



Charged lepton flavor violation for a probe to the neutrino masses and their hierarchy

Masato Yamanaka (Hosei Univ.)

Neutrino oscillation and LFV

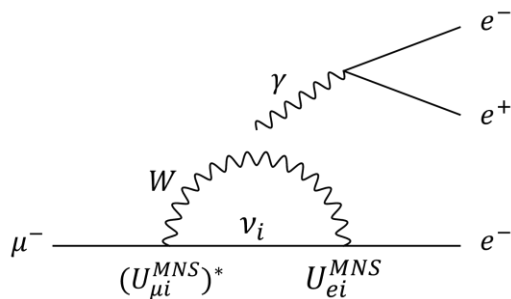
Neutrino oscillation calls new physics beyond the standard model (SM)

SM

Lepton number is **always** conserved

SM + ν oscillation

Will be discovered with $10^{55} \mu$ ☺



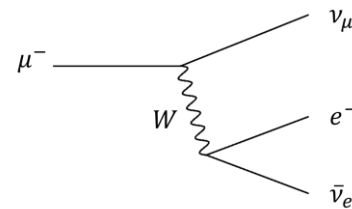
$$BR \approx 7.4 \times 10^{-55}$$

S. Petcov, Sov. J. Nucl. Phys. (1977)

G. Hernandez-Tome, et al, EPJC (2019)

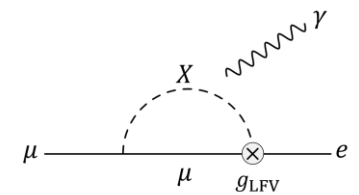
NuFIT 5.2 (2022)	Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 6.4$)		
	bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range	
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.303^{+0.012}_{-0.012}$	$0.270 \rightarrow 0.341$	$0.303^{+0.012}_{-0.011}$	$0.270 \rightarrow 0.341$
	$\theta_{12}/^\circ$	$33.41^{+0.75}_{-0.72}$	$31.31 \rightarrow 35.74$	$33.41^{+0.75}_{-0.72}$	$31.31 \rightarrow 35.74$
	$\sin^2 \theta_{23}$	$0.451^{+0.019}_{-0.016}$	$0.408 \rightarrow 0.603$	$0.569^{+0.016}_{-0.021}$	$0.412 \rightarrow 0.613$
	$\theta_{23}/^\circ$	$42.2^{+1.1}_{-0.9}$	$39.7 \rightarrow 51.0$	$49.0^{+1.0}_{-1.2}$	$39.9 \rightarrow 51.5$
	$\sin^2 \theta_{13}$	$0.02225^{+0.00056}_{-0.00059}$	$0.02052 \rightarrow 0.02398$	$0.02223^{+0.00058}_{-0.00058}$	$0.02048 \rightarrow 0.02416$
	$\theta_{13}/^\circ$	$8.58^{+0.11}_{-0.11}$	$8.23 \rightarrow 8.91$	$8.57^{+0.11}_{-0.11}$	$8.23 \rightarrow 8.94$
	$\delta_{CP}/^\circ$	232^{+36}_{-26}	$144 \rightarrow 350$	276^{+22}_{-29}	$194 \rightarrow 344$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.41^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.03$	$7.41^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.03$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.507^{+0.026}_{-0.027}$	$+2.427 \rightarrow +2.590$	$-2.486^{+0.025}_{-0.028}$	$-2.570 \rightarrow -2.406$

Example: muon decay in SM



μ number $+1 \rightarrow +1$
 e number $0 \rightarrow (+1) + (-1)$

Ex.: muon decay in physics beyond SM



μ number $+1 \rightarrow 0$
 e number $0 \rightarrow +1$

Neutrino oscillation and LFV

Neutrino oscillation calls new physics beyond the standard model (SM)

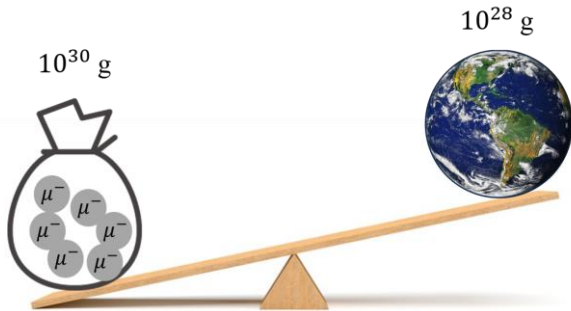
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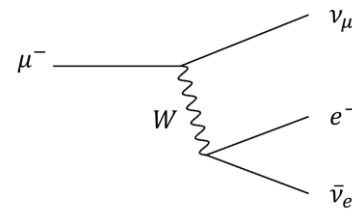
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Impossible!!



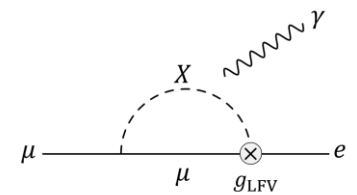
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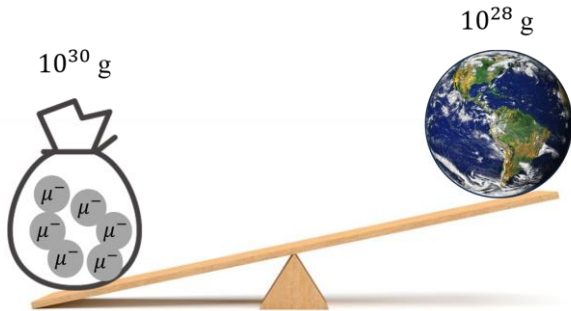
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In the physics beyond the SM

- accessible LFV rate by extra degrees of freedom
(new particles, additional space dimension, ...)
- not only evidence, but also sensitive to the extra degrees

ν mass generation scenarios

(1) Tree-level mass generation

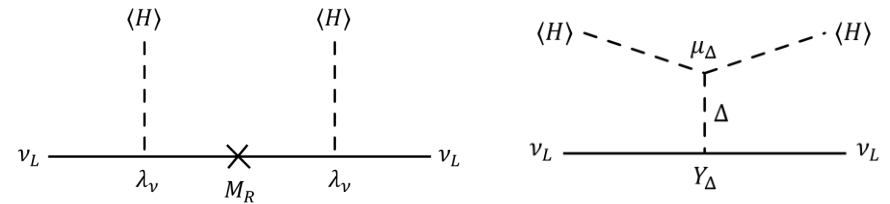
Type-I (-II, -III) Seesaw

Inverse Seesaw

Linear Seesaw

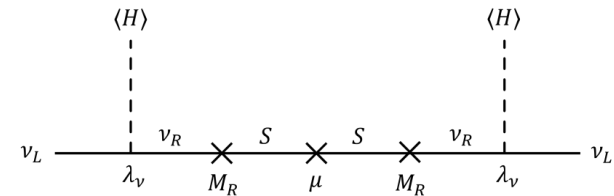
High- (Low-, middle-) scale Seesaw, etc

[with or without SUSY, extra dimension, etc]



Type I Seesaw

Type II Seesaw



Inverse Seesaw

(2) loop-level mass generation

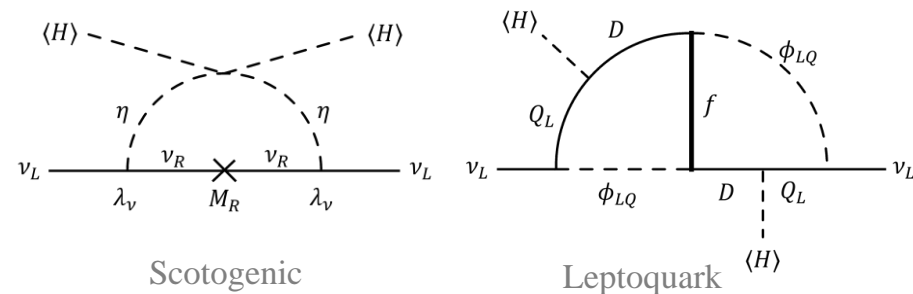
Scotogenic

Leptoquark

Zee-Babu

R-parity violating SUSY, etc

[1-loop, 2-loop, 3-loop, ...]



Scotogenic

Leptoquark

ν mass generation scenarios

(1) Tree-level mass generation

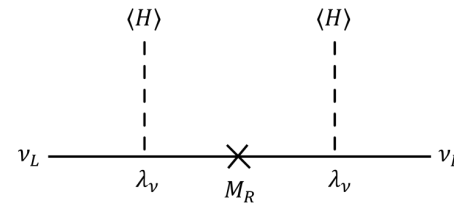
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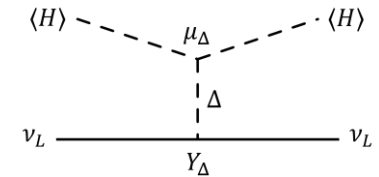
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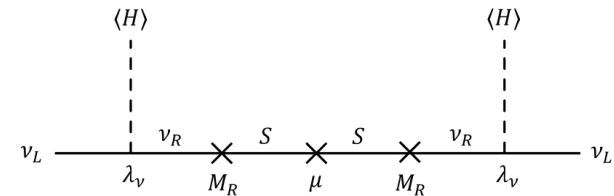
[with or without SUSY, extra dimension, etc]



Type I Seesaw



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Inverse Seesaw

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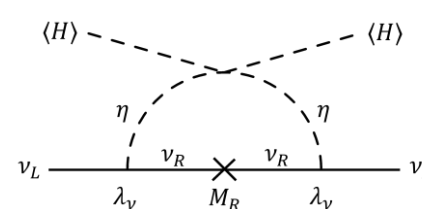
Scotogenic

Leptoquark

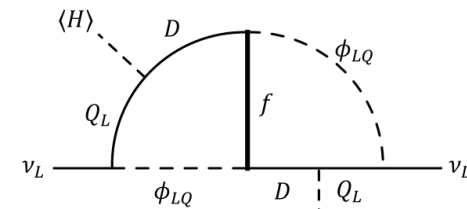
Zee-Babu

R-parity violating SUSY, etc

[1-loop, 2-loop, 3-loop, ...]



Scotogenic



Leptoquark

Find intrinsic patterns of correlation of observables for these scenarios!

How to unravel the physics behind the LFV

Unknown particle **indirectly** appears
in LFV reactions

Not appeared in direct observables

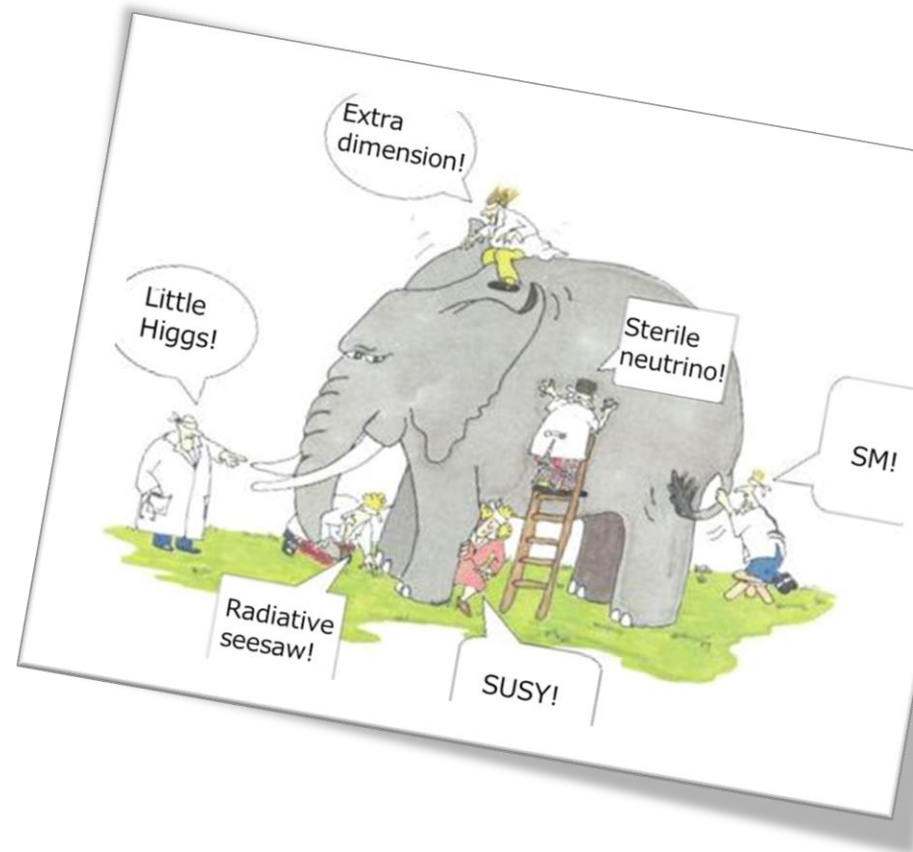
The more LFV processes, the “elephant”
is more clearly illustrated!

Many LFV observables as possible to
draw “unknown” from various angles

- ◆ $\mu^+ \rightarrow e^+ \gamma$
- ◆ $\mu^- \rightarrow e^-$ conversion in nuclei
- ◆ $\mu^- e^- \rightarrow e^- e^-$ in muonic atom
- ◆ $\tau \rightarrow 3\mu, \tau \rightarrow e\pi\pi, \tau \rightarrow \mu\gamma, \dots$, etc

Accurate connection between LFV
parameters and observables

- ◆ Characteristic signatures for each LFV operator
- ◆ Dependences on experimental stage
- ◆ Ratios and correlations of BRs etc



1. Introduction
2. Lepton flavor violating processes
3. ν mass generation scenarios and LFV
4. Summary

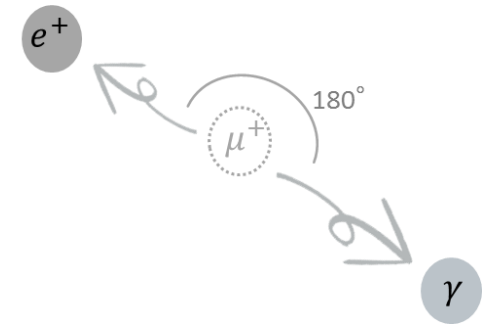


Lepton flavor violating processes

Radiative decay $\ell_i \rightarrow \ell_j \gamma$

Signal

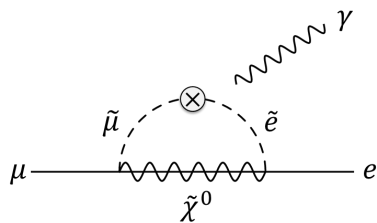
- back-to-back $e(\mu) + \gamma$,
- $\sum E = m_\mu$ (for $\mu \rightarrow e\gamma$), $\sum E = m_\tau$ (for $\tau \rightarrow \ell_j \gamma$)



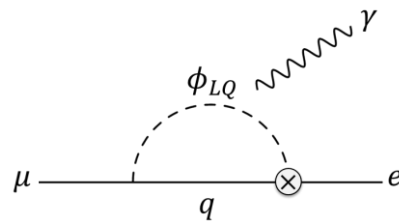
Experimental status

Process	BR limit	Future
$\mu \rightarrow e\gamma$	4.2×10^{-13} MEG (2016)	6.0×10^{-14} MEG II
$\tau \rightarrow e\gamma$	3.3×10^{-8} BABAR (2010)	9.0×10^{-9} Belle II
$\tau \rightarrow \mu\gamma$	4.2×10^{-8} Belle (2021)	6.9×10^{-9} Belle II

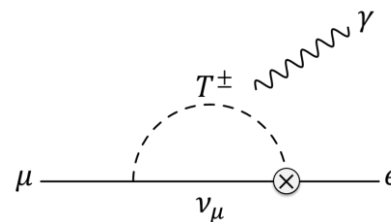
Probe to various models beyond the SM



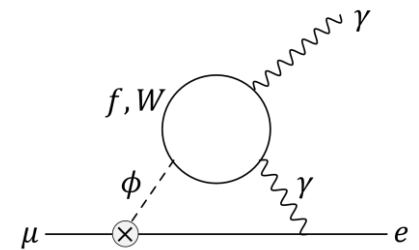
SUSY (+ Type-I SeeSaw)



Leptoquark, GUT models



Type-II SeeSaw,
extended Higgs models



Higgs LFV,
extended Higgs models

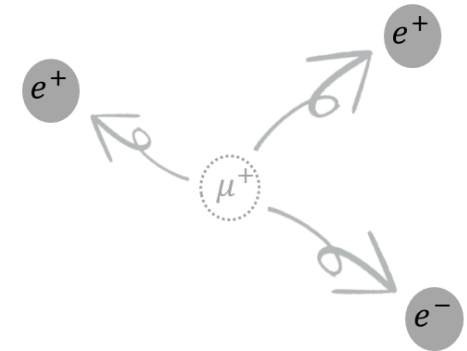
3 lepton decay $\ell_i \rightarrow \ell_j \ell_k \ell_k$

Signal

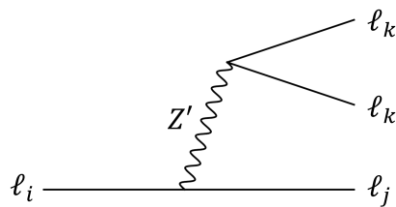
- $\sum E_e = m_\mu$ (for $\mu \rightarrow eee$), $\sum E_\ell = m_\tau$ (for $\tau \rightarrow \ell_j \ell_k \ell_k$)
- spatial momenta $\sum \vec{p}_e = \vec{0}$, time coincidence $\Delta t_{eee} = 0$

Experimental status

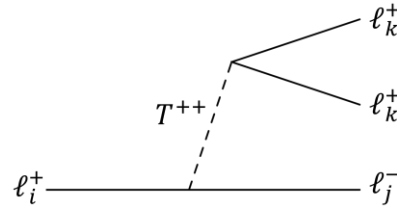
Process	BR limit	Future
$\mu \rightarrow eee$	1.0×10^{-12} SINDRUM (1988)	1.0×10^{-16} Mu3e
$\tau \rightarrow eee$	2.7×10^{-8} Belle (2010)	4.7×10^{-10} Belle II
$\tau \rightarrow \mu\mu\mu$	1.8×10^{-8} Belle (2010)	2.9×10^{-10} Belle II
$\tau \rightarrow \mu ee$	1.5×10^{-8} Belle (2010)	2.3×10^{-10} Belle II



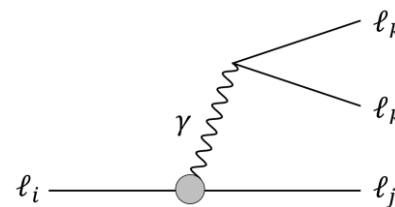
Probe to various models beyond the SM



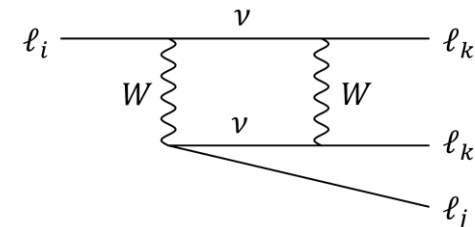
GUT models, Little Higgs, extra dimension models



Type-II SeeSaw, extended Higgs models



SUSY (+ Type-I SeeSaw)



ν MSM, sterile ν

LFV processes in muonic atom

Muonic atom

-- bound state of muon μ^- and nucleus N

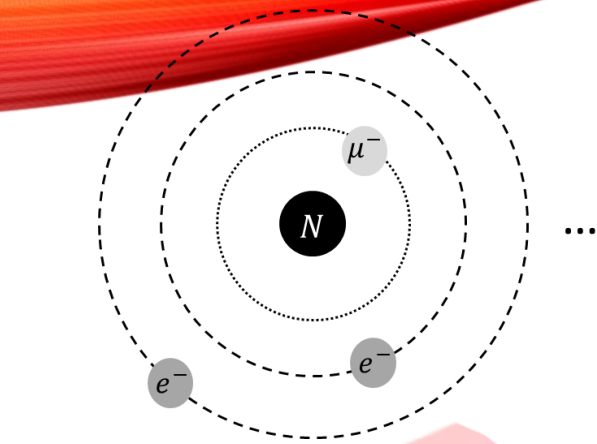
-- fate of muon in the SM

(1) muon decay in orbit

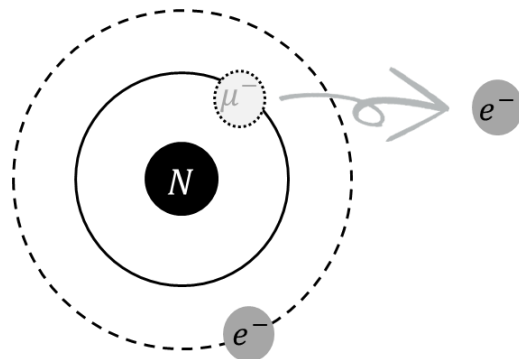
$$(\mu^- N(A, Z)) \rightarrow e^- + \bar{\nu}_e + \nu_\mu + N(A, Z)$$

(2) muon capture

$$(\mu^- N(A, Z)) \rightarrow \nu_\mu + N'(A, Z - 1)$$

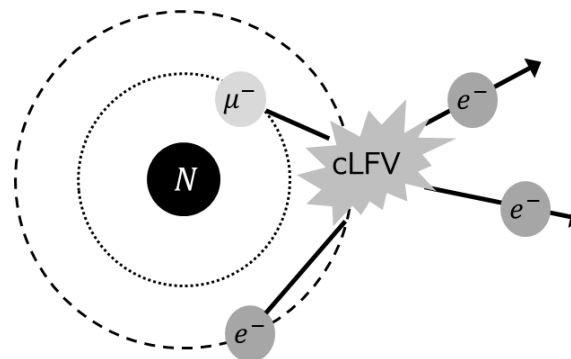


If LFV mediator couples with nucleon



$\mu^- \rightarrow e^-$ conversion

If LFV mediator couples mainly with leptons



$\mu^- e^- \rightarrow e^- e^-$

And also

- $\mu^- \rightarrow e^+$ conversion
- $\mu^- \rightarrow e^- \gamma$ in muonic atom
- $\mu^- \rightarrow e^- X$ (X : light boson)

$\mu^- \rightarrow e^-$ conversion in muonic atom

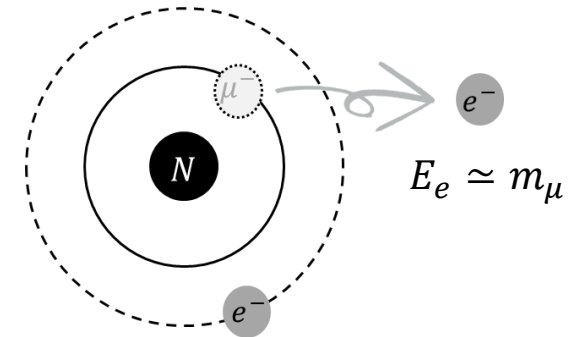
J. Steinberger and H. Wolfe, Phys. Rev. (1955)

Signal

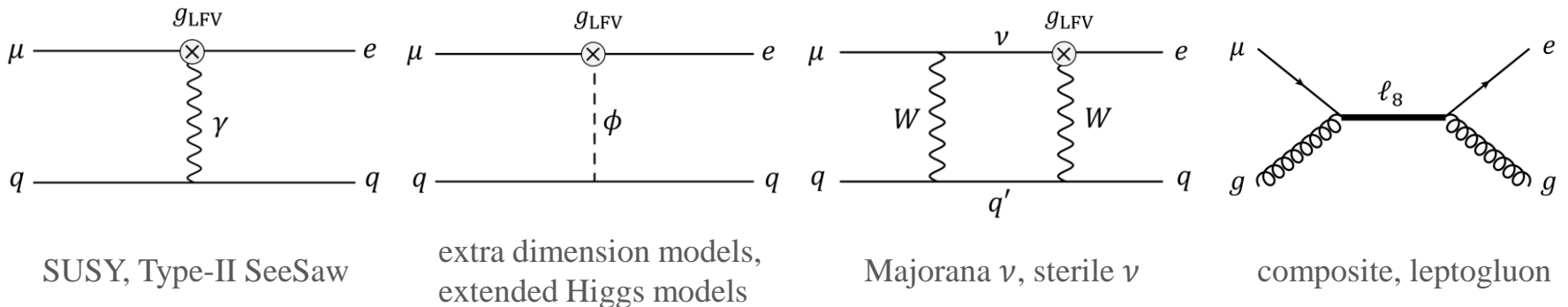
-- Monoenergetic electron $E_e \simeq 105 \text{ MeV}$

Experimental status

Process	BR limit	Future
$\mu^- \text{Au} \rightarrow e^- \text{Au}$	7.0×10^{-13} SINDRUM (2006)	N/A
$\mu^- \text{Ti} \rightarrow e^- \text{Ti}$	4.3×10^{-12} SINDRUM (2006)	N/A
$\mu^- \text{Al} \rightarrow e^- \text{Al}$	N/A	$a \text{ few} \times 10^{-17}$ COMET, Mu2e
$\mu^- \text{Si} \rightarrow e^- \text{Si}$	N/A	1.0×10^{-14} DeeMe



Probe to various LFV operators (pure leptonic operator, unlike $\mu \rightarrow e$ conv.)



$\mu^- e^- \rightarrow e^- e^-$ in muonic atom

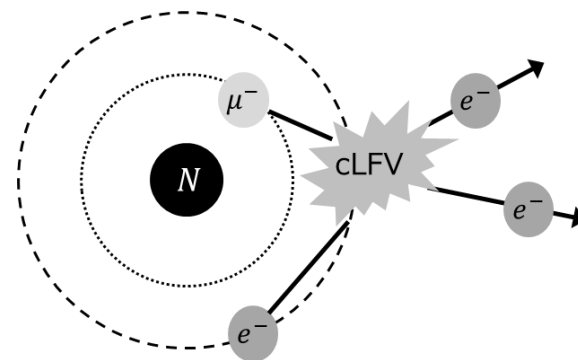
M. Koike, Y. Kuno, J. Sato, MY, PRL (2010)

Signal

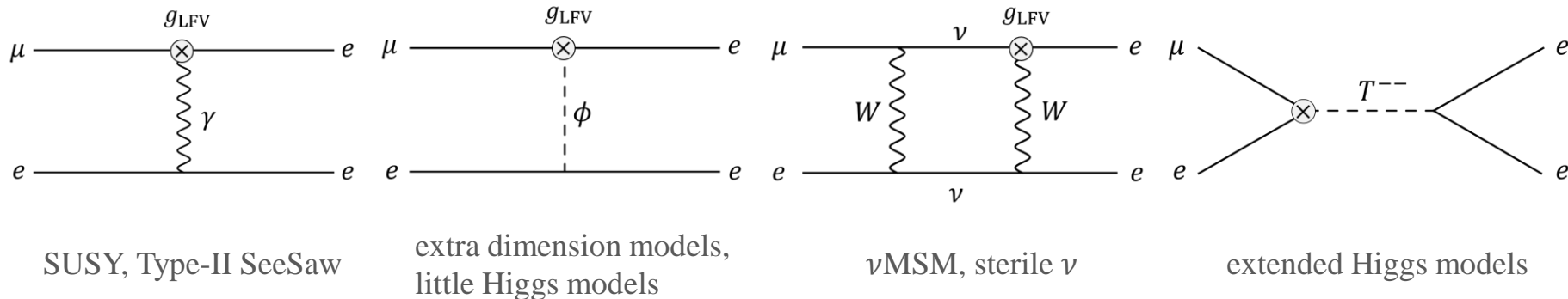
- back-to-back di-electron of $E_e \simeq m_\mu/2$
- time coincidence $\Delta t_{ee} = 0$

Experimental status

- Limit: N/A (New process!)
- included in physics programs of COMET (& Mu2e?)



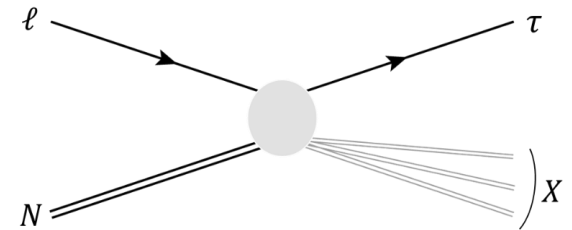
Probe to various LFV operators (pure leptonic operator, unlike $\mu \rightarrow e$ conv.)



LFV Deep inelastic scattering $e(\mu)N \rightarrow \tau X$

Signal

- τ with large momentum along the beam-axis
(highly depends on types of LFV operator)

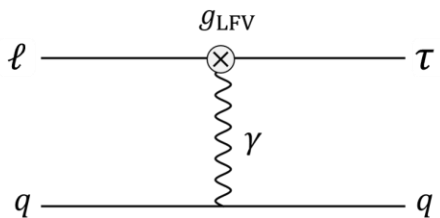


Experimental status

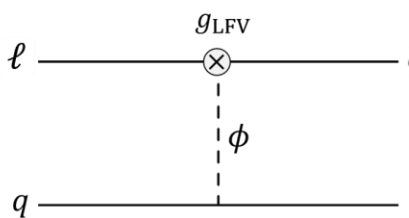
- Limit: HERA exp.
- Future: EIC, LHeC, ILC, ...

		$e \rightarrow \tau$ ZEUS			$F = 0$		
$\alpha\beta$	$S_{1/2}^L$ e^+u_α	$S_{1/2}^R$ $e^+(u+d)_\alpha$	$\tilde{S}_{1/2}^L$ e^+d_α	V_0^L e^+d_α	V_0^R e^+u_α	\tilde{V}_0^R $e^+(\sqrt{2}u+d)_\alpha$	V_1^L
11	$\tau \rightarrow \pi e$ 0.4 3.0	$\tau \rightarrow \pi e$ 0.2 2.5	$\tau \rightarrow \pi e$ 0.4 4.6	G_F 0.2 3.3	$\tau \rightarrow \pi e$ 0.2 3.3	$\tau \rightarrow \pi e$ 0.2 2.4	G_F 0.2 1.2
12		$\tau \rightarrow Ke$ 5 [3.1]	$K \rightarrow \pi\nu\bar{\nu}$ 10^{-3} 4.7	$\tau \rightarrow Ke$ 3 3.7	$\tau \rightarrow Ke$ 3 3.7	[2.7]	$K \rightarrow \pi\nu\bar{\nu}$ 2.5×10^{-4} 1.3
13	*	$B \rightarrow \tau e X$ 8 [5.1]	$B \rightarrow \tau e X$ 8 [5.1]	$B \rightarrow \nu X$ 2 4.6	$B \rightarrow \tau e X$ 4 4.6	*	$B \rightarrow \nu X$ 2 4.6
21		$\tau \rightarrow Ke$ 5 [16]	$K \rightarrow \pi\nu\bar{\nu}$ 10^{-3} 12	$\tau \rightarrow Ke$ 3 4.9	$\tau \rightarrow Ke$ 3 4.9	[6.2]	$K \rightarrow \pi\nu\bar{\nu}$ 2.5×10^{-4} 2.6
22	$\tau \rightarrow ee\bar{e}$ 20 [20]	$\tau \rightarrow ee\bar{e}$ 30 [11]	$\tau \rightarrow ee\bar{e}$ 66 [12]	$\tau \rightarrow ee\bar{e}$ 33 [6.2]	$\tau \rightarrow ee\bar{e}$ 33 [6.2]	11	$\tau \rightarrow ee\bar{e}$ 6.1 [4.3]
23	*	$B \rightarrow \tau e X$ 8 16	$B \rightarrow \tau e X$ 8 16	$B \rightarrow \nu X$ 2 12	$B \rightarrow \tau e X$ 4 12	*	$B \rightarrow \nu X$ 2 12
31	*	$B \rightarrow \tau e X$ 8 17	$B \rightarrow \tau e X$ 8 17	V_{cb} 0.2 5.4	$B \rightarrow \tau e X$ 4 5.4	*	V_{cb} 0.2 5.4
32	*	$B \rightarrow \tau e X$ 8 22	$B \rightarrow \tau e X$ 8 22	$B \rightarrow \nu X$ 2 7.6	$B \rightarrow \tau e X$ 4 7.6	*	$B \rightarrow \nu X$ 2 7.6
33	$\tau \rightarrow ee\bar{e}$ 30 [30]	$\tau \rightarrow ee\bar{e}$ 66 [30]	$\tau \rightarrow ee\bar{e}$ 33 [15]	$\tau \rightarrow ee\bar{e}$ 33 [15]	$\tau \rightarrow ee\bar{e}$ 33 [15]	*	$\tau \rightarrow ee\bar{e}$ 6.1 15

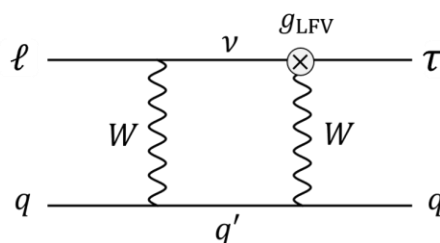
Probe to various models beyond the SM



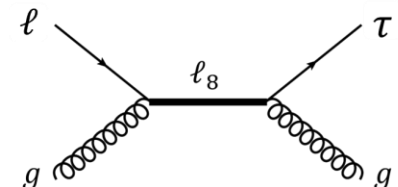
SUSY, Type-II SeeSaw



extra dimension models,
extended Higgs models



Majorana ν , sterile ν



composite, leptoquon



ν mass generation scenarios and LFV

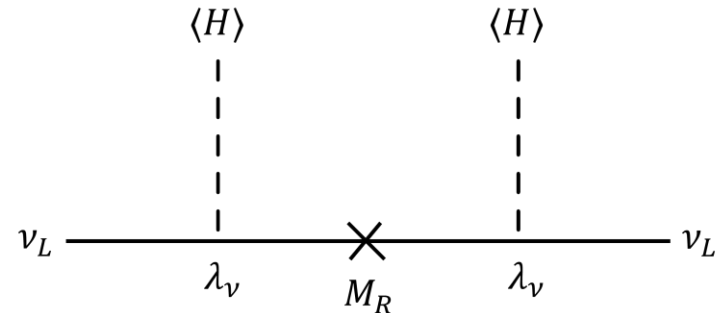
Tree-level m_ν generation: Type-I seesaw

P. Minkowski, PLB (1977)

T. T. Yanagida, Conf.Proc.C (1979)

SM + heavy right-handed neutrinos

- Tiny neutrino mass and mixing for natural size couplings $\lambda \sim \mathcal{O}(1)$
- Baryon asymmetry of the universe via leptogenesis



$$\mathcal{M}_\nu \sim \langle H \rangle^2 \lambda_\nu M_R^{-1} \lambda_\nu^T$$

All of LFV processes experimentally unreachable, $\Gamma_{\text{LFV}} \propto \left| m_D M_R^{-2} m_D^\dagger \right|^2$

S. Bilenky, S. Petcov, B. Pontecorvo, PLB (1977)

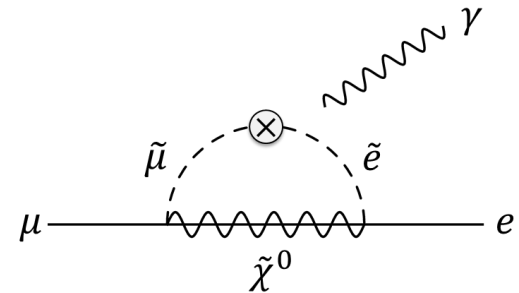
A. Broncano, M. Gavela, E. Jenkins, PLB (2003)

Discovery of LFV \longrightarrow Rule out the minimal type-I seesaw

Tree-level m_ν generation: Type-I seesaw

SM + heavy right-handed neutrinos + SUSY

- Tiny neutrino mass and mixing for natural size couplings $\lambda \sim \mathcal{O}(1)$
- Baryon asymmetry of the universe via leptogenesis + DM, GUT without desert, etc

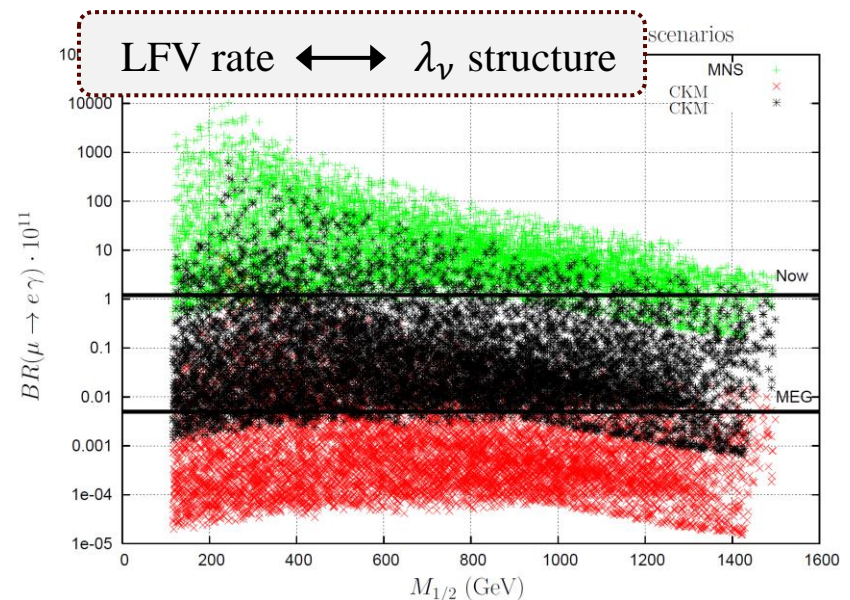


Flavor violating entries in slepton soft-breaking mass from RGE running of λ_ν

$$(\Delta m_{\tilde{L}}^2)_{ij} = -\frac{\ln[M_{\text{GUT}}/M_R]}{16\pi^2} (6m_0^2 + 2A_0^2) (\lambda_\nu^\dagger \lambda_\nu)_{ij}$$

F. Borzumati, A. Masiero, PRL (1986)

J. Hisano, T. Moroi, K. Tobe, M. Yamaguchi, PRD (1996)

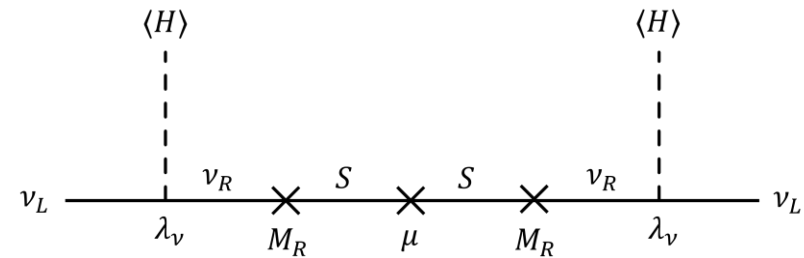


L. Calibbi, A. Faccia, A. Masiero, S. Vempati, PRD (2006)

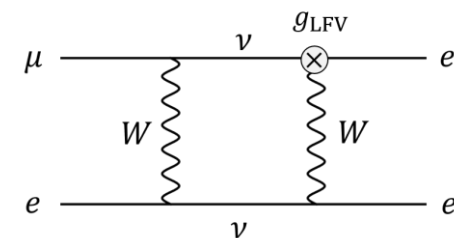
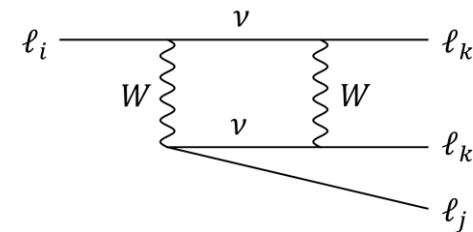
Tree-level m_ν generation: Type-I seesaw

SM + heavy RH neutrinos + sterile fermions
(Inverse seesaw) R. Mohapatra, J. Valle, PRD (1986)

- Tiny neutrino mass and mixing for natural size couplings $\lambda \sim \mathcal{O}(1)$ and twofold seesaw
- Baryon asymmetry of the universe via leptogenesis



$$\mathcal{M}_\nu \sim \lambda_\nu \langle H \rangle (M_R^T)^{-1} \mu M_R^{-1} \lambda_\nu^T \langle H \rangle \sim \frac{m_D^2}{M_R^2} \mu$$



Flavor violating charged current from non-unitarity of PMNS matrix due to extra mixing of leptons

$$\mathcal{L}_{W^\pm} = -\frac{g_w}{\sqrt{2}} W_\mu^- \sum_{\alpha=1}^3 \sum_{j=1}^{3+n_S} \mathbf{U}_{\alpha j} \bar{\ell}_\alpha \gamma^\mu P_L \nu_j + \text{H.c.}$$

J. Schechter, J. Valle, PRD (1980)

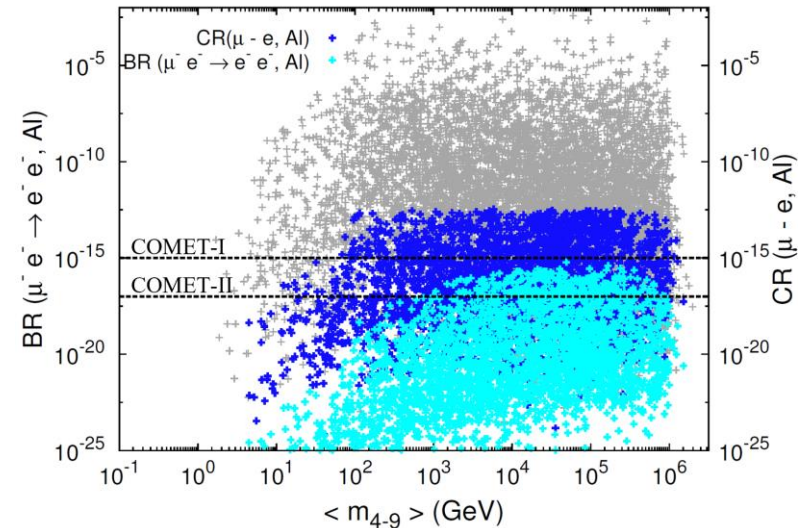
Tree-level m_ν generation: Type-I seesaw

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(Inverse seesaw) R. Mohapatra, J. Valle, PRD (1986)

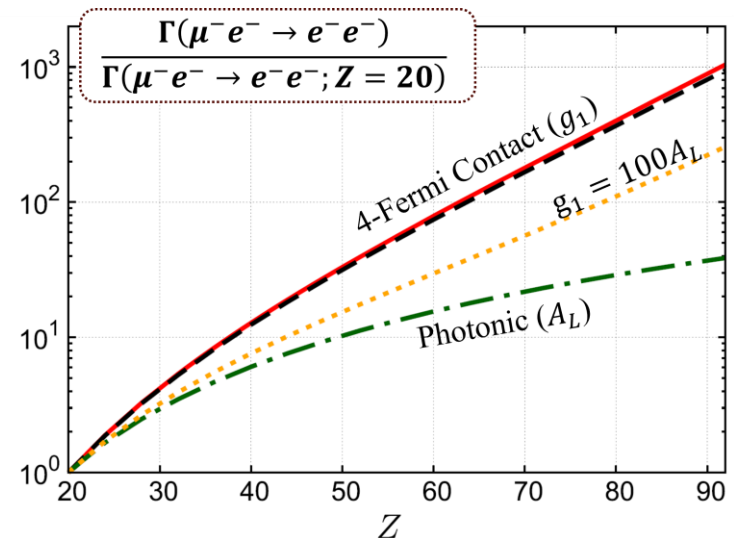
- Tiny neutrino mass and mixing for natural size couplings $\lambda \sim \mathcal{O}(1)$ and twofold seesaw
- Baryon asymmetry of the universe via leptogenesis

Significant contribution to $\mu^- e^- \rightarrow e^- e^-$ and $\mu \rightarrow e$ conversion, within reach of COMET and Mu2e

Z dependence of $\mu^- e^- \rightarrow e^- e^-$ could discriminate type-I seesaw models (SUSY type-I or inverse seesaw)



A. Abada, V. Romeri, A. Teixeira, JHEP (2016)



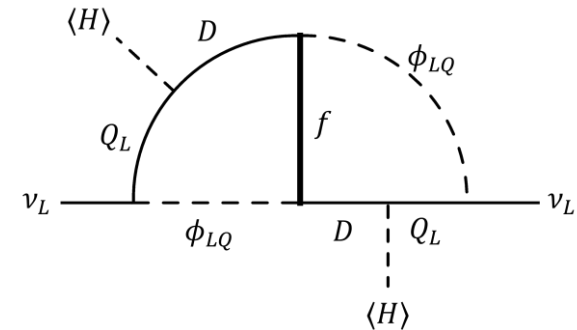
Y. Uesaka, Y. Kuno, J. Sato, T. Sato, MY, PRD (2018)

Radiative m_ν generation: Leptoquark

K. Babu, J. Julio, NPB (2010)

SM + leptoquark ϕ_{LQ} + color octet fermion f

- Tiny neutrino mass and mixing for natural size couplings $\lambda \sim \mathcal{O}(1)$ and loop suppression
- Accounting for $B \rightarrow D^{(*)}\tau\nu$ anomaly

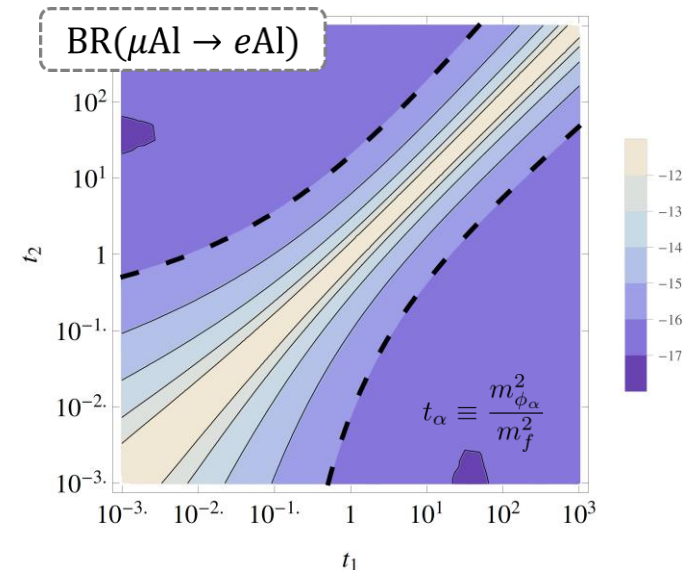


$$\mathcal{M}_\nu \sim 4 \frac{m_f m_b^2 V_{tb}^2}{(2\pi)^8} \sum_{\alpha, \beta=1}^{N_\phi} \left(\lambda_{i3\alpha}^{LQ} \lambda_{3\alpha}^{df} \right) (I_{\alpha\beta}) \left(\lambda_{j3\beta}^{LQ} \lambda_{3\beta}^{df} \right)$$

P. Angel, Y. Cai, N. Rodd, M. Shchmidt, R. Volkas, JHEP (2014)

Yukawa couplings of SM fermion and leptoquark violates lepton flavor conservation

Leading channel for leptoquark LFV:
 $\mu \rightarrow e$ conversion

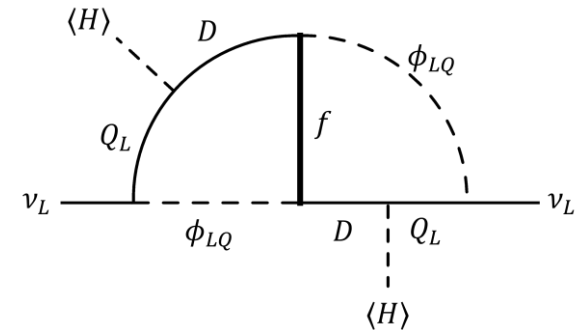


Radiative m_ν generation: Leptoquark

K. Babu, J. Julio, NPB (2010)

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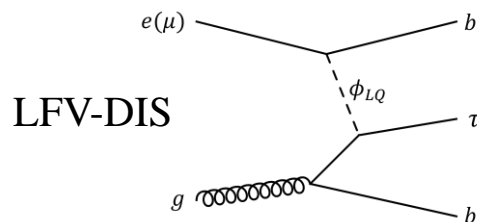


$$\mathcal{M}_\nu \sim 4 \frac{m_f m_b^2 V_{tb}^2}{(2\pi)^8} \sum_{\alpha, \beta=1}^{N_\phi} \left(\lambda_{i3\alpha}^{LQ} \lambda_{3\alpha}^{df} \right) (I_{\alpha\beta}) \left(\lambda_{j3\beta}^{LQ} \lambda_{3\beta}^{df} \right)$$

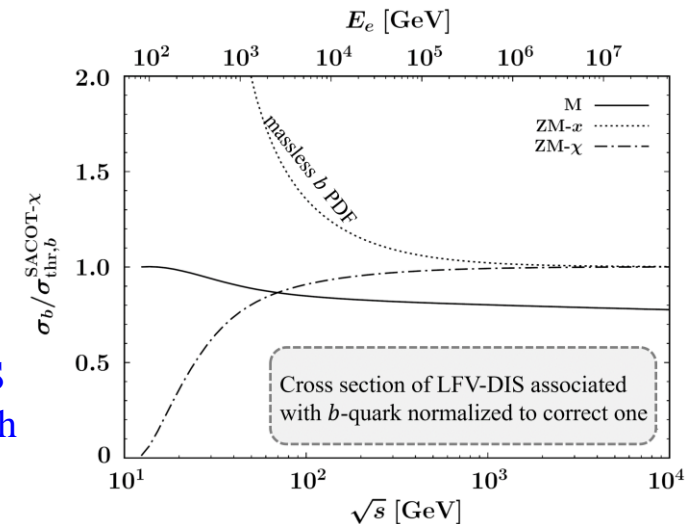
P. Angel, Y. Cai, N. Rodd, M. Shchmidt, R. Volkas, JHEP (2014)

How to check τ LFV?

How to discriminate this scenario from other m_ν generation scenarios?



Carefully formulate the DIS cross section associated with heavy quarks



Y. Kiyo, M. Takeuchi, Y. Uesaka, MY, JHEP (2022)



Summary

Summary

- Neutrino oscillation calls new physics beyond the SM
- Many ν mass generation scenarios
Verification \longleftrightarrow Find intrinsic patterns of LFV observables
- **Many LFV observables as possible** to draw “unknown”
from various angles
- **Accurate connection** between LFV parameters and observables
 - $\mu \rightarrow e\gamma$ in SUSY type-I seesaw
 - $\mu \rightarrow e$ conv. and $\mu^-e^- \rightarrow e^-e^-$ in inverse seesaw
 - $\mu \rightarrow e$ conv. and LFV-DIS in leptoquark-loop generation

