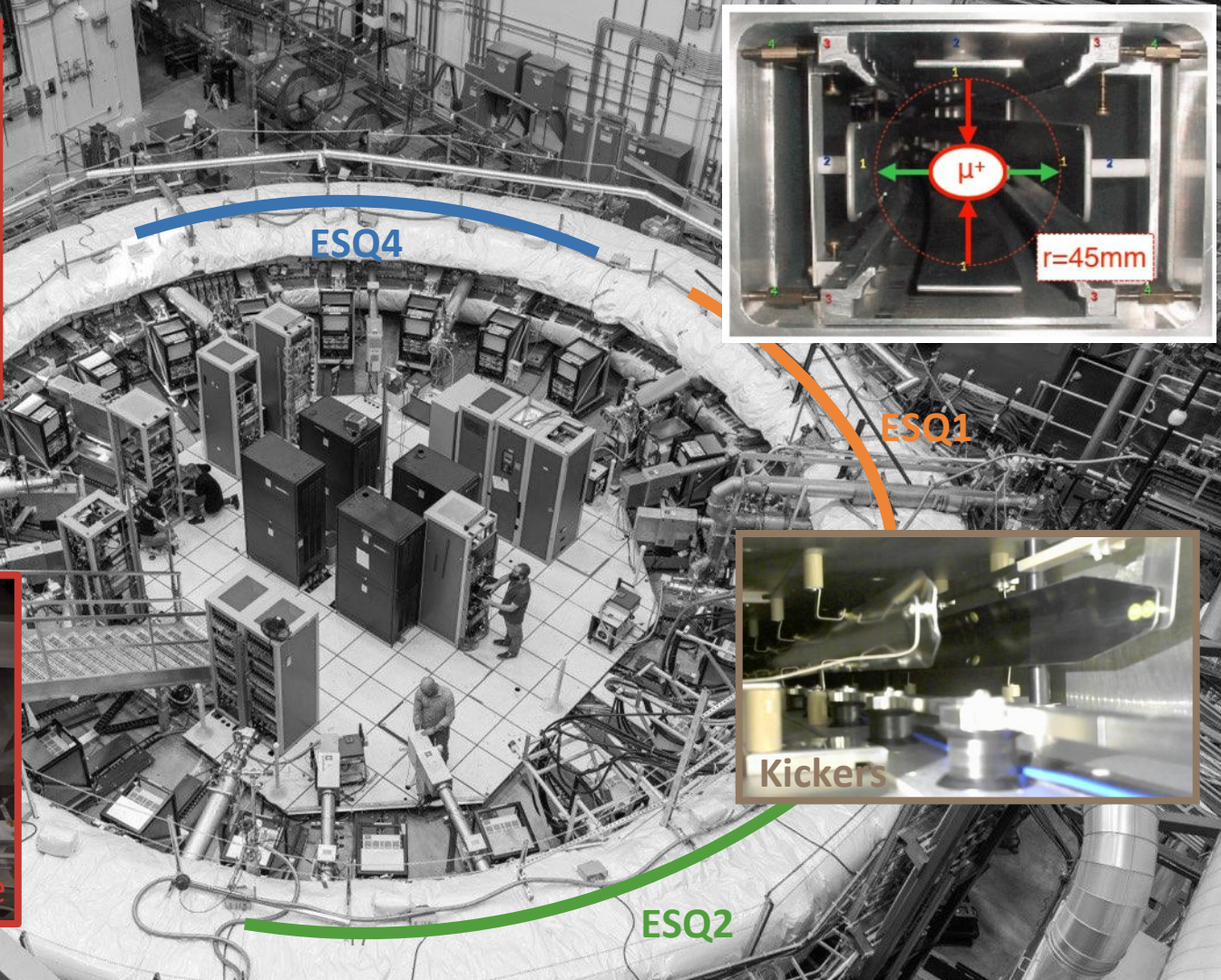
two independent analysis chains



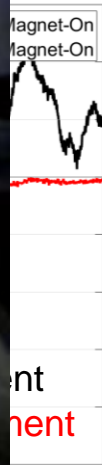
Total field maps Run-2/3: 69 (Run-1: 14)



uncertainty: 22 ppb



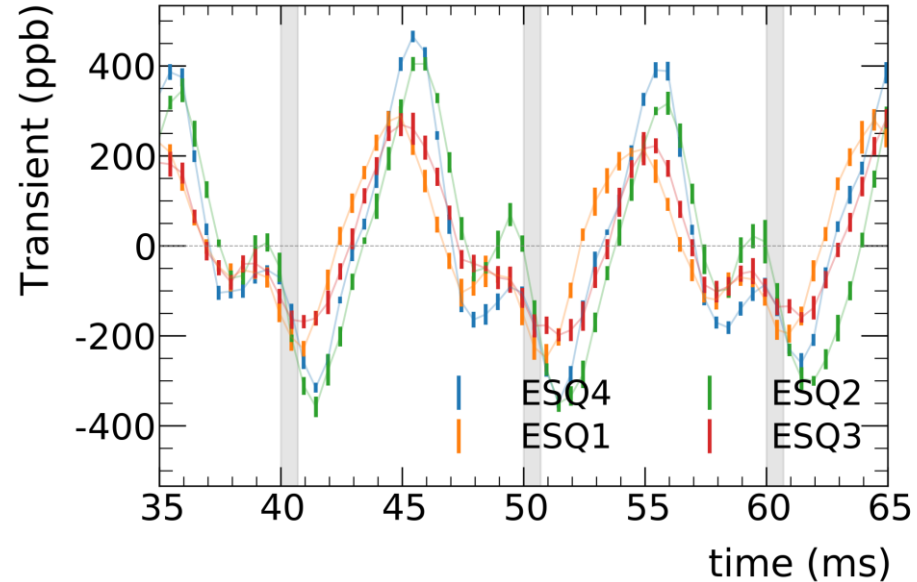
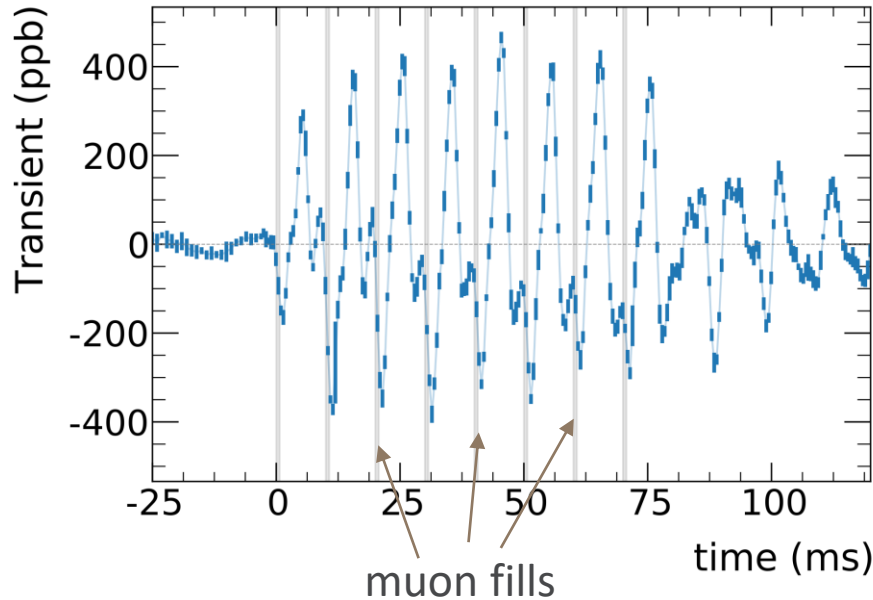
TR
Ed
Fil



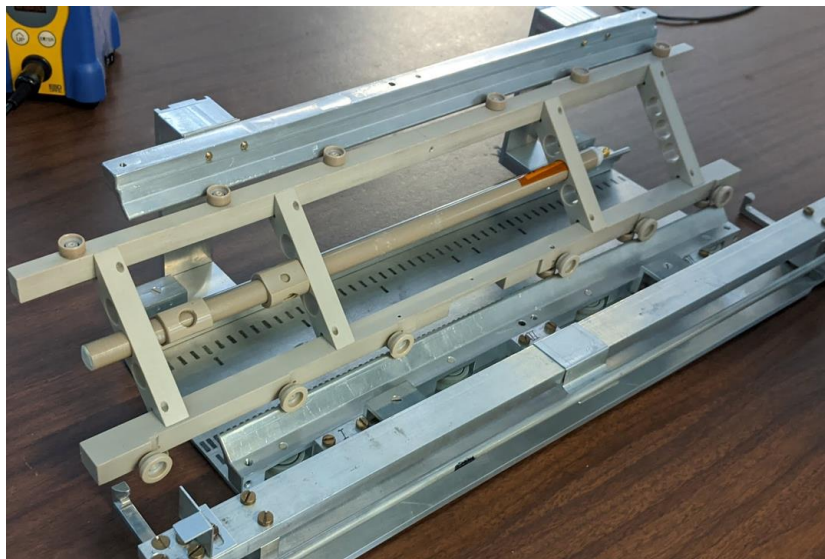
TRANSIENT FIELDS FROM ESQ VIBRATIONS

Mechanical vibrations of ESQ plates cause magnetic field changes.

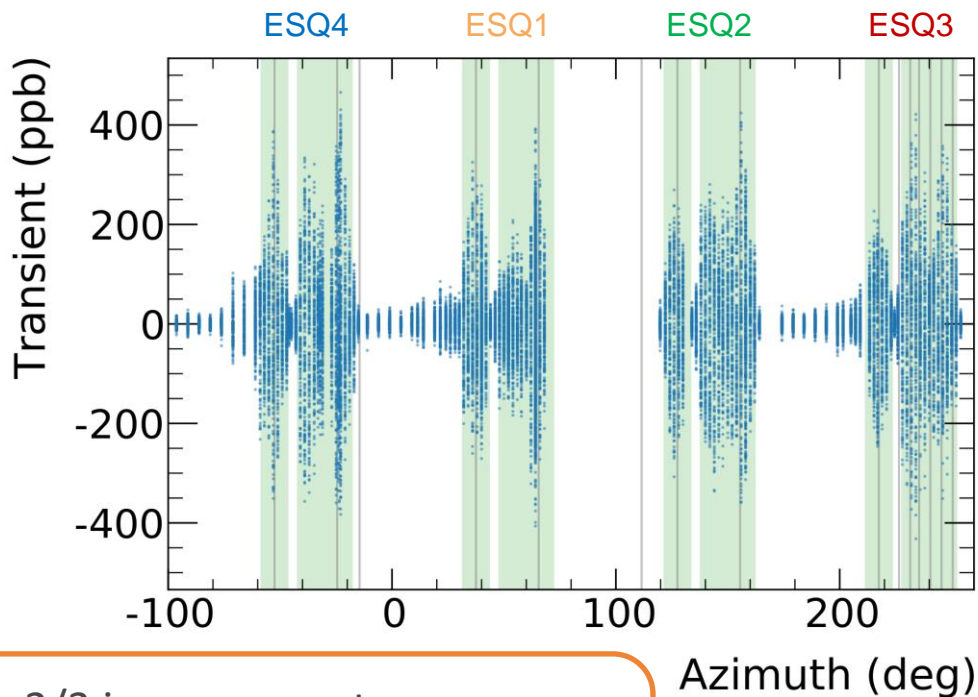
at one location (in ESQ 4)



TRANSIENT FIELDS FROM ESQ VIBRATIONS



vacuum sealed NMR probe

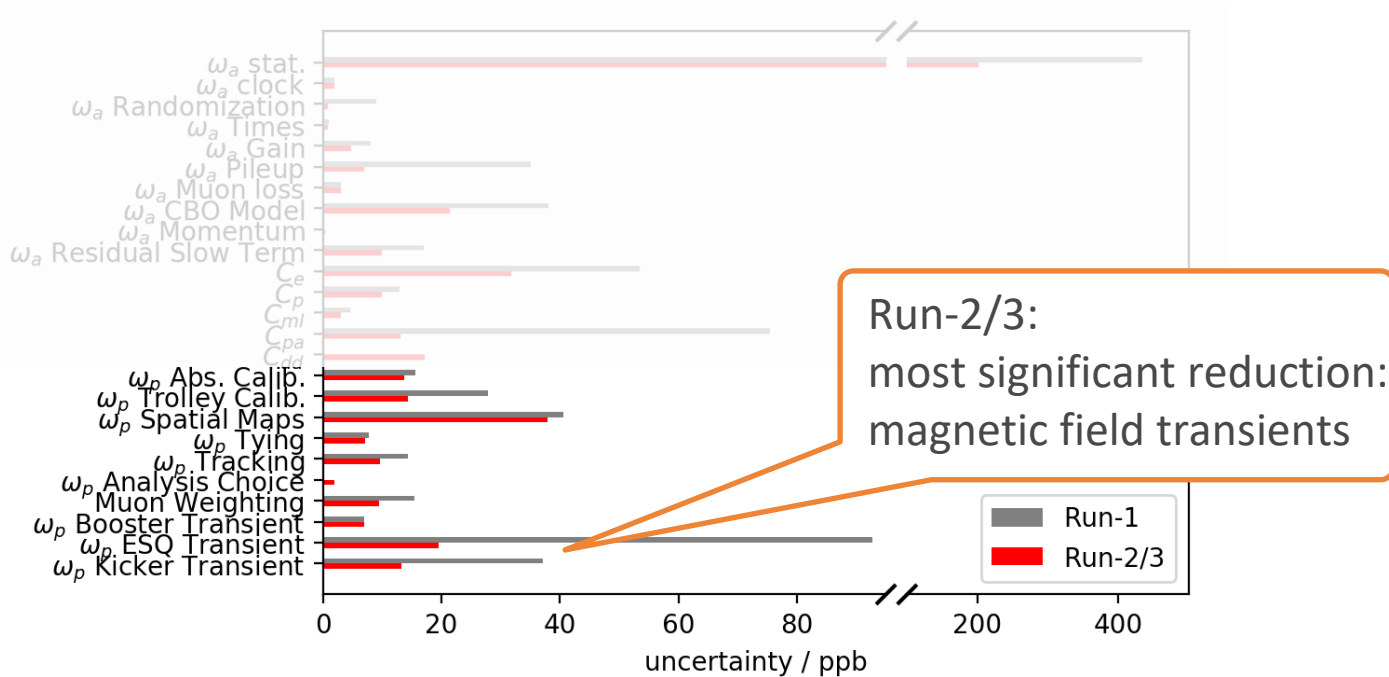


Run-2/3 improvement:
mapping of azimuthal dependence
uncertainty: 92 ppb -> 20 ppb

THE MAGNETIC FIELD OF RUN-2/3: SUMMARY

Total field syst. in Run-2/3: **52 ppb** (TDR goal: 70 ppb)

Outlook: syst. unc. expectation for Run-4/5/6 < 70 ppb



The Muon $g - 2$ Experiment was performed at the 326 Fermi National Accelerator Laboratory, a U.S. Department of Energy, Office of Science, HEP User Facility. Fermilab is managed by Fermi Research Alliance, 329 LLC (FRA), acting under Contract No. DE-AC02- 330 07CH11359. Additional support for the experiment was provided by the Department of Energy offices of HEP and NP (USA), the National Science Foundation (USA), the Istituto Nazionale di Fisica Nucleare (Italy), the Science and Technology Facilities Council (UK), the Royal Society (UK), the National Natural Science Foundation of China (Grant No. 11975153, 12075151), MSIP, NRF and IBS-R017-D1 (Republic of Korea), the German Research Foundation (DFG) through the Cluster of Excellence PRISMA+ (EXC 2118/1, Project ID 39083149), 340 the European Union Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreements No. 101006726, No. 734303, European Union STRONG 2020 project under grant agreement No. 824093 and the Leverhulme Trust, LIP-2021-01.



Argonne National Laboratory is a
U.S. Department of Energy laboratory
managed by UChicago Argonne, LLC.



TRANSIENT FIELDS FROM THE KICKERS

Description	Uncertainty [ppb]			
	2021	2022	Run-3b	Run-2/3a
vibration ambiguity	8.3	12.8	10.5	9.9
transient variance			4.2	3.9
azimuthal	3.1	4.7	3.9	3.7
transverse	4.4	6.8	5.6	5.3
calibration	0.3	0.2	0.3	0.3
baseline	2.5	0.2	1.3	1.2
scaling				1.7
pulse shape diff.				4.2
Sub total			13.3	13.3

TRANSIENT FIELDS FROM ESQ VIBRATIONS

Description	Correction [ppb]	Uncertainty [ppb]
frequency extraction		5
skin depth		2
stability over time		8
azimuthal averaging		11
transverse dependence		5.3
measurement apparatus		10.5
fill-by-fill variations		2
second bunch train		5
Sub total	-21.0	19.5

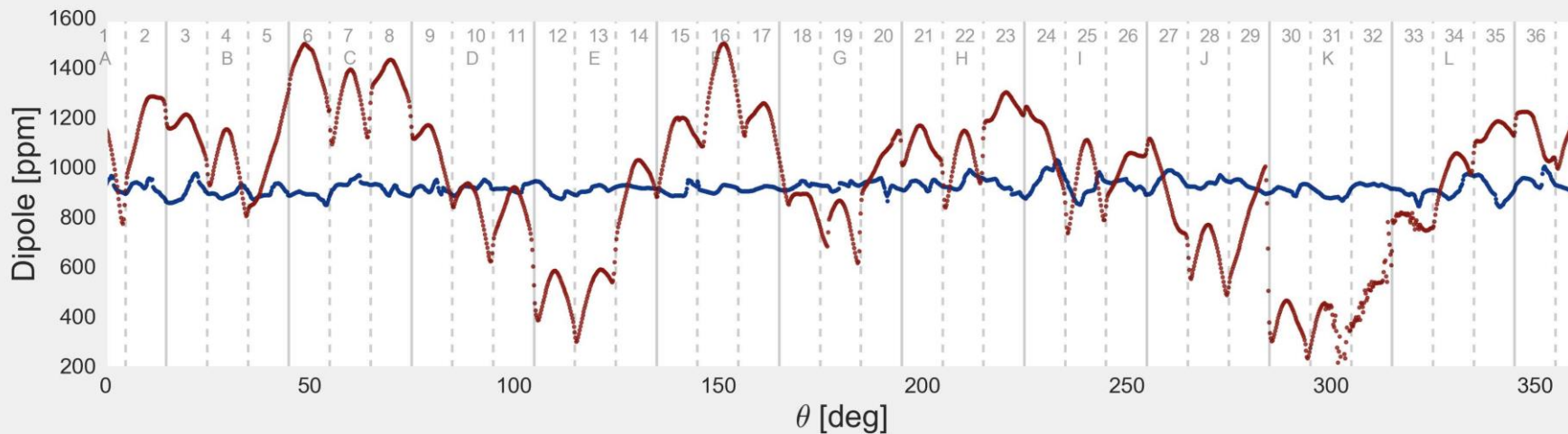
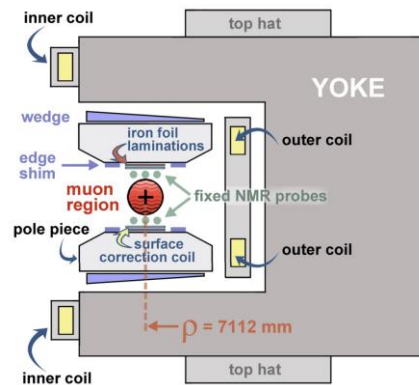
THE MAGNETIC FIELD OF RUN-2/3: SUMMARY

Description	Uncertainty [ppb]		
	Run-2	Run-3a	Run-3b
Calibration probe		8.9	
Trolley calibration		17.0	
Spacial Field Maps	37.2	38.5	38.1
Tracking	17.3	16.5	17.8
Muon Weighting	13.4	7.9	6.9
Transient Booster		7	
Transient Kicker		13.3	
Transient ESQ		19.5	
Sub total correlated			
Sub total uncorrelated			

Total field syst. in Run-2/3: 52 ppb (TDR goal: 70 ppb)

HOW TO STORE MUONS: MAGNETIC FIELD

Fermilab: ~15 ppm RMS (~75 ppm peak-to-peak)
BNL E821: ~35 ppm RMS (~200 ppm peak-to-peak)



MAGNET TEMPERATURE

